

# IN-MEDIUM EFFECTS ON THE $K^-/K^+$ RATIO AT GSI

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## Outline of Talk

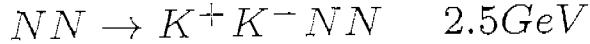
1.  $K^-/K^+$  ratio: medium effects?
2. Thermal models:  $K^+/K^-$  ratio
3. In-medium properties of  $K^-$
4. Results for  $K^+/K^-$  ratio at GSI
5. Conclusions

## $K^-/K^+$ ratio: medium effects?

HEAVY-ION COLLISIONS at GSI (1-2 AGeV):

$K^-$  in hot and dense matter<sup>a</sup>

- $K^-/K^+$  ratio: enhancement at energies below threshold ( $pp \leftrightarrow \text{nucleus-nucleus}$ )



- $K^-/K^+ \sim ct$  for C+C , Ni+Ni , Au+Au

Absorption  $K^-$  via  $K^- N \rightarrow Y\pi$  suppressed  
and/or enhanced  $K^-$  production

- Centrality independence of  $K^-/K^+$  ratio
  - $K^+$  and  $K^-$  yields strongly correlated <sup>b</sup>
  - Thermal models: free particles and volume cancels out exactly. <sup>c</sup>
  - “Broad-band equilibration” by Brown et al.<sup>d</sup>

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<sup>a</sup> Oeschler, *JPG* 28, 1787 (2002); Senger, *NPA* 685, 312 (2001);  
Sturm et al., *JPG* 28, 1895 (2002)

<sup>b</sup> Hartnack et al., *PRL* 90, 102302 (2003)

<sup>c</sup> Cleymans et al., *PRC* 60, 054908 (1999)

<sup>d</sup> Brown et al., *NPA* 690, 184c (2001); *NPA* 698, 483c (2002)

## Thermal models: $K^+/K^-$ ratio

Hadronic Gas Model ( $\mu_B, T$ ) <sup>a</sup>

using CANONICAL scheme for STRANGENESS

$K^+/K^-$  independent of VOLUME



independent CANONICAL OR  
GRAND-CANONICAL treatment

$$\frac{K^+}{K^-} = \frac{Z_{K^+}^1}{Z_{K^-}^1} \frac{Z_{K^-}^1 + Z_{B,S=-1}^1 + Z_{M,S=-1}^1}{Z_{K^+}^1 + Z_{M,S=+1}^1}$$

$K^+/K^- \sim 33$  at 1.93 AGeV in Ni+Ni <sup>b</sup>

Data described: <sup>c</sup>

$$T = 70 \pm 10 \text{ MeV}, \mu_B = 720 \pm 30 \text{ MeV}$$

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<sup>a</sup> Cleymans et al., PLB 485, 27 (2000) and PRC 59 ,1663 (1999)

<sup>b</sup> Menzel et al., PLB 495, 26 (2000)

<sup>c</sup> Cleymans et al., PRC 57, 3319 (1998)

## In-medium properties of $K^-$

$$\frac{K^+}{K^-} = 1 + \frac{Z_\Lambda^1 + Z_\Sigma^1 + Z_{\Sigma^*}^1}{Z_{K^-}^1} \sim e^{\frac{\mu_B + "U_{K^-}"}{T}}$$

- Mean-field for  $\Lambda$  and  $\Sigma$ , and Breit-Wigner for  $\Sigma^*$

$$Z_{\Lambda, \Sigma}^1 = g_{\Lambda, \Sigma} V \int \frac{d^3 p}{(2\pi)^3} e^{-\sqrt{\frac{m_{\Lambda, \Sigma}^2 + p^2}{T}} - U_{\Lambda, \Sigma}(\rho)} e^{\frac{\mu_B}{T}}$$

$$Z_{\Sigma^*}^1 = g_{\Sigma^*} V \int \frac{d^3 p}{(2\pi)^3} \int ds e^{-\sqrt{\frac{p^2 + s}{T}}} \frac{1}{\pi} \frac{m_{\Sigma^*} \Gamma}{(s - m_{\Sigma^*}^2)^2 + m_{\Sigma^*}^2 \Gamma^2} e^{\frac{\mu_B}{T}},$$

