# ELECTROMAGNETIC TESTS OF CHIRAL SYMMETRY



# Harald Merkel A1 COLLABORATION

- Introduction
  - Chiral Perturbation Theory
- Threshold  $\pi^0$  production off the Proton
  - Photo production (MAMI, SAL)
  - Electro production (NIKHEF, MAMI)
  - ► Low 4-momentum transfer  $Q^2 = 0.05 \, GeV^2/c^2$
  - Polarization structure functions
- Coherent  $\pi^0$  production off the Deuteron
  - Photo production (SAL)
  - Electro production (MAMI)
- Summary

### Symmetries of QCD

Starting point: QCD Lagrangian

$$\mathcal{L}_{QCD} = \sum_{f} \overline{q}_{f} (iD_{\mu}\gamma^{\mu} - m_{f})q_{f} - \frac{1}{4} \sum_{\alpha=1}^{8} G^{\alpha}_{\mu\nu} G^{\mu\nu,\alpha}$$

- Strong interaction (completely?) determined
- No analytic solution in confinement range  $E < 1 \,\mathrm{GeV}$
- Hadrons as  $q\bar{q}$  or qqq states
  - Quark masses 1% of proton mass
  - ► Hadron spectrum from  $SU(3)_{flavour}$
  - Resonance structure of nucleons

Access at  $E < 1 \,\text{GeV}$ : Symmetries

- Local Gauge Symmetry, C, P, T, etc.
- Chiral Symmetry  $\mathbb{SU}(3)_L \times \mathbb{SU}(3)_R$ 
  - ► Chiral limit  $m_u, m_d, m_s \rightarrow 0$ :

$$\mathcal{L}_{QCD}^{0} = \sum_{u,d,s} \left( \overline{q}_{R,f} i D_{\mu} \gamma^{\mu} q_{R,f} + \overline{q}_{L,f} i D_{\mu} \gamma^{\mu} q_{L,f} \right) - \frac{1}{4} \sum_{\alpha=1}^{8} G_{\mu\nu}^{\alpha} G^{\mu\nu,\alpha}$$

- $\blacktriangleright$  Not visible  $\Rightarrow$  spontaneous broken symmetry
- Goldstone theorem: 8 massless bosons
- Identified as 8 pseudo scalar mesons

### **Chiral Perturbation Theory**

Recipe for an "Effective Field Theory":

- Choose effective degrees of freedom: Nucleons, Pions
- Most general Lagrangian
- Symmetries of  $\mathcal{L}_{QCD}^{0}$
- Expansion in masses: Symmetry broken by  $-\overline{q}_f M q_f$
- Simultaneous expansion in p,  $q^2$
- "Power counting"

#### Problems:

- Degrees of freedom: Resonances?
- Limited range in p,  $q^2$
- Regularization ⇒ Low Energy Constants (LEC) Determined by experiment
- Convergence

#### Pion photo and electro production

$$\gamma^{(*)} + p \rightarrow \pi^0 + p$$

- Test of Chiral Perturbation Theory
  - Direct production of Goldstone Bosons
  - QED: photon coupling well known
  - ▶  $\pi^+$  production dominated by charge  $\Rightarrow \pi^0$
- Threshold production
  - Expansion in small momenta
  - Only s- and p wave multipoles contribute

$$\frac{d\sigma}{d\Omega} = \frac{q}{k} \left( A + B \cdot \cos \theta + C \cdot \cos^2 \theta \right)$$

$$A = E_{0+}^{2} + P_{23}^{2} \qquad P_{1} = 3E_{1+} + M_{1+} - M_{1-}$$
  

$$B = 2 \cdot Re(E_{0+}P_{1}^{*}) \qquad P_{2} = 3E_{1+} - M_{1+} + M_{1-}$$
  

$$C = P_{1}^{2} - P_{23}^{2} \qquad P_{3} = 2M_{1+} + M_{1-}$$
  

$$P_{23} = \frac{1}{2}(P_{2}^{2} + P_{3}^{2})$$

► Known energy dependence  $P_i(q) \sim q \cdot k$ 

- Theory
  - $\blacktriangleright E_{0+}$  slow convergence
  - $P_1, P_2$  "new Low Energy Theorems"
  - $\blacktriangleright \frac{P_3}{P_3}$  fit to data

