

**Kaon Condensation in Hyperonic Matter  
and Properties of Neutron Stars**

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**1. Introduction**

Strangeness in highly dense matter

- kaon condensation (in neutron stars)  
softening of EOS,  
thermal evolution (cooling via neutrino emission)

KN interaction in nuclei

K<sup>-</sup> optical potential

- KN data, kaonic atom data
- Subthreshold K<sup>+</sup> K<sup>-</sup> production in H.I.C  
in p-nucleus collisions

Search for deeply bound K<sup>-</sup> nuclear states

[Y. Akaishi and T. Yamazaki, Phys. Rev. C65 (2002) 044005.  
A. Dote, Y. Akaishi et al., nucl-th/0207085. ]

[T. Kishimoto, Phys. Rev. Lett. 83(1999)4701. ]

[M. Iwasaki et al., Nucl. Instrum. Methods Phys. Res. A 473(2001) 286.]

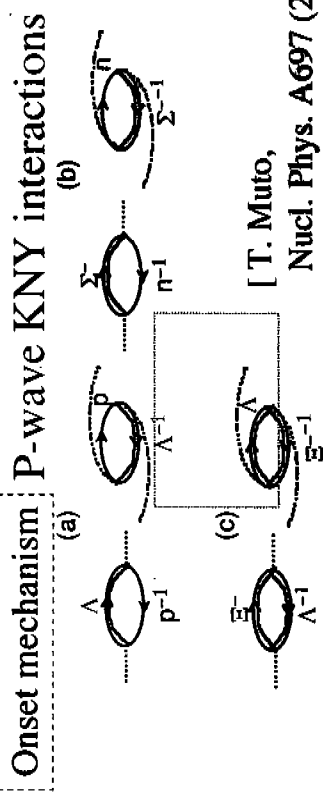
- hyperonic matter  
( $\Lambda$ ,  $\Sigma^-$ , ... in the ground state of neutron-star matter)

$$\rho_B^C = 2 \sim 4 \rho_0$$

[ M. Baldo, G.F. Burgio, H.J. Schulze,  
Phys. Rev. C61(2000), 055801.  
I. Vidana et al., Phys. Rev. C62 (2000), 035801.  
S. Nishizaki, Y. Yamamoto, T. Takatsuka,  
Prog. Theor. Phys. 105(2001), 607. ]

Interplay between kaon condensation  
and hyperons through kaon-baryon interaction

kaon condensation in hyperonic matter



[ T. Muto,  
Nucl. Phys. A697 (2002), 225. ]

Condensation of ( $\Xi^- \Lambda^{-1}$ )-(p  $\Lambda^{-1}$ ) or  
( $\Sigma^- n^{-1}$ )-(p  $\Lambda^{-1}$ ) pairs

Equation of state

We study the equation of state of the kaon-condensed phase  
and clarify the resulting properties of neutron stars.

Possibility of a (metastable) kaon-condensed self-bound star

## 2. Formulation

$SU(3)_L \times SU(3)_R$  chiral effective Lagrangian

[D. B. Kaplan and A. E. Nelson, Phys. Lett. B 175 (1986) 57.]

$$\mathcal{L} = \frac{1}{4} f^2 \text{Tr} \partial^\mu \Sigma^\dagger \partial_\mu \Sigma + \frac{1}{2} f^2 A_{\text{ssb}} (\text{Tr} M (\Sigma - 1) + \text{h.c.})$$

$$+ \text{Tr} \bar{\Psi} (i \not{\partial} - m_B) \Psi + \text{Tr} \bar{\Psi} i \gamma^\mu [V_\mu, \Psi] + D \text{Tr} \bar{\Psi} \gamma^\mu \gamma^5 [A_\mu, \Psi]$$

$$+ F \text{Tr} \bar{\Psi} \gamma^\mu \gamma^5 [A_\mu, \Psi] + a_1 \text{Tr} \bar{\Psi} (\xi M^\dagger \xi + \text{h.c.}) \Psi$$

$$+ a_2 \text{Tr} \bar{\Psi} \Psi (\xi M^\dagger \xi + \text{h.c.}) + a_3 (\text{Tr} M \Sigma + \text{h.c.}) \text{Tr} \bar{\Psi} \Psi,$$

