

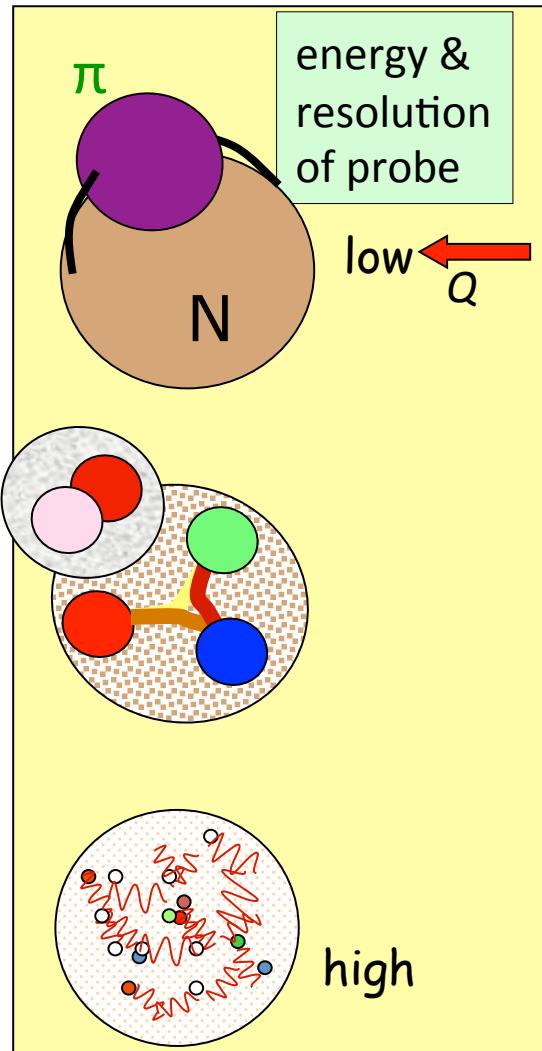
# Nucleon resonance transition form factors at JLab

Volker D. Burkert  
Jefferson Lab

- Introduction
- Magnetic dipole transition and quadrupole structure of  $\gamma p\Delta(1232)$
- Two states in the  $[70,1^-]_1$  supermultiplet  $N(1520)3/2^-$  &  $N(1535)1/2^-$
- The nature of the “Roper” resonance
- LC transition charge densities in transverse space
- Higher mass states and one unique resonance  $N(1676)5/2^-$
- Conclusions & Outlook



# Why electron beams?



Electron beams have tunable resolution ( $Q = e \cdot e'$ ) and are clean (e.m.) probes of the hadron structure.

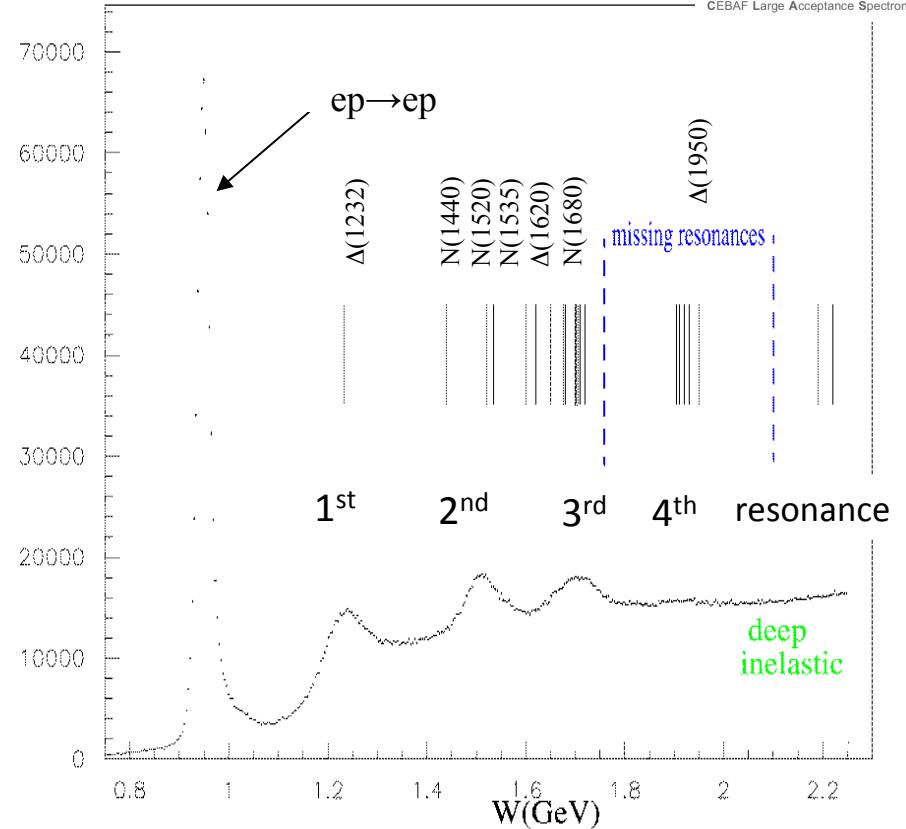
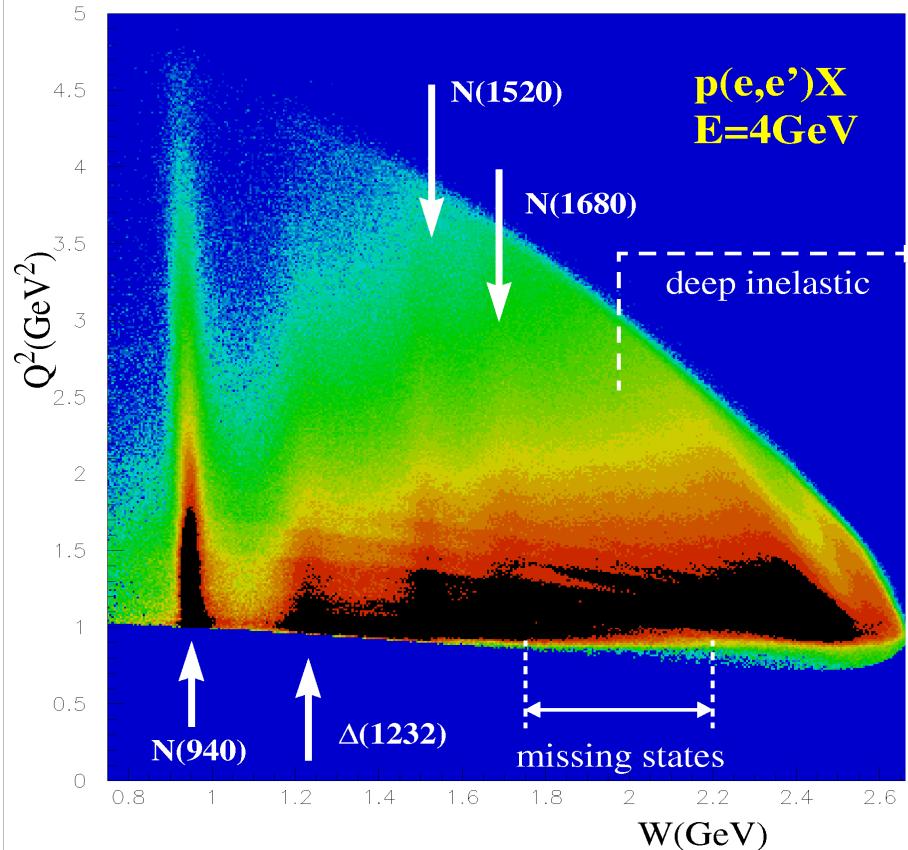
Central question in hadron physics:  
**“What are the effective degrees of freedom at varying distance scale and what do they reveal about the nucleon structure”?**

By measuring the resonance excitation strength with virtual photons we probe the contributions to the resonance strength from

- **hadronic degrees-of-freedom (meson-baryons)**
- **the evolution of dressed quarks to bare quarks**
- **hybrid baryons**
- **the running quark mass function**

# Inclusive Electron Scattering $ep \rightarrow e'X$

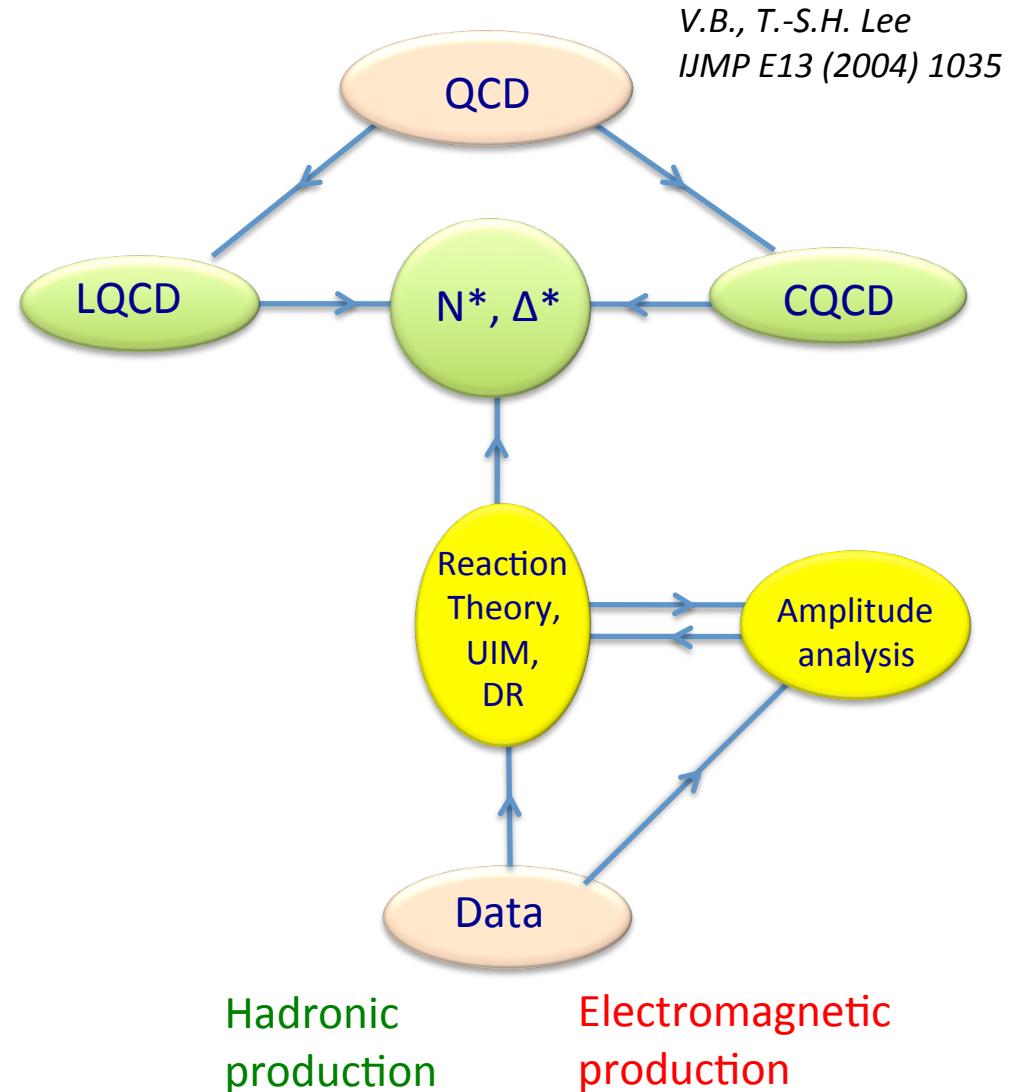
$$Q^2 = -(e-e')^2; \quad W^2 = (e-e'+p)^2$$



- Resonances cannot be uniquely separated in inclusive scattering
- measure exclusive processes with  $N\pi$ ,  $N\eta$  and  $N\pi\pi$  final states to identify specific QN

