

# Simulation of APPLE ID for APS-U

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# Outline

- Introduction to the “Generating Function” (GF) Method
- Simulation of end\_poles
- Benchmark Results
- Application to APS-U
- Summary



# Introduction

- GF-method was developed by J. Bahrtd and G. Wüstefeld<sup>1</sup> at BESSY (“BESSY” method)
- Applicable to any magnetic field, if the field
  - can be represented analytically
  - can be differentiated and integrated
- Very useful for ID simulation
  - Has periodic field
  - The differentiation/integration can be calculated easily
- Extremely useful for APPLE or similar ID simulation
  - Complex undulator structures – generates universal polarization mode depends on individual row’s longitudinal position and undulator gap (5D parameter space)
  - Total field is the linear superposition of field from each rows – no needs on repeatedly ID field calculation

<sup>1</sup> J. Bahrtd and G. Wüstefeld, “Symplectic tracking and compensation of dynamic field integrals in complex undulator structures,” PRSTAB 14, 040703 (2011).



# GF-Method

GF function – making a canonical transformation  $(x, p_x, y, p_y) \rightarrow (x, p_{xf}, y, p_{yf})$   
Solve the Hamiltonian-Jacobi equation through a Taylor expansion

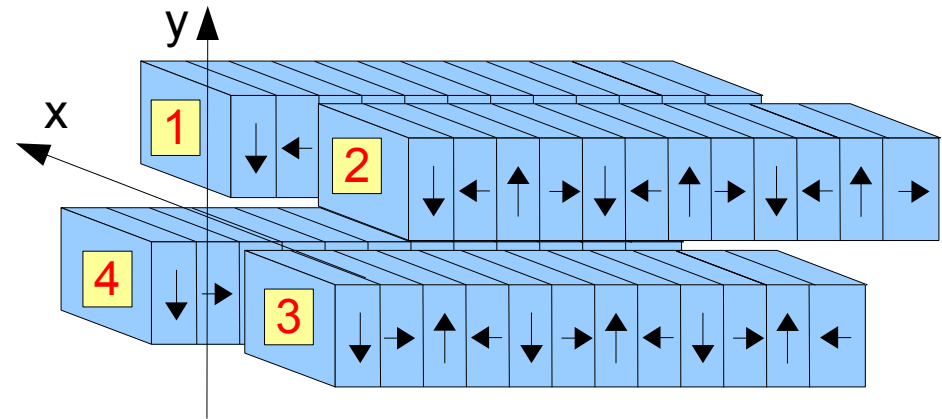
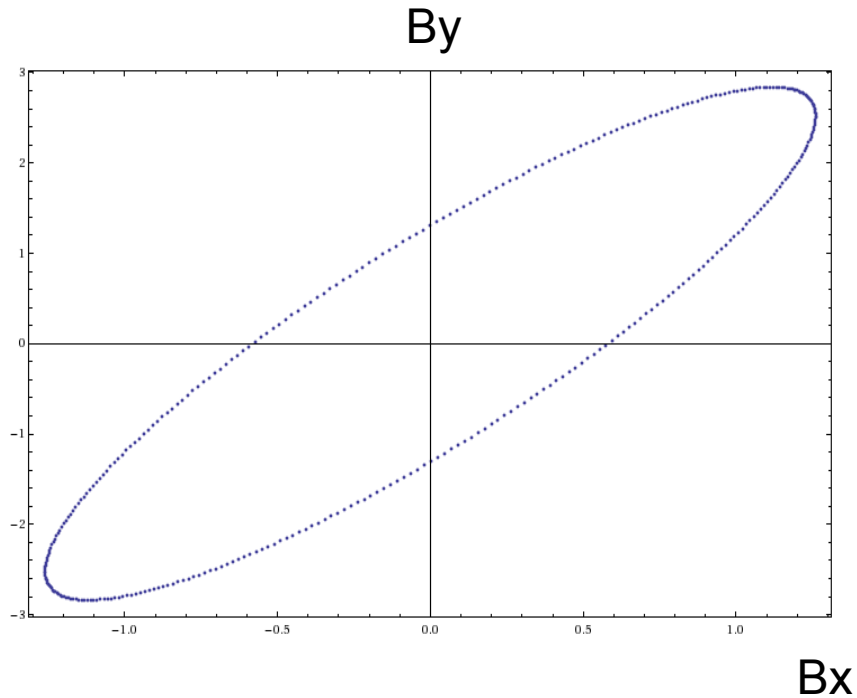
$$\begin{aligned}x_f &= x + p_{xf} \Delta z - f_{101} \\y_f &= y + p_{yf} \Delta z - f_{011} \\p_{xf} &= [(1 - f_{011y})(p_x + f_{002x} + f_{003x}) + f_{011x}(p_y + f_{002y} + f_{003y})] / p_n \\p_{yf} &= [(1 - f_{101x})(p_y + f_{002y} + f_{003y}) + f_{101y}(p_x + f_{002x} + f_{003x})] / p_n \\p_n &= (1 - f_{101x})(1 - f_{011y}) - f_{101y} f_{011x}\end{aligned}$$

step size

Uses gauge  $A_z = 0$

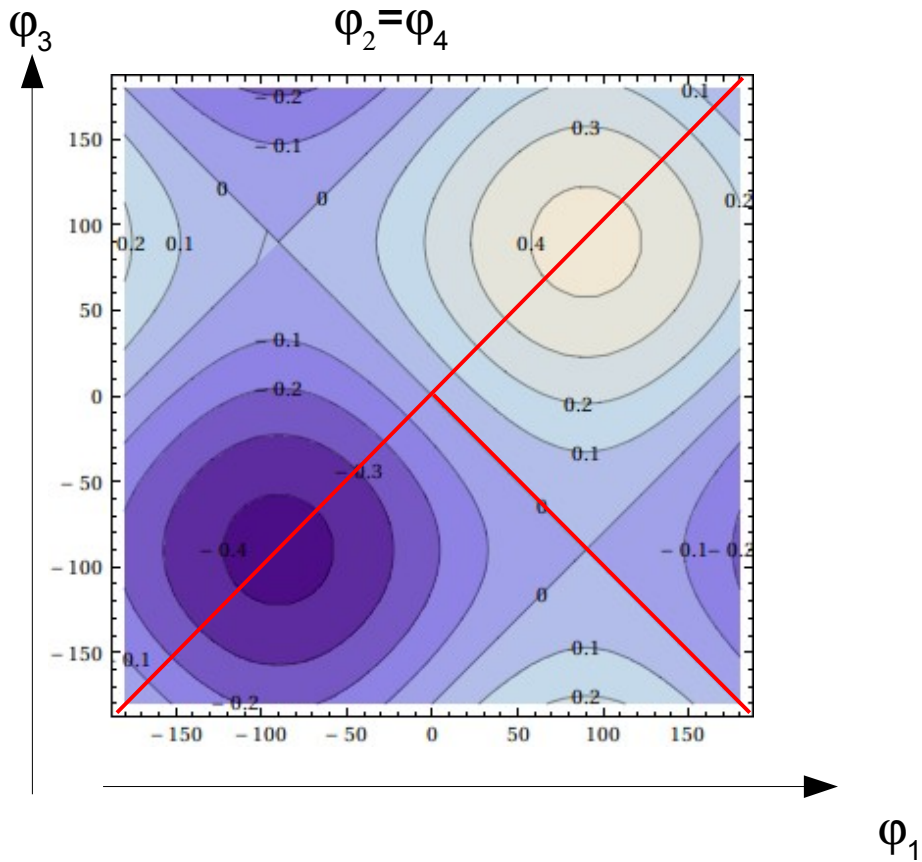
$$\left\{ \begin{aligned}f_{101} &= \int A_x dz \\f_{011} &= \int A_y dz \\f_{002} &= -\frac{1}{2} \int (A_x^2 + A_y^2) dz \\f_{003} &= \frac{1}{2} \left[ \int A_x dz \int \frac{\partial(A_x^2 + A_y^2)}{\partial x} dz' + \int A_y dz \int \frac{\partial(A_x^2 + A_y^2)}{\partial y} dz' \right]\end{aligned} \right.$$

# APPLE Device - Universal Mode

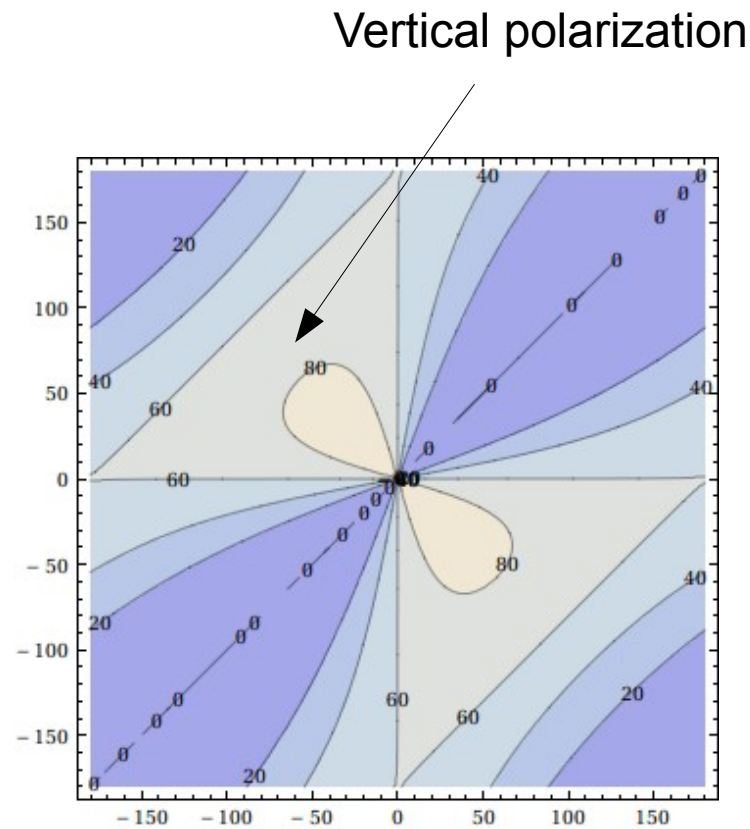


Can generate any state of polarization!

