



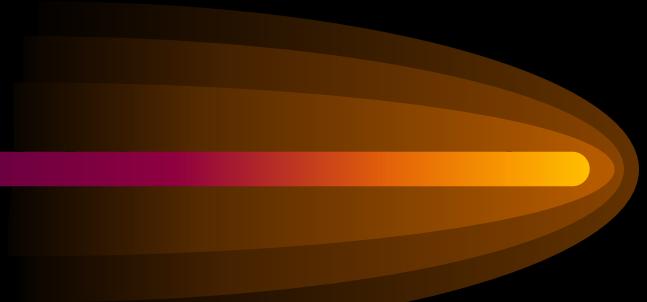
Synchrotron Light Interferometer

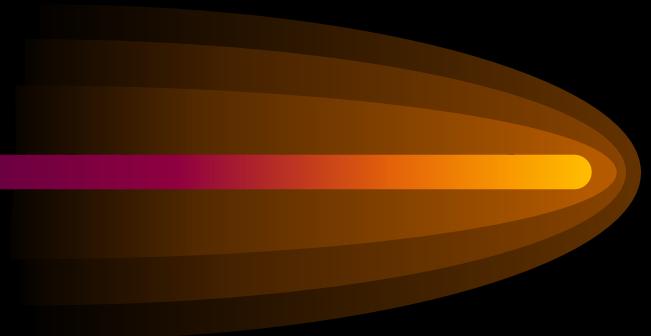
Project at Jefferson Lab

Pavel Chevtsov

February 21, 2003

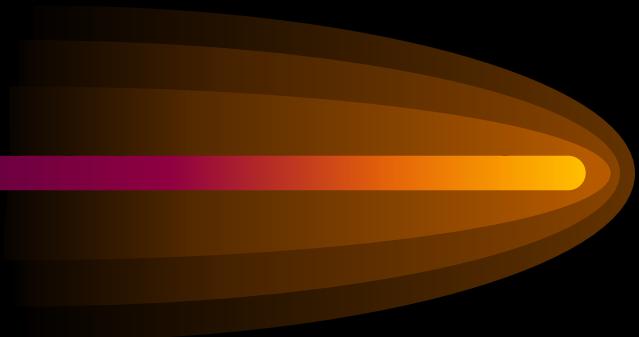
- Properties of Light
- Synchrotron Radiation
- Beam Diagnostics with Synchrotron Light
- Synchrotron Light Interferometer at Jefferson Lab
with some Experimental Results
- Conclusions





Properties of Light

Diffraction

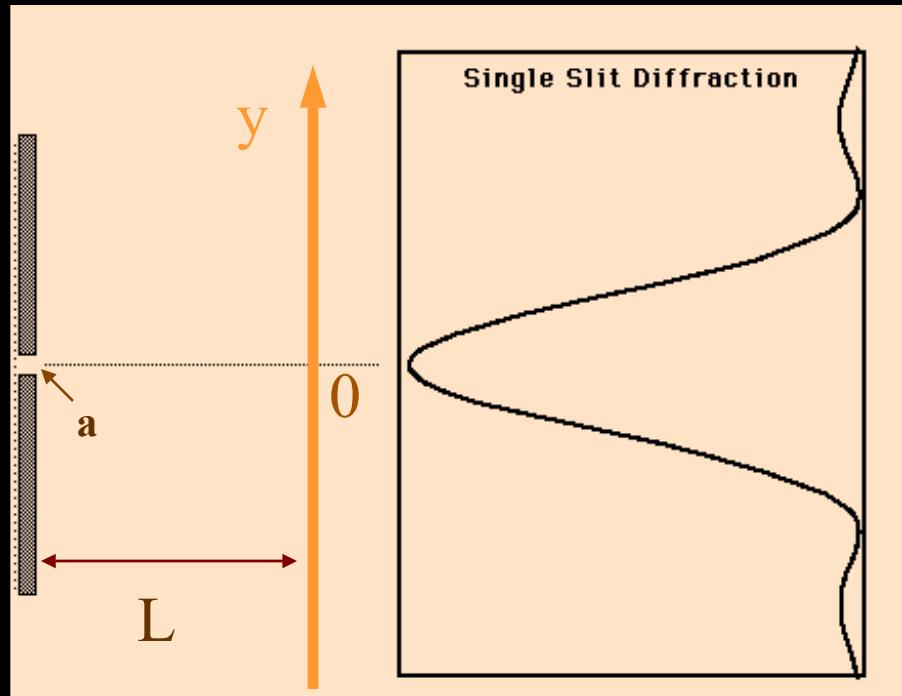


Diffraction is the spreading of waves around obstacles.



Diffraction describes how light interacts with its physical environment.

S



$$I(y) = I(0) \left[\frac{\sin(\alpha)}{\alpha} \right]^2$$

$$\alpha = k a y / (2L)$$

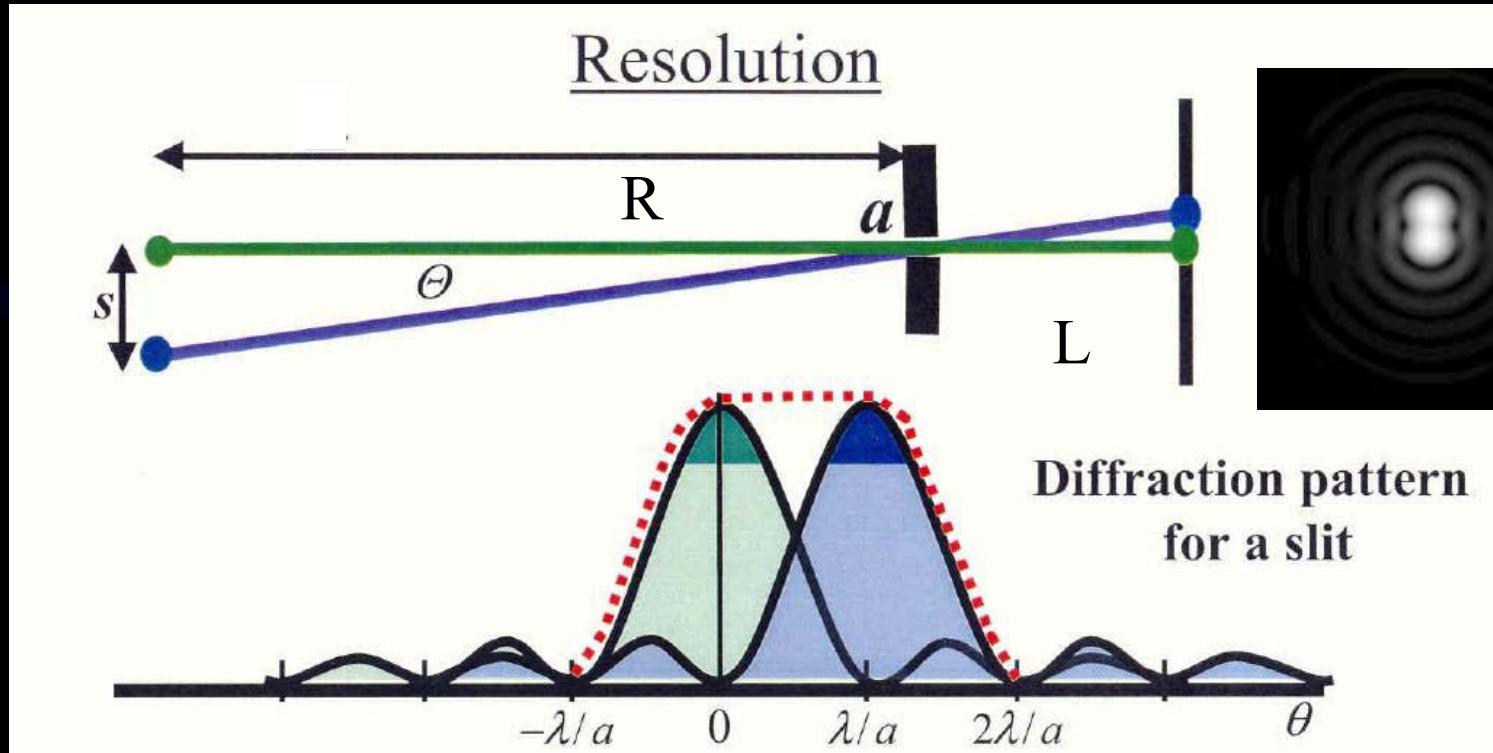
$$k = 2\pi/\lambda$$

Resolving power of image-forming systems

Diffraction of light limits the resolution of optical systems.
The images of two objects, which are very close to each other, overlap.



How close two points can be brought together before they can no longer be distinguished as separate ?

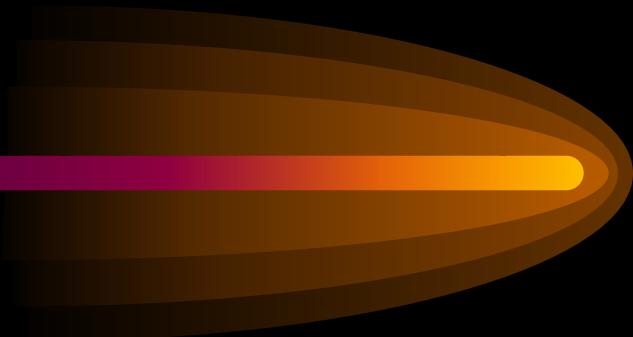


The **Rayleigh** criterion states that two similar diffraction patterns can just be resolved if the first zero of one pattern falls on the central peak of the other.



$$\left(\frac{s}{R}\right)_{\min} = \theta_{\min} = \frac{\lambda}{a}$$

Interference



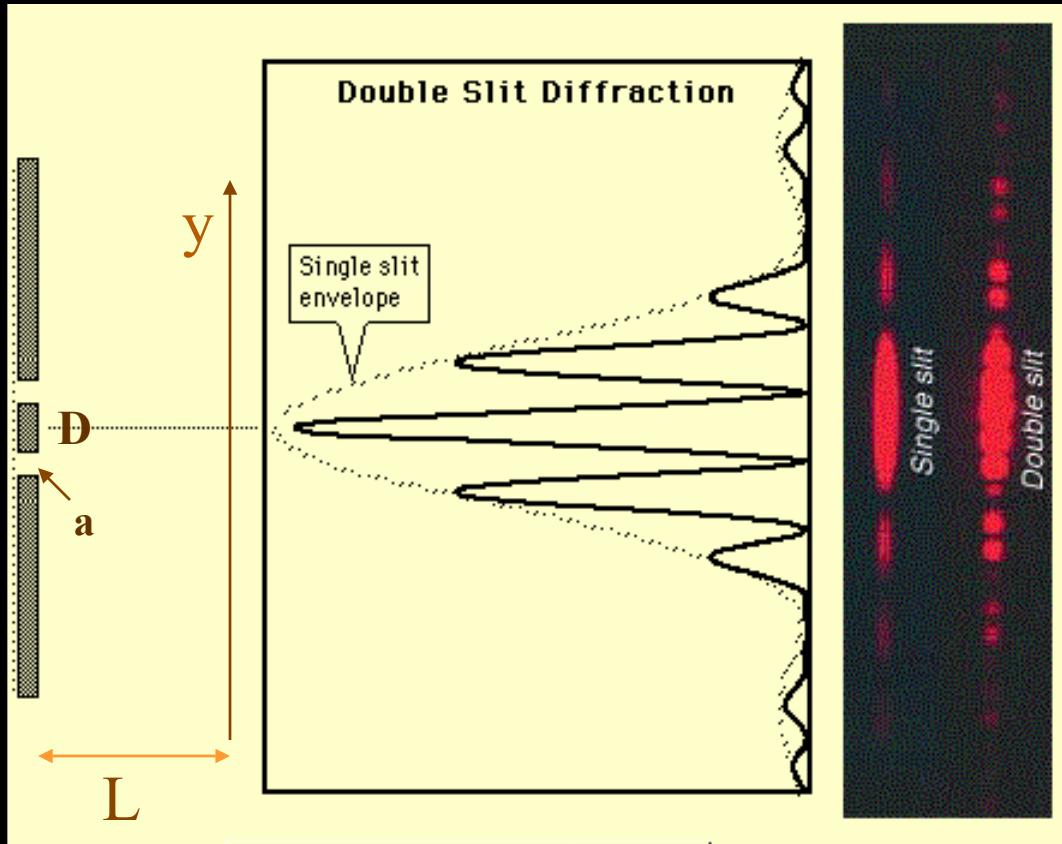
Interference is the net effect of the combination of two or more wave trains.



Interference results from the superposition of electromagnetic waves. It is the mechanism by which light interacts with light.



•
S

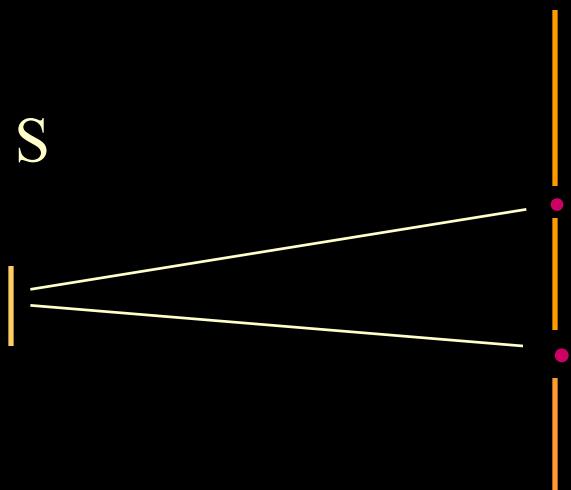


The intensity pattern is given by:

$$I(y) = I_0 \left[\frac{\sin(\alpha)}{\alpha} \right]^2 [1 + \cos(kDy/L)]$$

$$\alpha = kay/(2L)$$

If the light source is not “point-like”



$$I(y) = I_0 \left[\frac{\sin(\alpha)}{\alpha} \right]^2 [1 + V \cos(kDy/L + \varphi)]$$

$$\alpha = kay/(2L)$$

$$V = \frac{I_{\max} - I_{\min}}{I_{\max} + I_{\min}}$$

visibility (fringe contrast)

And the visibility and the “phase shift” φ are connected with the degree of coherence Γ : $V = |\Gamma|$, $\varphi = f(\arg \Gamma)$

Theorem of van Cittert – Zernike

The degree of coherence Γ is given by the Fourier transform of the intensity distribution of the source object.

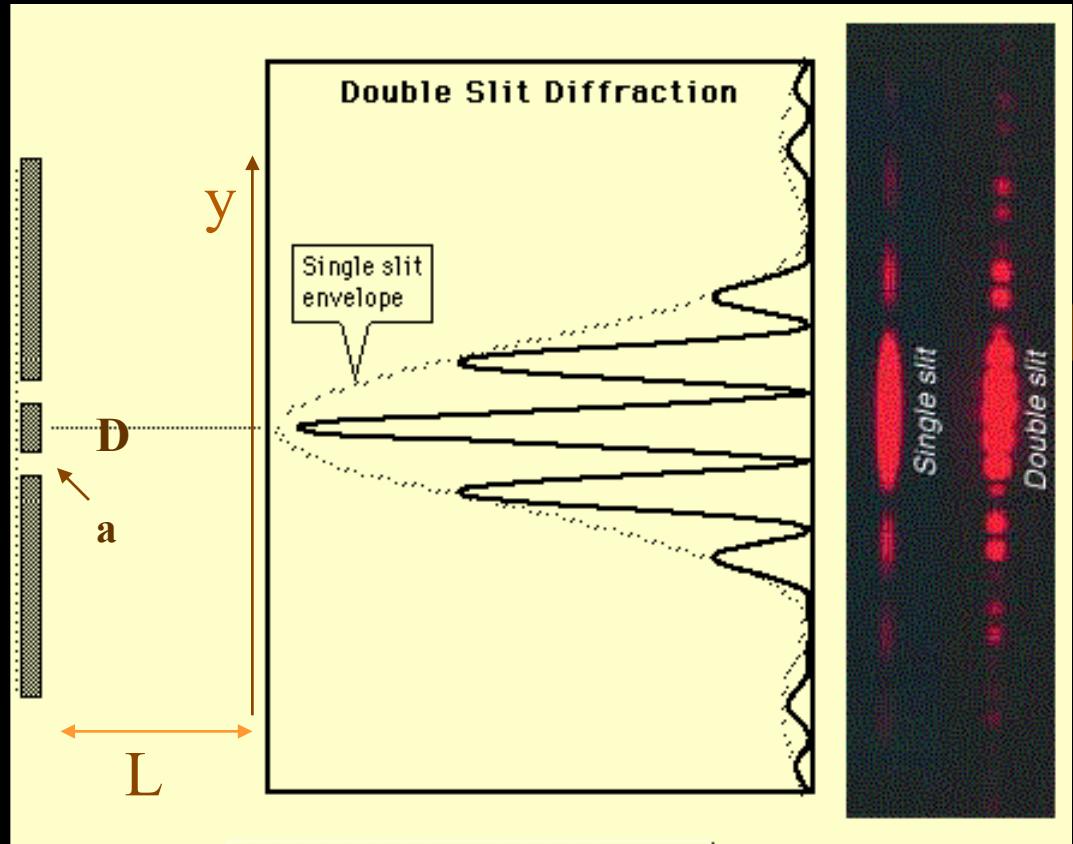


$$\Gamma(\theta) = \int I(\xi) \exp\{-i 2\pi \theta \xi\} d\xi$$

$$\Gamma = \frac{\Gamma(\theta)}{\Gamma(0)} \quad \theta = \frac{D}{\lambda R}$$

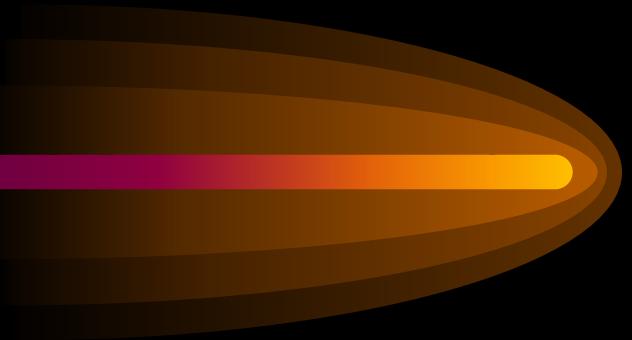
-
- the visibility of the interference fringe picture from a point source is equal to 1
 - a small source object gives a good visibility (fringe contrast)
 - a large source object gives a poor visibility (fringe contrast)

What is about the resolution of such a double slit assembly (interferometer) ?

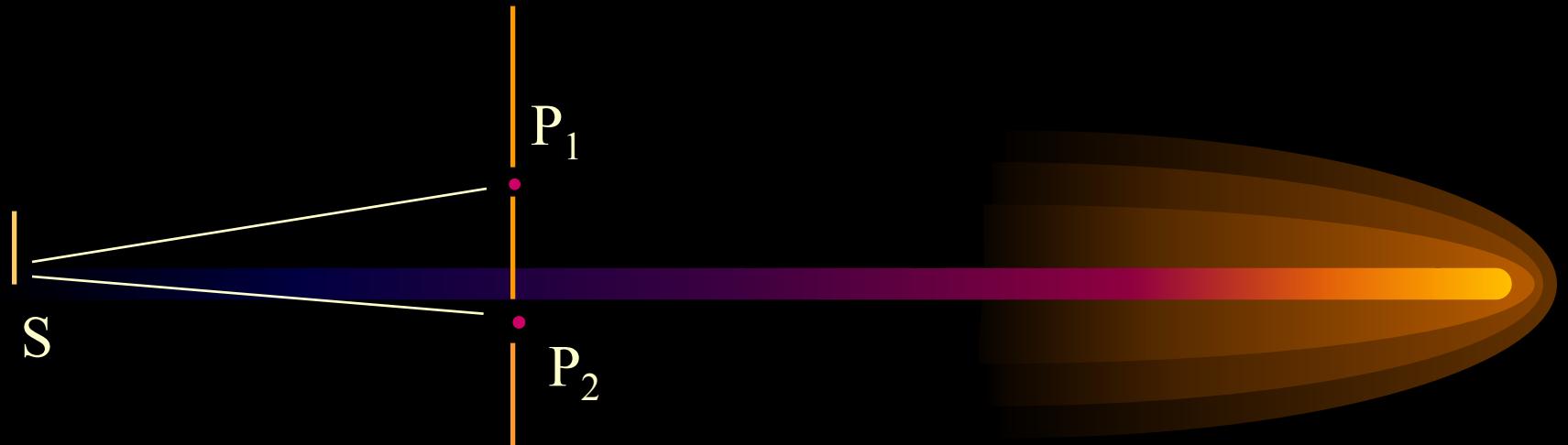


Following Rayleigh's criterion, $(\frac{S}{R})_{\min} = \theta_{\min} = \frac{\lambda}{2D}$

The resolution can be made very high ...



... but only if



P₁ and P₂ remain correlated:

for all typical points S in the source

$$| SP_1 - SP_2 | \ll \lambda_0^2 / \Delta\lambda$$

$\lambda_0^2 / \Delta\lambda$ is the coherence length for the bandwidth $\Delta\lambda$



Behavior of the function:

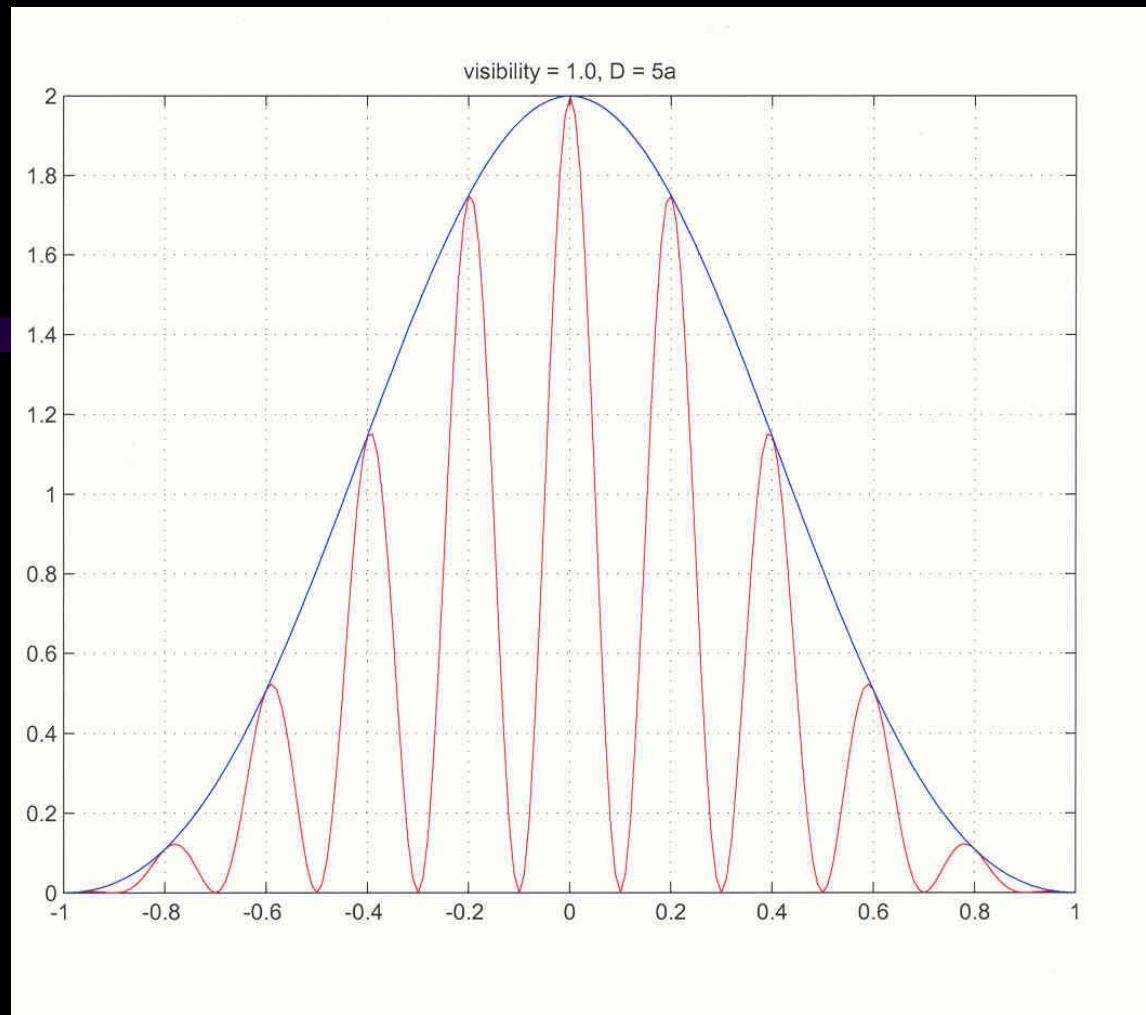
$$I(y) = \left[\frac{\sin(\alpha)}{\alpha} \right]^2 [1 + V \cos(kDy/L + \phi)]$$

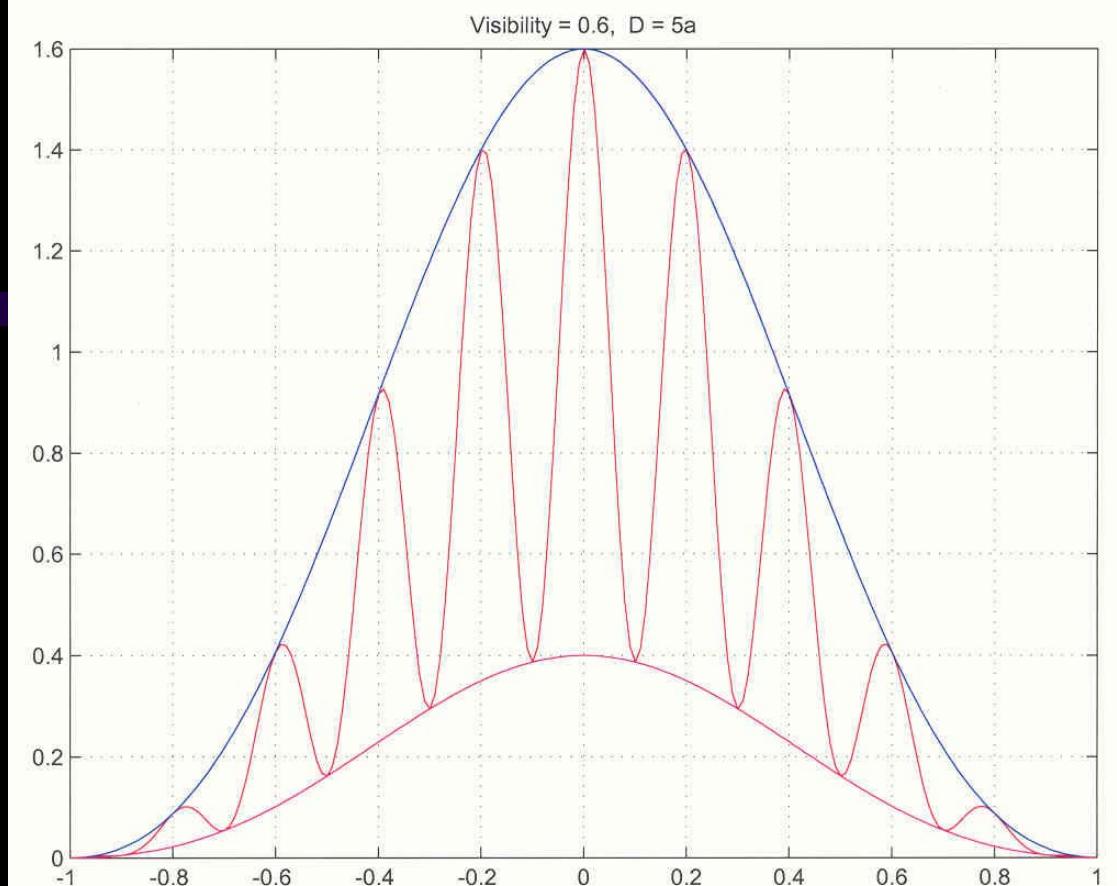
$$\alpha = kay/(2L)$$



$$\alpha = k a y / (2L)$$

$$I(y) = \left[\frac{\sin(\alpha)}{\alpha} \right]^2 [1 + V \cos(kDy/L + \phi)]$$

