



Quarks at the extreme: nucleon structure at large x

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Outline

- How do we see quarks (with large momentum fractions x) in the nucleon, and why are they important?
- Extraction of neutron structure from inclusive data
 - nuclear effects & d/u ratio
- New global “CJ” (CTEQ–Jefferson Lab) analysis
 - first serious foray into high- x , low- Q^2 region
 - implications of PDF uncertainties for high-energy colliders
- Future experiments

Looking for ^{high momentum} quarks in the nucleon
is like looking for the Mafia in Sicily –

everybody *knows* they're there,
but it's hard to find the evidence!

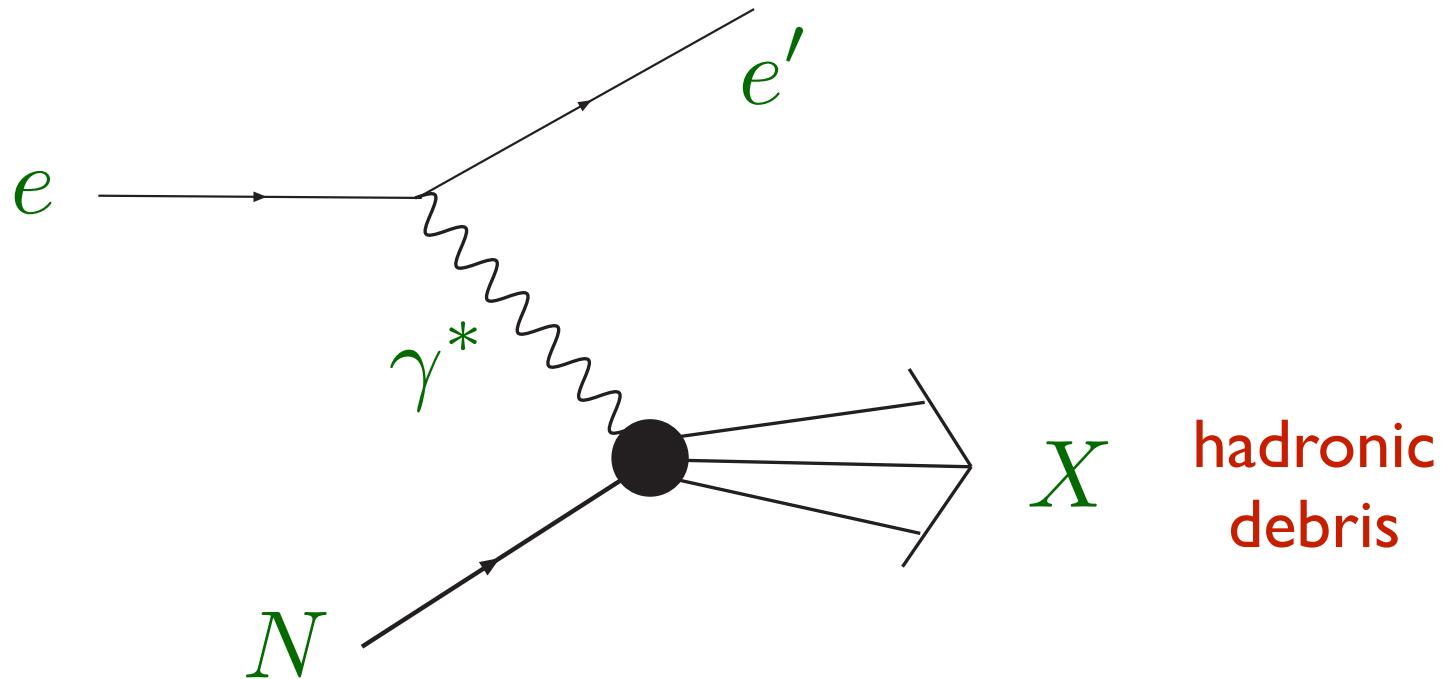
Anonymous



"QUARKS. NEUTRINOS. MESONS. ALL THOSE DAMN PARTICLES YOU CAN'T SEE. THAT'S WHAT DROVE ME TO DRINK. BUT NOW I CAN SEE THEM."

