Equilibrated Self-Consistent Calculation of Neutron Star and Generalized 3-Baryon Forces

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EOS of Dense Baryonic Matter

Phenomenological studies

- **Observed Properties of Neutron Stars(at low T)**
- Relativistic Heavy Ion Collisions(at high T)
- Theoretical studies at low T
 - **Non-relativistic G-matrix Calculations**
 - **Relativistic Dirac Approach**
 - **Relativistic Mean Field Approach**

Theoretical EOS may be too soft at low T

The G-matrix Calculations

Realistic Two-baryon Interactions Well-established at around Normal Density

Merits

Relativistic effectsDemeritsMany-body forcesApplicability at High Baryon DensitiesOne of the necessary conditions of the applicability:
Three-body forces can be treated as perturbationG-matrix calculations provide realistic results at up to 4-5ρ₀By only this method, we cannot discuss the whole of
neutron star.

Self-Consistency in baryonic matter calculation

For a given set of densities for constituent baryons, the single particle potentials(SPP) are determined by the solutions of the B-G equations which depend on SPP. (only the strong interaction is considered)

For a given total baryon number density,

baryon compositions are determined by chemical equilibrium, depending on SPP. SPP for each baryon is determined by the B-G equation which depends on both baryon compositions and SPP.

Equilibrated G-matrix calculation

A calculating method(not a new theoretical approach)

A given baryon density SPP:Single Particle Potentials Trial SPP(=0) Initial k_F Weak interaction

Iteration (chemical equilibrium)

New SPP

Strong interaction

At all densities, SPP for all baryons at bottom of Fermi sea are calculated. It is essential to determine correct thresholds of appearance of baryons.

The B-G equations

Results of Calculations

Compositions of Equilibrated Baryonic Matter

NN,YN,YY interactions:

NSC97e





Single Particle Potentials in Equilibrated Baryonic Matter

NN,YN,YY interactions:

NSC97e

NSC89



The point is that this method calculates the compositions and single particle potentials for all species in baryonic matter simultaneously.

Generalized 3-Baryon Forces

NNN 3-body force has a long history Fujita-Miyazawa force Brazil model(H.T. Coelho, T.K.Das, M.R. Rabilotta; M.R. Rabilotta, M.P.Isidro Filho) Tucson-Melbourne model(S.A.Coon et al.; B.G. Ellis, S.A.Coon, B.H.J. McKellar) Phenomenological pion-nucleon scattering amplitudes Δ mechanism, ρ -meson exchange mechanism BBB 3-Body Forces in high-density baryonic matter Phenomenological approach is difficult. Model-dependent approach is available. (The SU(3) model)

Generalized Δ -mechnism



 G_{mBD} and g_{mBB} , satisfy the SU(3) symmetry

3BF in static approximation

$$a = \frac{2}{3} \frac{2M_{\Delta} + M_{3} + M_{3}^{'}}{2M_{\Delta}^{2} - M_{3}^{2} - M_{3}^{'2}} + \frac{(M_{3}^{2} - M_{3}^{'2})^{2}}{12M_{\Delta}^{2}} \frac{2M_{\Delta} + M_{3} + M_{3}^{'}}{(2M_{\Delta}^{2} - M_{3}^{2} - M_{3}^{'2})^{2}}$$

$$b = -\frac{1}{12} \frac{2M_{\Delta} + M_{3} + M_{3}^{'}}{2M_{\Delta}^{2} - M_{3}^{2} - M_{3}^{'2}} \frac{(M_{3} + M_{3}^{'})^{2}}{M_{3}M_{3}^{'}} + \frac{(M_{3} - M_{3}^{'})^{2}(M_{3} + M_{3}^{'})^{2}(2M_{\Delta} - M_{3} - M_{3}^{'})}{48M_{\Delta}^{2}M_{3}M_{3}^{'}(2M_{\Delta}^{2} - M_{3}^{'2} - M_{3}^{'2} - M_{3}^{'2})}$$

$$G = \frac{(M_{1} + M_{1}^{'})^{2}(M_{2} + M_{2}^{'})^{2}}{12M_{1}M_{1}^{'}M_{2}M_{2}^{'}} G_{m'B3'\Delta}G_{mB3\Delta}g_{mB1'B1}g_{m'B2B2'}$$

$$W(1,2;3) = -G \frac{\overline{m}\overline{m'}}{(4\pi)^2} (\sigma_1 \cdot \nabla_{31}) (\sigma_2 \cdot \nabla_{23}) \{ a(\nabla_{31} \cdot \nabla_{23}) + bi\sigma_3 \cdot (\nabla_{31} \times \nabla_{23}) \} U(\overline{m}, r_{31}) U(\overline{m'}, r_{23}) \}$$

$$\overline{m} = (m^2 - (M_1 - M_1)^2)^{1/2}, \quad \overline{m}' = (m'^2 - (M_2 - M_2)^2)^{1/2}$$

