

# Beam Single Spin Asymmetry in Pion Electroproduction

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Semi-Inclusive Reactions Workshop  
Jefferson Lab, 18-21 May, 2005



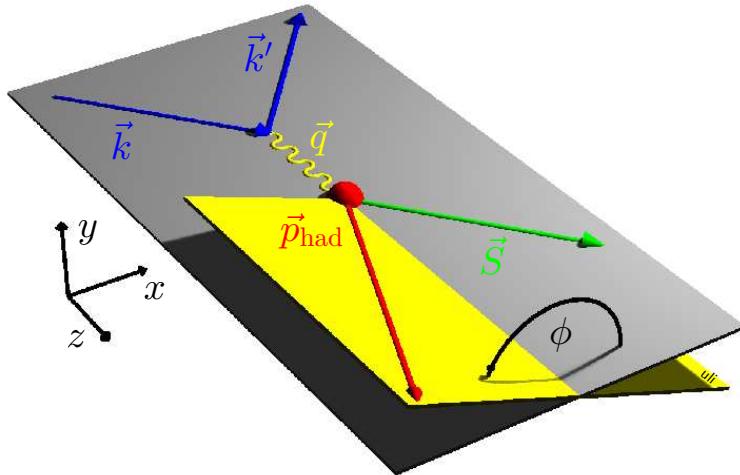
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(Yerevan Physics Institute / INFN Frascati)

# Semi Inclusive DIS:

$$\vec{e}p \rightarrow e'hX$$



$$\begin{aligned}
 Q^2 &= 4EE' \sin^2\left(\frac{\theta}{2}\right) \\
 \nu &= E - E' \\
 x &= \frac{Q^2}{2m\nu} \\
 y &= \frac{\nu}{E} \\
 z &= \frac{E_h}{\nu} \\
 \sin \phi &= \frac{[\vec{k}_1 \times \vec{k}_2] \cdot \vec{P}_\perp}{|\vec{k}_1 \times \vec{k}_2| |\vec{P}_\perp|}
 \end{aligned}$$

$$\sigma(\phi) = A_0 + A_1 \sin \phi + B_1 \cos \phi + A_2 \sin 2\phi + B_2 \cos 2\phi \dots$$

$$\frac{d^3\sigma_{UU}}{dx dy dz d\phi} = \frac{1}{2} \left( \frac{d^3\sigma^+}{dx dy dz d\phi} + \frac{d^3\sigma^-}{dx dy dz d\phi} \right)$$

$$\frac{2}{P} \frac{d^3\sigma_{LU}}{dx dy dz d\phi} = \frac{1}{P^+} \frac{d^3\sigma^+}{dx dy dz d\phi} - \frac{1}{P^-} \frac{d^3\sigma^-}{dx dy dz d\phi}$$

# DFs and FFs:

$$\text{Factorization} \Rightarrow \sigma^{eN \rightarrow ehX} = \sum f^{N \rightarrow q} \otimes \sigma^{eq \rightarrow eq} \otimes D^{q \rightarrow h}$$

↓ Distribution ↓ Fragmentation

$$\sigma_{unpol} \equiv \sigma_{UU} \propto (1 - y + y^2/2) \sum_{a,\bar{a}} e_a^2 \mathbf{x} f_1^a(x) D_1^a(z) \quad \text{KNOWN!}$$

$$\sigma_{pol} = \{\sigma_{UL}, \sigma_{LL}, \sigma_{UT}, \sigma_{LU}, \sigma_{LT}\}$$

↙ ↘  
 Beam Target polarization

$$\sigma_{UL} \propto S_L \sin \phi (2 - y) \sqrt{1 - y} \frac{M}{Q} \sum_{a,\bar{a}} e_a^2 x^2 \mathbf{h}_L^a(x) H_1^{\perp a}(z) + \dots$$

$$\sigma_{UT} \propto S_T (1 - y) \sin(\phi + \phi_s) \sum_{a,\bar{a}} e_a^2 \mathbf{x} h_1^a(x) H_1^{\perp a}(z) + \dots$$

$$\sigma_{LU} \propto \lambda_e \sin \phi y \sqrt{1 - y} \frac{M}{Q} \sum_{a,\bar{a}} e_a^2 x^2 [e^a(x) H_1^{\perp a}(z) + h_1^{\perp a}(x) E^a(z)]$$

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# Asymmetries:

$$A_{LU} = \frac{d\sigma^+ - d\sigma^-}{d\sigma^+ + d\sigma^-} = \frac{d\sigma_{LU}}{d\sigma_{UU}}$$

$$A_{LU} \propto \frac{e(x)H_1^\perp(z) + h_1^\perp(x)E(z)}{f_1(x)D_1(z)}$$

	Distribution	Fragmentation
Twist-2	$h_1^\perp$	$H_1^\perp$
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ADDITIONAL TERMS in the X-section!

$$\begin{aligned} \sigma_{LU} \propto & \lambda_e \sin \phi y \sqrt{1-y} \frac{M}{Q} \sum_{a,\bar{a}} e_a^2 x^2 \left[ xz e^a(x) H_1^{\perp a}(z) + h_1^{\perp a}(x) E^a(z) + \right. \\ & + \frac{M_h}{M} f_1^a(x) G^{\perp a}(z) - xz \frac{M}{M_h} g^{\perp a}(x) D_1^a(z) - \\ & \left. - \frac{m}{M} z f_1^a(x) H_1^{\perp a}(z) - \frac{m}{M_h} z h_1^{\perp a}(x) D_1^a(z) \right] \end{aligned}$$