Electron scattering

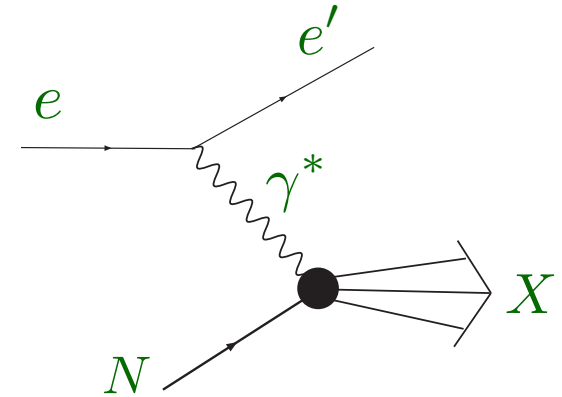
- Inclusive cross section for $e N \rightarrow e X$



→ one-photon exchange approximation

Electron scattering

■ Inclusive cross section for $e N \rightarrow e X$



$$\frac{d^2\sigma}{d\Omega dE'} = \frac{4\alpha^2 E'^2 \cos^2 \frac{\theta}{2}}{Q^4} \left(2 \tan^2 \frac{\theta}{2} \frac{F_1}{M} + \frac{F_2}{\nu} \right)$$

$$\left. \begin{aligned} \nu &= E - E' \\ Q^2 &= \vec{q}^2 - \nu^2 = 4EE' \sin^2 \frac{\theta}{2} \end{aligned} \right\} \boxed{x = \frac{Q^2}{2M\nu}} \quad \text{“Bjorken scaling variable”}$$

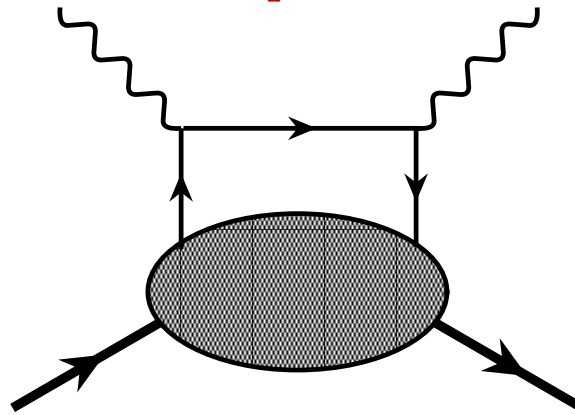
■ Structure functions F_1 , F_2

→ contain all information about structure of nucleon

■ Parton model

→ scatter from individual quarks (“*partons*”) in nucleon

$$F_2(x, Q^2) = x \sum_q e_q^2 q(x, Q^2) \quad (q=u, d, s \dots)$$



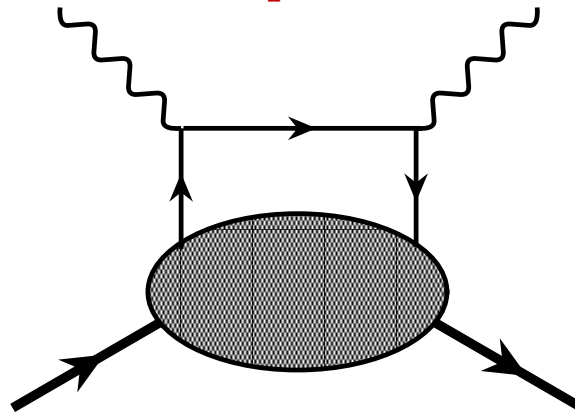
→ $q(x, Q^2)$ = probability to find quark type “ q ” in nucleon, carrying (light-cone) momentum fraction x

