

# Photoproduction of charmonium near threshold

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## Outline

1. Production of  $J/\psi, \psi'$  off a nucleon
  - ◇ Data: All energies
  - ◇ Theory: High energies - pQCD factorization theorem.
  - ◇ Theory: Near threshold - Is skewedness of gluon densities important?
2. Production off the nuclei
  - ◇ Coherence length
  - ◇  $J/\psi - \psi'$  paradox and Vector Dominance Model
  - ◇ Genuine  $J/\psi - N$  cross section
  - ◇ Heavy ion connection; evidence for large  $\sigma(\psi' - N)$ .
  - ◇ Collective effects
  - ◇ Experimental options
3. Open charm production

# Interaction of small color singlet dipoles with hadrons at high energies

Gauge invariance for a small dipole-hadron interaction  $\rightarrow$

Two gluon exchange model

$$\sigma = C b^2 \quad (\text{F.Low 75})$$

**C does not depend on  $E_{inc}$**

pQCD in the leading  $\log b$  approximation (Baym, Blattel, FS, 93)

$$\sigma^{inel}(b, E_{inc}) = \frac{\pi^2}{3} b^2 \alpha_s \times G_N(x, \frac{\lambda}{b^2})$$

Qualitative difference from QED: cross section rapidly increases with  $W$  - a fingerprint of small size dipole interaction in DGLAP kinematics. ( $\lambda(x = 10^{-3}, Q^2 = 10 \text{ GeV}^2 \approx 9)$ )

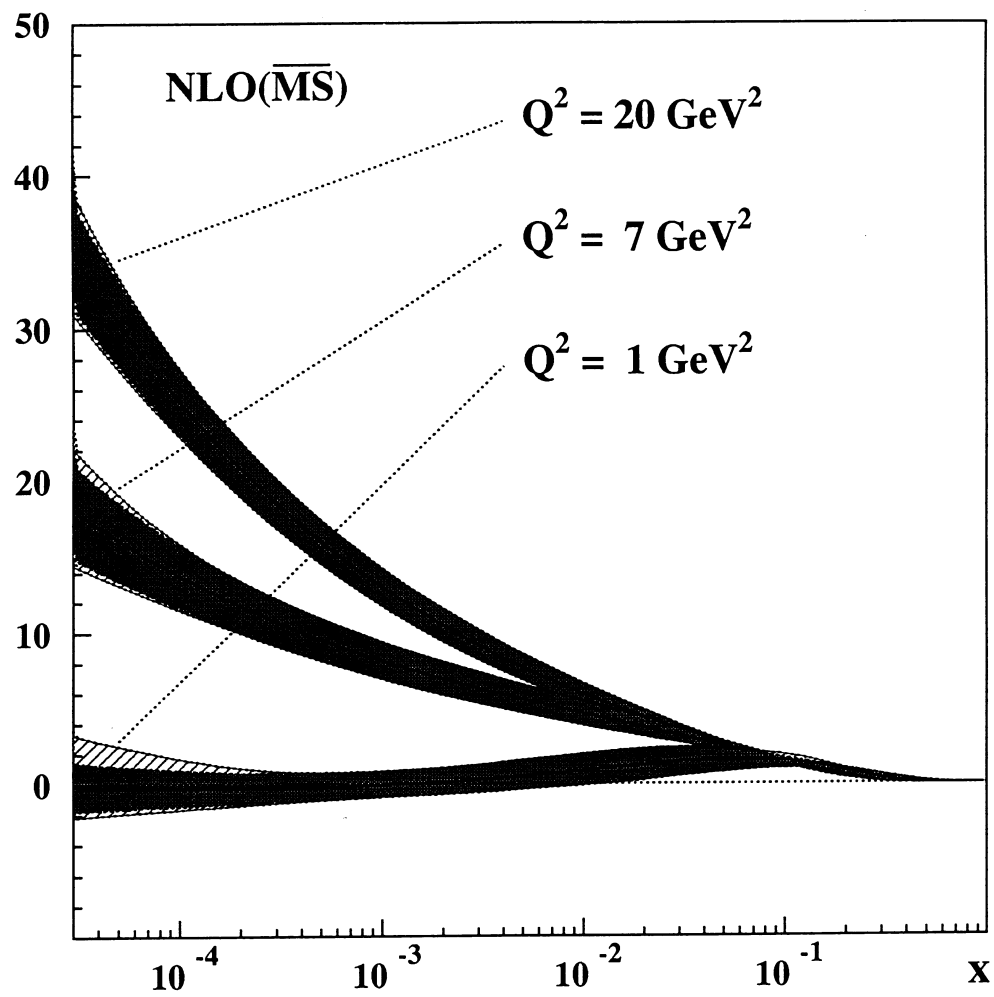
For color octet dipole cross section is **9/4** times larger.

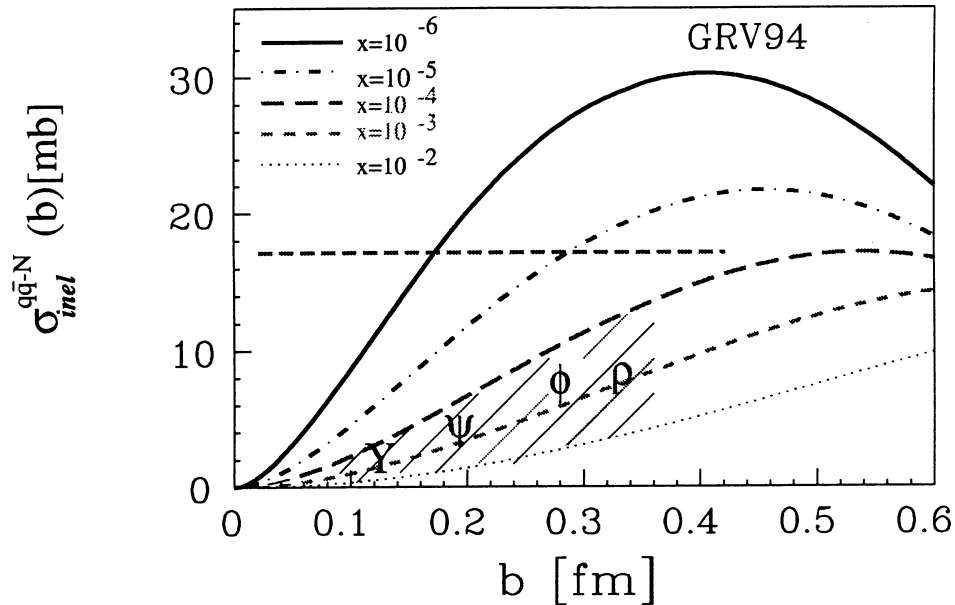
$$\Rightarrow \sigma(s, Q_{eff}^2 = 4 \text{ GeV}^2) \propto \left(\frac{s}{s_0}\right)^{0.2};$$