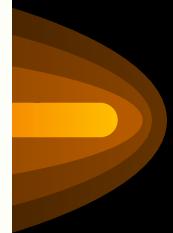
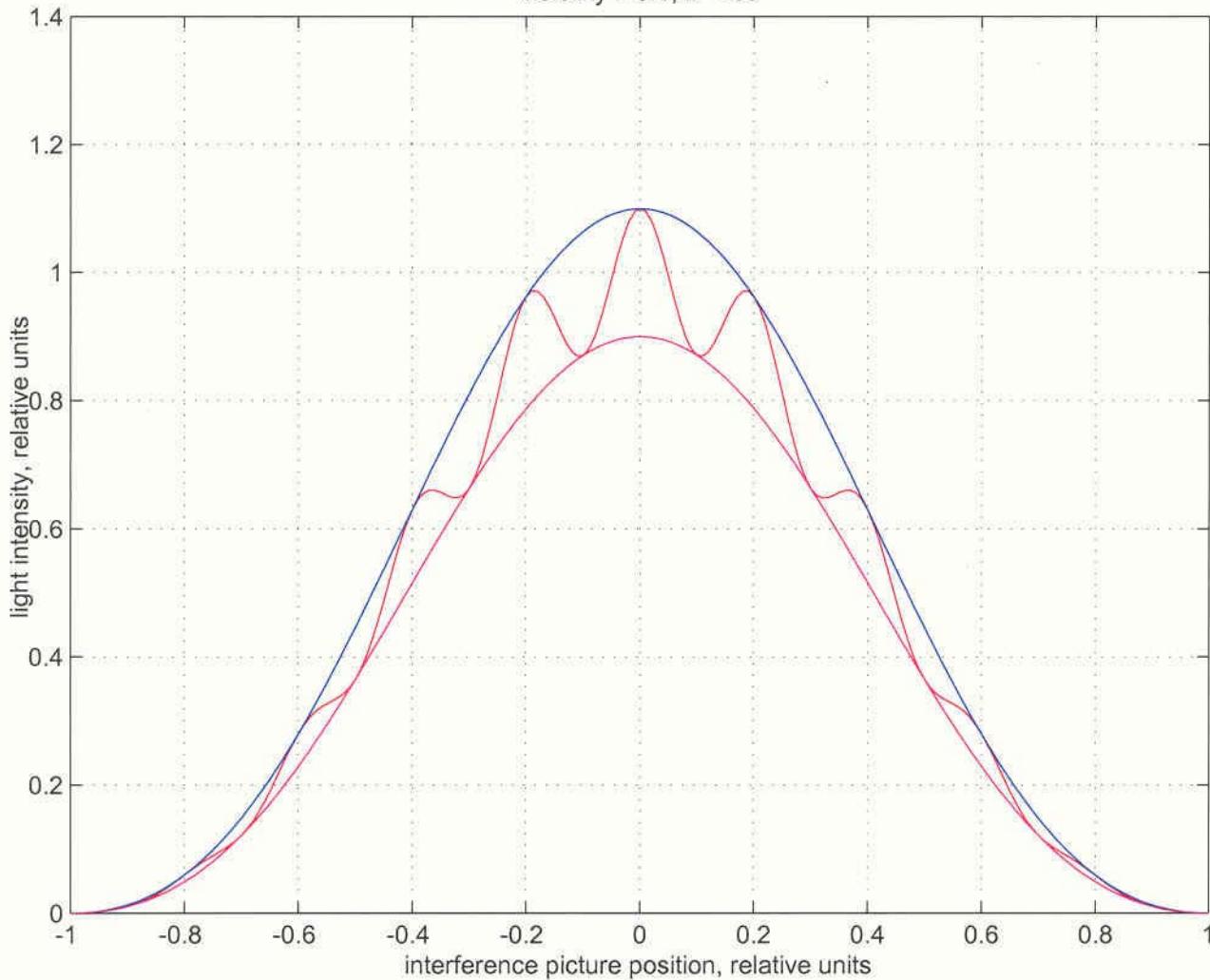


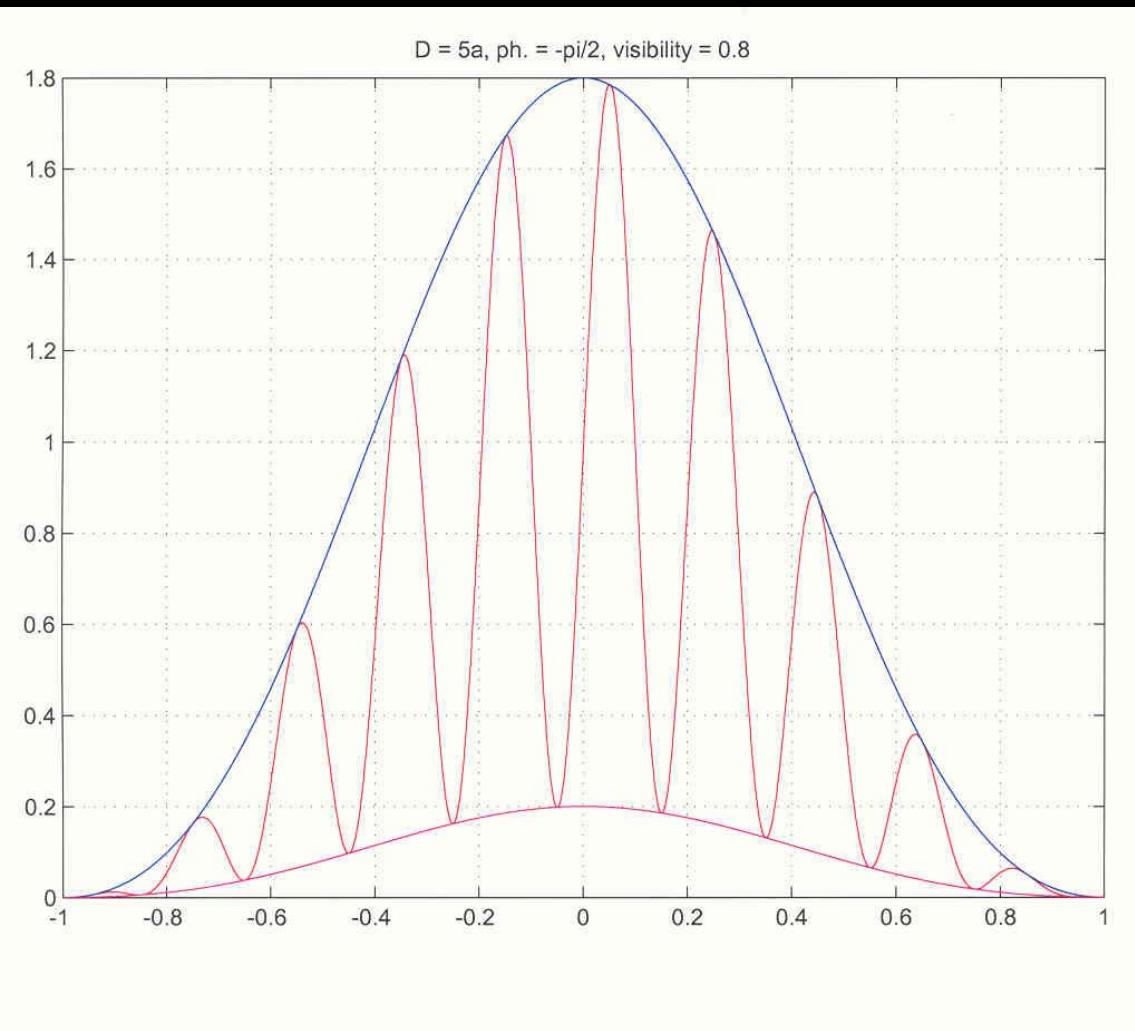


$$I(y) = \left[\frac{\sin(\alpha)}{a} \right]^2 [1 + V \cos(kDy/L + \varphi)]$$

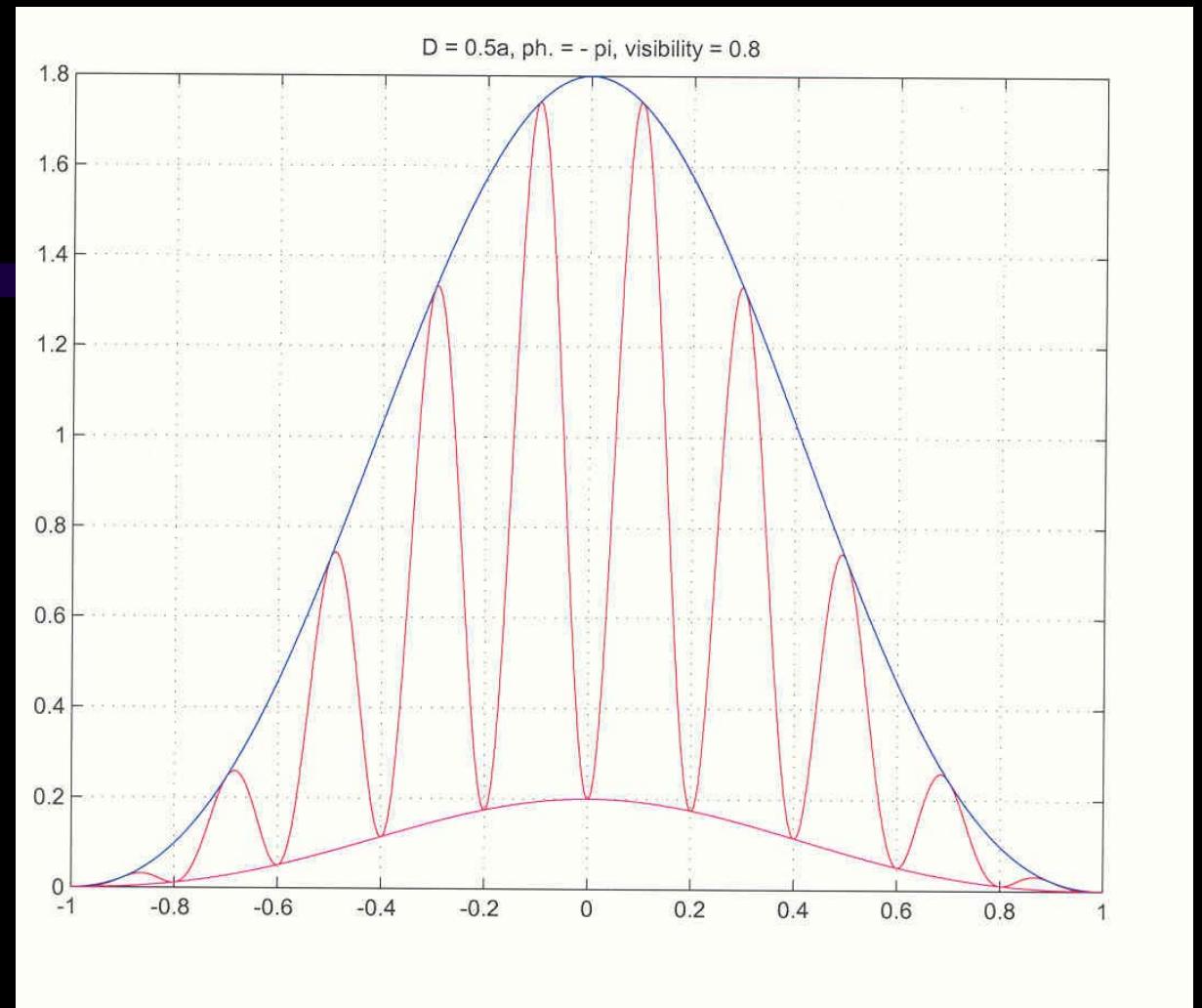
$$\text{Env}_{1,2}(y) = \left[\frac{\sin(\alpha)}{a} \right]^2 [1 \pm V]$$

visibility = 0.1, D = 5a

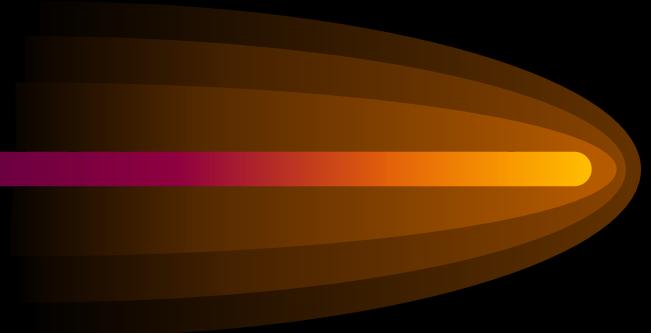




$$I(y) = \left[\frac{\sin(\alpha)}{\alpha} \right]^2 [1 + V \cos(kDy/L + \varphi)]$$



$$I(y) = \left[\frac{\sin(\alpha)}{\alpha} \right]^2 [1 + V \cos(kDy/L + \phi)]$$



Synchrotron Radiation

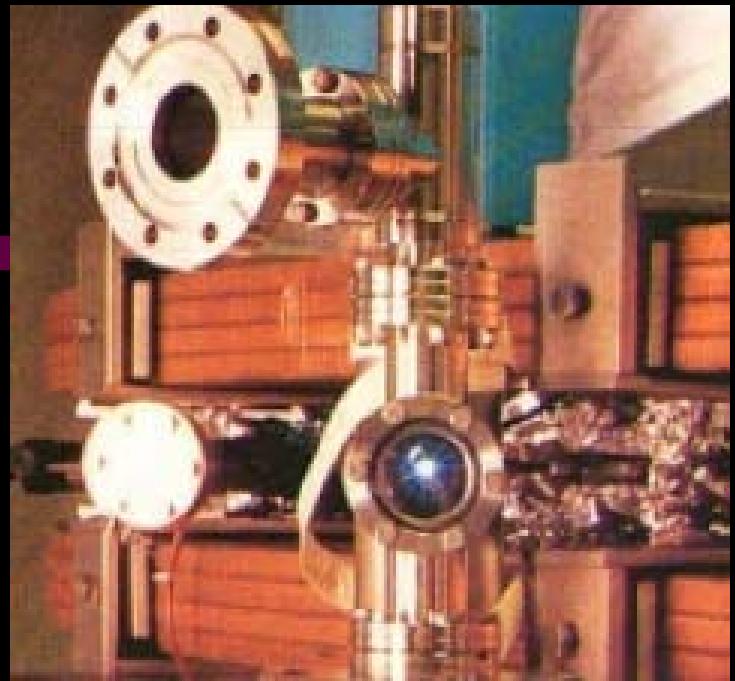
History - 1940th

Theory of radiation from relativistic particles

Pomeranchuk, Ivanenko, Sokolov, Ternov (USSR)
Schwinger (USA)

Synchrotron ideas - 1945

Veksler (USSR), McMillan (USA)

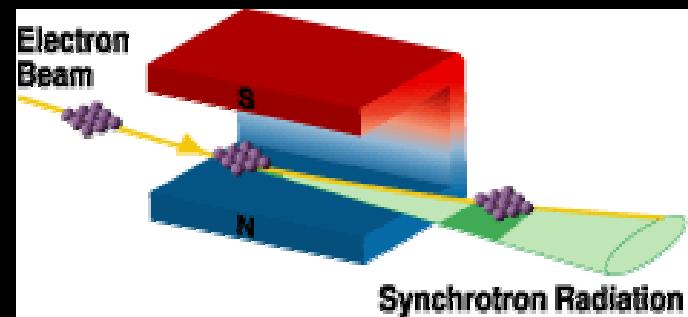


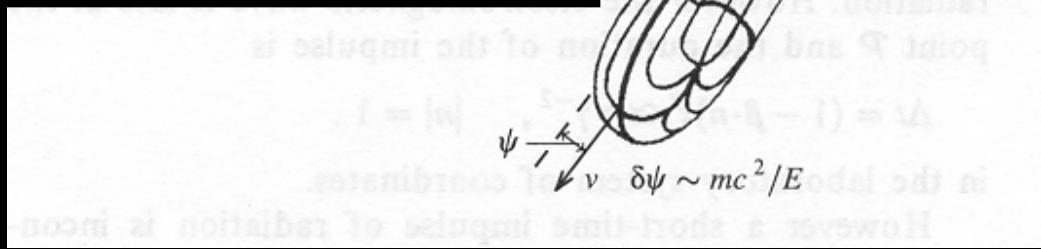
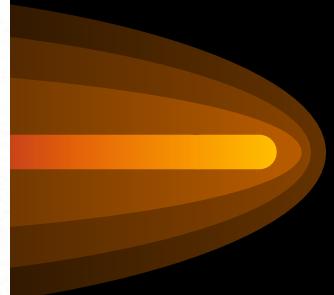
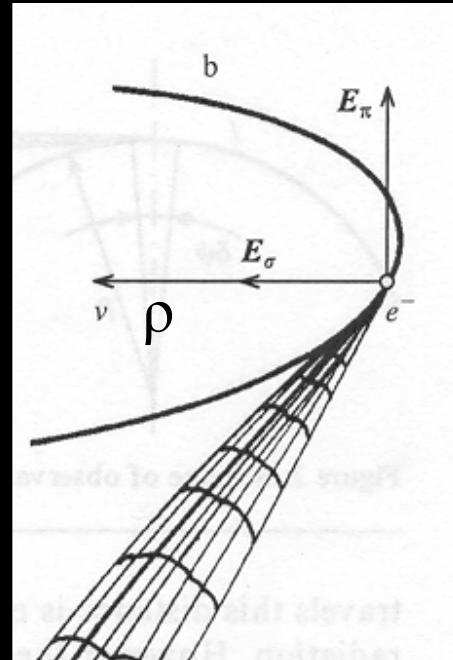
The first visual observation of synchrotron radiation was in 1947 from the General Electric synchrotron in the USA.

Synchrotron radiation (SR) is emitted from relativistic charged particles when their paths are changed.

By the magnetic field, for example.

Everywhere further we will consider only the synchrotron radiation from electrons generated in the bending magnets.



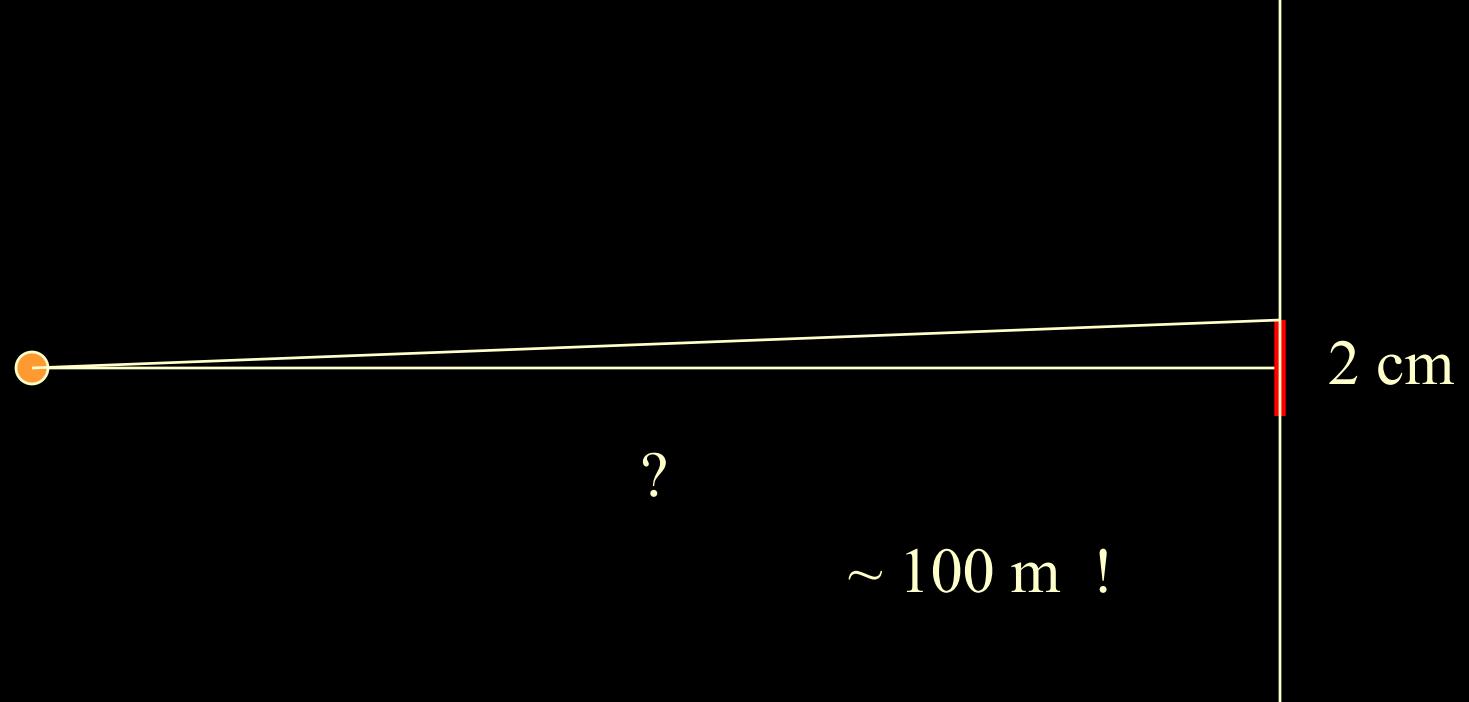


Because of the relativistic effect, the synchrotron radiation is emitted in a narrow cone in the forward direction, at a tangent to the orbit

$$\Psi \sim 1/\gamma \quad (5 \text{ GeV electrons} \rightarrow 10^{-4})$$

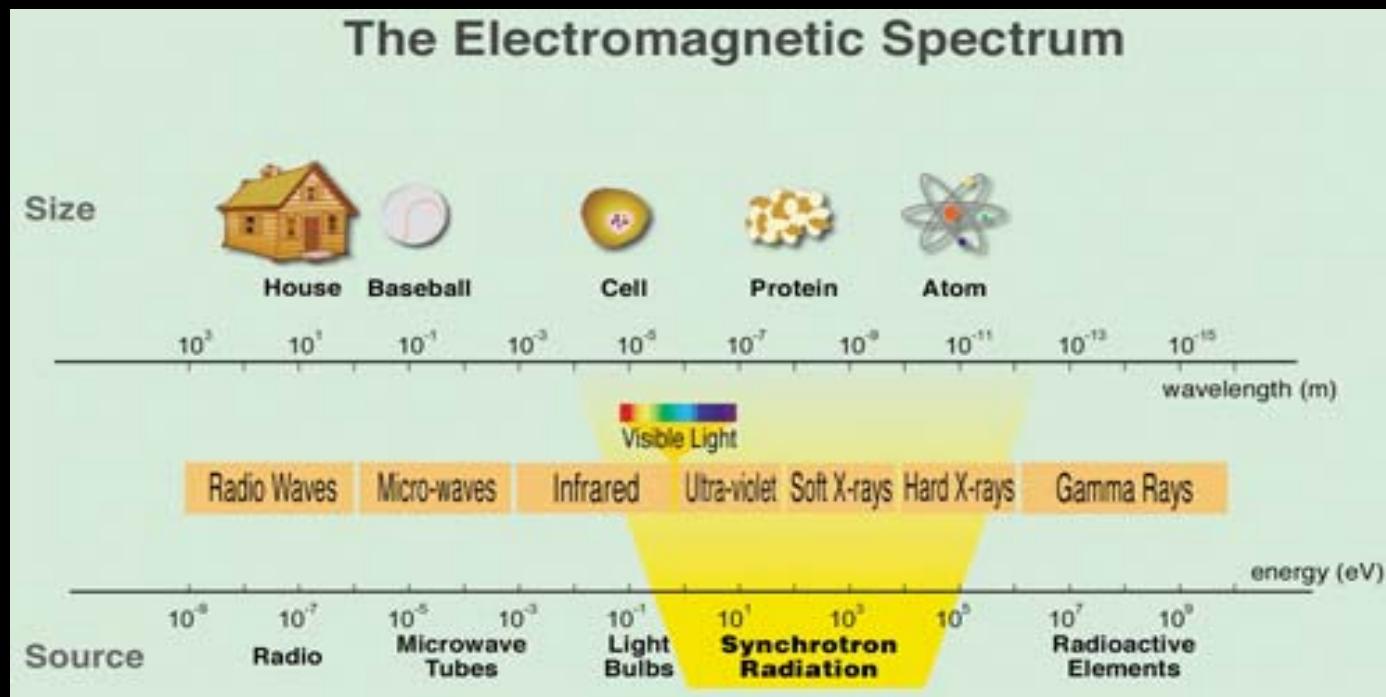


$\Psi \sim 1/\gamma$ (5 GeV electrons $\rightarrow 10^{-4}$)

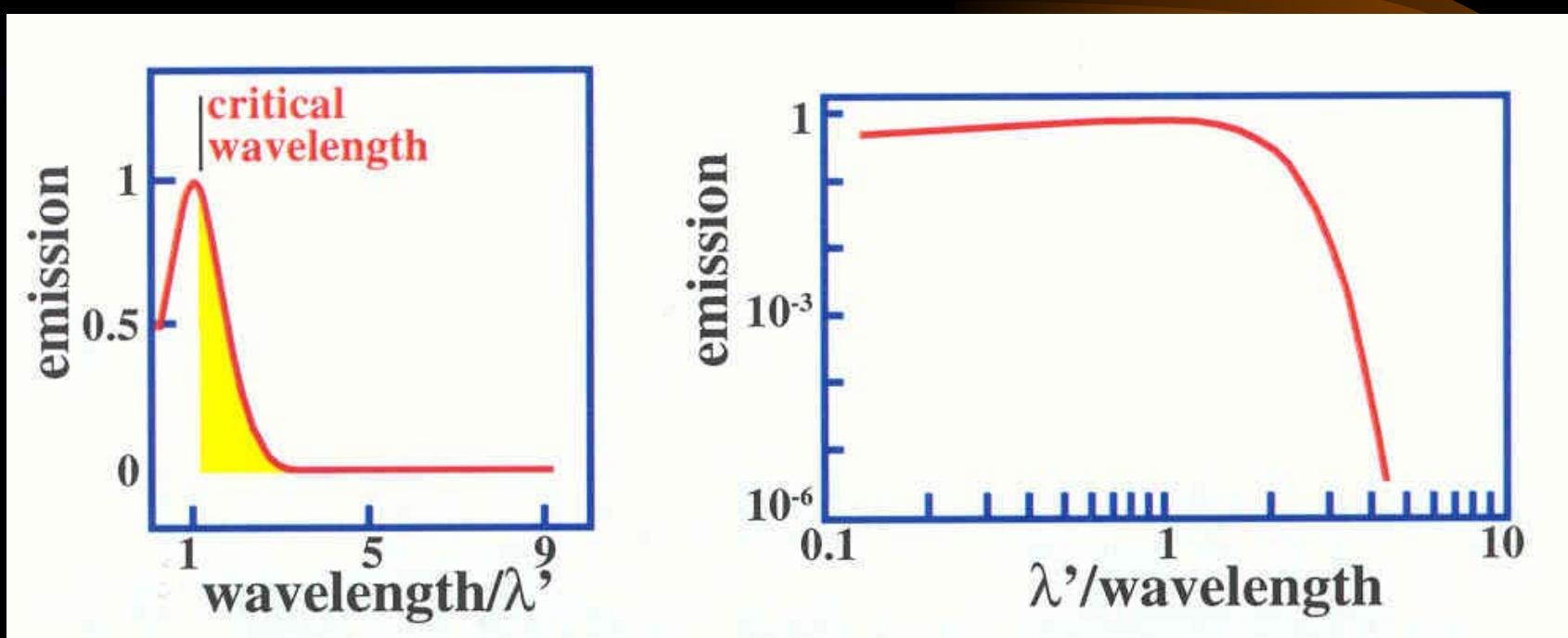


Synchrotron radiation

- extremely intense and highly collimated
- highly polarized (E_σ and E_π)
- has a wide energy spectrum (from infrared to γ -rays)



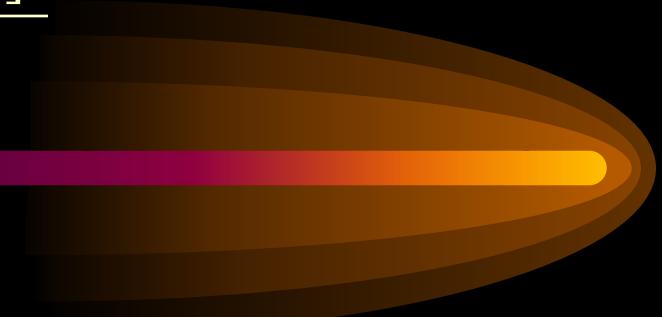
A typical energy spectrum of synchrotron radiation



The critical wavelength λ' (or λ_c) divides the radiated power into two equal parts: one-half of the power is radiated above this wavelength and one-half below.

The critical wavelength [A. Hofmann]

$$\lambda_c = \frac{4 \pi \rho}{3 \gamma^3}$$



Example: 5 GeV electrons, $\rho = 40$ m

$$\lambda_c = 0.16 \text{ nm}$$

At low frequencies the properties of synchrotron radiation are independent of the particle energy and depend only on the radius ρ of the curvature.

The rms opening angle for $\lambda \gg \lambda_c$

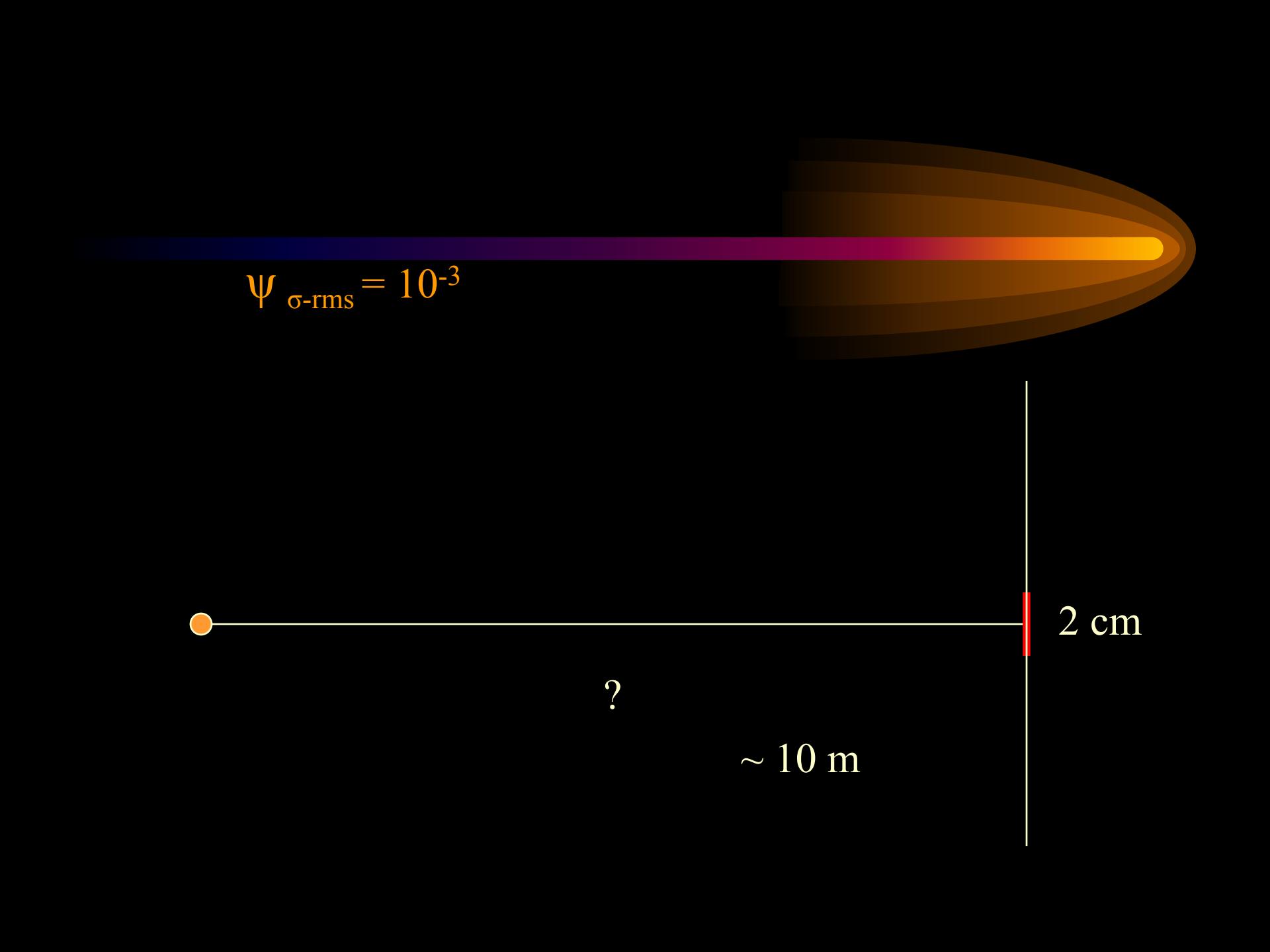
$$\Psi_{\sigma\text{-rms}} = 0.41 (\lambda / \rho)^{1/3}$$

$$\Psi_{\pi\text{-rms}} = 0.55 (\lambda / \rho)^{1/3}$$

Example: $\lambda = 630 \text{ nm}$, $\rho = 40 \text{ m}$

$$\Psi_{\sigma\text{-rms}} = 10^{-3}$$

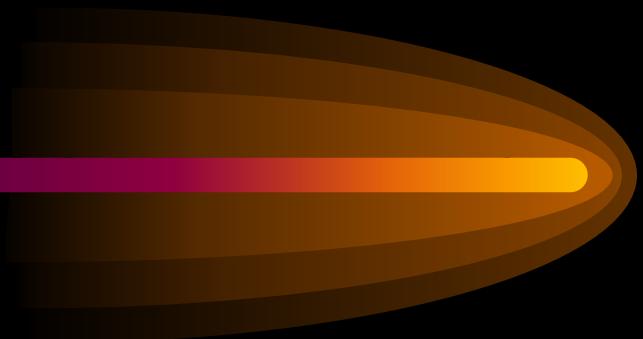



$$\Psi_{\sigma\text{-rms}} = 10^{-3}$$

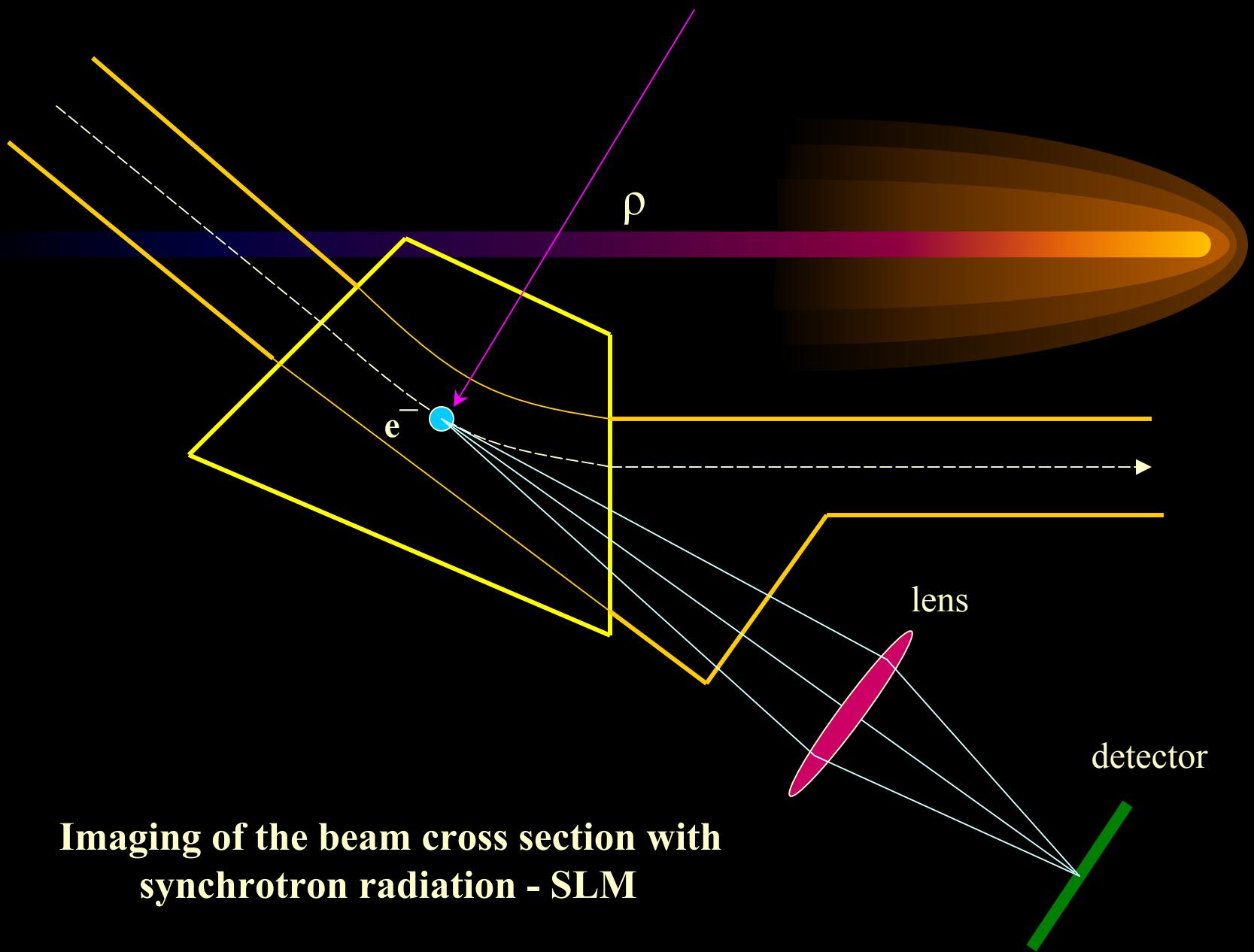
?

~ 10 m

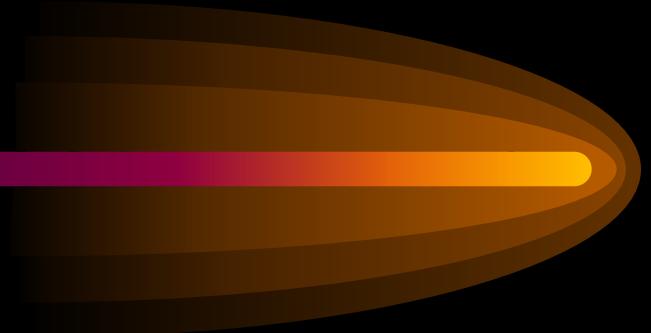
2 cm



Synchrotron Radiation Beam Diagnostics



**Imaging of the beam cross section with
synchrotron radiation - SLM**



The natural opening angle of the emitted light sets a limit to the resolution of the SLM

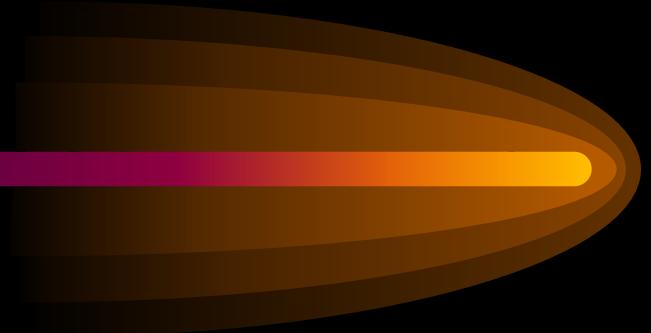
The diffraction limited resolution of synchrotron light imaging systems in the visible part of the spectrum [A.Hofmann]:

$$\sigma_S \approx 0.3 (\lambda^2 \rho)^{1/3}$$

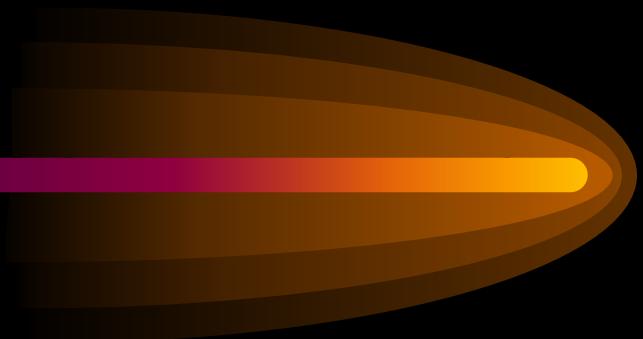
Example:

$$\lambda = 630 \text{ nm}, \quad \rho = 40 \text{ m}$$

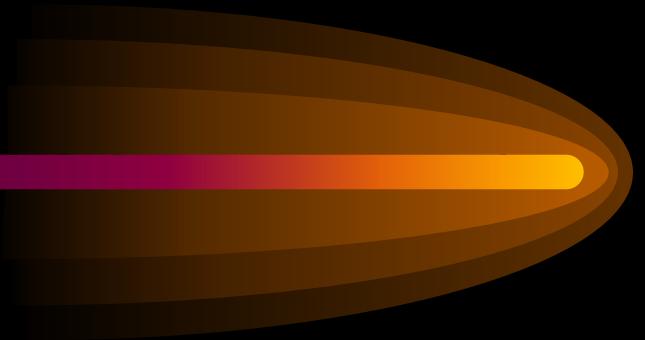
$$\sigma_S \approx 0.1 \text{ mm}$$



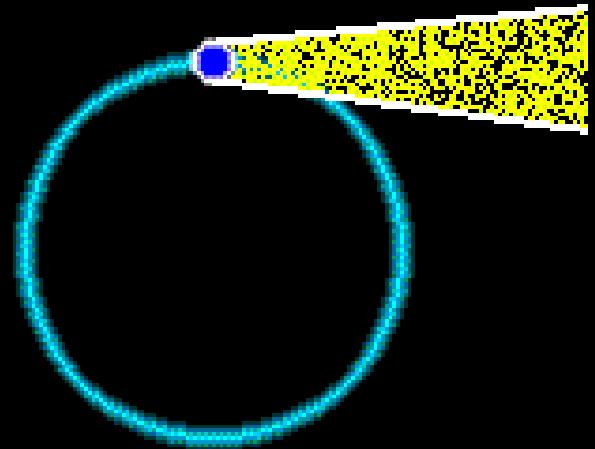
Can we build a synchrotron light interferometer and use
its data to measure smaller beam sizes ?



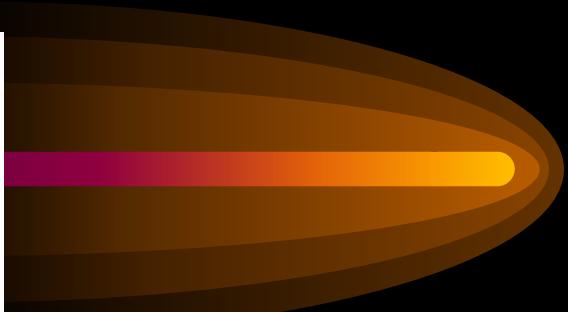
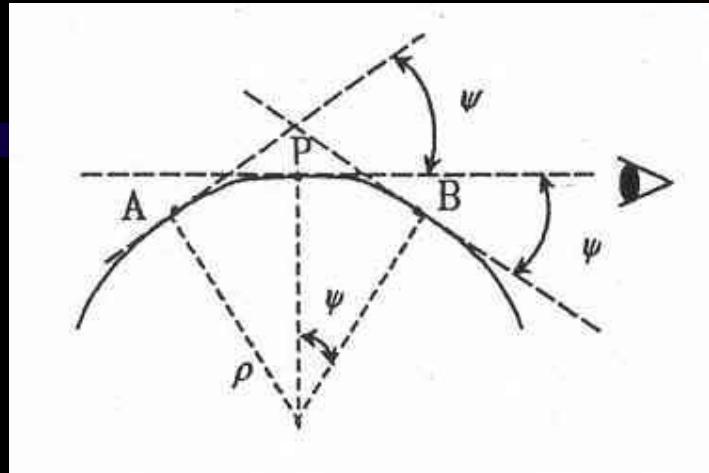
T. Mitsuhashi, Photon Factory, KEK, Japan



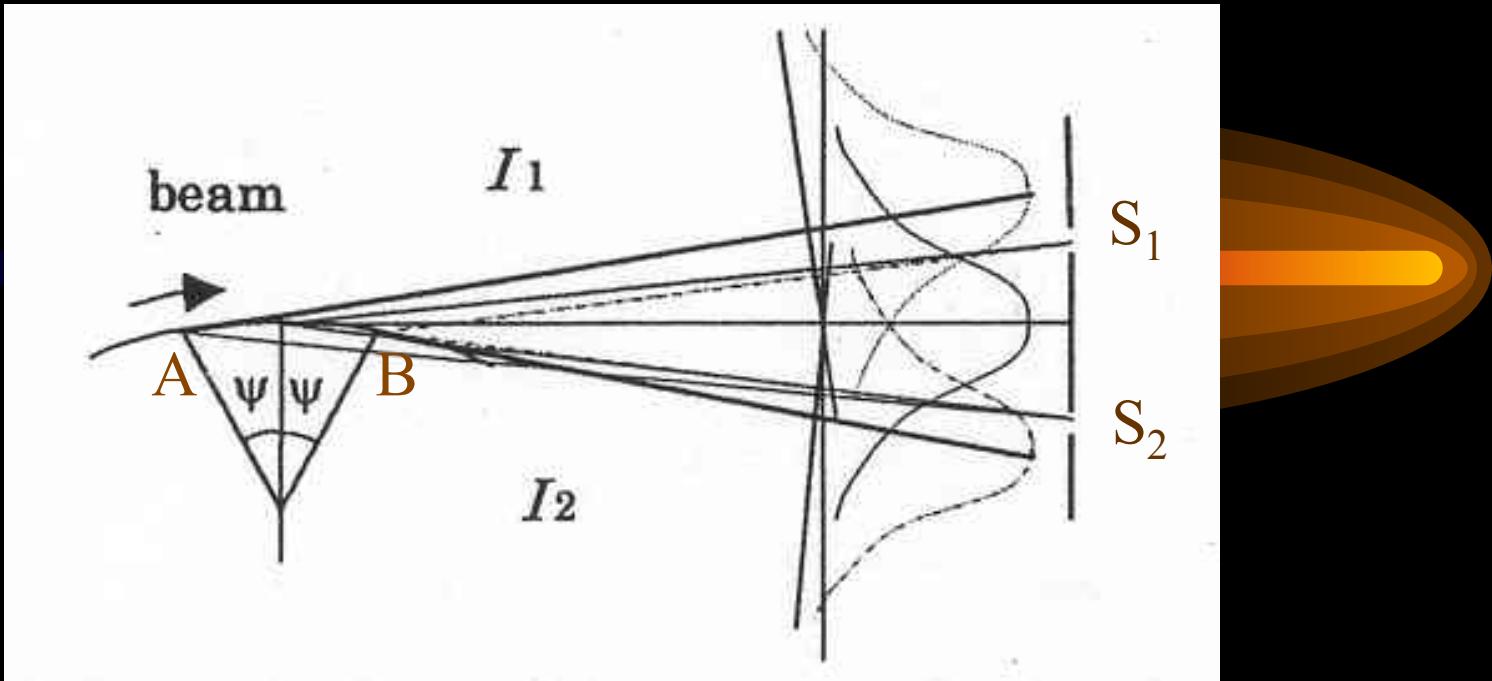
Problems



Synchrotron radiation is like a moving narrow searchlight in horizontal direction.

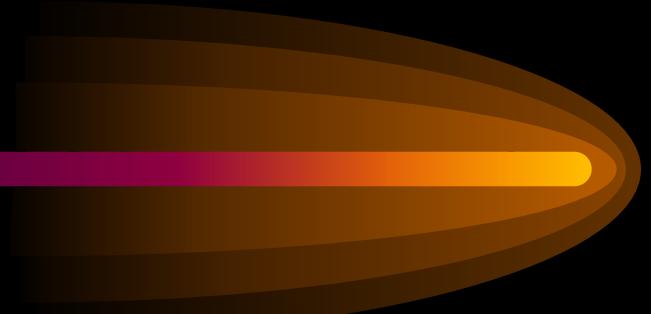


We observe photons coming from different positions when the electron moves from point A to point B. We must sum these photons.



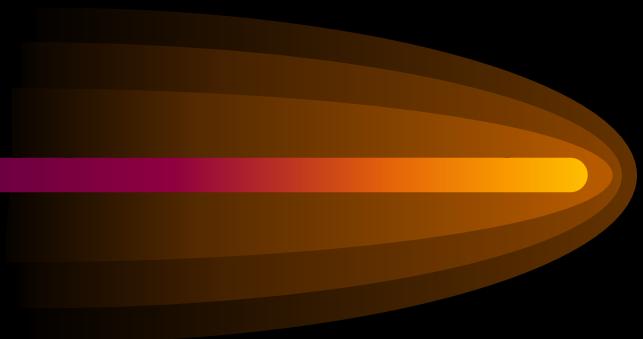
When an electron is moving from point A to point B,
the light is sweeping from slit S₁ to slit S₂.

- The intensities of two modes of light illuminating
the slits are different.



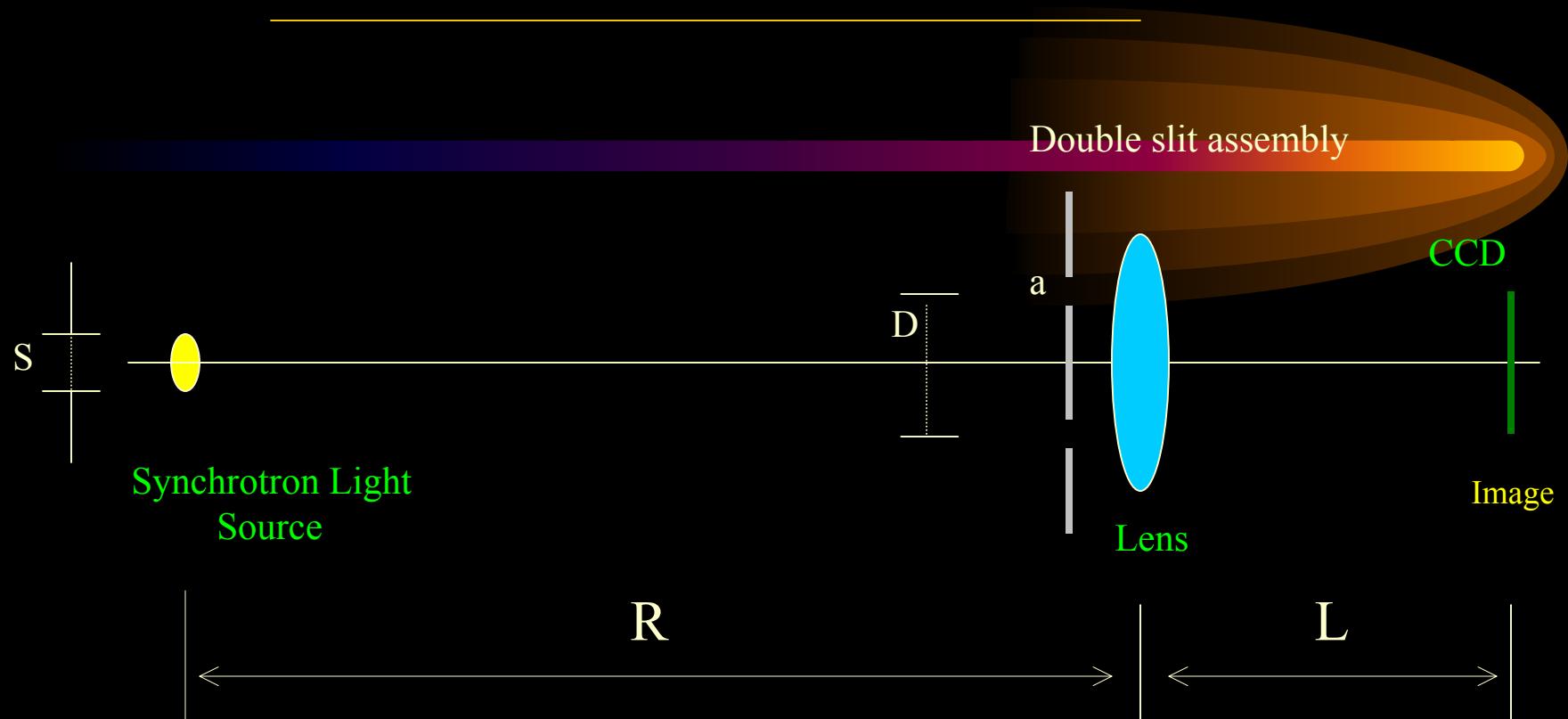
T. Mitsuhashi has modified the van Cittert-Zernike theorem and developed the method to calculate the beam size on the basis of the interference picture for the synchrotron light emitted by the beam.

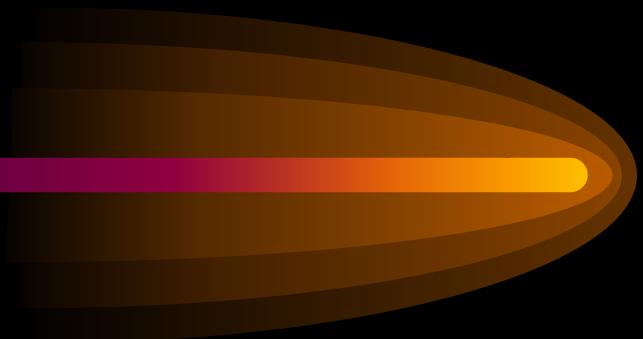
“Beam Profile and Size Measurement by the Use
of the Synchrotron Light Interferometer”



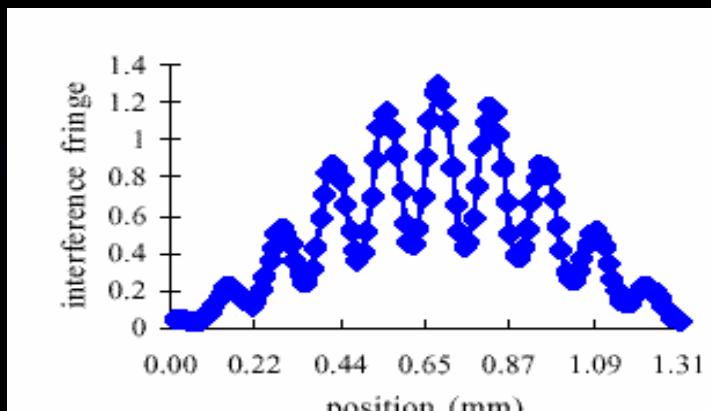
OK. Now we build our interferometer.

Synchrotron Radiation Interferometer

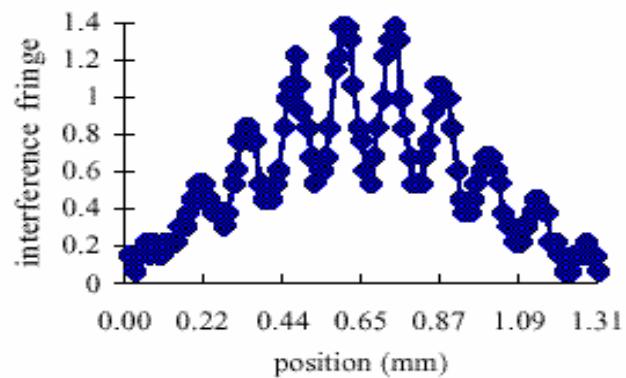




Problems

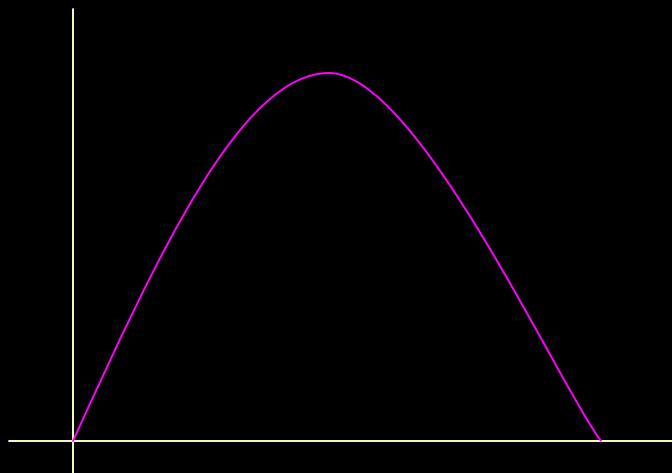


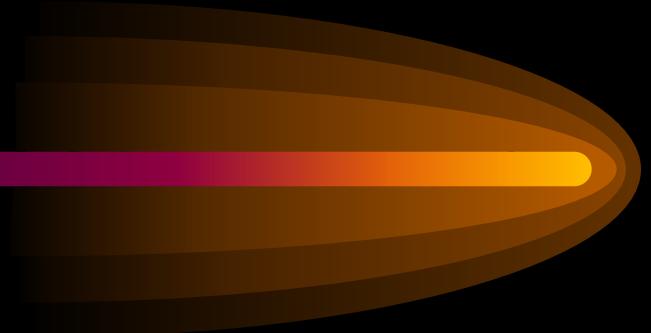
a) interferogram by s -polarized components.



b) interferogram by p-polarized components.

Two polarized components of the synchrotron light (p and s) are “in anti-phase”. Their superposition will not give us the interference fringes at all.
-> We get just a sort of a “SLM”.

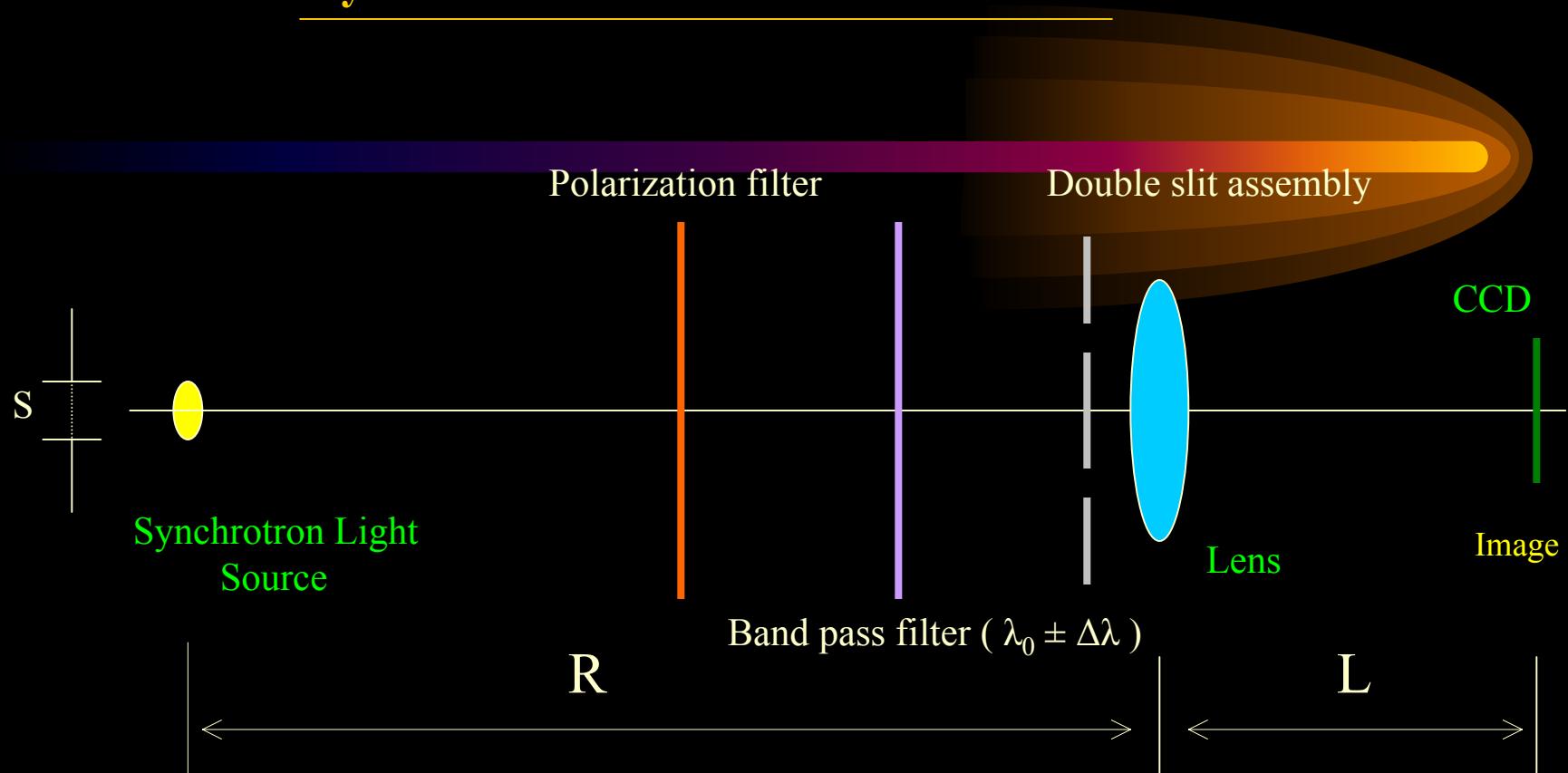




The synchrotron light is not monochromatic.

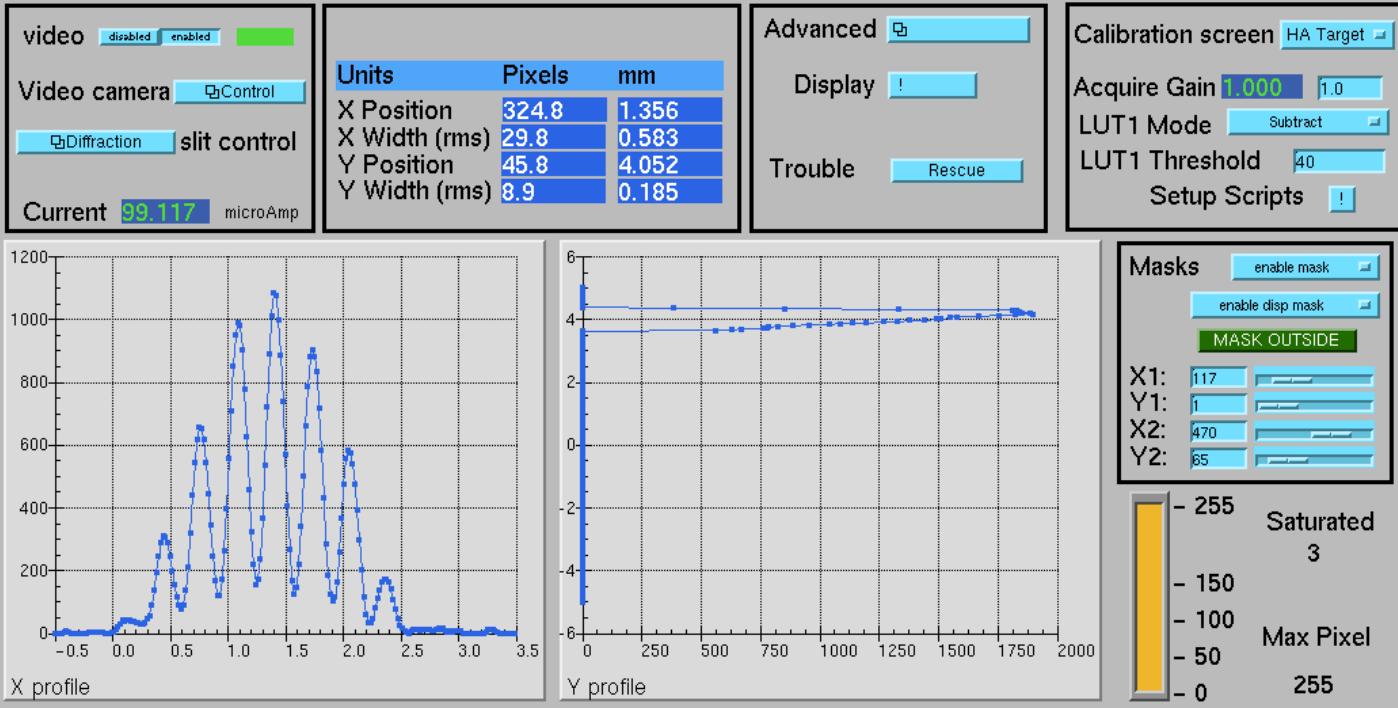
λ range is the whole visible spectrum !

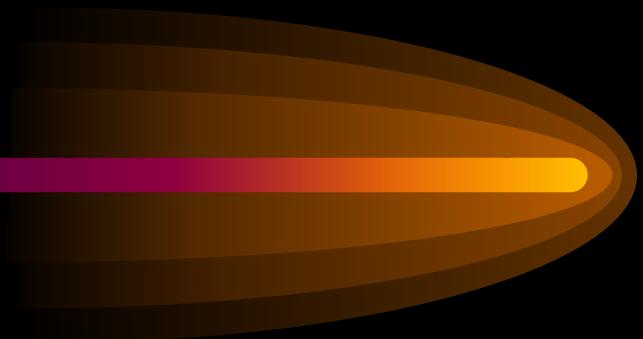
Synchrotron Radiation Interferometer



DataCube Setup for Hall A 1C12 SLM - Multiplex

(2002-04-15, Chevtsov)





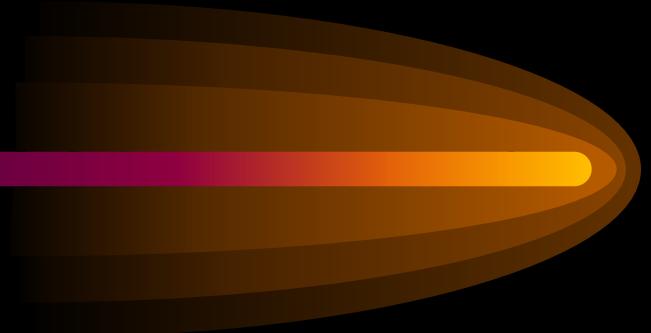
Beam Size Calculation

In case of a gaussian beam shape it is easy:

$$\Gamma(\theta) = \int I(\xi) \exp\{-i 2\pi \theta \xi\} d\xi \quad \Gamma = \frac{\Gamma(\theta)}{\Gamma(0)}$$

$$I(y) = I_0 \left[\frac{\sin(\alpha)}{\alpha} \right]^2 [1 + V \cos(kDy/L + \varphi)] \quad \alpha = kay/2L$$

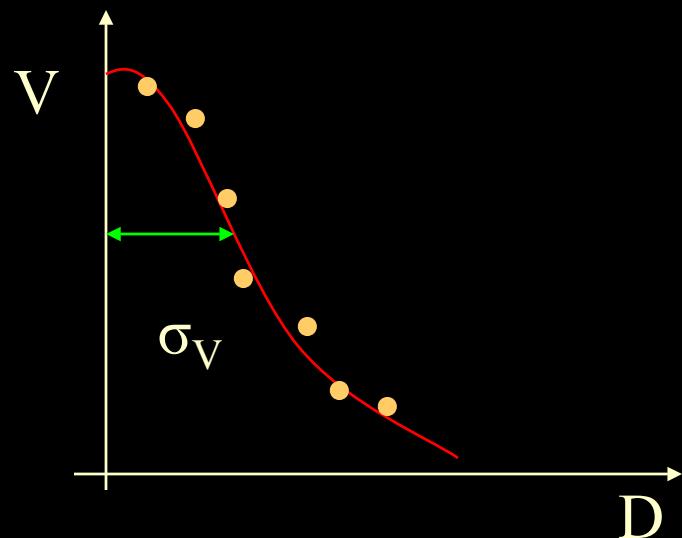
$$V = \exp\left(-\frac{2\pi^2 D^2 \sigma_{beam}^2}{\lambda^2 R^2}\right) = V(D)$$



Methods to calculate the beam size

1. We measure (experimentally) the contrast of the interferogram as a function of the slit separation D. Then we define the RMS of the visibility curve σ_V .

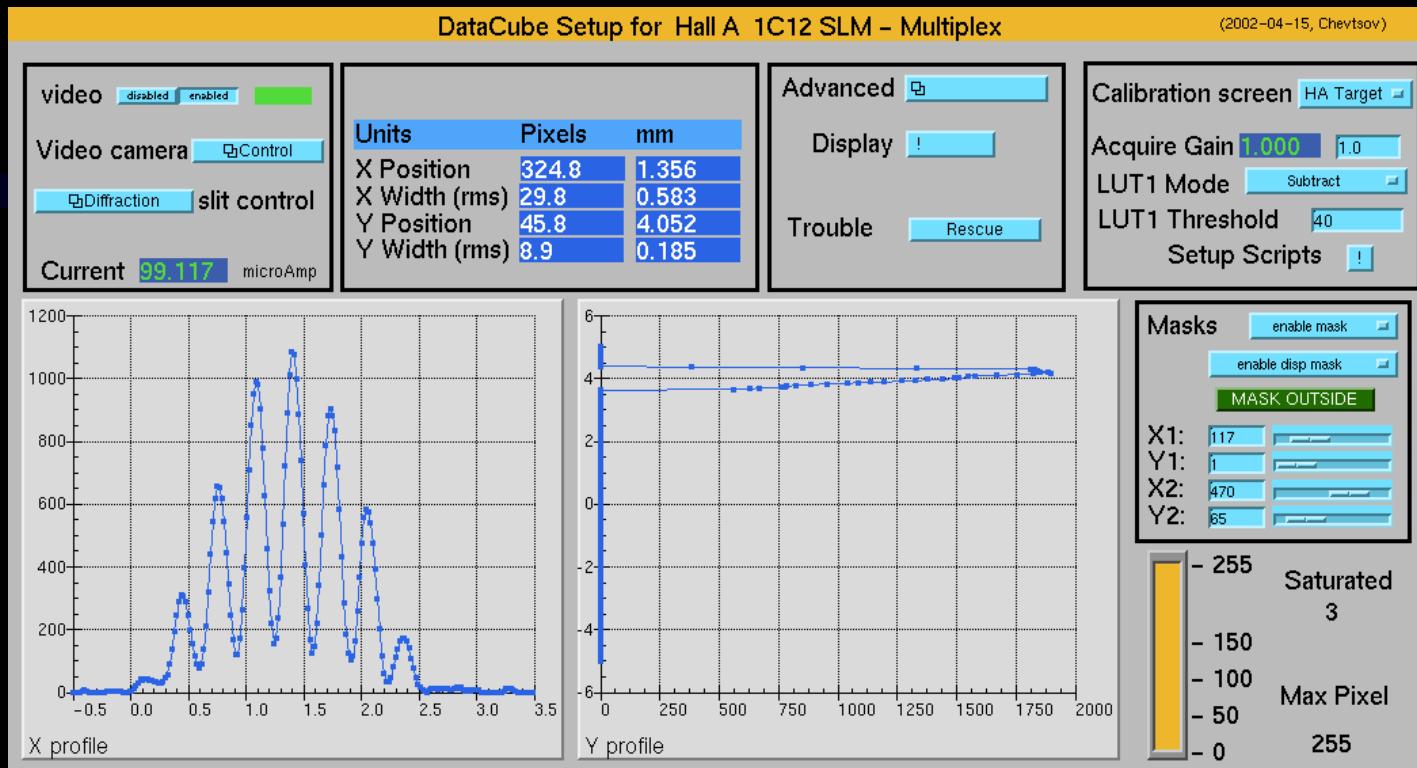
$$\sigma_{\text{beam}} = \frac{\lambda R}{2 \pi \sigma_V}$$





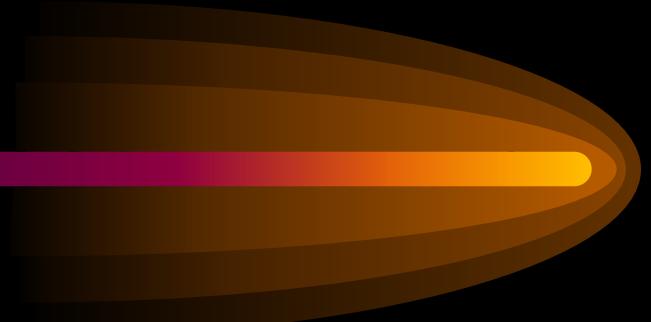
2. We can also measure the RMS beam size from one data of visibility which is measured at a fixed separation of a double slit assembly

$$\sigma_{\text{beam}} = \frac{\lambda R}{\pi D} \sqrt{0.5 \ln(1/V)}$$



$$V = 0.8$$

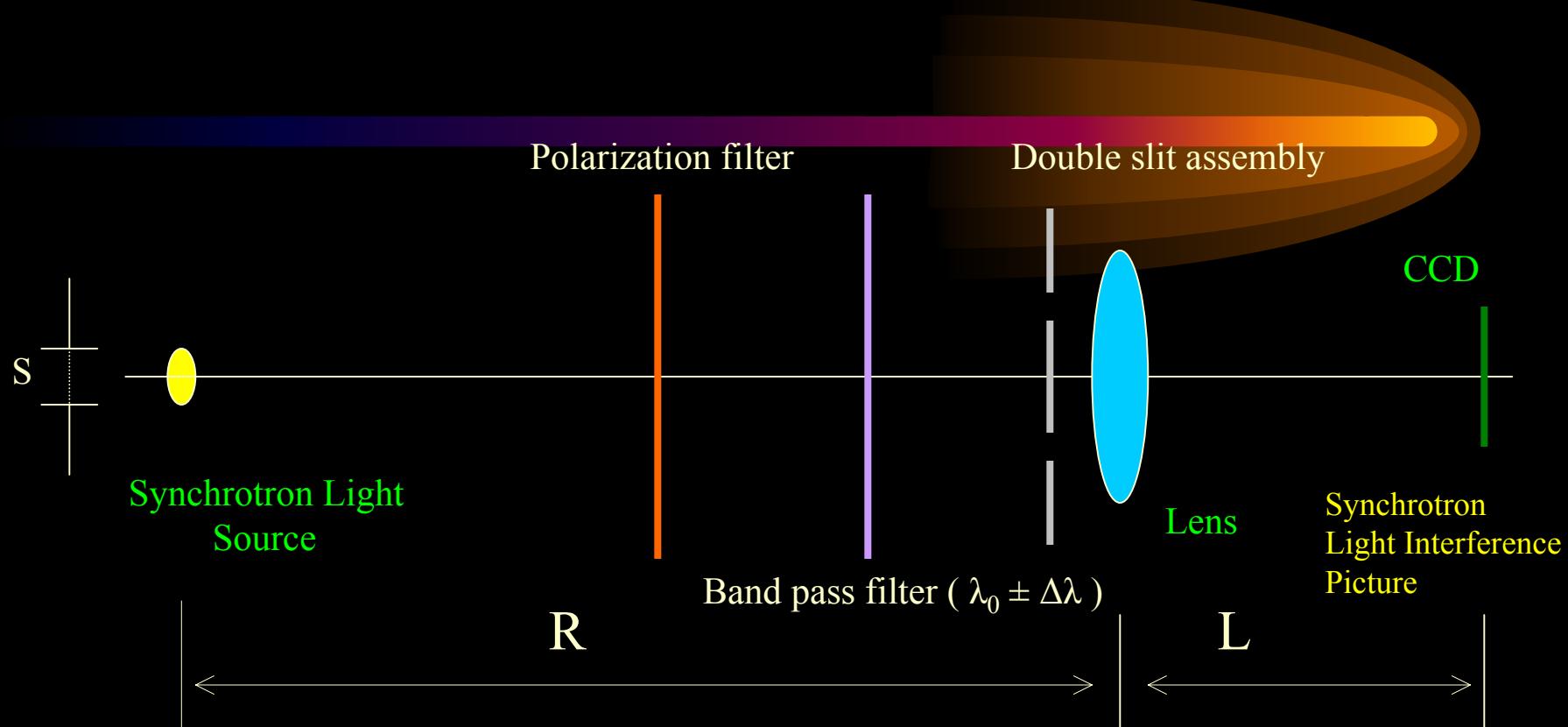
$$\sigma_S = 0.12 \text{ mm}$$



Synchrotron Light Interferometer at Jefferson Lab

Main Components

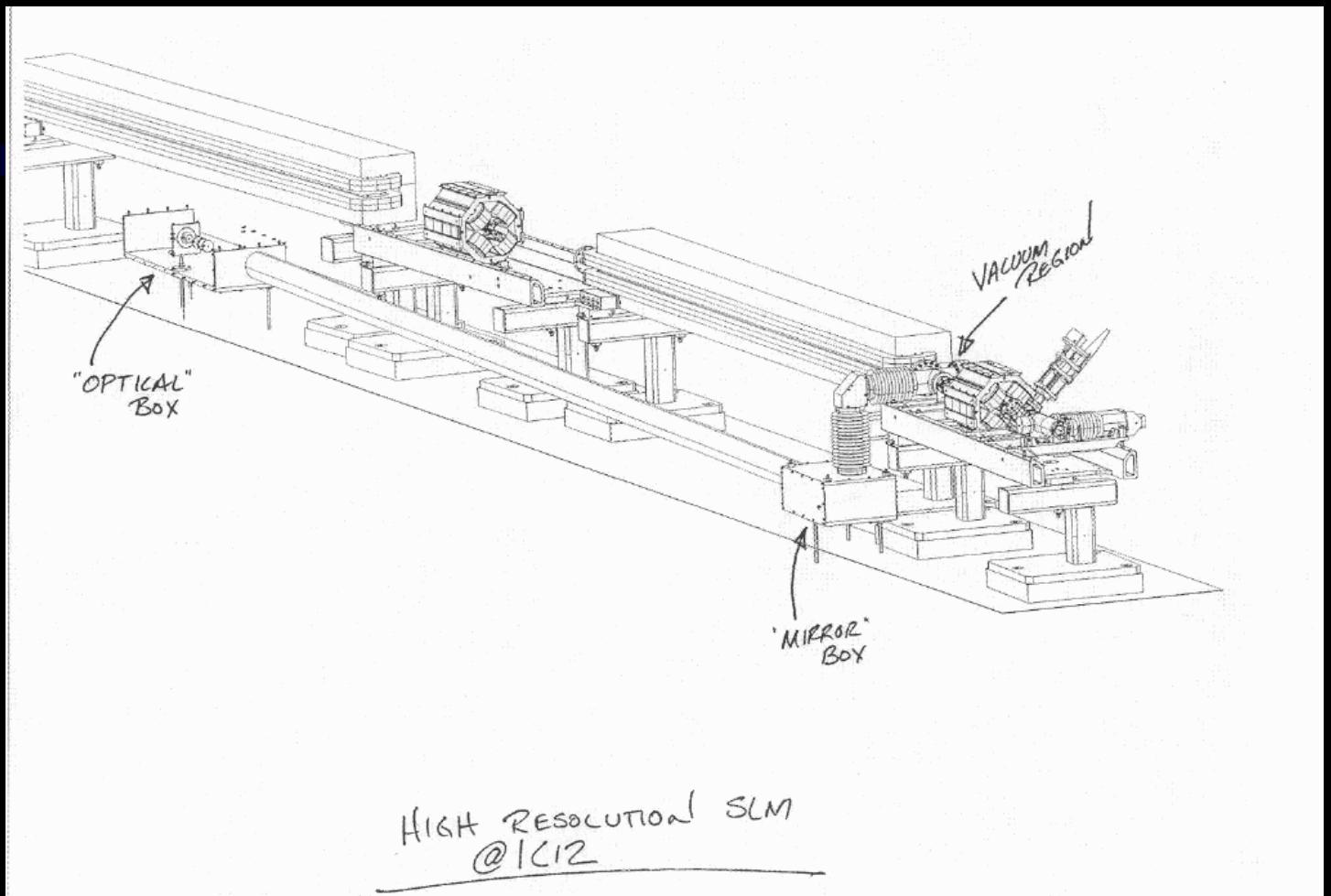
Synchrotron Radiation Interferometer at Jefferson Lab

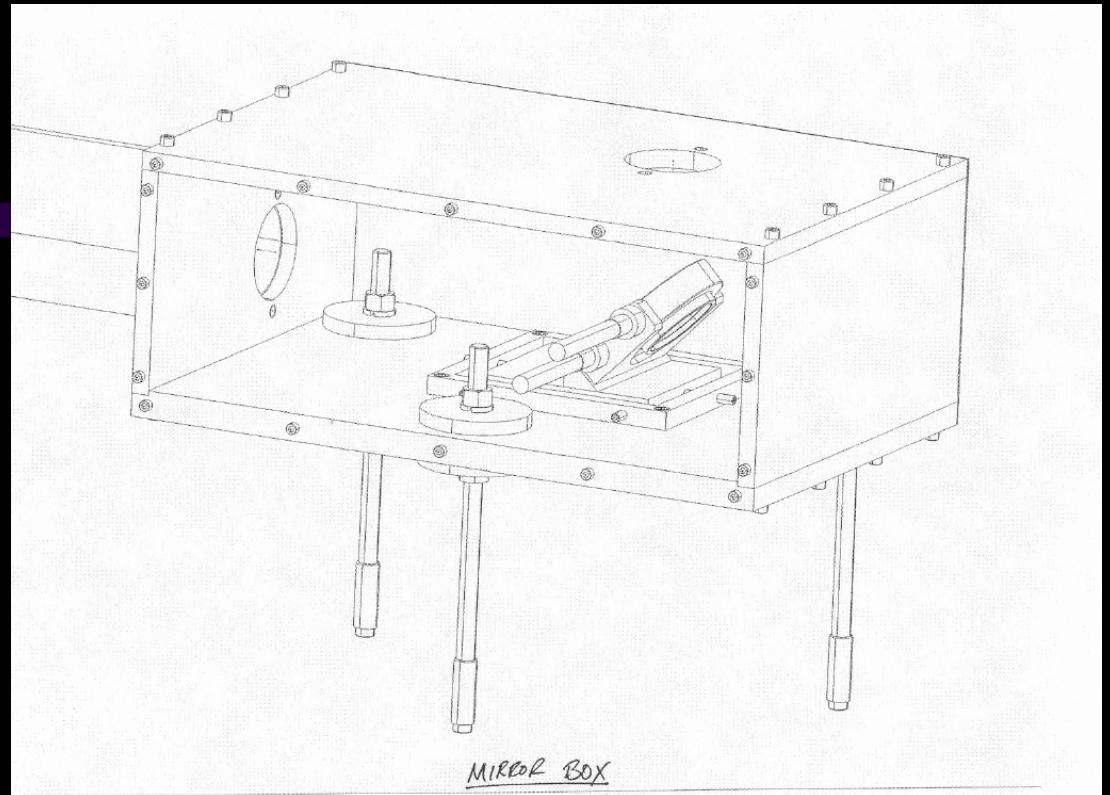


$$R = 9.18 \text{ m} \quad L = 1.12 \text{ m} \quad \lambda_0 = 630 \text{ nm} \quad \rho = 40 \text{ m}$$

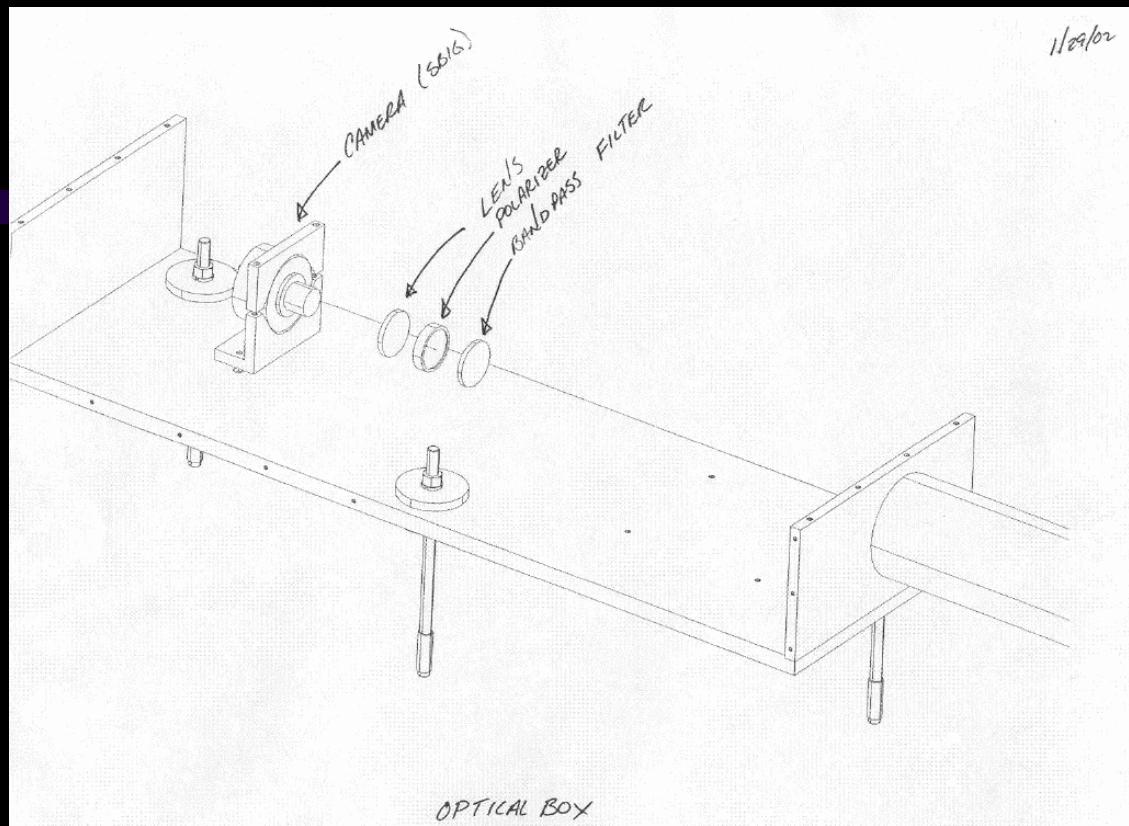


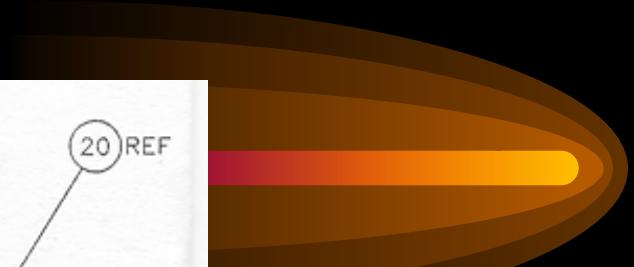
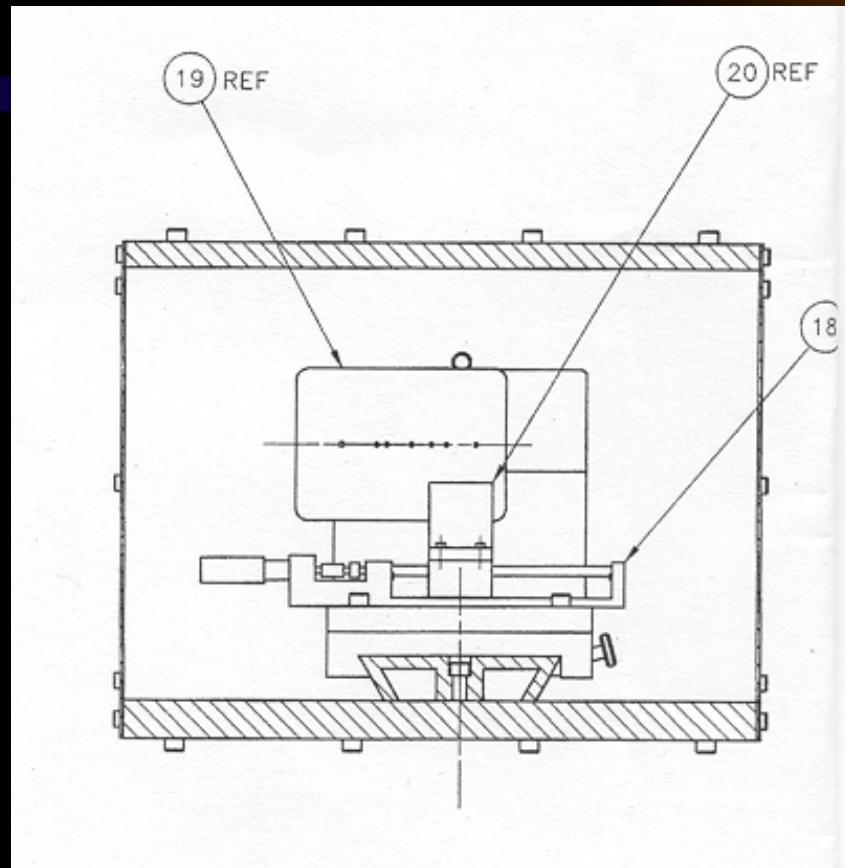
1C12

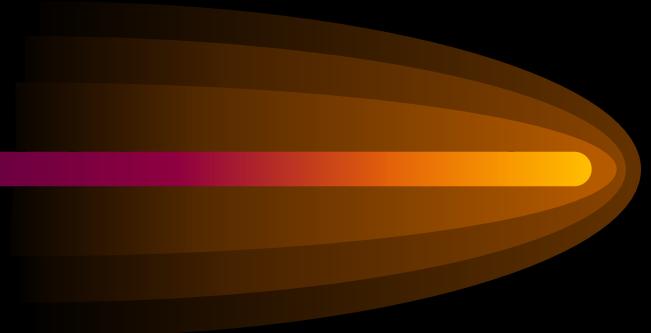




1/29/02

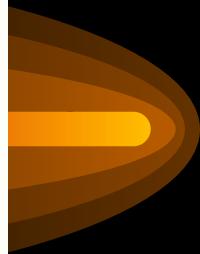
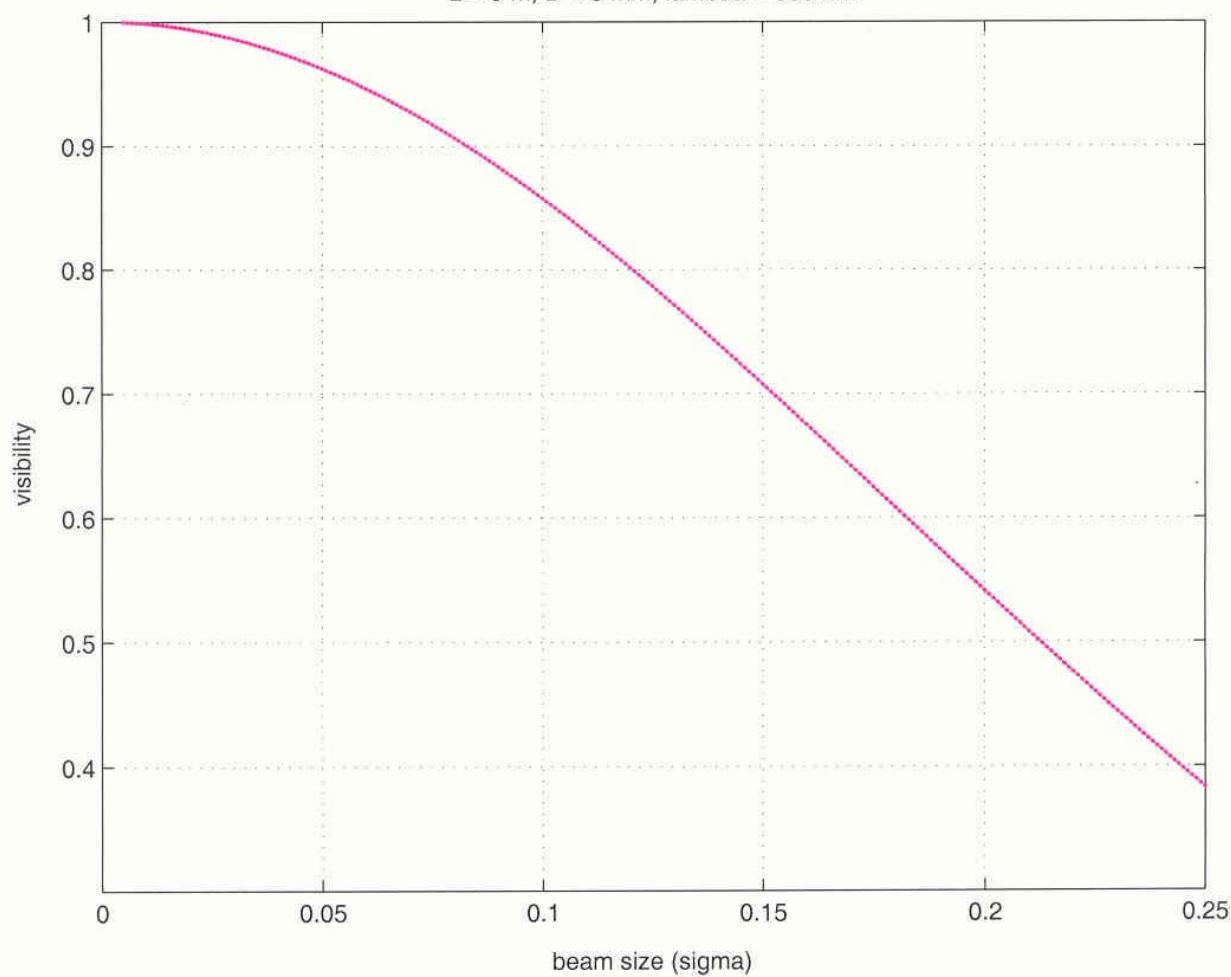


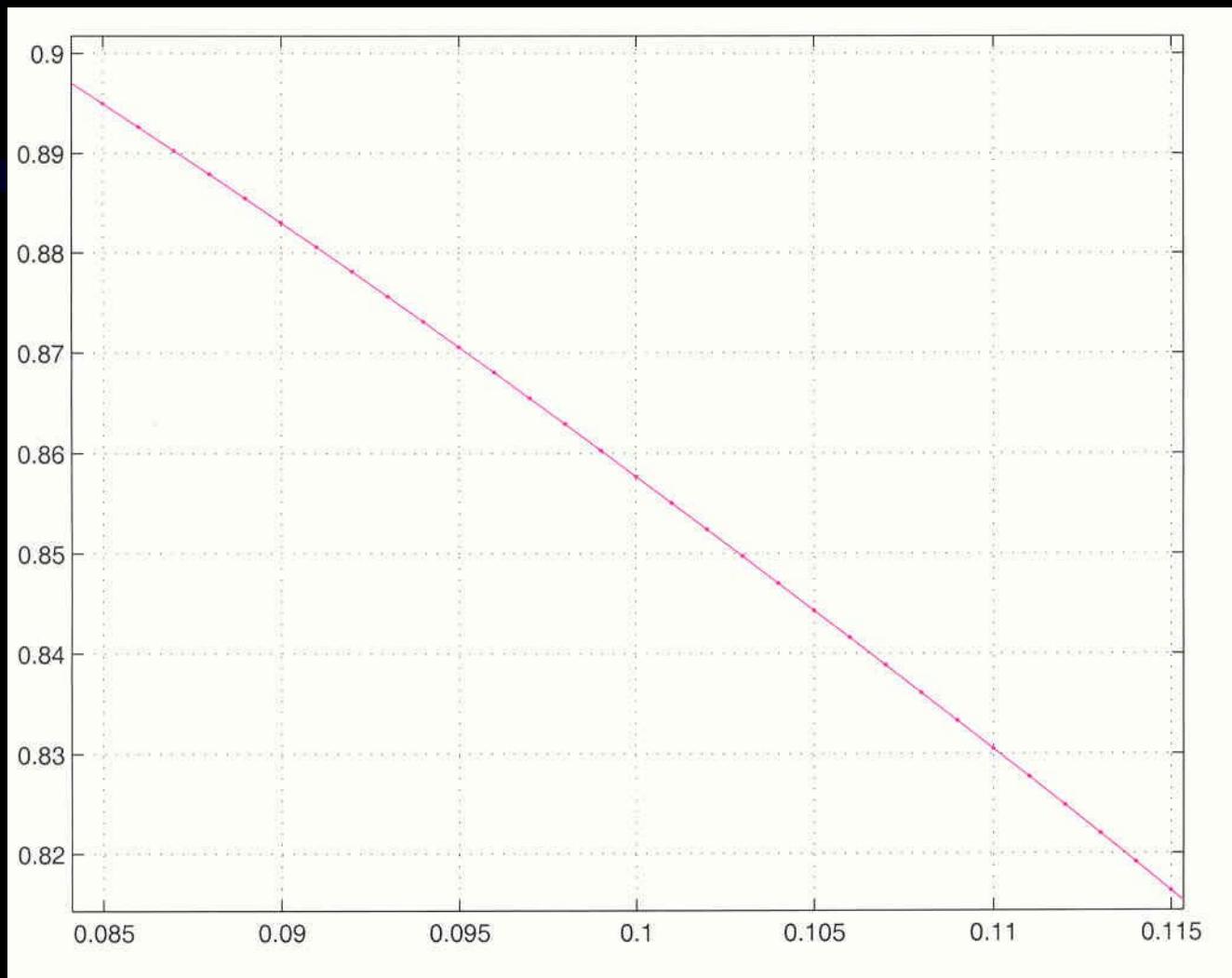




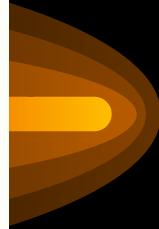
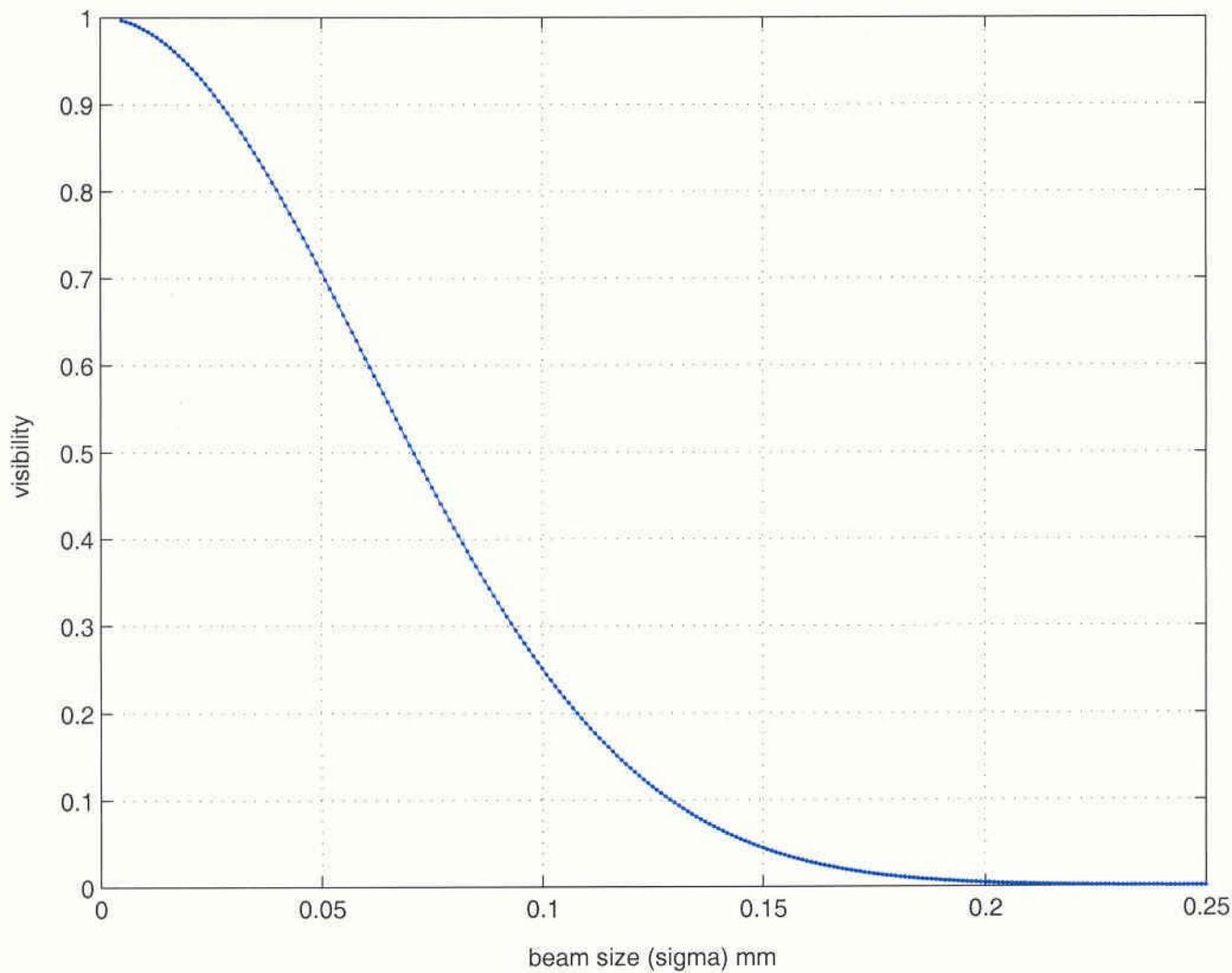
Resolution of our synchrotron light interferometer

$L = 9 \text{ m}$, $D = 5 \text{ mm}$, $\lambda = 630 \text{ nm}$

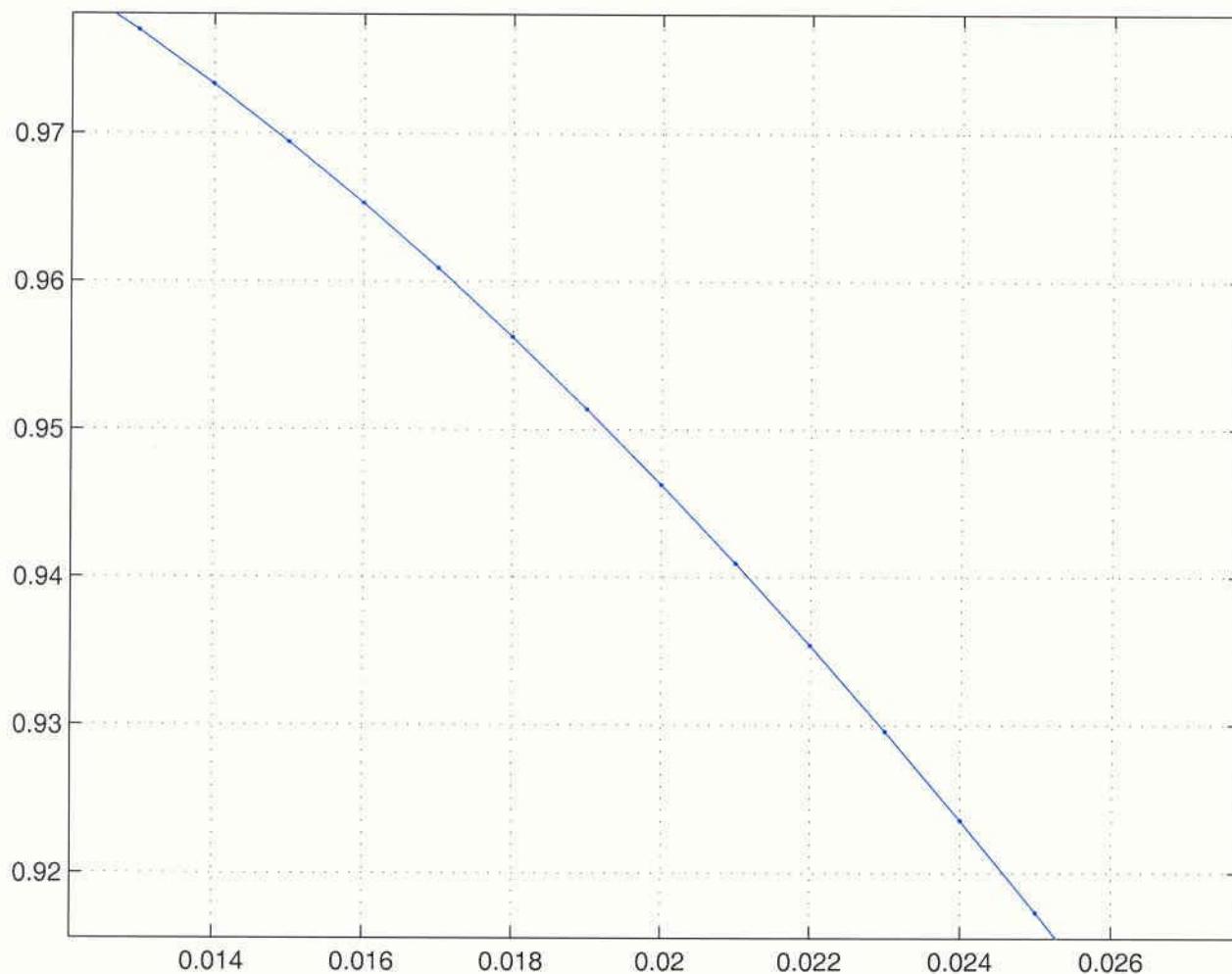


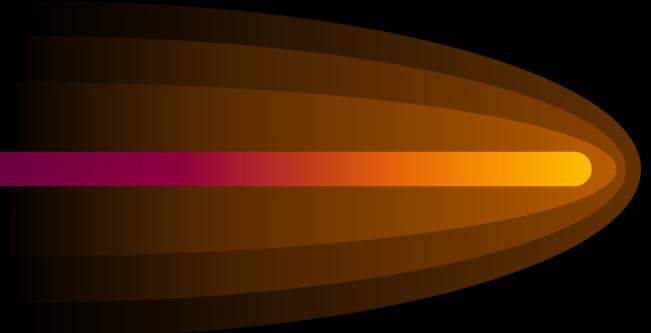


$L = 9 \text{ m}$, $\lambda = 630 \text{ nm}$, $D = 15 \text{ mm}$



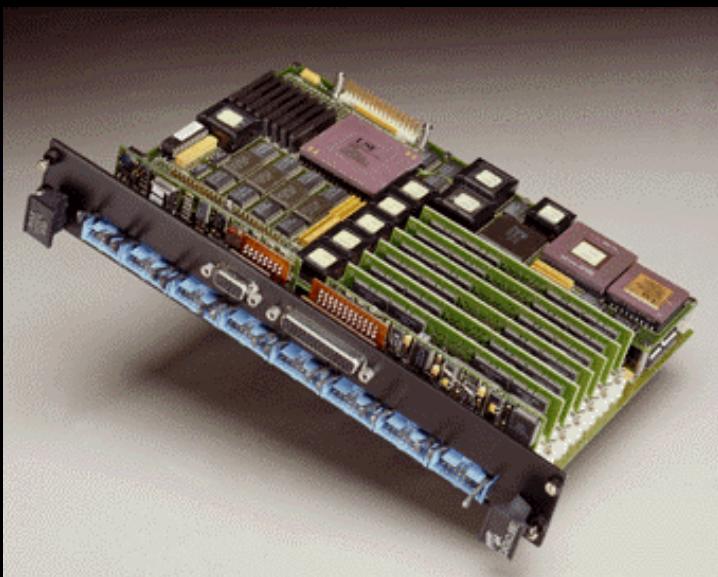
$L = 9 \text{ m}$, $\lambda = 630 \text{ nm}$, $D = 15 \text{ mm}$





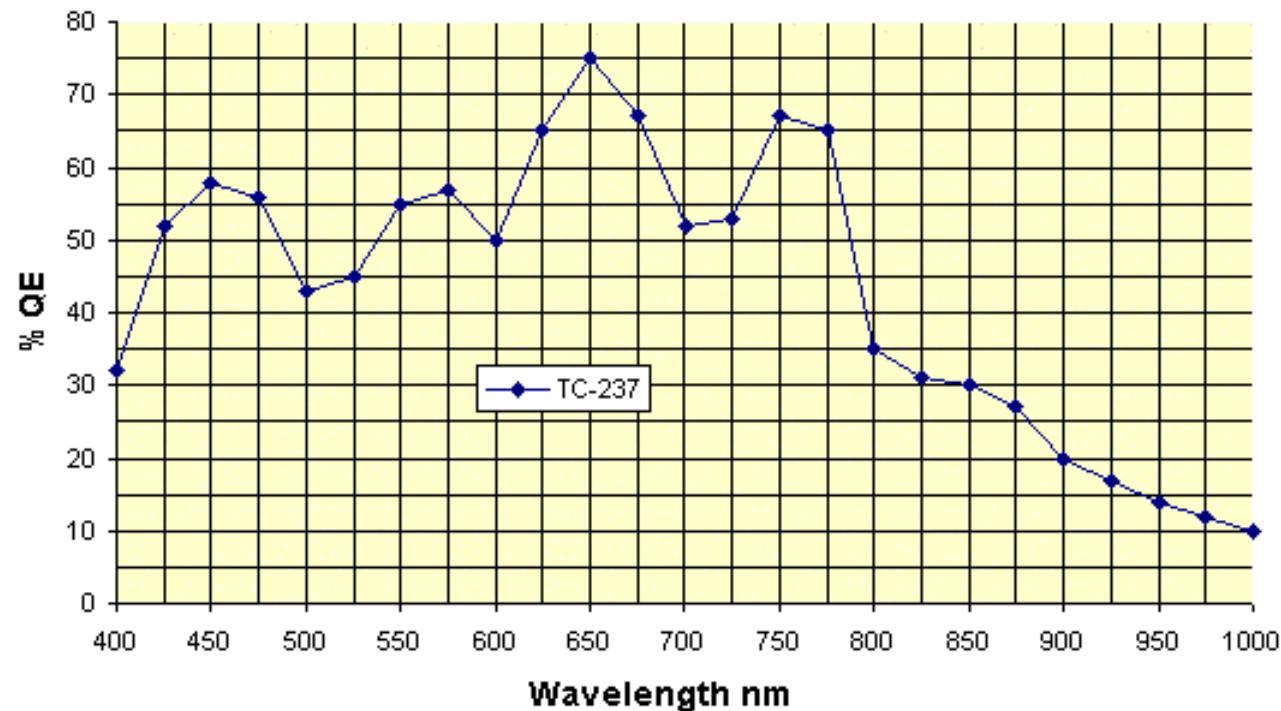
Our Synchrotron Light Interferometer

Main Control Components

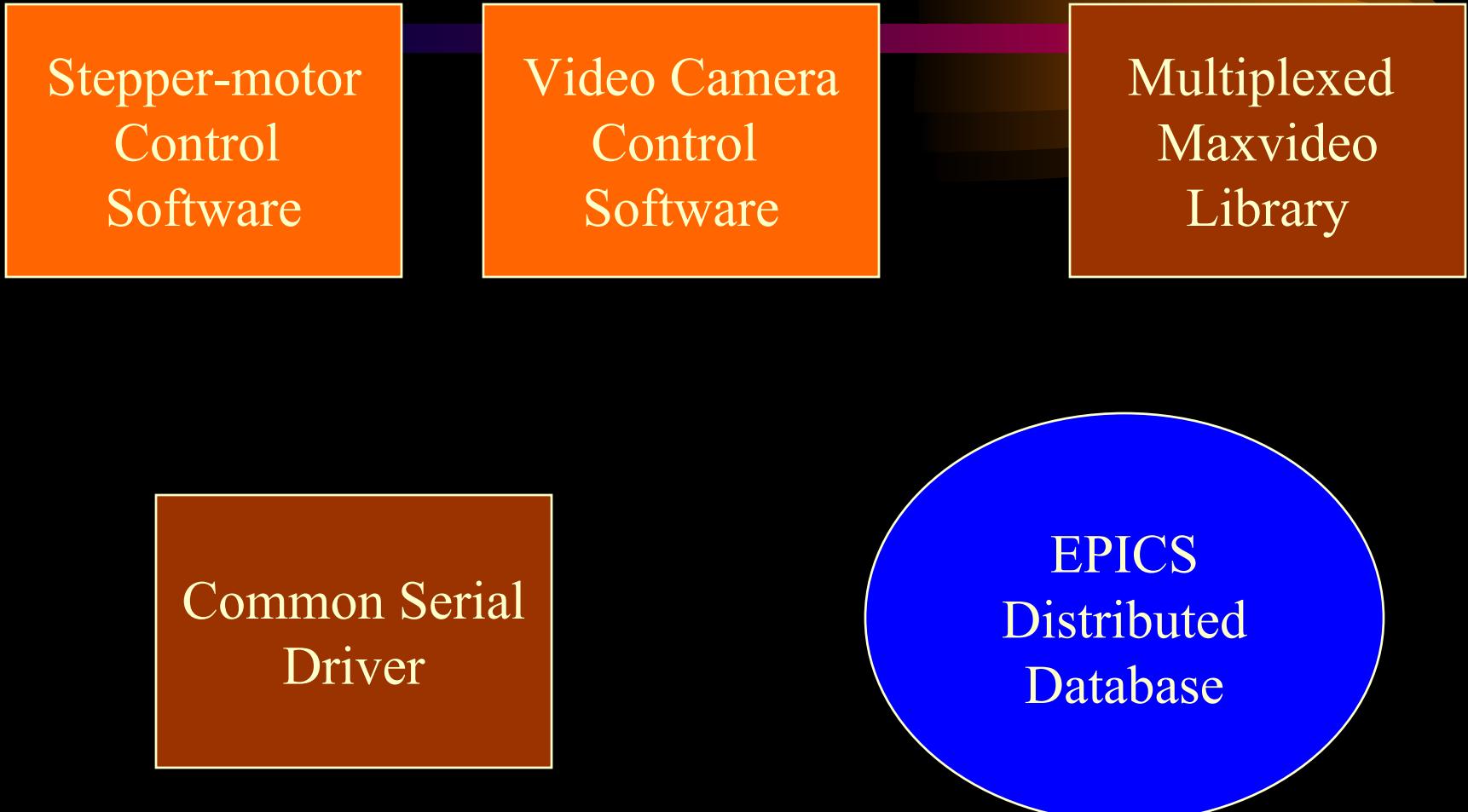


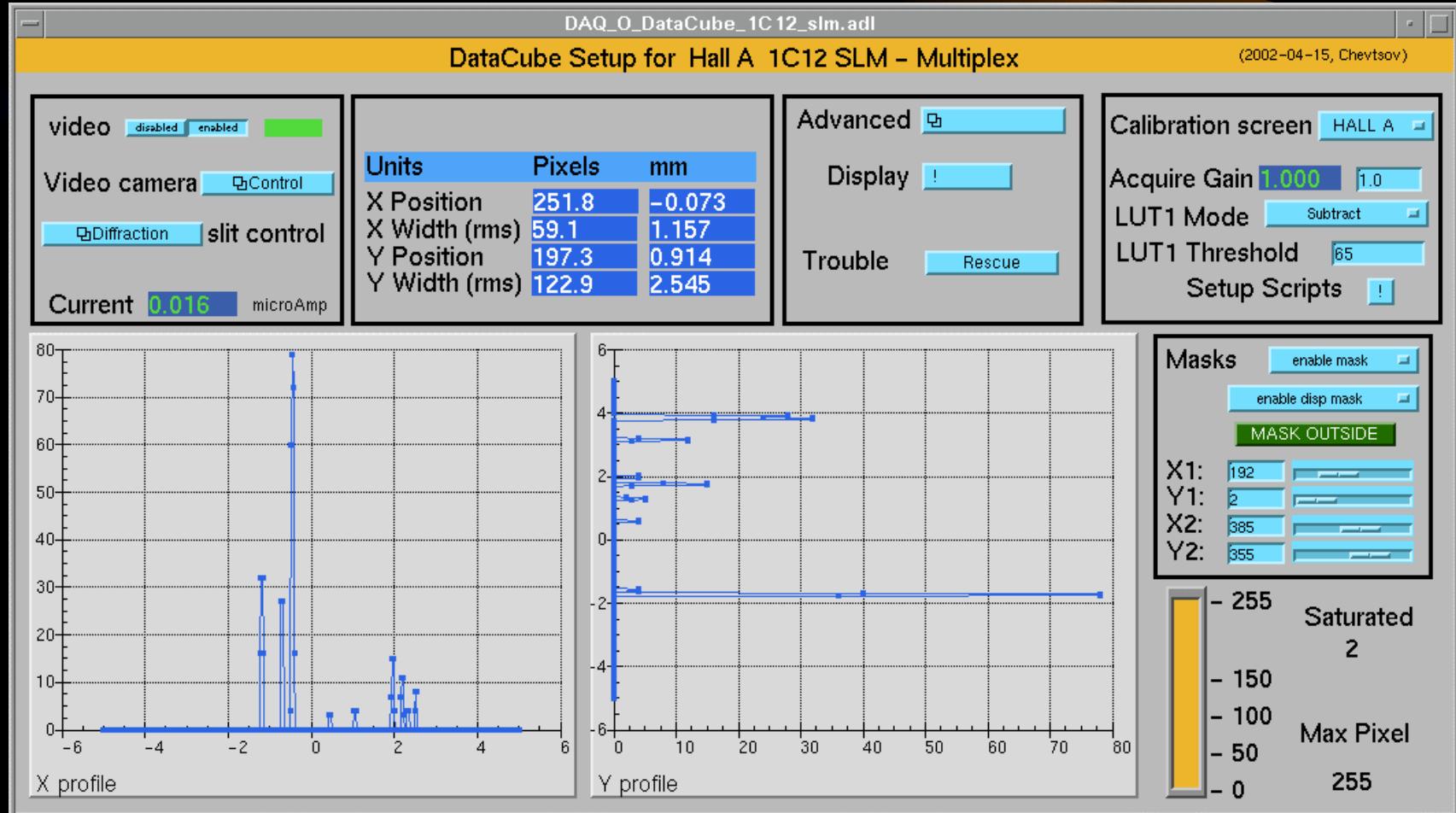


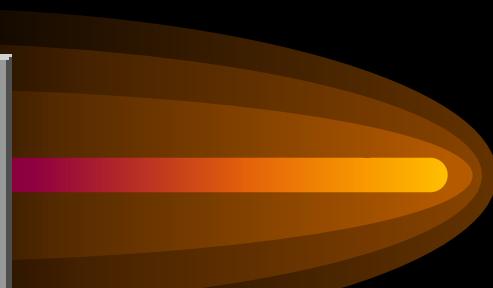
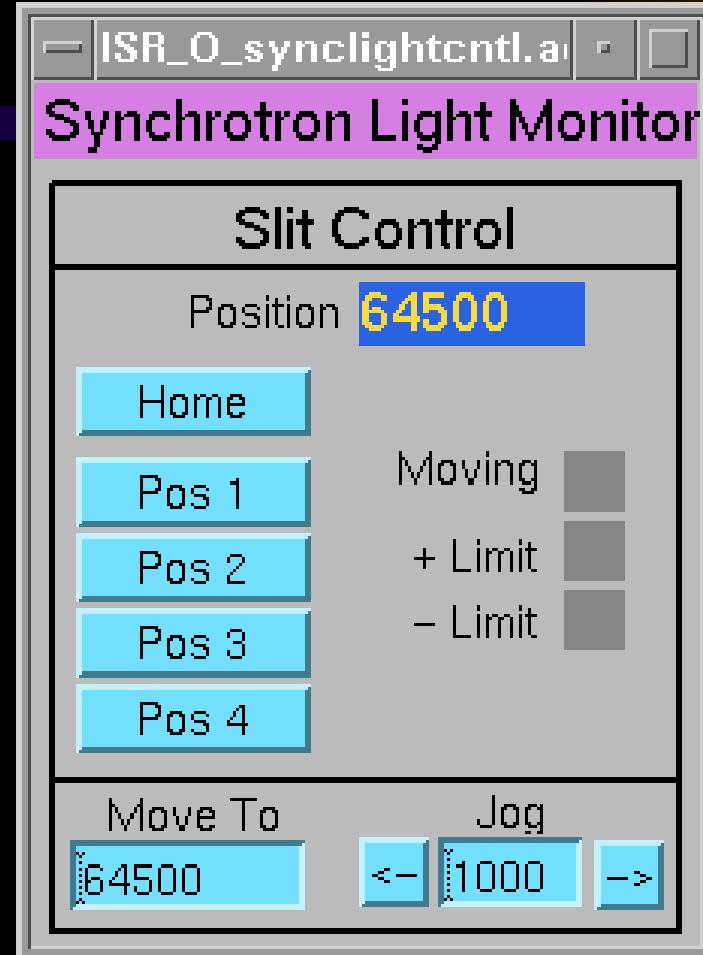
Quantum Efficiency ST-237 / Pixcel 237 / STV



Control Software Structure







STV CCD CAMERA CONTROL PANEL

focus image monitor

Acquire

IMAGE Norm,Exp=2.0s
øBright Contrast ø

parameter value

left right left right

Control

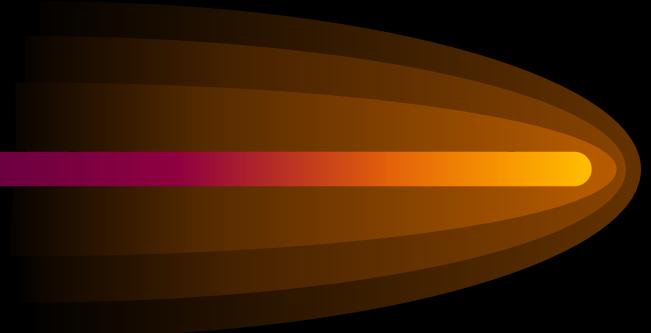
calibrate
track

display
fileops

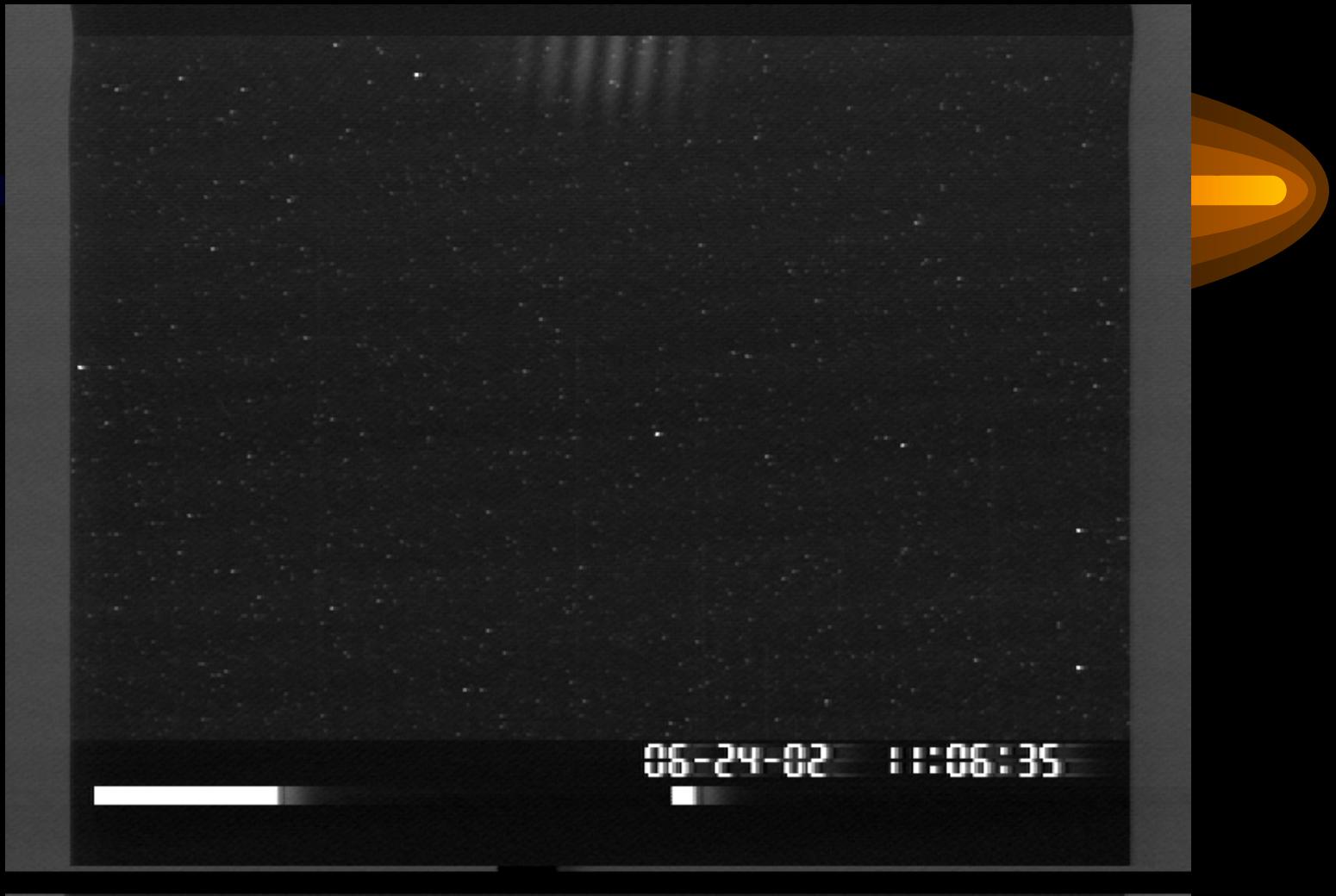
Guide Process

setup

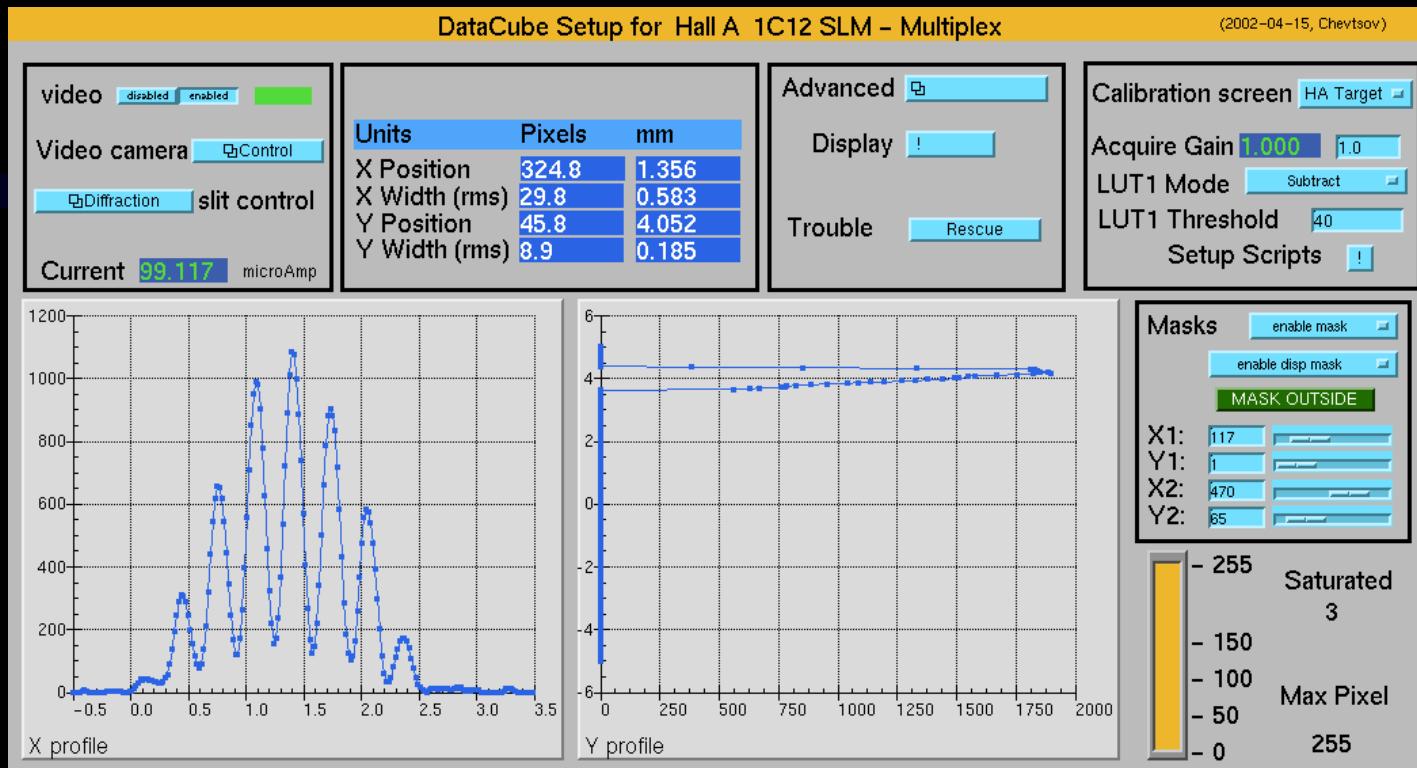
Setup Interrupt



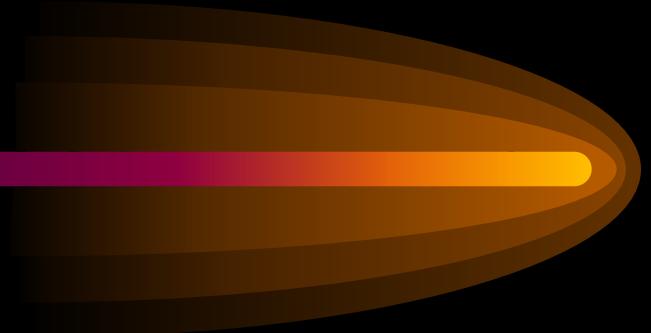
Very First Experimental Results



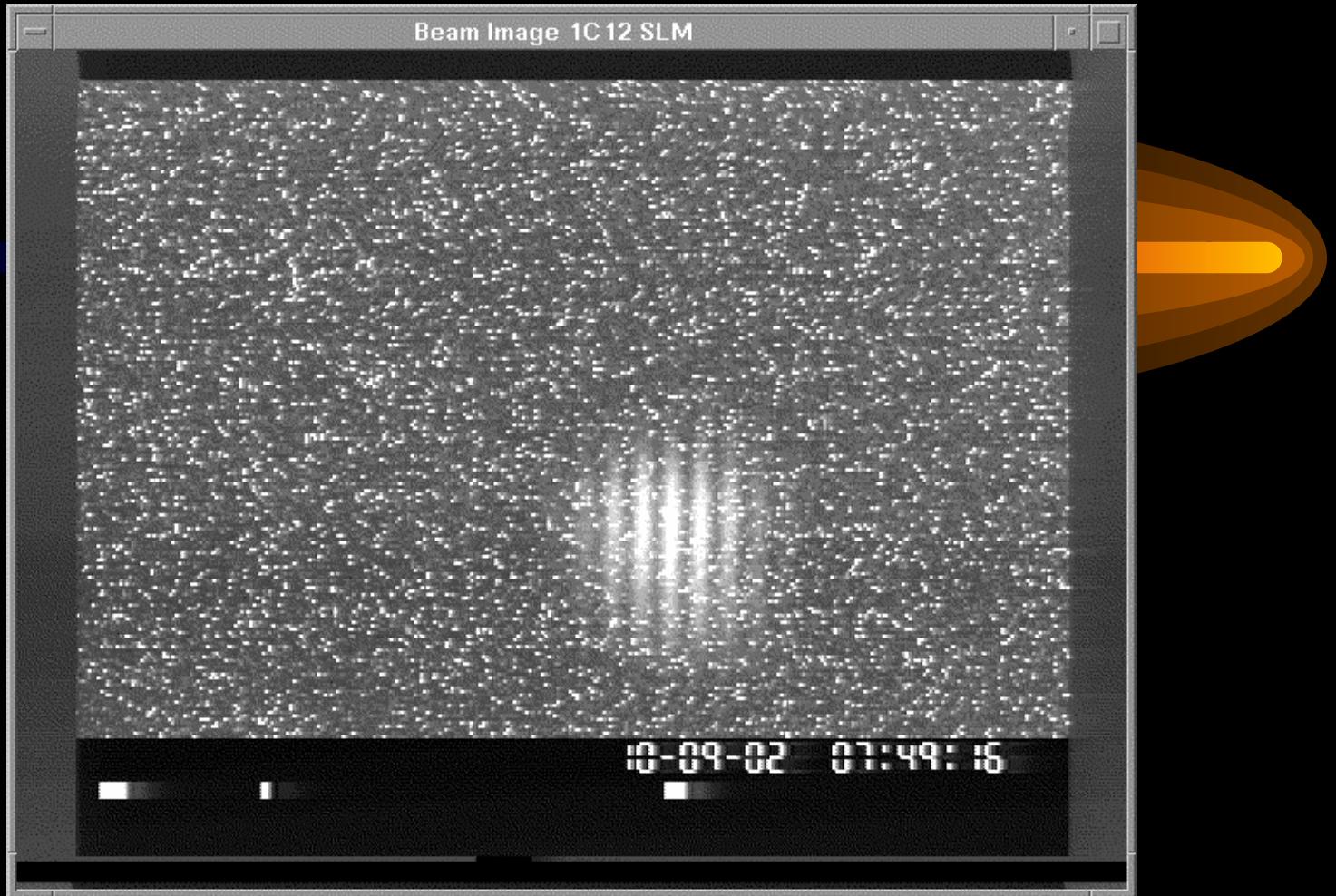
(exposure time = 2 sec)



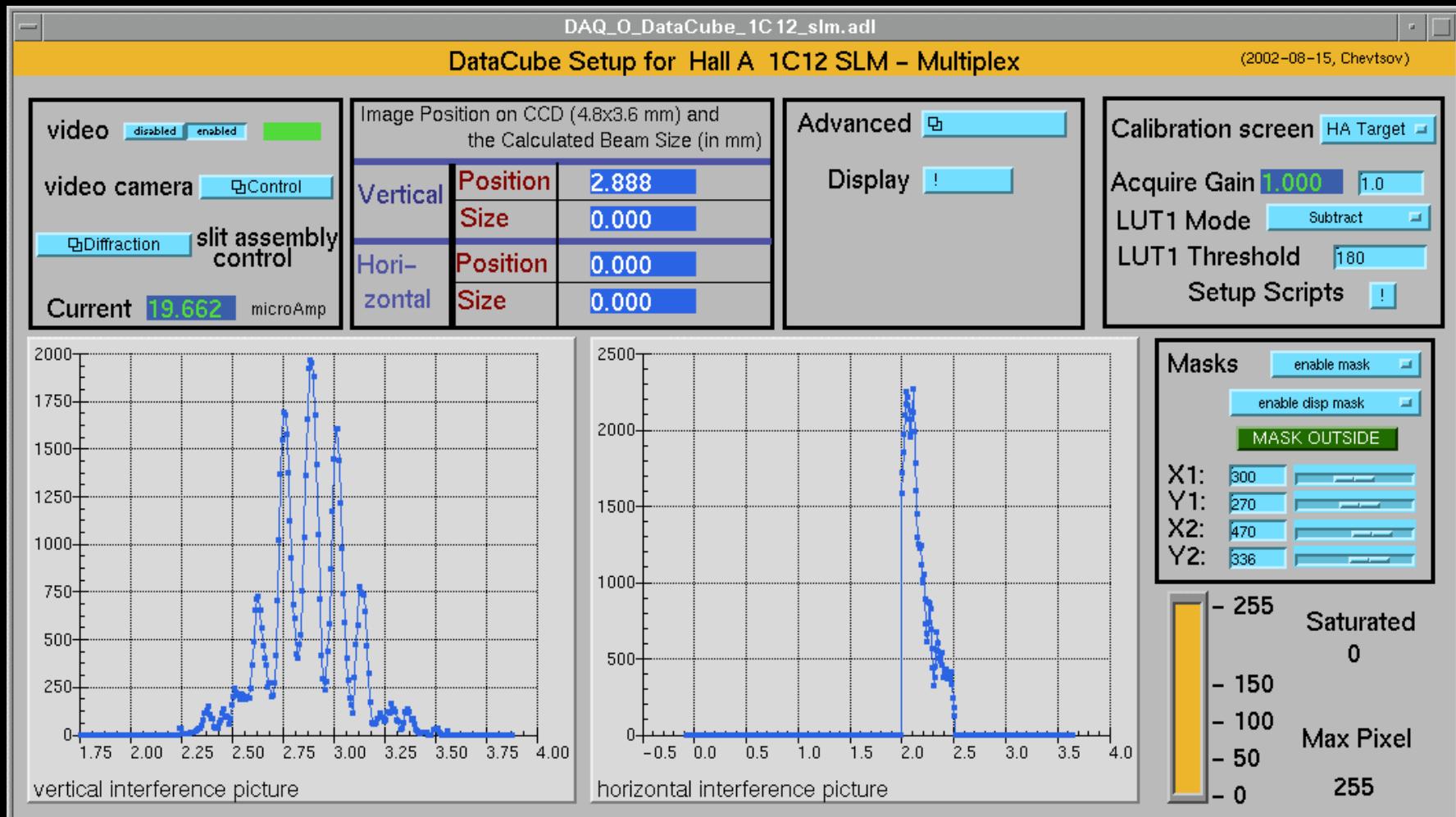
$$V = 0.8 \quad \sigma_S = 0.12 \text{ mm}$$



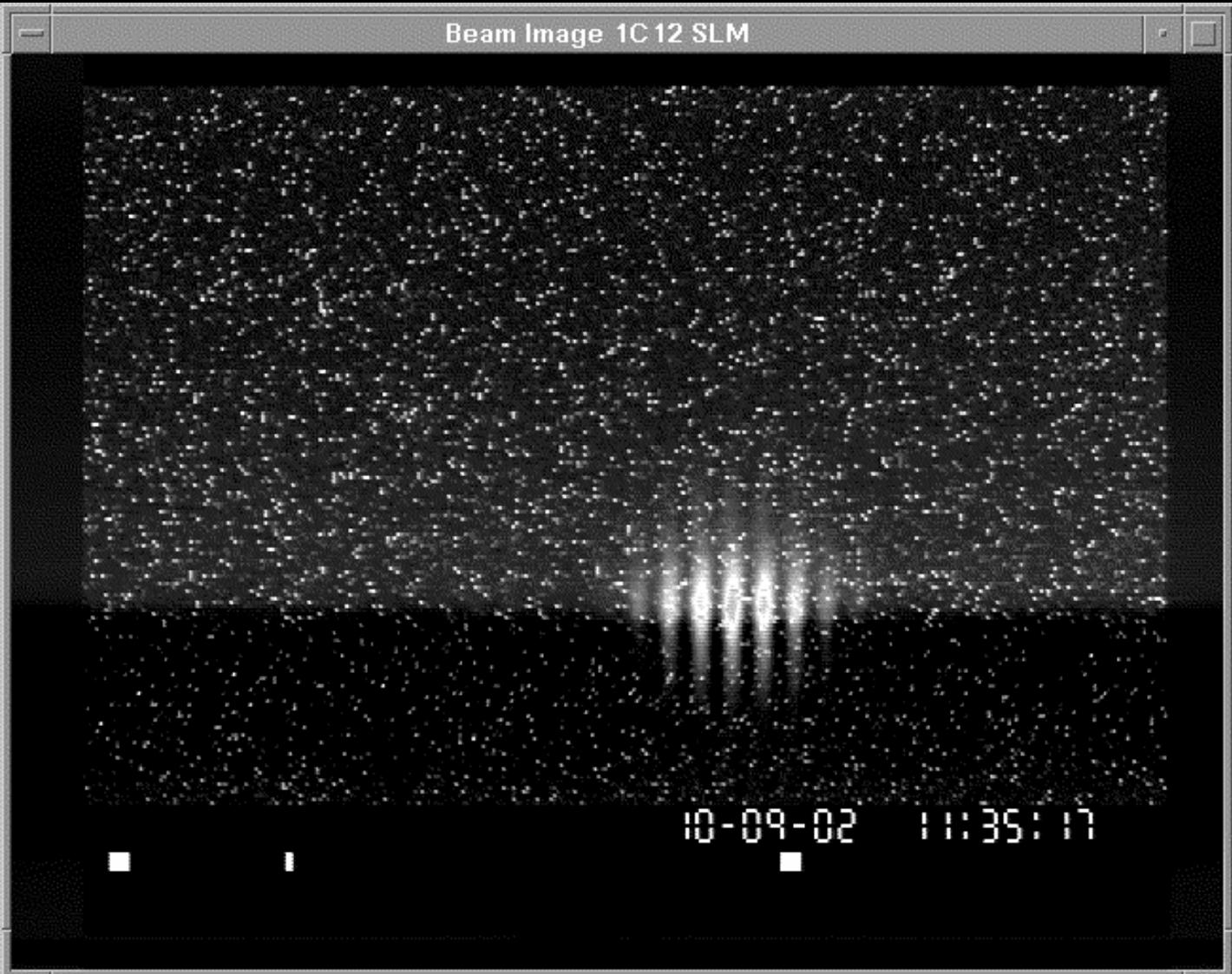
SLI Data After 2002 Summer Shutdown



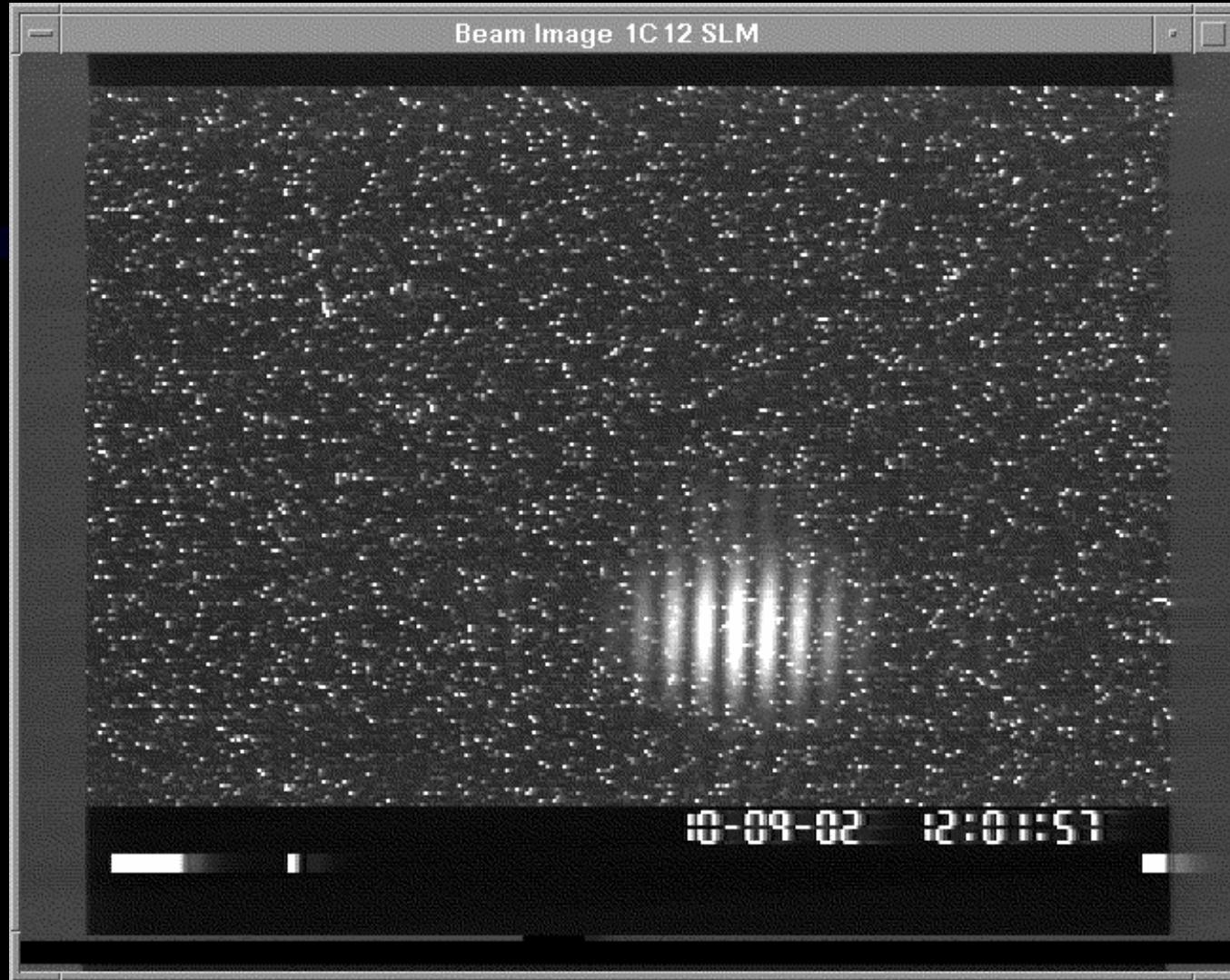
(exposure time = 50 sec)



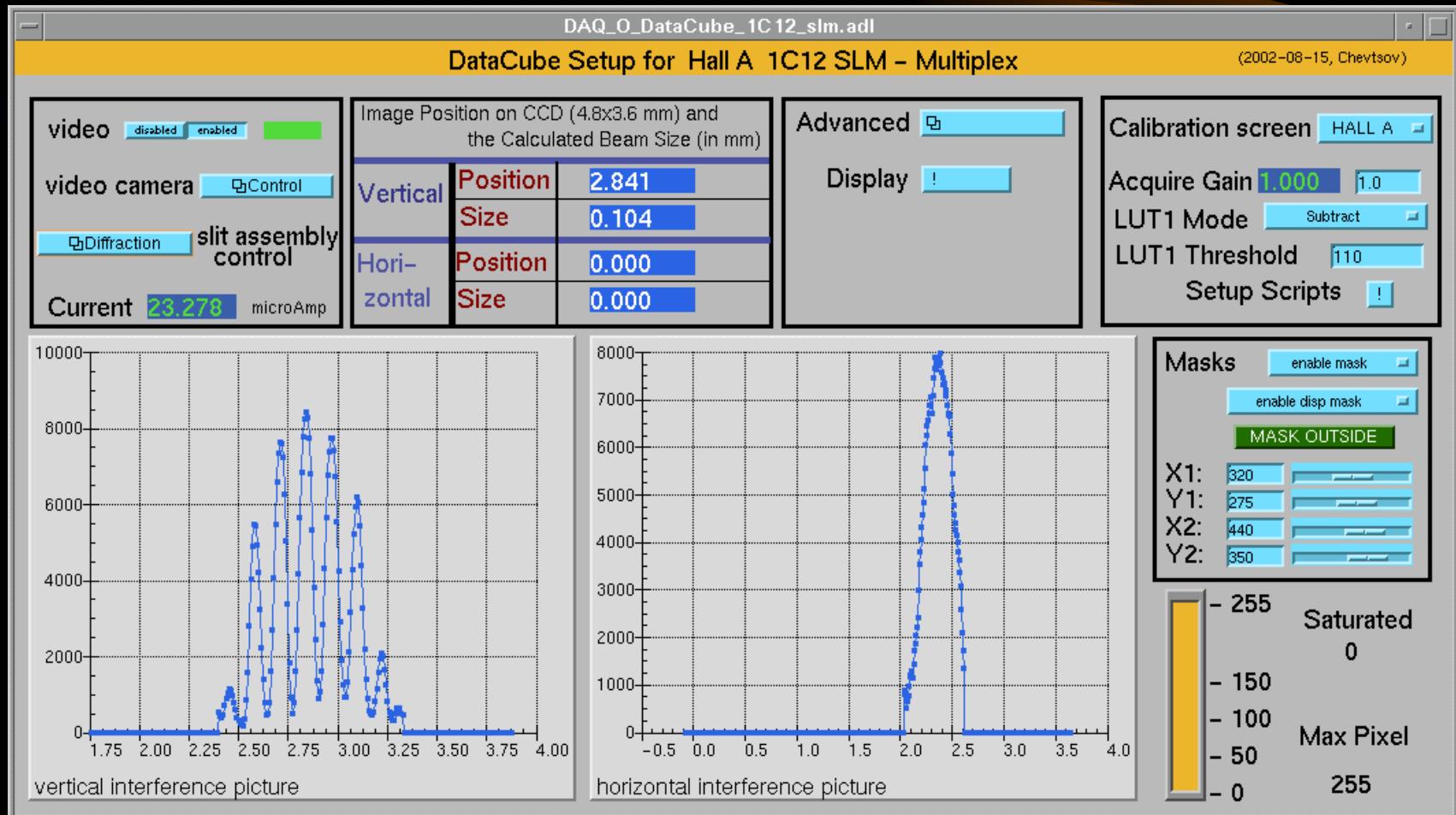
Beam Image 1C12 SLM



10-09-02 11:35:17



(exposure time = 10 sec)

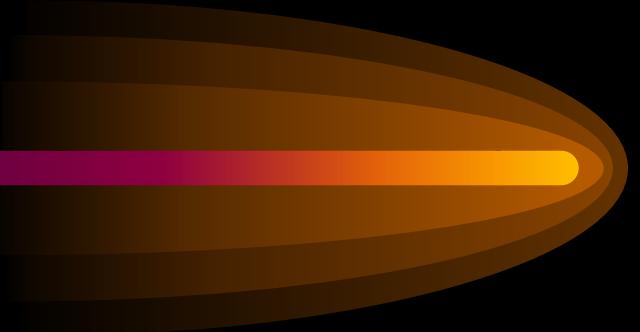


From - Thu Oct 10 10:44:23 2002
Received: (from majordom@localhost)
 by mailer.jlab.org (8.11.6/8.11.6) id g9ADBv915120;
 Thu, 10 Oct 2002 09:11:57 -0400 (EDT)
Received: from jlab.org (localhost [127.0.0.1])
 by mailer.jlab.org (8.11.6/8.11.6) with ESMTP id g9ADBSx15113;
 Thu, 10 Oct 2002 09:11:55 -0400 (EDT)
Message-ID: <3DA57C9A.7C97CC1A@jlab.org>
Date: Thu, 10 Oct 2002 09:11:54 -0400
From: Jay Benesch <benesch@jlab.org>
X-Mailer: Mozilla 4.78 [en] (X11; U; HP-UX B.10.20 9000/785)
X-Accept-Language: en
MIME-Version: 1.0
To: machine-ops@jlab.org
Subject: 8am mtg 10/10/02
Content-Type: text/plain; charset=us-ascii
Content-Transfer-Encoding: 7bit
Sender: owner-machine-ops@jlab.org
Precedence: bulk
Reply-To: Jay Benesch <benesch@jlab.org>

Day SHIFT SUMMARY

Shift began with beam delivery to both halls. At 10:00 we terminated beam delivery to the halls to do a spot move, repair Fast Feedback, and send CW G0 beam to the BSY dump. All of these things were achieved :)
Spot move increased A current to ~24uA.

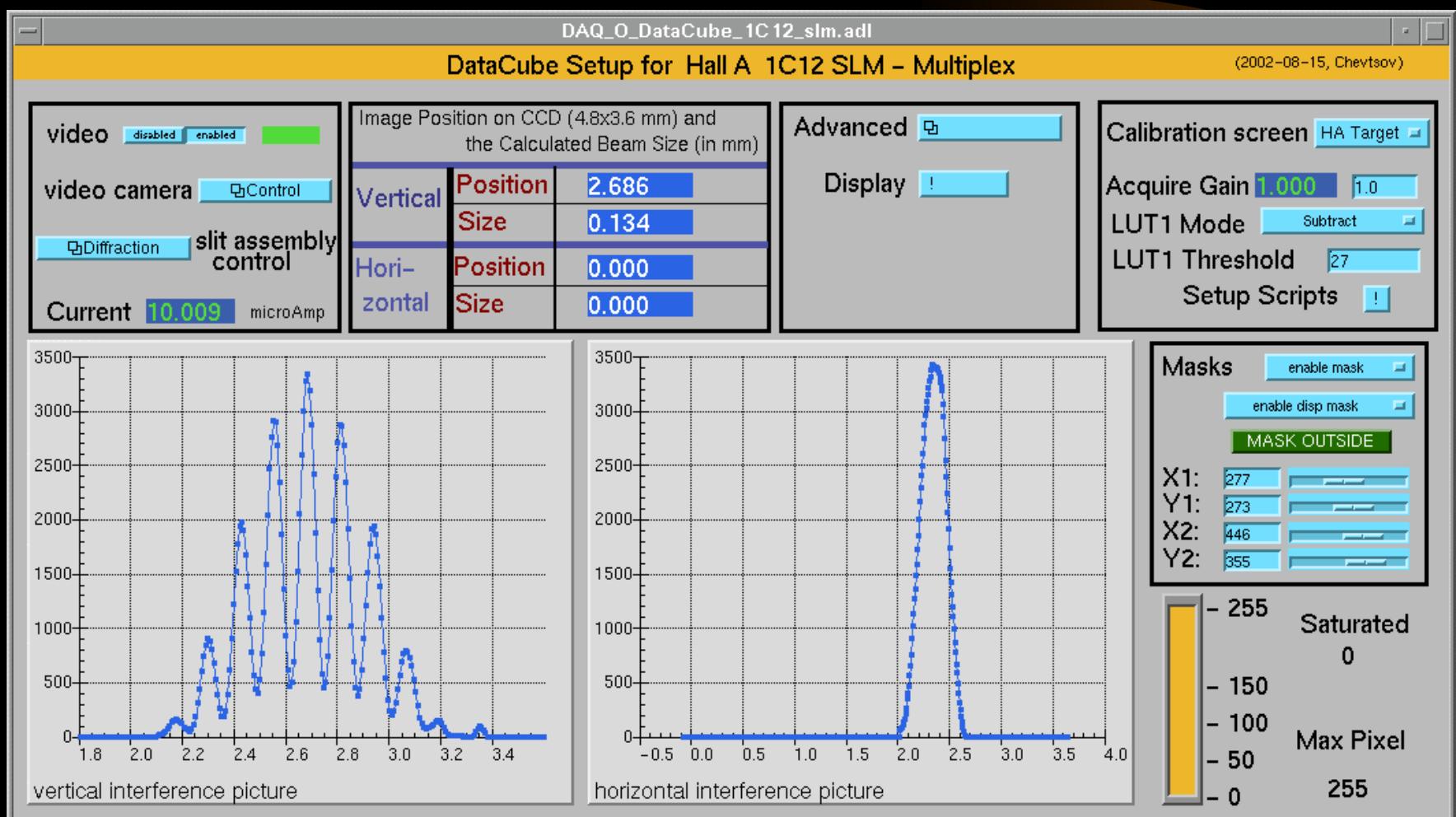
FFB restored by returning missing trim cards.
Steered ~12uA CW G0 beam to BSY dump. G0 beam delivery continued in parallel with delivery to halls A and B.

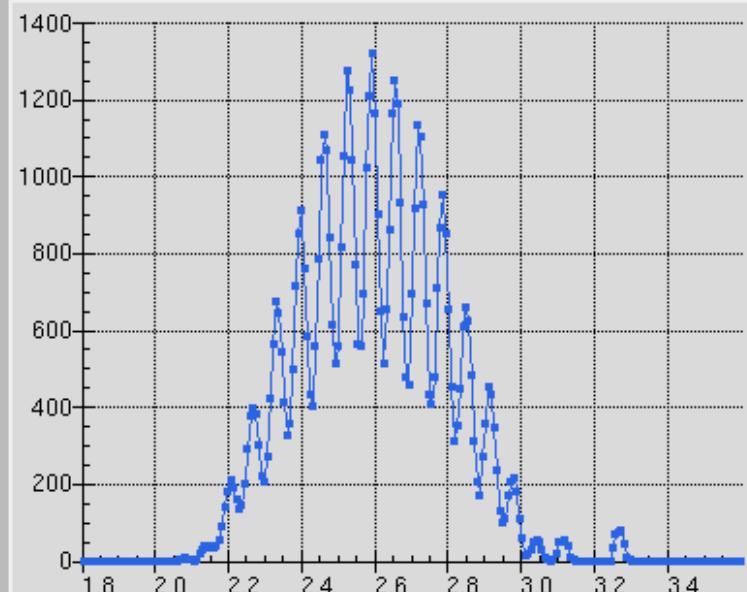


Recent Data

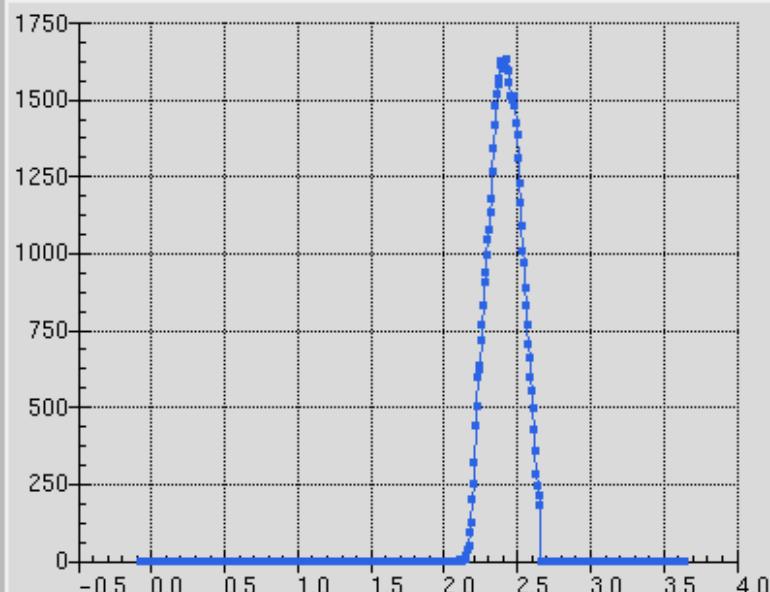


(exposure time = 15 sec)



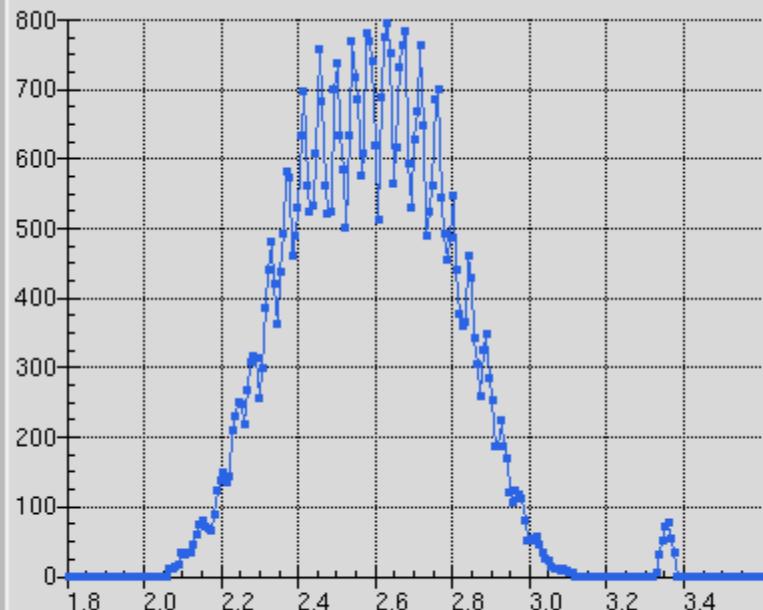


vertical interference picture

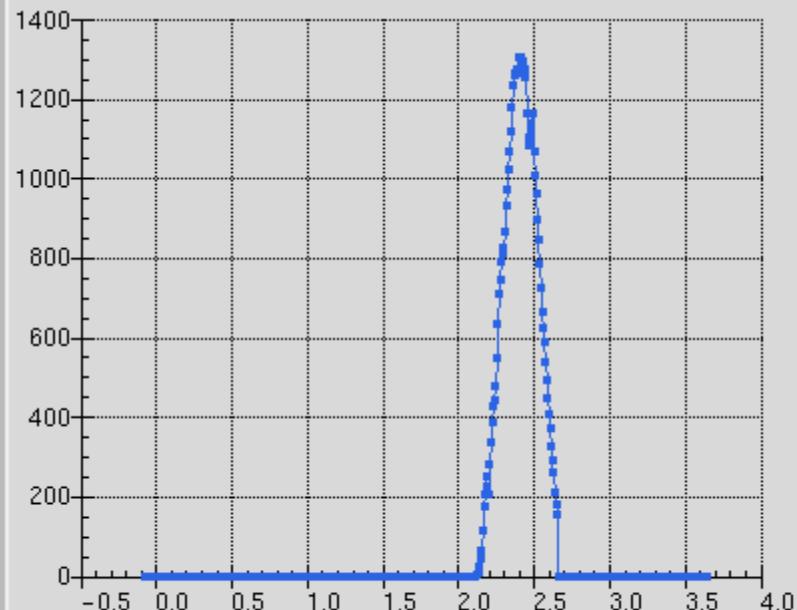


horizontal interference picture



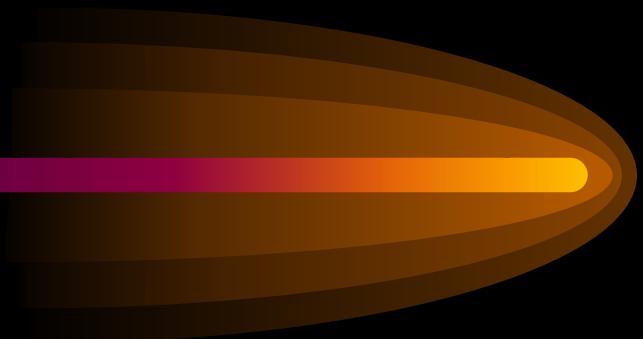


vertical interference picture

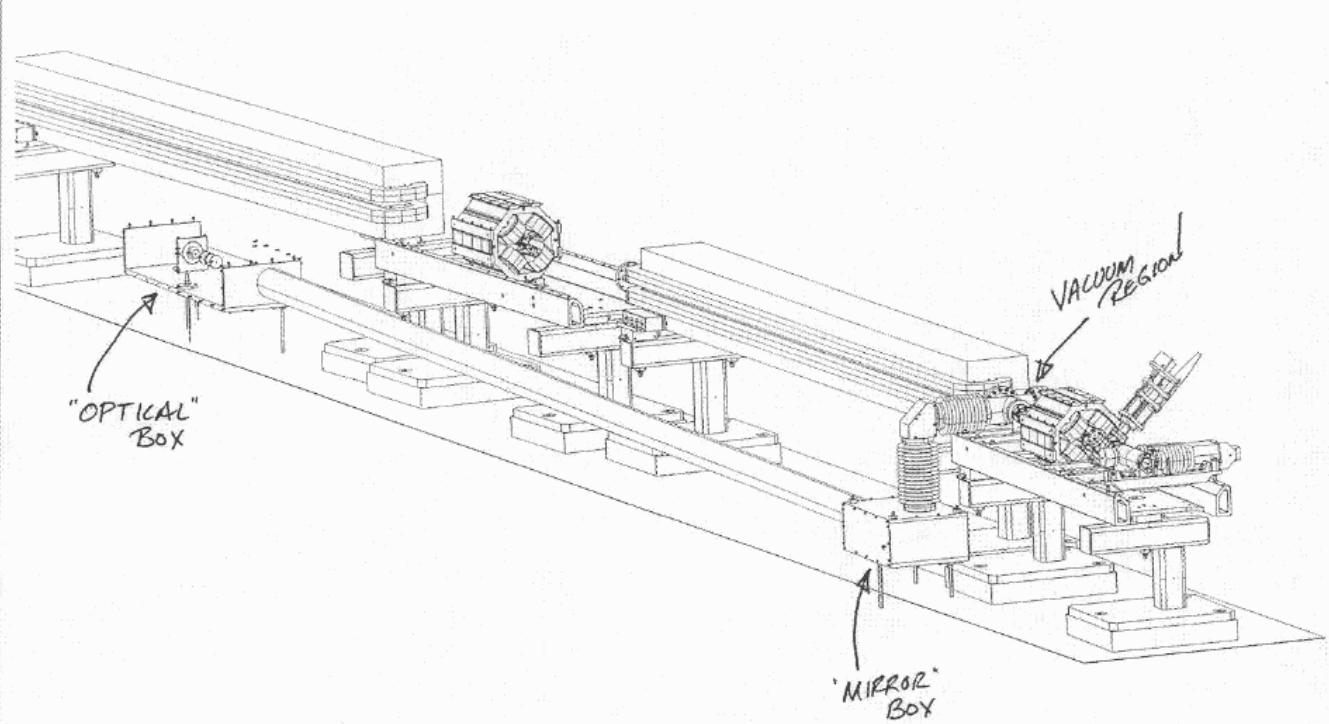


horizontal interference picture





Very Last Data



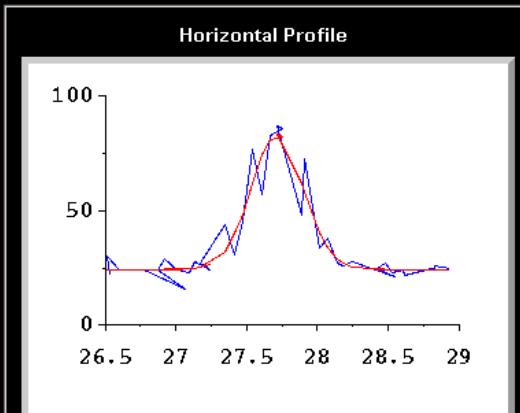
HIGH RESOLUTION SLM
@ IC12

MAG_O_1C_quads.adl

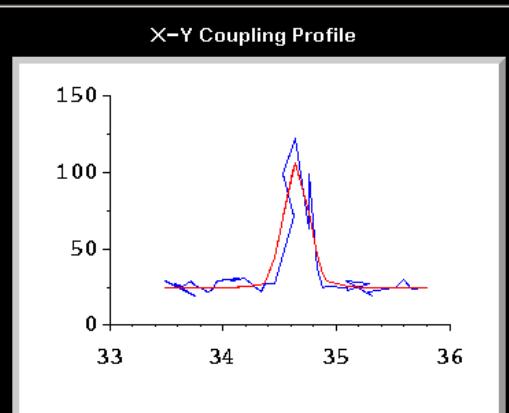
Quadrupoles for the 1C Region

M A G N E T M A C H	A O S F F L O O D P R A M P I N G	MAGNET NAME	HYSTERESIS LOOP SWITCH	INTEGRATED FIELD SET POINT DIPOLE UNITS IN GAUSS-CM QUADRUPOLE UNITS IN GAUSS SEXTUPOLE UNITS IN GAUSS/CM	CURRENT SETPOINT (amps)	CURRENT READBACK (amps)	S C R E P T S
● ● ●	● On Off	MQA1C01	● On Off	32991.699	3.065	3.063	!
● ● ●	● On Off	MQA1C02	● On Off	-53771.199	-5.495	-5.494	
● ● ●	● On Off	MQA1C03	● On Off	33732.102	3.139	3.137	
● ● ●	● On Off	MQA1C04	● On Off	40372.398	3.800	3.798	
● ● ●	● On Off	MQA1C05	● On Off	-21106.400	-2.249	-2.248	
● ● ●	● On Off	MQA1C06	● On Off	2735.050	0.091	0.089	
● ● ●	● On Off	MQA1C07	● On Off	-18061.000	-1.950	-1.949	
● ● ●	● On Off	MQA1C08	● On Off	25156.598	2.291	2.286	
● ● ●	● On Off	MQA1C09	● On Off	0.000	-0.177	-0.178	
● ● ●	● On Off	MQA1C10	● On Off	0.000	-0.177	-0.178	
● ● ●	● On Off	MQA1C11	● On Off	-20419.801	-2.182	-2.181	
● ● ●	● On Off	MQA1C12	● On Off	40953.801	3.858	3.854	
● ● ●	● On Off	MQA1C13	● On Off	-17858.699	-1.930	-1.929	
● ● ●	● On Off	MQA1C14	● On Off	0.000	-0.177	-0.177	
● ● ●	● On Off	MQA1C15	● On Off	0.000	-0.177	-0.178	
● ● ●	● On Off	MQA1C16	● On Off	22431.900	2.022	2.018	
● ● ●	● On Off	MQA1C17	● On Off	-13819.199	-1.533	-1.533	
● ● ●	● On Off	MQA1C18	● On Off	13987.000	1.192	1.190	
● ● ●	● On Off	MQA1C19	● On Off	-50556.801	-5.172	-5.172	
● ● ●	● On Off	MQA1C20	● On Off	41559.500	3.918	3.918	
● ● ●	● On Off	MQA1H01	● On Off	-6500.000	-0.815	-0.815	
● ● ●	● On Off	MQA1H04	● On Off	4081.280	0.222	0.215	
● ● ●	● On Off	MQA1H04A	● On Off	0.000	-0.177	-0.178	

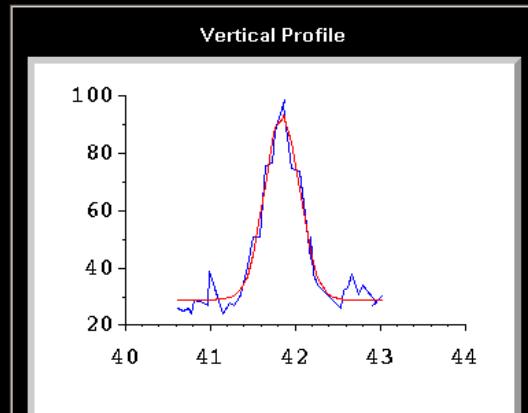
This screen is generated from the routine `./screen_codes/magnets/magpanel.c` V3.64 (Green, 2002-09-16)



Sigma(mm)	0.19	RMS(mm)	0.61
Position	27.72	Centroid	27.71



Sigma(mm)	0.11	RMS(mm)	0.59
Position	34.65	Centroid	34.63



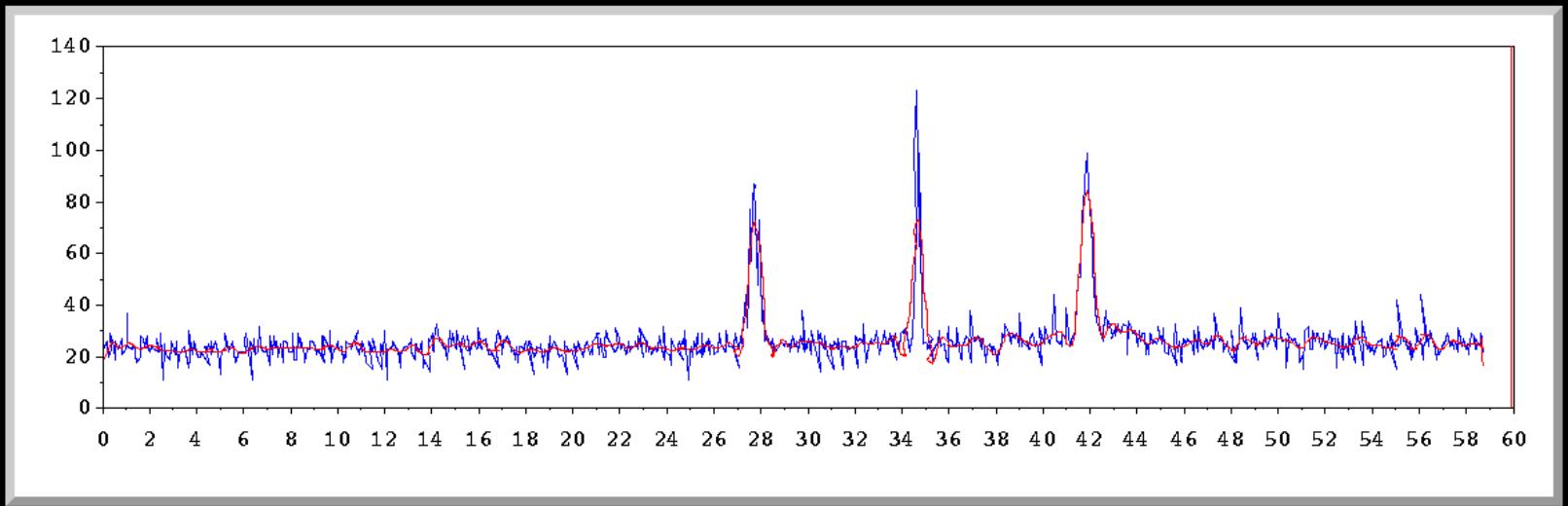
Sigma(mm)	0.20	RMS(mm)	0.61
Position	41.85	Centroid	41.84

Select Harp IHA1I01

Cycle Harp

Transfer Profile

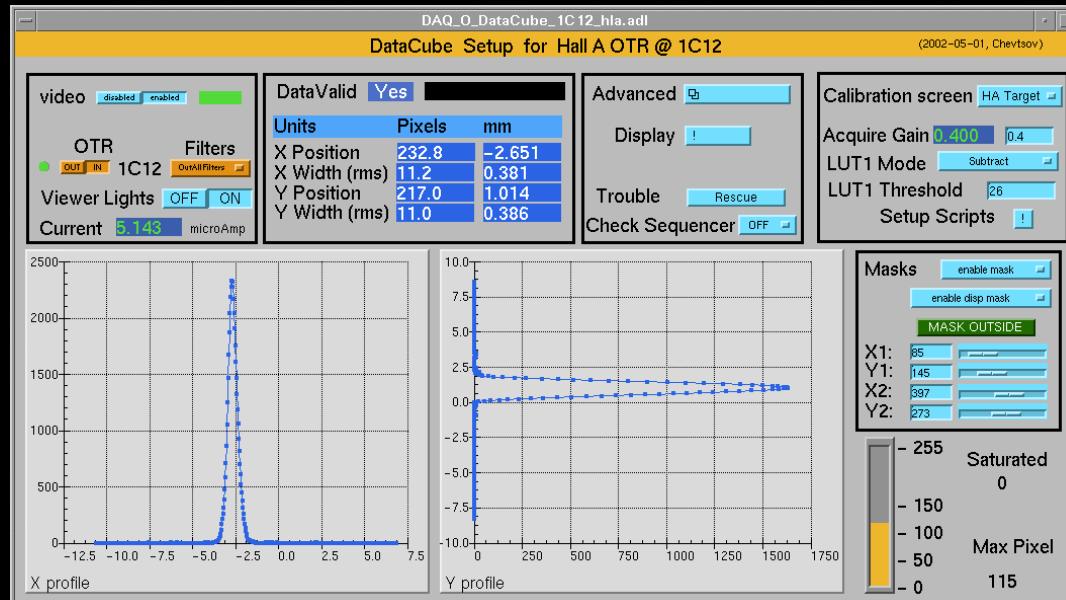
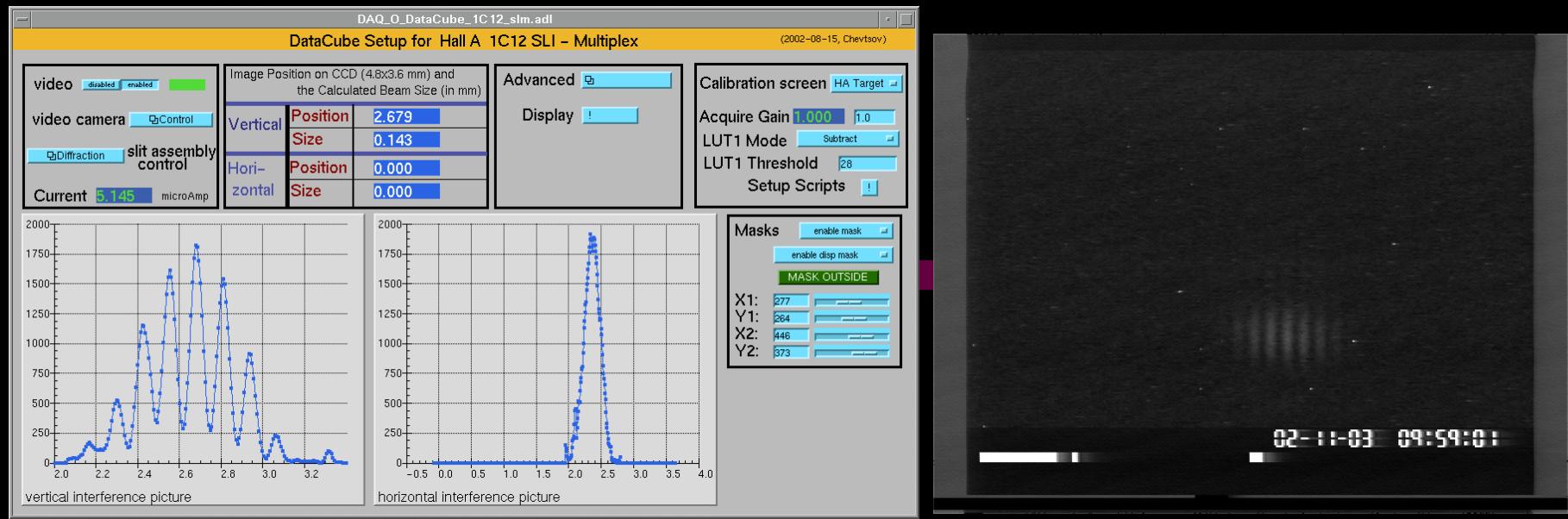
IHA1C12 Feb 11, 2003 10:23:07.1700 Scan Complete

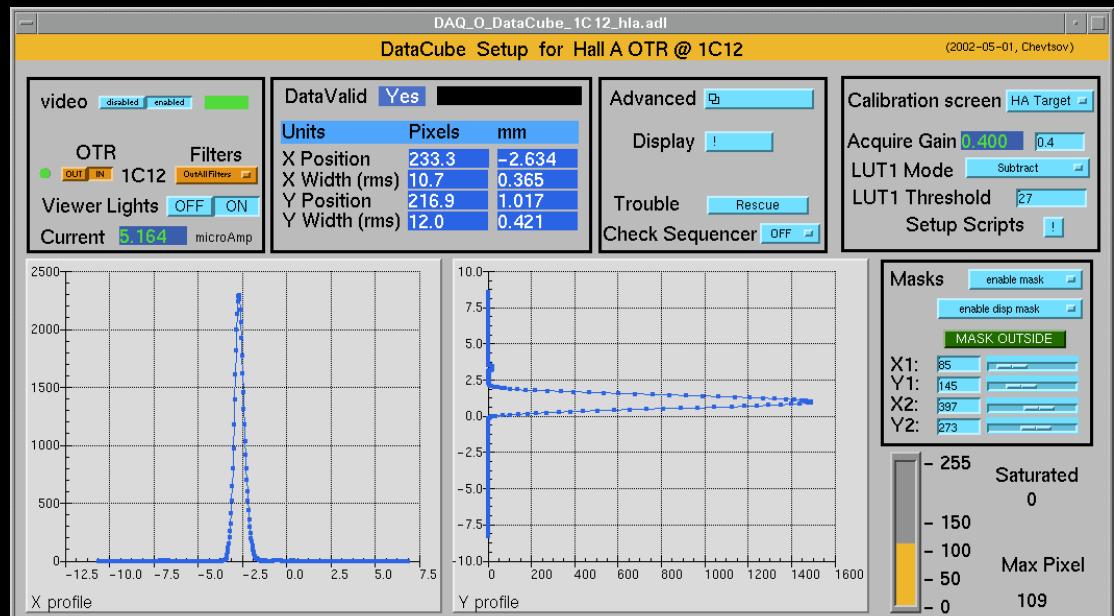
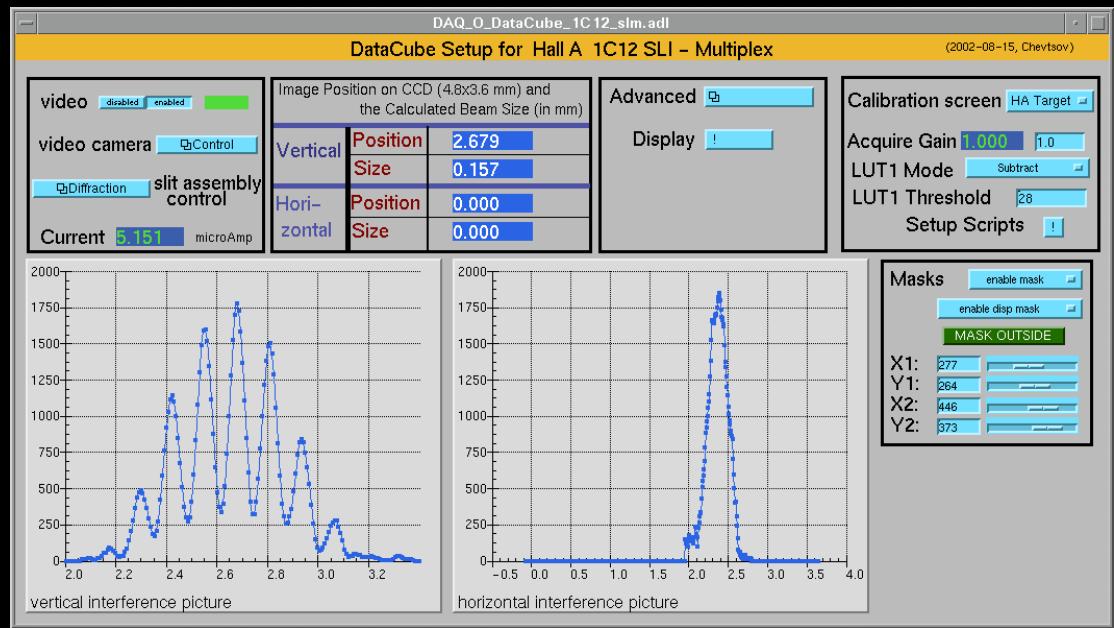


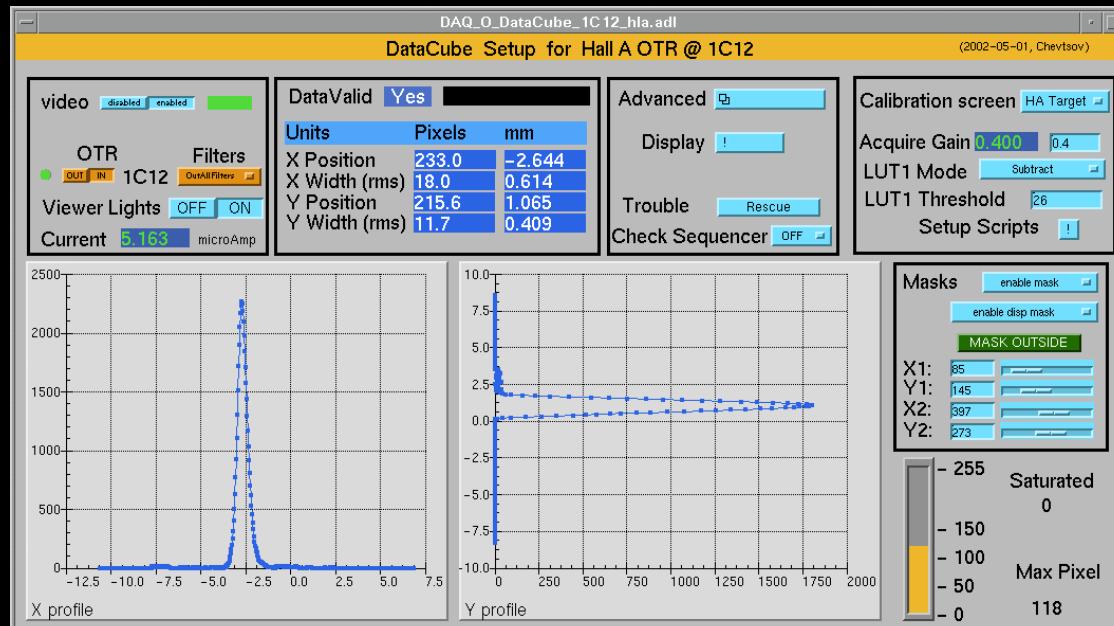
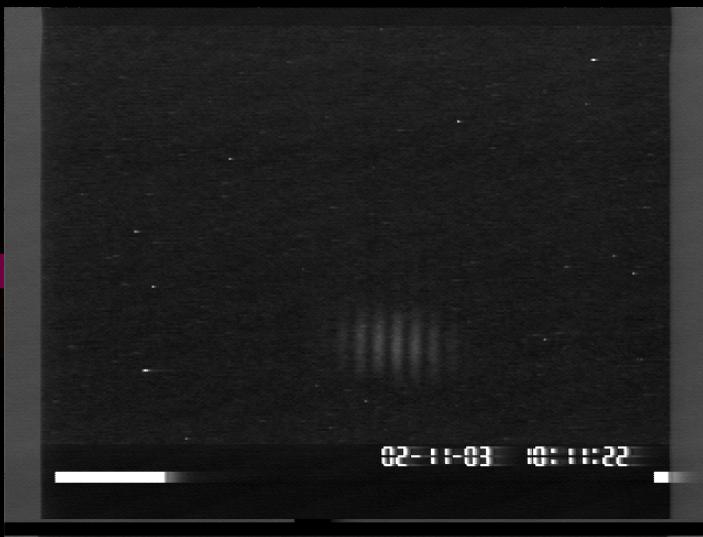
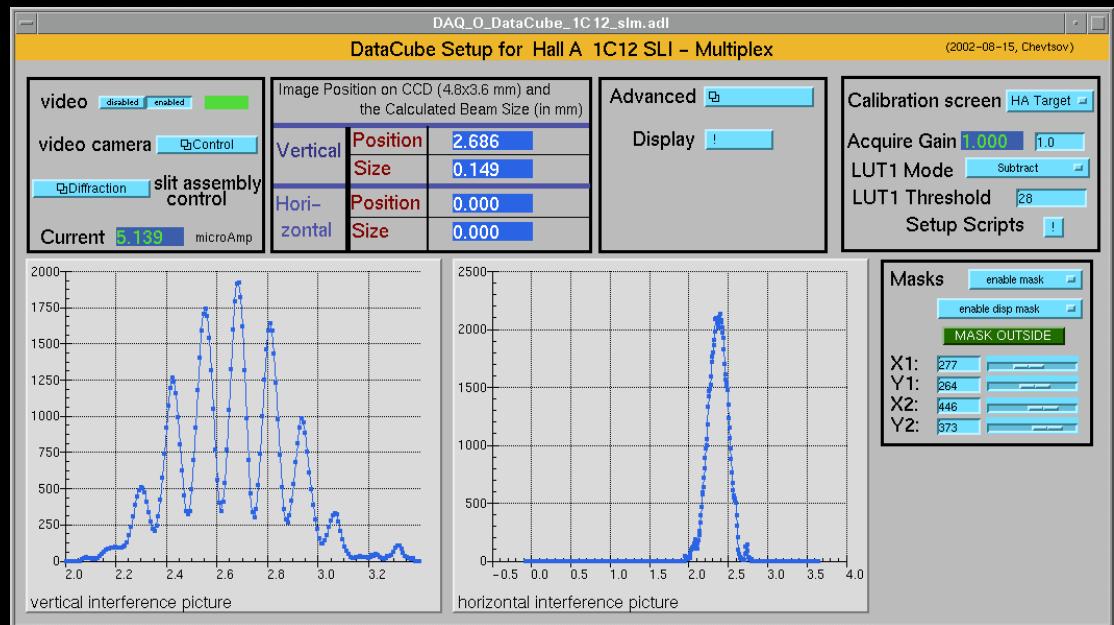
LPOff LP05 LP10 LP20 LP30

Version 3.0

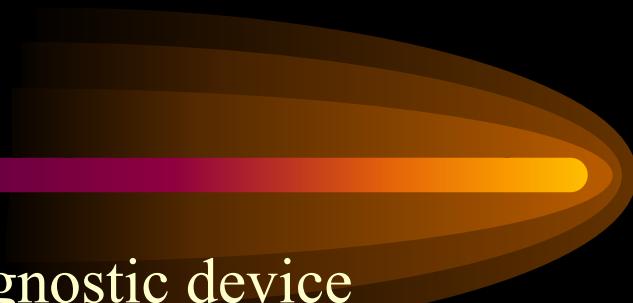
DSP Lpf .10 Xd->62.51 Yd->22.00 Loc@ 900







Summary



- Jefferson Lab has a modern beam diagnostic device based on non-invasive technology
- Jefferson Lab has a great experience in design and installation of such a device
- The resolution of this device can be made less than $10 \mu\text{m}$
- The device's operational current range:
a few microamps \rightarrow milliamps

SLI team:

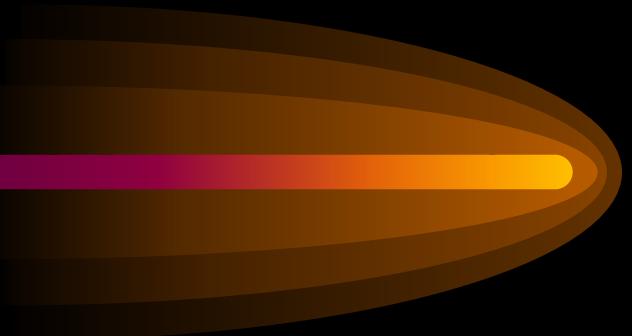
P. Chevtsov, J.-C. Denard, R. Hicks, K. Capek, D. Hardy,
D. Wetherholt, Z. Kursun

Special thanks to:

M. Tiefenback, G. Krafft, H. Areti, L. Merminga, J. Benesch,
A. Bogacz, A. Freyberger, Y. Derbenev, A. Hutton, K. White.

Many thanks to:

S. Suhring, M. Spata, O. Garza, all accelerator operators and
technicians.



E *N* *D*

Visibility as a function of the intensity imbalance (simulation)