$$x = \frac{p_q^+}{p_N^+} = \frac{p_q^0 + p_q^z}{p_N^0 + p_N^z}$$

■ Parton model

→ scatter from individual quarks (“*partons*”) in nucleon

$$F_2(x, Q^2) = x \sum_q e_q^2 q(x, Q^2) \quad (q=u,d,s\dots)$$



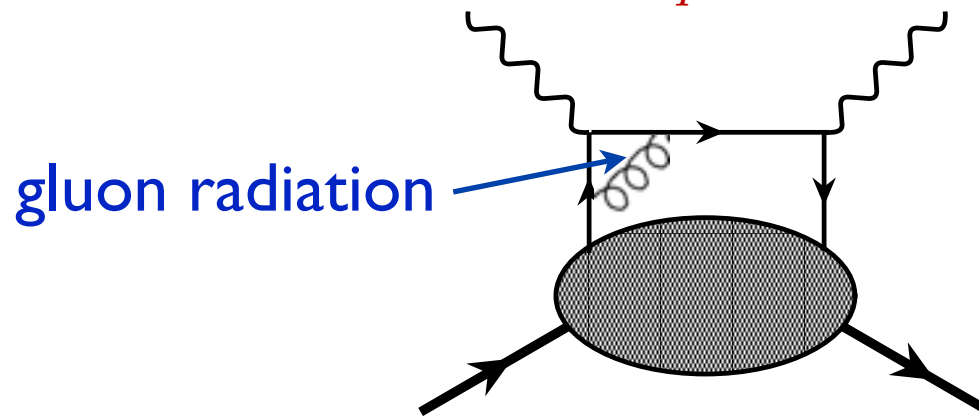
→ $q(x, Q^2)$ = probability to find quark type “ q ” in nucleon, carrying (light-cone) **momentum fraction x**