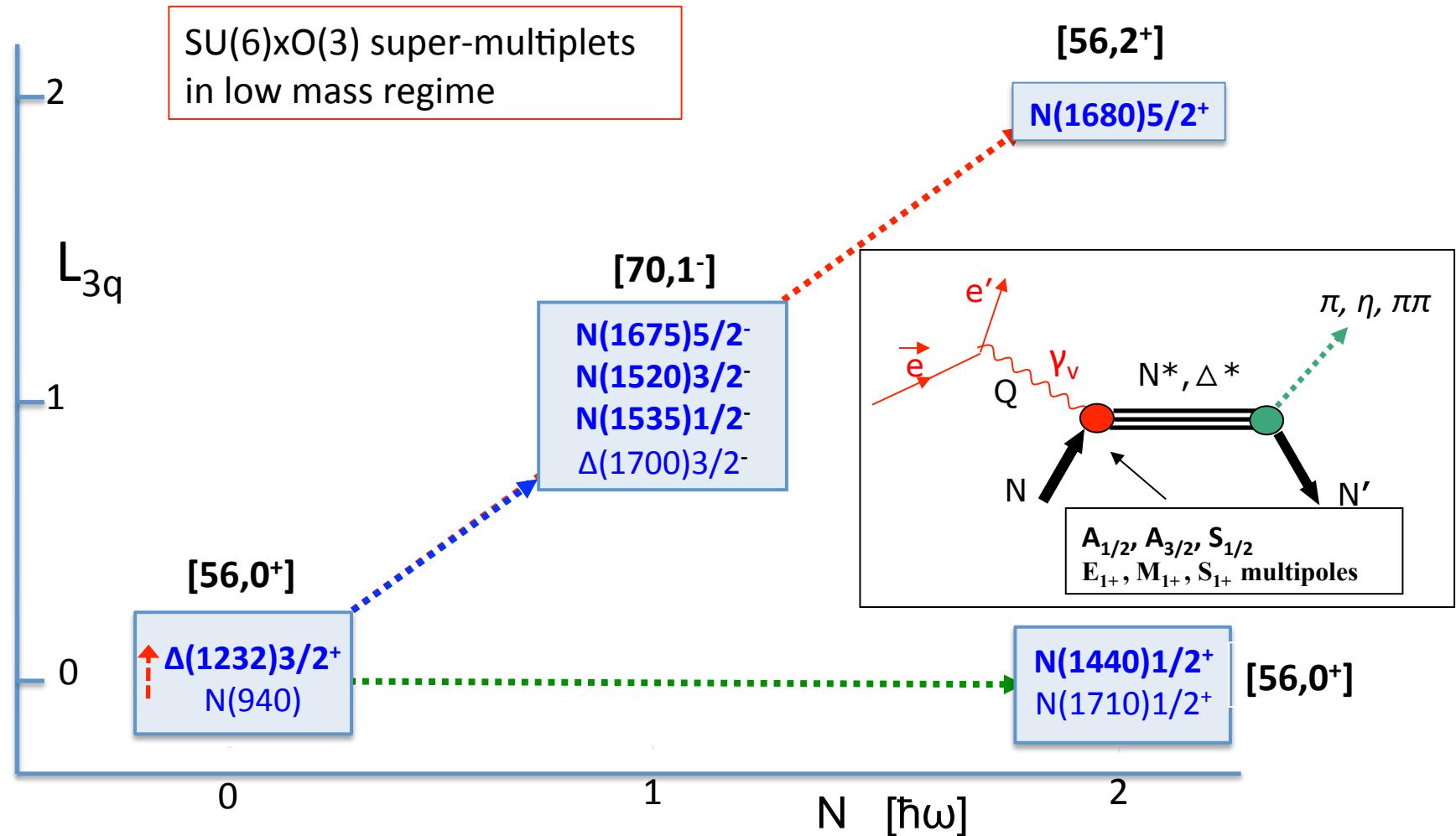
# Tools for $N^*$ and $\Delta^*$ analysis

- **UIM** includes  $\pi$  Born terms in s- and u-channel nucleon exchanges and t-channel meson exchanges ( $\pi, \rho, \omega, b_1, a_2, \dots$ ).
- In fixed-t **DR** the real part is determined from  $\pi$  Born terms + dispersion integral over imaginary parts of all known resonances.
- The  $p\pi^+\pi^-$  analysis uses a data-driven reaction model (JM) **JLAB-MSU**.



I.G. Aznauryan, T.-S. H. Lee, V. Mokeev.

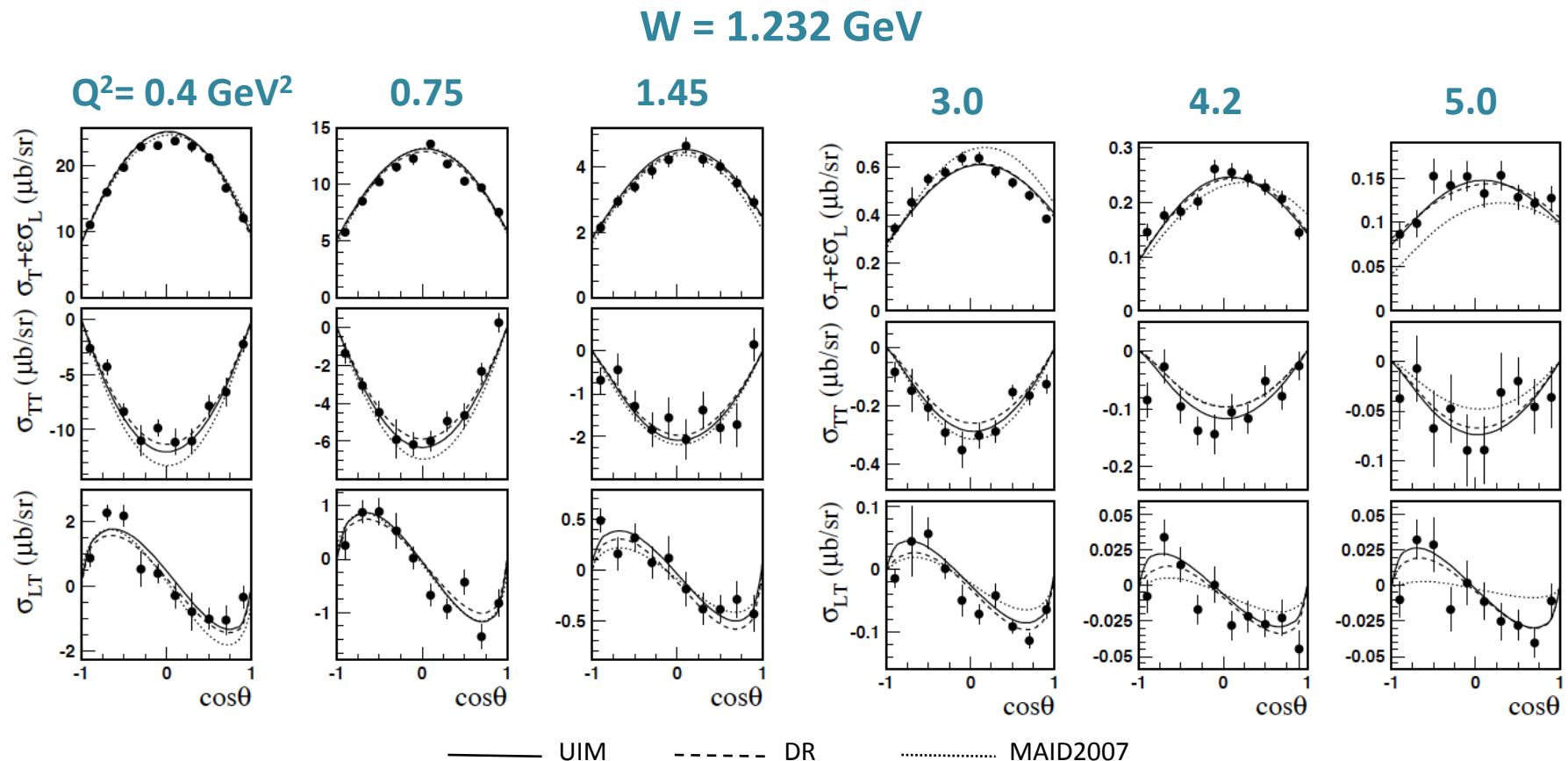
# Nucleon resonance transitions



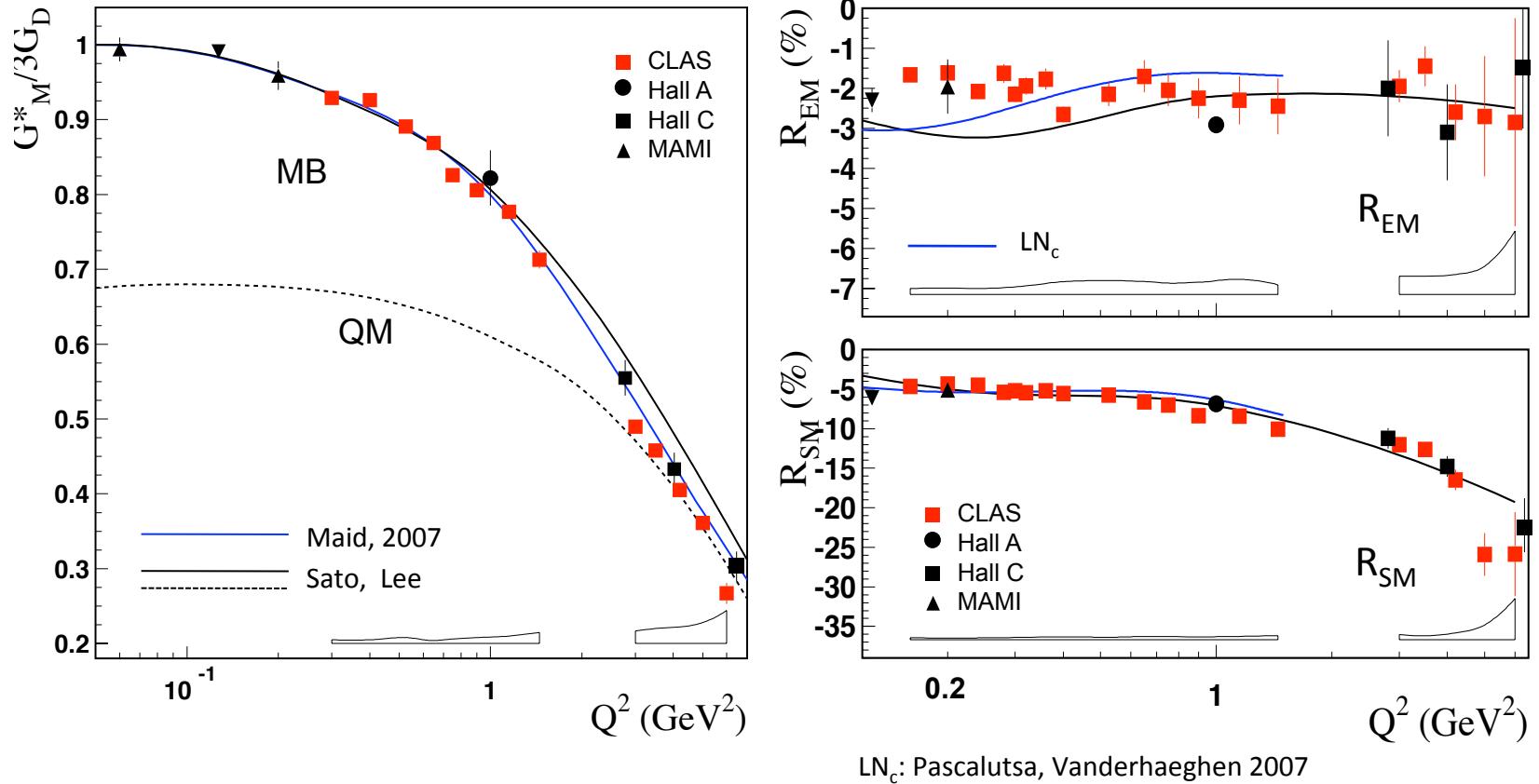
Results based on over 150,000 cross sections and polarization observables in  $W$ ,  $Q^2$ ,  $\cos\theta$ ,  $\phi$ .

# Response functions of $p\pi^0$ in $\Delta(1232)$

Measure azimuth and polar angle dependence of  $p(e,e'p)\pi^0$  cross section and polarization observables and extract resonant part with **UIM** and **DR** approach.