$$\sigma(s, Q_{eff}^2 = 40 \text{ GeV}^2) \propto \left(\frac{s}{s_0}\right)^{0.4}$$

$xg(x)$

ZEUS 1995





----- Unitarity limit for  $q\bar{q}$ -N scattering

Exclusive  $\rho, \phi, J/\psi, \Upsilon$  vector meson production probes  
 $10^{-4} \leq x \leq 10^{-2}, .1 \leq b \leq .35 fm$

**From S-channel unitarity (Froissart) bound** -  $\sigma_{inel} \geq \sigma_{el}$   
 the growth should stop - breakdown of DGLAP

$$\sigma_{small\ dipole-nucleon}^{inel} \sim 20mb \text{ ( FS \& Koeopf 96)}$$

Relevant for HERA where  $\sigma_{inel}^{color\ oct.-N}(10^{-4}, 10 GeV^2) \sim 16$   
 mb. -Breakdown before the BFKL dynamics could become  
 relevant

$$\text{For } A \sim 200 \quad \sigma_{inel}^{color\ oct.-A} \leq \pi R_A^2 \text{ implies for } A=200:$$

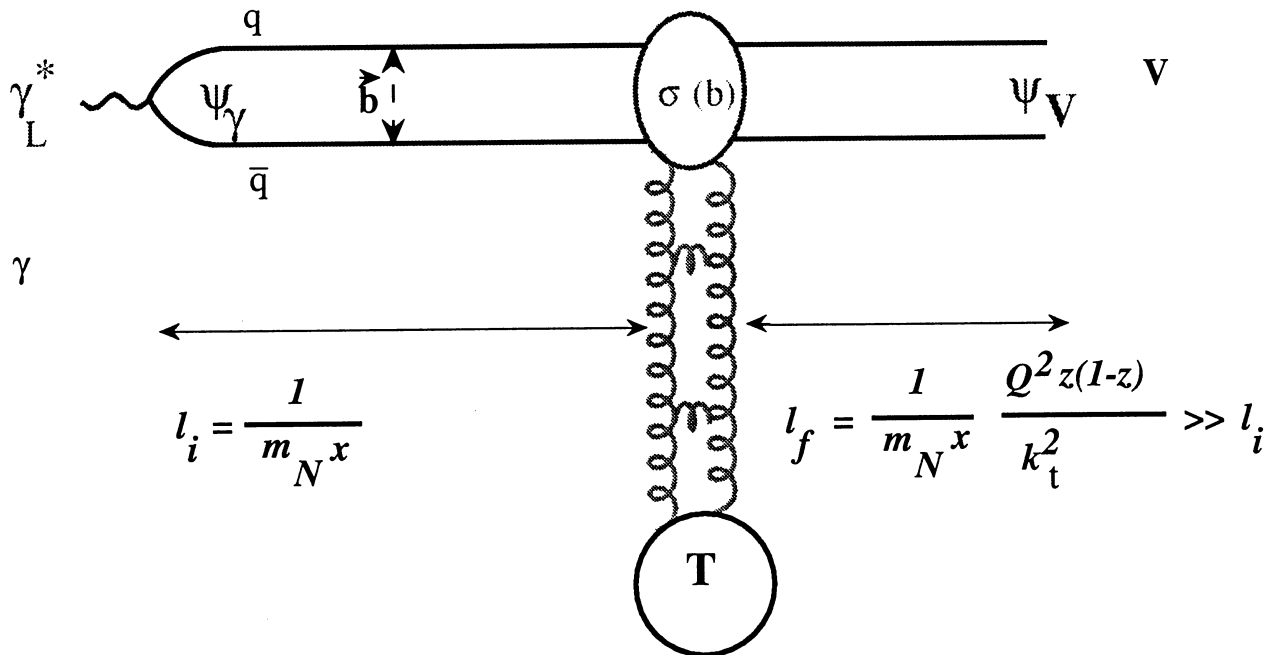
$$\sigma_{inel}^{gg-A} / A \sigma_{inel}^{gg-N} \leq 1/3 \text{ for } x = 10^{-4}, Q^2 = 10 GeV^2$$

$\Rightarrow$  Large nuclear gluon shadowing

# Vector meson diffractive production Theory and HERA data

Space-time picture of Vector meson production at small  $x$  in the target rest frame

Three stages of the  $\gamma_L^* + N \rightarrow V + N$  collision:



♣  $\gamma^*$  breaks up into  $\bar{q}q$  ( $p_q = (zq_0, k_t)$ ) with a lifetime

$$\tau_i = l_i/c = \frac{2q_0}{Q^2 + \frac{k_t^2 + m_q^2}{z(1-z)}} \approx \frac{1}{m_N x}; \quad l_i \geq 100 \text{ fm at HERA}$$

♣♣ The  $\bar{q}q$  pair then scatters off the target proton.

♣♣♣  $q\bar{q}$  then lives a time  $\tau_f = l_f/c = \frac{2q_0}{\frac{k_t^2 + m^2}{z(1-z)}}$  before the final

state vector meson is formed.  $\tau_f \geq \tau_i$ .

