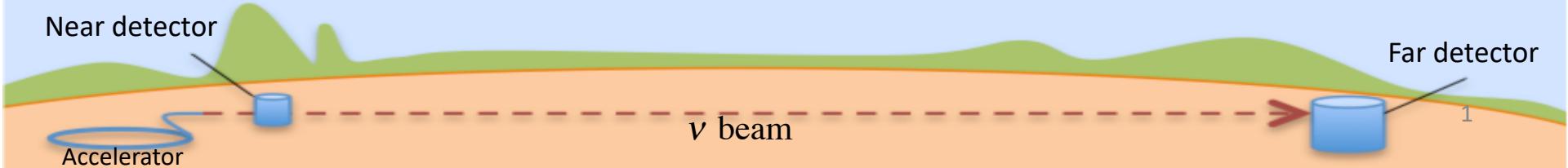


# Constraining neutrino-nucleus interactions with electron scattering data

Mariana Khachatryan - ODU

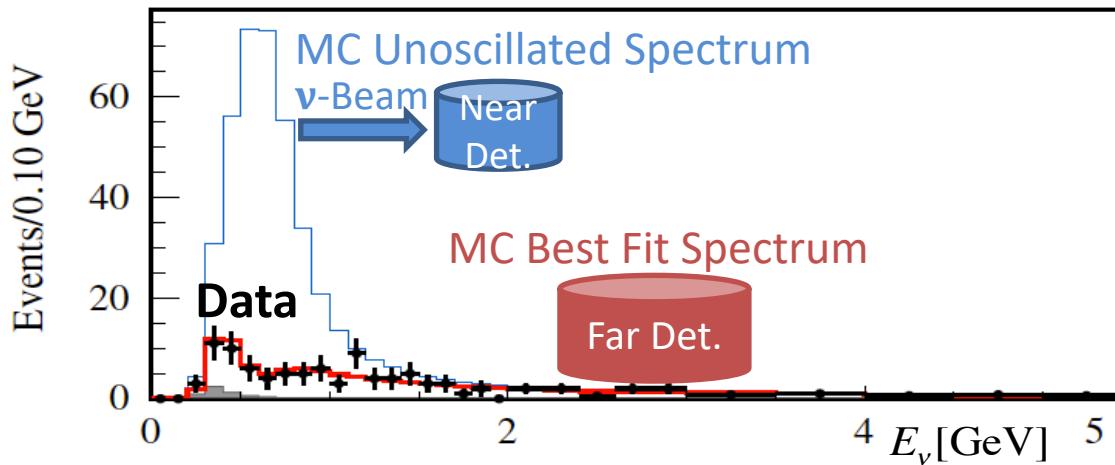


# Outline

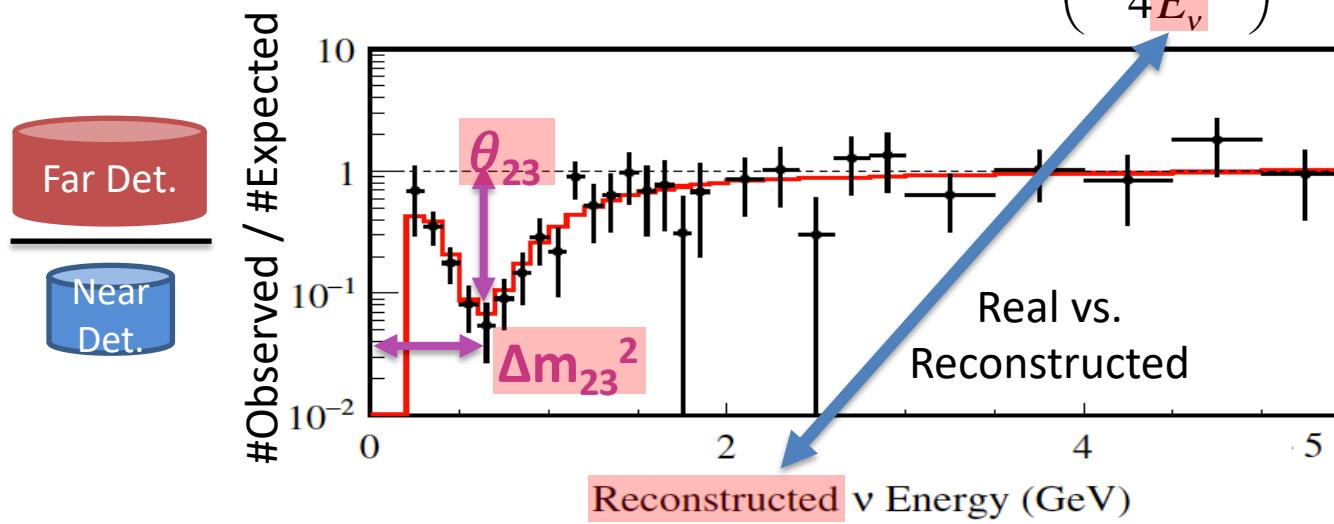
- The importance of energy reconstruction in neutrino oscillation experiments.
- What can we learn from e- scattering studies?
- Testing neutrino beam energy reconstruction methods with electron scattering JLab CLAS data.

# (Long Baseline) Oscillation Challenge

T2K experiment L=295km

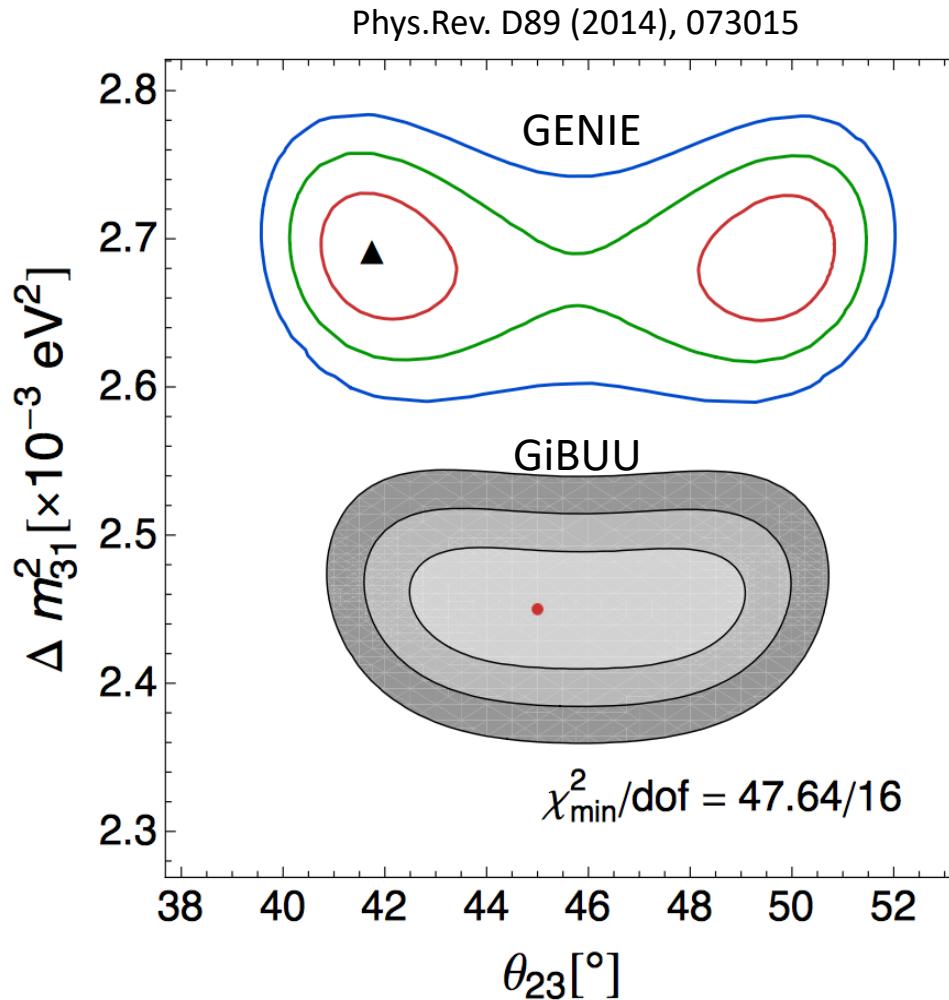


$$P(\nu_\mu \rightarrow \nu_\mu) = \sin^2(2\theta_{23}) \times \sin^2\left(\frac{\Delta m_{32}^2 L}{4E_\nu}\right)$$



# Neutrino-nucleus interaction modeling

=> Incorrect neutrino-nucleus interaction modeling can bias the extracted oscillation parameters



Events created with GiBUU and reconstructed with GiBUU and GENIE.

# Energy Reconstruction for QE reactions

## (1) Cherenkov detectors:

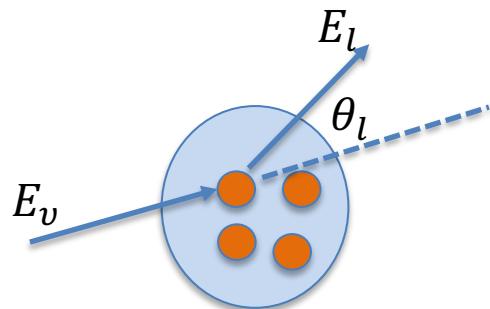
- Detect: leptons & pions
- Miss: protons and neutrons

## (2) Tracking detectors:

- Detect: Charged particles +  $\pi^0$
- Miss: Neutrons and charged particles below threshold.

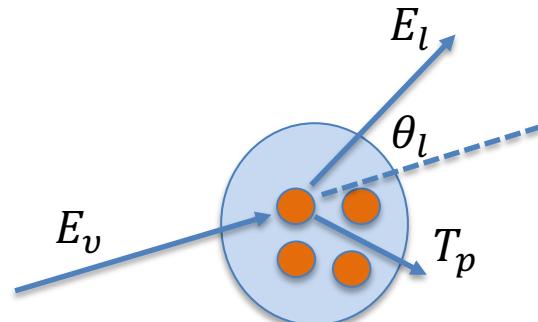
Use Lepton kinematics  
Assuming QE interaction

$$E_{QE} = \frac{2M\varepsilon + 2ME_l - m_l^2}{2(M - E_l + |k_l| \cos(\theta_l))}$$



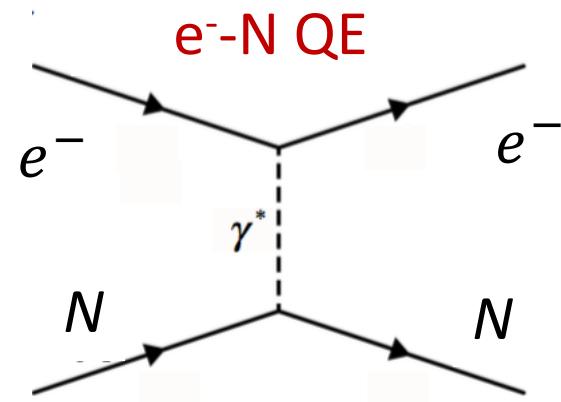
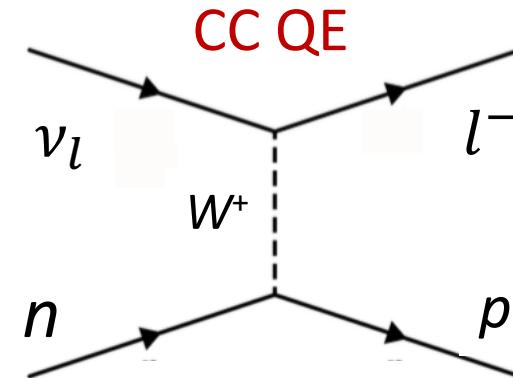
Use Final-State Calorimetry  
Assuming low residual excitations