Effective meson mass (< Free mass)

 $\Lambda = 5.0 \text{fm}^{-1} (= 986.6 \text{MeV})$

SU3-Model for Meson-Octet-Decuplet Coupling

Phenomenological evidence for the SU(3) model

N.P. Samios, M. Goldberg and B.T. Meadows Rev. Mod. Phys. Vol.46, p49, 1974.

The SU3-Model for Meson-Octet-Decuplet Coupling is confirmed.

10 irreducible representation:

 $\begin{array}{l} T_{[ab]}{}^{(cd)} = \psi_{[a}{}^{(c} \, \phi_{b]}{}^{d)} - (\text{Trace part}) \\ (cd): symmetrized \qquad [ab]: antisymmetrized \\ L_{int} = - \ G \ \Psi^{(abc)} \epsilon^{(akl} T_{[kl]}{}^{(bc))} \\ \Psi: \text{ decuplet baryons, } \quad \psi: \text{ octet baryons, } \quad \phi: \text{ octet mesons} \end{array}$

Contribution of 3BF to potential energy density

 $\mathbf{R} = \mathbf{V}(\mathbf{3BF})/\mathbf{V}(\mathbf{2BF}+\mathbf{3BF}) \coloneqq \mathbf{1} \ \% \sim \mathbf{1} \ \mathbf{0} \ \% \ \text{for} \ \mathbf{2\rho_0} \sim \mathbf{5\rho_0}$ V(3BF) $\propto \rho_{B1}\rho_{B2}\rho_{B3}$ rapidly increases with densities

But the results shown here is very preliminary: Only lowest order and only S-wave contributions, only pseudoscalar mesons are considered.





'nnn' is omitted here!

Summary

A New Calculating Method

Equilibrated G-matrix calculation, which determines the compositions and SPP simultaneously.

Generalized 3-Baryon Forces

Decuplet baryon excitation <- the SU(3) model Very preliminary result:

V(3BF)/V(2BF+3BF) = 1-10% for $2-5\rho_0$ only S-wave +higher partial waves, nnn lowest order +next order pseudoscalar +vector mesons

Chemical Equilibrium, Charge Neutrality and Baryon Number Density

 $\mu_{b} = m_{b} + k_{Fb}^{2}/2m_{b} + U_{b} (k_{Fb})$ for baryons (non-rela. approx.) $\mu_{e} = [m_{e}^{2} + k_{Fe}^{2}]^{1/2}, \ \mu_{\mu} = [m_{\mu}^{2} + k_{F\mu}^{2}]^{1/2} :$ for e⁻, μ^{-} (relativistic) Equilibrium Conditions:

$$\begin{split} \boldsymbol{\mu}_{p} &= \boldsymbol{\mu}_{\Sigma^{+}} = \boldsymbol{\mu}_{n} - \boldsymbol{\mu}_{e} \\ \boldsymbol{\mu}_{\Lambda} &= \boldsymbol{\mu}_{\Sigma 0} = \boldsymbol{\mu}_{\Xi 0} = \boldsymbol{\mu}_{n} \\ \boldsymbol{\mu}_{\Sigma^{-}} &= \boldsymbol{\mu}_{\Xi^{-}} = \boldsymbol{\mu}_{n} + \boldsymbol{\mu}_{e} \\ \boldsymbol{\mu}_{\mu} &= \boldsymbol{\mu}_{e} \end{split}$$

10 k_F are determined by 10 conditions

Charge neutrality condition:

 $k_{Fp}{}^3 + k_{F\Sigma +}{}^3 = k_{F\Sigma -}{}^3 + k_{F\Xi -}{}^3 + k_{Fe}{}^3 + k_{F\mu}{}^3$ Baryon Number Density:

 $\rho_{b} = (k_{Fp}^{3} + k_{Fn}^{3} + + k_{F\Lambda}^{3} + k_{F\Sigma-}^{3} + k_{F\Sigma0}^{3} + k_{F\Sigma+}^{3} + k_{F\Xi-}^{3} + k_{F\Xi0}^{3})/3\pi^{2}$

Potential Energy Densities in equilibrated baryonic matter

V(2BF+3BF) in MeV/fm³ NN,YN,YY interactions:

NSC97e





-30MeV/fm³ at around 5ρ₀