#### **Unitary Cusp**

- Pion pole dominance  $\Rightarrow$  strong  $\gamma + p \rightarrow n + \pi^+$
- Charge exchange amplitude







ChPT: Chiral Perturbation theory: V. Bernard *et al.*, Nucl. Phys. **B 383** (1992) 442 DR: Dispersion Relations: O. Hanstein *et al.*, Phys. Lett. **B 399** (1997) 13



# **Tagged Photon Facility**



- Energy range: 5%–94% of electron energy
- Energy resolution:  $\Delta E_{\gamma} = 2 \text{ MeV}$  at  $E_0 = 855 \text{ MeV}$
- Timing resolution: 1 ns
- Maximum count rate: 10<sup>8</sup> photons/s
- Luminosity (Target: 10cm  $H_2$ )  $L > 40 \frac{\text{Hz}}{\mu \text{barn}}$

# TAPS at MAMI



## **Differential Cross Section**





# Fit of A,B,C to Differential Cross Section



# Photo production



$$\sigma(\theta) = \frac{q}{k} \left( \mathbf{A} + \mathbf{B} \cdot \cos \theta + \mathbf{C} \cdot \cos^2 \theta \right)$$
(1)

A	=	$E_{0+}^2 + \frac{1}{2}(P_2^2 + P_3^2)$	$P_1 = 3E_{1+} + M_{1+} - M_{1-}$
B	=	$2 \cdot Re(\tilde{E}_{0+}P_1^*)$	$P_2 = 3E_{1+} - M_{1+} + M_{1-}$ $P_3 = 2M_{1+} + M_{1-}$
С	=	$P_1^2 - \frac{1}{2}(P_2^2 + P_3^2)$	

$$\sigma(\theta) \Rightarrow ReE_{0+}, P_1, (P_2^2 + P_3^2)/2$$

$$\sigma(\theta, \phi) = \sigma(\theta) \left[ 1 - P_{\gamma} \cdot \Sigma(\theta) \cdot \cos 2\phi \right]$$
(2)  
$$\Sigma(\theta) \sim \frac{1}{2} (P_3^2 - P_2^2)$$
  
$$\Sigma \Rightarrow (P_3^2 - P_2^2)/2$$

	$E_{0+}$	$P_1$	$P_2$	$P_3$
	$[10^{-3/m_{\pi}}]$	$[q\cdot k\cdot 10^{-3}/m_{\pi}^3]$	$[q \cdot k \cdot 10^{-3}/m_{\pi}^3]$	$[q \cdot k \cdot 10^{-3}/m_{\pi}^3]$
MAMI	-1.31±0.08	10.02±0.2	-10.5±0.2	13.1±0.1
SAL	-1.32±0.05	10.26±0.1		
ChPT	-1.16	10.33±0.6	-11.0±0.6	11.7±0.6
DR	-1.22	10.54	-11.4	10.2

## **Polarized Photon Asymmetry**

A. Schmidt et al., Phys. Rev. Lett. 87, 232501 (2001)



 $\sigma(\theta,\phi) = \sigma(\theta) \left( 1 - P_{\gamma} \cdot \Sigma(\theta) \cdot \cos 2\phi \right)$ 

## **Pion Electro Production**



$$\frac{d^{5}\sigma}{d\Omega_{e}dE'd\Omega_{\pi}^{*}} = \Gamma_{t}(\sigma_{T}(\theta) + \varepsilon \cdot \sigma_{L}(\theta) + \varepsilon \cdot \sigma_{T}(\theta) \cdot \cos 2\phi + \sqrt{2\varepsilon(1+\varepsilon)} \cdot \sigma_{TL}(\theta) \cdot \cos\phi + h \cdot \sqrt{2\varepsilon(1-\varepsilon)} \cdot \sigma_{TL'}(\theta) \cdot \sin\phi)$$

- $\bullet$  Additional longitudinal s and p waves
- Interference structure functions
- Multipoles depend on four-momentum transfer  $Q^2$