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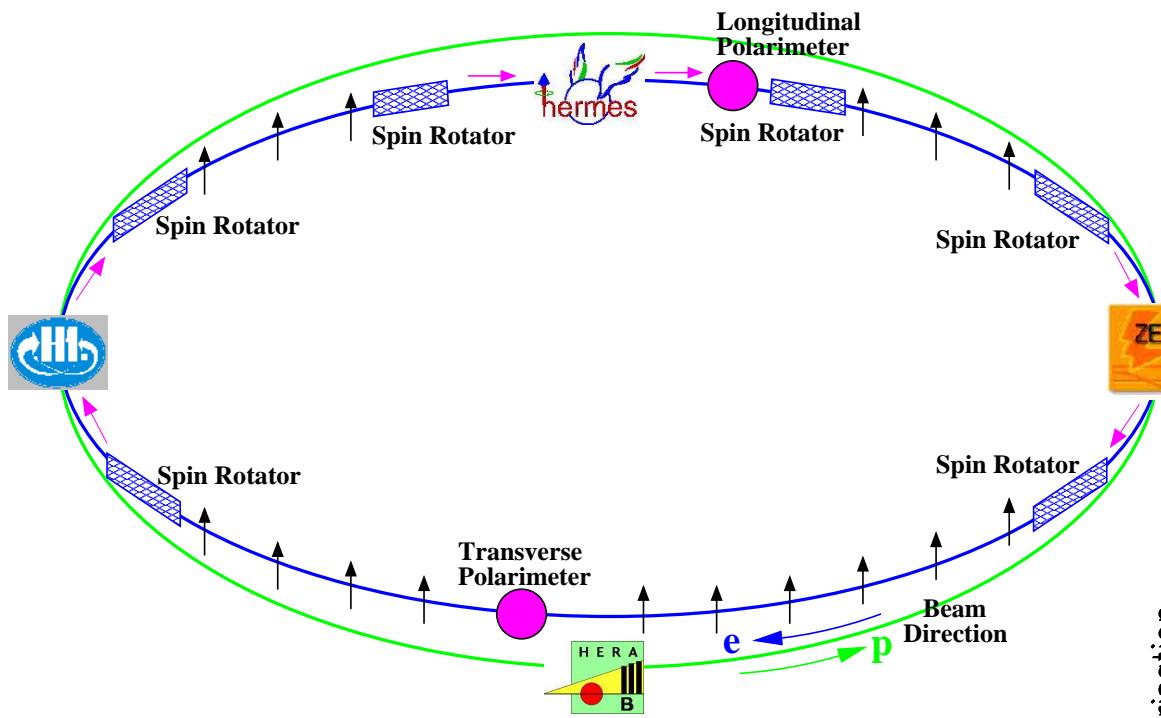
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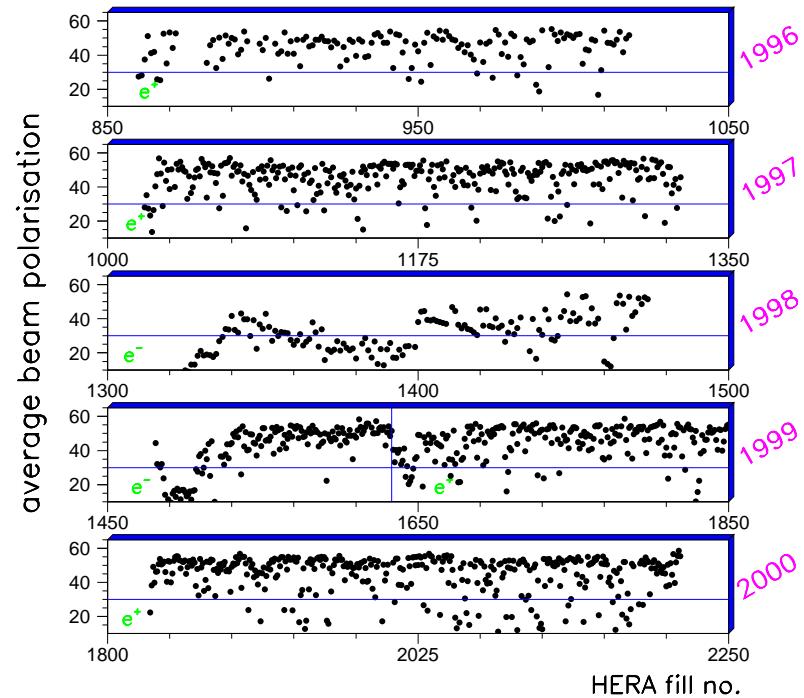
$$\sigma_{LU} \propto \lambda_e \sin \phi y \sqrt{1-y} \frac{M}{Q} \sum_{a,\bar{a}} e_a^2 x^2 [x z e^a(x) H_1^{\perp a}(z) + h_1^{\perp a}(x) E^a(z) +$$

