

# Nucleon (Spin) Structure at High X

J-FUTURE

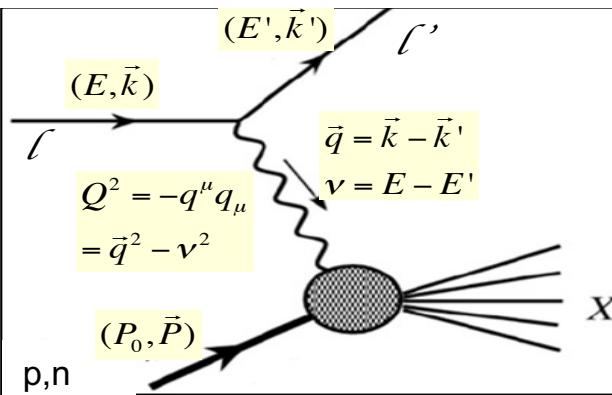
March 30, 2022



Sebastian Kuhn, *Old Dominion University*

# Overview

- Valence structure of the nucleon
  - Why do we care?
  - Where are we right now?
- Spin structure at high  $x$ 
  - Existing world data
  - Recent results (Exp. and Theory)
  - Upcoming experiments
- JLab at  $> 20$  GeV – what more can we do?
  - General considerations
  - Example: projections for  $A_{1n}$
- Conclusions



Parton model: DIS can access  $F_1(x) = \frac{1}{2} \sum_i e_i^2 q_i(x)$  (and  $F_2(x) \approx 2x F_1(x)$ )

Callan-Gross

Wandzura-Wilczek

$$g_1(x) = \frac{1}{2} \sum_i e_i^2 \Delta q_i(x) \quad \left( \text{and } g_2(x) \approx -g_1(x) + \int_x^1 \frac{g_1(y)}{y} dy \right)$$

At finite  $Q^2$ : pQCD evolution ( $q(x, Q^2), \Delta q(x, Q^2) \Rightarrow$  DGLAP equations), and gluon radiation

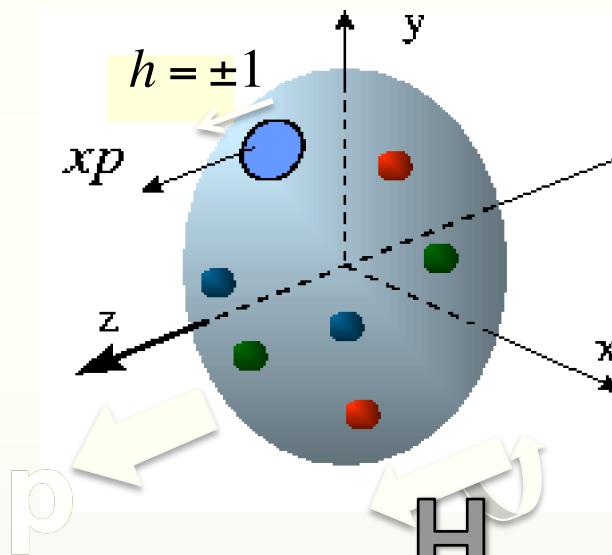
$$g_1(x, Q^2)_{pQCD} = \frac{1}{2} \sum_q^{N_f} e_q^2 [(\Delta q + \bar{\Delta q}) \otimes (1 + \frac{\alpha_s(Q^2)}{2\pi} \delta C_q) + \frac{\alpha_s(Q^2)}{2\pi} \Delta G \otimes \frac{\delta C_G}{N_f}]$$

$\Rightarrow$  access to gluons.  $\delta C_q, \delta C_G$  – Wilson coefficient functions

SIDIS: Tag the flavor of the struck quark with the leading FS hadron  $\Rightarrow$  separate  $q_i(x, Q^2), \Delta q_i(x, Q^2)$

Fixed target kinematics:  $Q^2 \approx M^2 \Rightarrow$  target mass effects, higher twist contributions and resonance excitations

- Non-zero  $R = \frac{F_2}{2x F_1} \left( \frac{4M^2 x^2}{Q^2} + 1 \right) - 1$ ,  $g_2^{HT}(x) = g_2(x) - g_2^{WW}(x)$
- Further  $Q^2$ -dependence (power series in  $\frac{1}{Q^n}$ )
- Ultra-low  $Q^2$ :  $\chi$ PT, EFT, ...



$$q(x; Q^2), \langle h \cdot H \rangle q(x; Q^2)$$

“1-D” Parton Distributions (PDFs)  
(integrated over many variables)

Duality?

# Valence Region: Structure Functions for $x \rightarrow 1$

- Dominated by up and down valence quarks  $\rightarrow$  quantum numbers of the nucleon
- Important for higher power  $x^n$  moments  $\rightarrow$  Mellin Moments, LQCD
- Related to high- $Q^2$ , lower  $x$  through DGLAP  $\rightarrow$  LHC
- MANY predictions based on pQCD and quark models:

SU(6)-symmetric proton wave function in the “naïve” quark model:

$$|p\uparrow\rangle = \frac{1}{\sqrt{18}} (3u\uparrow[ud]_{S=0} + u\uparrow[ud]_{S=1} - \sqrt{2}u\downarrow[ud]_{S=1} - \sqrt{2}d\uparrow[uu]_{S=1} - 2d\downarrow[uu]_{S=1})$$

In this model:  $d/u = 1/2$ ,  $\Delta u/u = 2/3$ ,  $\Delta d/d = -1/3$  for all  $x \Rightarrow$

$$\sum_q \Delta q = 1 \Rightarrow S_p = \frac{1}{2} \sum_q \Delta q = \frac{1}{2} \Delta \Sigma; \quad g_A^{(3)} = \Delta u - \Delta d = 5/3; \quad g_A^{(8)} = \Delta u + \Delta d - 2\Delta s = 1$$

Relativistic Correction: lower component reduces axial charge, adds to orbital angular momentum (p-wave)  $\Rightarrow$

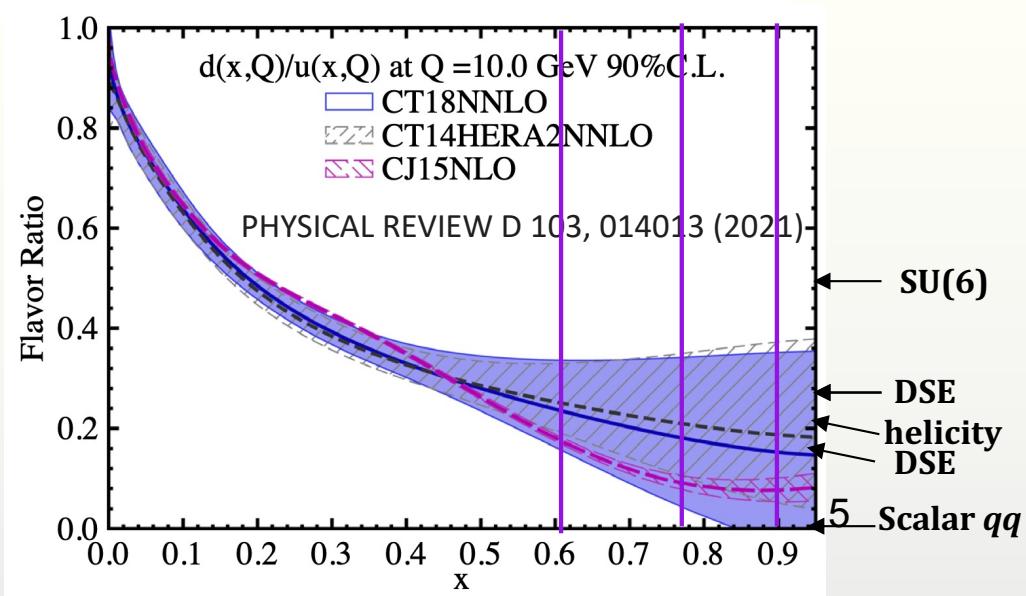
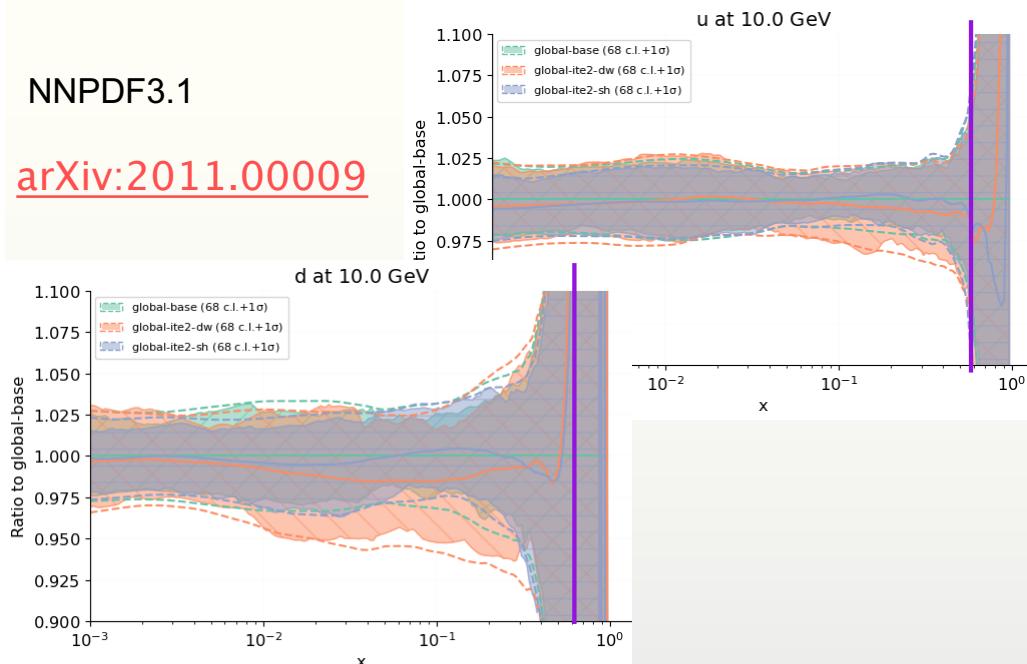
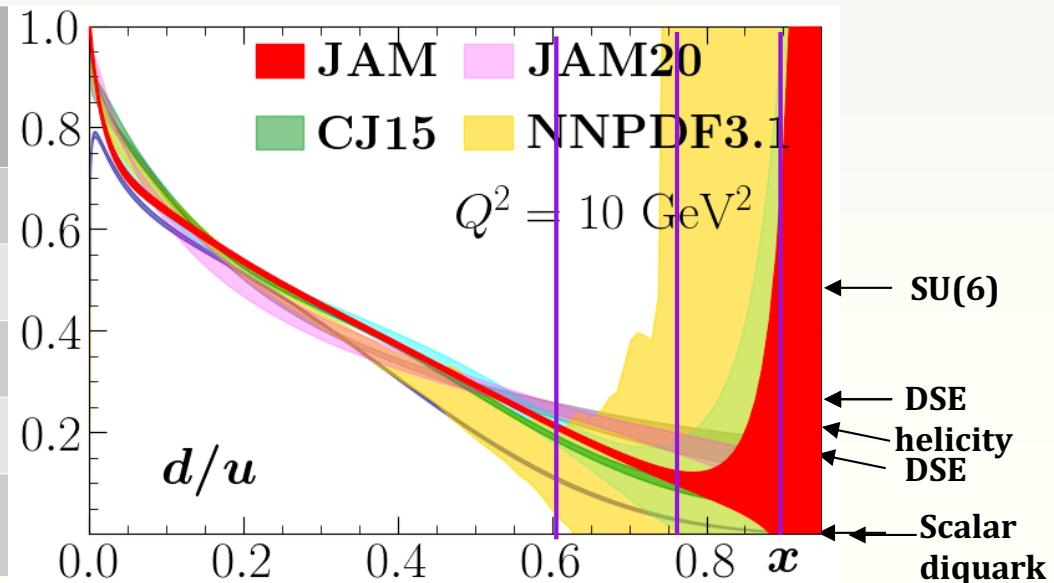
$$\sum_q \Delta q = \Delta \Sigma \approx 60\%; \quad g_A^{(3)} = \Delta u - \Delta d \approx 1.26; \quad g_A^{(8)} = \Delta u + \Delta d - 2\Delta s \approx 0.6$$

Hyperfine structure effect in QM:  $S=1$  suppressed  $\Rightarrow d/u = 0$ ,  $\Delta u/u = 1$ ,  $\Delta d/d = -1/3$   
for  $x \rightarrow 1 \Rightarrow A_{1p} = 1$ ,  $A_{1n} = 1$ ,  $A_{1D} = 1$

pQCD: helicity conservation ( $q\uparrow\uparrow p$ )  $\Rightarrow d/u \rightarrow 2/(9+1) = 1/5$ ,  $\Delta u/u \rightarrow 1$ ,  $\Delta d/d \rightarrow 1$  for  $x \rightarrow 1$   
Other approaches: Dyson-Schwinger Equation, statistical models, ...