- $K^-$  meson in hot and dense matter

- ON SHELL

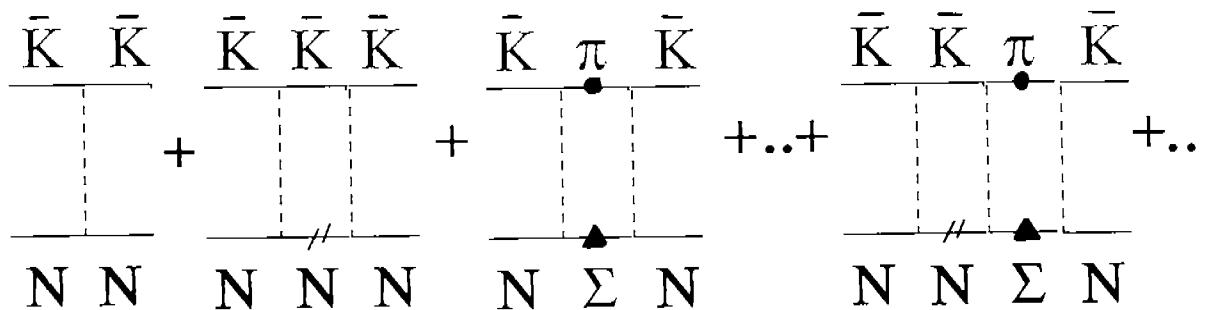
$$Z_{K^-}^1 = g_{K^-} V \int \frac{d^3 p}{(2\pi)^3} e^{-E_{K^-}/T}$$

$$E_{K^-} = \sqrt{m_{K^-}^2 + p^2} + \text{Re } U_{K^-}(p, E_{K^-}, \rho, T),$$

- SPECTRAL DENSITY

$$Z_{K^-}^1 = g_{K^-} V \int \frac{d^3 p}{(2\pi)^3} \int ds S_{\bar{K}}(p, \sqrt{s}, \rho, T) e^{-\sqrt{s}/T}$$

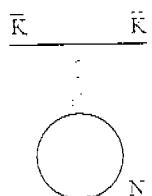
Microscopic calculation of the in-medium  $\bar{K}N$  interaction ( $G$ -matrix) and the  $K^-$  optical potential from  $T = 0$  to  $T$  finite in nuclear matter.



$$G = V + V \frac{Q}{\omega - H_0} V + V \frac{Q}{\omega - H_0} V \frac{Q}{\omega - H_0} V + \dots$$