Experiment:  $H(\vec{e}, e'p)\pi^0$ 

- Detection of recoil proton
- Lorenz boost  $\Rightarrow 4\pi$  in spectrometer acceptance
- Small cross section  $\Rightarrow$  high luminosity

# **Kinematics**



$\sigma_T(\theta) = \frac{p^*}{k^*} (A + B \cdot \cos \theta + C \cdot \cos^2 \theta)$ $\sigma_L(\theta) = \frac{p^*}{k^*} (A' + B' \cdot \cos \theta + C' \cdot \cos^2 \theta)$	$\sigma_{TL}(\theta) = \frac{p^*}{k^*} (D \cdot \sin \theta + E \cdot \sin \theta \cos \theta)$ $\sigma_{TT}(\theta) = \frac{p^*}{k^*} F \cdot \sin^2 \theta$ $\sigma_{TL'}(\theta) = \frac{p^*}{k^*} (G \cdot \sin \theta + H \cdot \sin \theta \cos \theta)$
$A =  E_{0+} ^2 + \frac{1}{2}( P_2 ^2 +  P_3 ^2)$ $B = 2 \cdot ReE_{0+}^* \cdot P_1$ $C =  P_1 ^2 - \frac{1}{2}( P_2 ^2 +  P_3 ^2)$	$A' =  L_{0+} ^2 +  P_5 ^2$ $B' = 2 \cdot ReL_{0+}^* \cdot P_4$ $C' =  P_4 ^2 -  P_5 ^2$
$D = -Re(E_{0+} \cdot P_5^* + L_{0+} \cdot P_2^*)$ $E = -Re(P_1 \cdot P_5^* + P_4 \cdot P_2^*)$ $F = \frac{1}{2}( P_2 ^2 -  P_3 ^2)$	$G = -Im(E_{0+} \cdot P_5^* + L_{0+} \cdot P_2^*)$ $H = Im(P_1 \cdot P_5^* + P_4 \cdot P_2^*)$

$P_1$	=	$3E_{1+} + M_{1+} - M_{1-}$	<b>P</b> <sub>4</sub>	=	$4L_{1+}+L_{1-}$
<b>P</b> <sub>2</sub>	=	$3E_{1+} - M_{1+} + M_{1-}$	$P_5$	=	$L_{1-} - 2L_{1+}$
$P_3$	=	$2M_{1+} + M_{1-}$			

# A1: 3-Spectrometer Setup



Spectrometer A:  $\alpha > 20^{\circ}$  p < 735 MeV/c  $\Delta \Omega = 28 \text{ msr}$  $\Delta p/p = 20\%$ 

Spectrometer B:  $\alpha > 8^{\circ}$   $p < 870 \,\text{MeV/c}$   $\Delta \Omega = 5.6 \,\text{msr}$  $\Delta p/p = 15\%$  Spectrometer C:  $\alpha > 55^{\circ}$  p < 655 MeV/c  $\Delta \Omega = 28 \text{ msr}$  $\Delta p/p = 25\%$ 

# A1: Spectrometer A



Momentum resolution:
Momentum acceptance:
Angular acceptance:

 $\delta p/p < 10^{-4}$   $\Delta p/p = 20\%$  $\Delta \Omega = 11.5^{\circ} \times 8.0^{\circ} = 28 \,\mathrm{msr}$  NIKHEF  $H(e, e'p)\pi^0$ 

 $Q^2 = 0.1 \,\mathrm{GeV^2/c^2}$ 



# MAMI $H(e, e'p)\overline{\pi^0}$

 $Q^2 = 0.1 \,\mathrm{GeV^2/c^2}$ 

#### $q^2 = -0.10 \text{ GeV}^2/c^2$ $\epsilon = 0.529$



M.O. Distler et al., Phys. Rev. Lett. 80 (1998) 2294.

Results  $H(e, e'p)\pi^0$  at  $Q^2 = 0.1 \,\text{GeV}^2/\text{c}^2$ 





- MAMI: M.O. Distler *et al.*, Phys. Rev. Lett. **80** (1998) 2294.
- ChPT: V. Bernard *et al.*, Nucl. Phys. A 607 (1996) 379.

