

Measurement of the  
Parity Violating Asymmetry  
in the  $N \rightarrow \Delta$  Transition

*(E04-101)*

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*College of William & Mary*

*for the*

*G0 Collaboration*

# Overview

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- Purpose:
  - Precise measurement of  $G^A_{N\Delta}$  and  $M_A$
- Data:
  - Runs concurrently with  $G^0$  Backward Angle:
    - Elastically scattered e's:  $G^0$
    - Inelastically scattered e's:  $N \rightarrow \Delta$
- Status:
  - Taking data:
    - LD2 @ 362MeV currently, 687MeV in March
  - Preliminary data analysis:
    - LH2 @ 362MeV & 687MeV
    - LD2 @ 687MeV

# Motivation

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- Measuring  $G_{N\Delta}^A$ 
  - General axial form factor for  $N$ 
    - How is the spin distributed?
  - Axial form factor for  $N \rightarrow \Delta^+$ 
    - How is the spin redistributed during transition?
- $A_{N\Delta}$  gives *direct access* to  $G_{N\Delta}^A$ 
  - Directly measure the axial (intrinsic spin) response during  $N \rightarrow \Delta^+$
- Axial mass  $M_A$ :
  - Describe  $Q^2$  dependence of  $G_{N\Delta}^A$

# Motivation

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- Reaction Mechanism (CQM)
  - $G^0$   $N$ - $\Delta$  Measurement:  $Z^0$  exchange (Neutral Current)
    - $ep \rightarrow e\Delta^+$ 
      - $Z^0$  induces quark spin flip
      - c.f.  $MI$  from  $\gamma$  induced quark spin flip
  - Previous Measurements:  $W^+$  exchange (Charged Current)
    - $\nu p \rightarrow \mu^- \Delta^{++}$  ,  $ep \rightarrow \pi^- \Delta^{++}$ 
      - Quark flavor change and spin flip
        - » different reaction mechanism

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→ *First measurement in neutral current process*

# Theory

$$A_{inel} = -\frac{G_F Q^2}{4\pi\alpha\sqrt{2}} \left[ \Delta_{(1)}^\pi + \Delta_{(2)}^\pi + \Delta_{(3)}^\pi \right]$$

$\Delta_{(1)} = 2(1 - \sin^2\theta_w) = 1$  (Standard Model)

$\Delta_{(2)} =$  non-resonant contrib. (small)

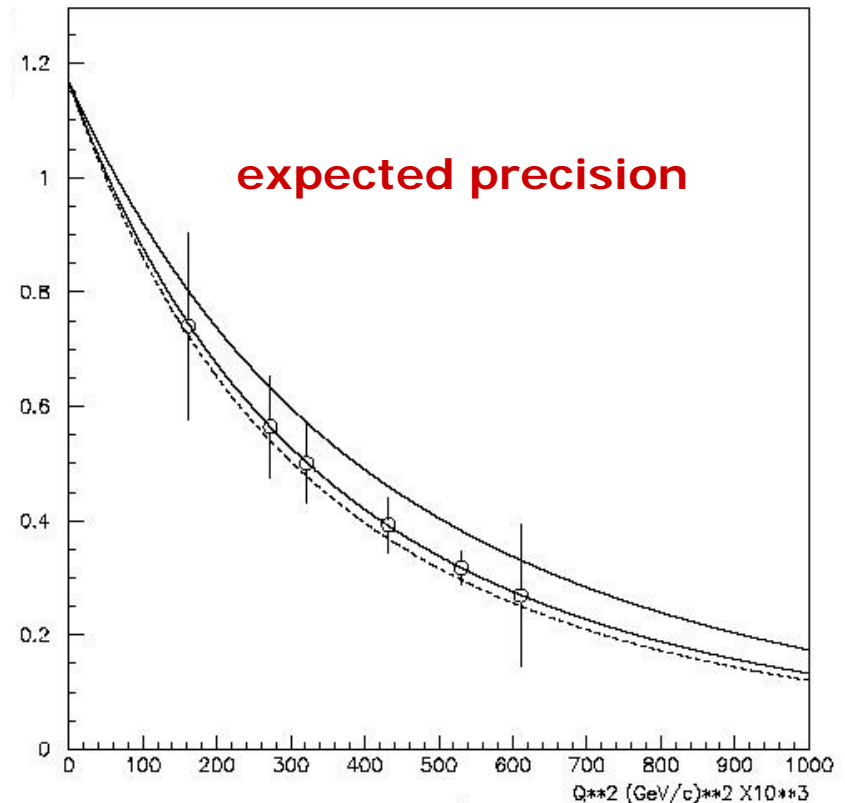
$\Delta_{(3)} = 2(1 - 4\sin^2\theta_w) F(Q^2, s) \rightarrow$  (*N- $\Delta$  resonance*)

At tree-level:

$$F(Q^2, s) \rightarrow G_{N\Delta}^A(Q^2)$$

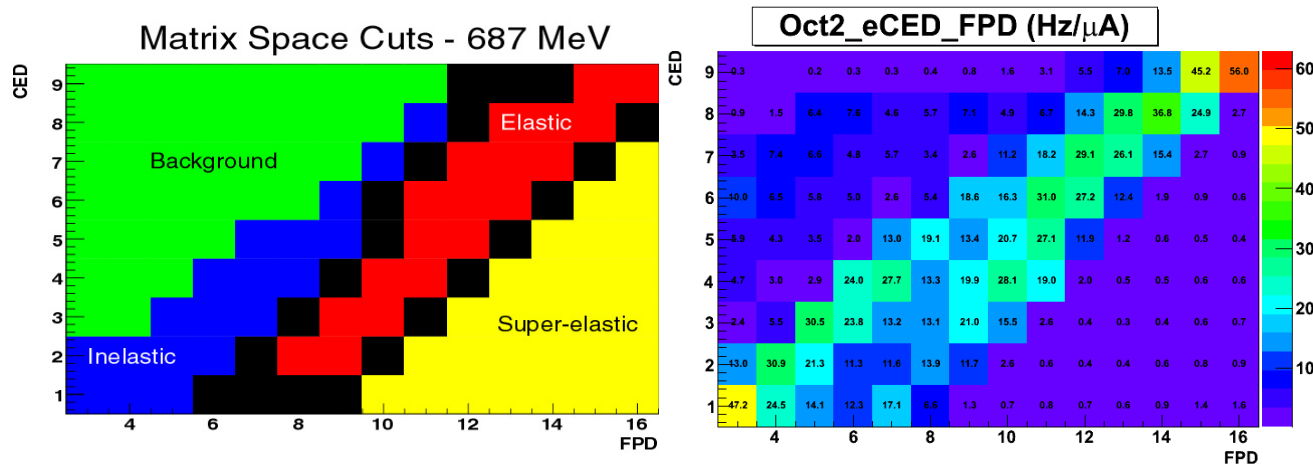
- $F$  contains kinematic information & all weak transition form factors  
 $\rightarrow$  Extract  $G_{N\Delta}^A$  from  $F$

