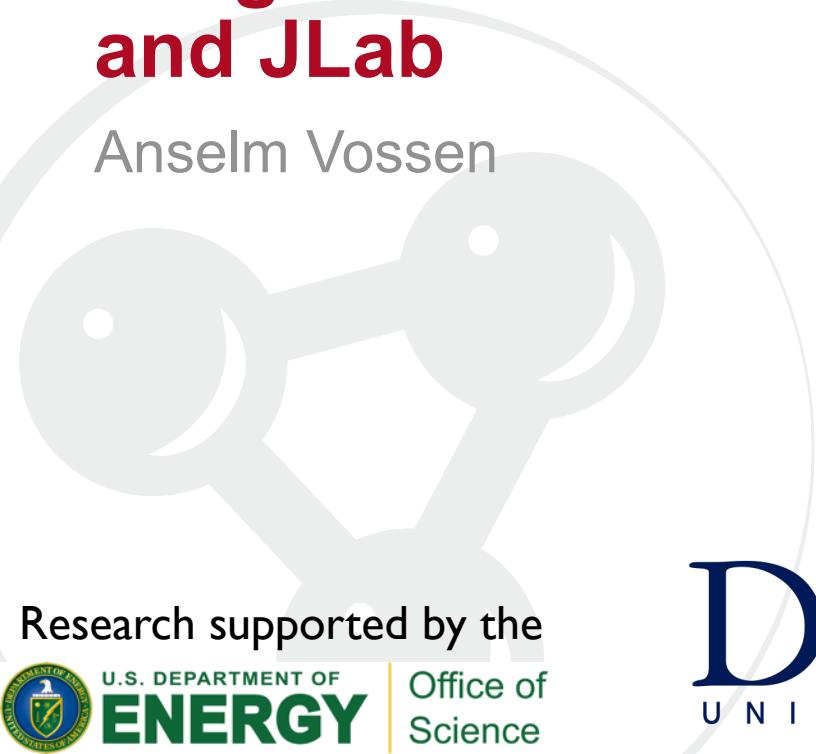


DNP, Halloween 2020

# Insights from and Prospects for Belle (II) and JLab

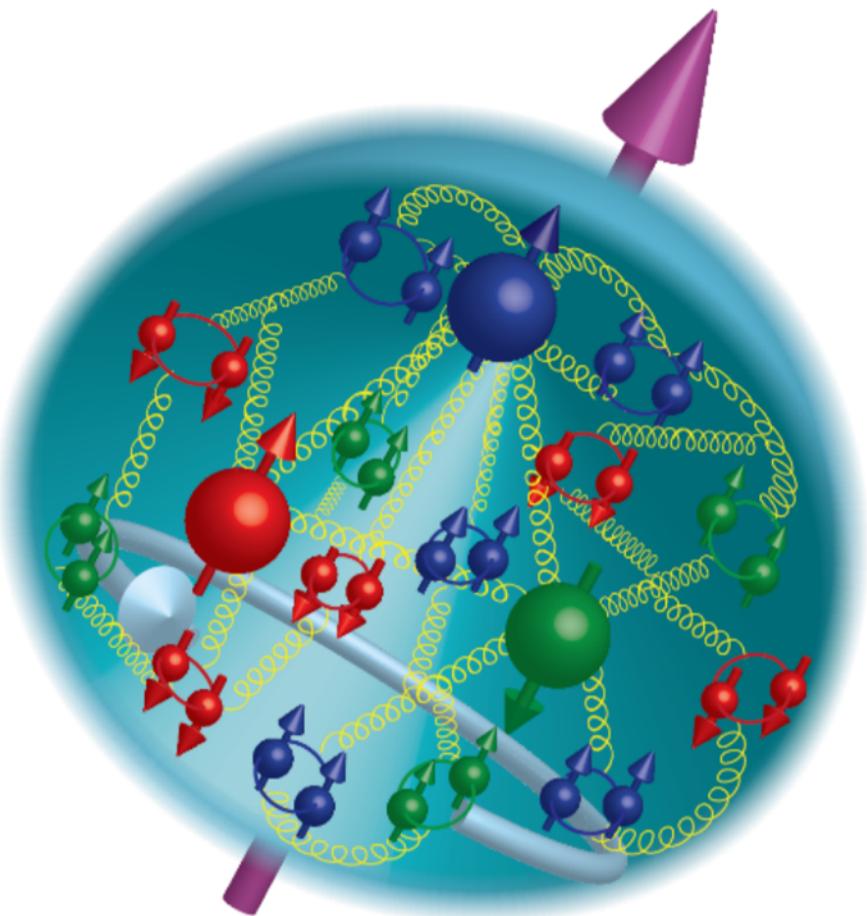
Anselm Vossen



Research supported by the  
 U.S. DEPARTMENT OF  
**ENERGY** | Office of Science

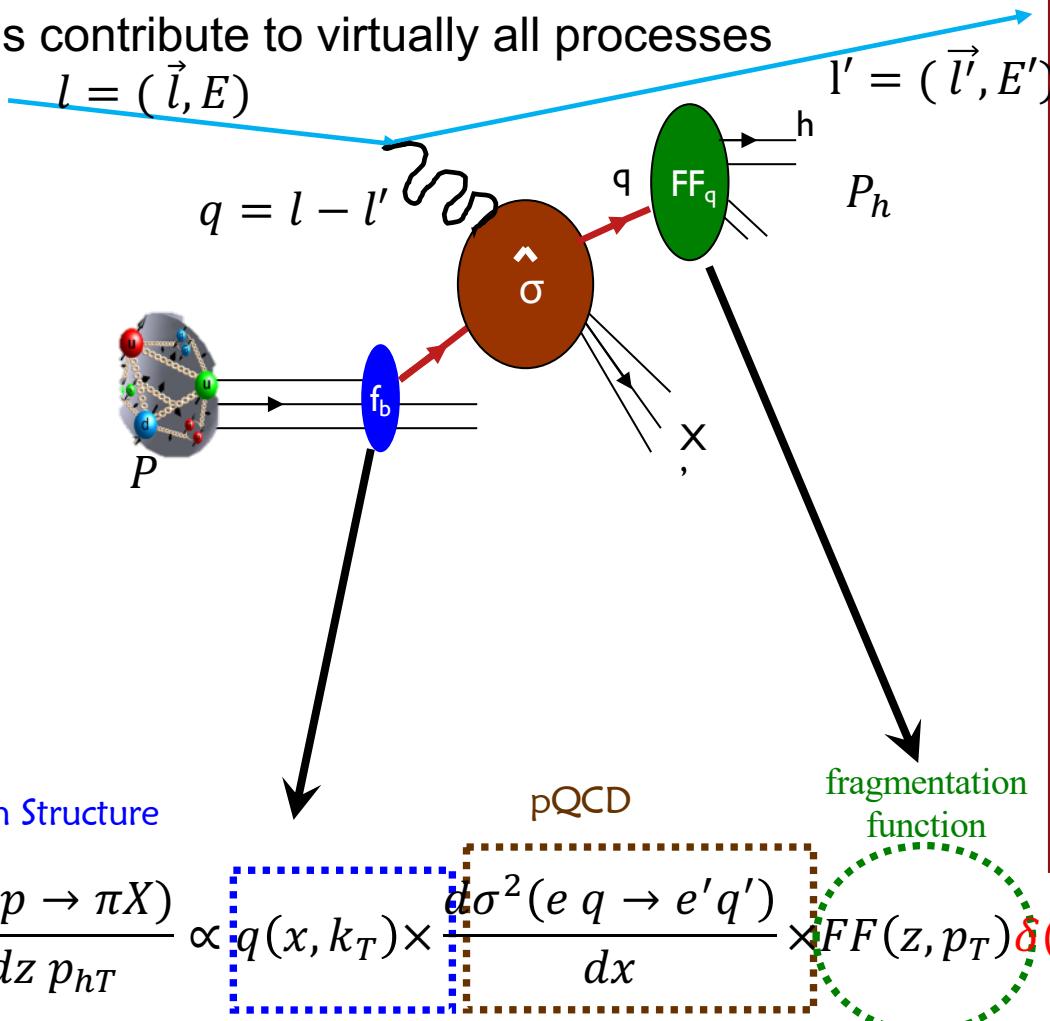
**Duke**  
UNIVERSITY

**Jefferson Lab**



# Hard Scattering is a premier tool to probe the quark and gluon degrees of freedom

- Proton Structure extracted using QCD factorization theorem
- FFs contribute to virtually all processes



- At fixed beam energy need **two** variables to characterize DIS event, e.g.  $Q^2, v \rightarrow x$  in scaling regime

$$-Q^2 = 4EE' \sin^2 \frac{\theta}{2}$$

"hard scale" of the probe

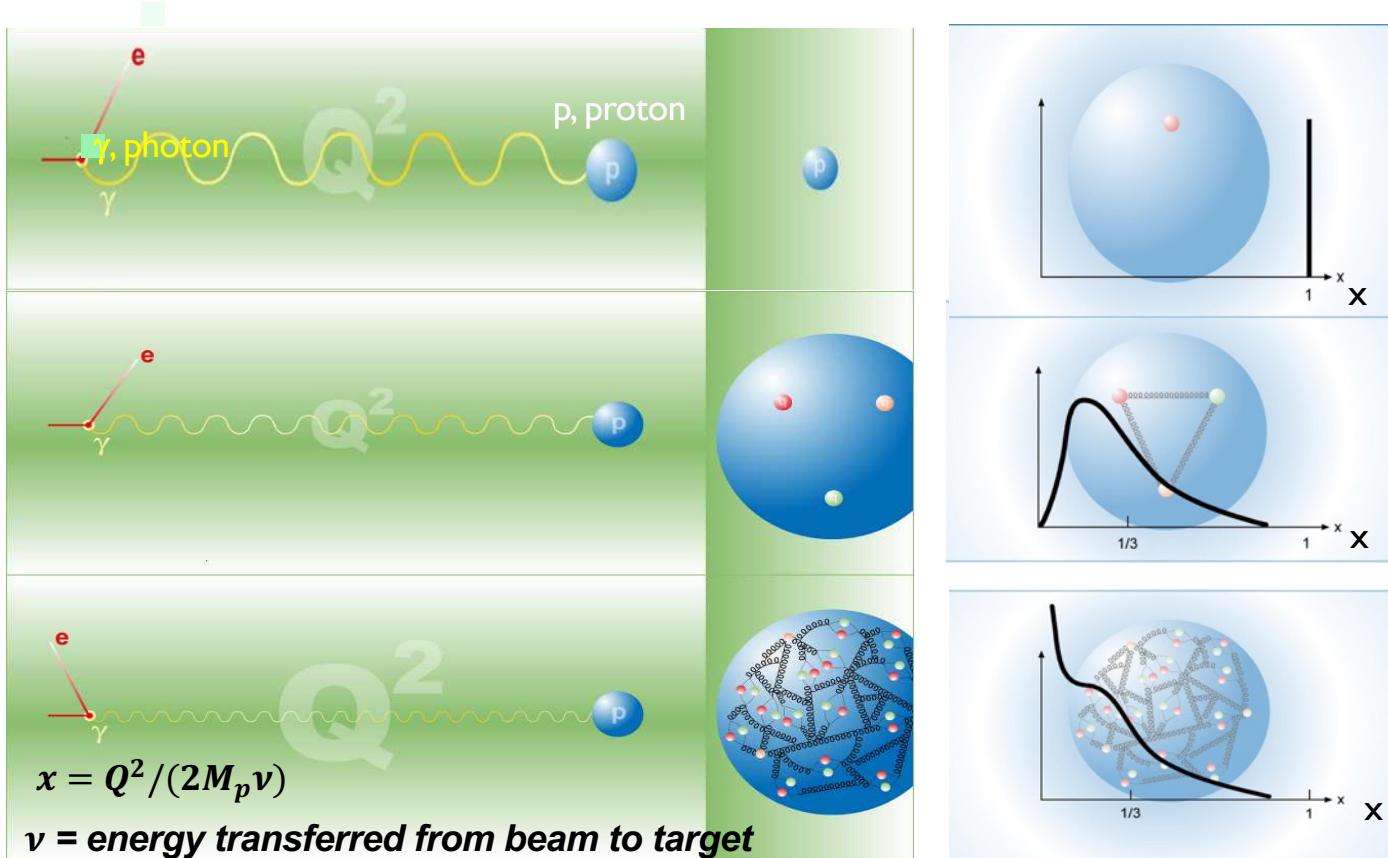
$$-x = \frac{Q^2}{2M_n v} :$$

bjorken **scaling variable**, in partonic picture momentum fraction of the struck parton

$$-z = \frac{P_\mu P_h^\mu}{P^\mu q_\mu}.$$

Fraction of quark momentum carried by outgoing hadron

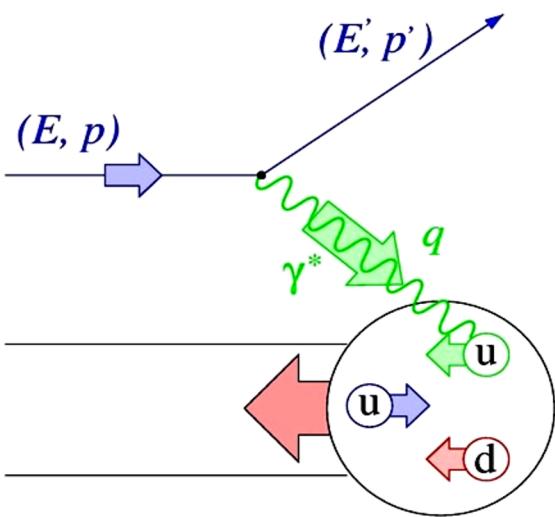
# Fraction of the proton momentum carried by the parton: $x$



