

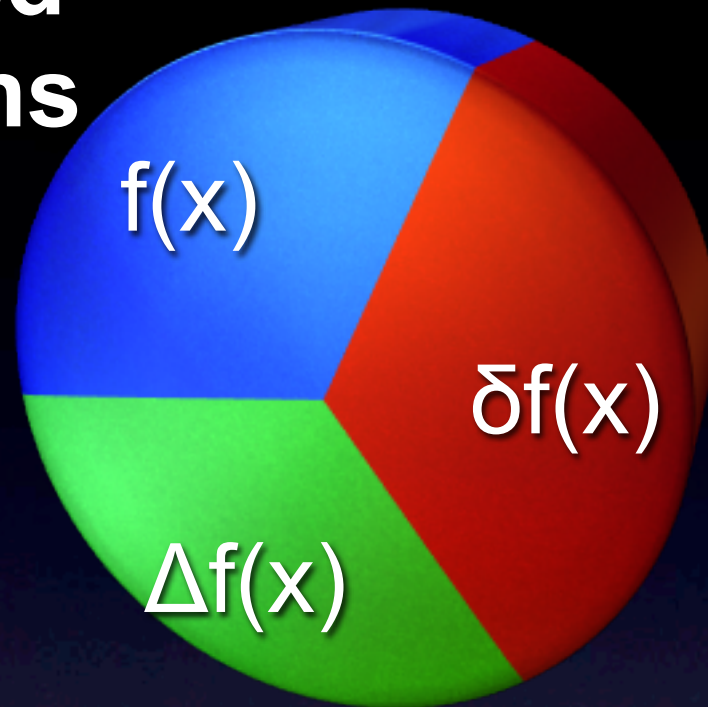
# Measurements of the Nucleon Spin-Structure Functions in and Above the Resonance Region for the Hall-B EG1 Experiment at Jefferson Laboratory

Robert Fersch  
Christopher Newport University  
Jefferson Laboratory (CLAS Collaboration)

# Structure of the Nucleon

Unpolarized  
distributions  
 $q, g$

Helicity  
 $\Delta q, \Delta g$



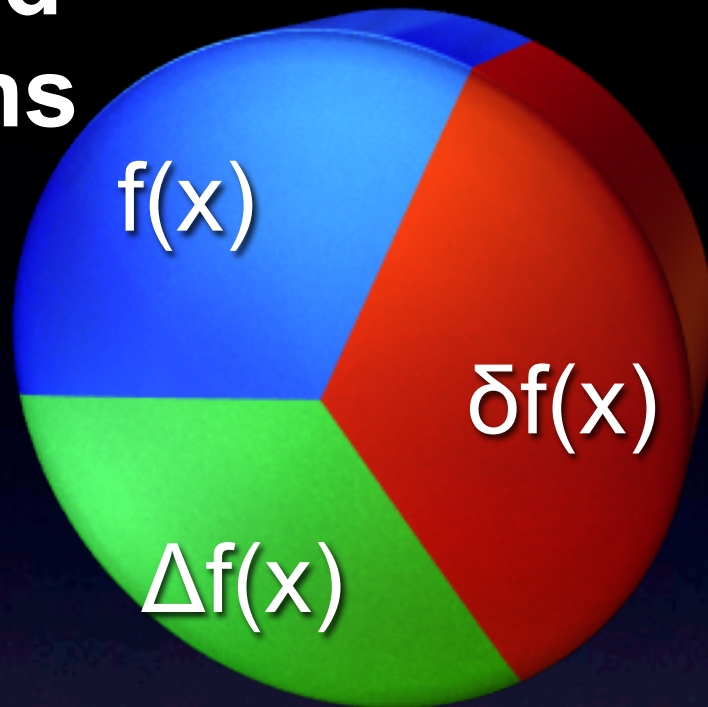
Transversity  $\delta q$

3 d.o.f. completely  
describe the nucleon at  
leading twist when  $k_T = 0$

# Structure of the Nucleon

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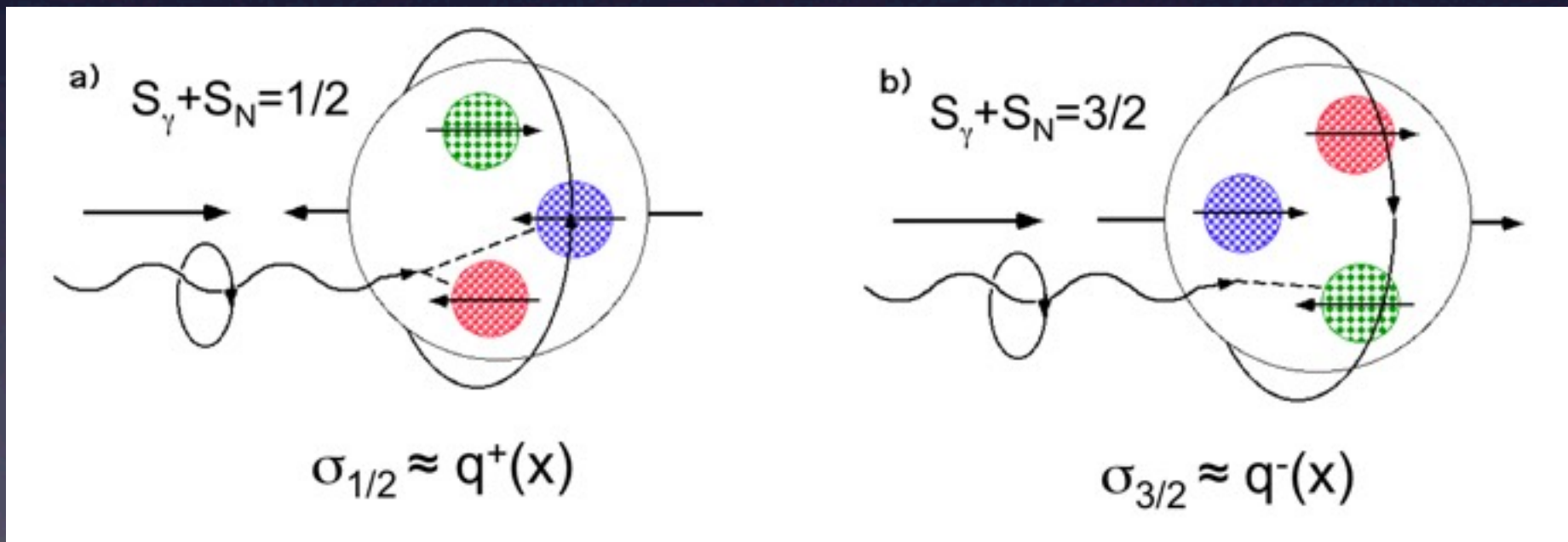


Transversity  $\delta q$

3 d.o.f. completely  
describe the nucleon at  
leading twist when  $k_T = 0$

**Helicity:**  
 $\Delta q = q^+ - q^-$

Incident electron  
couples to quarks  
of opposite  
longitudinal spin



Structure function  $g_1(x, Q^2) \sim \sigma_{1/2} - \sigma_{3/2}$

Requires longitudinally polarized beam *and* target

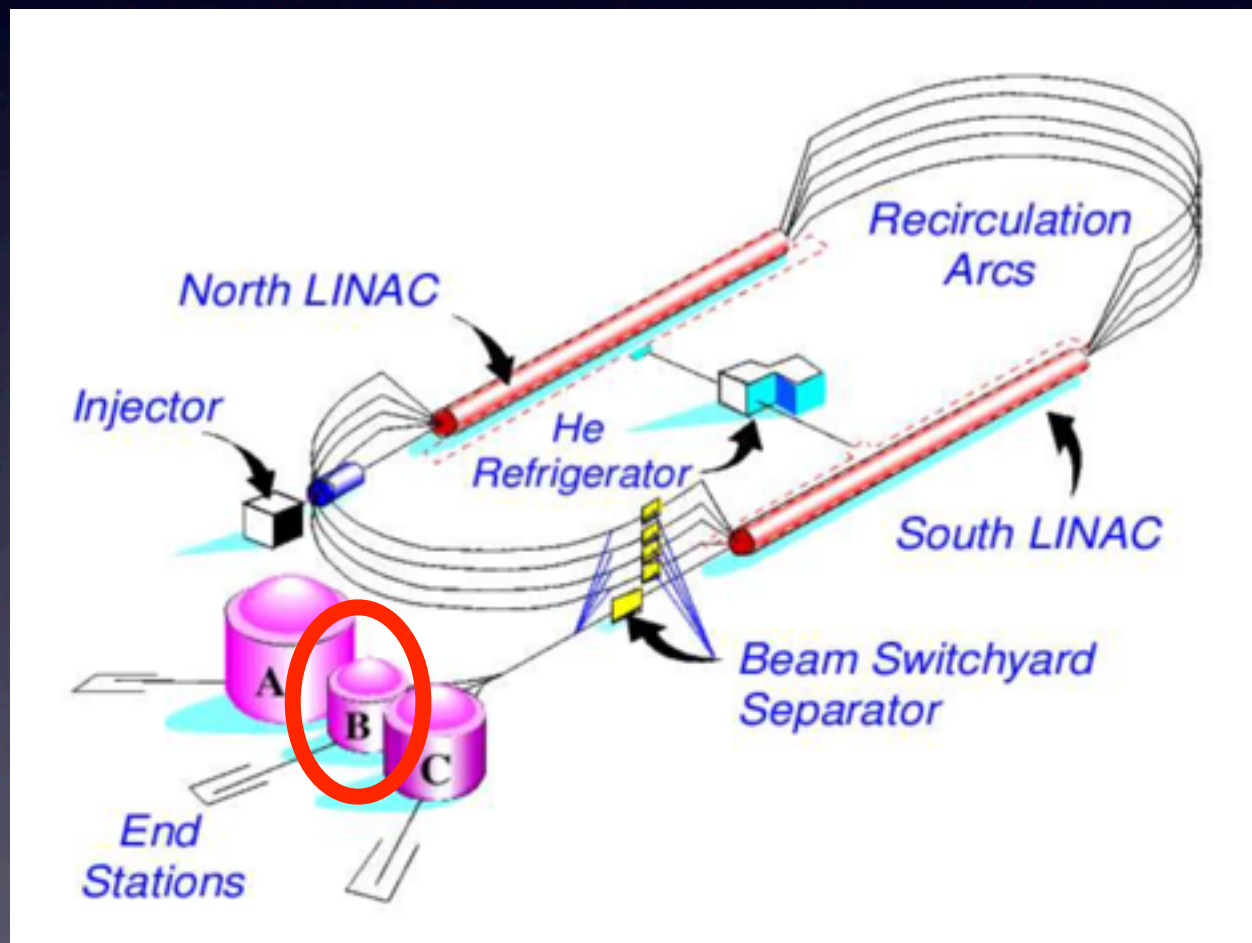


# The EG1 experiment

ran in CLAS for 7 months 2000-2001

4 beam energies used (1.6, 2.5, 4.2, 5.7 GeV)

## CEBAF Large Acceptance Spectrometer (Hall-B) at Jefferson Lab



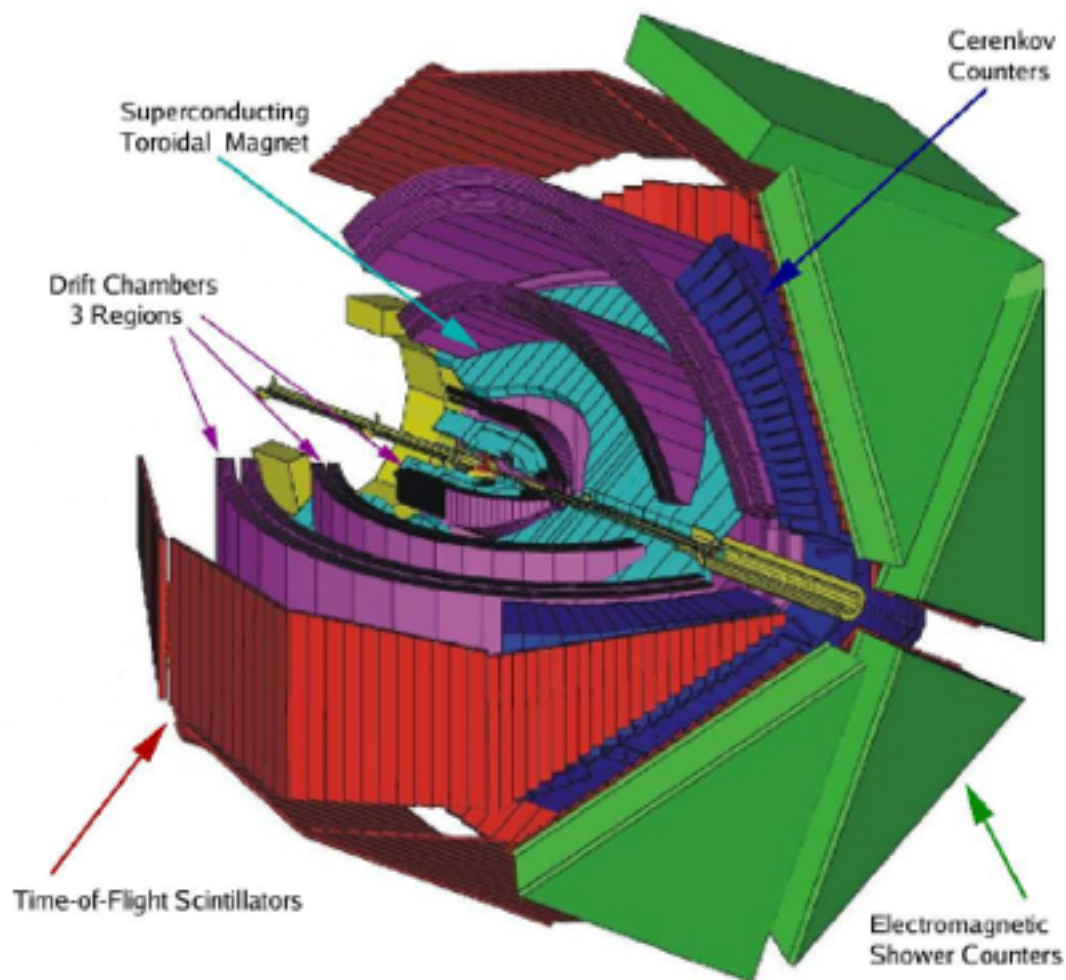
(~70%) polarized electron beam in energies up to 6 GeV

# The EG1 experiment

ran in CLAS for 7 months 2000-2001

4 beam energies used (1.6, 2.5, 4.2, 5.7 GeV)

## CEBAF Large Acceptance Spectrometer (Hall-B) at Jefferson Lab



Drift Chambers (momentum reconstruction)

Scintillation Counters (time-of-flight, PID)

Cherenkov Counters and Electromagnetic Calorimeters (separation of electrons from light hadrons)



# The EG1 experiment

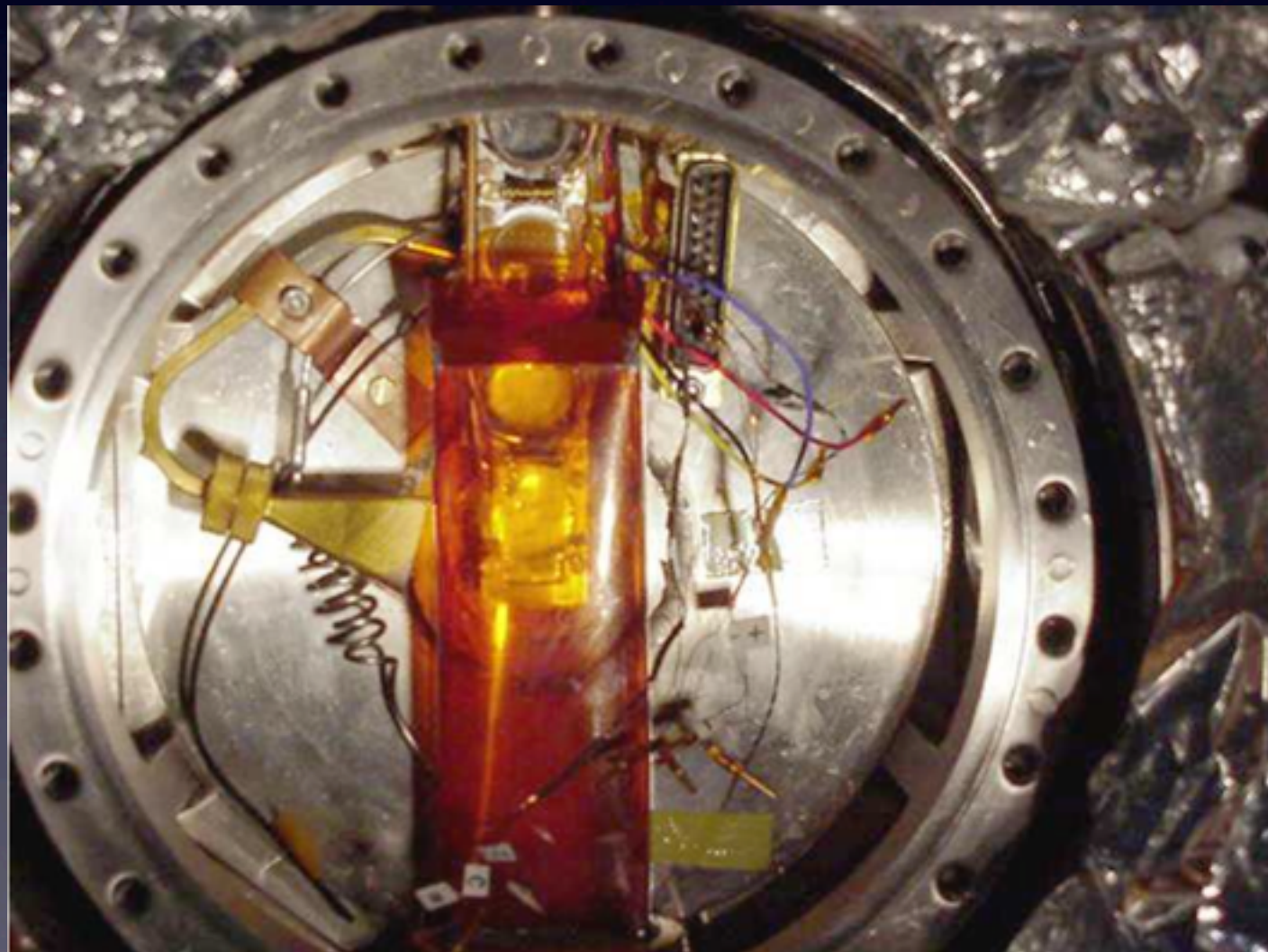
ran in CLAS for 7 months 2000-2001

4 beam energies used (1.6, 2.5, 4.2, 5.7 GeV)