$G_{N\Delta}^A(Q^2)$  vs  $Q^2$



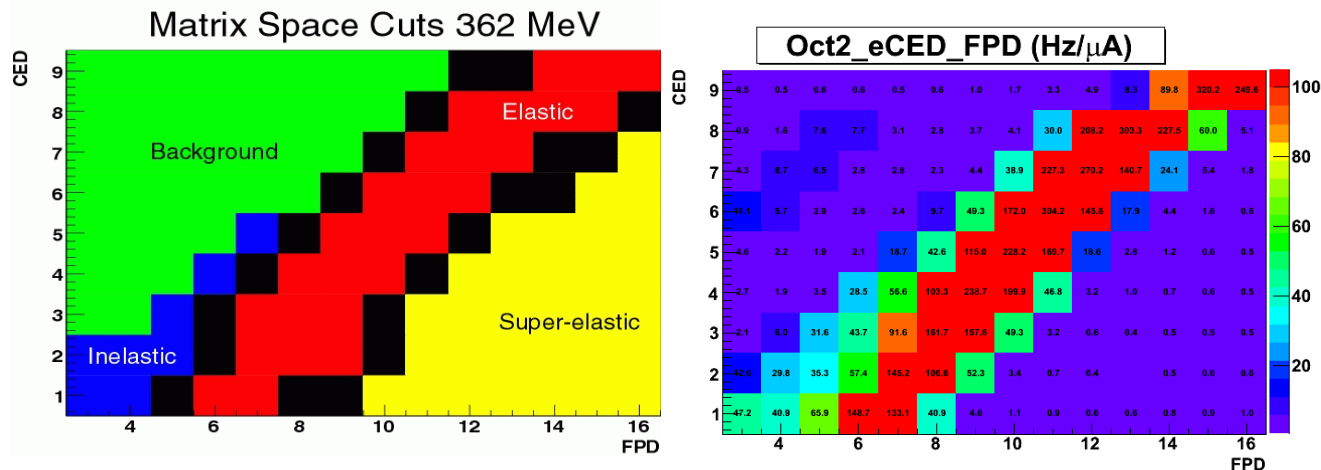
# Coincidence Rates: LH<sub>2</sub>

- High Energy LH<sub>2</sub>



**Total Charge  
Accumulated:  
~ 100C**

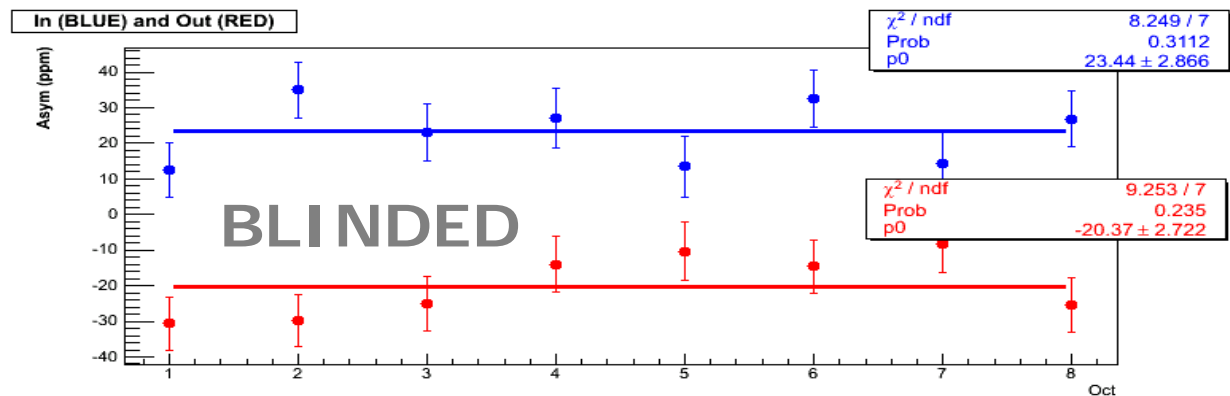
- Low Energy LH<sub>2</sub>



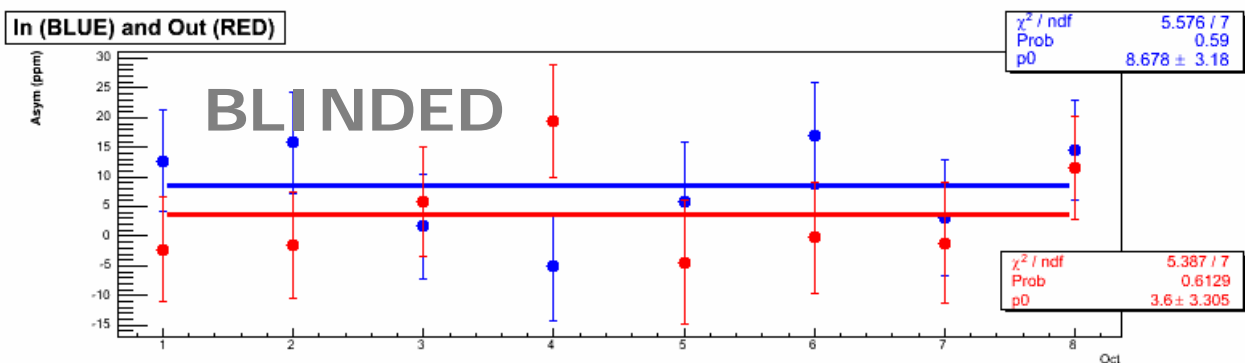
**Total Charge  
Accumulated:  
~ 90C**

# Asymmetries: LH<sub>2</sub>

- High Energy LH<sub>2</sub>: Average Along Inelastic Locus



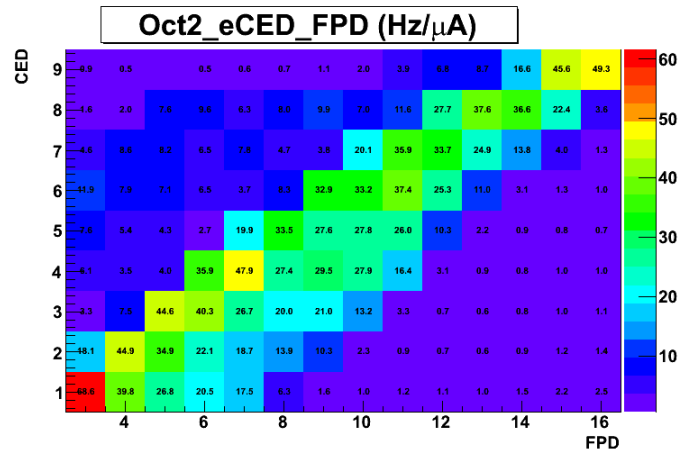
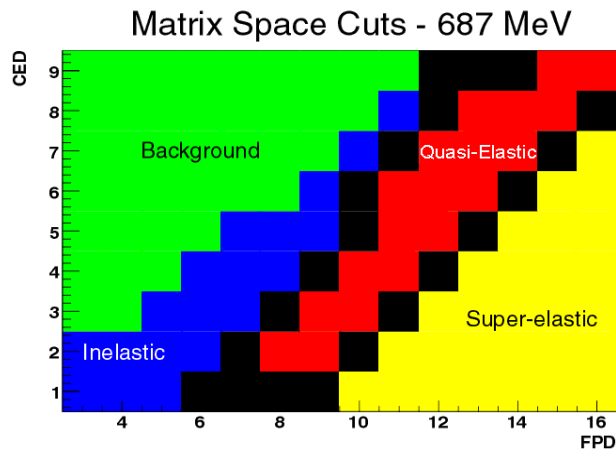
- Low Energy LH<sub>2</sub>: Average Along Inelastic Locus



→ Raw Asymmetries – no corrections!

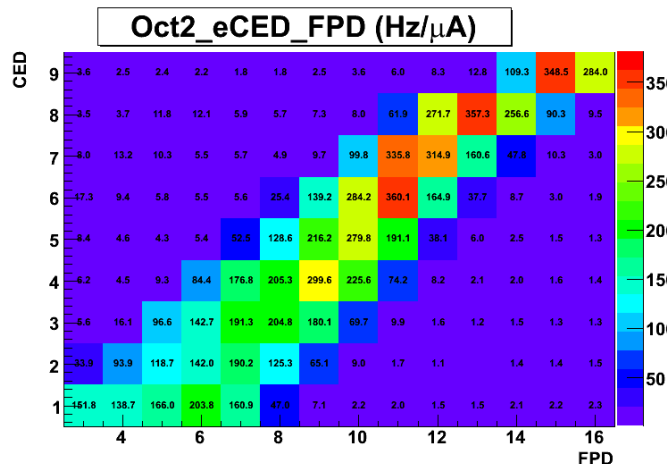
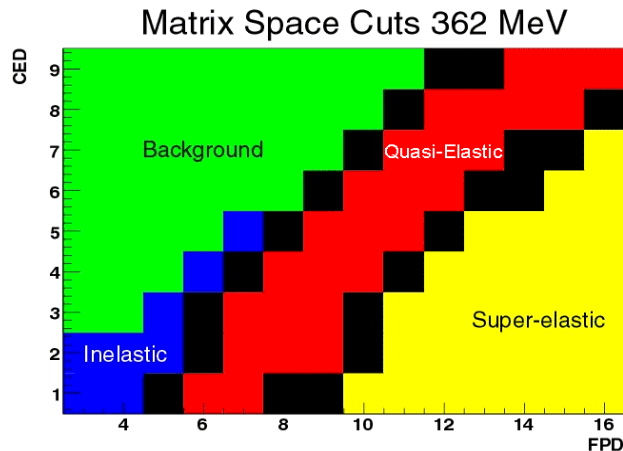
# Coincidence Rates: LD<sub>2</sub>