→ at large Q^2 , “Callan-Gross relation” $F_2 = 2x F_1$

■ Parton model

→ scatter from individual quarks (“*partons*”) in hadron

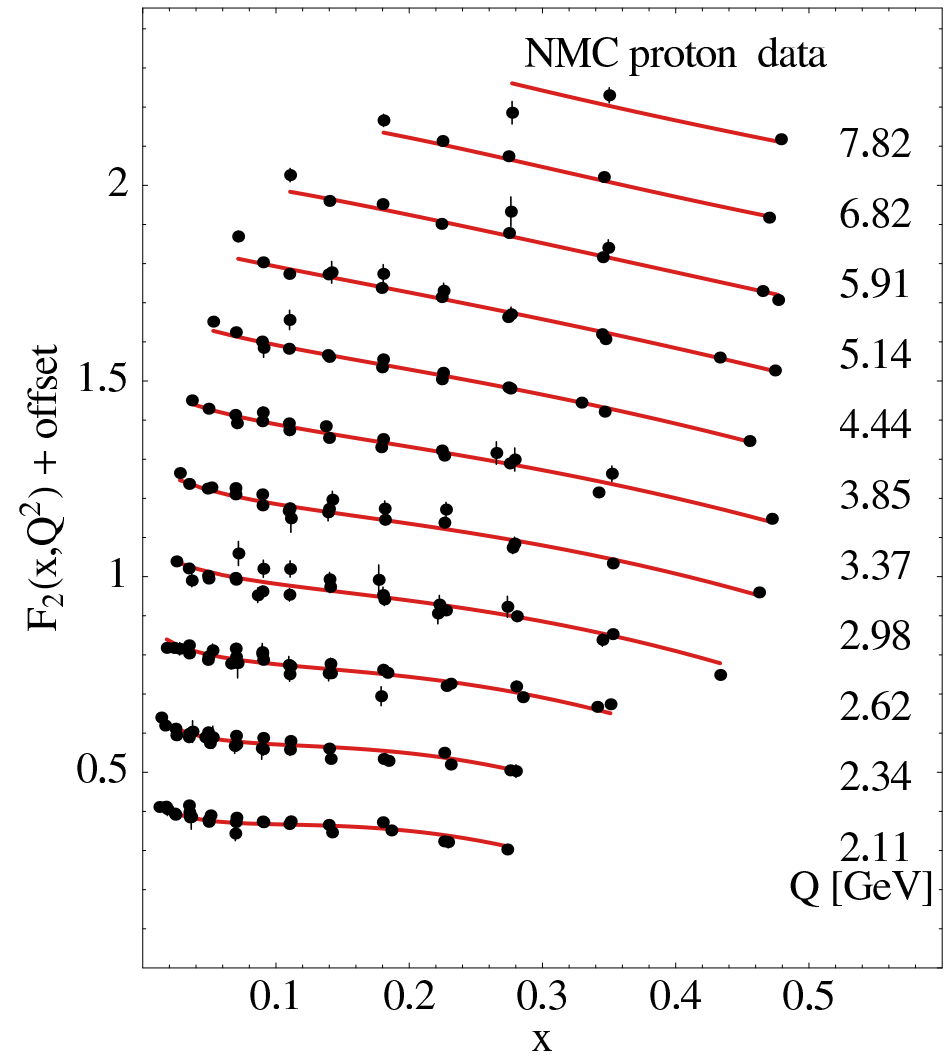
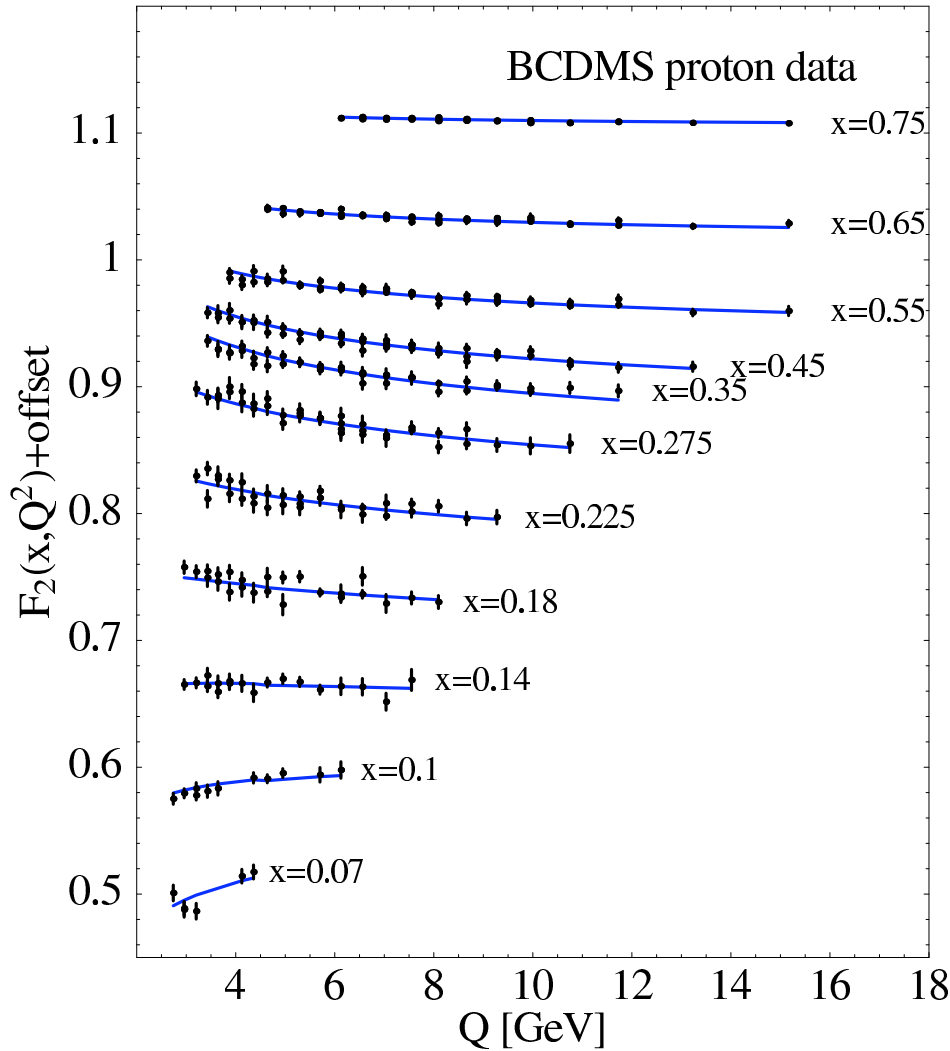
$$F_2(x, Q^2) = x \sum_q e_q^2 q(x, Q^2) \quad (q=u,d,s\dots)$$



→ at finite energy, Q^2 dependence given by
(perturbatively calculable) QCD evolution equations