$$E_{Cal} = E_l + T_p + \varepsilon$$

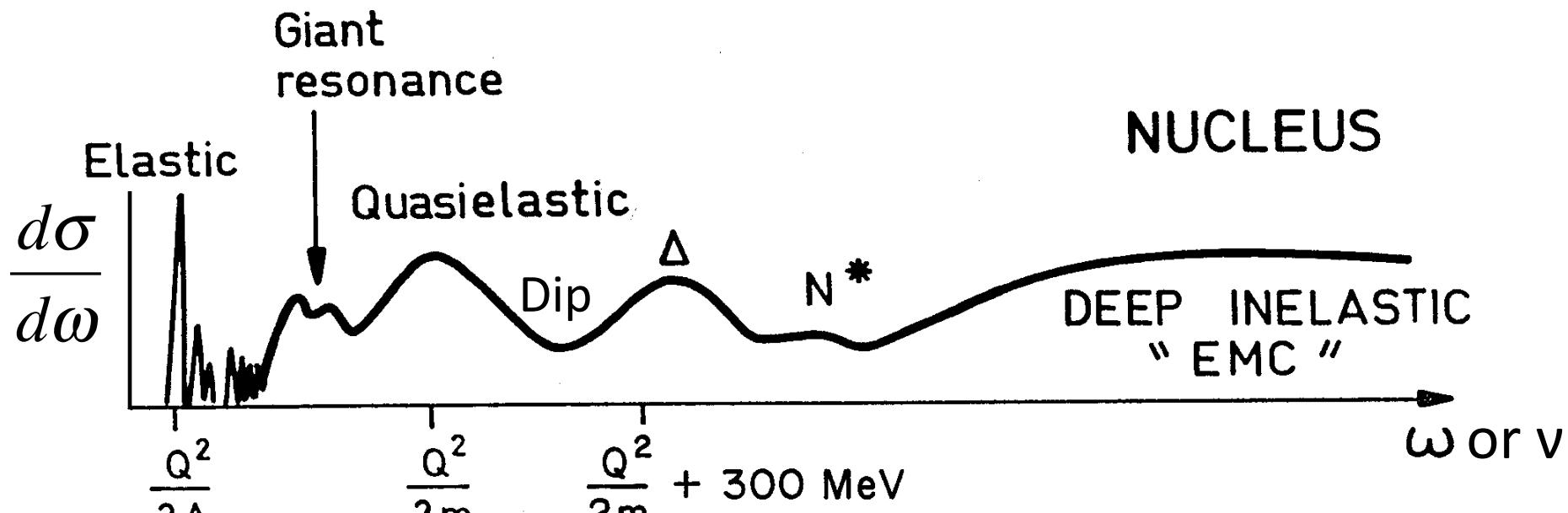


# Why electrons?

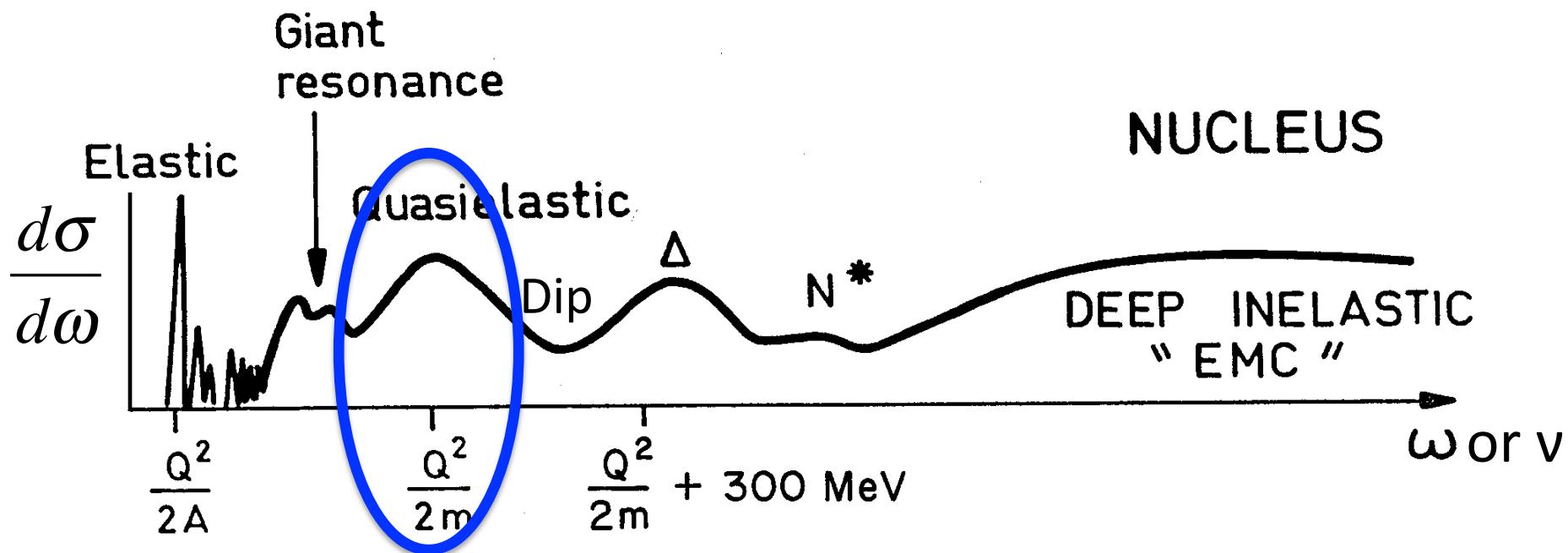
- Known incident energy
- High intensity
- Similar interaction with nuclei
  - Single boson exchange
  - CC Weak current [vector plus axial]
    - $j_\mu^\pm = \bar{u} \frac{-ig_W}{2\sqrt{2}} (\gamma^\mu - \gamma^\mu \gamma^5) u$
  - EM current [vector]
    - $j_\mu^{em} = \bar{u} \gamma^\mu u$
- Similar nuclear physics



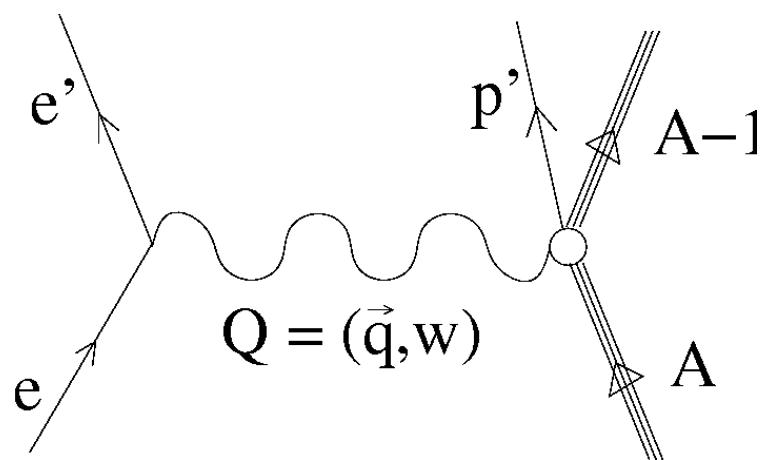
# Nuclear Physics



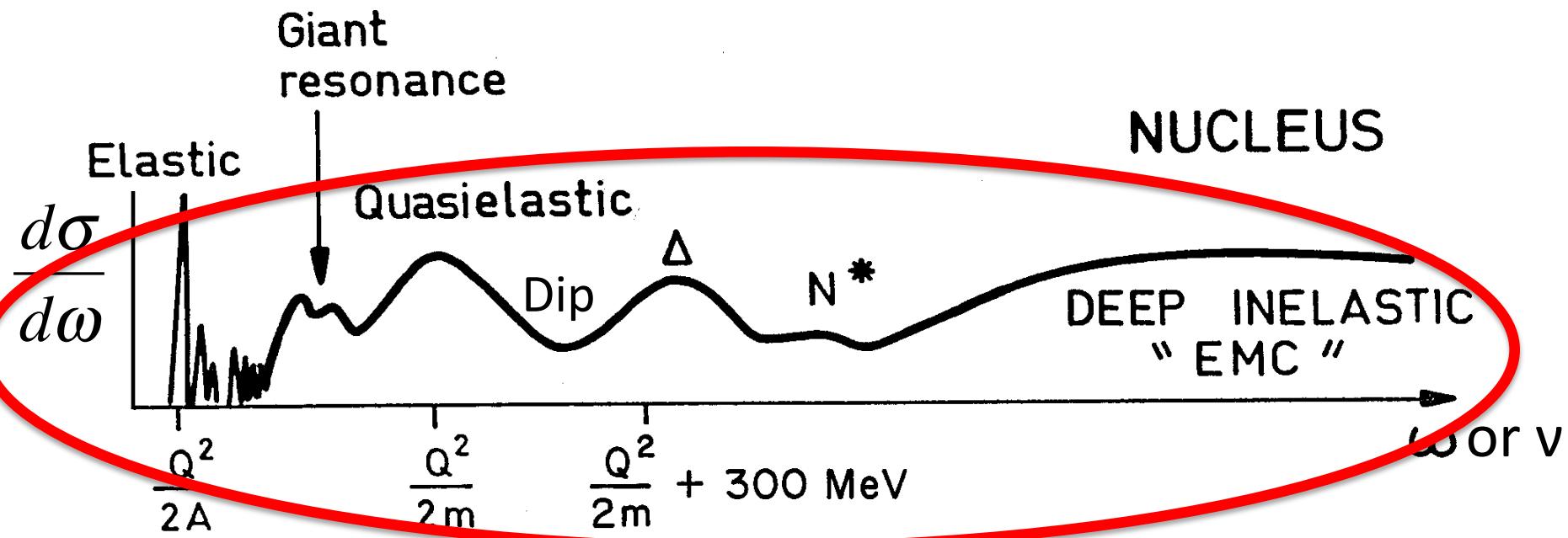
# Nuclear Physics



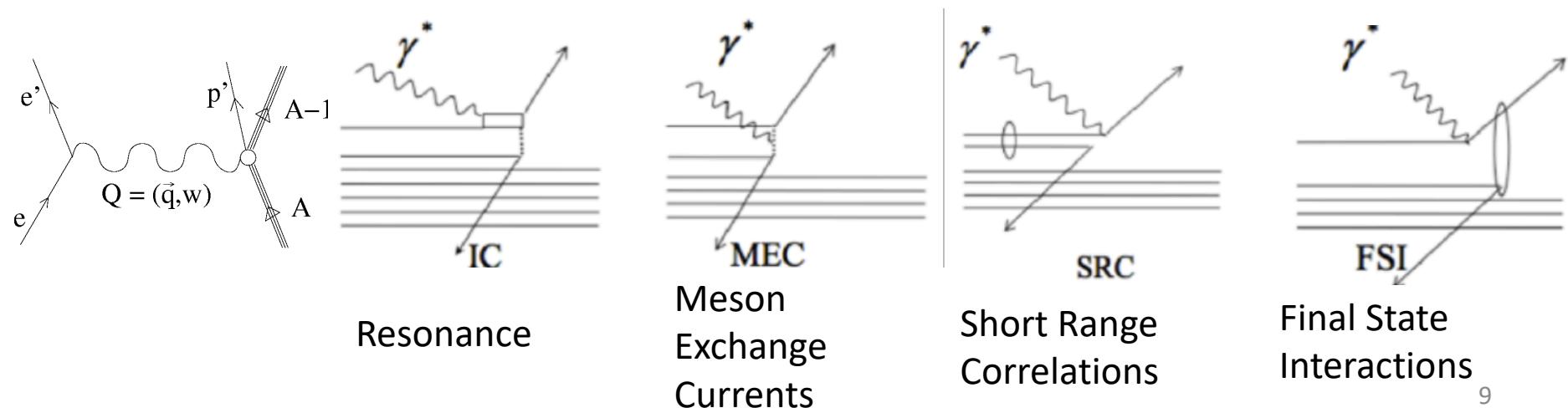
What neutrino expts want



# Nuclear Physics



What we get (even for Opi)



# E2a experiment

Targets:

CLAS:  ${}^3\text{He}$ ,  ${}^4\text{He}$ ,  ${}^{12}\text{C}$ ,  ${}^{56}\text{Fe}$

T2K: CH,  $\text{H}_2\text{O}$

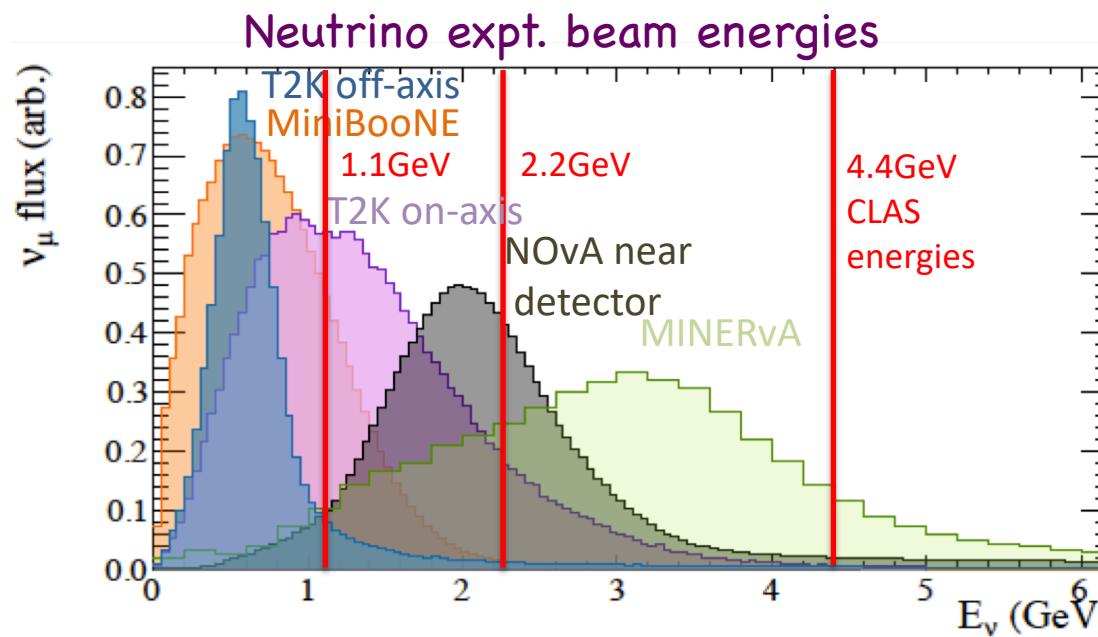
Minerva:  ${}^3\text{He}$ ,  ${}^4\text{He}$ , C, Fe,  $\text{H}_2\text{O}$

