



Polarization Observables in Kaon Photoproduction

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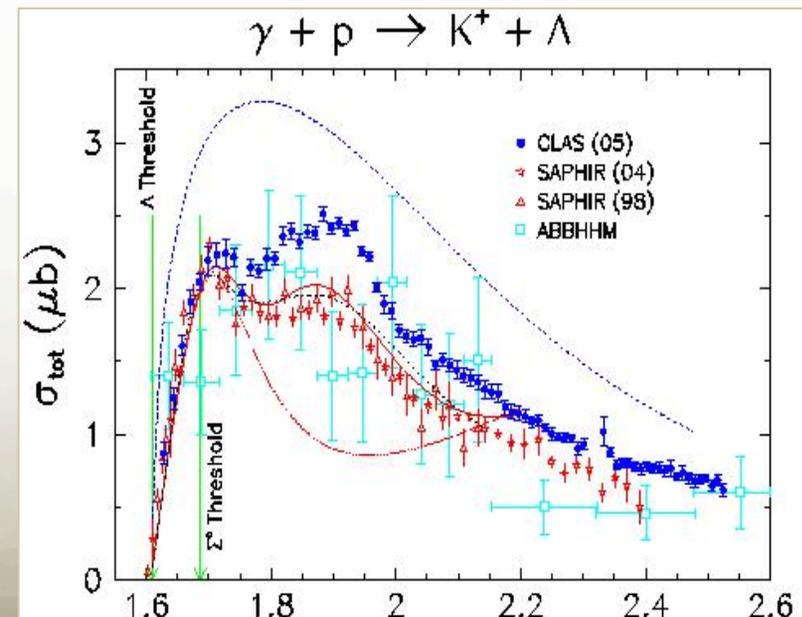
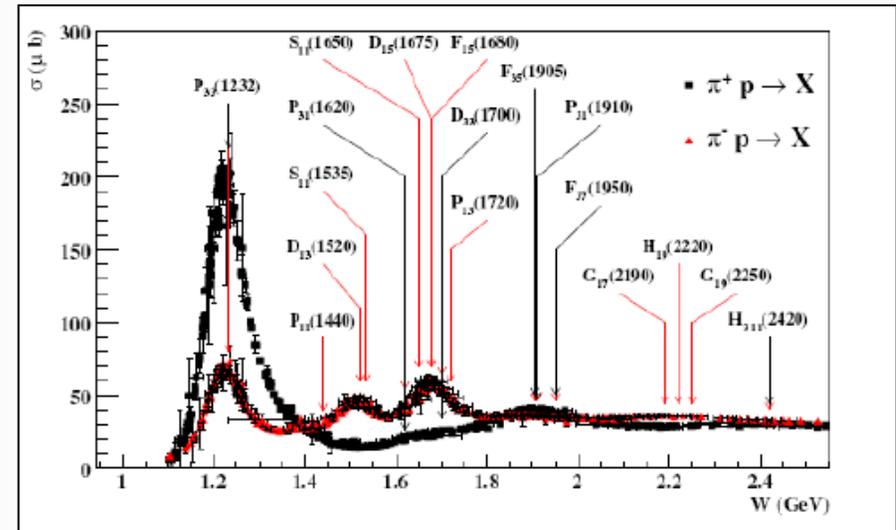
Outline

- Introduction
- Experimental Setup
- Event Selection
- Preliminary Results
- Conclusion



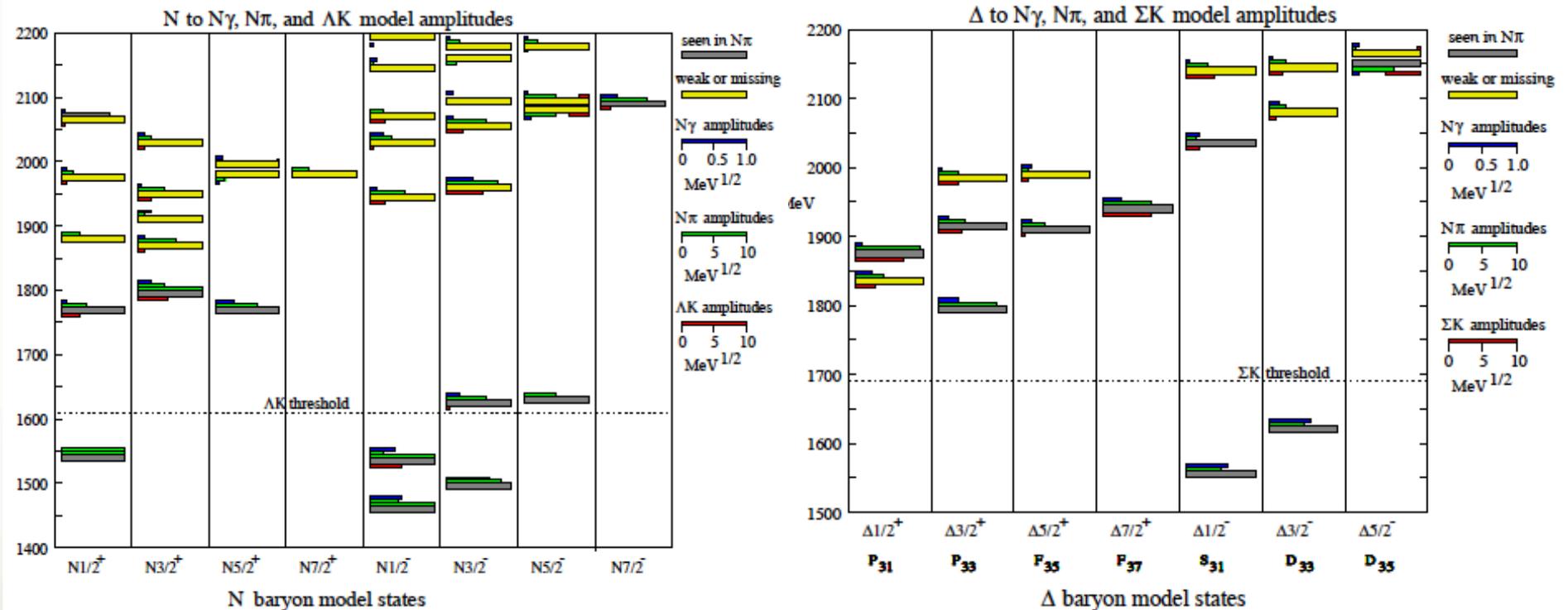
Baryon Resonances

- Approximate models are used to describe the nucleon spectrum
- Most resonances found in πN PWA
- Other channels may provide info on resonances that do NOT couple to πN
- $K^+ \Lambda$ is an isospin filter....no coupling to Δ^* ($I=3/2$)
- $K^+ \Lambda$ cross section easier disentangled since it only couples to a few N^* resonances (and those might couple weakly to πN !)





Constituent Quark Model

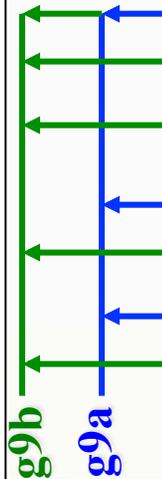


- Above 1850 MeV (N^*) and 1950 MeV (Δ^*) most have predicted states that have not been seen experimentally
- More model states predicted than observed so far



Polarization Observables

| Spin observable | Helicity representation |
|---|---|
| $\check{\Omega}^1 \equiv \mathcal{I}(\theta)$ | $\frac{1}{2}(H_1 ^2 + H_2 ^2 + H_3 ^2 + H_4 ^2)$ |
| $\check{\Omega}^4 \equiv \check{\Sigma}$ | $\text{Re}(-H_1H_4^* + H_2H_3^*)$ |
| $\check{\Omega}^{10} \equiv -\check{T}$ | $\text{Im}(H_1H_2^* + H_3H_4^*)$ |
| $\check{\Omega}^{12} \equiv \check{P}$ | $\text{Im}(-H_1H_3^* - H_2H_4^*)$ |
| $\check{\Omega}^3 \equiv \check{G}$ | $\text{Im}(H_1H_4^* - H_3H_2^*)$ |
| $\check{\Omega}^5 \equiv \check{H}$ | $\text{Im}(-H_2H_4^* + H_1H_3^*)$ |
| $\check{\Omega}^9 \equiv \check{E}$ | $\frac{1}{2}(H_1 ^2 - H_2 ^2 + H_3 ^2 - H_4 ^2)$ |
| $\check{\Omega}^{11} \equiv \check{F}$ | $\text{Re}(-H_2H_1^* - H_4H_3^*)$ |
| $\check{\Omega}^{14} \equiv \check{O}_x$ | $\text{Im}(-H_2H_1^* + H_4H_3^*)$ |
| $\check{\Omega}^7 \equiv -\check{O}_z$ | $\text{Im}(H_1H_4^* - H_2H_3^*)$ |
| $\check{\Omega}^{16} \equiv -\check{C}_x$ | $\text{Re}(H_2H_4^* + H_1H_3^*)$ |
| $\check{\Omega}^2 \equiv -\check{C}_z$ | $\frac{1}{2}(H_1 ^2 + H_2 ^2 - H_3 ^2 - H_4 ^2)$ |
| $\check{\Omega}^6 \equiv -\check{T}_x$ | $\text{Re}(-H_1H_4^* - H_2H_3^*)$ |
| $\check{\Omega}^{13} \equiv -\check{T}_z$ | $\text{Re}(-H_1H_2^* + H_4H_3^*)$ |
| $\check{\Omega}^8 \equiv \check{L}_x$ | $\text{Re}(H_2H_4^* - H_1H_3^*)$ |
| $\check{\Omega}^{15} \equiv \check{L}_z$ | $\frac{1}{2}(- H_1 ^2 + H_2 ^2 + H_3 ^2 - H_4 ^2)$ |



- Photoproduction of single pseudoscalar mesons is described by four complex helicity amplitudes, which describe all spin combinations of incoming and outgoing particles, leading to 16 bilinear products
- Polarization observables are combinations of the 16 bilinear products and can be extracted based on target, beam, and recoil polarization
- Not all observables are independent from each other

| Photon | Target | | | | Recoil | | | Target + Recoil | | | |
|---------------|------------|-----|--------|------|-----------|--------|-----------|-----------------|------------|-------------|-------------|
| | - | - | - | - | x' | y' | z' | x' | x' | z' | z' |
| | - | x | y | z | - | - | - | x | z | x | z |
| unpolarized | σ_0 | 0 | T | 0 | 0 | P | 0 | $T_{x'}$ | $-L_{x'}$ | $T_{z'}$ | $L_{z'}$ |
| linear pol. | $-\Sigma$ | H | $(-P)$ | $-G$ | $O_{x'}$ | $(-T)$ | $O_{z'}$ | $(-L_{z'})$ | $(T_{z'})$ | $(-L_{x'})$ | $(-T_{x'})$ |
| circular pol. | 0 | F | 0 | $-E$ | $-C_{x'}$ | 0 | $-C_{z'}$ | 0 | 0 | 0 | 0 |