 $Q^2 = 0.05 \,\mathrm{GeV^2/c^2}$ 



- H. Merkel *et al.*, Phys. Rev. Lett. **88**, 012301 (2002)
- Fit with s-waves = const., p-waves  $\sim p_{\pi}^{cms}$
- ChPT, V. Bernard et al., Nucl. Phys. A 607 (1996) 379-401
- MAID, D. Drechsel *et al.*, Nucl. Phys. A 645 (1999) 145-174
   and S. S. Kamalov *et al.*, Phys. Lett. B 522 (2001) 27-36

 $Q^2 = 0.05 \,\mathrm{GeV^2/c^2}$ 



- H. Merkel *et al.*, Phys. Rev. Lett. **88**, 012301 (2002)
- Fit with s-waves const., p-waves  $\sim p_{\pi}^{cms}$
- ChPT, V. Bernard et al., Nucl. Phys. A 607 (1996) 379-401
- MAID, D. Drechsel *et al.*, Nucl. Phys. A645 (1999) 145-174
   and S. S. Kamalov *et al.*, Phys. Lett. **B 522** (2001) 27-36

 $\gamma^* + p \rightarrow p + \pi^0$  Total Cross Section vs.  $Q^2$ 



- ChPT, V. Bernard et al., Nucl. Phys. A607 (1996) 379-401.

MAID, D. Drechsel *et al.*, Nucl. Phys. A645 (1999) 145-174.
 and S. S. Kamalov *et al.*, Phys. Lett. B 522 (2001) 27-36

•  $Q^2 = 0$  A. Schmidt *et al.*, Phys. Rev. Lett. **87**, 232501 (2001).  $Q^2 = 0.05 \,\text{GeV}^2/\text{c}^2$  H. Merkel *et al.*, Phys. Rev. Lett. **88**, 012301 (2002).  $Q^2 = 0.1 \,\text{GeV}^2/\text{c}^2$  M. O. Distler *et al.*, Phys. Rev. Lett. **80** 2294 (1998).

# Multipole amplitudes at threshold

Photon point $Q^2 = 0 \mathrm{GeV^2/c^2}$								
	$E_{0+}$	$L_{0+}$	$\hat{P_{23}}^{2}$	$\hat{P}_1$	$\hat{P}_4$	$\hat{P}_5$		
	(10	$^{-3}m_{\pi}^{-1})$	$(10^{-6}m_{\pi}^{-4})$		$(10^{-3}m_{\pi}^{-2})$			
MAMI	-1.33		111	9.5				
ChPT	-1.14	-1.70	105	9.3	-0.6	-0.2		
MAID	-1.16	-1.29	95	9.3	-3.0	2.2		

 $Q^2 = 0.05 \,\mathrm{GeV^2/c^2}$ 

		Z	0.00000	. / .		
MAMI	0.57	-1.29	100	12.0	0.29 –	1.9
	$\pm 0.11$	$\pm 0.02$	$\pm 3$	$\pm 0.3$	$\pm 0.33$ $\pm$	0.3
AmPS		(-)1.57				
		±0.96				
ChPT	0.27	-1.55	353	16.5	-0.72 -	0.2
MAID	0.76	-1.4	250	15.0	-1.75	1.9

 $Q^2 = 0.1 \,\mathrm{GeV^2/c^2}$ 

MAMI	0.58	-1.38	573	15.1	-2.3	0.1
	$\pm 0.18$	$\pm 0.01$	$\pm 11$	$\pm 0.8$	$\pm 0.2$	$\pm 0.3$
AmPS	1.99	-1.33	526	16.4	-1.0	-1.0
	$\pm 0.3$	fixed	$\pm 7$	$\pm 0.6$	$\pm 0.4$	$\pm 0.4$
ChPT	1.42	-1.33	571	20.1	-0.6	-0.1
MAID	2.2	-1.12	315	17.1	-1.1	1.4