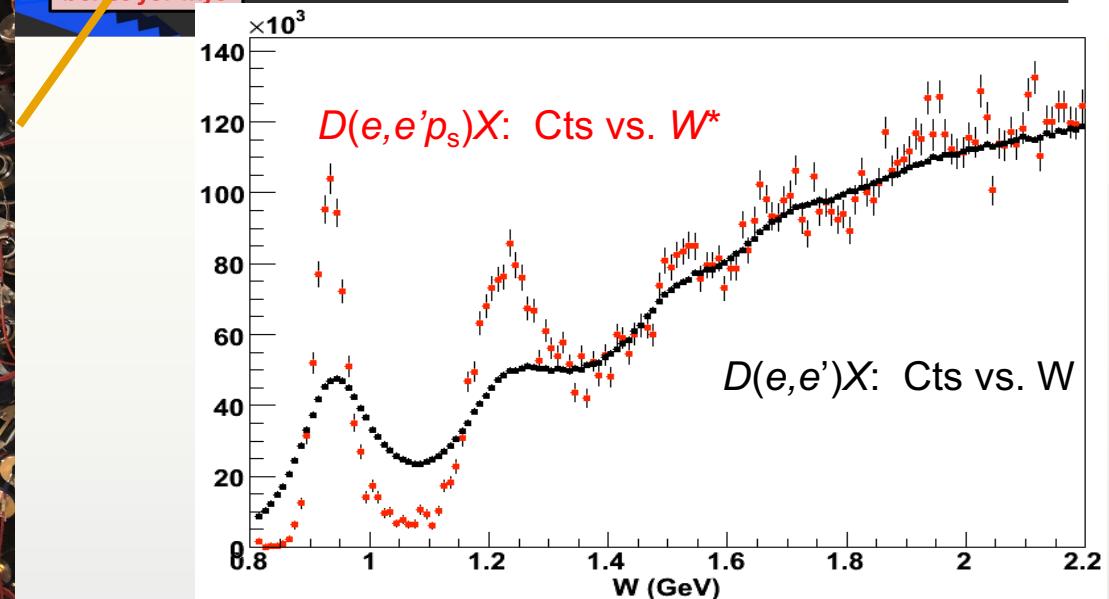
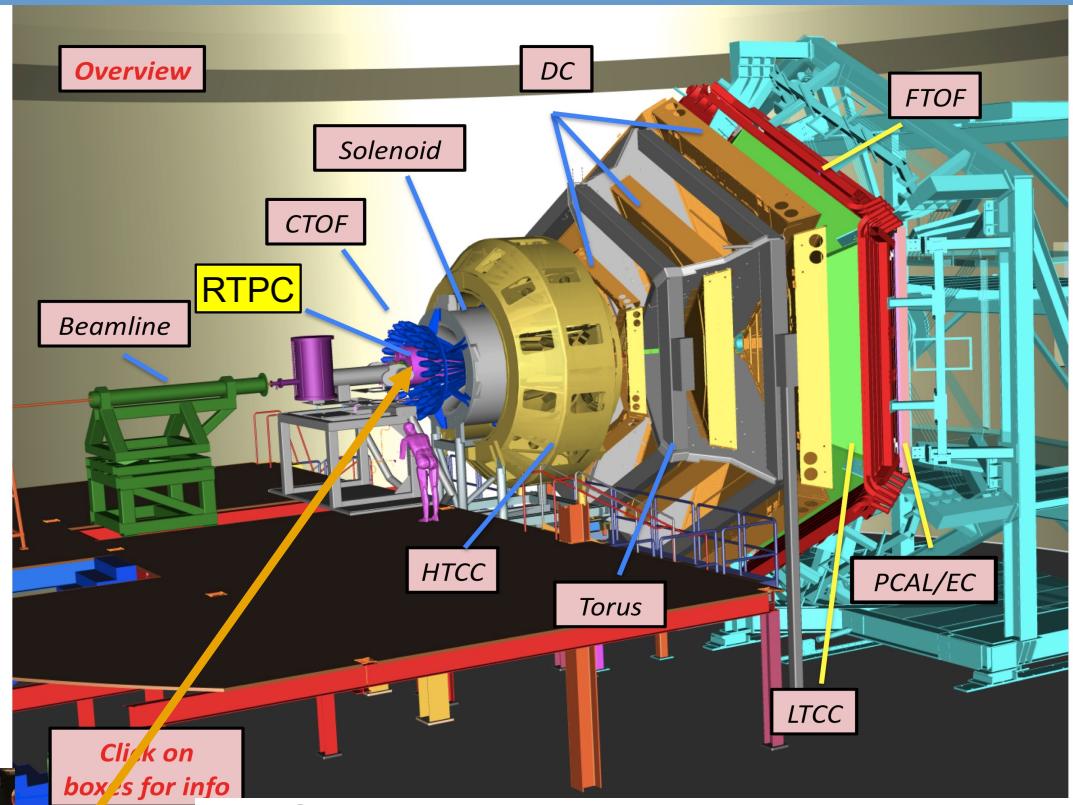
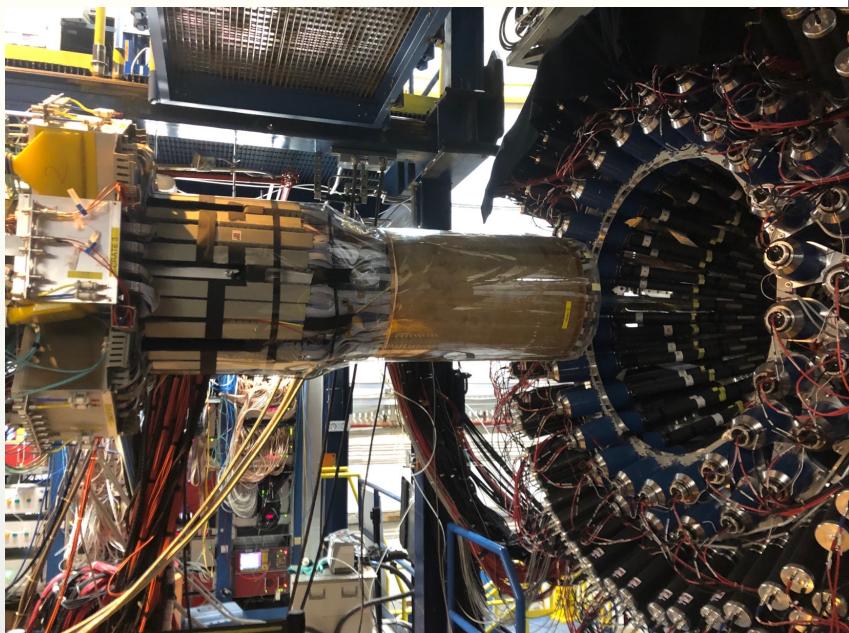
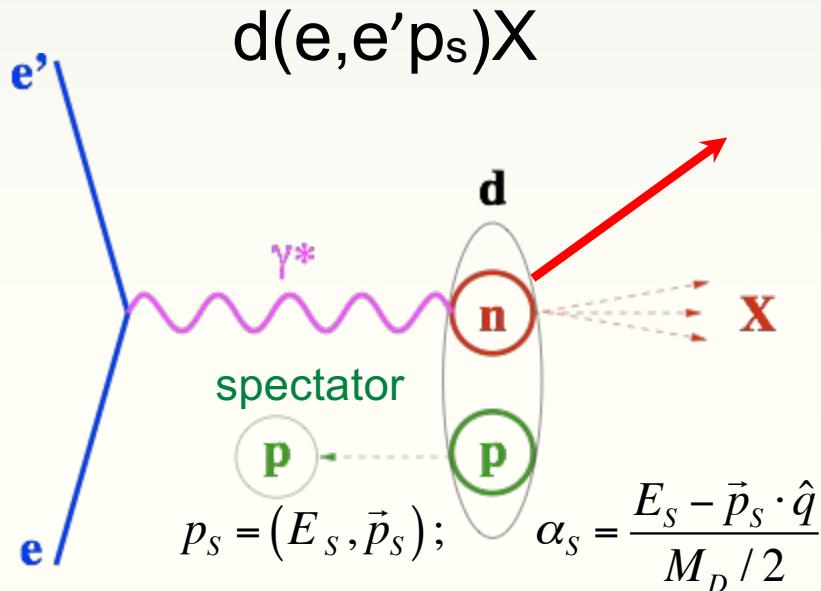
# Unpolarized PDFs – high $x$

Nucleon Model	$F_2^n/F_2^p$ $x \rightarrow 1$	$d/u$ $x \rightarrow 1$
SU(6) Symmetry	2/3	0.5
Scalar diquark dominance	1/4	0
DSE contact interaction	0.41	0.18
DSE realistic interaction	0.49	0.28
PQCD (helicity conservation)	3/7	0.2