Baryons  $\Psi \rightarrow (p, \Lambda, n, \Sigma^-)$   $M = \text{diag}(m_u, m_d, m_u)$

Meson fields ( $K^\pm$ )  $f = 93 \text{ MeV}$

$$\Sigma \equiv e^{2i\Pi/f} \quad \xi \equiv \Sigma^{1/2} = e^{i\pi_a T_a / f}$$

$$\Pi = \pi_a T_a = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 & 0 & K^+ \\ 0 & 0 & 0 \\ K^- & 0 & 0 \end{pmatrix} \quad V^\mu = \frac{1}{2} (\xi^\dagger \partial^\mu \xi + \xi \partial^\mu \xi^\dagger)$$

$$A^\mu = \frac{i}{2} (\xi^\dagger \partial^\mu \xi - \xi \partial^\mu \xi^\dagger)$$

Classical kaon field

$$K^{\pm, \text{cl}}(\mathbf{r}, t) = \frac{f}{\sqrt{2}} \theta e^{\pm i(\mu t - \mathbf{k} \cdot \mathbf{r})}$$

$\Theta$ : chiral angle,  $\mu$ : chemical potential,  $\mathbf{k}$ : momentum

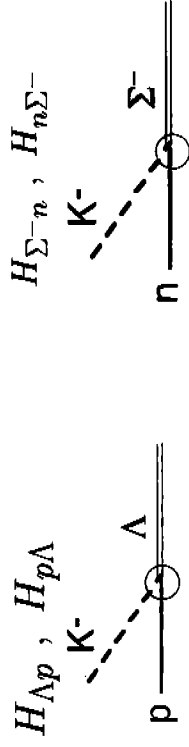
Effective Hamiltonian

$$\mathcal{H}_{\text{eff}} = \mathcal{H} + \mu(\rho_Q^B - \rho_Q^K - \rho_Q^e) = \mathcal{H}_{\text{eff}}^B + \mathcal{H}_{\text{eff}}^M + \mathcal{H}_{\text{eff}}^e$$

Baryonic part

$$H_{\text{eff}}^+ = \begin{pmatrix} \Lambda & P & \Sigma^- & n \\ H_{\Lambda\Lambda} & H_{\Lambda p} & 0 & 0 \\ H_{p\Lambda} & H_{pp} & 0 & 0 \\ 0 & 0 & H_{\Sigma-\Sigma^-} & H_{\Sigma-n} \\ 0 & 0 & H_{n\Sigma^-} & H_{nn} \end{pmatrix} \begin{pmatrix} \Lambda \\ P \\ \Sigma^- \\ n \end{pmatrix}$$

P-wave  $K^-$ -baryon int.



$$\text{KNY vertex renormalization } F = \frac{\Lambda^2 - m_K^2}{\Lambda^2 + \mathbf{k}^2} \quad (\Lambda = 1 \sim 2 \text{ GeV})$$

[B. Holzenkamp, K. Holinde and J. Speth, Nucl. Phys. A 500 (1989) 485.]

S-wave  $K^-$ -baryon int.



• KN-sigma term (scalar)

(Explicit chiral symmetry breaking)

• Tomozawa-Weinberg term (vector)

Quasi-particles

$$|\tilde{\Lambda}_\pm\rangle = \cos \phi \cdot |\Lambda_{\pm 1/2}\rangle \pm i \sin \phi \cdot |p_{\pm 1/2}\rangle$$

$$|\tilde{n}_\pm\rangle = \cos \phi' \cdot |n_{\pm 1/2}\rangle \pm i \sin \phi' \cdot |\Sigma_{\pm 1/2}^-\rangle$$

# Baryon - Baryon Interactions

Potential energy density  $\mathcal{E}_{pot}(\rho_\Lambda, \rho_p, \rho_\Sigma, \rho_n)$

[S. Balberg and A. Gal, Nucl. Phys. A625 ('97) 435]

$$V_i = \partial \mathcal{E}_{pot} / \partial \rho_i$$

$\Rightarrow$  Baryon potential

( $i = \Lambda, P, \Sigma, n$ )

$$H_{ii} \rightarrow H_{ii} = H_{ii} + V_i$$

## Baryon part

$$\mathcal{E}_{eff}^{B} = \sum_i \sum_{|p| \leq |p_F(i)} \sum_{\sigma = \pm 1/2} E_i^{(i)}(p) + \mathcal{E}_{pot} - \sum_{i=p, \Lambda, \Sigma, n, \Sigma} V_i \rho_i$$