$$F_2 \rightarrow F_2(x, \log Q^2)$$

Structure function data



Lai et al., Eur. Phys. J. C12 (2000) 375

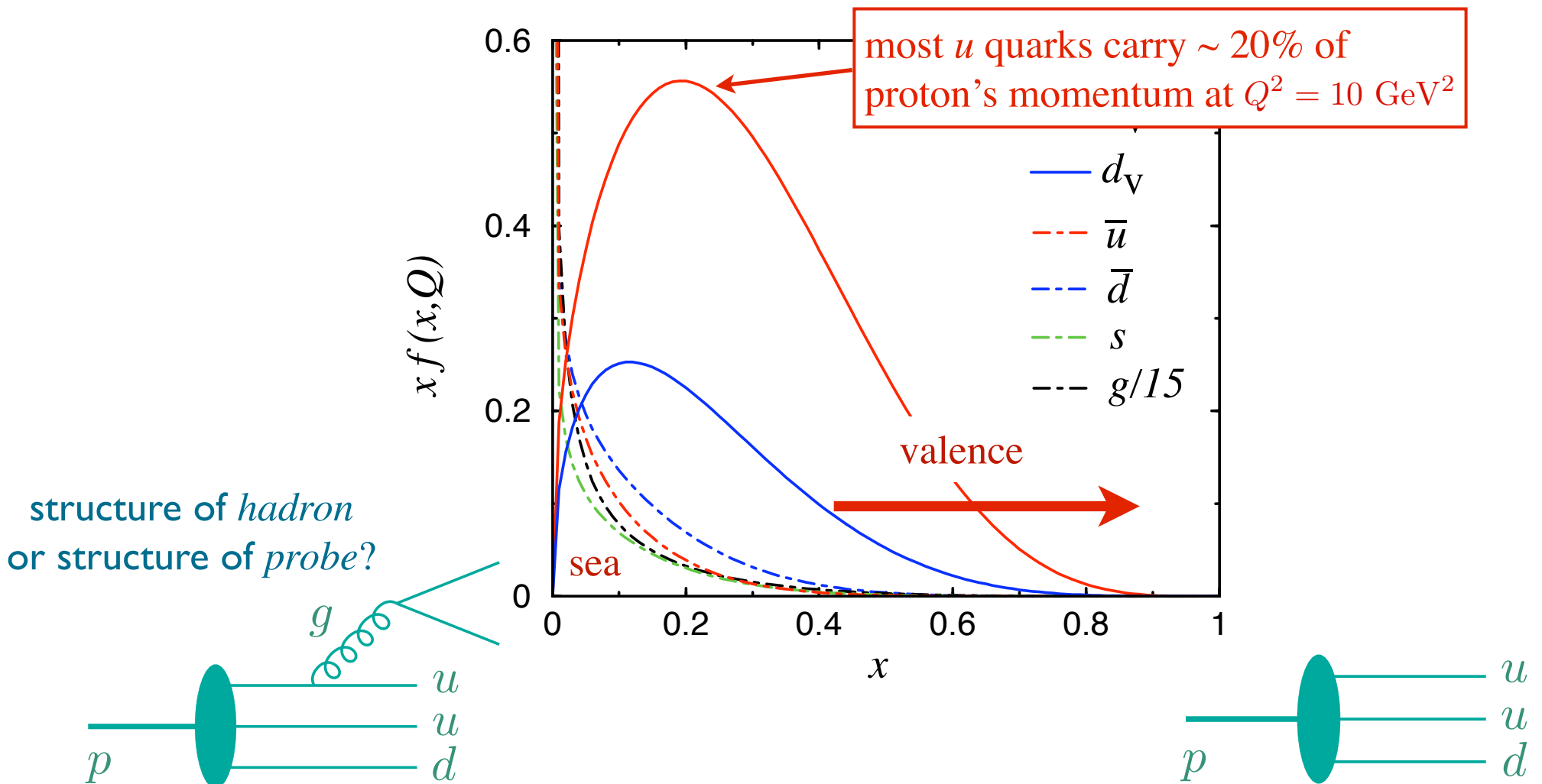
→ $\log Q^2$ dependence observed in data

Parton distribution functions (PDFs)

- PDFs extracted in global QCD analyses (CTEQ, MSTW, ...) of structure function data from e , μ & ν scattering (also from lepton-pair & W -boson production in hadronic collisions)
→ determined over large range of x and Q^2
- Provide basic information on structure of QCD bound states
- Needed to understand backgrounds in searches for physics *beyond the Standard Model* in high-energy colliders *e.g.* the LHC
→ Q^2 evolution feeds low x , high Q^2 from high x , low Q^2

Why are PDFs at large x interesting?