$$G = V + V \frac{Q}{\omega - H_0} G \quad \text{Bethe-Goldstone eq.}$$

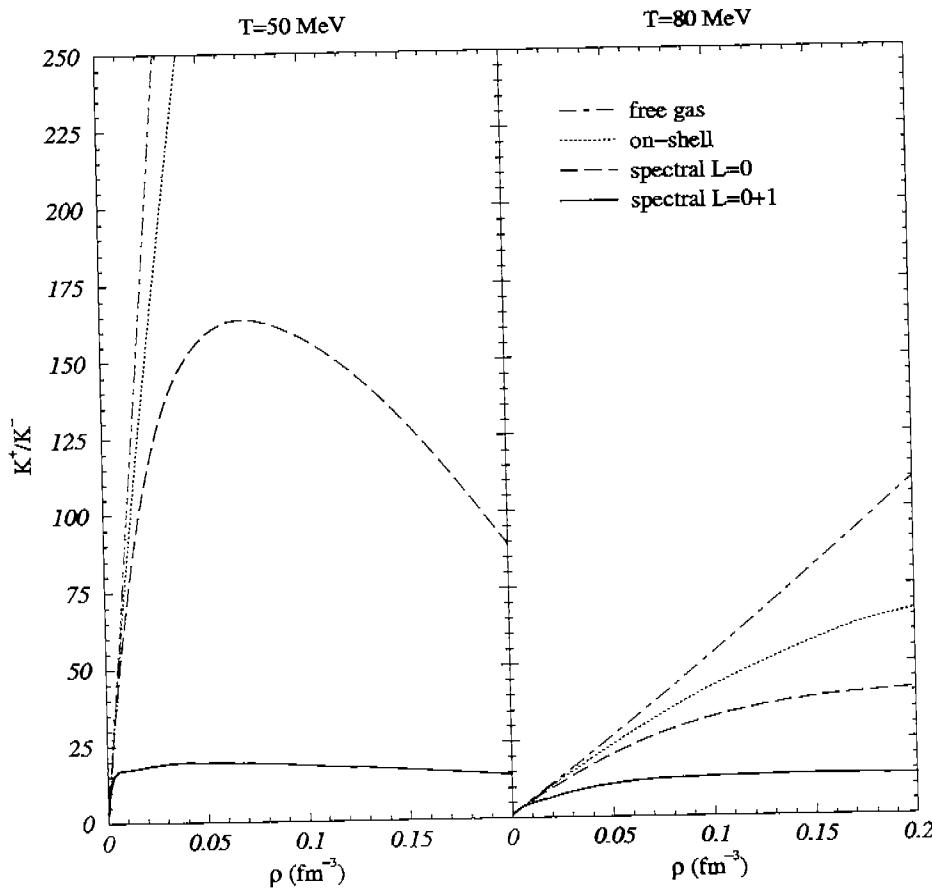
$\bar{K}$  properties



Jülich meson-exchange bare potential  $V$

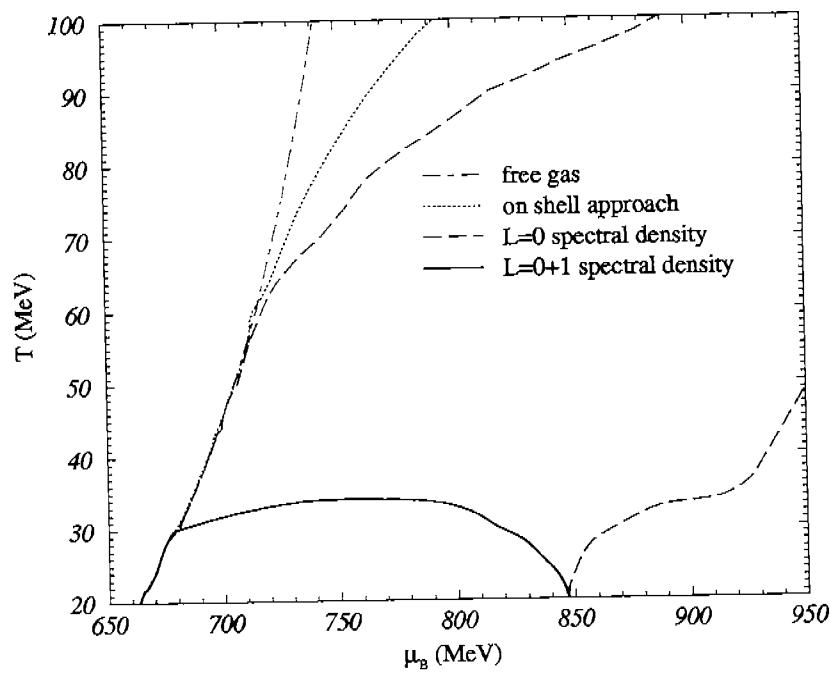
A. Müller et al., Nucl. Phys. A 513, 557 (1990)

## Results for $K^+/K^-$ ratio at GSI

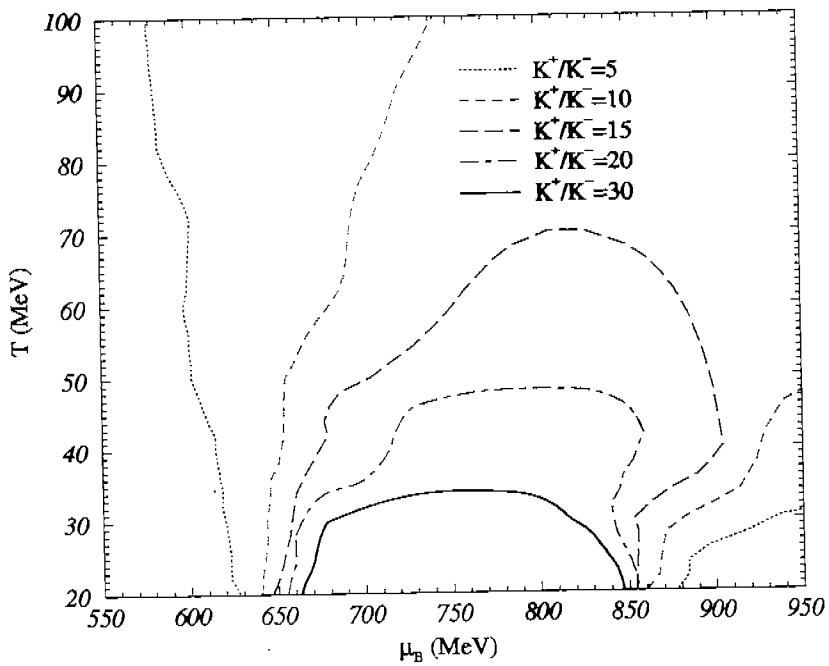


- $K^+/K^-$  ratio grows with  $e^{\mu_B/T}$
- $K^-$  properties in hot and dense matter make the curves bend down
- Inclusion of  $K^-$  spectral density implies additional attraction  $\rightarrow$  qualitative agreement with “Broad-band equilibration”

In-medium effects on the  $K^-/K^+$  ratio..



