QCD Across the Resolutions

One perspective on the Panorama of Physics at JLab

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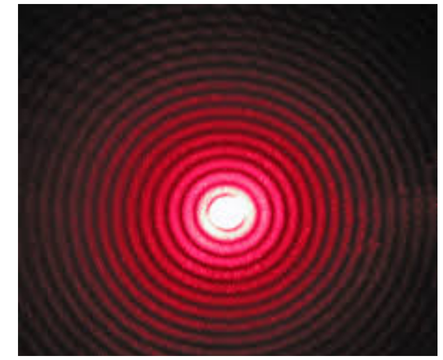
1. **Light and photons: the hidden universe**
2. **The game and stories of quantum fields**
3. **What makes QCD "different"**
4. **JLab and the dark universe**
5. **Exploring QCD: short and endless stories in the spinning proton**

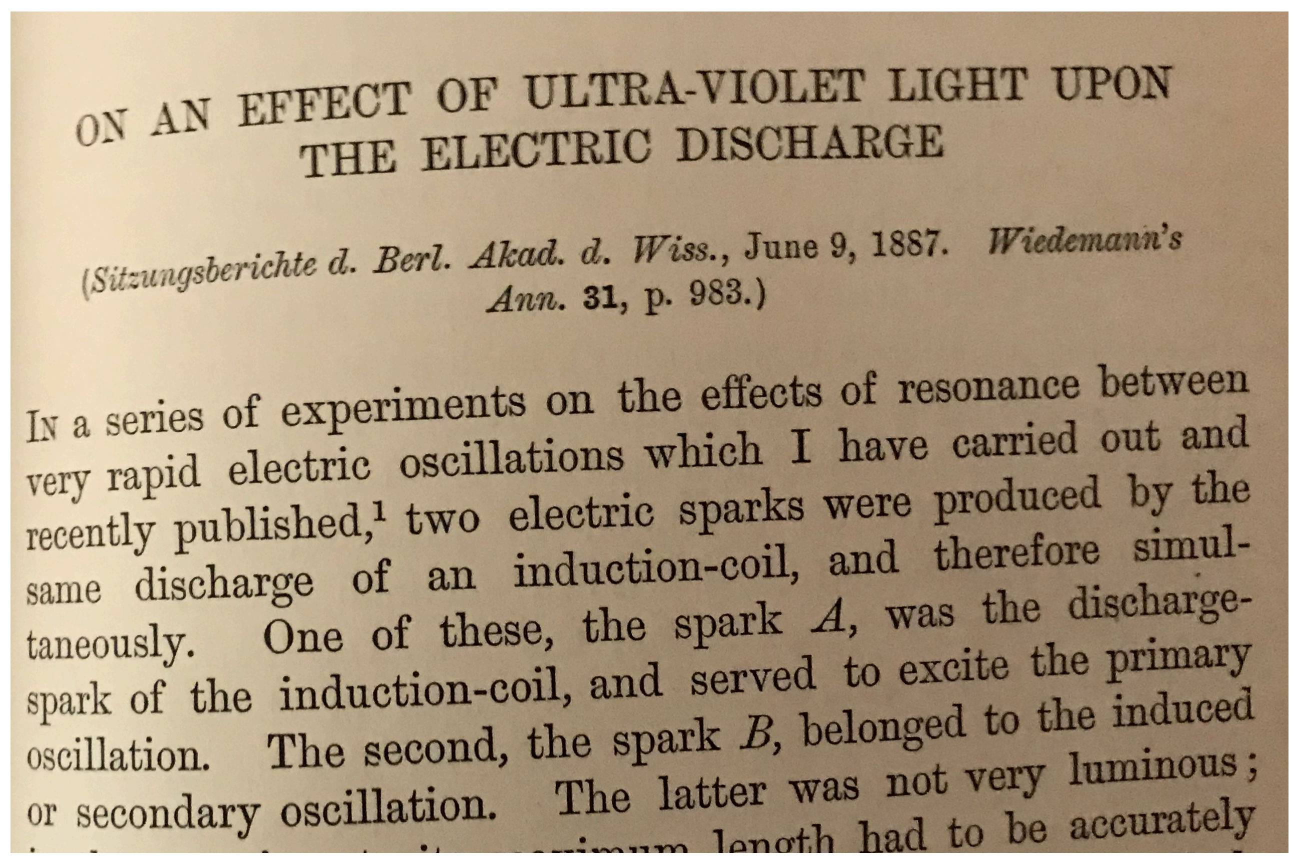
1. Light and photons

"The wave theory of light, which operates with continuous functions has proved itself splendidly . . . (Einstein, 1905)



One should keep in mind, however, that optical observations apply to time averages only . . . the energy of light [is] localized at points in space . . . and can be absorbed or generated only as a whole."

The photoelectric effect (Hertz,1887)



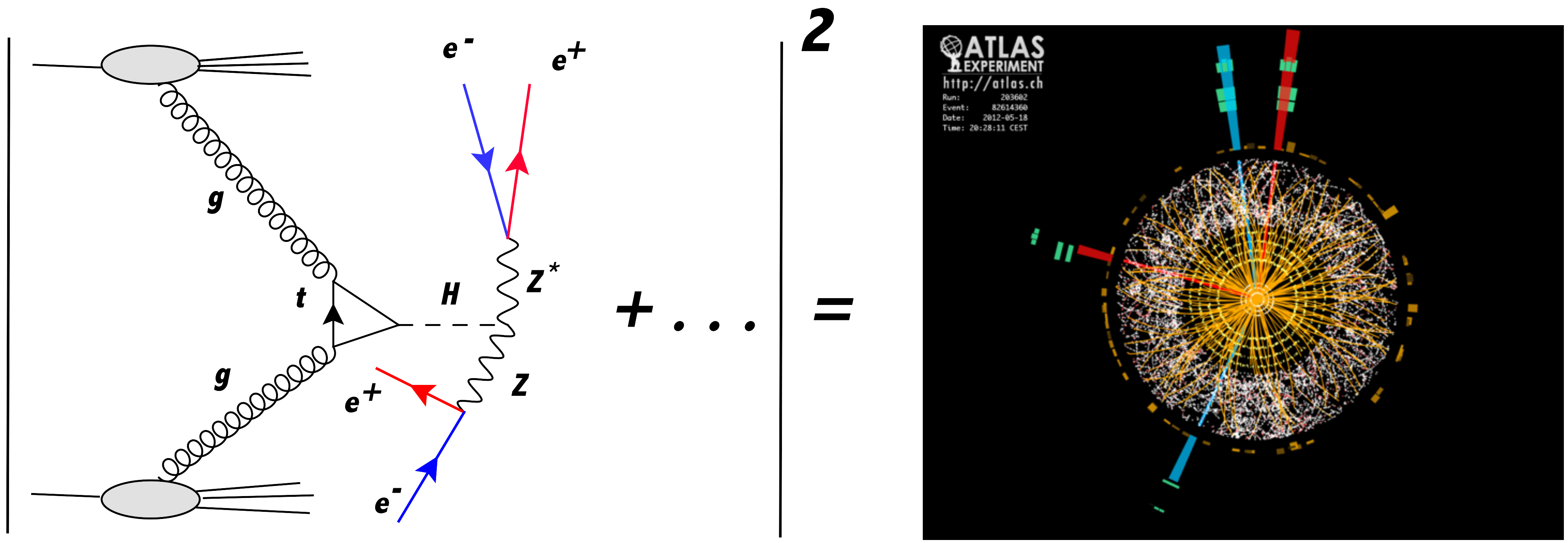
ON AN EFFECT OF ULTRA-VIOLET LIGHT UPON THE ELECTRIC DISCHARGE

(*Sitzungsberichte d. Berl. Akad. d. Wiss.*, June 9, 1887. *Wiedemann's Ann.* **31**, p. 983.)

In a series of experiments on the effects of resonance between very rapid electric oscillations which I have carried out and recently published,[1] two electric sparks were produced by the same discharge of an induction-coil, and therefore simultaneously. One of these, the spark *A*, was the discharge-spark of the induction-coil, and served to excite the primary oscillation. The second, the spark *B*, belonged to the induced or secondary oscillation. The latter was not very luminous; ... length had to be accurately

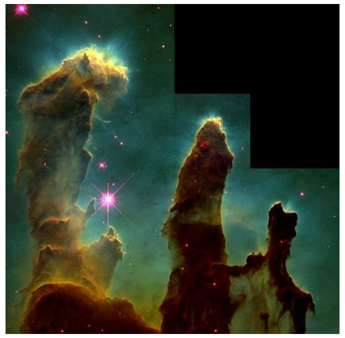
Density of photons is proportional to the square of the wave amplitude.

This set the stage for many great discoveries of the twentieth century: all matter (like photons) is described in terms of particles that are created or absorbed at infinitesimal points. At longer scales, these particles combine into "emergent" systems (like light waves).



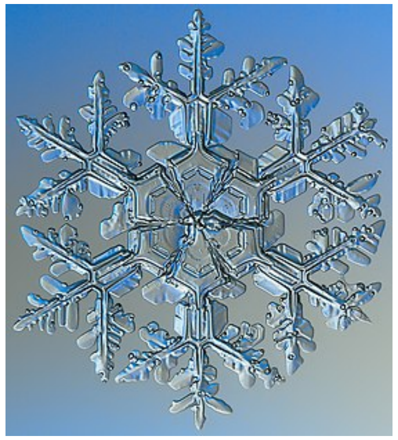
Emergent "degrees of freedom" are a universal feature of classical and quantum laws of nature

At scales we can see:

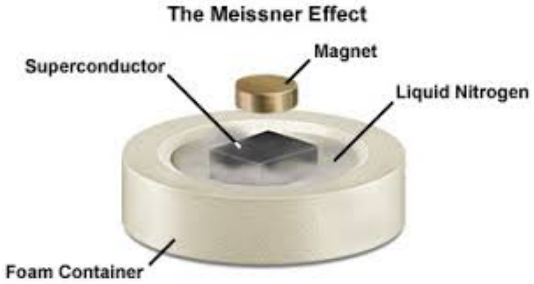


From hydrogen gas to galaxies and stars

From atomic magnetic moments to (anti)ferromagnetism



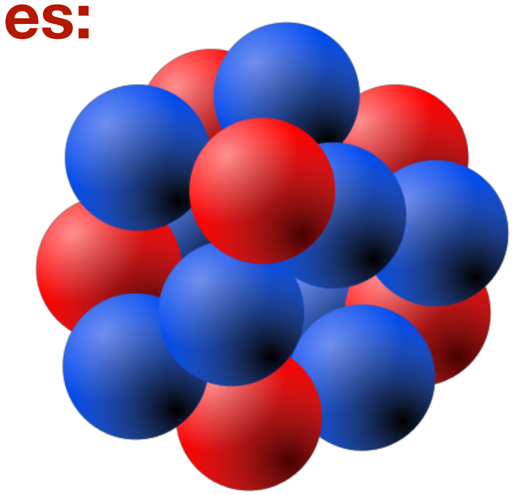
From molecules to phases of matter



From electrons and metals to superconductors

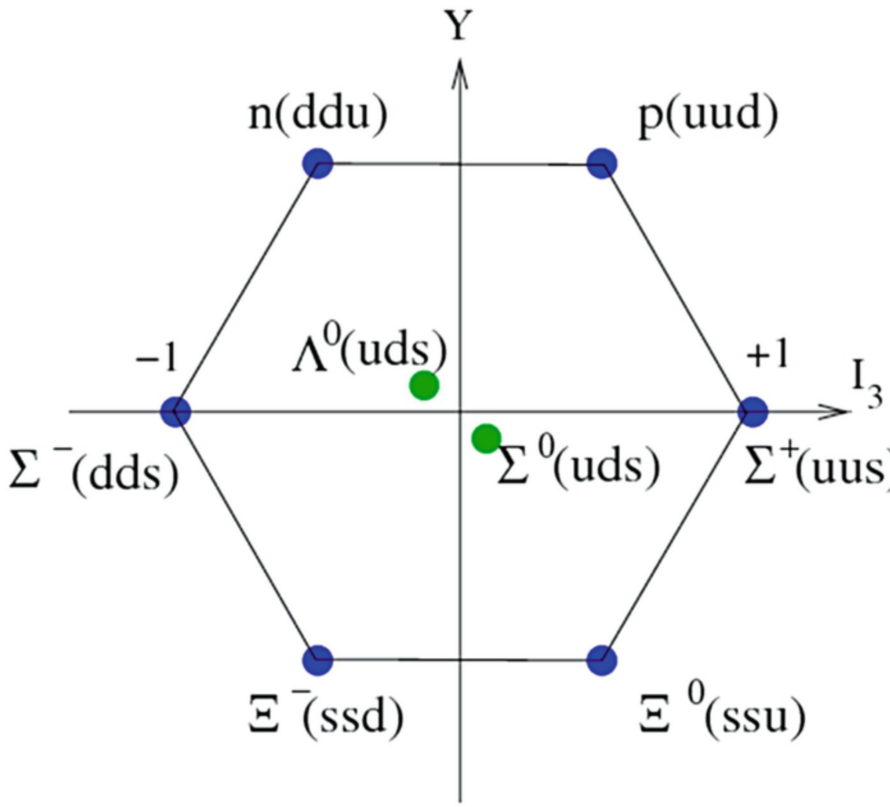
From chemistry to life itself

And at the micro scales:



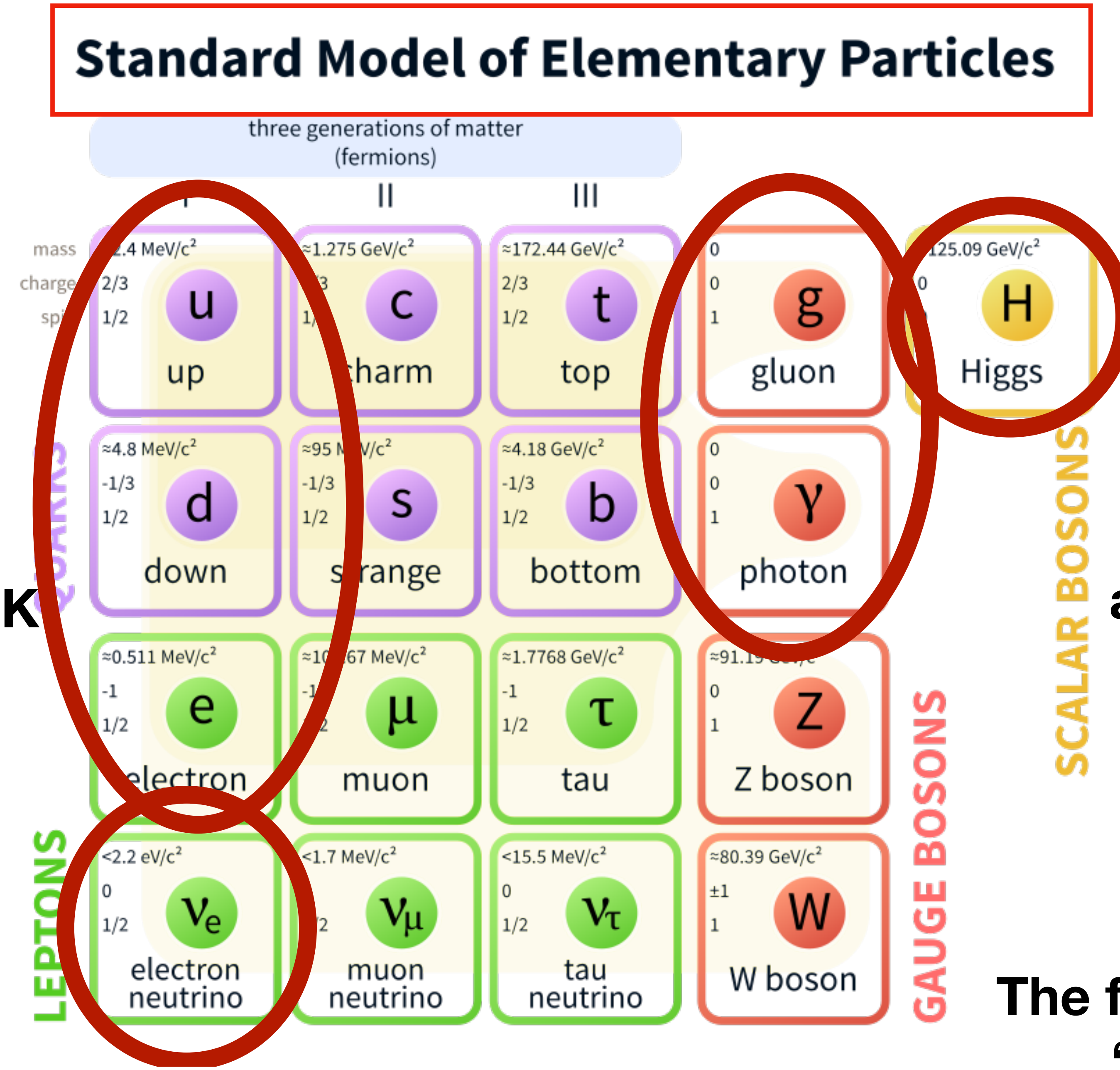
From protons and neutrons
to nuclei

From quarks
to protons, neutrons
and other baryons



At each step, the compound system has features qualitatively different than those of its constituents, yet following from them.