⇒ Similar to the case of  $\pi + T \rightarrow 2jets + T$  process,  
 $A(\gamma_L^* + p \rightarrow V + p)$  can be written as a convolution of the  
light-cone wave function of the photon  $\Psi_{\gamma^* \rightarrow |q\bar{q}\rangle}$ , the scattering  
amplitude of the hadron state,  $A(q\bar{q}T)$ , and the wave function  
of the vector meson,  $\psi_V$ . In the impact parameter space

$$A = \int d^2b \psi_{\gamma^*,L}(b) \sigma(b, s) \psi_V(b)$$

The leading twist parameter free answer is

$$\left. \frac{d\sigma_{\gamma^* N \rightarrow VN}^L}{dt} \right|_{t=0} = \frac{12\pi^3 \Gamma_{V \rightarrow e^+e^-} M_V \alpha_s^2(Q) \eta_V^2 \left| \left(1 + i\frac{\pi}{2} \frac{d}{d \ln x}\right) x G_T(x, Q^2) \right|^2}{\alpha_{EM} Q^6 N_c^2}$$

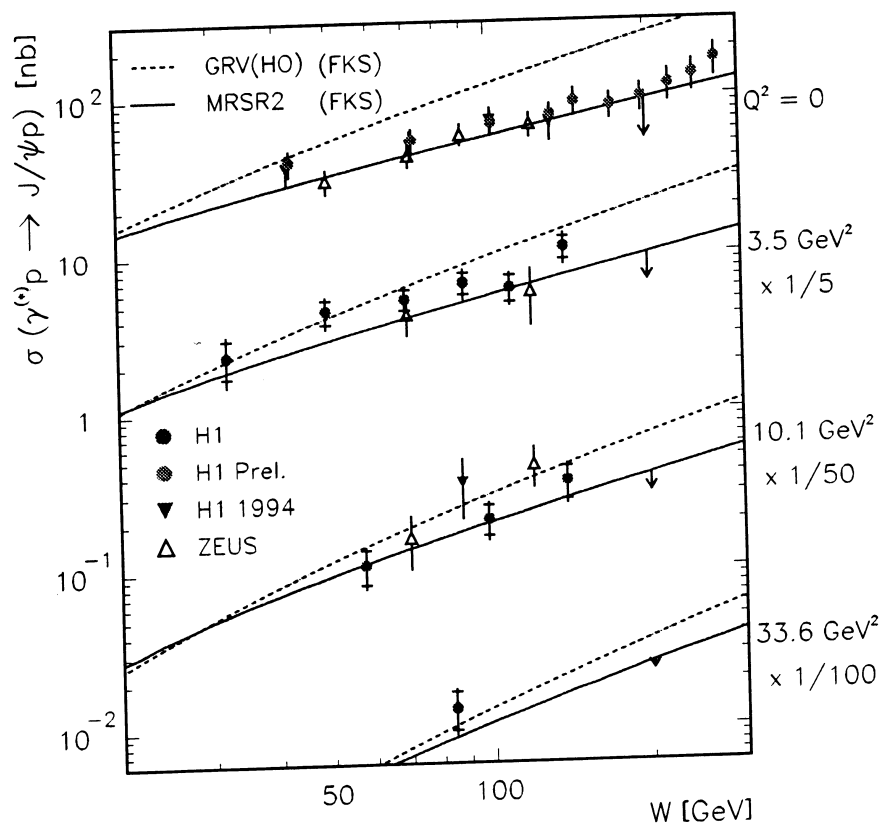
. Here,  $\Gamma_{V \rightarrow e^+e^-}$  is the decay width of  $V \rightarrow e^+e^-$ ;

$$\eta_V \equiv \frac{1 \int \frac{dz d^2k_t}{z(1-z)} \Phi_V(z, k_t)}{2 \int dz d^2k_t \Phi_V(z, k_t)} \rightarrow 3 \quad |_{Q^2 \rightarrow \infty}$$

Note: In the leading twist  $b=0$  in  $\psi_V(b)$ . Finite  $b$  effects in the  
meson wave function is one of the major sources of the higher  
twist effects.

Extensive data on VM production from HERA support *dominance of the pQCD dynamics*. Numerical calculations including finite b effects in  $\psi_V(b)$  explain key elements of high  $Q^2$  data. The most important ones are:

(i) Energy dependence of  $J/\psi$  production; absolute cross section of  $J/\psi, \Upsilon$  production.

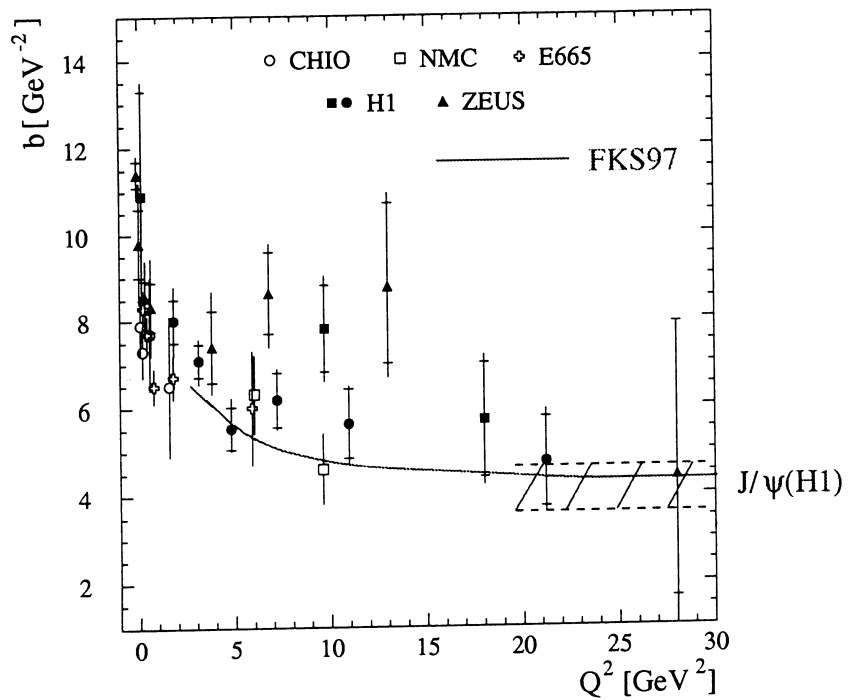
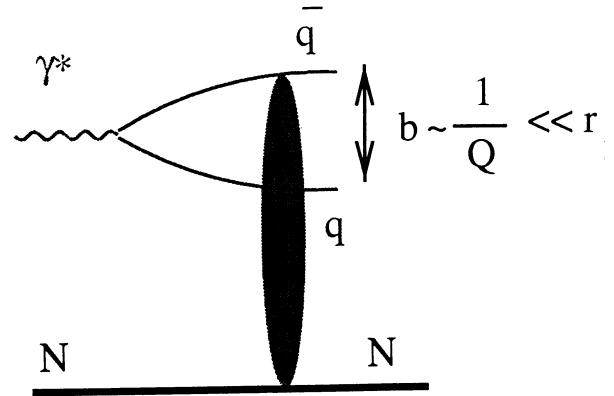