- Most direct connection between quark distributions and models of nucleon structure is via *valence* quarks
 - most cleanly revealed at $x > 0.4$



Valence quarks

- At large x , valence u and d distributions extracted from p and n structure functions

$$F_2^p \approx \frac{4}{9}u_v + \frac{1}{9}d_v$$

$$F_2^n \approx \frac{4}{9}d_v + \frac{1}{9}u_v$$

- u quark distribution well determined from *proton* data
- d quark distribution requires *neutron* structure function

$$\longrightarrow \frac{d}{u} \approx \frac{4 - F_2^n / F_2^p}{4F_2^n / F_2^p - 1}$$

Valence quarks

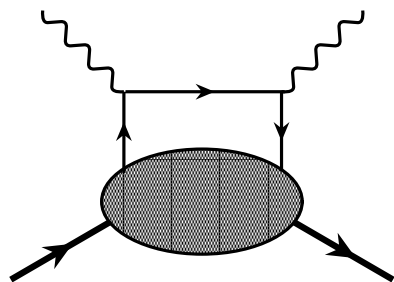
- Ratio of d to u quark distributions particularly sensitive to quark dynamics in nucleon
- SU(6) spin-flavor symmetry

proton wave function

$$p^\uparrow = -\frac{1}{3}d^\uparrow(uu)_1 - \frac{\sqrt{2}}{3}d^\downarrow(uu)_1$$

$$+ \frac{\sqrt{2}}{6}u^\uparrow(ud)_1 - \frac{1}{3}u^\downarrow(ud)_1 + \frac{1}{\sqrt{2}}u^\uparrow(ud)_0$$

50%	$S=0$	(qq)
50%	$S=1$	(qq)



interacting
quark

spectator
diquark

diquark spin

Valence quarks

- Ratio of d to u quark distributions particularly sensitive to quark dynamics in nucleon
- SU(6) spin-flavor symmetry

proton wave function

$$p^\uparrow = -\frac{1}{3}d^\uparrow(uu)_1 - \frac{\sqrt{2}}{3}d^\downarrow(uu)_1 \\ + \frac{\sqrt{2}}{6}u^\uparrow(ud)_1 - \frac{1}{3}u^\downarrow(ud)_1 + \frac{1}{\sqrt{2}}u^\uparrow(ud)_0$$

50%	$S=0$	(qq)
50%	$S=1$	(qq)

$$\rightarrow u(x) = 2 d(x) \text{ for all } x$$

$$\rightarrow \frac{F_2^n}{F_2^p} = \frac{2}{3}$$

Valence quarks

- But SU(6) symmetry is *broken*

e.g. scalar diquark dominance

$M_{\Delta} > M_N \implies (qq)_1$ has larger energy than $(qq)_0$

\implies *scalar diquark* dominant in $x \rightarrow 1$ limit

since only u quarks couple to *scalar* diquarks

$$\longrightarrow \frac{d}{u} \rightarrow 0$$

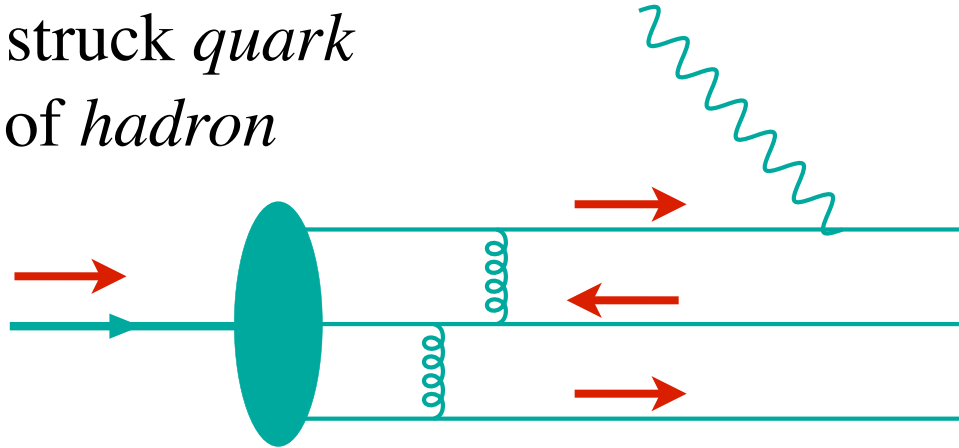
$$\longrightarrow \frac{F_2^n}{F_2^p} \rightarrow \frac{1}{4}$$

