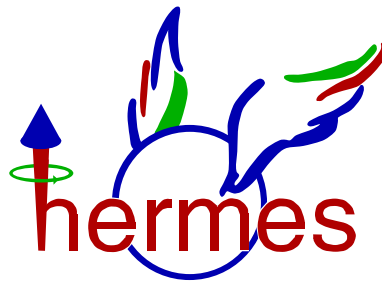
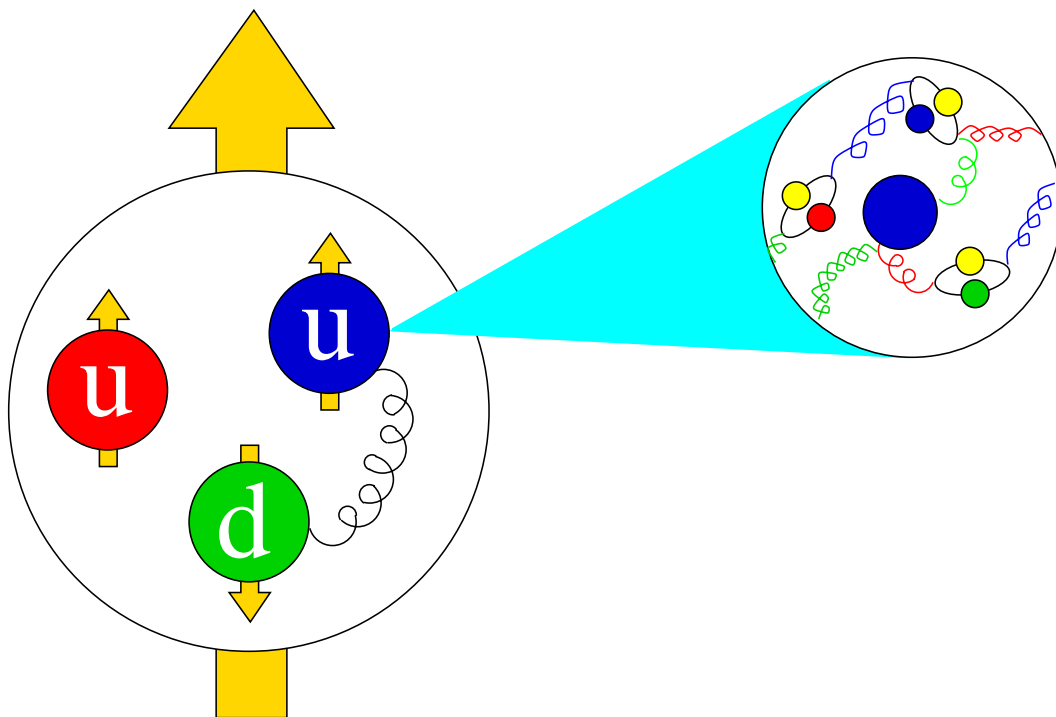


Polarized Structure Functions

Gerard van der Steenhoven (NIKHEF)



JLab, Newport News, 4 March 2002



9th Int. Conference on the Structure of Baryons



Introduction



- The origin of spin in the baryon octet:

$$\frac{1}{2} = \frac{1}{2}\Delta\Sigma_q + \Delta G + L_z$$

- Developing insight:

- EMC (SLAC, SMC and HERMES): $\Delta\Sigma_q \approx 0.3 \pm 0.1$
- The quark model: $\Delta\Sigma_q = (\uparrow\downarrow\uparrow) = 1.0$
- Relativistic MIT bag model: $\Delta\Sigma_q \simeq 0.60 - 0.75$

- Experimental questions:

- What about flavour dependence?

$$\Delta u(x), \Delta d(x), \Delta s(x)$$

- What about gluons?

$$\Delta G(x)$$

- What about orbital angular momentum?

Deeply Virtual Compton Scattering: L_z ?

- What about other baryons?

$$n, \Lambda^0, \dots$$

- What about lattice QCD?

longitudinal spin: $\Delta\Sigma_q \simeq 0.18 \pm 0.10$

transverse spin: $\delta\Sigma_q \simeq 0.56 \pm 0.09$

- Introduction

- Longitudinal spin:

- Inclusive experiments: $g_1^{n,p}(x), g_2^{n,p}(x)$
- Semi-inclusive experiments: $\Delta q_f(x)$
- Photo-production of high p_T -pairs: $\Delta G(x)$
- Deeply-virtual Compton scattering: $L_z(x)$
- Hyperon production: Λ -spin

- Transverse spin:

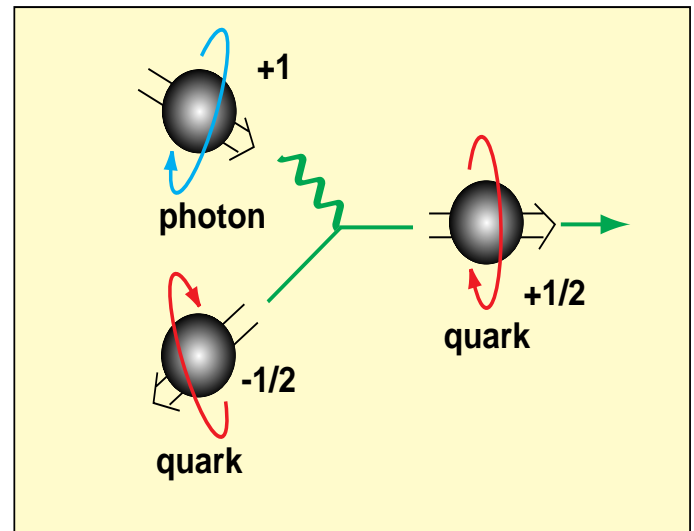
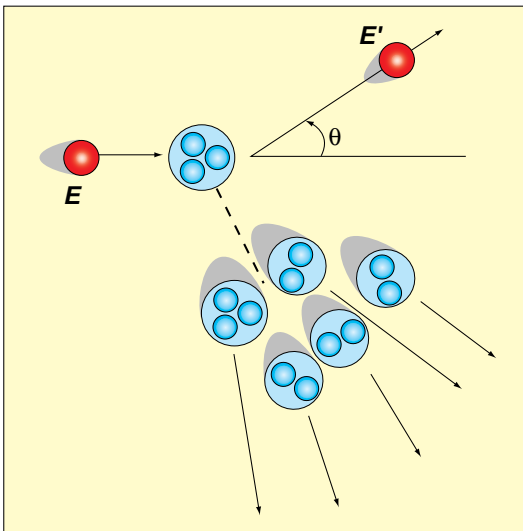
- Single-spin asymmetries in π -production: $h_1(x)$

$$h_1 = \begin{array}{c} \uparrow \\ \circ \\ \uparrow \\ \bullet \end{array} - \begin{array}{c} \uparrow \\ \circ \\ \bullet \\ \downarrow \end{array}$$

- Future perspectives:

- HERMES Run-II
- COMPASS
- RHIC-spin
- SLAC
- TESLA-N, EIC, ...

- Polarized Deep Inelastic Lepton Scattering:



- Asymmetry w.r.t. to target spin orientation:

$$A_1 = \frac{1}{DP_T P_B} \frac{N_{\uparrow\downarrow} - N_{\uparrow\uparrow}}{N_{\uparrow\downarrow} + N_{\uparrow\uparrow}}$$

- The spin-dependent structure function $g_1(x)$:

$$A_1 \simeq \frac{g_1(x)}{F_1(x)} \simeq \frac{1}{F_1(x)} \sum_f e_f^2 \Delta q_f(x)$$

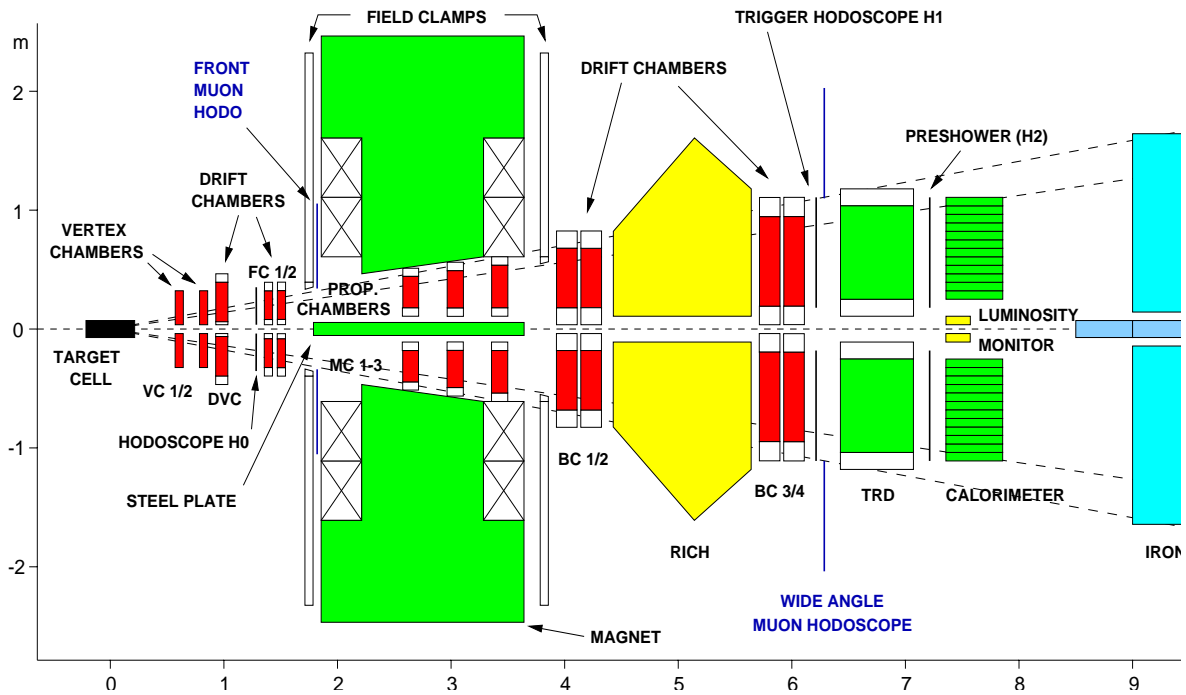
with the quark polarization:

$$\Delta q_f(x) = q_f^+(x) - q_f^-(x)$$

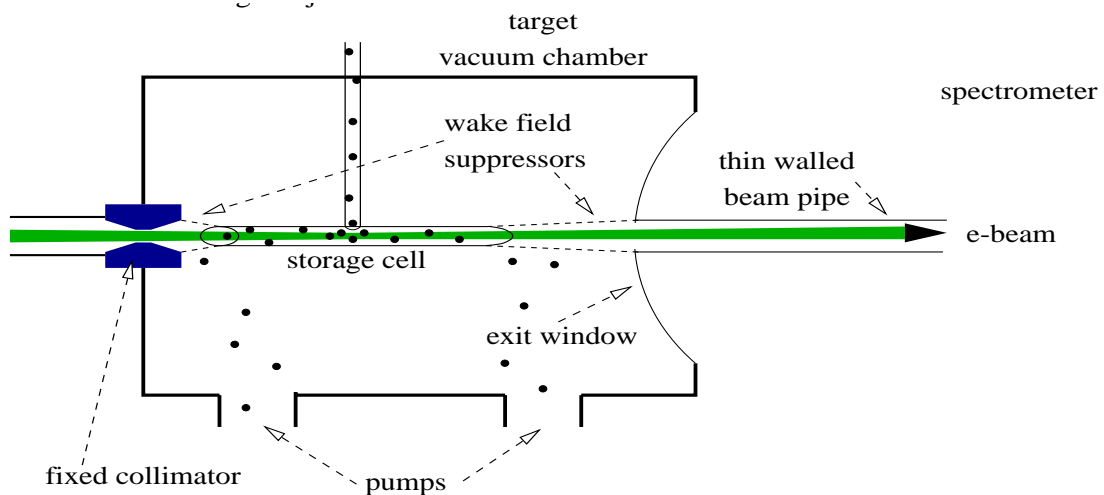
- General objective:

Spin structure of the nucleon

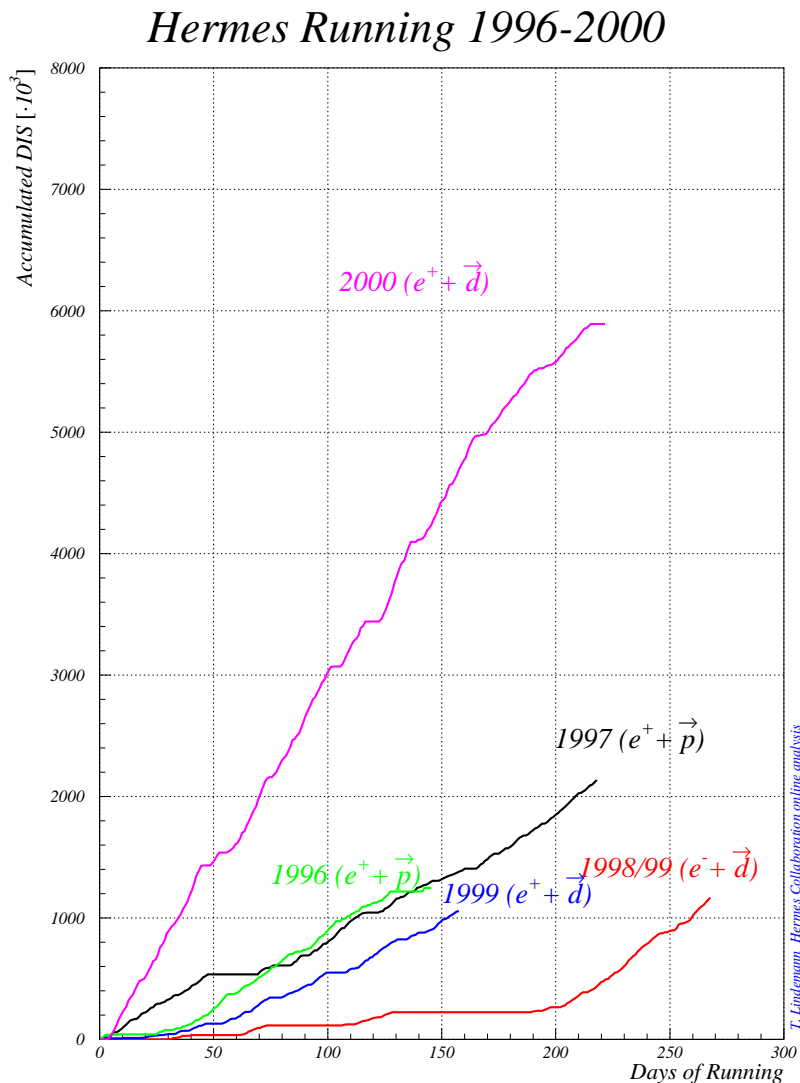
- The HERMES spectrometer at DESY:



- Internal Target ($^1\vec{H}$, $^2\vec{H}$, $^3\vec{He}$, ^4He , ^{14}N , ^{20}Ne , ^{84}Kr) :



- Accumulated polarized DIS events per year:

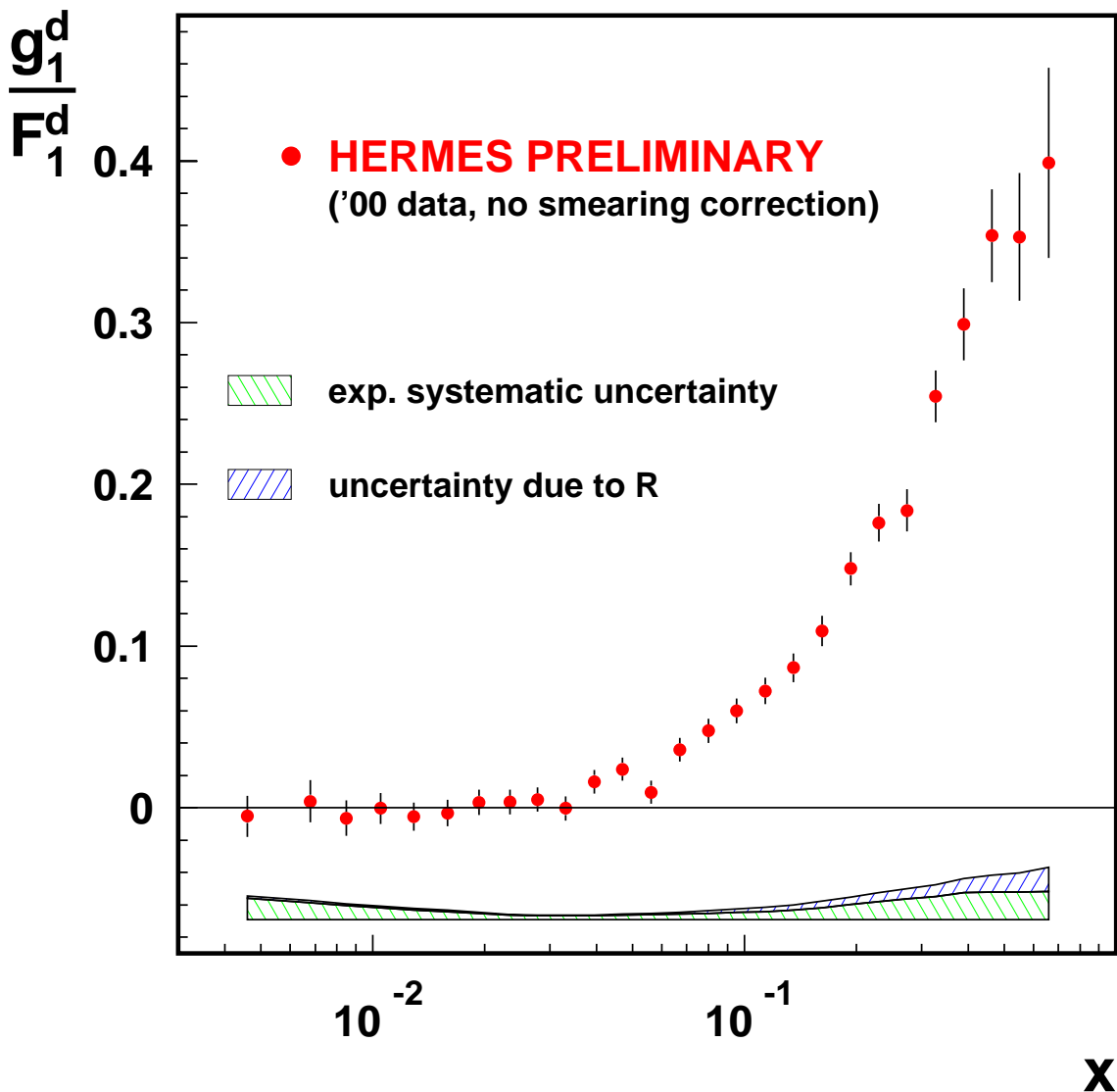


- Data taking in 2000:
 - cell size reduced to $21 \times 8.9 \text{ mm}^2$
 - lower cell temperature: $96 \rightarrow 62 \text{ K}$

Luminosity increased by factor 2.5 !!

- New deuterium data on $g_1^d(x)/F_1^d(x)$:

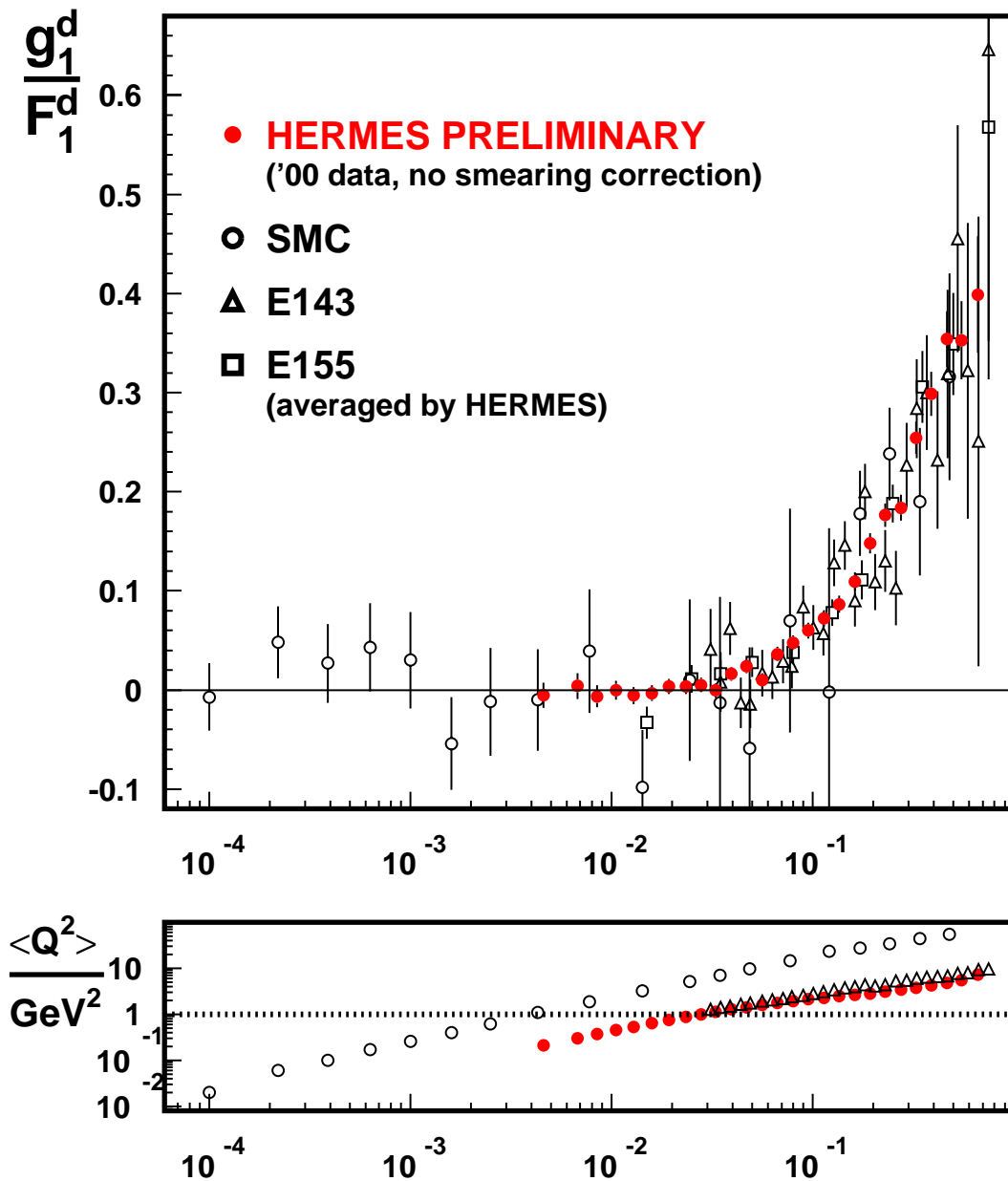
$$\frac{g_1^d}{F_1^d} = \frac{1}{1 + \gamma} \left(\frac{A_{//}^d}{D} - (\eta - \gamma)A_2^d \right)$$



- Observation:

HERMES probes down to $x \approx 4 \times 10^{-3}$

- Compare to existing data:

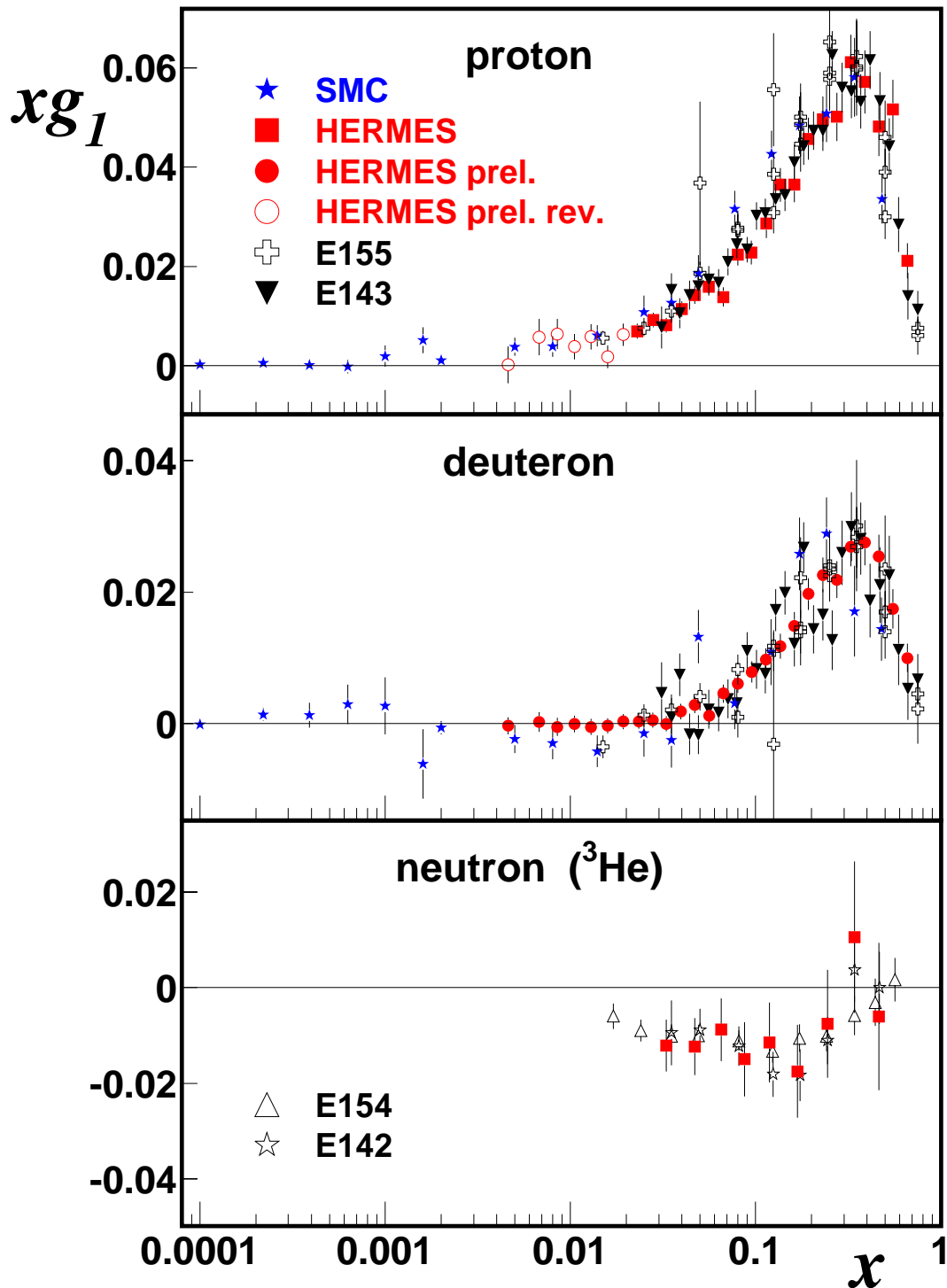


- Conclusion:

X

$g_1^d(x)$: no strong Q^2 dependence

- Overview of existing $xg_1(x)$ data:



- Preliminary data from SLAC E143 and E155x:

[$g_2(x)$ is sensitive to qg -correlations and higher twist]

$g_2^{WW}(x)$ exp.:

→ solid;

M. Stratmann (93):

→ dot-dash;

Gamberg-Weigel (97):

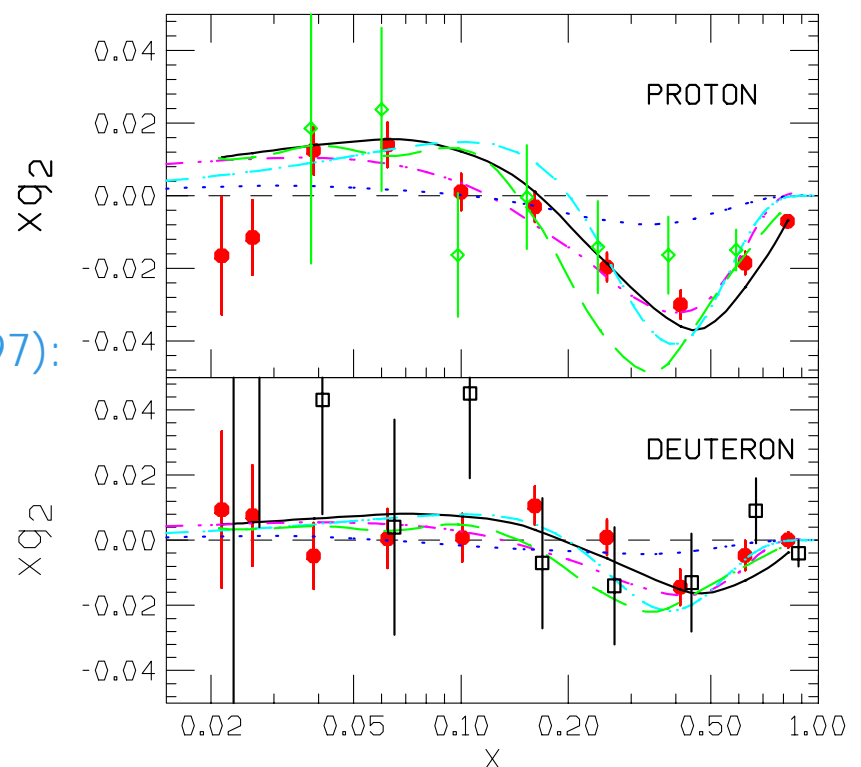
→ short-dash;

Song (96):

→ dotted;

Wakamatsu (96):

→ long-dash;



- Wandzura - Wilczek interpretation:

$$g_2^{WW}(x, Q^2) = -g_1(x, Q^2) + \int_x^1 \frac{g_1(y, Q^2)}{y} dy$$

$g_2(x, Q^2)$ dominated by twist-2 part



Semi-Inclusive Asymmetries



- Asymmetry for semi-inclusive hadron (h) production:

$$A_1^h(x) = \frac{\int dz \sum_f e_f^2 \Delta q_f(x) D_f^h(z)}{\int dz \sum_f e_f^2 q_f(x) D_f^h(z)} \propto \frac{N_{\uparrow\downarrow}^h - N_{\uparrow\uparrow}^h}{N_{\uparrow\downarrow}^h + N_{\uparrow\uparrow}^h}$$

- Define purity $P_f^h(x)$:

$$P_f^h(x) = \frac{e_f^2 q_f(x) \int D_f^h(z) dz}{\sum_f e_f^2 q_f(x) \int D_f^h(z) dz}$$

[probability that hadron h is produced when quark f is hit]

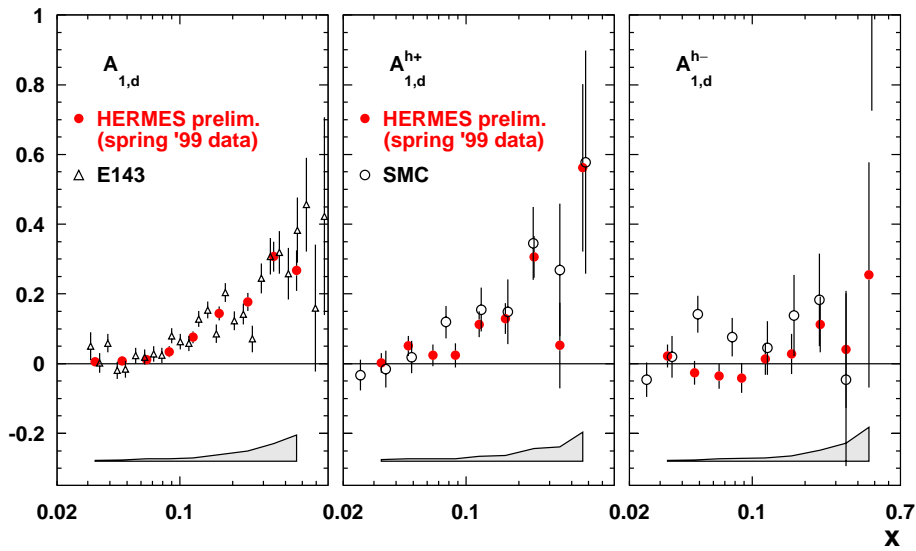
- Measure asymmetries on various targets:

$$\vec{A}(x) = \mathbf{P}(x) \vec{Q}(x)$$

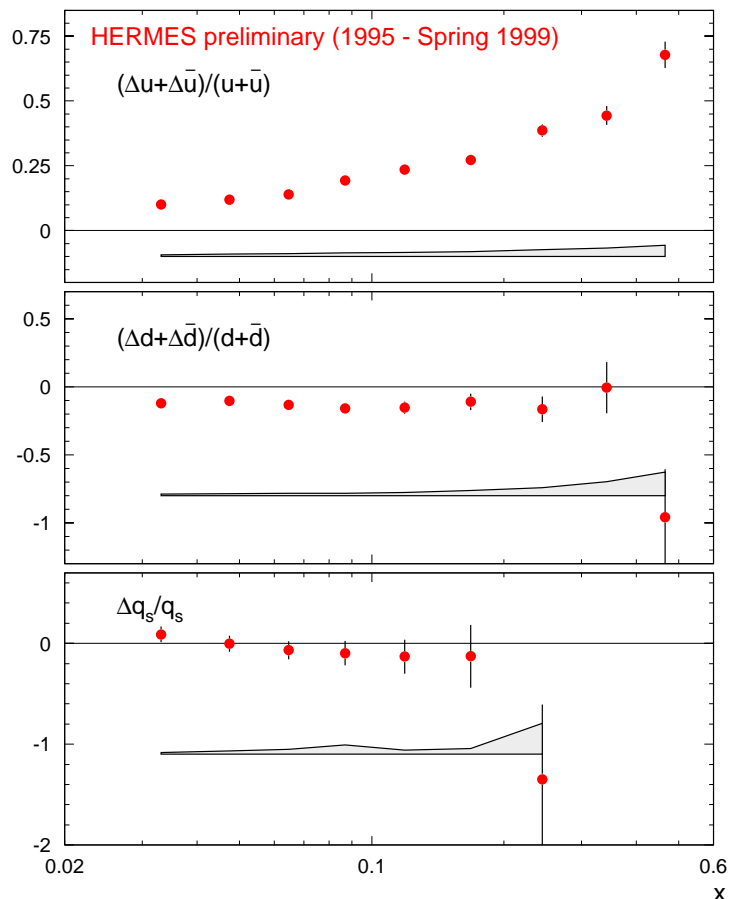
with $\vec{A}(x) = (A_{1p}, A_{1p}^{h+}, A_{1p}^{h-}, A_{1d}, \dots)$
and $\vec{Q}(x) = (\Delta u(x), \Delta d(x), \Delta \bar{u}(x), \dots)$

\Rightarrow Polarized quark distributions: $\Delta u(x), \Delta d(x), \dots$

- Measured semi-inclusive asymmetries $A_1^h(x)$:



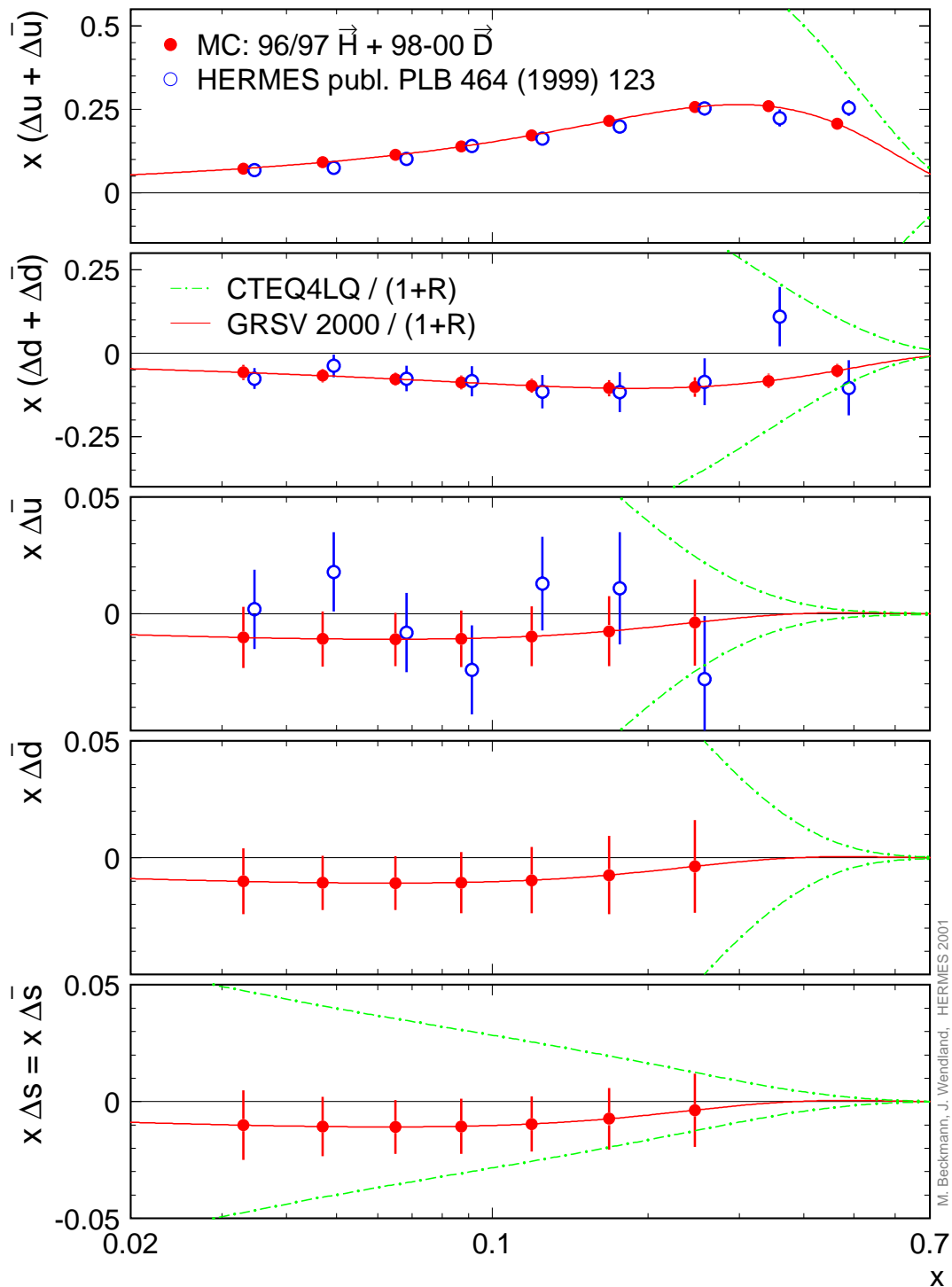
- Extracted quark spin distributions:



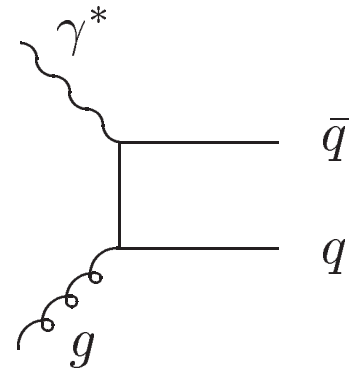
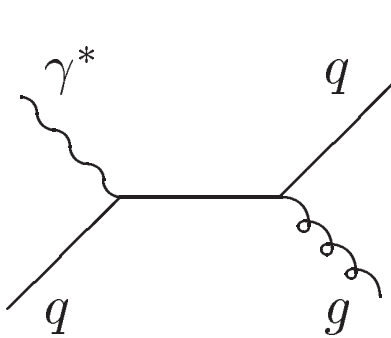
Spin - flavour separation.

