

SPIN TRANSPORT IN HMS

$$\begin{pmatrix} P_n^{fp} \\ P_t^{fp} \\ P_l^{fp} \end{pmatrix} = \begin{pmatrix} S_{nn} & S_{nt} & S_{nl} \\ S_{tn} & S_{tt} & S_{tl} \\ S_{ln} & S_{lt} & S_{ll} \end{pmatrix} \begin{pmatrix} P_n \\ P_t \\ P_l \end{pmatrix}$$

S_{ij} are functionals of trajectory:

$$S_{ij}(\theta_{tg}, y_{tg}, \phi_{tg}, p) \text{ or } S_{ij}(x_{fp}, \theta_{fp}, y_{fp}, \phi_{fp}, p)$$

SPIN vs VELOCITY PROPAGATION

$$\frac{d\vec{S}}{dt} = \frac{e}{m\gamma} \vec{S} \times \left[\frac{g}{2} \vec{B}^{\parallel} + \left(1 + \frac{g-2}{2} \gamma\right) \vec{B}^{\perp} \right]$$

$$\frac{d\vec{v}}{dt} = \frac{e}{m\gamma} \vec{v} \times \vec{B}^{\perp}$$

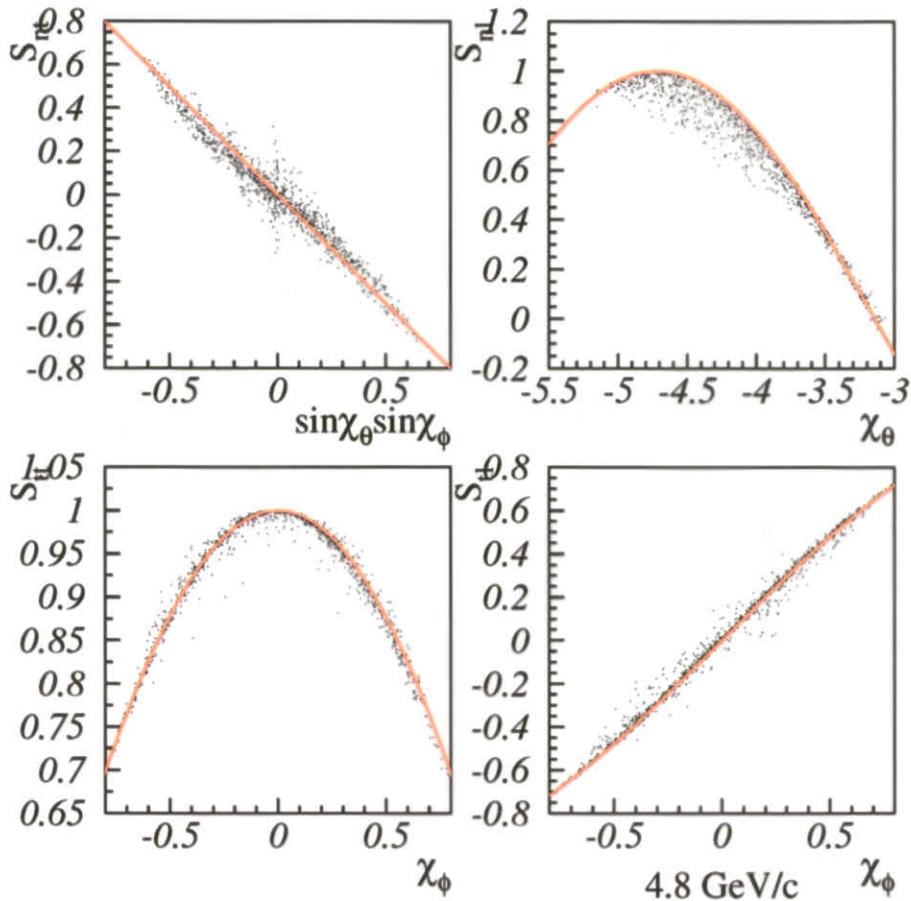
• $\vec{B}^{\parallel} = 0$

$$\chi_{\theta} = \gamma \left(\frac{g}{2} - 1 \right) \Delta\theta = f \cdot \Delta\theta$$

$$\chi_{\phi}(s) = \int_0^s \cos\chi_{\theta}(s) f d\phi(s) \simeq f \cdot \Delta\phi,$$