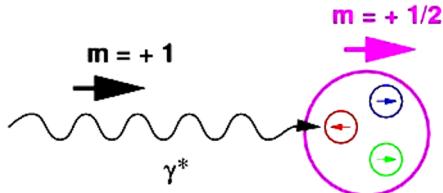
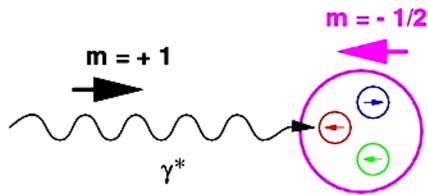
$Q^2$  = “Resolution”

$x$  = “Exposure”

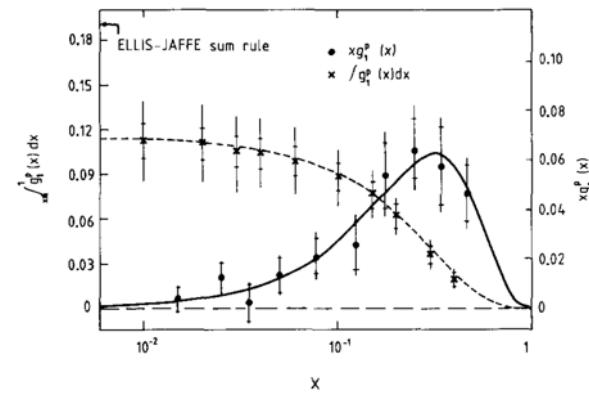
# Adding polarization



$$\sigma_{1/2} \sim \sum_i e_i^2 q_i^+$$



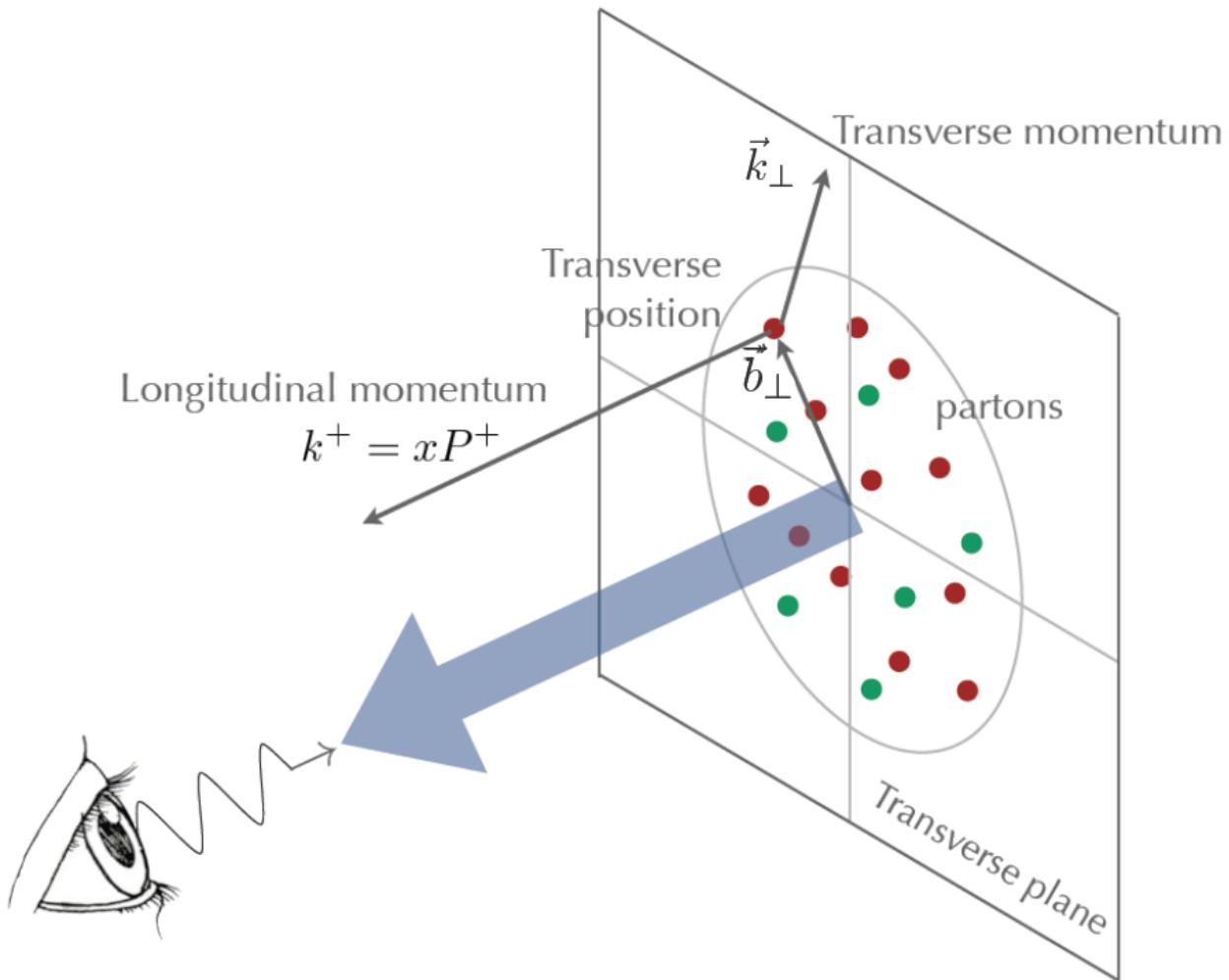
$$\sigma_{3/2} \sim \sum_i e_i^2 q_i^-$$



EMC, Phys. Lett. B206, 2,364 1988

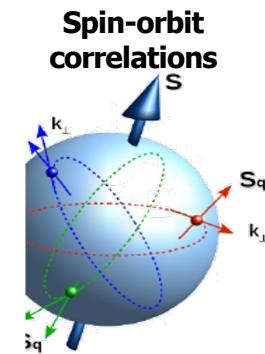
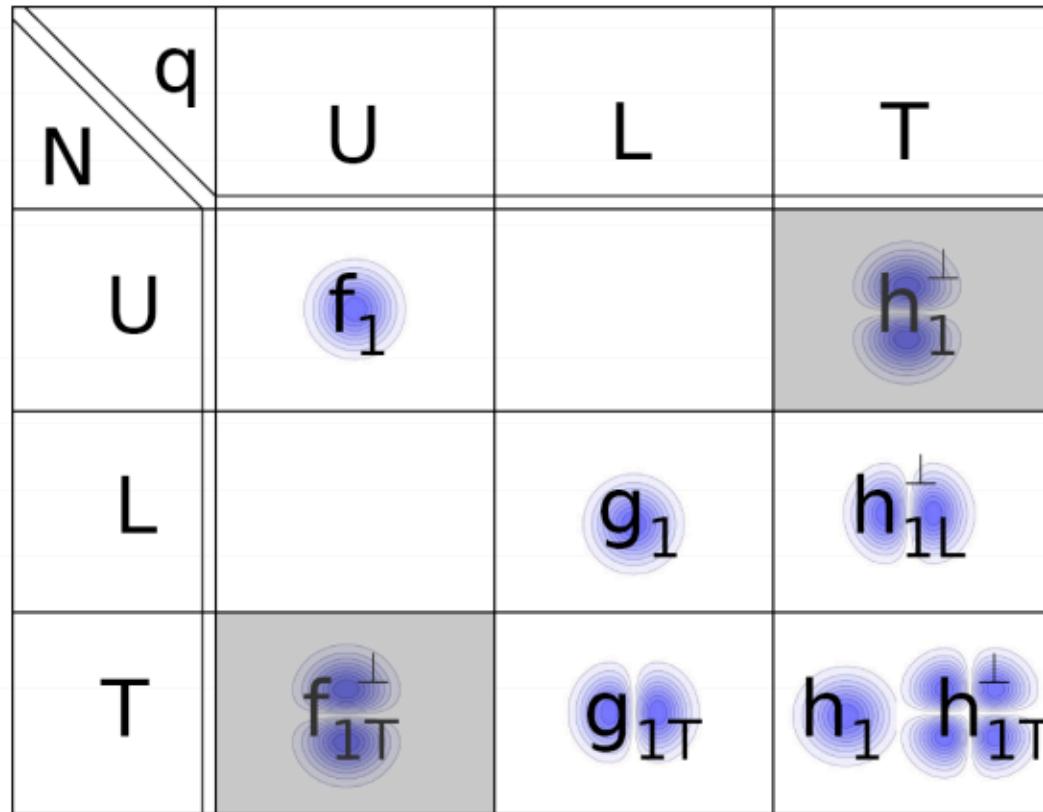
**Spin kills more theories than any other observable!**

# From 1D to 3D...( $x, k_T$ )

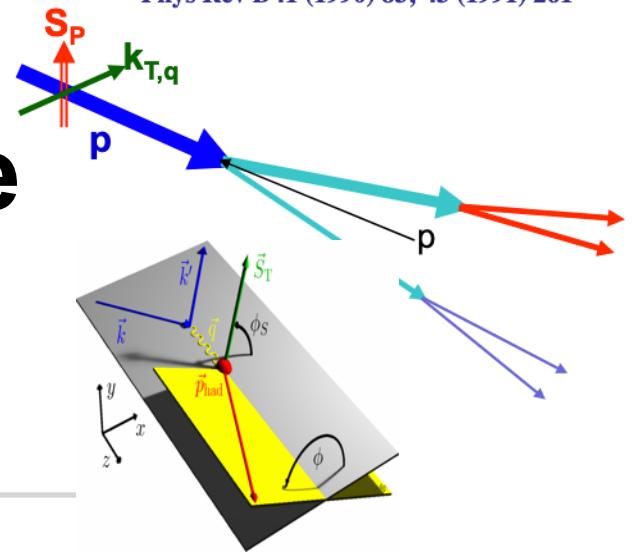


# With Polarization

- In addition to the spin-spin correlations can have spin momentum correlations!
- TMD PDFs  $f(x, k_T)$



# SIDIS X-section in the Parton Model



|                     |                  |  |   |  |
|---------------------|------------------|--|---|--|
| <b>Boer-Mulders</b> | $h_1^\perp =$    |  | - |  |
| <b>Worm Gear</b>    | $h_{1L}^\perp =$ |  | - |  |
| <b>Transversity</b> | $h_{1T}^\perp =$ |  | - |  |
| <b>Sivers</b>       | $f_{1T}^\perp =$ |  | - |  |
| <b>Pretzelosity</b> | $h_{1T}^\perp =$ |  | - |  |
| <b>Worm Gear</b>    | $g_{1L}^\perp =$ |  | - |  |

$$\{[1 + (1 - y)^2] \sum e_q^2 f_1^q(x) D_1^q(z, P_{h\perp}^2)$$

$$+ (1 - y) \frac{P_{h\perp}^{2,q,\bar{q}}}{4z^2 M_N M_h} \cos(2\phi_h^l) \sum_{q,\bar{q}} e_q^2 h_1^{\perp(1)q}(x) H_1^{\perp q}(z, P_{h\perp}^2)$$

$$- |S_L|(1 - y) \frac{P_{h\perp}^2}{4z^2 M_N M_h} \sin(2\phi_h^l) \sum_{q,\bar{q}} e_q^2 h_{1L}^{\perp(1)q}(x) H_1^{\perp q}(z, P_{h\perp}^2)$$

$$+ |S_T|(1 - y) \frac{P_{h\perp}}{z M_h} \sin(\phi_h^l + \phi_S^l) \sum_{q,\bar{q}} e_q^2 h_1^q(x) H_1^{\perp q}(z, P_{h\perp}^2)$$

$$+ |S_T|(1 - y + \frac{1}{2}y^2) \frac{P_{h\perp}}{z M_N} \sin(\phi_h^l - \phi_S^l) \sum_{q,\bar{q}} e_q^2 f_{1T}^{\perp(1)q}(x) D_1^q(z, P_{h\perp}^2)$$

$$+ |S_T|(1 - y) \frac{P_{h\perp}^3}{6z^3 M_N^2 M_h} \sin(3\phi_h^l - \phi_S^l) \sum_{q,\bar{q}} e_q^2 h_{1T}^{\perp(2)q}(x) H_1^{\perp q}(z, P_{h\perp}^2)$$

$$+ \lambda_e |S_L| y (1 - \frac{1}{2}y) \sum_{q,\bar{q}} e_q^2 g_1^q(x) D_1^q(z, P_{h\perp}^2)$$

$$+ \lambda_e |S_T| y (1 - \frac{1}{2}y) \frac{P_{h\perp}}{z M_N} \cos(\phi_h^l - \phi_S^l) \sum_{q,\bar{q}} e_q^2 g_{1T}^{(1)q}(x) D_1^q(z, P_{h\perp}^2)\}$$

Unpolarized

Polarized target

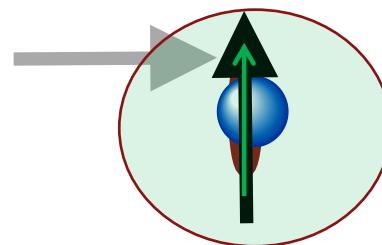
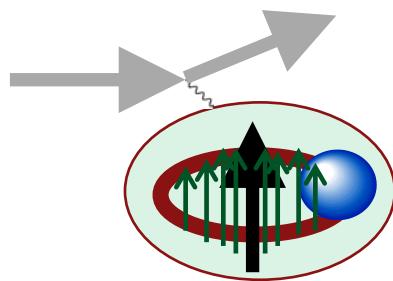
Polarized beam and target

