

QUANTUM NUMBERS OF

Θ^+ through the $K^+p \rightarrow \pi^+K^+n$ reaction

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- Most present theories of reactions creating the Θ^+ contain a fair amount of unknown parameters

- The $KN \rightarrow K\pi N$ reaction is well studied theoretically
 Θ^+ can appear through KN final state interaction

The production cross sections depend upon I, J, P of the Θ^+ . In particular, the polarization observables

MODEL:

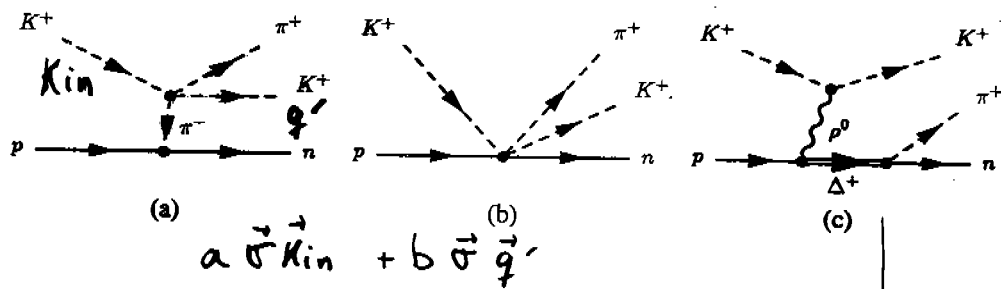


Figure 1: Feynman diagrams of the reaction $K^+p \rightarrow \pi^+K^+n$ in the model of Ref. [15].

$$\vec{S}_{P_\pi} \vec{S}_{P_p} \rightarrow \frac{2}{3} \vec{P}_\pi \vec{P}_p - \frac{i}{3} (\vec{P}_\pi \times \vec{P}_p) \vec{\sigma}$$

non spin-flip \uparrow

If we select $\vec{p}_{\pi^+} \approx 0$
then only spin-flip amplitude

K^+n rescattering

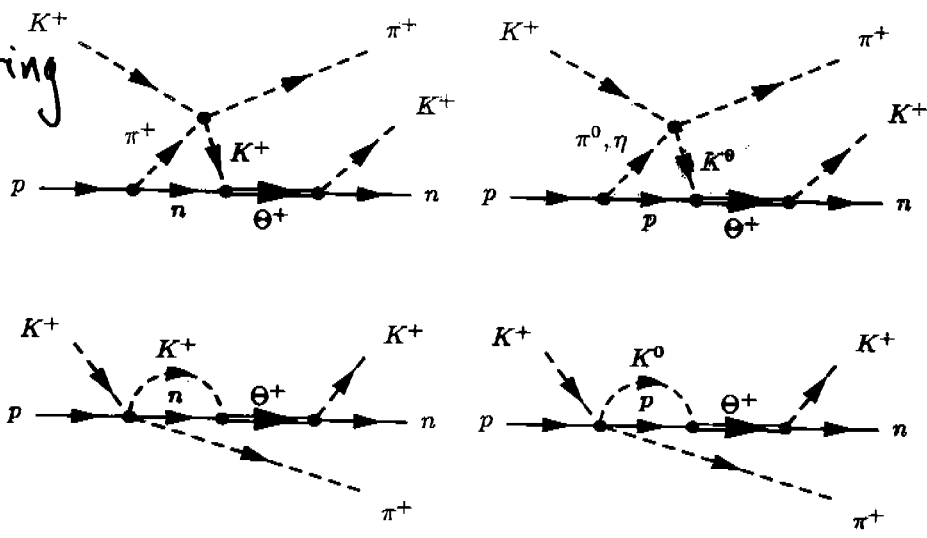
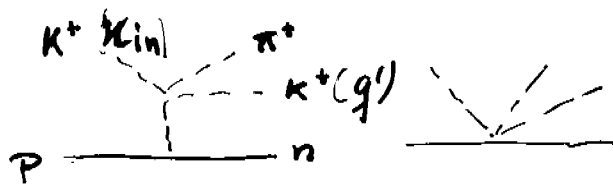


Figure 2: Feynman diagrams of the reaction $K^+p \rightarrow \pi^+K^+n$ with the Θ^+ resonance.