(ii) Absolute cross section of  $\rho$  production at  $Q^2 \sim 20-30 \text{ GeV}^2$  and its energy dependence at  $Q^2 \sim 20 \text{ GeV}^2$ . Explanation of the data at lower  $Q^2$  is more sensitive to the higher twist effects, and uncertainties of the low  $Q^2$  gluon densities.

(iii) Convergence of the t slopes

$B$  ( $\sigma = A \exp(Bt)$ ) of  
 $\rho$ -meson production  
 at large  $Q^2$  and  
 $J/\psi$  production

(Brodsky et al 94)



$\Rightarrow$  Small size  $q\bar{q}$  Fock components are present in light mesons.

$\Rightarrow$  At the transverse separations  $b \leq 0.3 \text{ fm}$  pQCD reasonably describes "small  $q\bar{q}$  dipole" - nucleon interactions.



$\sqrt{s} \leq 30 \text{ GeV}$ : competing model:

Color evaporation model:

$$\sigma(\gamma N \rightarrow J/\psi + X) = f_{J/\psi} \int_{4m_c^2}^{4m_D^2} \frac{dM^2}{s} \sigma\left(\frac{M^2}{s}\right).$$

$\sigma_{\gamma g} \rightarrow c\bar{c}(M^2)$

$$\sigma_{el} \propto x \sigma(x)$$

$$x = \frac{M^2}{s} \quad (*)$$

Note: Near threshold large corrections

to (\*)

$$x_{thr.} = \frac{m_\psi}{m_\psi + m_N}$$

not  $\frac{m_\psi^2}{(m_\psi + m_N)^2}$

Need for accurate measurement of energy dependence.

What happens for intermediate energies: 1 gluon or 2 gluon coupling?

For interpretation difference of  $\Gamma(x)$  and  $\Gamma(x_1, x_2)$  may become important if  $x$  large.

Consider  $x \sim 1$

$$\frac{1-x_q}{2} \xrightarrow{\sim} \frac{x_q - x}{(1-x_q)/2} \xrightarrow{\sim} \frac{x_q - x}{(1-x_q)/2}$$

$x_q$     $x_1$     $x_2$     $x_q - x$   
 (bracketed regions under  $x_1$  and  $x_2$ )

$$x_q - x \sim \frac{(1-x_q)}{2}$$

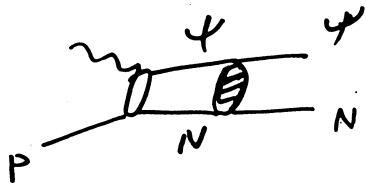
$\Rightarrow$  overlap integral  
 $\sim \text{const}(x)$

$$\Rightarrow \Gamma(x) \sim \Gamma^2(x_1, x_2)$$

may mimic 1 gluon model

Threshold  $\sigma$

If starting from  $E \sim 50 \text{ GeV}$   
and use  $x b(x)$  fit would lead  
to  $\sigma \ll \sigma_{\text{experimental}}$ .



Enhancement is  
possible if significant  
 $\psi N$  attraction

Brodsky & Miller estimate  $\sigma(\psi N) \approx 6 \text{ mb}$   
potential attractive [approximation:  $v^2/c^2 \ll 1$ ]  
not too good  
induced dipole - dipole gluon  
interaction. (van der Waals forces)

$\Rightarrow$  Accurate measurements of  
 $\sigma(\gamma + p \rightarrow \psi N)$  for  $8.2 \leq E_\gamma \leq 126 \text{ GeV}$   
&  $\sigma(\gamma + p \rightarrow \psi' N)$  for  $11 \leq E_\gamma \leq 136 \text{ GeV}$ .

Measurements close to threshold

$E_\gamma = 8.2 \text{ GeV}$  for  $\gamma + p \rightarrow \Psi + p$   
11 GeV for  $\gamma + p \rightarrow \Psi' + p$

(a) SLAC 1975

(b) Cornell 1975

$\left. \frac{d\sigma}{dt} \right|_{t=0}$  seems to be  $\approx \text{const}$  near  
threshold (but  $t_{\text{min}}$  increases!!)

$\Rightarrow$  To match SLAC data - steep increase  
between  $E_\gamma = 12 \text{ GeV}$  and  $13 \text{ GeV}$  ??