$S_L$  and  $S_T$ : Target Polarizations;  $\lambda e$ : Beam Polarization

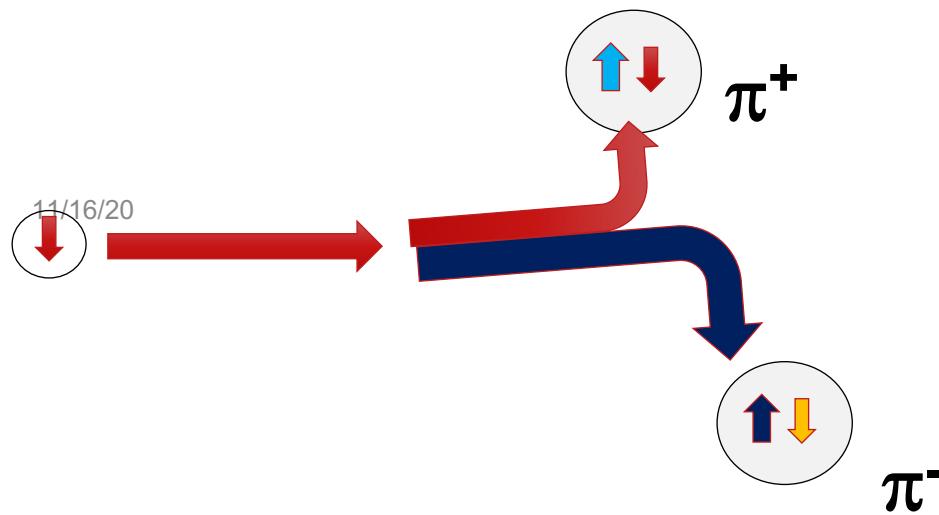
x: momentum fraction carried by struck quark, z: fractional energy of hadron

- TMDs related to the transverse polarization are difficult to access

- 



Need polarization dependent FFs as quark polarimeters



# Fragmentation Functions

## Observables:

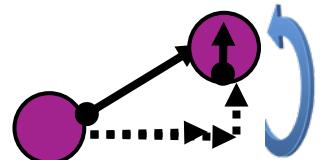
$z$ : fractional energy of the quark carried by the hadron

$p_{h,T}$ : transverse momentum of the hadron wrt the quark direction: **TMD FFs**



| Parton polarization →<br>Hadron Polarization ↓ | Spin averaged   | longitudinal | transverse  |
|--|---|--------------|---|
| spin averaged                                  | $D_1^{h/q}(z, p_T) = \left[ \bullet \rightarrow \text{orange circle} \right]$ |              | $H_1^{\perp h/q}(z, p_T) = \left[ \uparrow \bullet \rightarrow \text{blue circle} \right] - \left[ \downarrow \bullet \rightarrow \text{blue circle} \right]$ |
| longitudinal                                   |   |              |   |
| Transverse (here $\Lambda$ )                   |   |              |   |

# Adding polarization in the final state....



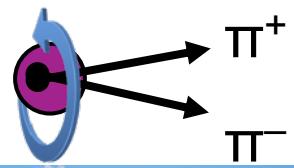
## Observables:

$z$ : fractional energy of the quark carried by the hadron

$p_{h,T}$ : transverse momentum of the hadron wrt the quark direction: **TMD FFs**

| Parton polarization →<br>Hadron Polarization ↓ | Spin averaged  | longitudinal  | transverse  |
|--|--|---|---|
| spin averaged                                  | $D_1^{h/q}(z, p_T) = \left[ \bullet \rightarrow \text{red circle} \right]$                               |   | $H_1^{\perp h/q}(z, p_T) = \left[ \uparrow \rightarrow \text{blue circle} \right] - \left[ \downarrow \rightarrow \text{blue circle} \right]$                           |
| longitudinal                                   |  | $G_1^{h/q}(z, p_T) = \left[ \bullet \rightarrow \text{red circle} \right] - \left[ \bullet \rightarrow \text{red circle} \right]$ |   |
| Transverse (here $\Lambda$ )                   | $D_{1T}^{\perp \Lambda/q}(z, p_T) = \left[ \bullet \rightarrow \text{blue circle with up arrow} \right]$ |   | $H_1^{q/\Lambda}(z, p_T) = \left[ \uparrow \rightarrow \text{red circle with up arrow} \right] - \left[ \downarrow \rightarrow \text{red circle with up arrow} \right]$ |

- Theoretically many more, in particular with polarized hadrons in the final state and transverse momentum dependence → similar to PDFs encoding spin/orbit correlations
- Determining final state polarization needs self analyzing decay ( $\Lambda$ )
- Gluon FFs similar but with circular/linear polarization (not as relevant for  $e^+e^-$ )



## DI-HADRON FRAGMENTATION FUNCTIONS

Additional Observable:

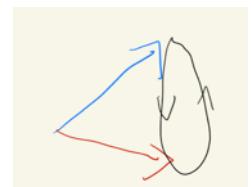
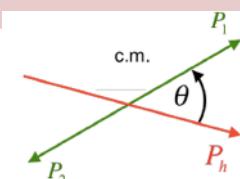
$$\vec{R} = \vec{P}_1 - \vec{P}_2 :$$

The relative momentum of the hadron pair is an additional degree of freedom:

*the orientation of the two hadrons w.r.t. each other and the jet direction can be an indicator of the quark transverse spin*

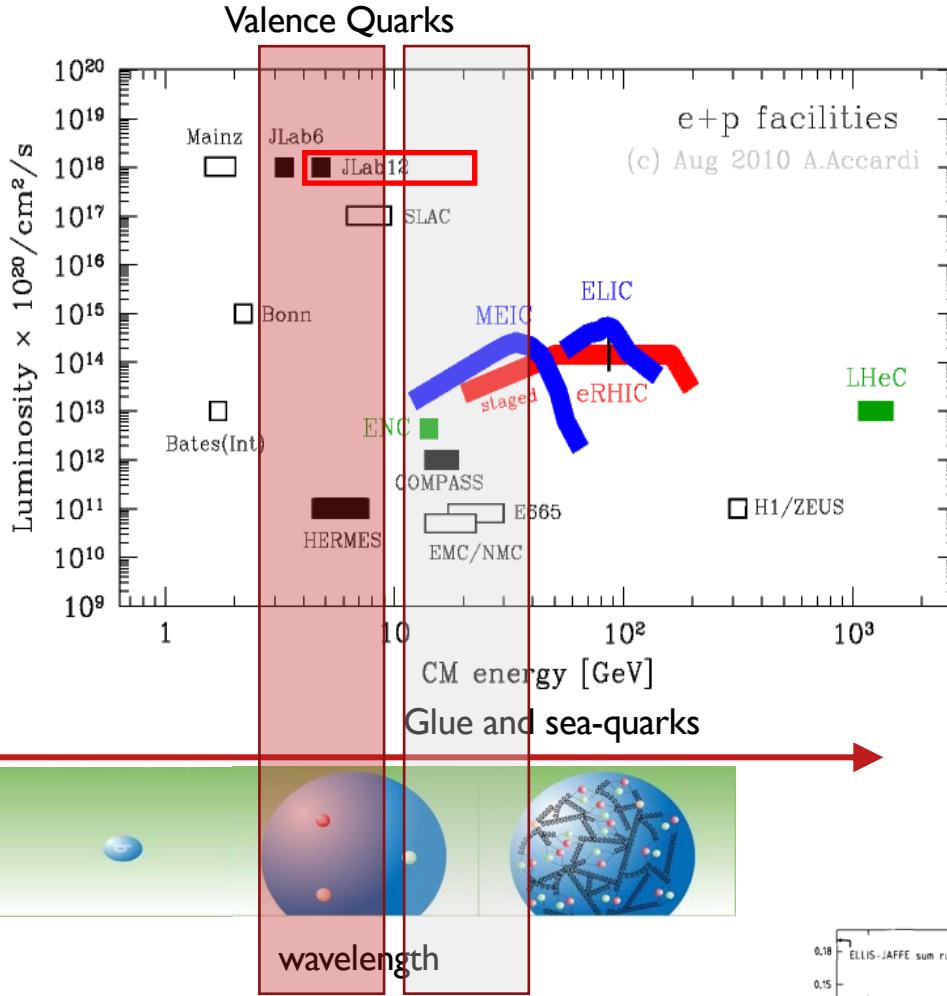


| Parton polarization →<br>Hadron Polarization ↓         | Spin averaged         | longitudinal   | transverse   |
|--|-----------------------|--|--|
| spin averaged  | $D_1^{h/q}(z, M)$<br> |  | $H_1^{\perp h/q}(z, p_T \mathbf{M}, (\mathbf{Ph}), \theta)$ 'Di-hadron Collins'                      |
| Needs Interference with j<br>Longitudinal OAM          |                       |  |  |
| Needs Interference with<br>Transverse OAM<br>component | Type equation here.   | $\mathbf{G}_1^\perp(z, \mathbf{M}, \mathbf{P}_h, \theta) =$<br>T-odd, chiral-even<br>→jet handedness<br>QCD vacuum structure | $\mathbf{H}_1^\perp(z, \mathbf{M}, (\mathbf{P}_h), \theta) =$ .<br>T-odd, chiral-odd<br>Colinear<br> |

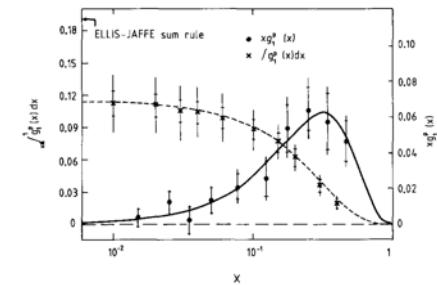


- Relative momentum of hadrons can carry away angular momentum
  - Partial wave decomposition in  $\theta \rightarrow$   
**Needs to be mapped completely!! (no information yet)**
    - Energy dependence? ( $\rightarrow$  VM fractions....)
  - Relative and total angular momentum  $\rightarrow$  In principle endless tower of FFs

# Comparison to Previous and Planned Facilities



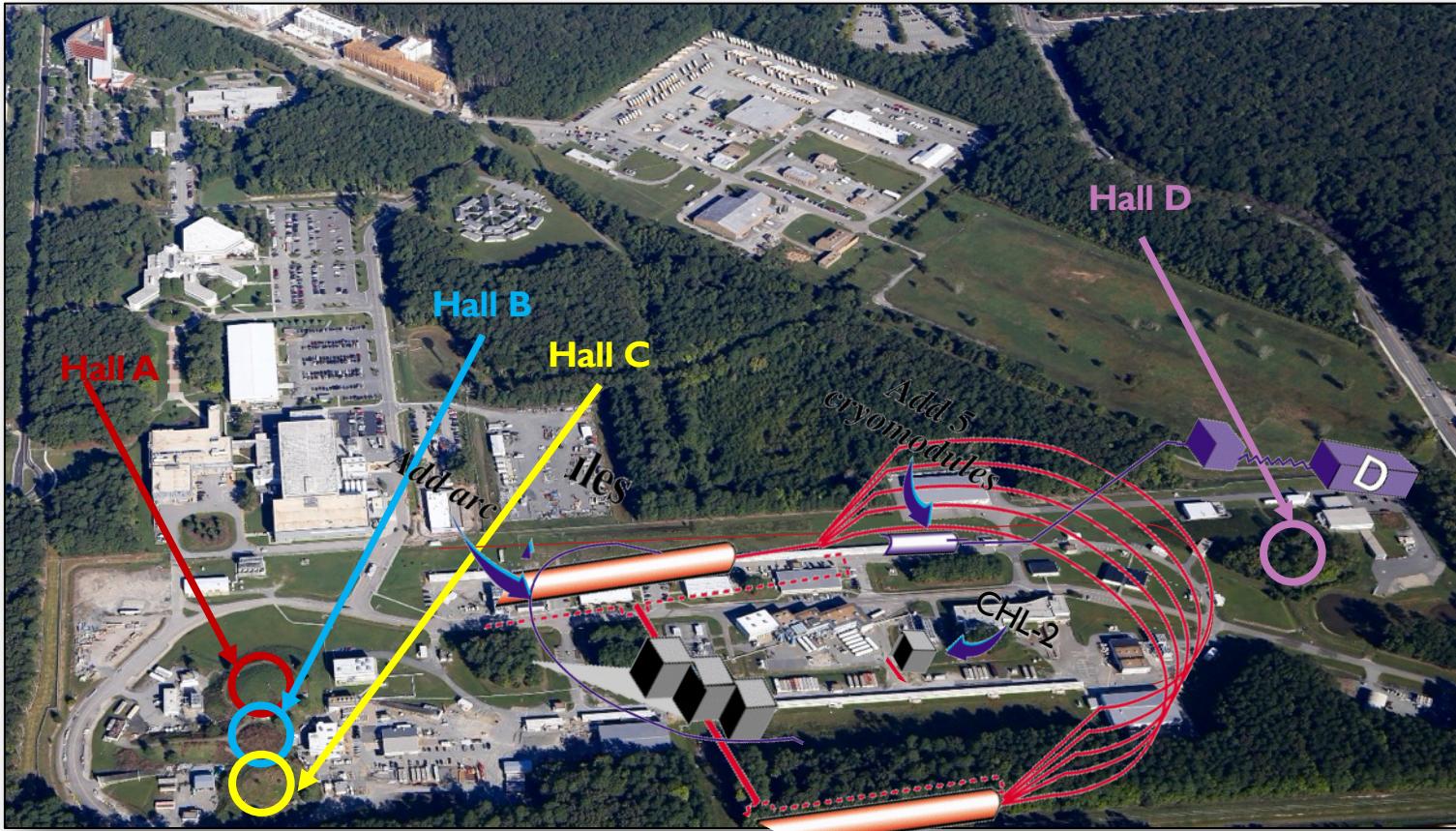
- naïve constituent model and experimental results:  
Valence region important for nucleon spin properties
- **To extract 3D structure: Need luminosity**