$T(\mu_B)$  for  $K^+/K^- = 30$  within different approaches



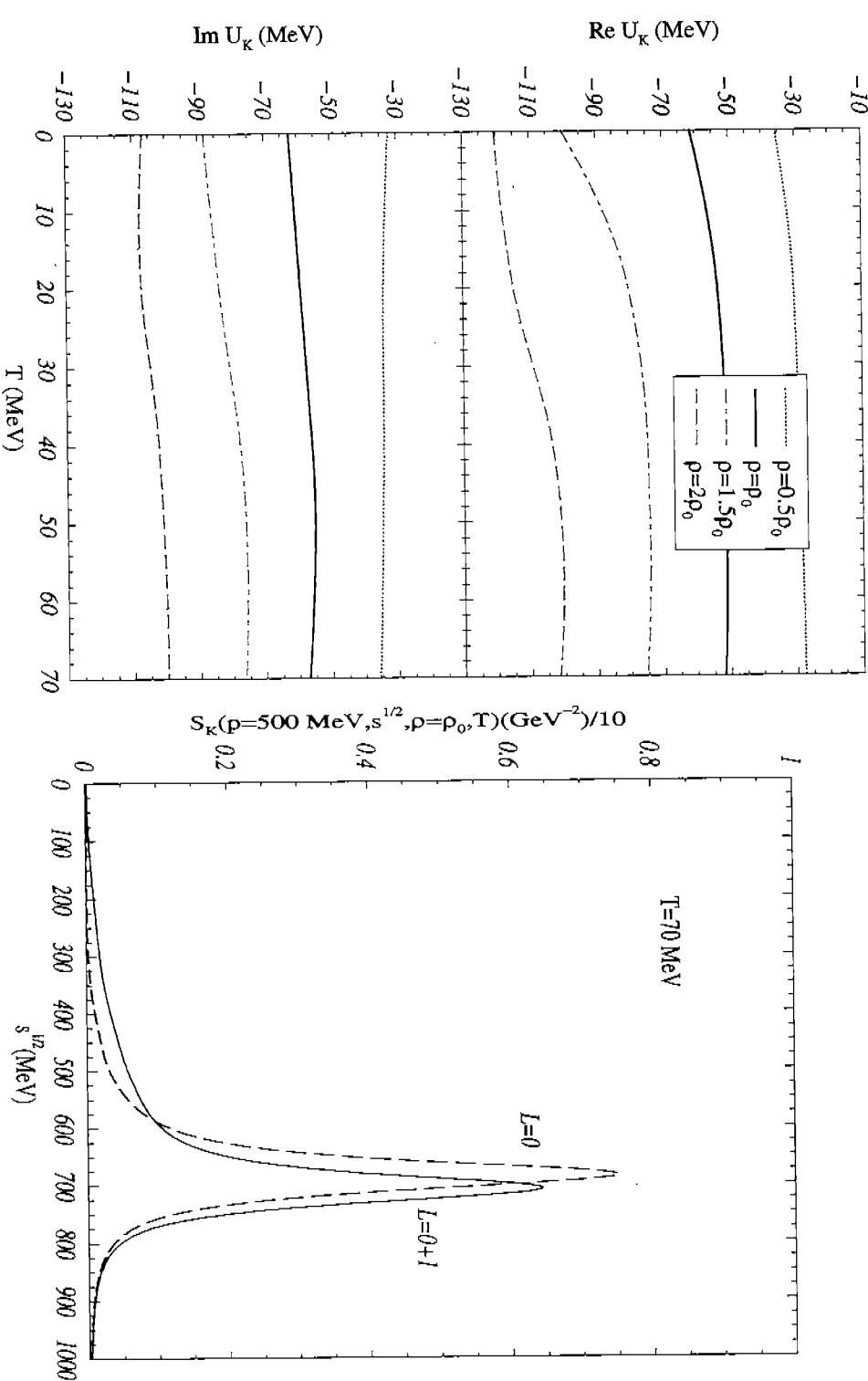
Different  $K^+/K^-$  ratios using the  $K^-$  spectral density

## Conclusions

- $T(\mu_B)$  compatible with  $K^-/K^+$  is very delicate depending very strongly on the approach ( $T \approx 35$  MeV and  $\mu_B \rightarrow 850$  MeV for  $K^+/K^- \approx 30$  with the  $K^-$  spectral density).
- On-shell approach does not achieve Brown's "Broad-band equilibration" because of a stronger increase of  $\mu_B$  with density and a less attractive  $U_{K^-}$ .
- "Broad-band equilibration" obtained only when the  $K^-$  spectral density is used. However,  $K^-$  is in excess  $\Rightarrow$  dynamical non-equilibrium effects to explain the smaller number of  $K^-$  detected.

*Tolós, Polls, Ramos and Schaffner-Bielich,  
Phys. Rev. C 68, 024903 (2003)*

L. Tolos, A. Ramos, and A. Polls, Phys. Rev. C 65, 054907 (2002)



1. On-shell approximation(left panel); in-medium  $U_{K^-}$  at finite temperature.
2.  $K^-$  spectral density (right panel) using  $K^-$  self-energy.