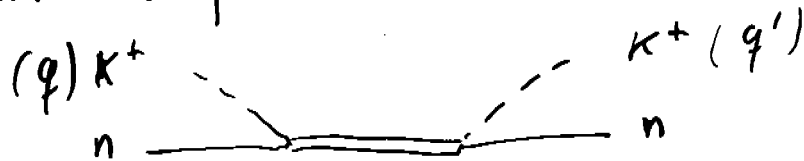
- Tree level amplitudes



evaluated using
the meson-meson
and meson baryon chiral Lagrangians

$$-it = a \vec{\sigma} \cdot \vec{k}_{in} + b \vec{\sigma} \cdot \vec{q}'$$

- KN resonant amplitude



$$t^{(s)} = \frac{g_{K^+n}^2}{M_I - M_R + i \frac{\Gamma}{2}}$$

(-) sign if
 $K^0 p \rightarrow K^+ n$

and $I=0$

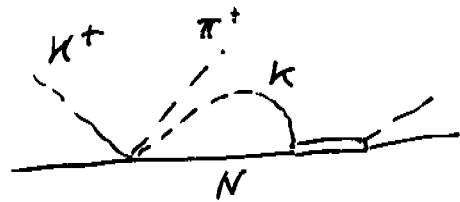
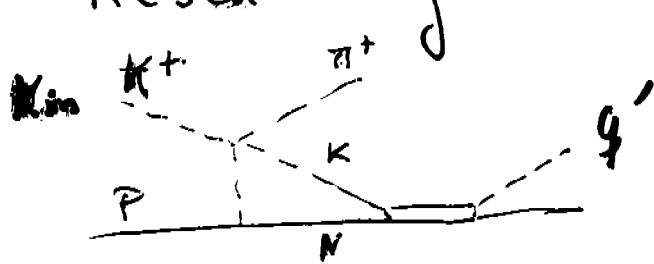
$$t^{(p)} = \frac{\bar{g}_{K^+n}^2 \vec{\sigma} \cdot \vec{q}' \vec{\sigma} \cdot \vec{q}}{M_I - M_R + i \frac{\Gamma}{2}}$$

$$t^{(p, 3/2)} = \frac{\tilde{g}_{K^+n}^2 \vec{S} \cdot \vec{q}' \vec{S} \cdot \vec{q}}{M_I - M_R + i \frac{\Gamma}{2}}$$

$$g_{K^+n}^2 = \frac{\pi M_R \Gamma}{M_q} ; \bar{g}_{K^+n}^2 = \frac{\pi M_R \Gamma}{M_q^3} ; \tilde{g}_{K^+n}^2 = \frac{3\pi M_R \Gamma}{M_q^3}$$

with Γ sampling $\theta^+ \rightarrow K^+ n, K^0 p$

- Rescattering terms



$$KN \begin{cases} K^+ n \\ K^0 p \end{cases}$$

$$-i \tilde{t}^{(s)} \approx \frac{g_{K^+n}^2}{M_Z - M_R + i\frac{\Gamma}{2}} \quad c \quad \vec{\sigma} \cdot \vec{K}_{in} \quad S_I$$

$$-i \tilde{t}^{(p, \frac{1}{2})} = \frac{\bar{g}_{K^+n}^2}{M_Z - M_R + i\frac{\Gamma}{2}} \quad d \quad \vec{\sigma} \cdot \vec{q}' \quad S_I$$

$$-i \tilde{t}^{(p, \frac{3}{2})} = \frac{\tilde{g}_{K^+n}^2}{M_Z - M_R + i\frac{\Gamma}{2}} \quad (+ \vec{\sigma} \cdot \vec{K}_{in} + g \vec{\sigma} \cdot \vec{q}') S_I$$