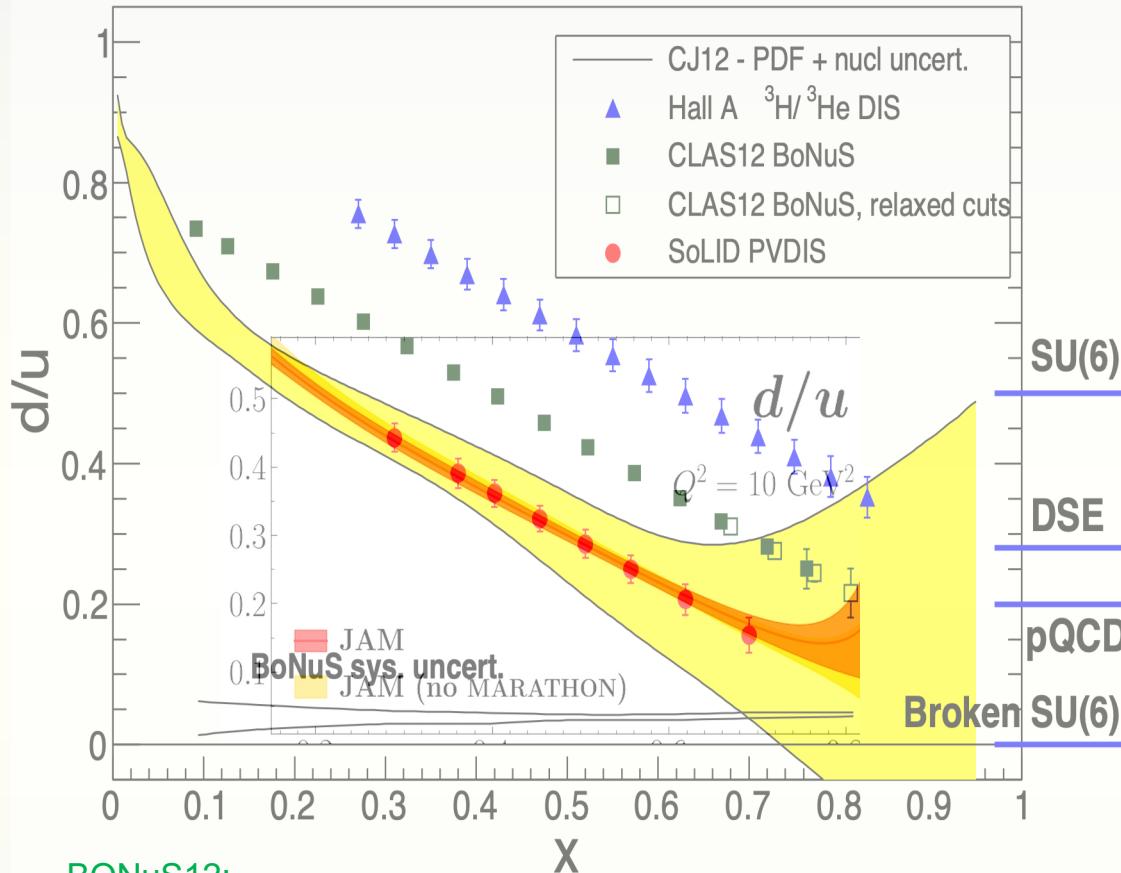
# BONuS12 with CLAS12

$F_{2n}/F_{2p}$  through spectator tagging



# Projected JLab@12 GeV d/u Extractions

Marathon and BonuS12

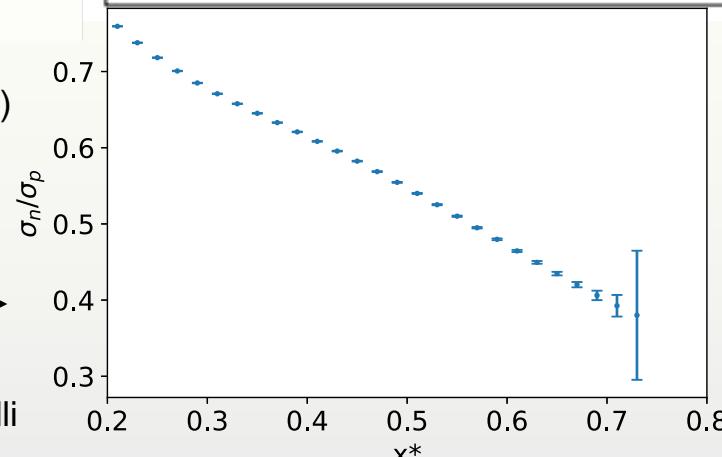
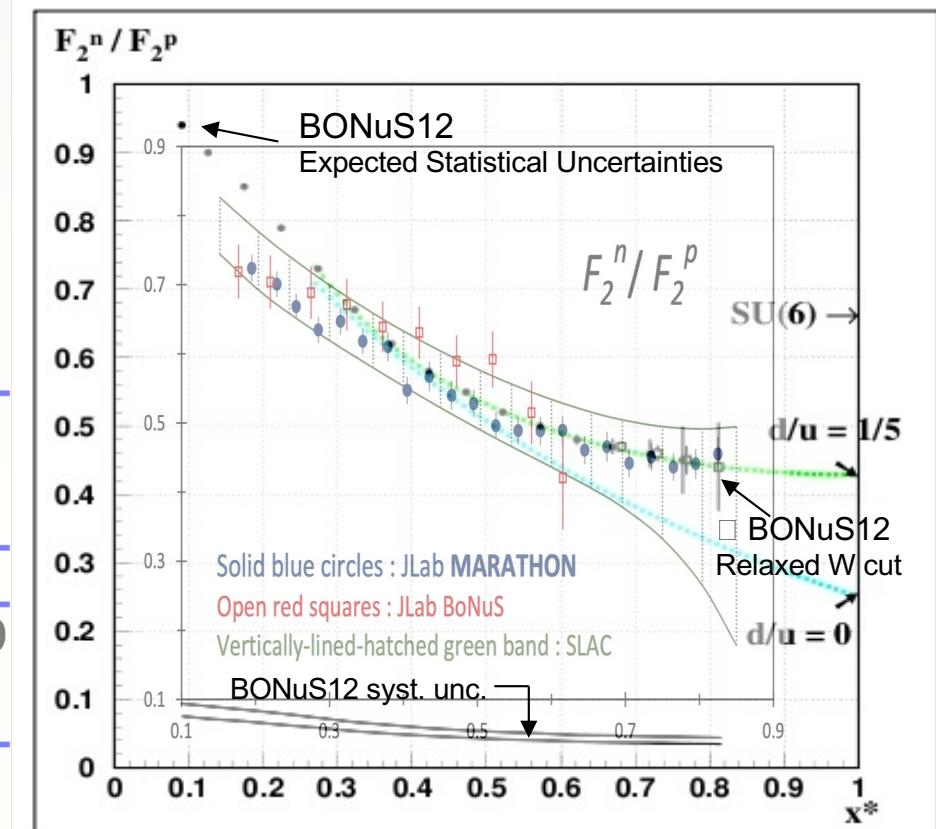


BonuS12:

**Dark Symbols:**  $W^* > 2 \text{ GeV}$  ( $x^*$  up to 0.8, bin centered  $x^* = 0.76$ )

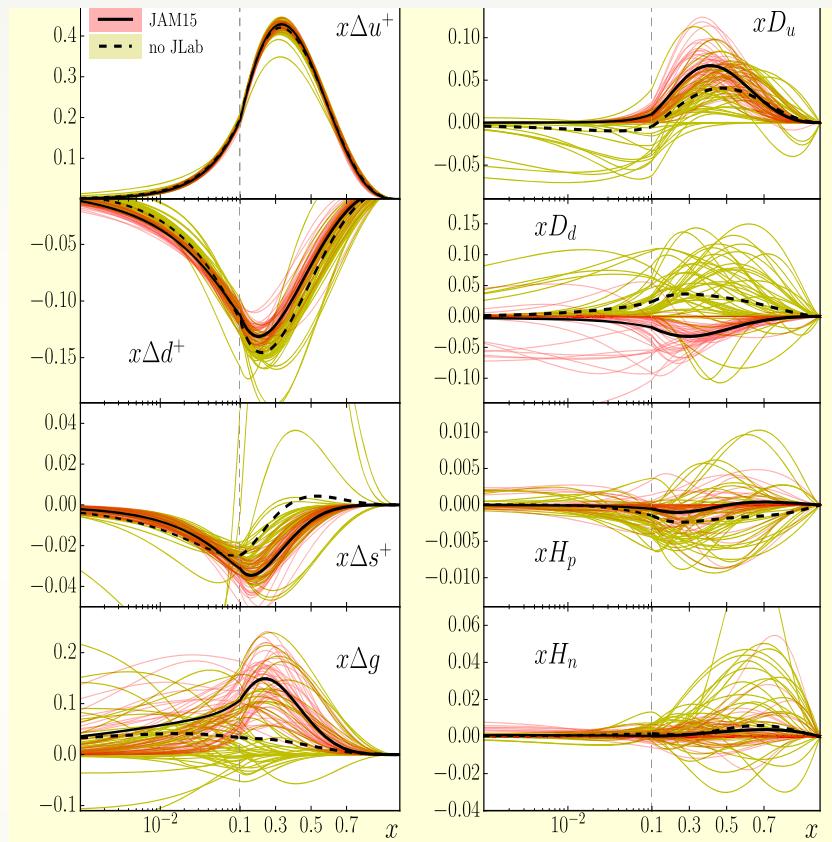
**Open Symbols:** “Relaxed cut”  $W^* > 1.8 \text{ GeV}$  ( $x^*$  up to 0.83)

...also: Additional data from ALERT and TDIS



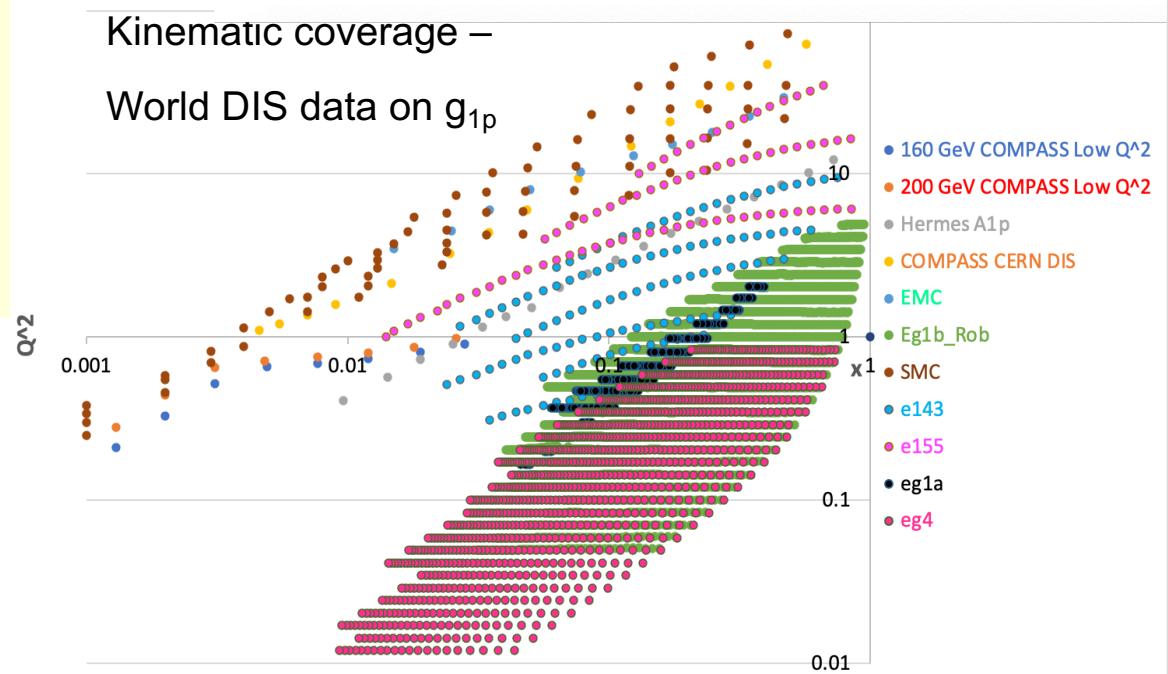
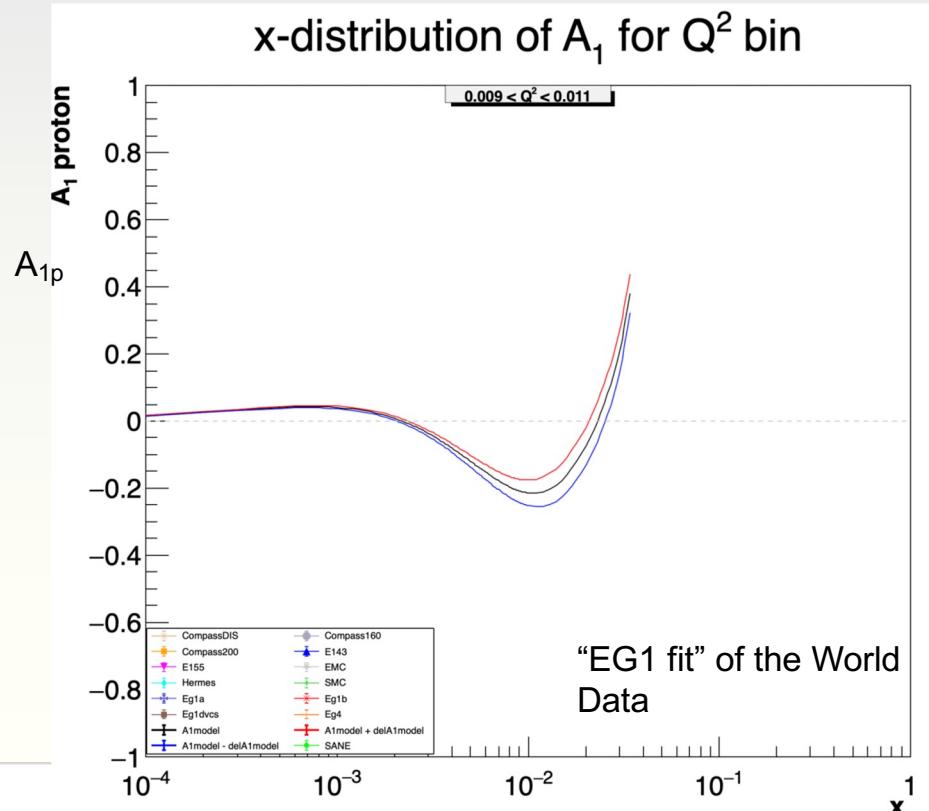
Courtesy Arun Tadepalli