Yet everything we can “see” is made up of the matter and force particles that are players in the game of the



BARYONS:
THREE QUARKS

MESONS:
QUARK/ANTIQUARK

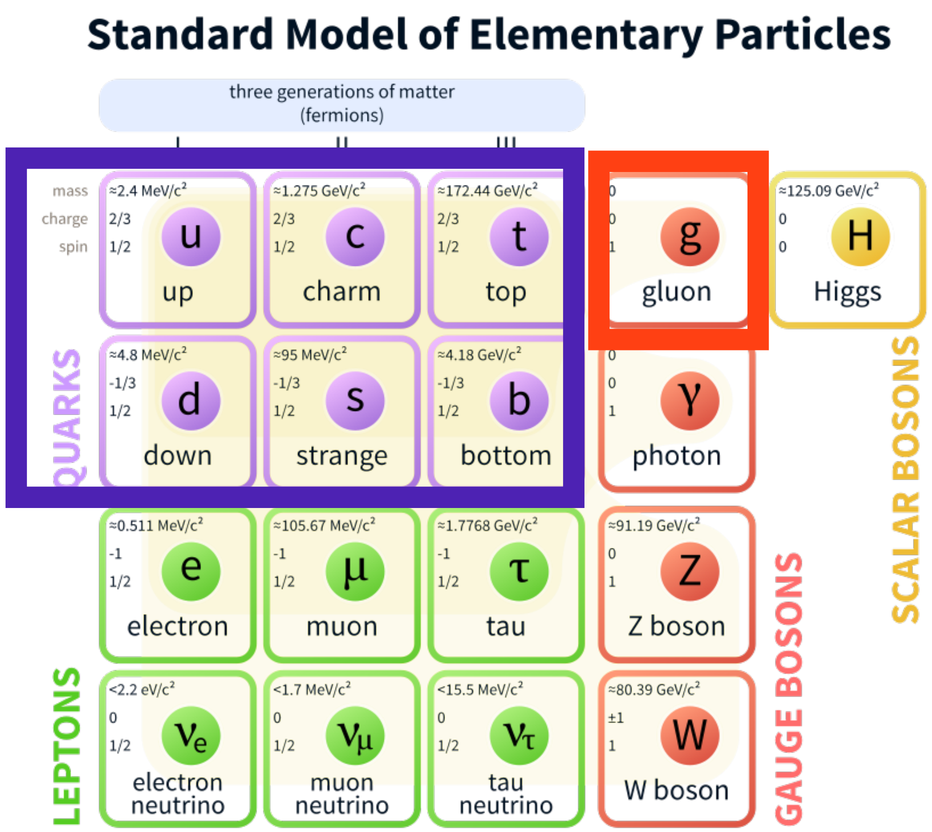
Supply the forces that hold nuclei and atoms together

Don’t usually see them but they’re all over the place

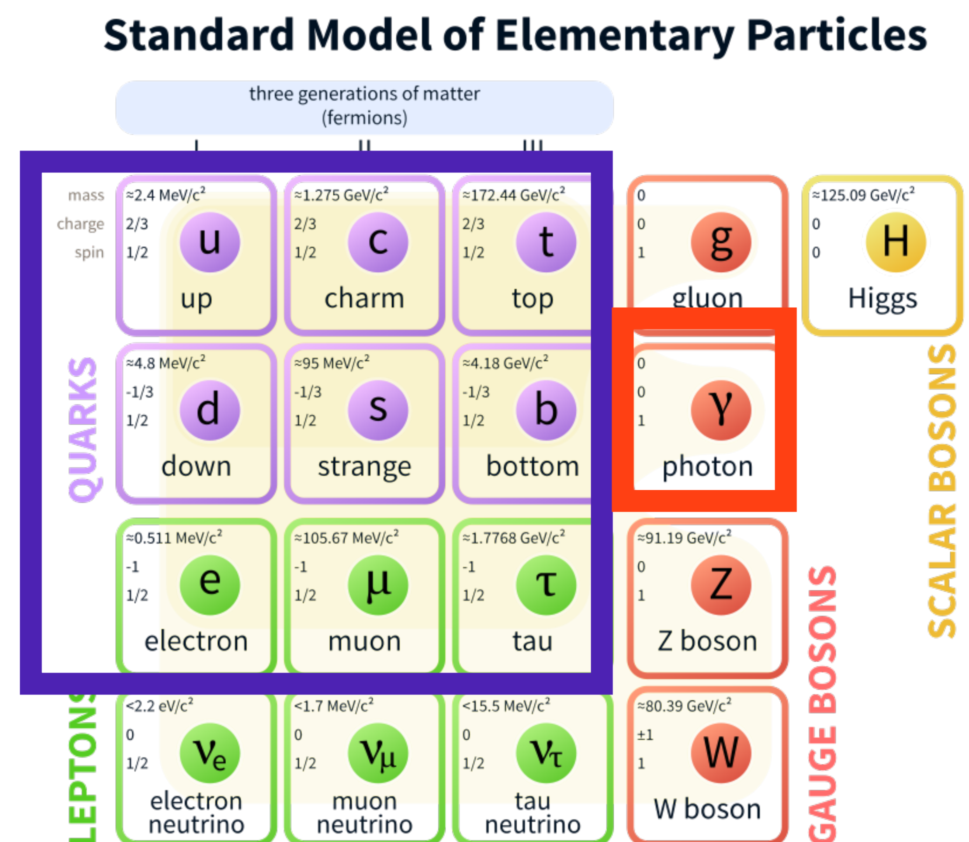
The fermions carry “spin 1/2”
The basic quantum of angular momentum and force particles “spin 1”.
Their spin directions can change, but never, ever slow down.

FORCES

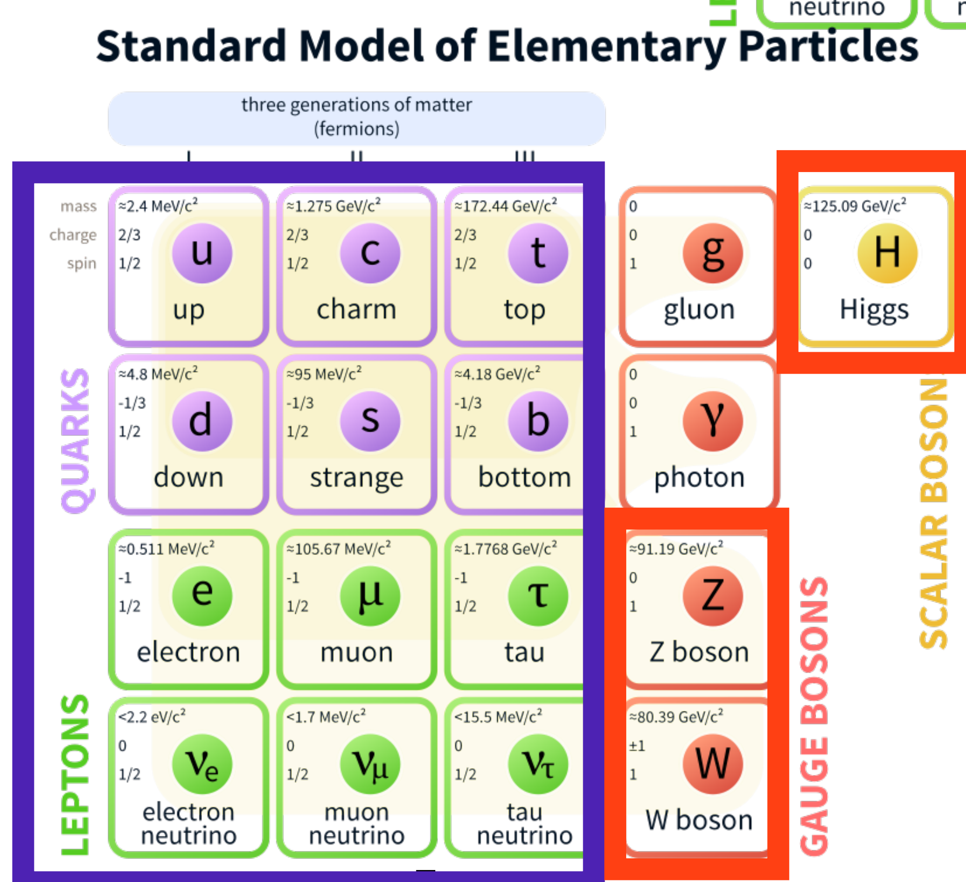
The strongly interacting fermions & their gluon (QCD):



The charged fermions & their photon (QED):



All the fermions experience the weak force:



Where have they been? The three unseen realms

- Right after the Big Bang, all particles mixed freely. Decays were balanced by production, but as the universe expanded and cooled, high energy collisions ceased.

- **Heavy particles decayed and were not replaced, and are now found only in short-lived virtual states, from which they can only emerge with sufficient energy before decaying once again.**

- **Yet other components of the universe appear to be "hidden" from us by not sharing E&M: dark matter.**

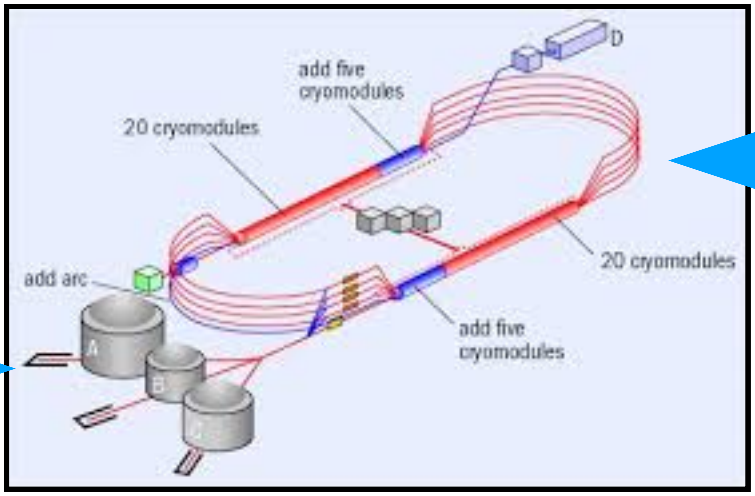
- **Stable quarks and gluons retreated to the tiny volumes of protons and neutrons, surrounded at great relative distances by electrons and photons.**

Experiments and theory at Jefferson Laboratory seeks out matter in each of these realms.

JLab is using the players: quarks, gluons, electrons and photons. . .

Quantum field theory provides the rules.

Nucleons await them in the experimental halls.



Electrons are accelerated around the loops

Quantum field theory systematizes the "duality" between fundamental and emergent, and we use each to explore the other.

2. The Game of Quantum Fields

The Rules: Equations that govern the visible universe.

For ΔT a small time:

("Amplitude" for a new list of particles at time $T + \Delta T$)

=

(ΔT) x [rule for changing the list] x (Lists of particles at time T)

(Schroedinger equation)

Rules act on any list of fermions and bosons

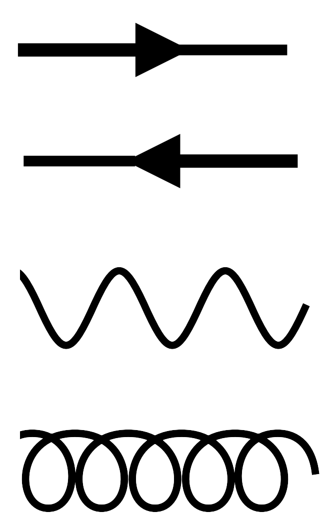
that we represent as

Quark or lepton

Anti-quark or anti-lepton

Photon or weak boson

Gluon

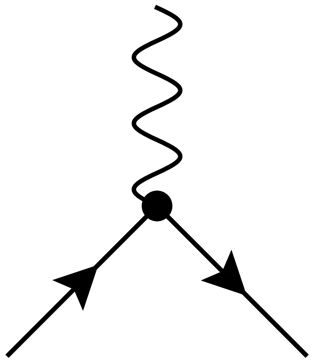


The list of particles is a possible configuration of the field(s) associated with those particles

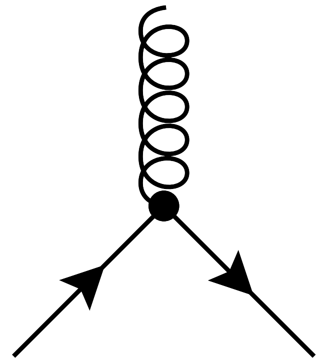
The Beautiful Theories of the Standard Model

Here are the rules for the electromagnetic, strong and weak forces. They are each proportional to a "charge": electric: e, strong: g_s, or weak: g_W.

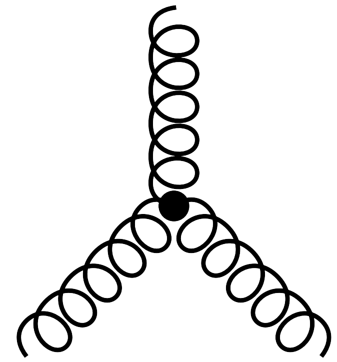
Rules for three particles



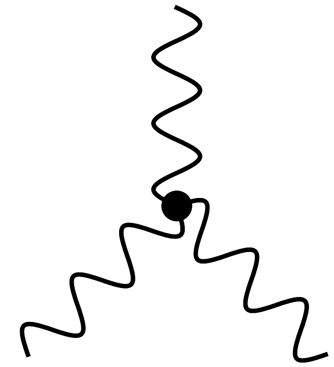
charge e



charge g_s



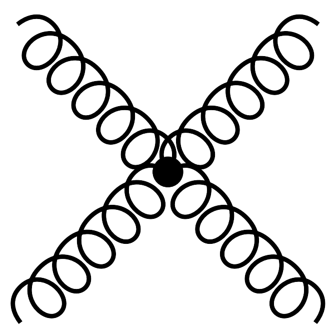
charge g_s



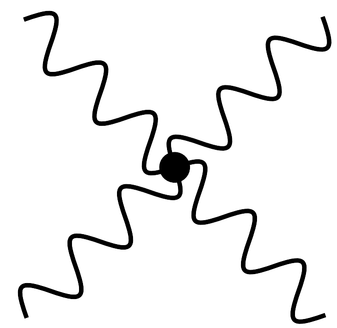
charge g_W

Rules for four particles

Yang-Mills theories (1954) for the strong and weak interactions - charged vector particles.



charge $(g_s)^2$

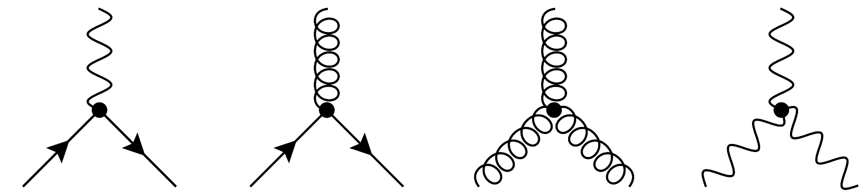


charge $(g_W)^2$

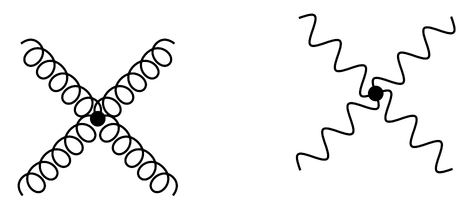
All time directions are allowed! (Dirac, 1928)

So, these:

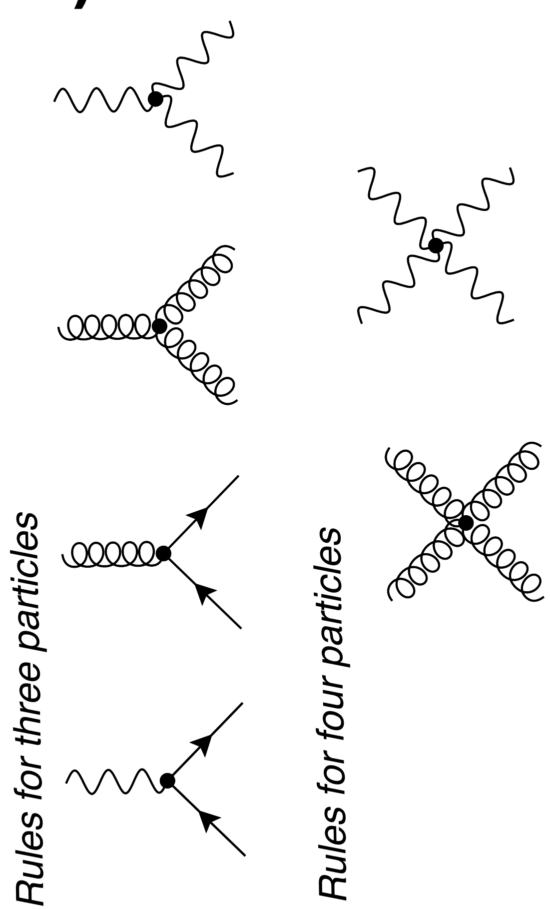
Rules for three particles



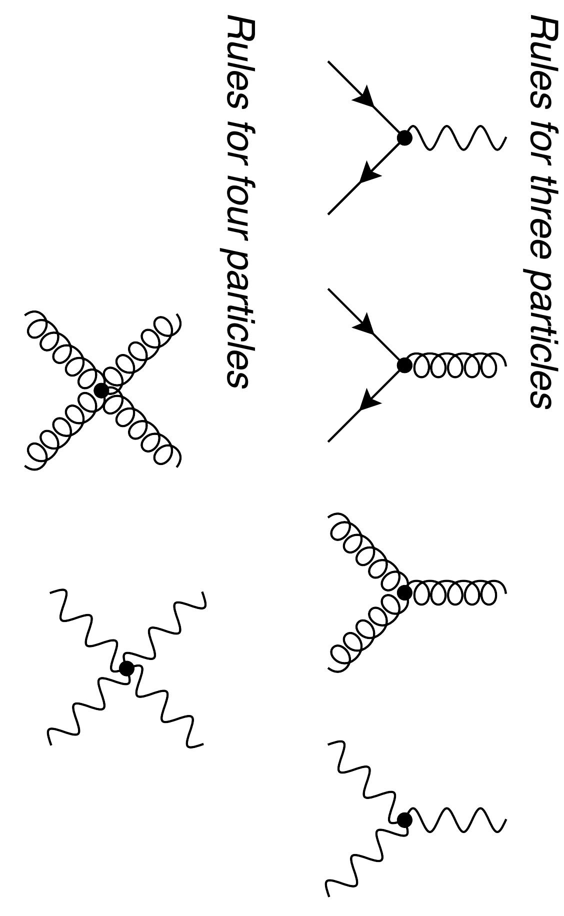
Rules for four particles



Implies these:
(pair production and antiparticles)

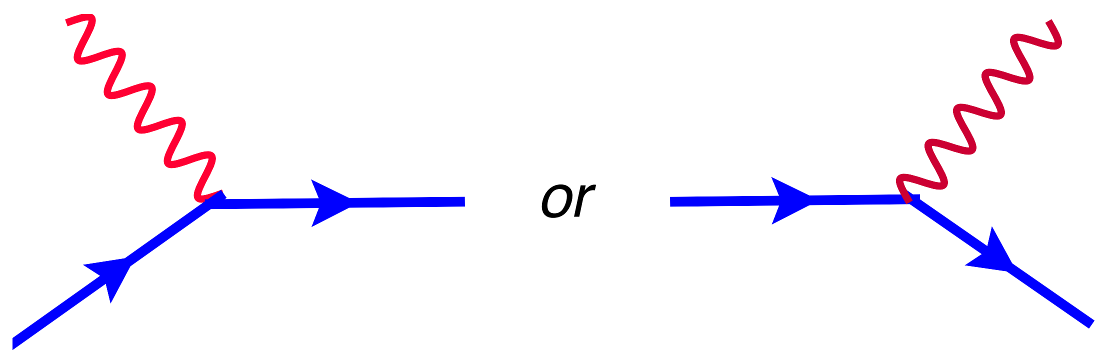


and these too:
(pair annihilation)

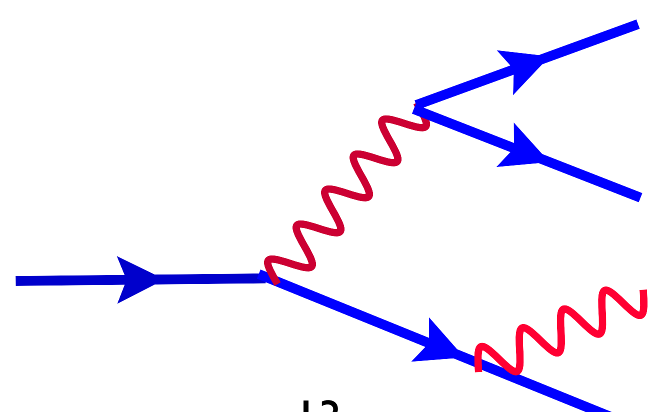


Here's how it works: the stories:

There is a kind of restlessness in nature: every single particle is constantly trying to unwind a whole new world out of itself, and at the same time to ravel it back up, always through simple steps that increase or decrease the number of particles by one or two.



And it keeps going on and on.