$$A_{UL} + \frac{M_h}{M} f_1^a(x) G^{\perp a}(z) - x z \frac{M}{M_h} g^{\perp a}(x) D_1^a(z) - A_{LU}^{jet}$$
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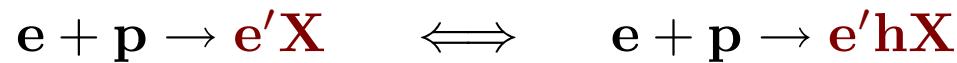
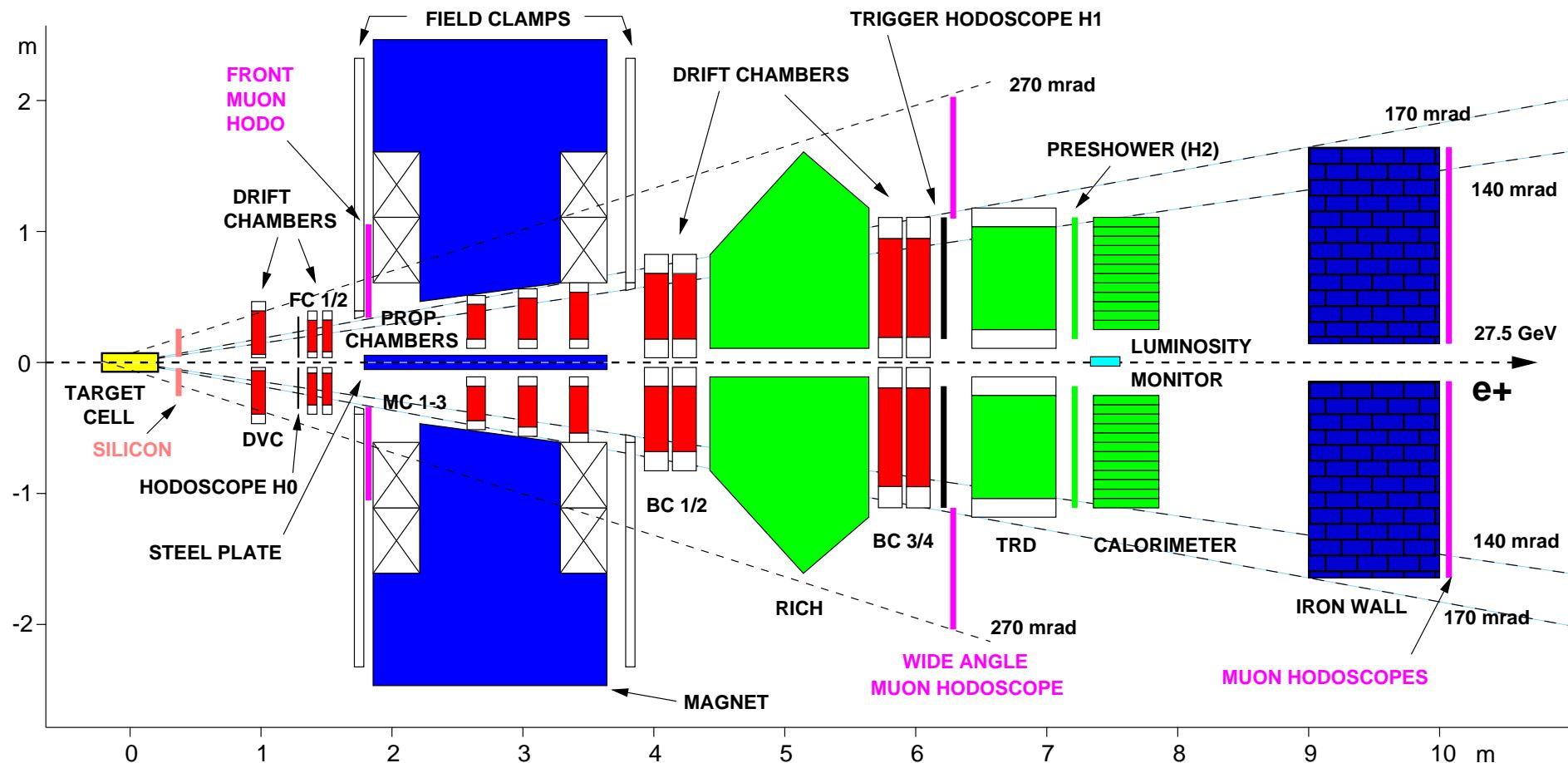
# HERA setup:



HERA-e beam self-polarized due to  
emission of synchrotron radiation  
⇒ **Sokolov-Ternov effect**  
 $\langle P_{\text{beam}} \rangle \approx 55\%$