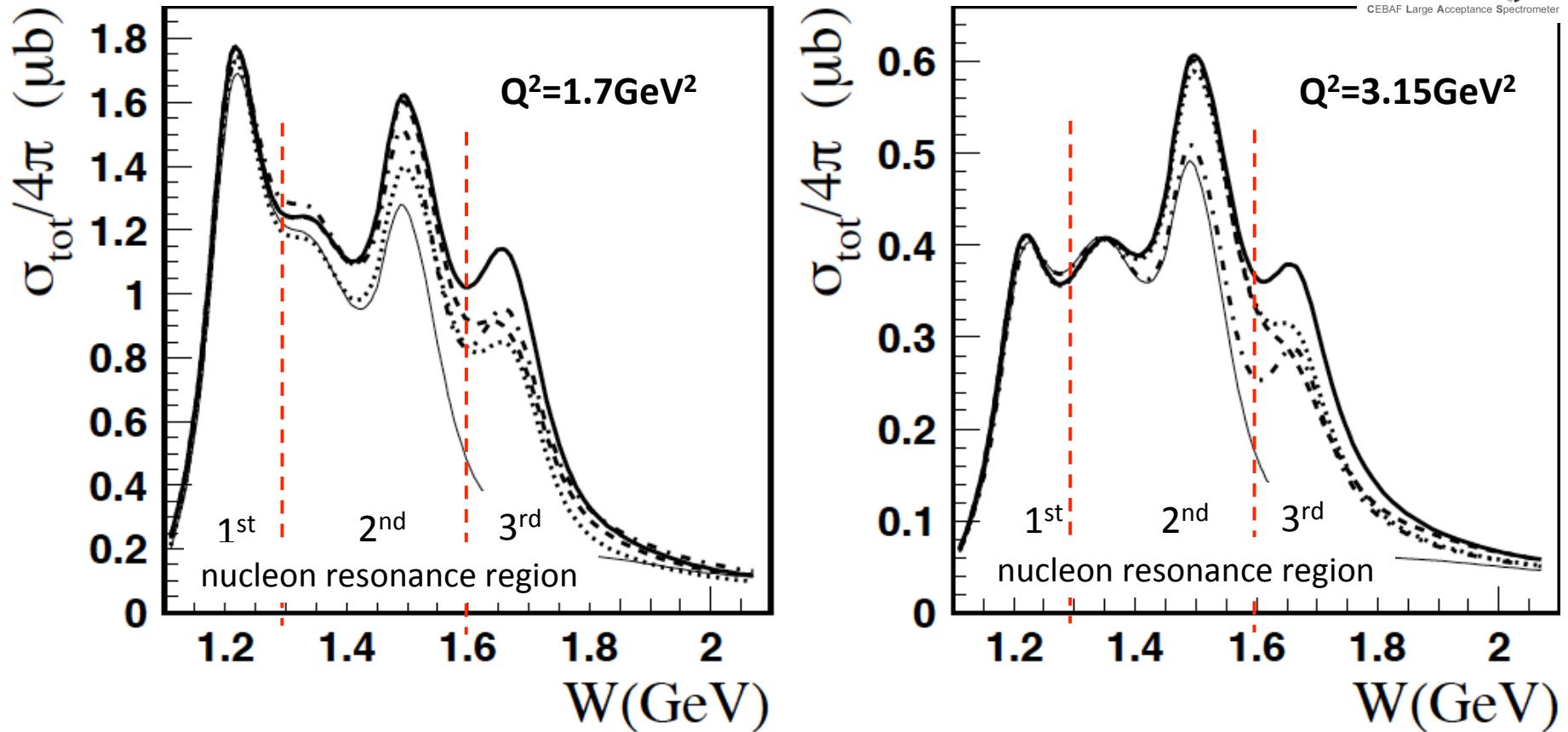
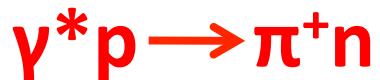


# The $N\Delta(1232)$ Transition



- Large MB contributions (1/3) needed to describe magnetic dipole transition at  $Q^2=0$
- For  $G^*_M$  the MB contribution are decreasing with increasing  $Q^2$
- $R_{EM}$  and  $R_{SM}$  described with MB contributions only
- No approach to asymptotic behavior  $R_{EM} \Rightarrow +100\%$

# Total cross section at $W < 2.1$ GeV



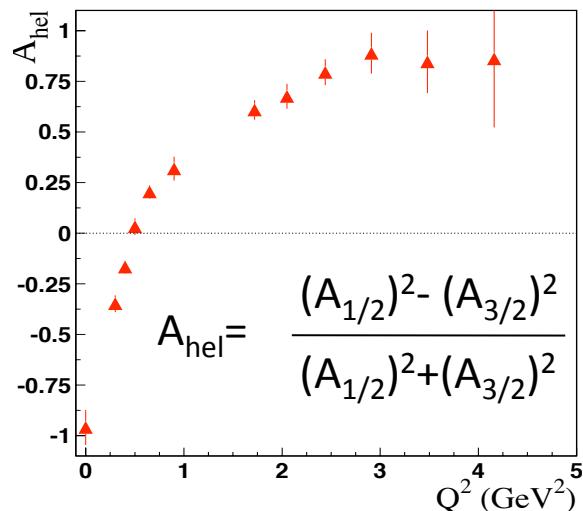
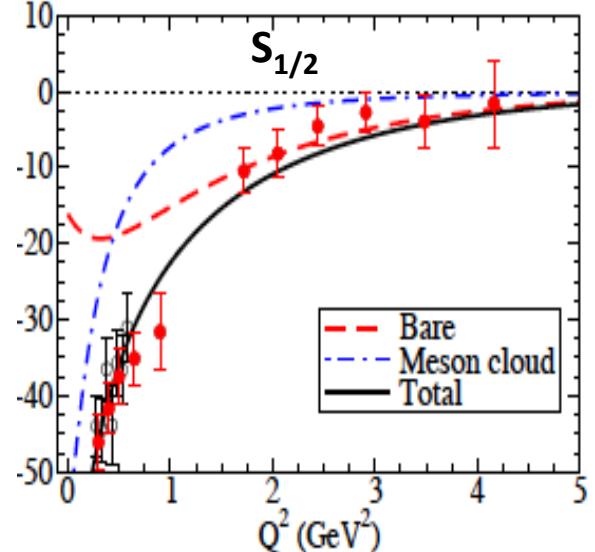
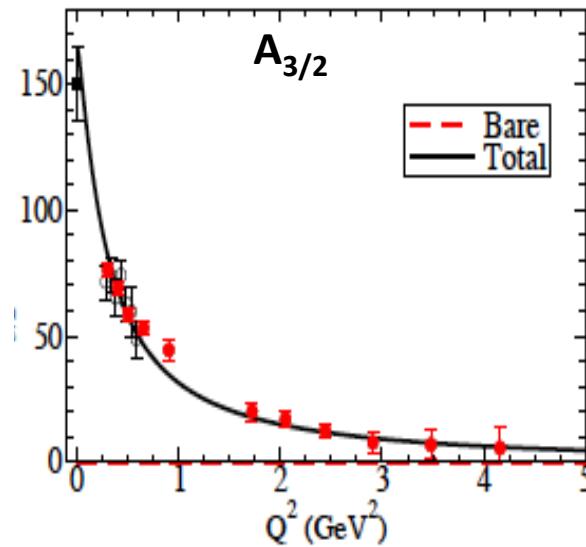
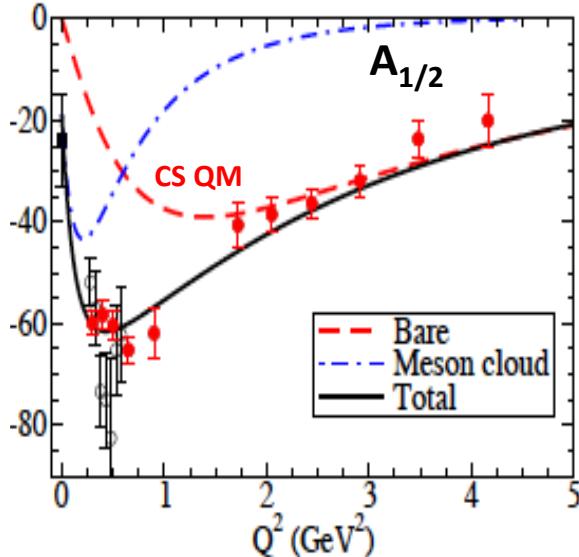
Access “Roper” N(1440)1/2<sup>+</sup>, N(1520)3/2<sup>-</sup>, and N(1535)1/2<sup>-</sup>

K. Park *et al.*, PR C77 (2008) 015208; PR C91 (2015) 045203

# Electrocouplings of $\gamma_N(1520)3/2^-$



Aznauryan et al. (CLAS), PRC80, 055203 (2009), V. Mokeev et al. (CLAS), PRC86, 035203 (2012)



- Lowest negative parity spin 3/2 state  $\Rightarrow$  3 amplitudes
- Firmly established switch from  $A_{3/2}$  dominance at  $Q^2=0$  to  $A_{1/2}$  dominance at  $Q^2 > 1 \text{ GeV}^2$ .

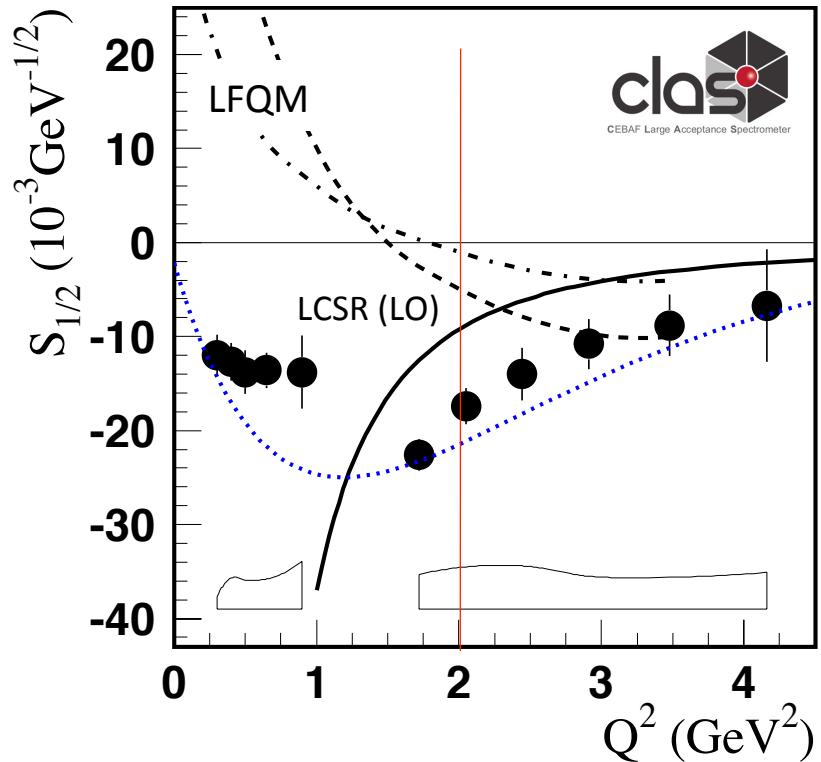
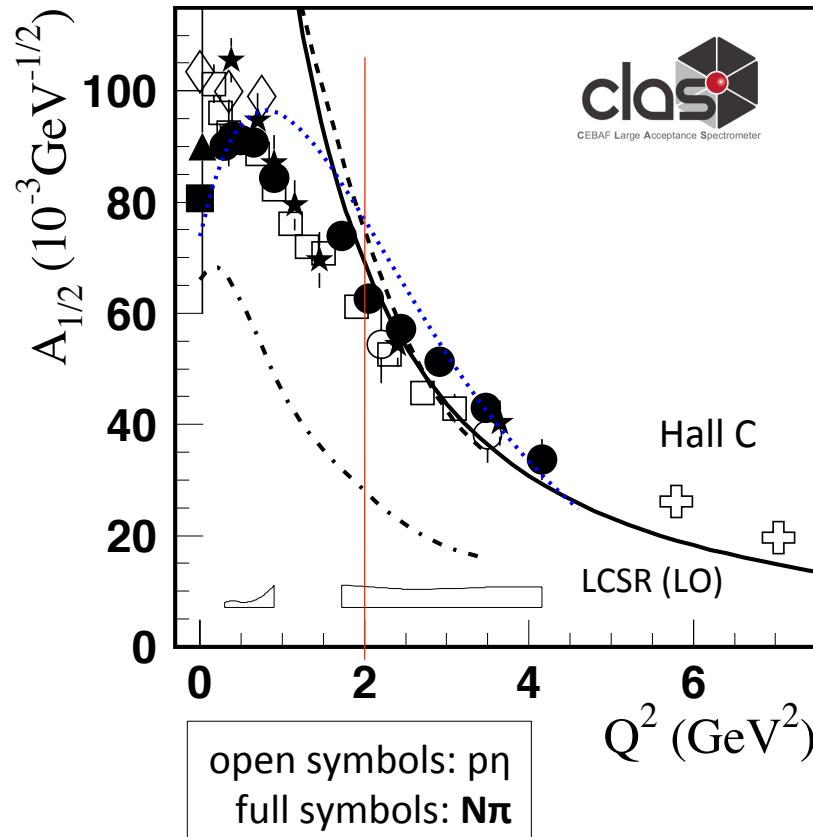
- $A_{1/2}$  strength at high  $Q^2$  from bare quarks
- MB dominate amplitudes at low  $Q^2$
- $A_{3/2} = 0$ , not computed in this model