# Spin Structure Functions in the last 40 years

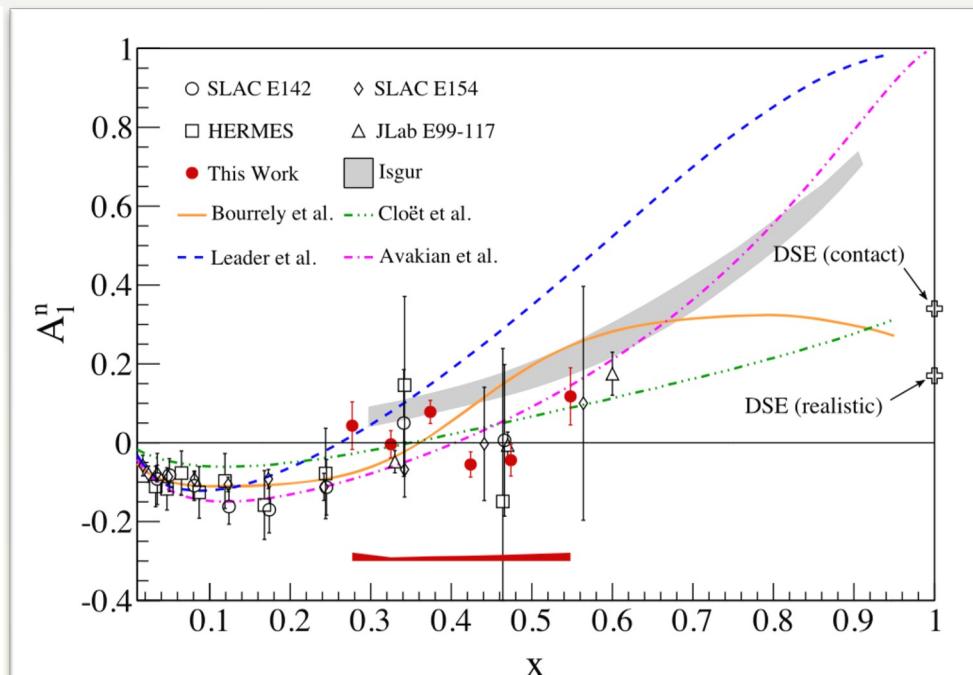
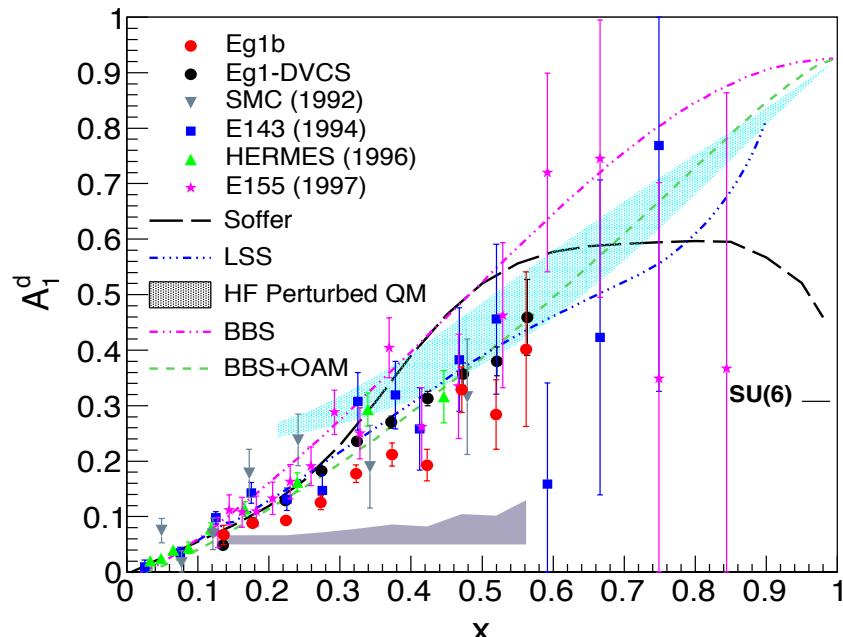
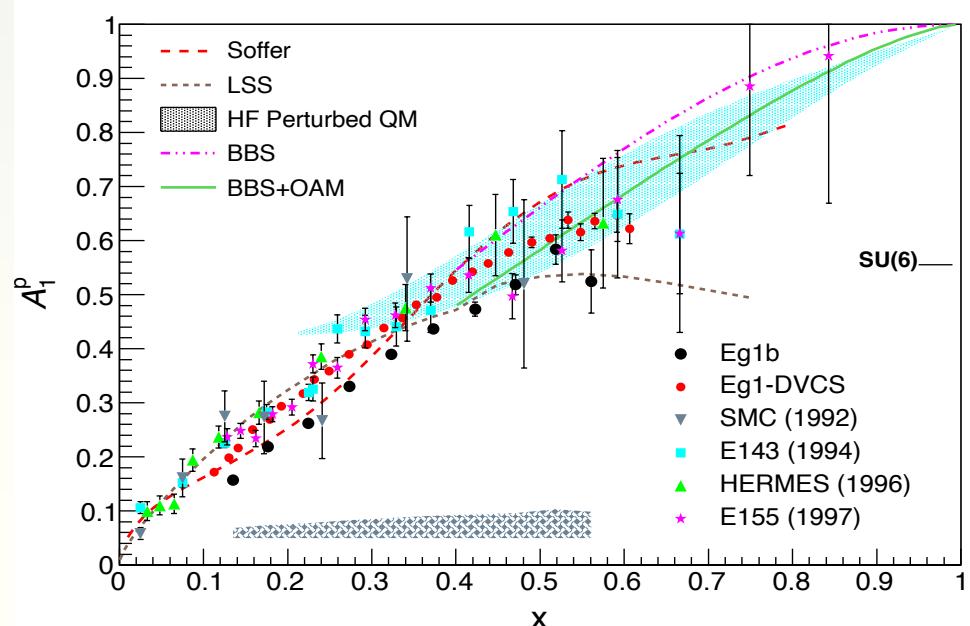


Nobuo Sato, W. Melnitchouk, S. E. Kuhn, J. J. Ethier, and A. Accardi: "Iterative Monte Carlo analysis of spin-dependent parton distributions", Phys. Rev. D **93**, 074005 (5 April 2016).

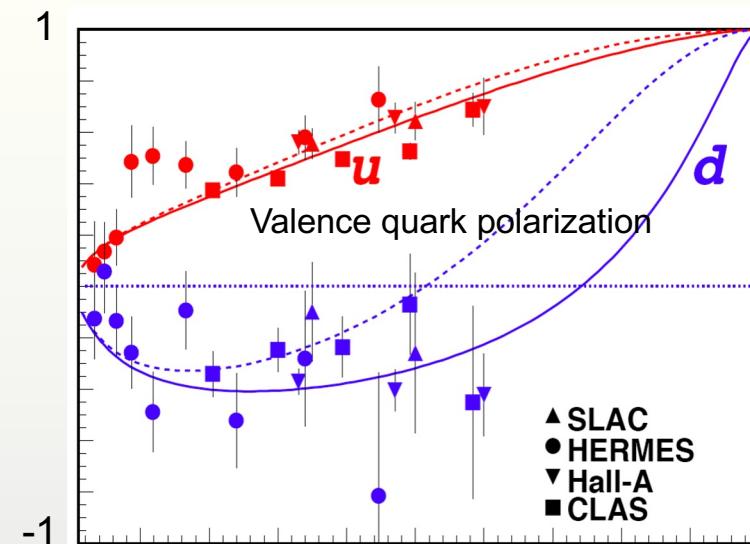
A. Deur, Y. Prok, V. Burkert, D. Crabb, F.-X. Girod, K. A. Griffioen, N. Guler, S. E. Kuhn, and N. Kvaltine: "High precision determination of the  $Q^2$  evolution of the Bjorken sum", Phys. Rev. C **90**, 012009 (July 2014).



# Existing Spin Structure Functions at high $x$



Parno et al., Phy Let B DOI: 10.1016/j.physletb.2015.03.067  
 X. Zheng et al., PRL 92, 012004 (2004); PRC 70, 065207 (2004)



# Present Status on polarized PDFs

- Newest JAM analysis including RHIC and COMPASS data

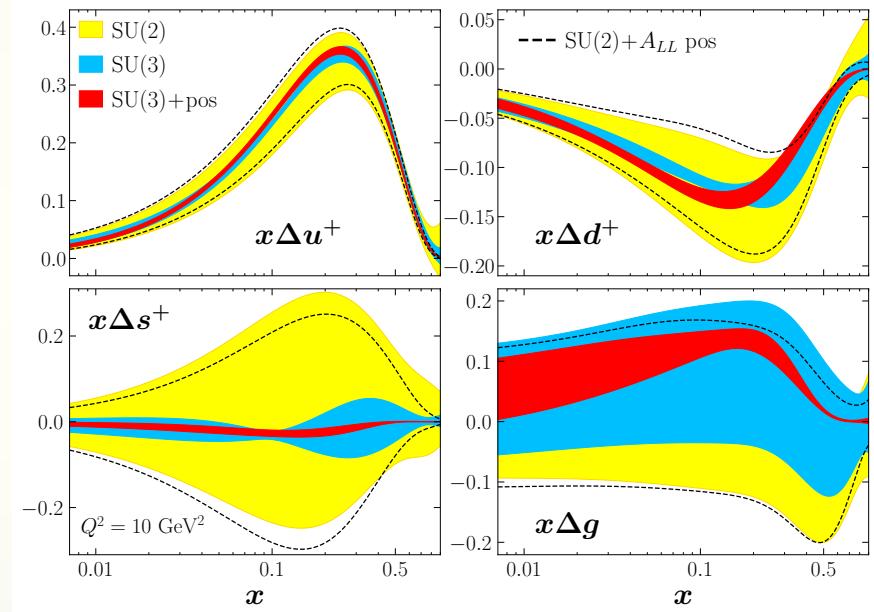
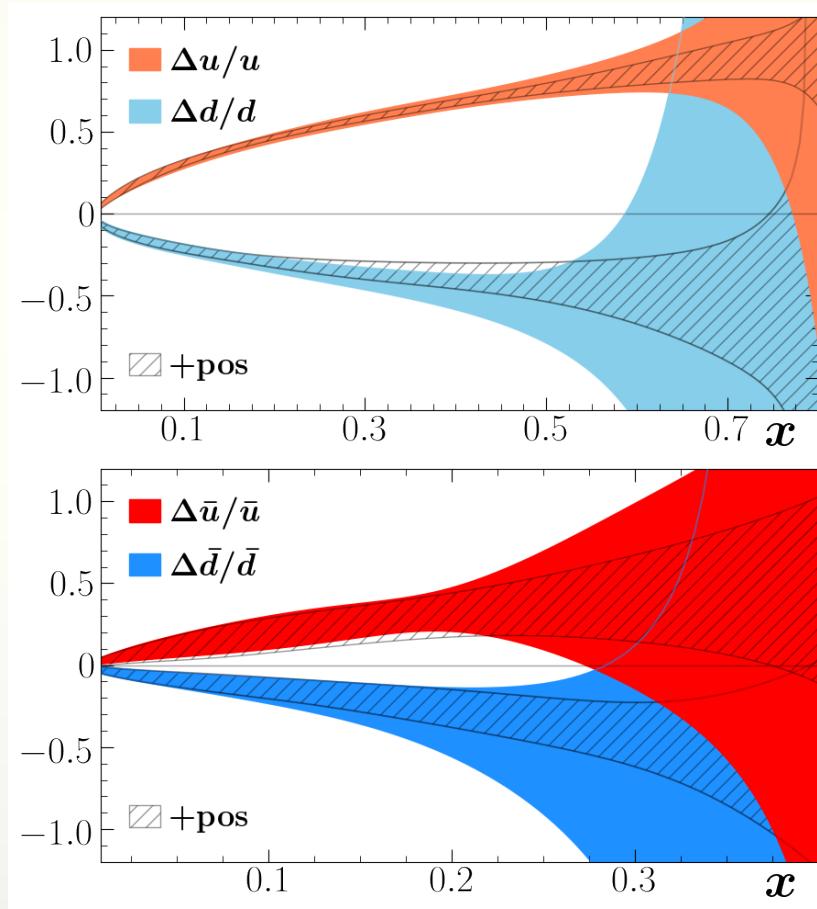
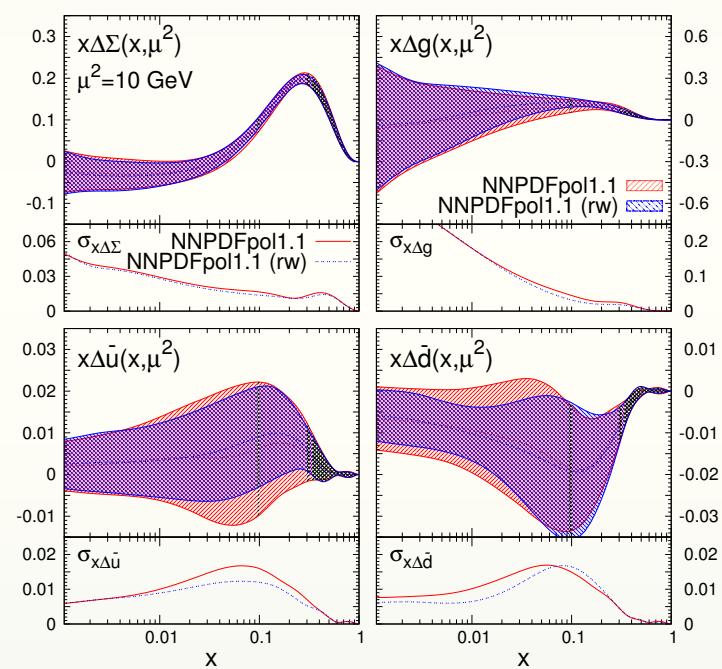
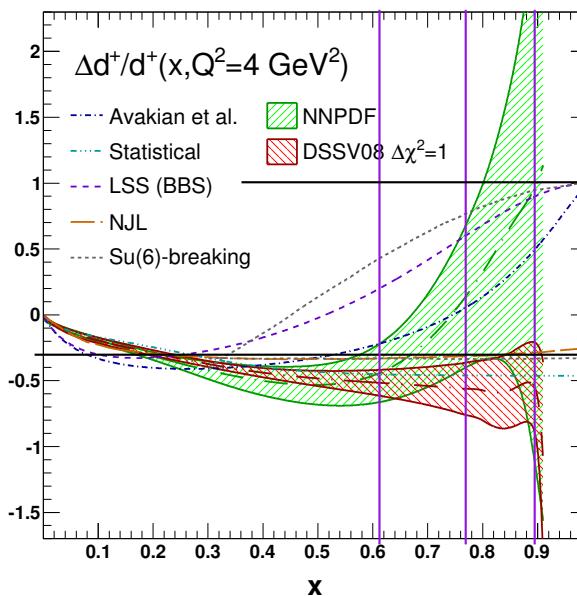
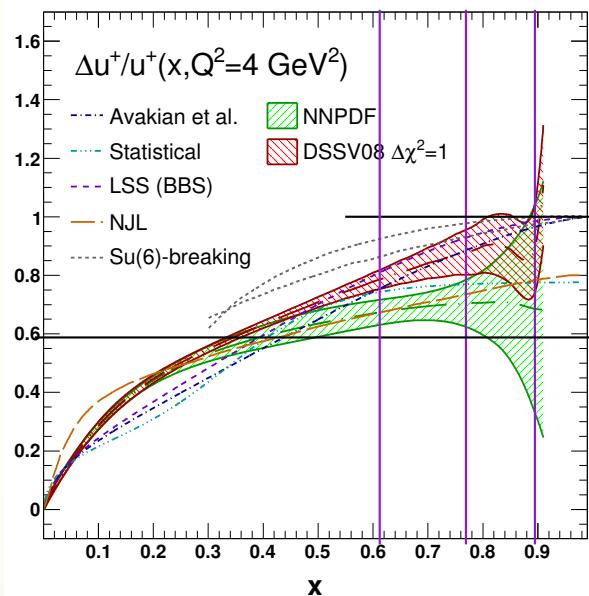


FIG. 6. Expectations values for spin-dependent  $\Delta u^+$ ,  $\Delta d^+$ ,  $\Delta s^+$ , and  $\Delta g$  PDFs at  $Q^2 = 10 \text{ GeV}^2$  fitted under various theory assumptions according to the SU(2) (yellow  $1\sigma$  bands), SU(3) (blue  $1\sigma$  bands) and SU(3)+positivity (red  $1\sigma$  bands) scenarios, as well as with the SU(2) scenario but filtered to ensure  $A_{LL}$  positivity at large  $x$  (dashed lines).