- High Energy LD<sub>2</sub>



**Total Charge Accumulated:**  
~ 37C  
*(more to come)*

- Low Energy LD<sub>2</sub>

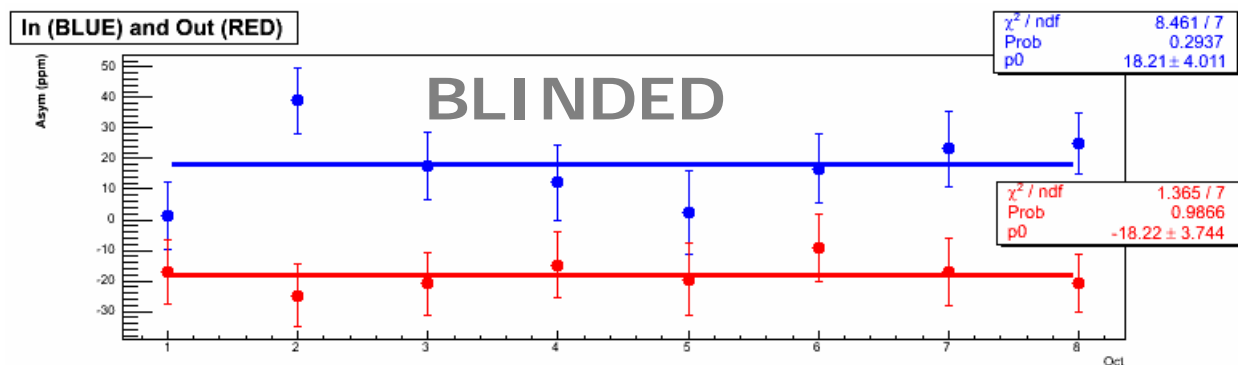


**Total Charge Accumulated:**  
~ 26C  
*(more to come)*

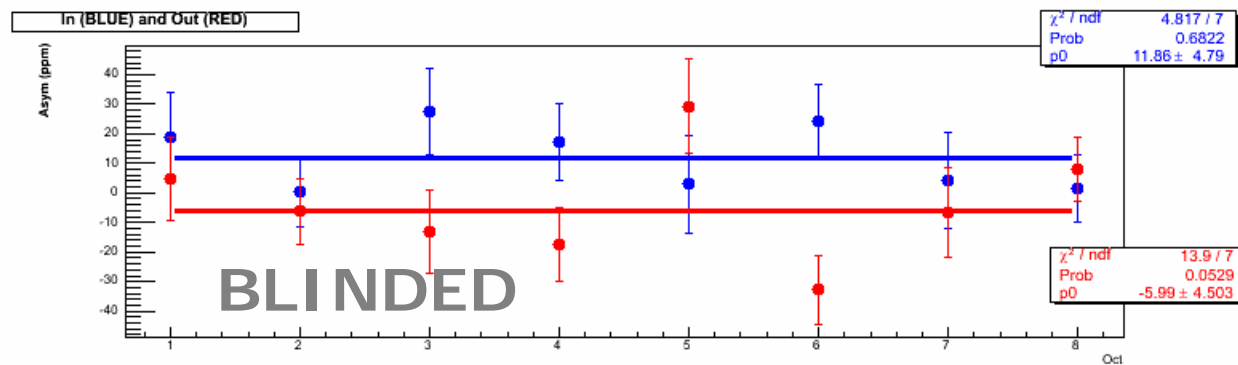


# Asymmetries: LD<sub>2</sub>

- High Energy LD<sub>2</sub>: Average Across Inelastic Locus



- Low Energy LD<sub>2</sub>: Average Across Inelastic Locus



→ Raw Asymmetries – no corrections!

*A work in progress...*

# Analysis Strategy

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- General Corrections: Same process as  $G^0$ 
  - Beam/Instrument related
    - Dead time/Randoms
    - Helicity correlated beam properties
    - Beam polarization
  - Background
    - Dilution factors
    - Background from target
    - Pion contamination

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*Currently ongoing...*

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# Analysis Strategy

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- Specific to  $N \rightarrow \Delta^+$ 
  - Find  $Q^2$  “bins”
    - Use simulation results to find evolution of  $Q^2$  along locus
      - 2 or 3 bins for 687 MeV
      - 1 bin for 362 MeV
    - From here can find  $G^A_{N\Delta}(Q^2)$  and  $M_A(Q^2)$
- Note on  $LD_2$ :
  - Apply same process as  $LH_2$ 
    - Treat as an incoherent process
  - No dedicated calculation exists
    - Expect theoretical interest in such a measurement

# Summary

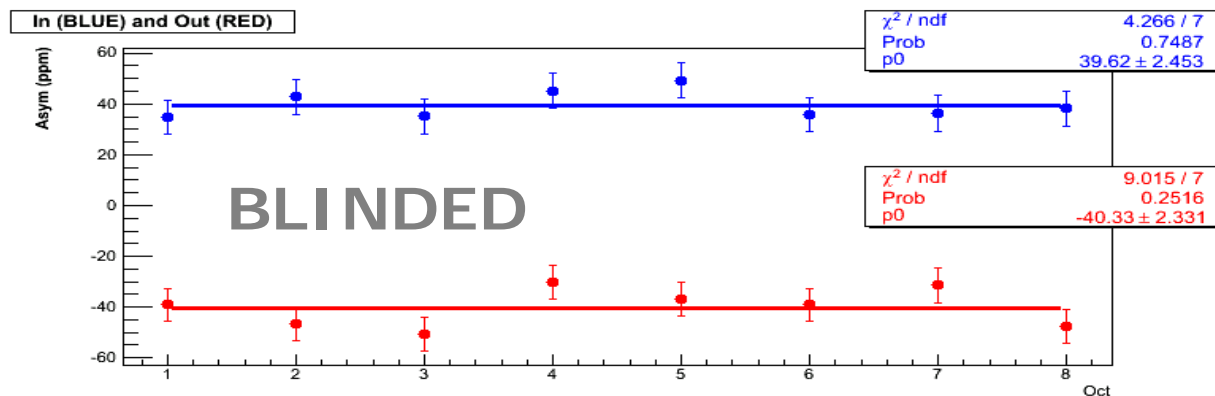
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- Measurement of  $G_{N\Delta}^A$ 
  - First time measurement in neutral current reaction
- Data Progress
  - $G^0$  Backward taking data until late March
- Analysis Progress
  - Working on corrections
    - Beam related
    - Backgrounds
  - Working with simulation
    - Finding the appropriate  $Q^2$  bins