S_I	$K^+ n$	$K^0 p$
$I=0$	1	1
$I=1$	-1	1

Interference between tree level and rescattering amplitudes

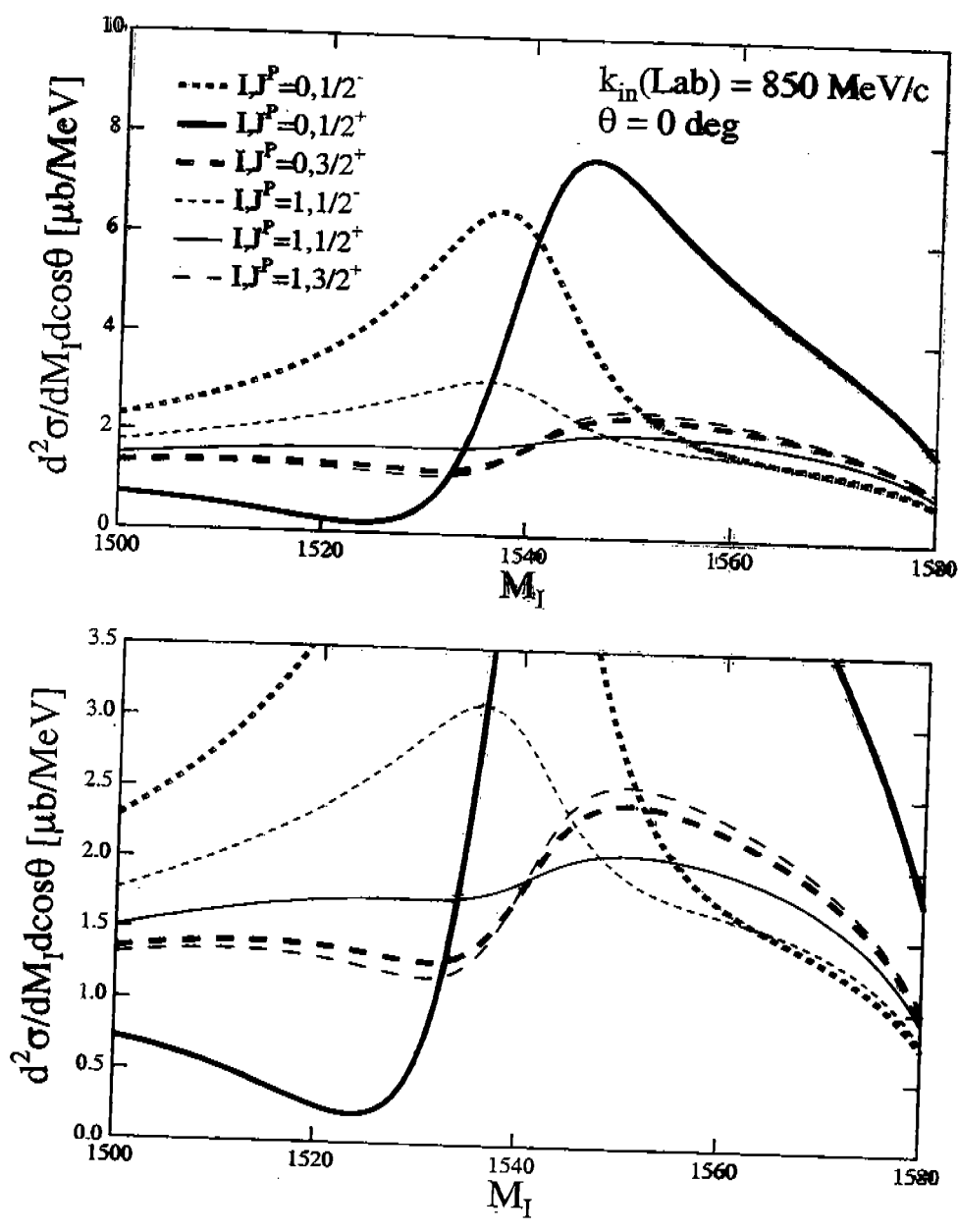


Figure 4: The double differential cross sections $d^2\sigma/dM_I d\cos\theta$ with $\theta = 0$ (forward direction) for $I = 0, 1$ and $J^P = 1/2^-, 1/2^+, 3/2^+$. Below, detail of the lower part of the upper figure of the panel.