# Present Status on polarized PDFs

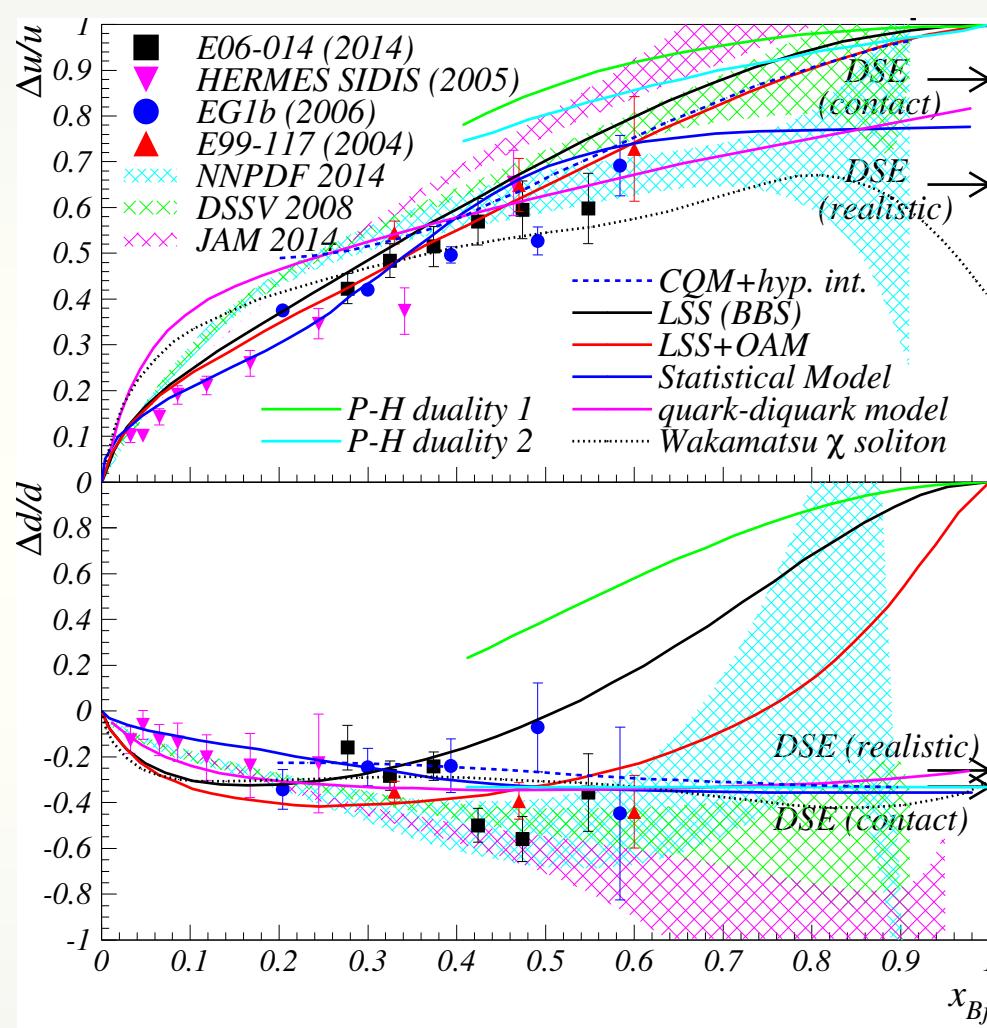
- NNPDFpol1.1+RHIC W data analysis



arXiv:1410.7290v2 [hep-ph] 23 Jan 2015

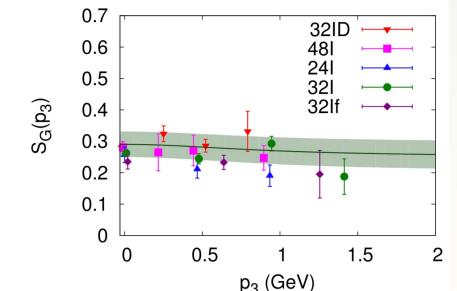
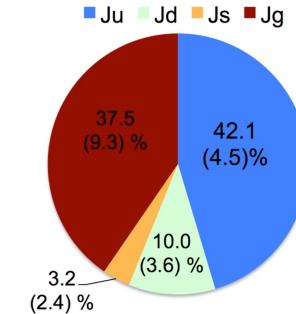
arXiv:1702.05077v1 [hep-ph] 16 Feb 2017

# Recent theoretical predictions

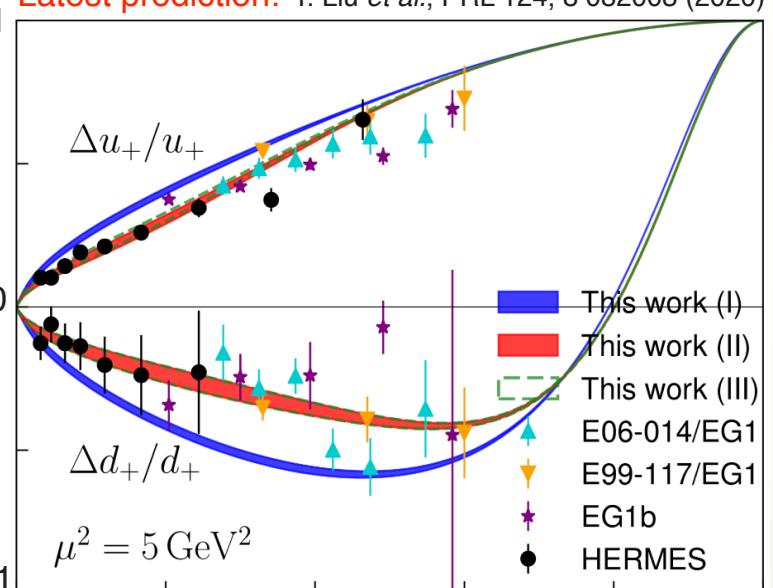


Full 12 GeV Data set will significantly constrain valence + sea quark and gluon PDF fits, higher twist effects and sum rules

Ji, Yuan and Zhao: arXiv2009.01291 [hep-ph] 2 Sep 2020



Latest prediction: T. Liu et al., PRL 124, 8 082003 (2020)



From AdS/QCD determination of GPDs.

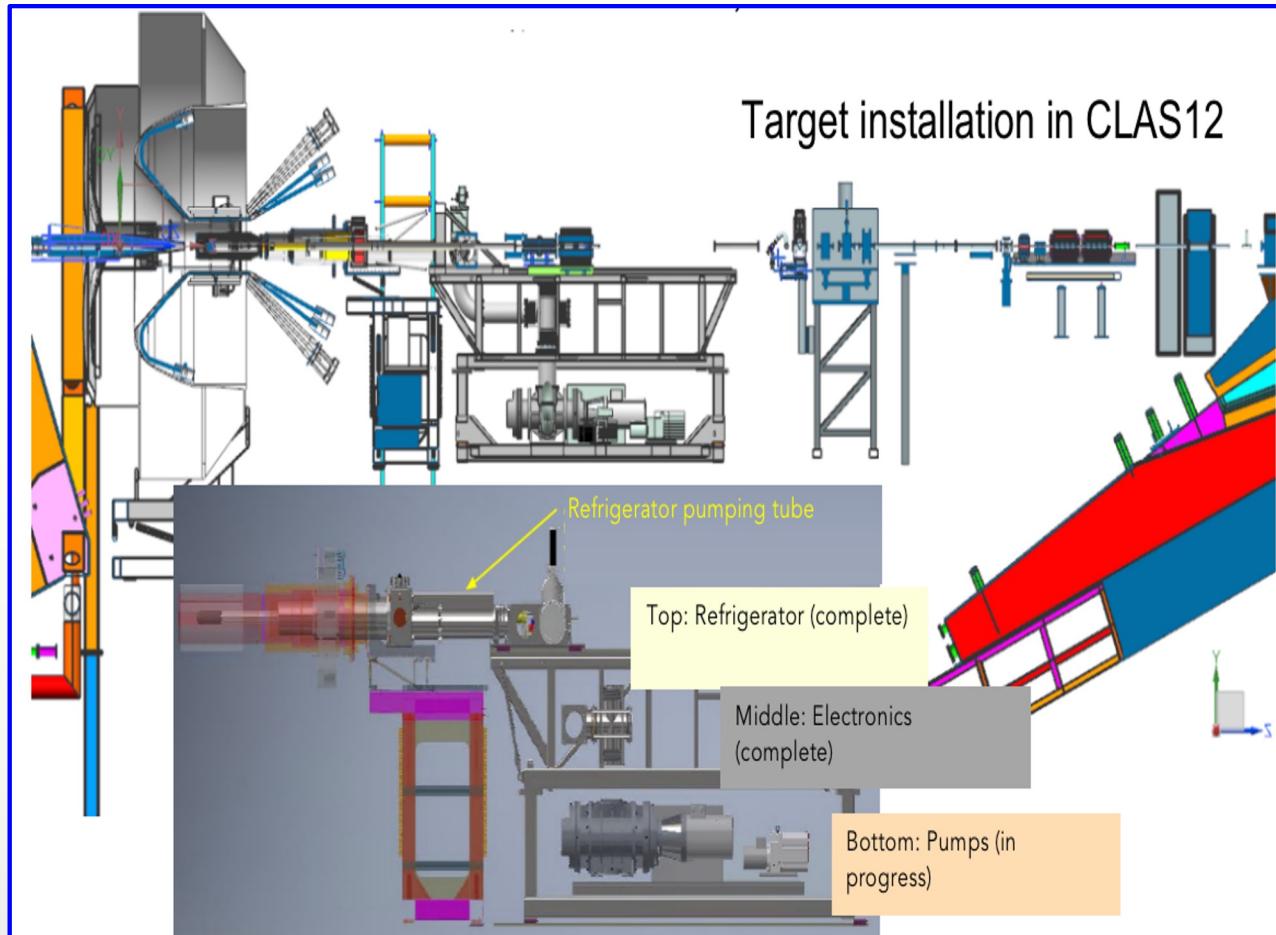
No free parameters.

Predicts Δd/d changes sign near x=0.8.

Reproduces QCD counting rules used for BBS/LSS.