Microboone: Ar

Miniboone: mineral oil (C, H, O)

Nova:  $\text{C}_6\text{H}_3(\text{CH}_3)_3$

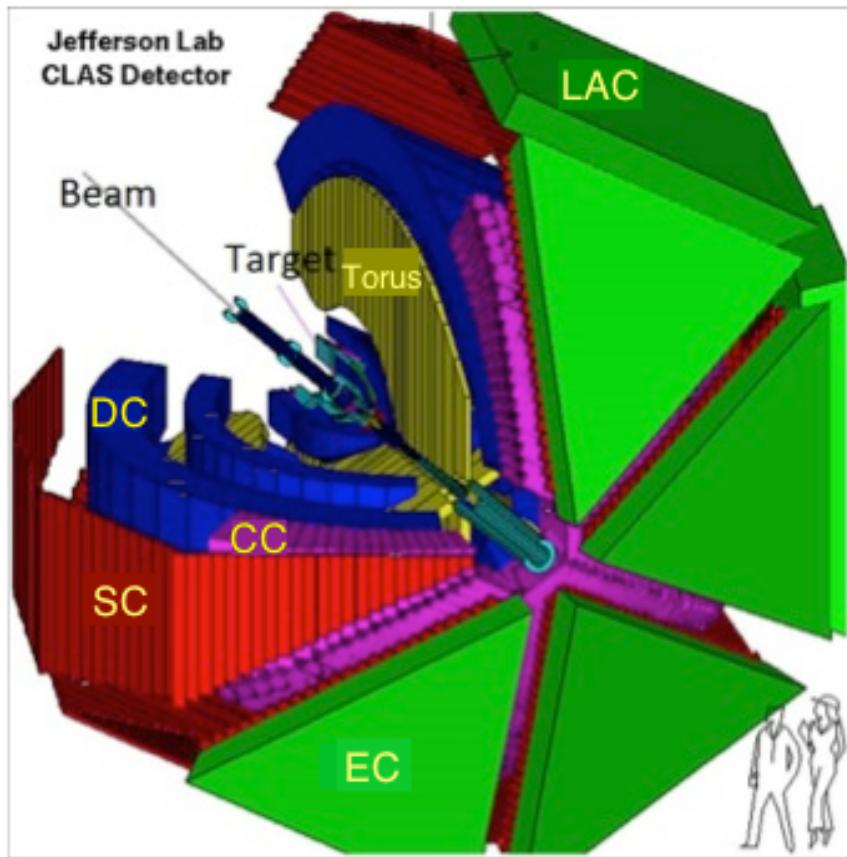
DUNE: Ar



Scale the electron scattering data with  $1/\sigma_{\text{Mott}}$   
to have 'neutrino like' data!

# CLAS detector package

## 3D view



- ❖ 4 $\pi$  acceptance (almost).
- ❖ Charged particles (8-143°):
  - $P_p > 300$  MeV/c
  - $P_\pi > 150$  MeV/c
- ❖ Neutral particles:
  - EM calorimeter (8-45°)

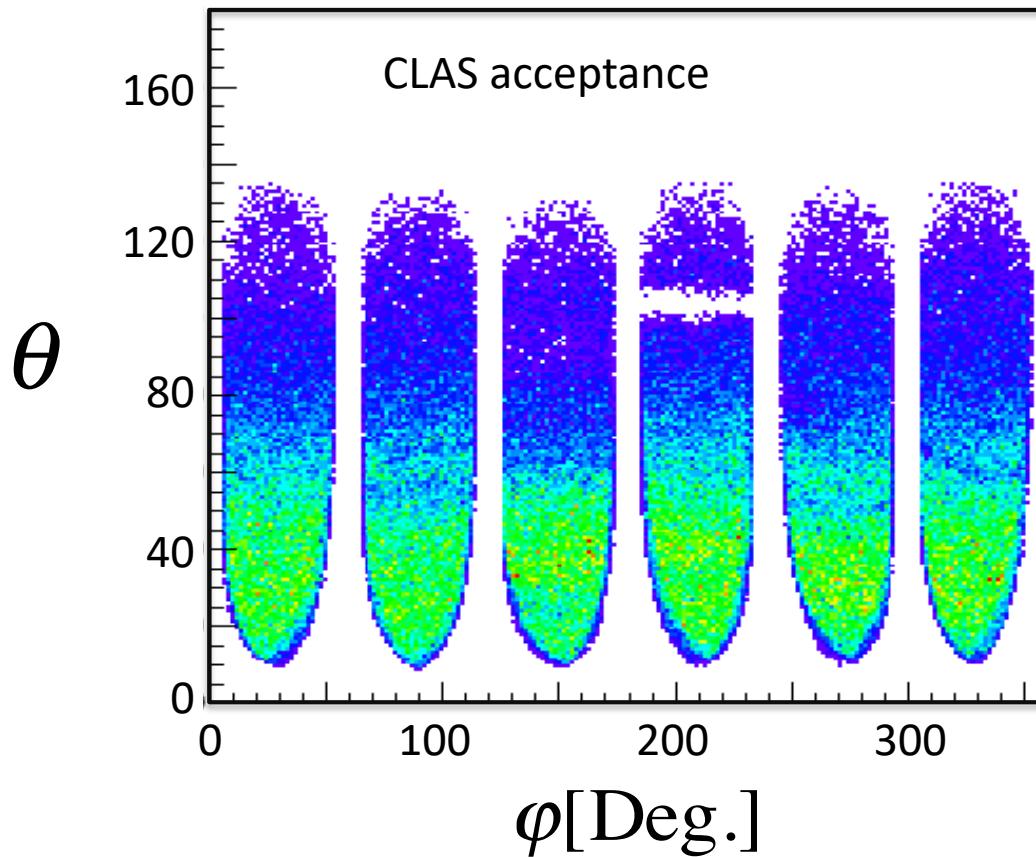
As close to QE as one can get:

- Scattered electron,
- Knockout proton,
- Zero pion,
- Zero  $\gamma$  in the EC.

# Background Subtraction

Want  $0\pi$  ( $e,e'$ ) and ( $e,e'p$ ) events.

Need to account for undetected  $\pi, \gamma$  and extra protons.



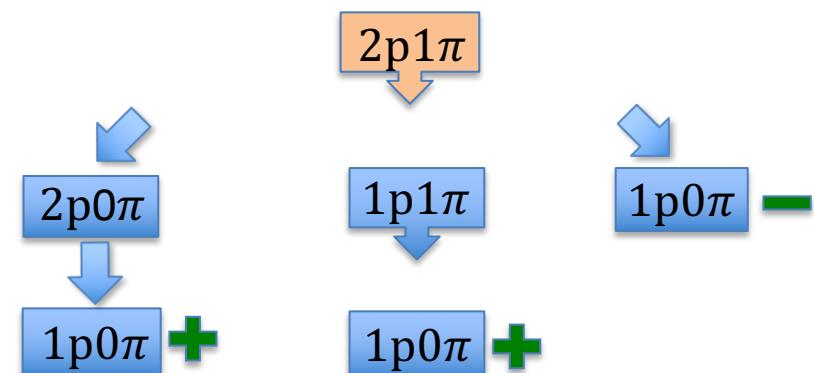
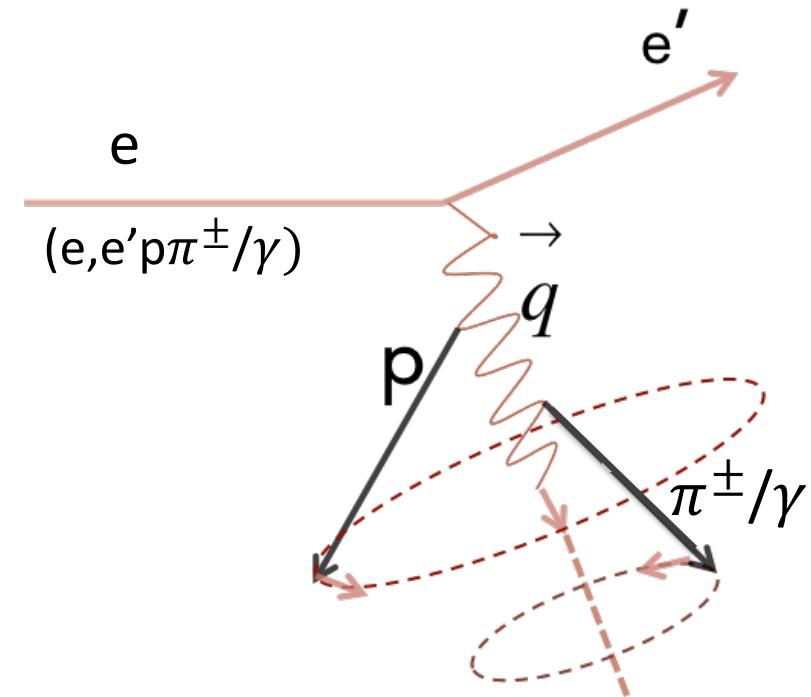
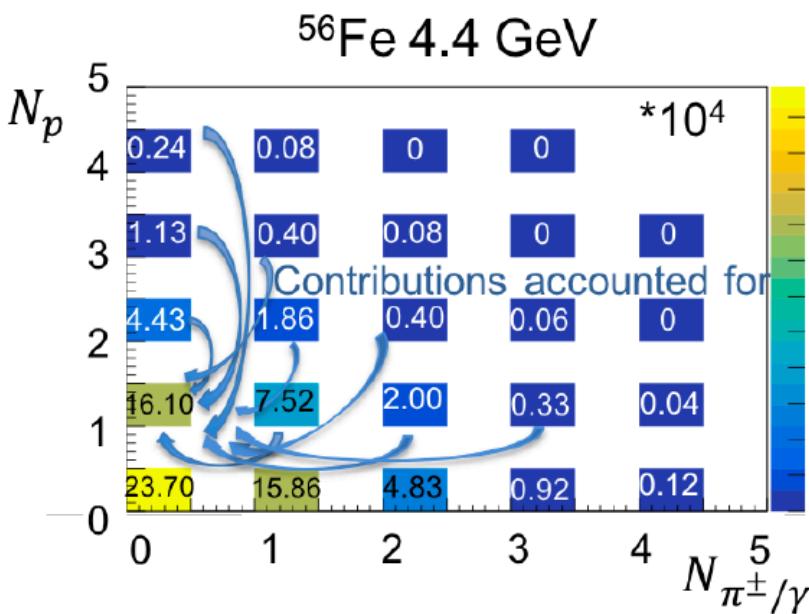
# Background Subtraction in $(e, e' p)$ analysis

Want  $A(e, e' p)$  events.

Subtract for undetected  $\pi, \gamma$  and multiple  $p$ .