## CLAS Longitudinally Polarized Target

- $^{15}\text{NH}_3$  and  $^{15}\text{ND}_3$  target cells
- Typical polarizations of 75% (H) and 30% (D)
- $^{12}\text{C}$  and LHe target cells for unpolarized background subtraction

ammonia  
target  
cell

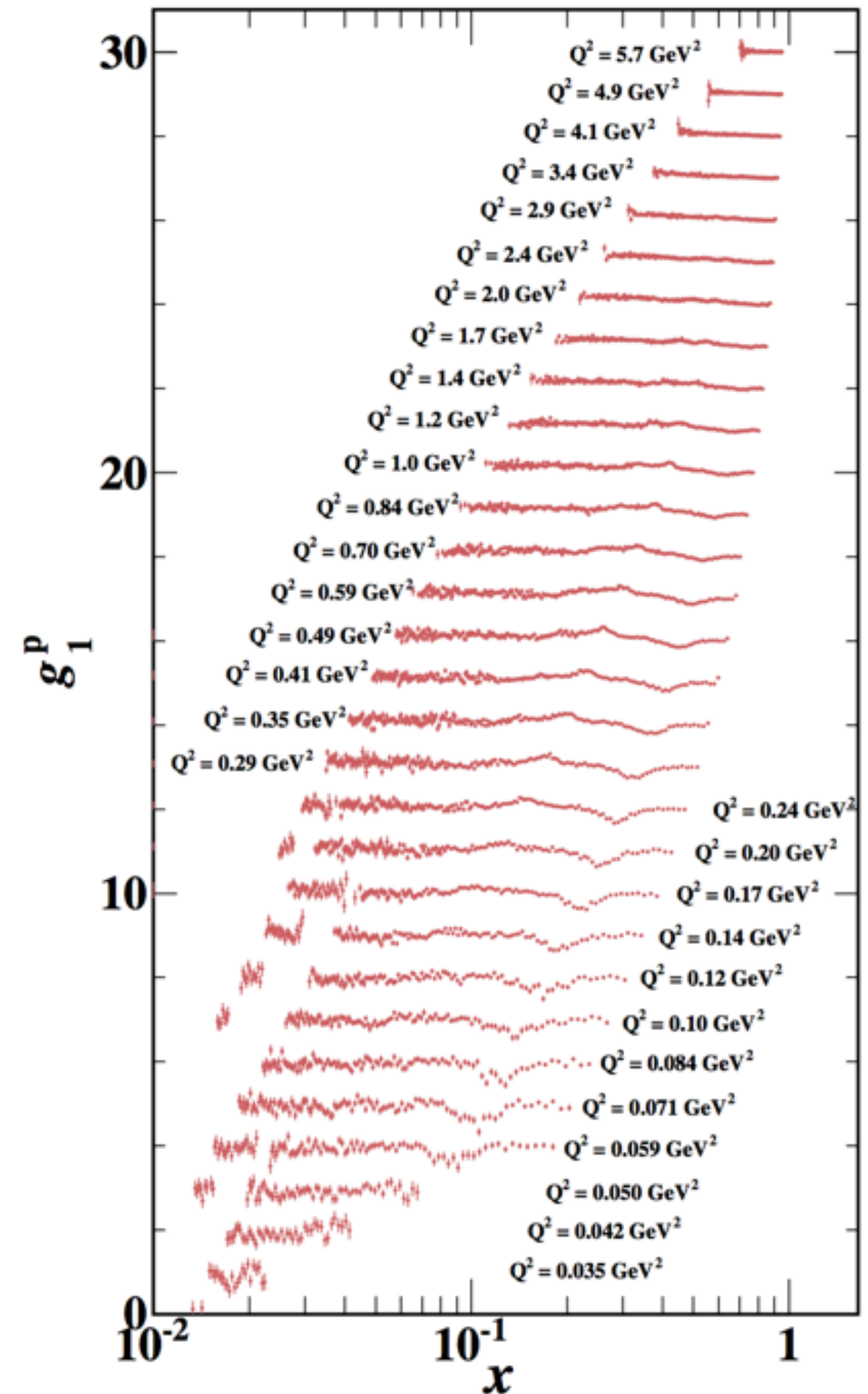
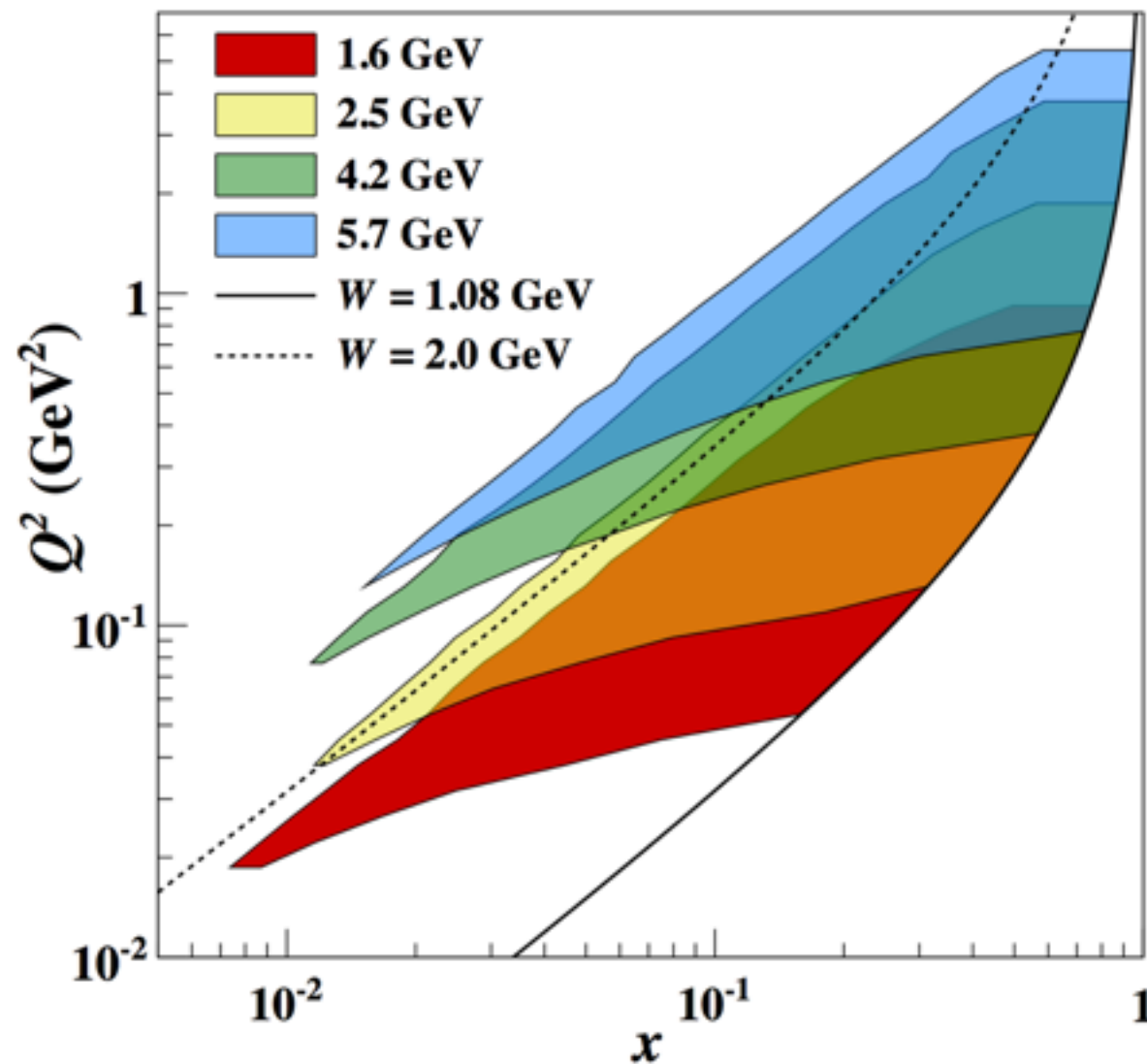


# The EG1 experiment

ran in CLAS for 7 months 2000-2001

4 beam energies used  
(1.6, 2.5, 4.2, 5.7 GeV)

## Kinematic coverage & statistics





# Many papers already published using EG1 data (including a study of Bloom-Gilman duality):

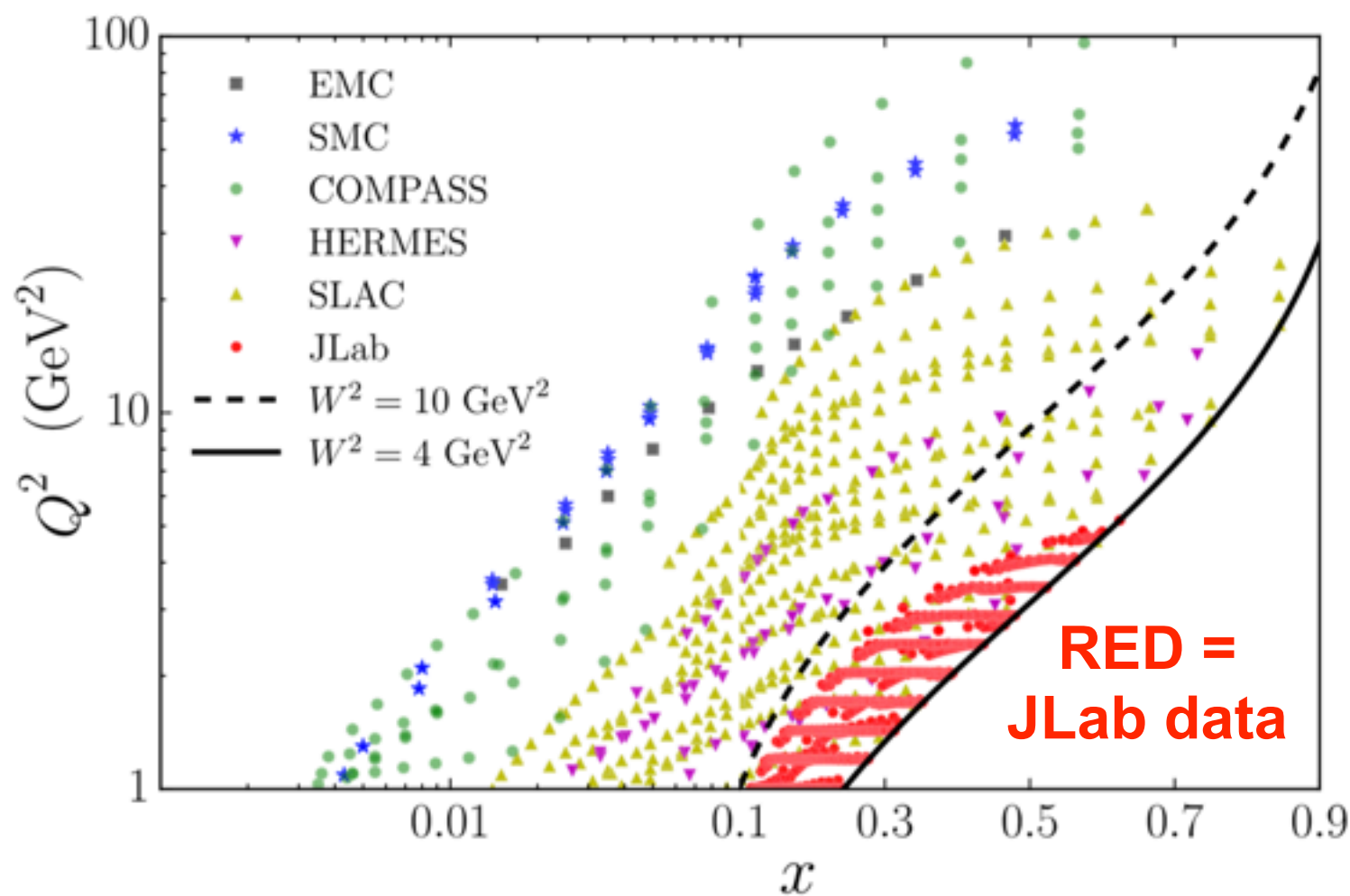
- N. Guler *et al.* (CLAS Collaboration), "Precise Determination of the Deuteron Spin Structure at Low to Moderate  $Q^2$  with CLAS and Extraction of the Neutron Contribution", Phys. Rev. C 92, 055201 (2015).
- P. Bosted *et al.* (CLAS Collaboration), "Target and Beam-Target Spin Asymmetries in Exclusive  $\pi^+$  and  $\pi^-$  electroproduction with 1.6- to 5.7-GeV electrons", Phys. Rev. C 94, 055201 (2016)
- H. Avakian *et al.* (CLAS Collaboration), "Measurement of Single and Double Spin Asymmetries in Deep Inelastic Pion Electroproduction with a Longitudinally Polarized Target", Phys. Rev. Lett. 105, 262002 (2010).
- Y. Prok *et al.* (CLAS Collaboration), "Moments of the Spin Structure Functions  $g_1^p$  and  $g_1^d$  for  $0.05 < Q^2 < 3.0 \text{ GeV}^2$ ", Phys. Lett. B 672, 12 (2009).
- A. Biselli *et al.* (CLAS Collaboration), "First Measurement of Target and Double Spin Asymmetries for  $ep \rightarrow e'p\pi^0$  in the Nucleon Resonance Region Above the  $\Delta(1232)$ ", Phys. Rev. C 78, 045204 (2008).
- P.E. Bosted *et al.* (CLAS Collaboration), "Ratios of  $^{15}\text{N}/^{12}\text{C}$  and  $^4\text{He}/^{12}\text{C}$  Inclusive Electroproduction Cross Sections in the Nucleon Resonance Region", Phys. Rev. C 78, 015202 (2008).
- P.E. Bosted *et al.* (CLAS Collaboration), "Quark-Hadron Duality in Spin Structure Functions  $g_1^p$  and  $g_1^d$ ", Phys. Rev. C 75, 035203 (2007).
- K.V. Dharmawardane *et al.* (CLAS Collaboration), "Measurement of the  $x$  and  $Q^2$  Dependence of the Spin Asymmetry  $A_1$  of the Nucleon", Phys. Lett. B. 641, 28 (2006).
- S. Chen *et al.* (CLAS Collaboration), "Measurement of Deeply Virtual Compton Scattering with a Polarized Proton Target", Phys. Rev. Lett. 97, 072002 (2006).
- A. Biselli *et al.* (CLAS Collaboration), "Study of  $ep \rightarrow e'p\pi^0$  in the  $\Delta(1232)$  Mass Region Using Polarization Asymmetries", Phys. Rev. C 68, 035202 (2003).
- R. Fatemi *et al.* (CLAS Collaboration), "Measurement of the Spin Structure Functions in the Resonance Region for  $Q^2$  from 0.15 to 1.6  $\text{GeV}^2$ ", Phys. Rev. Lett. 91, 222002 (2003).
- J. Yun *et al.* (CLAS Collaboration), "Measurement of Inclusive Spin Structure Functions of the Deuteron with CLAS", Phys. Rev. C 67, 055204 (2003).
- R. DeVita *et al.* (CLAS Collaboration), "First Measurement of the Double Spin Asymmetry in  $ep \rightarrow e'\pi^+n$  in the Resonance Region", Phys. Rev. Lett. 88, 082001 (2002).



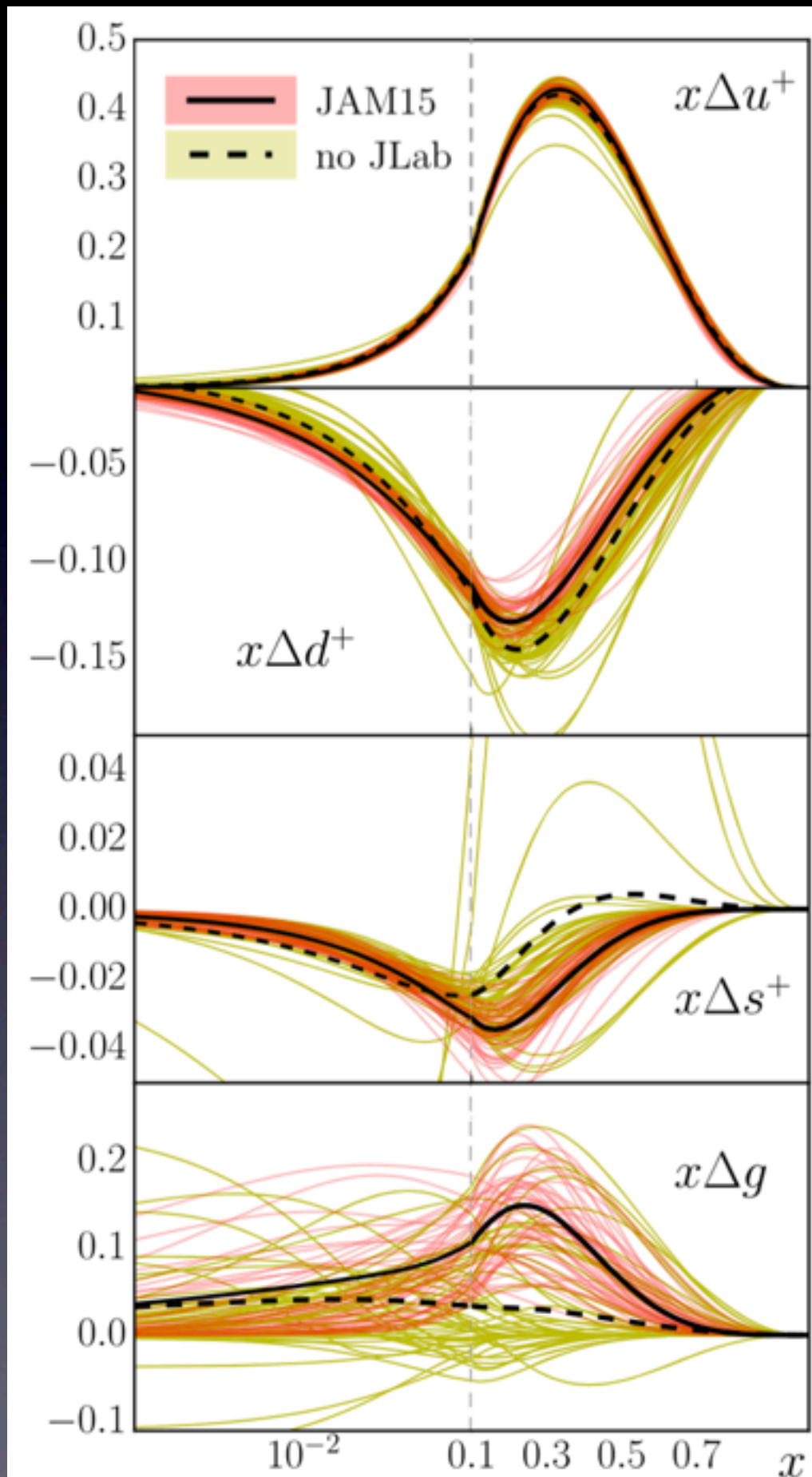
# Impact of JLab / EG1 data on polarized PDFs

**Global analysis by JAM (JLab  
Angular Momentum group)  
Theory group (W. Meltinchouk *et al.*)**

**Phys Rev D 93, 074005 (2016)**



# spin distributions within the nucleon





# Final proton “long paper” is now available pending publication in Phys. Rev. C

arXiv:1706.10289

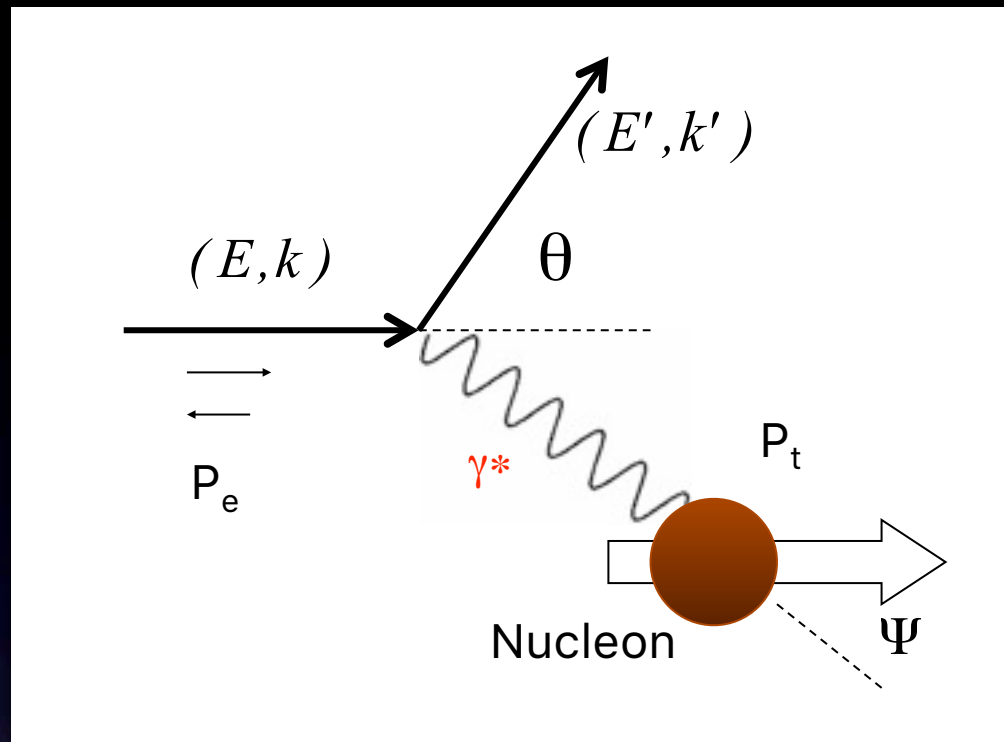
## Determination of the Proton Spin Structure Functions for $0.05 < Q^2 < 5 \text{ GeV}^2$ using CLAS