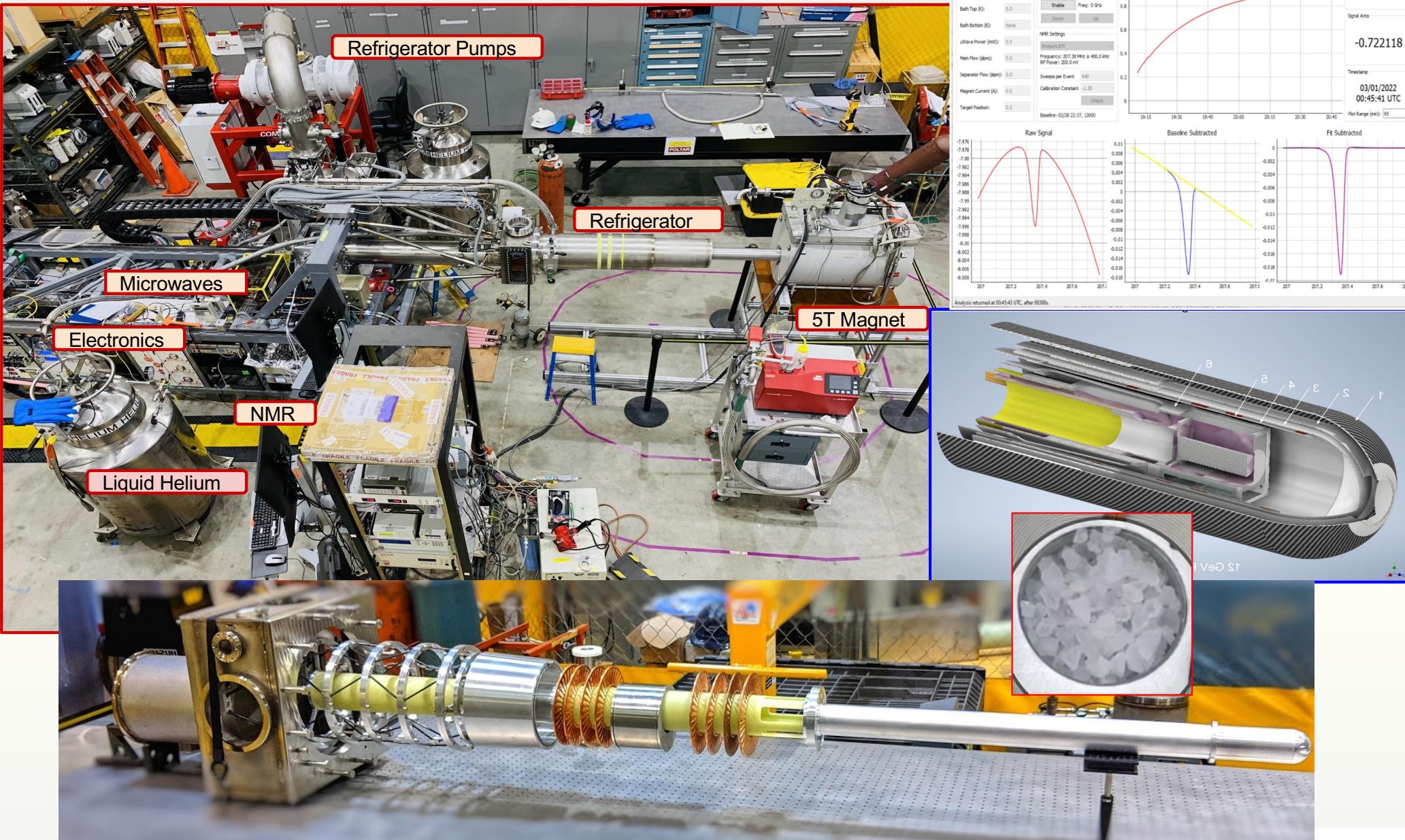
# RG-C with CLAS12

- Measure DIS inclusive spin structure functions ( $A_1, g_1$ ) of the proton and deuteron.
  - Include tagging with  $\pi, K$  SIDIS to extract flavor-separated  $\Delta q$
- Measure spin- and transverse momentum-dependent (TMD) PDFs (SIDIS).
- Deeply Virtual Compton Scattering (DVCS) to access Generalized Parton Distributions (GPDs)-Measure target single and beam/target double spin asymmetries in proton and neutron DVCS.



- Scheduled from June 2022 through March 2023 (240 Calendar Days)
- 10.6 GeV, 10 nA polarized electrons on 3 g/cm<sup>2</sup> polarized NH<sub>3</sub> / ND<sub>3</sub> ( $\mathcal{L} = 10^{35}$ )
- Dynamic Nuclear Polarization at 1 K, 5 T with 140 GHz  $\mu$ wave on irradiated ammonia
- Continuation of EG1, EG1-dvcs, EG4 to 12 GeV era
- Could in principle run at 24 GeV with somewhat higher luminosity (2x)

# Longitudinally Polarized Target for CLAS12



**Jefferson Lab**

  
**OLD DOMINION**  
UNIVERSITY®

 **UNIVERSITY**  
of  
**VIRGINIA**

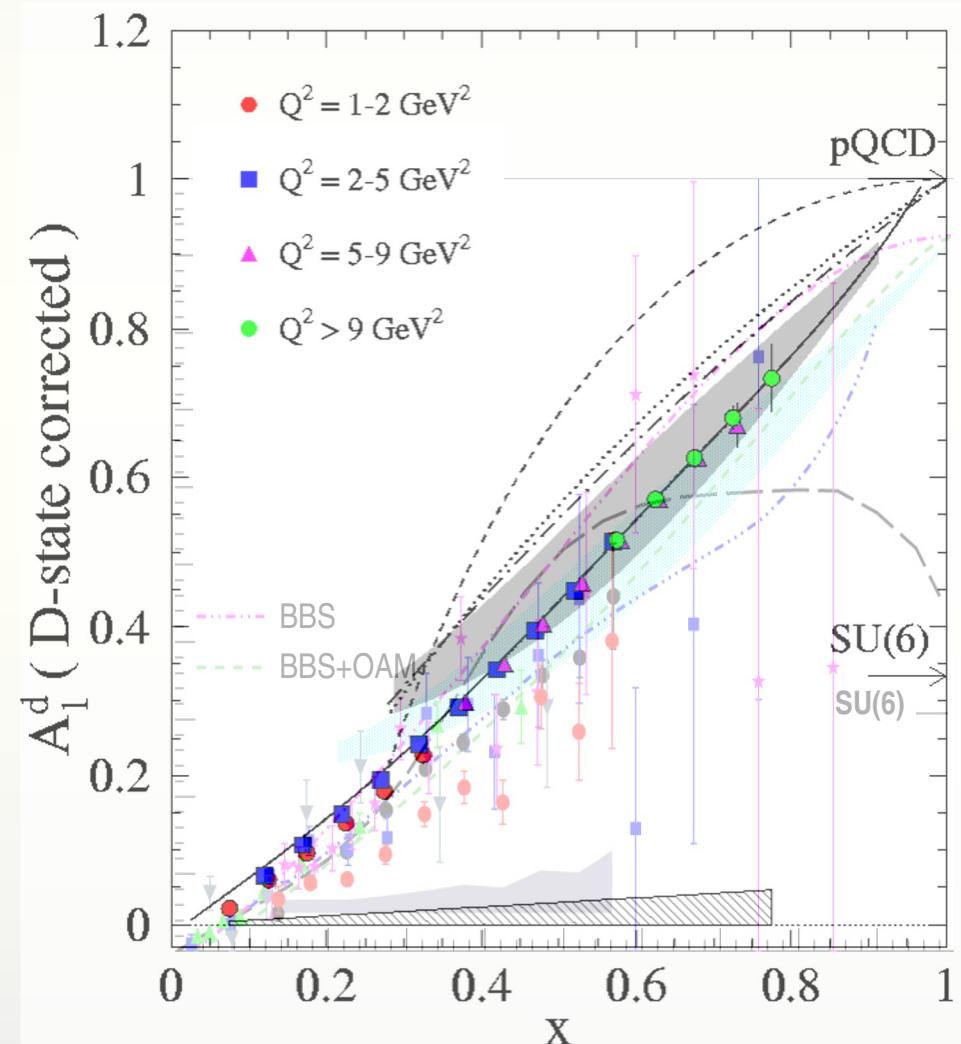
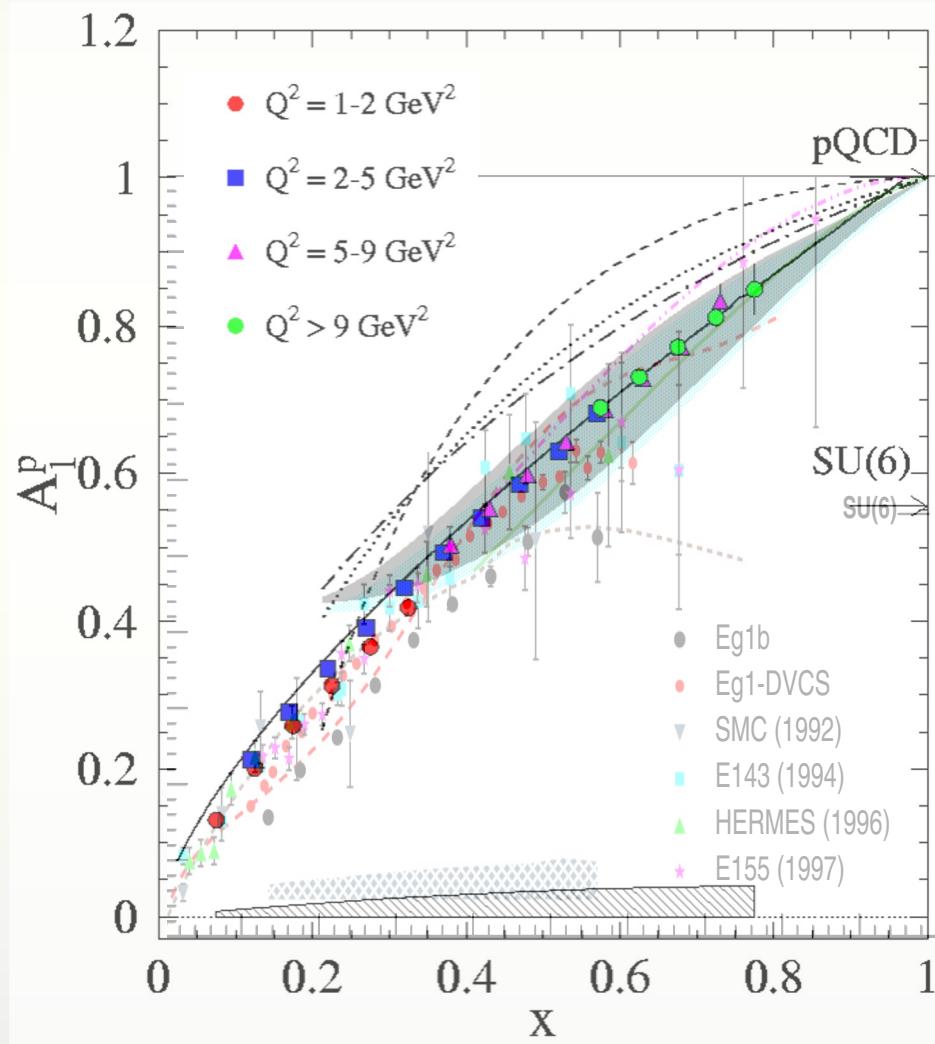
  