Data Driven Correction:

1. Use measured  $(e, e' p\pi)$  events,
2. Rotate  $\pi$  around  $q$  to determine their acceptance,
3. Subtract  $(e, e' p)\pi$  contributions
4. Do the same for 2p, 3p, 2p+  $\pi$  etc

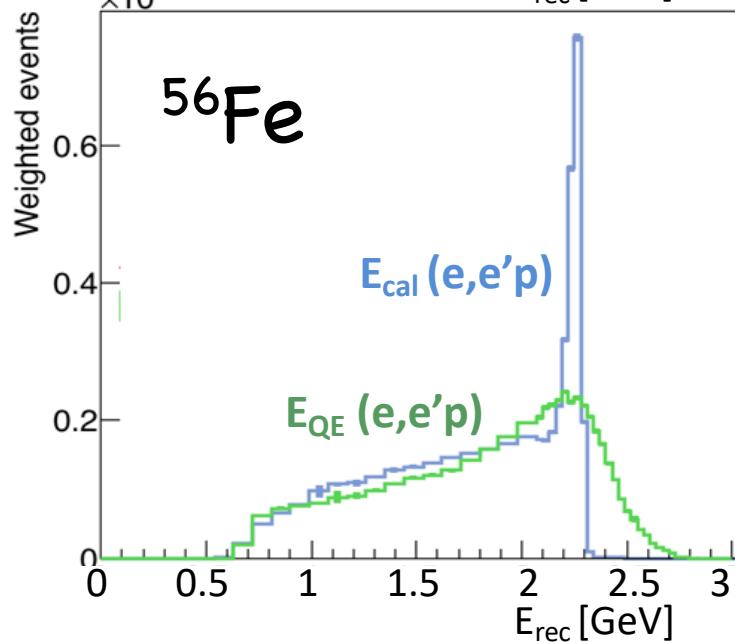
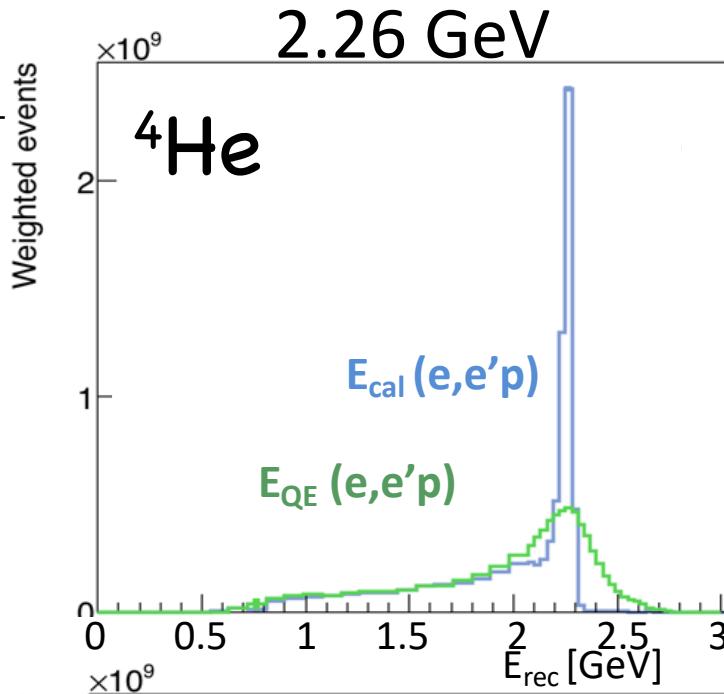


# Results

# Large A dependence

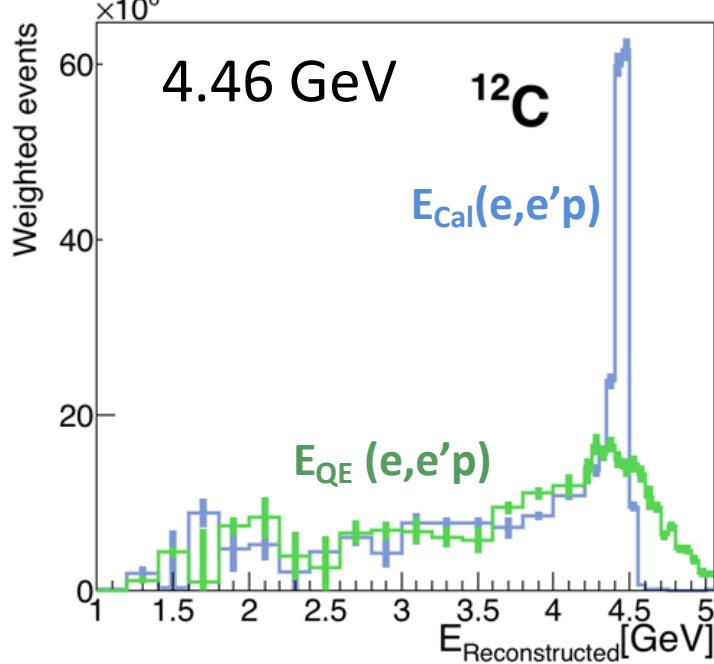
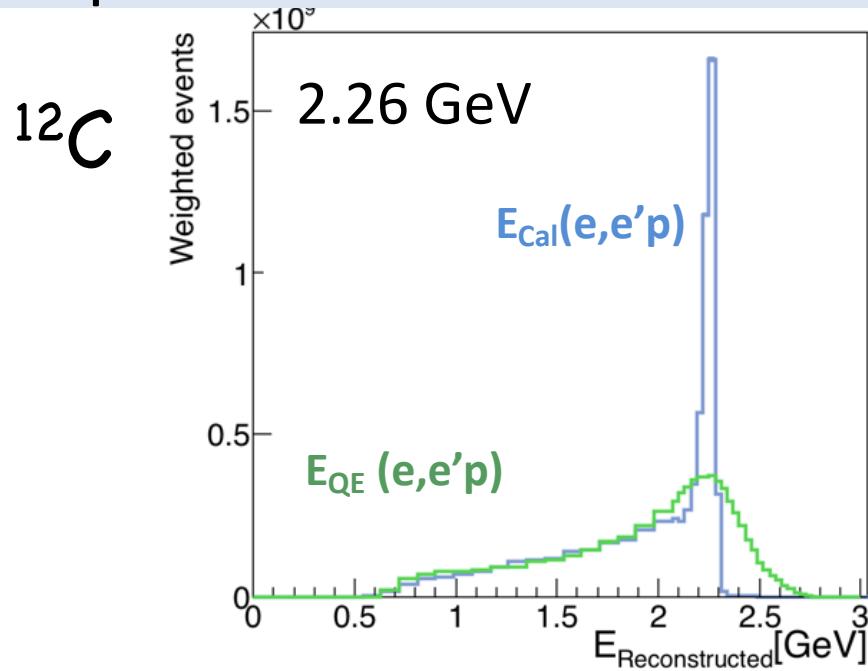
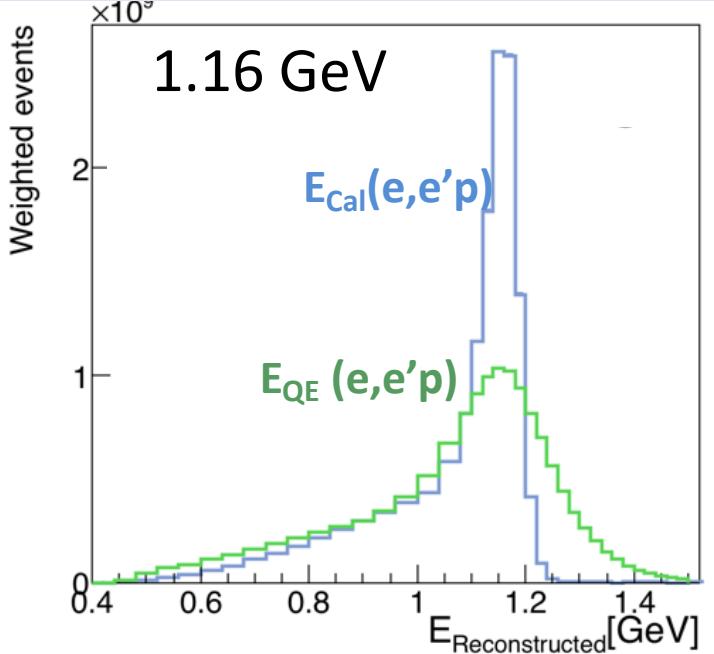
$$E_{QE} = \frac{2M\varepsilon + 2ME_l - m_l^2}{2(M - E_l + |k_l|cos(\theta_l))}$$

$$E_{Cal} = E_l + T_p + \varepsilon$$



1.  $E_{QE}$  has worse peak resolution than  $E_{Cal}$ .
2. Same tail for  $E_{QE} + E_{Cal}$ .
3.  $^{56}\text{Fe}$  is predominantly tail.
4.  $^{56}\text{Fe}$  is much worse than  $^4\text{He}$ .

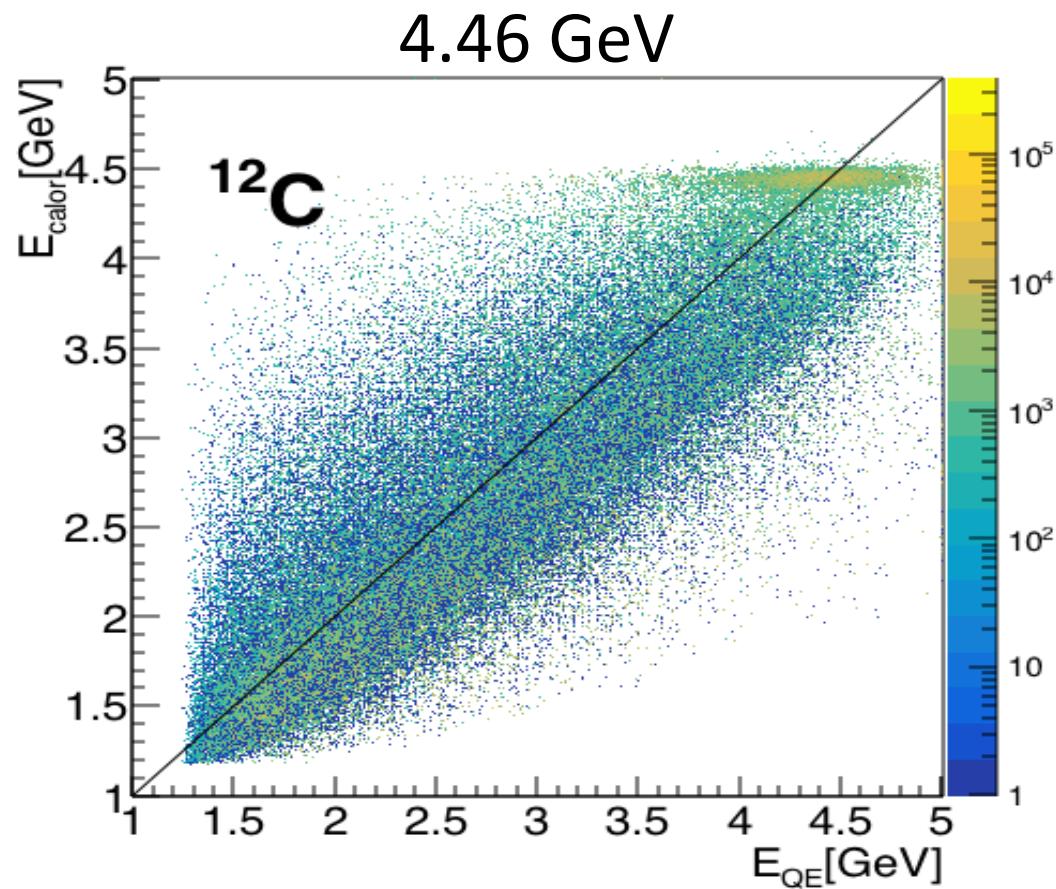
# E dependence



Better reconstruction at lower energies.

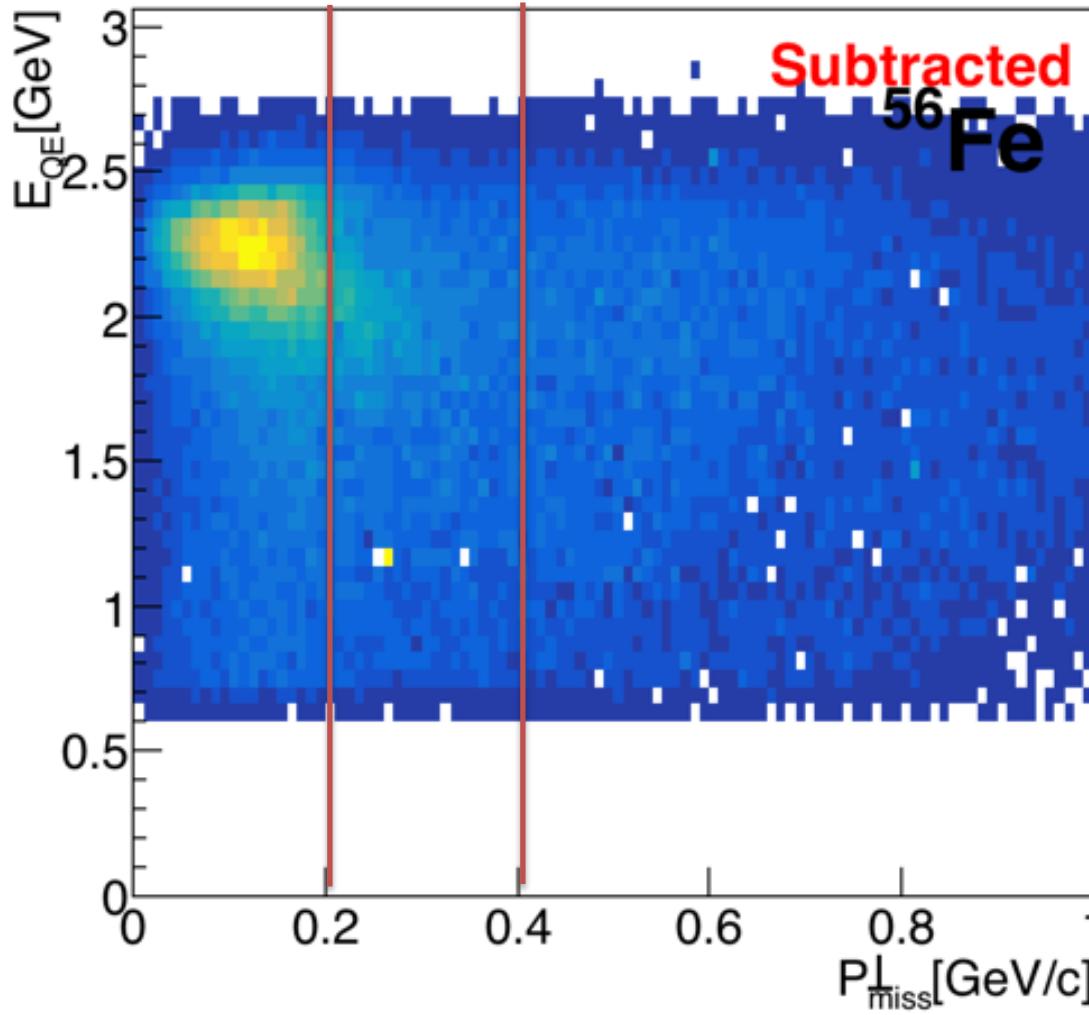
# $E_{QE}$ vs $E_{Cal}$

Agreement between two methods  
doesn't imply correct energy  
reconstruction.