Pair creation - particle and antiparticle (same mass opposite charge(s))

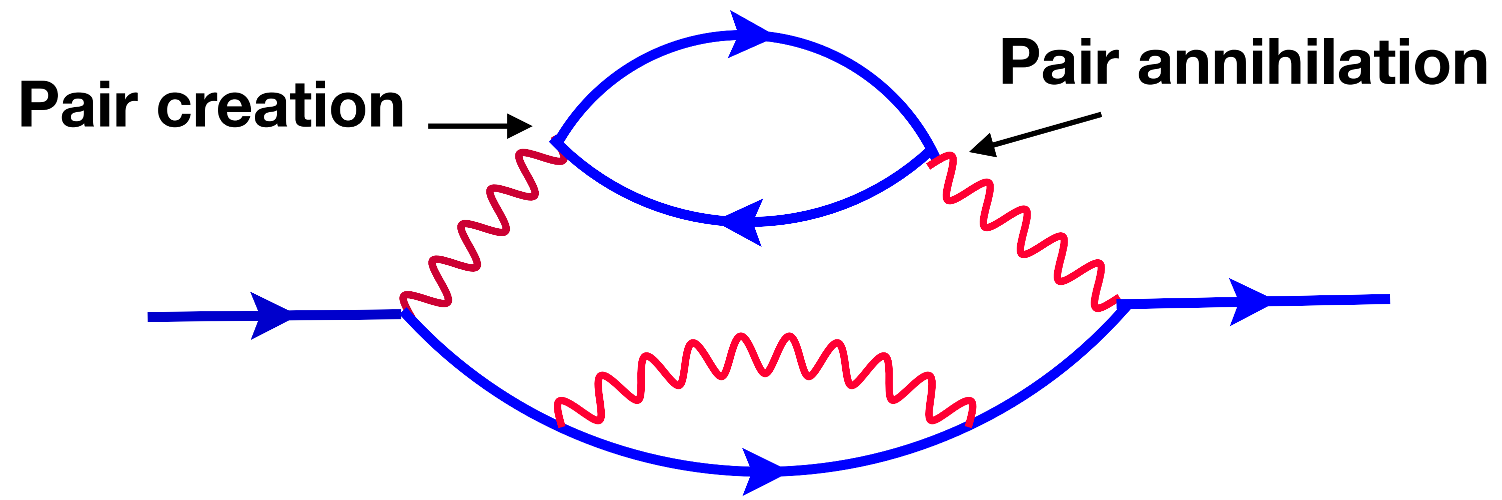
Radiation

But, sadly, for an isolated electron, all of these states have energy greater than the electron's energy, by some amount, say ΔE.

These are called ``virtual states", and they live only for a time of about

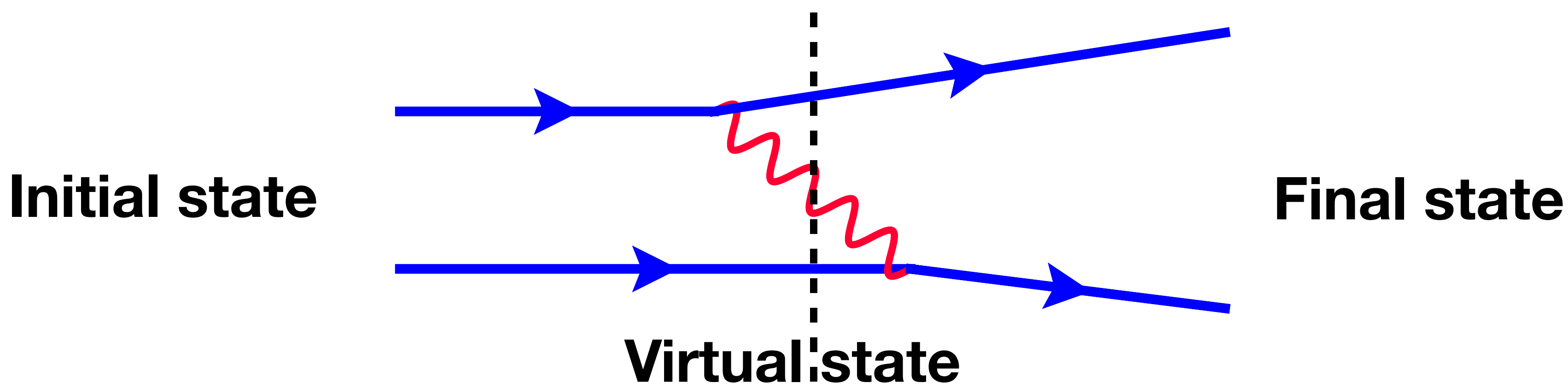
$$T = h/\Delta E$$

before they are wound back in, like

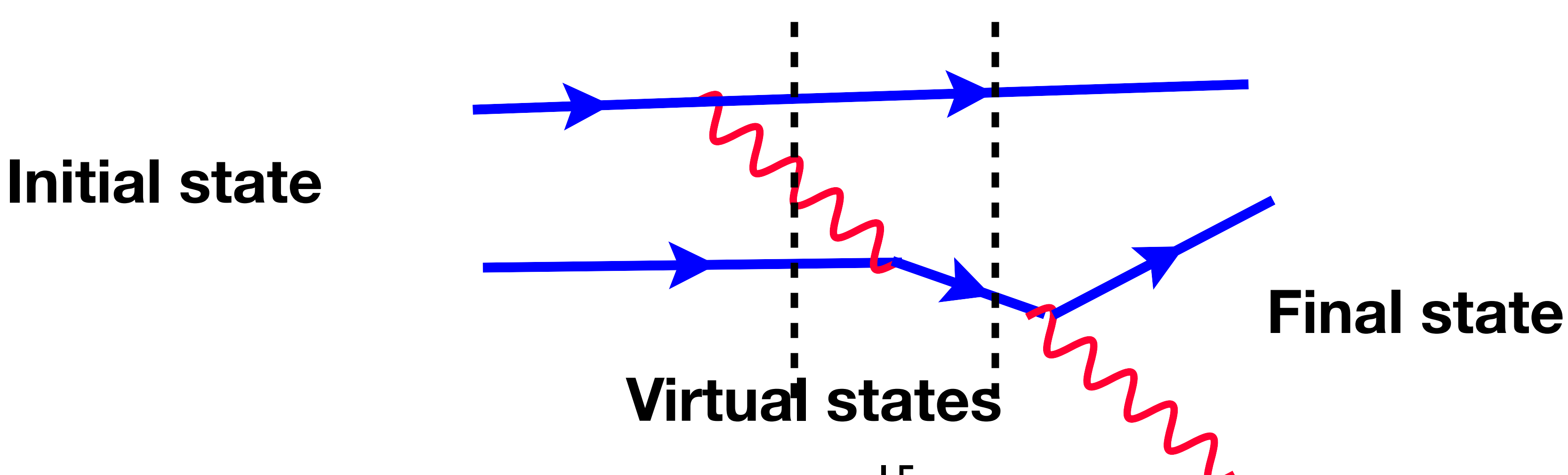


And no matter how hard it tries, each particle in isolation returns always to itself, only to start all over again.

But starting with two particles in a state, together they have enough energy to produce new states by spending short amounts of time in a series of virtual states. "Scattering".

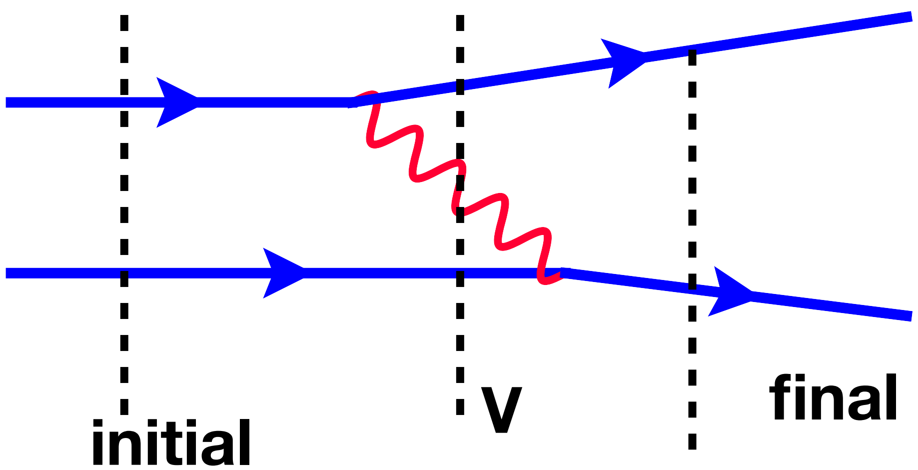


The higher their energy, the more states they can bring about. This is how things happen . . . for example, X-rays are made by adding another virtual state.



From pictures to predictions

For each process given by a picture, there are rules to calculate a wave height, or "amplitude" (Feynman). The amplitude is just a number, found like this:

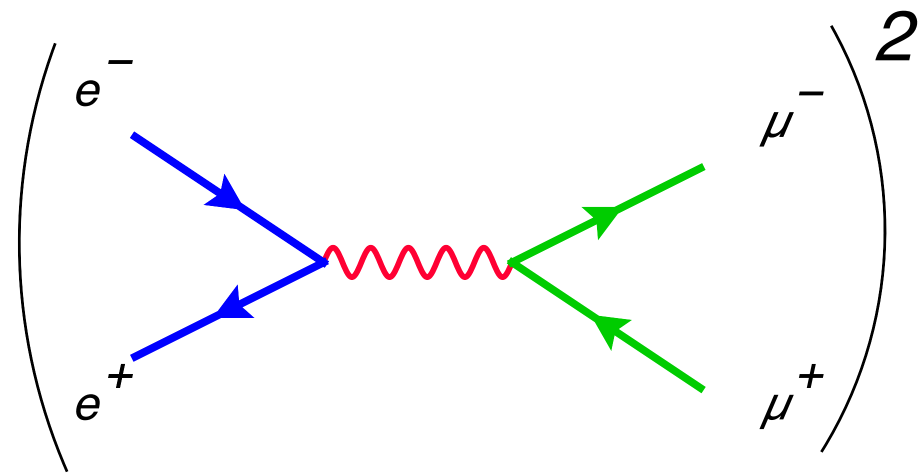


$$= e^2 \left(\frac{\Delta T_V}{h} \right) \times \text{(factors of particle energy)}$$

$$\Delta T_A = \frac{h}{E_V - E_{initial}}$$

The PROBABILITY for any process to happen is proportional to the SQUARE OF THE AMPLITUDE, just as the density of photons in a wave is proportional to the square of the Electric field.

For example, the amplitude that corresponds to the creation of a muon-antimuon pair from an electron-positron pair in a head-on collision, the probability is given by



= $e^4/8\pi$ when the muon is in the same direction as the electron
= $e^4/16\pi$ when the muon is produced at right angles to the electron

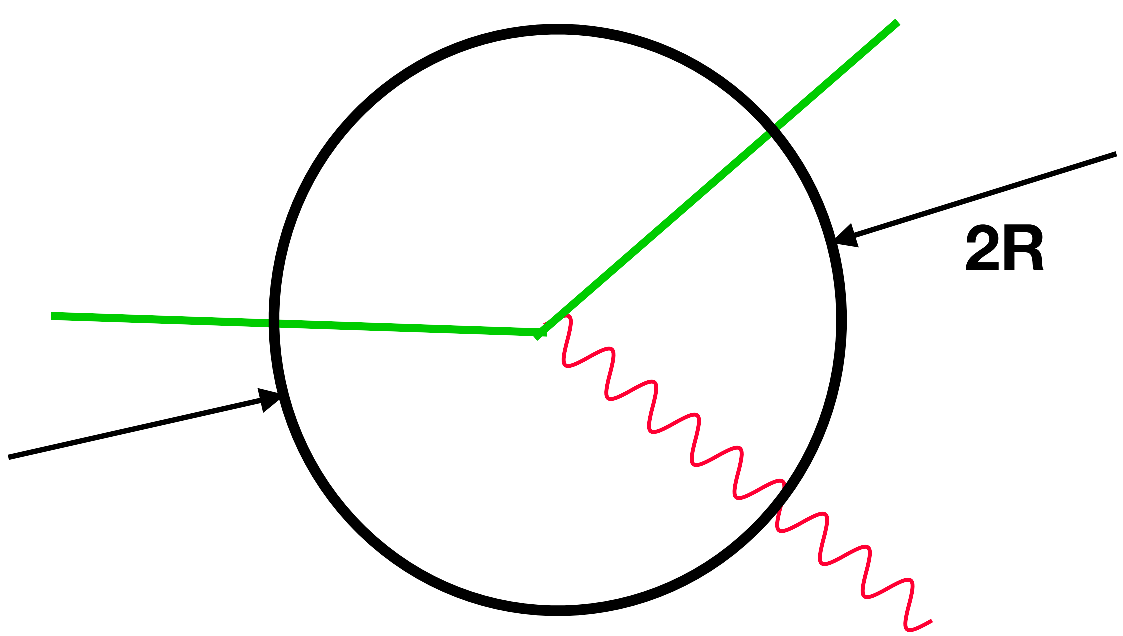
Simple!

But it gets more complicated quickly with more virtual states.
Because e is small, however, this prediction is pretty accurate.

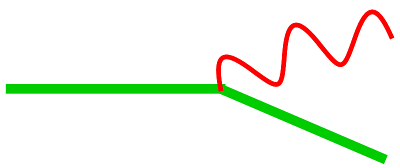
This is quantum field theory.

There is no limit to how short a time virtual states might live — no limit to the energy they might have.

So the closer you look at an interaction, the more you will find. Look inside a radius R, and find not only



but also . . .