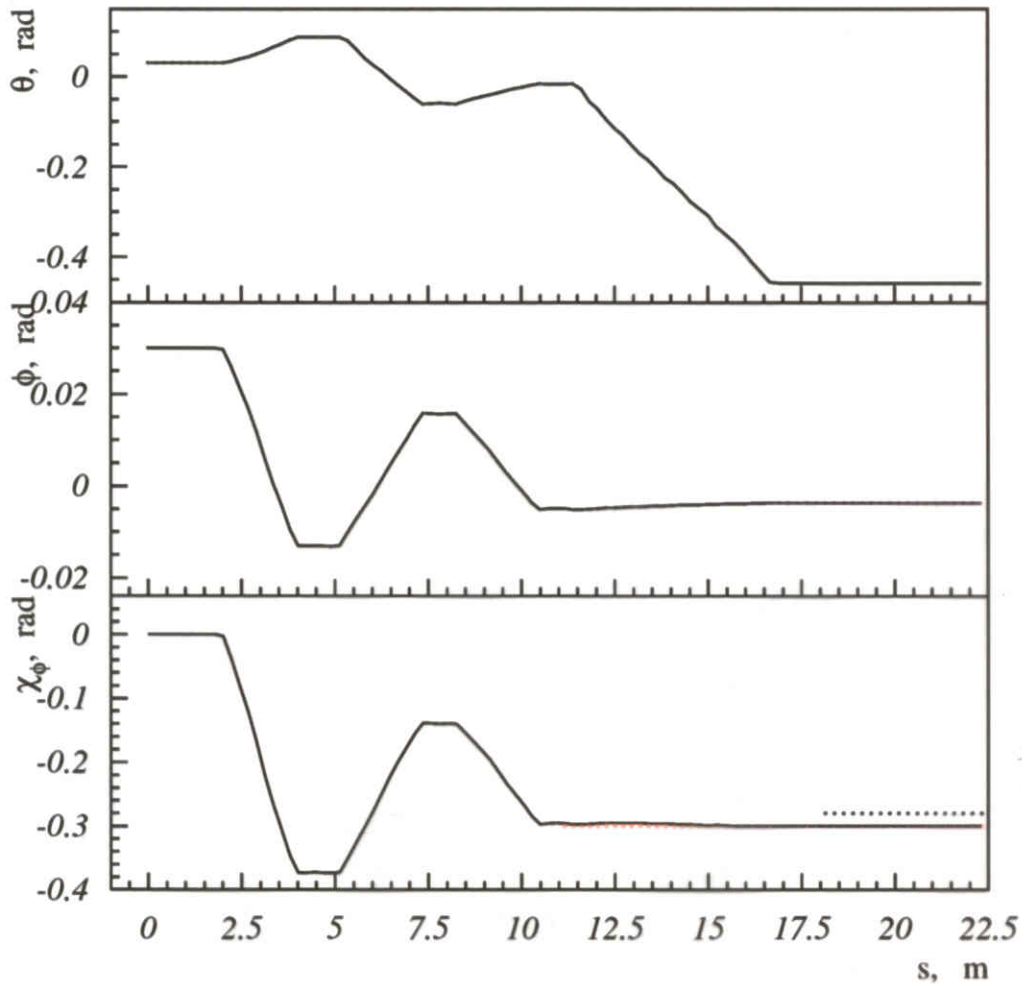
$$S_{nt} = -\sin\chi_{\theta} \sin\chi_{\phi} \quad S_{nl} = \sin\chi_{\theta}$$

$$S_{tt} = \cos\chi_{\phi} \quad S_{tl} = \sin\chi_{\phi}$$



HMS is the best spectrometer for polarization measurements

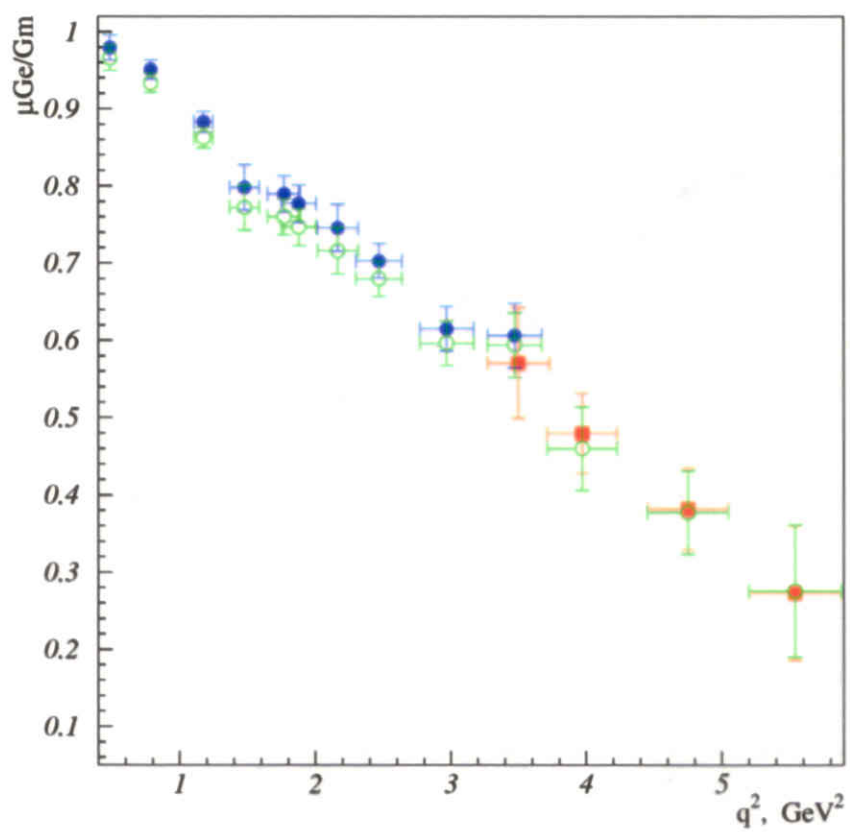
$$\chi_\phi(s) = \int_0^s \cos\chi_\theta(s) f d\phi(s) \quad \chi_\theta = f \cdot \Delta\theta$$