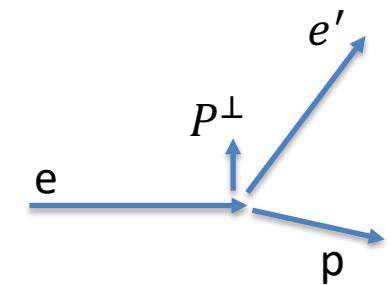


## How do we do better?

2.2 GeV  $^{56}\text{Fe}$

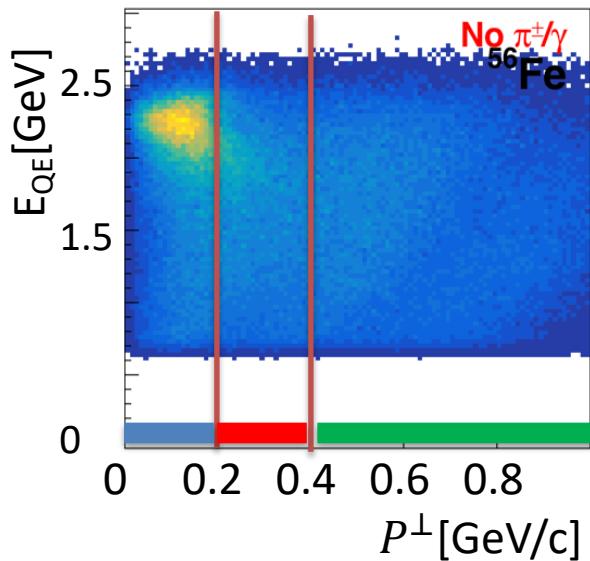


$$P^\perp = P_e^\perp + P_p^\perp = P_{\text{init}}^\perp$$



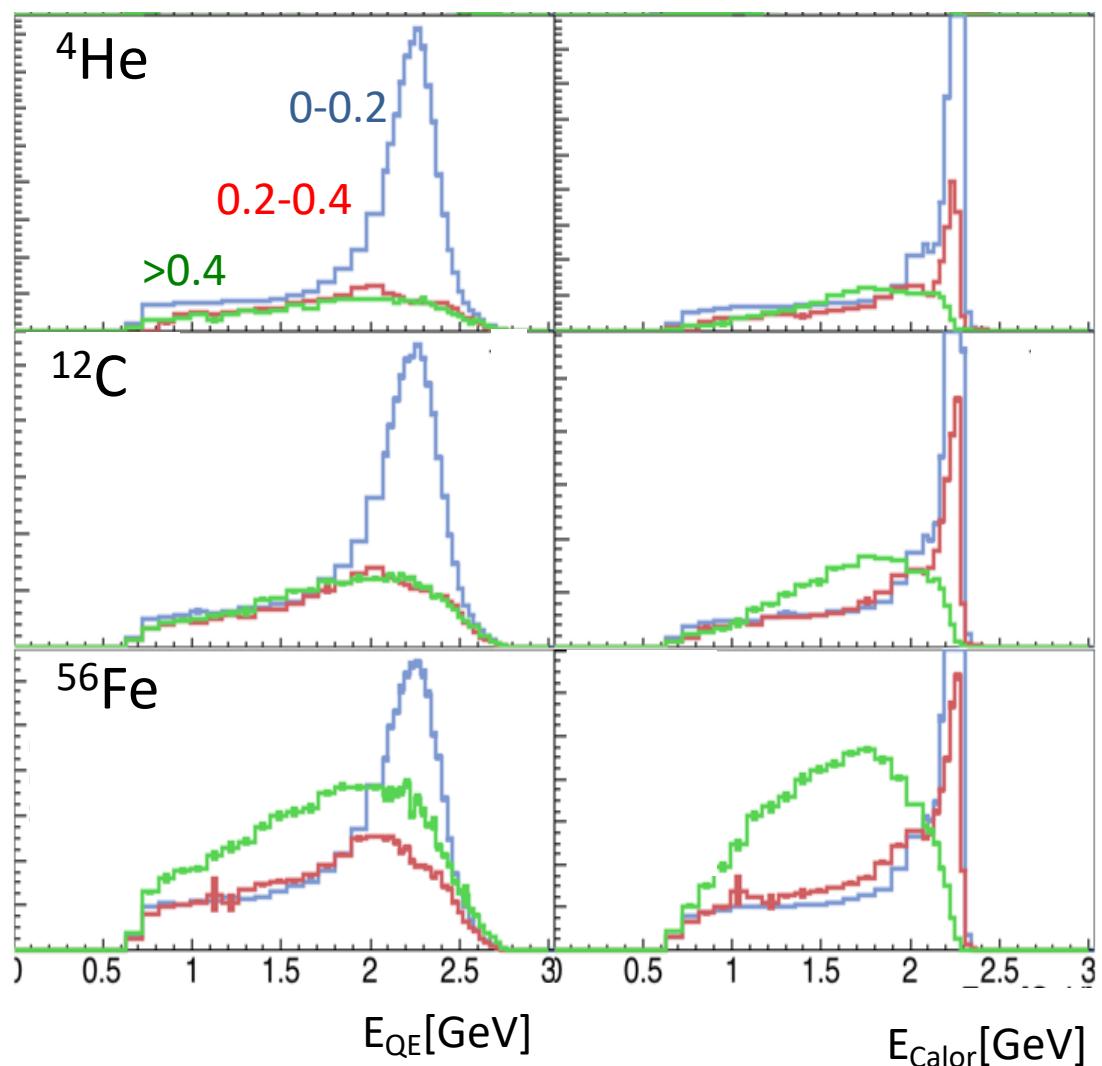
# $P_{\text{miss}}^{\perp}$ slices

2.2 GeV



$E_{\text{QE}}$

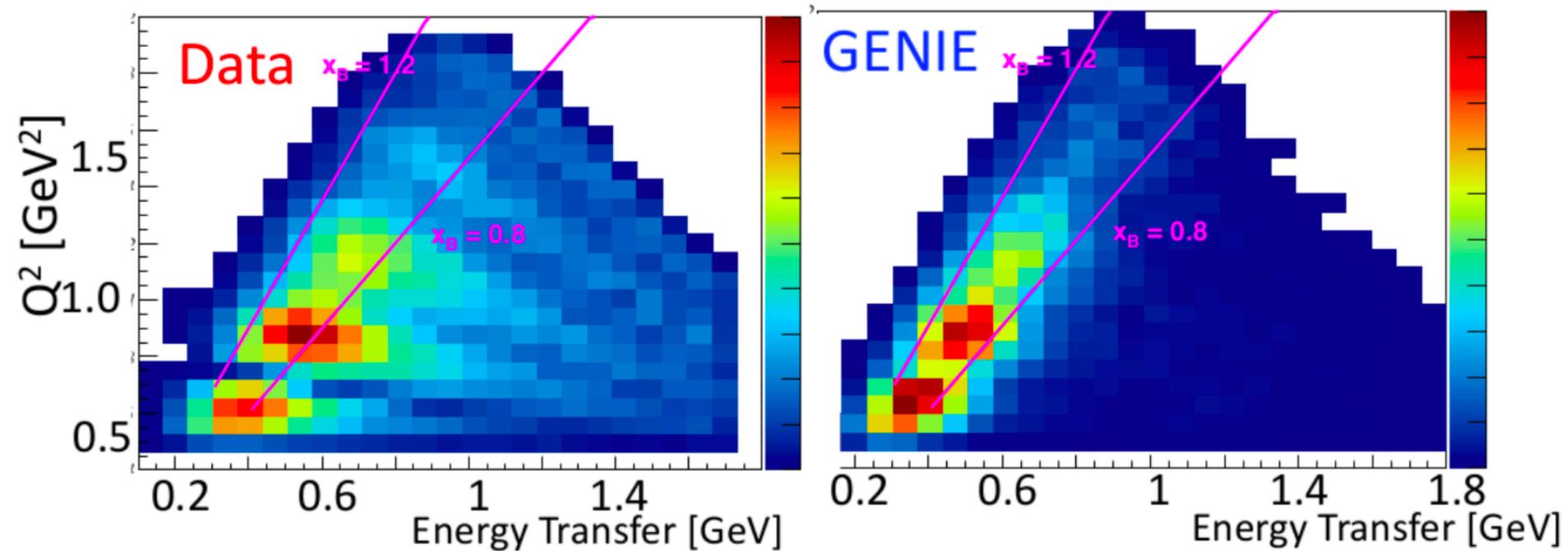
$E_{\text{Cal}}$



1. Large  $P_{\text{miss}}^{\perp}$   $\rightarrow$  bad reconstruction.

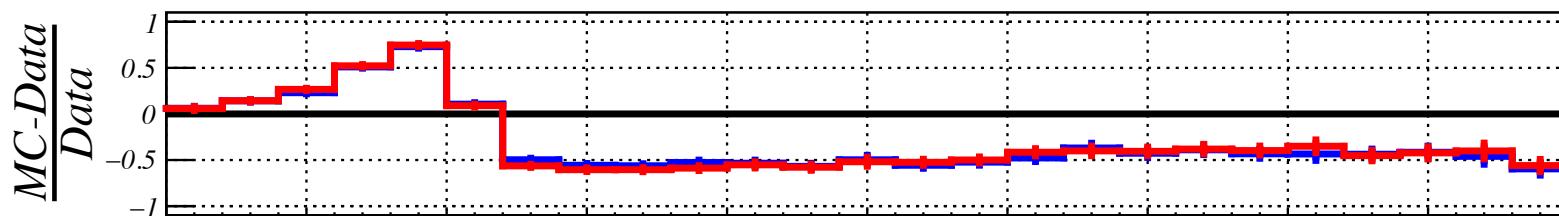
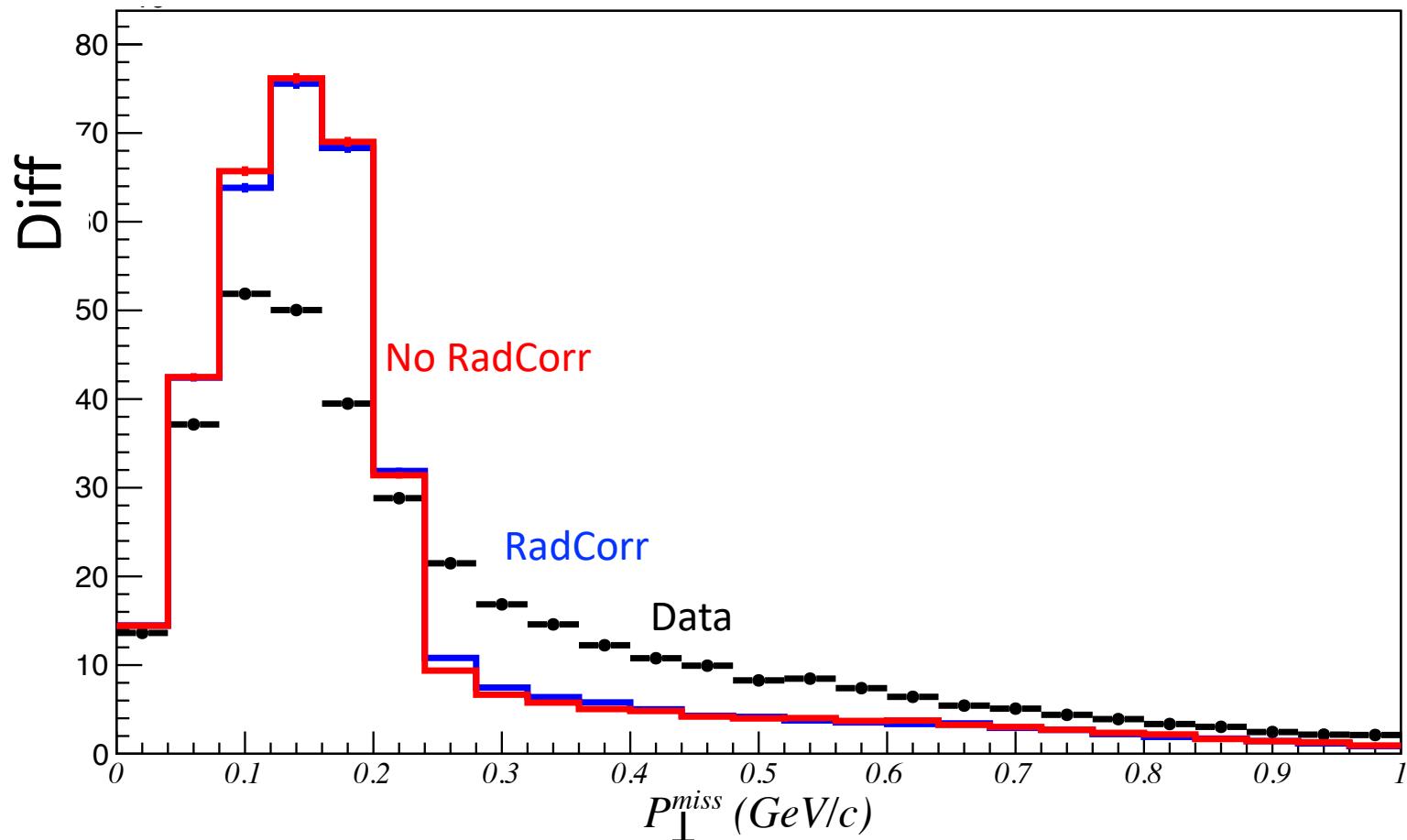
# Data – Generator Comparisons