$\Rightarrow$  Perhaps data of SLAC & Cornell  
are not consistent

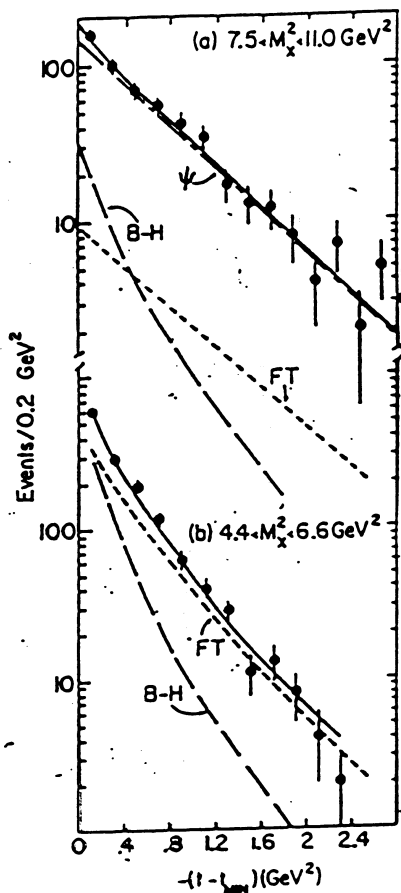


FIG. 2.  $t - t_{\min}$  distributions for  $c-c$  events in two mass regions. The solid curves represent the sum of the contributions from Bethe-Heitler pairs (B-H),  $n-n$  and  $n-c$  feedthrough (FT), and for (a) the fit to the  $\psi$  cross section described in the text.

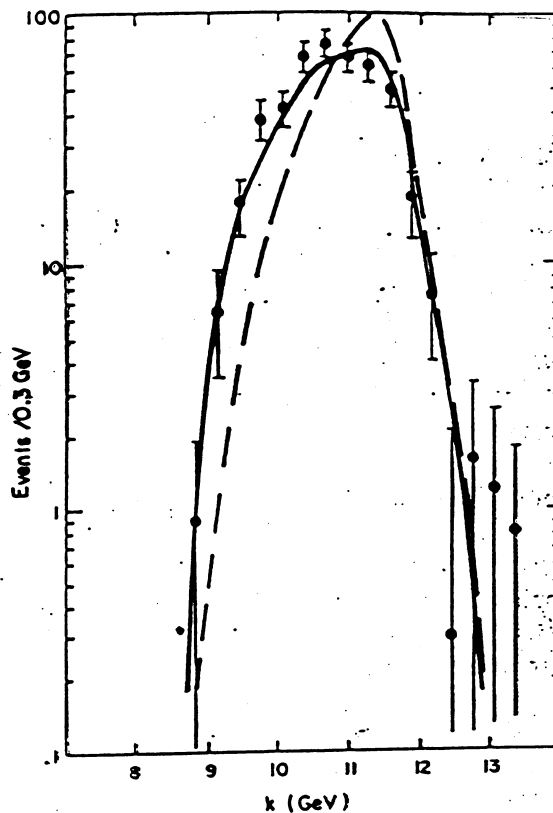


FIG. 3. The reconstructed photon energy distribution for the  $\psi$  events with Bethe-Heitler pairs and feedthroughs subtracted. The solid line is the expected tribution for a cross section  $d\sigma/dt = 0.9 \exp(-1.2t)$ . The dashed line is for  $d\sigma/dt = 0.144(k-8.2)^2 \exp(-1.2t)$  nb/GeV<sup>2</sup>.

$\frac{d\sigma}{dt} \Big _{t=0}$	$9.3 \leq E_\gamma \leq 10.4$	$0.94 \pm 0.20$	$\frac{nb}{GeV^2}$
	$10.4 \leq E_\gamma \leq 11.1$	$1.10 \pm 0.17$	
	$11.1 \leq E_\gamma \leq 11.8$	$0.60 \pm 0.12$	

Threshold enhancement?

$\gamma p \rightarrow \psi p$  attraction in  $\psi N$ -channel?

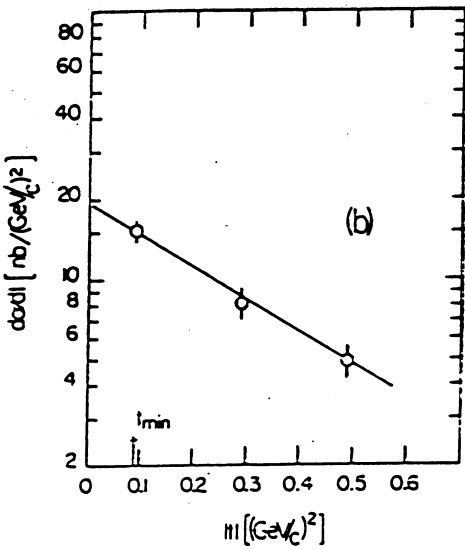
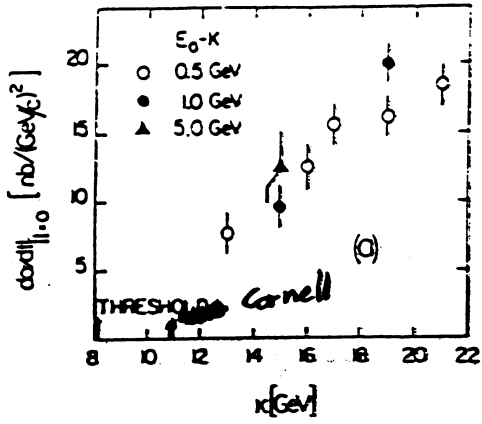


FIG. 2. (a) Cross section extrapolated to  $t=0$  for  $\psi(3100)$  as function of energy. Thresholds for  $\psi(3100)$  and  $\psi(3700)$  are indicated. (b) Differential cross section for  $\psi(3100)$  for  $k=19$  GeV and  $E_0=20$  GeV as a function of  $t$ .  $b=2.9 (\text{GeV}/c)^{-2}$ .

$$\sigma_{\text{tot}}(\gamma p \rightarrow \psi p) \Big|_{20 \text{ GeV}} \approx 7 \text{ nb}$$

$$\sigma_{\text{tot}}(\gamma p \rightarrow \text{charm}) \approx 62 \pm 8 \text{ (+15, -10.) nb}$$

$$\sigma(\gamma p \rightarrow D \bar{D} \text{bar}) = 17 \begin{matrix} +8 \\ -6 \end{matrix}$$

$$\Rightarrow \sigma(\gamma p \rightarrow \bar{D} \Lambda_c) \gg \sigma(\gamma p \rightarrow D \bar{D} + X)$$