**Interference Structure-Functions** 

$$\frac{d^{5}\sigma}{d\Omega_{e}dE'd\Omega_{\pi}^{*}} = \Gamma_{t}(\sigma_{T}(\theta) + \varepsilon \cdot \sigma_{L}(\theta) + \varepsilon \cdot \sigma_{T}(\theta) \cdot \cos 2\phi + \sqrt{2\varepsilon(1+\varepsilon)} \cdot \sigma_{TL}(\theta) \cdot \cos\phi + h \cdot \sqrt{2\varepsilon(1-\varepsilon)} \cdot \sigma_{TL'}(\theta) \cdot \sin\phi)$$

Motivation:

- $\sigma_{TT}$  Separation of transverse *p* waves
- $\sigma_{TL}$  Separation of longitudinal p waves
- $\sigma_{TL'}$  Unitary cusp at  $\pi^+$  threshold

 $\Rightarrow$  *ImL*<sub>0+</sub>

**Experiment:** 

- Polarized beam h = 75%
- Out of Plane  $\phi_{LAB} = 8^\circ \Rightarrow \phi_{CMS} = 90^\circ$

Extended kinematical range

$$0 MeV/c < p_{\pi}^{*} < 100 MeV/c \ \phi_{CMS} = 0^{\circ}, \ 90^{\circ}, \ -90^{\circ}$$

 $\Rightarrow$  14 kinematical setups





# Interference Asymmetries

$$\frac{d^{5}\sigma}{d\Omega_{e}dE'd\Omega_{\pi}^{*}} = \Gamma_{t}(\sigma_{T}(\theta) + \varepsilon \cdot \sigma_{L}(\theta) + \sqrt{2\varepsilon(1+\varepsilon)} \cdot \sigma_{TL}(\theta) \cdot \cos\phi + \varepsilon \cdot \sigma_{TT}(\theta) \cdot \cos 2\phi + h \cdot \sqrt{2\varepsilon(1-\varepsilon)} \cdot \sigma_{TL'}(\theta) \cdot \sin\phi)$$

$$A_{TL} = \frac{\sqrt{2\epsilon(1+\epsilon)} \cdot \sigma_{TL}(\theta)}{\sigma_{T}(\theta) + \epsilon \cdot \sigma_{L}(\theta)}$$

$$= \frac{\sigma(\phi = 0) - \sigma(\phi = \pi)}{\sigma(\phi = 0) + \sigma(\phi = \pi)}$$

$$A_{TT} = \frac{\epsilon \cdot \sigma_{TT}(\theta)}{\sigma_{T}(\theta) + \epsilon \cdot \sigma_{L}(\theta)}$$

$$= \frac{\sigma(0) + \sigma(\pi) - 2\sigma(\pi/2)}{\sigma(0) + \sigma(\pi) + 2\sigma(\pi/2)}$$

$$A_{TL'} = \frac{\sqrt{2\epsilon(1-\epsilon)} \cdot \sigma_{TL'}(\theta)}{\sigma_{T}(\theta) + \epsilon \cdot \sigma_{L}(\theta)}$$

$$= \frac{\sigma(h = 1) - \sigma(h = -1)}{\sigma(h = 1) + \sigma(h = -1)}$$

$$A_{TL'} = \frac{\sqrt{2\epsilon(1-\epsilon)} \cdot \sigma_{TL'}(\theta)}{\sigma_{T}(\theta) + \epsilon \cdot \sigma_{L}(\theta)}$$

$$A_{TL'} = \frac{\sqrt{2\epsilon(1-\epsilon)} \cdot \sigma_{TL'}(\theta)}{\sigma_{T}(\theta) + \epsilon \cdot \sigma_{L}(\theta)}$$

$$A_{TL'} = \frac{\sqrt{2\epsilon(1-\epsilon)} \cdot \sigma_{TL'}(\theta)}{\sigma_{T}(\theta) + \epsilon \cdot \sigma_{L}(\theta)}$$

$$A_{TL'} = \frac{\sqrt{2\epsilon(1-\epsilon)} \cdot \sigma_{TL'}(\theta)}{\sigma_{T}(\theta) + \epsilon \cdot \sigma_{L}(\theta)}$$

$$A_{TL'} = \frac{\sqrt{2\epsilon(1-\epsilon)} \cdot \sigma_{TL'}(\theta)}{\sigma_{T}(\theta) + \epsilon \cdot \sigma_{L}(\theta)}$$