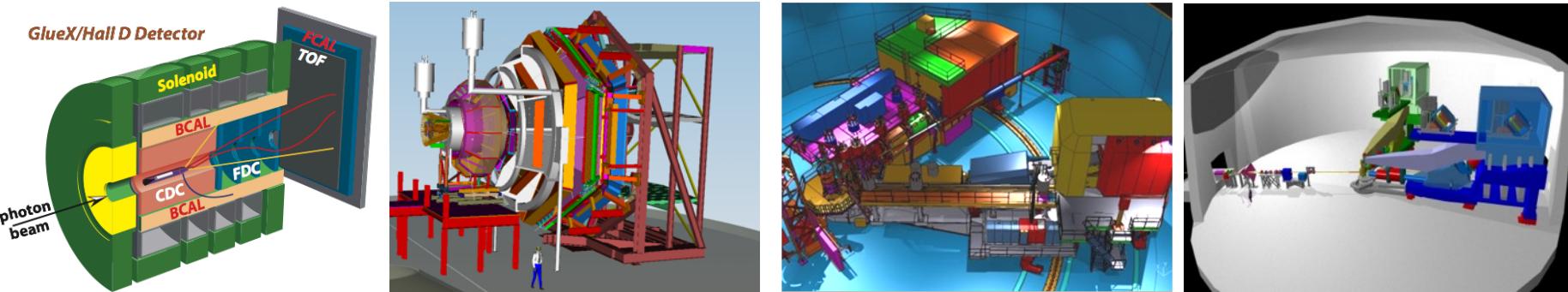
# Jefferson Lab



# Jefferson Lab with CEBAF at 12 GeV

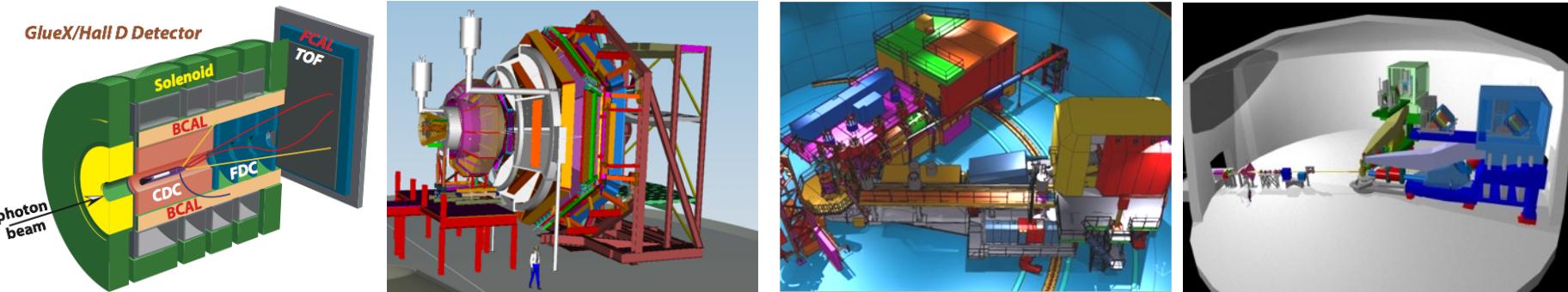


# Detector Requirements: Complementarity



| Hall D                                   | Hall B               | Hall C                        | Hall A               |
|--|----------------------|-------------------------------|----------------------|
| excellent hermeticity                    | luminosity $10^{35}$ | energy reach                  | custom installations |
| polarized photons                        | hermeticity          | precision                     |                      |
| $E_\gamma \sim 8.5\text{-}9 \text{ GeV}$ |                      | 11 GeV beamline               |                      |
| $10^8$ photons/s                         |                      | target flexibility            |                      |
| good momentum/angle resolution           |                      | excellent momentum resolution |                      |
| high multiplicity reconstruction         |                      | luminosity up to $10^{38}$    |                      |
|  |                      | particle ID                   |                      |

# Detector Requirements: Complementarity



| Hall D                                   | Hall B               | Hall C                     | Hall A               |
|--|----------------------|----------------------------|----------------------|
| excellent hermeticity                    | luminosity $10^{35}$ | energy reach               | custom installations |
| polarized photons                        | hermeticity          | precision                  |                      |
| $E_\gamma \sim 8.5\text{-}9 \text{ GeV}$ |                      | 11 GeV beamline            |                      |
| $10^8 \text{ photons/s}$                 |                      | target flexibility         |                      |
| good momentum/angle resolution           |                      | excellent moment           |                      |
| high multiplicity reconstruction         |                      | luminosity up to $10^{38}$ |                      |
| particle ID                              |                      |                            |                      |



# Tentative Timelines relevant for TMD program shown here

## CLAS12 in Hall B

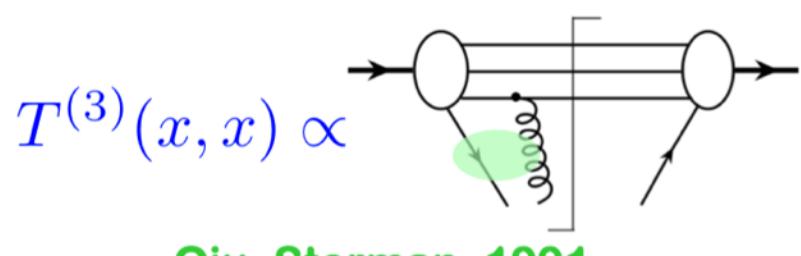
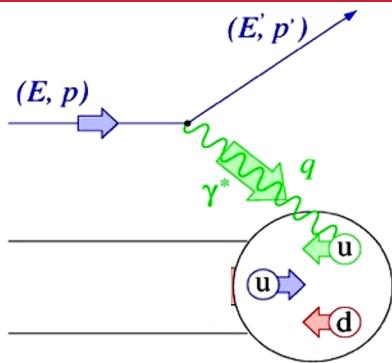
- 2018-2020: unpolarized proton/deuterium target – long. polarized beam  
→ Results shown here correspond to 15% of approved p-Data (120/90 beam days)
- FY22 polarized long target?
- Polarized He3 (long/trans)
- Polarized transverse HD

## Hall A

- 2023 Transverse single spin asymmetries on He3 (64 beam days)
- 2028 SoLID with He3/proton target (long/transverse)



# $F_{LU}$ is sensitive to $e(x)$



Qiu, Sterman, 1991, ...

- Twist-3 encode quark-gluon correlations
- Collinear twist-3  $e(x), h_L(x), g_T(x)$
- $e(x)$  can be interpreted as transverse force on transversely polarized quarks by the gluon field after being struck

# Accessing $e(x)$ in di- and single hadron $F_{LU}$

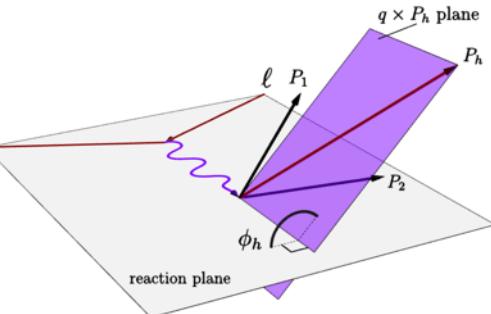
- Di-hadrons: extra degree of freedom of di-hadron FFs allow more targeted access

$$F_{LU}^{\sin \phi_R} = -x \frac{|\vec{R}| \sin \theta}{Q} \left[ \frac{M}{M_{\pi\pi}} x e^q(x) H_1^{\triangleleft q}(z, \cos \theta, M_{\pi\pi}) + \frac{1}{z} f_1^q(x) \tilde{G}(z, \cos \theta, M_{\pi\pi}) \right]$$

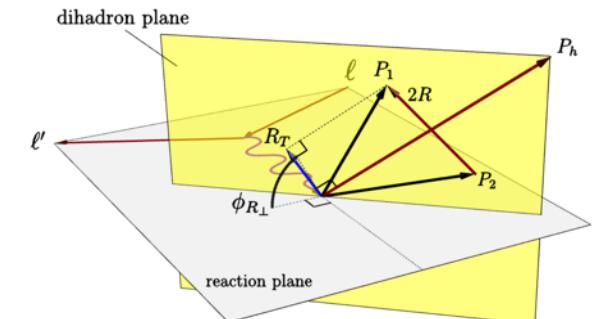
- In single hadrons: Complicated combination of four terms in the structure function.
- TMD factorization at twist-3 not yet proven!

$$F_{LU}^{\sin \phi_h} = \frac{2M}{Q} \mathcal{C} \left[ -\frac{\hat{h} \cdot k_T}{M_h} \left( x e [H_1^\perp] + \frac{M_h}{M} f_1 [\tilde{G}^\perp] \right) + \frac{\hat{h} \cdot p_T}{M} \left( x g^\perp [D_1] + \frac{M_h}{M} h_1^\perp [\tilde{E}] \right) \right]$$

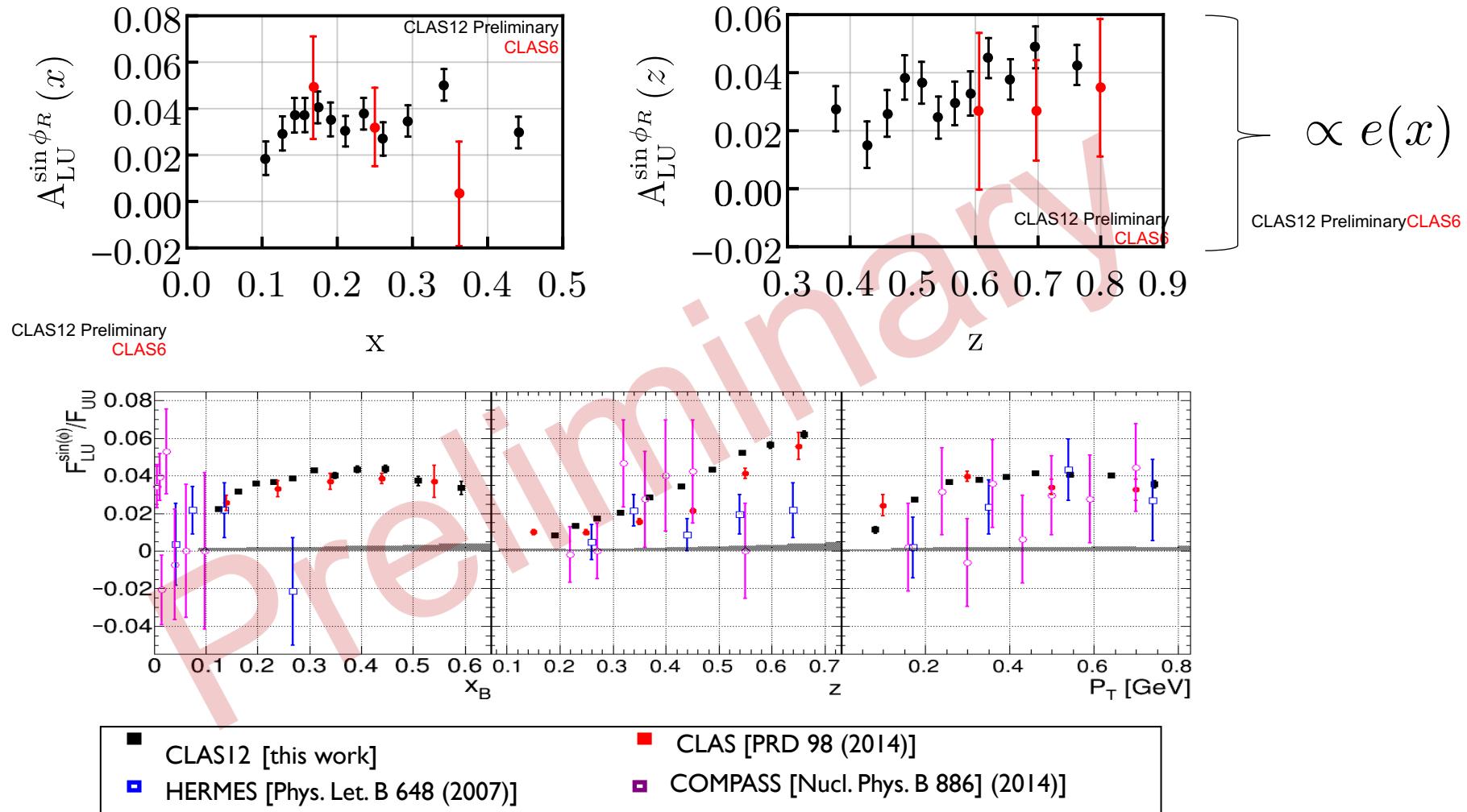
twist-3 pdf      Collins FF      unpolarized PDF      twist-3 FF  
 twist-3 t-odd PDF      unpolarized FF      Boer-Mulders      twist-3 FF



$$\begin{aligned} \vec{P}_h &= \vec{P}_\pi^+ + \vec{P}_\pi^-, \\ 2\vec{R} &= \vec{P}_\pi^+ - \vec{P}_\pi^- \end{aligned}$$