$\Upsilon/\Psi$  photoproduction at  $E_\gamma \leq 206 \text{ eV}$

- Average longitudinal distance in  $\gamma \rightarrow c\bar{c}$  transition small

$$z \approx \frac{2E_\gamma}{4m_c^2} \approx 1 \text{ fm}$$

$$\dots \quad l_{\text{coh}} = \frac{2P_\Psi}{m_{\Psi'}^2 - m_\Psi^2} = \frac{P_\Psi}{m_\Psi} \cdot \frac{1}{m_{\Psi'} - m_\Psi}$$

$\underbrace{\hspace{1.5cm}}_{\gamma\text{-factor}}$

$$\approx \gamma/3 \cdot \text{fm}.$$

$\Rightarrow$  For  $P_{\Upsilon/\Psi} \leq 20 \text{ GeV}$  genuine  $\Upsilon N$  interaction can be studied in  $\gamma A$  scattering

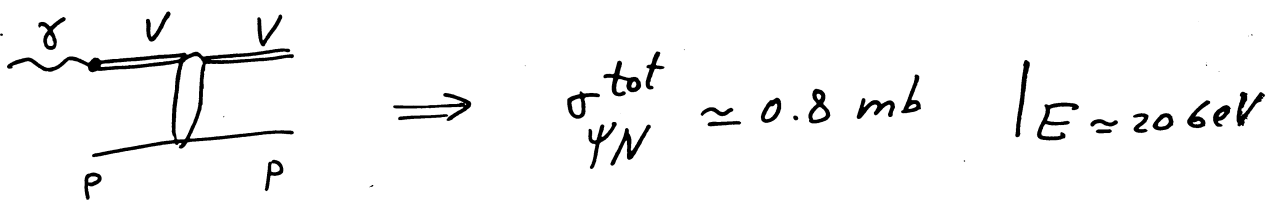
[F.S. Ferrara 90]

$\sigma_{\Upsilon N}$  is Needed for interpretation of  $\Upsilon/\Psi$  data from AA collisions at CERN

# Charmonium - Nucleon cross section

$\sigma_{\psi N} \sim 1 \text{ mb}$  often used.

Origin - vector dominance model



$$\Rightarrow \sigma_{\psi N}^{\text{tot}} \approx 0.8 \text{ mb} \quad | E \approx 2060 \text{ eV}$$

Paradox (FS 85)

Apply VDM to  $\psi'$

production  $\Rightarrow$

$$\sigma_{\psi' N}^{\text{tot}} / \sigma_{\psi N}^{\text{tot}} \approx 0.7$$

violates geometry of strong interactions

$$r_{\psi'} / r_{\psi} \approx 2 \Rightarrow \sigma_{\psi' N} / \sigma_{\psi N} = \left( \frac{r_{\psi'}}{r_{\psi}} \right)^2 = 4$$

Explanation  $\psi'$  &  $J/\psi$  produced in small

configurations  $r \sim 1/mv$

$$\sigma_{\psi' N}(\text{eff}) / \sigma_{\psi N}(\text{eff}) \approx \left( \frac{m_{\psi}}{m_{\psi'}} \right)^2 \approx 0.7$$

$$\Rightarrow \sigma_{\text{eff}}(\psi N) \ll \sigma_{\psi N}$$

FS 85



Experiment: SLAC 77 [bremstr. beam  
 $E_0 = 20 \text{ GeV}$ ]

$$\frac{\sigma(\gamma + \text{Be} \rightarrow \psi + A')}{\sigma(\gamma + \text{Ta} \rightarrow \psi + A')} \Big|_{\text{incoh.}} = 1.21 \pm 0.07$$

$$\Rightarrow \sigma_{\psi N} = 3.5 \pm 0.8 \text{ mb}$$

- expansion effect  
small) and would  
increase  $\sigma_{\psi N}$

Compare  $\sigma_{\psi N} (\text{VDM}) < 1 \text{ mb}$

confirms explanation of  $\psi/\psi'$  paradox

What is dynamics of  $\sigma_{\psi N}$ ?