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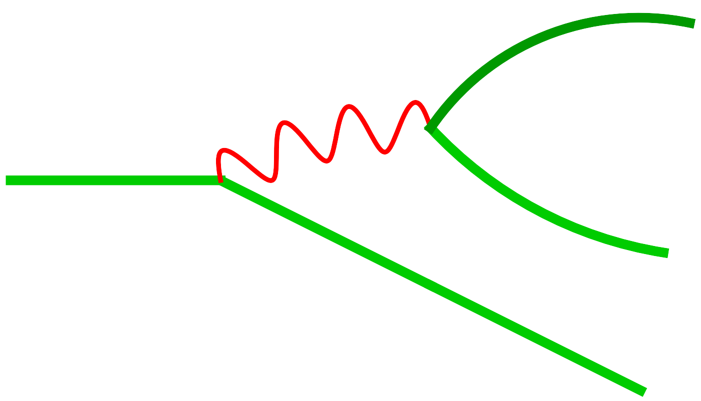
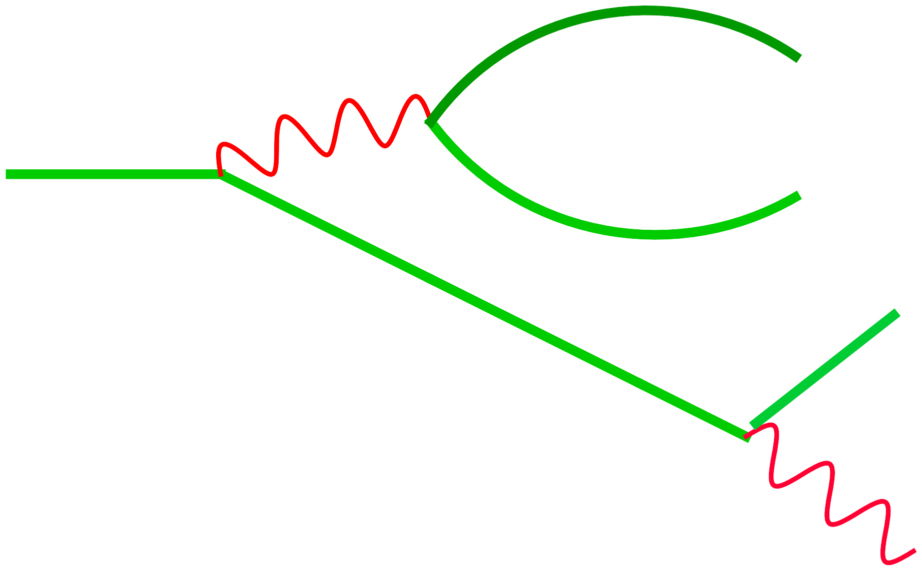
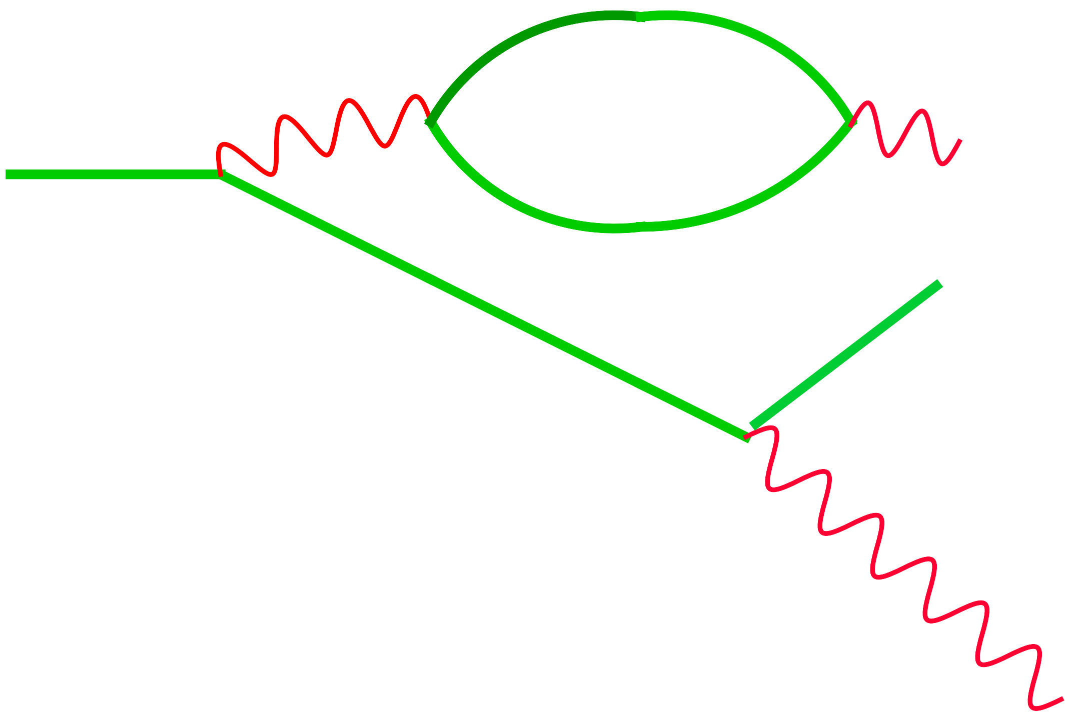
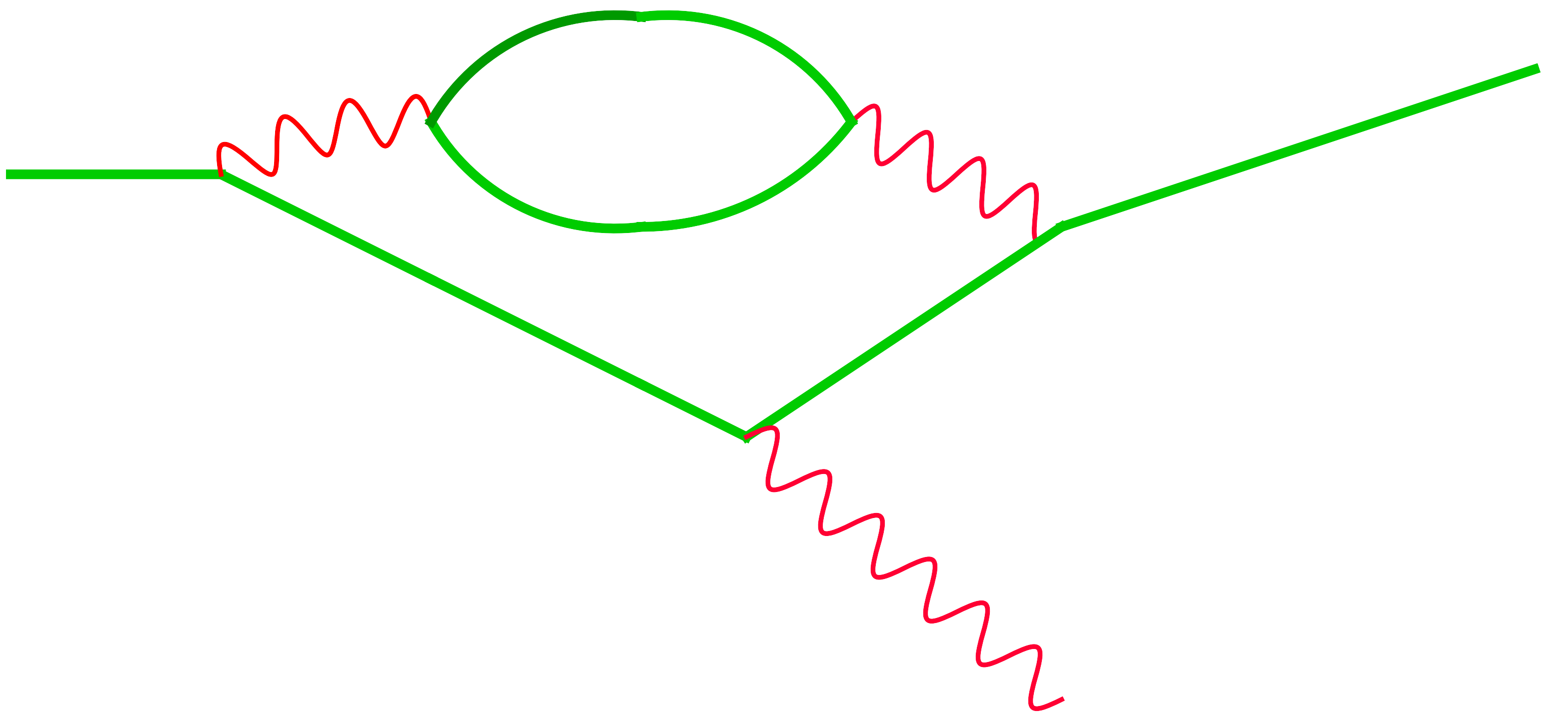
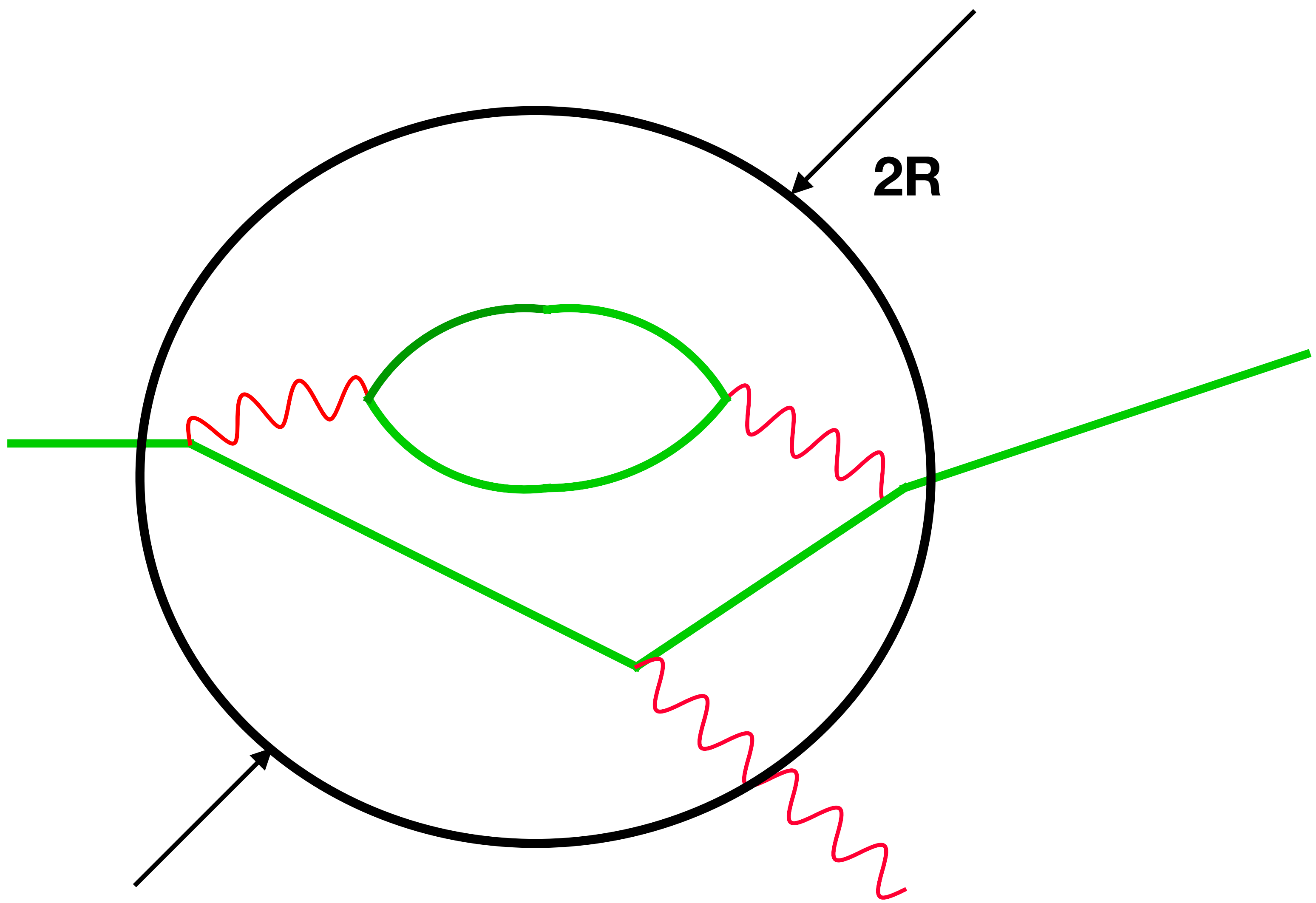






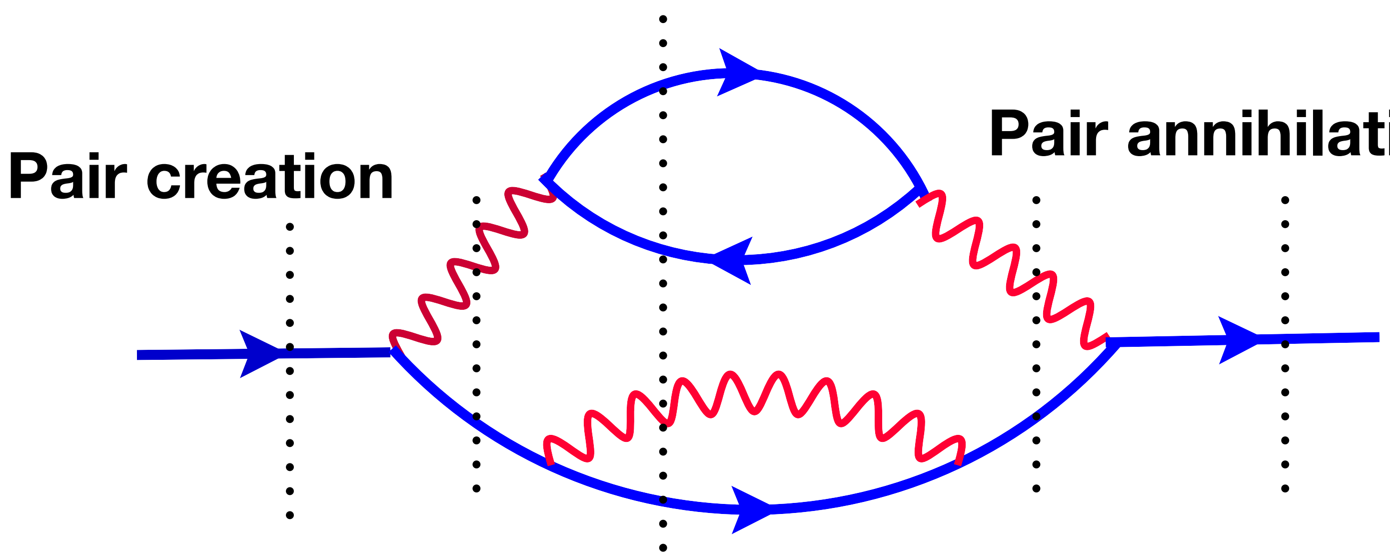


We can actually calculate how all these diagrams depend on R. This is called the "running coupling" and is usually given as a function of the de Broglie wavelength that corresponds to radius R: $\alpha(p=h/\lambda)$ [$\alpha=e^2/4\pi$]. For QED this technique is not such a big effect, but it is very important for the strong interactions.



What do we see? "States" Collections of particles that don't change in time

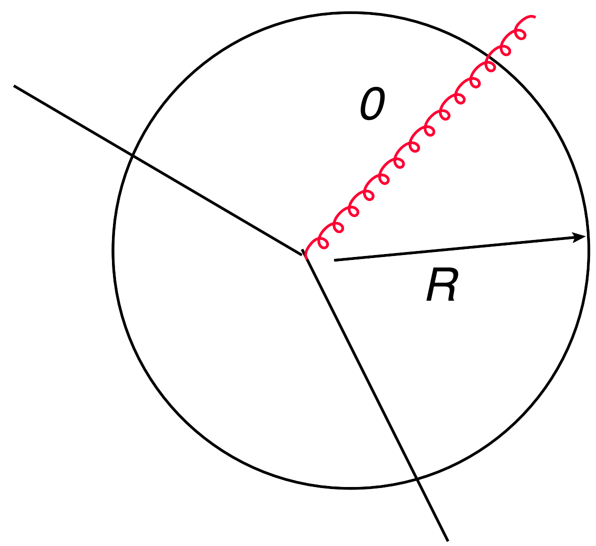
[rule for changing the list] x (Sum of lists of particles) = (Same sum of lists of particles)

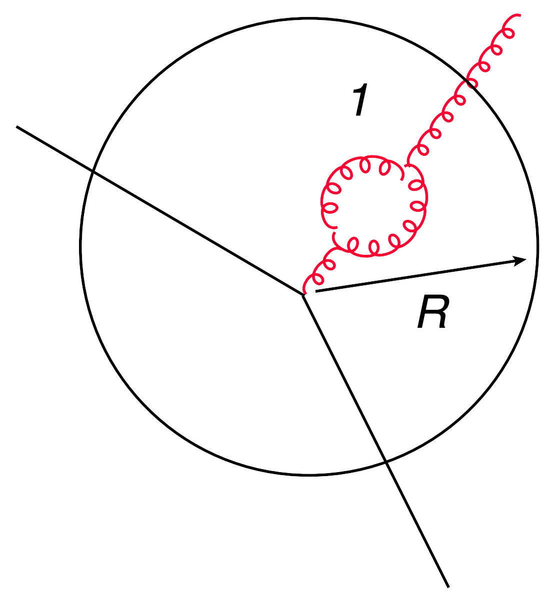


Individual electrons are really collections of these states and more, but its still. "just an electron with some friends".

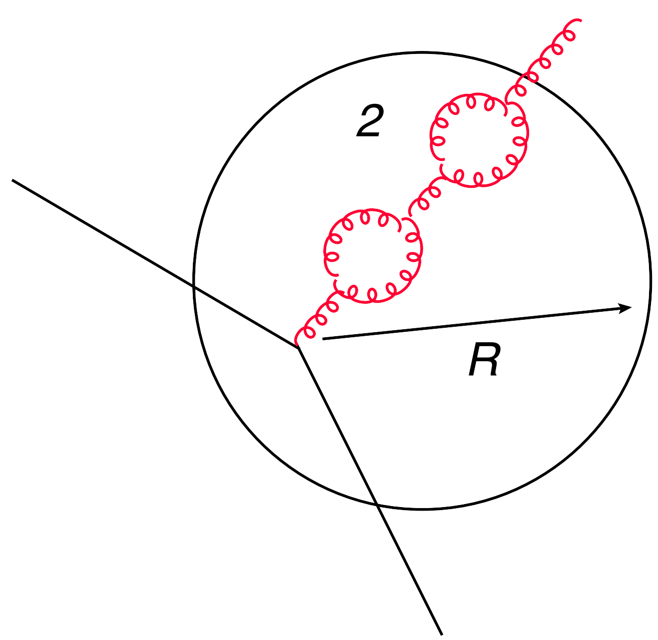
3. What makes QCD different

But quarks are very, very different. Why? States with two extra gluons add up to infinity for R about 1 Fermi. There has to be a nearby source to absorb them. Quarks cannot appear alone; this is called “confinement”.





This is not something proven, but demonstrated by “numerical lattice simulations” which provide beautiful agreement in hadronic mass differences



+ . . .

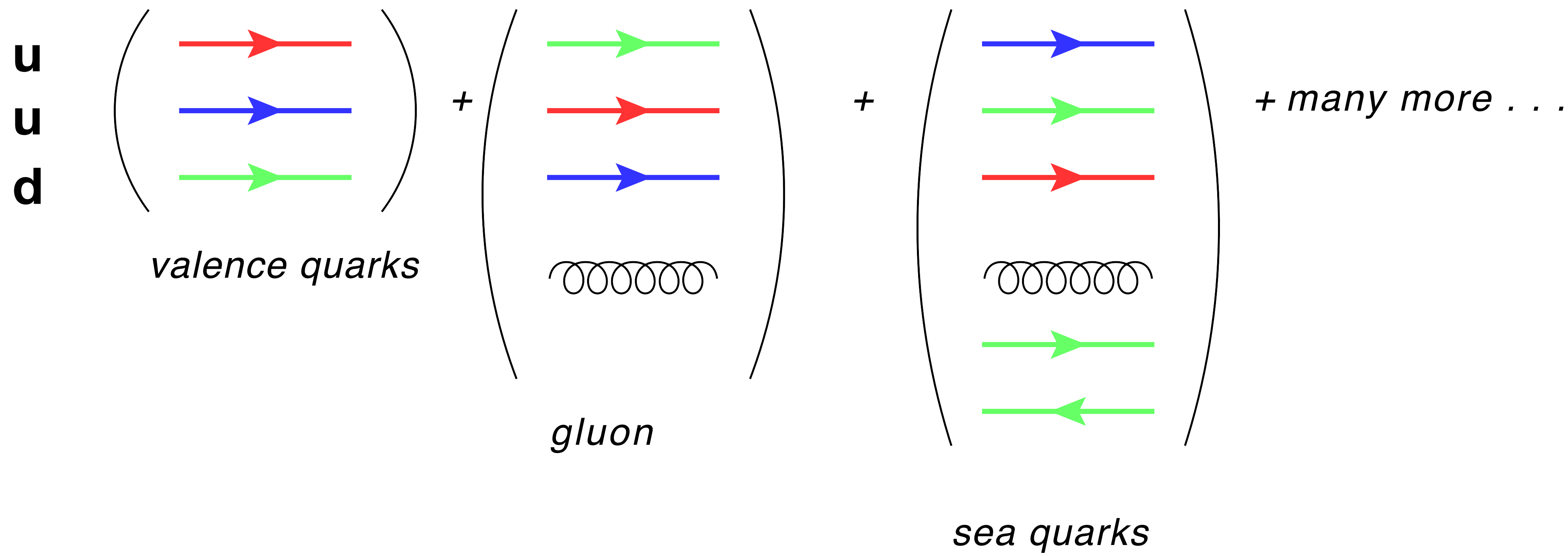
Each increases with R.

For R about 1 fm, they are all equal!

Asymptotic Freedom: Smaller (Larger) R gives weaker (stronger) forces

This means that the "states" of QCD are really different.
They are the protons, neutrons and other hadrons,
mostly made of three quarks (baryons). and quark-antiquark (mesons).

Our world, of course, is mostly protons, neutrons and the nuclei they can make. In our pictures, they are represented like:



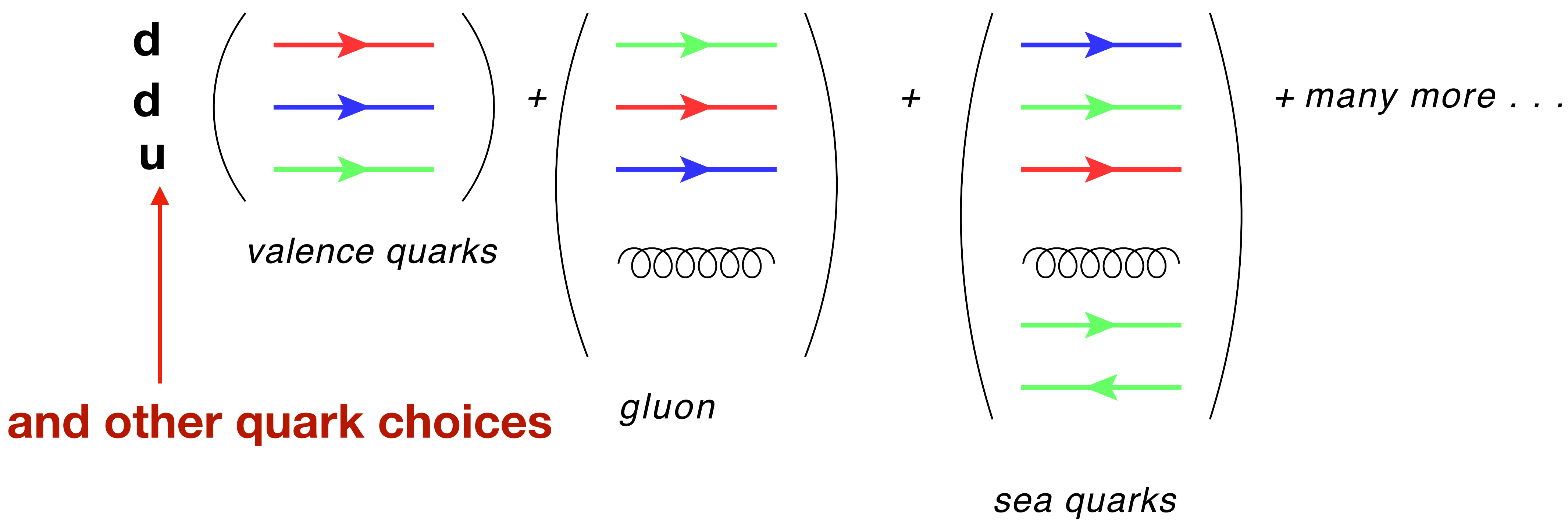
= | proton >

Taken all together, the proton has spin-1/2, the same as an electron or a single quark. It has a definite mass and charge +1. It is extraordinarily stable, and is the ultimate decay product for heavier solutions to the QCD Schrodinger equation.

