





















# • Structure Functions:

$$P_{LL}(q_{cm}) = -2\sqrt{6} M_N G_E(\tilde{Q}^2) P^{(01,01)0}(q_{cm})$$

$$P_{TT}(q_{cm}) = -3 G_M(\tilde{Q}^2) \frac{q_{cm}^2}{\tilde{q}_0} \times \left[ P^{(11,11)1}(q_{cm}) - \sqrt{2}\tilde{q}_0 P^{(01,12)1}(q_{cm}) \right]$$

$$P_{LT}(q_{cm}) = \sqrt{\frac{3}{2}} \frac{M_N q_{cm}}{\tilde{Q}} G_E(\tilde{Q}^2) P^{(11,11)0}(q_{cm}) + \frac{3}{2} \frac{\tilde{Q} q_{cm}}{\tilde{q}_0} P^{(01,01)1}(q_{cm})$$

# • in an unpolarized VCS experiment:

 $d\sigma(ep\gamma) = d\sigma(\text{BH+Born}) + (PhaseSpace) \times$ 

$$\left[ v_1 \left[ P_{LL}(q_{cm}) - \frac{1}{\epsilon} P_{TT}(q_{cm}) \right] + v_2 \left[ P_{LT}(q_{cm}) \right] + O(q'_{cm}) \right]$$

 $v_1, v_2 =$  known kinematic functions of  $q_{cm}, \epsilon, heta_{\gamma\gamma cm}, \phi_{\gamma\gamma}$  .

• At fixed  $q_{cm}$  and  $\epsilon$ , one measures two structure functions :  $P_{LL} - P_{TT}/\epsilon$  sensitive to electric GP  $\alpha(Q^2)$   $P_{LT}$  sensitive to magnetic GP  $\beta(Q^2) \rightarrow$  to be compared to Model predictions



B.Pasquini, M.Gorchtein, D.Drechsel, A.Metz, M.Vanderhaeghen (*Eur. Phys. J. A 11 (2001) 185*)

• Dispersion integrals:



- $\gamma^* N \rightarrow \pi N$  taken from MAID2000
- Asymptotic parts and contributions beyond  $\pi N$
- two free parameters:  $\Lambda_{\alpha}$ ,  $\Lambda_{\beta}$  related to polarizabilities  $\alpha$  and  $\beta$ :

$$\alpha(Q^2) - \alpha^{\pi N}(Q^2) = \frac{\alpha_0^{exp} - \alpha_0^{\pi N}}{(1 + Q^2/\Lambda_{\alpha}^2)^2} , \qquad \text{same relation for } \beta$$

• no  $q'_{cm}$  expansion; DR  $(\gamma^* p \to \gamma p)$  cross section includes all orders in  $q'_{cm}$ • limited to  $\sqrt{s} = W \le (M_N + 2m_\pi)$ , and not limited to small  $Q^2$ 









VCS at Low Energy : experiments					
where	$Q^2$ (GeV <sup>2</sup> )	$(\gamma^*p)$ c.m. energy $\sqrt{s}$	$p \operatorname{cone}_{\theta_{pq}}$	data taking	status (@ end 2001)
MAMI A1 Coll.	0.33	$< (M_N + M_\pi)$	<b>10</b> °	1995+97	published
JLab (A) E93-050	1.0, 1.9	< 1.9 <b>GeV</b>	<b>6°, 3</b> °	1998	final stage
Bates E97-03	0.05	$< (M_N + M_\pi)$	28° 00ps	2000	analysis
Bates <b>E97</b> -05	0.12	$\sim 1.232~{\rm GeV}$	14-20° OOPS	2001	analysis

- **Detection:** magnetic spectrometers ( $\gamma$  = missing particle)
- High Resolution: separate  $\gamma$  and  $\pi^0$  missing mass peaks
- accurate measurement of absolute cross sections  $d^5\sigma(ep \rightarrow ep\gamma)$

(good knowledge of acceptance) (effect of GPs is small)







BATES E97-03 VCS experiment



• Status: analysis in progress (data taking: year 2000) 2001 spectrometer optics studies (sieve-slit in OHIPS) Missing mass  $\gamma$  peak, proton spectrometers MC studies 2002 MC studies, normalization of data

### • Lab achievement:

1st use of high duty factor beam in South Hall Ring 1st use of full OOPS system

Set I	$Q^2 = 1.0 \text{ GeV}^2$	$\sqrt{s}$ mostly below pion threshold $\sqrt{s}$ mostly below pion threshold Resonances: $1.0 < \sqrt{s} < 2.0$ GeV	100000 events
Set II	$Q^2 = 1.9 \text{ GeV}^2$		46000 events
Set III	$Q^2 = 1.0 \text{ GeV}^2$		28000 events

• Key points of experimental analysis:

 $\star$  (I,II) vicinity of elastic peak  $\Rightarrow$  CUTS (punchthrough protons)

**\*** accurate **Monte-Carlo** for solid angle calculation

- reproduce experimental resolution
- include radiative corrections
- use realistic input cross section

• Advantages:

- $\star$  Lorentz boost  $\rightarrow$  large acceptance w.r.t. outgoing photon phasespace
- $\star$  several methods to extract structure functions  $P_{LL} P_{TT}/\epsilon$  and  $P_{LT}$