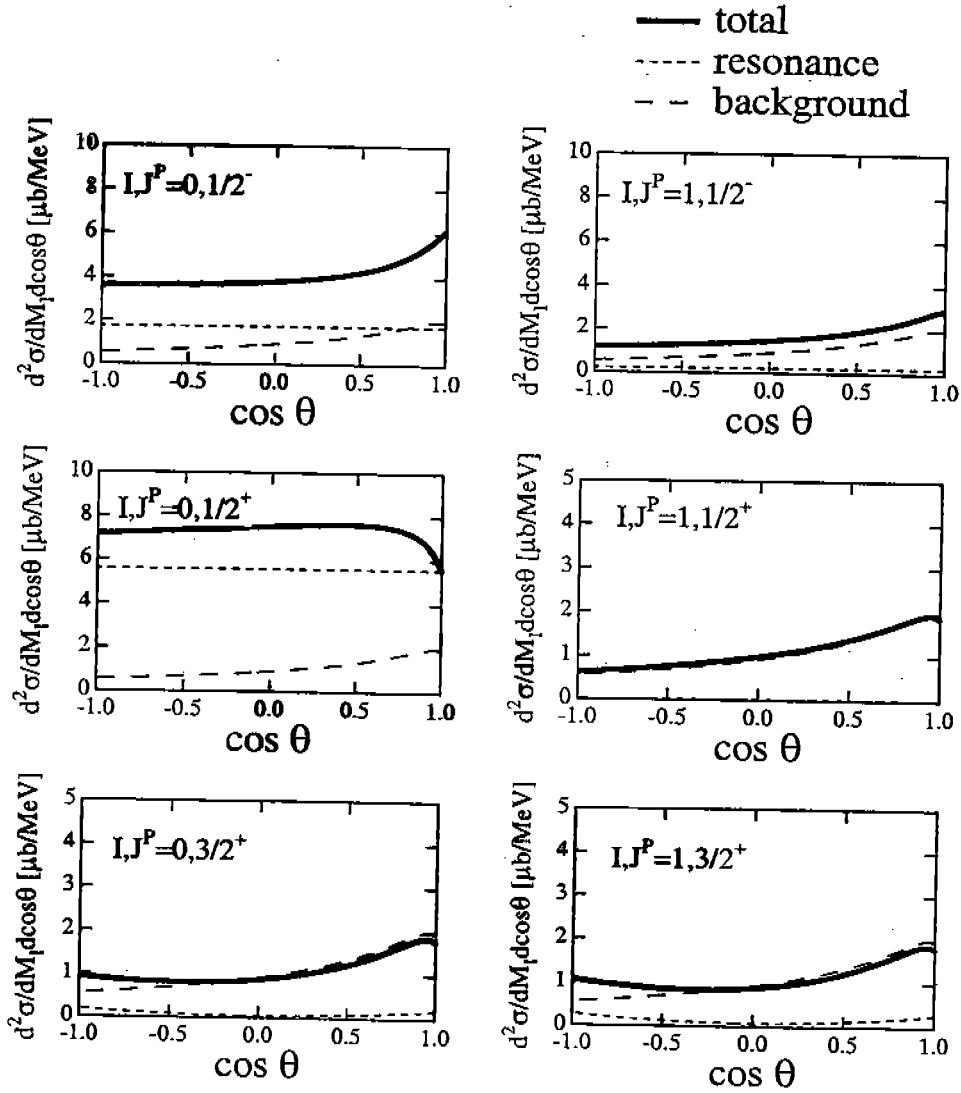


Figure 5: Angular dependence of the double differential cross sections $d^2\sigma/dM_I d\cos\theta$ with $M_I = 1540$ MeV at the resonance peak for $I = 0, 1$ and $J^P = 1/2^-, 1/2^+, 3/2^+$.

- Polarization observables

KN S-wave $\theta^+ \rightarrow 1/2^-$

KN P-wave $\theta^+ \rightarrow 1/2^+, 3/2^+$

Resonant term s-wave $\sim \vec{\sigma} \cdot \vec{k}_{in}$ only

" " p-wave $\sim \vec{\sigma} \cdot \vec{q}'$ also

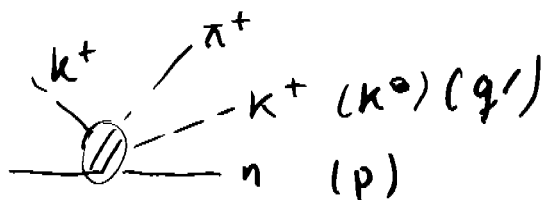
Take z direction along \vec{k}_{in} (k^+ incident)

initial N polarization $1/2$ in z direction

final " " $-1/2$ " "

$$\langle -1/2 | \vec{\sigma} \cdot \vec{k}_{in} | 1/2 \rangle = k_{in} \langle -1/2 | \sigma_z | 1/2 \rangle = 0$$

$$\begin{aligned} \langle -1/2 | \vec{\sigma} \cdot \vec{q}' | 1/2 \rangle &= q' \sin \theta \langle -1/2 | \sigma_x | 1/2 \rangle \\ &\sim q' \sin \theta \end{aligned}$$



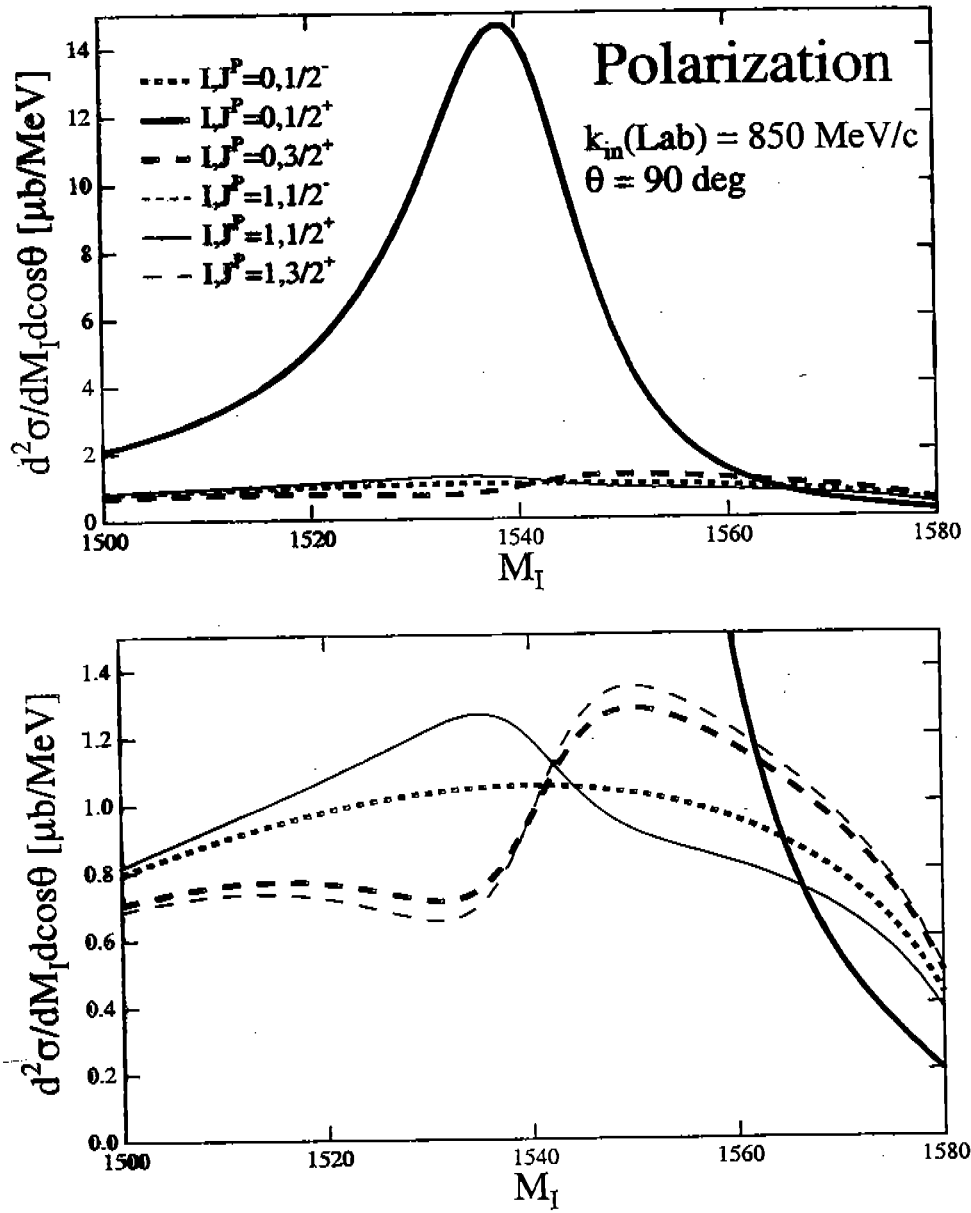


Figure 6: The double differential cross sections of polarized amplitude with $\theta = 90$ for $I = 0, 1$ and $J^P = 1/2^-, 1/2^+, 3/2^+$. Below, detail of the lower part of the upper figure of the panel.