$$A_{TL'} = \frac{\sqrt{2\epsilon(1-\epsilon)} \cdot \sigma_{TL'}(\theta)}{\sigma_{T}(\theta) + \epsilon \cdot \sigma_{L}(\theta)}$$

$$A_{TL'} = \frac{\sqrt{2\epsilon(1-\epsilon)} \cdot \sigma_{TL'}(\theta)}{\sigma_{T}(\theta) + \epsilon \cdot \sigma_{L}(\theta)}$$

$$A_{TL'} = \frac{\sqrt{2\epsilon(1-\epsilon)} \cdot \sigma_{TL'}(\theta)}{\sigma_{T}(\theta) + \epsilon \cdot \sigma_{L}(\theta)}$$

$$A_{TL'} = \frac{\sqrt{2\epsilon(1-\epsilon)} \cdot \sigma_{TL'}(\theta)}{\sigma_{T}(\theta) + \epsilon \cdot \sigma_{L}(\theta)}$$

$$A_{TL'} = \frac{\sqrt{2\epsilon(1-\epsilon)} \cdot \sigma_{TL'}(\theta)}{\sigma_{T}(\theta) + \epsilon \cdot \sigma_{L}(\theta)}$$

$$A_{TL'} = \frac{\sqrt{2\epsilon(1-\epsilon)} \cdot \sigma_{TL'}(\theta)}{\sigma_{T}(\theta) + \epsilon \cdot \sigma_{L}(\theta)}$$

$$A_{TL'} = \frac{\sqrt{2\epsilon(1-\epsilon)} \cdot \sigma_{TL'}(\theta)}{\sigma_{T}(\theta) + \epsilon \cdot \sigma_{L}(\theta)}$$

$$A_{TL'} = \frac{\sqrt{2\epsilon(1-\epsilon)} \cdot \sigma_{TL'}(\theta)}{\sigma_{T}(\theta) + \epsilon \cdot \sigma_{L}(\theta)}}$$

$$A_{TL'} = \frac{\sqrt{2\epsilon(1-\epsilon)} \cdot \sigma_{TL'}(\theta)}{\sigma_{T}(\theta) + \epsilon \cdot \sigma_{L}(\theta)}}$$

$$A_{TL'} = \frac{\sqrt{2\epsilon(1-\epsilon)} \cdot \sigma_{TL'}(\theta)}{\sigma_{T}(\theta) + \epsilon \cdot \sigma_{L}(\theta)}}$$

$$A_{TL'} = \frac{\sqrt{2\epsilon(1-\epsilon)} \cdot \sigma_{TL'}(\theta)}{\sigma_{T}(\theta) + \epsilon \cdot \sigma_{L}(\theta)}}$$

$$A_{TL'} = \frac{\sqrt{2\epsilon(1-\epsilon)} \cdot \sigma_{TL'}(\theta)}{\sigma_{T}(\theta) + \epsilon \cdot \sigma_{L}(\theta)}}$$

$$A_{TL'} = \frac{\sqrt{2\epsilon(1-\epsilon)} \cdot \sigma_{TL'}(\theta)}{\sigma_{T}(\theta) + \epsilon \cdot \sigma_{L}(\theta)}}$$

# Asymmetrie $A_{TL'}$

#### $q^2 = -0.05 \text{ GeV}^2/c^2$ $\epsilon = 0.933$

![](_page_27_Figure_2.jpeg)

•  $A_{TL'}$  consistent with Chiral Perturbation Theory

### **Neutron Amplitude**

- Pion production off the proton
  - Low Energy Constants fixed by experiment
- Pion production off the neutron
  - No further Low Energy Constants
  - Strong prediction of ChPT
  - Additional isospin breaking effects
- Access: Deuteron as neutron target

![](_page_28_Figure_8.jpeg)

**Fermi** momentum  $\approx$  reaction momentum

Coherent production

![](_page_28_Figure_11.jpeg)

Deuteron structure has to be unfolded
 Measure <u>E<sub>d</sub></u>, try to extract <u>E<sub>0+</sub><sup>nπ<sup>0</sup></sup></u>

