# Nuclear Structure and Short-Range Correlations (Day 1) Or Hen – MIT

Hampton University Graduate School (HUGS), June 6<sup>th</sup> 2017, JLab, Newport-News VA. Laboratory for Nuclear Science @

Hen/Lab

#### **Course Outline**

Day I: Overview of Nuclear Systems and EM Probes.

**Day II:** Nuclear Structure. (Short / Long Range) (Experiment / Theory)

Day III: Cross Connections.

(QCD in Nuclei: Modification and Transparency) (Contact Formalism and Short-Range Universality) (Neutrino Physics) (Neutron Stars)

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Day I: Overview of Nuclear Systems and EM Probes.

# After today's overview, I want to hear from you what you want to learn!

Theory / Detectors / High energy / low energy

### Modern nuclear physics: From nothing to everything



### This Course: Two Systems and Their Interactions

#### Systems:

- nucleus as a collection of bound protons and neutrons,
- nucleon as a collection of bound quarks.

#### Interactions:

- Nuclear Interactions from quark interactions,
- Nuclear Medium Effects on quarks distributions.



## (Some) Quantities of Interest

#### Nuclear structure:

- Shape (radii / deformation / ...),
- Electro-magnetic charge distribution (form factor),
- Nucleon momentum distribution (wave function),
- Clustering and correlations,

#### Nucleon Structure:

- Nuclear forces from quark interactions
- Quark structure of bound and free nucleons

### Nuclear Challenge



Nuclei are a low energy phenomena, => QCD is non perturbative!



#### Nuclear Many-Body Challenge

#### Many-body Schrödinger Equation

$$\sum_{i} \left\{ -\frac{\hbar^2}{2m_i} \nabla_i^2 \Psi(\vec{r}_1, \dots, \vec{r}_N, t) \right\} + U(\vec{r}_1, \dots, \vec{r}_N) \Psi(\vec{r}_1, \dots, \vec{r}_N, t) = i\hbar \frac{\partial}{\partial t} \Psi(\vec{r}_1, \dots, \vec{r}_N, t)$$

#### Main Challenges:

- 1. No 'fundamental' Interaction.
- 2. Complex phenomenological parametrizations (e.g. over 18 operators)





#### **Solution: Effective Theories**



\* Should converge to exact solution

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\* Should converge to exact solution

- **<u>Goal</u>**: Study the internal structure (and dynamics) of complex objects
- Means: using high energy lepton scattering
- Reaction determined by two variables:
  - $Q^2 = -q^2$  Interaction-Scale
  - $x_B = Q^2/(2m_pv)$  Dynamics





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**Goal:** Study the internal structure (and dynamics) of complex objects

**Means:** using high energy lepton scattering

100s eV – 100s keV: Material structure





**<u>Goal</u>:** Study the internal structure (and dynamics) of complex objects

**Means:** using high energy lepton scattering



#### Worldwide Effort





#### **Postcard collection**







### (e,e'): Energy transfer defines physics



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#### Everything is interesting...



#### ...But we will focus on 3 regions





#### 1. Elastic

- structure of the nucleon / nucleus
  - Form factors, charge distributions, spin dependent FF

#### 2. Quasielastic (QE)

- Shell structure
  - Momentum distributions
  - Occupancies
- Short Range Correlated nucleon pairs
- Nuclear transparency and color transparency
- 3. Deep Inelastic Scattering (DIS)
  - The EMC Effect and Nucleon modification
  - Quark hadronization in nuclei

### **Quick Overview: Elastic**



- Nuclear charge (proton) radius
- Nuclear Neutron radius
- Nucleon Form-Factors and charge densities







incoming e-

 $\rightarrow \theta = 32.8^{\circ}$ Electron energy = 454.3 MeV  $\rightarrow$   $\lambda = 2.73 \text{ fm}$ 

Calculated radius = 3.07 fm

Measured rms radius = 3.19 fm





### Weak Interaction: Neutron Distribution





Applications of PV at Jefferson Lab

- Nucleon Structure (strangeness) -- HAPPEX / G0
- Standard Model Tests (  $\sin^2 \theta_W$ ) -- e.g. Qweak



Nuclear Structure (neutron density) : PREX

#### Weak Interaction: Neutron Distribution



#### **Clean Probe Couples Mainly to Neutrons**

	proton	neutron
Electric charge	1	0
Weak charge	80.0	1

#### Weak Interaction: Neutron Distribution



#### **Clean Probe Couples Mainly to Neutrons**

	proton	neutron
Electric charge	1	0
Weak charge	0.08	1

High Accuracy:

$$\frac{dA}{A} = 3\% \quad \rightarrow \quad \frac{dR_n}{R_n} = 1\%$$

 $R_n$  = neutron matter radius

#### From Intuition to Formalism

Lab frame kinematics

**Invariants:**   $p^{\mu}p_{\mu} = M^2$   $Q^2 = -q^{\mu}q_{\mu} = |\vec{q}|^2 - \omega^2$  $W^2 = (q^{\mu} + p^{\mu})^2 = p'_{\mu}p'^{\mu}$ 