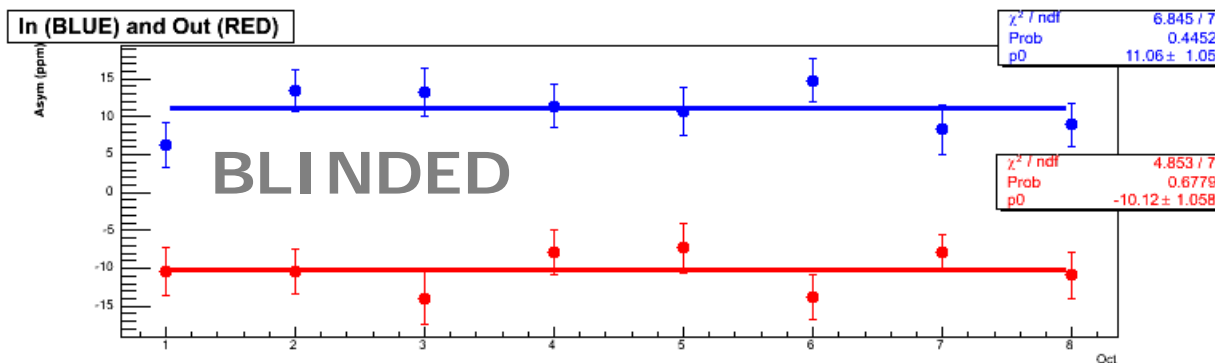
**The end... let the backups begin!!**

# Asymmetries: LH2

- High Energy LH2: Average Along Elastic Locus



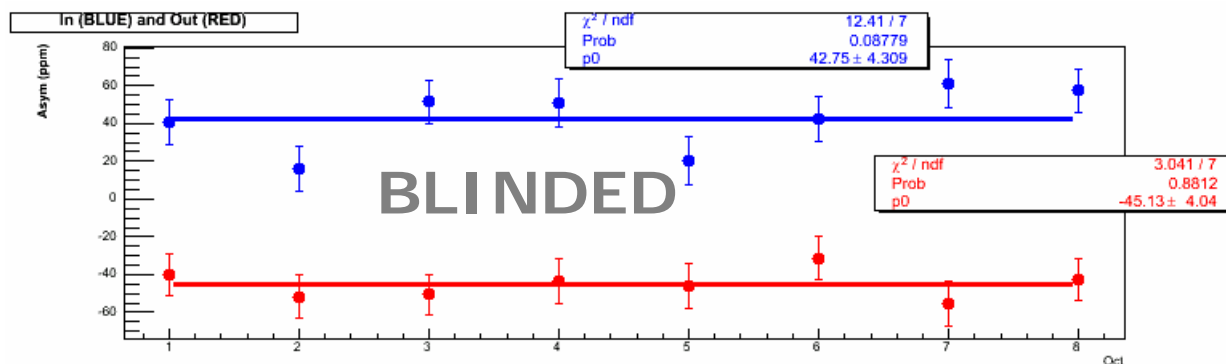
- Low Energy LH2: Average Along Elastic Locus



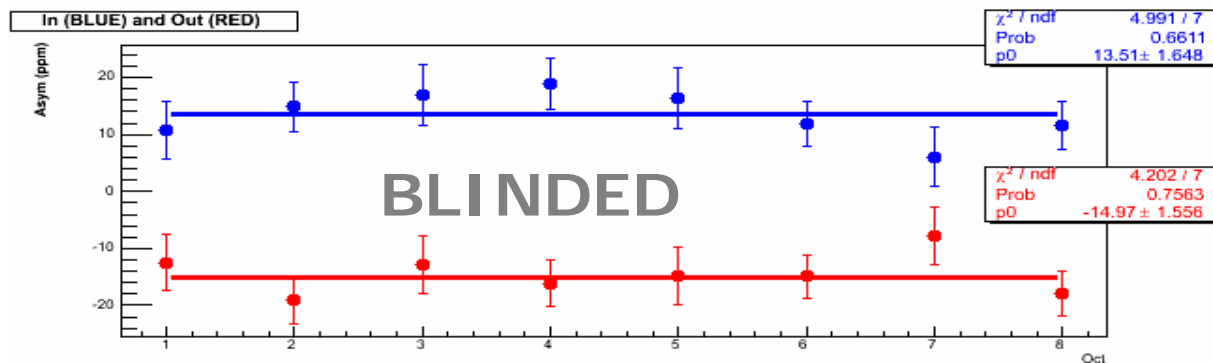
→Raw Asymmetries – no corrections!

# Asymmetries: LD2

- High Energy LD2: Average Across Elastic Locus



- Low Energy LD2: Average Across Elastic Locus



→ Raw Asymmetries – no corrections!

*A work in progress...*

# Non-resonant Contributions

*Nimai C. Mukhopadhyay et al., Nucl. Phys. A633,481 (1998)*

$E(\text{GeV})$	$\theta_{lab}(^\circ)$	$Q^2((\text{GeV}/c)^2)$	$\Delta_{(2)}^\pi / \Delta_{(3)}^\pi$
0.4	90	0.035	0.06
0.5	90	0.106	0.16
0.6	90	0.192	0.27
0.7	90	0.291	0.39

$\Delta_{(2)}^\pi(E_{0+}^{1/2,0,3/2}, S_{0+}^{1/2,0,3/2}, E_{1+}^{1/2,0,3/2}, M_{1+}^{1/2,0,3/2}, \text{etc.})$

*CLAS(ep, ed, etc. single  $\pi$  production w/polarization)*

*H. Schmieden, Eur. Phys. J. A1:427-433,1998*



The end again....

I told you this was the end, why are you  
still looking?

Are you calling me a liar?!

Ok, you got me... there are more... but  
they don't count!

Unused..... fun and games

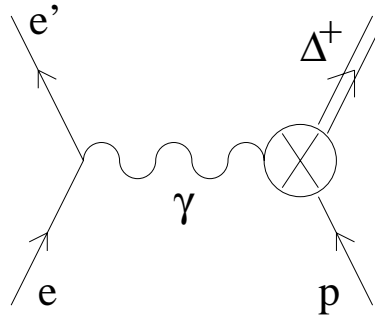
# Beam time, resource request

- \* *0 days*

- \* *0 additional resources*

- \* *Simultaneous* running w/ *G0 backward angle*

# Siegert Contribution



$$A_{PV}^{\gamma} \propto \frac{G_F}{\alpha} Q^2 \left[ a \frac{\omega}{Q^2} + \text{Anapole} \right]$$

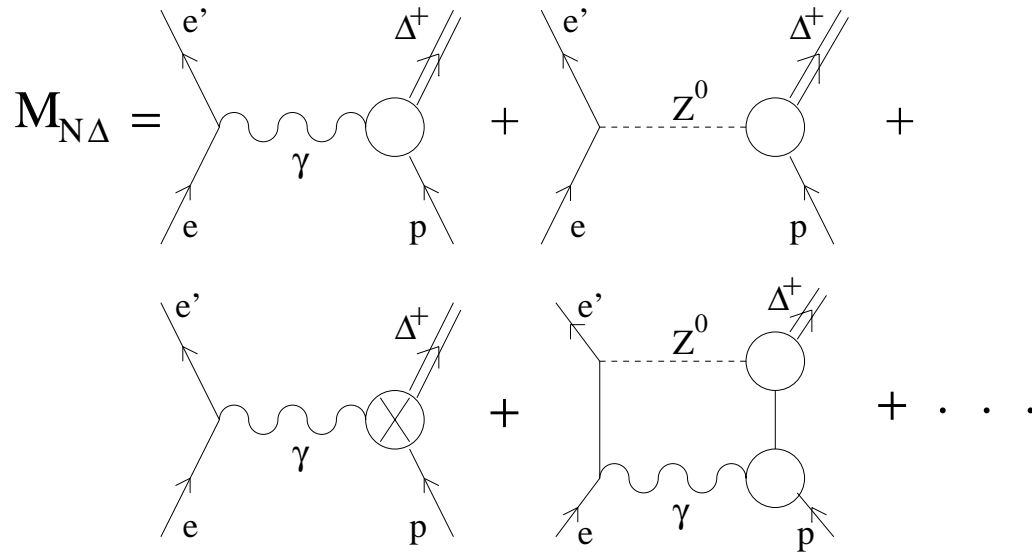
↑

PV  $\gamma N \Delta$  E1 amplitude (Siegert's Theorem)  $\rightarrow \mathbf{d}_{\Delta} (\sim g_{\pi})$

$$\rightarrow A_{PV}^{\gamma} (Q^2 = 0) \neq 0!$$

Same **M.E.** driving Weak Hyperon Decay (e.g.  $\Sigma^+ \rightarrow p \gamma$ )