$$\theta_1 = \theta_3 \quad \theta_2 = \frac{\pi}{2} \quad \theta_4 = -\frac{\pi}{5}$$



Ellipse area (0 – linear mode)



Red line – most APPLE device operational parameter space

# APPLE Field

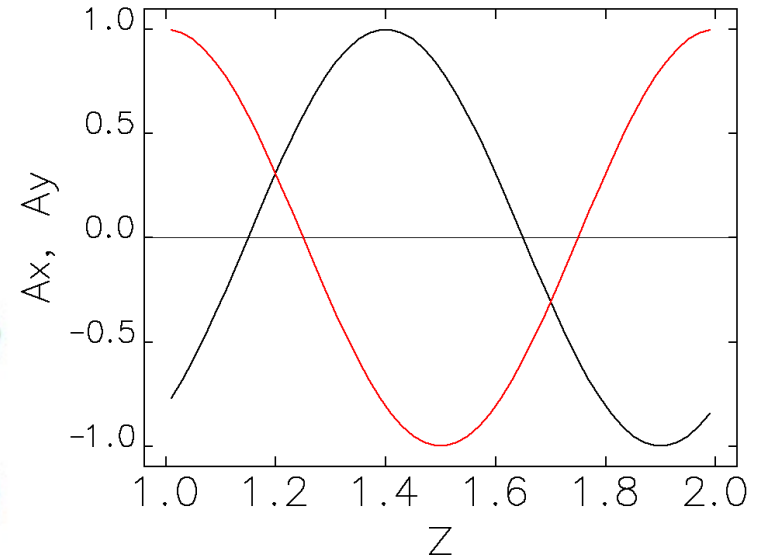
$$A_{x,i} = \sum_{j=1}^n f(x, y, gap) \sin(k_{zj} \cdot z + \varphi_i)$$

integration is easily be done for 1 or more period  
Fast tra

Total filed:

$$A_x = \sum_{j=1}^n (C_x \cdot \sin(k_{zj} \cdot z) + D_x \cdot \cos(k_{zj} \cdot z))$$

$$A_y = \sum_{j=1}^n (C_y \cdot \sin(k_{zj} \cdot z) + D_y \cdot \cos(k_{zj} \cdot z))$$



The GF method is implemented in elegant with expansion to universal mode  
–  $\varphi_i$  can be varied freely.

# End\_pole Configuration

- To preserve beam orbit going through undulator unchanged (in linear approximation), the ID field should satisfy following conditions

$$\int B_x dz = 0 \quad \int B_y dz = 0$$
$$\int dz \int B_x dz' = 0 \quad \int dz \int B_y dz' = 0$$

with  $B_x = B_0 \cos(k_z * z + \theta_x)$     $B_y = B_0 \cos(k_z * z + \theta_y)$

which means  $\theta_{x,y} = 0$  or  $\pi$

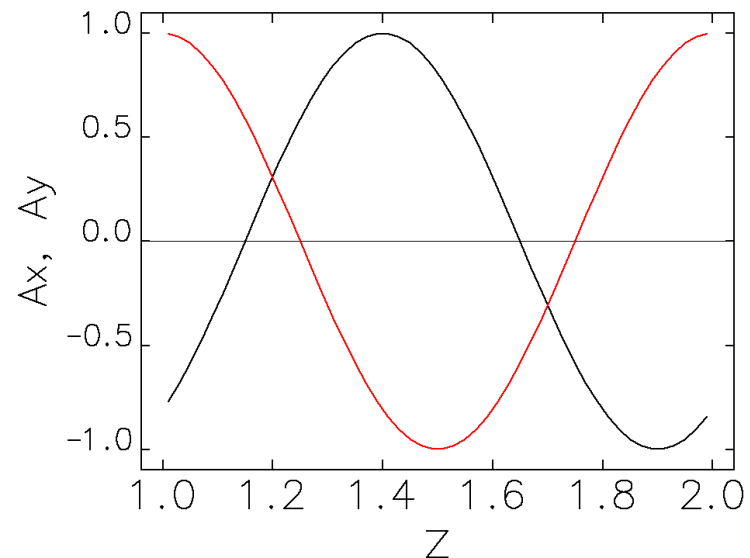
**Ax,y has to be at zero crossing at the entrance and exit**

- The conditions is filled through careful end-poles configuration design
- The simulation routine must preserve this feature



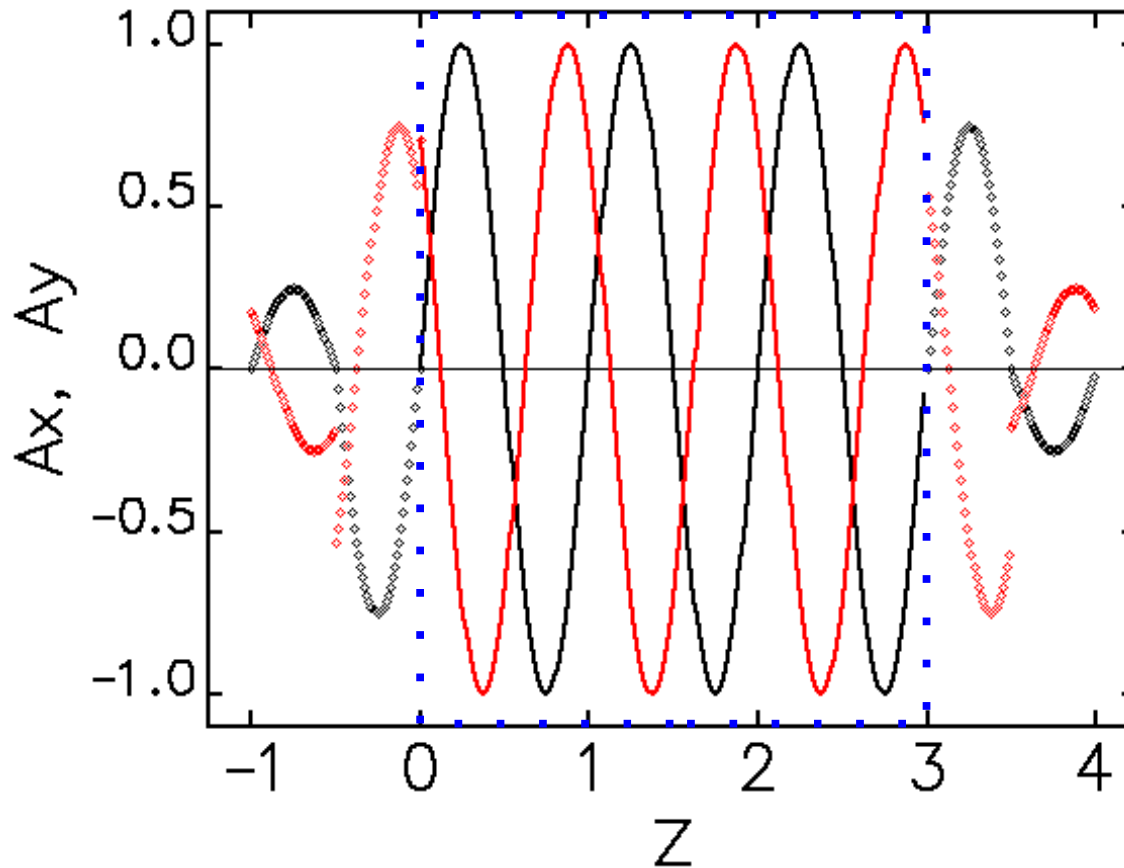
# Simulation of End\_poles

- Universal mode –  $A_x, y$  can not be zero at the same time at any  $z$  location
  - Unmatched beam orbit if only simulate normal poles
- Reduced strength end\_pole approximation (half period)  
0.25, -0.75, 1, -1, ..., 0.75, -0.25
- Replace end\_pole effect with matching section
- Improved end\_pole configuration (future)