R.G. Fersch,<sup>7</sup> N. Guler,<sup>29</sup> P. Bosted,<sup>36</sup> A. Deur,<sup>36</sup> K. Griffioen,<sup>42</sup> C. Keith,<sup>36</sup> S.E. Kuhn,<sup>29</sup> R. Minehart,<sup>41</sup> Y. Prok,<sup>29</sup>  
K.P. Adhikari,<sup>25</sup> Z. Akbar,<sup>12</sup> M.J. Amarian,<sup>29</sup> S. Anefalos Pereira,<sup>17</sup> G. Asryan,<sup>43</sup> H. Avakian,<sup>36,17</sup> J. Ball,<sup>6</sup>  
I. Balossino,<sup>16</sup> N.A. Baltzell,<sup>36</sup> M. Battaglieri,<sup>18</sup> I. Bedlinskiy,<sup>22</sup> A.S. Biselli,<sup>9,4</sup> W.J. Briscoe,<sup>14</sup> W.K. Brooks,<sup>37,36</sup>  
S. Bültmann,<sup>29</sup> V.D. Burkert,<sup>36</sup> Frank Thanh Cao,<sup>8</sup> D.S. Carman,<sup>36</sup> A. Celentano,<sup>18</sup> S. Chandavar,<sup>28</sup> G. Charles,<sup>29</sup> T.  
Chetry,<sup>28</sup> G. Ciullo,<sup>16,10</sup> L. Clark,<sup>39</sup> L. Colaneri,<sup>8</sup> P.L. Cole,<sup>15,36</sup> N. Compton,<sup>28</sup> M. Contalbrigo,<sup>16</sup> O. Cortes,<sup>15</sup>  
V. Crede,<sup>12</sup> A. D'Angelo,<sup>19,32</sup> N. Dashyan,<sup>43</sup> R. De Vita,<sup>18</sup> E. De Sanctis,<sup>17</sup> C. Djalali,<sup>34</sup> G.E. Dodge,<sup>29</sup> R. Dupre,<sup>21</sup>  
H. Egiyan,<sup>36,42</sup> A. El Alaoui,<sup>37</sup> L. El Fassi,<sup>25</sup> L. Elouadrhiri,<sup>36</sup> P. Eugenio,<sup>12</sup> E. Fanchini,<sup>18</sup> G. Fedotov,<sup>34,33</sup> A. Filippi,<sup>20</sup>  
J.A. Fleming,<sup>38</sup> T.A. Forest,<sup>15</sup> M. Garçon,<sup>6</sup> G. Gavalian,<sup>36,26</sup> Y. Ghandilyan,<sup>43</sup> G.P. Gilfoyle,<sup>31</sup> K.L. Giovanetti,<sup>23</sup>  
F.X. Girod,<sup>36,6</sup> C. Gleason,<sup>34</sup> E. Golovatch,<sup>33</sup> R.W. Gothe,<sup>34</sup> M. Guidal,<sup>21</sup> L. Guo,<sup>11,36</sup> K. Hafidi,<sup>1</sup> H. Hakobyan,<sup>37,43</sup>  
C. Hanretty,<sup>36</sup> N. Harrison,<sup>36</sup> D. Heddle,<sup>7,36</sup> K. Hicks,<sup>28</sup> M. Holtrop,<sup>26</sup> S.M. Hughes,<sup>38</sup> Y. Ilieva,<sup>34,14</sup> D.G. Ireland,<sup>39</sup>  
B.S. Ishkhanov,<sup>33</sup> E.L. Isupov,<sup>33</sup> D. Jenkins,<sup>40</sup> D. Keller,<sup>41</sup> G. Khachatryan,<sup>43</sup> M. Khachatryan,<sup>29</sup> M. Khandaker,<sup>27,\*</sup>  
A. Kim,<sup>8</sup> W. Kim,<sup>24</sup> A. Klein,<sup>29</sup> F.J. Klein,<sup>5</sup> V. Kubarovsky,<sup>36,30</sup> V.G. Lagerquist,<sup>29</sup> L. Lanza,<sup>19</sup> P. Lenisa,<sup>16</sup>  
K. Livingston,<sup>39</sup> H.Y. Lu,<sup>34</sup> B. McKinnon,<sup>39</sup> C.A. Meyer,<sup>4</sup> M. Mirazita,<sup>17</sup> V. Mokeev,<sup>36,33</sup> R.A. Montgomery,<sup>39</sup>  
A. Movsisyan,<sup>16</sup> C. Munoz Camacho,<sup>21</sup> G. Murdoch,<sup>39</sup> P. Nadel-Turonski,<sup>36</sup> S. Niccolai,<sup>21</sup> G. Niculescu,<sup>23</sup>  
I. Niculescu,<sup>23</sup> M. Osipenko,<sup>18</sup> A.I. Ostrovidov,<sup>12</sup> M. Paolone,<sup>35</sup> R. Paremuzyan,<sup>26</sup> K. Park,<sup>36,24</sup> E. Pasyuk,<sup>36,2</sup>  
W. Phelps,<sup>11</sup> S. Pisano,<sup>17</sup> O. Pogorelko,<sup>22</sup> J.W. Price,<sup>3</sup> D. Protopopescu,<sup>26,†</sup> B.A. Raue,<sup>11,36</sup> M. Ripani,<sup>18</sup> D.  
Riser,<sup>8</sup> A. Rizzo,<sup>19,32</sup> G. Rosner,<sup>39</sup> P. Rossi,<sup>36,17</sup> P. Roy,<sup>12</sup> F. Sabatié,<sup>6</sup> C. Salgado,<sup>27</sup> R.A. Schumacher,<sup>4</sup>  
Y.G. Sharabian,<sup>36</sup> A. Simonyan,<sup>43</sup> Iu. Skorodumina,<sup>34,33</sup> G.D. Smith,<sup>38</sup> D. Sokhan,<sup>39</sup> N. Sparveris,<sup>35</sup> I. Stankovic,<sup>38</sup>  
S. Stepanyan,<sup>36</sup> I.I. Strakovsky,<sup>14</sup> S. Strauch,<sup>34</sup> M. Taiuti,<sup>13,‡</sup> Ye Tian,<sup>34</sup> B. Torayev,<sup>29</sup> M. Ungaro,<sup>36,30</sup>  
H. Voskanyan,<sup>43</sup> E. Voutier,<sup>21</sup> N.K. Walford,<sup>5</sup> X. Wei,<sup>36</sup> L.B. Weinstein,<sup>29</sup> N. Zachariou,<sup>38</sup> and J. Zhang<sup>36,29</sup>

(The CLAS Collaboration)



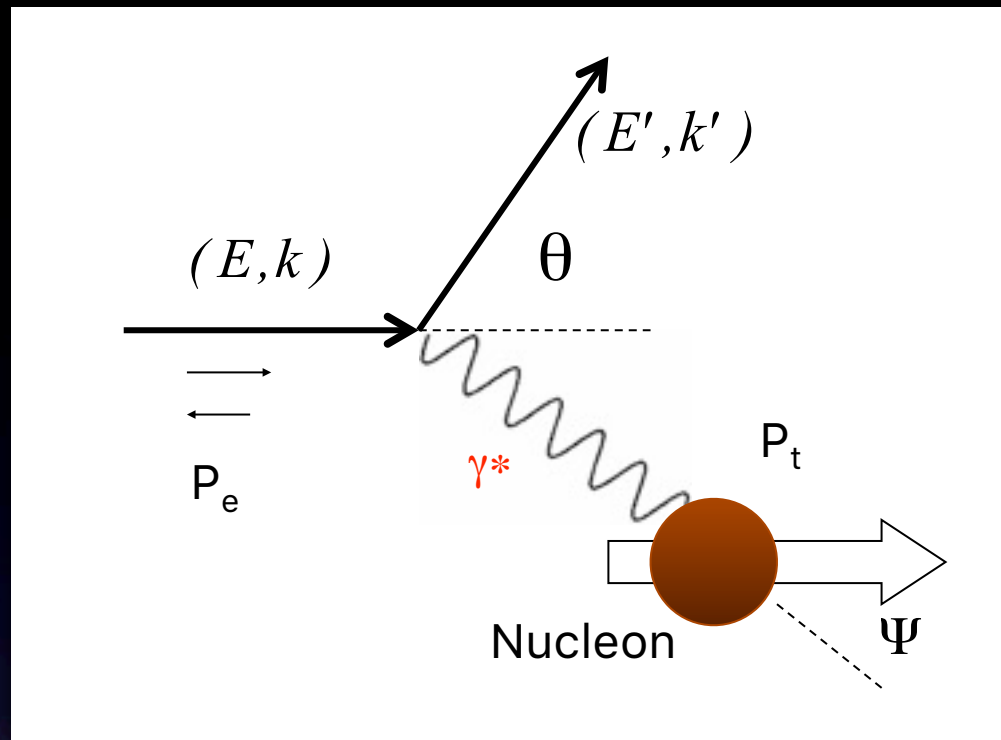
# Analysis of Polarized Inclusive $ep$ scattering



Double spin asymmetry  
between  $+$  ( $\uparrow\uparrow, \downarrow\downarrow$ ) and  $-$  ( $\uparrow\downarrow, \downarrow\uparrow$ )  
beam and target polarizations

$$A_{\parallel} = \frac{1}{P_b P_t F_{DF}} \frac{n^+ - n^-}{n^+ + n^-}$$

# Analysis of Polarized Inclusive ep scattering

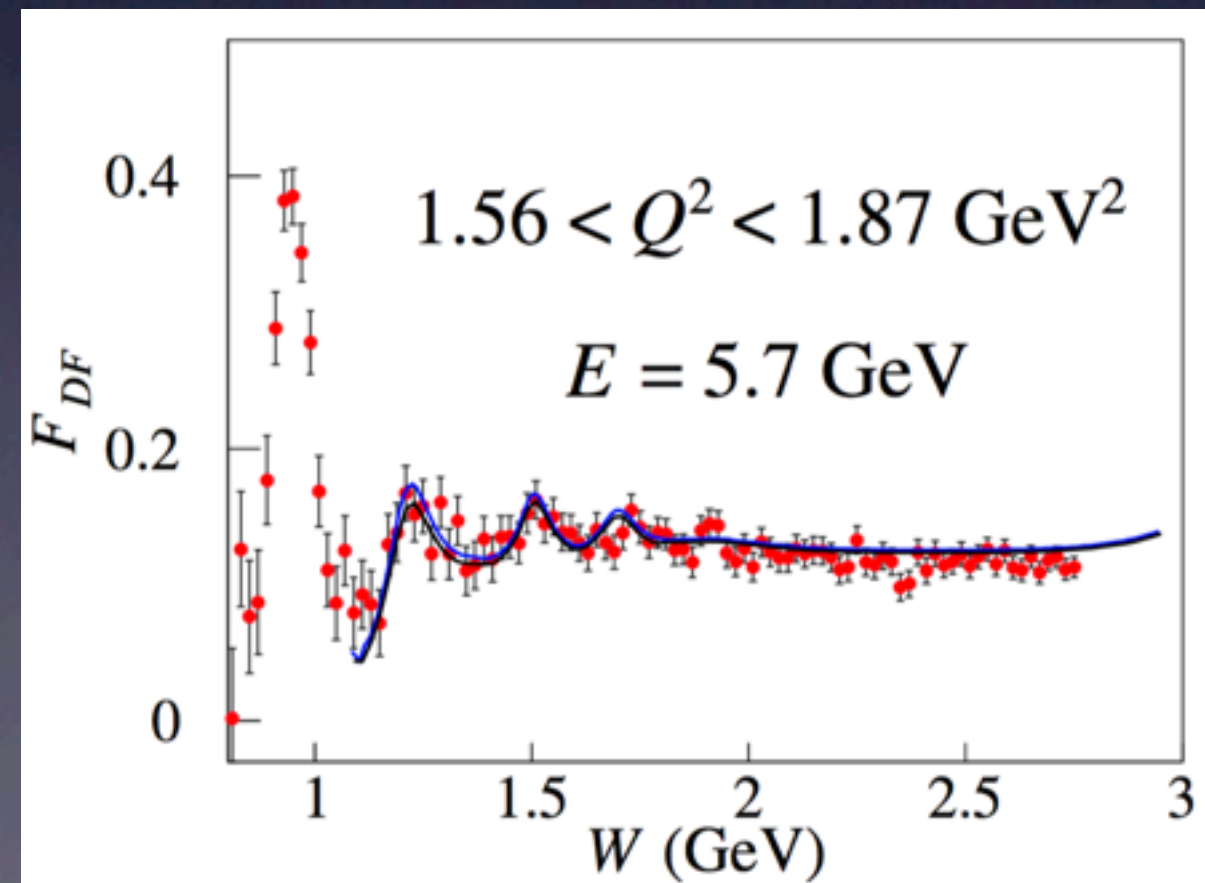
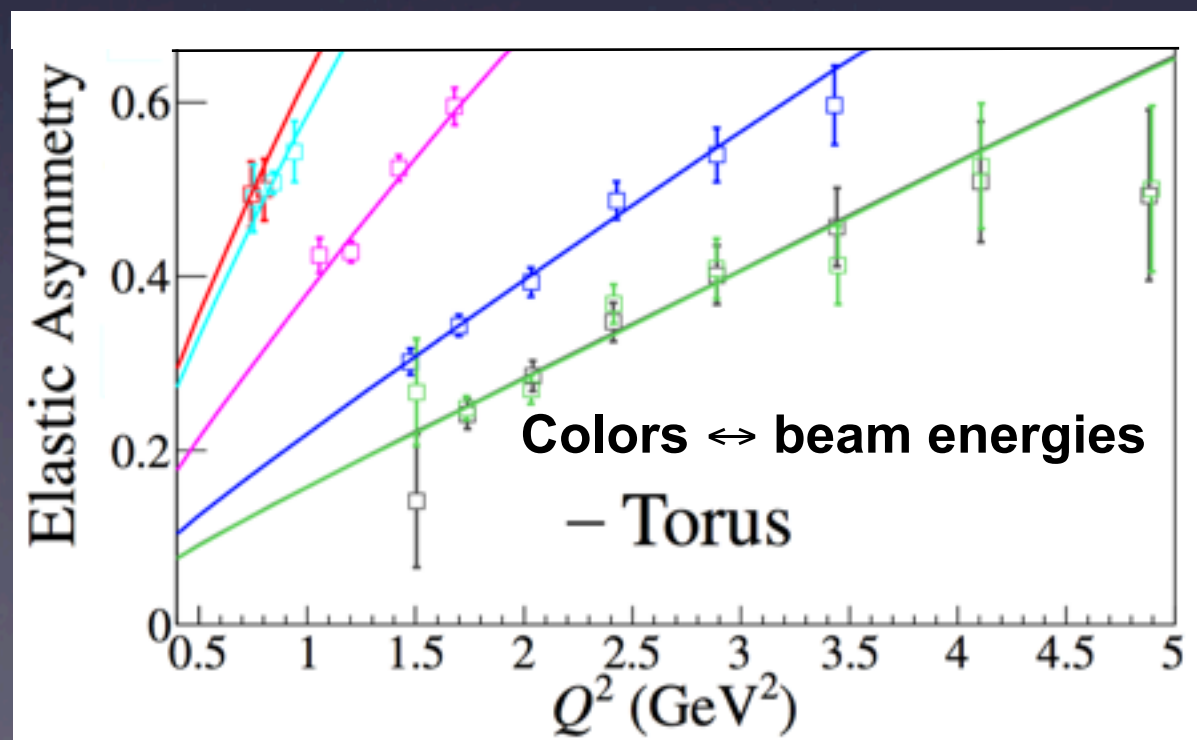


Double spin asymmetry  
between + ( $\uparrow\uparrow, \downarrow\downarrow$ ) and - ( $\uparrow\downarrow, \downarrow\uparrow$ )  
beam and target polarizations

$$A_{\parallel} = \frac{1}{P_b P_t F_{DF}} \frac{n^+ - n^-}{n^+ + n^-}$$

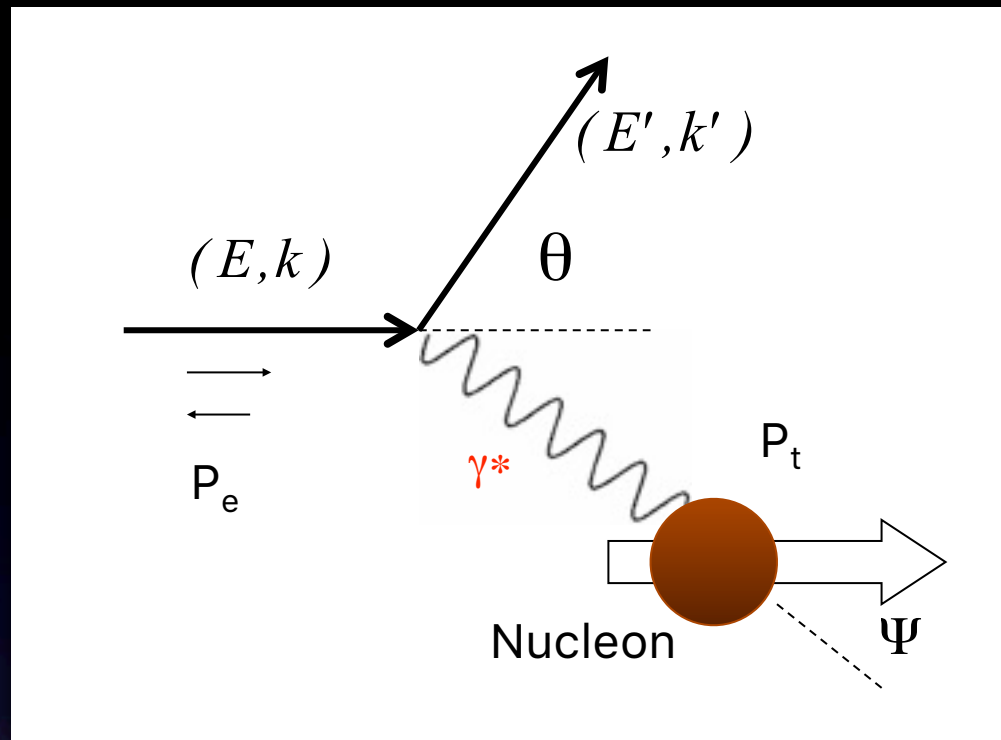
Polarization product from elastic  
asymmetry normalization to global data  
(polarized background)

Dilution factor from  $^{12}\text{C}$ , LHe  
runs and radiated cross section  
model (unpolarized background)





# Analysis of Polarized Inclusive ep scattering



Double spin asymmetry  
between + ( $\uparrow\uparrow, \downarrow\downarrow$ ) and - ( $\uparrow\downarrow, \downarrow\uparrow$ )  
beam and target polarizations