**CS QM:** G. Ramalho and M. T. Peña, PR D89 (2014) 094016

# Electrocouplings of $\gamma_\nu pN(1535)1/2^-$

## Is it a 3-quark state or a hadronic molecule?

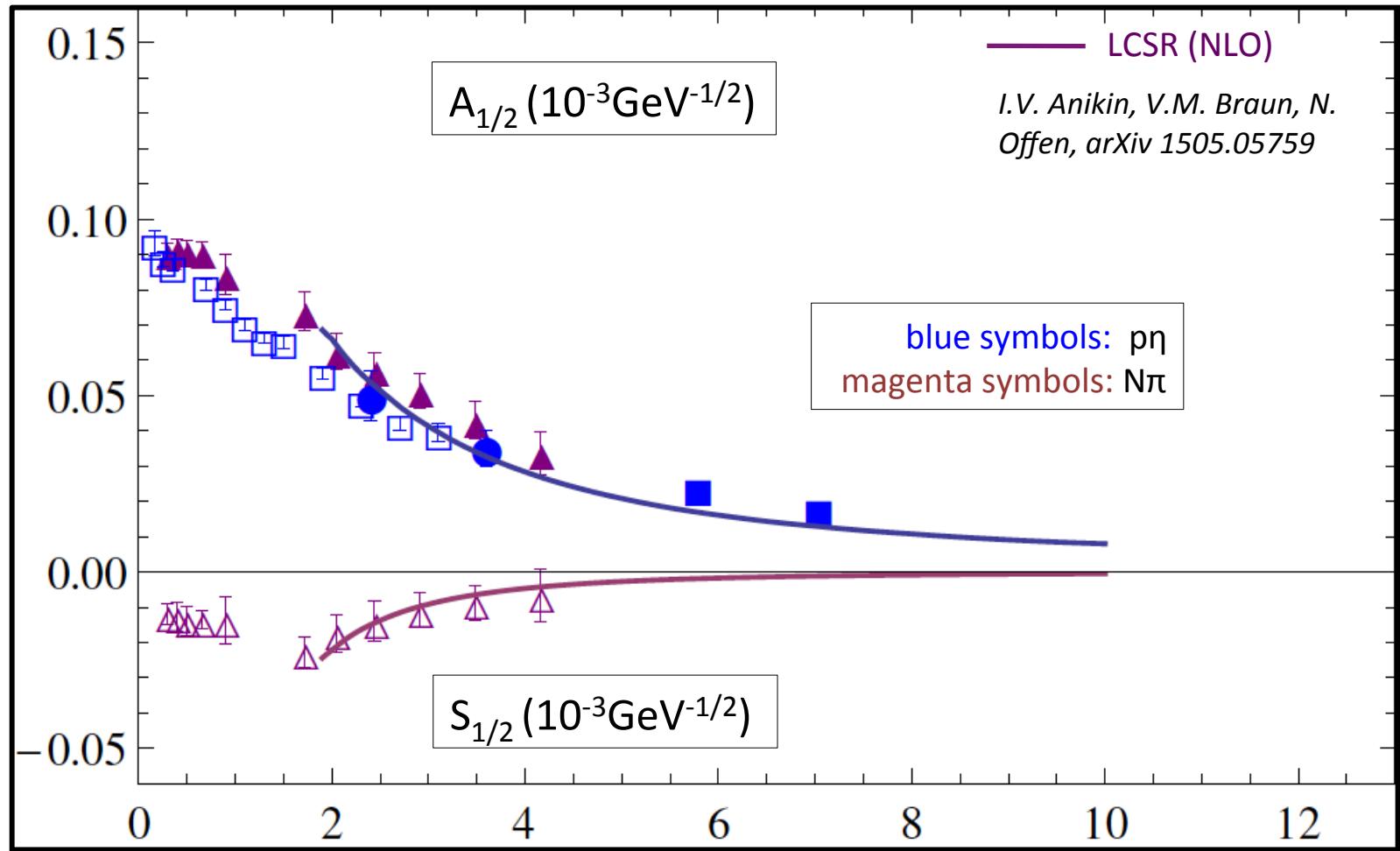
- Chiral unitary model analyses: state may have large  $K\Lambda$  and  $p\phi$  components



LCSR: V.M. Braun et al., PRL 103 (2009)

$K\Lambda$  or  $p\phi$  could explain low  $Q^2$  behavior that contrasts LFQM predictions.

# Electrocouplings of $\gamma_v p N(1535) 1/2^-$ in QCD

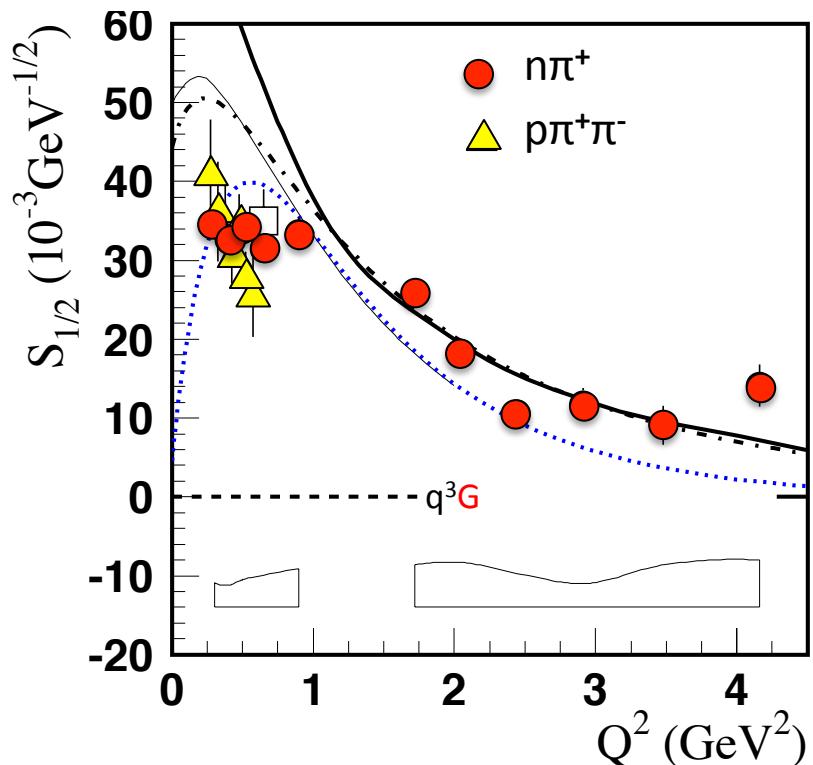
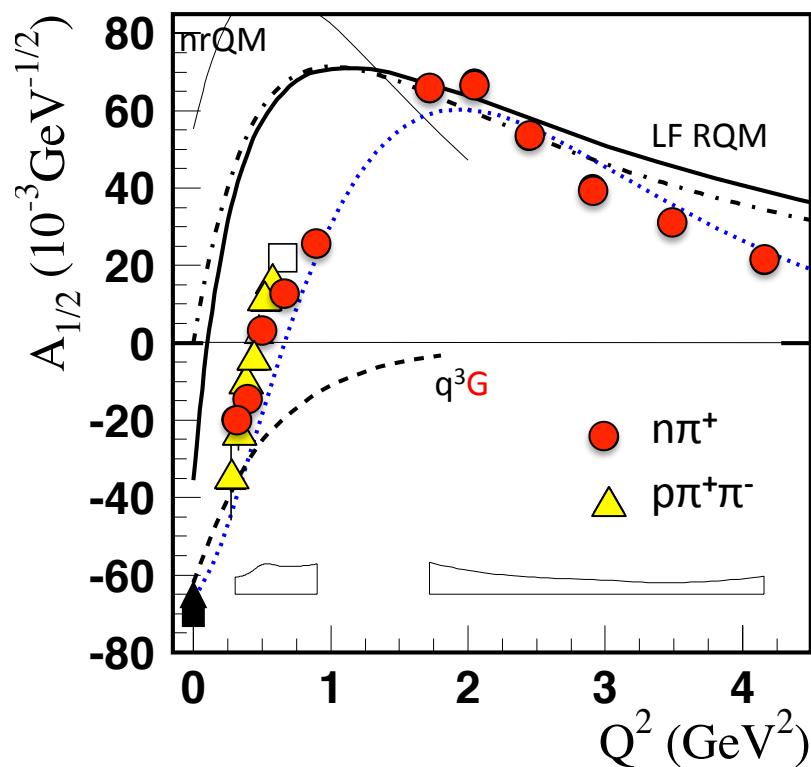


Quantitative description at  $Q^2 \geq 2 \text{ GeV}^2$ .

# Electrocouplings of 'Roper' $\gamma_v pN(1440)1/2^+$



Aznauryan *et al.* (CLAS), PRC80, 055203 (2009), V. Mokeev *et al.* (CLAS), PRC86, 035203 (2012)



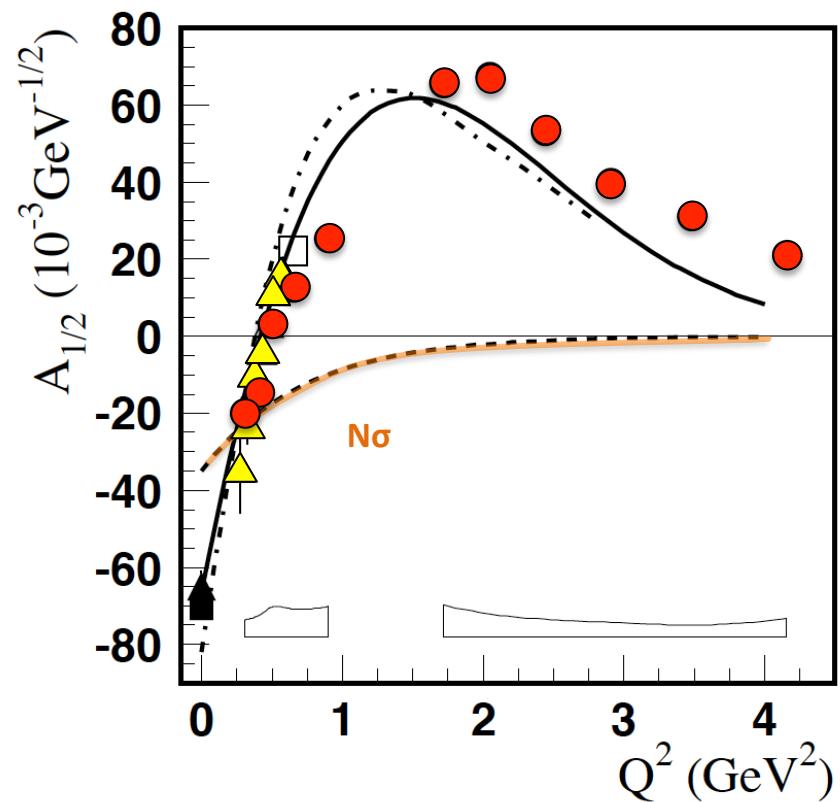
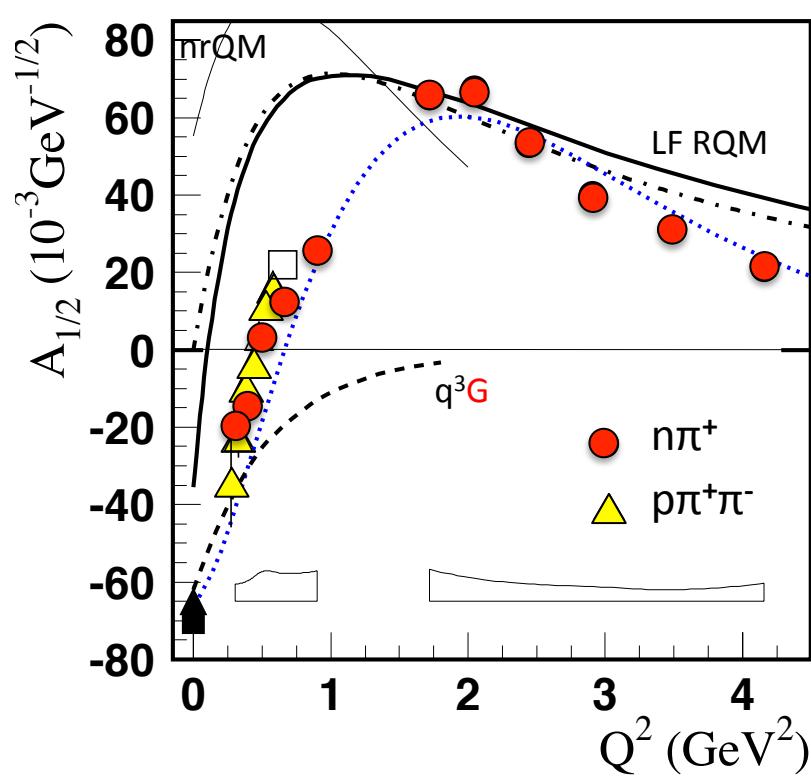
- $A_{1/2}$  changes sign and has large magnitude at high  $Q^2$
- $N\pi$  and  $N\pi\pi$  give consistent results
- QM assign state to the 1<sup>st</sup> radial excitation - fails to reproduce low  $Q^2$  behavior, LCQM better at large  $Q^2$
- Both  $A_{1/2}(Q^2)$  and  $S_{1/2}(Q^2)$  are inconsistent with hybrid baryon model prediction