p QCD for  $\sigma(c\bar{c}N)$  for

$E_\gamma \sim 20 \text{ GeV}$  leads to

$$\sigma_{\text{hard}}^{\text{tot}} (\gamma/\psi - N) \approx 0.2 \text{ mb}$$

New NA-48

AA data

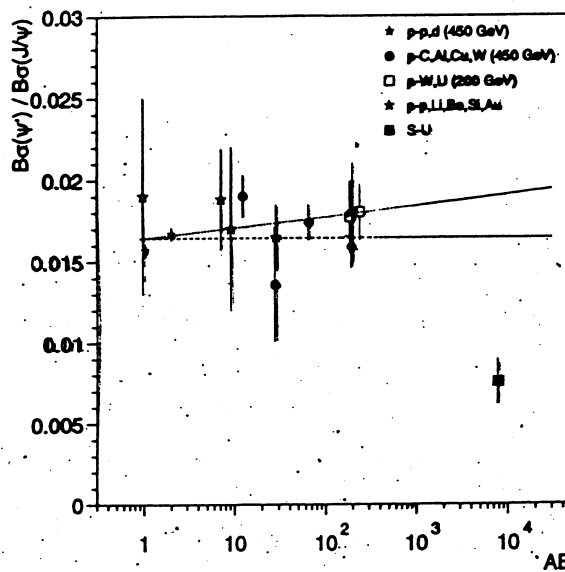
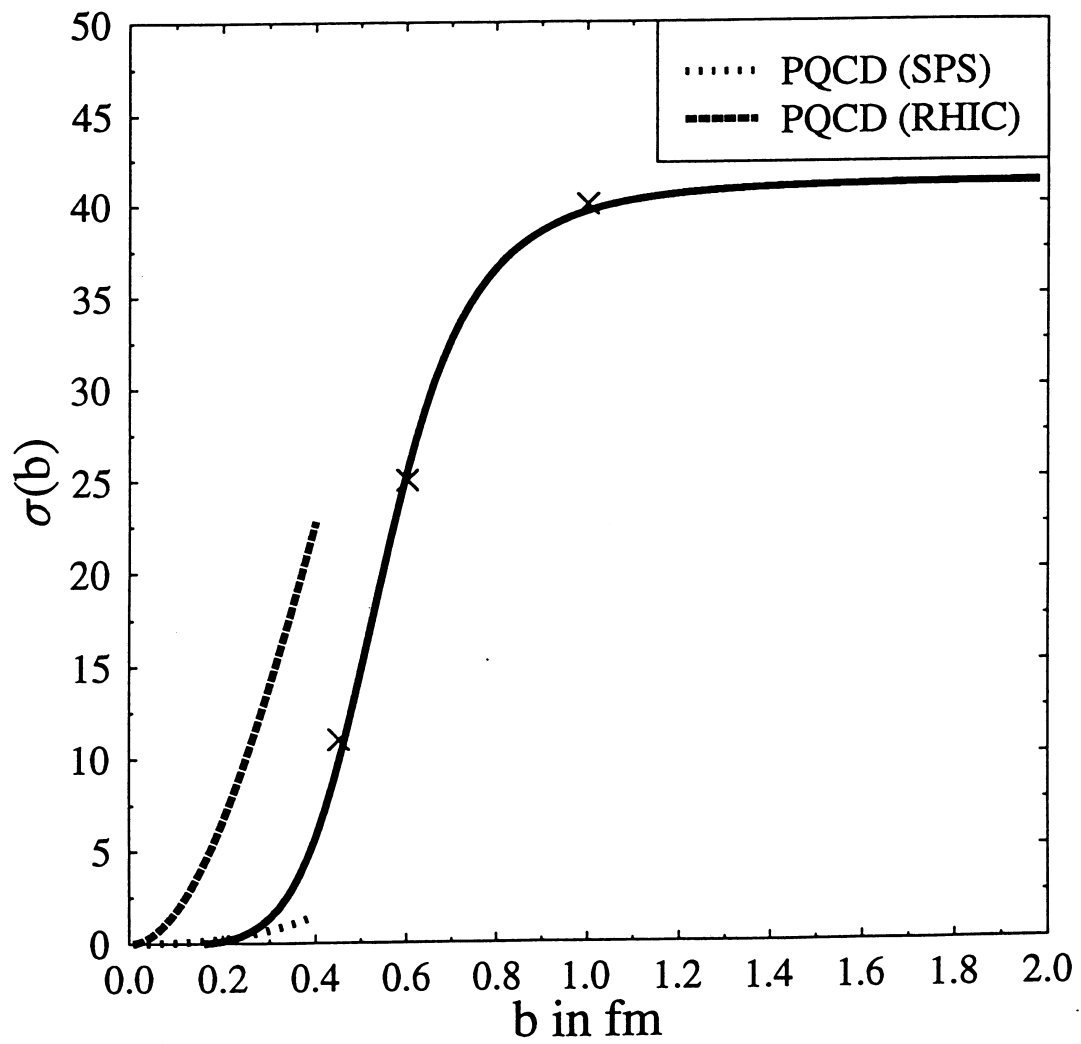


Figure 4: Ratio between  $\psi$  and  $J/\psi$  production cross-sections,  $B'_{\mu\mu}\sigma^{\psi} / B_{\mu\mu}\sigma^{\psi}$ , as a function of  $A \times B$ . See the text for the meaning of the lines.

$$\Rightarrow \sigma(\psi/N) = 20 \text{ mb}$$

agrees well with our predictions.



for  $E_\gamma \sim 20 \text{ GeV}$  leads to  $\sigma_{\text{hard}} \leq 0.2 \text{ mb}$

Recent analysis L. Gerland, F.S, Stöcker, Greife  
 dominant contribution from large  
 transverse  $c\bar{c}$  separations. Matching  
 pQCD for small  $b$ , and soft QCD  
 for  $b \approx 0.3 \text{ fm}$

$\sigma_{\psi N} = 3.6 \text{ mb}$ ,  $\sigma_{\psi' N} = 20 \text{ mb}$

$\sigma_{\chi_{c10} N} = 6.8 \text{ mb}$   $\sigma_{\chi_{c11}} = 15.8 \text{ mb}$   
 $m=0$   $m=1$

Allows to explain  $3/\psi$  A-dependence  
 in pA, BA scattering at CERN

Strong absorption in  $\gamma A \rightarrow \psi' A'$

prediction  $\rightarrow$

$\frac{A_{\text{eff}}}{A}$	0.76	0.551	0.38
A	9	50	200

$\Rightarrow$   $J/\psi$  interaction at intermediate energies is small but not governed by perturbative QCD.

(soft interactions of  $c\bar{c}$  in rare large configurations in  $J/\psi$ )

Need much better  $J/\psi$  data, and  $\psi'$  photoproduction data.

How to look

$$\psi N \rightarrow \psi N$$

$\Rightarrow p_t$  broadening

$$\psi N \rightarrow \psi N^*$$

energy loss

$$\psi N \rightarrow \bar{D}_c \Lambda_c$$

$e\mu$  events?

$$\psi N \rightarrow \psi' N$$

different  $\psi'$  energy

than in  $\delta p \rightarrow \psi' p$

[ $\gamma$  beam much better than electron beam]

$$\psi N \rightarrow \chi N$$

? feasible?  
(since  $\frac{\sigma(\delta p \rightarrow \chi p)}{\sigma(\gamma p \rightarrow \psi p)} \ll 1$ )

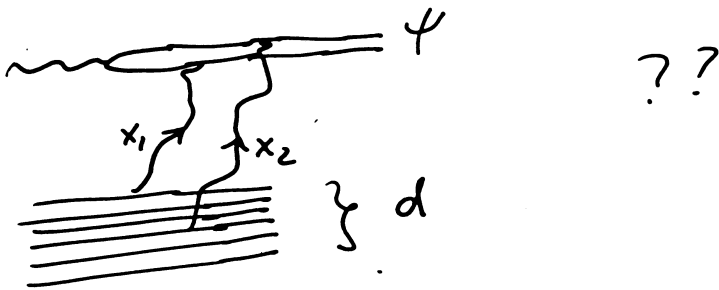
Note  $\psi N \rightarrow \bar{D}_c \Lambda_c$  leads to rather

low velocity  $\Lambda_c \rightarrow \frac{p_{\Lambda_c}}{m_{\Lambda_c}} \sim 0.4$

good chances to form

charm hypernuclei

Close to threshold  $E_\gamma \leq 12.6 \text{ eV}$   
 nuclear short-range correlation effects ??