#### From Intuition to Formalism (Elastic)

Recoil factor  

$$\frac{d\sigma}{d\Omega} = \sigma_M \frac{E}{E} \left\{ \left[ F_1^2(Q^2) + \frac{Q^2}{4M^2} \kappa^2 F_2^2(Q^2) \right] + \frac{Q^2}{2M^2} [F_1(Q^2) + \kappa F_2(Q^2)]^2 \tan^2 \frac{\theta}{2} \right\}$$

$$= \sigma_M \frac{E}{E} \left[ \frac{G_E^2(Q^2) + \tau G_M^2(Q^2)}{1 + \tau} + 2\tau \tan^2 \frac{\theta}{2} G_M^2(Q^2) \right]$$

$$= \sigma_M \frac{E}{E} \left[ \frac{Q^4}{q^4} R_L(Q^2) + \left( \frac{Q^2}{2q^2} + \tan^2 \frac{\theta}{2} \right) R_T(Q^2) \right]$$
Mott cross section:  $\sigma_M = \frac{\alpha^2 \cos^2 \left( \frac{\theta_e}{2} \right)}{4E^2 \sin^4 \left( \frac{\theta_e}{2} \right)}$ 

 $\begin{array}{l} \label{eq:posterior} \begin{tabular}{l} \label{eq:posterior} \end{tabular} P_1, \end{tabular} F_1, \end{tabular} F_2: \end{tabular} \e$ 

#### Form Factors: Cross-Sections



#### Form Factors: Polarization Transfer






#### Form Factors: Polarization Transfer

$$I_{0}P_{x} = -2\sqrt{\tau(1+\tau)}G_{E}G_{M}\tan(\theta/2)$$
$$I_{0}P_{z} = \frac{1}{M}(E-E')\sqrt{\tau(1+\tau)}G_{M}^{2}\tan^{2}(\theta/2)$$

$$\frac{G_E^2}{G_M^2} = \frac{-P_x}{P_z} \frac{E+E'}{2M} \tan(\theta/2)$$



#### **LARGE Discrepancy!**

(2 photon exchange? More on this if we have time at the end)



Neutron is negative in its center and positive in the edge!!!



## Quick Overview: Quasi-Elastic



- Momentum Densities: Fermi Gas
- Y-Scaling
- Shell Structure and spectroscopic factors



## What is a Nucleus ?



# Fermi gas model: how simple a model can you make ?

Initial nucleon energy:  $KE_i = p_i^2 / 2m_p$ Final nucleon energy:  $KE_f = p_f^2 / 2m_p = (\vec{q} + \vec{p}_i)^2 / 2m_p$ Energy transfer:  $v = KE_f - KE_i = \frac{\vec{q}^2}{2m_p} + \frac{\vec{q} \cdot \vec{p}_i}{m_p}$ Expect: •Peak centroid at  $v = q^2/2m_p + \varepsilon$ 

e'

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- •Peak width  $2qp_{\text{fermi}}/m_{\text{p}}$
- •Total peak cross section =  $Z\sigma_{ep} + N\sigma_{en}$



#### Scaling

•The dependence of a cross section, in certain kinematic regions, on a single variable.

- •scaling validates the scaling assumption.
- •Scale-breaking indicates new physics.

•At moderate Q<sup>2</sup> and x>1 we expect to see evidence for y-scaling, indicating that the electrons are scattering from quasifree nucleons

• y = minimum momentum of struck nucleon

•At high  $Q^2$  we expect to see evidence for x-scaling, indicating that the electrons are scattering from quarks.

•x =  $Q^2/2mv$  = fraction of nucleon momentum carried by struck quark (in infinite momentum frame)



Assumption: scattering takes place from a quasi-free proton or neutron in the nucleus.

y is the momentum of the struck nucleon parallel to the momentum transfer:  $y \approx -q/2 + mv/q$  (nonrelativistically)

IF the scattering is quasifree, then F(y) is the integral over all perpendicular nucleon momenta (nonrelativistically).

Goal: extract the momentum distribution n(k) from F(y).

# Assumptions & Potential Scale Breaking Mechanisms

- No Final State Interactions (FSI)
- No internal excitation of (A-1)
- Full strength of Spectral function can be integrated over at finite *q*
- No inelastic processes (choose y<0)</li>
- No medium modifications (discussed later)



Final State Interactions (FSI) complicate this simple picture



Benhar et al. PRC 44, 2328 Benhar, Pandharipande, PRC 47, 2218 Benhar et al. PLB 3443, 47

# But what about the Shell Model?

• Many-Body Hamiltonian:

$$H = \sum_{i=1}^{A} \frac{p^2}{2m_N} + \sum_{i < j=1}^{A} v_{2body}(i, j) + \sum_{i < j < k=1}^{A} v_{3body}(i, j, k) + \dots$$

• Mean-Field Approximation:

 $H = \sum_{i=1}^{A} \frac{p^2}{2m_N} + \sum_{i=1}^{A} V(i)$ 

- Results in an "atom-like" shell model:
  - Ground state energies
  - Excitation Spectrum
  - Spins
  - Parities







(response functions, that is)

(When you include electron and proton spin, there are 18!)