# Radiative Corrections

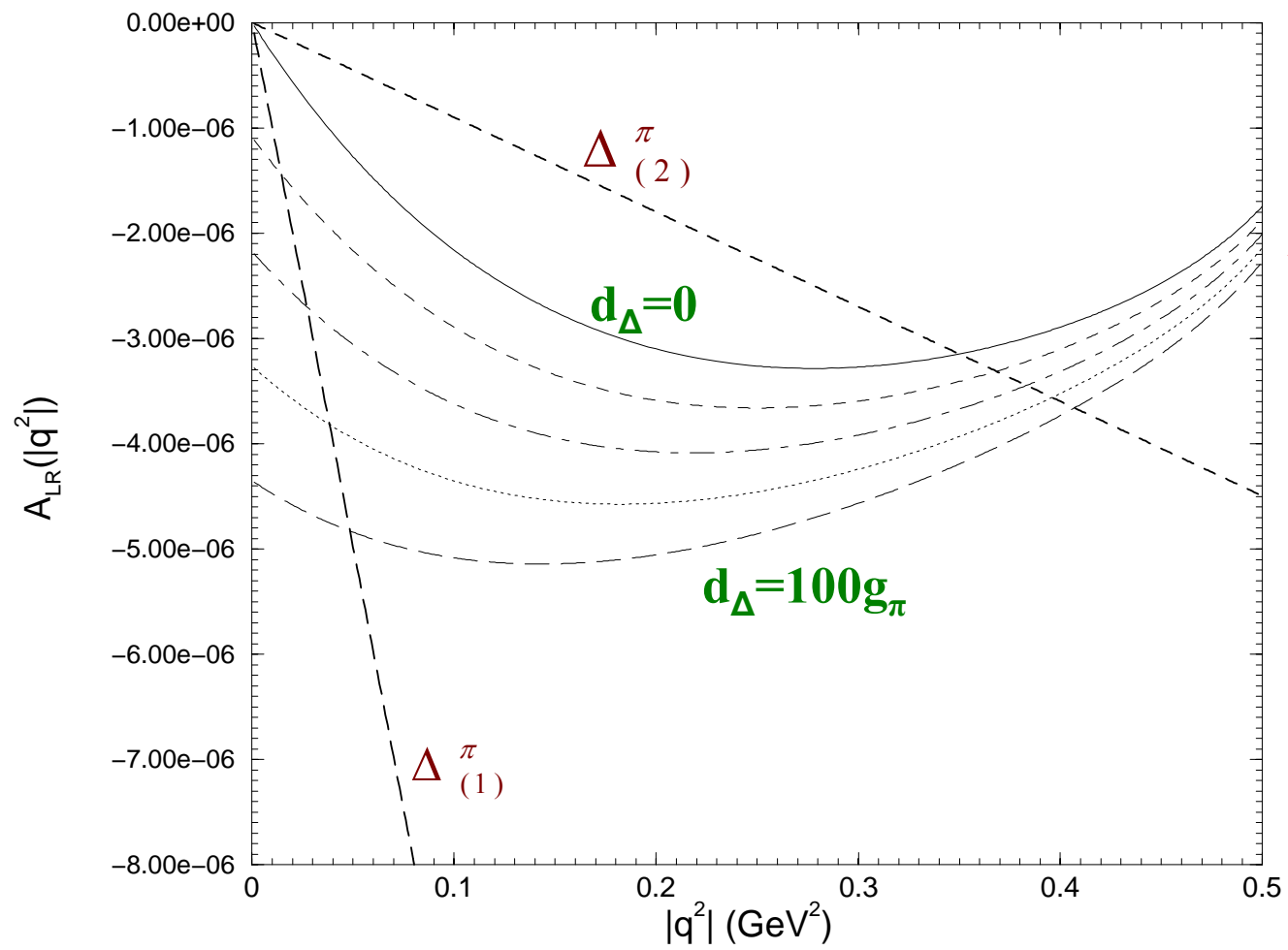


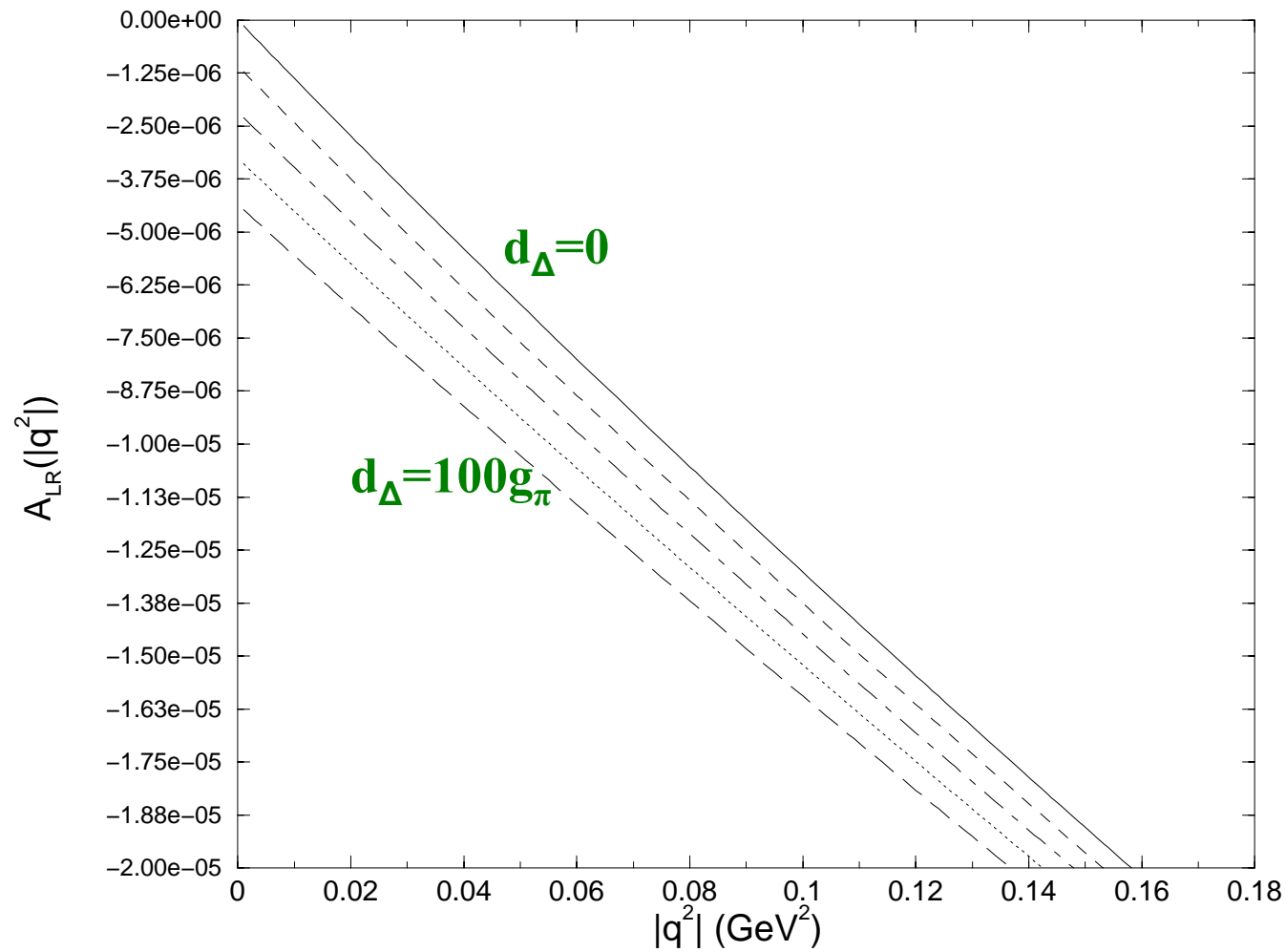
$$\Delta_{(3)}^{\pi} \propto \left(1 + R_A^{\Delta}\right) G_{N\Delta}^A$$