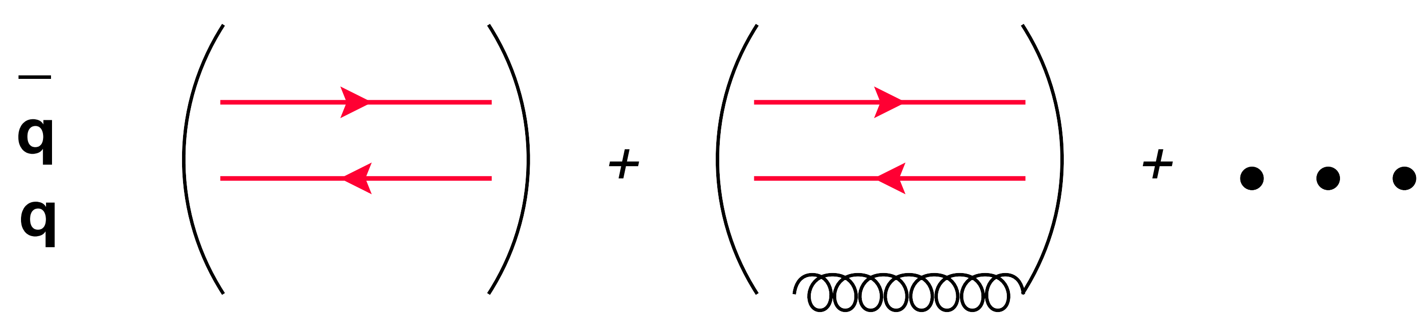
The other “classic” states:

[rule for changing the list] x (Sum of lists of particles)
= (Same sum of lists of particles)

| neutron > =



| meson > =

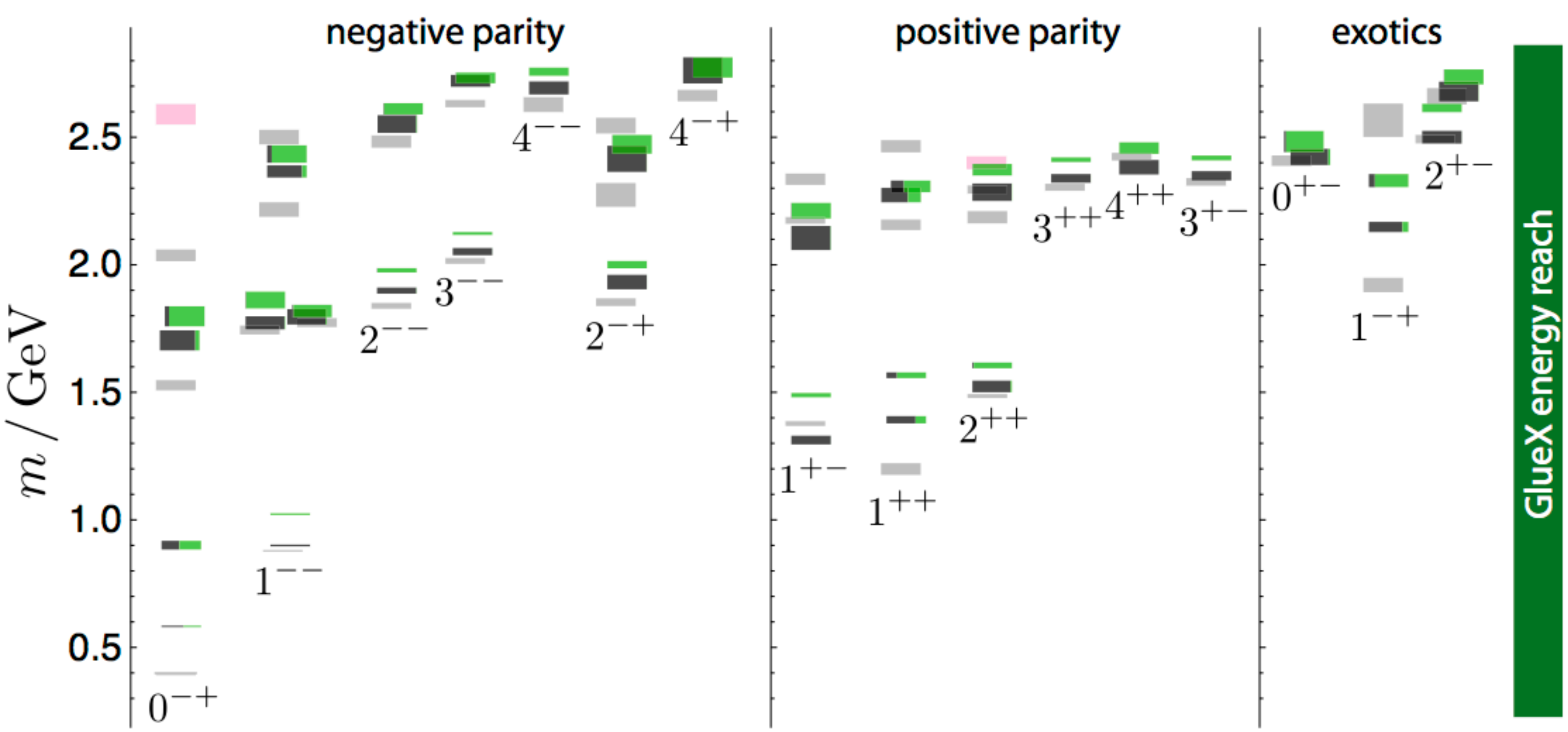


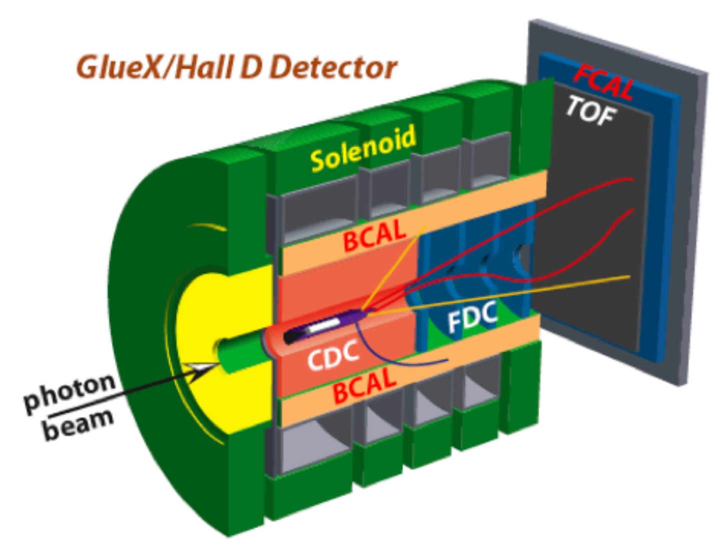
“On the lattice”: very roughly — the computer starts with list of just three quarks, or a quark and an antiquark fixed at some position. The state can be given “extra” properties, like spin and left-right symmetry (parity).

Fun part: “uncertainty principles” in QFT mean that states of all energies will emerge.

It then solves the Schoedinger equation (rules for how the list changes in time) and looks for the lowest energy state that is produced.

For example, from the USQCD Collaboration collaboration web site):

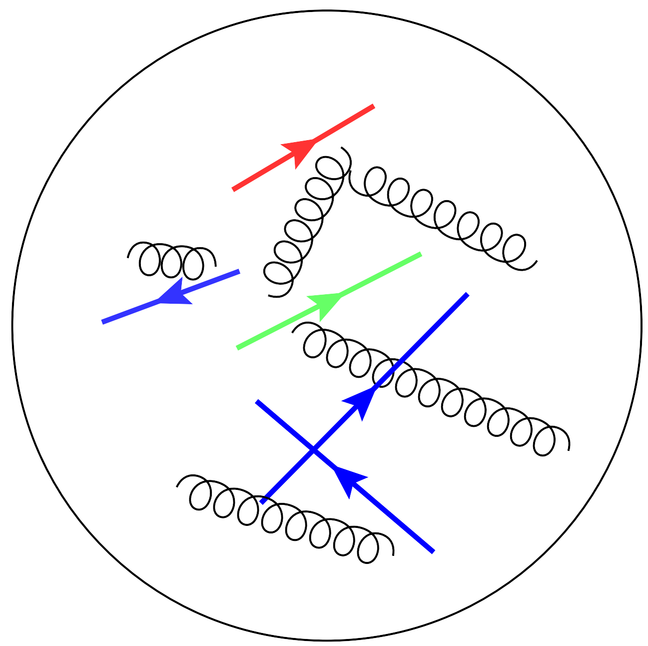


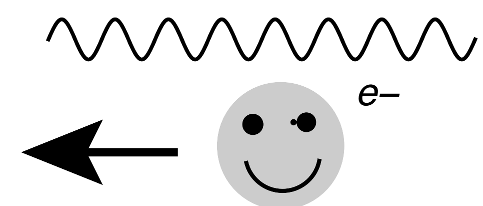


Lattice QCD calculations of the meson spectrum suggest the presence of many exotics.

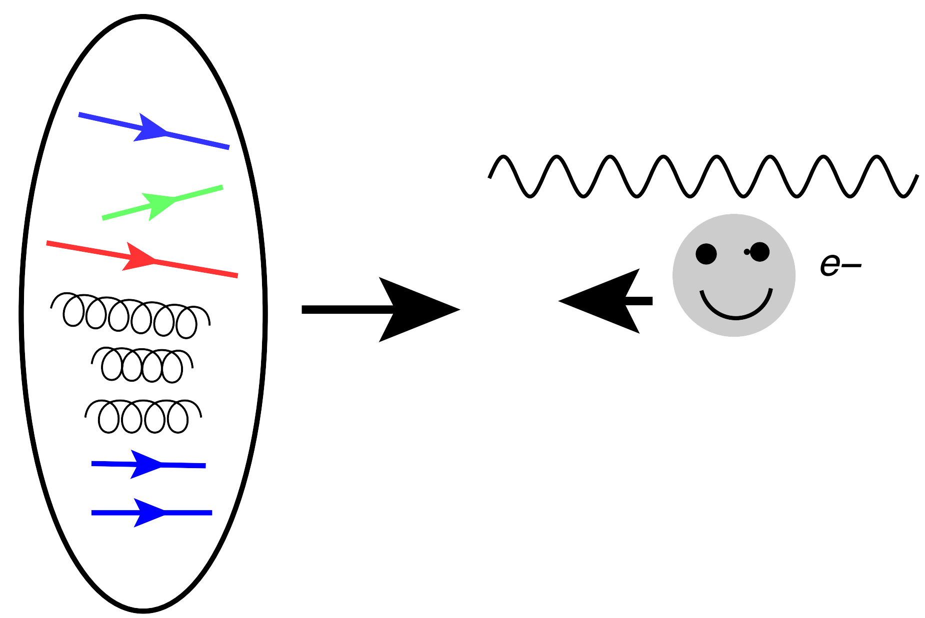
What a proton looks like at JLAB, and why you need high energy to see inside:

At rest, a proton looks like this, with partonsgoing every which way.





But from the electron’s point of view,they all line up (almost)



To a good approximation, an electron arrives in a virtual state with a single extra photon.   Only that photon interacts directly with quarks in the proton. How much can you get from that?

Quite a lot!   When that photon is absorbed by a quark

1. The proton may remain "whole", but start moving: elastic scattering.

2. It may produce an "excited" heavier proton: quasi elastic scattering.

3. It may break up the proton: inelastic scattering, and produce other particles, anticipated or not in QCD.

4. If it transfers a lot of energy: "deeply inelastic".

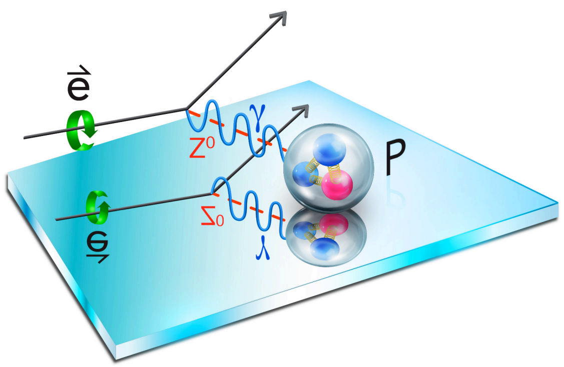
We'll see a little of what we can learn from each of these.

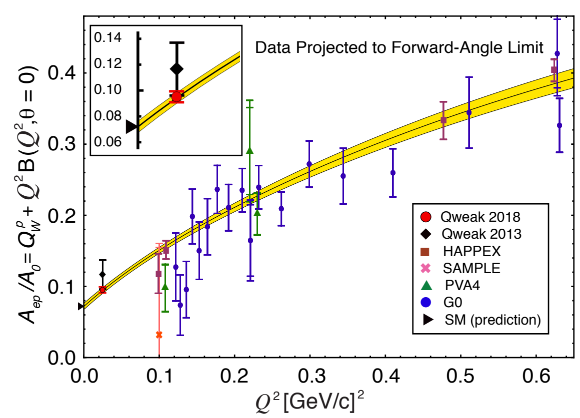
It may also be accompanied not by a photon, but by a short-lived, heavy particle like the Z-boson (a brief detour).

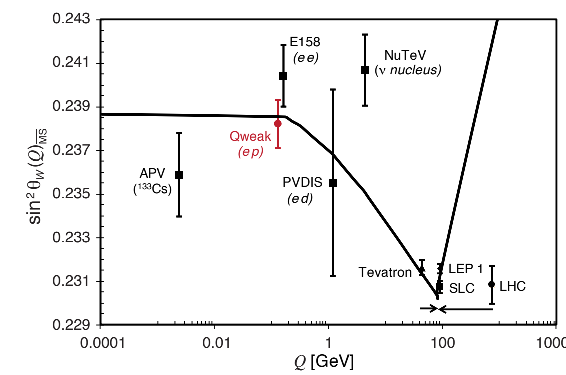
4. JLab and Dark World

Electron-proton elastic scattering through Z exchange is exquisitely sensitive to the parameters of the Standard Model, through spin-dependent parity violation.

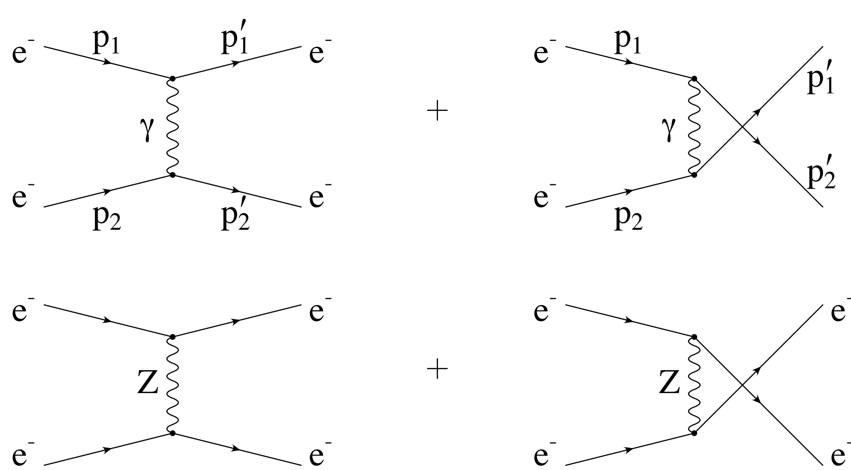
Qweak 2019 (1905.08283)

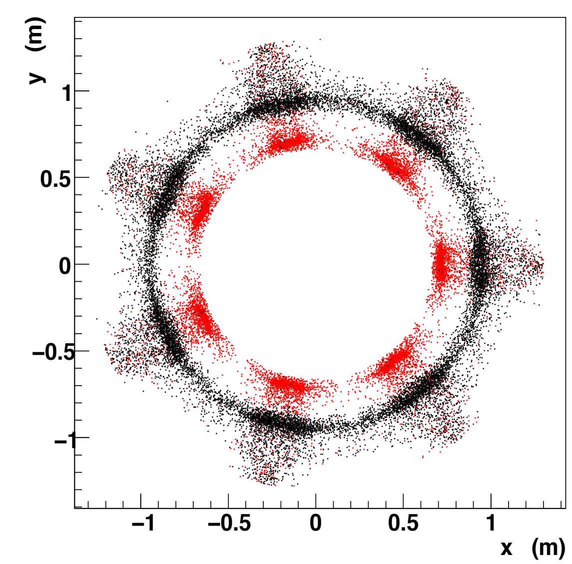






In the future the "Moeller" experiment will push tests for non-standard forces through measurement of ee elastic scattering, kinematically distinguishable from ep.

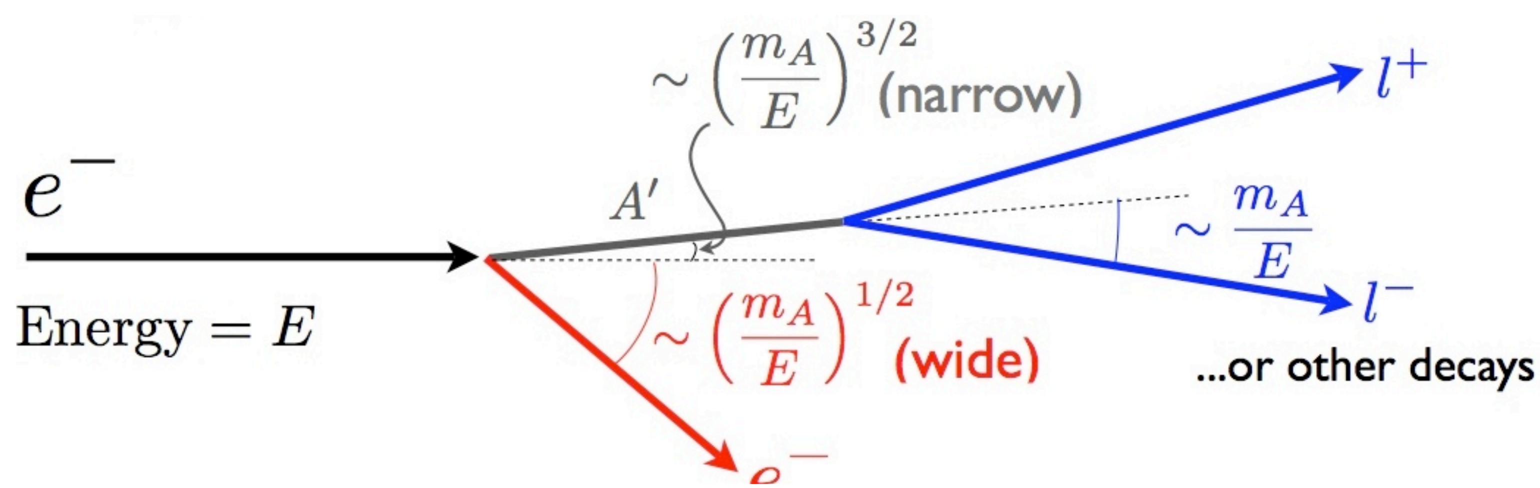




Moeller proposal, 2008

JLab and the Dark World, Cont'd

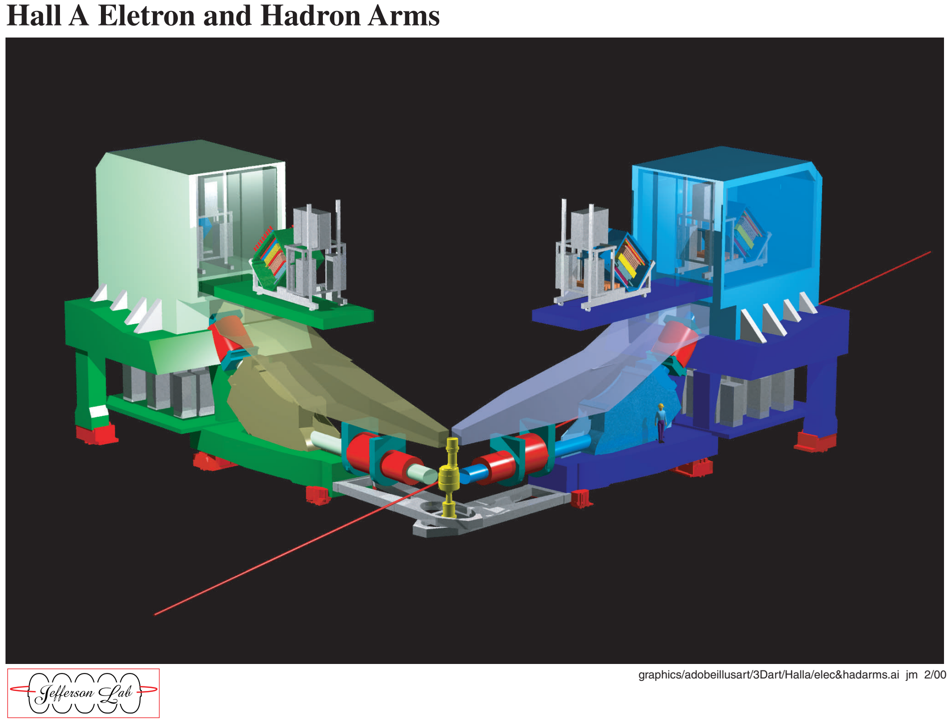
The electron may emit a new kind of particle: "dark photon", a "portal" to dark matter in many theories, not detectable in previous direct-detection experiments.