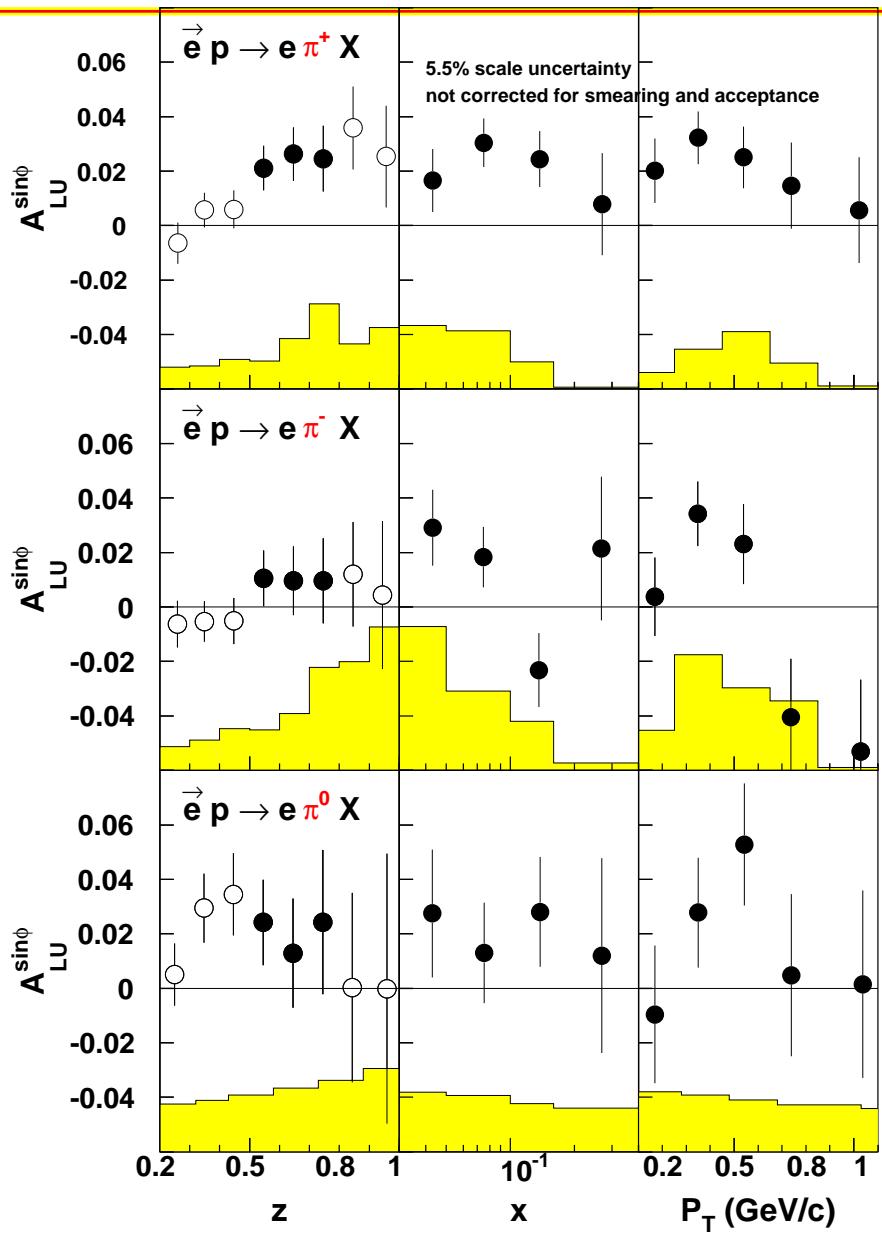
# HERMES Spectrometer:



# Beam SSA at HERMES

Asymmetry extraction:

$$A_{LU}^{\pm} = \frac{1}{P^{\pm} N^{\pm}} \sum_{i=1}^{N^{\pm}} \sin \phi$$



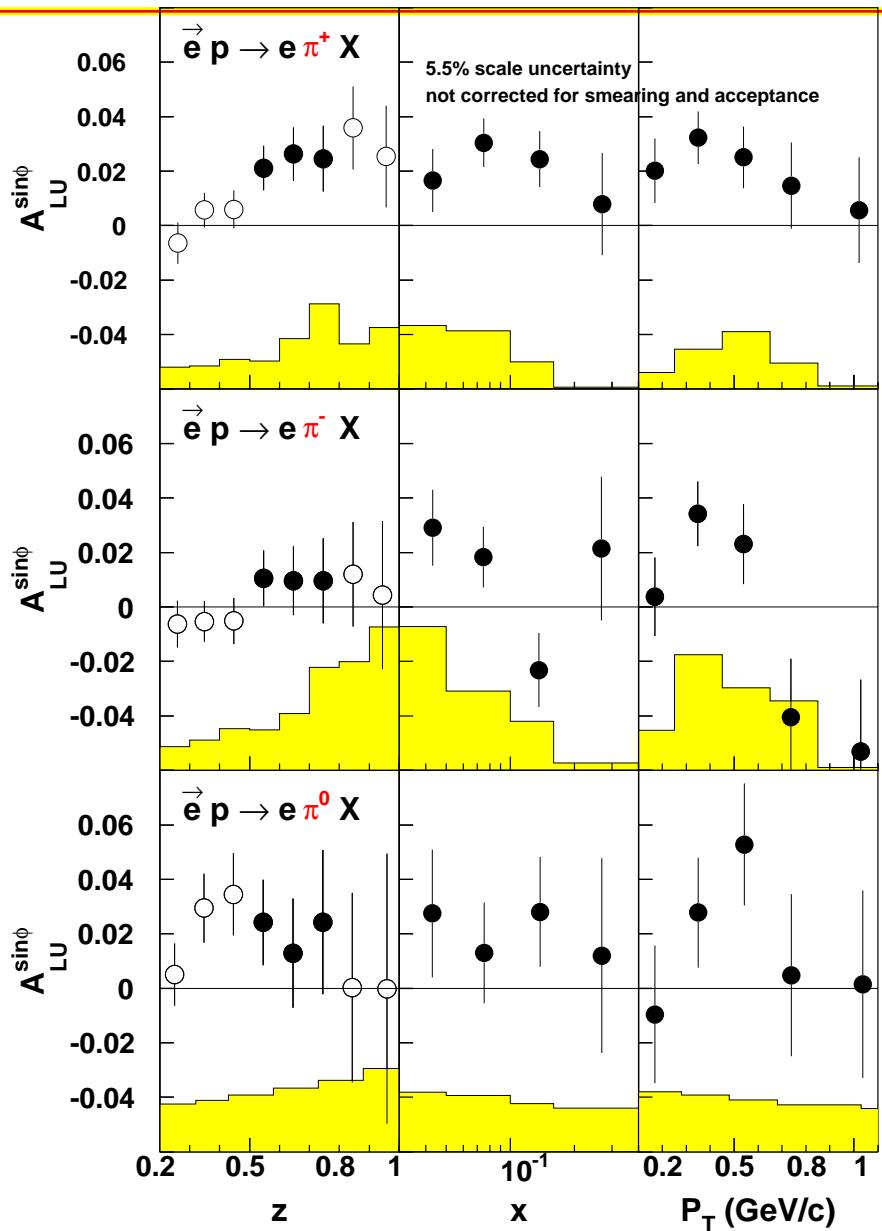
# Beam SSA at HERMES

Asymmetry extraction:

$$A_{LU}^{\pm} = \frac{1}{P^{\pm}N^{\pm}} \sum_{i=1}^{N^{\pm}} \sin \phi$$

Fit method:

$$A(\phi) = \frac{N^+L^- - N^-L^+}{N^+L^-P^- + N^-L^+P^+}$$

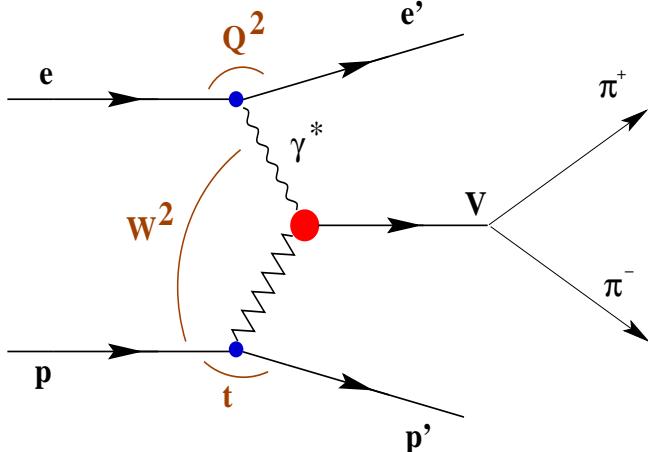


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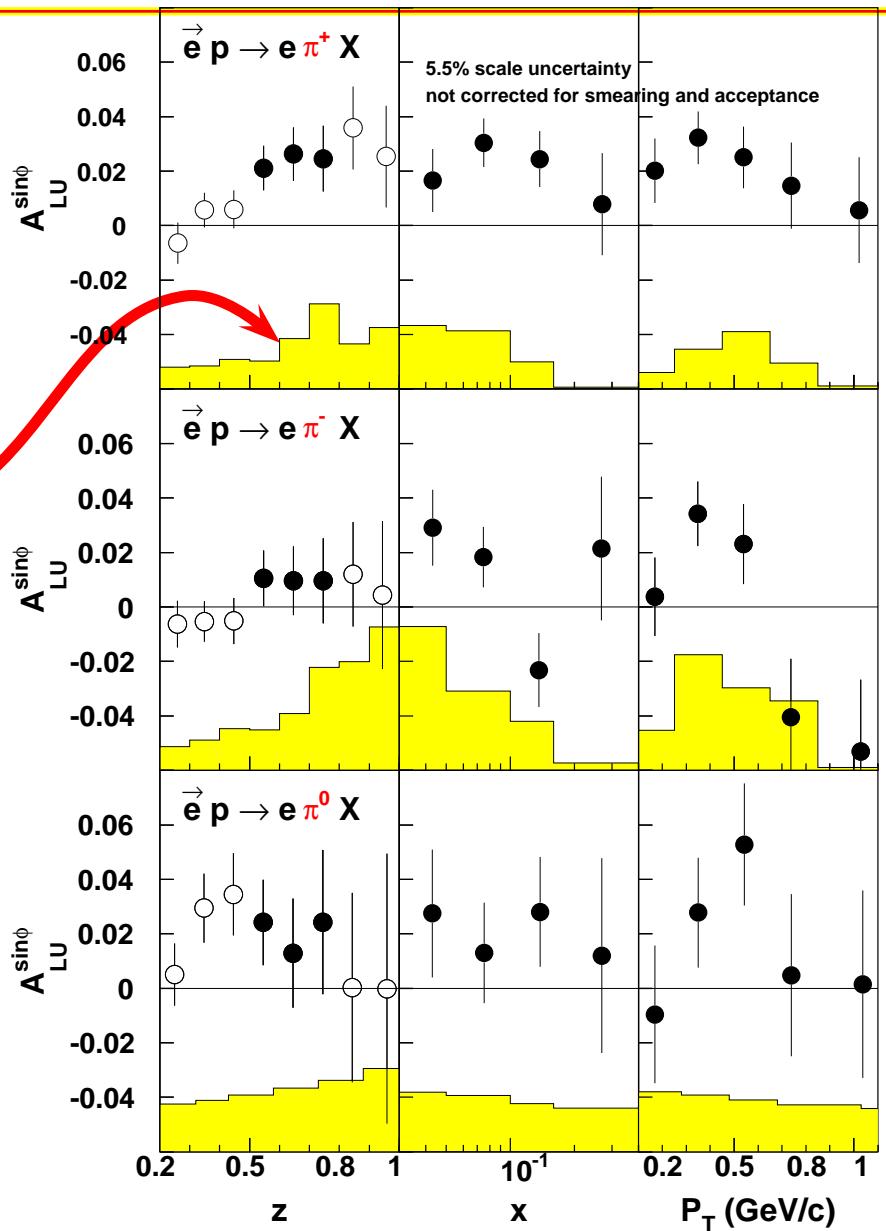
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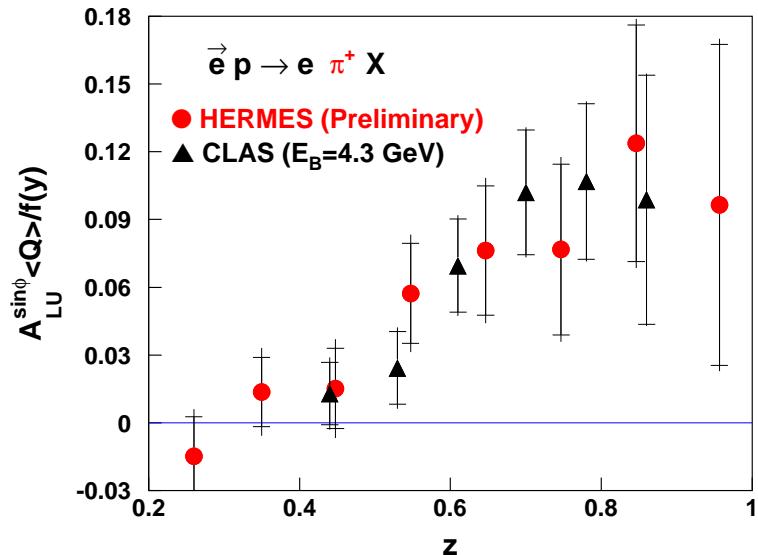
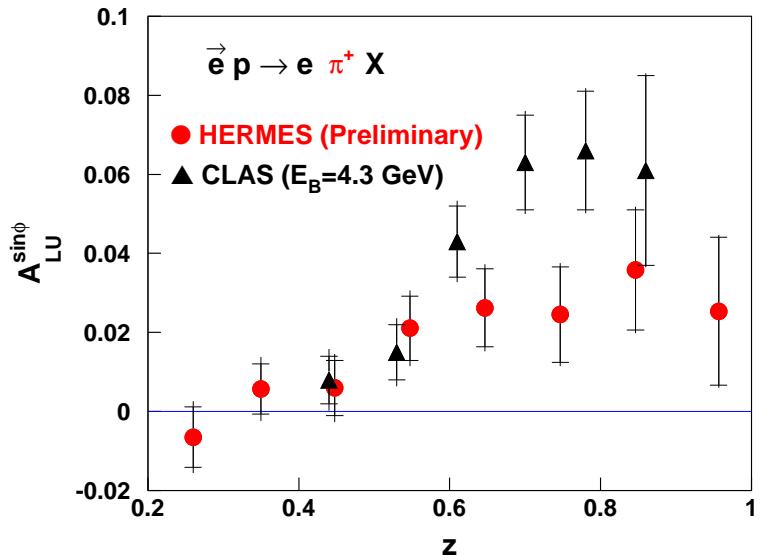
Interpretive error from VM