$$R_A^{\Delta} = R_A^{ewk} + R_A^{Siegert} + R_A^{Anapole} + R_A^{Box} + \dots$$

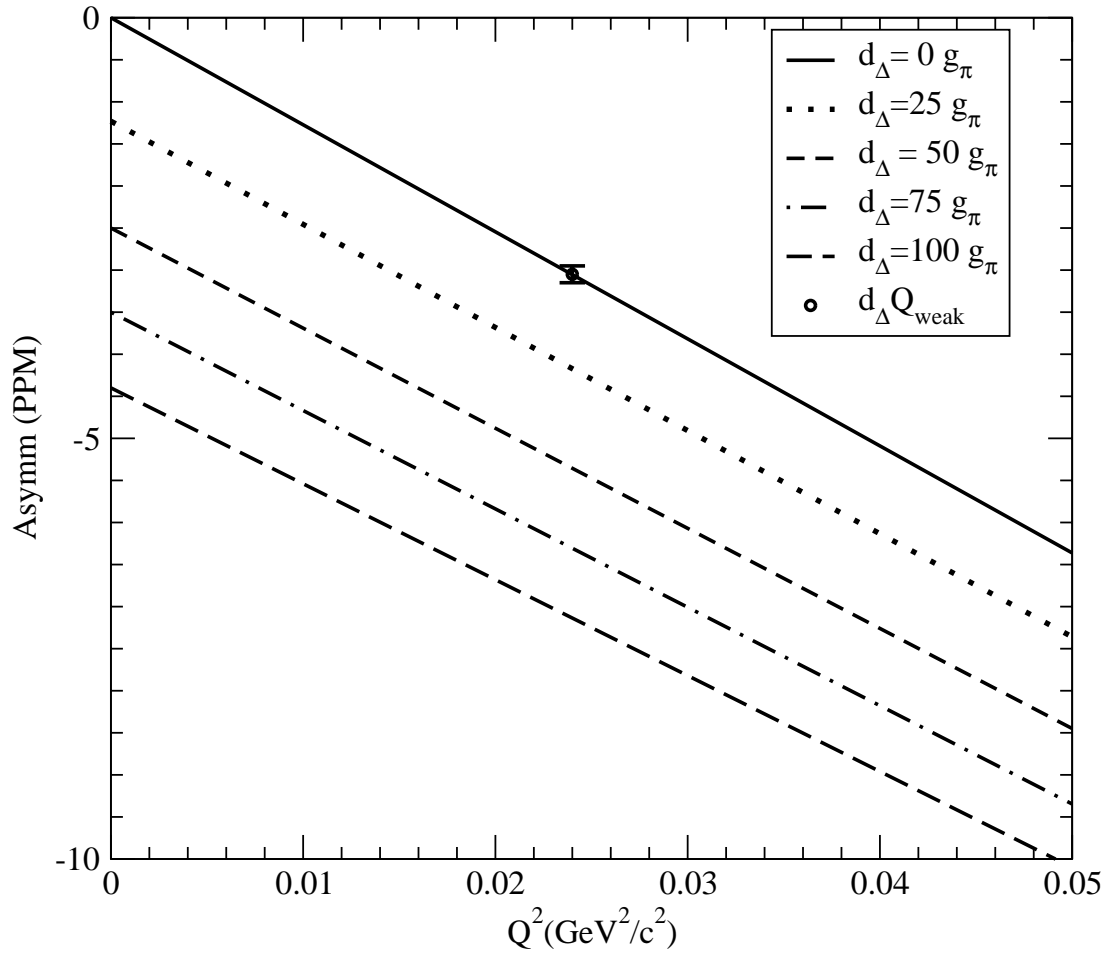
S.-L. Zhu et al., hep-ph/0107076 (July 2001)







Q



PAC24 LOI

*LaTech*

1 week beam time

# Asymmetries: LD2 @ 362MeV

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- Inelastic Locus w/o Randoms Correction

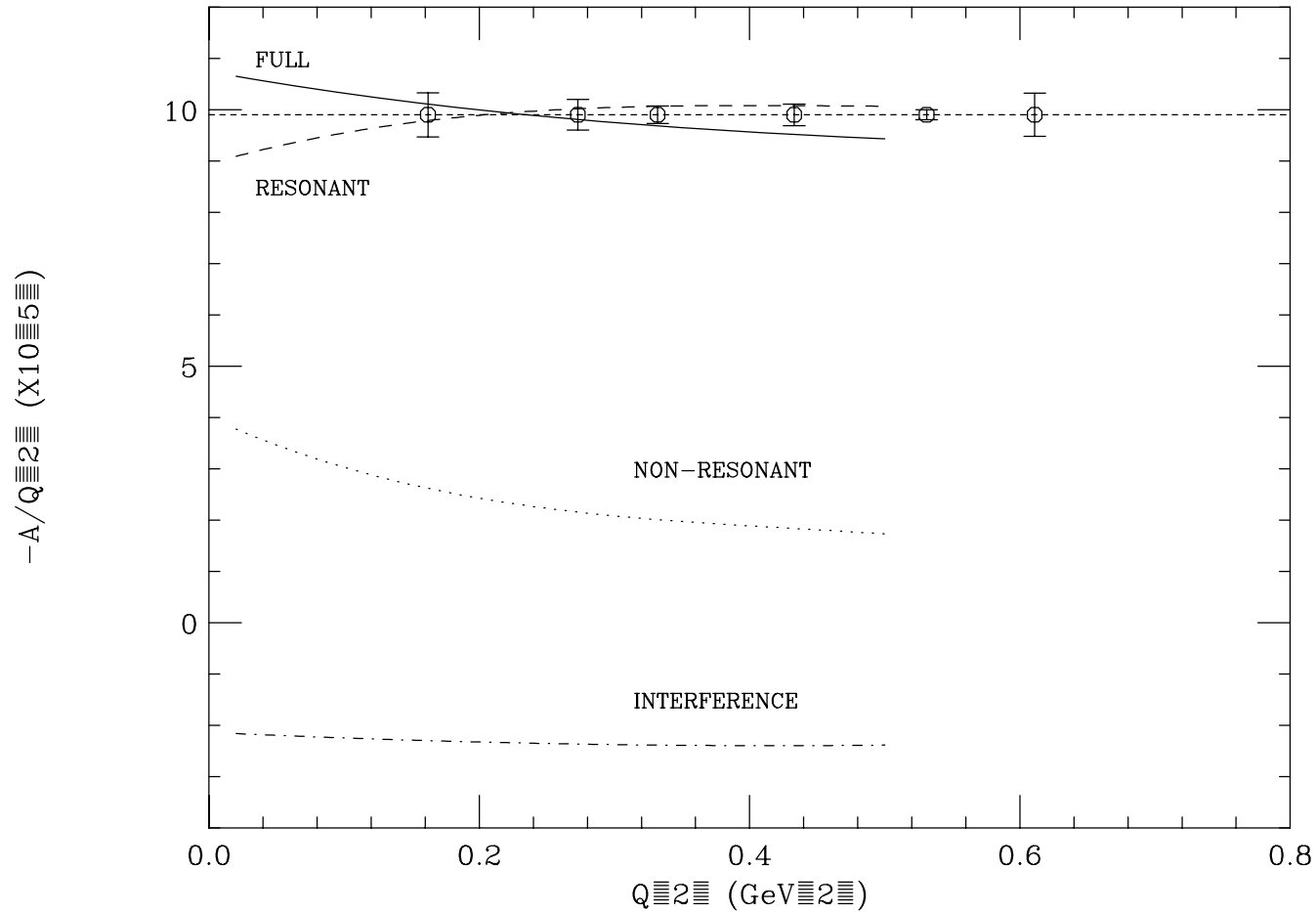
BLINDED

- Inelastic Locus w/ Randoms Correction

BLINDED

A work in progress...