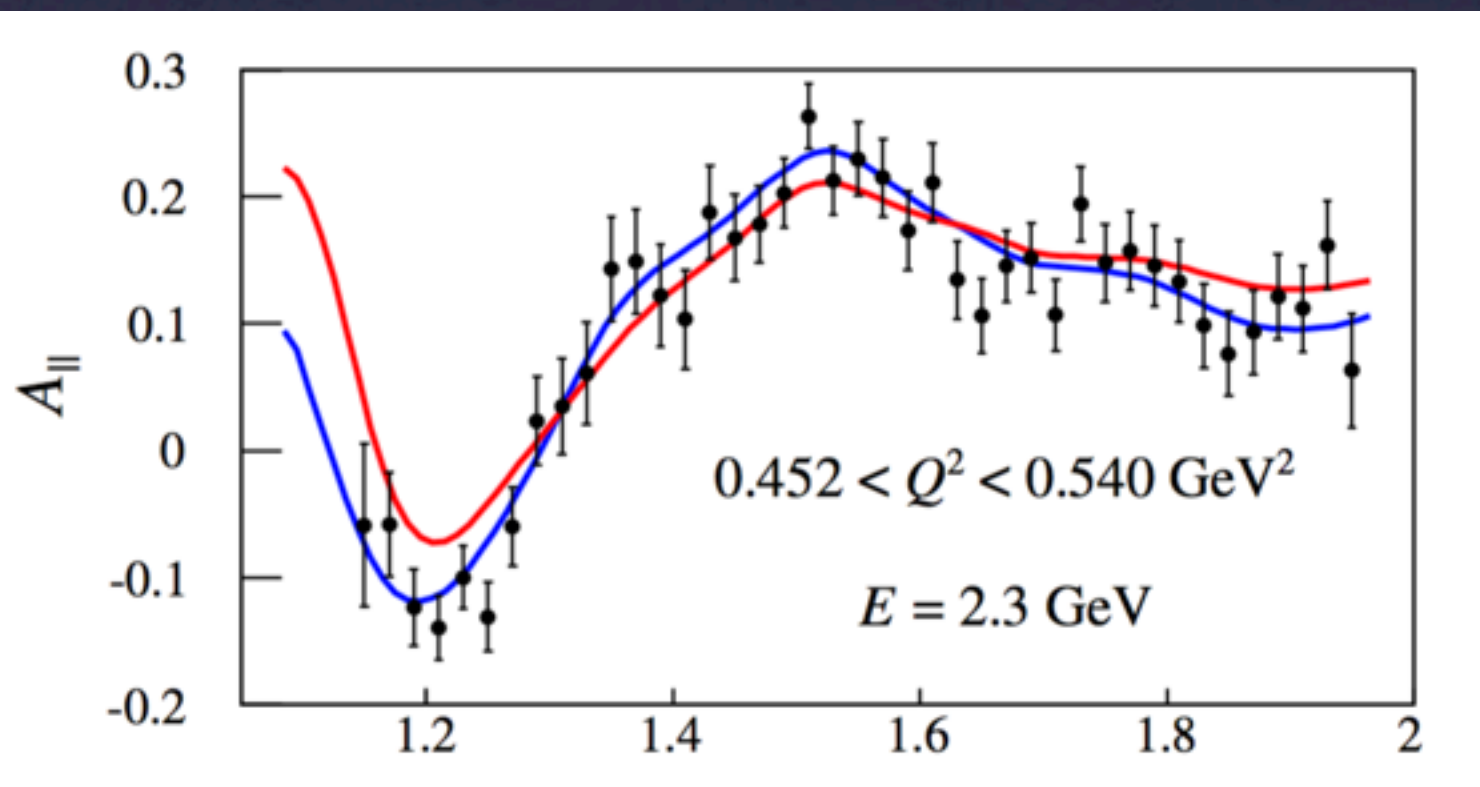
$$A_{||} = \frac{1}{P_b P_t F_{DF}} \frac{n^+ - n^-}{n^+ + n^-}$$

## Physics quantities

virtual photon asymmetries  $A_1$  and  $A_2$

$$A_{||}(\nu, Q^2) = D[A_1(\nu, Q^2) + \eta A_2(\nu, Q^2)]$$

**Radiative corrections** (difference between red, blue lines)  
(also nuclear polarization and  $e^+e^-$  corrections)



spin structure functions  $g_1$  and  $g_2$

$$\frac{A_{||}}{D} = (1 + \eta\gamma) \frac{g_1}{F_1} + \gamma(\eta - \gamma) \frac{g_2}{F_1}$$

(kinematics/models)

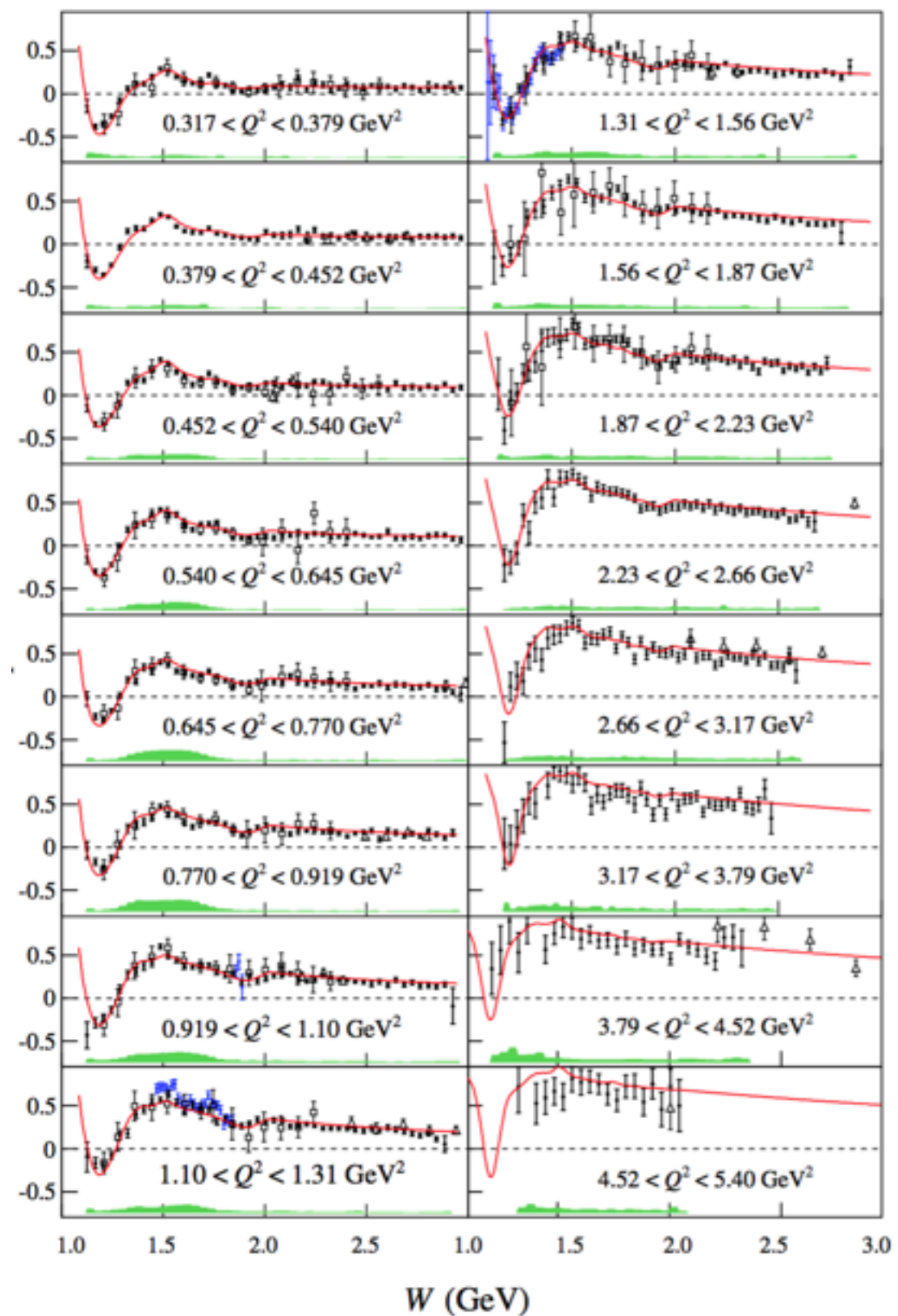
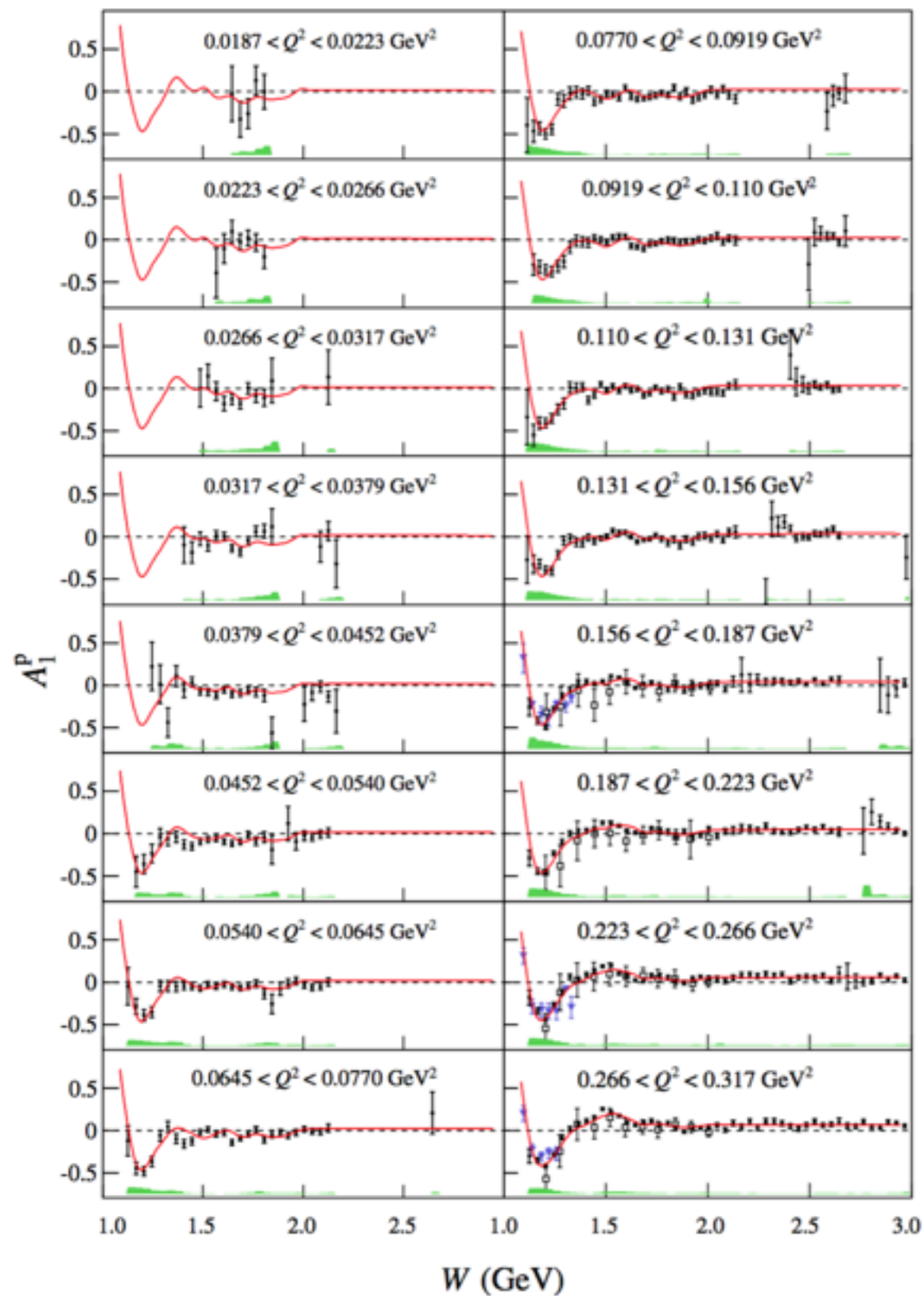
$$D = \frac{1 - E'\epsilon/E}{1 + \epsilon R}; \quad \eta = \frac{\epsilon \sqrt{Q^2}}{E - E'\epsilon} \quad R = \frac{\sigma_L}{\sigma_T}$$