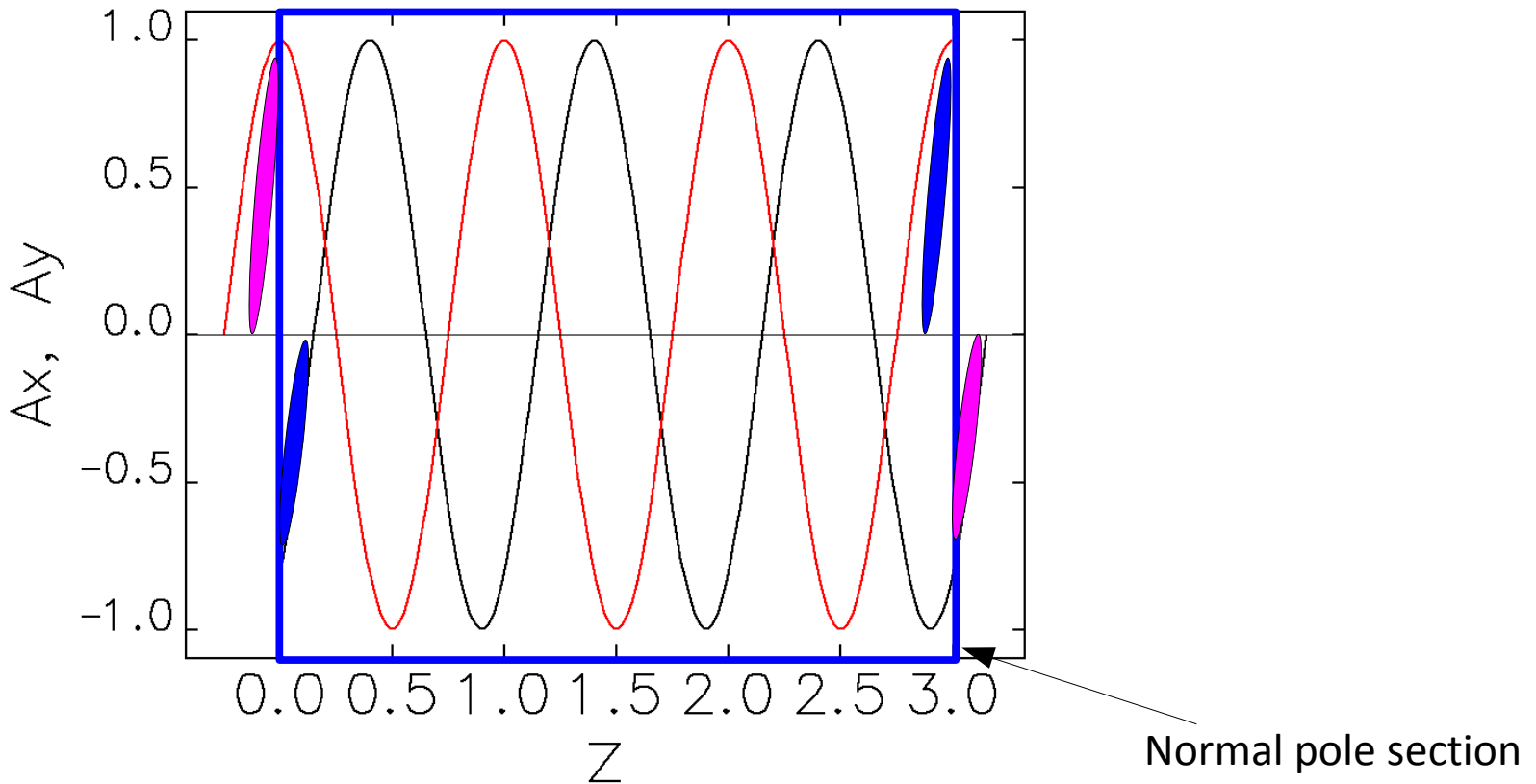


# Reduced Strength End\_pole Approximation

- Easy to implement
- Non-zero  $A_{x,y}$  at entrance/exit and discontinuous function
- Good result agrees with other methods (J. Bahrtdt)



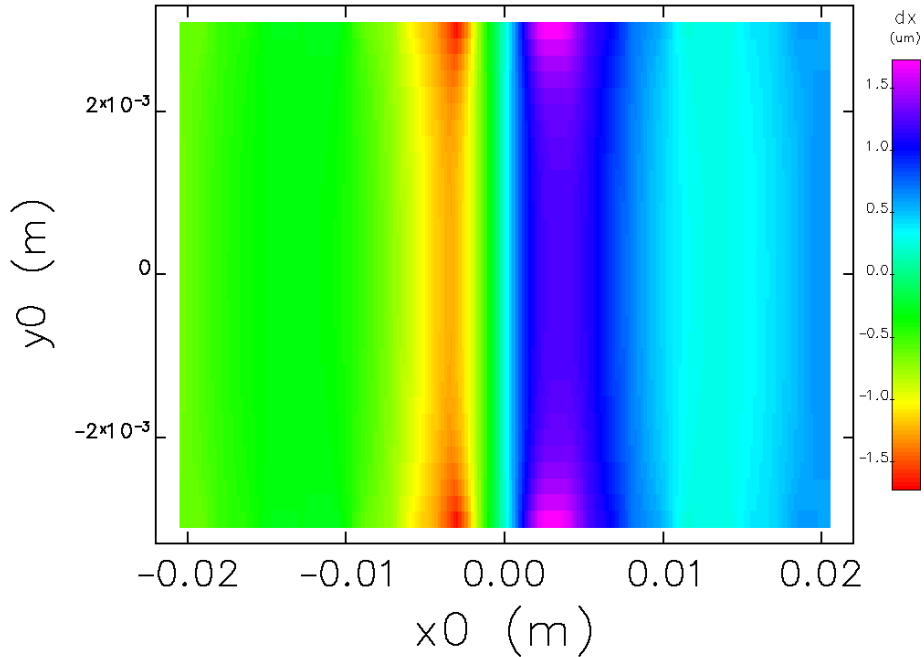
# Replace End\_pole Effects with Matching Section



- Add (red) or remove (blue) part field region at the entrance/exit (also used in CWIGGLER)
- Guaranty orbit match for any polarization mode
- Implementation becomes a little bit harder – calculation of  $dz_x$ ,  $dz_y$  ( $x, y$  dependent)