(And if you scatter from a polarized spin-1 target, there are 41. Double Yikes!!)

where



# <sup>16</sup>O(e,e'p) and shell structure



 $1p_{1/2},\,1p_{3/2}$  and  $1s_{1/2}$  shells visible

Momentum distribution as expected for /= 0, 1 Fissum et al, PRC <u>70</u>, 034606 (2003)

#### But we do not see enough protons!

NIKHEF



#### But we do not see enough protons! (More to come...)



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## Quick Overview: Deep Inelastic



- Structure Functions
- EMC Effect





#### Partonic Structure



# **Partonic Structure:** $F_2(x,Q^2) = \sum_i e_i^2 \cdot x \cdot f_i(x)$



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$$\frac{d^2\sigma}{d\Omega dE'} = \sigma_A = \frac{4\alpha^2 E'^2}{Q^4} \left[ 2\frac{F_1}{M} \sin^2\left(\frac{\theta}{2}\right) + \frac{F_2}{V} \cos^2\left(\frac{\theta}{2}\right) \right]$$

## Partonic – Nucleonic Interplay



Quark – Anti-quark Pair 00000 Gluon Quark



**Quiz:** What is the *simplest* example of nuclear interaction affecting partonic properties?

(winner gets a beer)



**Quiz:** What is the *simplest* example of nuclear interaction affecting partonic properties?

#### Answer:

The nuclear interaction that binds the deuteron also makes the neutron stable.

- Simplest nuclear system = Deuteron,
- Free neutron is unstable: decays in ~ 10 minuets,
- Bound in the Deuteron, a neutron can live forever!

# Interplay Challenge: 'Strength 'Scales



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## **EMC Effect**

- Deviation of the per-nucleon DIS cross section ratio of nuclei relative to deuterium from unity.
- Universal shape for 0.3<x<0.7 and 3<A<197.
- ~Independent of Q<sup>2</sup>.
- Overall increasing as a function of A.
- No fully accepted theoretical explanation.



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### **EMC: Nuclear Effect on Partons**



# Theory: 1000 papers, 3 Ideas

#### 1. Proper treatment of 'known' nuclear effects

[explain some of the effect, up to x≈0.5. Sensitive to SRCs]

- Nuclear Binding and Fermi motion, Pions, Coulomb Field.
- No modification of bound nucleon structure.

#### 2. Bound Nucleons are 'larger' than free nucleons.

- Larger confinement volume => slower quarks.
- Mean-Field effect.
- Momentum Independent.
- Static.

#### 3. Short-Range Correlations

- Beyond the mean-field.
- Determined by SRC pairs counting.
- Dynamical!

#### EMC – Everyone's Model is Cool (G. A. Miller)

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#### **Summary (1):** Modern nuclear physics -From nothing to everything



## Summary (2): Today's overview

Elastic scattering (Form Factors, FF):

- Nuclei + virtual photon
- Nuclei + Z boson
- Nucleons + virtual photon => Nucleon charge FF
- Nucleons + Z boson

- => Nuclear charge FF
- => Nuclear neutron FF
- => Nucleon strange FF + ...

Quasielsatic scattering:

- Scaling and momentum distributions
- Shell structure and spectroscopic factors
- Correlations
- ...

**Deep Inelastic Scattering:** 

- Nucleons => Structure functions and PDFs
- Nuclei => In-medium structure functions and nuclear PDFs

### Summary (3): Never mix between what we Know / Measure / Reconstruct / Extract

- Know:
  - Beam probe (particle type + energy)
  - Target
- Measure:
  - Scattered probe
  - Additional particles emitted
  - Cross-sections
- Reconstruct:
  - Short Lived particles
  - Missing momentum
  - Missing Energy
- Extract:
  - Physics! (momentum distribution, shell occupancies ...)
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- Extract:

• Physics! (momentum distribution, shell occupancies ...)

Increasing level of assumptions (i.e. model dependencies)

# **Tomorrow:** Short-Range nuclear Structure

#### Theory:

- 1. Beyond the mean-field: NN Correlations,
- 2. Effective vs. ab-initio calculations
- 3. Phase-equivalent NN interactions
- 4. Reaction theory: confronting theory and experiment.

### **Experiment:**

- 1. (e,e'), (e,e'N), (e,e'NN) => Details of NN correlations,
- 2. Correlations in asymmetric nuclei,
- 3. NN interactions at short distances.

#### **Contact Formalism: Effective theory for short-distance.**