Available World Data

| $\gamma p \rightarrow K^+ \Lambda$ | Observ. | N_{data} | χ^2_1/N_{data} |
|------------------------------------|-------------------|-------------------|----------------------------|
| [43] CLAS | $d\sigma/d\Omega$ | 1320 | 0.69 |
| [51] LEPS | Σ | 45 | 2.11 |
| [50] GRAAL | Σ | 66 | 2.95 |
| [43] CLAS | P | 1270 | 1.82 |
| [50] GRAAL | P | 66 | 0.59 |
| [52] GRAAL | T | 66 | 1.62 |
| [40] CLAS | C_x | 160 | 1.52 |
| [40] CLAS | C_z | 160 | 1.58 |
| [52] GRAAL | $O_{x'}$ | 66 | 1.95 |
| [52] GRAAL | $O_{z'}$ | 66 | 1.66 |

Available data used by Bonn-Gatchina solution (BG2011-12)

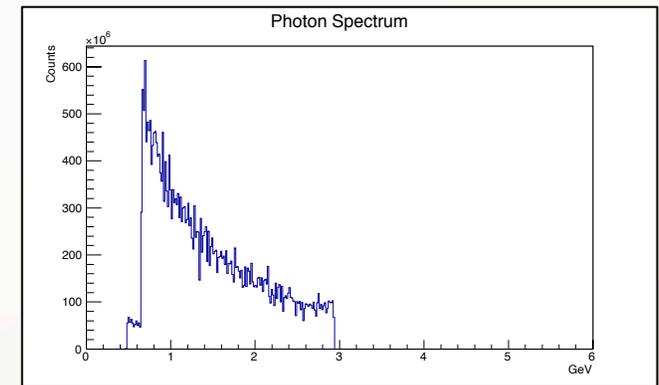
Clear lack in data for kaon photoproduction!!

| $\gamma p \rightarrow K^+ \Sigma^0$ | Observ. | N_{data} | χ^2_1/N_{data} |
|-------------------------------------|-------------------|-------------------|----------------------------|
| [62] CLAS | $d\sigma/d\Omega$ | 1590 | 1.44 |
| [51] LEPS | Σ | 45 | 1.23 |
| [52] GRAAL | Σ | 42 | 1.99 |
| [62] CLAS | P | 344 | 2.69 |
| [40] CLAS | C_x | 94 | 1.95 |
| [40] CLAS | C_z | 94 | 1.66 |
| $\gamma p \rightarrow K^0 \Sigma^+$ | Obsv. | N_{data} | χ^2_1/N_{data} |
| [63] CLAS | $d\sigma/d\Omega$ | 48 | 3.84 |
| [64] SAPHIR | $d\sigma/d\Omega$ | 160 | 1.91 |
| [65] CBT | $d\sigma/d\Omega$ | 72 | 0.76 |
| [66] CBT | $d\sigma/d\Omega$ | 72 | 0.62 |
| [65] CBT | P | 72 | 0.90 |
| [66] CBT | P | 24 | 0.94 |
| [66] CBT | Σ | 15 | 1.73 |



Experimental Setup

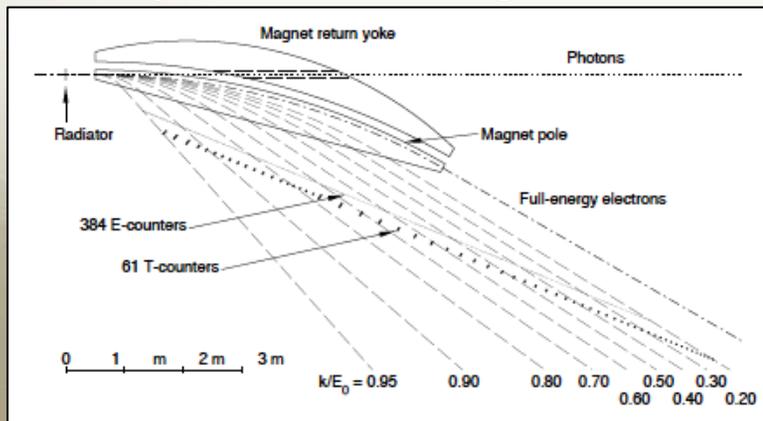
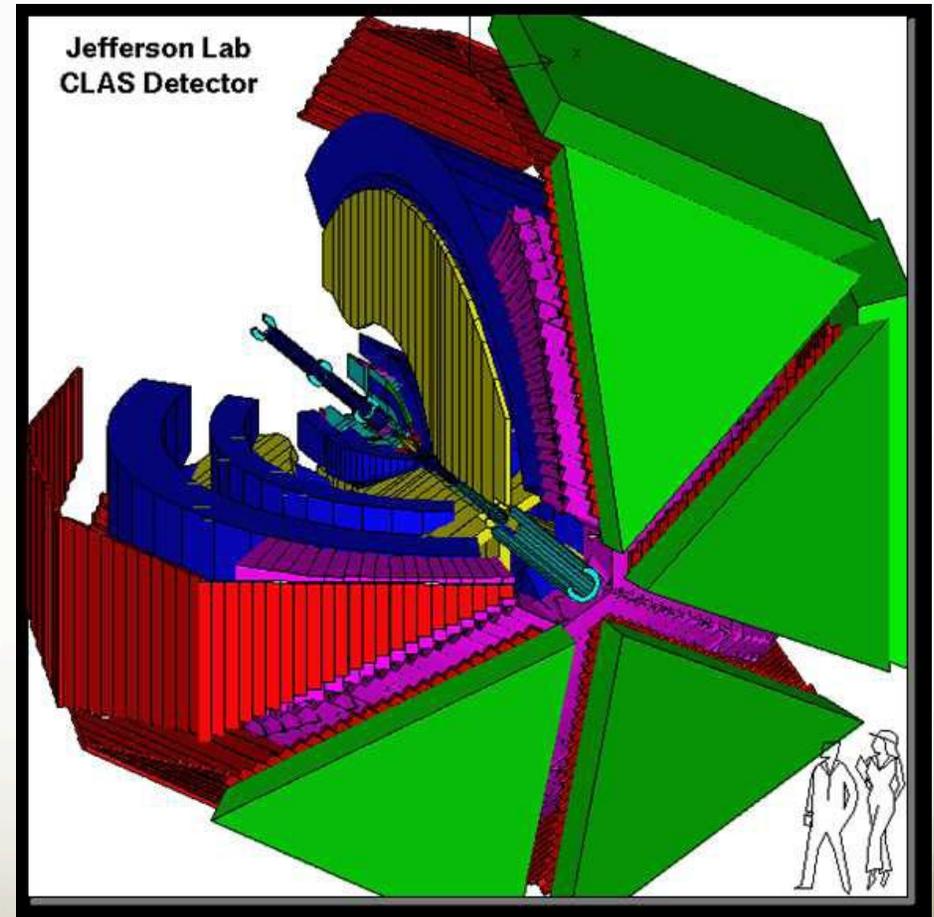
- The **FROST** experiment was first approved in 2002 with CLAS, ran in two parts in 2007-2008 (g9a-longitudinally polarized target) and 2010 (g9b-transversely polarized target)
- Butanol **FRO**zen **S**pin **T**arget with free protons polarized
- Polarized photon beam
 - Circularly (Au radiator)
 - Linearly (Diamond radiator)
- Photon beam energies from 0.5 to 3.0 GeV (circular) and 1.1 to 2.1 GeV (linear)
- 10 billion events collected (g9a)
14 billion events collected (g9b)
- ‘Complete measurement’: all beam-target and target-recoil observables from $K^+ \Lambda$ and $K^+ \Sigma^0$ final states





JLab, CLAS, and the Tagger

- Up to 5 passes for a max of ~ 6 GeV (upgrade allows ~ 12 GeV)
- After bremsstrahlung, recoil electrons are bent towards the electron dump via a dipole magnetic field created by the tagger magnet
- Tagger had ability to measure electron energies that are then used to calculate the energy associated with the photons and timing of accelerator
- CLAS had almost full acceptance, 80% of 4π coverage



$$E_{\gamma} = E_{\text{beam}} - E_{\text{e scattered}}$$

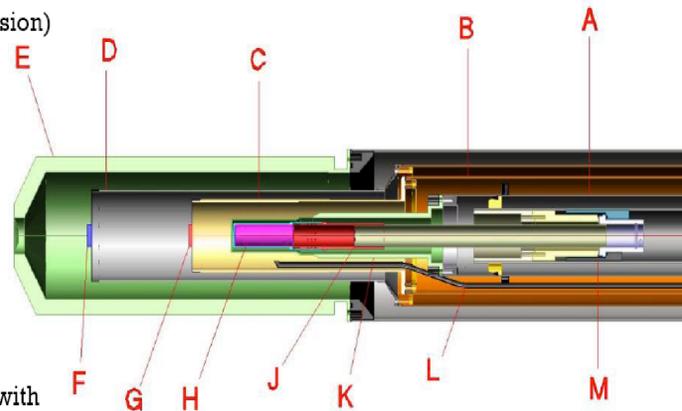


FROST Target

The FroST target and its components:

- A: Primary heat exchanger
- B: 1 K heat shield
- C: Holding coil
- D: 20 K heat shield
- E: Outer vacuum can (Rohacell extension)
- F: CH₂ target
- G: Carbon target
- H: Butanol target
- J: Target insert
- K: Mixing chamber
- L: Microwave waveguide
- M: Kapton coldseal

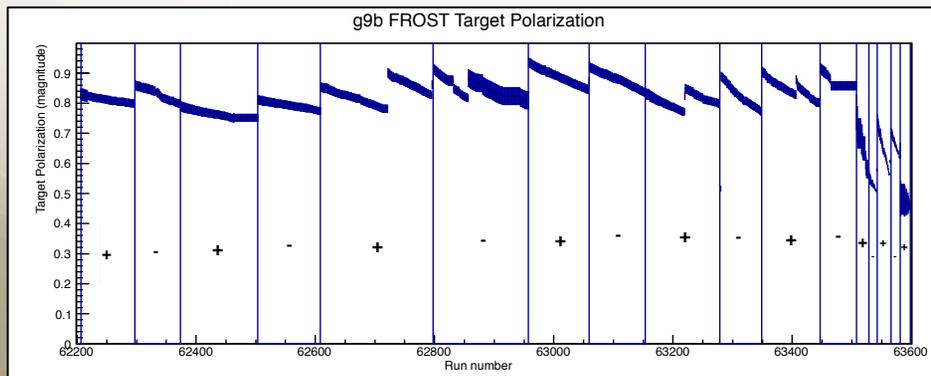
Butanol Composition:
C₄H₉OH + liquid He



Performance Specs:

Base Temp: 28 mK w/o beam, 30 mK with
 Cooling Power: 800 μW @ 50 mK, 10 mW @ 100 mK, and 60 mW @ 300 mK
 Polarization: +82%, -90%
 1/e Relaxation Time: 2800 hours (+Pol), 1600 hours (-Pol)

- Butanol in LHe bath
- Polarizing 5 Tesla magnet aligns free proton spins
- Holding coil keeps proton polarized

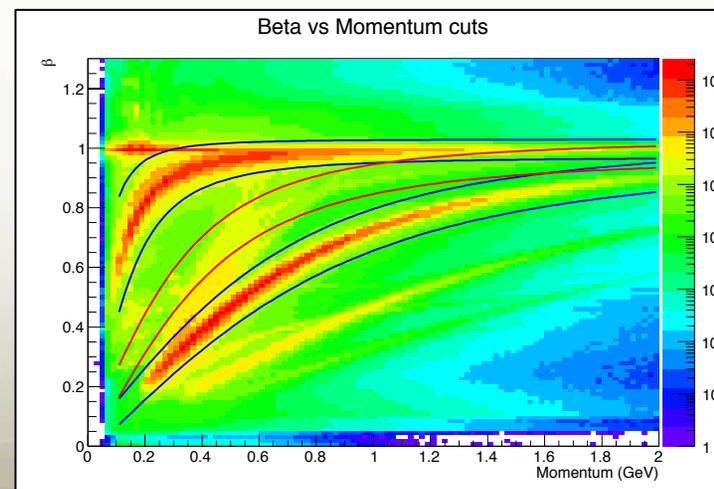
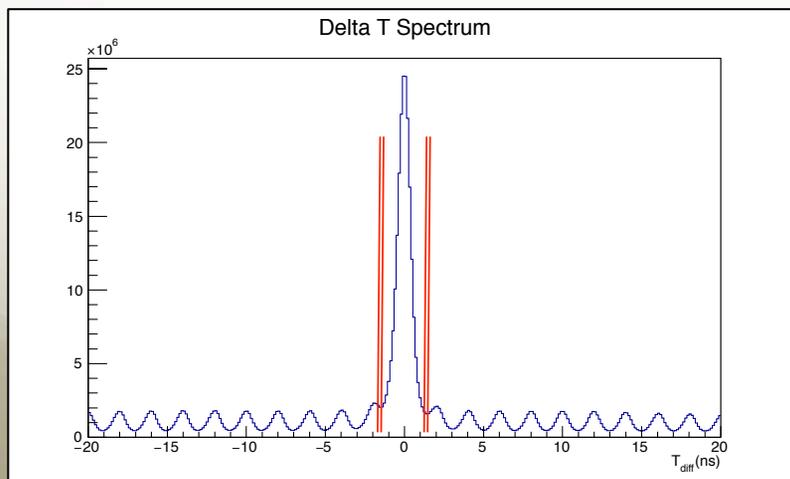


Target re-polarized
 ~once per week!!



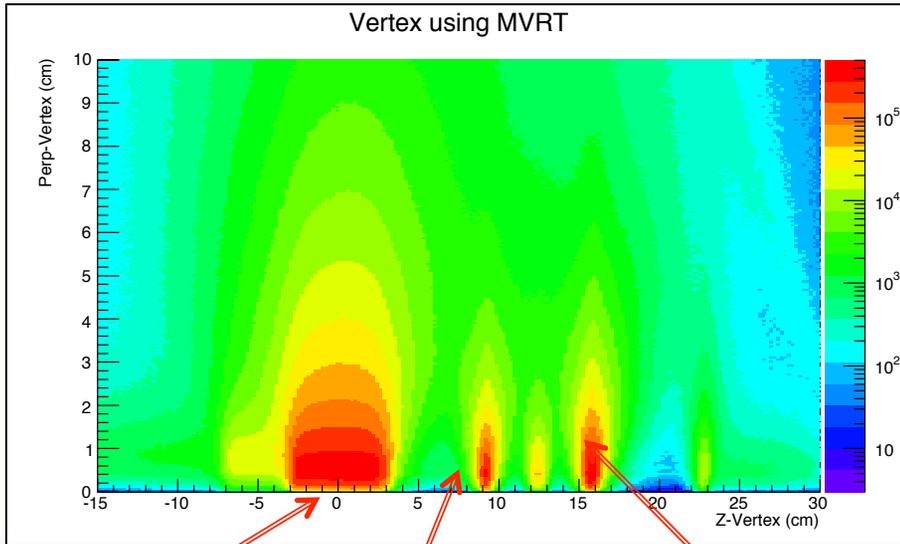
Event Selection

- Skimmed data for events
 - $\gamma p \rightarrow K^+ \Lambda \rightarrow K^+ p(\pi^-)$ AND $\gamma p \rightarrow K^+ \Sigma^0 \rightarrow K^+ \Lambda \gamma \rightarrow K^+ p(\gamma \pi^-)$
- One proton, one kaon identified
- One photon identified with cut on coincidence of ± 1 ns
- Only two positively charged particles





Vertices

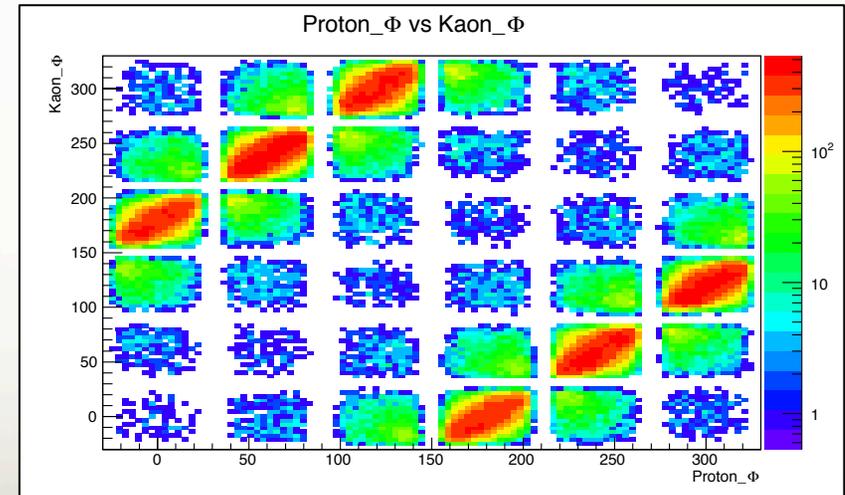
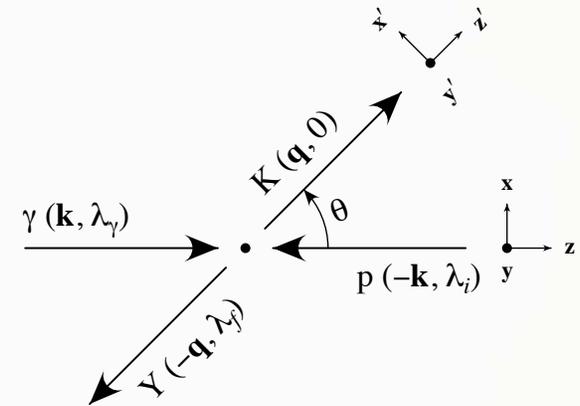


Butanol

Carbon

CH₂

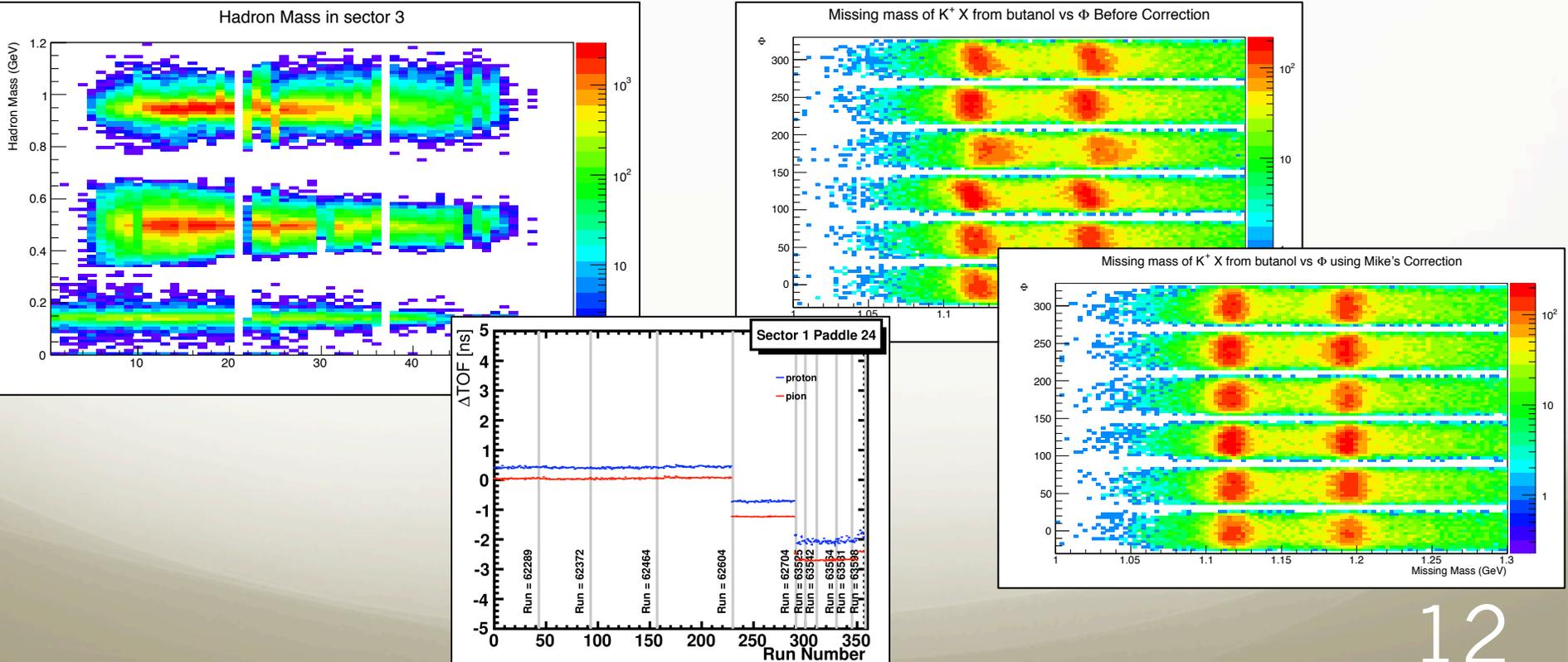
- Cut on kaon event vertex
- Check whether p from Λ decay vertex by comparing azimuthal angles of p and K⁺ (p almost in same direction as Λ , which is opposite of K⁺ in CM frame)





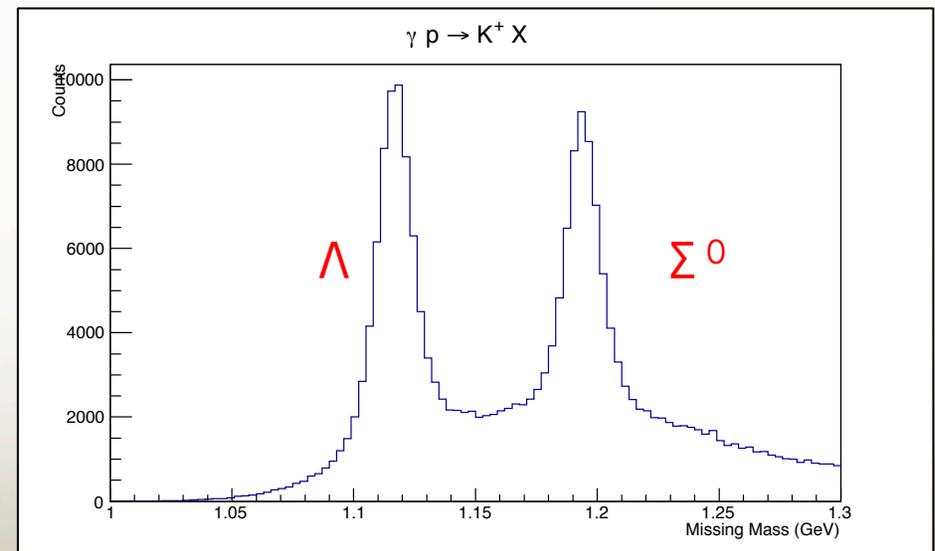
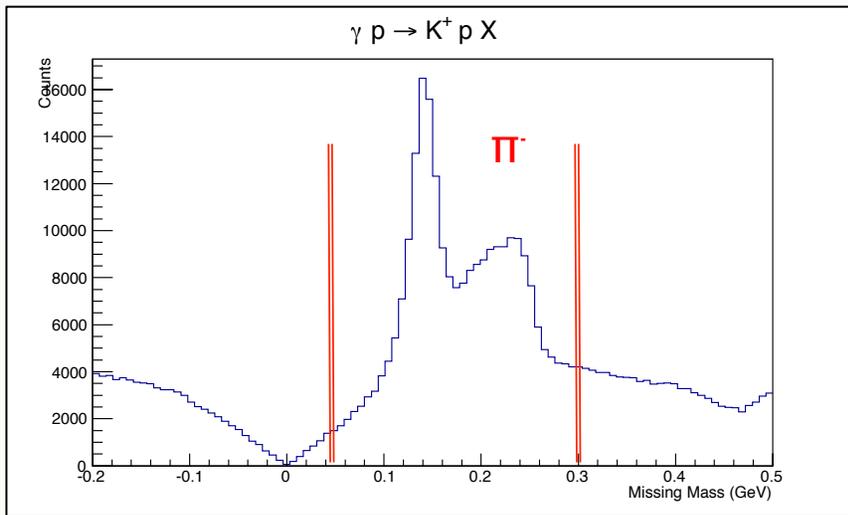
Corrections to Data

- Bad TOF paddles cut
- Sector dependent momentum correction applied
- Timing offset between protons and pions in TOF corrected





Missing Mass Cuts





Extracting φ -dependent Observables: Moment Method

$$\frac{d\sigma}{d\Omega} = \frac{d\sigma_0}{d\Omega} \left(1 + P_{XY}^{lab} P_c F \cos\phi - P_{XY}^{lab} T \sin\phi \right)$$

Define phi dependent density function within each W and cosine bin

$$f^{i,j}(\varphi) \equiv \rho L \int_{E_{i-1}}^{E_i} \int_{\cos\theta_{j-1}}^{\cos\theta_j} \varepsilon(E, \theta, \varphi) \frac{d^3\sigma}{d(\cos\theta)dEd\varphi} d(\cos\theta)dE$$

Expand density function $f(\phi)$ in Fourier series...

$$f_a^{i,j}(\varphi) = a_0 + \sum_{m=1}^{\infty} [a_m \cos(m\varphi) + b_m \sin(m\varphi)]$$

$$Y_{l,n} = \int_0^{2\pi} f_l^{i,j}(\phi) \cos(n\phi) d\phi$$

$$Z_{l,n} = \int_0^{2\pi} f_l^{i,j}(\phi) \sin(n\phi) d\phi$$

Separate cosine/sin terms



Moment Method Continued

$$Y_{l,n} = \int_0^{2\pi} f_l^{i,j}(\phi) \cos(n\phi) d\phi \quad Z_{l,n} = \int_0^{2\pi} f_l^{i,j}(\phi) \sin(n\phi) d\phi$$

$$T = 2 \frac{\bar{Z}_{A,1} + \bar{Z}_{B,1} - \bar{Z}_{C,1} - \bar{Z}_{D,1}}{P_C(\bar{Y}_{A,0} + \bar{Y}_{B,0} - \bar{Y}_{A,2} - \bar{Y}_{B,2}) + P_A(\bar{Y}_{C,0} + \bar{Y}_{D,0} - \bar{Y}_{C,2} - \bar{Y}_{D,2})}$$

$$F = \frac{2(P_A + P_C)}{P_A P_C (\lambda_A + \lambda_C)} \frac{P_C(\bar{Y}_{A,1} - \bar{Y}_{B,1}) + P_A(\bar{Y}_{D,1} - \bar{Y}_{C,1})}{P_C(\bar{Y}_{A,0} + \bar{Y}_{B,0} + \bar{Y}_{A,2} + \bar{Y}_{B,2}) + P_A(\bar{Y}_{C,0} + \bar{Y}_{D,0} + \bar{Y}_{C,2} + \bar{Y}_{D,2})}$$

λ_A – positive helicity
 λ_C – negative helicity

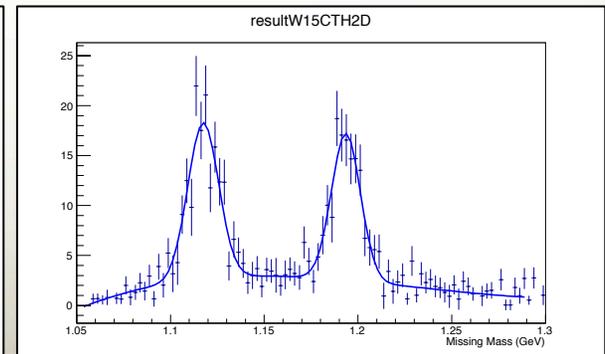
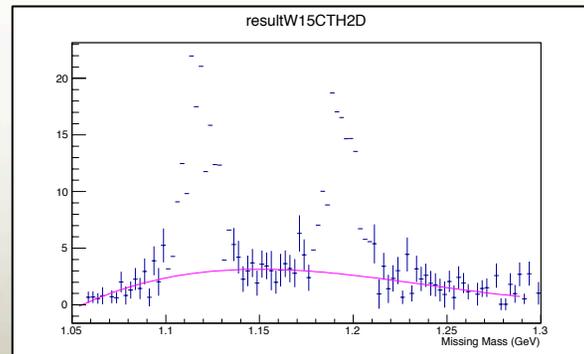
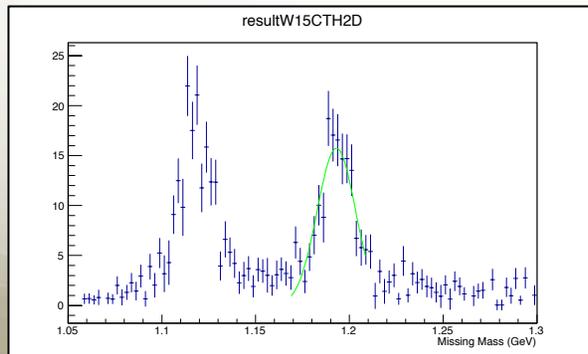
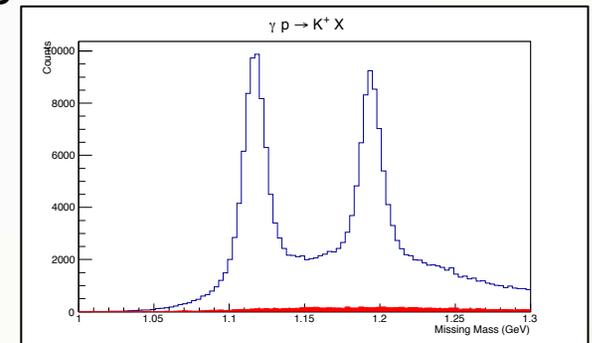
P_A – positive target polarization
 P_C – negative target polarization

T_x and T_z are double polarization observables with a transverse target polarization and recoil polarization in the Λ decay plane and calculated in similar way with moments!!



Background Subtraction

- Quasi-free kaon production is suppressed on **carbon** – so need to subtract free protons from bound protons
 - Fit Λ and Σ^0 signals with Gaussian
 - Fit remaining background with cubic polynomial
 - Then make a combined fit
 - Do for every $\cos \theta$ bin in every W bin!



Butanol – C_4H_9OH – only 10 free protons, 64 bound protons!!



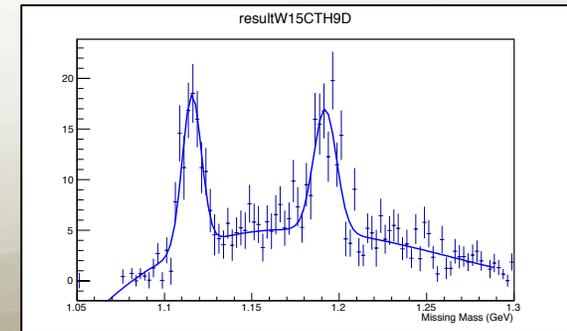
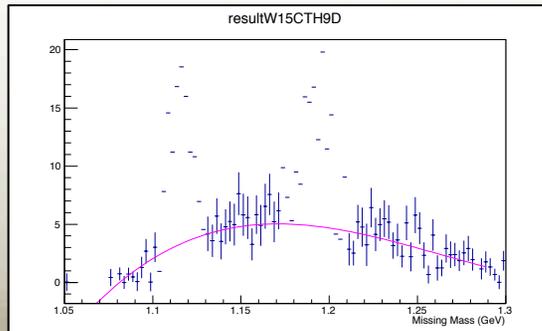
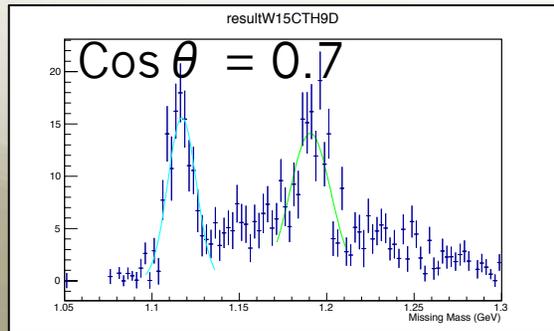
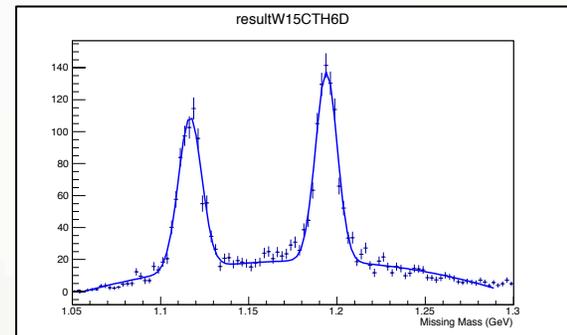
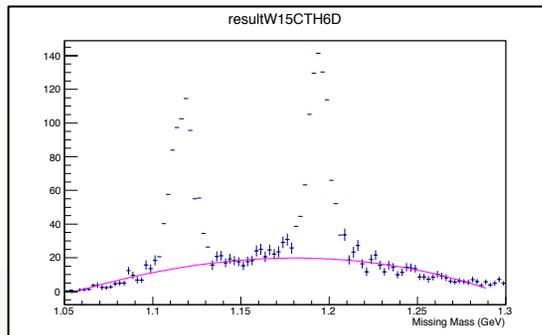
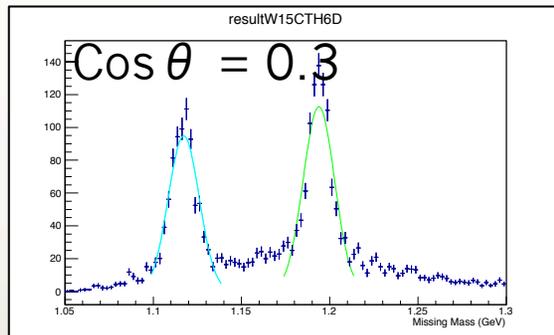
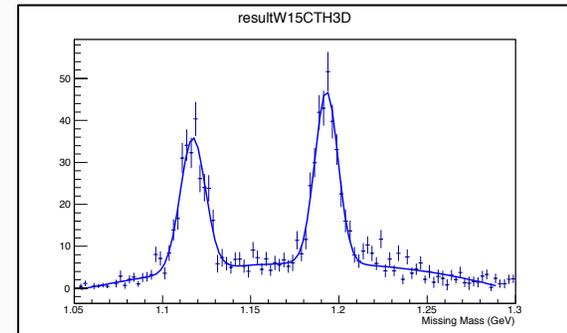
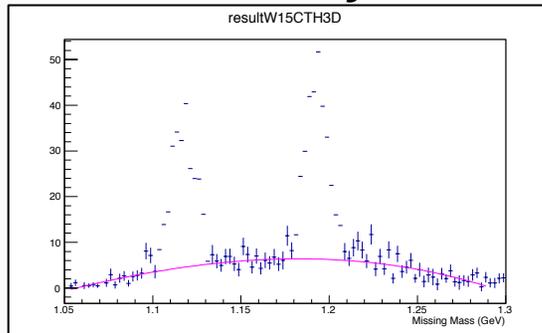
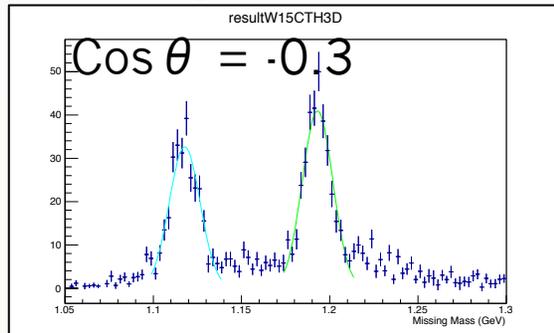
Background Subtraction

Example of Background Subtraction for $W = 1875$ MeV

Gaussian

3rd Order Polynomial

Global





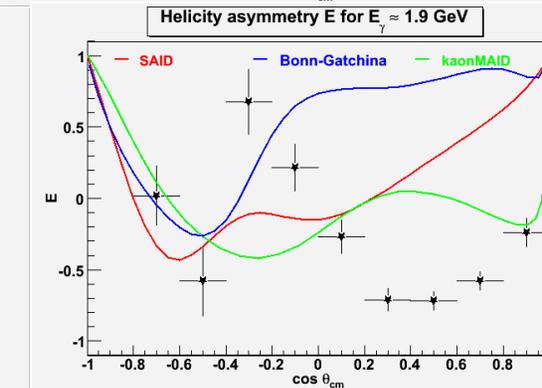
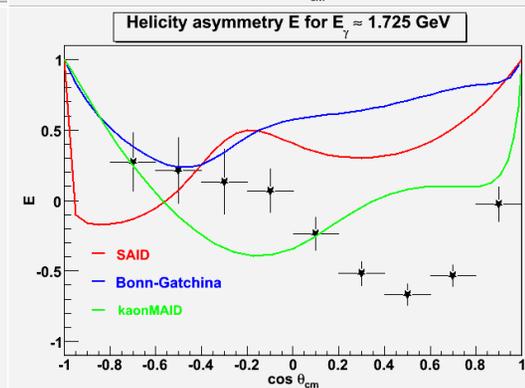
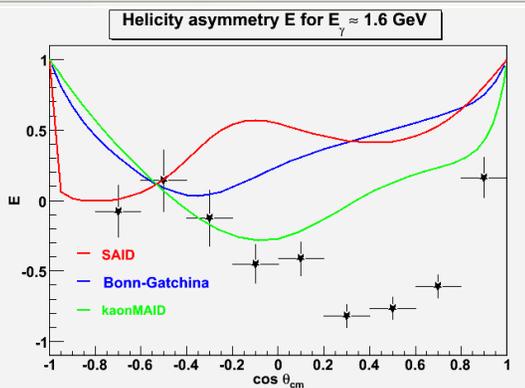
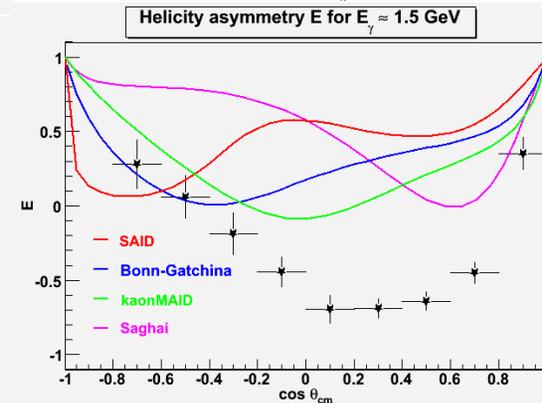
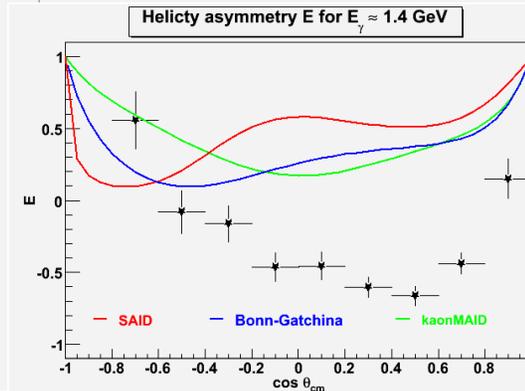
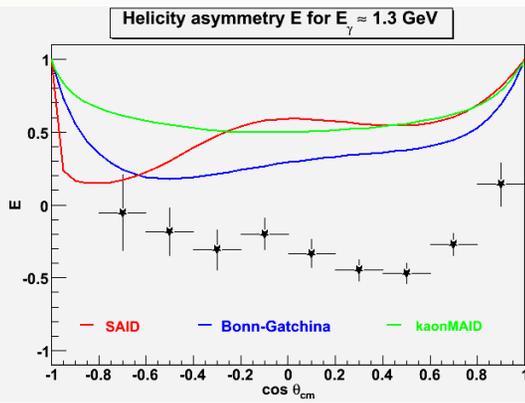
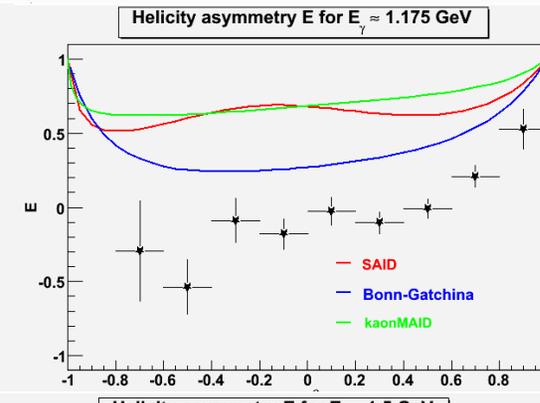
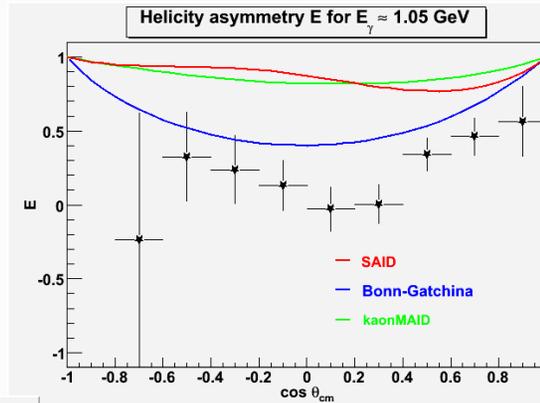
Results

- Results for E , L_x , L_z , T , F , T_x , and T_z
- Compared to theoretical models
 - KAON-MAID...isobar model
 - Bonn-Gatchina (BOGA)...coupled channel PWA
 - RPR-Ghent...isobar model



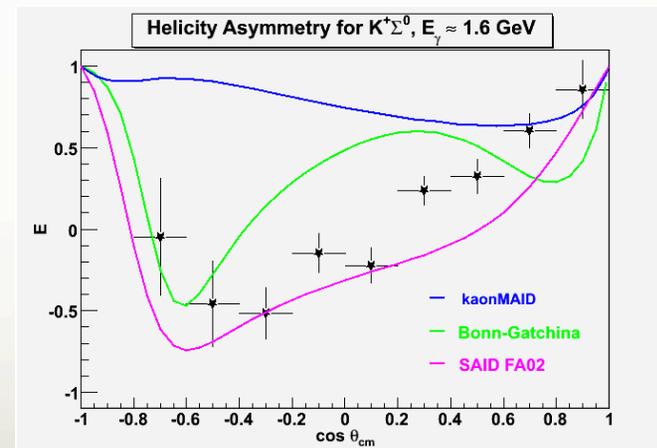
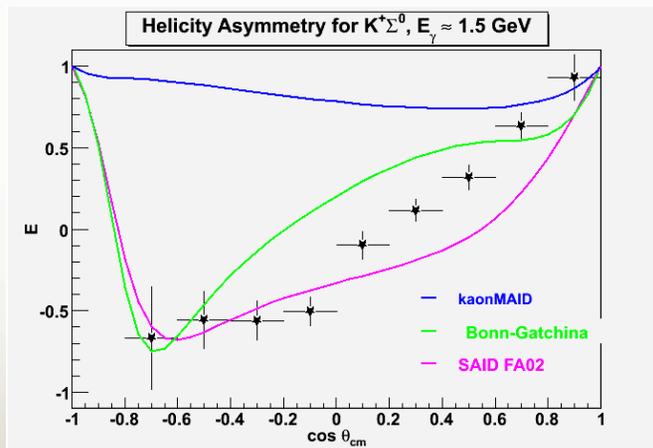
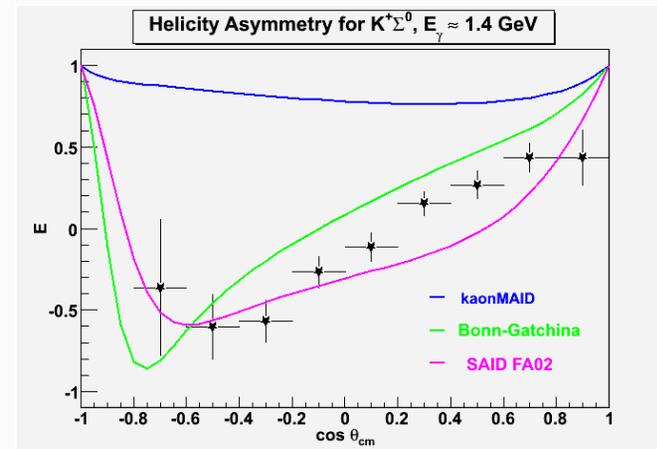
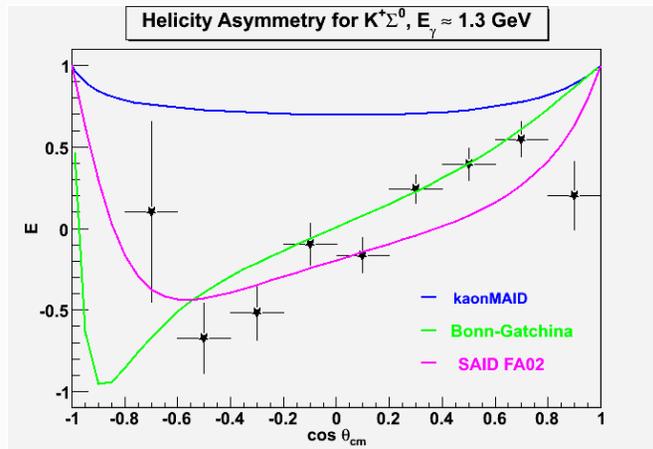
E for $K^+ \Lambda$

$$E = \frac{D_{eff}}{P_T P_\gamma} \frac{N_{1/2} - N_{3/2}}{N_{1/2} + N_{3/2}}$$





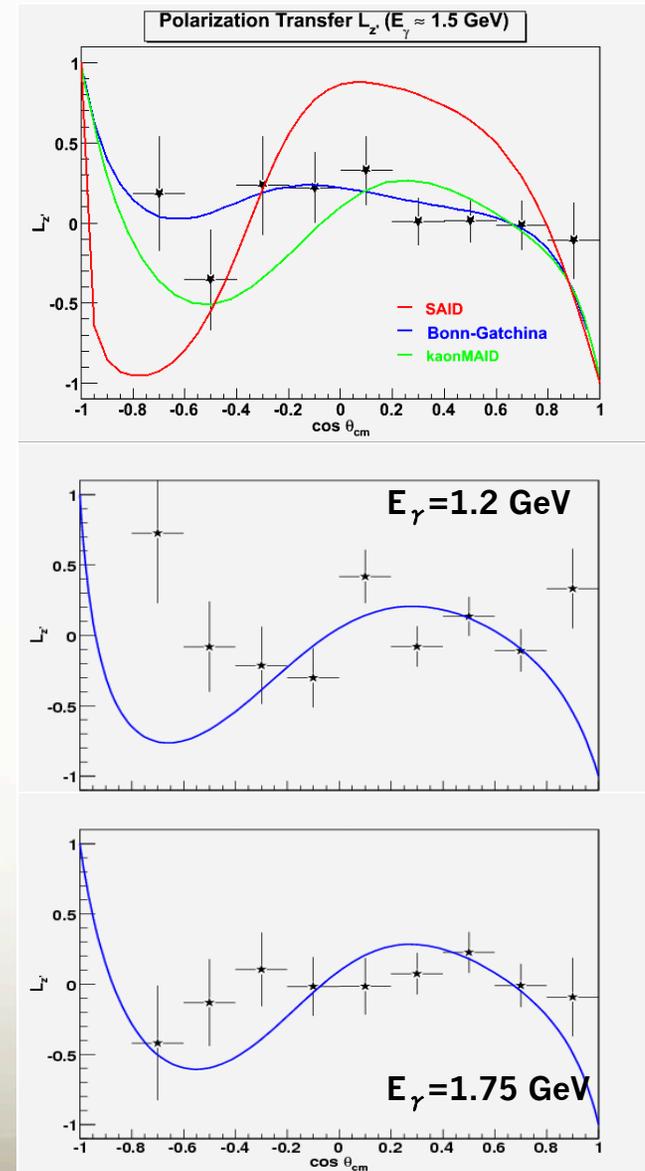
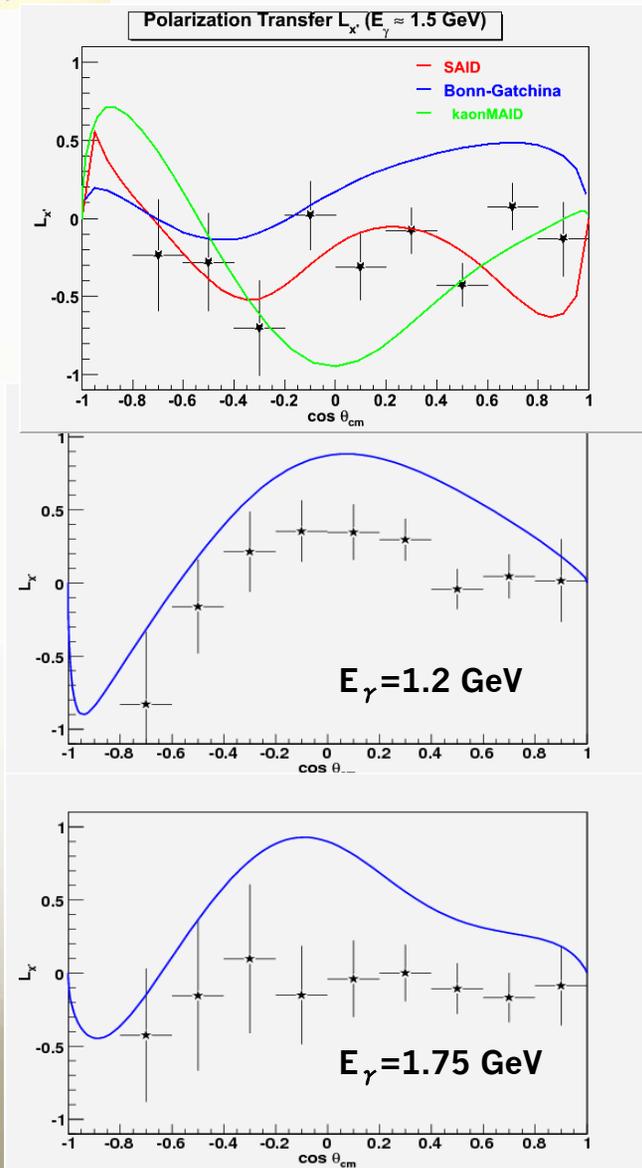
E for $K^+ \Sigma^0$



$$E = \frac{D_{eff}}{P_T P_y} \frac{N_{1/2} - N_{3/2}}{N_{1/2} + N_{3/2}}$$



L_x and L_z for $K^+ \Lambda$





T for $K^+ \Lambda$

Data:

CLAS g9b

Bonn78

GRAAL09

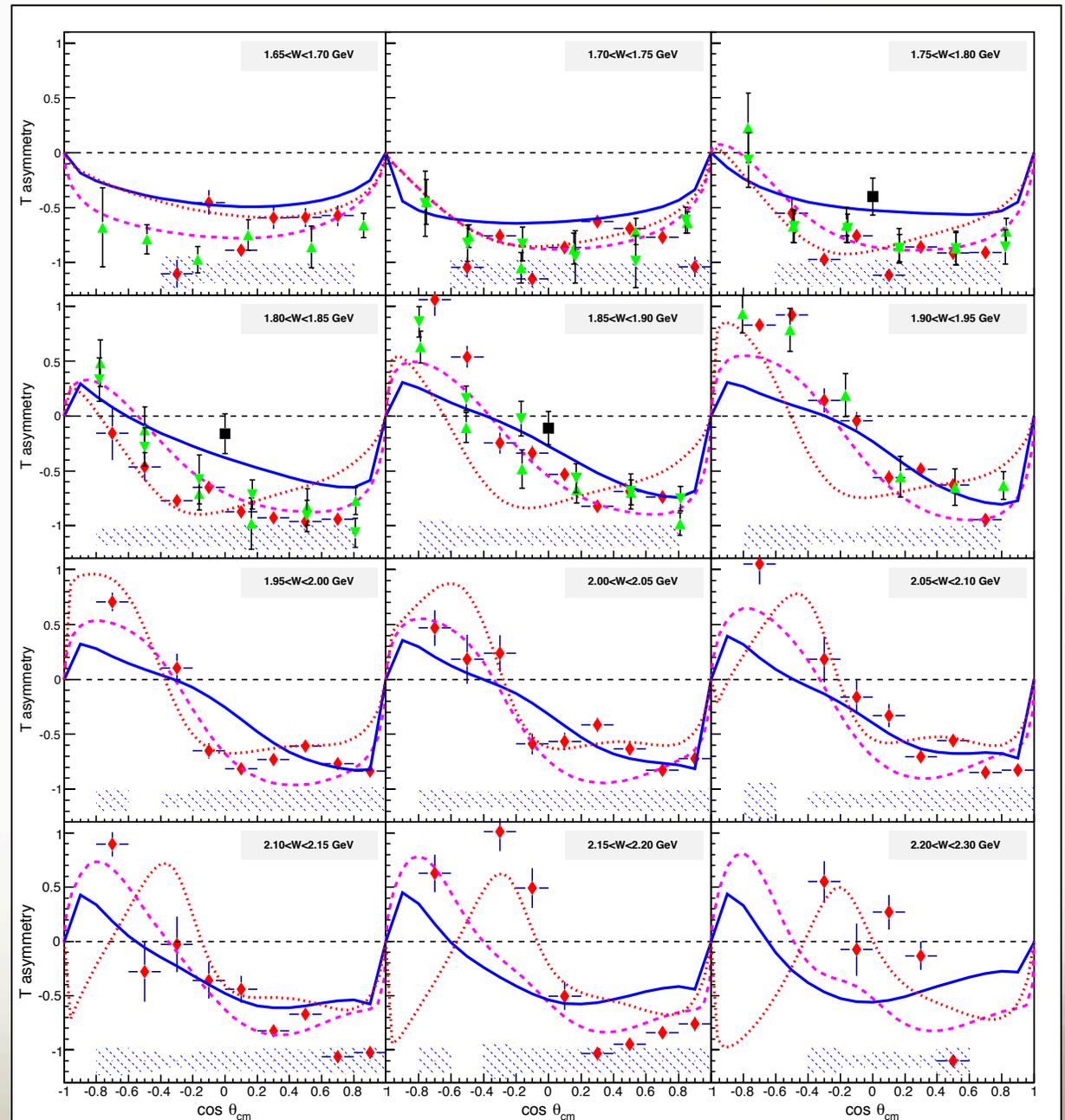
Models:

RPR-Ghent

Kaon-MAID

BOGA

Not yet compared to
Paterson *et al.*,
PRC **93** 065201 (2016)



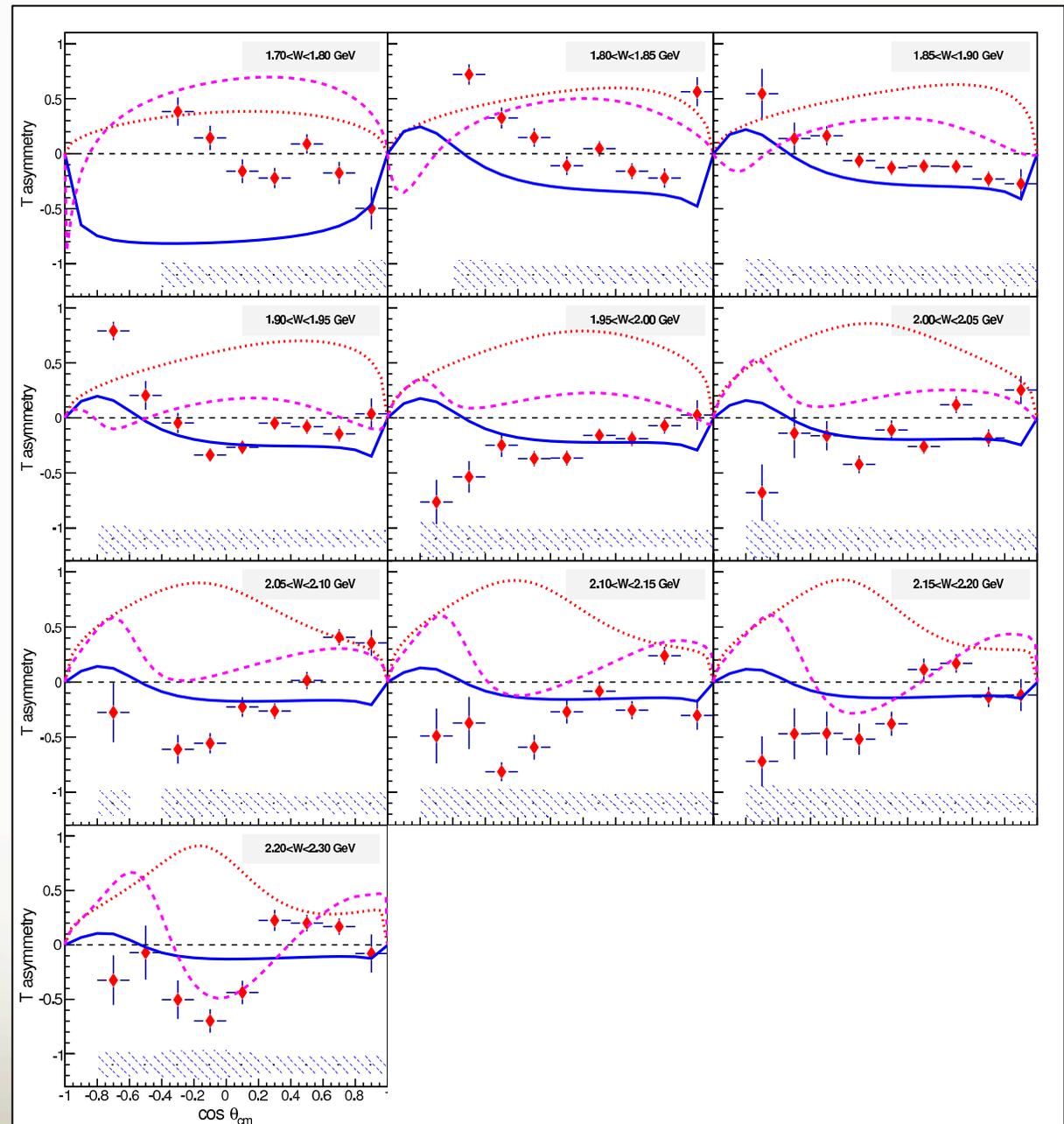


T for $K^+ \Sigma^0$

Data:
CLAS g9b

Models:
RPR-Ghent
Kaon-MAID
BOGA

Not yet compared to
Paterson *et al.*,
PRC **93** 065201 (2016)

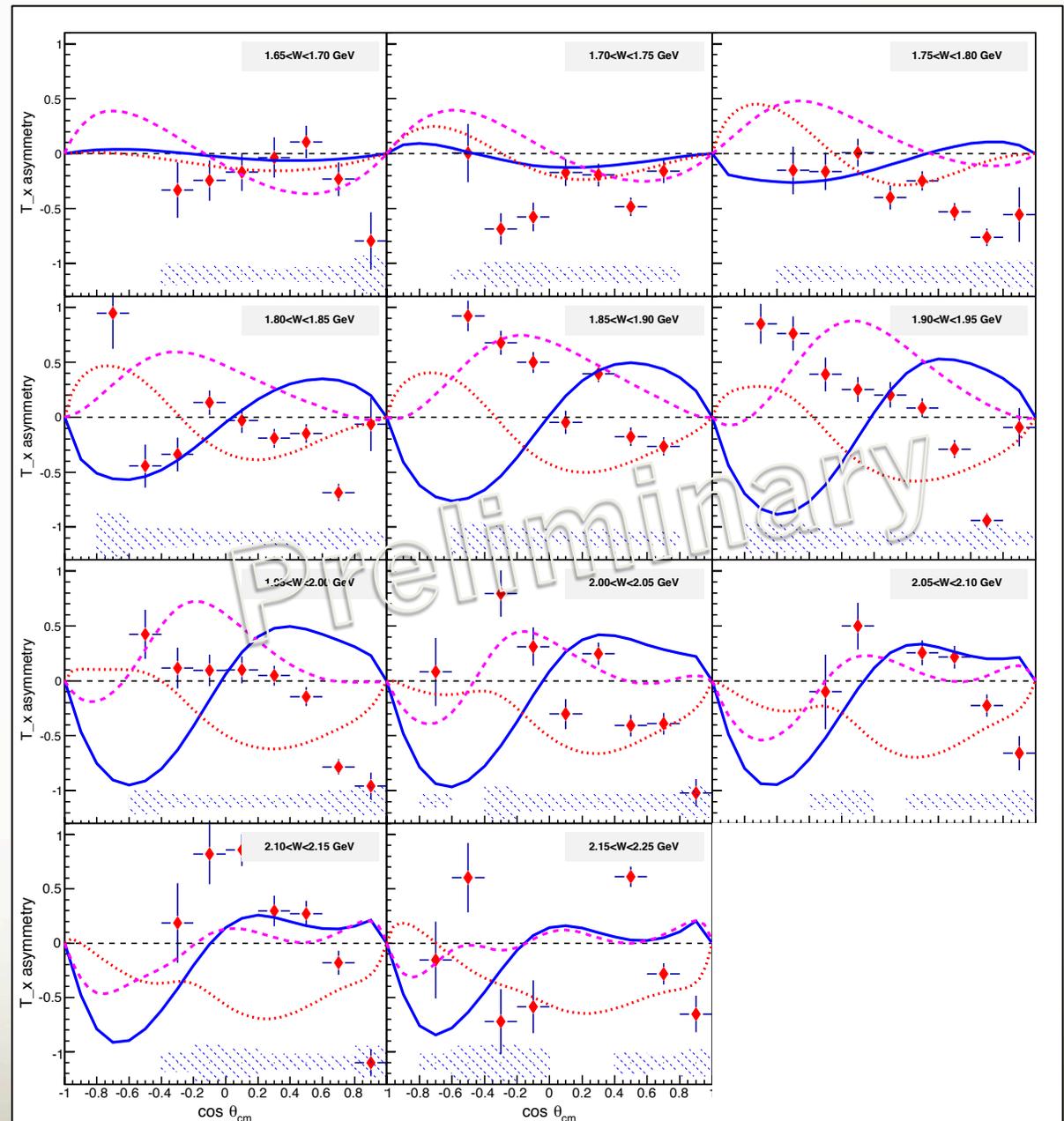




T_x for $K^+ \Lambda$

Data:
CLAS g9b

Models:
RPR-Ghent
Kaon-MAID
BOGA

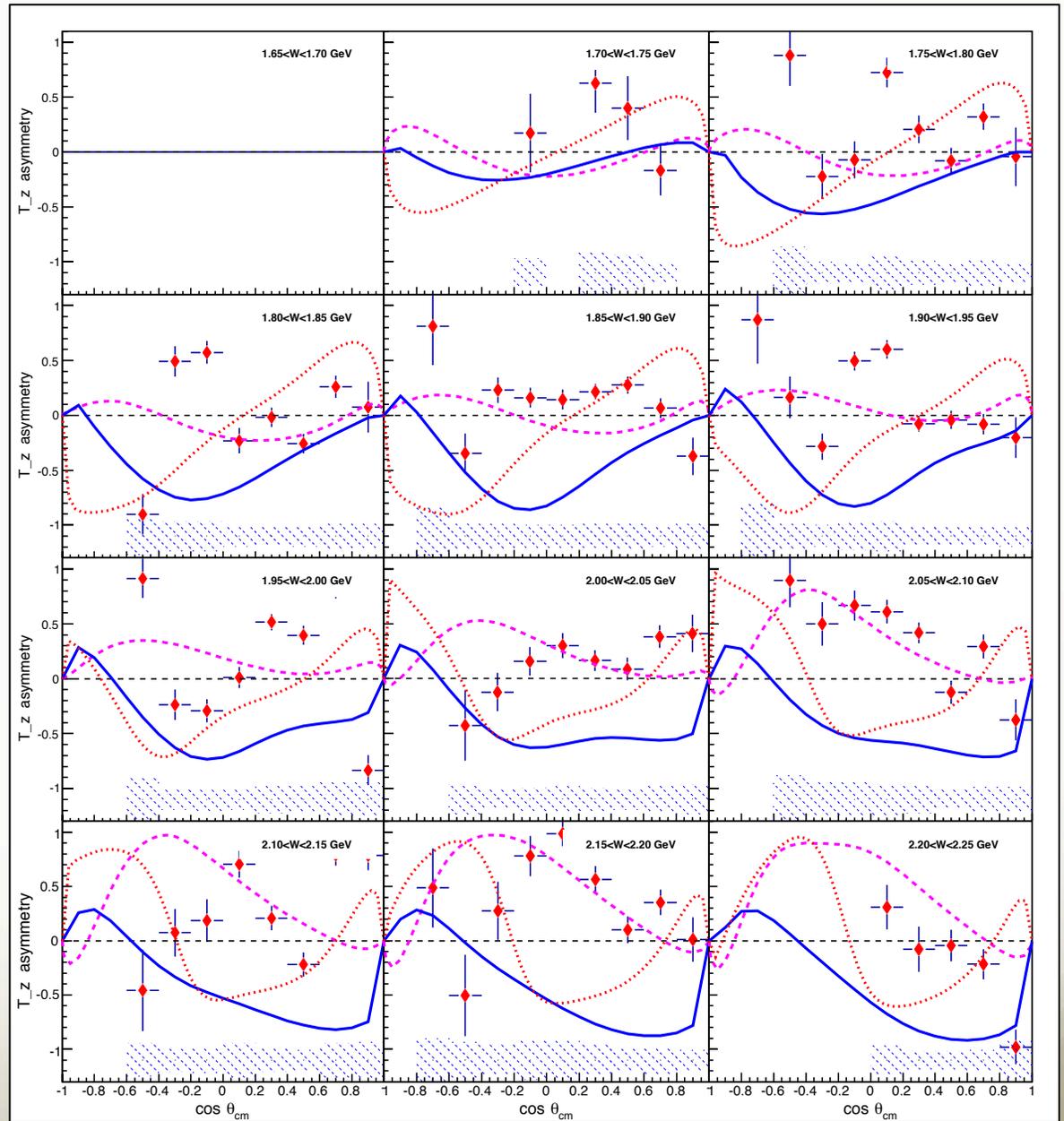




T_z for
 $K^+ \Lambda$

Data:
CLAS g9b

Models:
RPR-Ghent
Kaon-MAID
BOGA

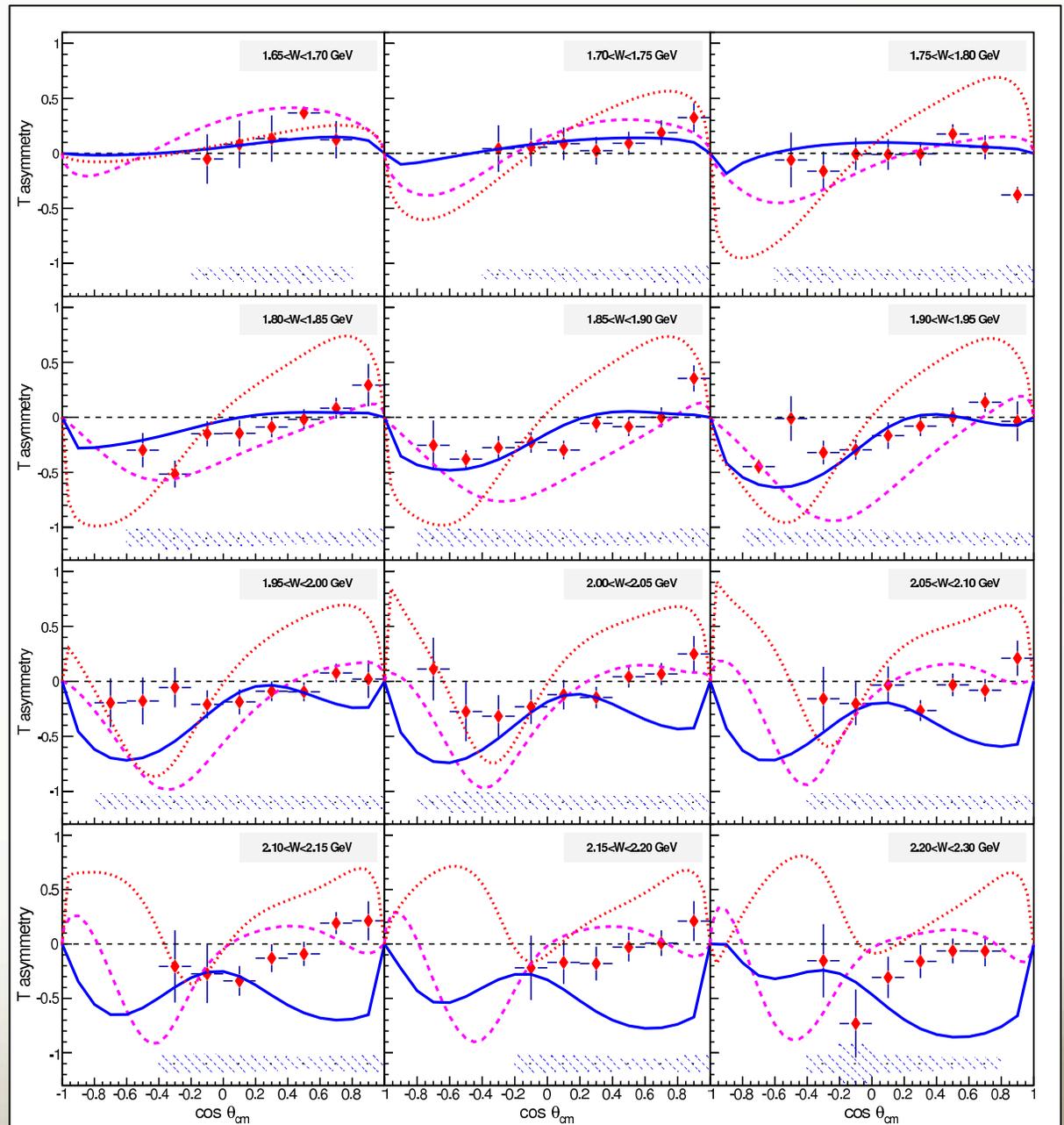




F for $K^+ \Lambda$

Data:
CLAS g9b

Models:
RPR-Ghent
Kaon-MAID
BOGA

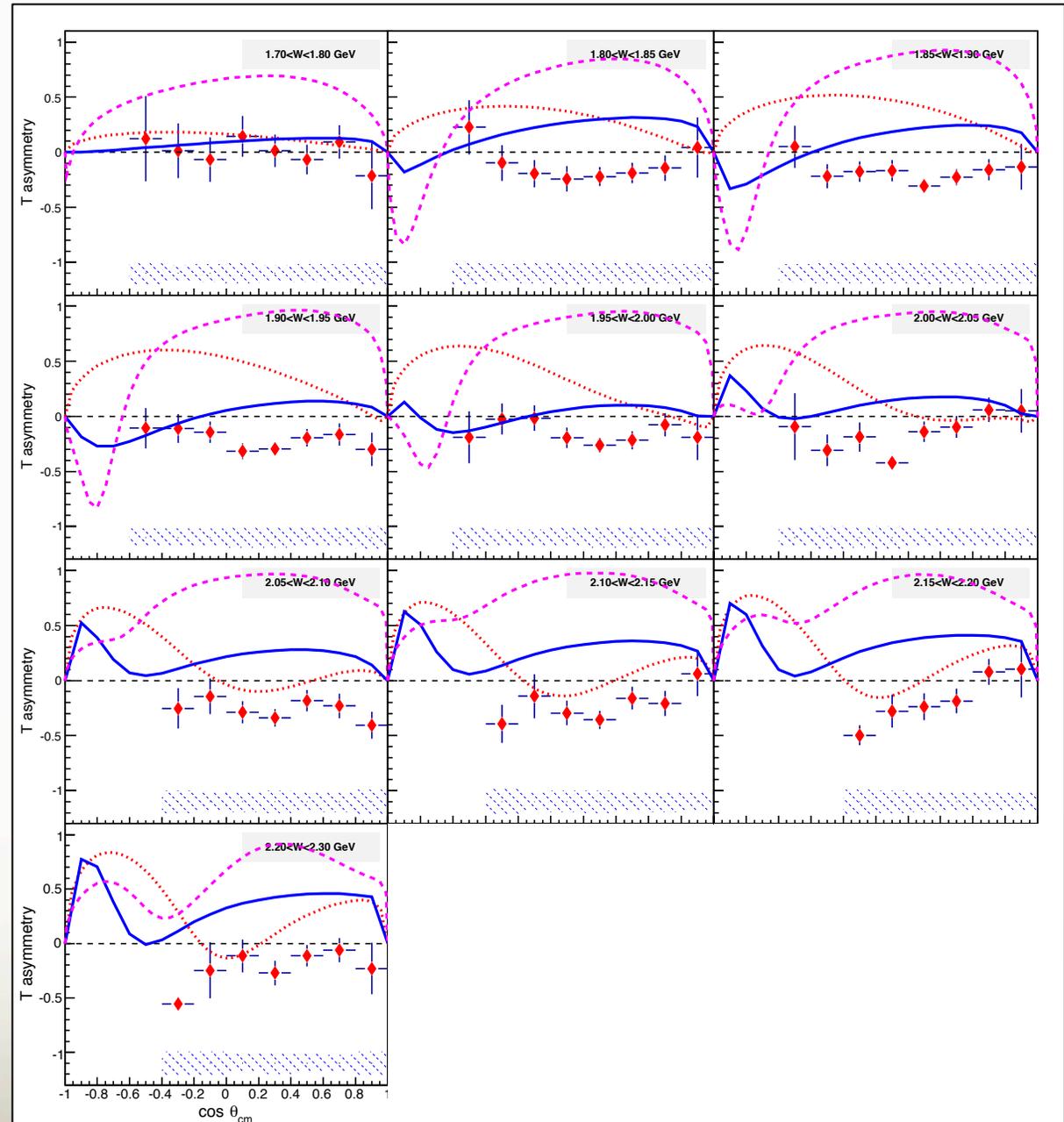




F for $K^+ \Sigma^0$

Data:
CLAS g9b

Models:
RPR-Ghent
Kaon-MAID
BOGA





Conclusion

- More kaon photoproduction data necessary to help solve missing resonance problem
- First results for many of the observables for kaon photoproduction
- Working on publishing results...slowly...
- Models and PWA results only partially consistent with data: can expect that resonance parameters will greatly improve with this data