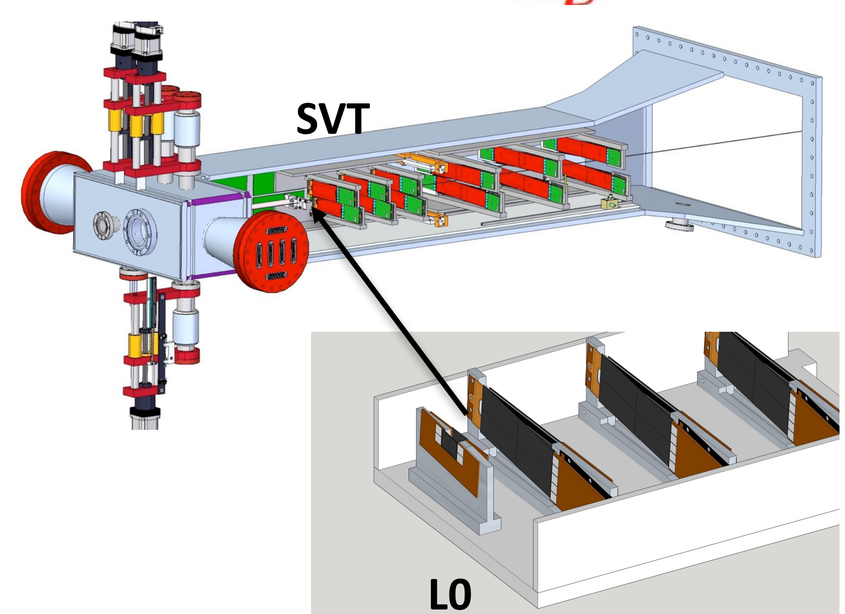


APEX Hall A

Wojtsekhowski, 2018

Hall A Eletron and Hadron Arms





HPS (Hall B)

Stepanyan, 2017

5. Exploring QCD at JLab

JLab and the hidden world of the strong interactions.

Through the looking glass into the micro world of the nucleon.

The emergent structure that mediates between the point like quarks and the macro world.

What's going on in there?

A selection . . .

1. **DIS valence distributions and TMDs**
2. **Excited nucleons and duality**
3. **Elastic scattering and the nucleon radius**
4. **Exotic States**
5. **DVCS, GPDs and nucleon structure**
6. **Nuclear structure and short-range correlations**

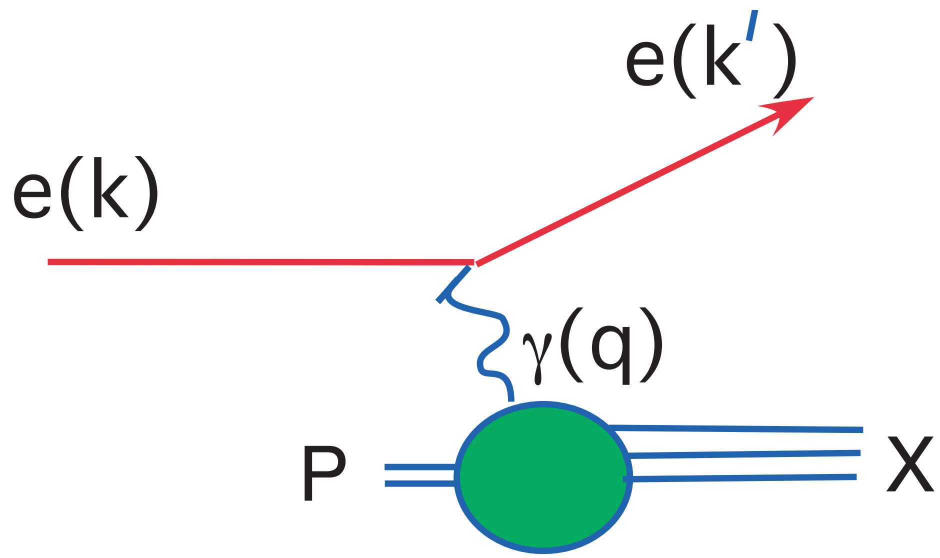
1. DIS and Transverse Momentum Distributions

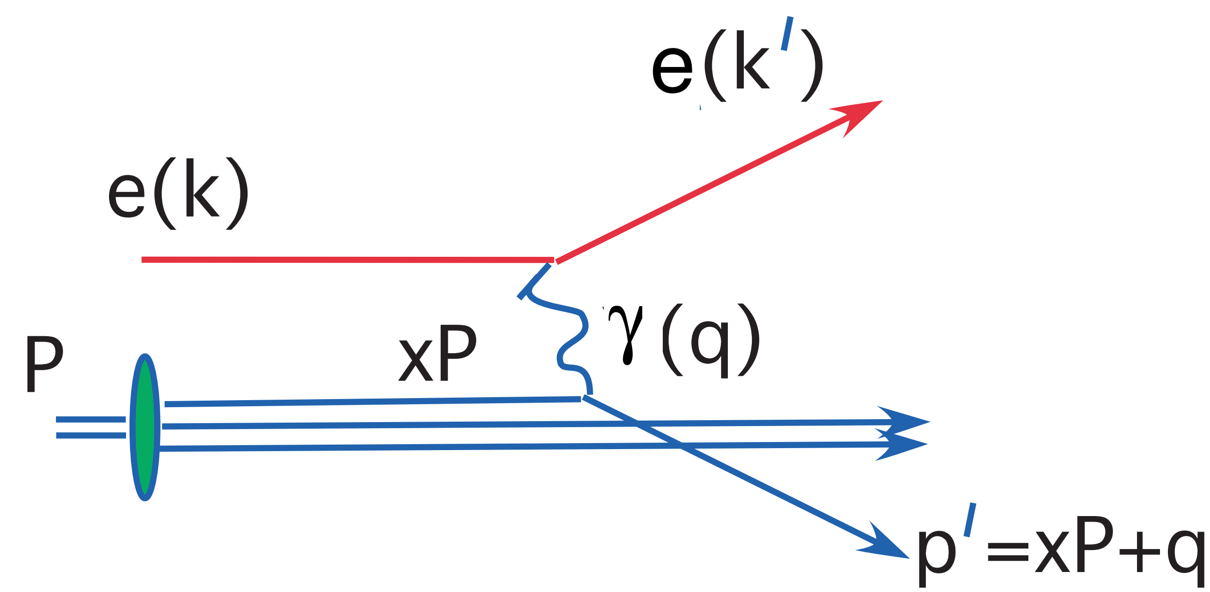
- To make a long story short: Quantum Chromodynamics (QCD) reconciled the irreconcilable. Here was the problem.

1. Quarks and gluons explain spectroscopy, but aren't seen directly – confinement.

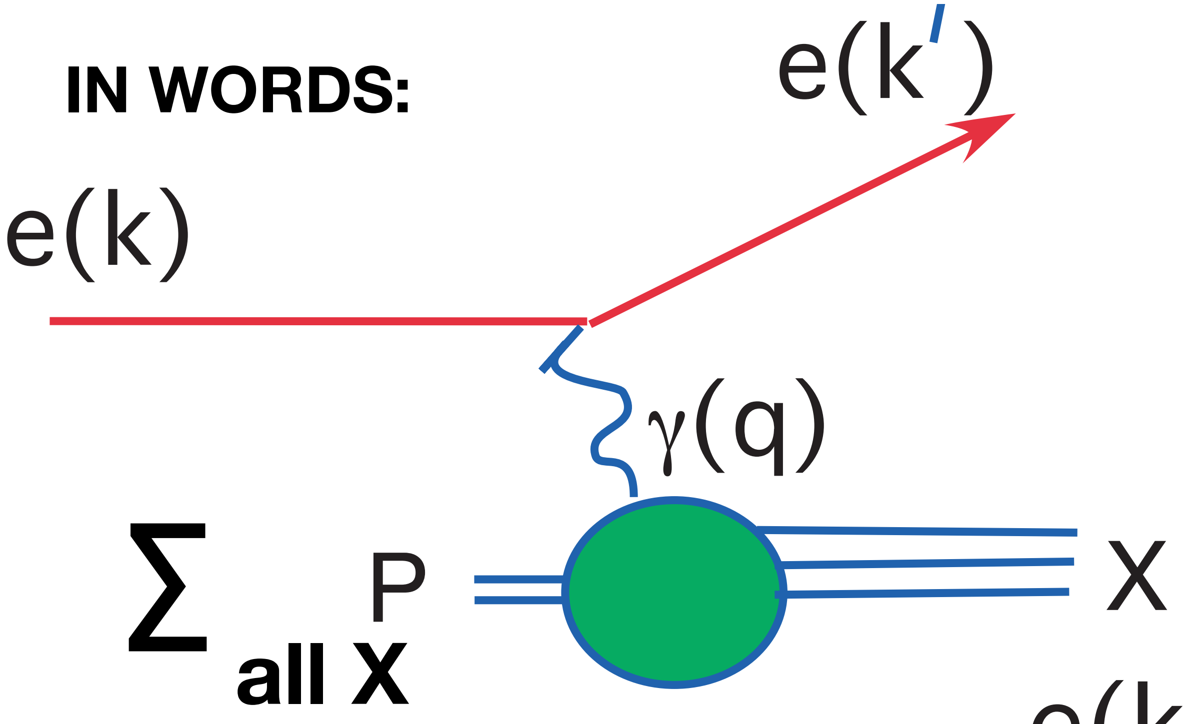
2. In highly ("deep") inelastic, electron-proton scattering, the inclusive cross section was found to well-approximated by lowest-order elastic scattering of point-like (spin-1/2) particles (="partons" = quarks here) a result called "scaling":

$$\frac{d\sigma_{e+p}(Q,p\cdot q)}{dQ^2}\Big|_{\text{inclusive}} \quad \propto \quad F\left(x=\frac{Q^2}{2p\cdot q}\right)\frac{d\sigma^{\text{free}}_{e+\text{spin}\,\frac{1}{2}}}{dQ^2}\Big|_{\text{elastic}}$$



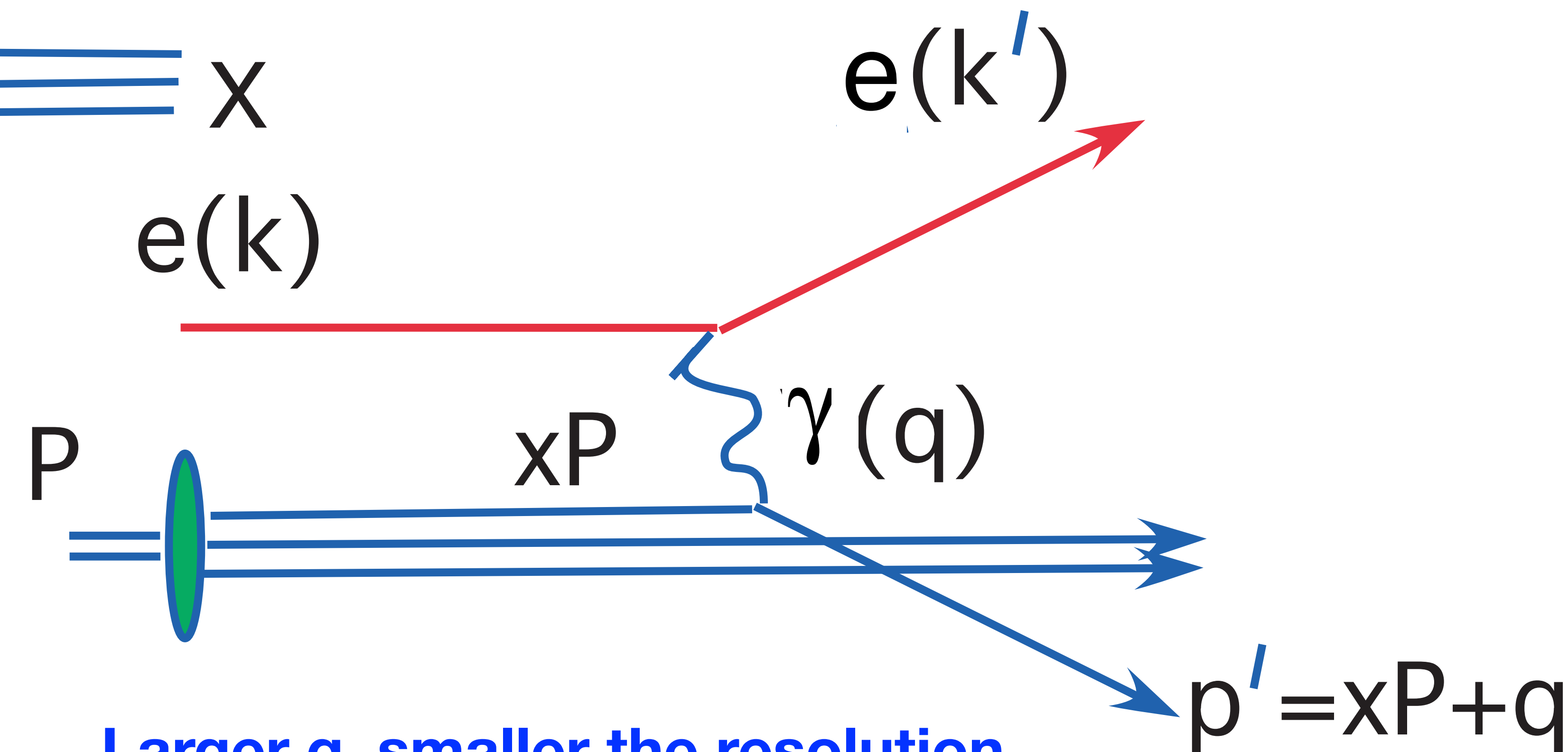


IN WORDS:



The "Inclusive" probability (Cross section) was found to be . . .

proportional to the scattering probability for free charged quarks.

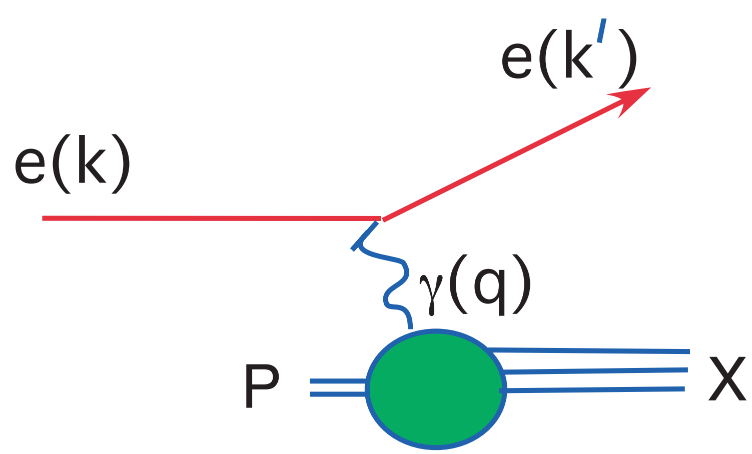


But the free quarks never showed up in experiments.
HOW CAN A CONFINED PARTICLE SCATTER FREELY?
ASYMPTOTIC FREEDOM.

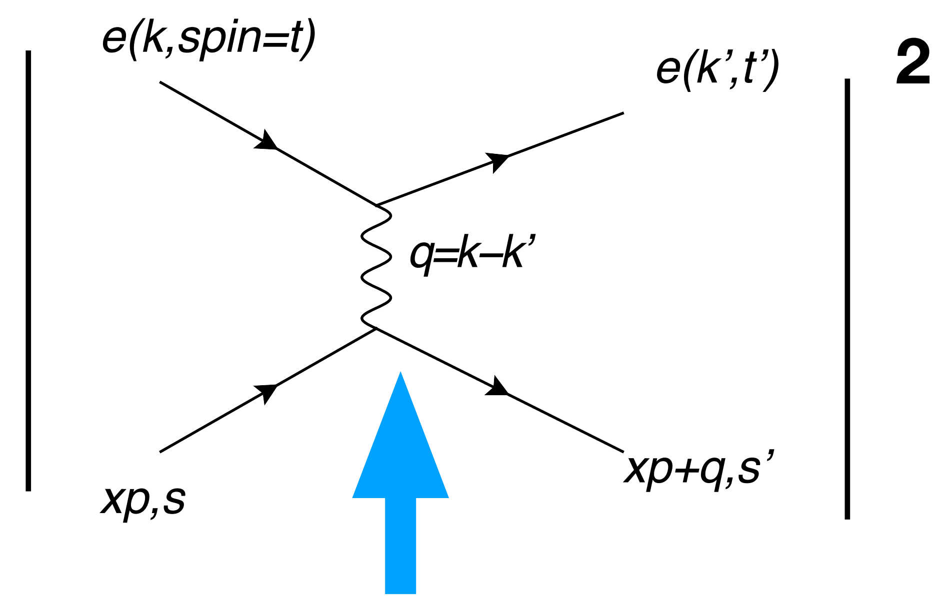
Larger q, smaller the resolution.
x is the fraction of proton's momentum carried by the parton.
DIS measures how partons share the nucleon's momentum. In the short time of the scattering, the quark is effectively fee. Confinement is too late to affect the inclusive cross section.