## meson part

$$\mathcal{E}_{eff}^M = -\frac{1}{2} f^2 (\mu^2 - k^2) \sin^2 \theta + f^2 m_K^2 (1 - \cos \theta)$$

## lepton part

$$\mathcal{E}_{eff}^e = \frac{\mu^4}{4\pi^2} - \mu \frac{\mu^3}{3\pi^2} = -\frac{\mu^4}{12\pi^2}$$

total energy density

$$\mathcal{E}_{eff} = \mathcal{E}_{eff}^B + \mathcal{E}_{eff}^M + \mathcal{E}_{eff}^e$$

Given  $\mu_B$ ,  $\frac{\partial \mathcal{E}_{eff}}{\partial \rho_i} = 0$  ( $i = \Lambda, P, \Sigma, n$ )

$$\mu_\Lambda = \mu_P = \mu_\Sigma = \mu_n = \mu$$

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Parameters

$$\delta = \gamma = 5/3$$

Saturation property of symmetric nuclear matter

$$\rho_0 = 0.16 \text{ fm}^{-3}$$

$$\text{binding energy} = 16 \text{ MeV}$$

$$a_{NN} = -859.5 (\text{MeV} \cdot \text{fm}^3)$$

$$c_{NN} = 1300.8 (\text{MeV} \cdot \text{fm}^{3\gamma})$$

symmetry energy at  $\rho_0$

$$b_{NN} = 212.8 (\text{MeV} \cdot \text{fm}^3)$$

depth of  $V_\Lambda = -27 \text{ MeV}$

$$a_{\Lambda N} \rho_0 + c_{\Lambda N} \rho_0^\gamma = -27 \text{ MeV}$$

$\Lambda$  single-particle orbitals  $\downarrow$

$$a_{\Lambda N} = -387.0 (\text{MeV} \cdot \text{fm}^3)$$

$$c_{\Lambda N} = 738.8 (\text{MeV} \cdot \text{fm}^{3\gamma})$$

[D. J. Millener, C. B. Dover and A. Gal, Phys. Rev. C38 (1998), 22700. ]