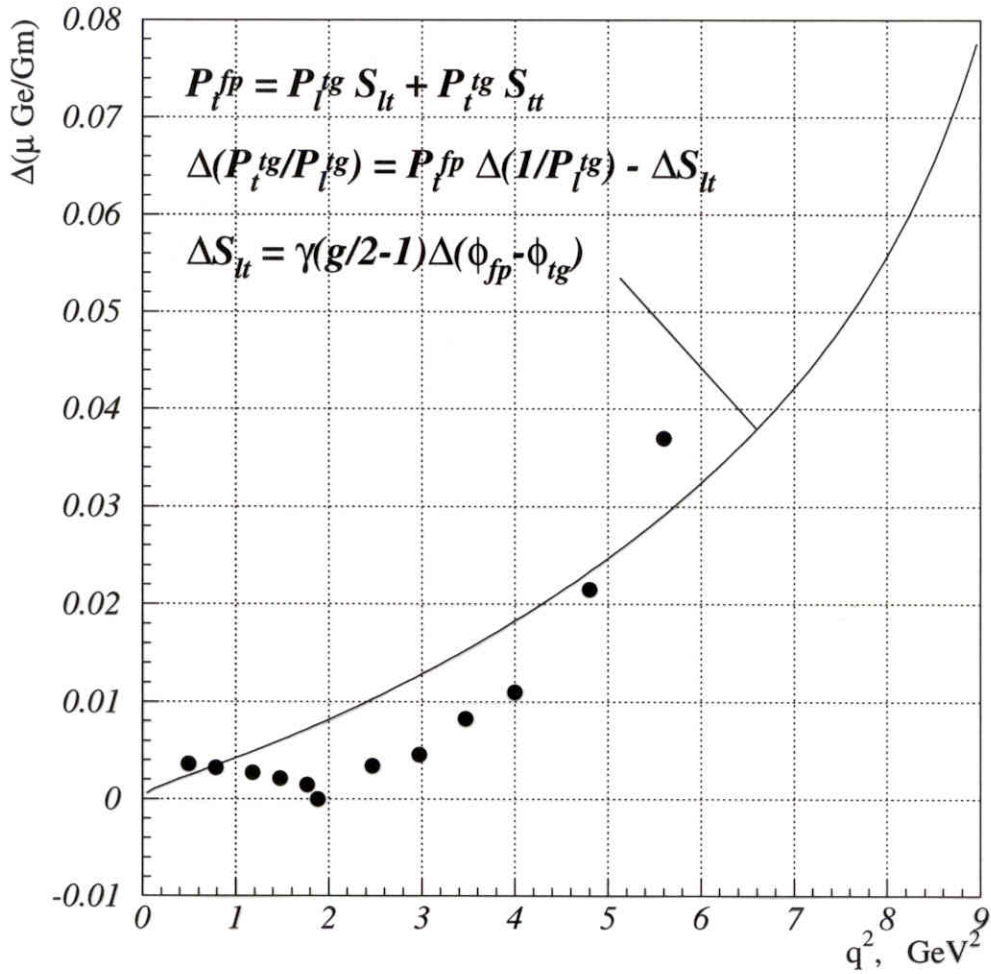


$$\chi_\phi(s) = \int_0^s \cos(\sim 0) f d\phi(s) + \int_0^s \cos\chi_\theta(s) f \cdot 0,$$