estimated from Monte-Carlo.



# Comparison with CLAS:

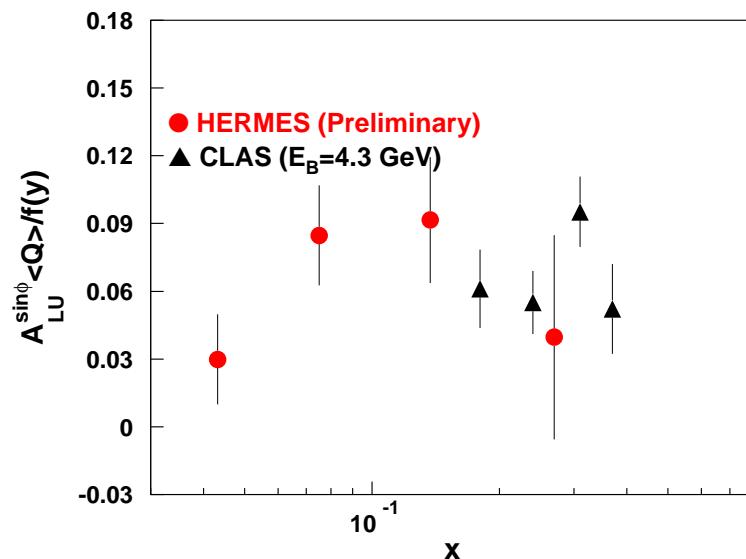
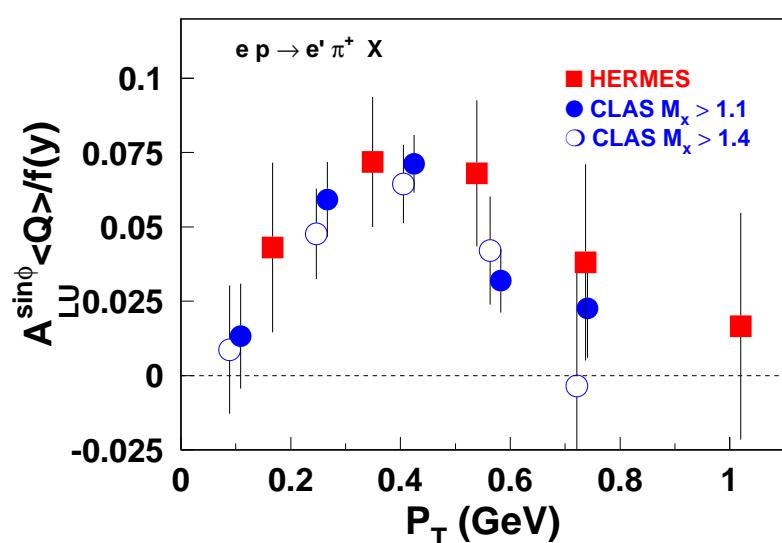


In leading order (neglecting  $\sigma_L/\sigma_T$ ):

$$f(y) = \frac{\sqrt{2(1-y)}}{1-y+y^2/2}$$

Strong kinematic suppression factor in HERMES ( $0.7 \rightarrow 0.35$  at higher  $z$ ) roughly constant ( $f(y) \simeq 0.7$ ) in CLAS.