$V_{\Sigma^-}$  potential

[J. Dabrowski,

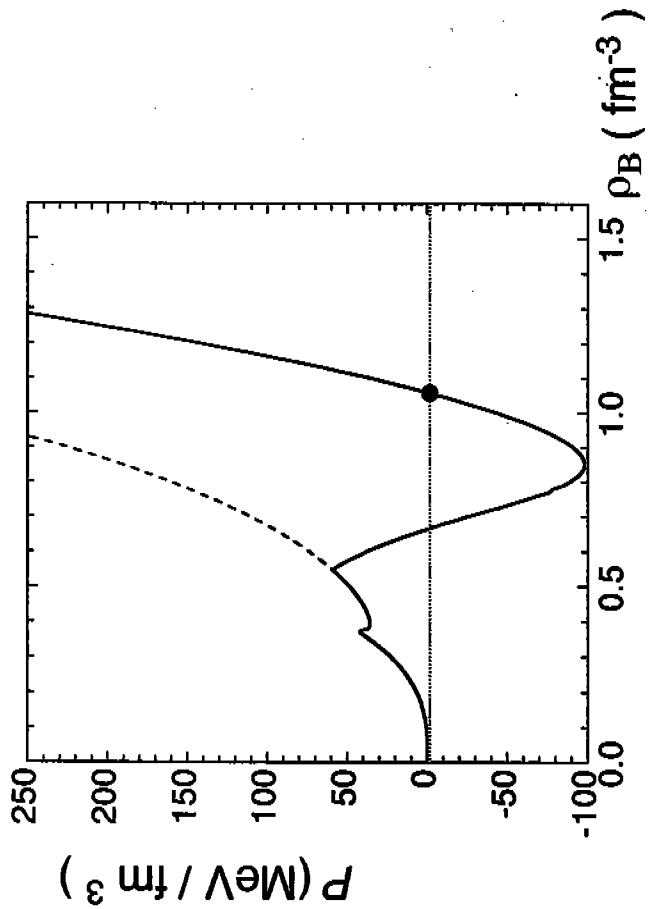
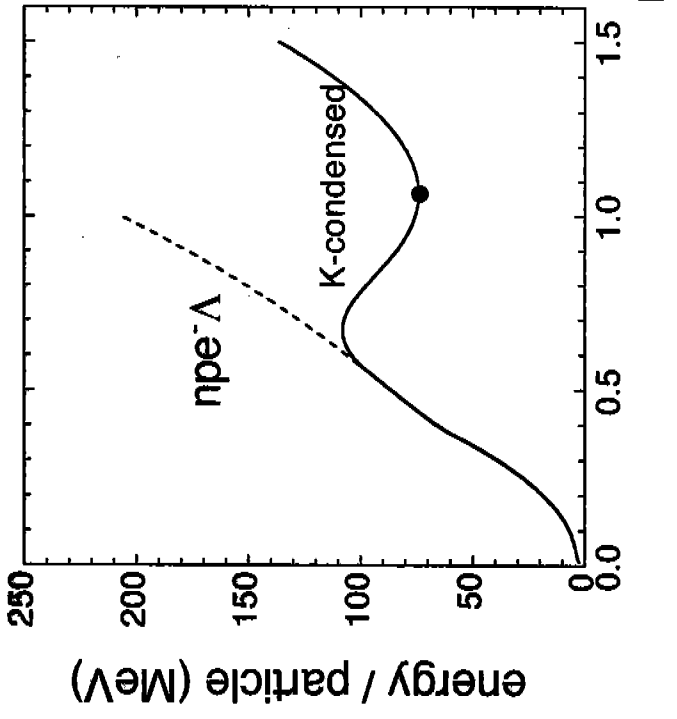
(1) repulsive case Phys. Rev. C60 (1999), 025205. ]

$$V_{\Sigma^-}(k_\Sigma) = V_0(k_\Sigma) - \frac{1}{2} V_1(k_\Sigma) \cdot \frac{Z-N}{A}$$

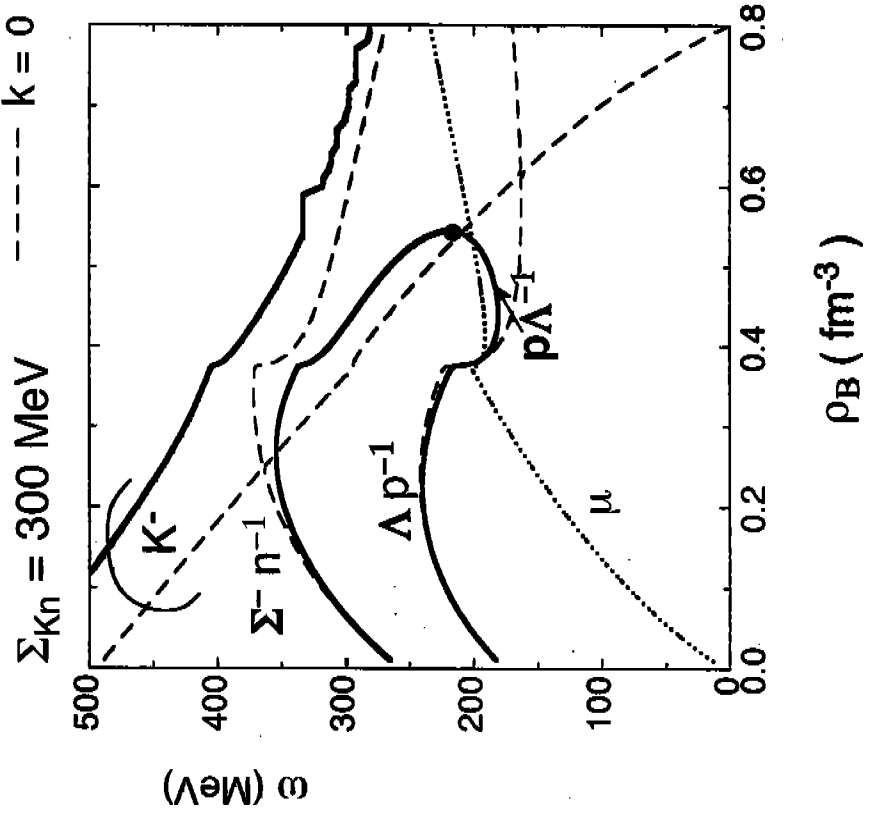
$$a_{\Sigma N} \rho_0 + c_{\Sigma N} \rho_0^\gamma = V_0 = 23.5 \text{ MeV}$$