$$\chi_\phi(s) = f \cdot \Delta\phi + 0,$$

$$\mu G_e / G_m$$



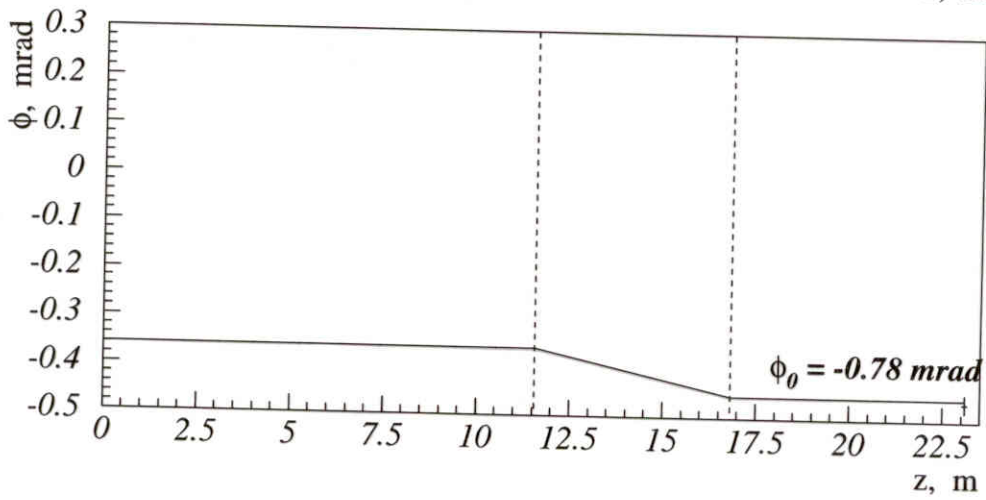
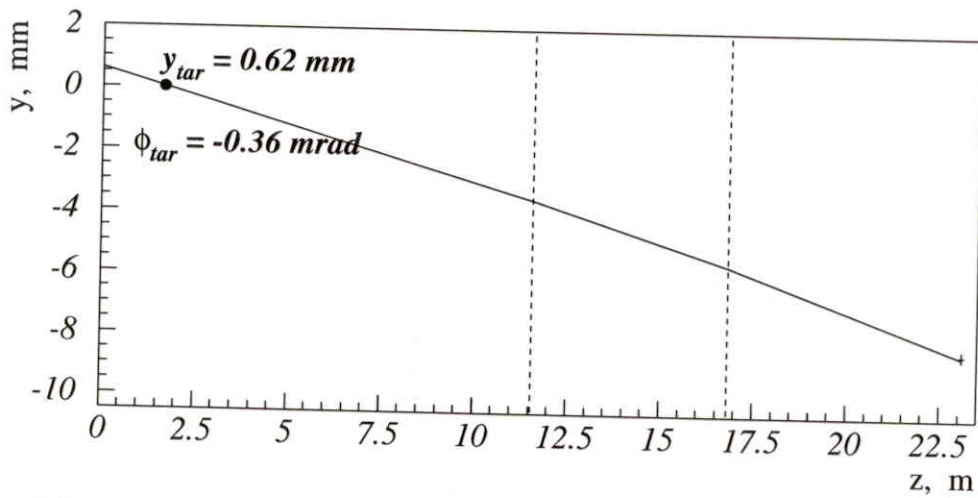