$x$  is smaller in this case

Example  $E_\gamma = 8.2 \text{ eV}$

$$x(\gamma p) = 0.77$$

$$p_\psi = 6.2 \text{ eV}$$

$$x(\gamma d) = 0.6$$

$$p_\psi = 7.4 \text{ eV}$$

Threshold  $E_\gamma = m_\psi + \frac{m_\psi^2}{2 m_{\text{eff target}}}$

$$E_\gamma^{(1)} = 8.22 \text{ eV}$$

$$E_\gamma^{(2)} = 5.66 \text{ eV}$$

$$E_\gamma^{(3)} = 4.8 \text{ eV}$$

$$E_\gamma^{(\infty)} = 3.1 \text{ eV}$$

beam dump with  
 6 eV beam. ?!

Note Effect of nuclear enhancement  
should be local [small volume  
of  $\delta$  interaction with  $c\bar{c}$   
production]

$\Rightarrow$  Exotics using lightest nuclei

${}^4\text{He}$ ,  ${}^6\text{Li}$ , ...

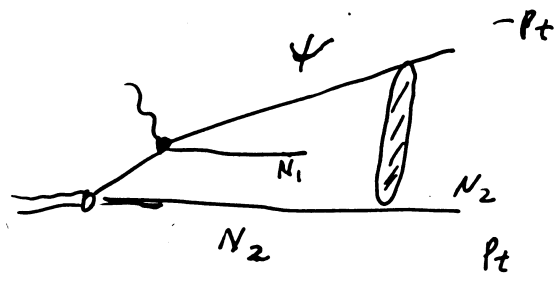
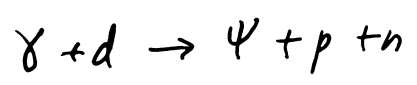
& final state interactions

using  $A \geq 40$  nuclei

Since probability of exotics per nucleon  
in  ${}^{12}\text{C}$  and  $A \sim 200$  rather  
close.



Use of recoil to study  $\gamma/\psi + N$   
 elastic scattering via

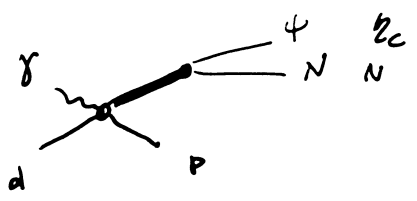


Expect  $d\sigma(\psi N \rightarrow \psi N) / dP_t^2 \propto e^{-4P_t^2}$

- tails to rather large  $P_t$ .

$\theta_{lab} \approx 80^\circ - 70^\circ$

& Look for bound states (Brodsky et al)



Missing mass with  $l^+l^-$   
 trigger.

Note: Structure of recoil.

For threshold ( $E_\gamma = 82$ )  $\gamma + p \rightarrow \psi + p$

$$\underline{p_N \approx 2.6 \text{ eV}}$$

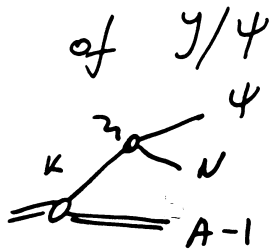
For the same  $E_\gamma$  :  $\gamma + d \rightarrow \psi + d$  :  $p_d = 0.76$

For  $E_\gamma = 11.6 \text{ eV}$

$$p_N \cdot \text{min} = 0.76 \text{ eV}/c$$

$$p_N \perp \text{max} = 1.06 \text{ eV}/c$$

Fermi motion model for production



$k_{\min}(E_\gamma)$  ?

$E_\gamma$ (GeV)	$A=2$ (pair correlations)	$A=4$
5.5		0.57
5.8	0.74	0.50
6	0.53	0.39
6.5	0.32	0.27
7	0.19	0.17
7.5	0.1	0.09

$\Rightarrow$  For  $E_\gamma \approx 7.6 \text{ GeV}$

$$\sigma_{\gamma A \rightarrow \psi X} / A \approx \sim (10^{-2} - 10^{-1}) \text{ nb}$$

$\Rightarrow$   $A$ -dependence in the impulse approximation model may be strongly  $E_\gamma$ -dependent.

for  $E_\gamma \leq 5.56 \text{ eV}$  — short range correlations dominate

$E_\gamma \geq 76 \text{ eV}$  mean field

Caveats : (i) collective initial interactions:

- 2 gluons from two different nucleons

(ii) Attraction in the final state



Bound states??

Comment on open charm production.

Threshold for  $\gamma + p \rightarrow \bar{D}^0 + \Lambda_c \leftarrow E_\gamma = 8.76 \text{ eV}$

corresponds to  $p_{D^0}, p_{\Lambda_c} \sim 4-56 \text{ eV}/c$ .

Data: SLAC  $E_\gamma \sim 206 \text{ eV}$

$\bar{D} \Lambda > D \bar{D}$

- How large is  $\sigma$  for  $E_\gamma \sim 10 \text{ keV}$ ??
- For  $\bar{D}$  - would  $\Lambda_c$  be polarized.
- small partial branchings  $\Rightarrow$  trigger?
- semileptonic decays?

Nuclei  $\Rightarrow$  A-dependence of  $D, \Lambda_c$

Expect  $\rho_{\text{coh}}$  small  $\Rightarrow$  measure

$\sigma_{DN}, \sigma_{\Lambda_c N}$   
 $\downarrow \quad \quad \downarrow$   
12-15 mb    25-30 mb

Naive  
expectation

Strong A-dependence, change of  
the momentum distribution.

## $\Sigma\Sigma$ Study of charmonium photoproduction

- Unique source of information about "charmonium - nucleon" interaction - heavy quark QCD
- Connection to heavy ion physics.