Basic example of a *factorized cross section:*

Product of a "universal" F(x) with a "process dependent" partonic (quark or gluon) cross section that we can compute with perturbative rules. Photon scattering can also depends on the spin of the quark.



= F(x,spin)



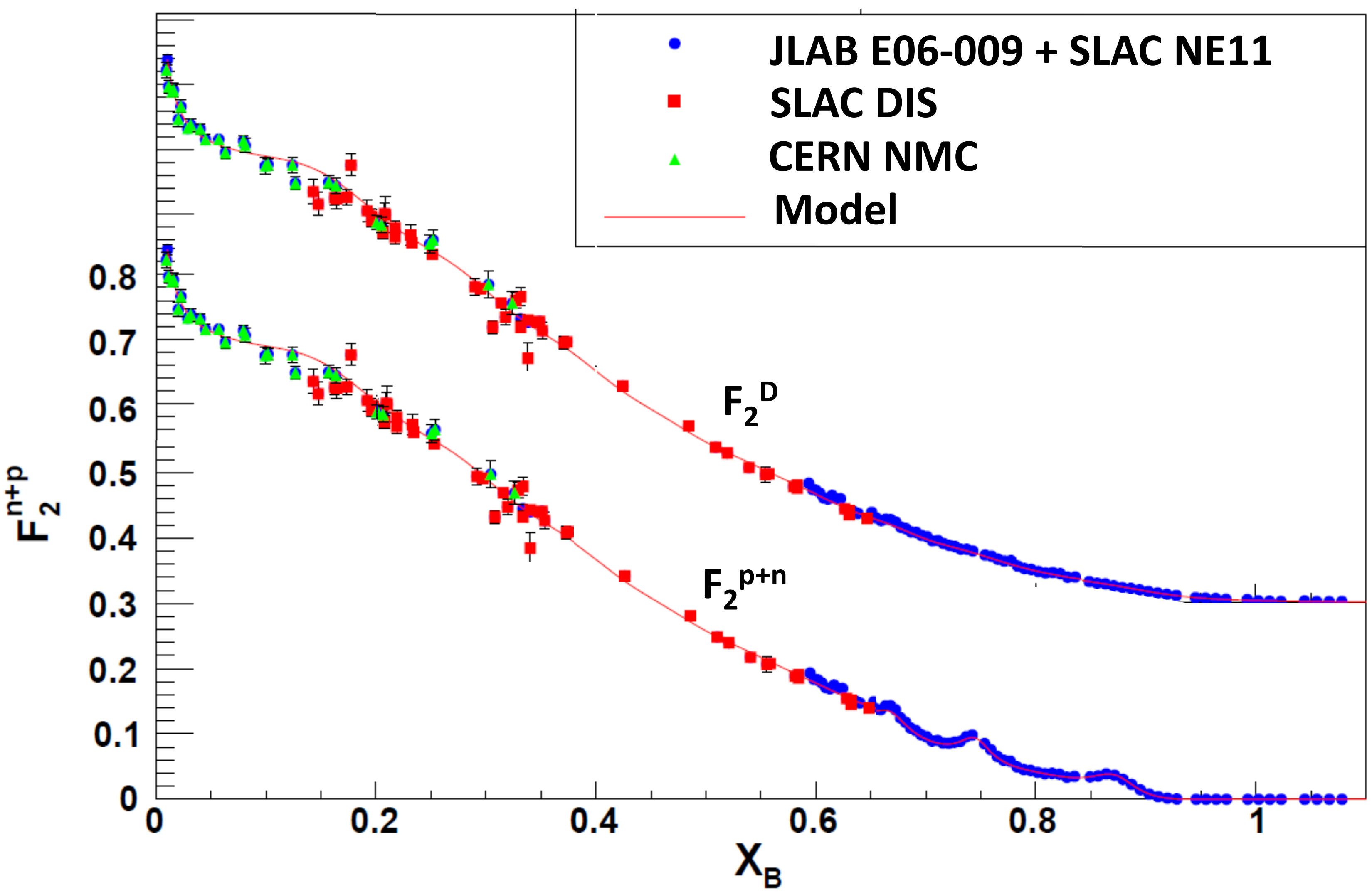
Just a single "story" - all the rest "sums to unity" if we don't ask what happens to the quark!

F(x) here is a "quark distribution" — just a function of x and spin

Important "corrections" can be computed in principle.

In effect, a beam of electrons is a machine for detecting quarks.

Unprecedented senstivity to large-x quark distributions.
(ED6-009) Hall C 2019.
Of special interest both to new-physics searches at high energy, and to nuclear structure.



And, the quark doesn’t have to be moving exactly in the same direction as the proton!

Other measurements (single-inclusive DIS) are sensitive to this extra motion transverse momentum distributions or TMDs.

These cross sections factorize too, into parton distributions, and “fragmentation functions” that depend on the “extra” transverse motion of the quarks and gluons

Corrections here are even more important, but can still be computed in principle.

With electron scattering we can measure the momentum fractions of quarks, their transverse momentum variations, and how their spin is connected to the spin of the proton and to their transverse momentum

This gives a family of functions to measure — and together they demonstrate the full correlation of single quarks to the momentum and spin of the proton.

QFT expression for such distributions: itself a story.
A quark disappears, and then reappears.

All this is to pick out the wave corresponding to the scattered quark

And the proton here

The quark reappears here!

The photon scatters the quark here. It disappears from the story.

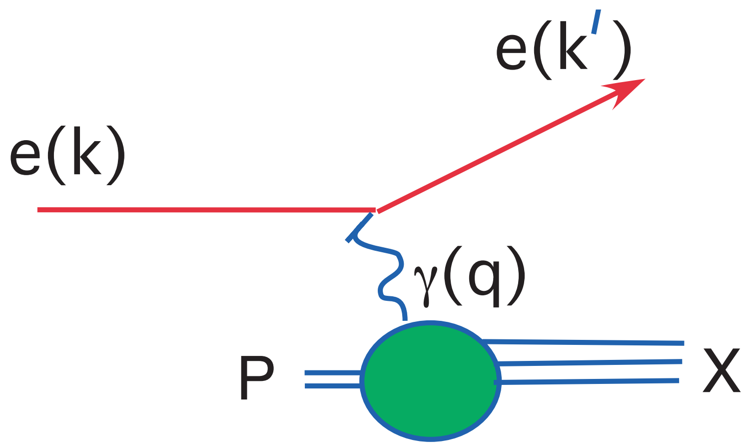
Start with a proton

$$\Phi^q = \frac{1}{2}\int \frac{d\xi^-}{2\pi}\,\frac{d^2\vec{\xi}_T}{(2\pi)^2}\,e^{ik\cdot\xi}\,\langle P;S|\,\bar{\psi}^q(0)\,\gamma^+\,\mathcal{W}_{TMD}\,\psi^q(\xi)\,|P;S\rangle\Big|_{\xi^+=0}$$

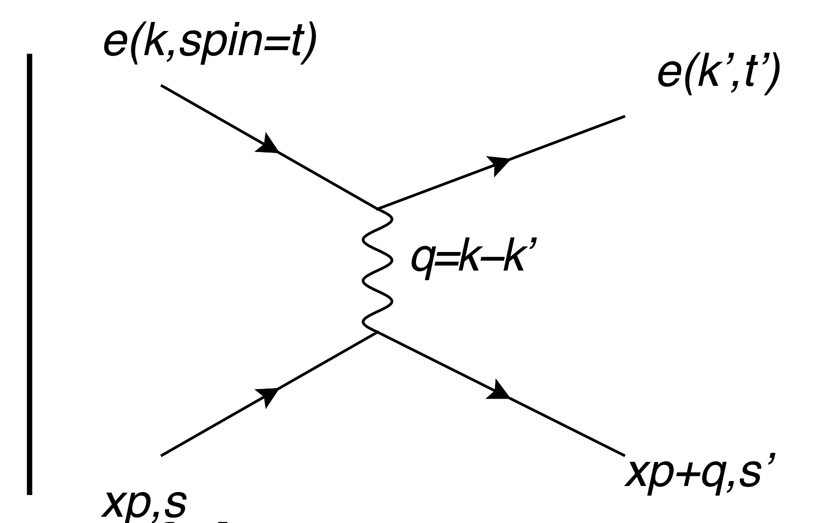
$$= f_1^q(x,\vec{k}_T^{\,2}) + \frac{(\vec{S}_T\times\vec{k}_T)\cdot\hat{P}}{M}\,f_{1T}^{\perp q}(x,\vec{k}_T^{\,2})$$

2. Electron-positron scattering to excited nucleons

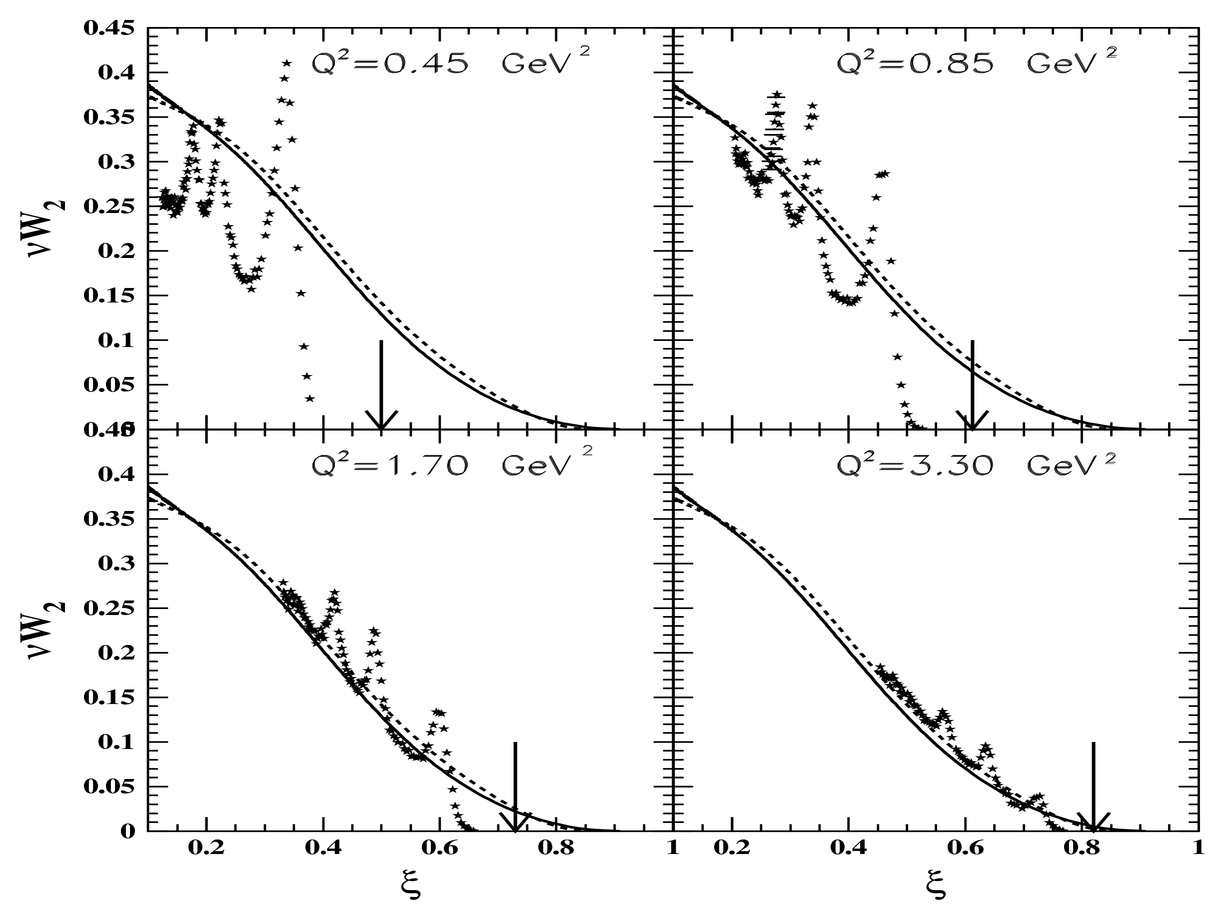
For intermediate momentum transfer compare



= F(x,spin)



To the production of heavier, unstable versions of the proton. Not just one, but all the quarks are scattered together, and yet the two probabilities are closely related:



Quark-hadron duality:

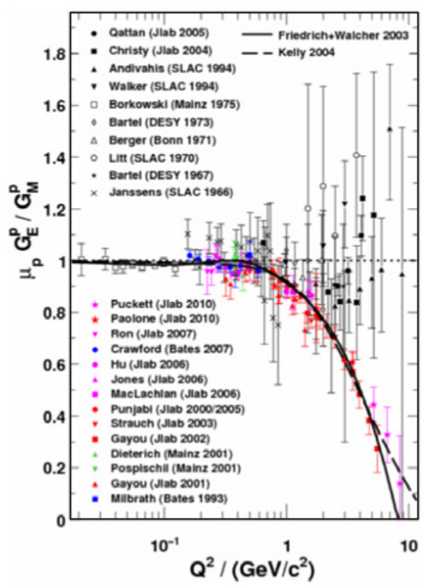
Melnitchouk, Keppel, Ent (2005)

3. Elastic Scattering and the Nucleon Radius

$$\frac{d\sigma}{d\Omega} = \left(\frac{d\sigma}{d\Omega}\right)_{\text{Mott}} \left(\frac{E'}{E}\right) \frac{1}{1+\tau} \left(G_E^{p\,2}(Q^2) + \frac{\tau}{\varepsilon} G_M^{p\,2}(Q^2)\right)$$

Still lots to do at large and small momentum transfer

E. Cisbani, 2014



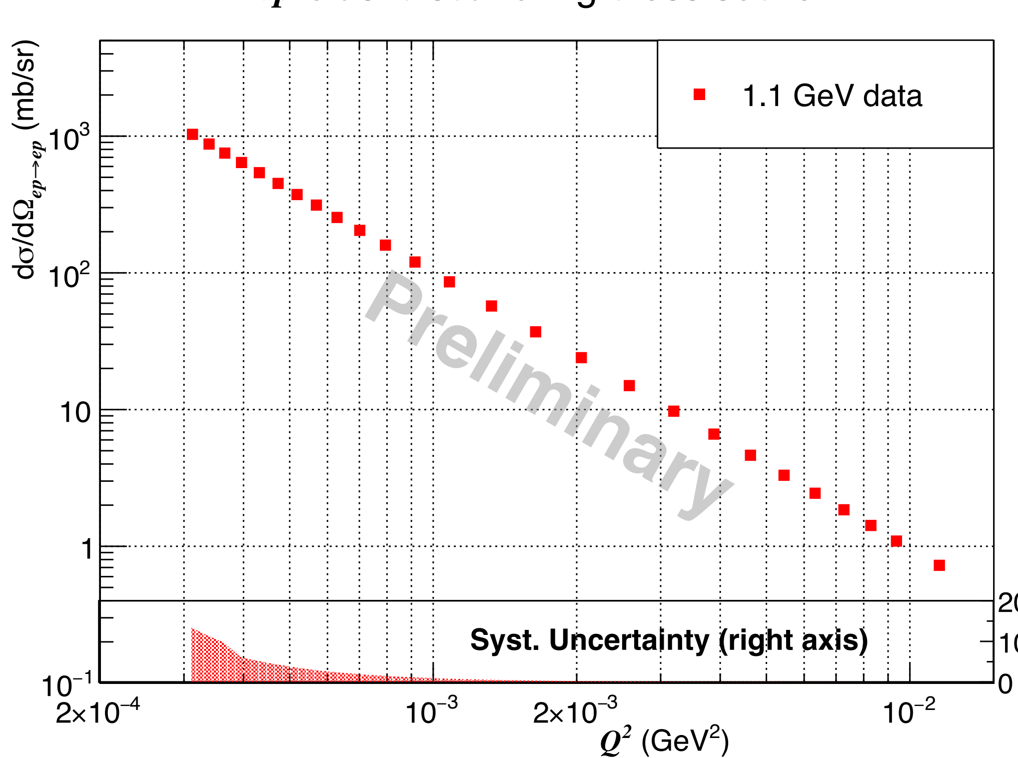
Special interest in low Q²: radius!

pRad:

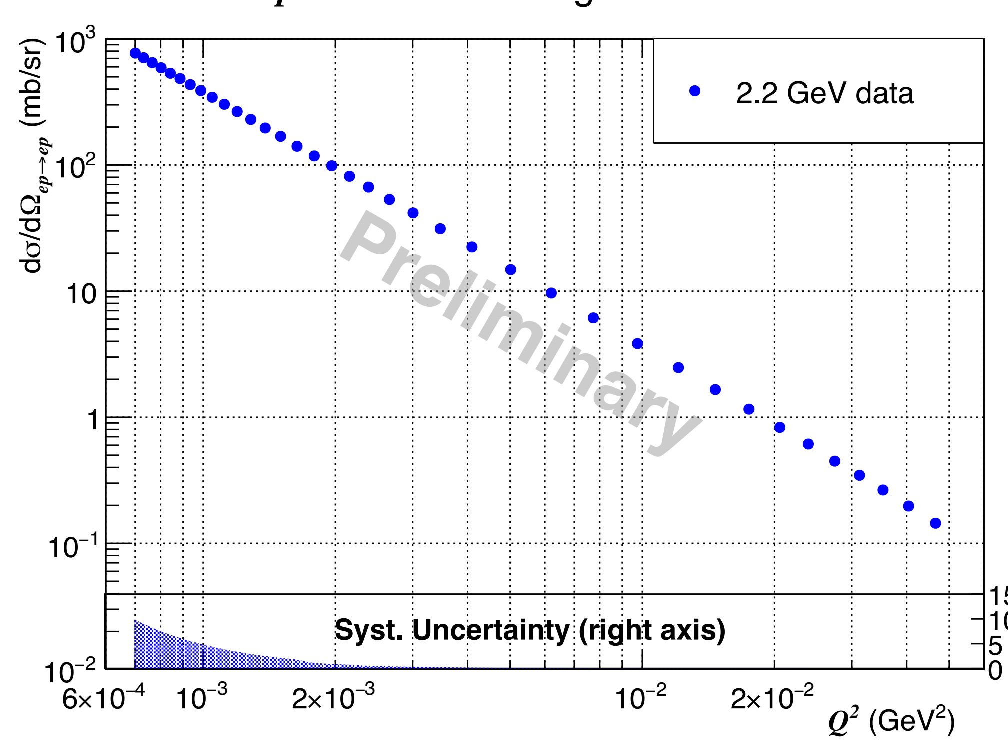
$$G_E^p(Q^2) = 1 - \frac{Q^2}{6}\langle r^2\rangle + \frac{Q^4}{120}\langle r^4\rangle + \ldots$$