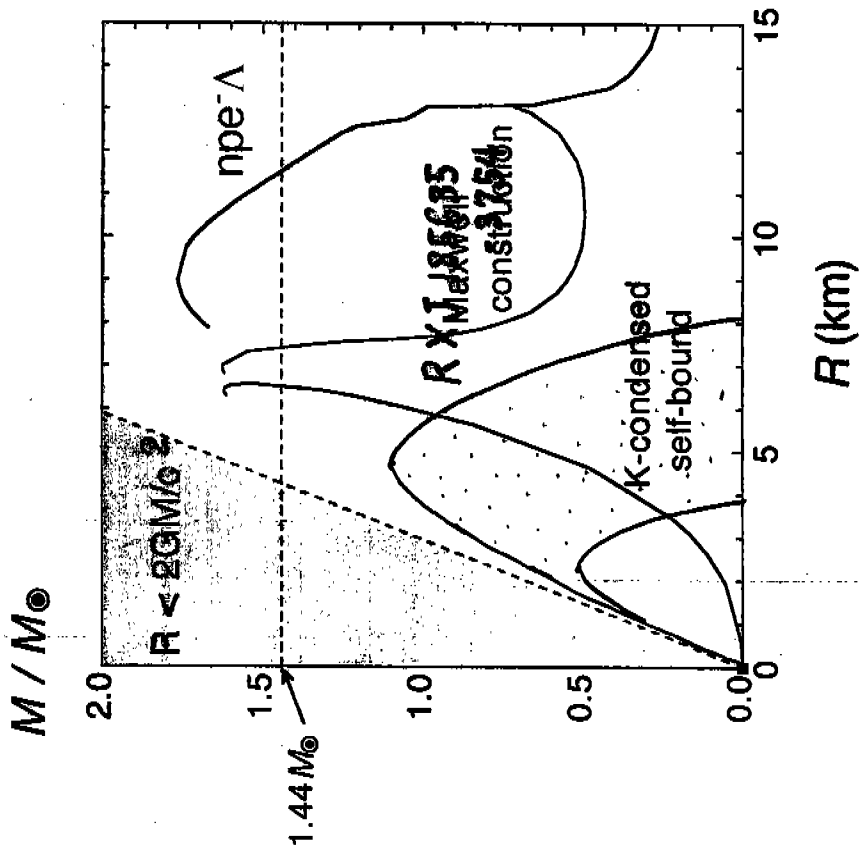
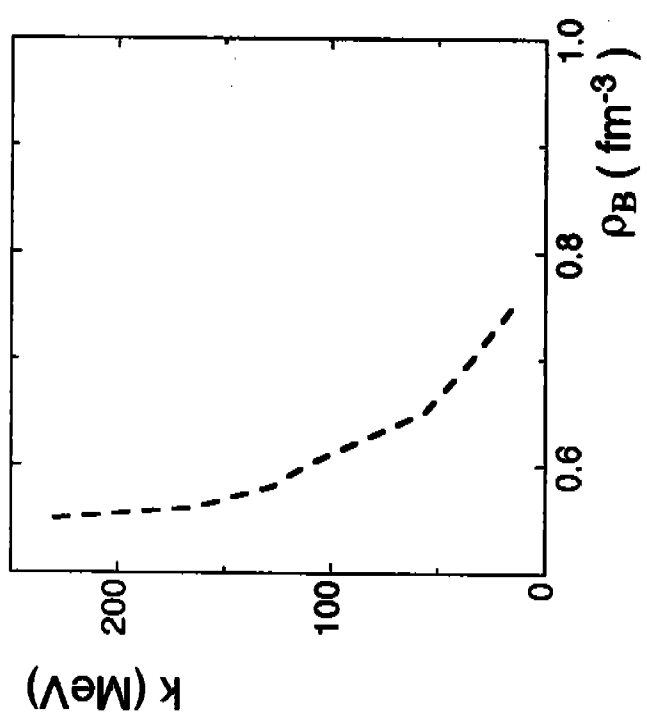
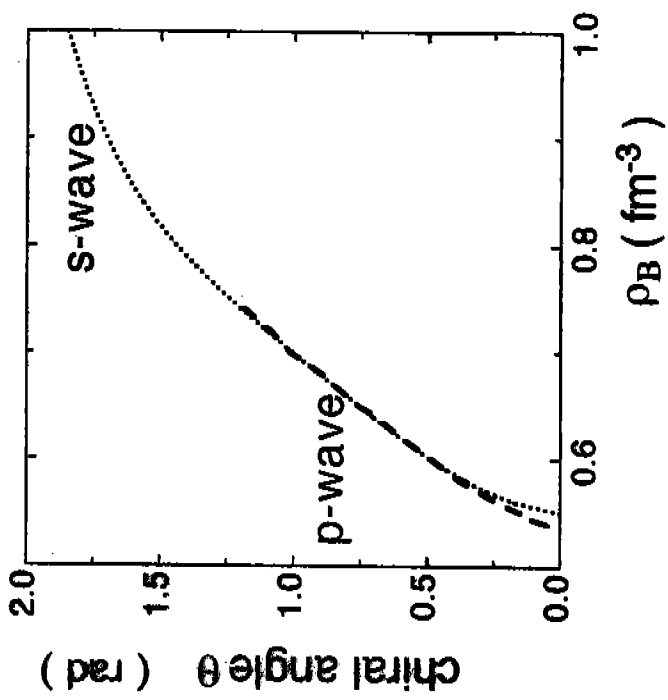
$$b_{\Sigma N} \rho_0 = \frac{1}{2} V_1 = 40.2 \text{ MeV}$$