- Expected data quality with '00 data included:

HERMES Δq extraction — MC projection



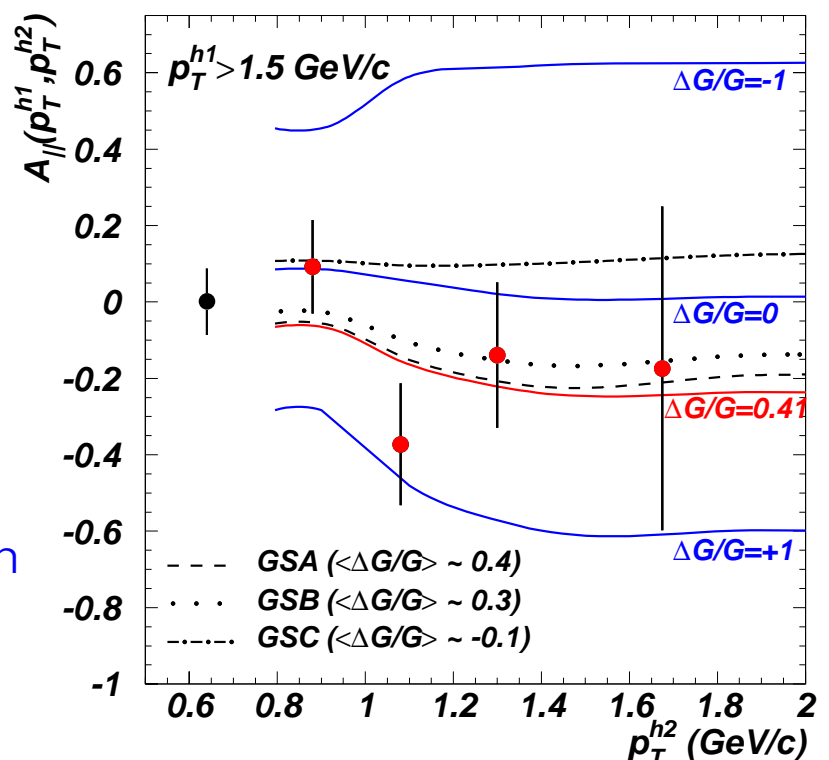
- pQCD Compton graph and Photon-Gluon Fusion:



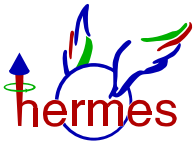
- Asymmetry for high- p_T pions ($R = \sigma_{PGF}/\sigma_{Com}$):

$$A_{LL}^{eN \rightarrow h_1 h_2} = \hat{a}_{QCDC} \frac{\Delta q}{q} \frac{1}{1+R} + \hat{a}_{PGF} \frac{\Delta G}{G} \frac{R}{1+R}$$

- Target spin-asymmetry on long. polarized ^1H :



HERMES Collaboration
PRL 84 (2000) 2584

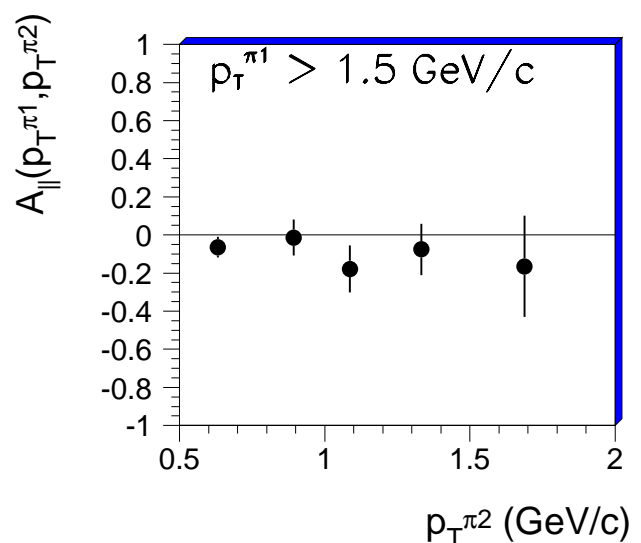
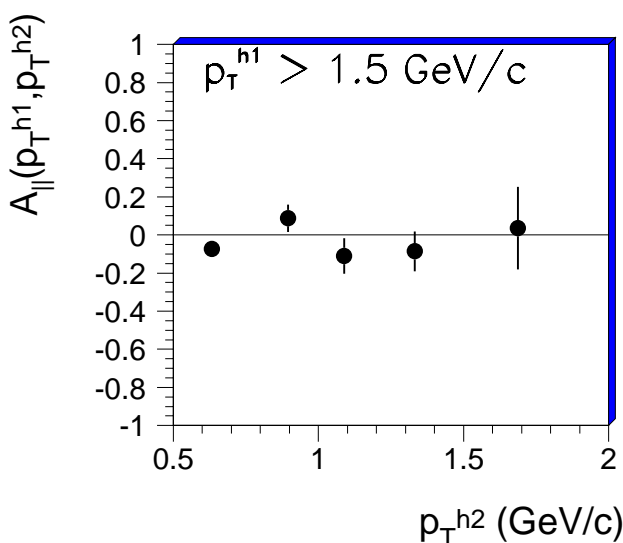
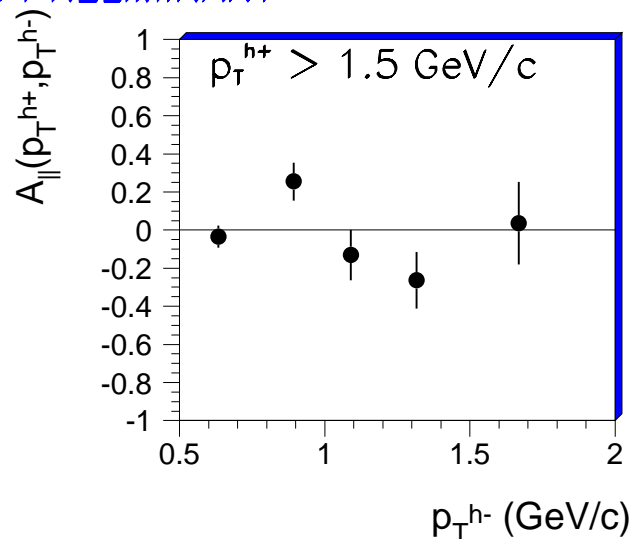
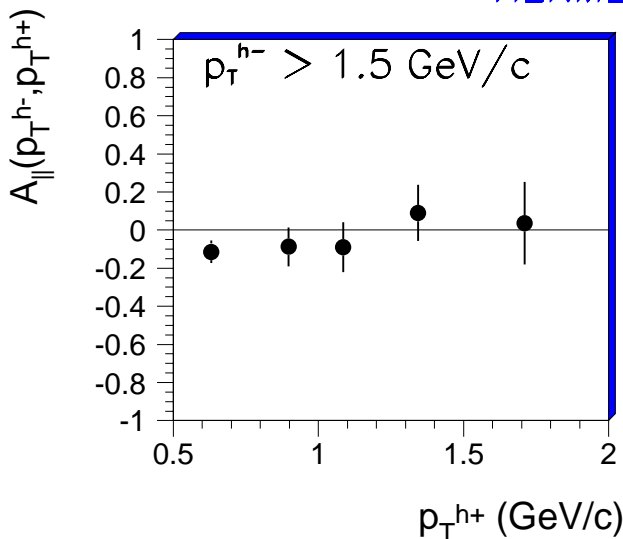


High- p_T hadron pairs on ^2H



- Require oppositely charged hadron pairs:
 - PGF produces only (+ -) pairs: **favored**
 - pQCD on ^1H \rightarrow more + hadrons: **disfavored**
- Preliminary results on ^2H :

HERMES PRELIMINARY



Systematic error 8.7%

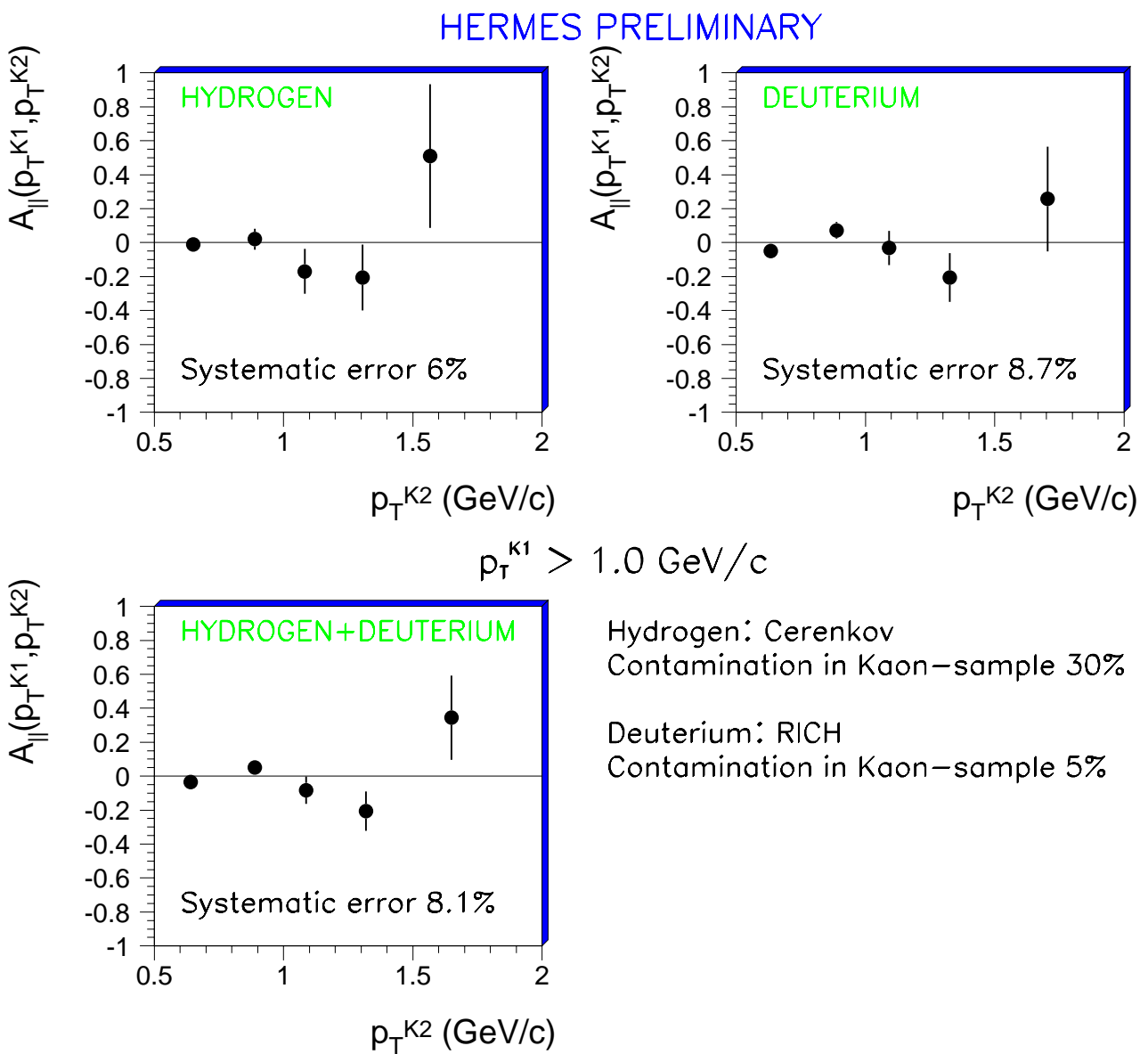
DEUTERIUM Target



High- p_T kaon pairs

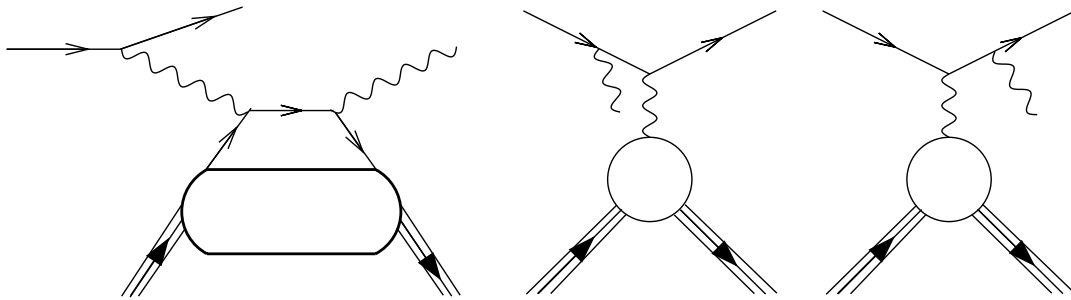


- Strangeness production suppressed in pQCD....
- High- p_T kaon pairs on ^1H and ^2H :