T. Gasparian 2018 ECT

ep elastic scattering cross section



ep elastic scattering cross section

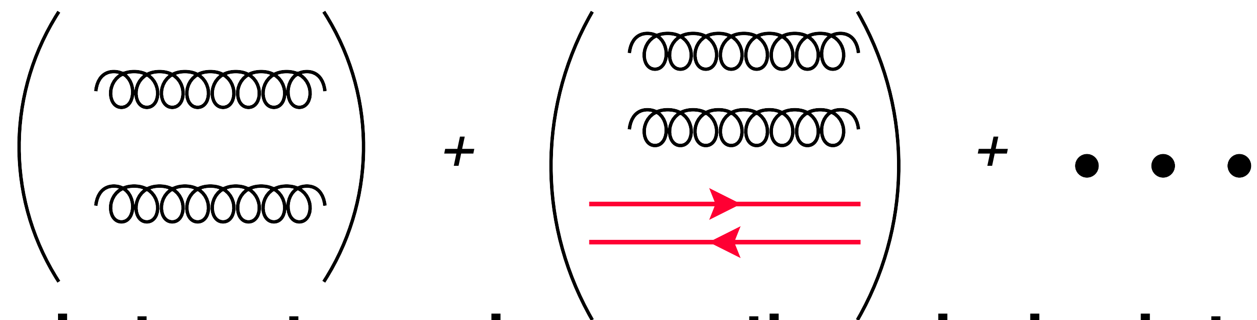


4. Exotic States

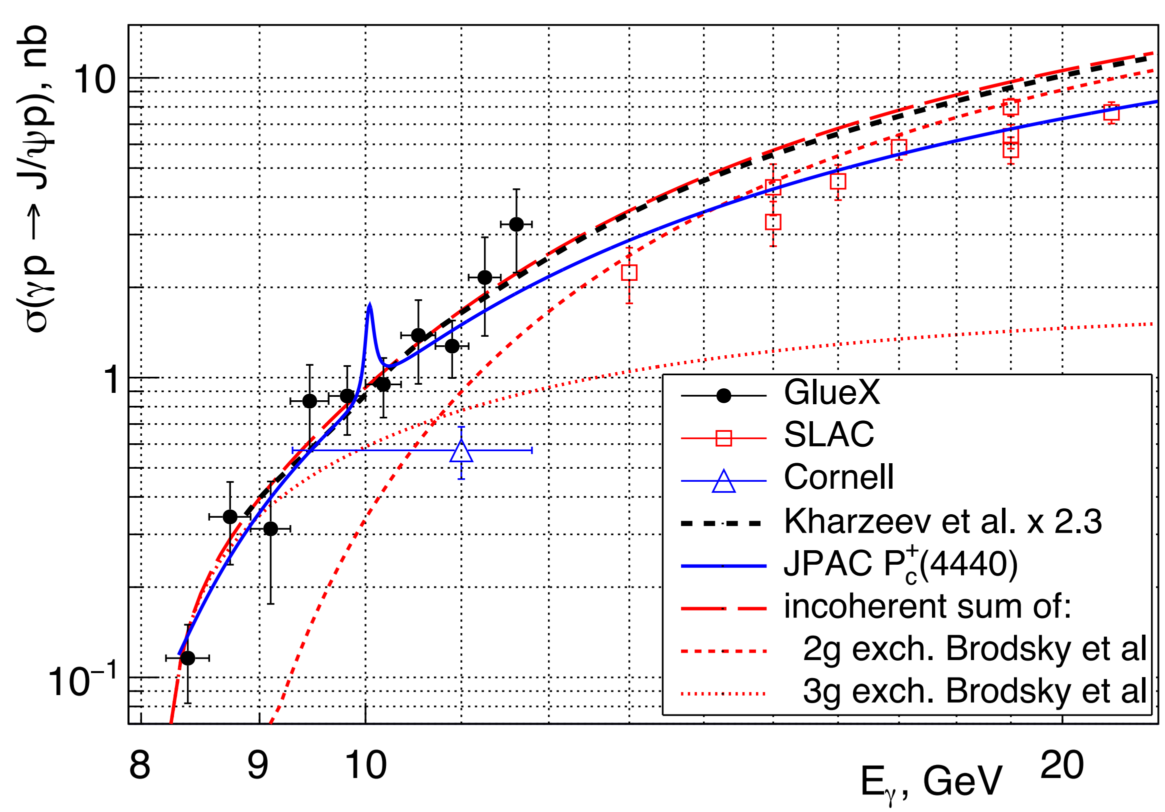
Photons evolve into quark pairs that can pick up gluons in the proton . . .

Computer simulations provide other possible QCD states not found in the classic quark model: glueballs, “multi-quarks”

| glue ball > =



GlueX: using “real” photons to produce exotic and mixed states.
Here, early results on J/Psi (ccbar):



GlueX May 2019
12 GeV

5. DVCS and Generalized Parton Distributions

**Single-quark distributions from DIS and SIDS tell a great story.
But there is much more. Two-photon processes, like**

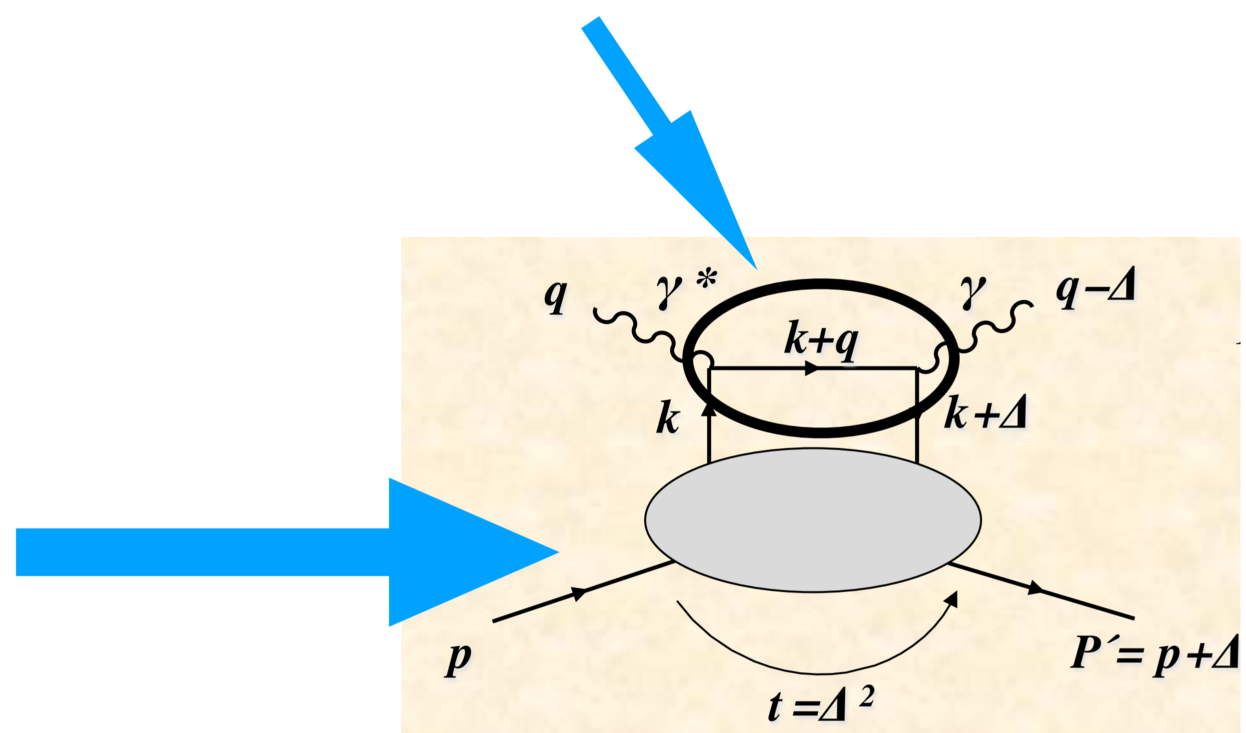
Deeply Virtual Compton Scattering (DVCS)

**reveal correlations between positions and momenta within the proton
within information on angular momenta and other extended structure:**

“tomography”.

**By making one photon
state very virtual
the process factorizes
into the story of the
proton and the story of
the scattering itself.**

**We can calculate the latter.
We measure the former.**

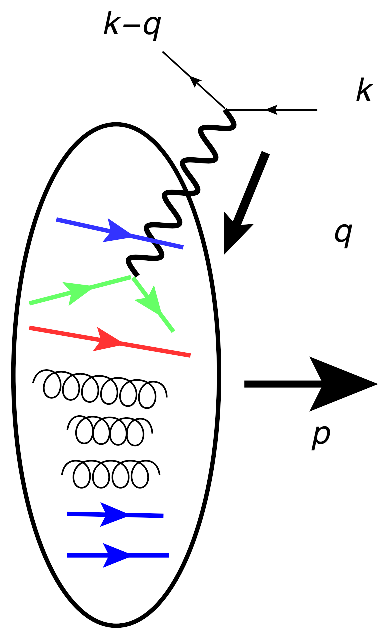


credit: S. Kumano

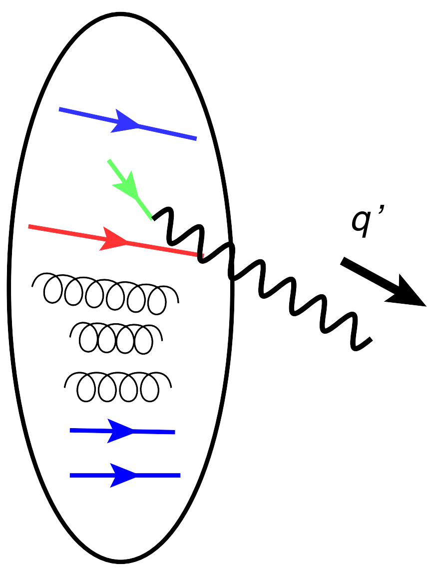
$\Delta = q - q'$

The proton stories are encoded in expressions like:

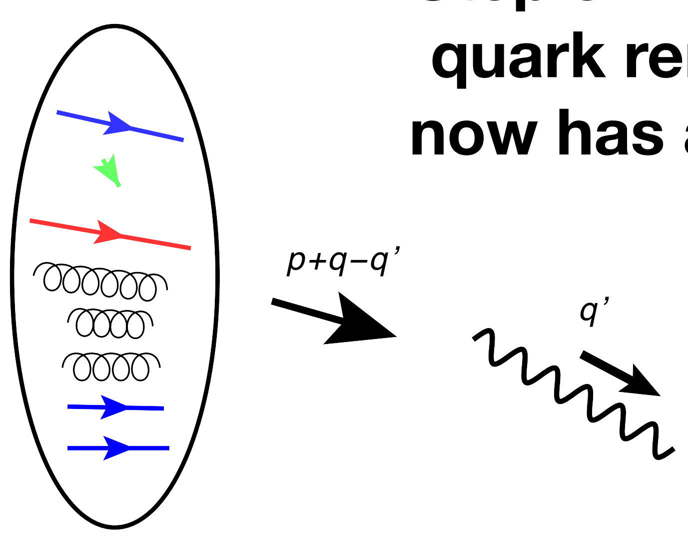
$$\boxed{\int \frac{dz^-}{4\pi} e^{ixP^+z^-} \langle p' | \bar{\psi}(-z/2)\gamma^+\psi(z/2) | p \rangle \Big|_{z^+=0,\vec{z}_\perp=0}}$$



Step 1: Electron exchanges virtual photon with a quark



Step 2: Quark travels some distance, then re-emits another photon



Step 3: The photon escapes, but the quark remains in the proton, which now has a different total momentum

In all this, varying spin the spin of the election and/or the proton gives information on the spin of the quark. These give a family of generalized parton distributions.

An unprecedented example: the pressure distribution (a “gravitational form factor”). At 6 GeV from CLAS, with 12 pending (in red):

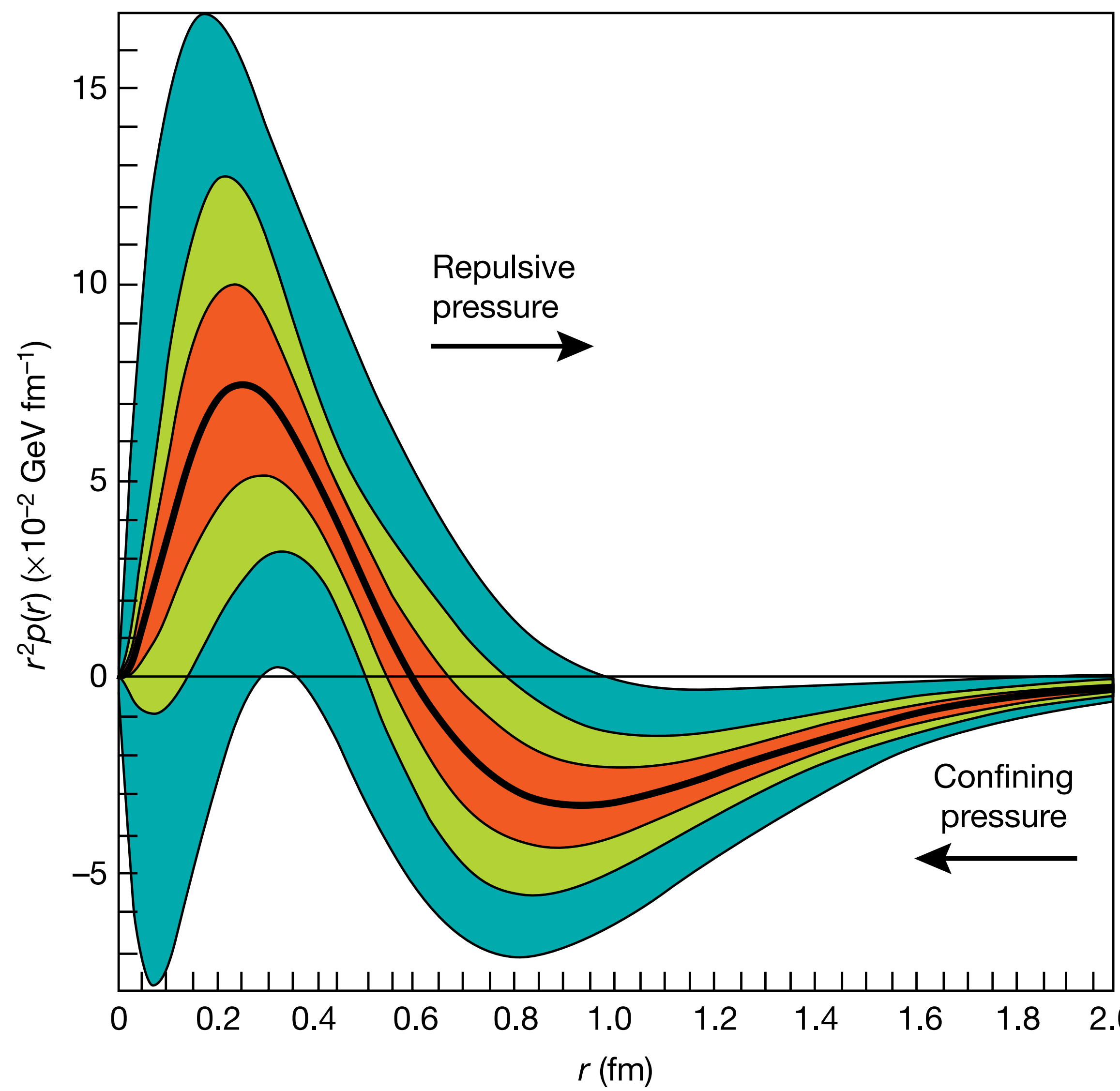


Fig. 1 | Radial pressure distribution in the proton.

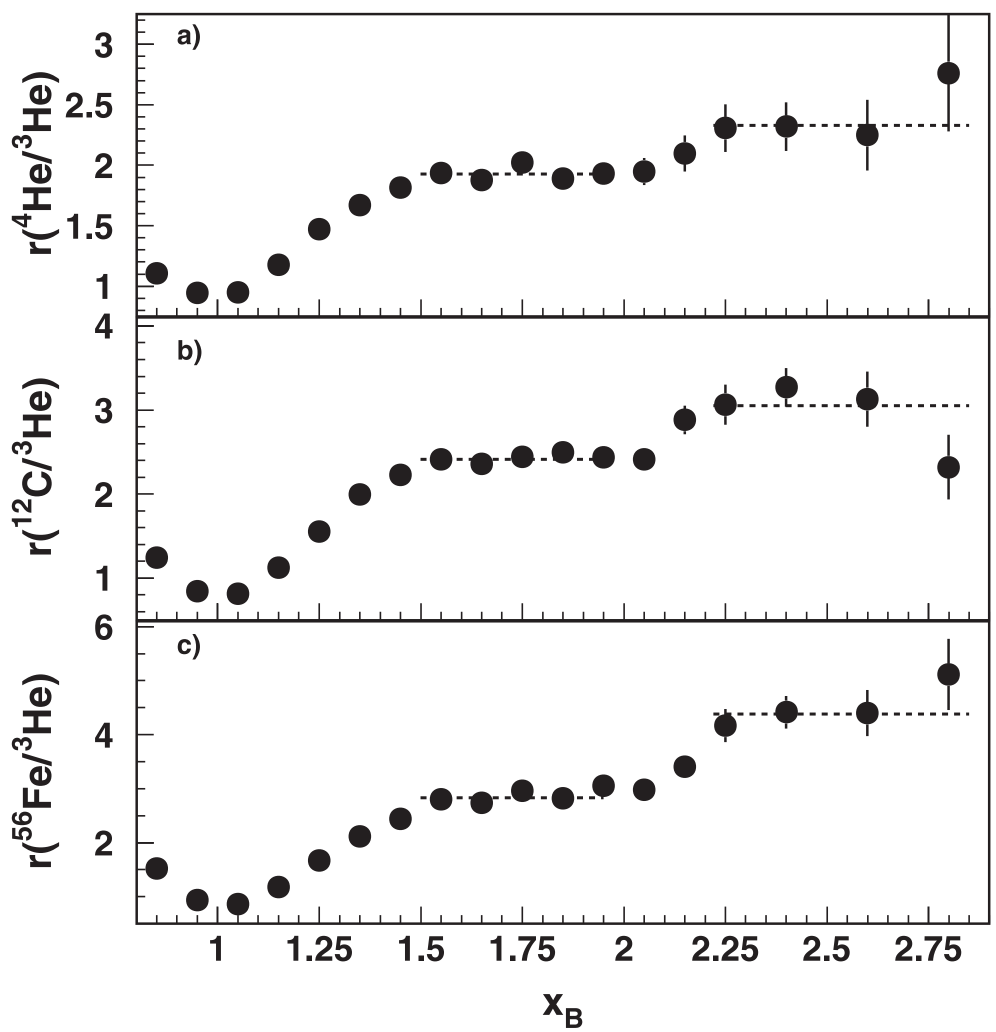
Nature, 2019

6. Nuclear Structure

)

"This close, but no closer." The stability of nuclei depends on repulsive forces at short distances. To understand them, detect pairs and triplets lurking right at the edge.

$$r(A, {}^3\mathrm{He}) = \frac{A(2\sigma_{ep} + \sigma_{en})}{3(Z\sigma_{ep} + N\sigma_{en})} \frac{3\mathcal{Y}(A)}{A\mathcal{Y}({}^3\mathrm{He})} R^A_{\mathrm{rad}},$$



Seeing two and three nucleons inside He, C and Fe scatter together.

From CLAS (PRL 2006): short-range correlations (6 GeV

Like so much else, the very structure of our world is implicit in what we find here. . .

Each of these areas and much more will be explored in the 12 GeV era at JLab.

And, I should add at the future Electron-Ion Collider.

It should be exciting

Good luck!