$\Sigma_{Kn} = 305$   
MeV



—  $k = 250$  MeV  
- - -  $k = 0$  MeV





[ J. J. Drake et al.,

*Astrophys. J.* 572 (2002) 996.

$$R_{\infty} = \frac{R}{\sqrt{1 - 2GM/Rc^2}}$$

#### 4. Summary and concluding remarks

We have studied the equation of state (EOS) with kaon condensation in hyperonic matter and its effects on neutron-star structure. We have taken into account the p-wave kaon-baryon interactions as well as the s-wave ones on the basis of chiral symmetry, and have used the nonrelativistic effective baryon-baryon interactions.

##### Results

At a critical density, ( $\rho_B^C \sim 3.5 \rho_0$ )

The system becomes unstable with respect to a pair creation of collective modes with  $K^+$  and  $K^-$  quantum numbers (pair condensation), which originates from the p-wave kaon-baryon interactions.

**EOS of the condensed phase**

- In the well-developed phase, the s-wave kaon-baryon attractions are dominant as compared with the p-wave ones.
- much softening due to kaon condensation in addition to that due to hyperons

The energy of the system has a local minimum with respect to a baryon number density.

The pressure becomes negative in certain density interval.

→ Possibility of a (metastable) kaon-condensed self-bound star

→ Kaon dynamics in highly dense matter

##### Future problems

Suppression effects of softening of EOS

- relativistic effects  
(suppression of the s-wave scalar attraction at high densities)

##### RMF theories

[ H. Fujii, et al., Nucl. Phys. A 597 (1996) 645.

S. Banik and D. Bandyopadhyay,

Phys. Rev. C 64 (2001) 055805.

Phys. Rev. C 66 (2002) 065801. ]

- form of effective baryon-baryon interactions  
repulsive three-body forces between hyperons and nucleons  
[ S. Nishizaki, Y. Yamamoto and T. Takatsuka,  
Prog. Theor. Phys. 108 (2002) 703. ]

- short-range correlations between baryons  
[ E. E. Kolomeitsev and D. N. Voskresensky,  
Phys. Rev. C 68 (2003) 015803. ]

Subthreshold baryons  $\Lambda(1405)$ ,  $\Sigma(1385)$  . .

Formation scenario

for a self-bound kaon-condensed star