$$\gamma = \frac{2Mx}{\sqrt{Q^2}}$$

$$A_{||}(\nu, Q^2) = D[A_1(\nu, Q^2) + \eta A_2(\nu, Q^2)]$$

**$A_1$  for the proton shown against world data**

**Note coverage in resonance region over wide  $Q^2$**

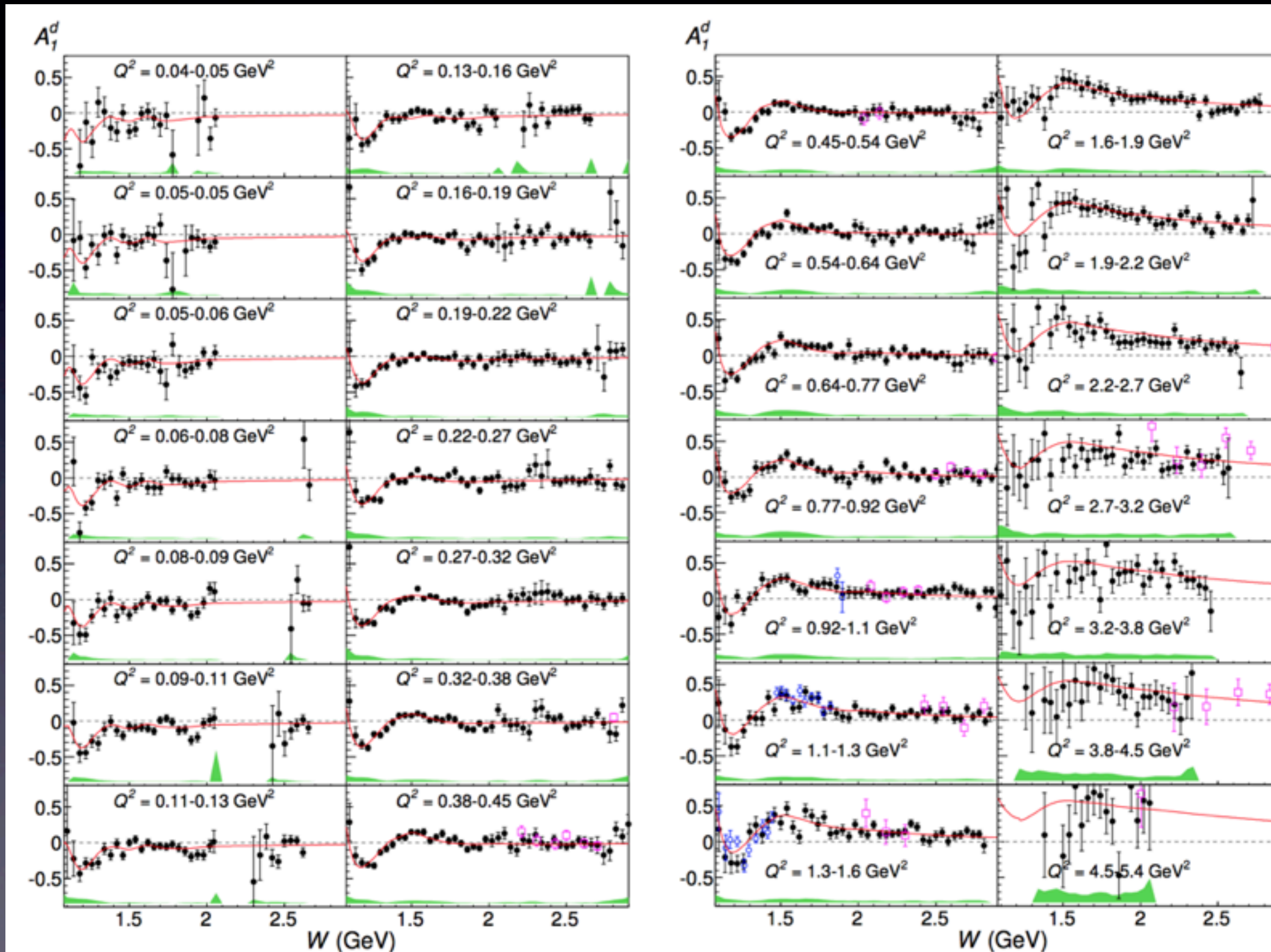




$$A_{||}(\nu, Q^2) = D[A_1(\nu, Q^2) + \eta A_2(\nu, Q^2)]$$

**$A_1$  for the deuteron shown against world data**

**Coverage comparable to that of proton**

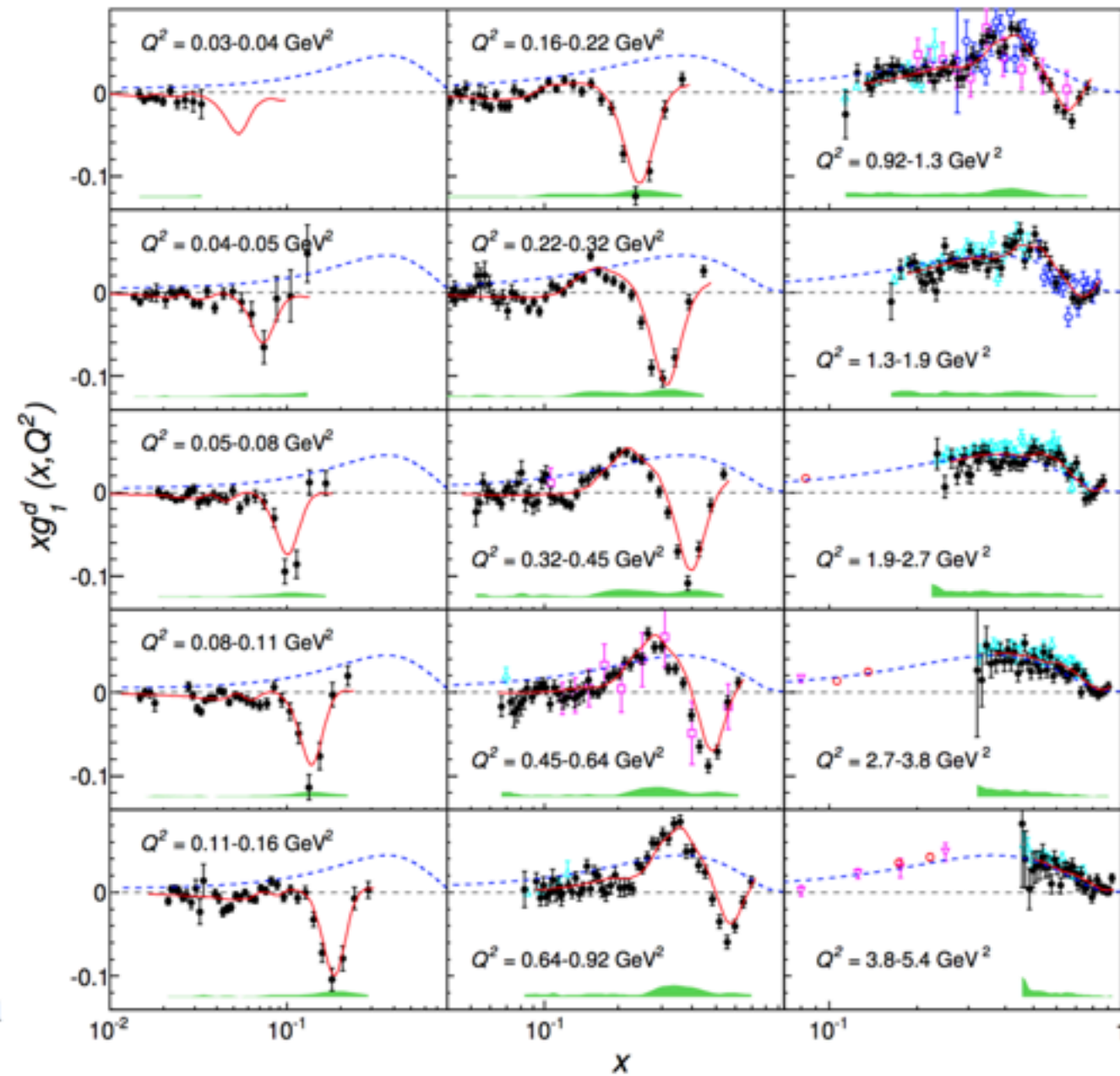
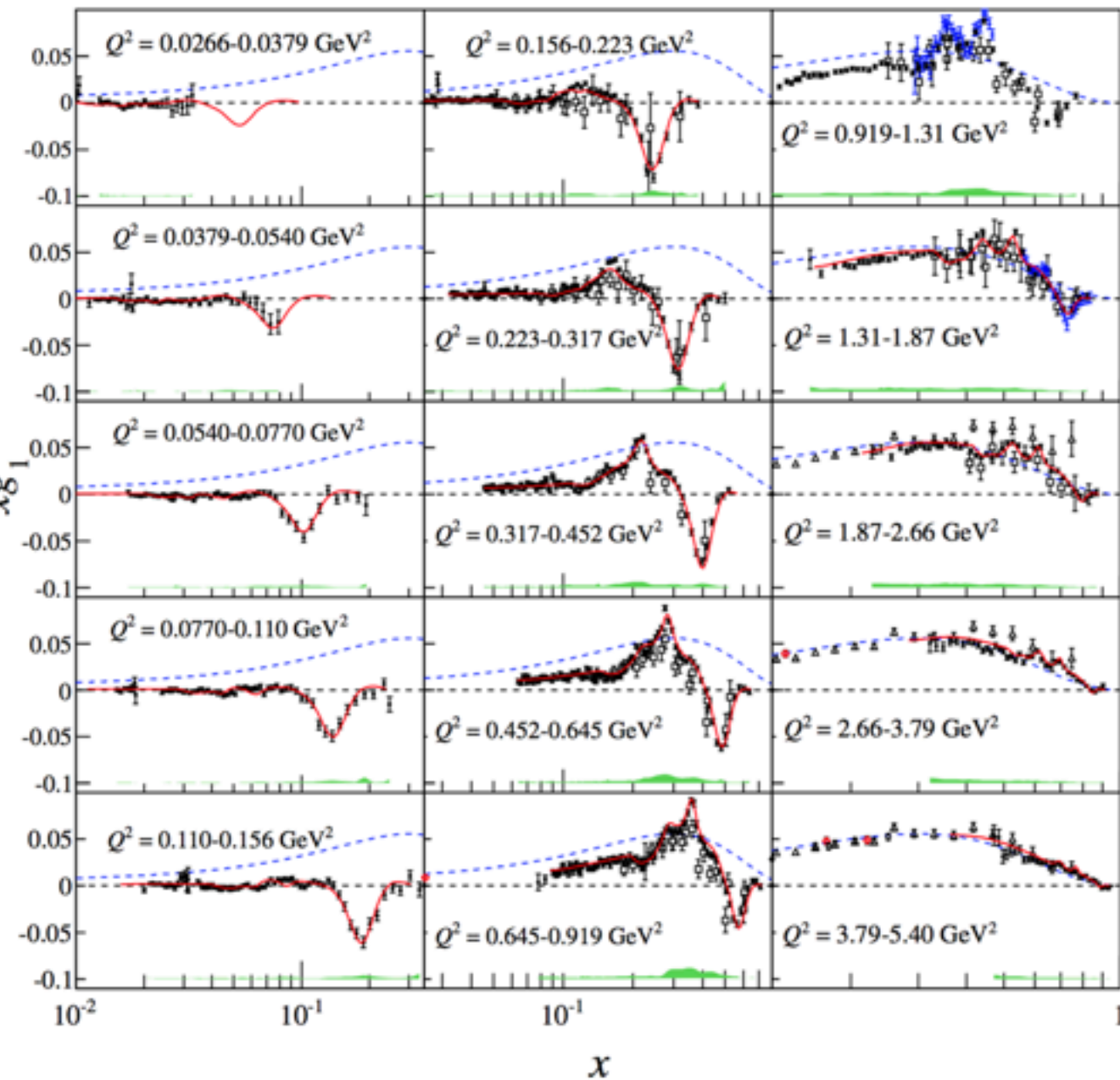


$g_1$  shown against world data

$$\frac{A_{||}}{D} = (1 + \eta\gamma) \frac{g_1}{F_1} + \gamma(\eta - \gamma) \frac{g_2}{F_1}$$

Proton

Deuteron

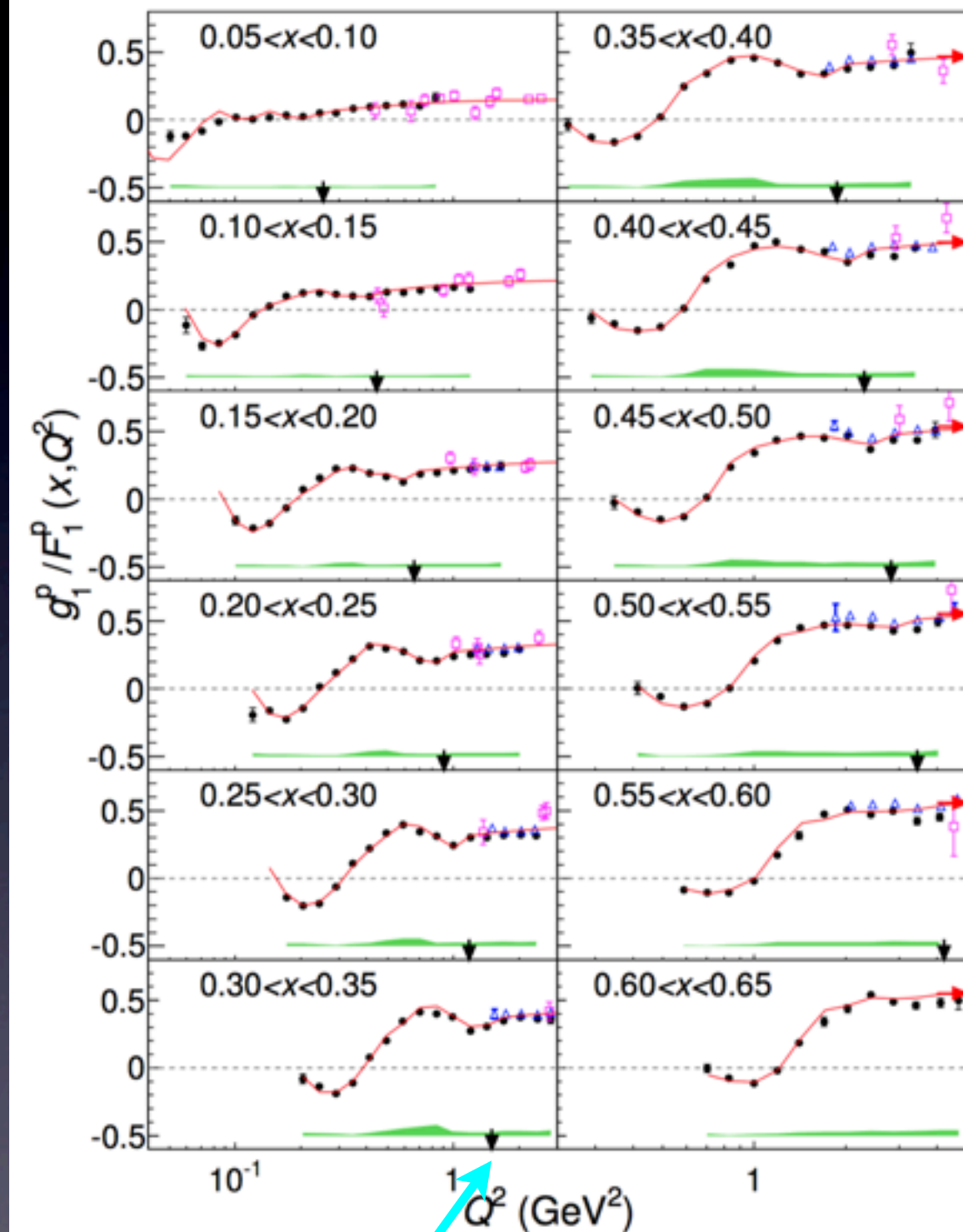




# $g_1/F_1$ vs. $Q^2$

(shown with E143, EG1-DVCS data)

$$\frac{A_{||}}{D} = (1 + \eta\gamma) \frac{g_1}{F_1} + \gamma(\eta - \gamma) \frac{g_2}{F_1}$$



DIS limit  
( $W = 2$  GeV)

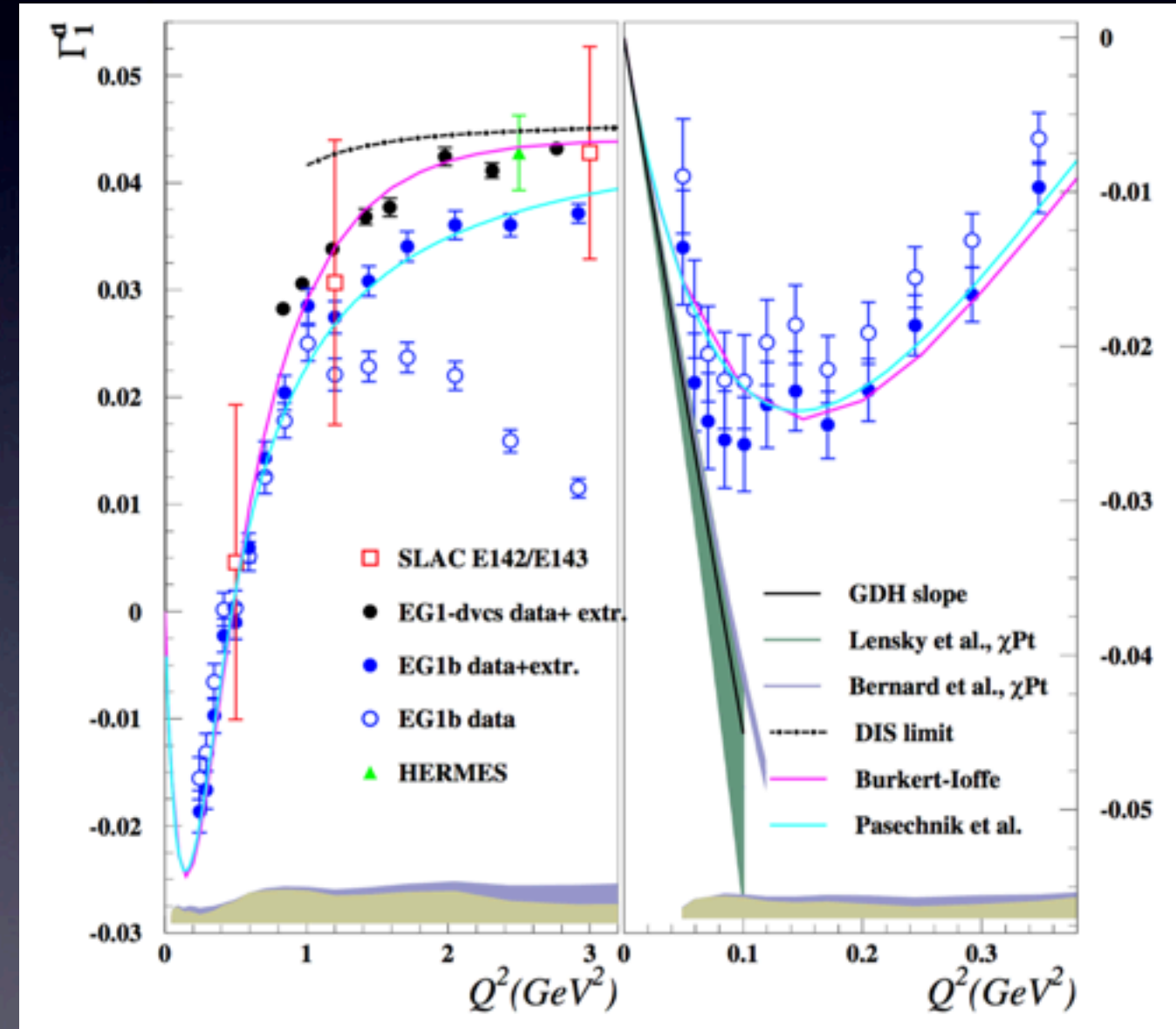
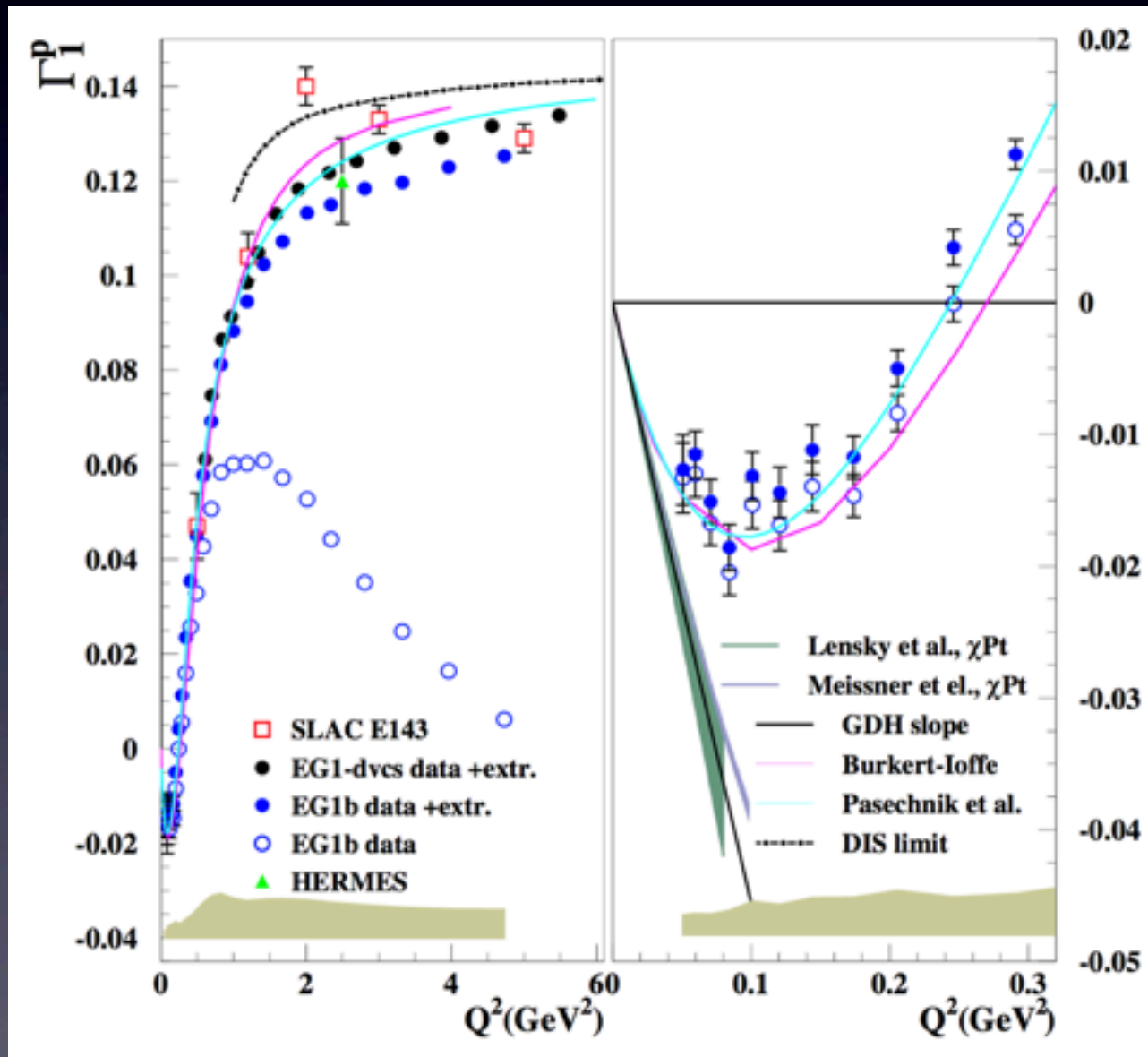
NLO PDF  
fit at  $Q^2 = 5$  GeV<sup>2</sup>

# Moments of $g_1$ Needed to test *sum rules* and determine matrix elements in the OPE (Operator Product Expansion)

$$\Gamma_1 = \int g_1 dx \quad (\text{integrated over } x \text{ from } x=0.001 \text{ to elastic threshold})$$

Proton

Deuteron



(...“truncated moments” used to test local duality...)