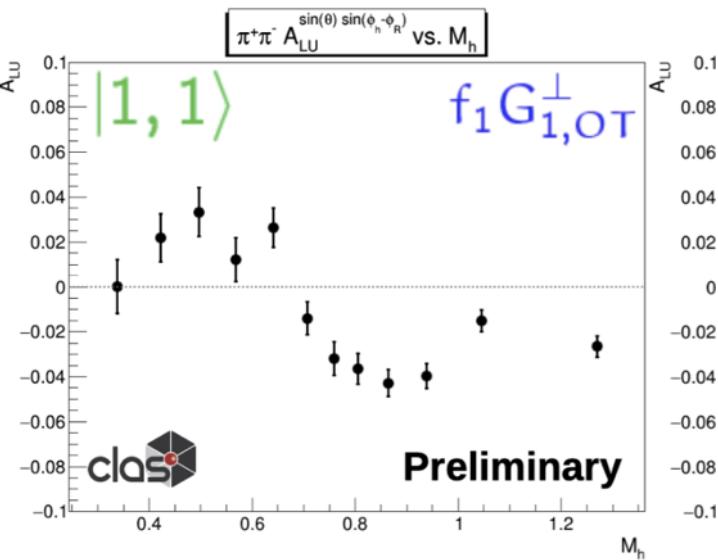
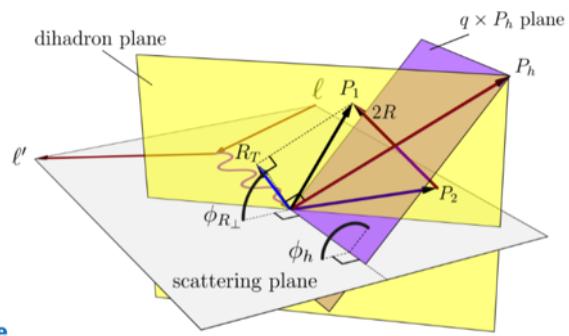
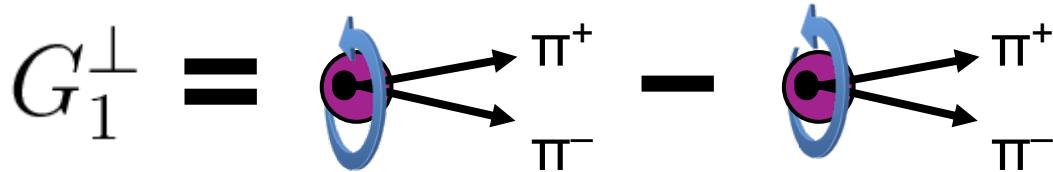


# $\sin(\phi_R)$ modulations



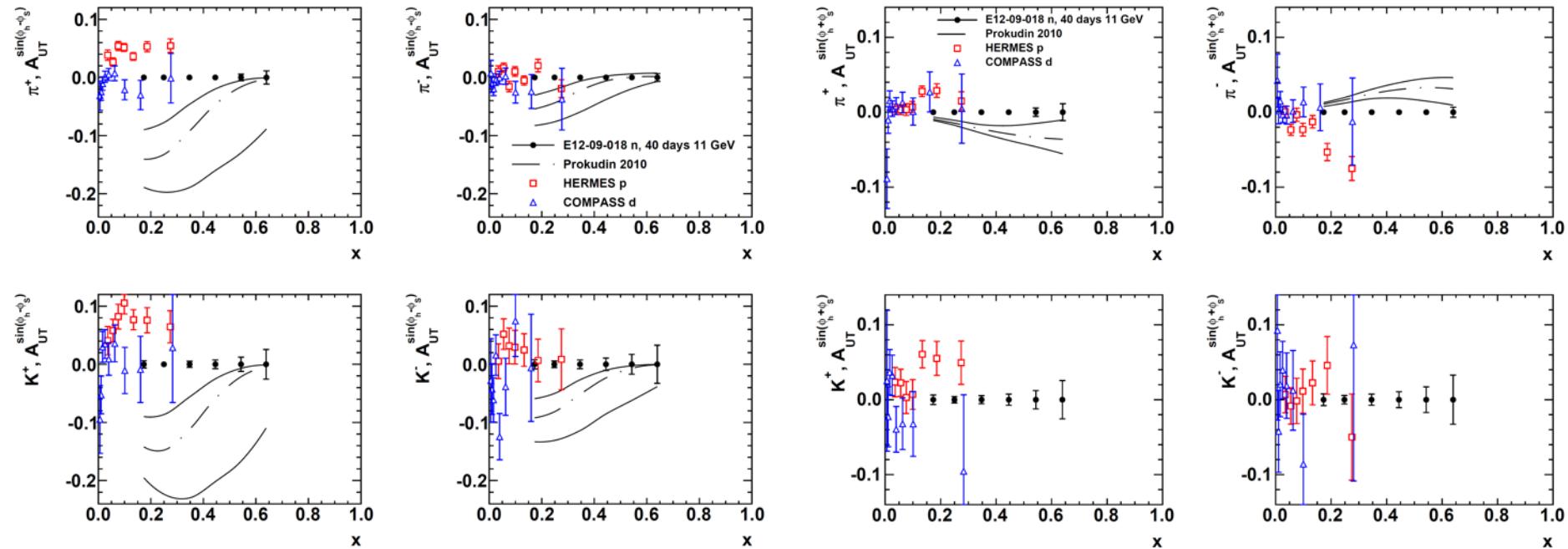
**Focus of this CLAS12 study:** A multidimensional study in  $Q^2$ ,  $x_B$ ,  $z$  and  $P_T$

# Wormgear FF $G_1^\perp$



- If we allow for transverse momentum, enters cross-section at leading twist
- $\sigma_{LU} \propto \sin(\phi_h - \phi_R) f(x) G_1^\perp(z)$
- First measurement!
- See talk by Christopher Dilks

# SBS+BB Projected Results: Collins and Sivers SSAs

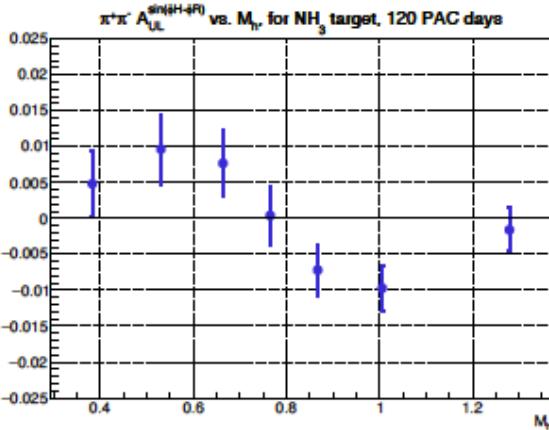


**Projected  $A_{UT}^{Sivers}$  vs.  $x$  (11 GeV data only)**

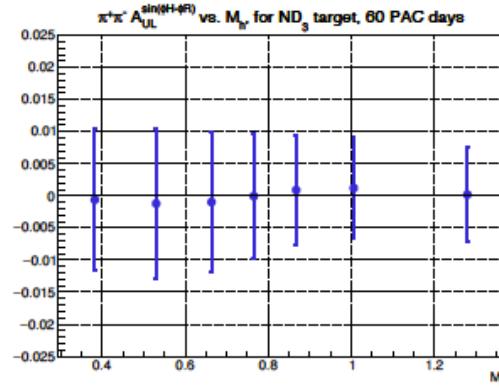
**Projected  $A_{UT}^{Collins}$  vs.  $x$  (11 GeV data only)**

- E12-09-018 will achieve statistical FOM for the neutron  $\sim 100X$  better than HERMES proton data and  $\sim 1000X$  better than Hall A E06-010 neutron data. *Near-future more precise COMPASS deuteron data will sharpen expected impacts, urgency of E12-09-018*
- SBS installation starts 2020. E12-09-018 could run as early as 2022; 2023 more likely.

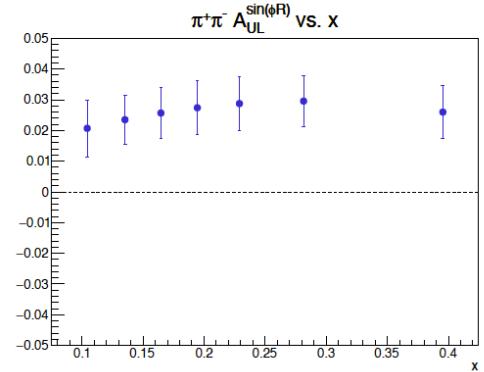
# Future running with polarized targets



$A_{UL}$  projections sensitive to  $G_1^\perp$  for 120 PAC days on  $NH_3$



$A_{UL}$  projections sensitive to  $G_1^\perp$  for 60 PAC days on  $ND_3$



$A_{UL}$  projections sensitive to  $h_L$  for 30 PAC days on  $He_3$

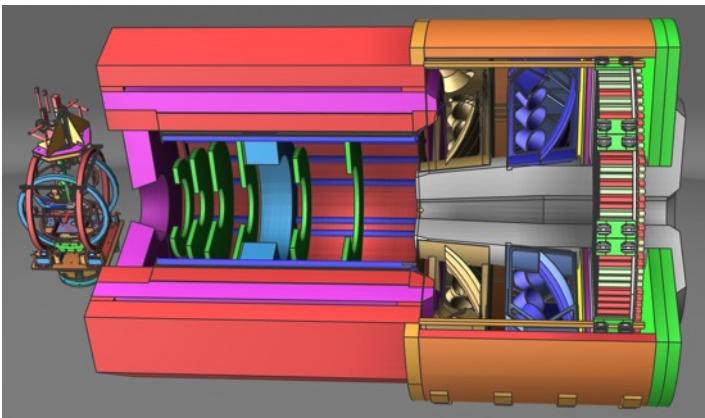
| Target | Dilution $f$ | Polarization $P$ |
|--------|--------------|------------------|
| $NH_3$ | 0.2          | 0.85             |
| $ND_3$ | 0.285        | 0.35             |

- $He_3$ : 50% polarization, 0.27 dilution
- Compared to Hall A: Can do di-hadrons and easier access to transverse momentum dependence
- Statistics in Hall A likely better

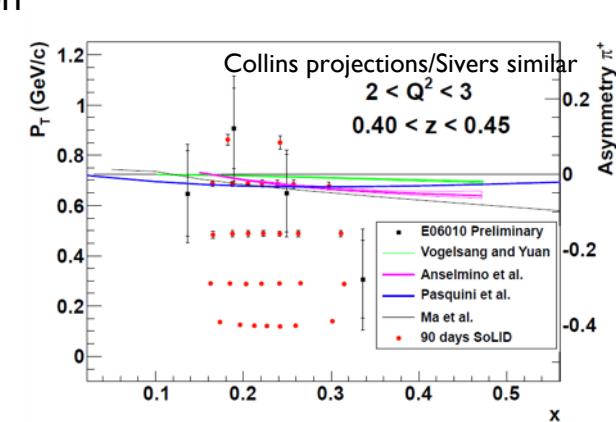
# Nucleon momentum tomography and confined motion

## Polarized $^3\text{He}$ ("neutron") @ SoLID

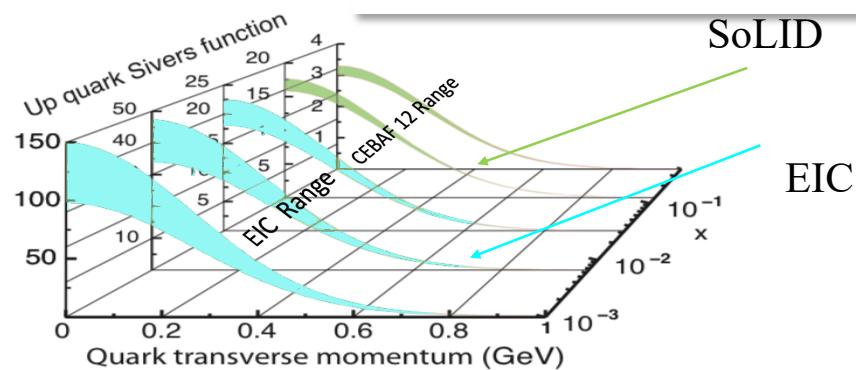
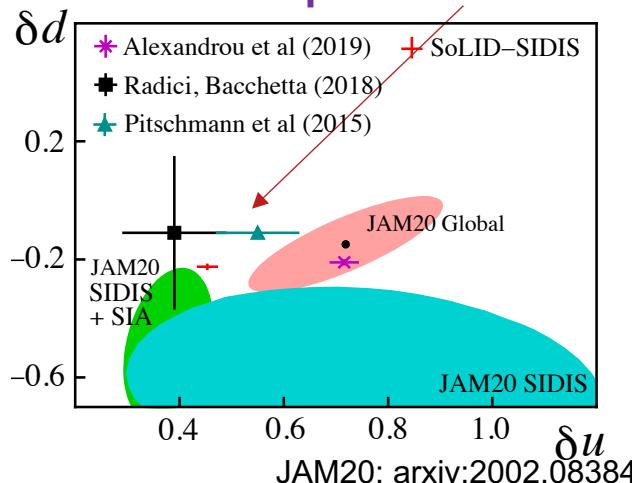
SoLID provides **unique** capability combining **high luminosity** ( $10^{37-39} \text{ /cm}^2/\text{s}$ ) (>100 of CLAS12; >1000 times of EIC) and **large acceptance** with full  $\phi$  coverage to maximize the science return of the 12-GeV CEBAF upgrade



- Sivers: an example of TMDs
- Confined quark motion inside nucleon
- Quantum correlations between nucleon spin and quark motion
- QCD dynamics



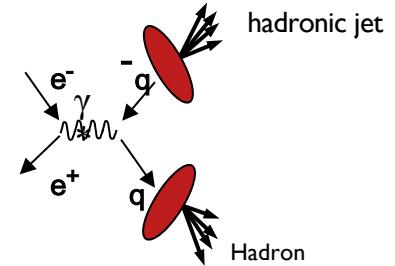
## SoLID impact on tensor charge



- Tensor charge: a fundamental QCD quantity to test lattice QCD
- Probe new physics combined with EDMs