**CHRISTOPHER NEWPORT**  
UNIVERSITY

# Predicted Data from CLAS12 - DIS

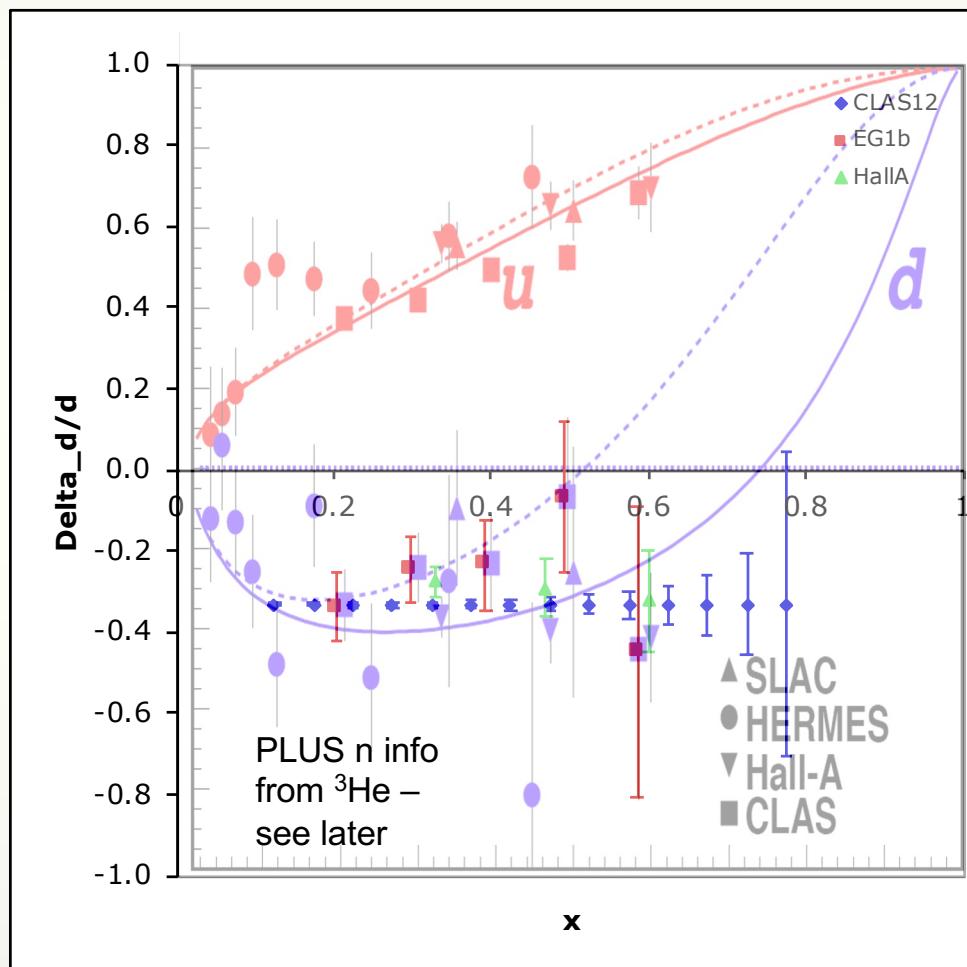
Proton

$W > 2; Q^2 > 1$

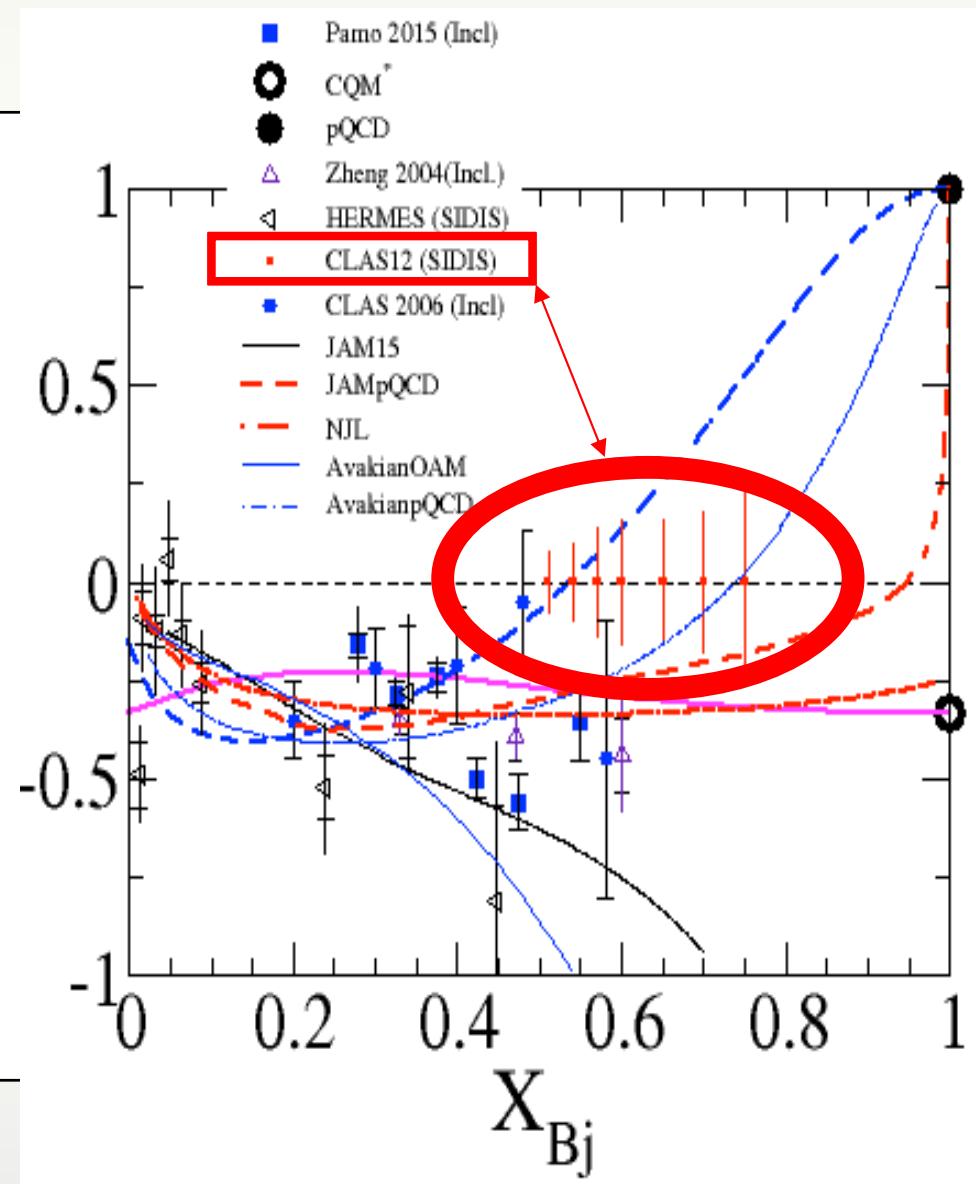
Deuteron



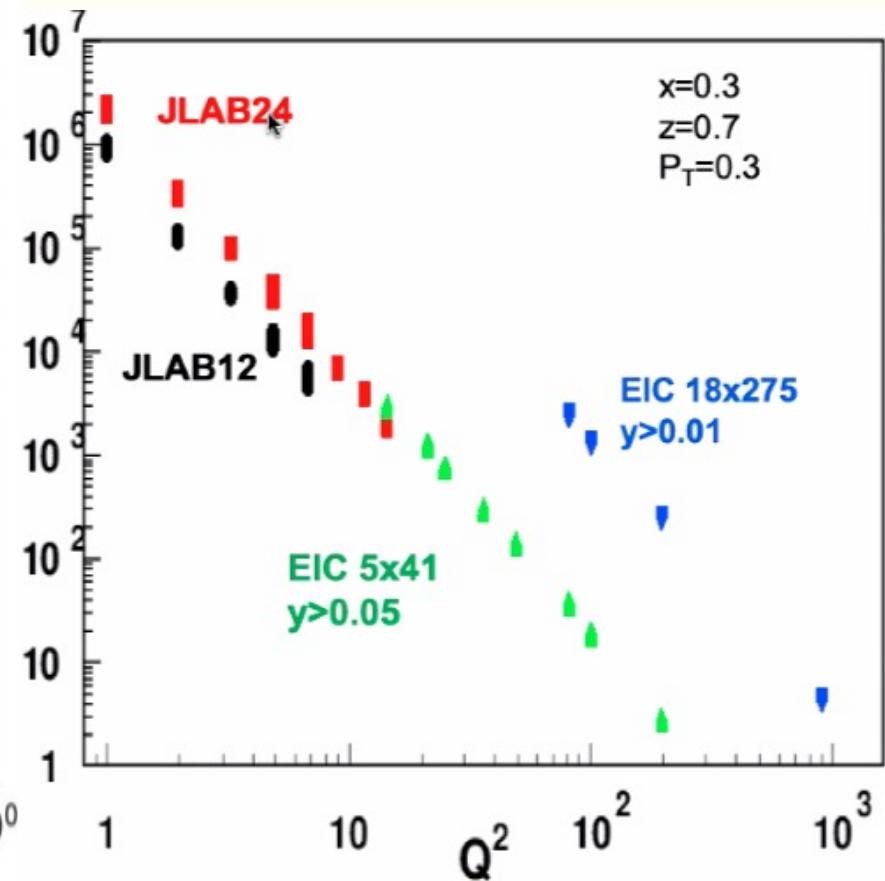
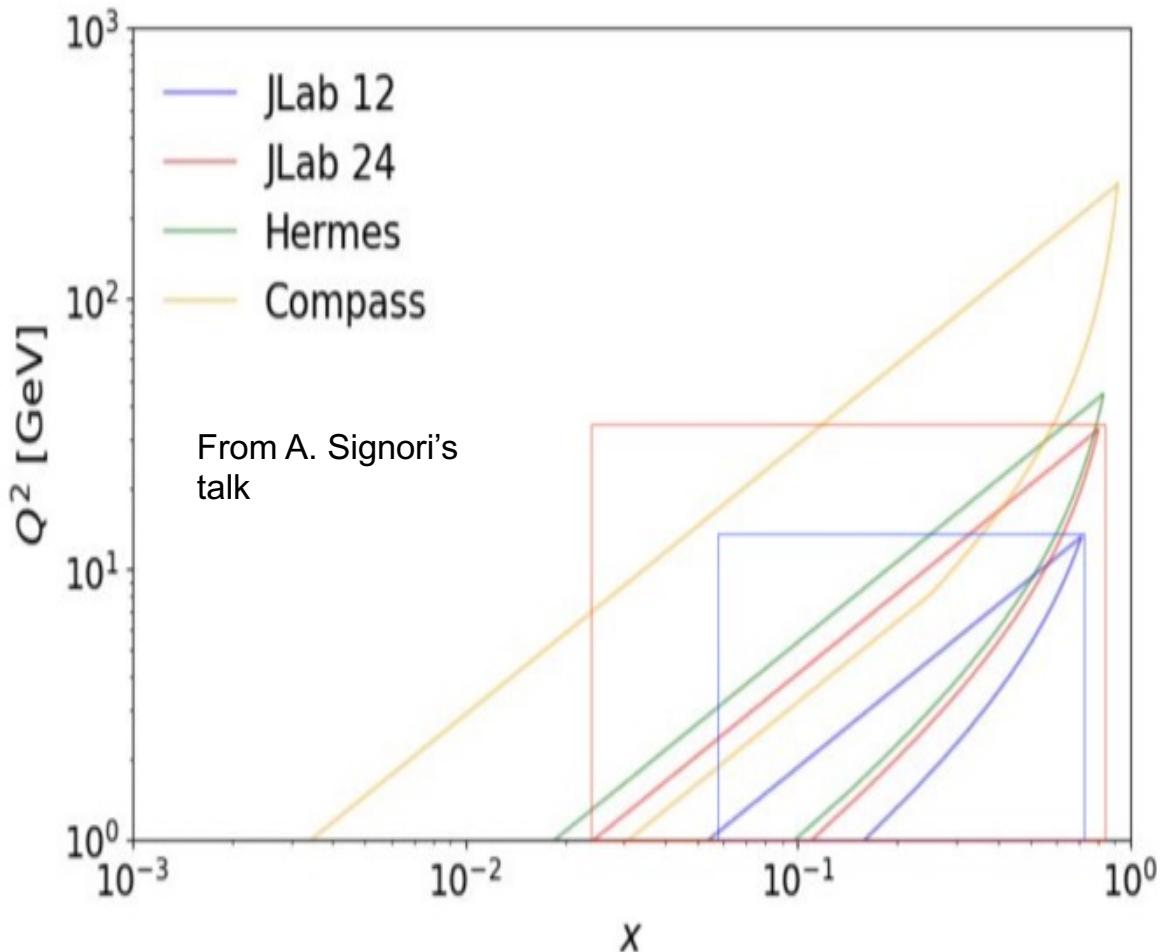
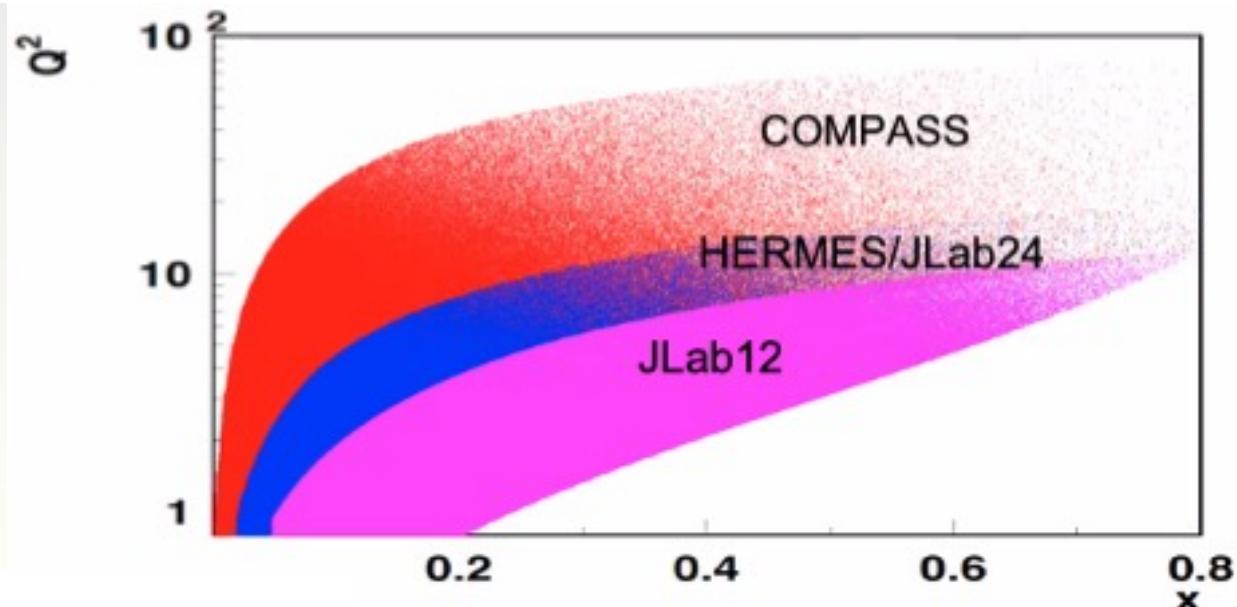
# Example: $\Delta d/d$