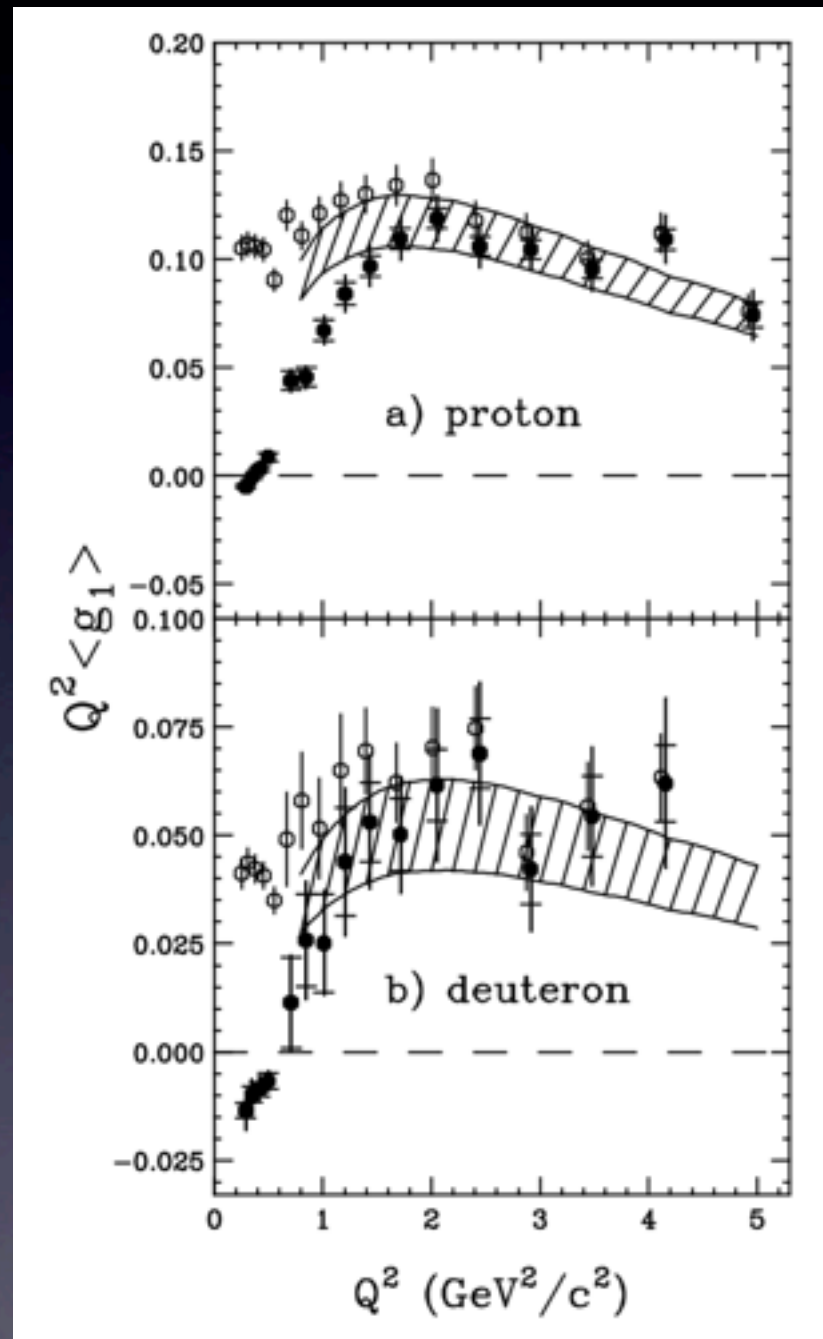
# Tests of Bloom-Gillman Duality

Averaging over resonances - comparing  
to extrapolated NLO PDFs

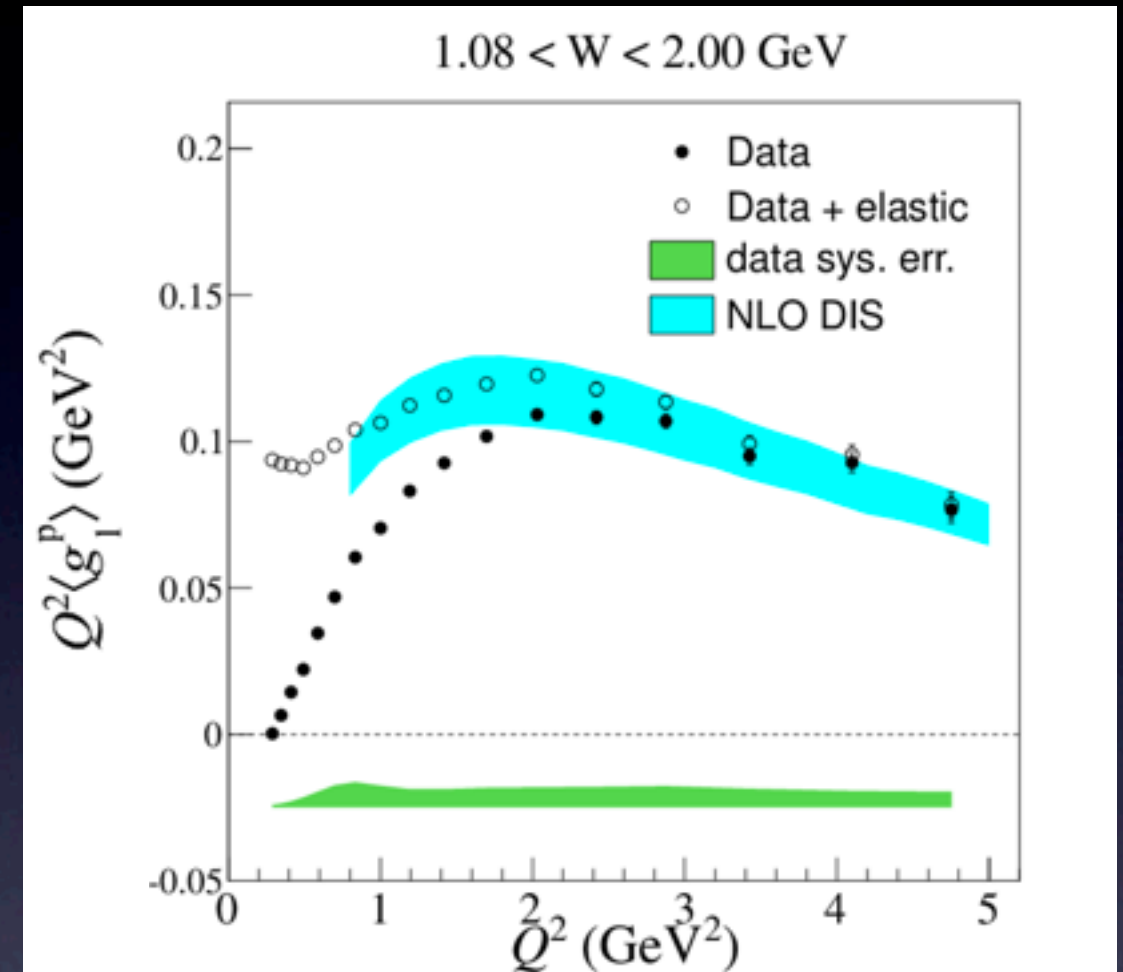
$$\langle g_1(Q^2) \rangle = \frac{\int_{x_l}^{x_h} g_1(x, Q^2) dx}{x_h - x_l}$$

**new proton results**

**previous results**



1.6, 5.7 GeV results only  
(Bosted, *et al.* Phys. Rev. C 75, 035203 (2007))



extended analysis including  
all 4 beam energies (1.6, 2.5, 4.2, 5.7 GeV)

**Parton Distribution Functions:**  
Determined to NLO, fit to  $g_{1\text{QCD}}$  above  
resonance region  
Target mass corrections included  
(Blümlein and Tkabdzke)  
**10(20)% error for proton(deuteron)**  
(estimate of high-x resummation error)

# Tests of Bloom-Gillman Duality

Averaging over resonances - comparing  
to extrapolated NLO PDFs  
(see also Bosted, *et al.* Phys. Rev. C 75, 035203 (2007))

Dominating  
resonances:

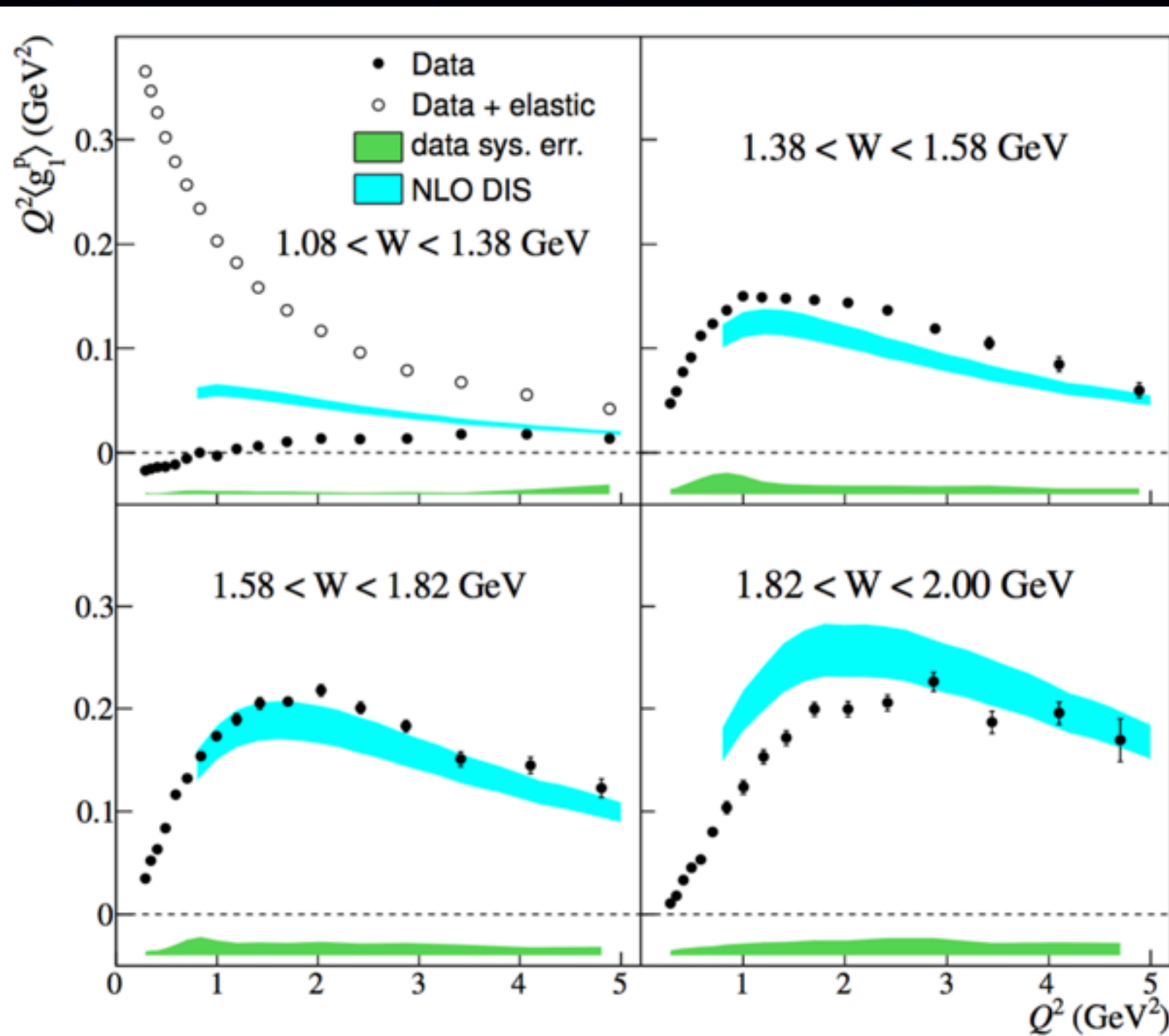
“local” duality results for the proton

$\Delta(1232)$   $\sigma_{3/2}$

elastic  $\sigma_{1/2}$

dominant at  
low  $Q^2$ :  
 $F_{15}(1680)$   $\frac{\sigma_{3/2}}{\sigma_{1/2}}$   
at larger  $Q^2$   $\nearrow$

$S_{11}(1650)$   
 $S_{31}(1620)$   
 $D_{33}(1700)$



$P_{11}(1440)$   
 $S_{11}(1535)$   $\sigma_{1/2}$

$D_{13}(1520)$   $\frac{\sigma_{3/2}}{\sigma_{1/2}}$   
 $\nwarrow$  dominates  
above  $Q^2 > 1$

Large  
number of  
less well-  
established  
resonances



## Summary:

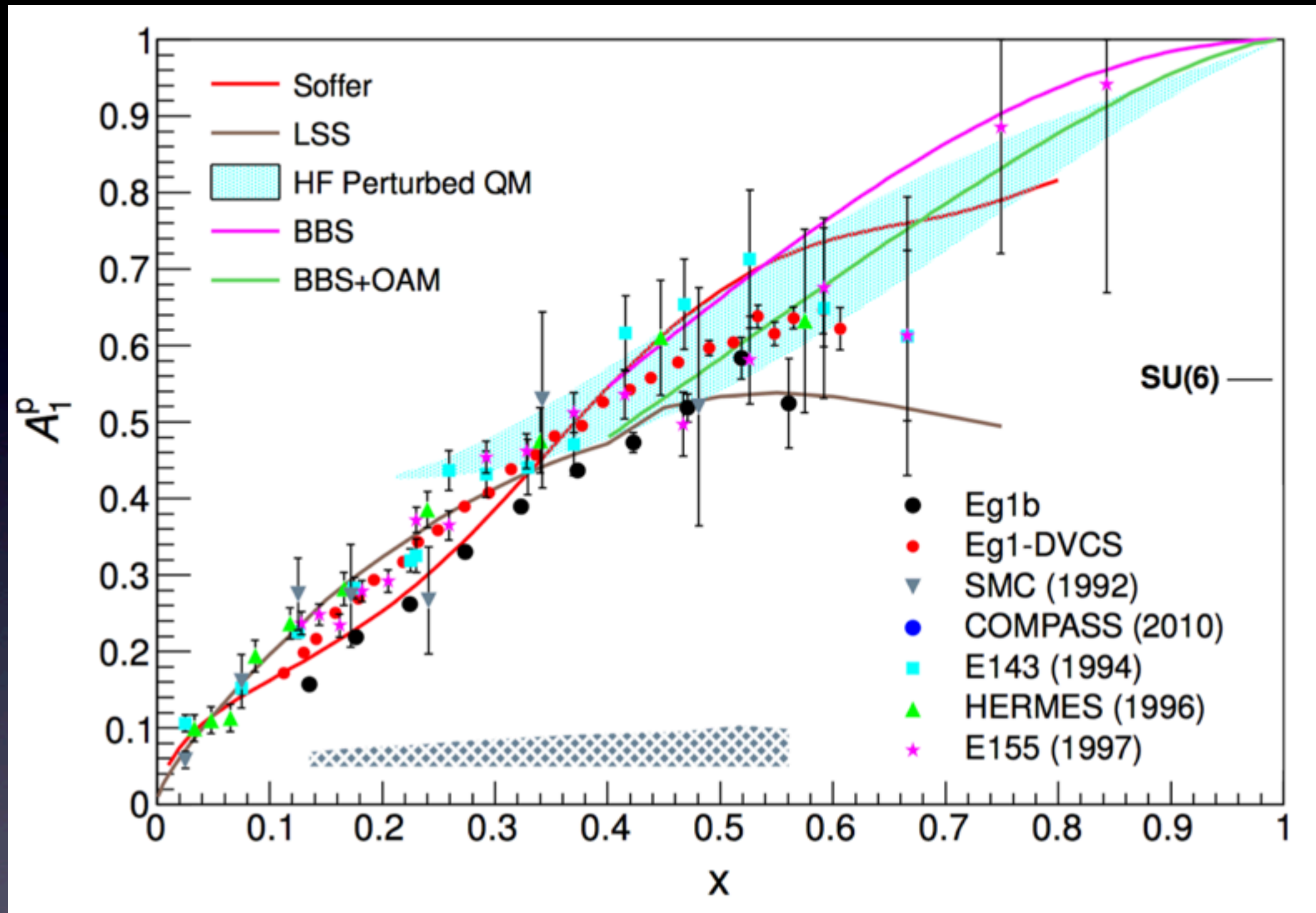
**The EG1 data set (from Jefferson Laboratory Hall-B) offers by far the most comprehensive data coverage of the  $g_1$  polarized structure function available in the resonance region for the study of quark-hadron duality.**

**Analyzed data tables from this experiment are now available and pending final publication in Phys. Rev. C.**

# EXTRA SLIDES



# $A_1$ Deep Inelastic Scattering ( $Q^2 > 1 \text{ GeV}^2$ , $W > 2 \text{ GeV}$ )

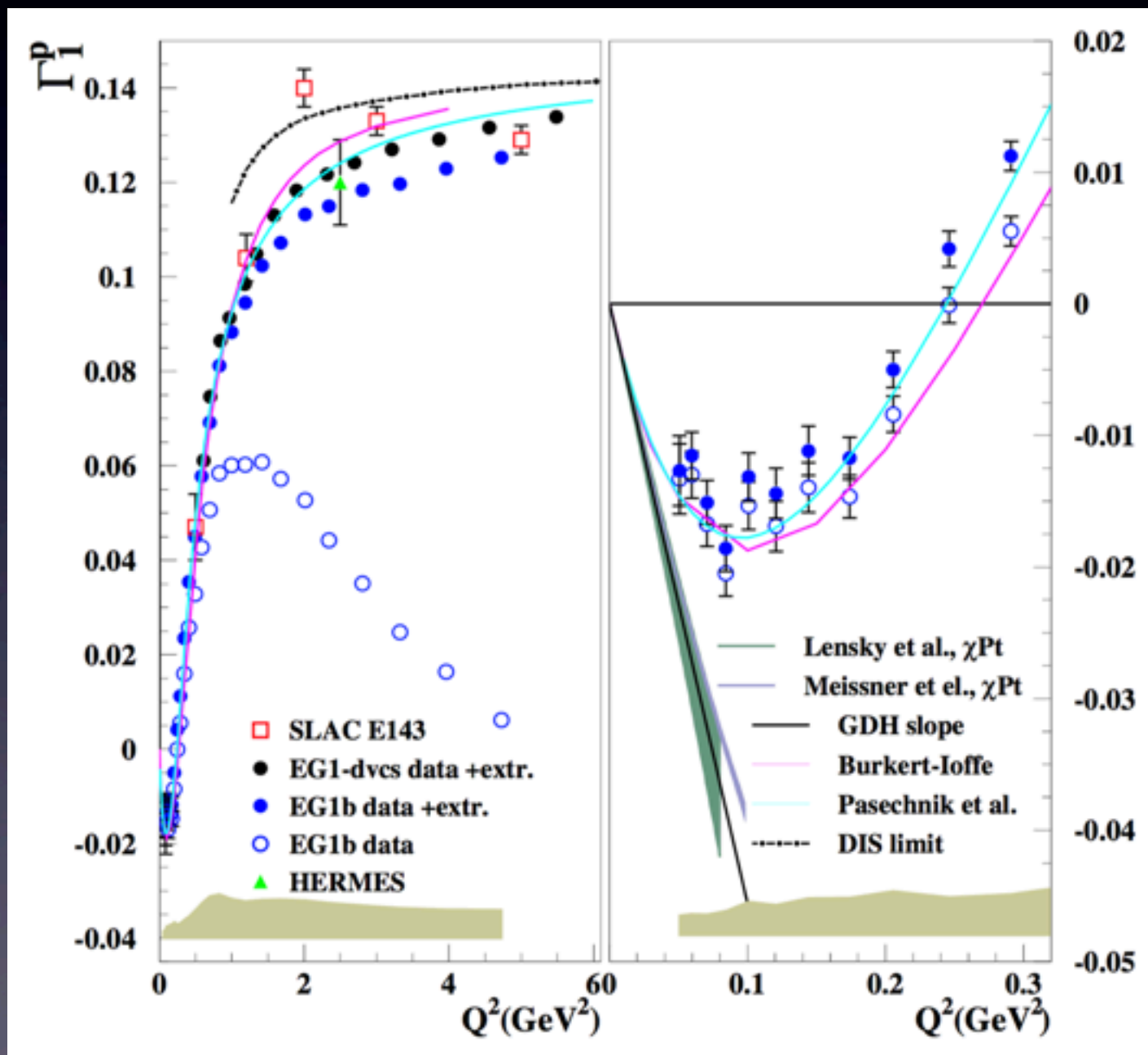


DIS results at high  $x$  provide insights into QCD models of the nucleon

# Moments of $g_1$ Needed to test *sum rules* and determine matrix elements in the OPE (Operator Product Expansion)

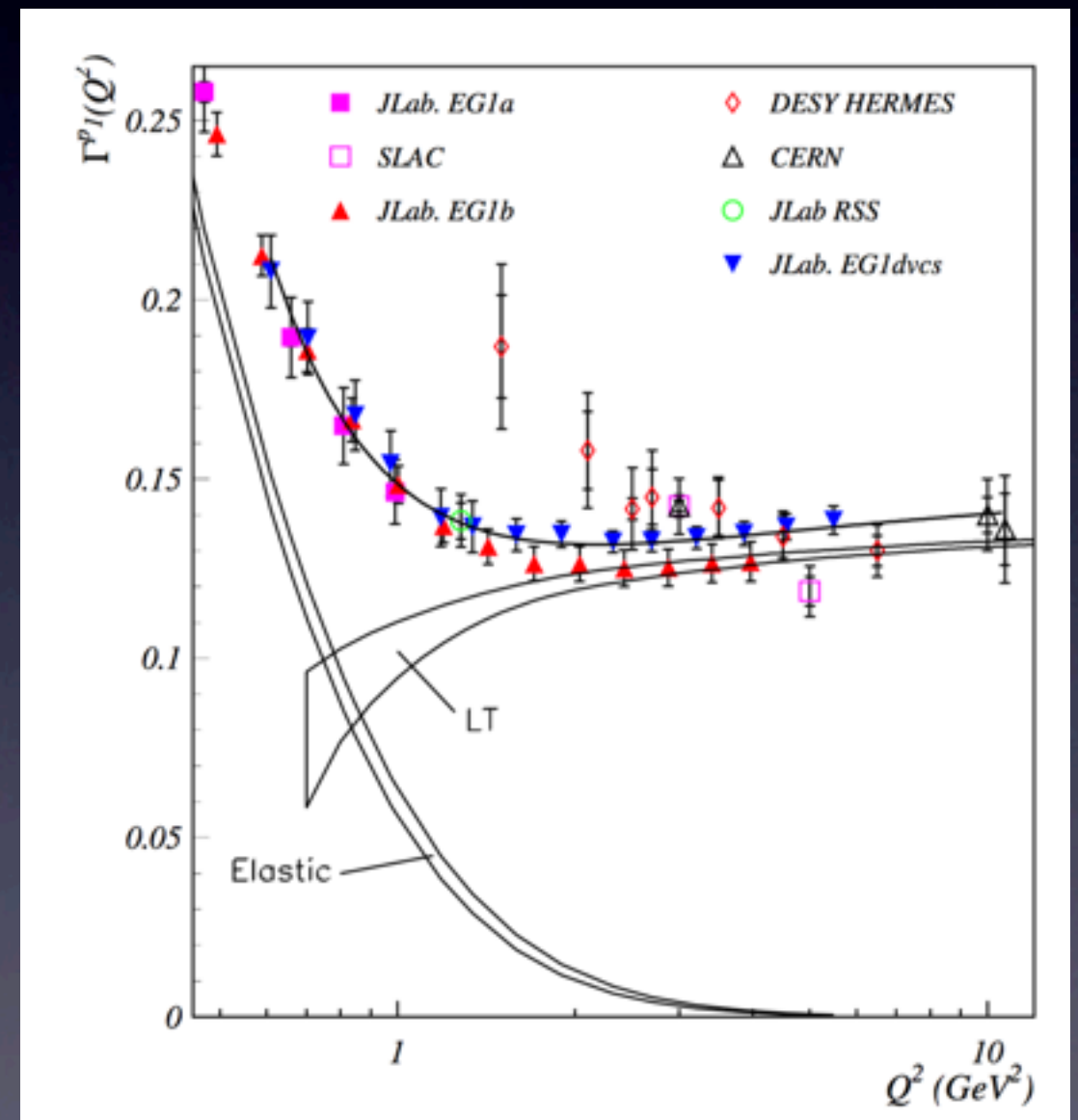
$$\Gamma_1 = \int g_1 dx \quad (\text{integrated over } x \text{ from } x=0.001 \text{ to elastic threshold})$$