$C(e,e'p)$  2.26 GeV



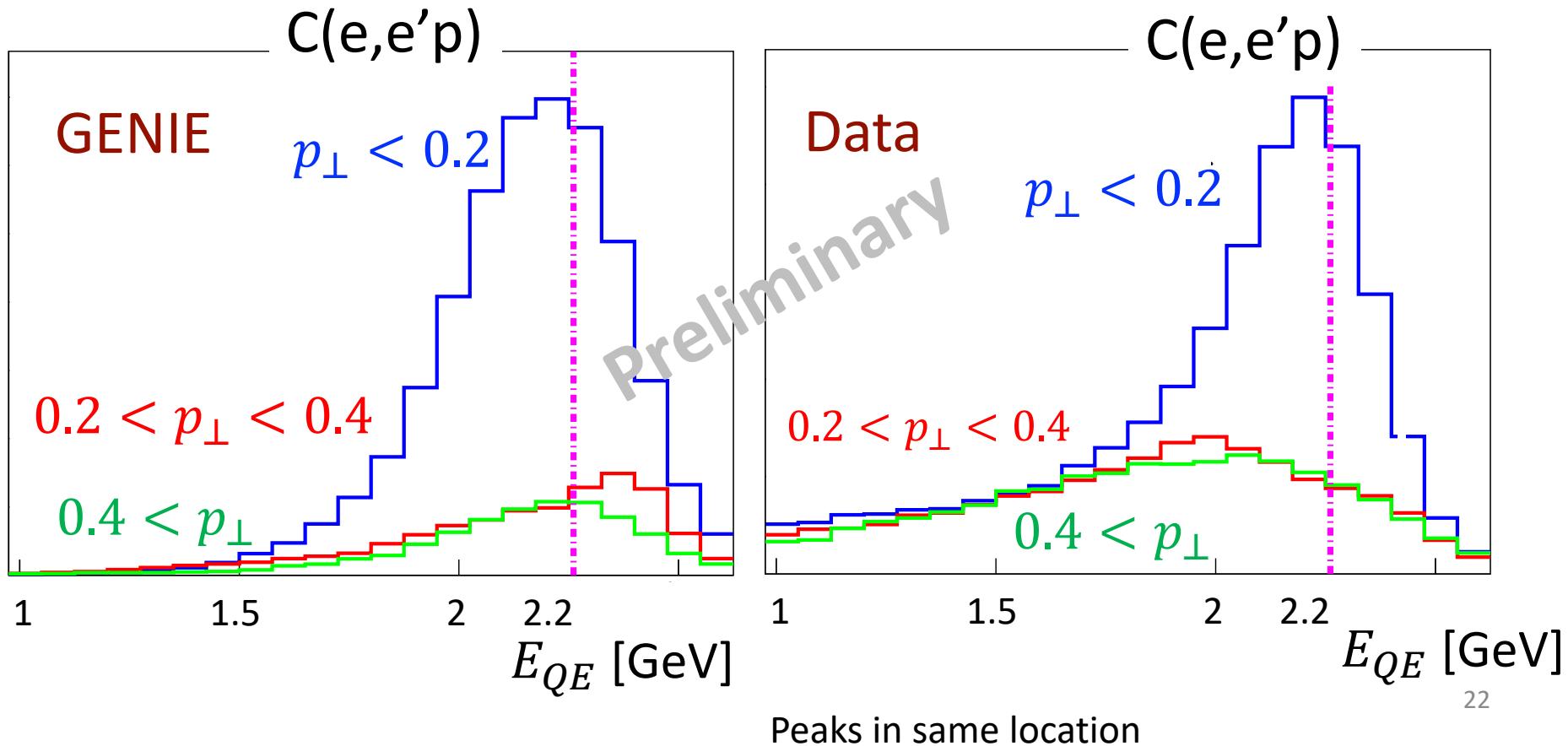
# $0\pi$ Data vs Genie: everywhere

$C(e,e'p)$  2.26 GeV

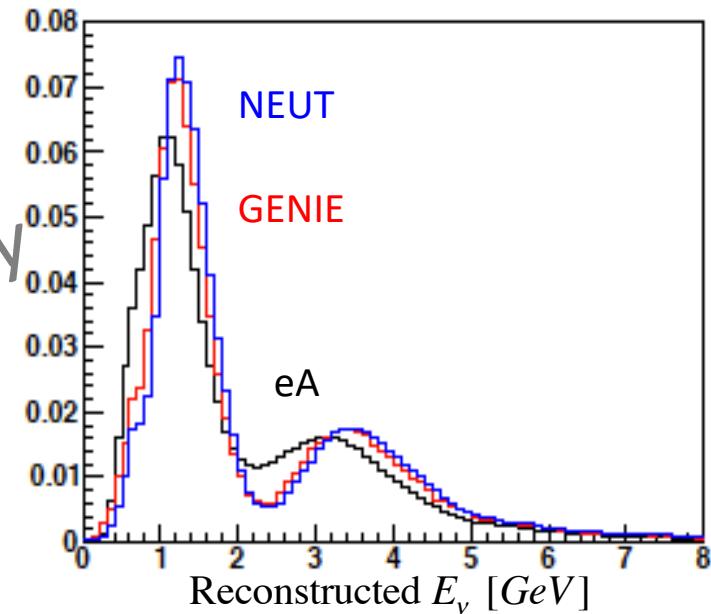
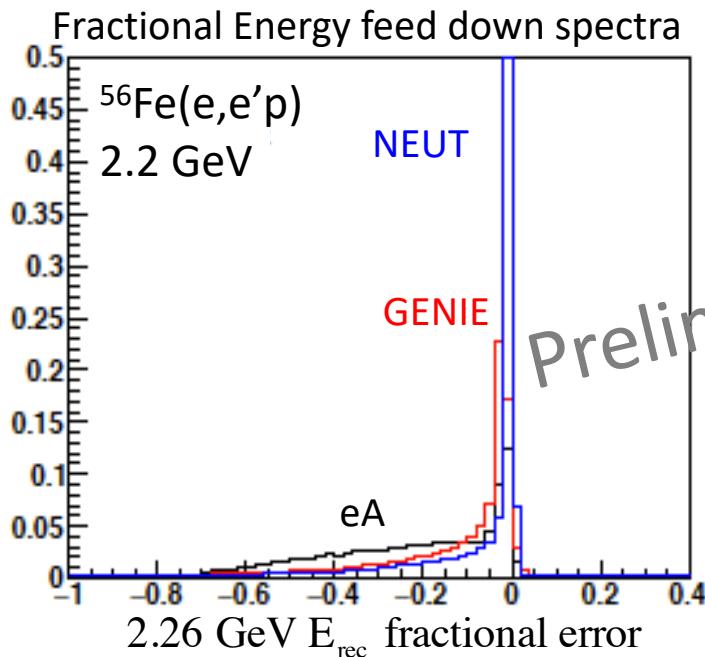


# Data vs Genie: $E_{beam}$ Reconstruction

$$E_{QE} = \frac{2M\varepsilon + 2ME_l - m_l^2}{2(M - E_l + |k_l|cos(\theta_l))}$$



# Potential impact on DUNE oscillation analysis



- Compare  $E_{rec}$  for eA to  $E_{rec}$  for  $\nu A$
- Used 2.26 GeV eA  $E_{rec}$  for all incident energies
- Threw events with  $\nu A$  Genie
- Reconstruct with  $\nu A$  Neut or eA data

-> Very different  
oscillation parameters!

Will do with latest data.

# Summary

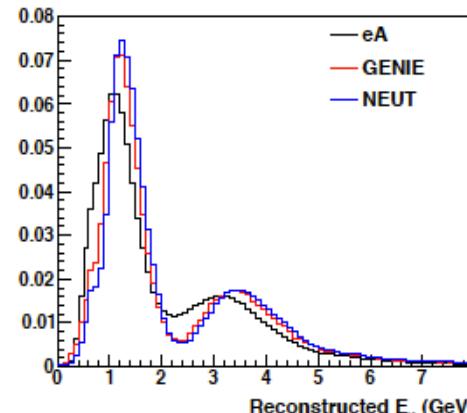
## 1. The first use of electron data to test neutrino energy reconstruction algorithms

- select zero-pion events to enhance quasi-elastic signal
  - ❖ Subtract for undetected  $\pi$ ,  $\gamma$  and extra p.
- just using scattered lepton ( $E_{QE}$ )
  - ❖ used in Cherenkov-type neutrino detectors
- total energy of electron plus proton ( $E_{Cal}$ )
  - ❖ used in calorimetric neutrino detectors