- More statistics needed (+ MC studies)

- Off-shell photon*-quark scattering:
 - Detect e' and γ , and require: $E_{miss} = 0$



- Ji's sumrule [Phys. Rev. Lett. 78 (1997) 610]:

$$\int x dx [H(x, \Delta^2, \xi) + E(x, \Delta^2, \xi)] = A_q(\Delta^2) + B_q(\Delta^2)$$

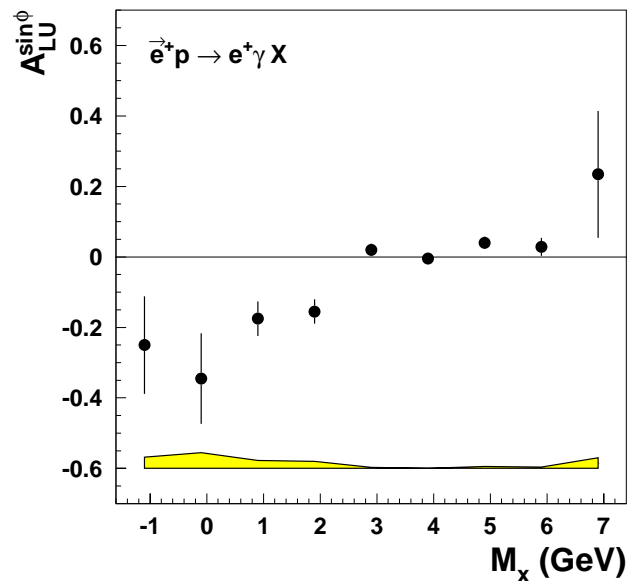
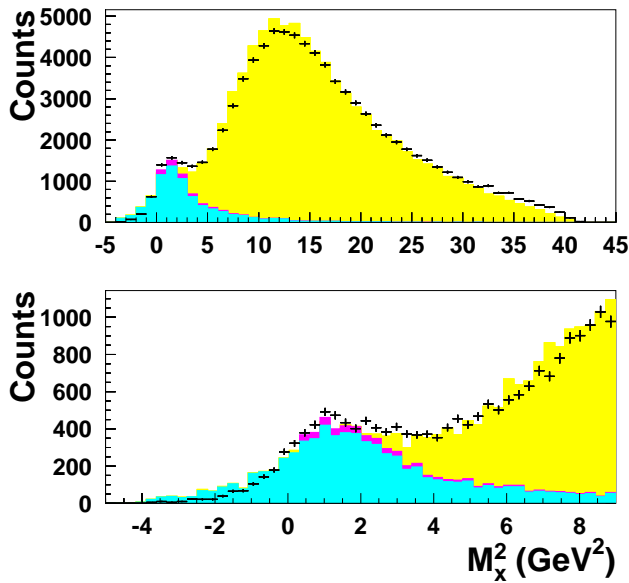
with $\Delta^2 = -t$ and

$$\lim_{\Delta^2 \rightarrow 0} [A_q(\Delta^2) + B_q(\Delta^2)] = 2J_{quark} = \Sigma_q + 2L_q$$

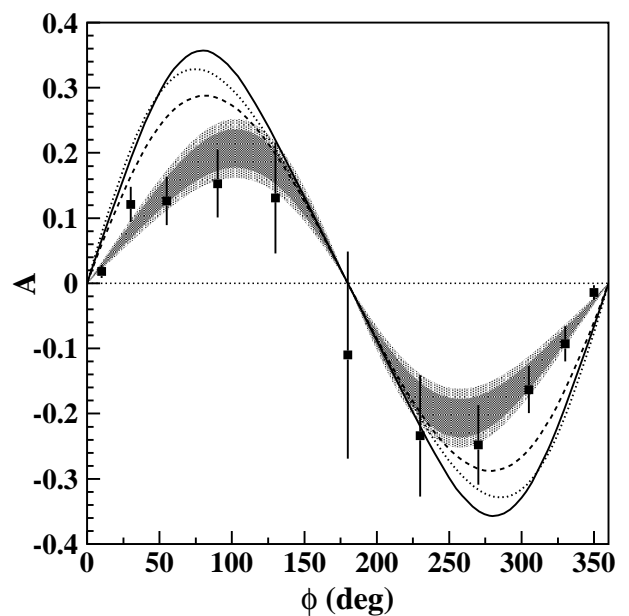
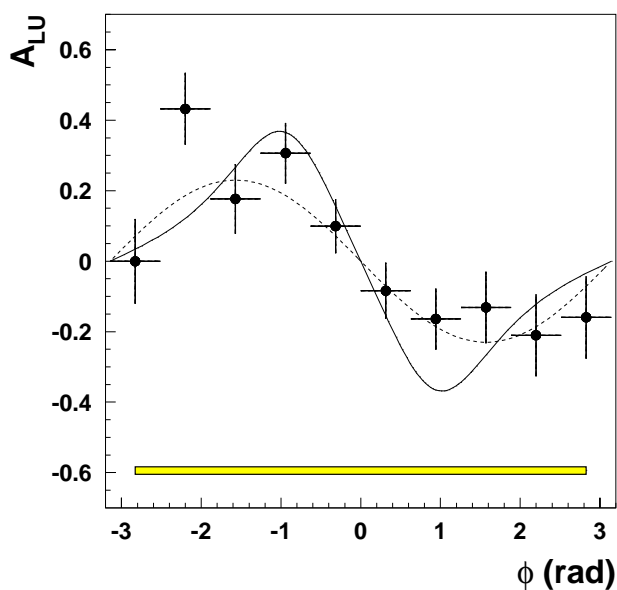
\Rightarrow DVCS: total quark angular momentum

- Experimental considerations:
 - Interference with Bethe-Heitler process:
 - DVCS \otimes BH makes DVCS measurable
 - Detect scattered photon, but suppress π^0 's
 - Observe azim. asymmetry: $A_{LU}^{BetheHeitler} = 0$

- Missing mass spectrum and $A_{LU}^{\sin\phi} = \frac{2}{N} \sum_{i=1}^N \frac{\sin\phi_i}{(P_t)_i}$:



- Azimuthal (ϕ) distributions from HERMES & JLab:



- Exclusive leptonproduction of photon:

$$\frac{d^4\sigma}{d\phi dt dQ^2 dx} = \frac{xy^2}{32 (2\pi)^4 Q^4} \frac{|\tau_{\text{BH}} + \tau_{\text{DVCS}}|^2}{(1 + 4x^2 m^2/Q^2)^{1/2}}$$

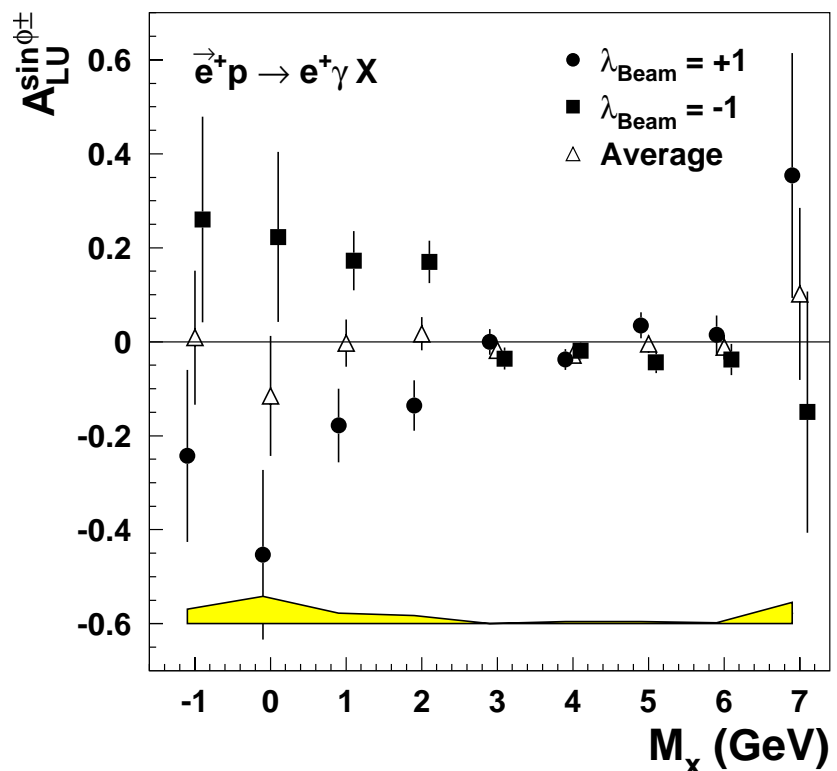
- Leading order interference term:

$$(\tau_{\text{BH}}^* \tau_{\text{DVCS}} + \tau_{\text{DVCS}}^* \tau_{\text{BH}})_{\text{pol}} = \frac{4\sqrt{2} m e^6}{t Q x} \cdot \frac{1}{\sqrt{1-x}}$$

$$\times e_l \times P_l \left[-\sin \phi \cdot \sqrt{\frac{1+\epsilon}{\epsilon}} \text{Im} \tilde{M}^{1,1} \right]$$

- Extract $\sin(\phi)$ -moment, $A_{LU}^{\sin \phi^\pm} = \frac{2}{N^\pm} \sum_{i=1}^{N^\pm} \frac{\sin \phi_i}{|P_l|_i}$:

Data show
expected
helicity
dependence!



- Beam-charge asymmetry with unpolarised leptons:

$$d\sigma(e^+p) - d\sigma(e^-p) \sim \cos \phi_\gamma \times \operatorname{Re} \left\{ F_1 \mathcal{H}_1 + \frac{x_B}{2 - x_B} (F_1 + F_2) \tilde{\mathcal{H}}_1 - \frac{\Delta^2}{4M^2} F_2 \mathcal{E}_1 \right\}$$

- Beam-spin asymmetry with polarised positrons:

$$d\sigma(e^{\uparrow}p) - d\sigma(e^{\leftarrow+}p) \sim \sin \phi_\gamma \times \operatorname{Im} \left\{ F_1 \mathcal{H}_1 + \frac{x_B}{2 - x_B} (F_1 + F_2) \tilde{\mathcal{H}}_1 - \frac{\Delta^2}{4M^2} F_2 \mathcal{E}_1 \right\}$$

- Relate DVCS amplitudes $\mathcal{H}_1, \tilde{\mathcal{H}}_1, \dots$ to GPDs:

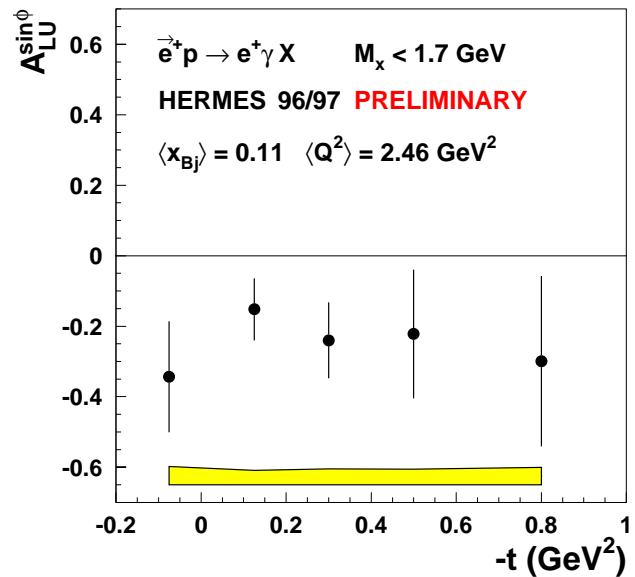
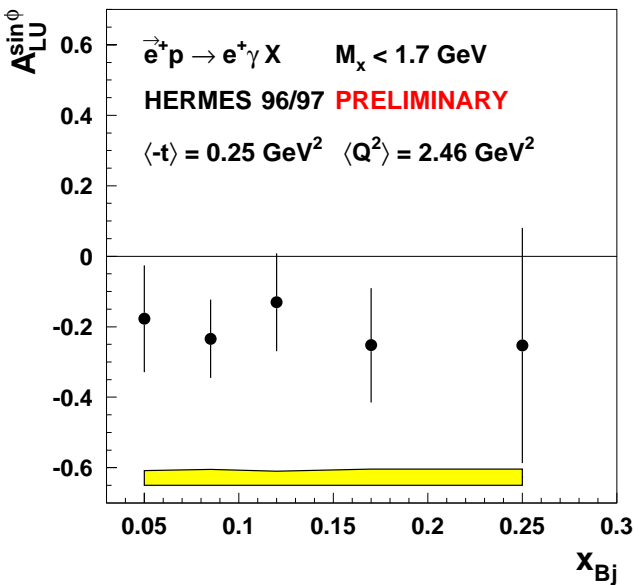
$$\operatorname{Im} \mathcal{H}_1 = -\pi \sum_q e_q^2 (H(\xi, \xi, \Delta^2) - H(-\xi, \xi, \Delta^2))$$

$$\operatorname{Im} \tilde{\mathcal{H}}_1 = -\pi \sum_q e_q^2 (\tilde{H}(\xi, \xi, \Delta^2) + \tilde{H}(-\xi, \xi, \Delta^2))$$

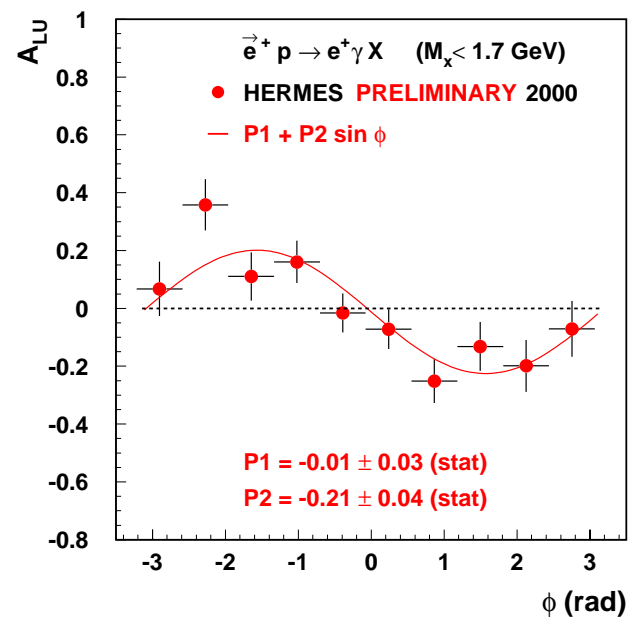
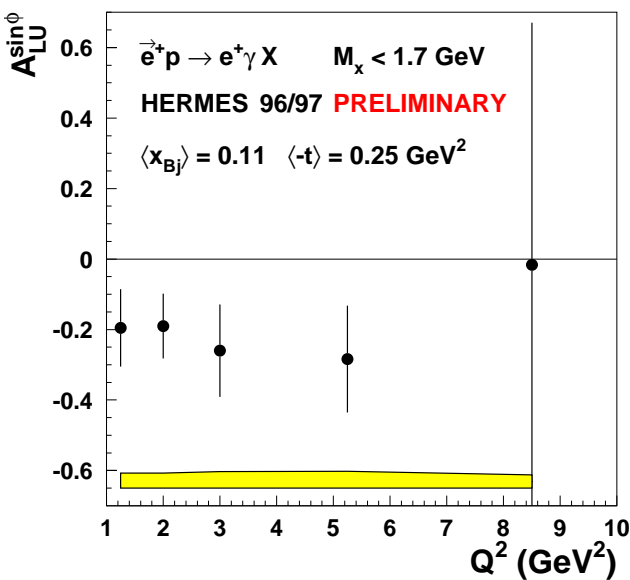
$$\operatorname{Re} \mathcal{H}_1 = \sum_q e_q^2 [P \int_{-1}^{+1} H(x, \xi, \Delta^2) \left(\frac{1}{x - \xi} + \frac{1}{x + \xi} \right) dx]$$

$$\operatorname{Re} \tilde{\mathcal{H}}_1 = \sum_q e_q^2 [P \int_{-1}^{+1} \tilde{H}(x, \xi, \Delta^2) \left(\frac{1}{x - \xi} - \frac{1}{x + \xi} \right) dx]$$

- Dependence of $A_{LU}^{\sin\phi}$ on x and $-t$:



- Q^2 -dependence and new 2000 data for $A_{LU}^{\sin\phi}$:



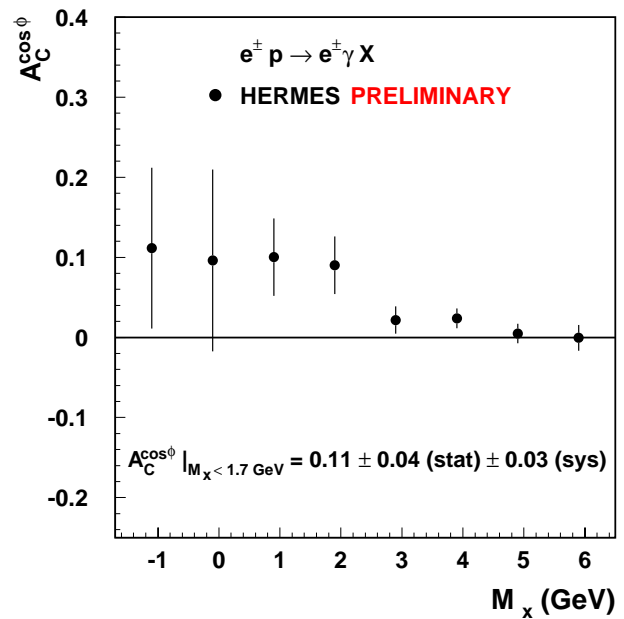
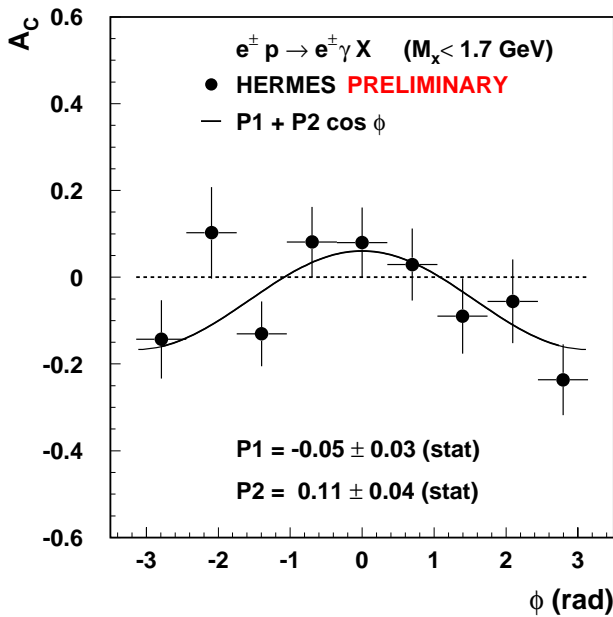
No Q^2 -dependence: hard scattering regime!



DVCS: beam-charge asymmetry



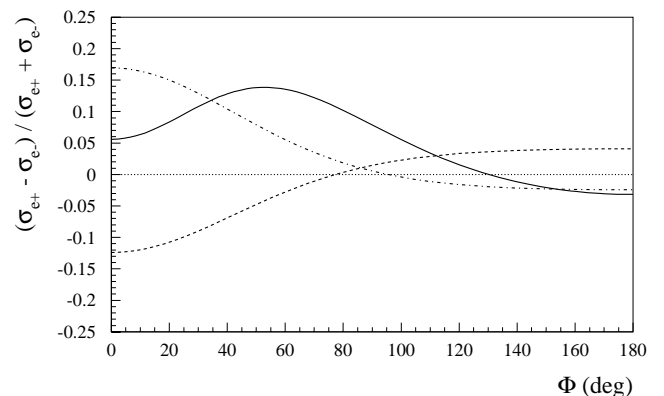
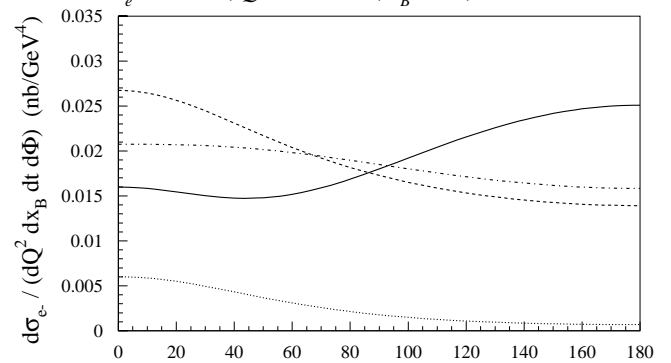
- First data for $A_C = \frac{N^{e^+} - N^{e^-}}{N^{e^+} + N^{e^-}}$ on ^1H :



- Calculation by Kivel et al. [hep-ph/0012136]:

$$e^-/e^+ + p \rightarrow e^-/e^+ + p + \gamma$$

$$E_e = 27 \text{ GeV}, Q^2 = 2.5 \text{ GeV}^2, x_B = 0.3, t = -0.25 \text{ GeV}^2$$



BH + twist 2 + D-term

BH + tw 2 + tw 3 + D-term

BH only

BH + twist 2 - D-term

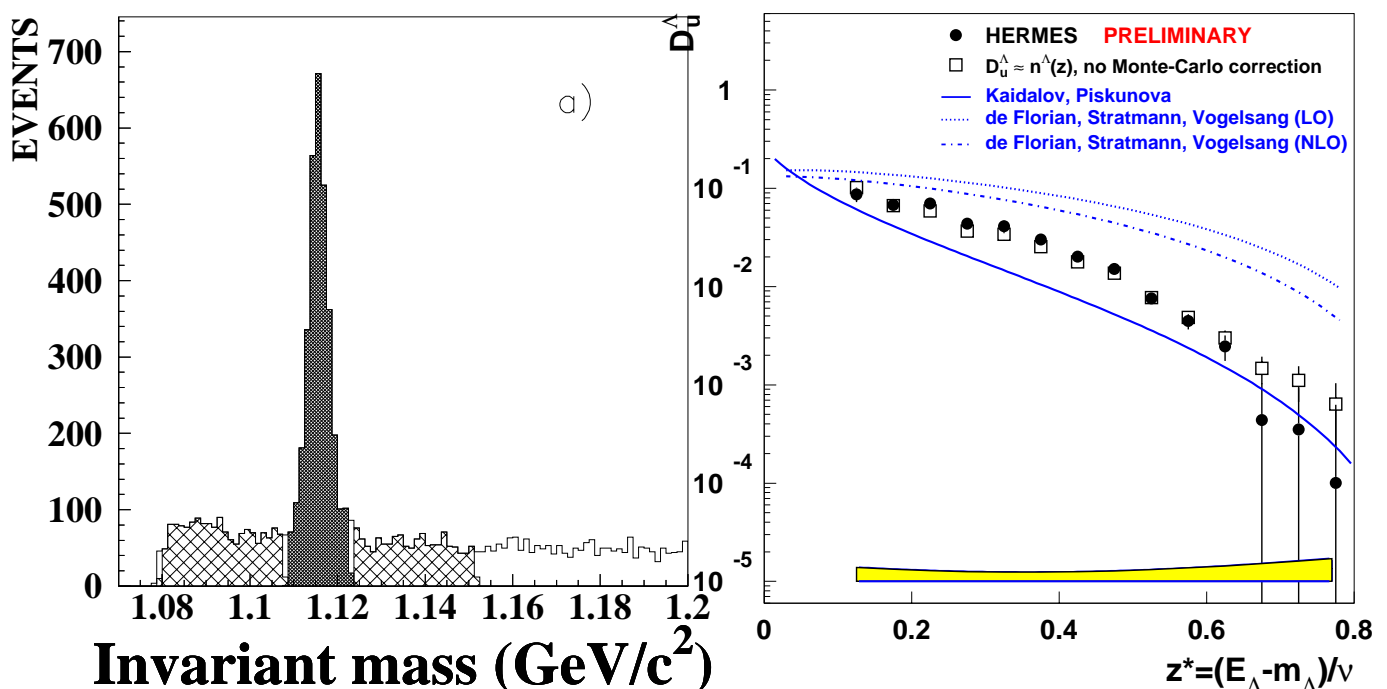
- Two schemes for the Λ spin content:
 - Quark parton model: $\Delta s = 1.00$
 - SU(3) flavour symm.: $\Delta s = 0.6, \Delta u = \Delta d = -0.2$
- Measure the Λ polarization from $\Lambda \rightarrow p\pi^-$:

$$\frac{1}{N} \frac{dN}{d\Omega} = \frac{1}{4\pi} (1 + 0.64 \vec{P}_\Lambda \cdot \hat{p})$$