$$\Delta(\phi_{fp} - \phi_{tg}) = 1 \text{ mrad}$$

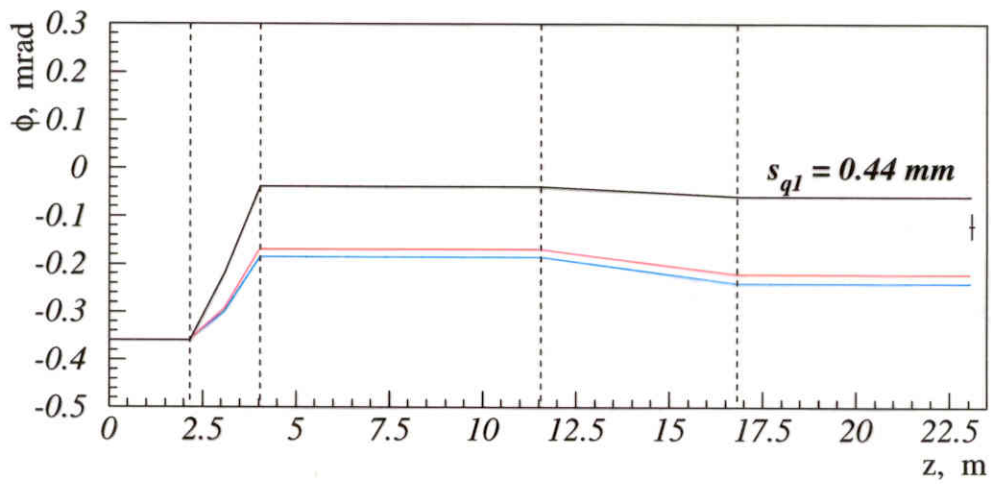
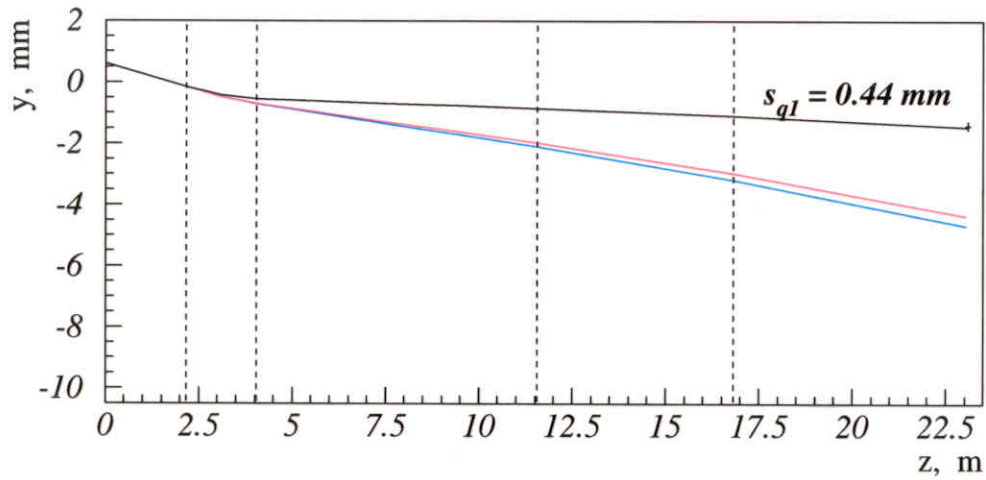
Elastic scattering of a 1.202GeV beam on 0.69cm carbon target at 13.15° with sieve slit

Name	Q1	Q2	Q3
nom.	1	1	1
"d"	0	0	0
"q1"	-0.7003	0	0
"q2"	0	0.3959	0
"q3"	0	0	-0.5745
"q1r"	0.7	1	1
"q2r"	1	0.7	1
"q3r"	1	1	0.7

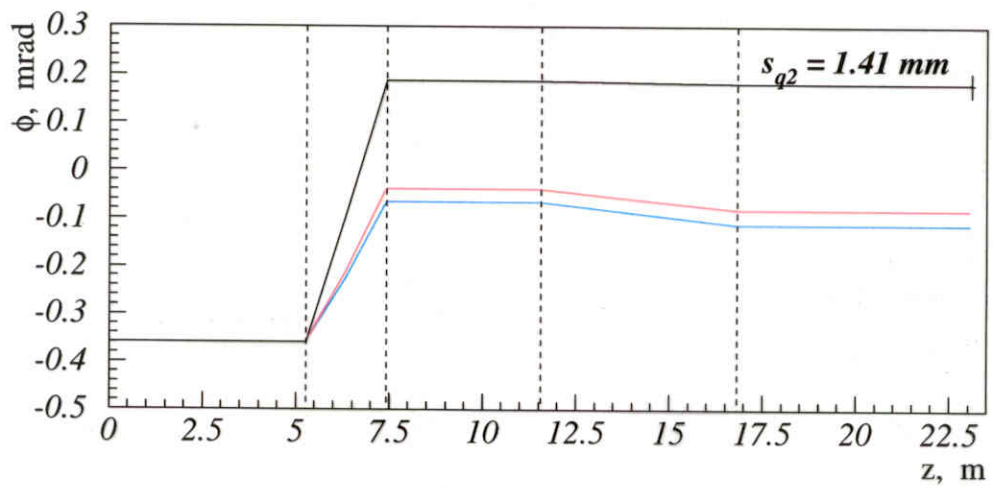
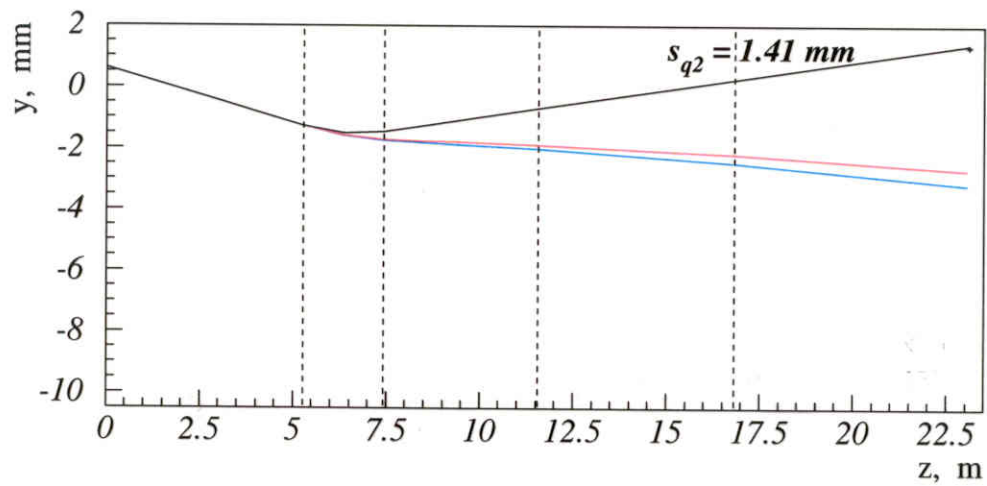




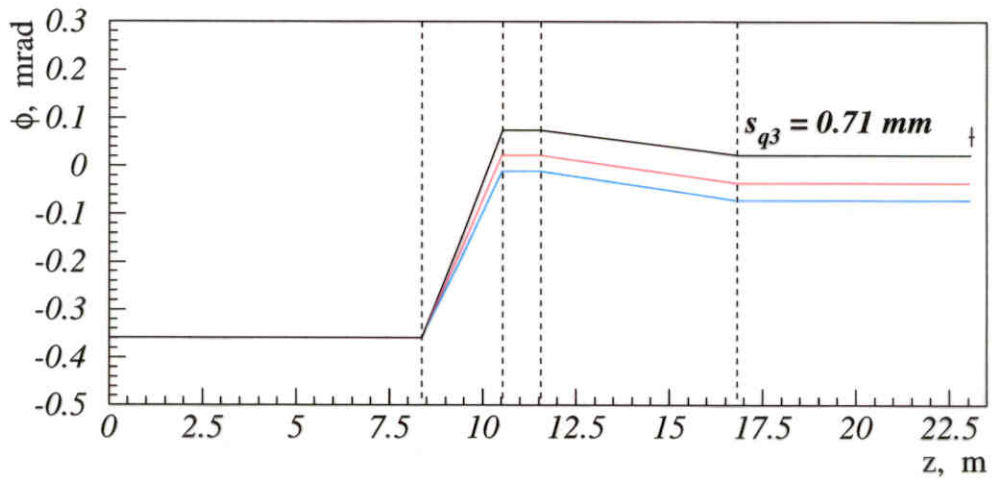
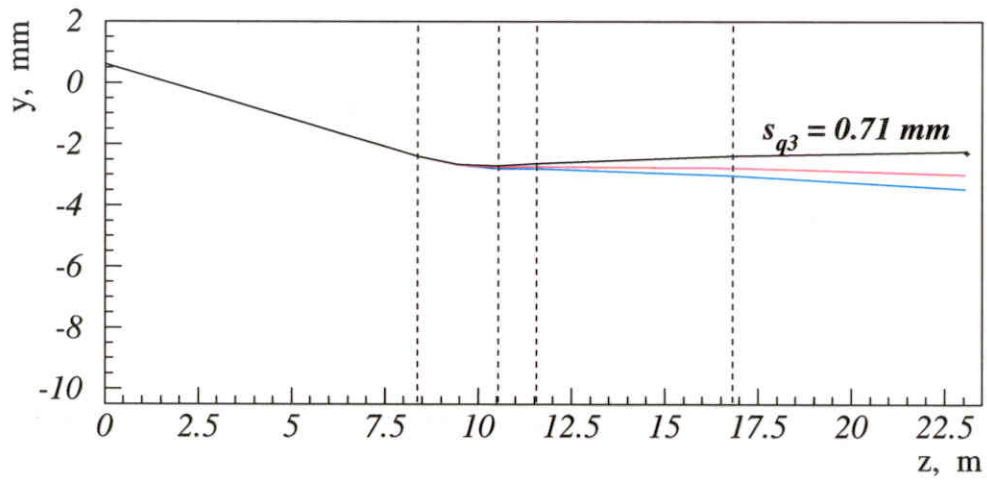
dipole only