**Absolute normalisation** : under control at the  $\sim$  2 % level

- Elastic (*ep*) cross sections
- $(ep\gamma)$  cross sections at low  $q'_{cm}$ 
  - $\star$  almost no GP effect
  - \*  $\chi^2$  test between [*renorm.factor*] ×  $d\sigma_{exp}$  and  $d\sigma_{BH+Born}$  (+GPs)
  - $\star$  reduced  $\chi^2 \sim 1~~{\rm and}~~|renorm.factor-1.00| \leq 0.02$

## **Choice of proton EM Form Factors** (in $\sigma_{BH+Born}$ ) :

- $\star$   $G_M^p$  param.of Bosted (P.Bosted, Phys.Rev. C 51 (1995) 409)
- $\rightarrow \star$   $G_M^p$  param.of Brash et al. differs by 1.8 (2.4) % at  $Q^2 = 1(2)$  GeV<sup>2</sup> (E.Brash et al., hep-ex/0111038)
- $\rightarrow \star \ \mu G_E/G_M$  from JLab expt (O.Gayou et al., Phys.Rev.Lett.88:092301,2002)





JLab-E93050. fit of Generalized Polarizabilities by Method A



### JLab E93-050 VCS in the Resonance Region



• excitation scan in  $W = \sqrt{s}$  , from  $M_N$  to 1.9 GeV

- 1st measurement of 5-fold  $d\sigma(ep\gamma)$  in this channel
- see how resonances show up (missing res.?)

- fixed 
$$Q^2 = \mathbf{1} \; \mathbf{GeV}^2$$

- backward angle  $\theta_{\gamma\gamma cm}$  (keep Bethe-Heitler small)

### E93050 - Photon Electroproduction versus Phi and W

5-fold cross section:  $d^5\sigma(ep \rightarrow ep\gamma)/dk'_{lab}d\Omega_{elab}d\Omega_{\gamma\gamma cm}$ at  $Q^2 = 1 \text{ GeV}^2$ ,  $\theta_{\gamma\gamma cm} = 167.2^{\circ}$ 





#### Principle:

- make a chisquare between experimental cross sections and cross sections given by DR model
- adjust the free parameters by minimizing chisquare

at 
$$Q^2 = 1 \text{ GeV}^2$$

$$P_{LL} = +1.85 +/-0.24(stat) +0.30-0.49(syst) GeV^{-2}$$
  
 $P_{TT} = -0.418 GeV^{-2}$  (given by the model)

$$P_{\rm LL} - P_{\rm TT} / 0.95 = +2.29 +/- 0.24 (stat) GeV^{-2}$$

$$P_{LT} = -0.53 +/-0.12(stat) +0.16-0.03(syst) GeV^{-2}$$

# (JLab: Preliminary)

$$P_{LL}(q) - P_{TT}(q)/\epsilon$$

$Q^2$	$q_{cm}$	$\epsilon$	Structure function
$(GeV^2)$	(MeV/c)		(GeV <sup>-2</sup> )
0.33	600	0.62	LET: +23.7 $\pm$ 2.2 (stat) $\pm$ 4.3 (syst)
1.0	1080	0.95	<b>LET:</b> +2.31 $\pm$ 0.22(stat) $\pm$ 0.35(syst) $\pm$ •
	1133	0.95	DR : +2.29 $\pm$ 0.24(stat) $^{-0.49}_{+0.30}$ (syst)
1.9	1600	0.88	<b>LET:</b> +0.56 $\pm$ 0.07(stat) $\pm$ 0.11(syst) $\pm$ •
	1600	0.88	DR: [+0.43,+0.84]

 $P_{LT}(q)$ 

$Q^2$ (GeV <sup>2</sup> )	$q_{cm}$ (MeV/c)	$\epsilon$	Structure function (GeV <sup>-2</sup> )	
0.33	600	0.62	$LET: - 5.0 \qquad \pm 0.8  (stat) \ \pm 1.8  (syst)$	
1.0	1080	0.95	<b>LET:</b> $-0.42$ $\pm$ 0.11 (stat) $\pm$ 0.02(syst) $\pm$ •	
	1133	0.95	DR : $-$ 0.53 $\pm$ 0.12(stat) $^{-0.03}_{+0.16}$ (syst)	
1.9	1600	0.88	<b>LET:</b> +0.009 $\pm$ 0.041(stat) $\pm$ 0.005(syst) $\pm$ •	
	1600	0.88	<b>DR</b> : [-0.05,+0.02]	



### High W: comparison VCS/RCS



**Related topics**  neutron Generalized Polarizabilities ? neutron polarizabilities (at  $Q^2 = 0$ ) poorly known:  $\alpha_n = (1.20 \pm 0.15 \pm 0.20) \times 10^{-3} fm^3$ J. Schiedmayer et al., PRL 66 (1991) 1015 (discussed  $\rightarrow \leq 2.10^{-3} fm^3$ )  $\alpha_n = (0.8 \pm 1.0) \times 10^{-3} fm^3$ L.Koester et al., Z.Phys. A 329 (1988) 229  $\alpha_n = (0.0 \pm 0.5) \times 10^{-3} fm^3$ L.Koester et al., Phys.Rev. C 51 (1995) 3363  $\beta_n = ?$ isospin-averaged nucleon polarizabilities:  $\alpha - \beta \ = \ (2.6 \pm 1.8) \times 10^{-4} \ fm^3$ D.Hornidge et al., PRL 84 (2000) 2334

- nucleus GPs ?
- pion GPs, and all other hadrons ...