Up-to-date estimate RG-C  
Inclusive and semi-inclusive data



# From 12 to 24 GeV



# 24 GeV

- Halve distance to  $x = 1$  AND to  $x = 0$
- Increase  $Q^2$  range for all  $x \rightarrow$  DGLAP
- Even for same  $x$ ,  $Q^2$ : higher energy  $\rightarrow$  higher rates  $\rightarrow$  better statistics
- "*SuperRosenbluth*" – expand range in  $\varepsilon$  for fixed  $x$ ,  $Q^2$
- Higher  $Q^2$ : Suppress higher twist, study logarithmic resummation
- Extend SIDIS to higher  $x$ ,  $Q^2$ :  
high- $x$  sea quarks, gluons, ...
- Issues: Still need to avoid nuclear uncertainties.
- Example:  $A_{1n}$  at 24 GeV

# $A_{1n}$

- Projection using Hall C's
  - HMS @ 30 deg, 4.6 GeV
  - SHMS @ 20 deg, 7.8 GeV
- "F1F2-21 fit" for  ${}^3\text{He} \rightarrow$  neutron "nuclear correction"
- 30 days beam time, latest polarized  ${}^3\text{He}$  target performance (40cm, 50%, 30uA)
- projections (12 and 24 GeV) plotted on pQCD

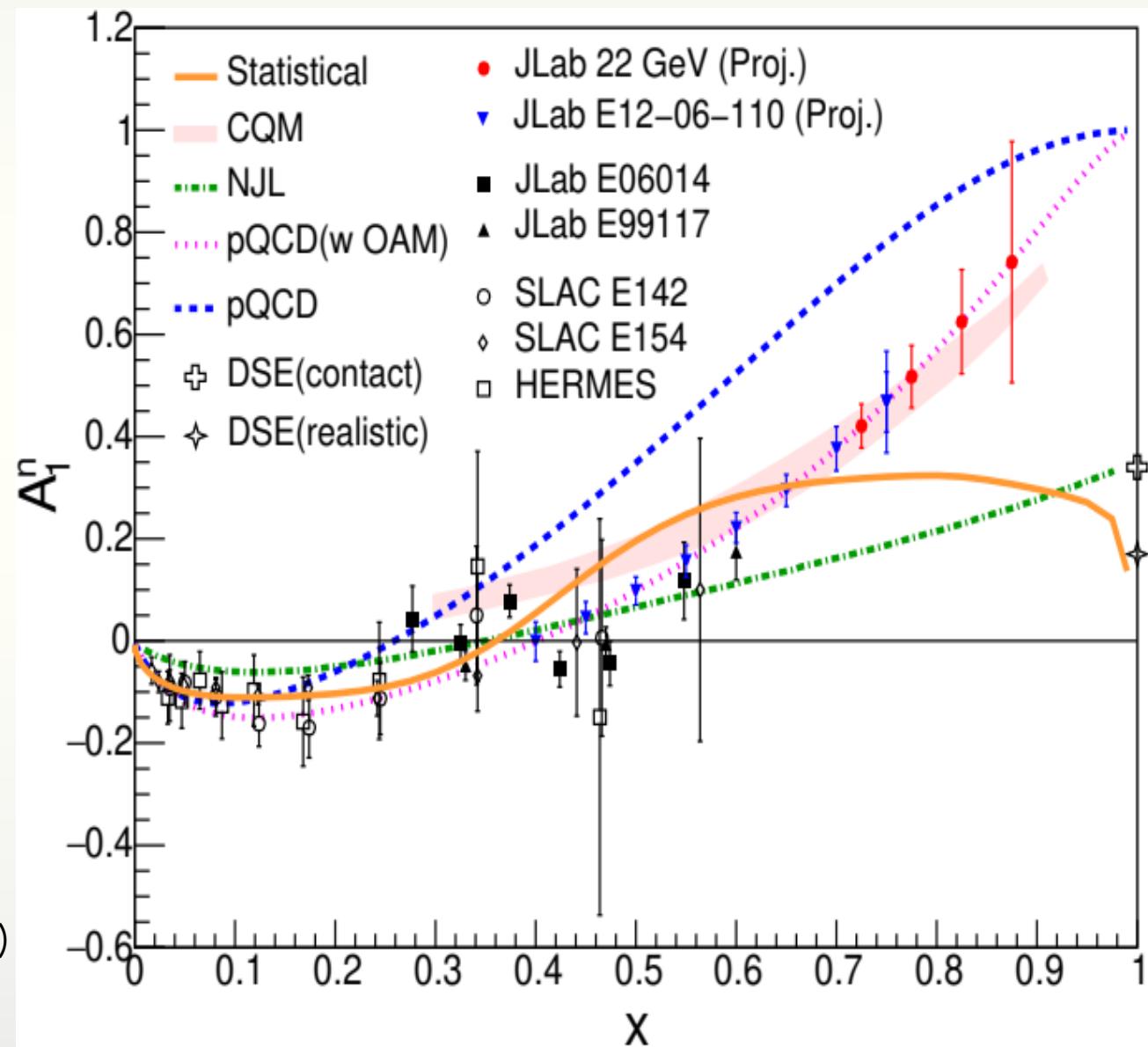


Figure credit:

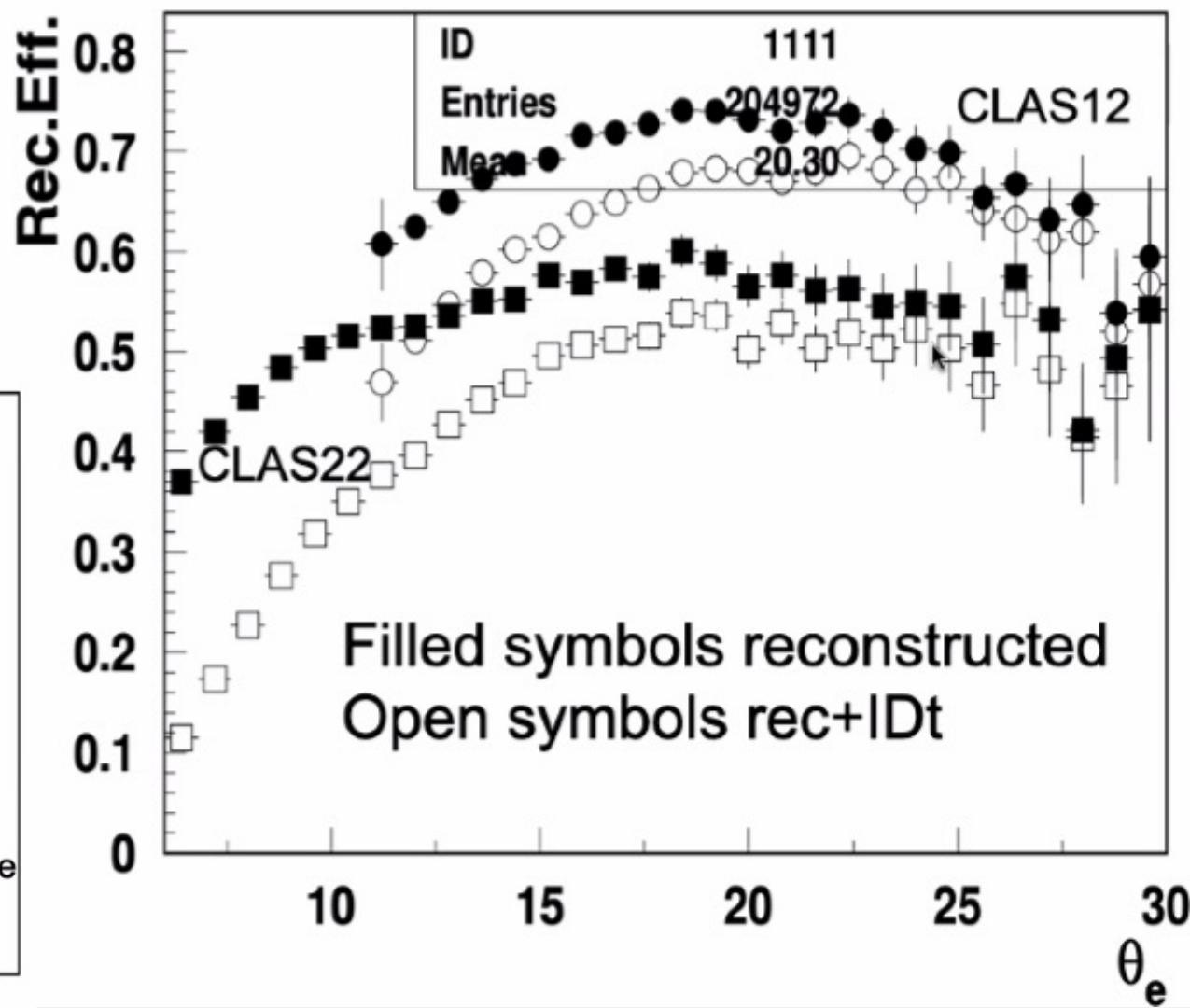
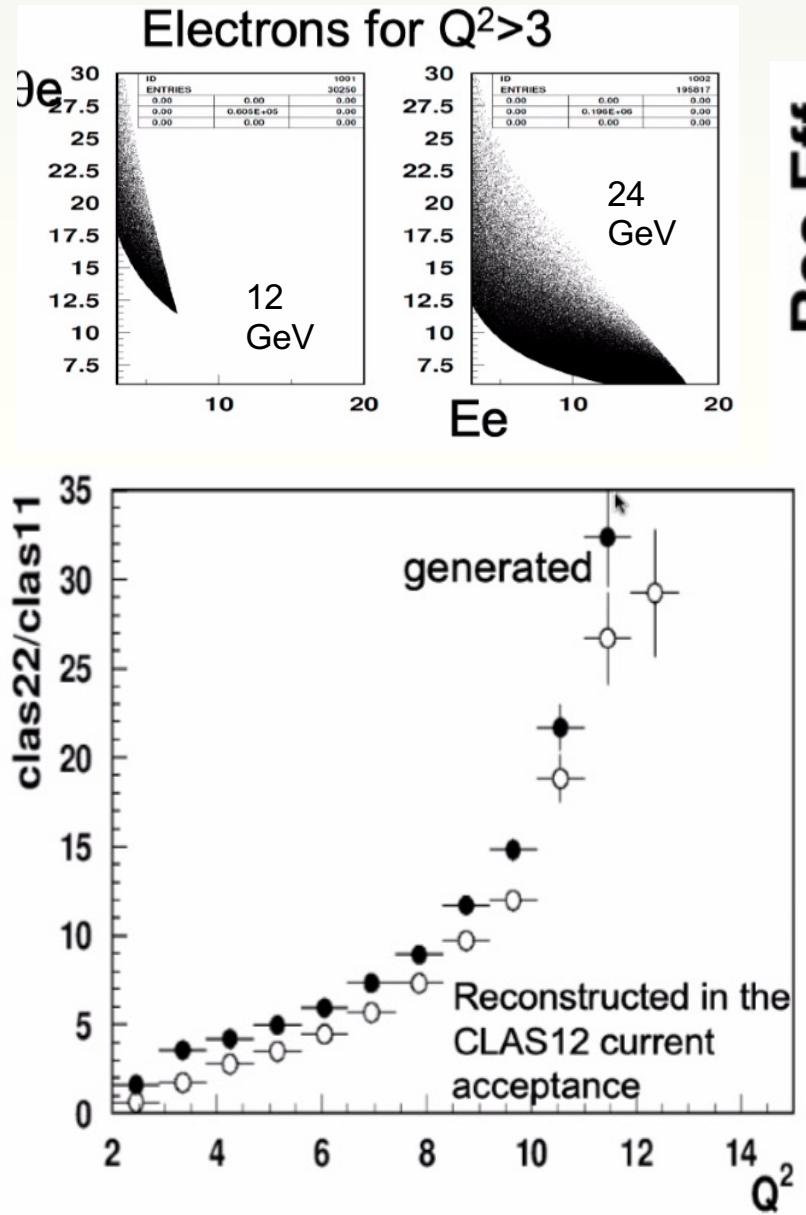
Cameron Cotton (UVA/HUGS2021)

David Flay (JLab)

Thanks to X. Zheng

# Kinematic Reach with CLAS12

Credit: H. Avakian



# Conclusions

- Structure functions in the valence region remain of high interest
- Jefferson Lab at 12 GeV will make significant impact on our understanding of this region
- 24 GeV can expand the coverage in  $x$  from 0.75 to 0.9, thereby minimizing the extrapolation to  $x \rightarrow 1$ .
- Larger range in  $Q^2$  and higher count rates  $\rightarrow$  minimize theoretical uncertainties and increase statistics even at lower  $x$ .
- 24 GeV necessary to close the gap with EIC
- Remaining issues: extracting neutron (polarized) structure functions from measurements on nuclei ( $d$ ,  ${}^3\text{He}$ ).