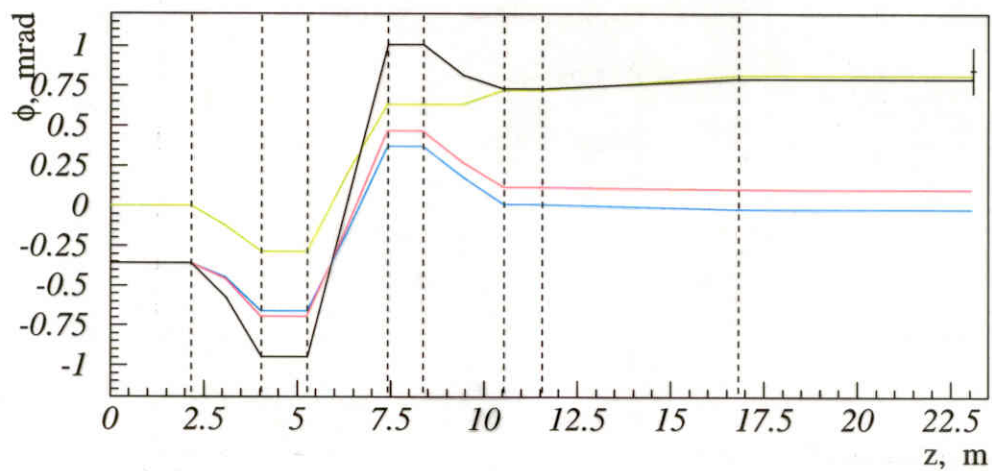
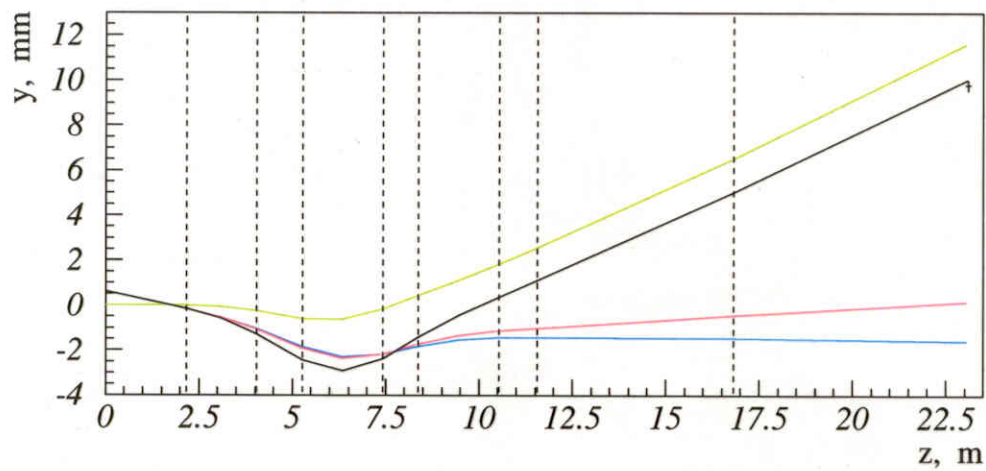
dipole $+q_1$