## 2. Only 0.1-0.66 of events reconstruct to within 5% of the beam energy

- better for lighter nuclei
- improved by a transverse momentum cut

## 3. First preliminary attempt to quantify the impact of this work on oscillation analysis.



## 4. Under CLAS analysis review.

## 5. Anticipate paper submission soon.

**Chris Marshal  
(LBL)**

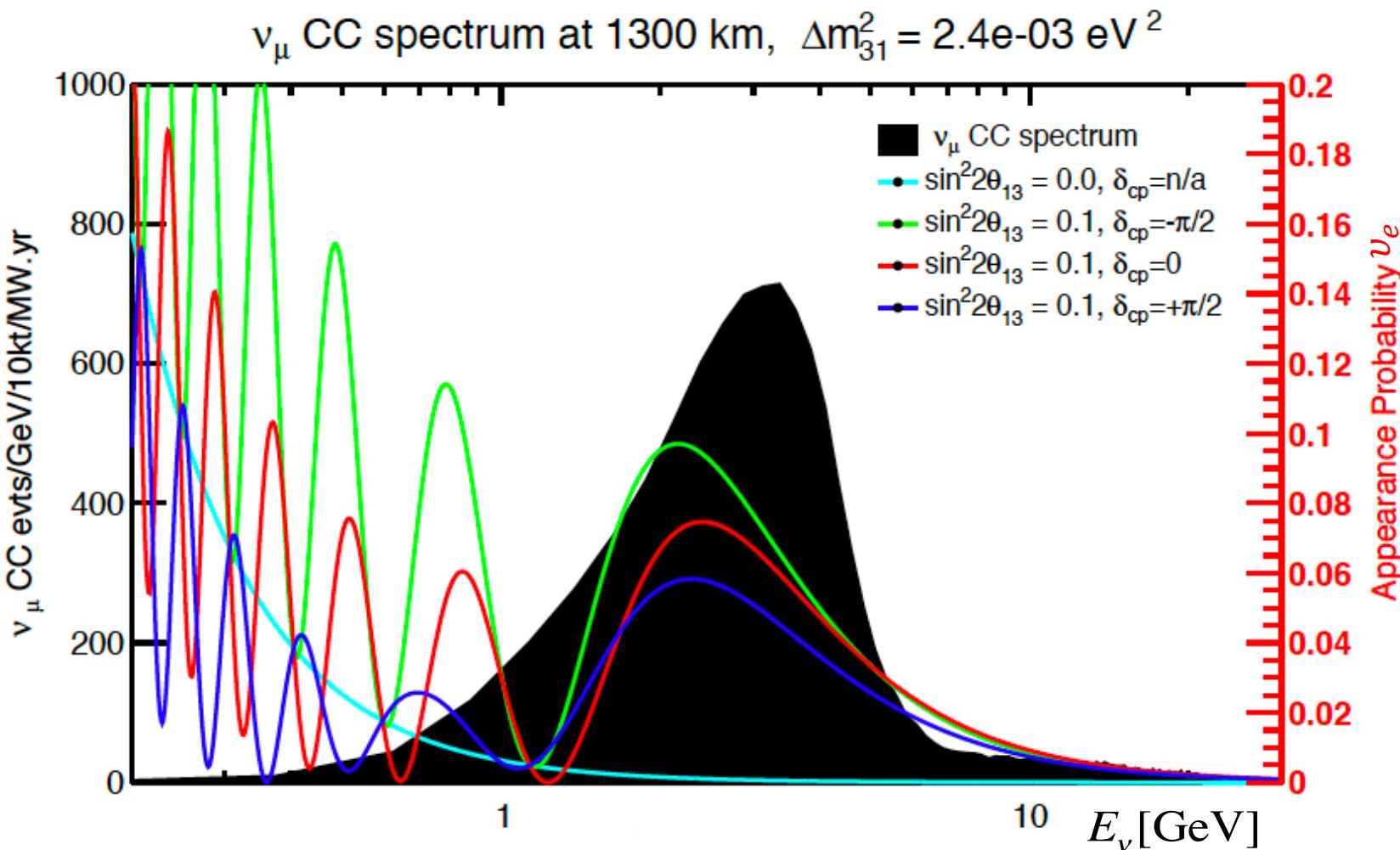


**Afroditi  
Papadopoulou  
(MIT@FNAL)**



**Adi Ashkenazi  
(MIT@FNAL)**

# Appearance probability expected in DUNE for three different sets of values of $\delta_{CP}$ and $\theta_{13}$

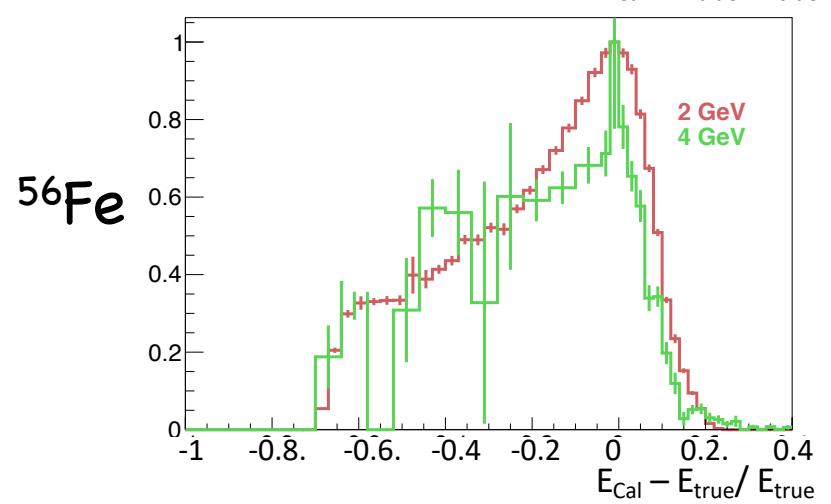
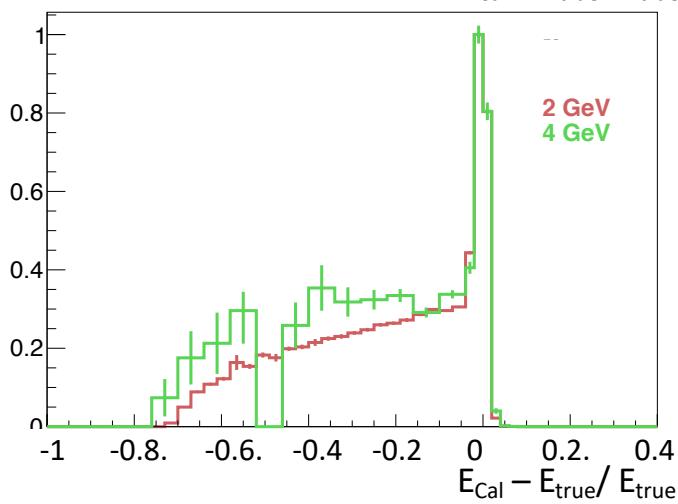
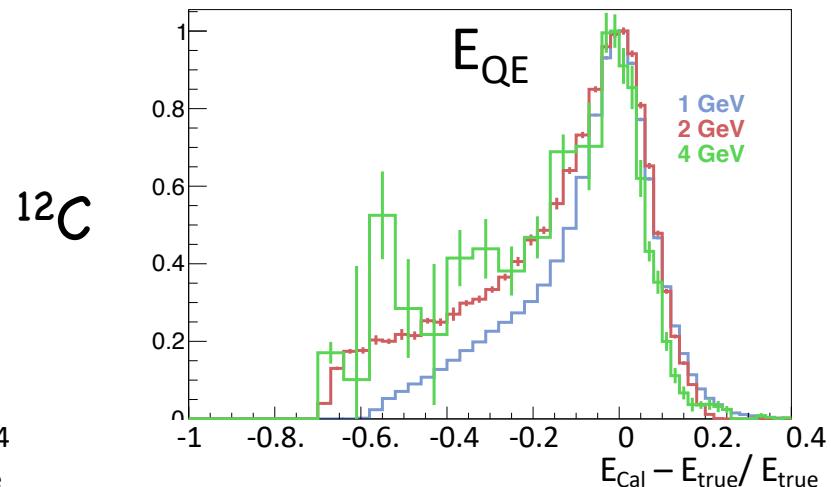
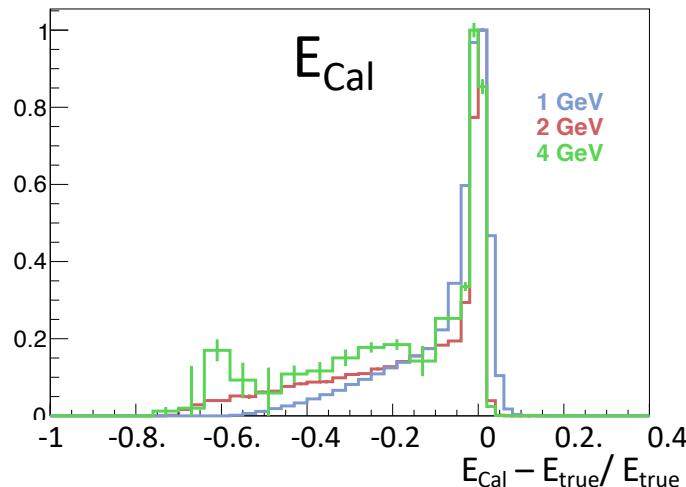


Need  $\Delta E_\nu < 0.1 \text{ GeV}$ .

# Fractional energy feed down ( $E_{\text{rec.}} - E_{\text{true}} / E_{\text{true}}$ )

$(e, e' p)$

The fractional energy feed down is bigger at higher energies.



## Percent of events reconstructed to within 5% of the beam energy

|                  | 1.1 GeV     |                | 2.2 GeV     |                | 4.4 GeV     |                |
|------------------|-------------|----------------|-------------|----------------|-------------|----------------|
|                  | $E_{QE}$ 1e | $E_{Cal}$ 1e1p | $E_{QE}$ 1e | $E_{Cal}$ 1e1p | $E_{QE}$ 1e | $E_{Cal}$ 1e1p |
| $^3\text{He}$    | 44          | 66             | 32          | 54             | 21          | 41             |
| $^4\text{He}$    |             |                | 25          | 46             | 16          | 32             |
| $^{12}\text{C}$  | 28          | 47             | 22          | 39             | 13          | 27             |
| $^{56}\text{Fe}$ |             |                | 17          | 25             | 10          | 16             |

From 10 to 66% of events reconstruct to within  
5% of beam energy.

# Error sources (new)

- Statistical error.
- Errors of the weights for subtraction of undetected pions and protons.
  - ✧ Statistical error due to number of  $(e,e'\pi)$  events used to determine undetected pion contribution
  - ✧ Rotate  $(e,e'\pi)$  events enough times to reduce statistical error below 1%.
- Systematic error due to the  $\phi$ -dependence of the pion cross section modeled and found to be negligible (less than 1%).

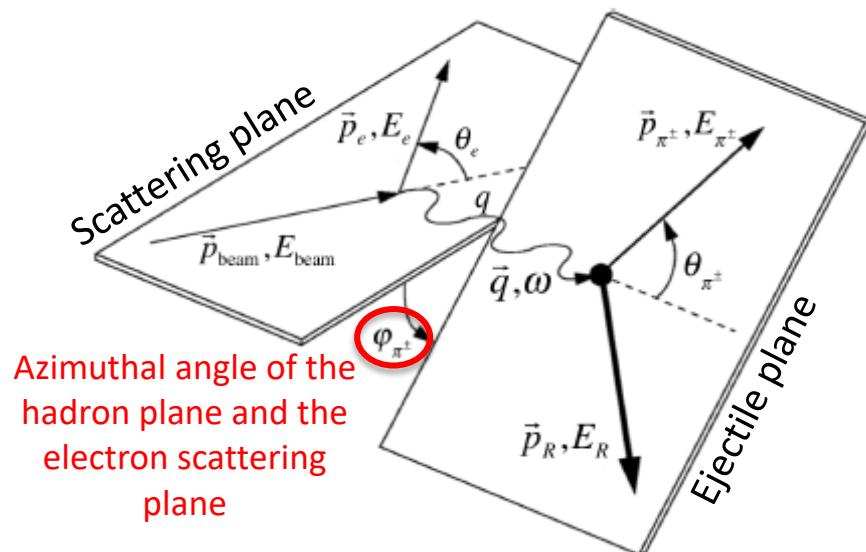
# Error sources

-Systematic error due to the  $\phi$ -dependence of the cross section.

$$\frac{d^6\sigma}{d\Omega_e d\Omega_p dE_{\text{miss}} d\omega} = K \sigma_{\text{Mott}} [v_L R_L + v_T R_T + v_{LT} R_{LT} \cos(\varphi) + v_{TT} R_{TT} \cos(2\varphi)]$$

$K$  = (phase space)

$v = v(q, \omega)$  electron kinematics



# Phi dependence

Cross section for unpolarized pion electroproduction on a single nucleon:

$$\frac{d\sigma}{d\Omega_\pi^*}(W, Q^2, \theta_\pi, \phi_\pi) = A + B \cos \phi + C \cos 2\phi$$

$$A = (\sigma_T + \epsilon \sigma_L) \frac{p_\pi^*}{k_\gamma^*}$$

$$B = \sigma_{LT} \frac{p_\pi^*}{k_\gamma^*} \sin \theta_\pi \sqrt{2\epsilon(\epsilon+1)}$$

$$C = \sigma_{TT} \frac{p_\pi^*}{k_\gamma^*} \sin^2 \theta_\pi \epsilon$$

$$k_\gamma = \frac{W^2 - M^2}{2M} \quad k_\gamma^* = k_\gamma M/W \quad \epsilon = \frac{1}{1 + 2(1 + \frac{\nu^2}{Q^2} \tan^2 \frac{\theta_e}{2})}$$

Where  $p_\pi^*$ ,  $\theta_\pi$  and  $\phi_\pi$  are the momentum, scattering and azimuthal angles of the  $\pi^0$  in the CM frame.

Weight without  $\phi$  dependence

$$W = \frac{\sum_{i=1}^{N_{Undet}} 1}{\sum_{i=1}^{N_{Det}} 1}$$

Weight with  $\phi$  dependence

$$W = \frac{\sum_{i=1}^{N_{Undet}} 1 + B/A \cos \phi_\pi + C/A \cos 2\phi_\pi}{\sum_{i=1}^{N_{Det}} 1 + B/A \cos \phi_\pi + C/A \cos 2\phi_\pi}$$

# Phi dependence

Use maximum of structure functions from Markov et al. paper [ref] for  $\cos\theta_\pi = 0.1$  and  $0.4 \leq Q^2 \leq 1 \text{ GeV}^2$ .  
 The absolute values are the biggest for  $Q^2=0.45 \text{ GeV}^2$ .  
 $\sigma_T + \epsilon\sigma_L = 30 \mu b$ ,  $\sigma_{TT} = -10 \mu b$  and  $\sigma_{LT} = -2 \mu b$ .