#### **Coherent Photo Production: SAL**

- Detection of  $\pi^o \rightarrow \gamma \gamma$  with IGLOO Detektor
- Deuteron breakup calculated
- Extrapolation of s wave cross section  $\rightarrow$  threshold
- $E_d$  20% less than Chiral Perturbation Theory

![](_page_29_Figure_5.jpeg)

SAL J. C. Bergstrom *et al.*, Phys. Rev. C57,6 (1998) 3203
 ChPT S. R. Beane *et al.*, Nucl, Phys. A618 (1997) 381

### Differential Cross Section ( $\epsilon = 0.59$ )

![](_page_30_Figure_1.jpeg)

- I. Ewald et al., Phys. Lett. B 499 (2001) 238-244
  - Three values of photon polarization  $\epsilon$  $\Rightarrow$  transverse-longitudinal separation
  - Full coverage in azimuthal angle  $\phi$

### **L-T Separation**

![](_page_31_Figure_1.jpeg)

 $\sigma(W,q^2) = \sigma_T(W,q^2) + \varepsilon_L \sigma_L(W,q^2)$ 

![](_page_31_Figure_3.jpeg)

# Separation of s and p waves

 $\bullet$  only *s* and *p* waves at threshold

• p waves  $\sim$  pion CMS momentum  $p_{\pi}^{*}$ 

$$\frac{d\sigma}{d\Omega} = \frac{p_{\pi}^*}{k_{\gamma}^*} \left\{ A + Bp_{\pi}^{*2} + Cp_{\pi}^* \cos\theta + Dp_{\pi}^{*2} \cos^2\theta + \varepsilon_L \cdot (E + Fp_{\pi}^{*2} + Gp_{\pi}^* \cos\theta + Hp_{\pi}^{*2} \cos^2\theta) \right\}$$

![](_page_32_Figure_4.jpeg)

# Comparison with ChPT

V. Bernard, H. Krebs, U.-G. Meißner, Phys. Rev. C 61 (2000) 58201

![](_page_33_Figure_2.jpeg)

- $|E_d|$  to small, consistent with photo production
- $|L_d|$  clear disagreement
- threshold cross section

$$a_0 = |E_d|^2 + \varepsilon_L |L_d|^2$$

 $\Rightarrow$  1/10 of prediction

### **Explanation for Discrepancy**

M. Rekalo and E. Tomasi-Gustafsson, nucl-th/0112063

![](_page_34_Figure_2.jpeg)

• Final  $d\pi^0$  state:

 $J^{P} = 1^{-} \Rightarrow |pn\rangle = \frac{1}{\sqrt{2}}(|p\uparrow n\downarrow\rangle + |p\downarrow n\uparrow\rangle)$ 

• Intermediate state for  $l_{nn} = l_{\pi} = 0$ : Pauli principle:

 $|nn\rangle = \frac{1}{\sqrt{2}}(|n\uparrow n\downarrow\rangle - |n\downarrow n\uparrow\rangle) \Rightarrow J^P = 0^-$ 

• Coherent sum  $\Rightarrow$  exact cancellation  $\Rightarrow$  No rescattering AND no *s*-wave cusp!

#### Summary

- Existing data
  - $\blacktriangleright$  Photo production  $\checkmark$
  - ► NIKHEF  $Q^2 = 0.05 \,\mathrm{GeV^2/c^2}$
  - ► NIKHEF  $Q^2 = 0.1 \text{ GeV}^2/c^2$  (√)
  - ► MAMI  $Q^2 = 0.1 \text{ GeV}^2/c^2$  (√)

New data set

- ► MAMI  $Q^2 = 0.05 \, {\rm GeV^2/c^2}$
- Fifth structure function
- $\triangleright \sigma_{TT}$  interference  $\Rightarrow$  Separation of p waves
- Data sets inconsistent?
  - No discrepancy between data sets!
  - Strong  $Q^2$  dependence unlikely?
  - ► JLab proposal E-01-014
  - ► MAMI experiment:  $\Rightarrow Q^2$  dependence
- Coherent production from the deuteron
  - ► Photo production √?????
  - Elektro production 1/10 of prediction
  - ► Pauli ⇒ no rescattering
  - Neutron amplitude in impulse approximation