# Comparison with CLAS(cont.):

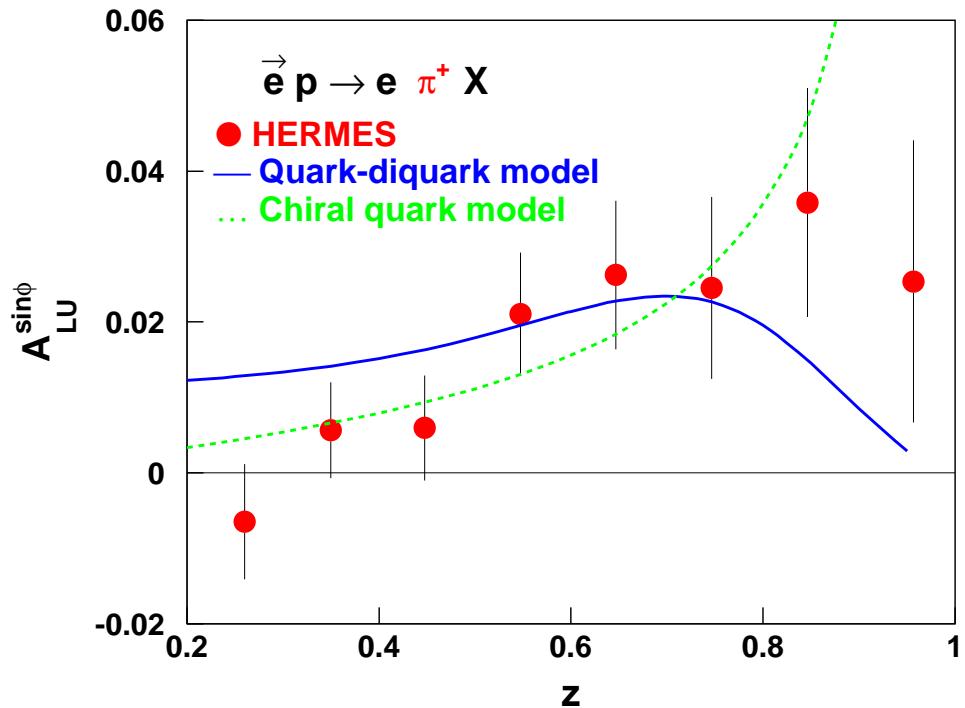


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# Comparison with Theory:



Average kinematics:

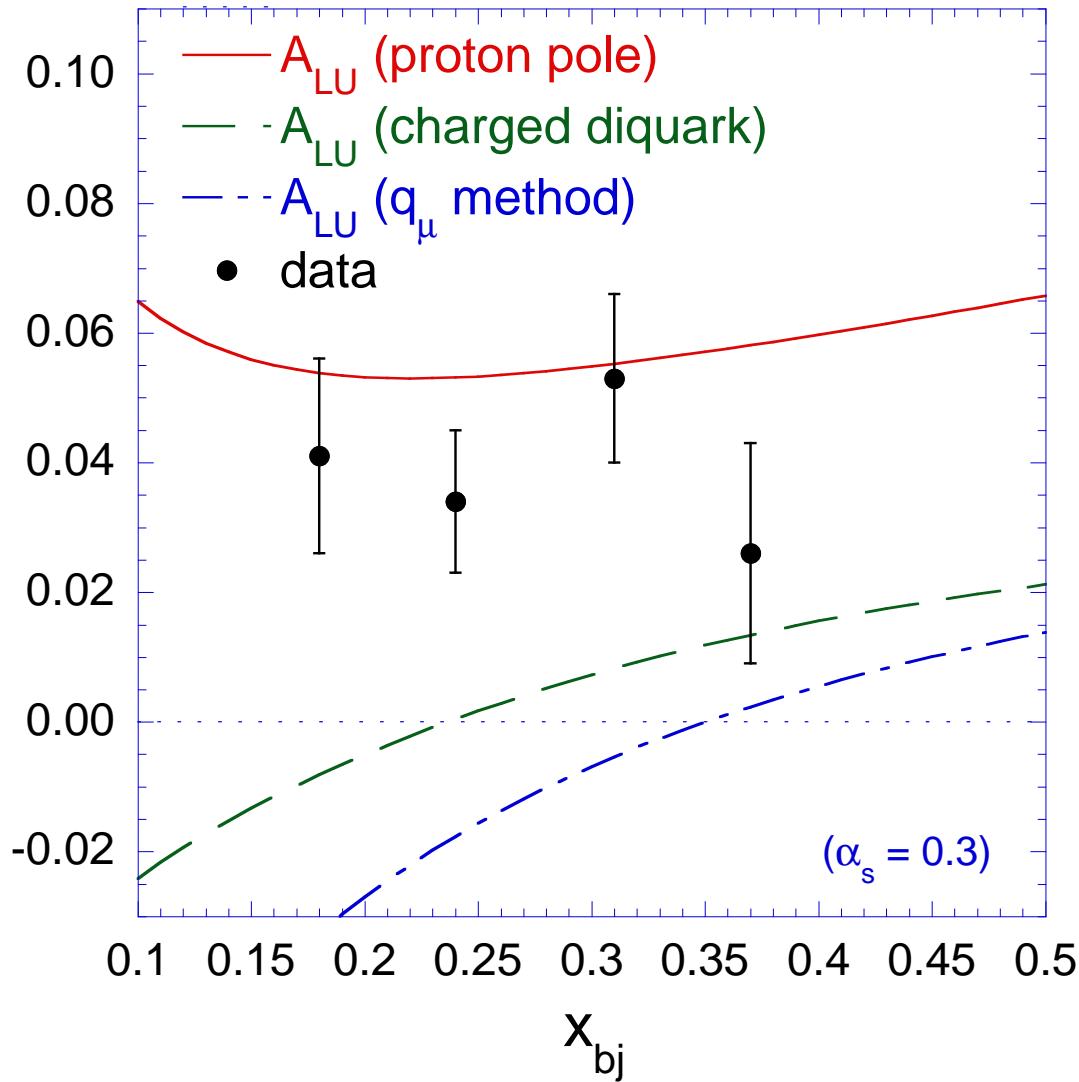
$$\langle P_T \rangle = 0.45 \text{ GeV}$$