# Access of FFs for light mesons in $e^+e^-$ (spin averaged case)

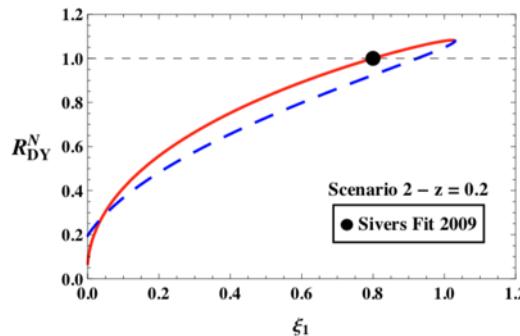
$$\frac{1}{\sigma_{\text{tot}}} \frac{d\sigma^{e^+e^- \rightarrow hX}}{dz} := \frac{1}{\sum_q e_q^2} (2F_1^h(z, Q^2) + F_L^h(z, Q^2)),$$



$$2F_1^h(z, Q^2) = \sum_q e_q^2 \left( D_1^{h/q}(z, Q^2) + \frac{\alpha_s(Q^2)}{2\pi} \left( C_1^q \otimes D_1^{h/q} + C_1^g \otimes D_1^{h/g} \right)(z, Q^2) \right)$$

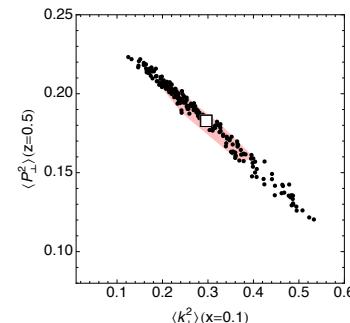
- Cleanest process → testbed for QCD calculations

- SIDIS necessary to extract flavor dependence of FFs  
but cannot disentangle source of pT

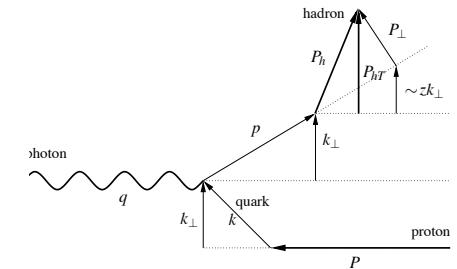


variation in Sivers effect varying  $\xi = \frac{k_T}{p_T}$

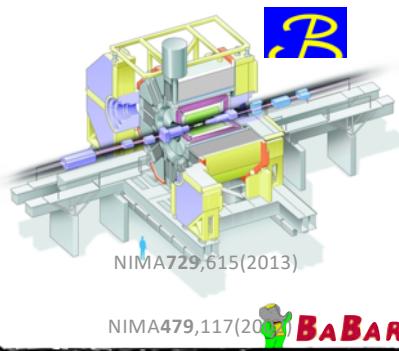
Phys. Rev. D98 (2018) no.9, 094023



JHEP 1311 (2013) 194

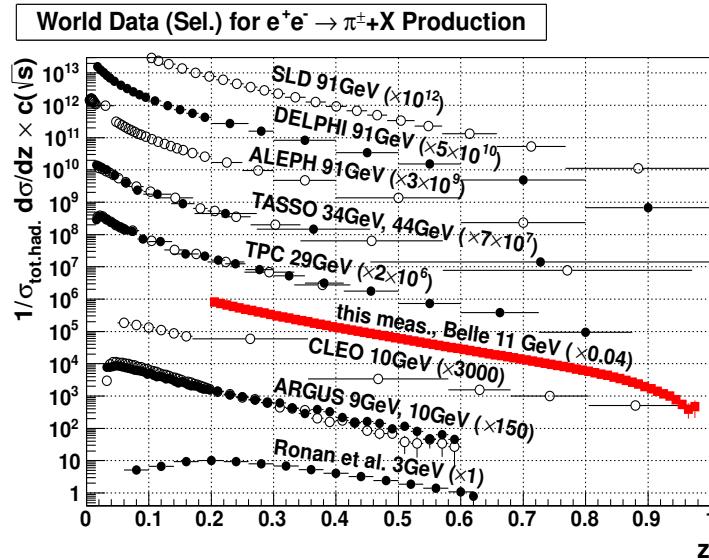
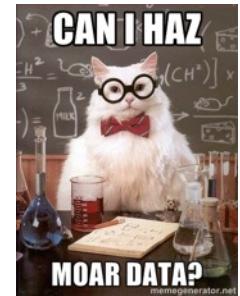


- Asymmetric-energy  $e^+e^-$  collider
- $\sqrt{s} \sim 10.6$  GeV ( $\Upsilon(4S)$ )
- $\beta\gamma=0.425$
- $L \sim 1 \text{ ab}^{-1}$



- Asymmetric-energy  $e^+e^-$  collider
- $\sqrt{s} \sim 10.6$  GeV ( $\Upsilon(4S)$ )
- $\beta\gamma=0.65$
- $L \sim 500 \text{ fb}^{-1}$

# Role of b-factories



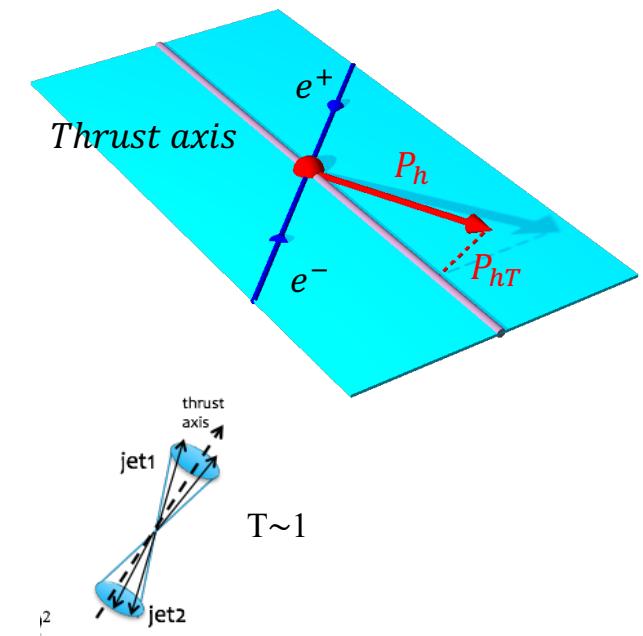
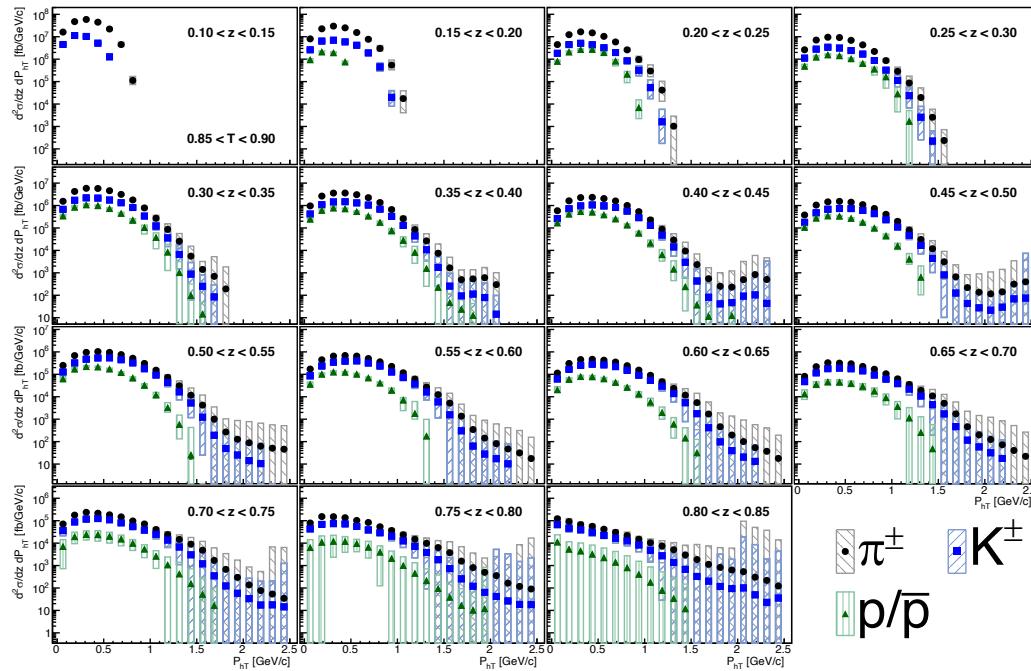
Phys.Rev.Lett. 111 (2013) 062002 (Belle)  
Phys.Rev. D88 (2013) 032011 (BaBar)

- Dominated by B factories
- Limited lever arm in  $\sqrt{s}$  in particular at high  $z$
- Precision data includes charged single hadrons  $\pi$ ,  $K$ ,  $p$ ,  $D$ ,  $\Lambda$ , charmed baryons...
- Well described at NNLO (e.g. DSS, NNFF)

# New: $P_T$ dependence

## Seidl et al, Phys.Rev. D99 (2019) no.11, 112006

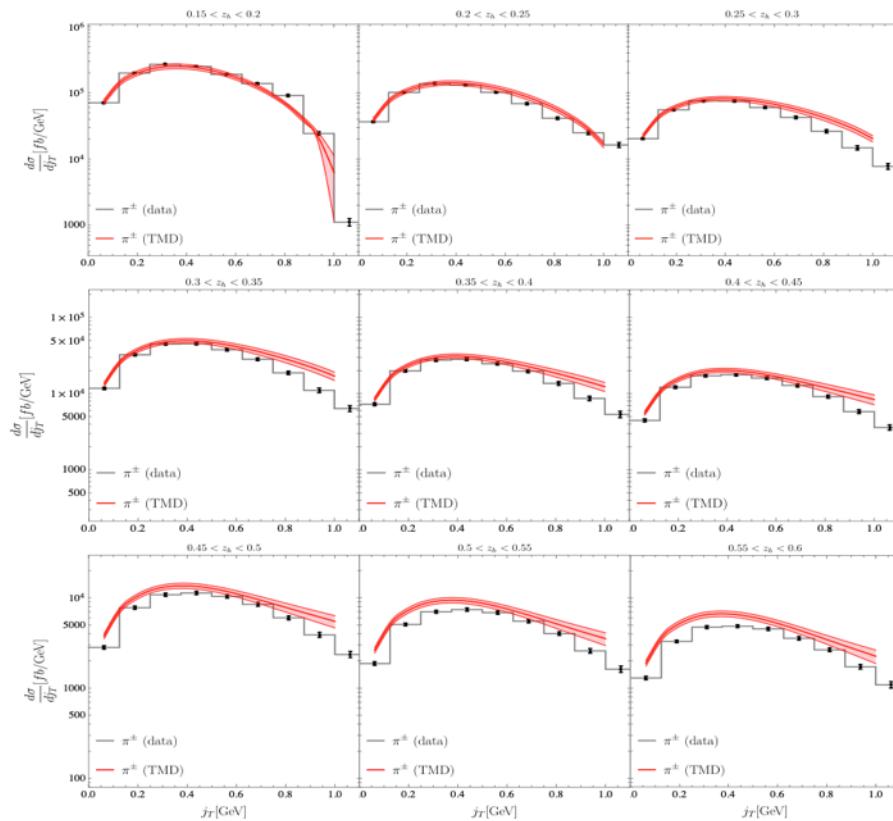
- Quasi inclusive hadron production gives access to transverse momentum in fragmentation
- **Transverse momentum measured with respect to thrust axis**



- $0.85 < \text{Thrust } T < 0.9$ 
  - Transverse momenta mostly Gaussian
  - Possible deviations for large  $P_{hT}$  tails, but also large uncertainties

# Theory description of $p_T$ vs thrust made progress

- Factorization and resummation derived



From Kang, Shao, Zhao  
e-Print: [2007.14425](#) [hep-ph]

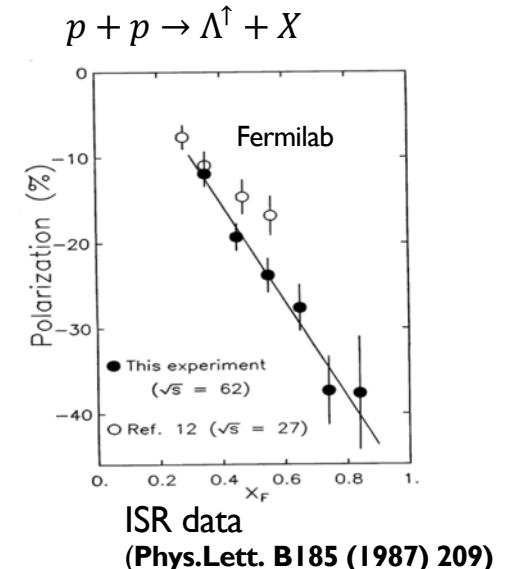
See also Boglione, Simonelli e-Print: [2007.13674](#) [hep-ph]  
Makris, Ringer, Waalewijn [2009.11871](#) [hep-ph]

# Polarized Hyperon Production

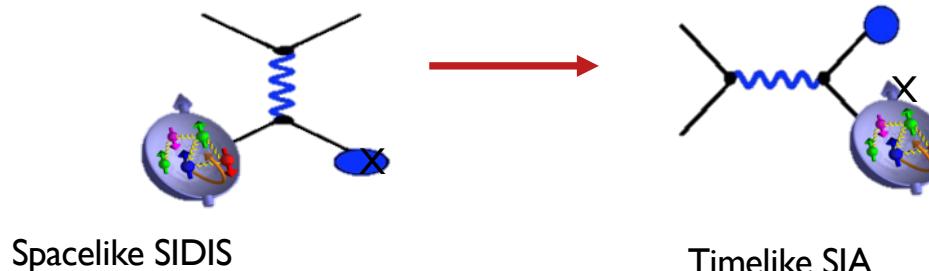
PRL36, 1113 (1976); PRL41, 607 (1978)

- Large  $\Lambda$  transverse polarization in unpolarized pp collision
- Caused by polarizing FF  $D_{1T}^\perp(z, p_\perp^2)$ ?
- Polarizing FF is chiral-even, has been proposed as a test of universality
- OPAL experiment at LEP has studied transverse  $\Lambda$  polarization, no signal observed.  
Eur. Phys. J. C2, 49 (1998)
- $\Lambda^\uparrow$  production counterpart of the Sivers function.