# Effective Lagrangian Model



$E=424,585,799 \text{ MeV}$

700 hours each

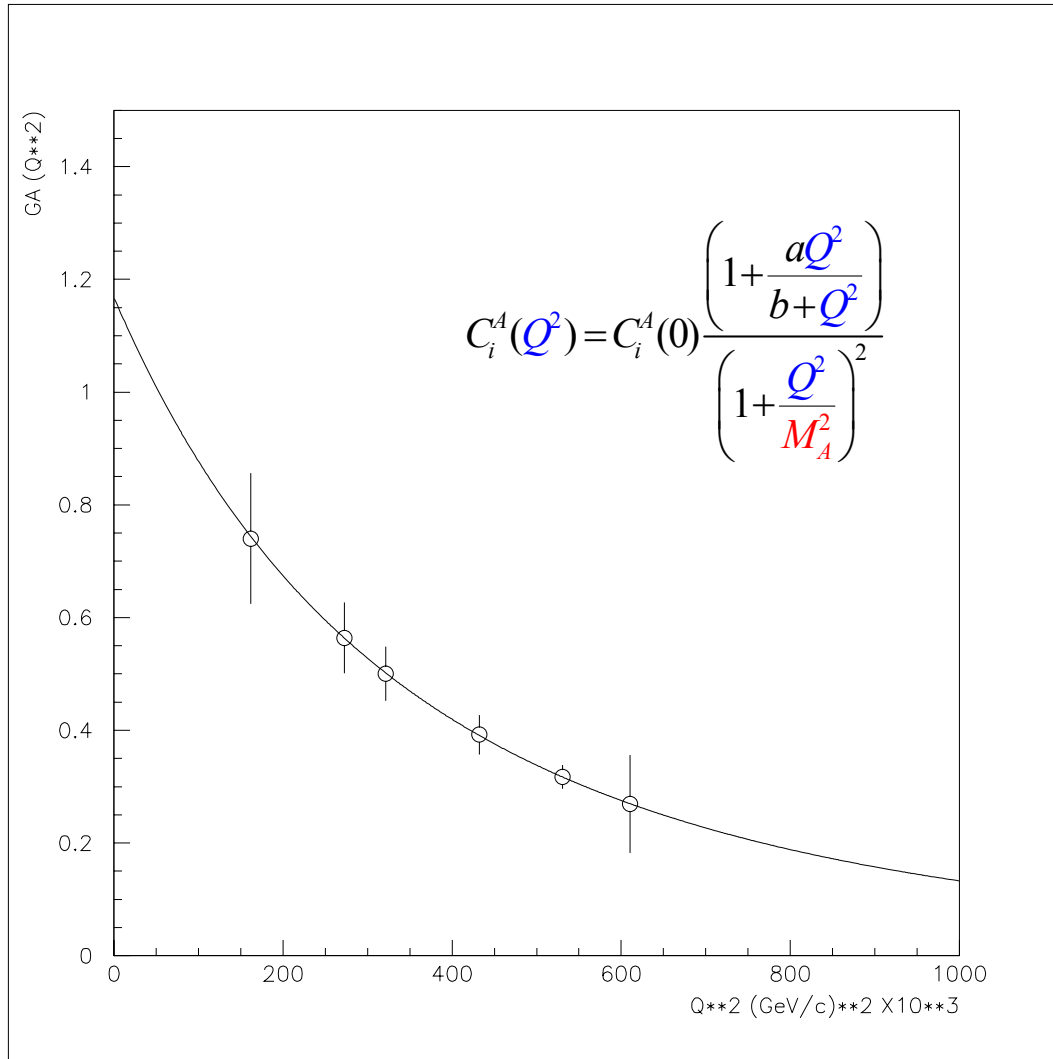
$P=70\%$

$I=80 \mu\text{A}$

20 cm  $\text{LH}_2$

*H.-W. Hammer and D. Drechsel, Z. Phys. A353, 321 (1995)*

# Adler Model (modified dipole form)



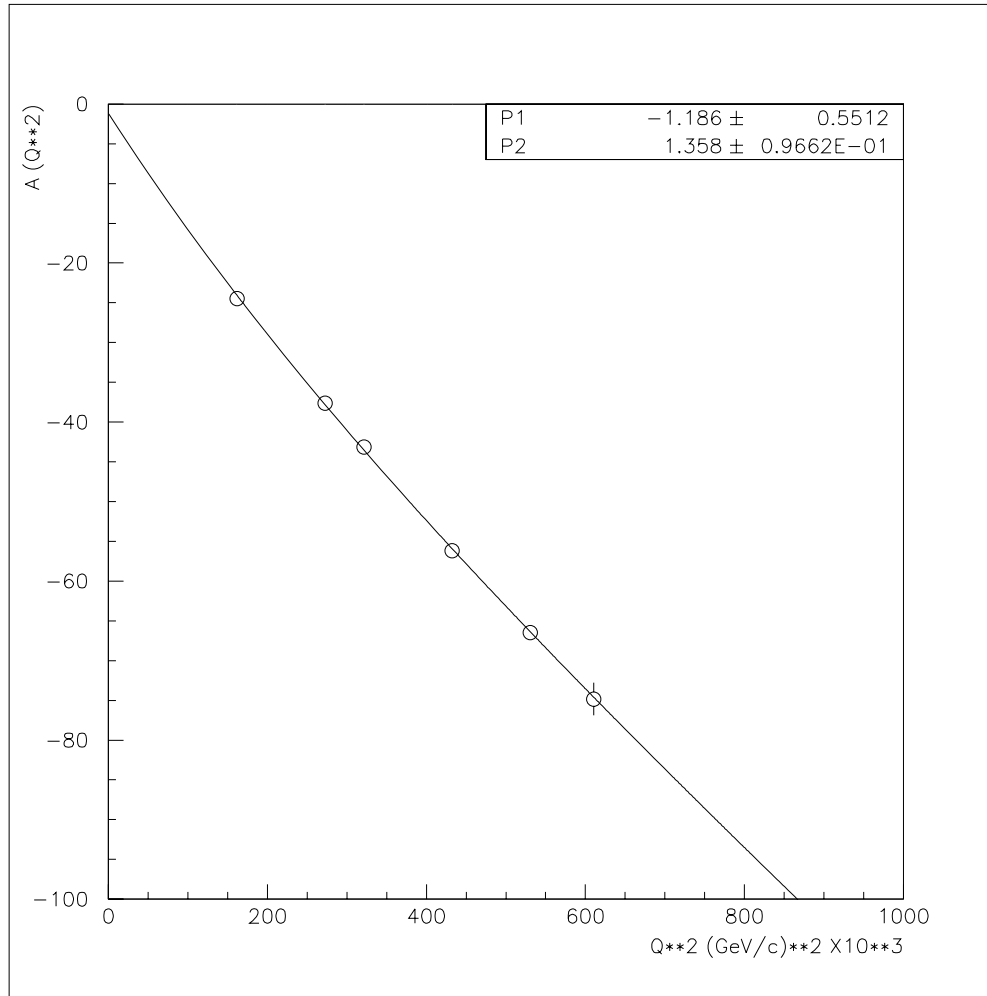
$$\delta M_A = 0.031 \text{ GeV}$$

vs.

$$\delta M_A^v = 0.090 \text{ GeV}$$

*S.L. Adler, Ann. Phys. 50, 189 (1968)*

# Effect on $\delta M_A$

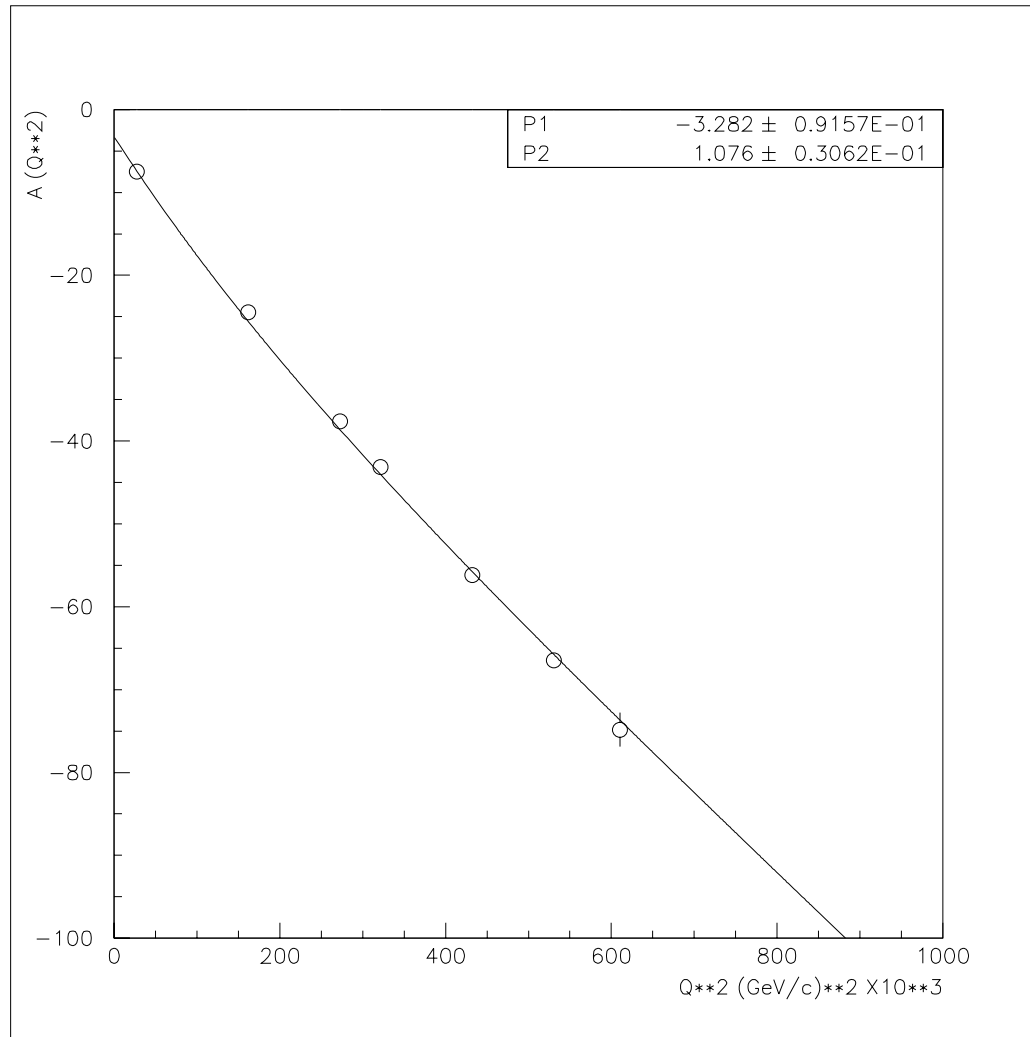


$$\delta d_{\Delta} = 0.55 \text{ ppm}$$

$$\sim 14 g_{\pi}$$

$$\delta M_A = 0.097 \text{ GeV}$$

$\delta M_A, \delta d_\Delta$  w/  $G0$  &  $Q_{weak} N \rightarrow \Delta$

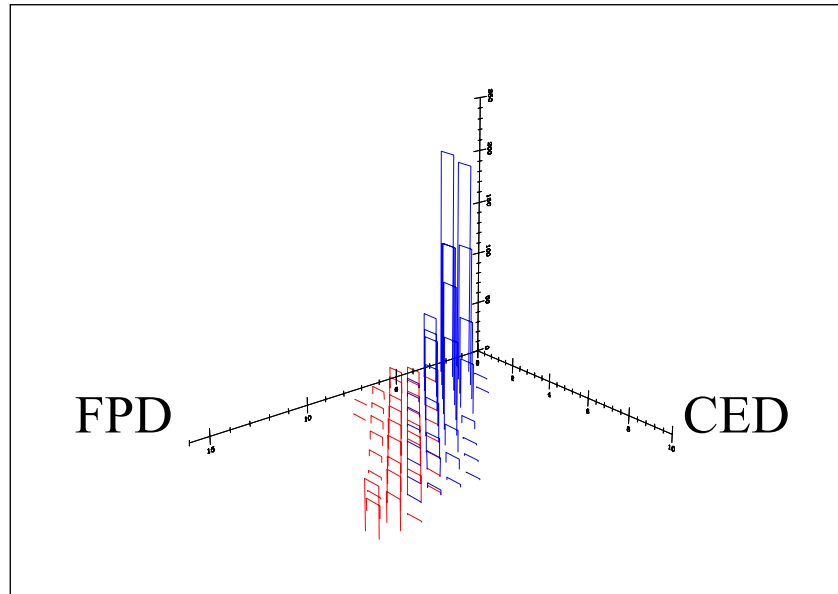


$$\delta d_\Delta = 0.091 \text{ ppm}$$
$$\sim 2.3 g_\pi$$

$$\delta M_A = 0.031 \text{ GeV}$$



# Elastics, Inelastics, and Contamination



- Elastics

- Inelastics

*Phenomenological approach:*

- \* *Fit  $A_{inel}$  vs. CED-FPD (or  $Q^2$  and  $W$ )*

$$A_{inel} = a + bQ^2 + cW \left[ + d(Q^2)^2 + eW^2 + fQ^2W + \square\square\square \right]$$

- \* *Extrapolate under elastic locus*

- \* *Error on  $A_{inel}$  from fit uncertainty*

$$\delta A_{inel} = \delta A_{inel} \left( \delta a, \delta b, \delta c, \dots, \delta Q^2, \delta W \right)$$

# Theory: Steve Wells

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$$A_{N\Delta}^{PV} = \frac{G_F}{\sqrt{2}} \frac{Q^2}{2\pi\alpha} \left[ \Delta_{(1)}^\pi + \Delta_{(2)}^\pi + \Delta_{(3)}^\pi \right]$$

$\Delta_{(1)}^\pi$  :  $T=1$ , standard model coupling  $(1 - 2 \sin^2 \theta_W)$

$\Delta_{(2)}^\pi$  : Non-resonant contributions (small)

$\Delta_{(3)}^\pi$  :  $T=1$ , axial vector nucleon response

$$\propto G_{N\Delta}^A$$

*In elastic-inelastic overlap region:*

$$A_{meas} = \frac{\sigma_{el} A_{el} + \sigma_{inel} A_{inel}}{\sigma_{el} + \sigma_{inel}}$$

$$A_{el} = \left(1 + \frac{\sigma_{inel}}{\sigma_{el}}\right) A_{meas} - \frac{\sigma_{inel}}{\sigma_{el}} A_{inel} \quad \text{or} \quad A_{inel} = \left(1 + \frac{\sigma_{el}}{\sigma_{inel}}\right) A_{meas} - \frac{\sigma_{el}}{\sigma_{inel}} A_{el}$$

*Elastics:*

$$\delta A_{el} = \sqrt{\left(1 + \frac{\sigma_{inel}}{\sigma_{el}}\right)^2 \delta A_{meas}^2 + \left[\delta \frac{\sigma_{inel}}{\sigma_{el}}\right]^2 A_{meas}^2 + \left(\frac{\sigma_{inel}}{\sigma_{el}}\right)^2 \delta A_{inel}^2 + \left[\delta \frac{\sigma_{inel}}{\sigma_{el}}\right]^2 A_{inel}^2}$$

*What is  $A_{inel}$ ,  $\delta A_{inel}$ ?*

*Inelastics:*

$$A_{inel} = \frac{\sigma_{\Delta} A_{\Delta} + \sigma_{Al} A_{Al}}{\sigma_{\Delta} + \sigma_{Al}}$$

$$A_{\Delta} = \left(1 + \frac{\sigma_{Al}}{\sigma_{\Delta}}\right) A_{inel} - \frac{\sigma_{Al}}{\sigma_{\Delta}} A_{Al}$$

$$\delta A_{\Delta} = \sqrt{\left(1 + \frac{\sigma_{Al}}{\sigma_{\Delta}}\right)^2 \delta A_{inel}^2 + \left[\delta \frac{\sigma_{Al}}{\sigma_{\Delta}}\right]^2 A_{inel}^2 + \left(\frac{\sigma_{Al}}{\sigma_{\Delta}}\right)^2 \delta A_{Al}^2 + \left[\delta \frac{\sigma_{Al}}{\sigma_{\Delta}}\right]^2 A_{Al}^2}$$

\* Measure  $A_{Al}$ ,  $\delta A_{Al}$  with dedicated “frame”, “empty target” runs

# Data Summary: LH2

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- **High Energy LH2:**

$$\rightarrow Q^2 = 0.62 \text{ (GeV/c)}^2$$

**Total accumulated charge ~ 100C**