(“first moment” of  $g_1$ )



see also Prok, *et al.* Phys. Rev. B 672, 12 (2009)

## Higher Twist analysis of $\Gamma_1$ (includes elastic contribution)



Extraction of higher twist elements through a fit by A. Deur



# Forward Spin Polarizability see also Prok, et al. Phys. Rev. B 672, 12 (2009)

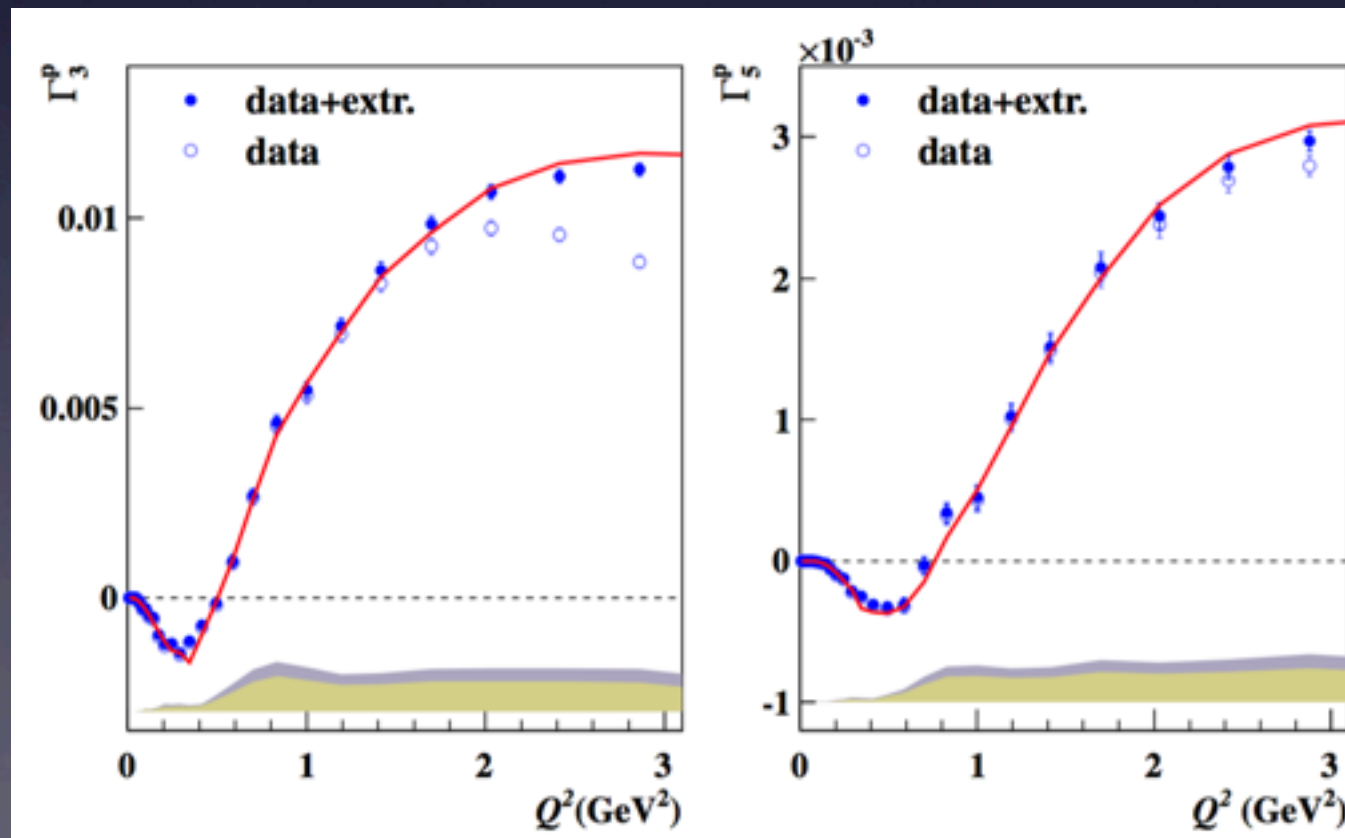
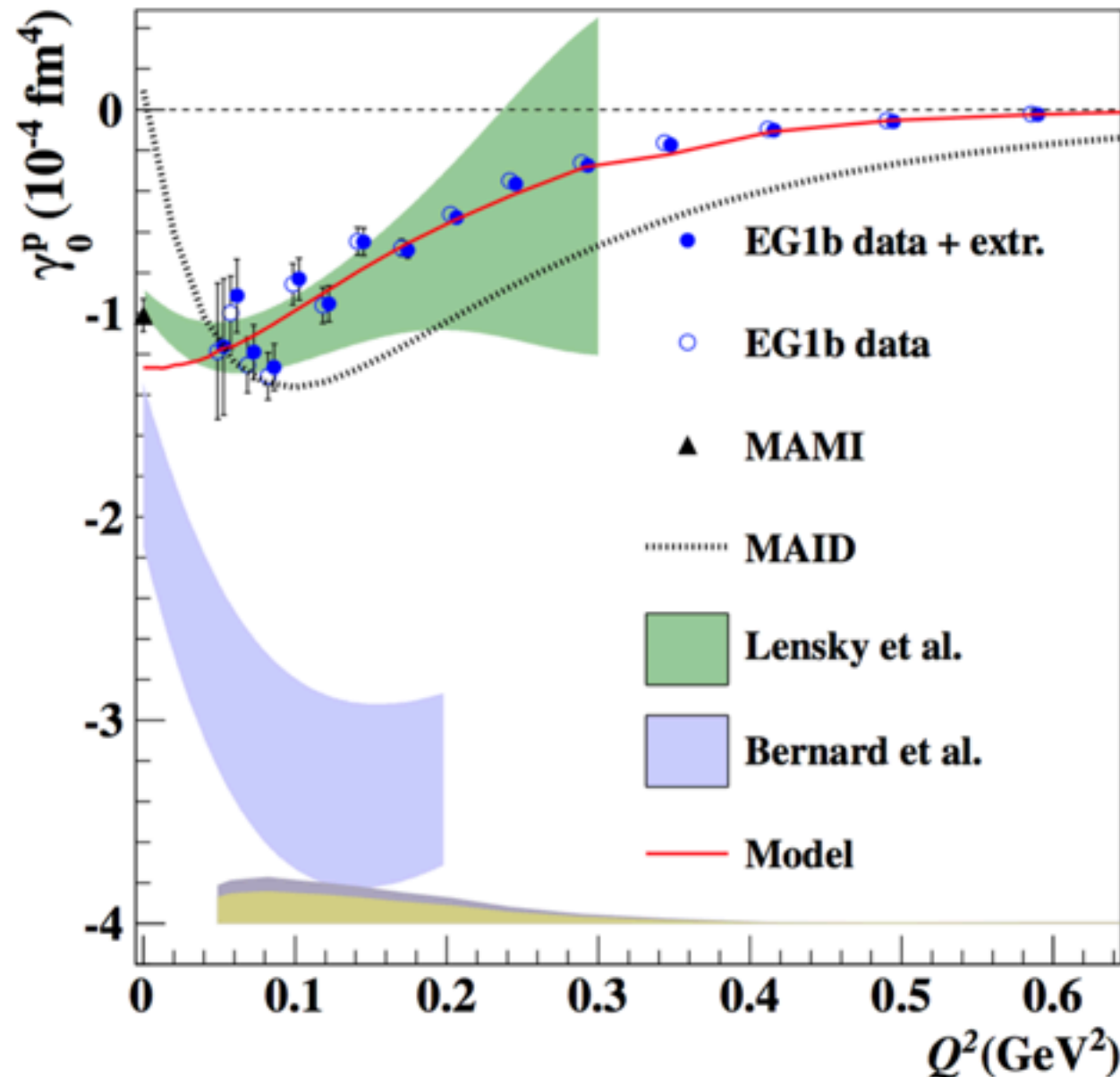
For scattering cross-sections in terms of Compton amplitudes

$$\begin{aligned}\gamma_0 &= \frac{1}{4\pi} \int_{\nu_{th}}^{\infty} \frac{\sigma_{3/2} - \sigma_{1/2}}{\nu'^3} d\nu' \\ &= \frac{16M^2\alpha}{Q^6} \int_0^{x_{th}} x^2 A_1(x, Q^2) F_1(x, Q^2) dx\end{aligned}$$

## Higher Moments

Large x-range provided opportunity to measure these

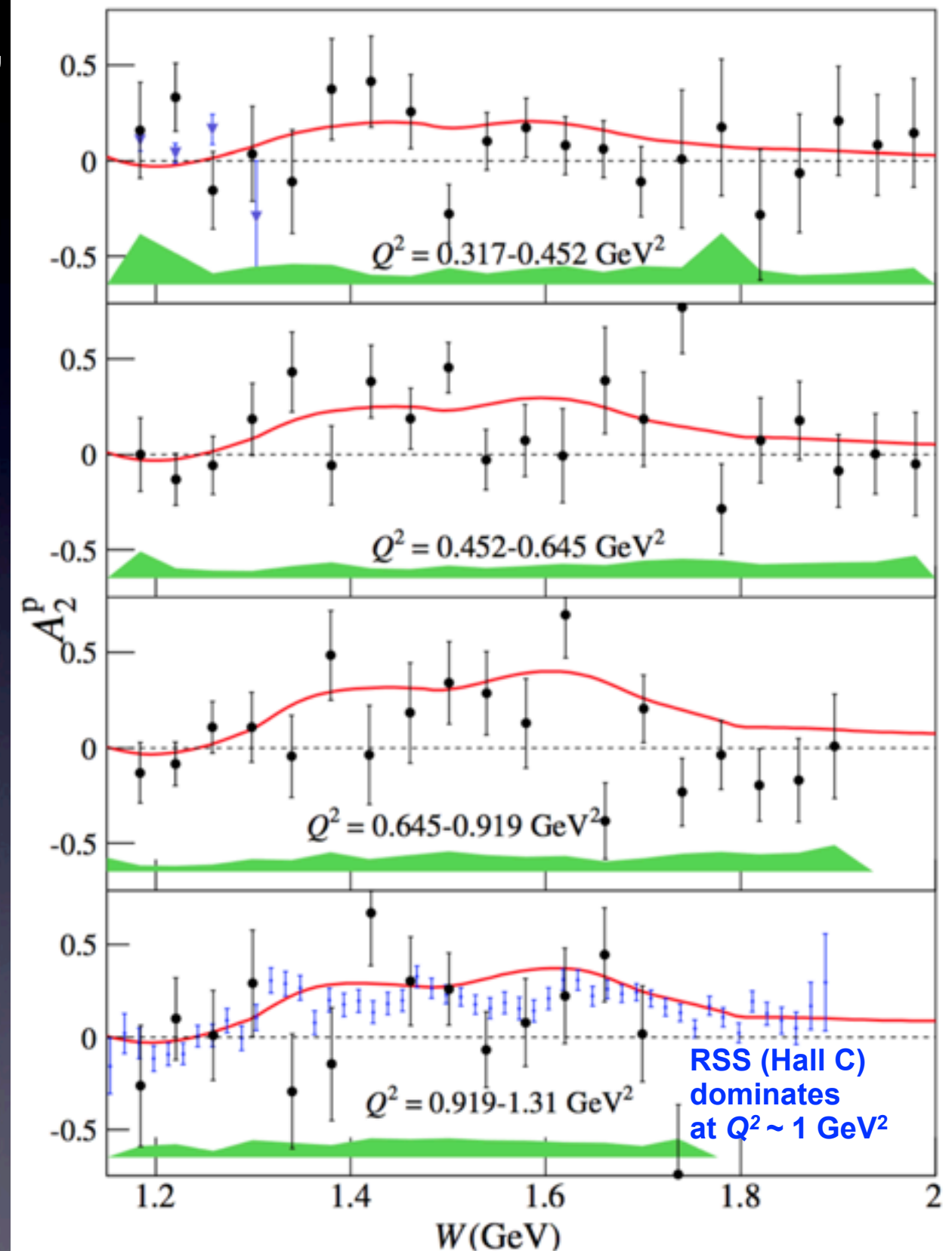
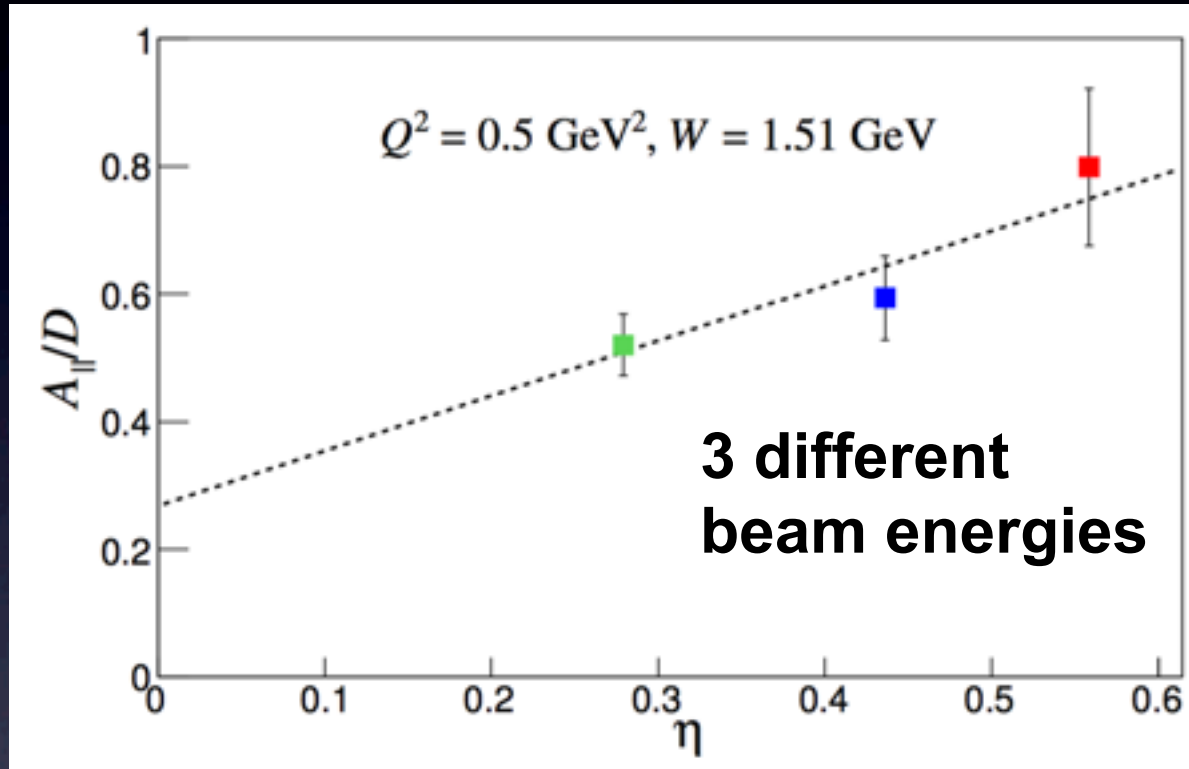
$$\Gamma_1^n = \int x^{n-1} g_1(x, Q^2) dx$$



# First extraction of $A_2$ and $g_2$ from EG1 data

little world data available!

$$A_1 + r \circledast A_2 = \frac{A_{||}}{D} \quad \begin{array}{l} A_1 = \text{y-intercept,} \\ A_2 = \text{slope} \end{array}$$



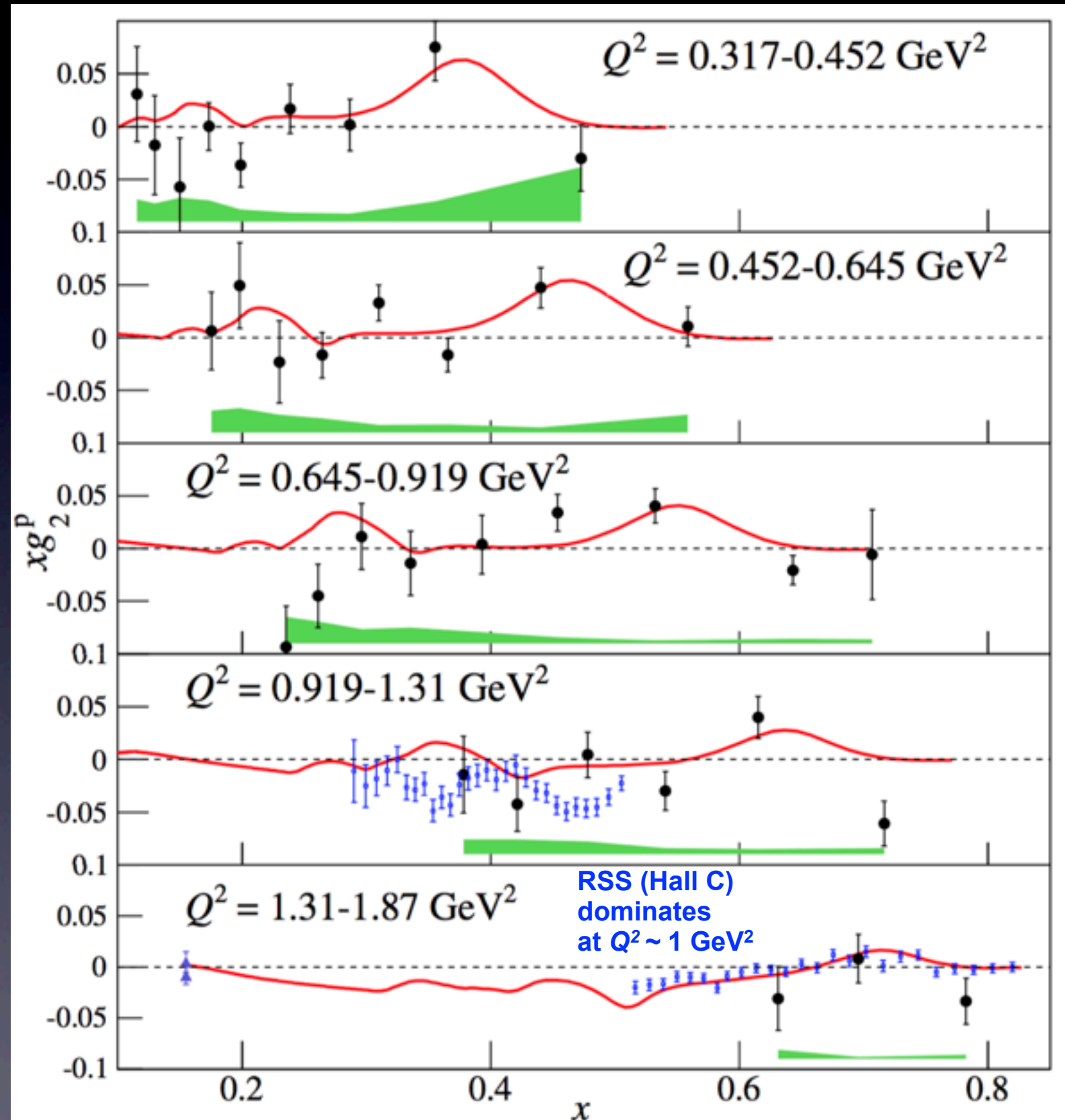


# First extraction of $A_2$ and $g_2$ from EG1 data

little world data available!