Polarization

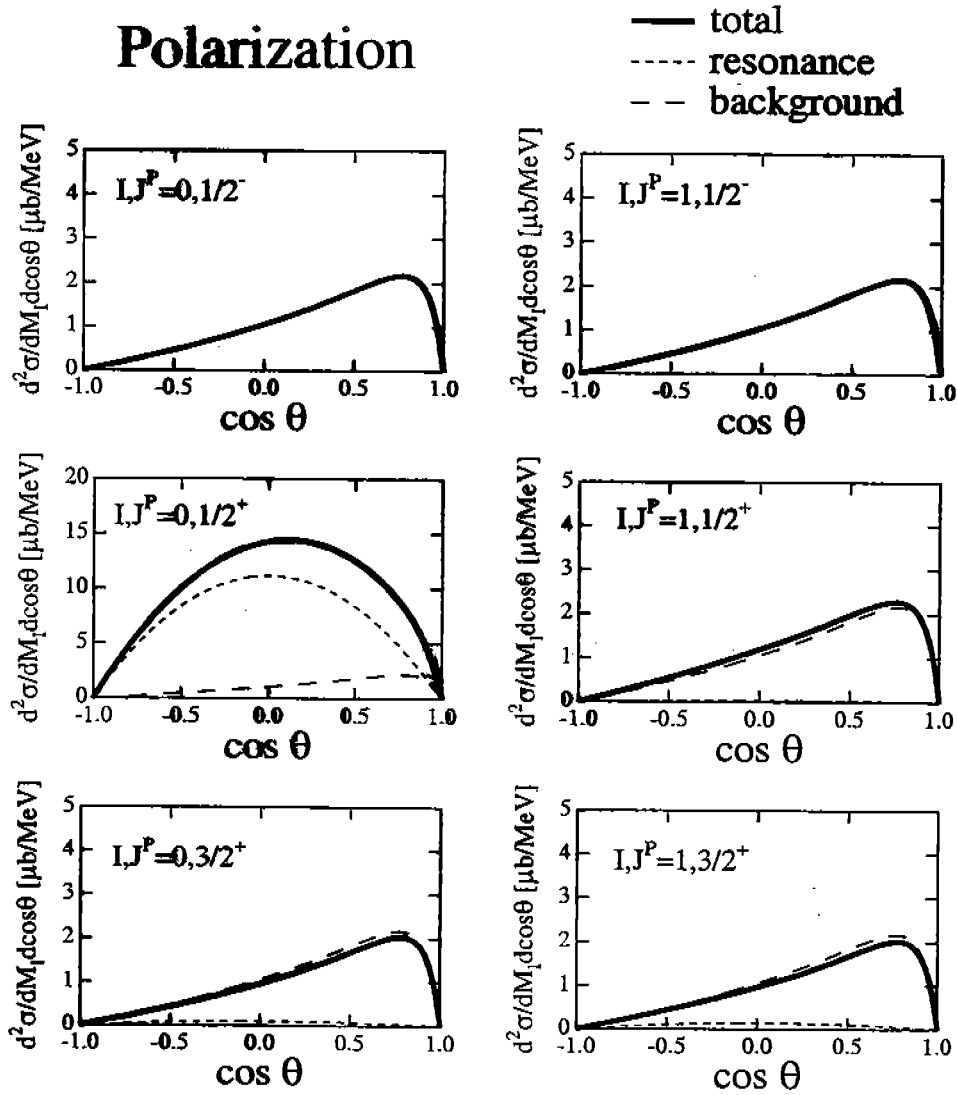


Figure 7: Angular dependence of the double differential cross sections of polarized amplitude with $M_I = 1540$ MeV at the resonance peak for $I = 0, 1$ and $J^P = 1/2^-, 1/2^+, 3/2^+$.

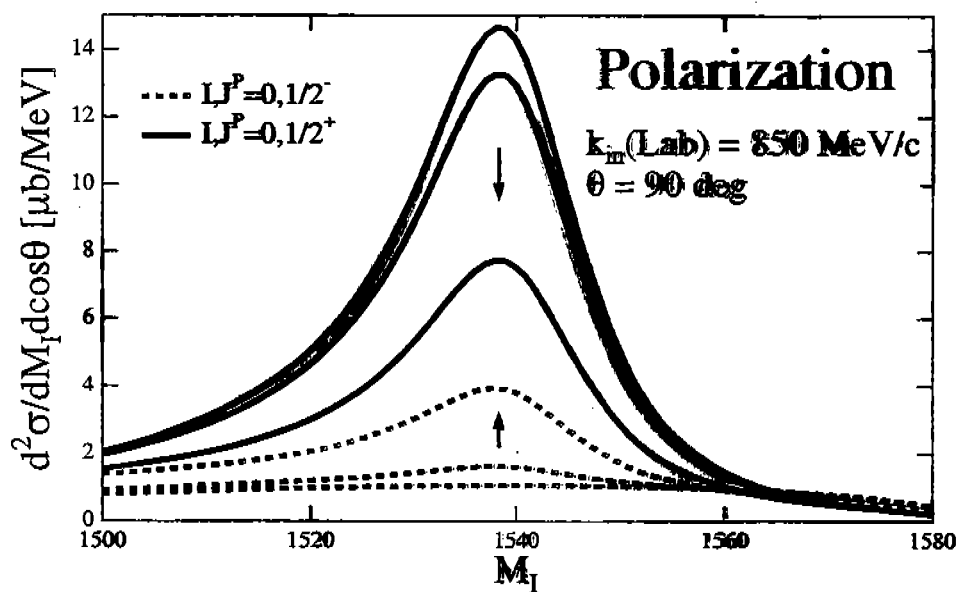


Figure 8: Effects of incomplete polarization on the double differential cross sections at $\theta = 90$ degrees. Three solid and dashed lines are for 100 %, 80 % and 0 % (along the direction of an arrow) polarization for $J^P = 1/2^\pm$ and $I = 0$.

CONCLUSIONS

- The $K^+p \rightarrow \pi^+ K^+ n$ (K^0p) reaction is a good tool to determine the spin, isospin and parity of the θ^+ , through studies of invariant mass distributions, angular distributions and polarization
- In particular, a clear signal at $\theta_{K^+ \text{ final}} = 90^\circ$ of the $\langle -1/2 | t | 1/2 \rangle$ transition would settle the θ^+ to $I=0$
 $J^P = 1/2^+$