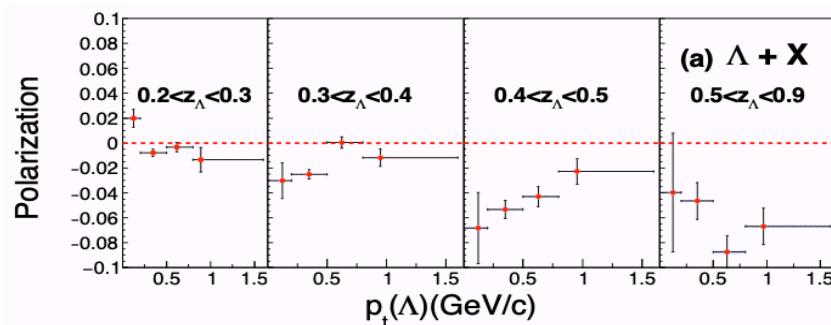
PRL105, 202001 (2010)



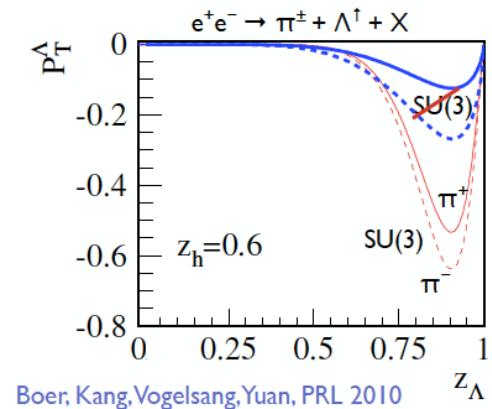
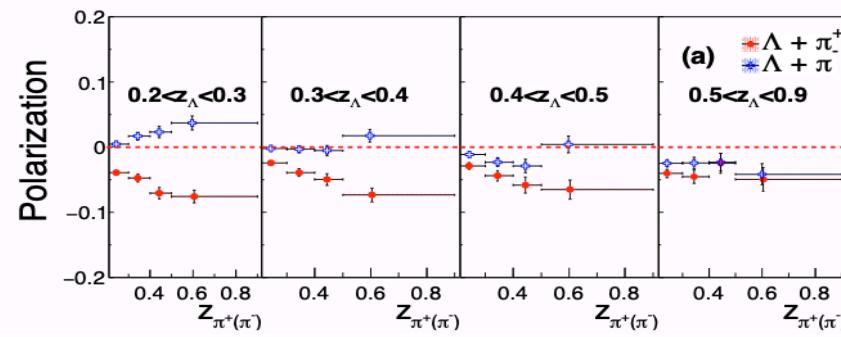
$$x_F = p_L / \max p_L \sim_{LO} x_1 - x_2 \sim_{forward} x_1$$



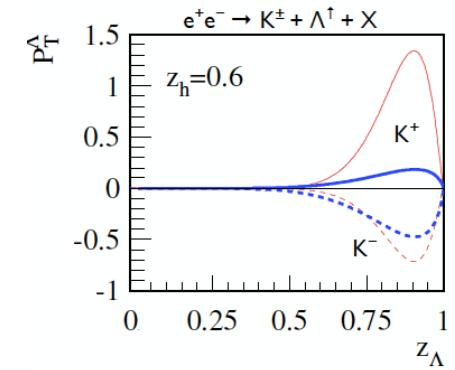
# $z_\Lambda, p_T$ Dependence of observed $\Lambda$ polarization



Y. Guan, Phys.Rev.Lett. 122 (2019) 4, 042001

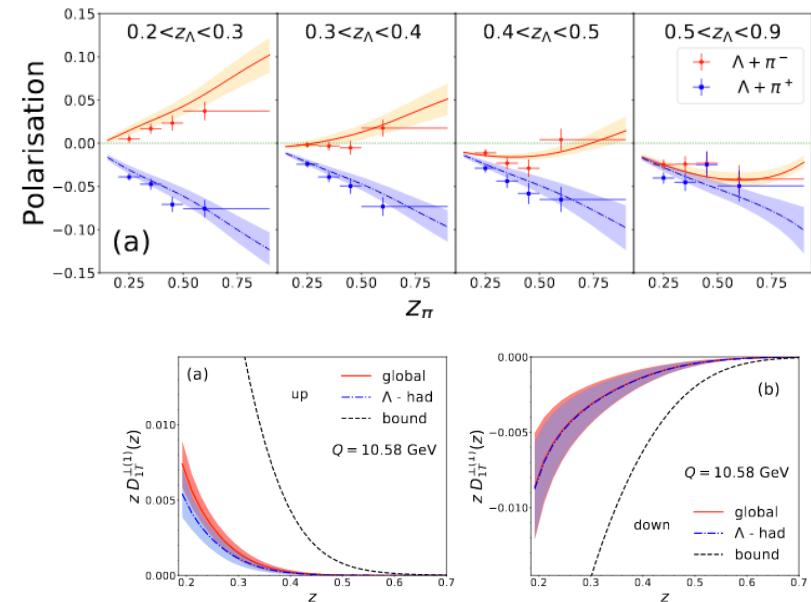
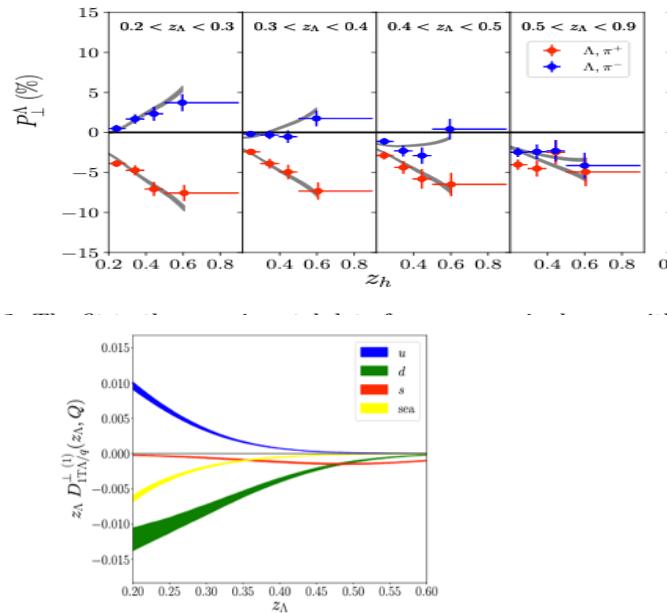


Boer, Kang, Vogelsang, Yuan, PRL 2010

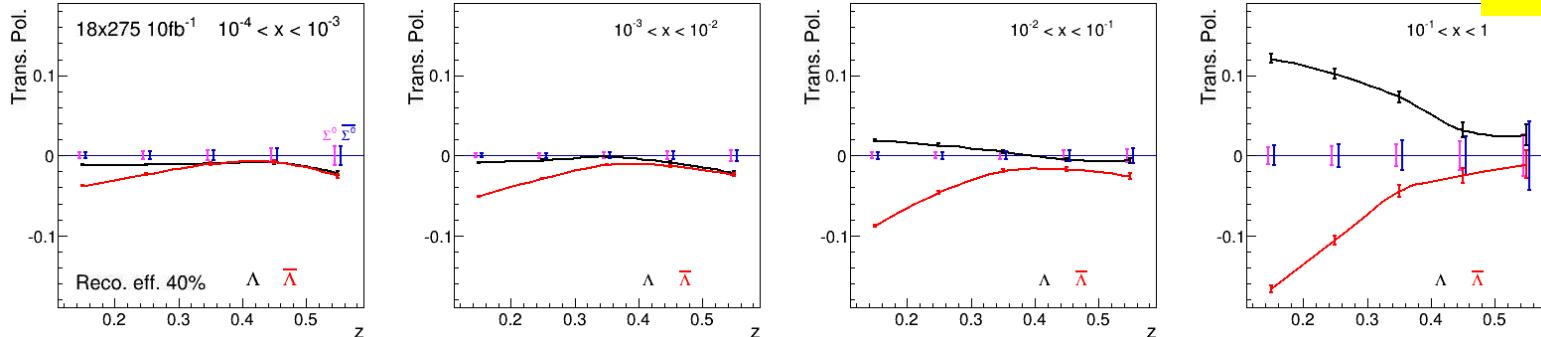


- Polarization rises with  $p_t$  in the lowest  $z_\Lambda$  and highest  $z_\Lambda$  bin. But the dependence reverses around 1 GeV in the intermediate  $z_\Lambda$  bins → **Unexpected!** (might be related to fragmenting quark flavor dependence on  $z_1, z_2$ )
- Correlation with opposite hemisphere light meson → quark flav/charge dependence

# Extraction of Lambda FF from Belle data

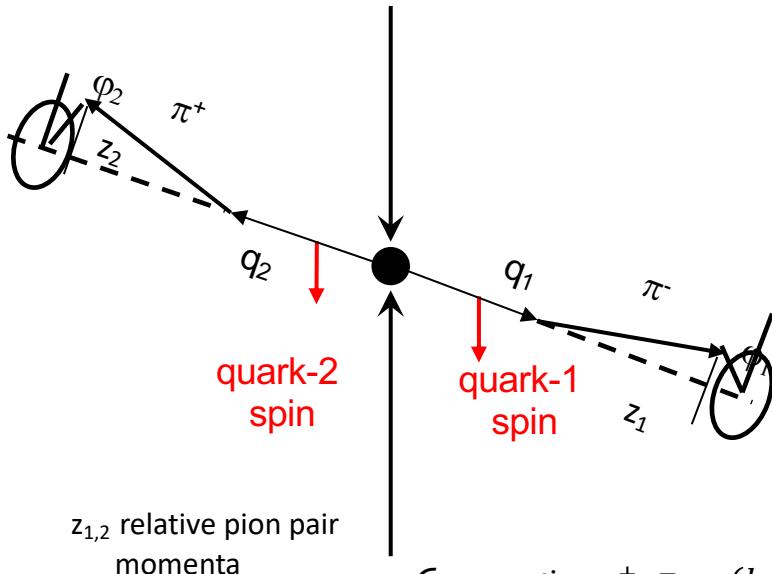


Callos, Kang, Terry, 2003.04828 [hep-ph], (left) D'Alesio, Murgia, Zaccheddu, Phys.Rev.D 102 (2020) 5, 054001 (right)



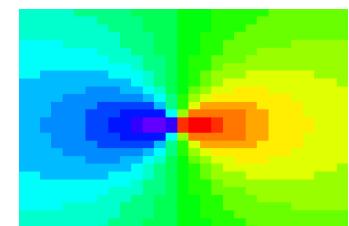
$\Lambda^\uparrow$  at the EIC

# Collins FFs in $e^+e^-$



- First non-zero independent measurement of the Collins effect for pion pairs in  $e^+e^-$  annihilation by Belle Collaboration @  $\sqrt{s} \sim 10.6$  GeV (PRL 111,062002(2008), PRD 88,032011(2013)) leads to first extraction of transversity (Phys.Rev. D75 (2007) 054032 ) from SIDIS and  $e^+e^-$ 
  - Confirmed by BaBar @  $\sqrt{s} \sim 10.6$  GeV (PRD 90,052003 (2014); PRD 92,111101(R)(2015) for KK and  $K\pi$ )
  - Measured at BESIII @  $\sqrt{s} = 3.65$  GeV (PRL 116,42001(2016))

$$\begin{aligned} \text{Cross-section } & e^+e^- \rightarrow (h_1 h_2)(\bar{h}_1 \bar{h}_2) + X \\ & \propto D_1^\perp \bar{D}_1^\perp + H_1^\perp \bar{H}_1^\perp \cos(\phi_1 + \phi_2) \end{aligned}$$



- Access spin dependence and  $p_T$  dependence (convolution or in jet) without PDF complication
- Made possible by B-factory luminosities

# New $P_t$ dependence from Belle

- Trend consistent with BaBar
- Direct comparison difficult due to different correction schemes (thrust vs  $q\bar{q}$  –axis)

**Unlike/Likesign**

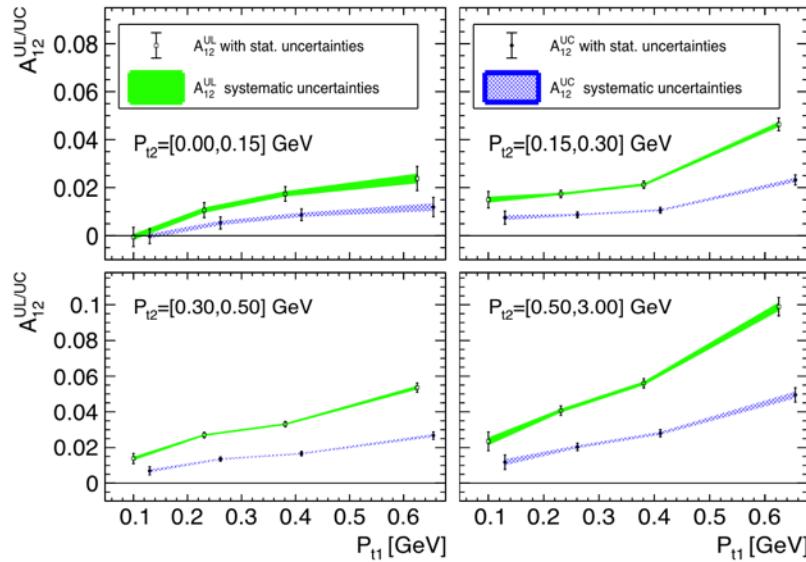
Ratios to cancel acceptance effects

Unlike:

$\text{fav}^*\text{fav} + \text{dis}^*\text{dis}$

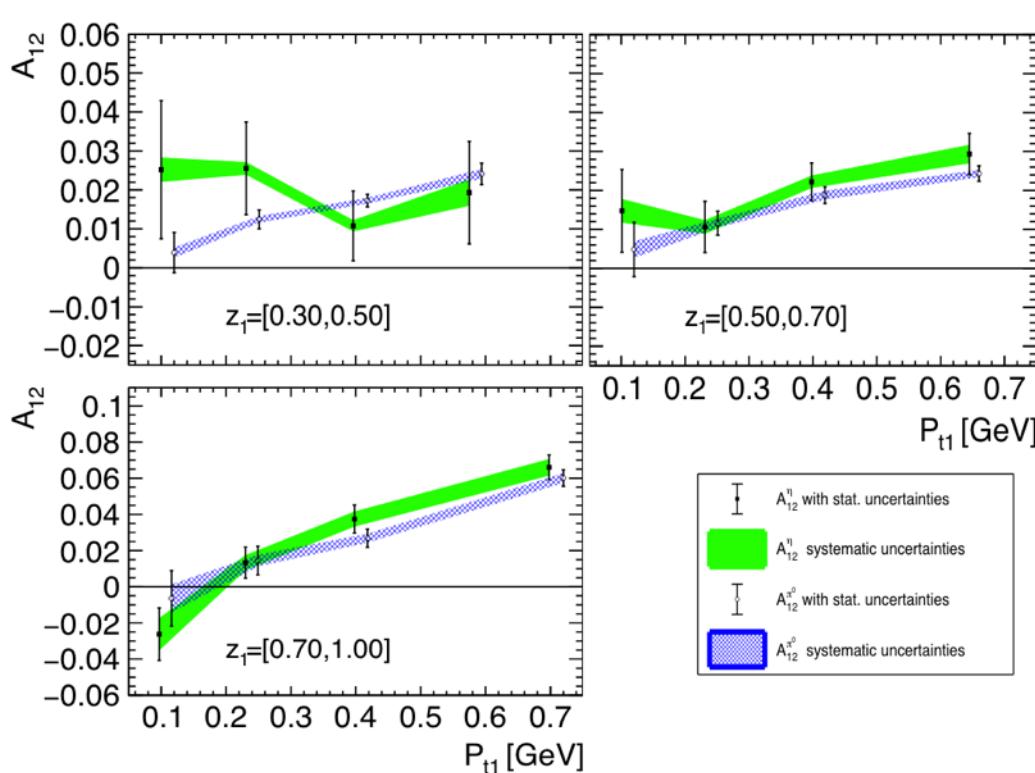
Like:

$\text{fav}^*\text{dis}$



# New $\pi^0/\eta$ from Belle

- Rise with  $z_{1,2}$ , similar to charged pions

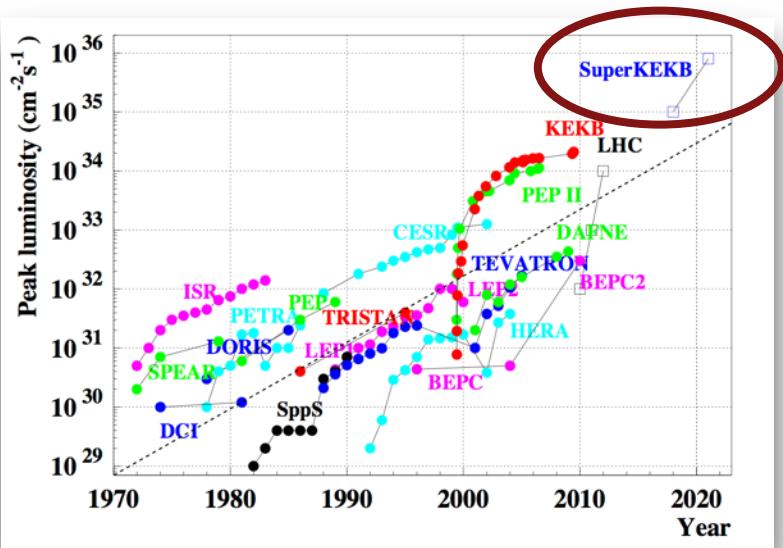


$$\mathcal{R}_{12}^{\pi^0} = \frac{R_{12}^{0\pm}}{R_{12}^L} = \frac{\pi^0\pi^+ + \pi^0\pi^-}{\pi^+\pi^+ + \pi^-\pi^-}$$

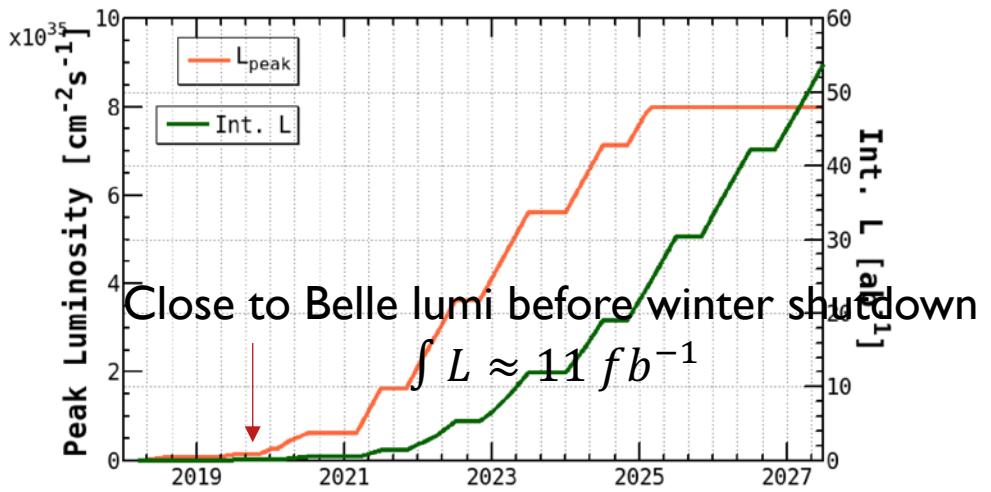
$$\mathcal{R}_{12}^\eta = \frac{R_{12}^{\eta\pm}}{R_{12}^L} = \frac{\eta\pi^+ + \eta\pi^-}{\pi^+\pi^+ + \pi^-\pi^-}$$

# The future is now: Next Generation B factory SuperKEKB

- 



Belle/KEKB recorded  $\sim 1000 \text{ fb}^{-1}$ . Now have to change units on the y-axis to  $\text{ab}^{-1}$

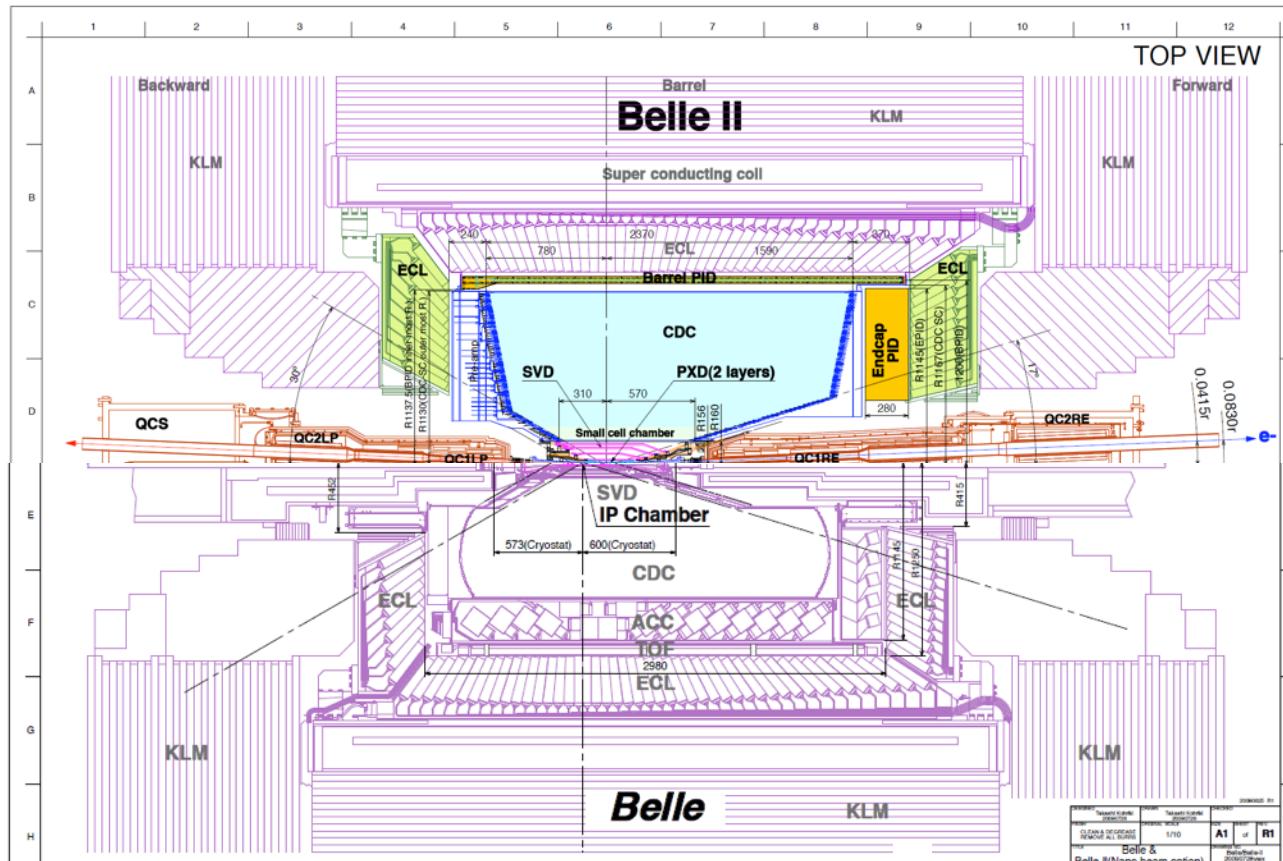


Beam currents *only* a factor of two higher than KEKB ( $\sim$ PEPII)

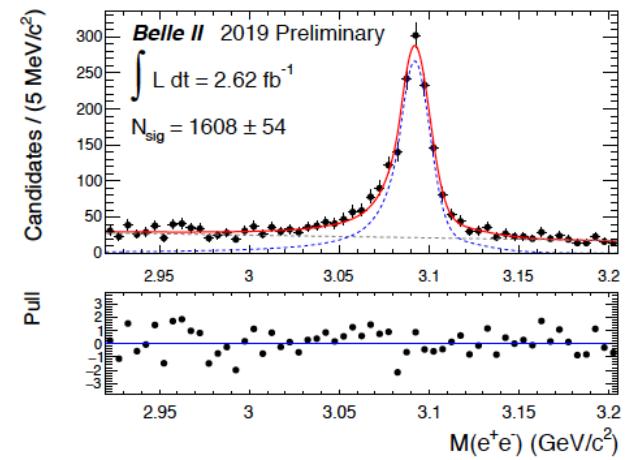
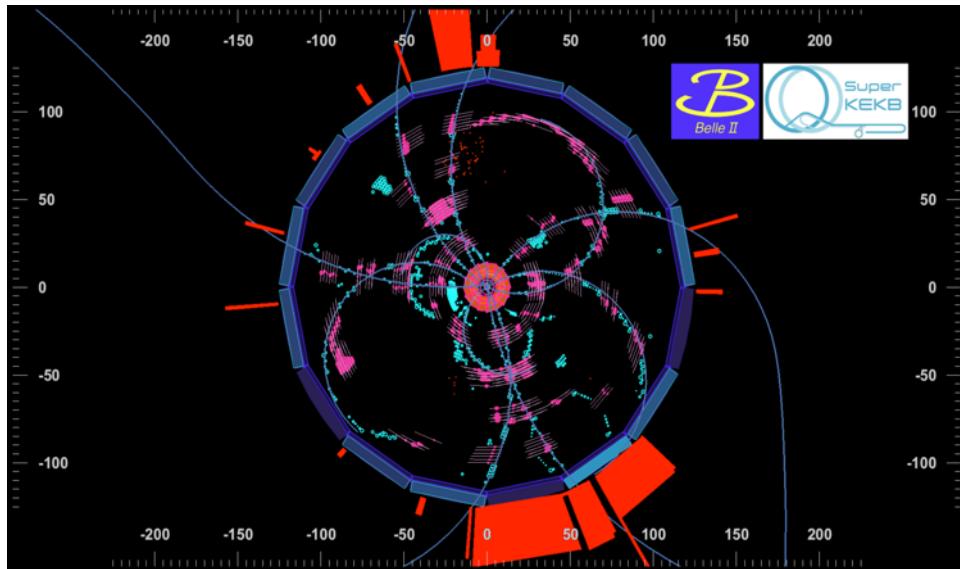
“nano-beams” are the key; vertical beam size is **50nm** at the IP

- $\int L$  needed to map out fully differential  $d\sigma$  of polarized FF
  - $\theta$ , flavor dependence for di-hadrons
  - $p_T, z, z_{\pi, K}$  for  $\Lambda$  (also correction for feed-down needs statistics)
  - Kaon single hadrons

# Belle II Detector (comp. to Belle)



## 2019: First Collisions in Phase 3, the Physics Run



Clear signals for  $B \rightarrow J/\psi X$  in  $\sim 1/2$  of Phase 3 data.

# Conclusion

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- Jlab has rich program in TMD physics, 3D nucleon Femtography in general
  - Near term: CLAS12 has first exciting results available
  - Medium term: Hall A/SoLID will provide unparalleled precision
- 
- Belle/Belle II has rich program to study hadronization
  - Results crucial ingredient to extract transverse momentum dependence/flavor dependence of TMDs from single/di-hadron channels
  - Lambda production in  $e^+e^-$  provides complimentary tests of QCD