$$\langle Q^2 \rangle = 2.4 \text{ GeV}^2$$

- L.Gamberg, D.Hwang, K.Oganessyan, Phys. Lett. B584 (2004) 276, (hep-ph/0311221)  
Quark-diquark spectator model,  $e(x)H_1^\perp(z)$  dominant;  
F.Yuan, Phys.Lett. B589 (2004) 28-34, (hep-ph/0310279)  
Chiral quark model,  $h_1^\perp(x)E(z)$  contribution only.

# Comparison with Theory (CLAS):

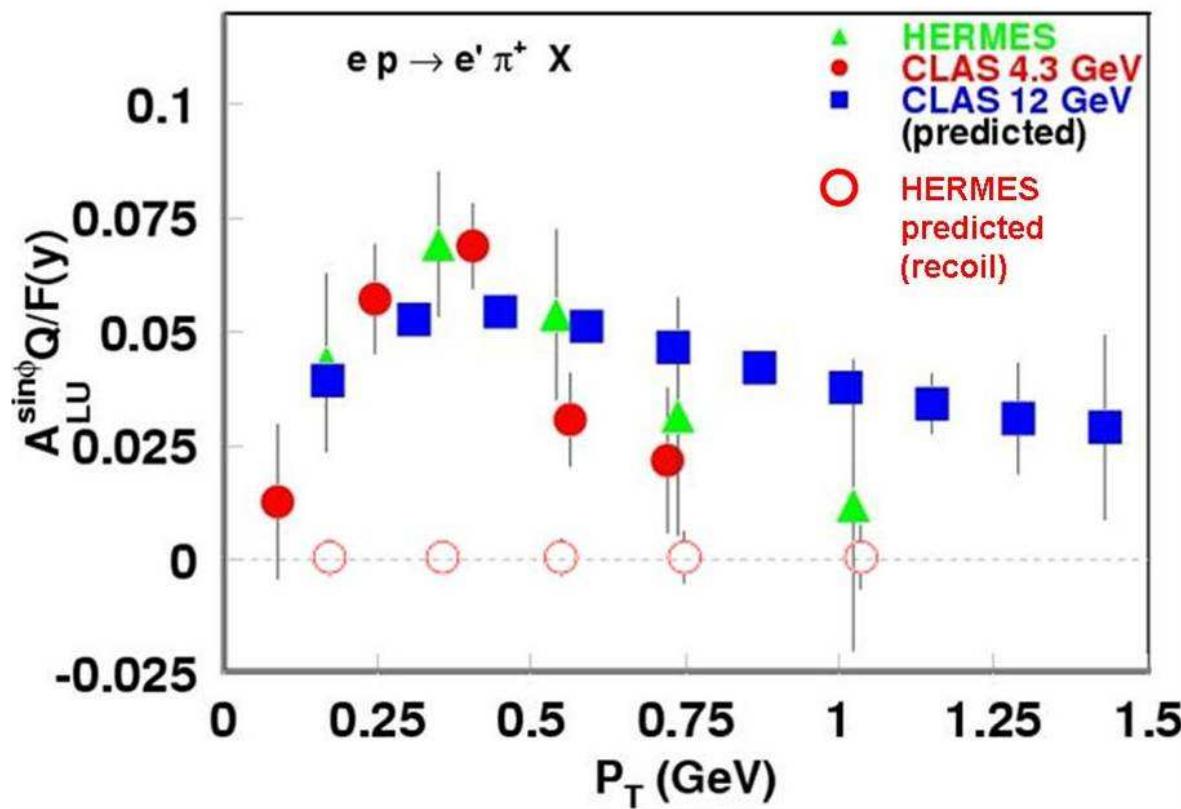
Beam Spin Asymmetry,  $E_{\text{beam}} = 4.25 \text{ GeV}$



A.Afanasev, C.Carlson, hep-ph/0308163 (to be published soon)

# Future:

CLAS 12GeV upgrade  $\iff$  HERMES Recoil upgrade



# Conclusions and Outlook:

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- First measurement of Beam SSA for all pions
- Independent source of information about  $H_1^\perp$  Collins function
- Possibility to access a set of new DFs and FFs
- Agreement with CLAS measurement of BSA for  $\pi^+$  (after kinematic range corrections)
- Agreement with some theoretical model calculation

Still to come:

- HERA run II with >3M of DIS on hydrogen
- HERMES with Recoil - high lumi data + better separation of exclusive channels
- CLAS 12GeV upgrade - wider kinematic range, more statistics

# Backup slides

The asymmetry of  $\rho^0$  decay products (from data) and their contamination in the pion sample:

