

PIBETA: A new precise measurement of rare pion and muon decays

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- motivation
- about the experimental method
- our working results
 - pion beta decay: $\pi^+ \rightarrow \pi^0 e^+ \nu$
 - radiative pion decay: $\pi^+ \rightarrow e^+ \nu \gamma$
- further plans

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PIBETA Experiment: MOTIVATION

Provide precision tests of Standard Model and QCD predictions:

- $\pi^+ \rightarrow \pi^0 e^+ \nu_e$ – main goal
 - SM tests from CKM unitarity
- $\pi^+ \rightarrow e^+ \nu_e \gamma$ ($e\bar{e}$)
 - F_A/F_V , π polarizability (χ PT prediction)
 - tensor coupling besides $V - A$
- $\mu^+ \rightarrow e^+ \nu_e \bar{\nu}_\mu \gamma$ ($e\bar{e}$)
 - departures from $V - A$ in $\mathcal{L}_{\text{weak}}$
- $\pi^+ \rightarrow e^+ \nu_e$ – 2nd phase
 - $e-\mu$ universality
 - pseudoscalar coupling besides $V - A$
 - massive neutrino, Majoran, ...

VECTOR CURRENT CONSERVATION

(a) Leptonic current (as in μ decay):

$$l^\alpha(x) = \bar{e}(x)\gamma^\alpha(1 - \gamma_5)\nu_e(x)$$

$$\langle e | l^\alpha | \nu_e \rangle \rightarrow \bar{u}_e \gamma^\alpha (1 - \gamma_5) u_\nu \quad (V - A \text{ form})$$

(b) Hadronic current (as in $n \rightarrow p e \bar{\nu}$):

$$\langle p | h^\alpha | n \rangle \rightarrow \bar{u}_p \gamma^\alpha (G_V - G_A \gamma_5) u_\nu$$

with $G_V \simeq 1$ and $G_A \simeq 1$. Puzzling!!

Large strong correction expected!

1956 Gerstein + Zeldovich	formulated the
1958 Feynman + Gell-Mann	CVC hypothesis

Analogy with electric charge: $Q(p) \equiv Q(e)$, i.e.,

$$Q(\text{bare } p) \equiv Q(\text{screened } p)$$

due to exact conservation of electric charge.

Cabibbo Universality

Cabibbo (1963):

$$G_V = G_\mu \cos \theta_C (= G_\mu V_{ud}) \quad \cos \theta_C \simeq 0.97$$

weak quark mixing: $\mathbf{d}' = \cos \theta_C \mathbf{d} + \sin \theta_C \mathbf{s}$.

With 3 generations, Cabibbo–Kobayashi–Masakawa matrix (1973):

$$\begin{pmatrix} u \\ d \end{pmatrix} \begin{pmatrix} c \\ s \end{pmatrix} \begin{pmatrix} t \\ b \end{pmatrix} \longrightarrow \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$

CKM unitarity:

$$|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 \stackrel{?}{=} 1.$$

Experimental limits on V_{ud} have come from:

- (a) superallowed Fermi nuclear β decays,
- (b) neutron β decay.

These have disagreed in the past.

Pure vector weak (Fermi β) decays

$$A(J^\pi) \rightarrow B(J^\pi) + e + \bar{\nu}$$

with $J(e + \bar{\nu}) = 0$, i.e., $\vec{S}(e) = -\vec{S}(\nu)$.

Guaranteed when $J^\pi(A) = J^\pi(B) = 0^+$ or 0^- .

In nuclei $0^+ \rightarrow 0^+$ are called **superallowed β** transitions.

No direct axial vector contribution, only from “loop corrections”.

Neutron decay: $n(\frac{1}{2}^+) \rightarrow p(\frac{1}{2}^+) + e^- + \bar{\nu}_e$

has both **V** and **A** transition amplitudes.

Status of CKM Unitarity

$|V_{us}| \simeq 0.2196 \pm 0.0026$ from K_{e3} decays.

$|V_{ub}| \simeq 0.0036 \pm 0.0007$ from B decays.

(a) Superallowed Fermi nuclear β decays

Longstanding discrepancies between Ormand & Brown
and Towner & Hardy ft values “reconciled” in 1990:

$$|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 = 0.9962 \pm 0.0016,$$

or $1 - 2.4\sigma$.

(b) Neutron β decay has varied considerably:

$$\sum_{i=1}^3 |V_{ui}|^2 = 1.0096 \pm 0.0044, \text{ or } 1 + 2.3\sigma,$$

[after Erozolimskii et al. (1990); since retracted]

$$\sum_{i=1}^3 |V_{ui}|^2 = 0.9917 \pm 0.0028, \text{ or } 1 - 3.0\sigma.$$

[Abele et al (2002); at odds w/world data set]

(c) Pion β decay – this work

Pion Beta Decay:

$$\pi^\pm \rightarrow \pi^0 e^\pm \nu \quad \text{BR} \simeq 1 \times 10^{-8}$$

Pure vector transition: $0^- \rightarrow 0^-$

Theoretical decay rate at tree level:

$$\begin{aligned} \frac{1}{\tau_0} &= \frac{G_F^2 |V_{ud}|^2}{30\pi^3} \left(1 - \frac{\Delta}{2M_+}\right)^3 \Delta^5 f(\epsilon, \Delta) \\ &= 0.40692(22) |V_{ud}|^2 (\text{s}^{-1}) . \end{aligned}$$

With radiative and loop corrections we get:

$$\frac{1}{\tau} = \frac{1}{\tau_0} (1 + \delta) ,$$

so that the branching ratio is

$$\begin{aligned} BR(\pi\beta) &= \frac{\tau_+}{\tau_0} (1 + \delta) \\ &= 1.0593(6) \times 10^{-8} (1 + \delta) |V_{ud}|^2 . \end{aligned}$$

Recent calculations of pion beta decay radiative corrections

(1) In the light-front quark model

[W. Jaus, Phys. Rev. D 63 \(2001\) 053009.](#)

- total RC for pion beta decay:

$$\delta = (3.230 \pm 0.002) \times 10^{-2} .$$

(2) In chiral perturbation theory

[V. Cirigliano, M. Knecht, H. Neufeld and H. Pichl,
hep-ph/0209226](#)

- χ PT with e-m terms up to $\mathcal{O}(e^2 p^2)$
- theoretical uncertainty of 5×10^{-4} in extracting $|V_{ud}|$ from $\text{BR}(\pi_{e3(\gamma)})$.

Experimental accuracy of the pion beta decay rate

Best result published to date:

$$BR(\pi^+ \rightarrow \pi^0 e^+ \nu) = (1.026 \pm 0.039) \times 10^{-8} ,$$

i.e., about 4 % [[McFarlane et al. \(1985\)](#)].

Accuracy	Constraints or cross-checks on
$\leq 1\%$	CVC and radiative corrections
$\sim 0.5\%$	Add to SAF & $n\beta$ input to V_{ud}
$< 0.3\%$	Failure of CKM unitarity (?): <ul style="list-style-type: none">○ 4th generation coupling○ $m_{Z'}$○ Λ of compositeness○ SUSY viol. of $q-l$ universality○ signal of a smaller G_F (ν osc.)

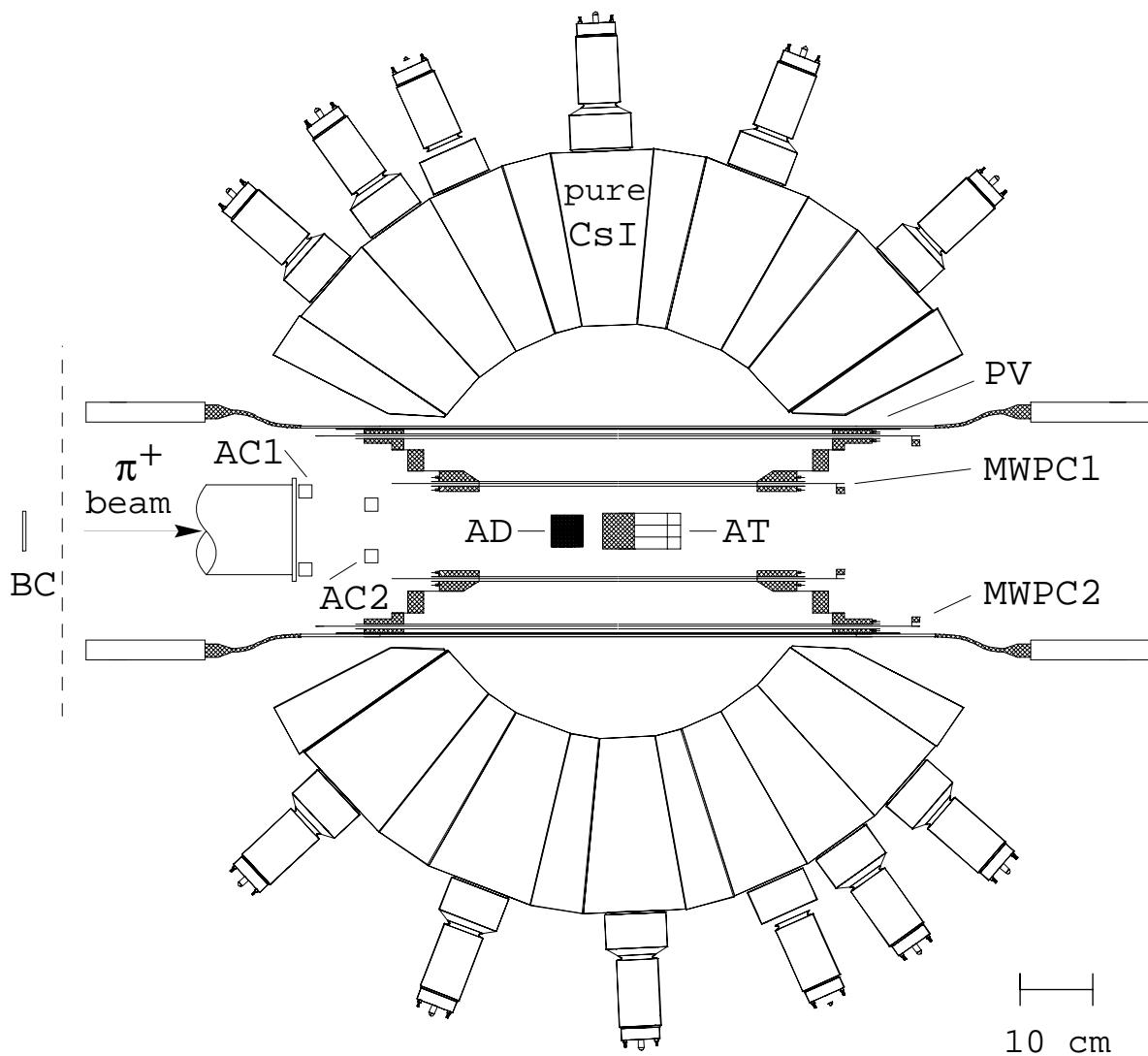
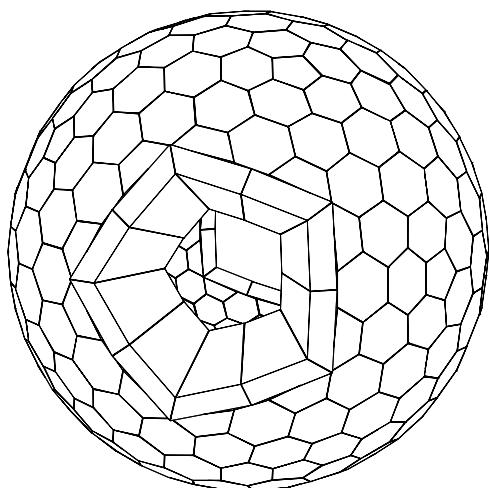
Design of the Experiment

*Pion and Muon Decays
in the PIBETA Experiment*

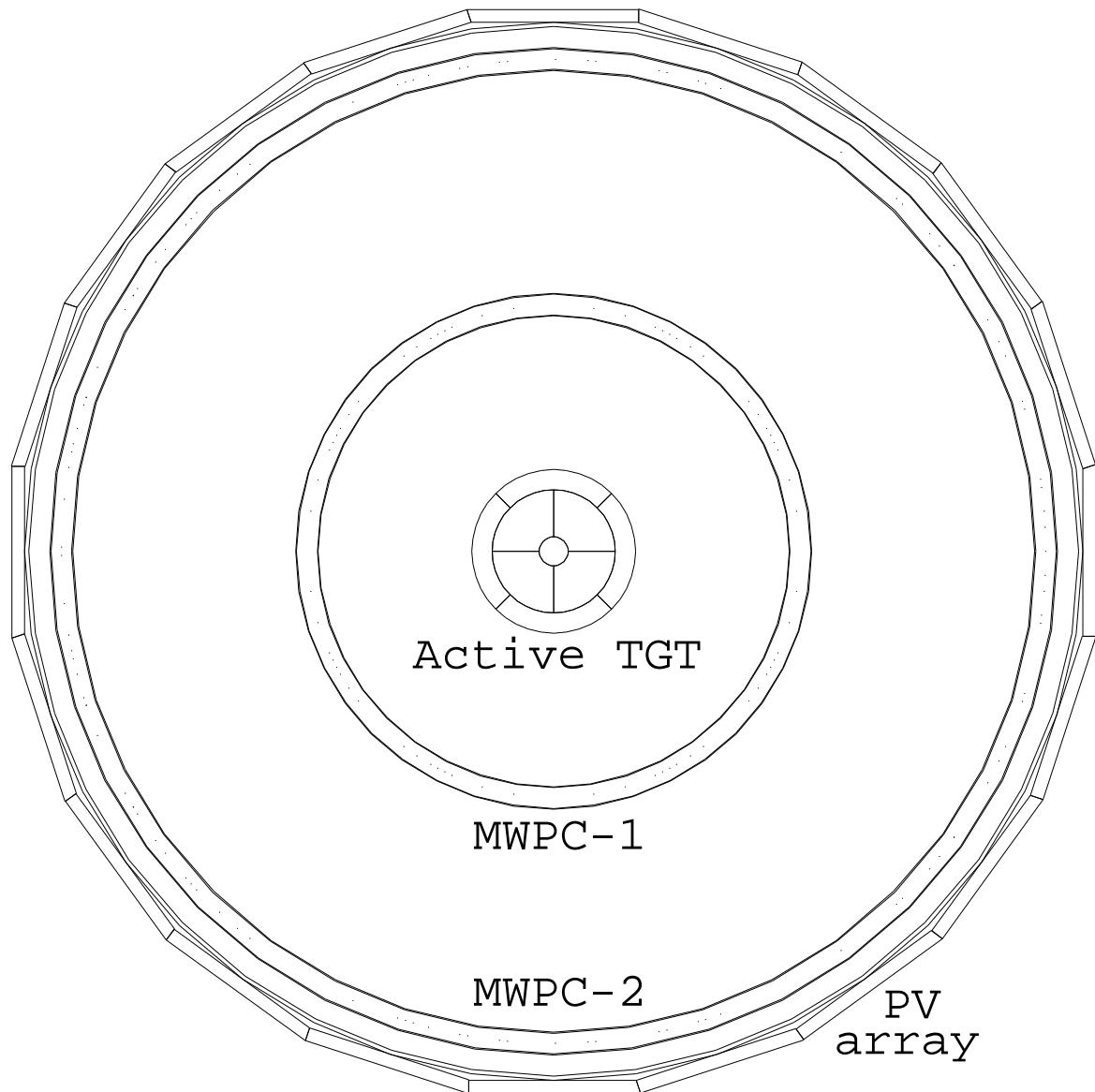
$\pi^+ \rightarrow \mu^+ \nu$	(1.0),	
$\mu^+ \nu \gamma$	$(\sim 2.0 \times 10^{-4})$	
$e^+ \nu$	$(\sim 1.2 \times 10^{-4})$	normalize to
$e^+ \nu \gamma$	$(\sim 5.6 \times 10^{-8})$	measure
$\pi^0 e^+ \nu$	$(\sim 1.0 \times 10^{-8})$	measure
$\pi^0 \rightarrow \gamma \gamma$	(~ 0.9880)	measure
$e^+ e^- \gamma$	$(\sim 1.2 \times 10^{-2})$	measure
$e^+ e^- e^+ e^-$	$(\sim 3.1 \times 10^{-5})$	
$e^+ e^-$	$(\sim 6.2 \times 10^{-8})$	
$\mu^+ \rightarrow e^+ \nu \bar{\nu}$	(1.0)	normalize to
$e^+ \nu \bar{\nu} \gamma$	(~ 0.014)	measure
$e^+ \nu \bar{\nu} e^+ e^-$	$(\sim 3 \times 10^{-5})$	measure

PIBETA Experiment:

- stopped π^+ beam
- segmented active tgt.
- 240-elem. CsI(p) calo.
- central tracking
- digitized PMT readout
- cosmic μ antihouse
- stable temp./humidity



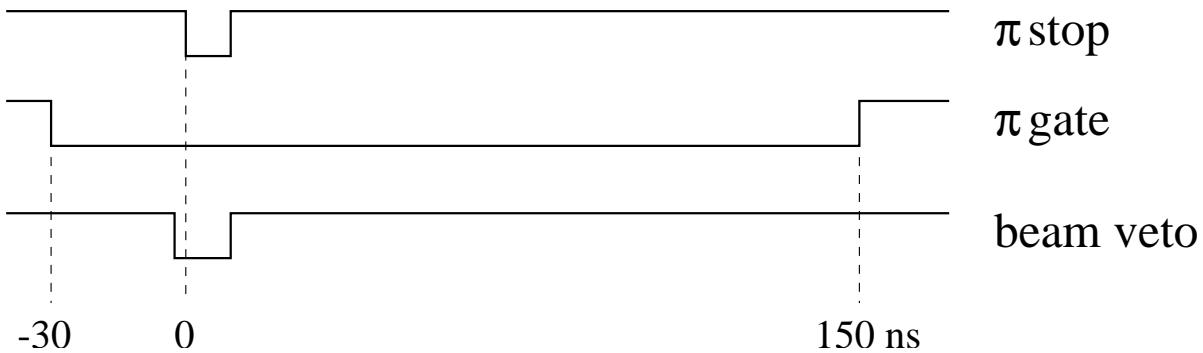
CENTRAL DETECTOR REGION



(beam is perpendicular at center)

Experimental Method: Summary

- Detect π^+ decays at rest (during a delayed 180 ns gate).



- Use prescaled $\pi^+ \rightarrow e^+ \nu$ (π_{e2}) decays for normalization.
- Accept every $\pi\beta$ trigger – unbiased ($\gamma\gamma$ coincidences above Michel endpoint)

$$\frac{1}{\tau_{\pi\beta}} = \frac{1}{\tau_{\pi^+}} \cdot \frac{BR_{e\nu} f_{\text{presc}}}{BR_{\pi^0 \rightarrow \gamma\gamma}} \cdot \frac{A_{e\nu}}{A_{\pi\beta}} \cdot \frac{N_{\pi\beta}}{N_{e\nu}}$$

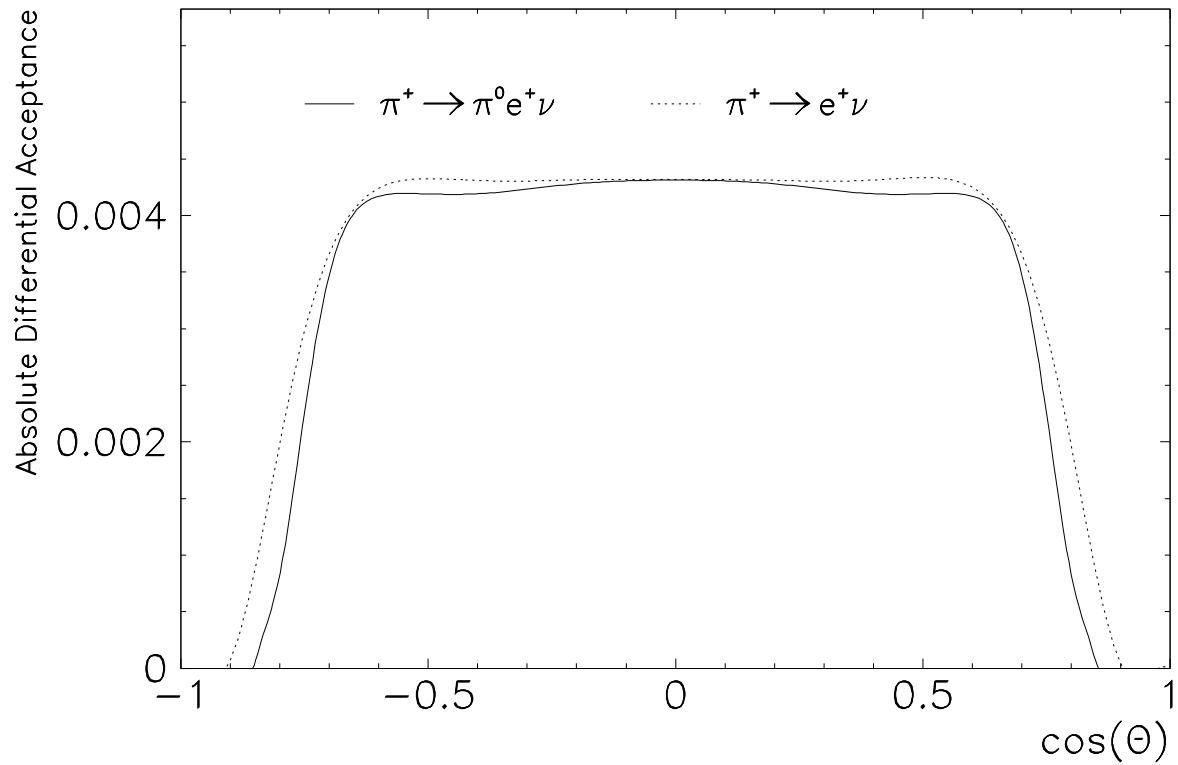
$A_{\pi\beta}$, $A_{e\nu}$ are acceptances for the $\pi\beta$ and π_{e2} decay modes, respectively.

Experimental method (cont'd.)

$A_{\pi\beta}$, $A_{e\nu}$ influenced by:

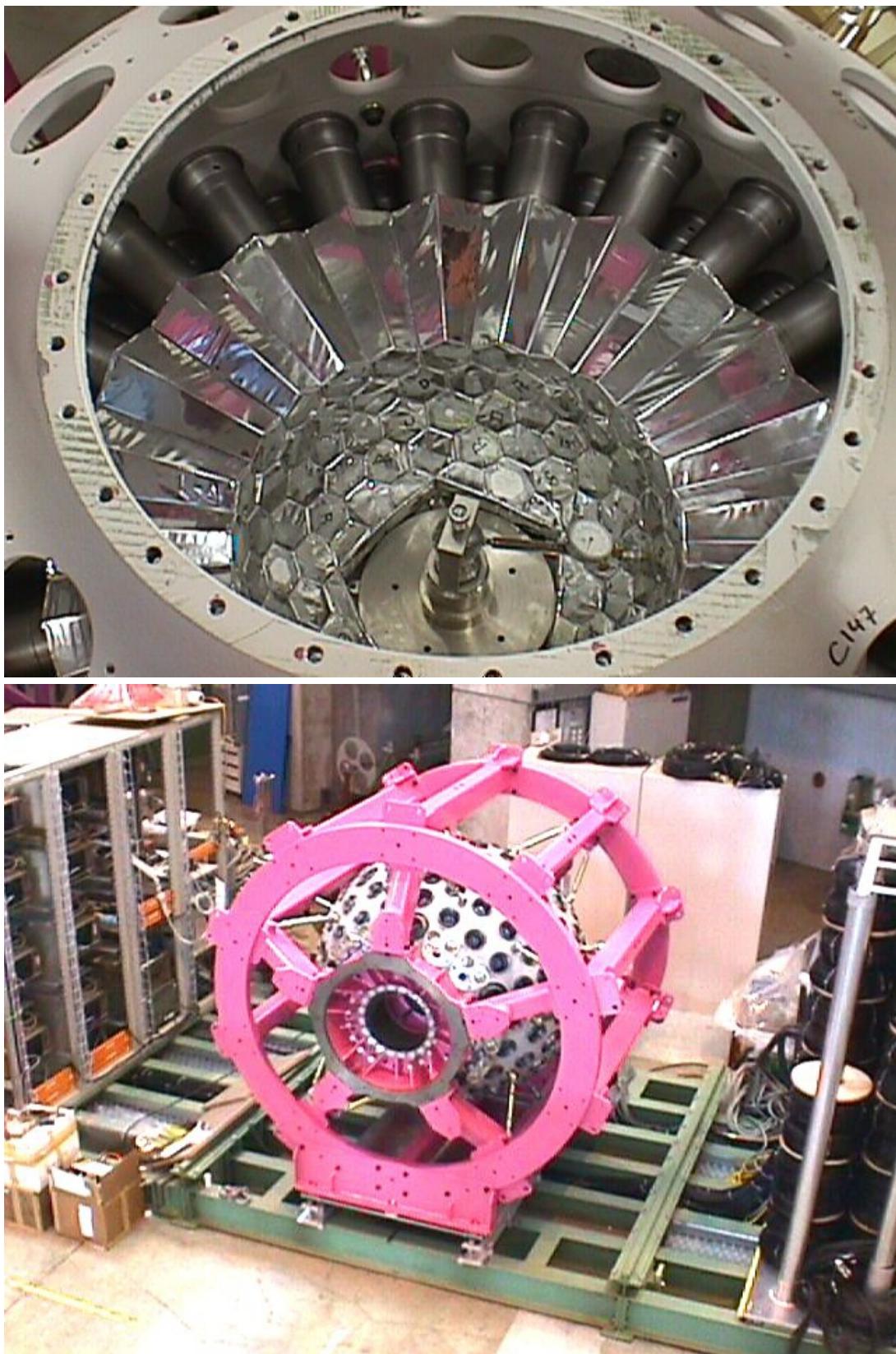
- geometry (including beam spot, alignment, cracks),
- e-m shower leak-through, backsplash, etc.,
- e-m interactions in TGT and tracking detectors,
- volume uniformity of CsI light response, photoelectron statistics,
- gain stability of CsI detector modules,
- photonuclear and e knockout react's in CsI.

Key acceptances compared



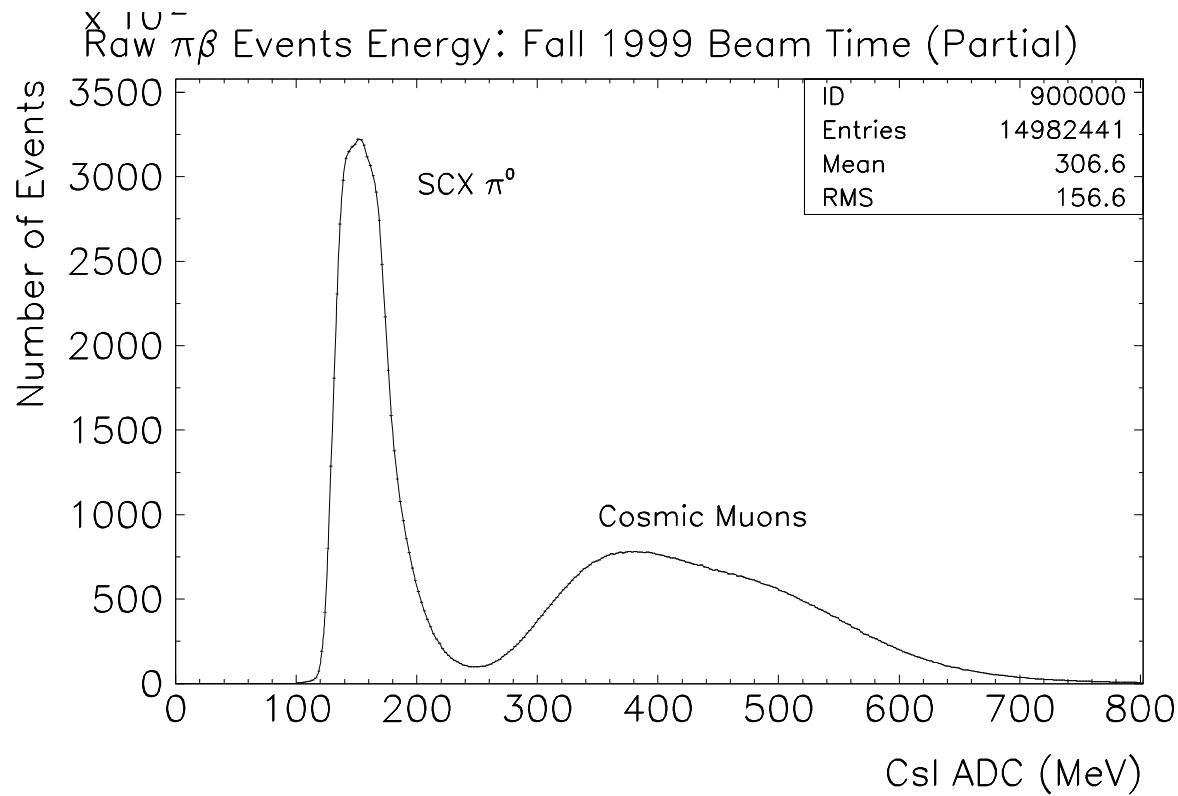
GEANT calculated acceptances for the $\pi\beta$ and π_{e2} decays as a function of $\cos\theta$.

PIBETA Detector Assembly (1998)



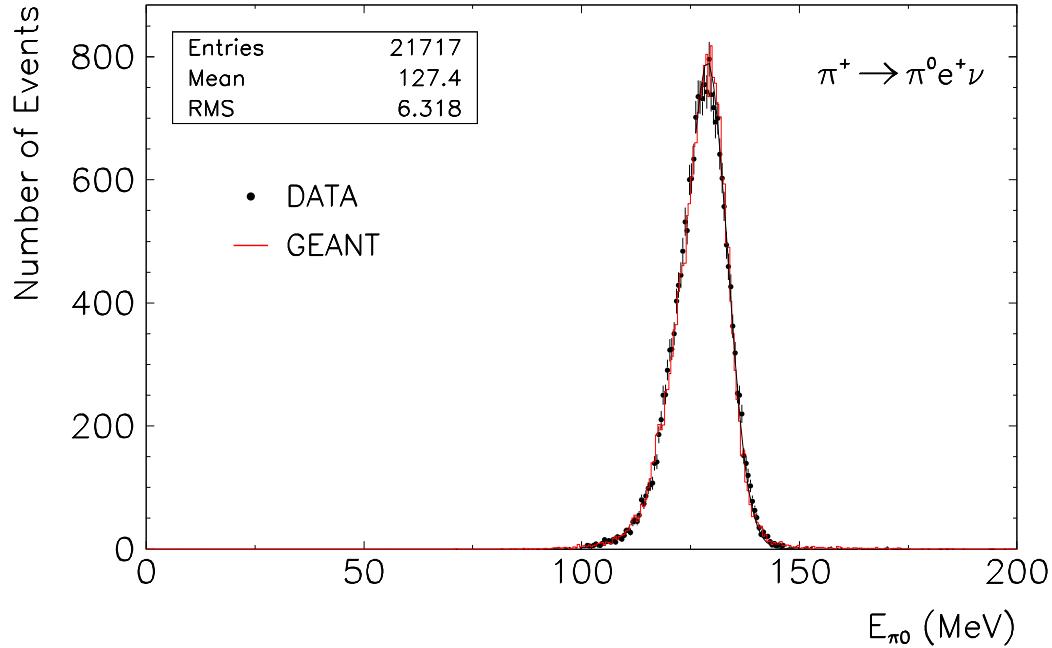
Detector Performance

Online “ $\pi\beta$ ” Energy Spectrum:

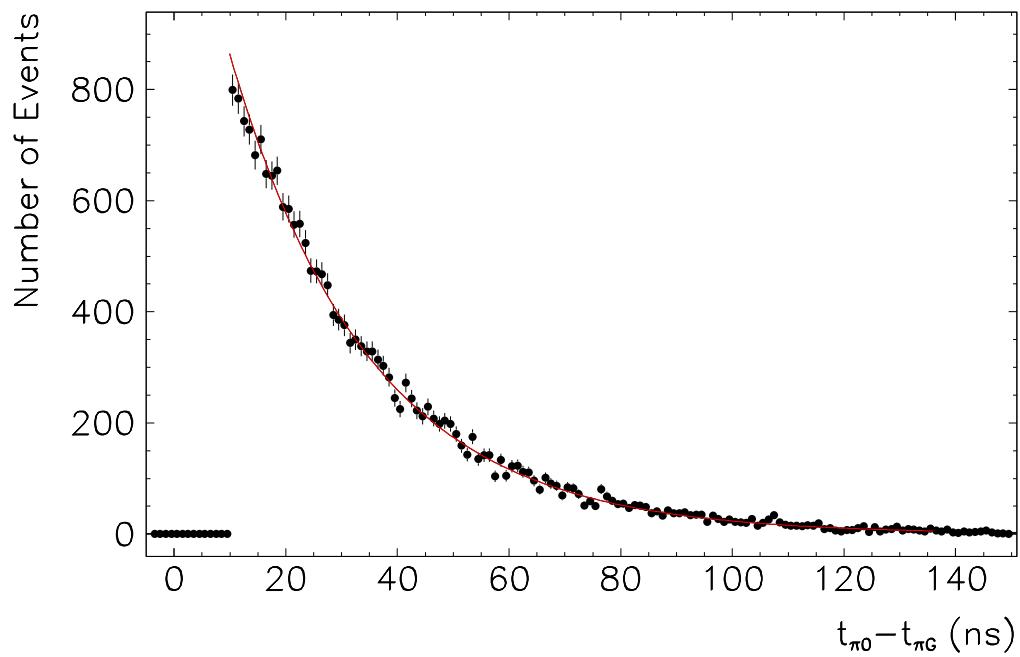


True $\pi\beta$ events buried deep under overwhelming background!

Preliminary Results: $\pi^+ \rightarrow \pi^0 e^+ \nu$

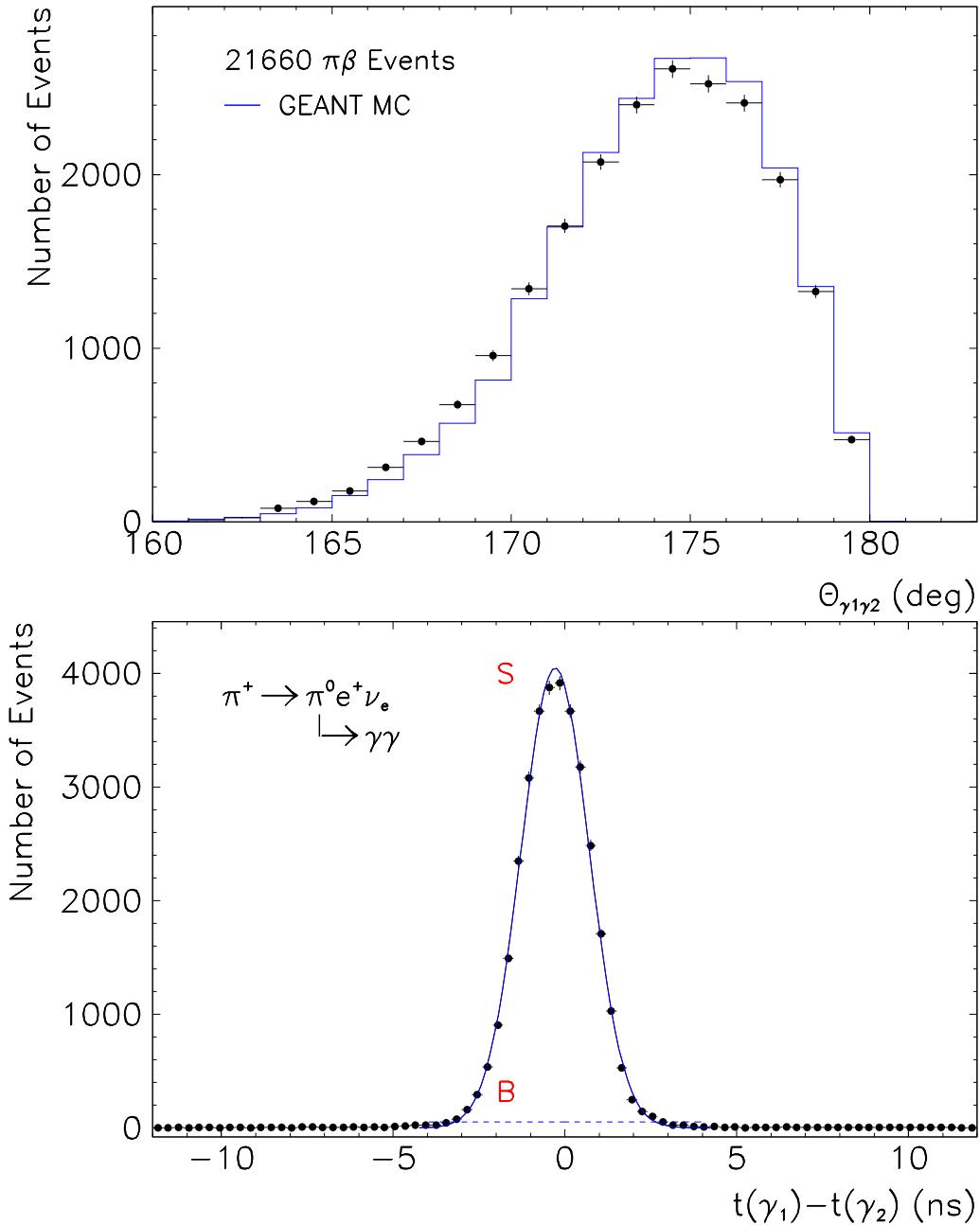


1999/2000 Partial $\pi\beta$ Analysis Results – Preliminary

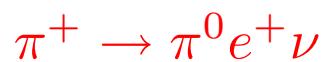
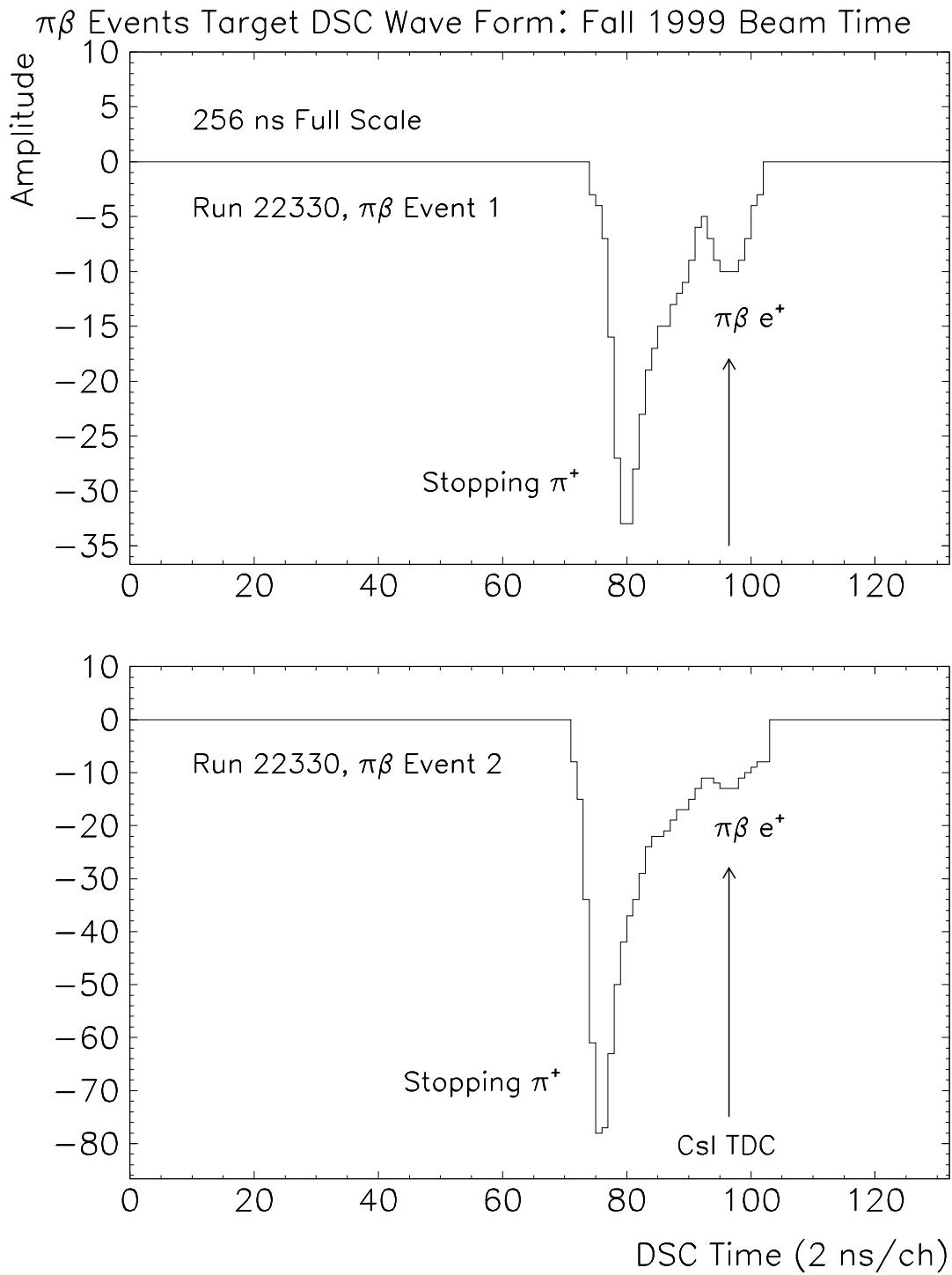


Preliminary Results: $\pi^+ \rightarrow \pi^0 e^+ \nu$

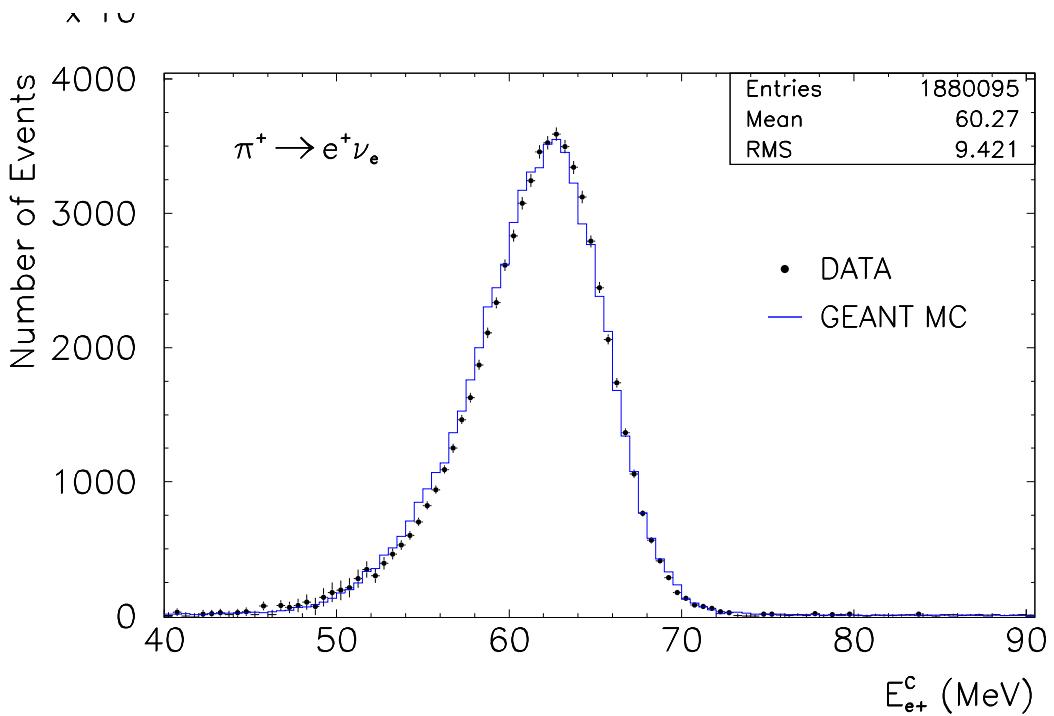
1999/2000 Partial $\pi\beta$ Analysis Results – Preliminary



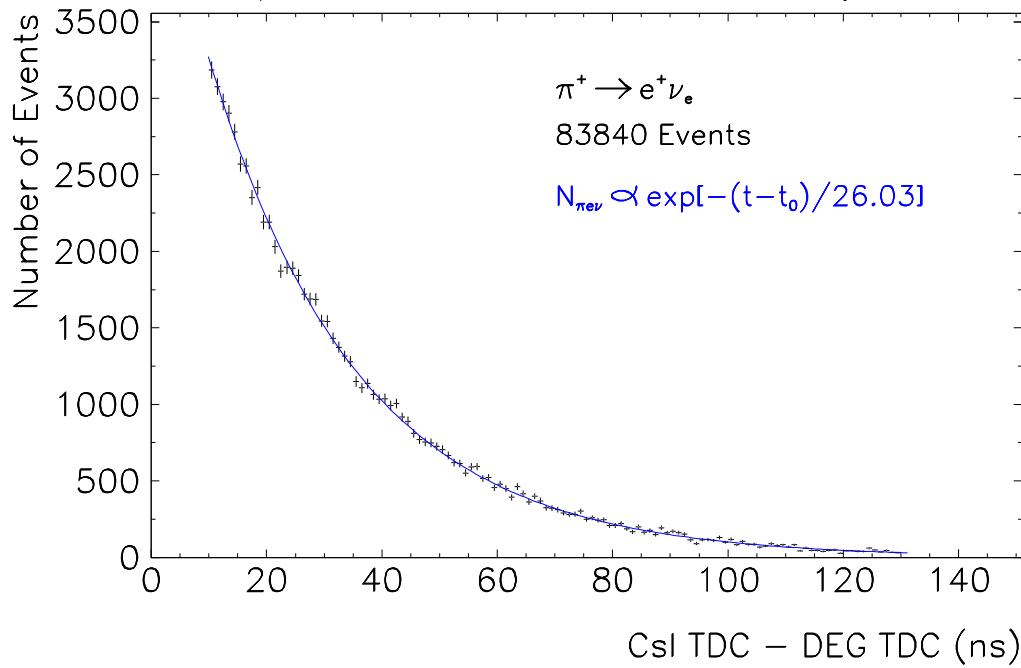
Domino Sampling Chip (DSC) Analysis



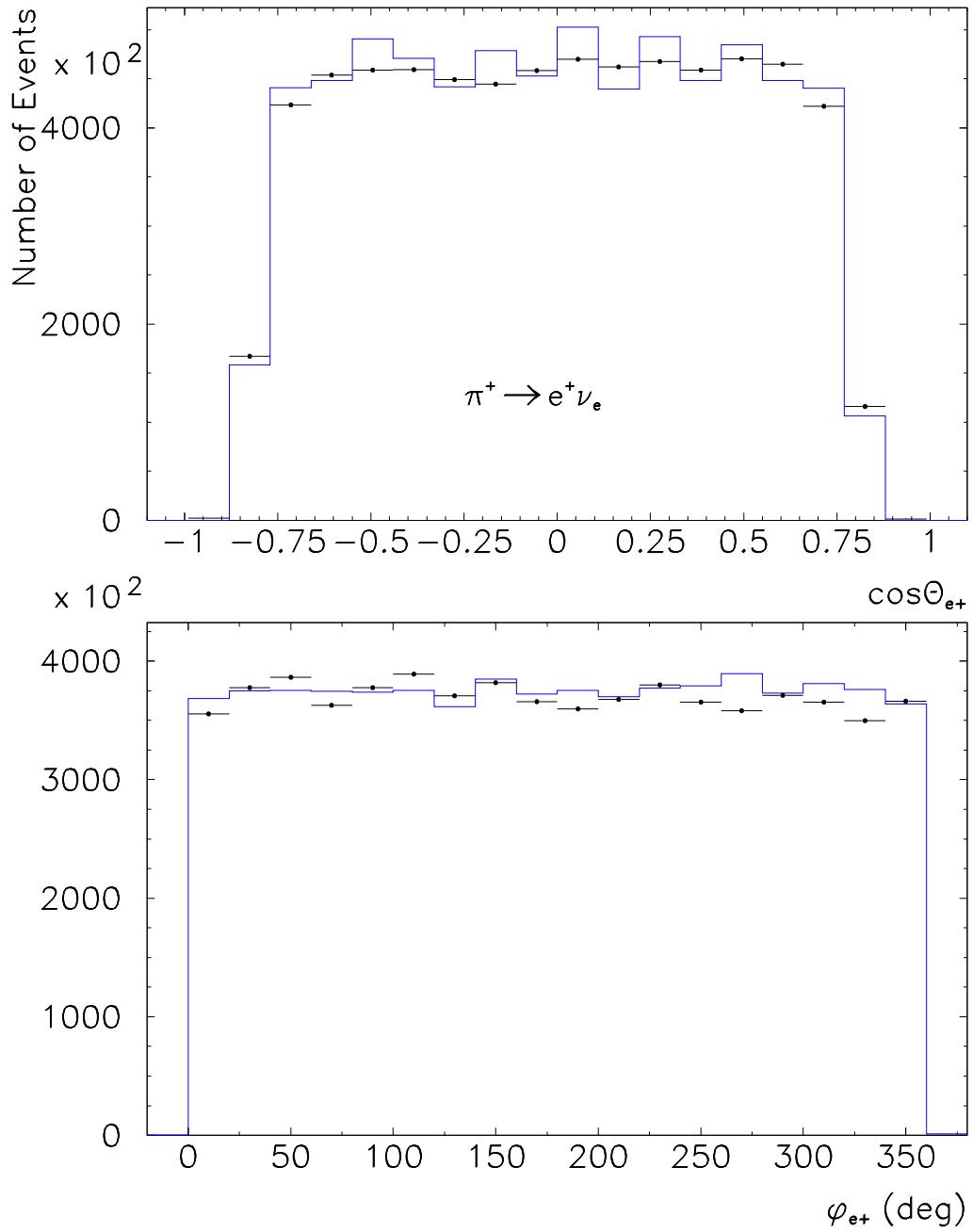
Preliminary Results: $\pi^+ \rightarrow e^+ \nu$



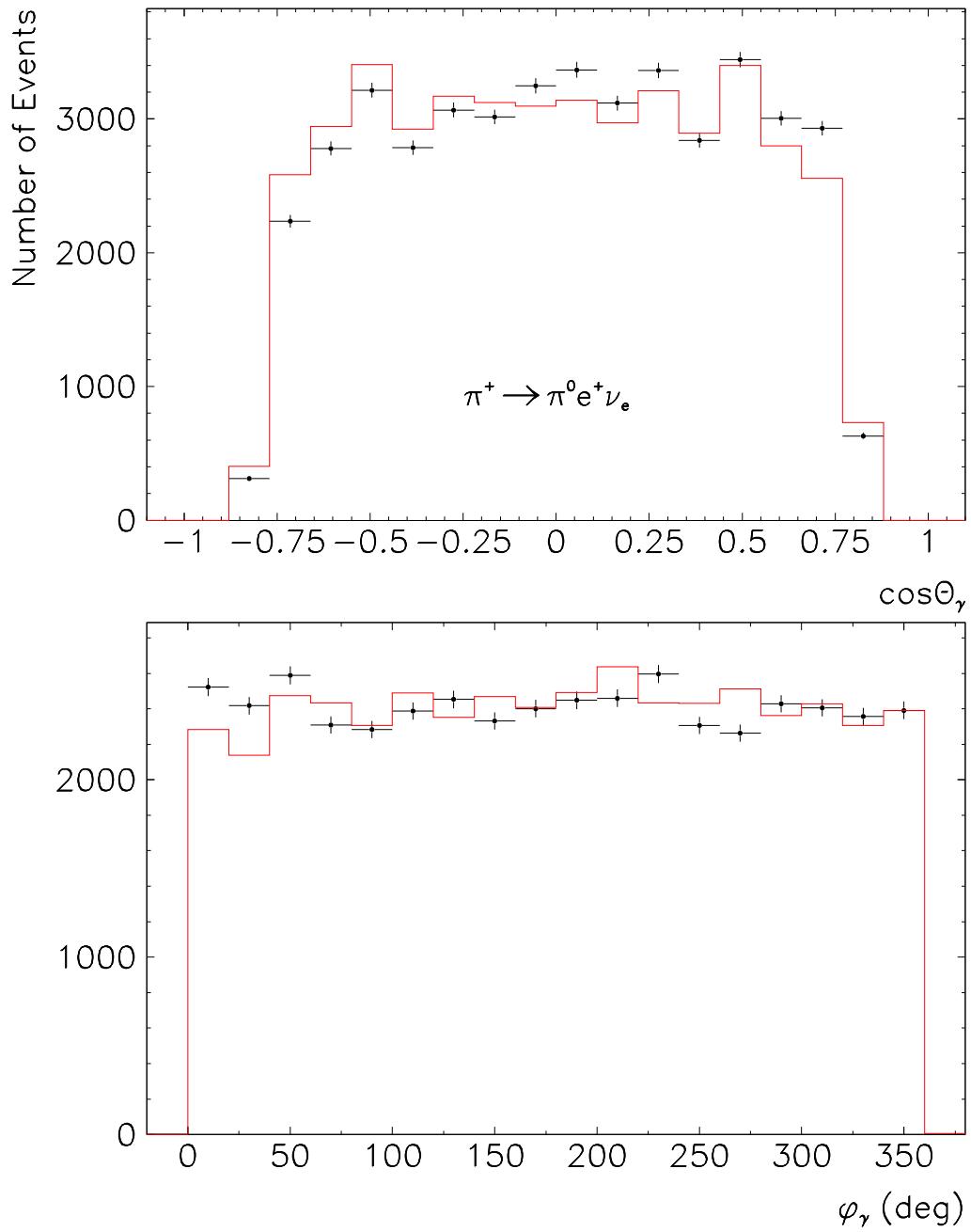
1999/2000 Partial Results – Preliminary



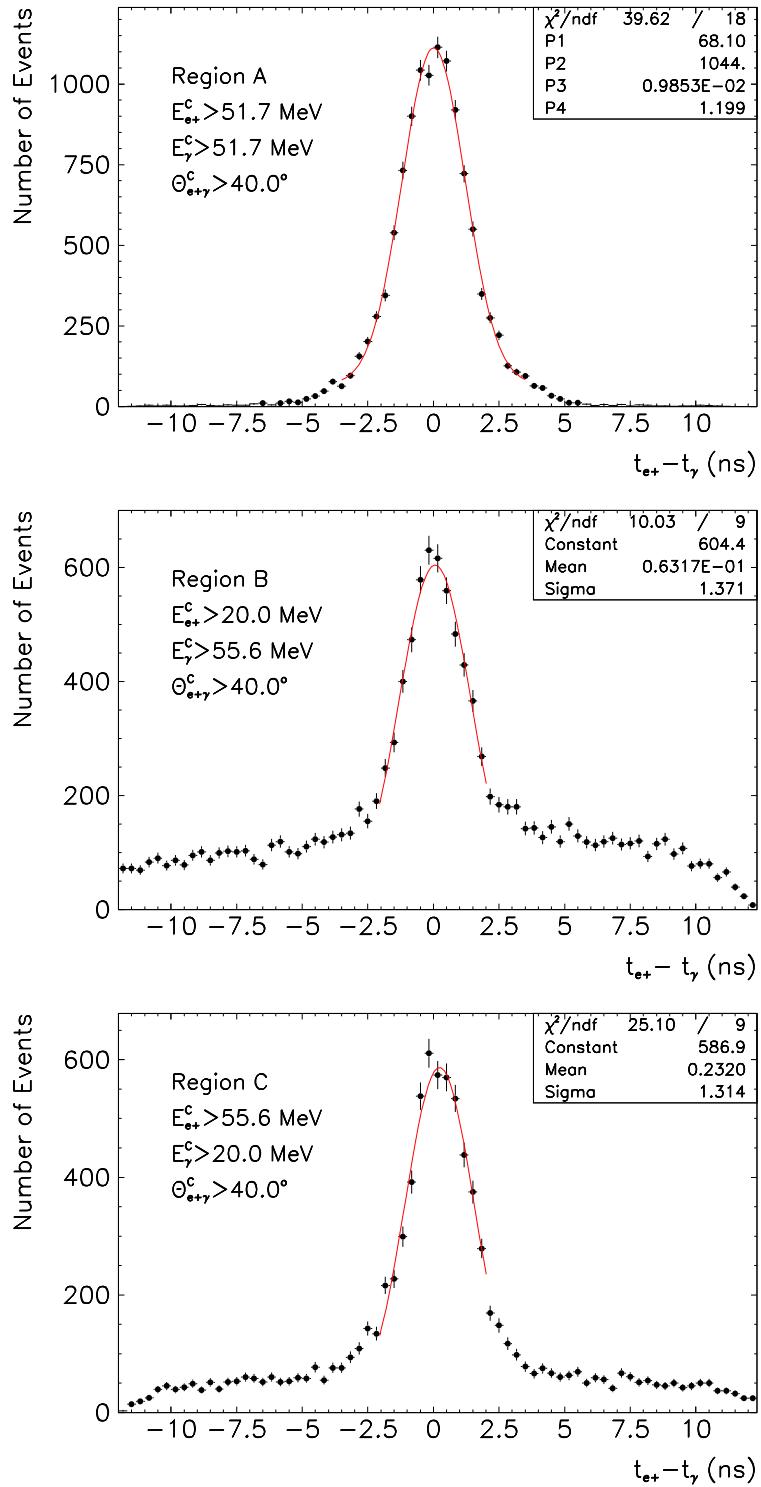
Angular acceptance: $\pi^+ \rightarrow e^+ \nu$



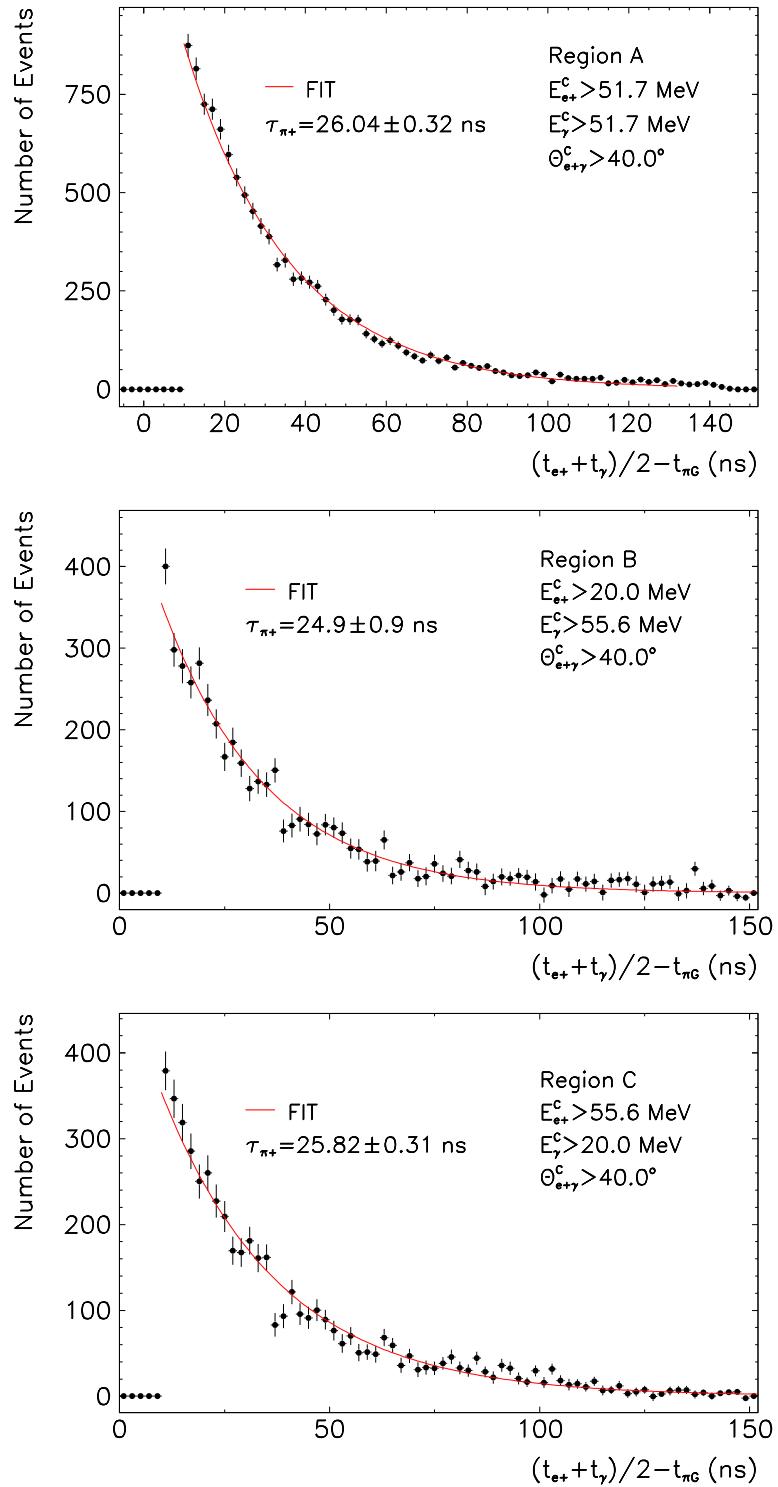
Angular acceptance: $\pi^+ \rightarrow \pi^0 e^+ \nu$



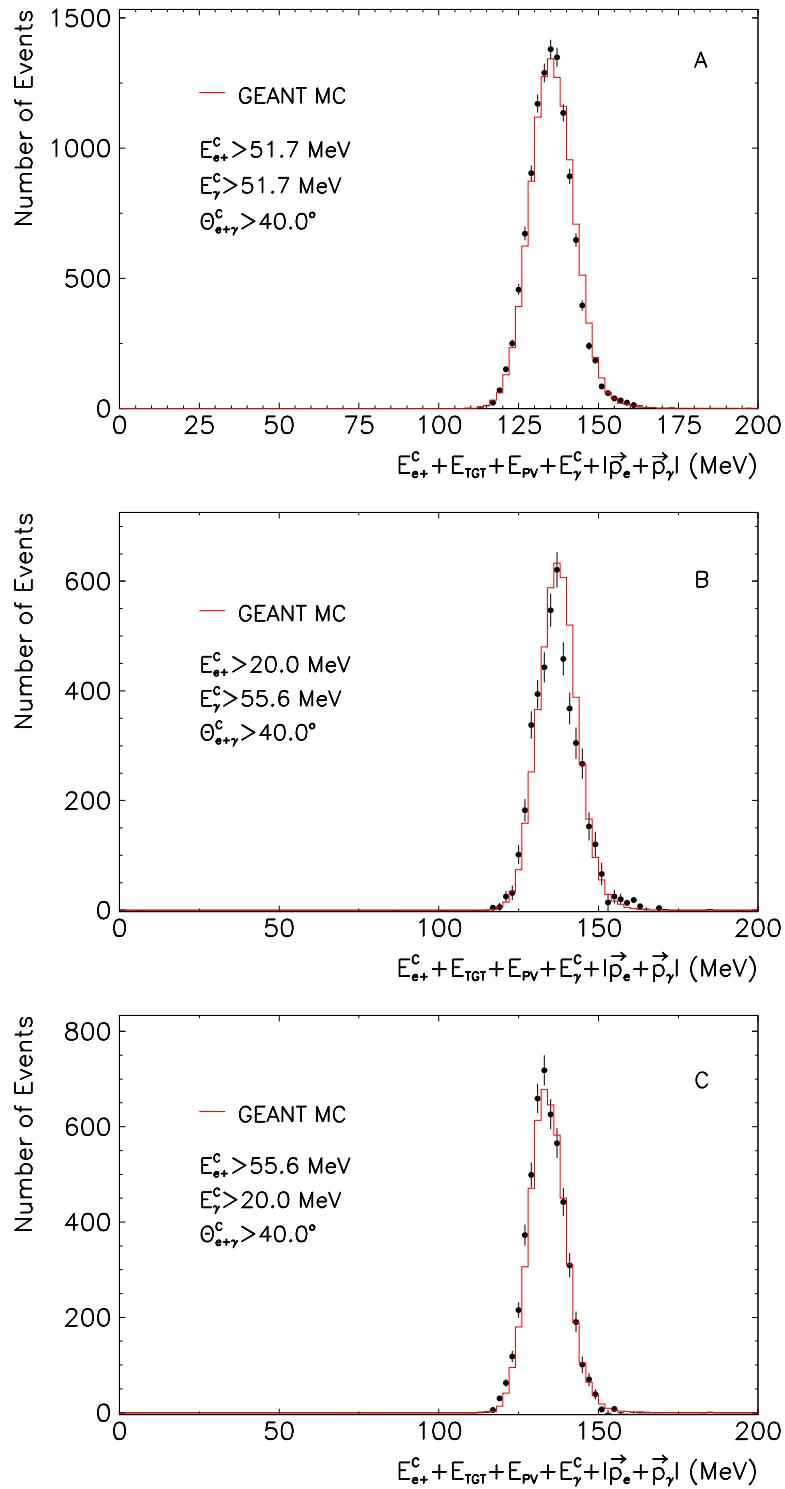
Preliminary Results: $\pi^+ \rightarrow e^+ \nu \gamma$ (S/B)



Preliminary Results: $\pi^+ \rightarrow e^+ \nu \gamma$ (t)



Preliminary Results: $\pi^+ \rightarrow e^+ \nu \gamma$ (m_π)

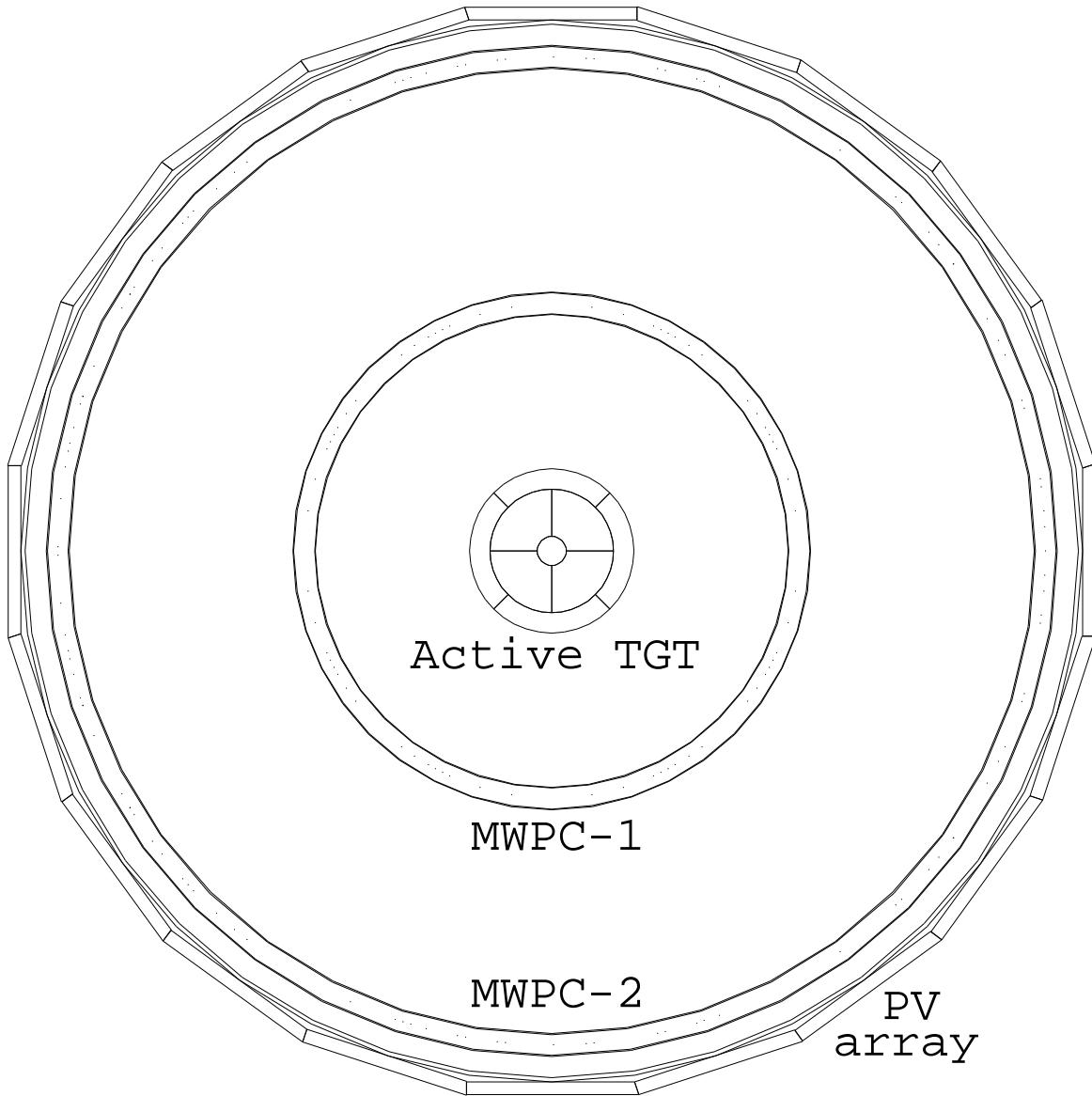


Experiment Systematics

Main sources of uncertainty:

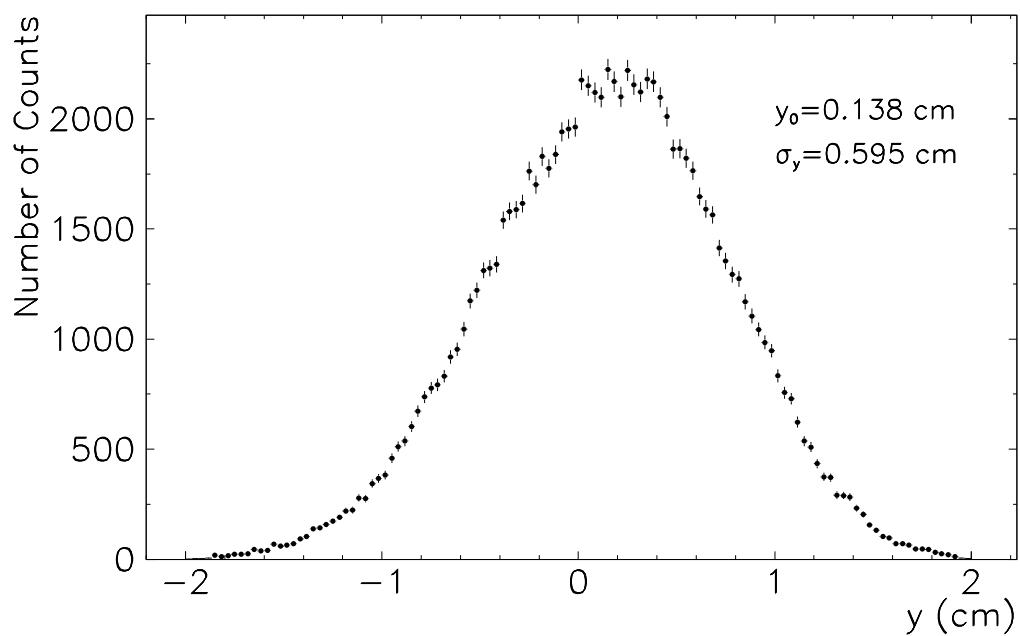
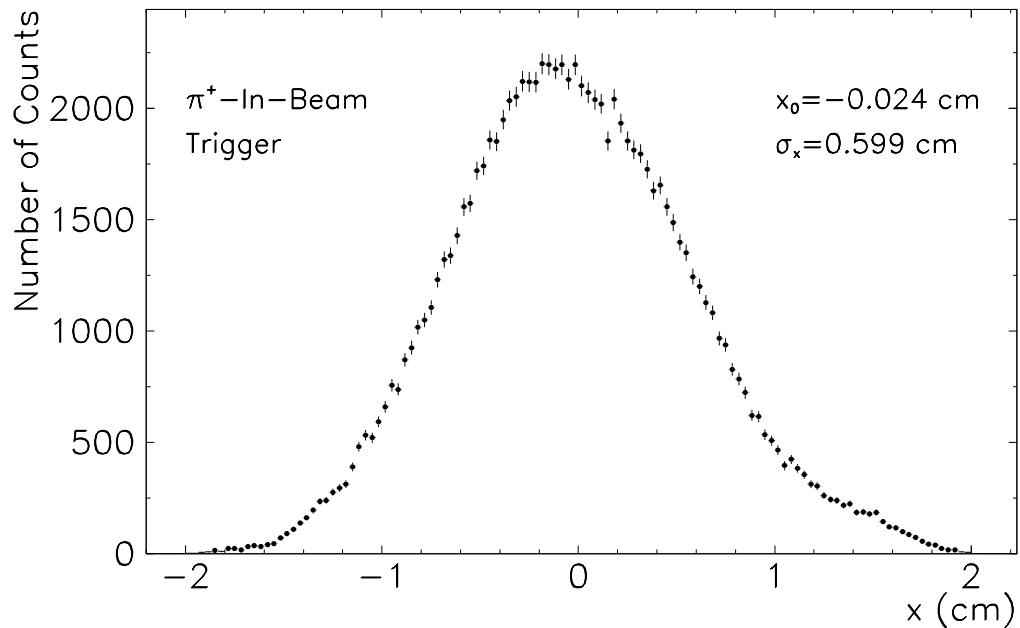
- Acceptance: beam geometry
- Timing: pion decay fraction
- External: $\text{BR}(\pi \rightarrow e\nu)$

Central detector region revisited

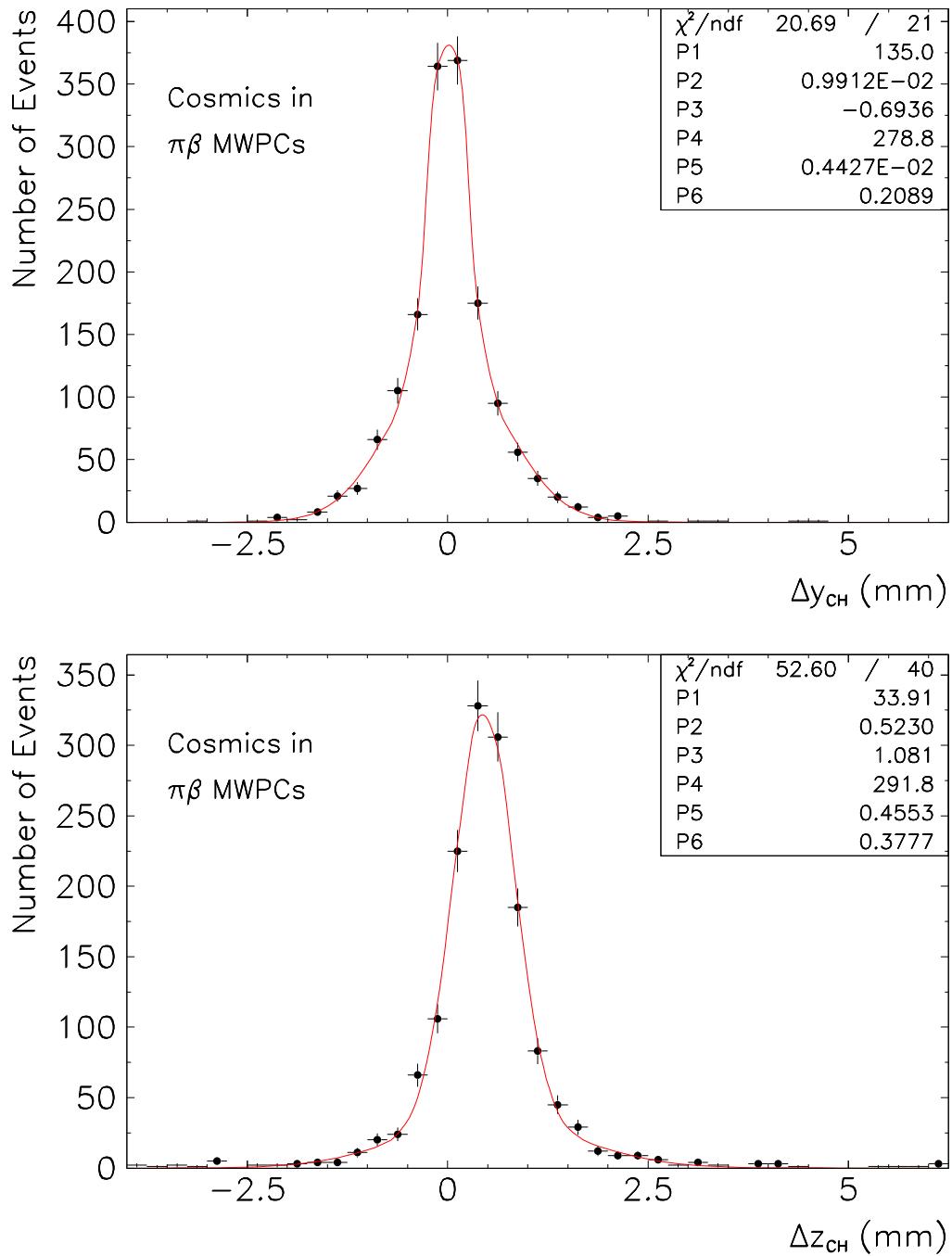


(beam is perpendicular at center)

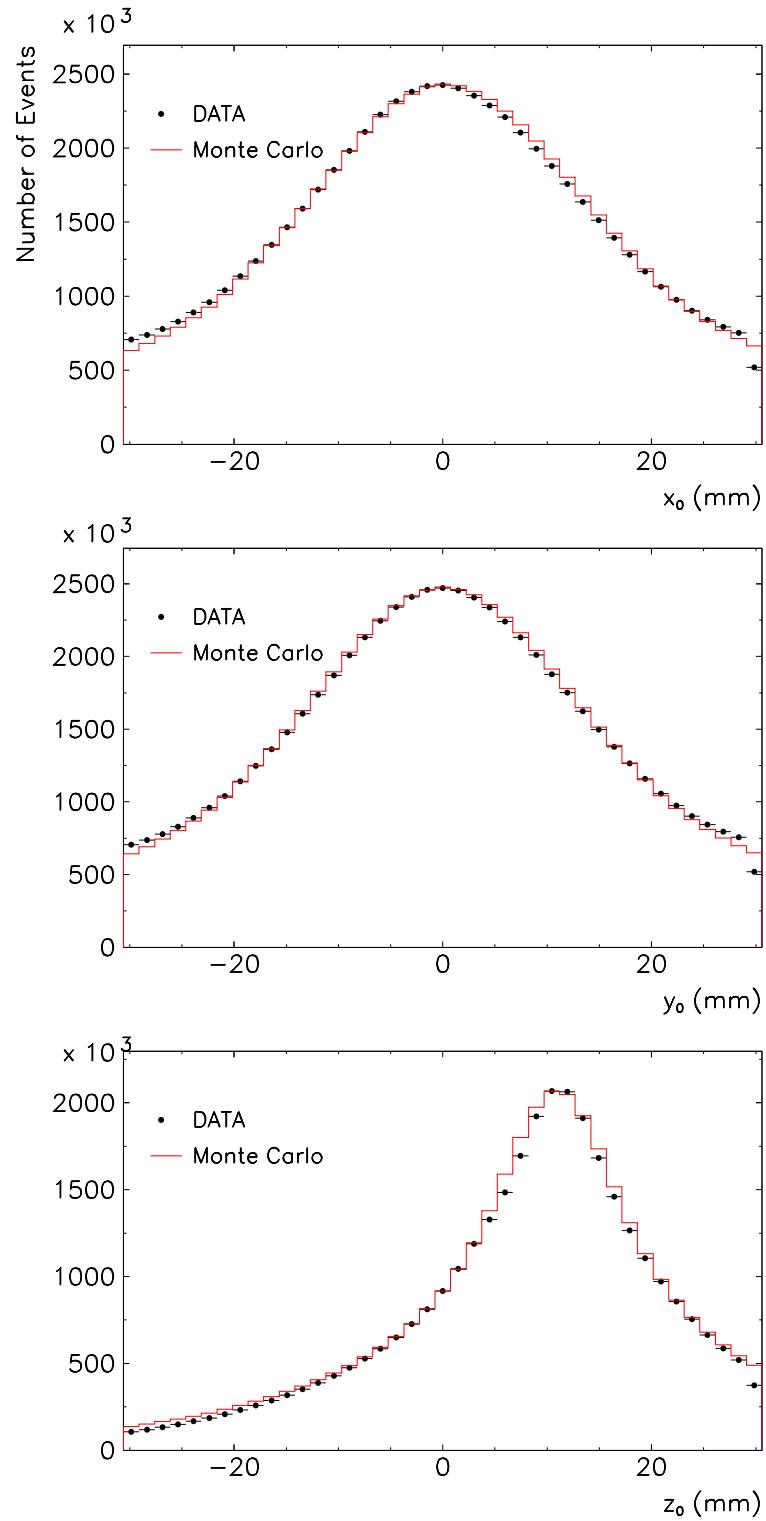
Beam geometry: TGT rate deconvolution



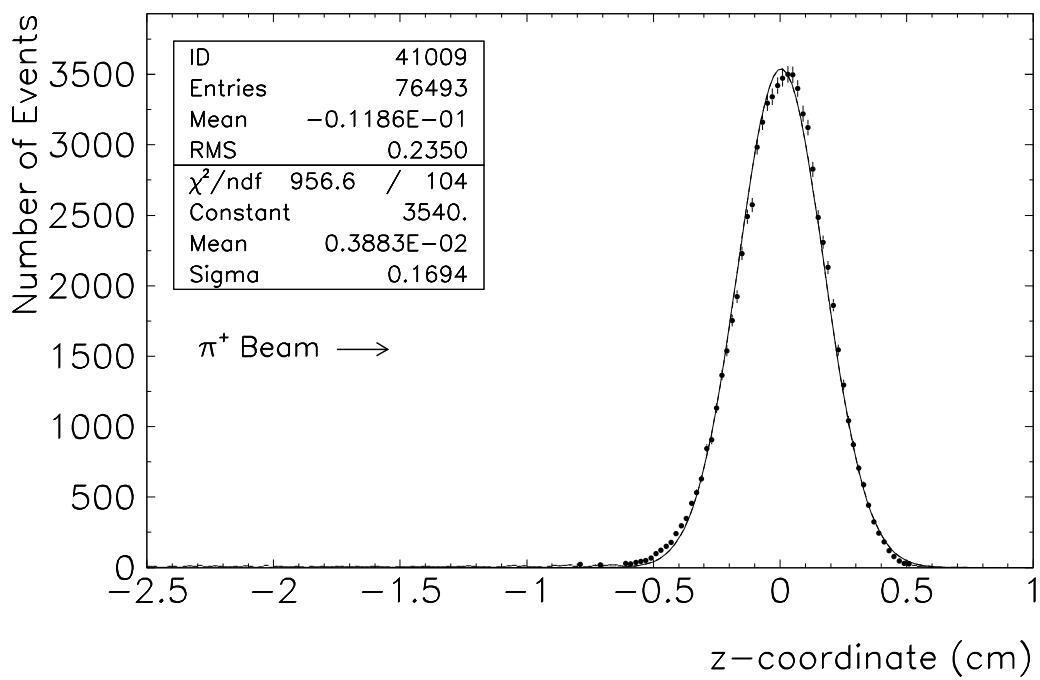
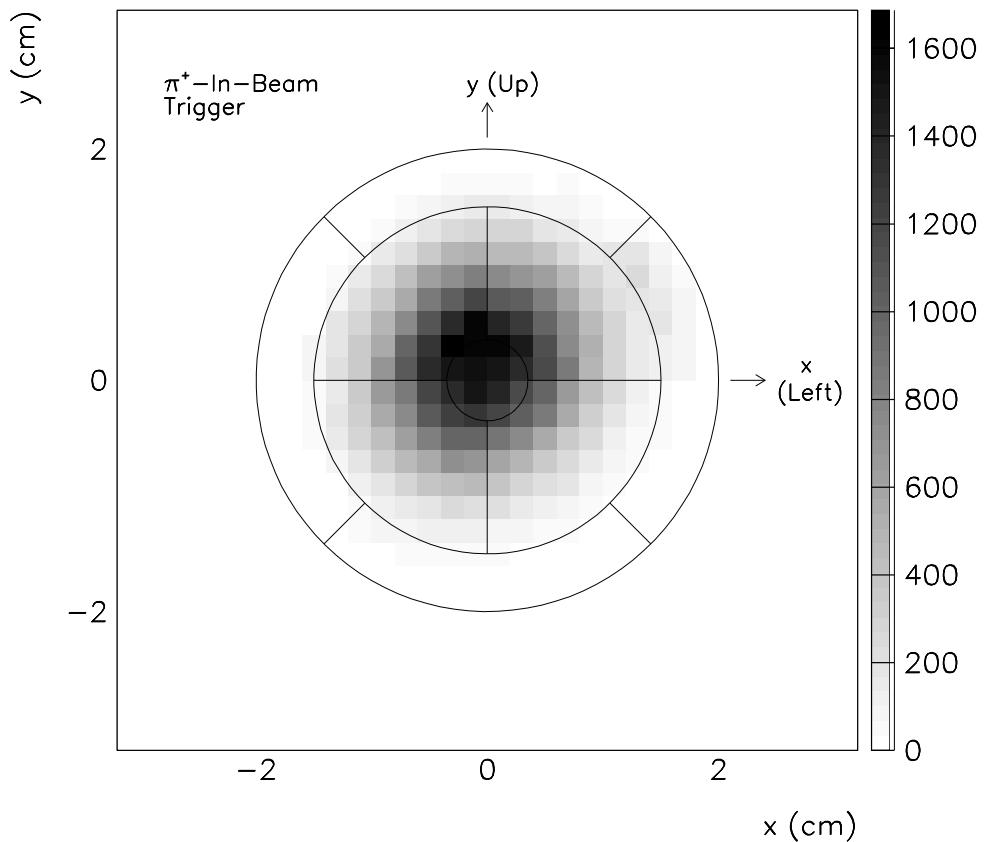
TGT tomography: MWPC resolution



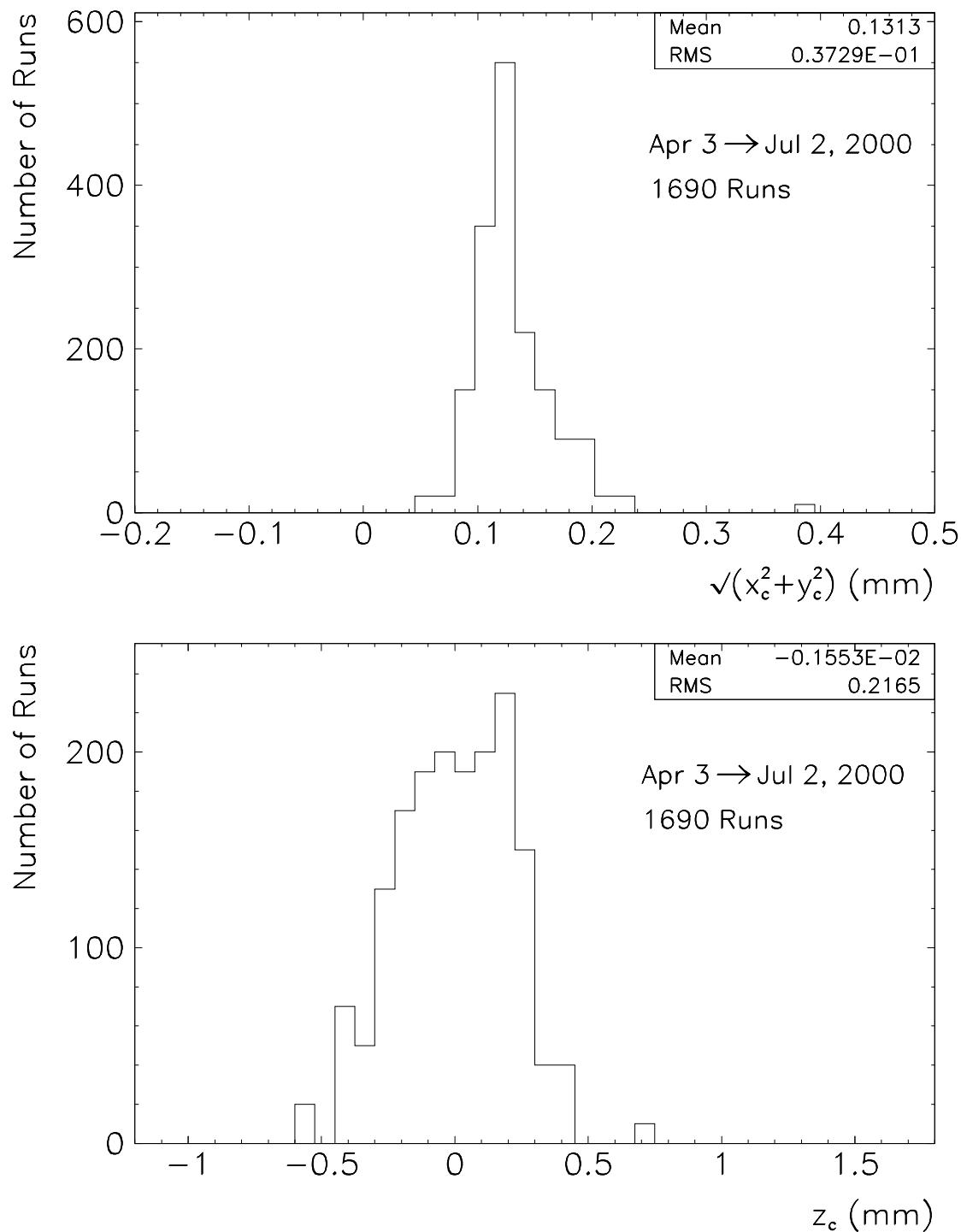
TGT tomography: track reconstruction



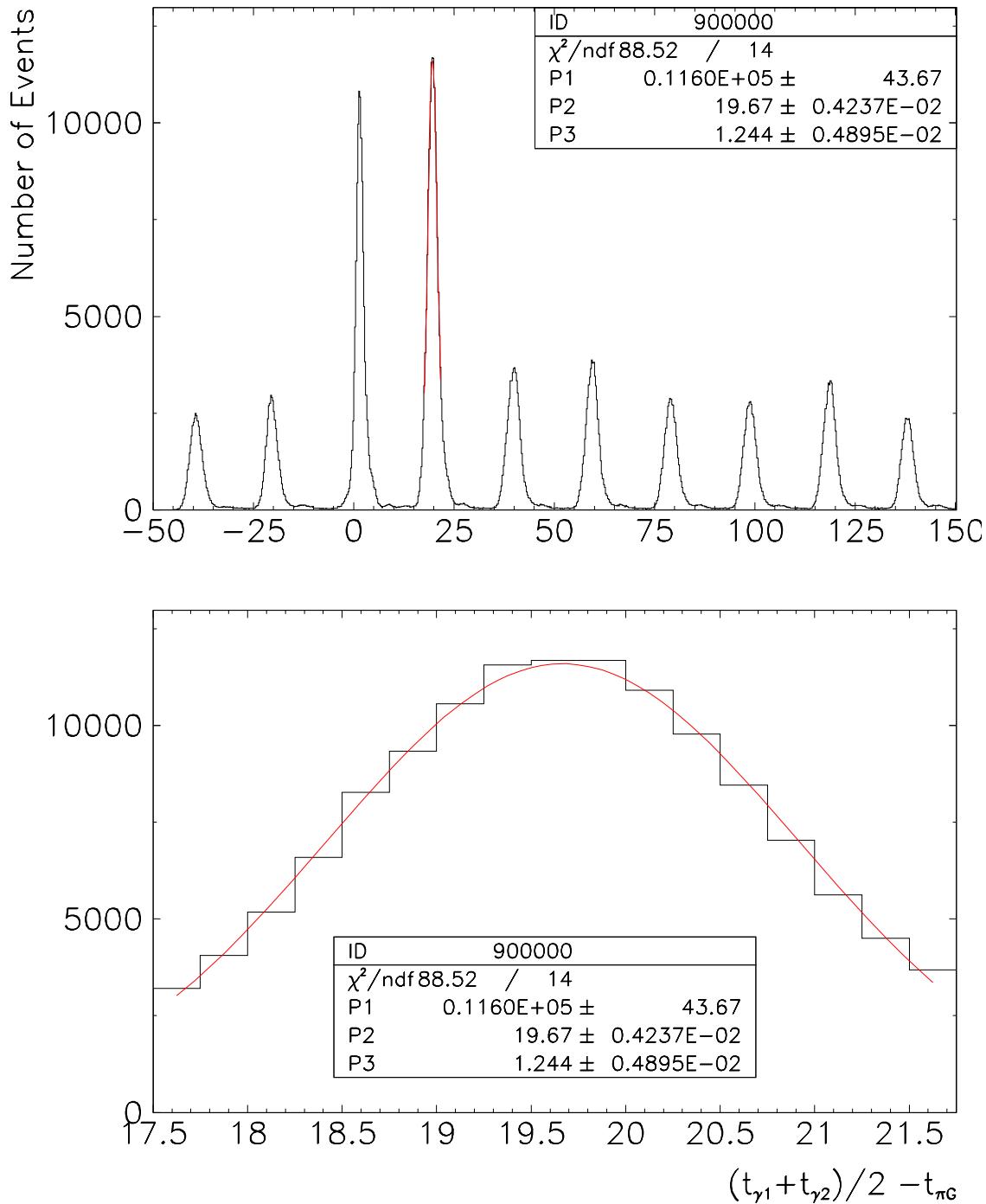
Beam geometry: π^+ stopping distribution



Beam stability



Pion stop timing



$\Delta t_{\text{peak}} \approx 4 \text{ ps}$

Preliminary Results

$$\pi^+ \rightarrow \pi^0 e^+ \nu$$

Branching Ratio for $\pi\beta$ Decay

Our Preliminary Interim Result:

$$\text{BR} \simeq 1.044 \pm 0.007 \pm 0.009 \times 10^{-8}$$

(stat.) (syst.)

PRELIMINARY

McFarlane et al. (Phys. Rev. D 1985):

$$\text{BR} \simeq 1.026 \pm 0.039 \times 10^{-8}$$

SM Prediction (PDG, 2002):

$$\begin{aligned} \text{BR} = & 1.038 - 1.041 \times 10^{-8} & (90\% \text{ C.L.}) \\ & (1.005 - 1.008 \times 10^{-8} & \text{excl. rad. corr.}) \end{aligned}$$

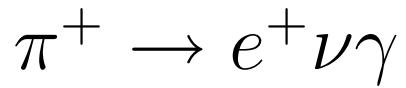
$$\text{PDG 2002: } V_{ud} = 0.9734(8)$$

$$\text{PIBETA prelim: } V_{ud} = 0.9765(56).$$

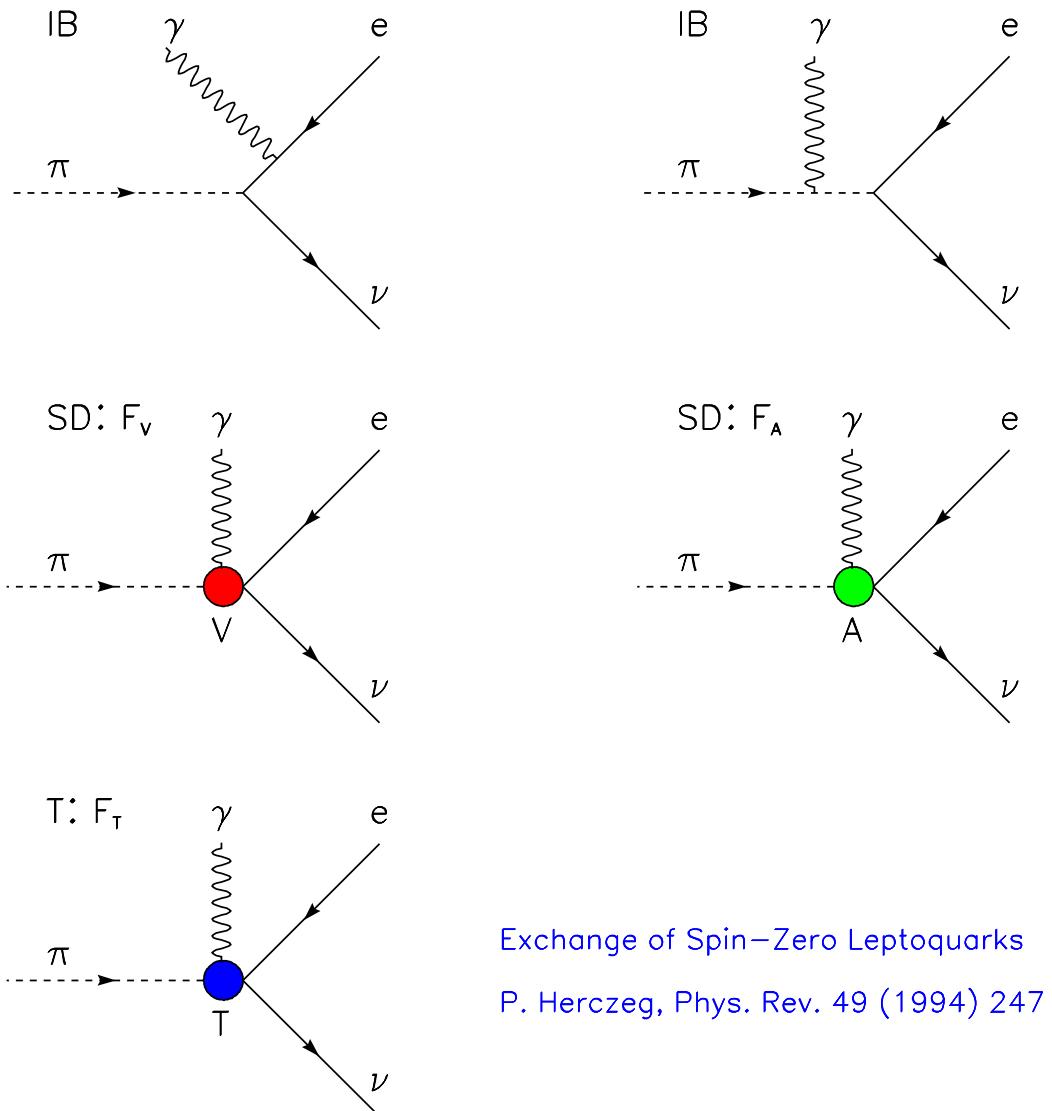
Summary of $\pi\beta$ Uncertainties

at end of analysis phase:	current	final
	(%)	(%)
external		
pion lifetime	0.019	0.019
$BR(\pi \rightarrow e\nu)$	0.33	$\sim 0.1?$
$BR(\pi^0 \rightarrow \gamma\gamma)$	0.032	0.032
internal		
$A(\pi\beta)/A(e\nu)$	0.5	< 0.3
$\Delta t(\gamma - e)$	0.03	0.03
E threshold	< 0.1	< 0.1
statistical:	0.7	~ 0.4
total:	~ 0.9	$\lesssim 0.5$

Radiative Pion Decay



Anything beside $V-A$ in RPD?



AVAILABLE DATA on *Pion Form Factors*

$$|\mathcal{F}_V| \stackrel{\text{cvc}}{=} \frac{1}{\alpha} \sqrt{\frac{2\hbar}{\pi \tau_{\pi^0} m_{\pi^0}}} = 0.0259(5) .$$

$\mathcal{F}_A \times 10^4$	reference
106 ± 60	Bolotov et al. (1990)
135 ± 16	Bay et al. (1986)
60 ± 30	Piilonen et al. (1986)
110 ± 30	Stetz et al. (1979)
116 ± 16	world average (PDG 2002)

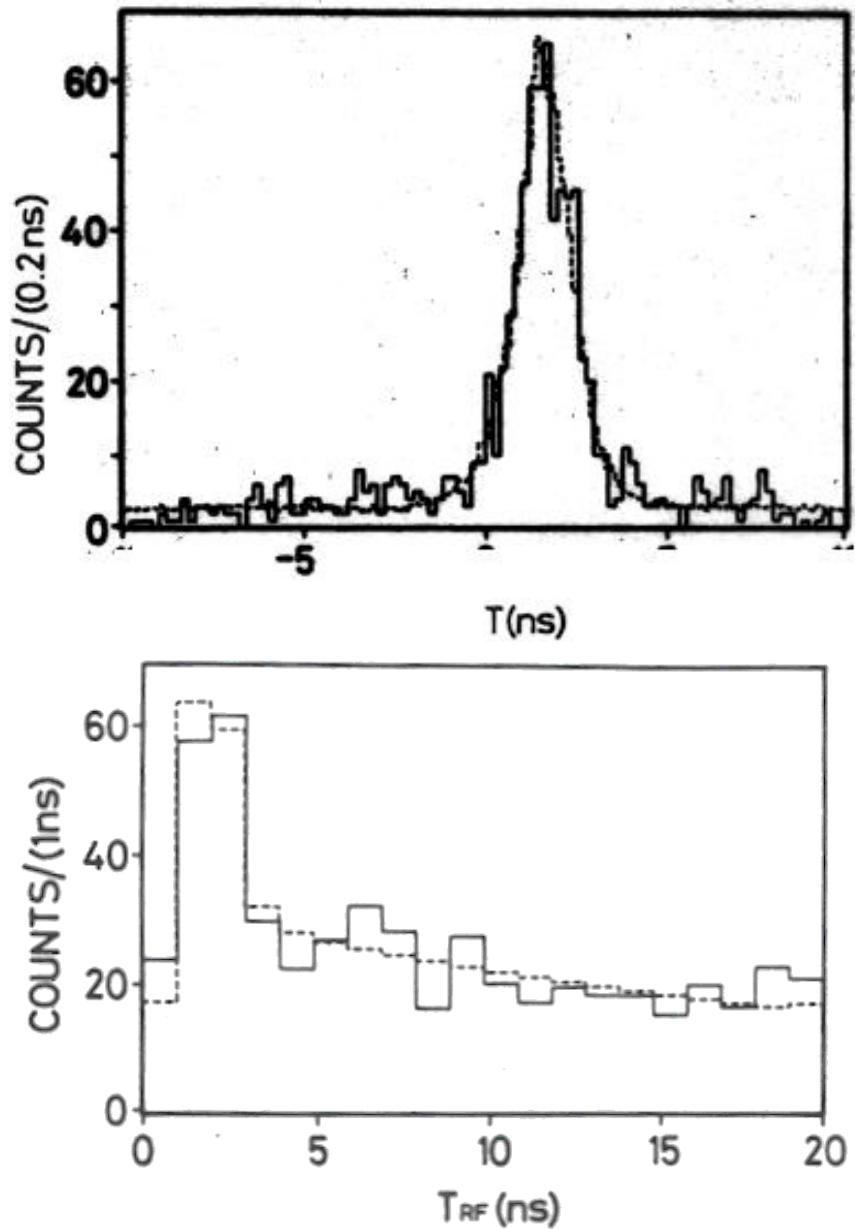
Poblaguev (1990, '92) found:

- (a) inconsistencies in data set (part. ISTRa data),
- (b) need to include $T q-l$ coupling:

$$\mathcal{F}_T \sim -0.0056 \pm 0.0017 .$$

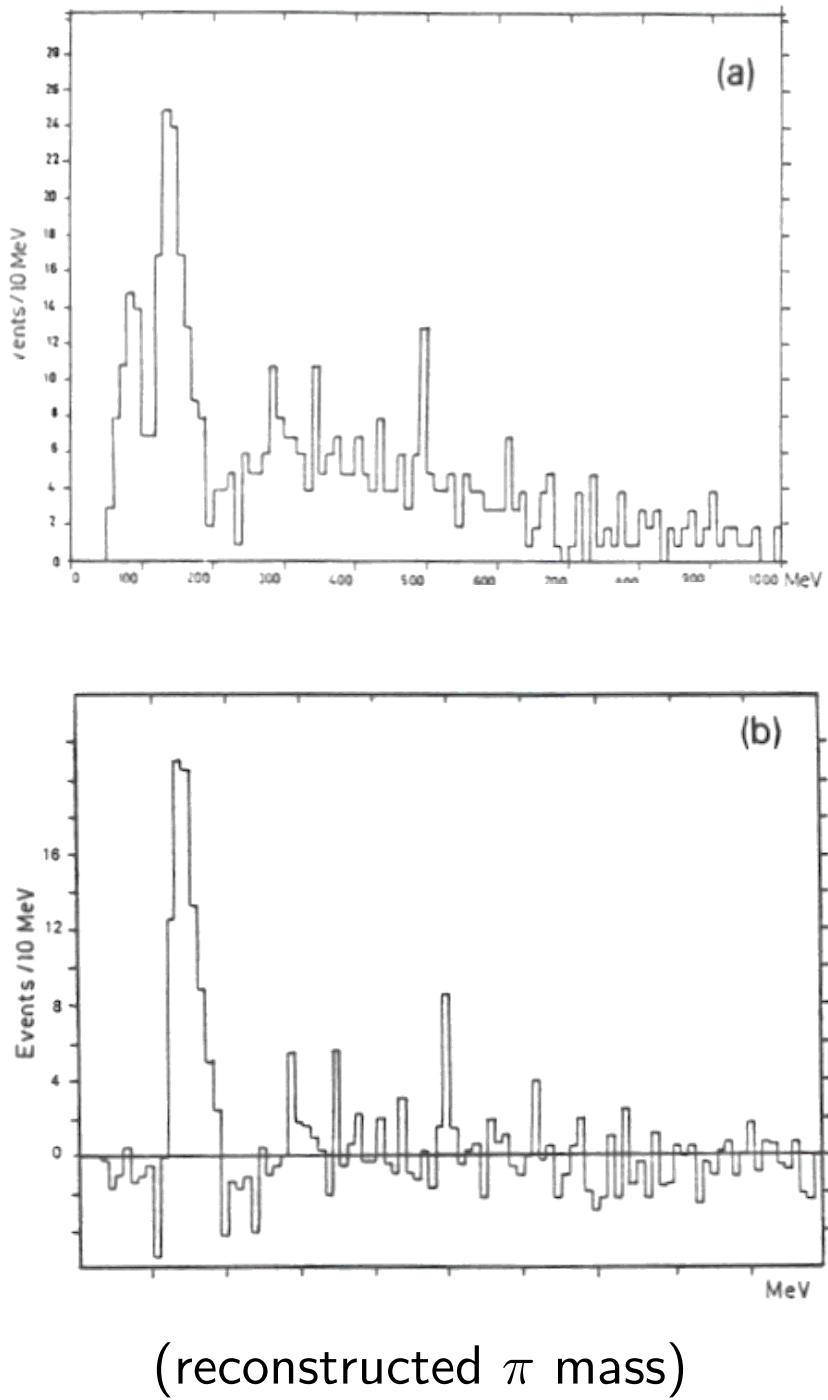
Herczeg (1994) confirmed there is room (barely) for F_T of the above order of magnitude. Only plausible explanation—leptoquarks at tree level.

Previous $\pi \rightarrow e^+ \nu \gamma$ experiments



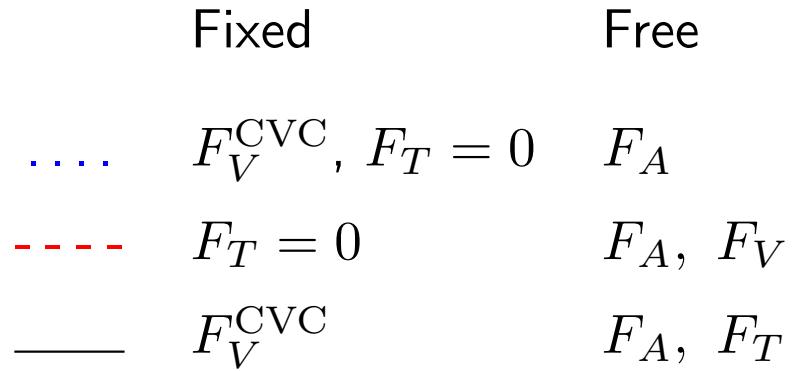
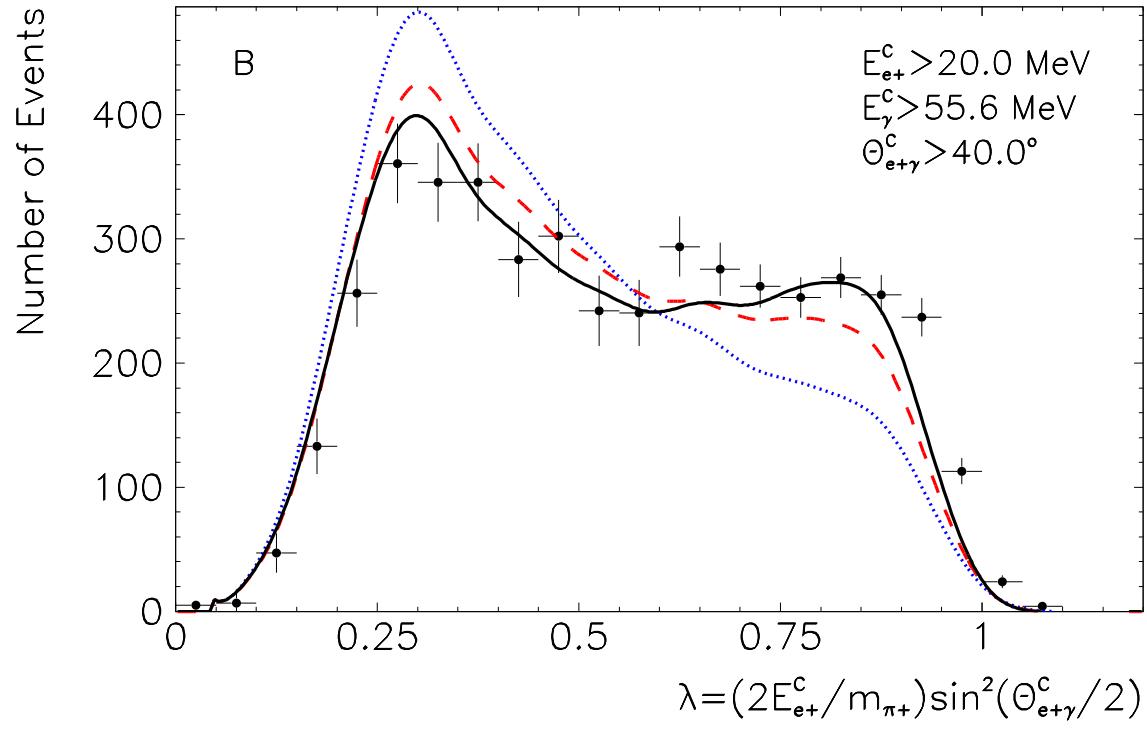
Bay et al., PSI 1986

Previous $\pi \rightarrow e^+ \nu \gamma$ experiments



Bolotov et al., IHEP, Protvino, 1990

PRELIMINARY RESULTS: $\pi^+ \rightarrow e^+ \nu \gamma$



A Glimpse at Pion Form Factors

- based on analysis of regions A and B only,
- 2-dim fits exclude border regions in acceptance

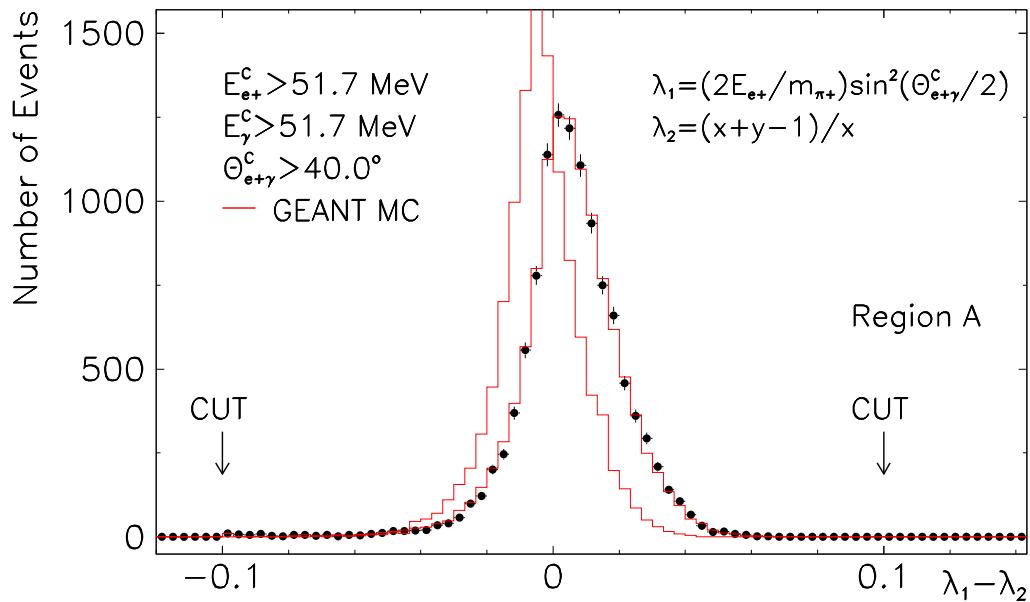
Fit	Fixed parameters	Fit parameters	χ^2
	$F_V: 0.0170(80)$		
'PDG'	$F_A: 0.0116(16)$	none	9.2
	$F_T: 0$		
'SM'	$F_V: 0.0259(5)$	$F_A: -0.0028(1)$	5.6
	$F_T: 0$		
all free	$F_T: 0$	$F_V: 0.0136(13)$	2.3
no T		$F_A: 0.0136(13)$	
CVC	$F_V: 0.0259(5)$	$F_A: 0.0067(6)$	1.1
+T		$F_T: -0.0017(1)$	

In the meantime we:

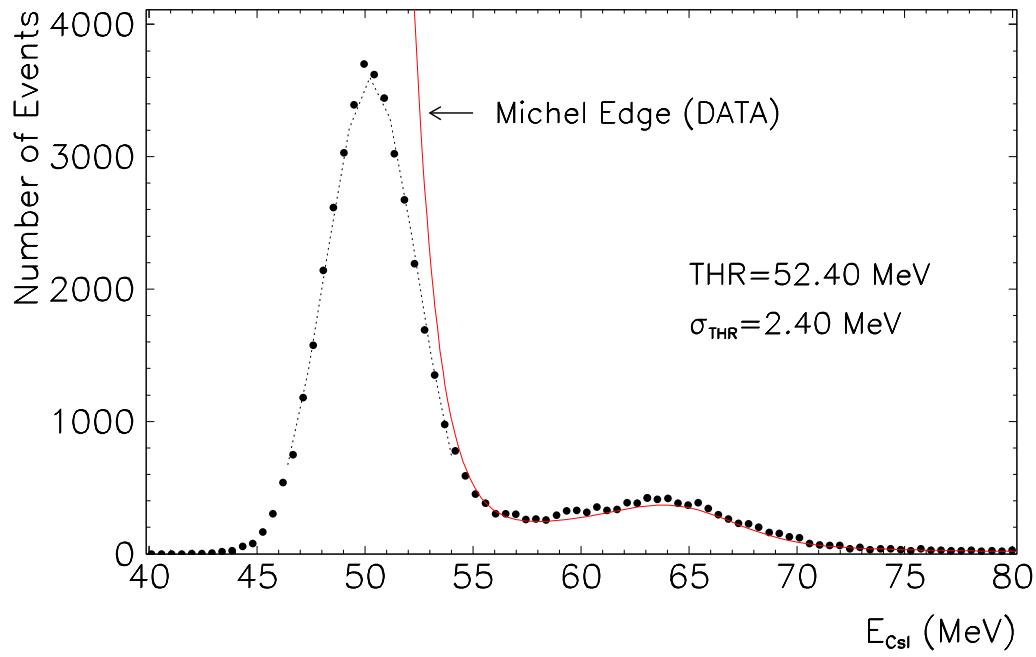
- have reduced region C background,
- have refined aspects of MC simulation,
- are pursuing additional global fit strategies.

A Closer Look at Energy Calibration

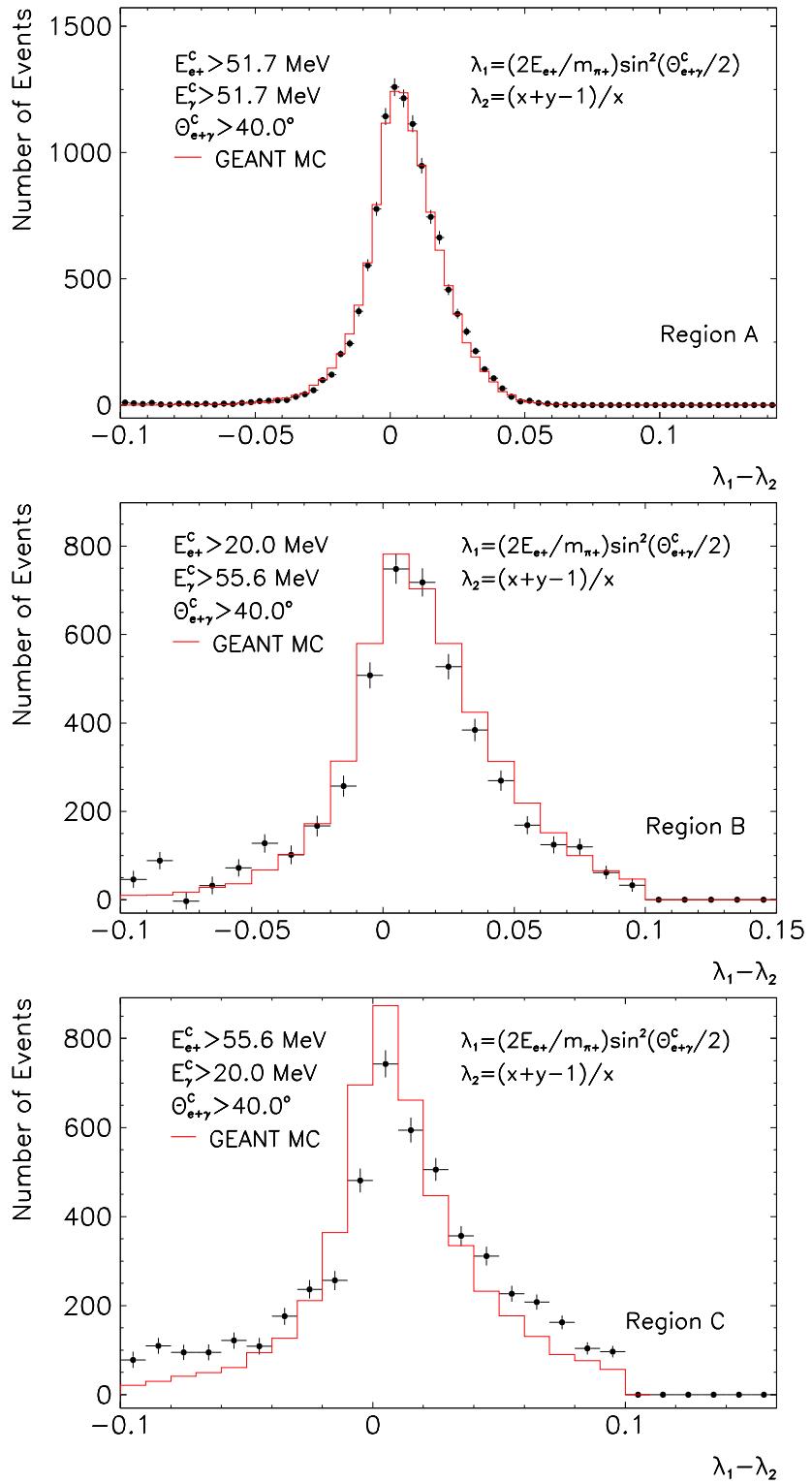
effect of a 1% gain variation:



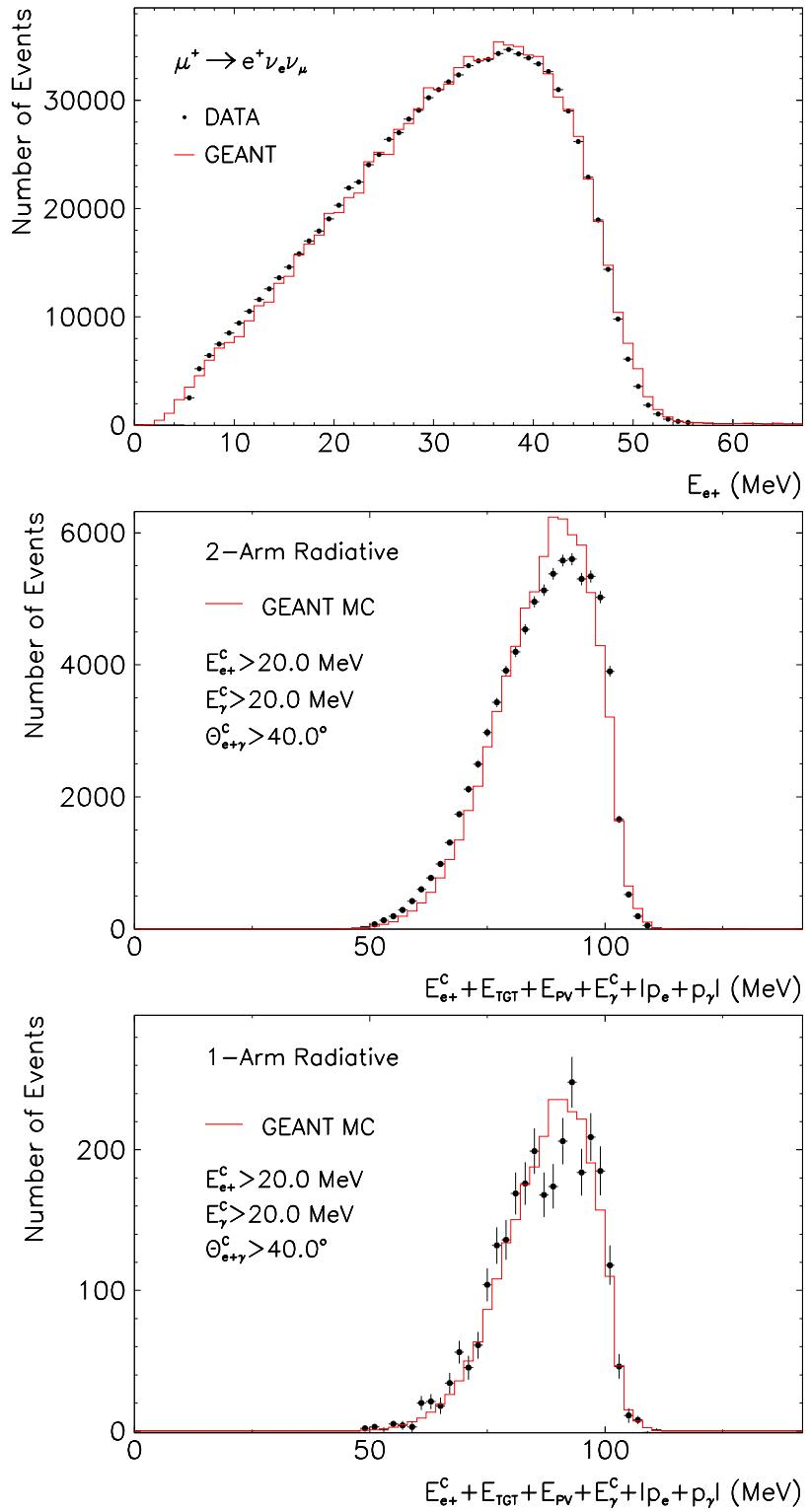
Michel edge and π_{e2} peak:



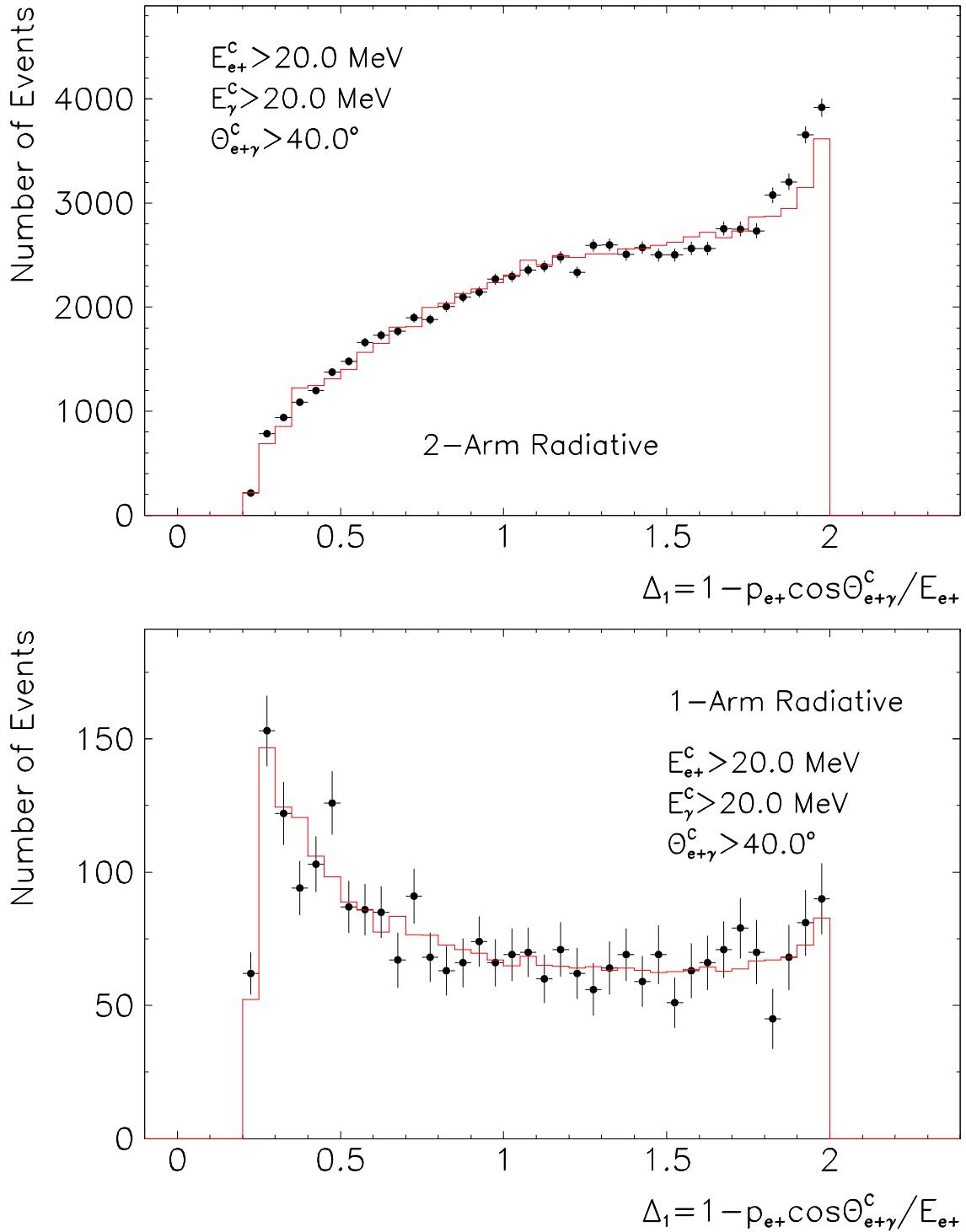
More on Energy Calibration



A Look at Muon Decays



More on Radiative Muon Decays



What We've Learned

- Very high precision experiments are needed in order to study truly rare processes.
- There appear to be no surprises in the pion beta decay channel.
- The accepted description of the $\pi \rightarrow e\nu\gamma$ process is inadequate, and will require revision.

Plans for the Future

- Bring analysis up to the proposed level of uncertainty.
- Prepare new proposal and collaboration for a precise $\pi \rightarrow e\nu$ measurement.
- We are actively considering a new search for the $\pi^0 \rightarrow \gamma\gamma\gamma$ decay using the PIBETA apparatus.

<http://pibeta.phys.virginia.edu/>
<http://pibeta.web.psi.ch/>