- Determine $u \rightarrow \Lambda$ spin transfer $D_{LL'}^\Lambda$:

$$D_{LL'}^\Lambda = \frac{\vec{P}_\Lambda \cdot \hat{L}'}{P_B D(y)} = \frac{\sum_f e_f^2 q_f^N(x) \Delta D_f^\Lambda(z)}{\sum_f e_f^2 q_f^N(x) D_f^\Lambda(z)} \approx \frac{\Delta D_u^\Lambda(z)}{D_u^\Lambda(z)}$$

- Electroproduction of Λ hyperons at HERMES:



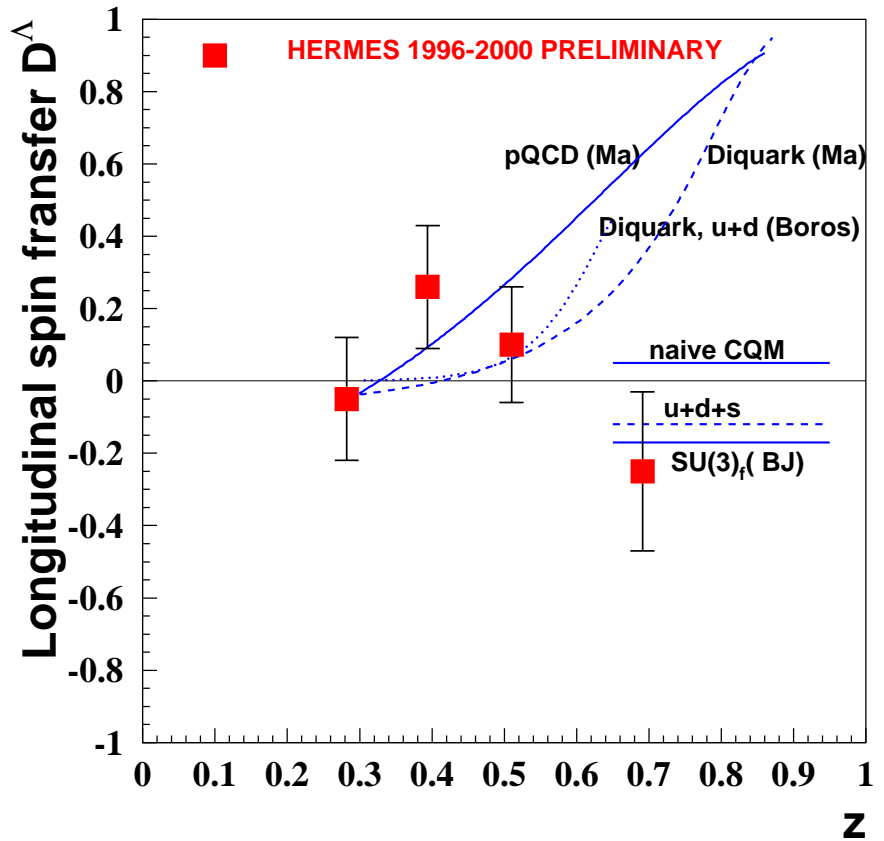


The Λ spin structure - 2



- Data for $u \rightarrow \Lambda$ spin transfer:

$\langle D_{LL'}^\Lambda \rangle = 0.04(9)$
 consistent with
 $\Delta u^\Lambda \approx 0$
 (CQM prediction).

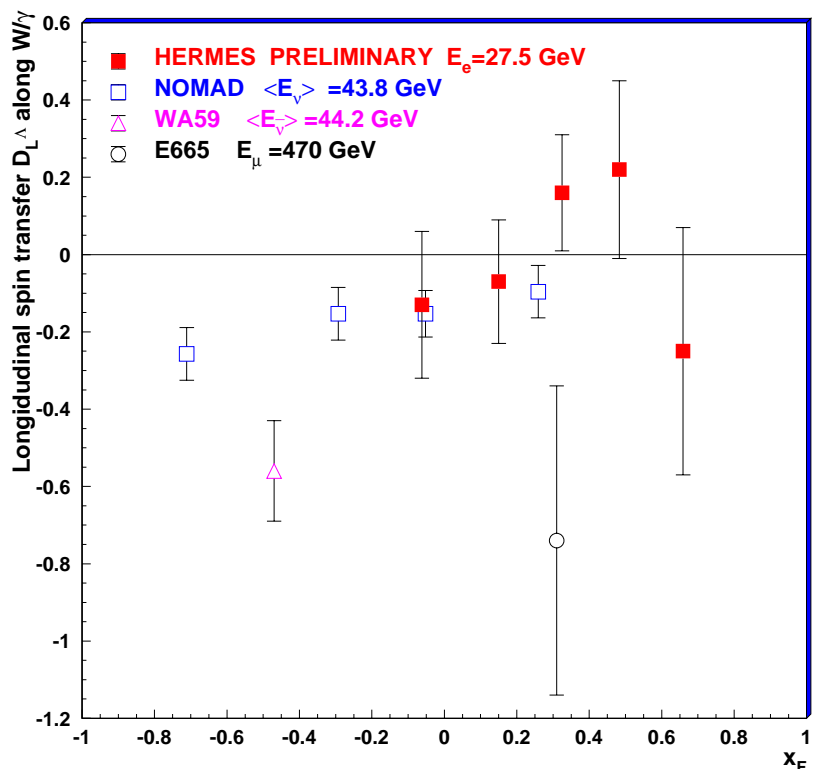


- Negative polarisation for $x_F (= \frac{2p_L}{W}) < 0$:

NOMAD Collab.
 NPB 588 (2000) 3

Contributions from:

- $\Sigma^* \rightarrow \Lambda \pi$
- $\Sigma^0 \rightarrow \Lambda \gamma$
- $\Xi^0 \rightarrow \Lambda \pi^0$



- Three leading order distribution functions:

$$f_1 = \text{[Diagram: circle with black dot]} \quad \text{momentum carried by quarks}$$

$$g_1 = \text{[Diagram: circle with black dot and red arrow right]} - \text{[Diagram: circle with black dot and red arrow left]} \quad \text{longitudinal quark spin, } \Delta\Sigma$$

$$h_1 = \text{[Diagram: circle with black dot and red arrow up]} - \text{[Diagram: circle with black dot and red arrow down]} \quad \text{transverse quark spin, } \delta\Sigma$$

- Importance of $h_1(x)$ measurements:

- HERMES data: $\Delta\Sigma = 0.30 \pm 0.04 \pm 0.09$
- $\Delta\Sigma$ is so small because of axial anomaly:

* Redistribution of angular momentum in nucleon:

$$\frac{1}{2}\Delta\Sigma \approx +0.15, \quad \Delta G \approx +1.0, \quad L_z \approx -0.65$$

* Redistribution is less in transverse case:

$$\Delta\Sigma < \delta\Sigma < 1 \quad (\text{Quark Parton Model})$$

* Lattice QCD calculation (Phys. Rev. D 56 (1997) 433):

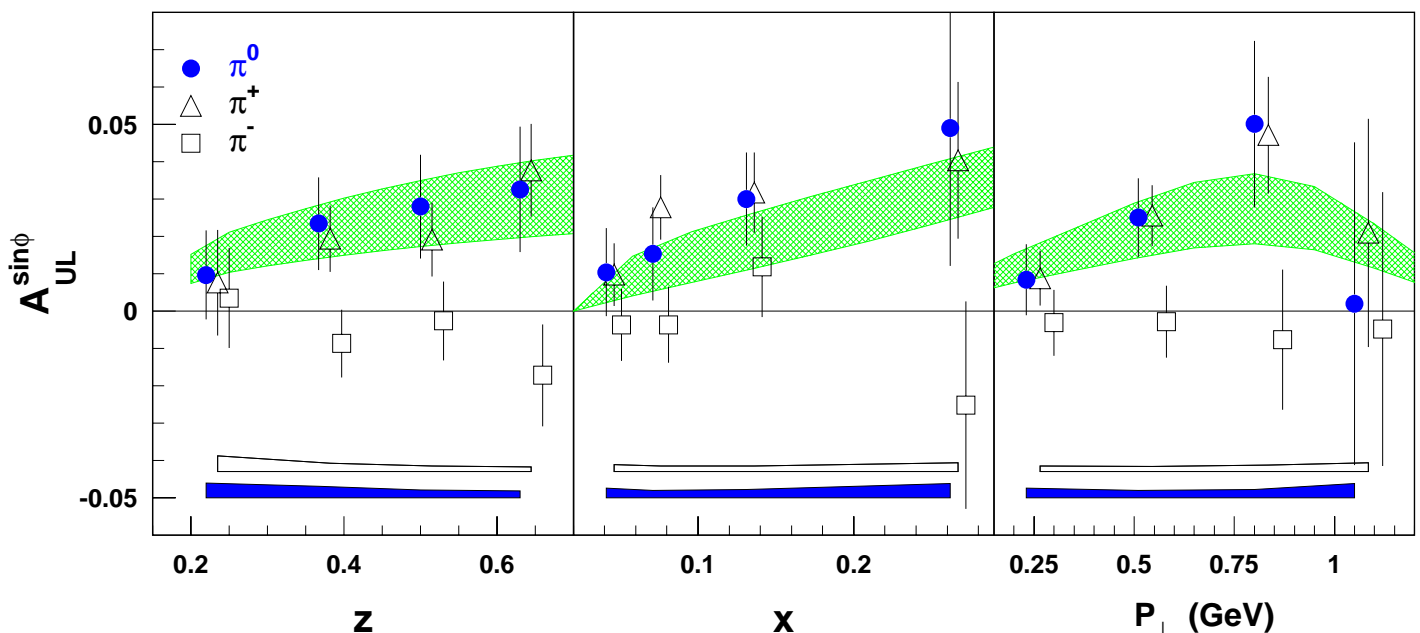
$$\Delta\Sigma = 0.18(10) \quad \text{and} \quad \delta\Sigma = 0.56(9)$$

- The structure function $h_1(x)$ is **chirally odd** :
 - Not accessible in inclusive DIS
 - Use semi-inclusive DIS with chirally-odd $H_1^{\perp(1)u}(z)$
 - Assume u -quark dominance
 - Asymmetry for Collins process:

$$A_T^{\pi^+}(x, y, z) = P_T \cdot D_{nn} \cdot \frac{\delta u(x)}{u(x)} \cdot \frac{H_1^{\perp(1)u}(z)}{D_1^u(z)},$$

- $H_1^{\perp(1)u}$ depends on $\phi_c = \phi_h + \phi_s - \pi$

- Evidence for transversity from HERMES ¹H data:



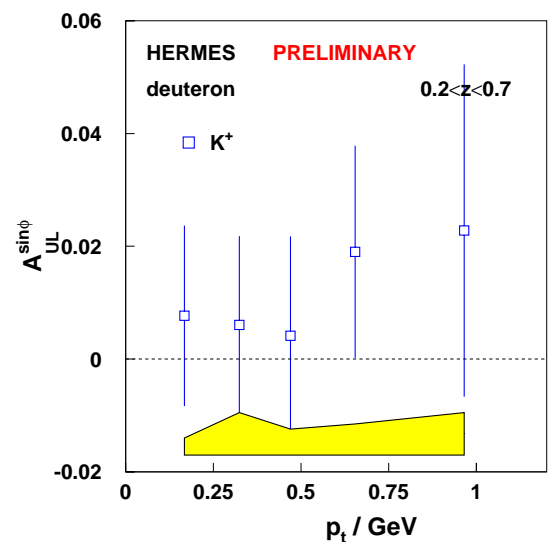
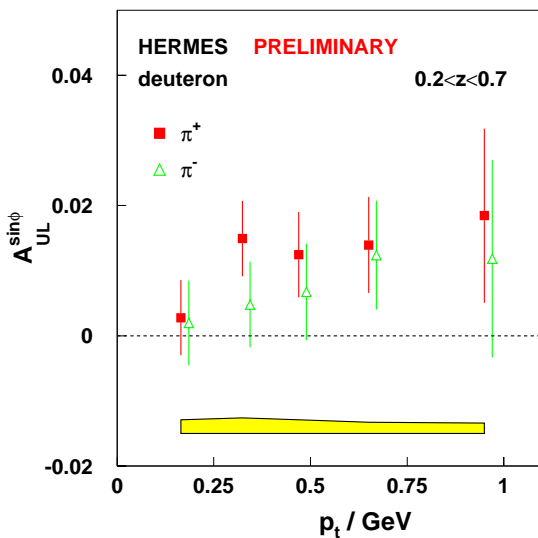
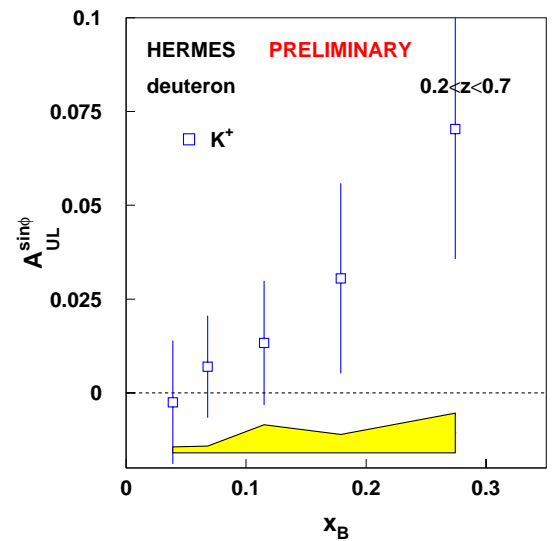
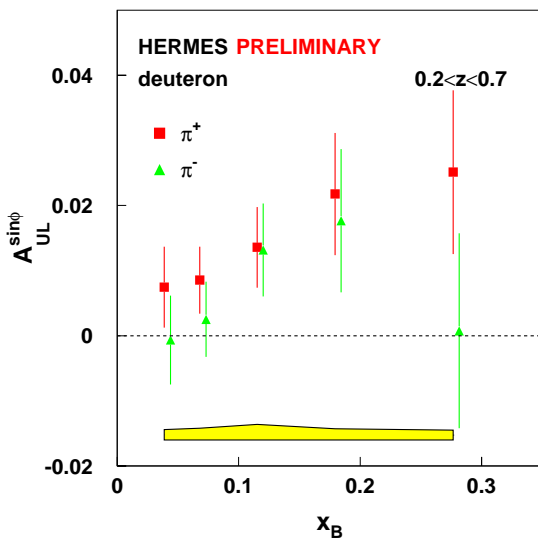
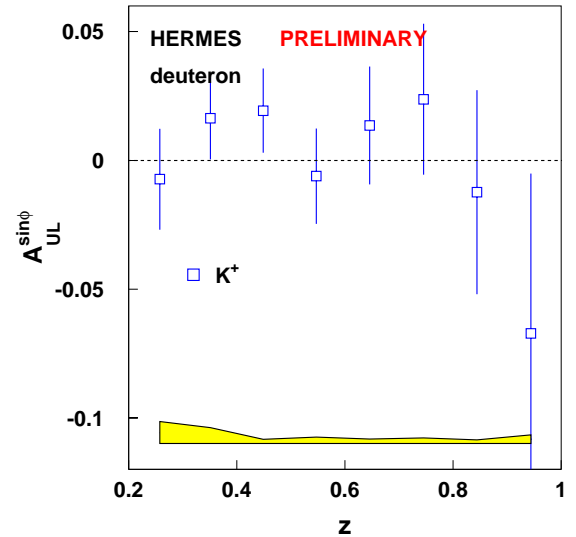
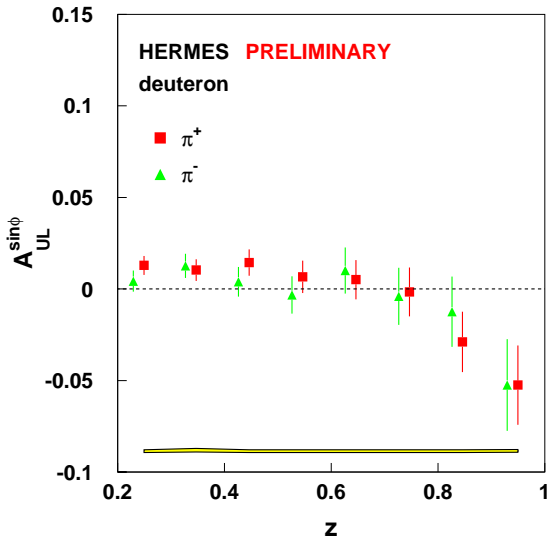
[HERMES, PRL 84 (2000) 4047 and PRD 64 (2001) 097101]



Single-Spin Asymmetries on ^2H



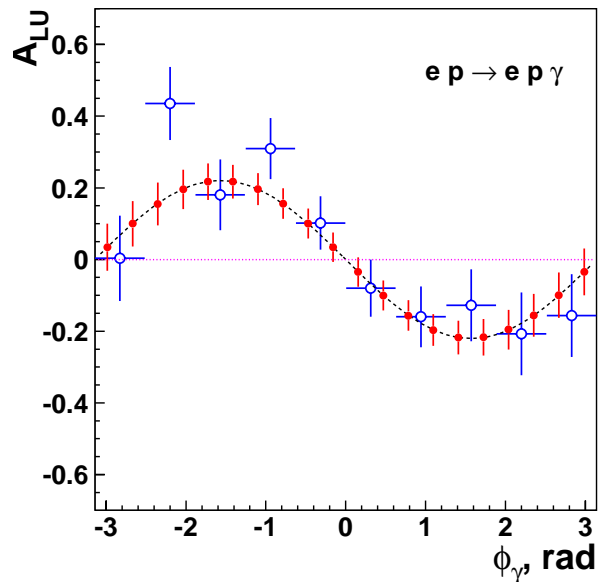
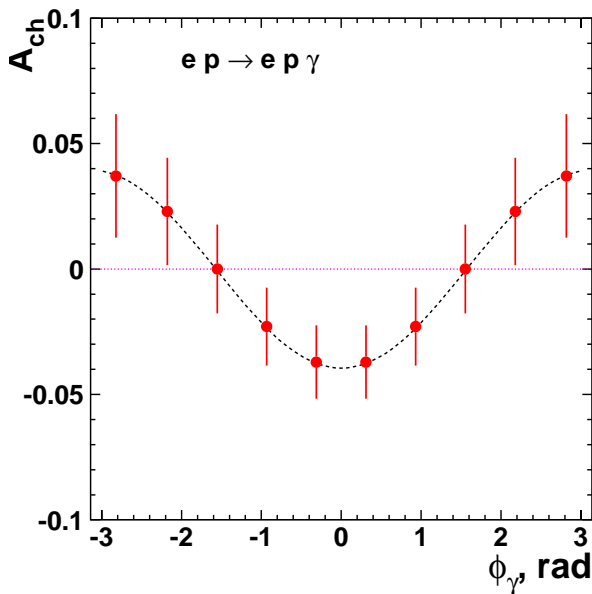
- z, x, p_{\perp} -dependences of $A_{UL}^{\sin\phi}$ for $\pi^{+/-}$ and K^+ :



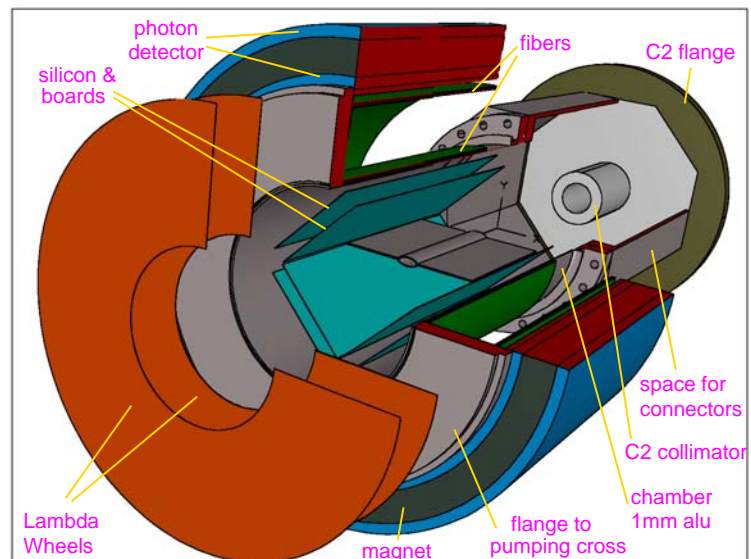
- HERMES - Run II: 2001 – 2006

- Transverse spin 2001 - 2003
- Longitudinal spin 2003 - 2004
- Excl. react. w. **Recoil Detector** : 2004 - 2006
- Unpolarized end-of-fill runs 2001 - 2006

Simulated DVCS data with Recoil Detector (1 yr run):



- HERMES - Run III
(beyond 2006 ?)

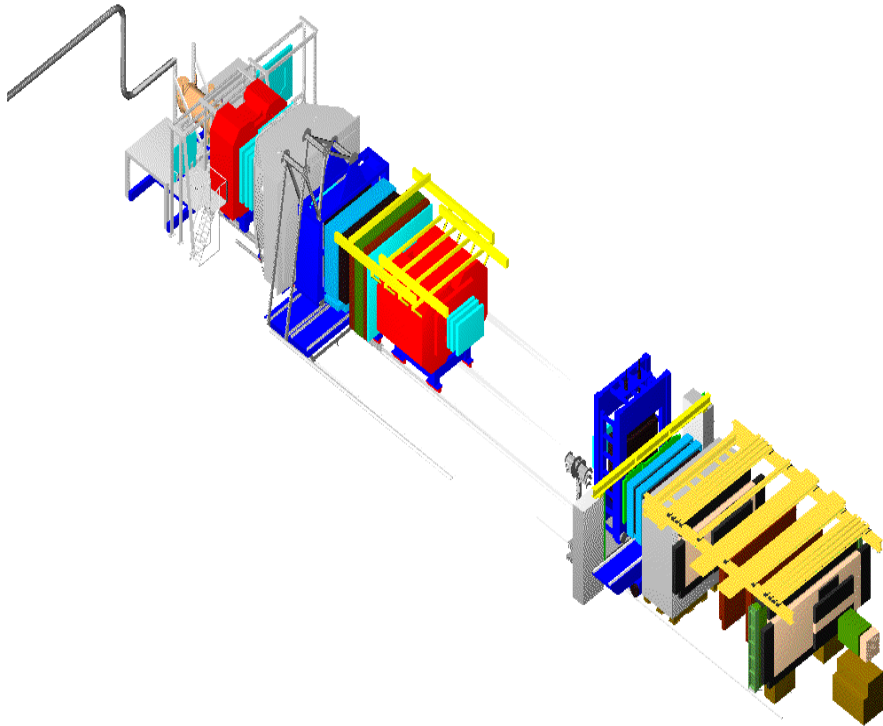




Future: COMPASS



- The Compass experiment at CERN:



- Successful commissioning in 2001:
 - Most detectors commissioned at $2 \cdot 10^8 \mu/s$.
 - Tracking: half of the channels
 - ${}^6\text{LiD}$ target hosted in SMC magnet: $P = \pm 45\%$
 - 2 weeks smooth data taking
- Prospects for 2002:
 - Complete tracking and finish commissioning
 - First measurement of $\Delta G/G$ in 3 month run
 - Other objectives: $\delta q(x)$, $h_1(x)$, ΔD^Λ , spectroscopy



Future: RHIC



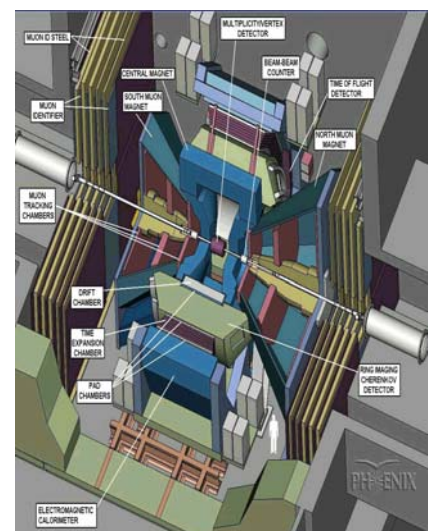
- RHIC at BNL as seen by LANDSAT:



- Experimental break-through at RHIC:

Colliding polarized protons at $\sqrt{s} = 200$ GeV

- $P_{proton} = 70\%$ at injection and 25 % at 100 GeV
- Luminosity: $1.5 \cdot 10^{30} \text{ cm}^{-2}\text{s}^{-1}$
- Physics: transverse spin asymmetries A_N
- Longitudinal polarization: spin rotators in 2002
 - Measure $\Delta G/G$ from jets, $c\bar{c}$, ...
 - Measure Δq_f from W^+ production
- The PHENIX experiment:



- End-station A at SLAC:
 - E160: single spin-asymm. for inelastic J/Ψ
 - E161: open charm photoproduction $\rightarrow \Delta G/G$
- What to expect in coming years?
 - Polarized quark distributions
 - Polarized gluon distribution
- The big challenges in spin physics:
 - The role of orbital angular momentum:

Analysis and interpretation of DVCS $\rightarrow J_q?$
 - The role of transverse spin:

Measure the (x, Q^2) -dependence of $h_1(x)$
- The more distant future (> 2010):
 - Electron-Ion Collider at BNL: $10 \otimes 250 \text{ GeV}^2$
 - TESLA-N at DESY: $250 \text{ GeV } e^+$ on fixed target