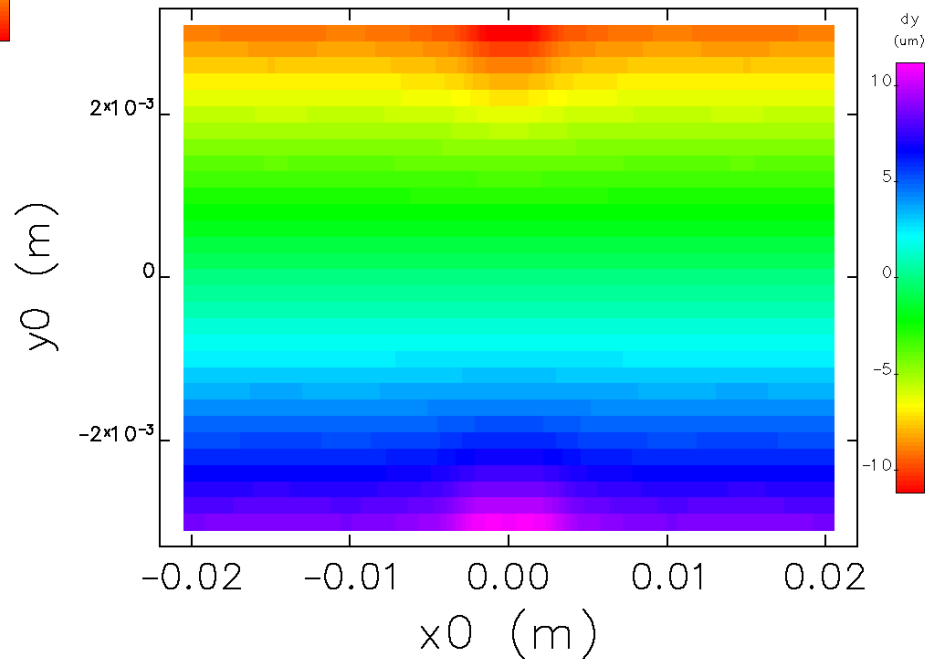
# Simulation Result - Orbit Mismatch

New Model - Orbit Displacement

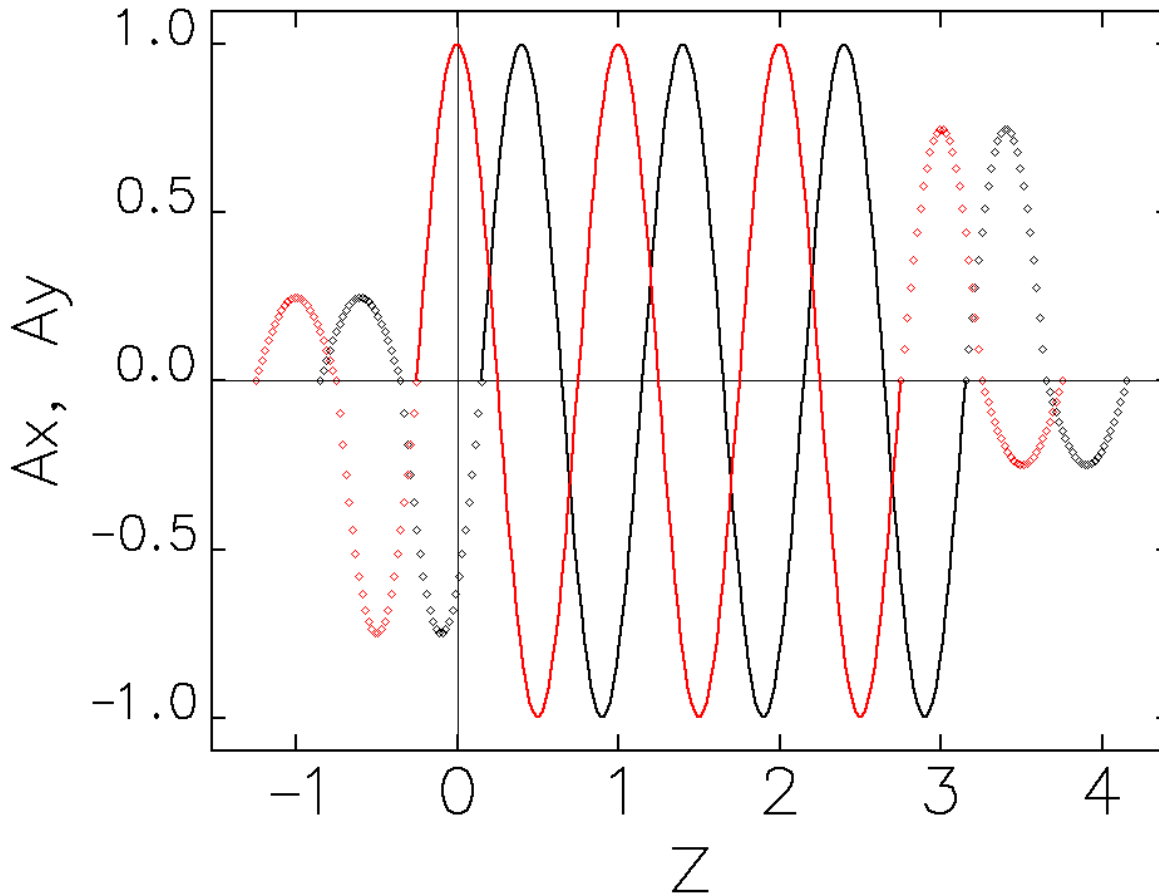


Non-linear effects  
A few micron meters

New Model - Orbit Displacement



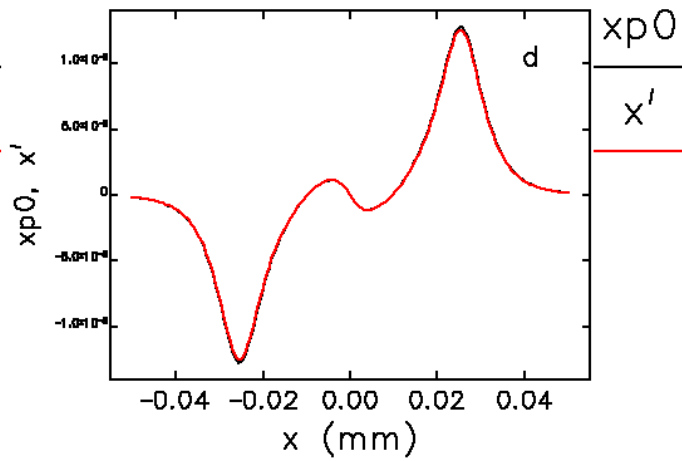
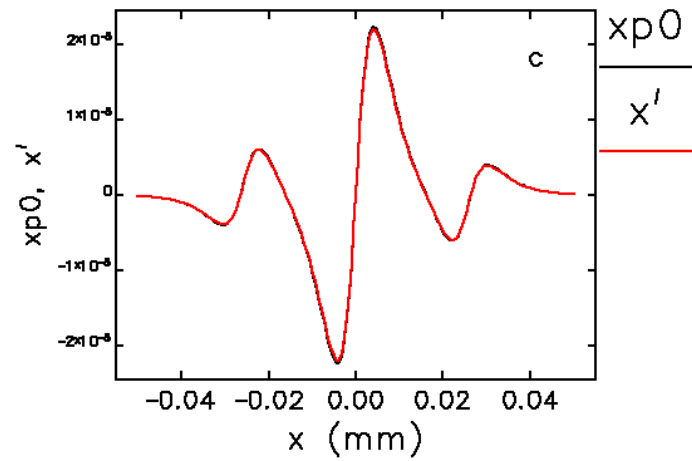
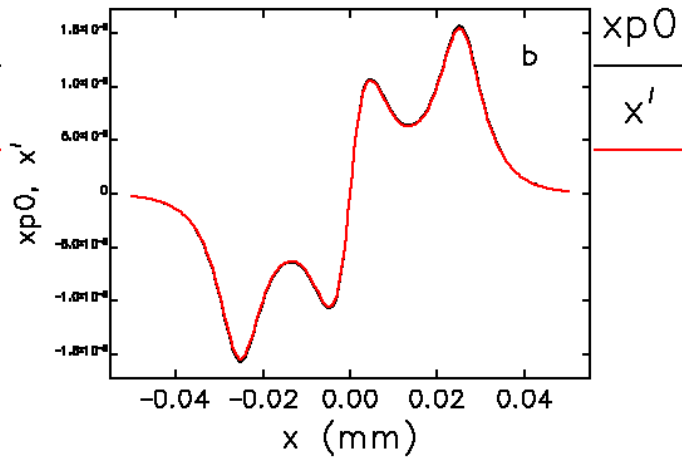
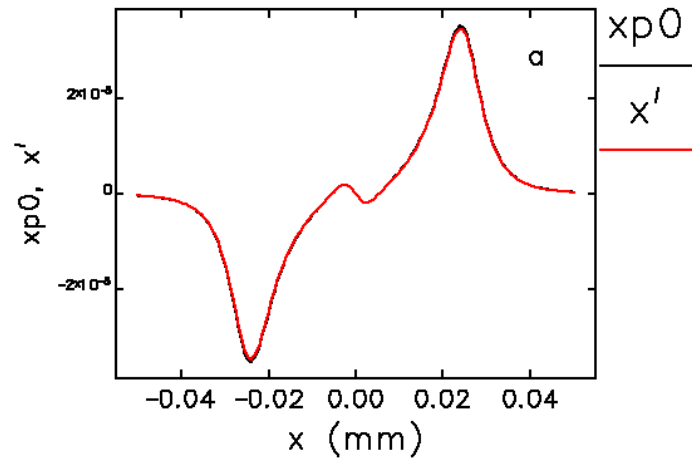
# Improvement (future)



To make model more close to real situation

With/without reduced strength end-pole – only a few percent off of the total kick strength

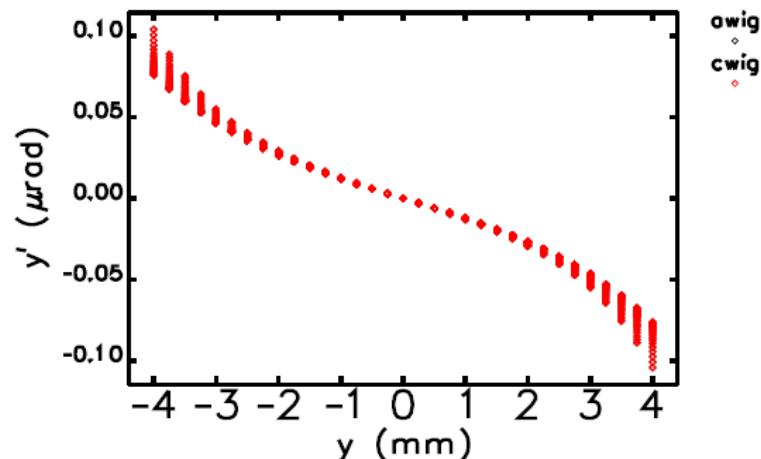
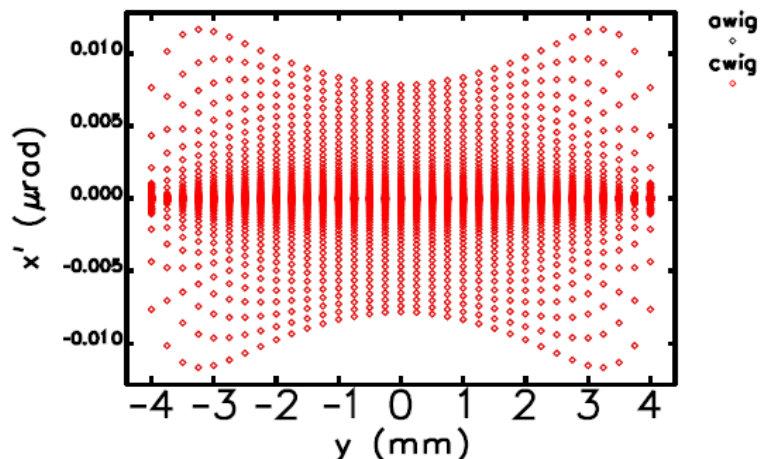
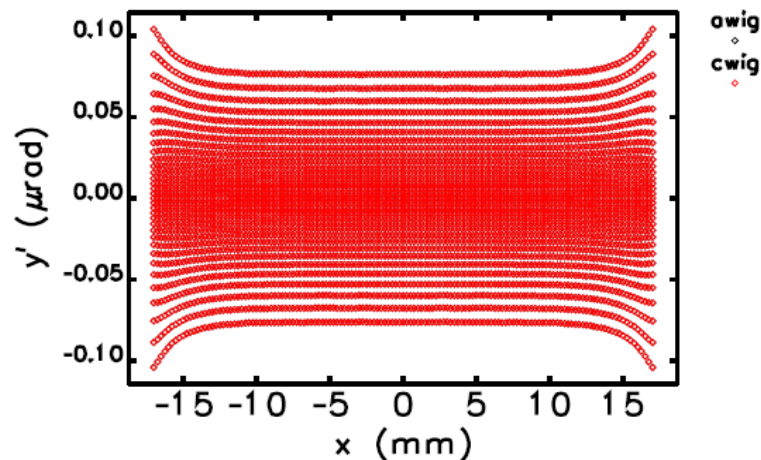
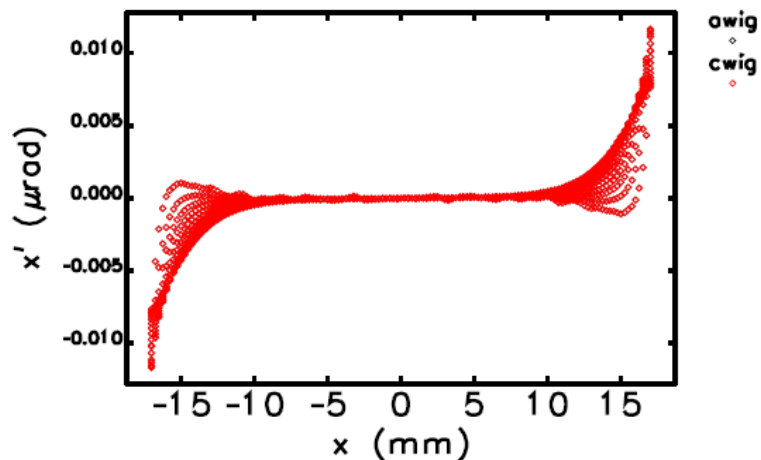
# Benchmark Result - comparing with theoretic value



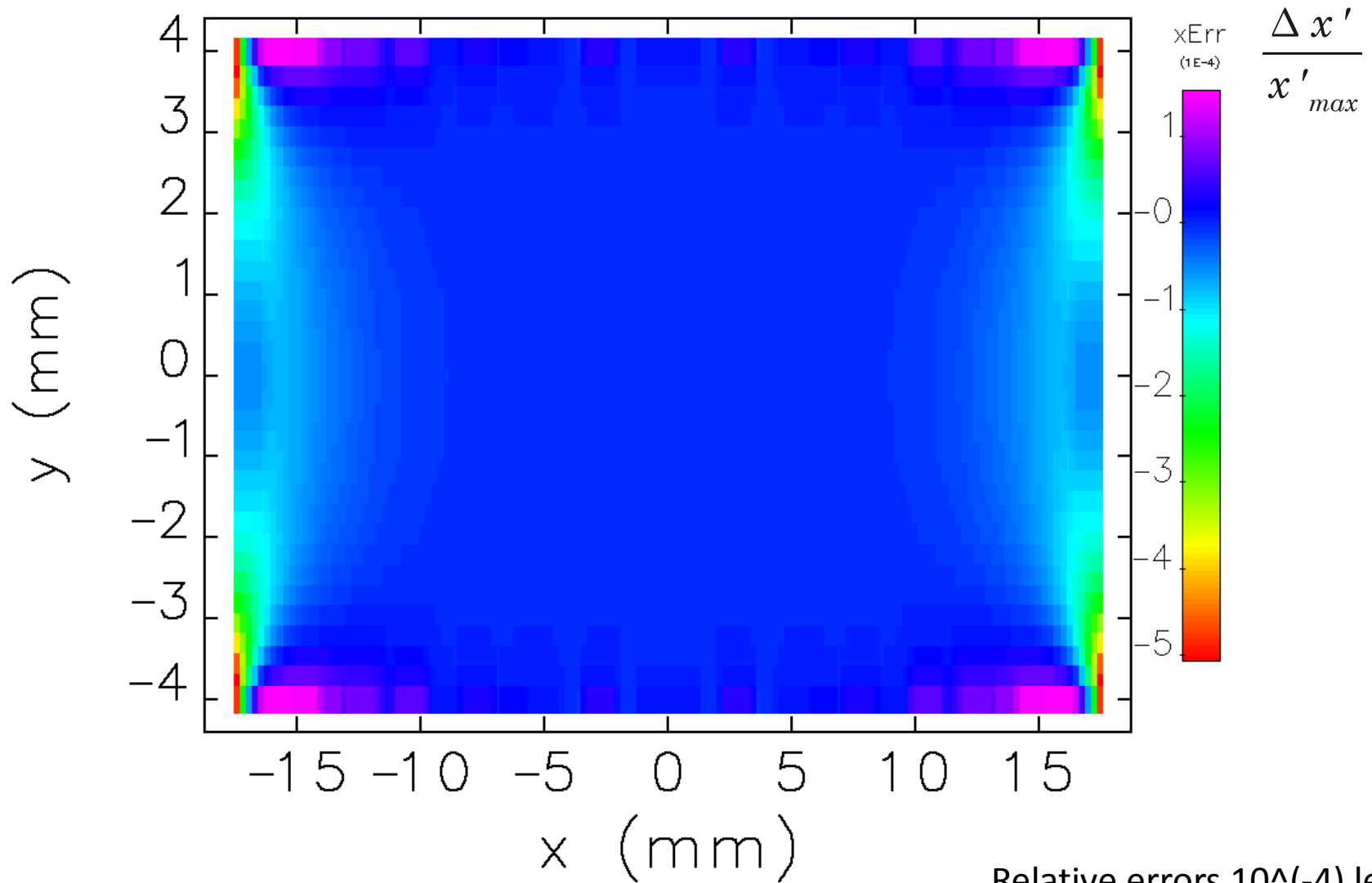
- (a)  $\theta_2 = \theta_4 = 0$
- (b)  $\theta_2 = \theta_4 = \frac{\pi}{2}$
- (c)  $\theta_2 = \theta_4 = \pi$
- (d)  $\theta_2 = -\theta_4 = \frac{\pi}{2}$



# Benchmark Result - comparing with elegant



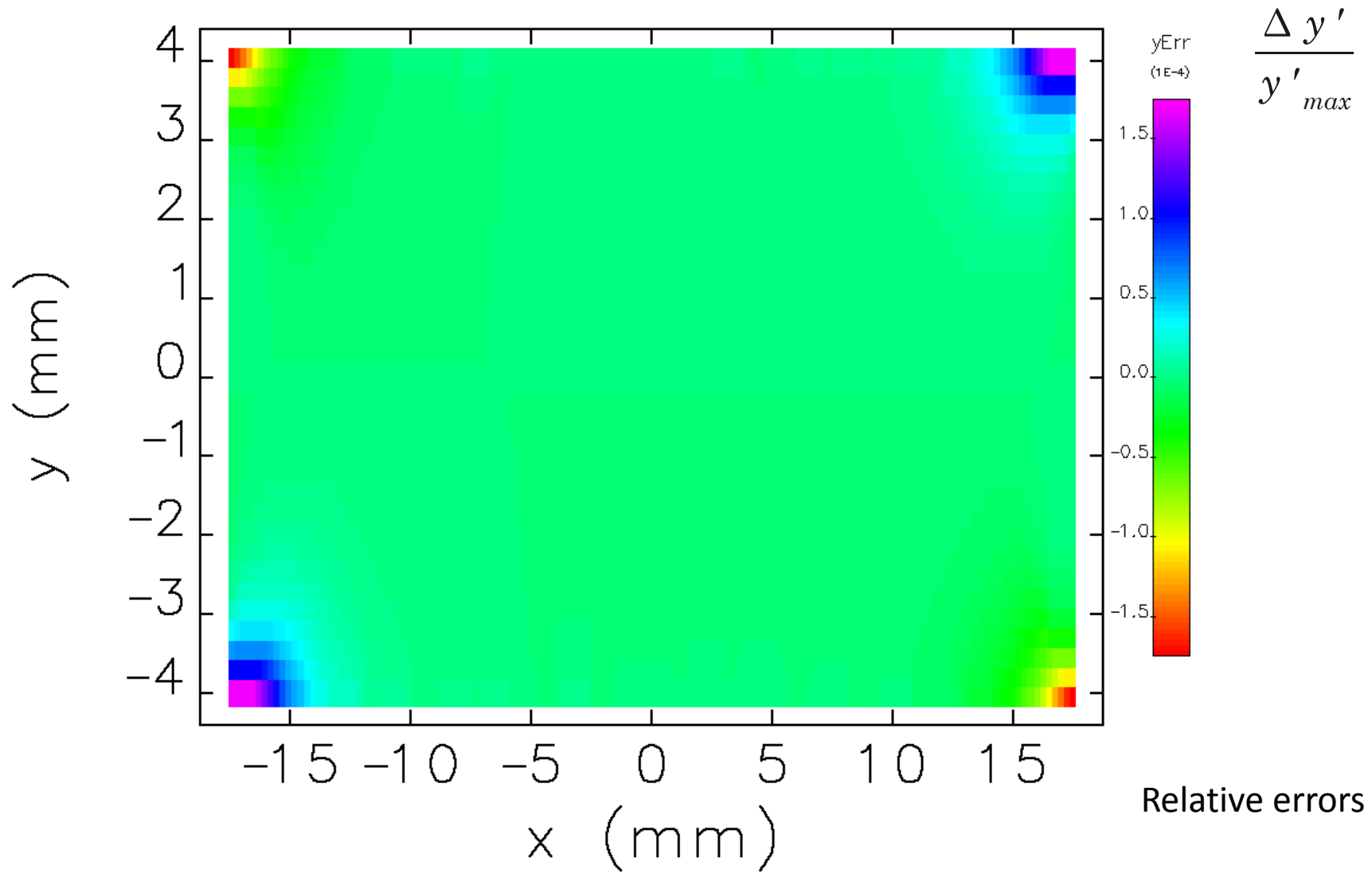
U28 (planar undulator) Black: GF method; red: CWIGGLER (Y. Wu's canonical tracking) method  
Calculation CPU time:  $\sim 30\text{s}$  (GF) vs.  $\sim 30\text{min}$  (CWIGGLER) (first harmonic, 9 step per period)  
CWIGGLER is good: strong wiggler field; rich longitudinal harmonics.



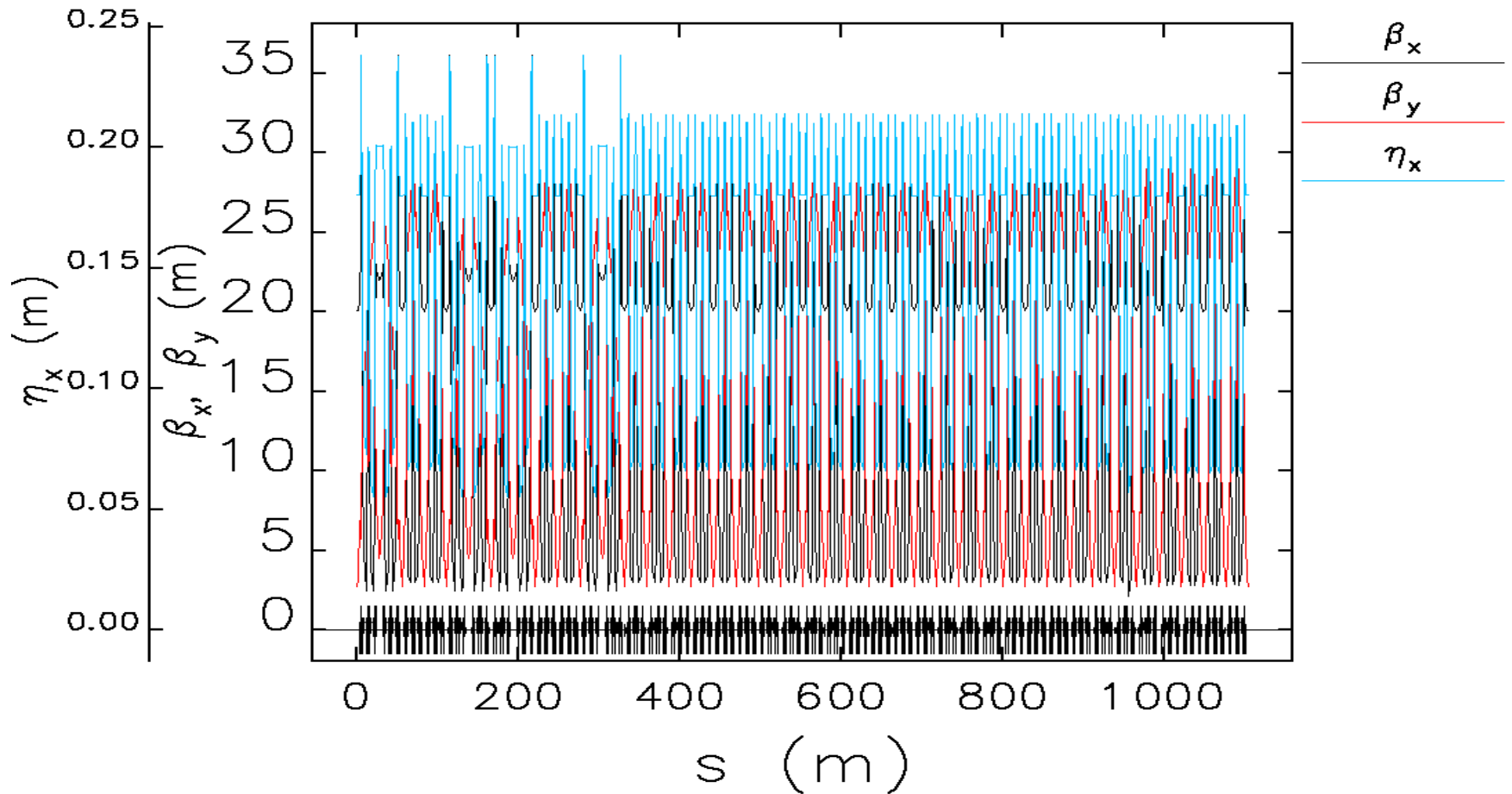
Relative errors  $10^{-4}$  level







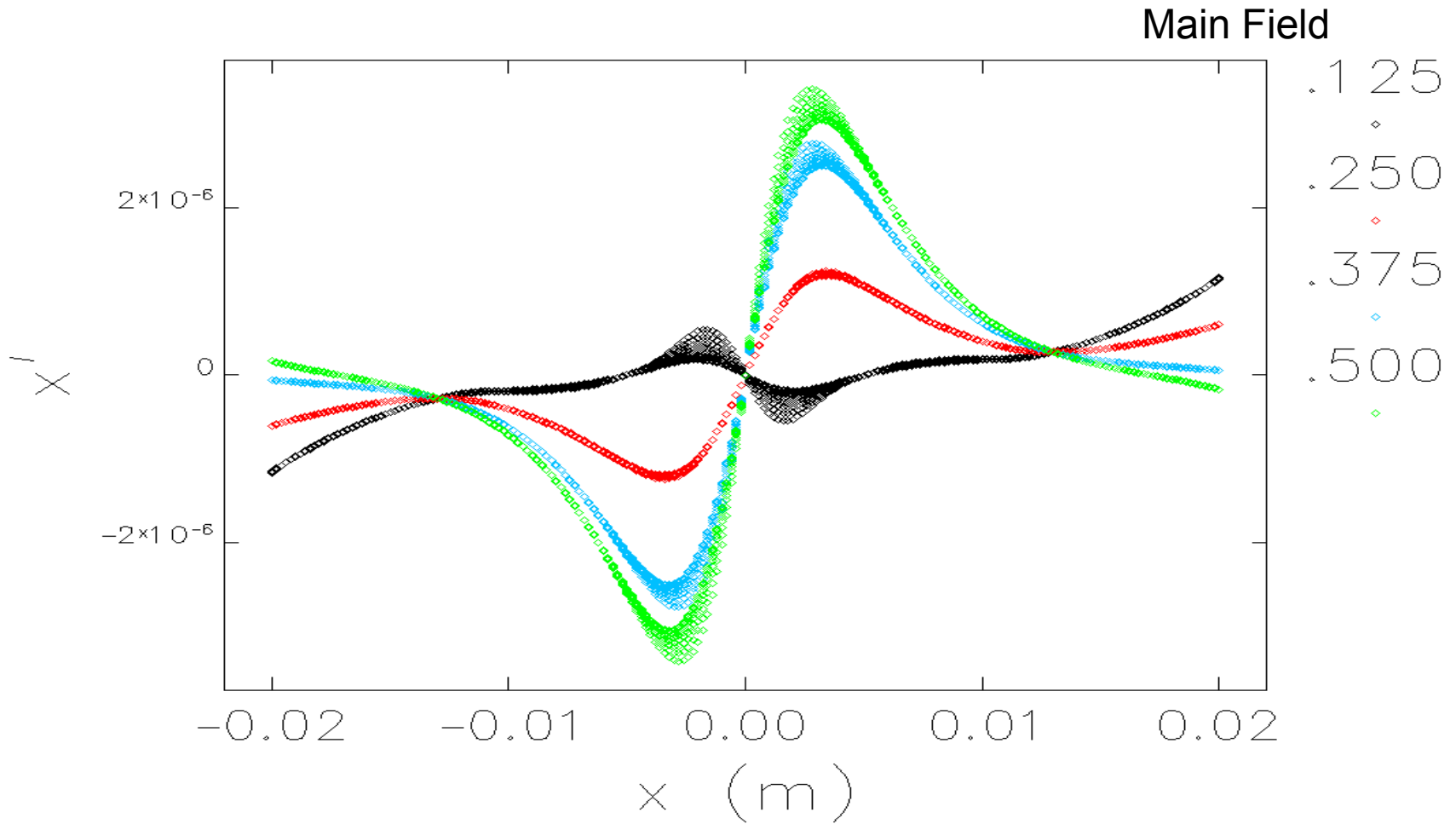
# APS-U Optics



Courtesy by M. Borland

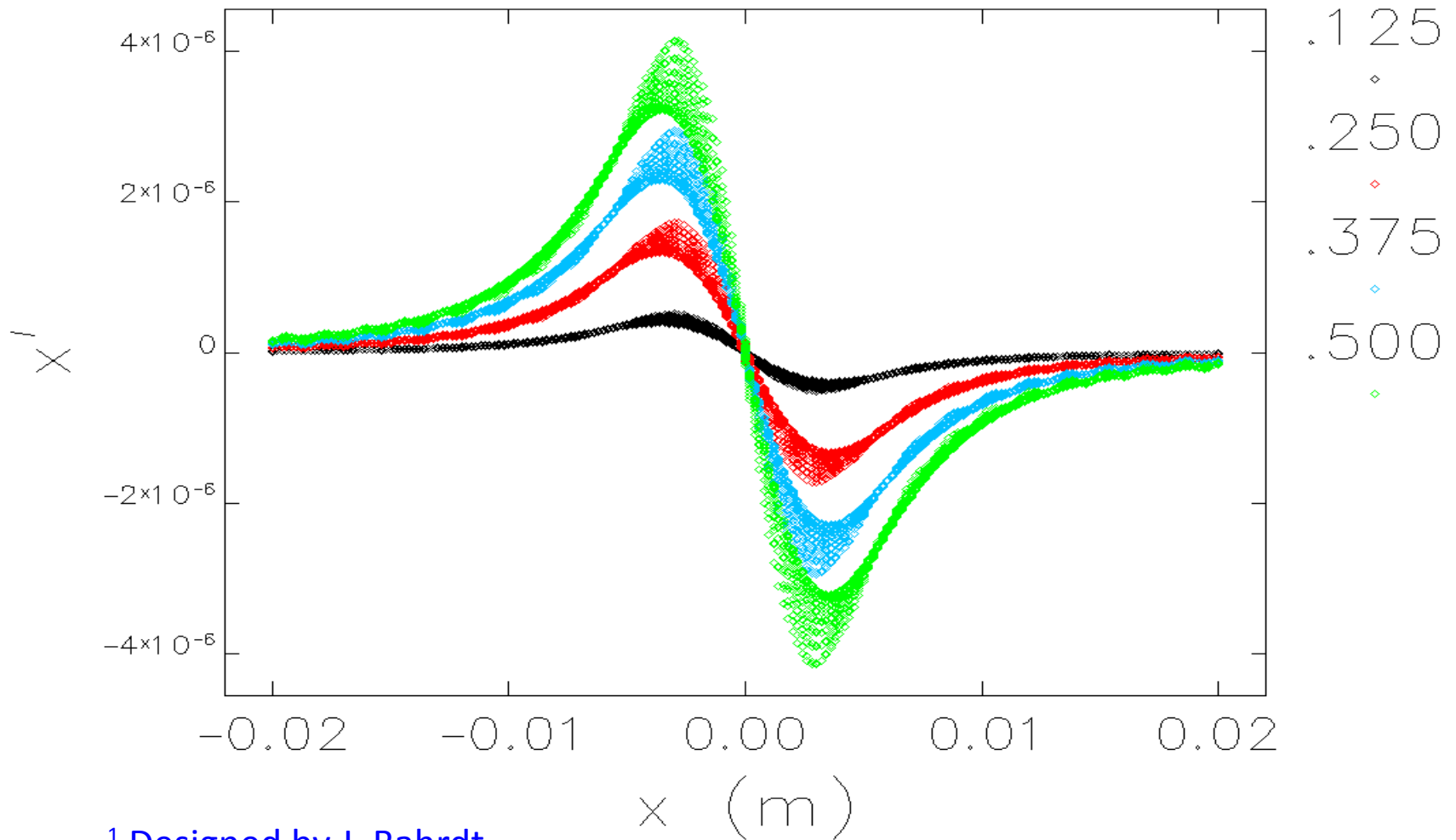


# APPLE ID for APS-U<sup>1</sup>



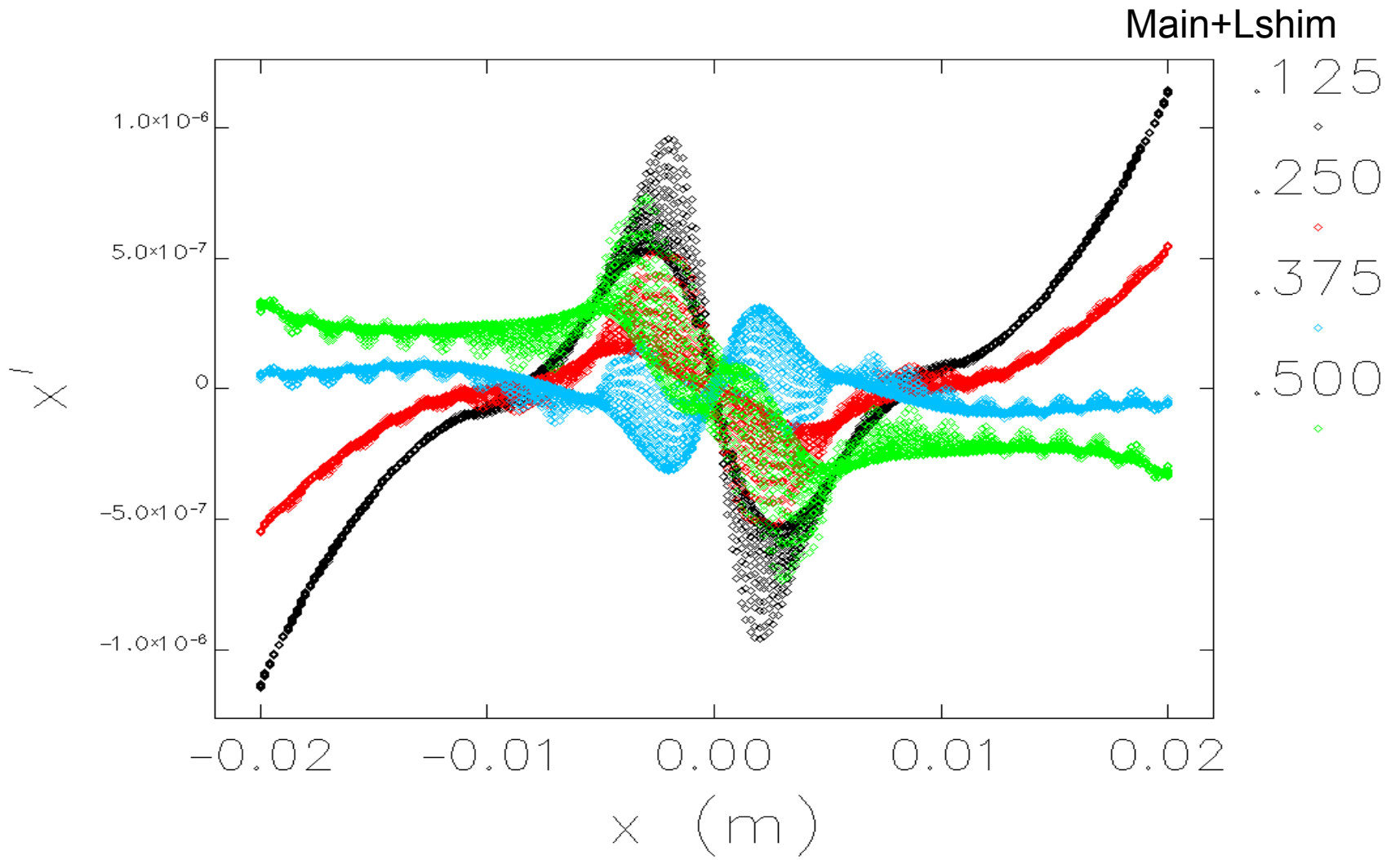
<sup>1</sup> Designed by J. Bahrtdt

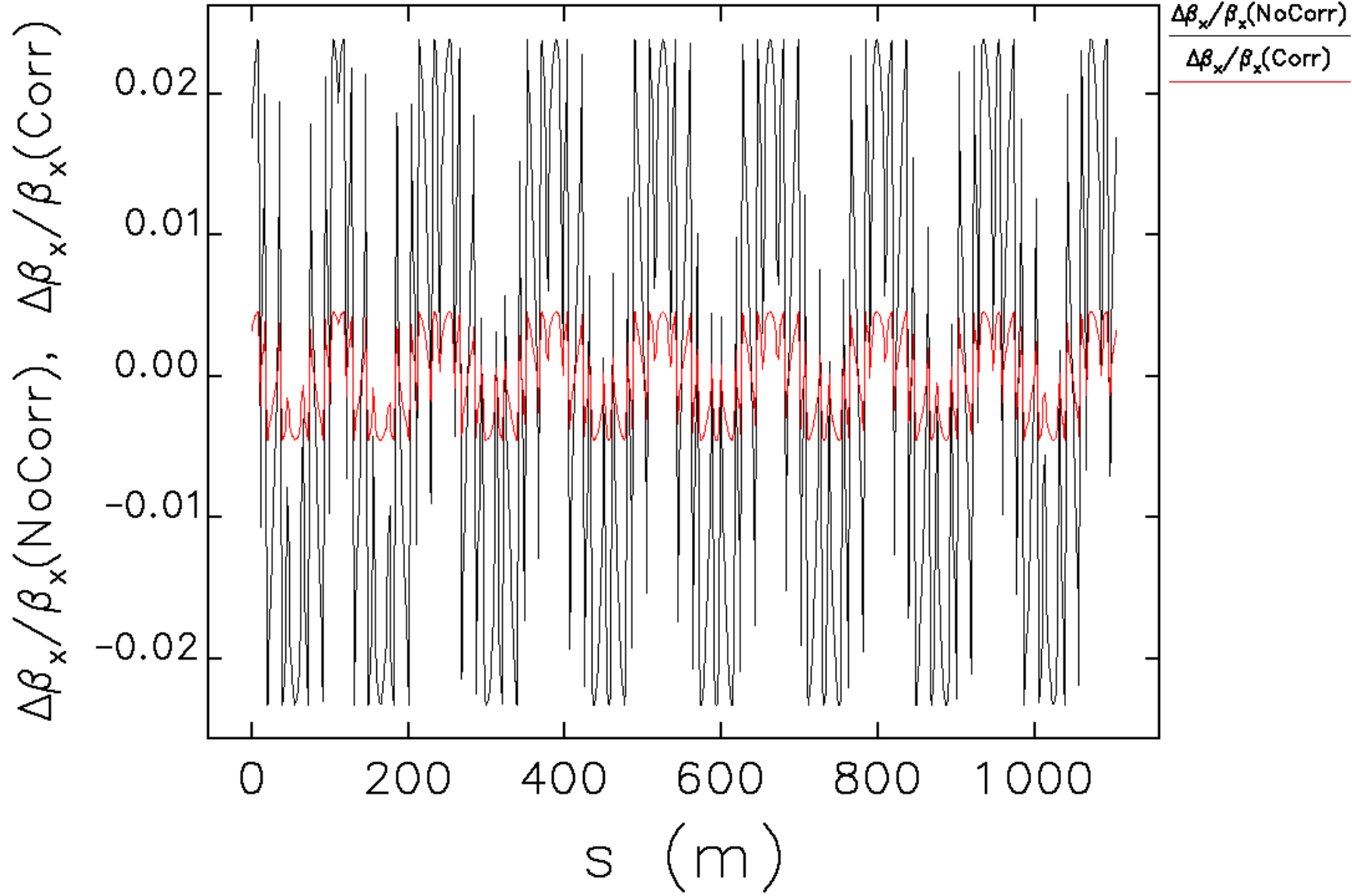
# L-shim

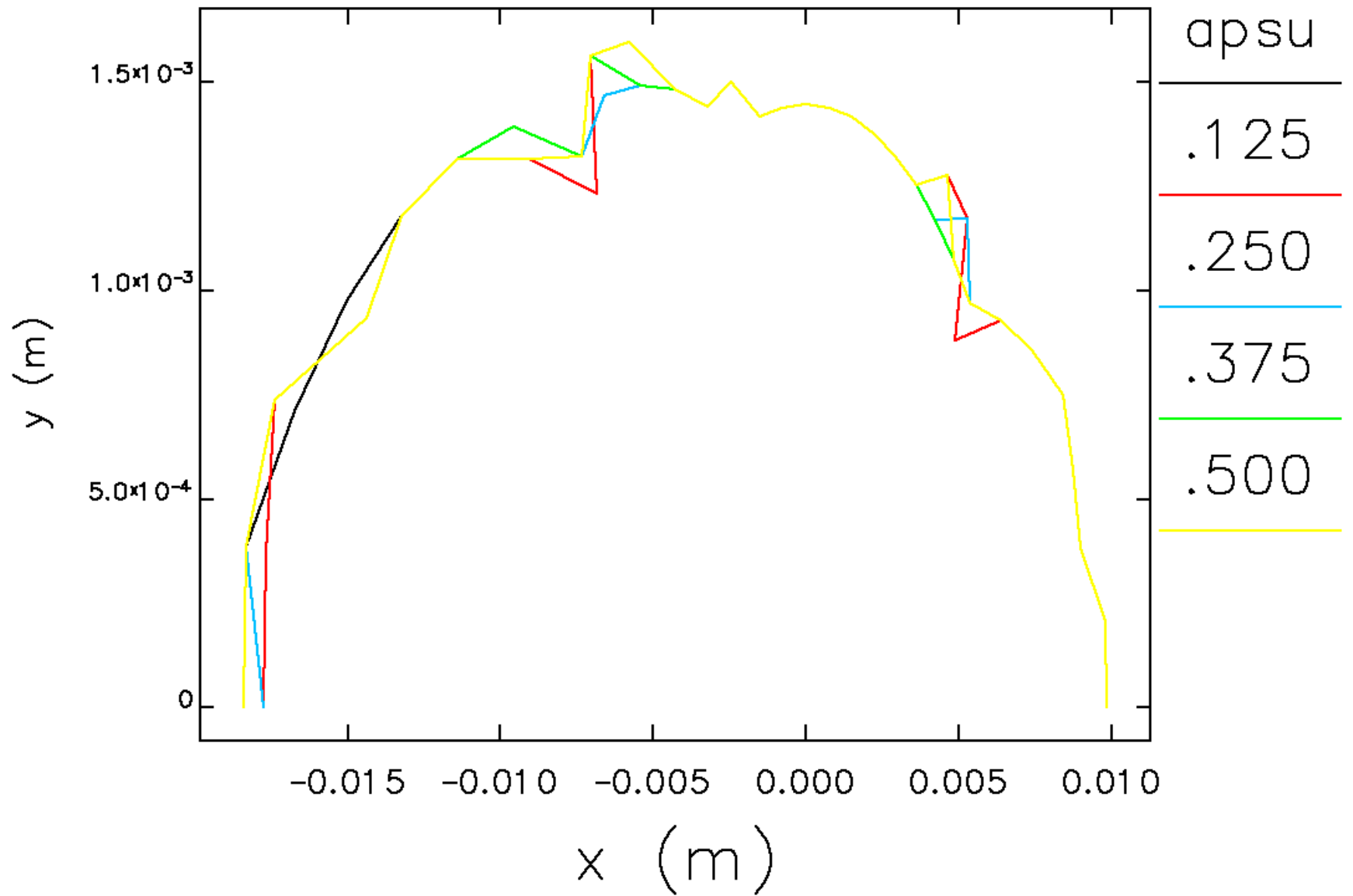


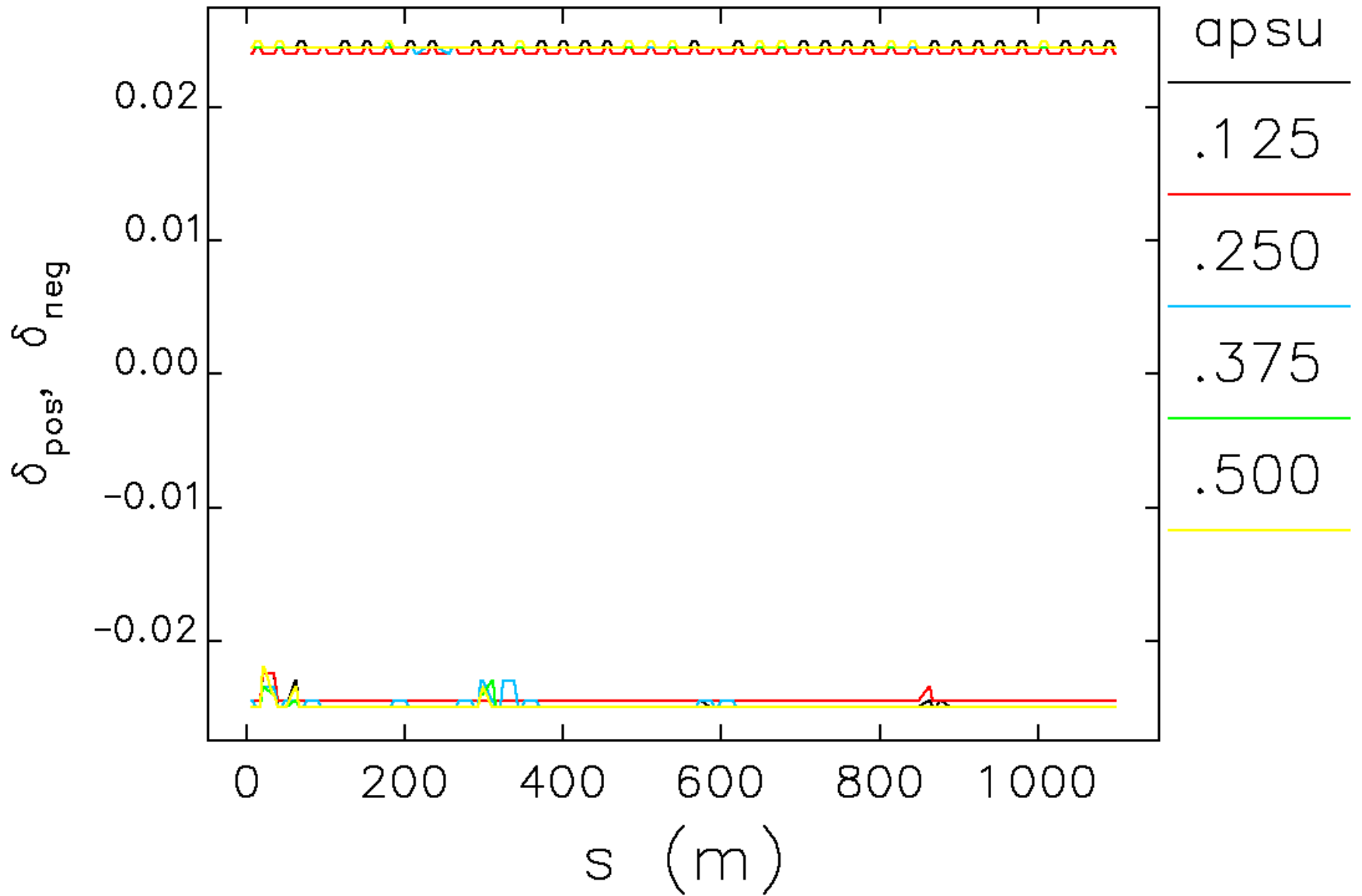
<sup>1</sup> Designed by J. Bahrdt  
Not scaled properly













# Summary

- GF-method + L-shim correction is implemented in elegant
- Applicable to universal mode
- Improved end\_pole effects treatment
- Excellent agreement with other methods
- Fast tracking speed (period field)
- Perturbation to APS-U optics checked