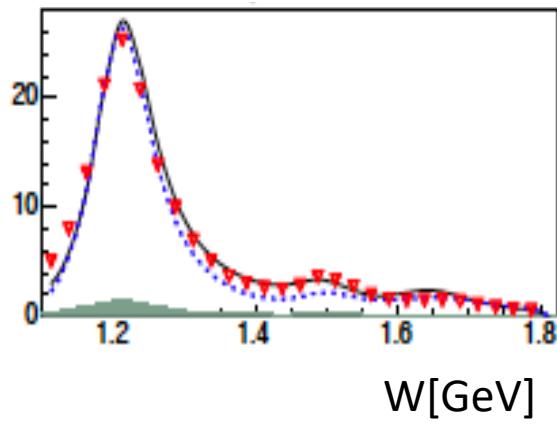
$$A = (\sigma_T + \epsilon\sigma_L) \frac{p_\pi^*}{k_\gamma^*}$$

$$B = \sigma_{LT} \frac{p_\pi^*}{k_\gamma^*} \sin \theta_\pi \sqrt{2\epsilon(\epsilon + 1)}$$

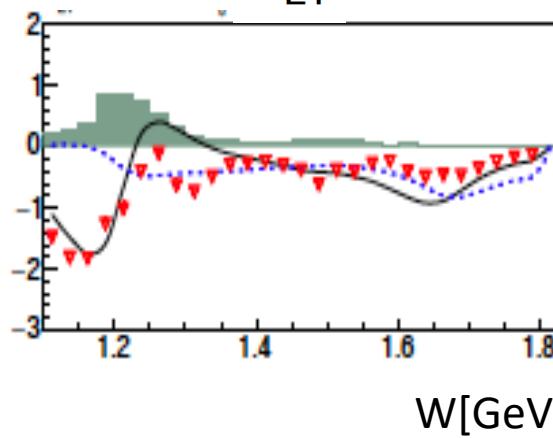
$$C = \sigma_{TT} \frac{p_\pi^*}{k_\gamma^*} \sin^2 \theta_\pi \epsilon$$

$$\cos\theta_{\pi_0}^* = 0.1 \quad Q^2 = 0.45 \text{ GeV}^2$$

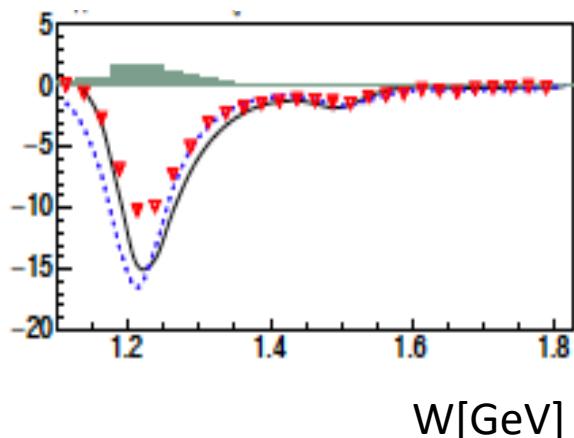
$$\sigma_T + \epsilon\sigma_L$$



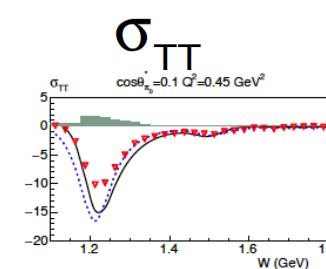
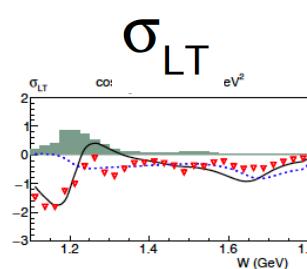
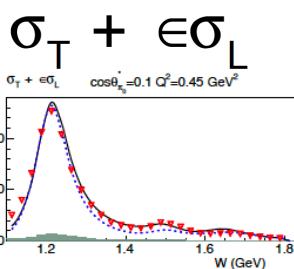
$$\sigma_{LT}$$



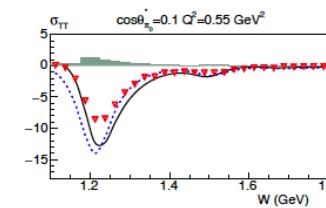
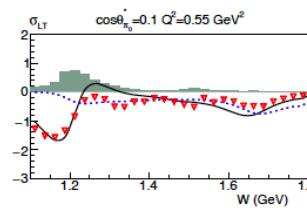
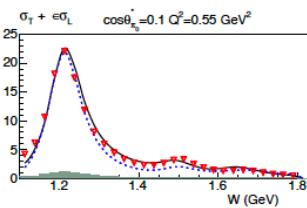
$$\sigma_{TT}$$



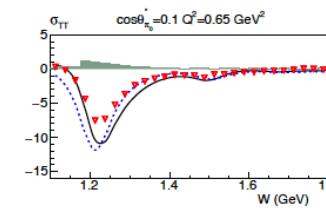
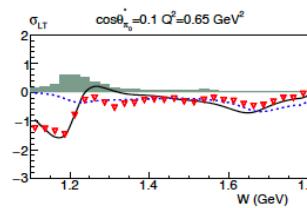
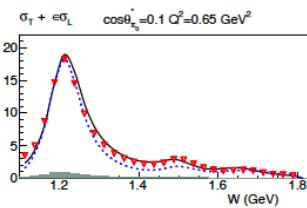
$Q^2 = 0.45 \text{ GeV}^2$



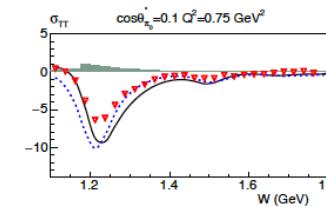
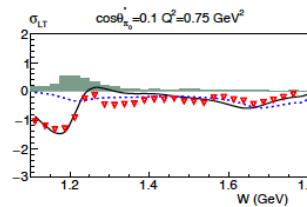
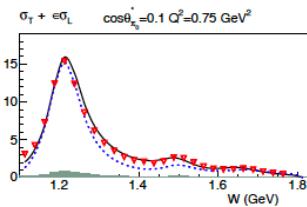
$Q^2 = 0.55 \text{ GeV}^2$



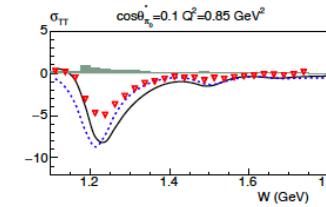
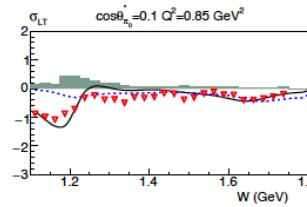
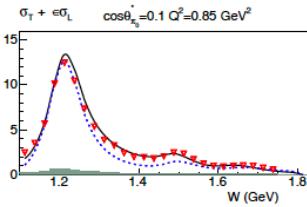
$Q^2 = 0.65 \text{ GeV}^2$



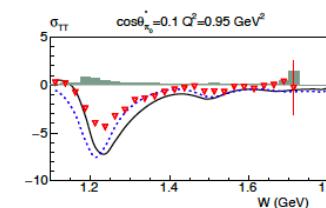
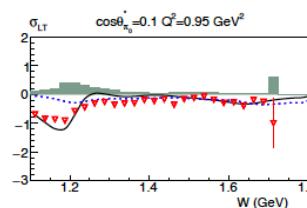
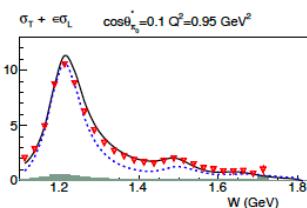
$Q^2 = 0.75 \text{ GeV}^2$



$Q^2 = 0.85 \text{ GeV}^2$

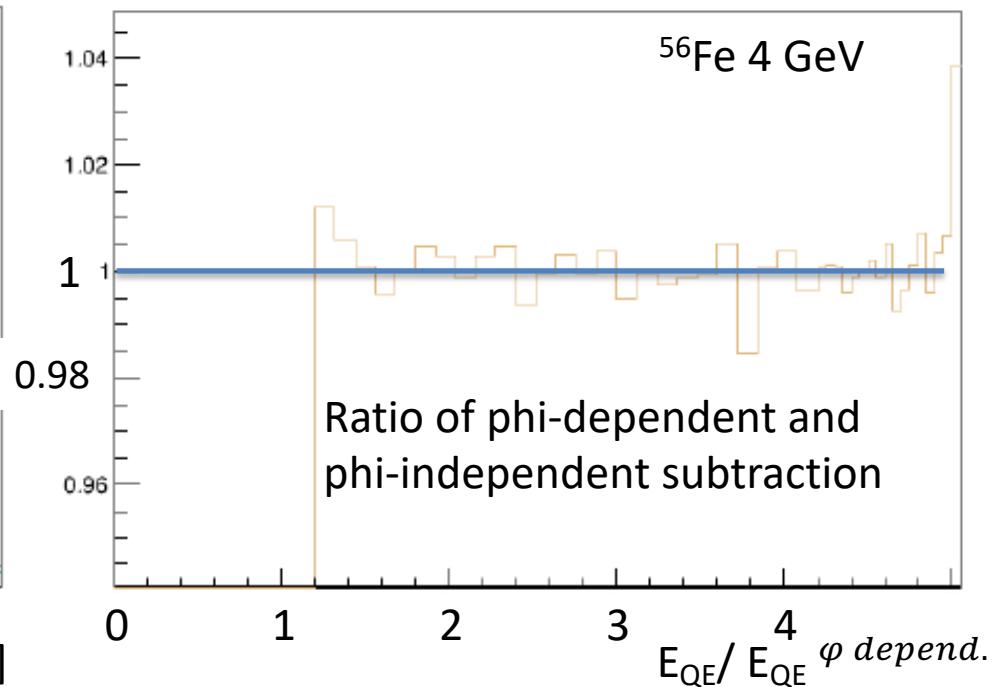
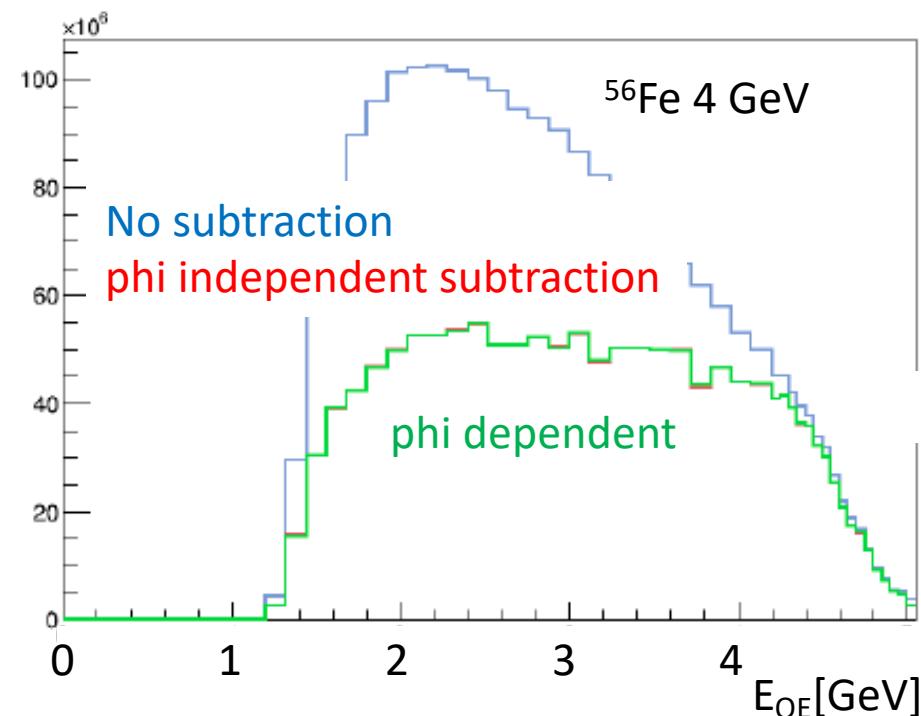


$Q^2 = 0.95 \text{ GeV}^2$



# Error sources: Phi dependence

Subtracting for undetected one  $\pi$  events in  $^{56}\text{Fe}(e,e')$  4 GeV analysis



Negligible phi dependence!