$g_2$  extracted similarly

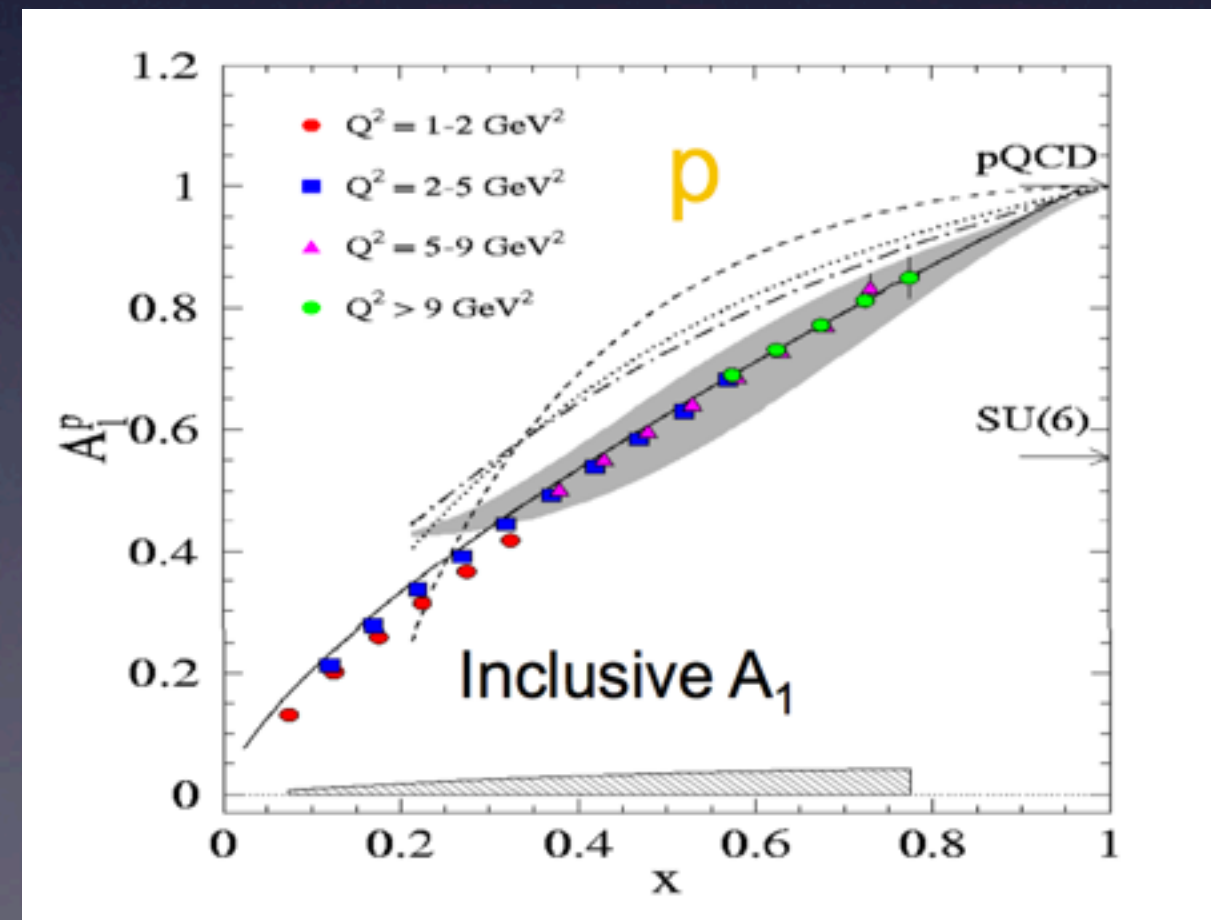
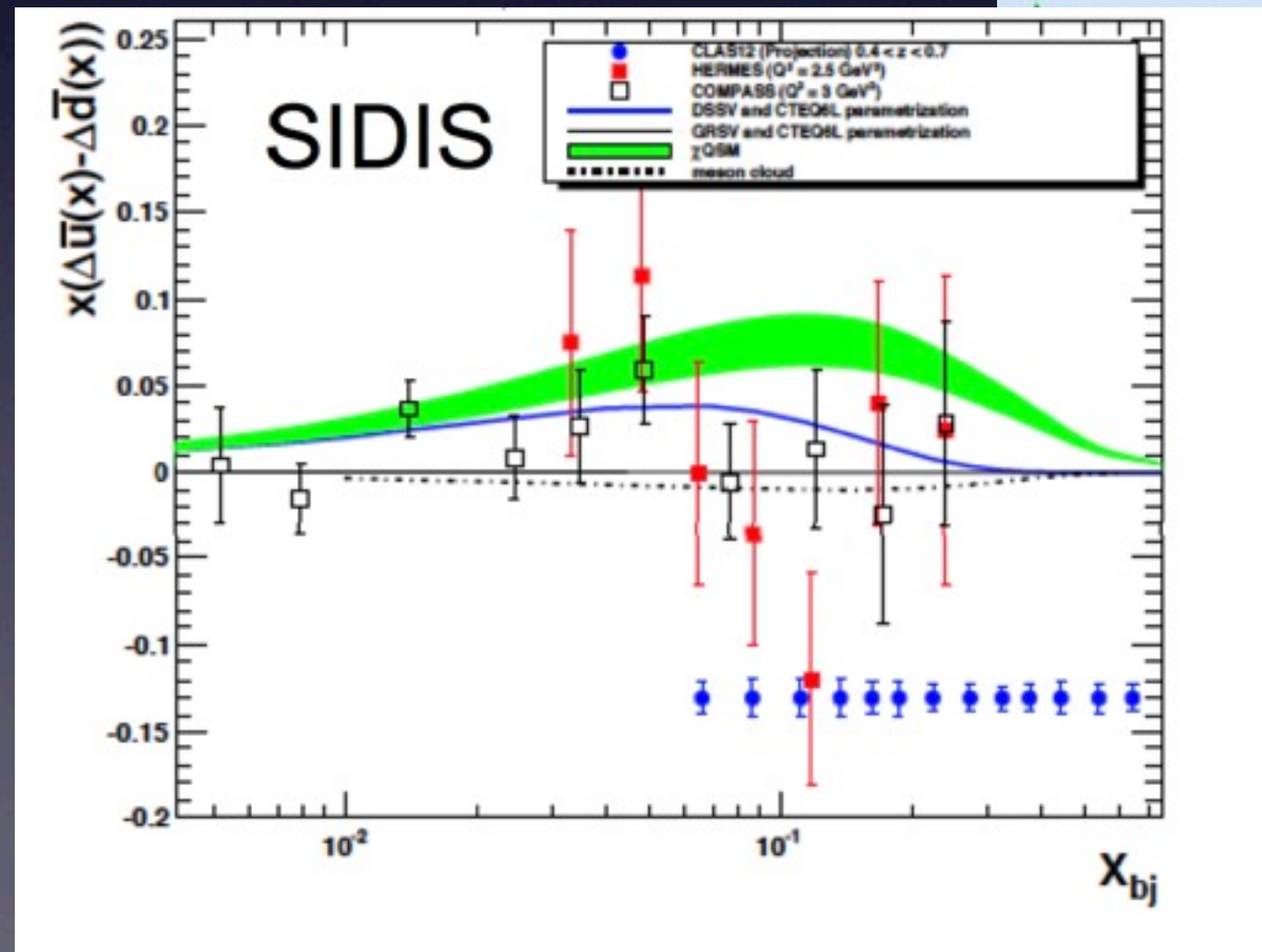
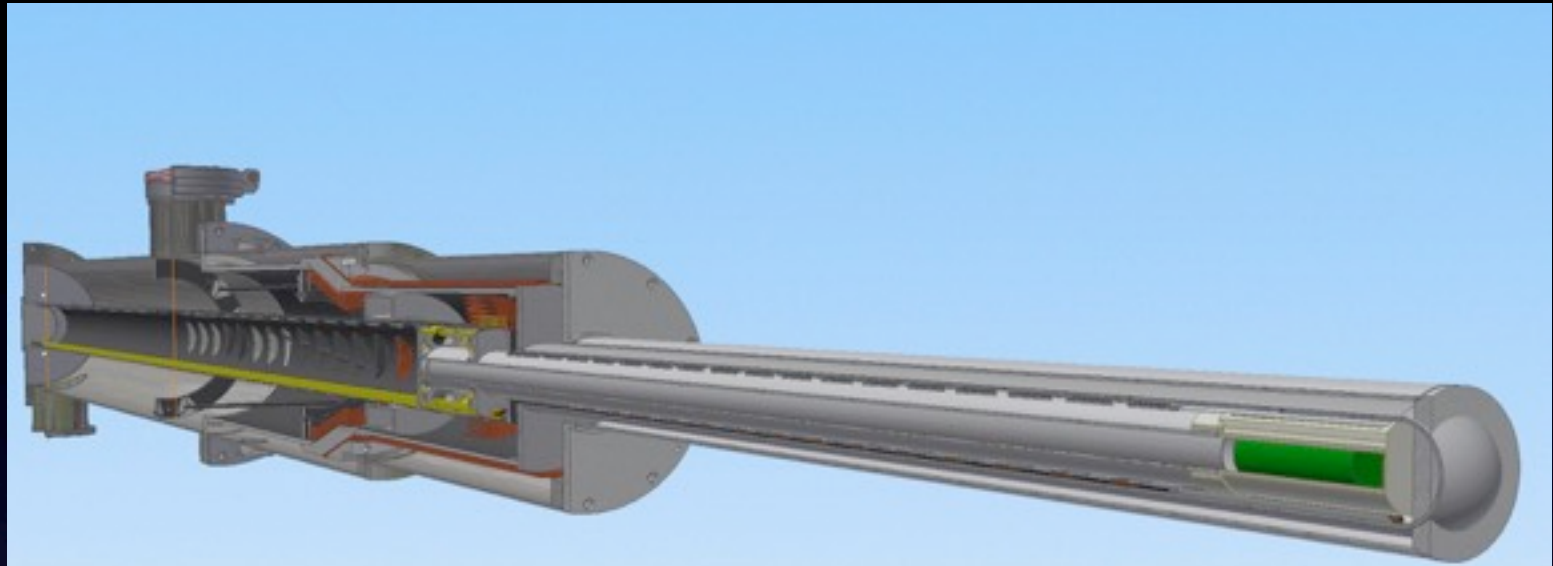
$$\frac{A_{||}}{D} = (1 + \eta\gamma) \frac{g_1^p}{F_1^p} + \gamma(\eta - \gamma) \frac{g_2^p}{F_1^p}$$



-Many EG1 publications helped build global models of nucleon spin structure!

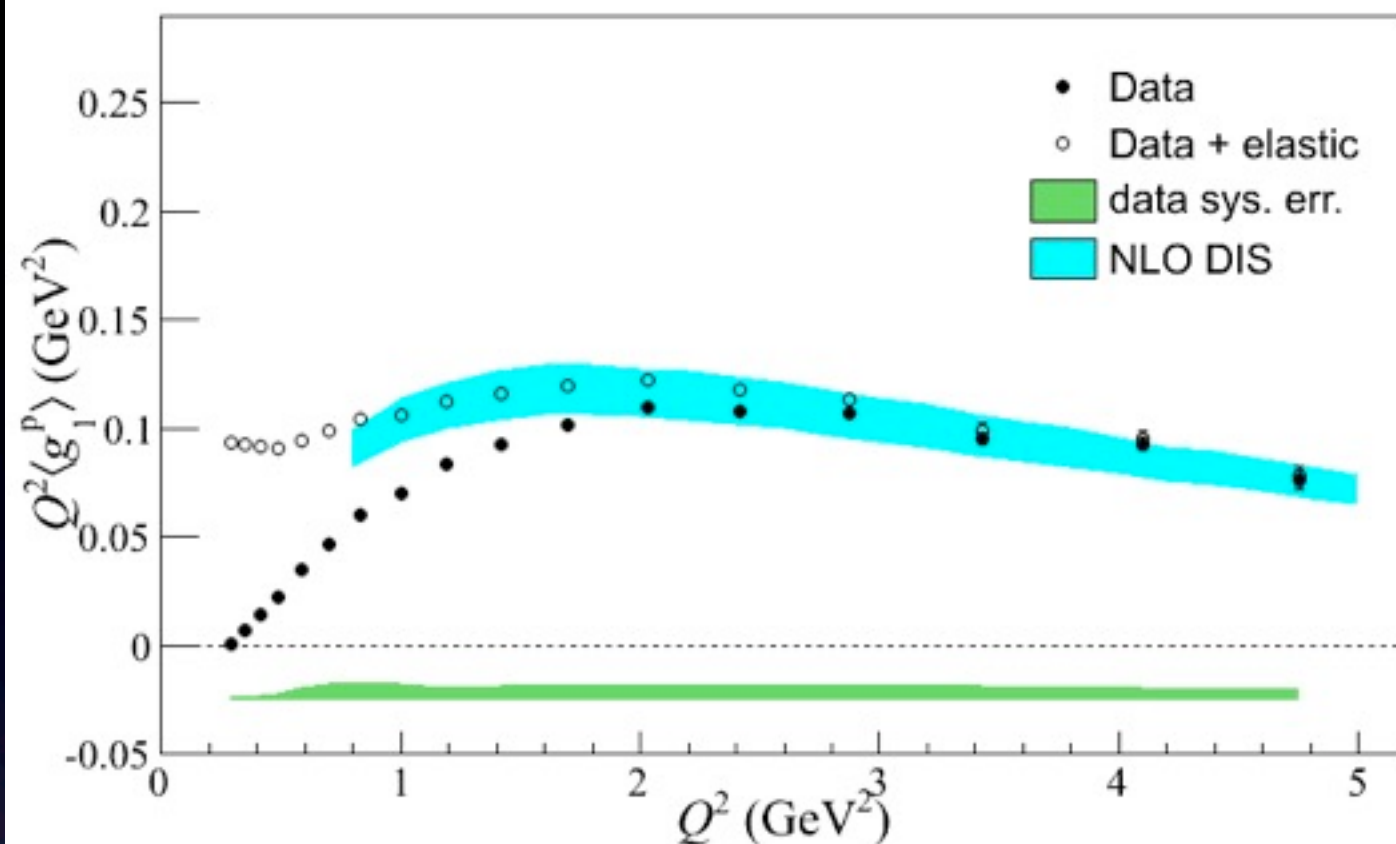
CLAS12 longitudinally polarized target design

-The 12 GeV longitudinally polarized target: higher  $x$  means better testing of QCD models

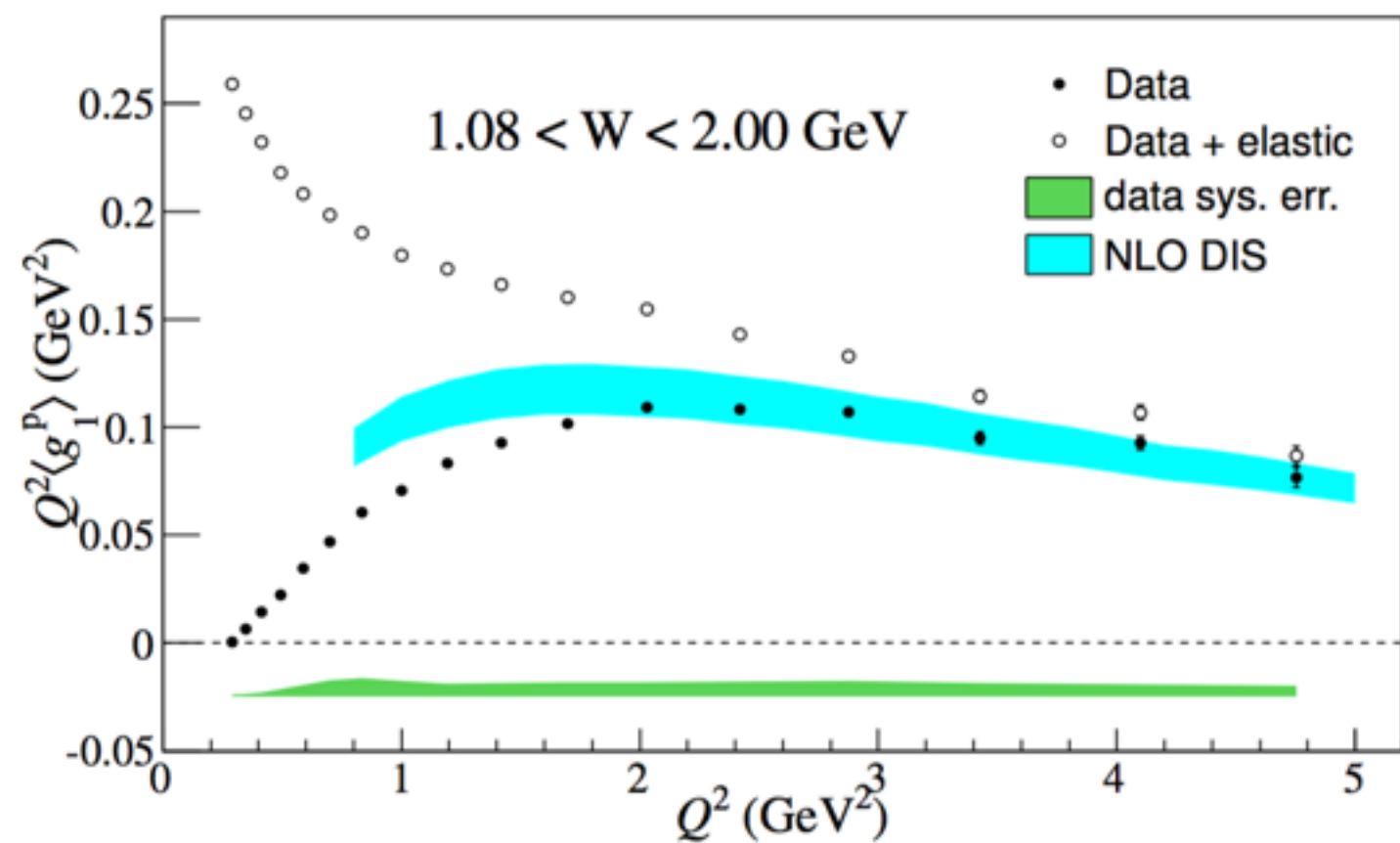




$1.08 < W < 2.00 \text{ GeV}$



$1.08 < W < 2.00 \text{ GeV}$



## Blümlein and Tkbladzke Target Mass Corrections

$$g_1^{TM}(x, Q^2) = \frac{x}{\xi(1+\gamma)^{3/2}} g_1^{QCD}(\xi, Q^2) \\ + \frac{(x+\xi)\gamma}{\xi(1+\gamma)^2} \int_{\xi}^1 \frac{du}{u} g_1^{QCD}(u, Q^2) \\ - \frac{\gamma(2-\gamma)}{2(1+\gamma)^{5/2}} \int_{\xi}^1 \frac{du}{u} \int_u^1 \frac{dv}{v} g_1^{QCD}(v, Q^2)$$

Blümlein and Takbladzke, Nucl. Phys.  
B553, 427 (1999)

$$\xi \equiv 2x / (1 + \sqrt{1 + 4M^2 x^2 / Q^2})$$

## Errors due to high-x resummation:

Bianchi, Fantoni, Liuti, Phys. Rev. D 69, 014505 (2004)