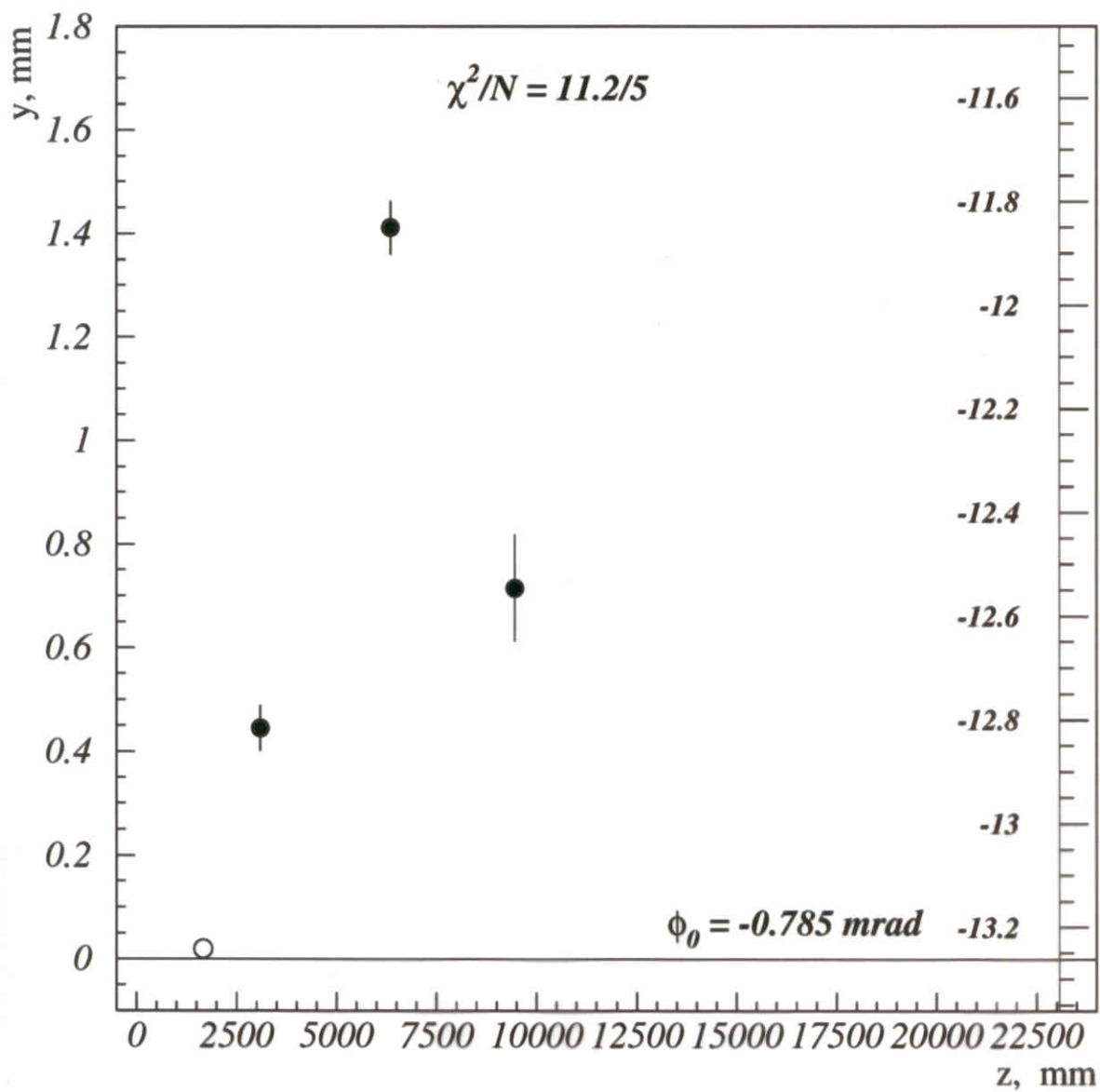
dipole + q2



dipole + q3



nominal setting



uncertainty of $\Delta\phi < 0.3 \text{ mrad}$

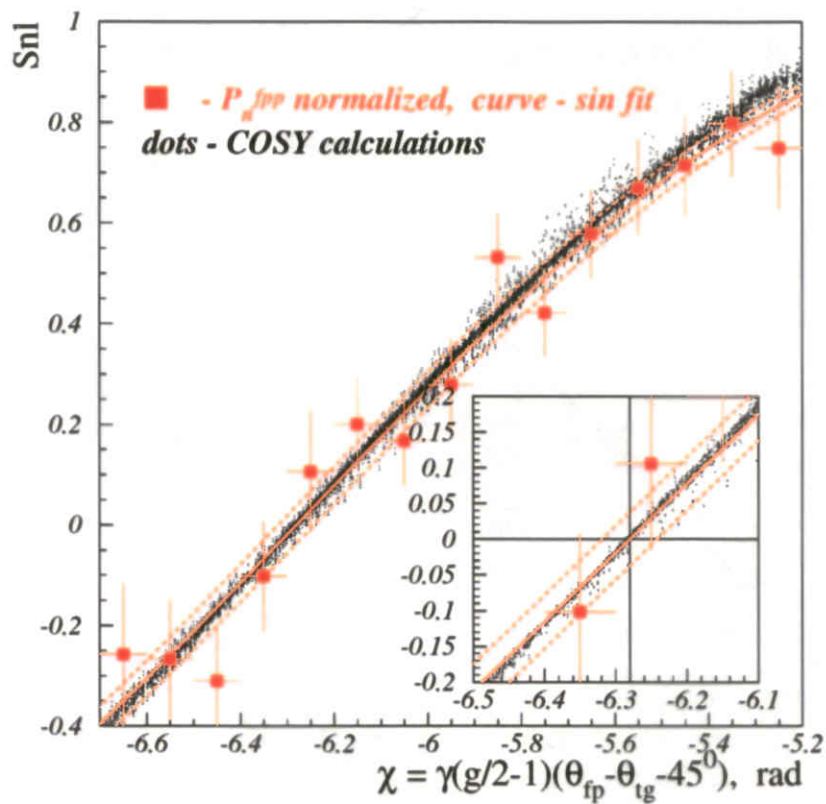
Measuring the total bending angle in dispersive plane

$$P_n^{fpp} \sim S_{nl}$$

$$\Delta\chi = 35\text{mrad}$$

$$\Delta\theta = 4.4\text{mrad}$$

GEP-II experiment for $Q^2 = 5.6\text{GeV}^2$



CONCLUSIONS

- For HMS, the spin matrix elements with very good precision are functions only of the bend angles, therefore, **HMS is very good for spin measurements**
- The total bend angle in the non-dispersive plane $\Delta\phi$ has been measured with a precision of less than 0.3mrad