LF-RQM: I.G. Aznauryan, 2007  
G. Ramalho, K. Tsushima, 2010

# Electrocouplings of 'Roper' $\gamma_v pN(1440)1/2^+$



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- Both  $A_{1/2}(Q^2)$  and  $S_{1/2}(Q^2)$  are inconsistent with hybrid model prediction
- Significant  $N\sigma$  coupling needed to describe small  $Q^2$  behavior

# The “Roper” resonance in 2015

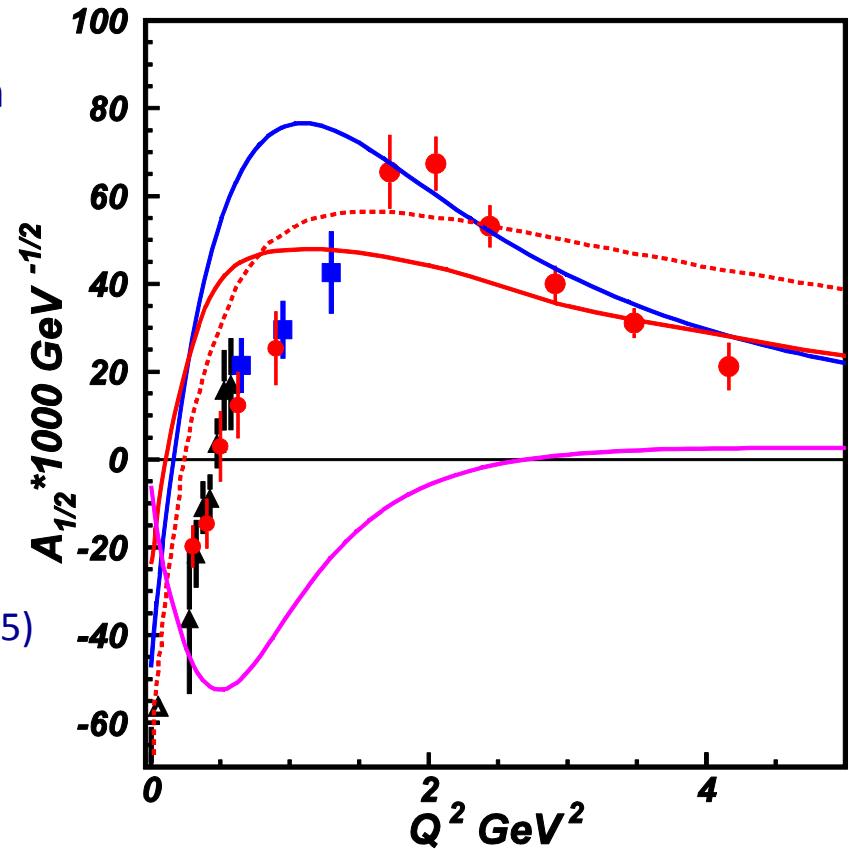
Description of the  $N(1440)1/2^+ A_{1/2}$  electro-coupling in LF QM that incorporate the inner core of three dressed quarks in the first radial excitation and outer meson-baryon (MB) cloud:

— N $\pi$  loops to model MB cloud; running quark mass, in LF RQM. I.G. Aznauryan, V.B., Phys. Rev. C85, 055202 (2012).

— N $\sigma$  loops to model MB cloud; frozen constituent quark mass. I.T. Obukhovsky, et al., Phys. Rev. D89, 014032 (2014).

— Quark core contributions from DSE/QCD (2015) J. Segovia et al., arXiv:1504.04386

— MB cloud inferred from the CLAS data as the difference between the data and quark core evaluated in DSE/QCD.



The structure of  $N(1440)1/2^+$  resonance is determined by the interplay between a core of three dressed quarks in the 1<sup>st</sup> radial excitation and the external meson-baryon cloud.

# Light-cone N\* transition charge densities

$$A_{1/2} = e \frac{Q_-}{\sqrt{K} (4M_N M^*)^{1/2}} \left\{ \underline{F_1^{NN^*}} + \underline{\overline{F_2^{NN^*}}} \right\},$$

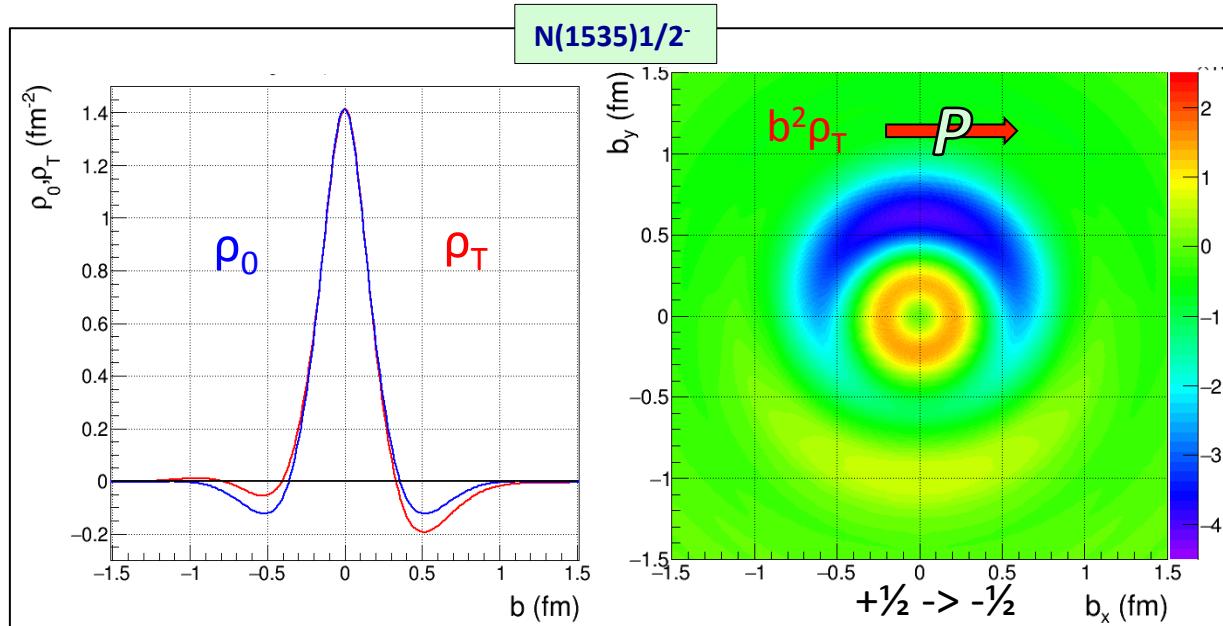
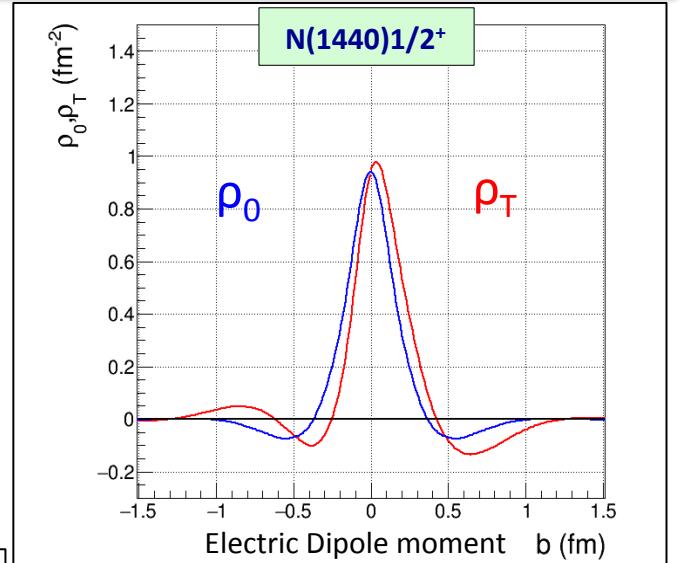
L. Tiator, M. Vanderhaeghen,  
PLB 672 (2009) 344

$$S_{1/2} = e \frac{Q_-}{\sqrt{2K} (4M_N M^*)^{1/2}} \left( \frac{Q_+ Q_-}{2M^*} \right) \frac{(M^* + M_N)}{Q^2} \left\{ \underline{F_1^{NN^*}} - \frac{Q^2}{(M^* + M_N)^2} \underline{\overline{F_2^{NN^*}}} \right\}$$

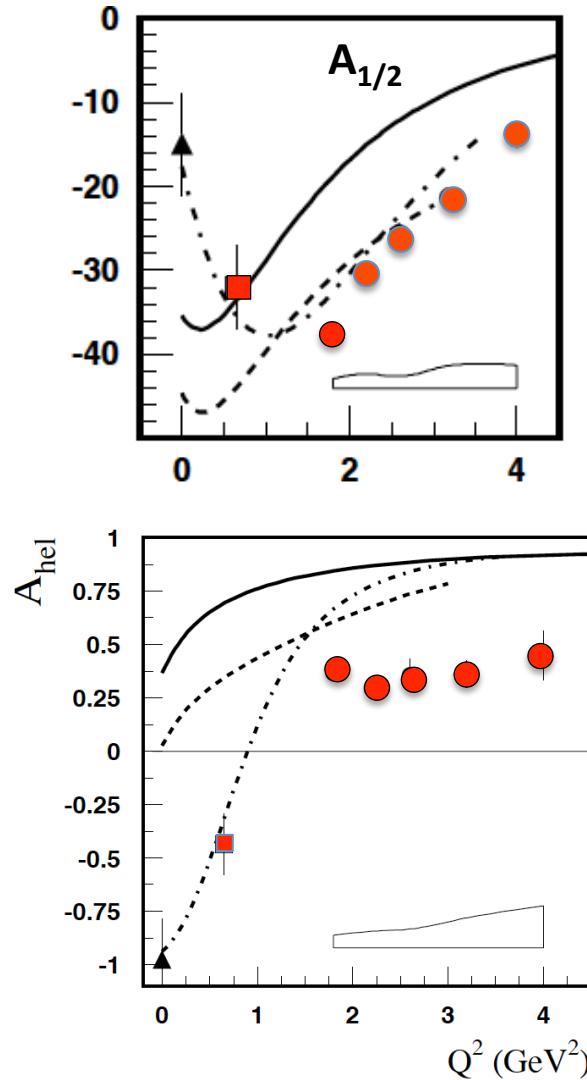
$$\rho_0^{NN^*}(\vec{b}) = \int_0^\infty \frac{dQ}{2\pi} Q J_0(bQ) F_1^{NN^*}(Q^2)$$

Exp:  $0 < Q^2 < 4.5-7 \text{ GeV}^2$

$$\rho_T^{NN^*}(\vec{b}) = \rho_0^{NN^*}(b) + \sin(\phi_b - \phi_S) \int_0^\infty \frac{dQ}{2\pi} \frac{Q^2}{(M^* + M_N)} J_1(bQ) F_2^{NN^*}(Q^2)$$



# Electrocouplings of $\gamma_v p N(1680) 5/2^+$



K. Park et al., PRC91 (2015) 045203

$$A_{\text{hel}} = \frac{(A_{1/2})^2 - (A_{3/2})^2}{(A_{1/2})^2 + (A_{3/2})^2}$$

- Switch from  $A_{3/2}$  dominance at  $Q^2 = 0$  to  $A_{1/2}$  at high  $Q^2$  dominance slower than predicted from CQM.
- Are there large MB contributions in  $A_{3/2}$  at high  $Q^2$ ?

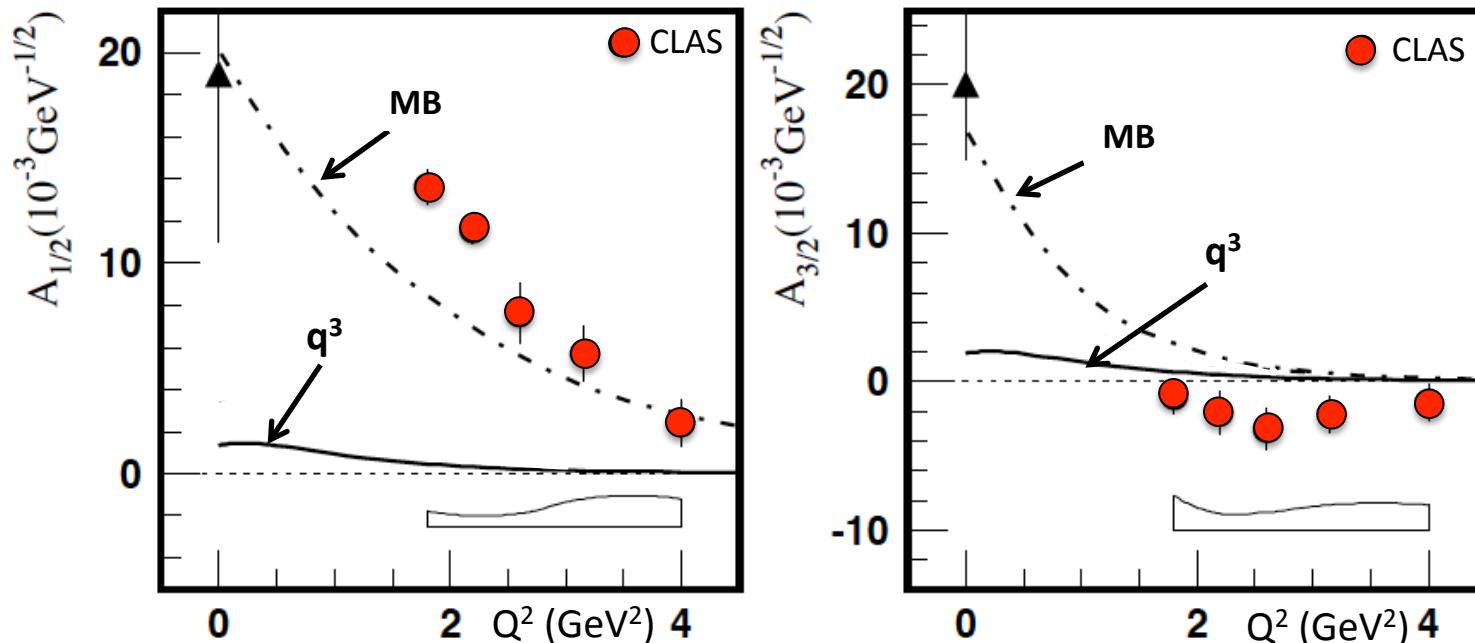
# MB contribution to $\gamma_v p N(1675)5/2^-$



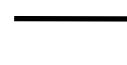
Quark components to the helicity amplitudes of the  $N(1675)5/2^-$  are strongly suppressed for proton target.

Single Quark Transition:  
 $A_{1/2}^p = A_{3/2}^p = 0$

I. Aznauryan, V.B., arXiv:1412.1296

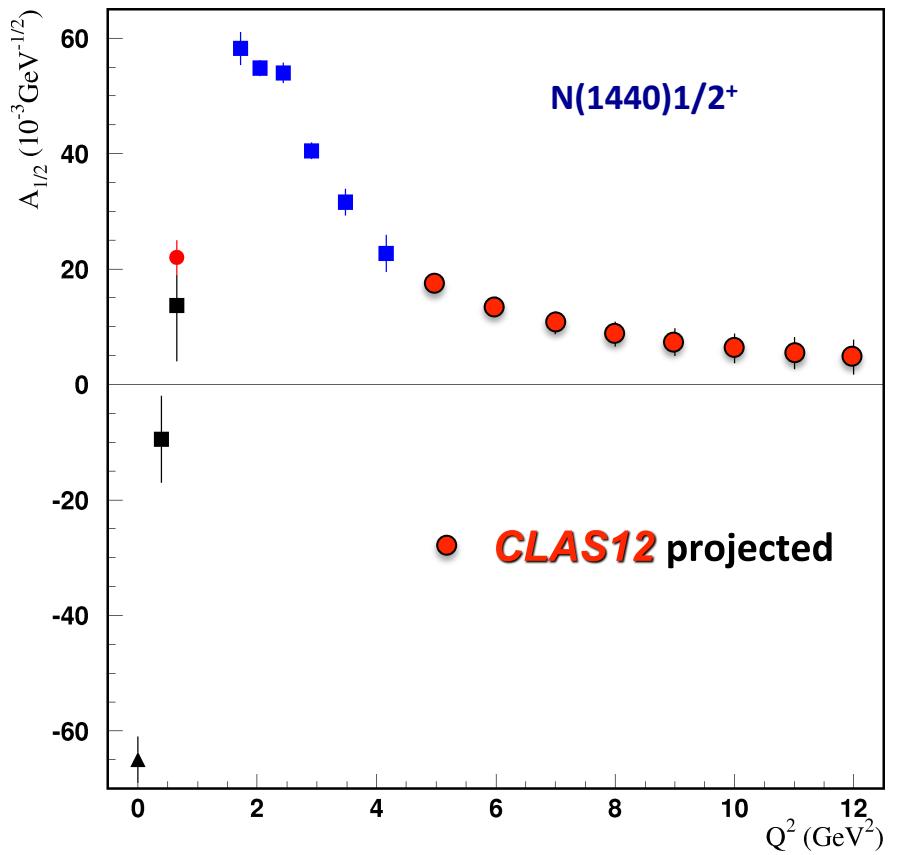
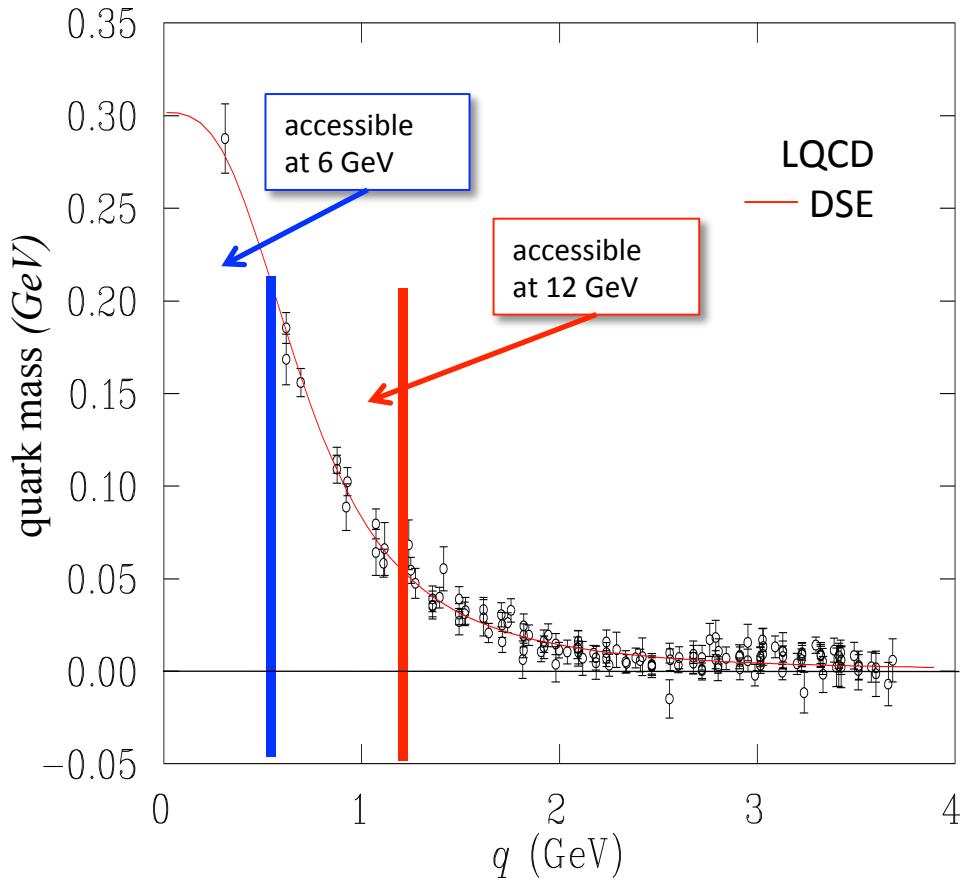


- Measures the meson-baryon contribution to  $\gamma^* p N(1675)5/2^-$  directly
- Calibrate the dynamical coupled-channel model input



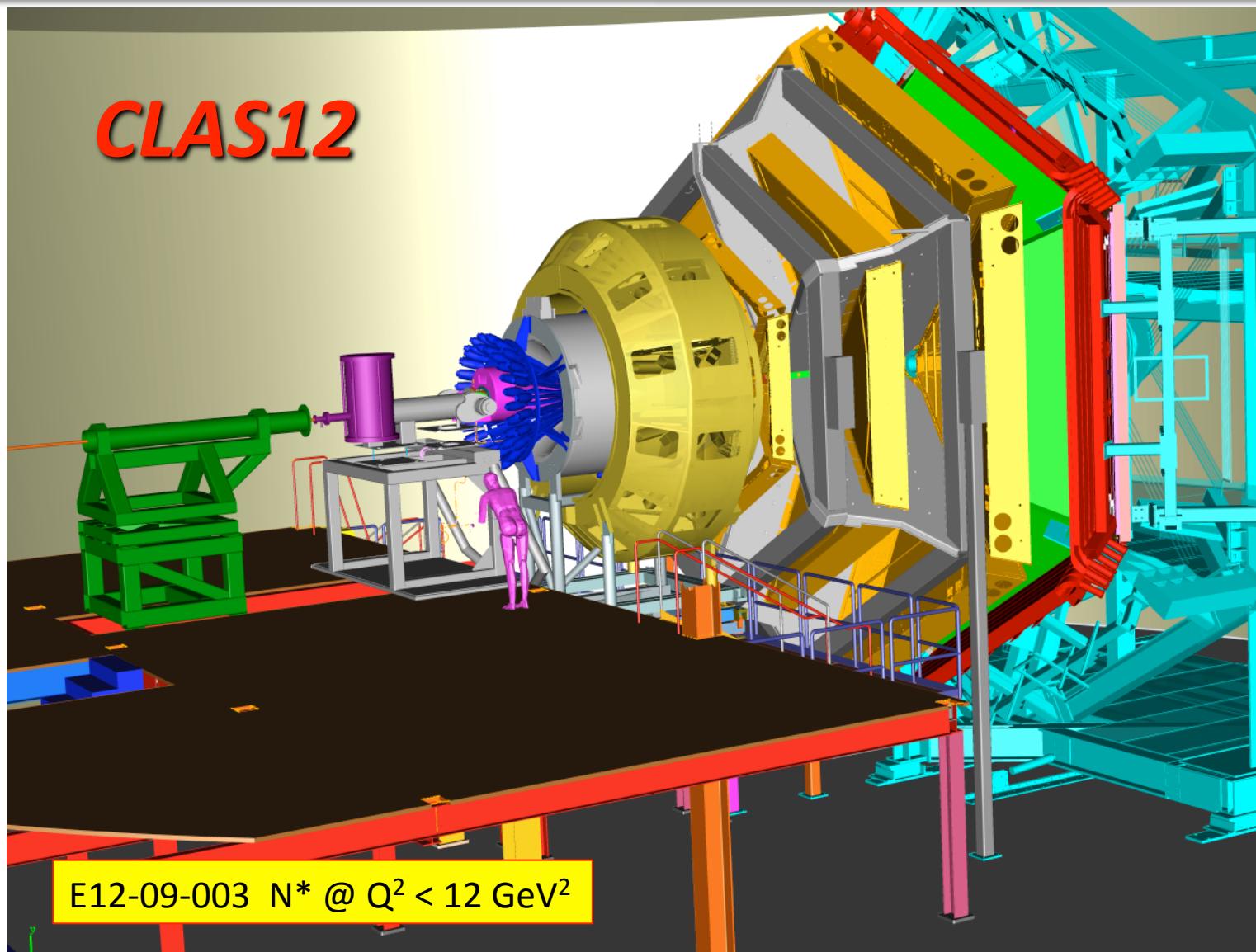
E. Santopinto and M. M. Giannini, PRC 86, 065202 (2012)  
B. Juliá-Díaz, T.-S.H. Lee, et al., PR C 77, 045205 (2008)

# Probing the running quark mass at JLab12



Nucleon resonance transitions amplitudes probe the quark mass function from constituent quarks to dressed quarks and elementary quarks.

# N\* Transition FF Physics @ JLAB12



# Conclusions & Outlook

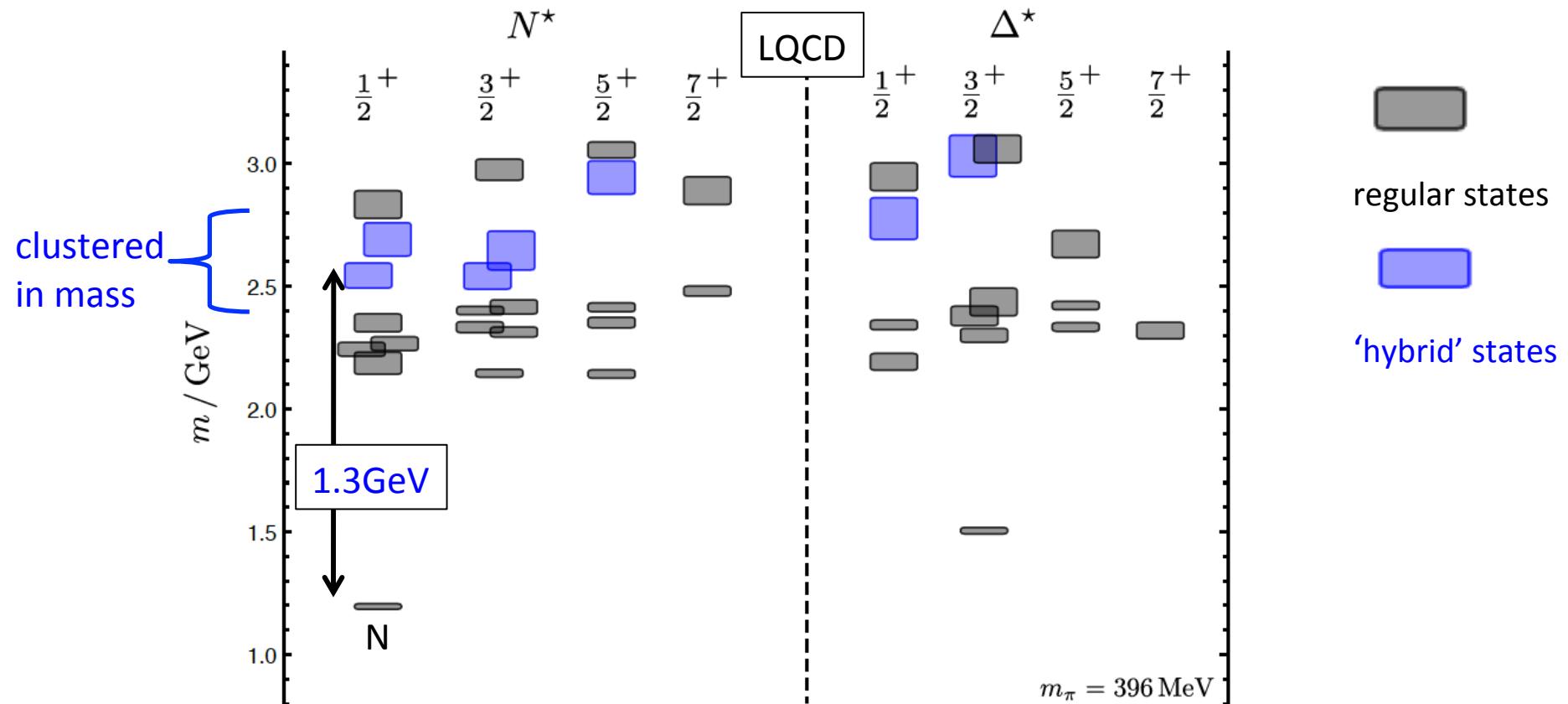
- The 3-quark core becomes dominant to MB contributions in electroexcitation with  $Q^2 > 2\text{-}4 \text{ GeV}^2$  in all studied excited states.
- The structure of the Roper resonance is determined by the interplay between the core of 3 dressed quarks in the 1<sup>st</sup> radial excitation and the external meson-baryon cloud.
- Transverse charge transition densities reveal significant differences for different excited states.
- Precise computation of electromagnetic transition form factors has become a topic of strong QCD.
- Planned experiment with CLAS12 at JLab@12GeV will measure resonances at highest  $Q^2$  as a probe of the running quark mass.
- Electroexcitation of resonances may be an essential tool to isolate gluonic baryon excitations that can be explored with CLAS12.

# Additional slides

# Gluonic Baryons $q^3G$

J.J. Dudek and R.G. Edwards, PRD85 (2012) 054016

T. Barnes and F.E. Close, PLB128, 277 (1983)

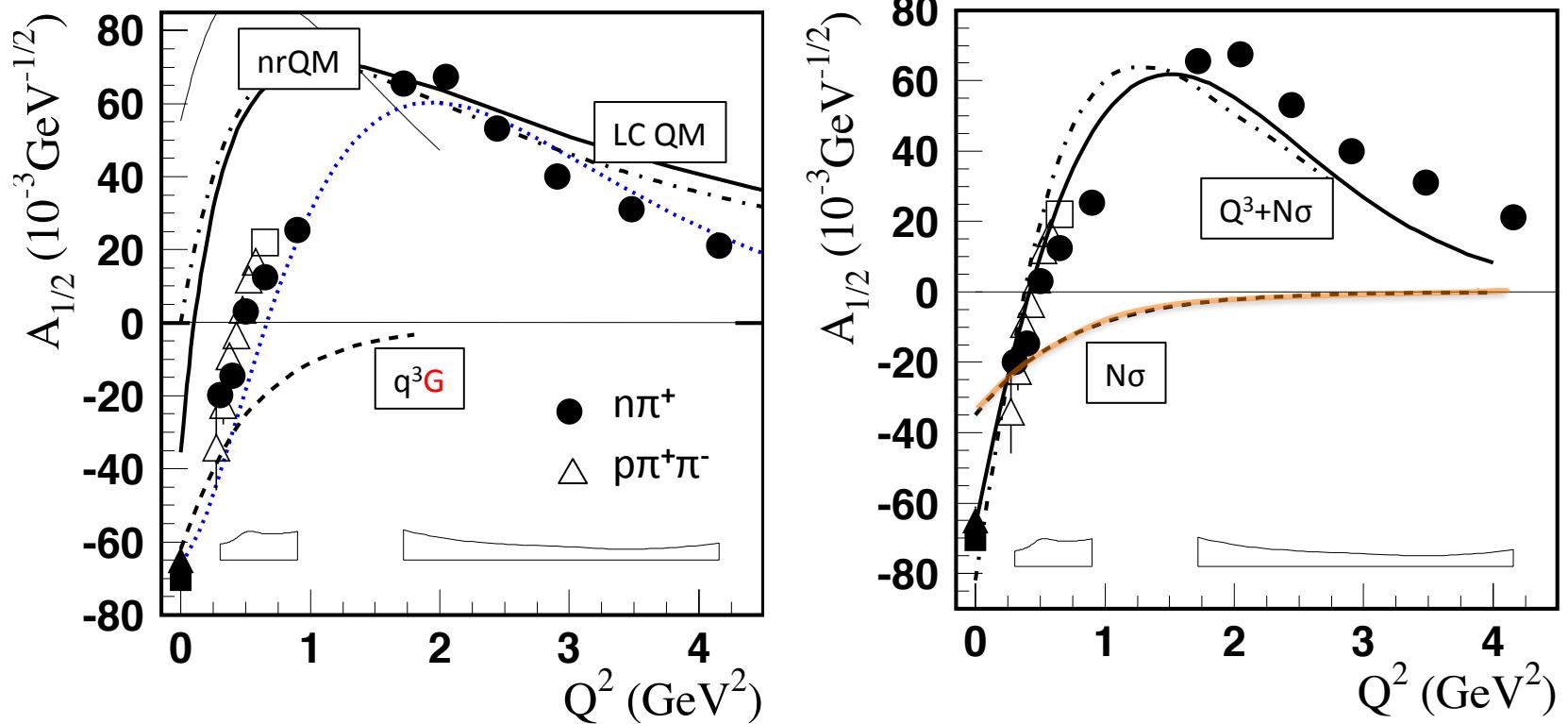


Hybrid states have same  $J^P$  values as  $q^3$  baryons. How to identify them?

- Overpopulation of  $N1/2^+$  and  $N3/2^+$  states compared to QM projections?
- Transition form factors in electroproduction?

# Electrocouplings of ‘Roper’ N(1440)1/2<sup>+</sup>

Aznauryan et al. (CLAS), PRC80, 055203 (2009), V. Mokeev et al. (CLAS), PRC86, 035203 (2012)



- nrQM assign it to the 1<sup>st</sup> radial excitation of the nucleon, but fails in  $A_{1/2}$
- $A_{1/2}$  dominant amplitude at high  $Q^2$  indicates radial  $q^3$  excitation but fails at low  $Q^2$
- Significant meson-baryon coupling needed to describe small  $Q^2$  behavior
  - $A_{1/2}(Q^2)$  and  $S_{1/2}(Q^2)$  are inconsistent with gluonic excitation

# Unitary Isobar Model (UIM)

MAID Model: D. Drechsel, O. Hanstein, S. Kamalov, L. Tiator, Nucl.Phys. A 645 (1999) 145

$$L_{\pi NN} = \frac{\Lambda^2}{\Lambda^2 + |\mathbf{q}|^2} L_{\pi NN}^{PV} + \frac{|\mathbf{q}|^2}{\Lambda^2 + |\mathbf{q}|^2} L_{\pi NN}^{PS}.$$

$$\text{Unitarized}(M_{l\pm}, E_{l\pm}, S_{l\pm})_{background} = (M_{l\pm}, E_{l\pm}, S_{l\pm})_{background} (1 + i h_{l\pm}).$$

$$aA_{l\pm}^R(B_{l\pm}^R, S_{l\pm}^R) = \hat{A}_{l\pm}(\hat{B}_{l\pm}, \hat{S}_{l\pm}) \frac{M\Gamma_{tot}e^{i\phi}}{M^2 - W^2 - iM\Gamma_{tot}} f_{\gamma N}(W) \quad f_{\gamma N}(W) = \left( \frac{|\mathbf{k}|}{|\mathbf{k}_r|} \right)^n \left( \frac{X^2 + |\mathbf{k}_r|^2}{X^2 + |\mathbf{k}|^2} \right)$$

$$\Gamma_{\pi N} = \beta_{\pi N} \Gamma \left( \frac{|\mathbf{q}|}{|\mathbf{q}_r|} \right)^{2l+1} \left( \frac{X^2 + |\mathbf{q}_r|^2}{X^2 + |\mathbf{q}|^2} \right)^l \frac{M}{W} \quad \Gamma_{inel} = (1 - \beta_{\pi N}) \Gamma \left( \frac{|\mathbf{q}_{2\pi}|}{|\mathbf{q}_{2\pi,r}|} \right)^{2l+4} \left( \frac{X^2 + |\mathbf{q}_{2\pi,r}|^2}{X^2 + |\mathbf{q}_{2\pi}|^2} \right)^{l+2}$$

Include Regge exchanges at high  $s$ , I. Aznauryan,

$$\begin{aligned} \text{Background} &= [N + \pi + \rho + \omega]_{UIM} \text{ at } s < s_0, \\ &= [N + \pi + \rho + \omega]_{UIM} \frac{1}{1 + (s - s_0)^2} + Re[\pi + \rho + \omega + b_1 + a_2]_{Regge} \frac{(s - s_0)^2}{1 + (s - s_0)^2} \text{ at } s > s_0. \end{aligned}$$

# Fixed-t DRs for invariant Ball amplitudes



Dispersion relations for 6 invariant Ball amplitudes:

17 Unsubtracted Dispersion Relations

$$ReB_i^{(\pm,0)}(s, t, Q^2) [ReB_3^{(+,0)}(s, t, Q^2)] = R_i^{(v,s)}(Q^2) \left( \frac{1}{s - m_N^2} + \frac{\eta_i \eta^{(+,-,0)}}{u - m_N^2} \right) + \frac{P}{\pi} \int_{s_{thr}}^{\infty} ImB_i^{(\pm,0)}(s', t, Q^2) \left( \frac{1}{s' - s} + \frac{\eta_i \eta^{(+,-,0)}}{s' - u} \right) ds'$$

(i=1,2,4,5,6)

1 Subtracted Dispersion Relation

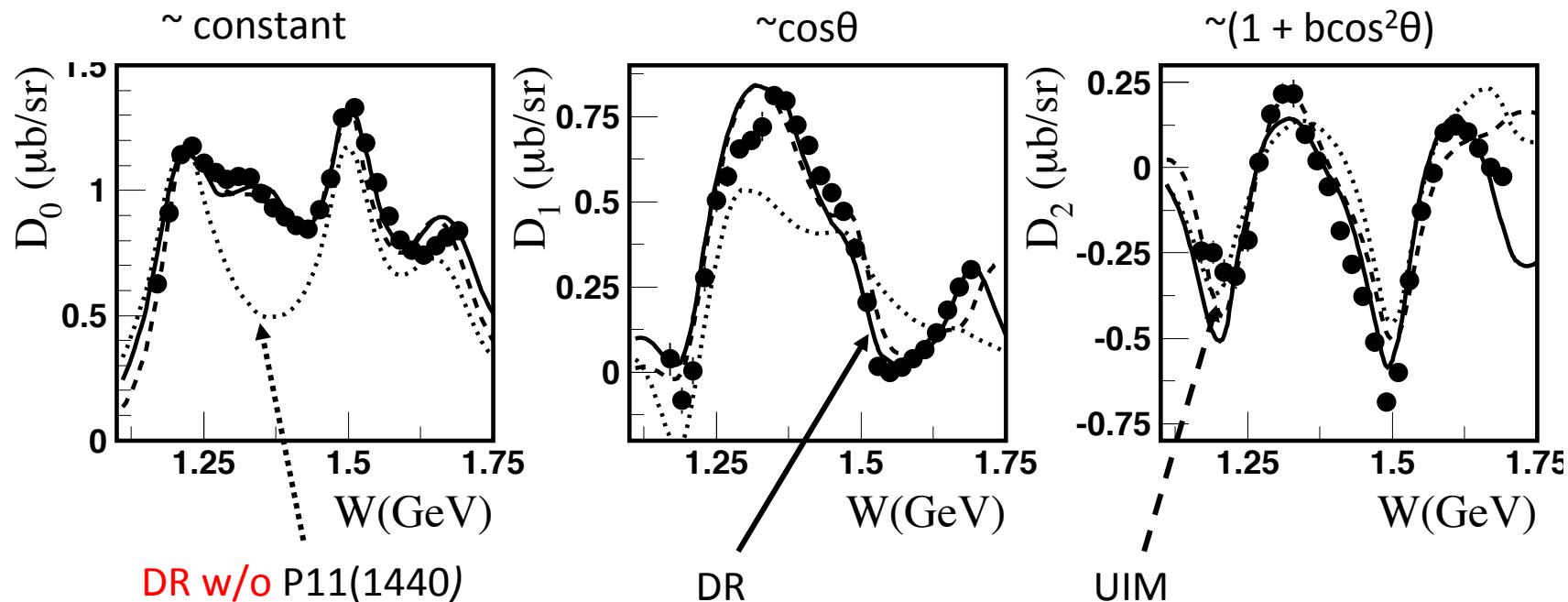
$$ReB_3^{(-)}(s, t, Q^2) = R_3^{(v)}(Q^2) \left( \frac{1}{s - m_N^2} + \frac{1}{u - m_N^2} \right) - eg \frac{F_\pi(Q^2)}{t - m_\pi^2} + f_{sub}(t, Q^2) + \frac{P}{\pi} \int_{s_{thr}}^{\infty} Im B_3^{(-)}(s', t, Q^2) \left( \frac{1}{s' - s} + \frac{1}{s' - u} \right) ds'$$

From fit to high  $Q^2$  data:  $f_{sub}(t, Q^2) = -(1.62 + 0.5*t) + Q^2(0.32 + 0.11*t)$

# Legendre moments reveal large N(1440)1/2<sup>+</sup>

$n\pi^+$

$Q^2=2.05 \text{ GeV}^2$

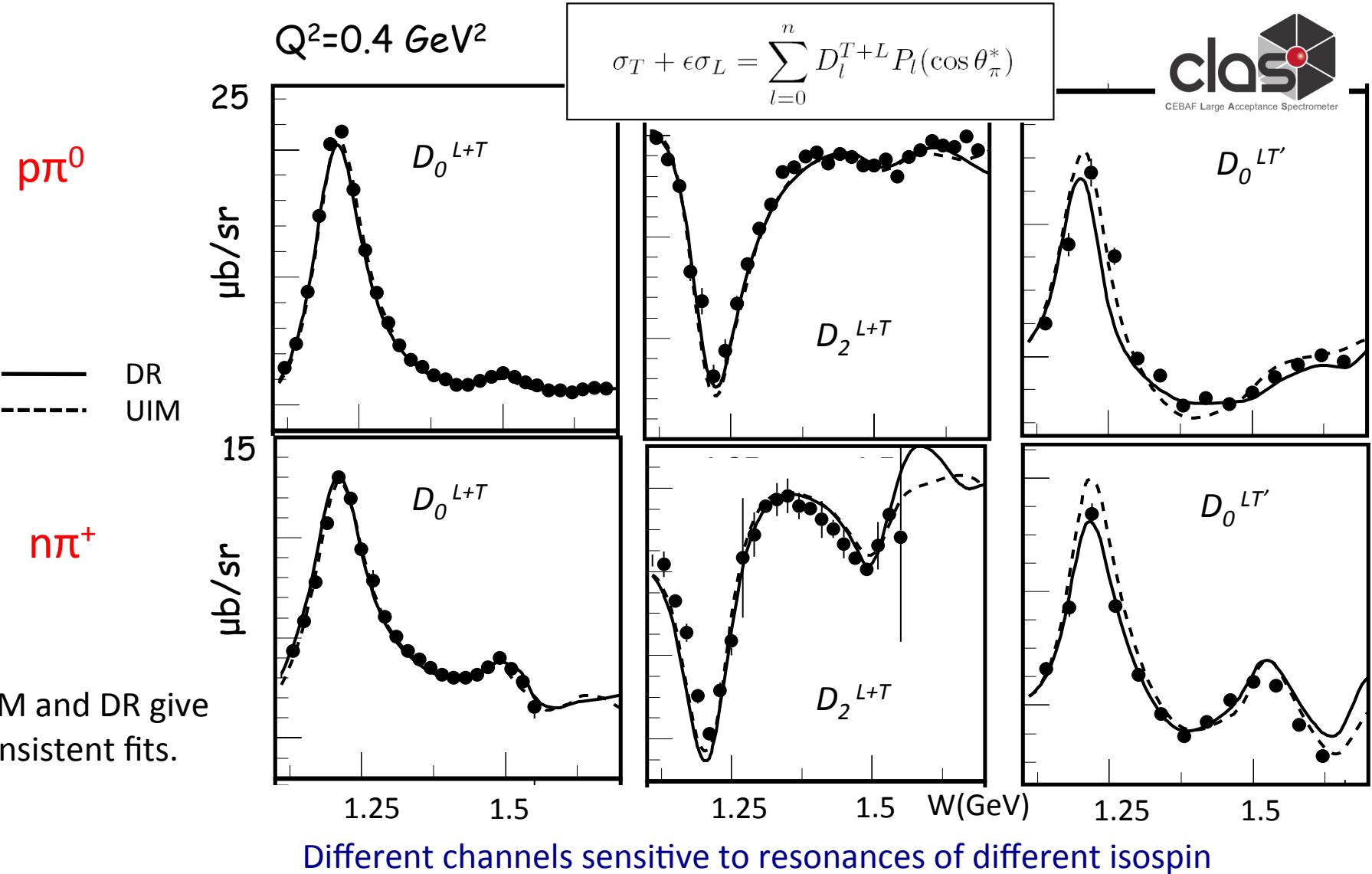


Peaks in P33, D13/S11 region,  
broad enhancement from P11  
partial wave (Roper).

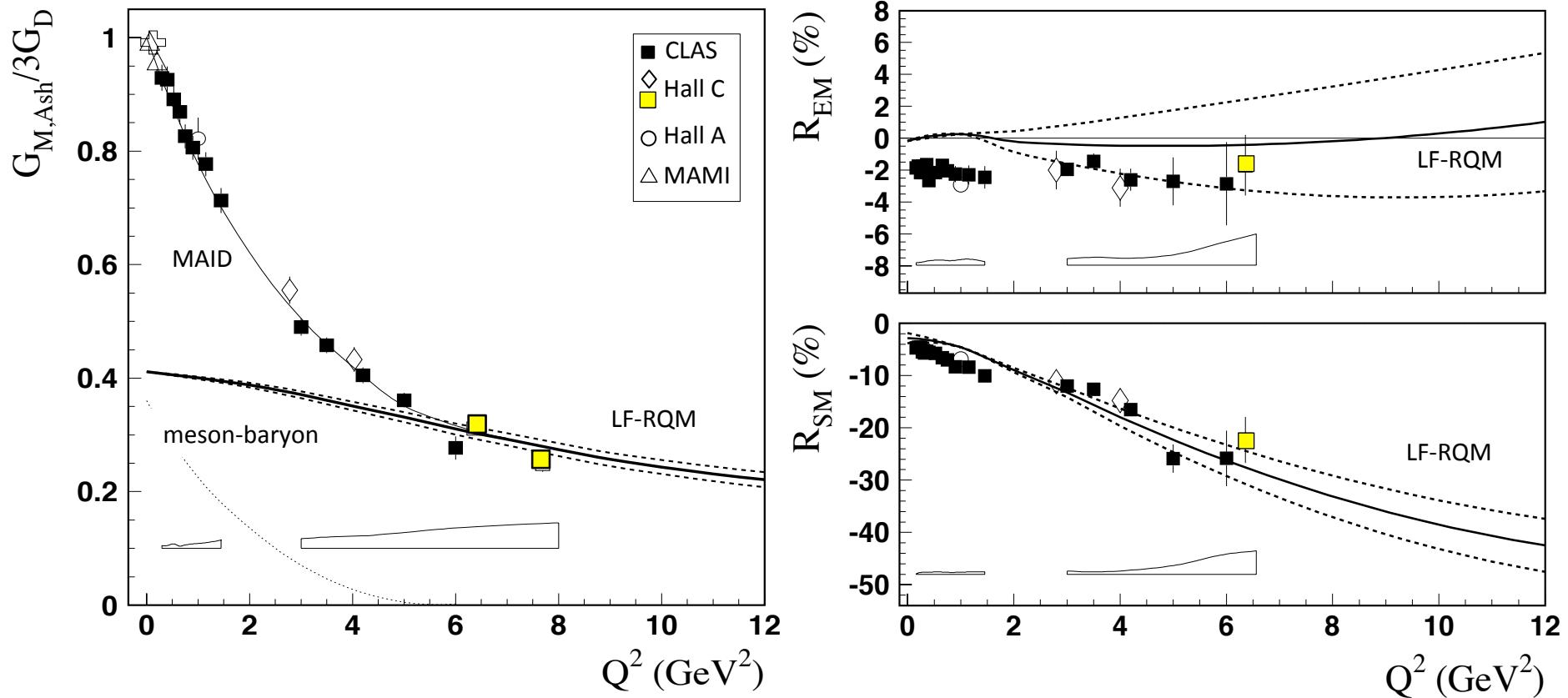
Broad structure from  
1.2 to 1.5GeV due to s-  
p interference terms.

Dip in  $\Delta$  region  
S11-D13 interference

# Legendre Moments for $e p \rightarrow e N \pi$



# The $N\Delta(1232)$ Transition in $\gamma^* p \rightarrow p\pi^0$



- LF-RQM quark core and MB of similar magnitude at  $Q^2=0$ .
- Describes  $G_M$  at  $Q^2 \geq 5 \text{ GeV}^2$ .
- Transition to asymptotic behavior  $R_{EM} \rightarrow +100\%$  not in sight. Described with MB.
- Predicts  $R_{SM}$  to continue to grow in magnitude at large  $Q^2$ . ( $\text{AdS/QCD} \Rightarrow -100\%$ )

LF-RQM: I. Aznauryan, VB; prel. (2015)