Feynman 1972, Close 1973, Close/Thomas 1988

Valence quarks

- Alternatively, SU(6) can be broken by hard gluon exchange

helicity of struck *quark*
= helicity of *hadron*



$$q^{\uparrow} \gg q^{\downarrow}$$

\Rightarrow *helicity-zero diquark* dominant in $x \rightarrow 1$ limit

$$\rightarrow \frac{d}{u} \rightarrow \frac{1}{5}$$

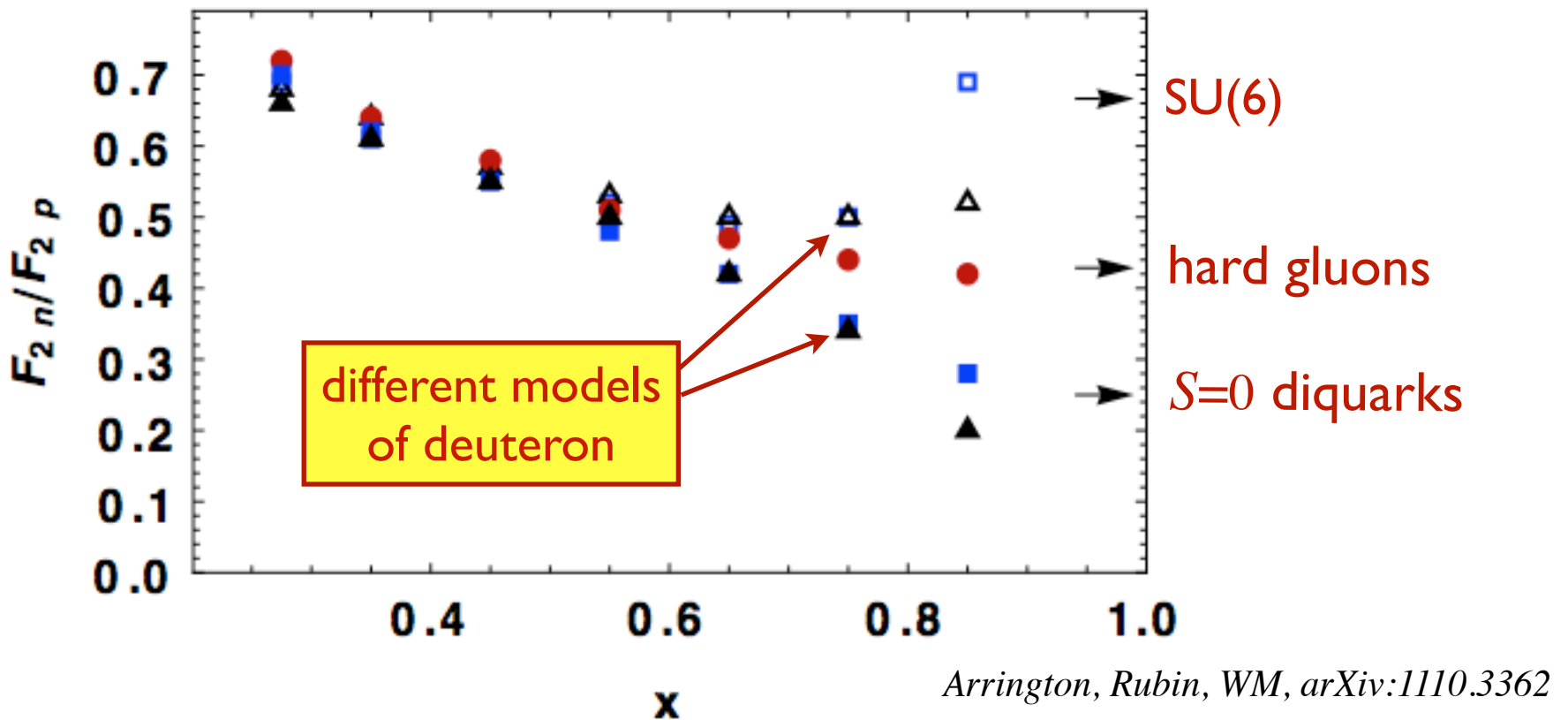
$$\rightarrow \frac{F_2^n}{F_2^p} \rightarrow \frac{3}{7}$$

Farrar, Jackson 1975

Deuteron corrections

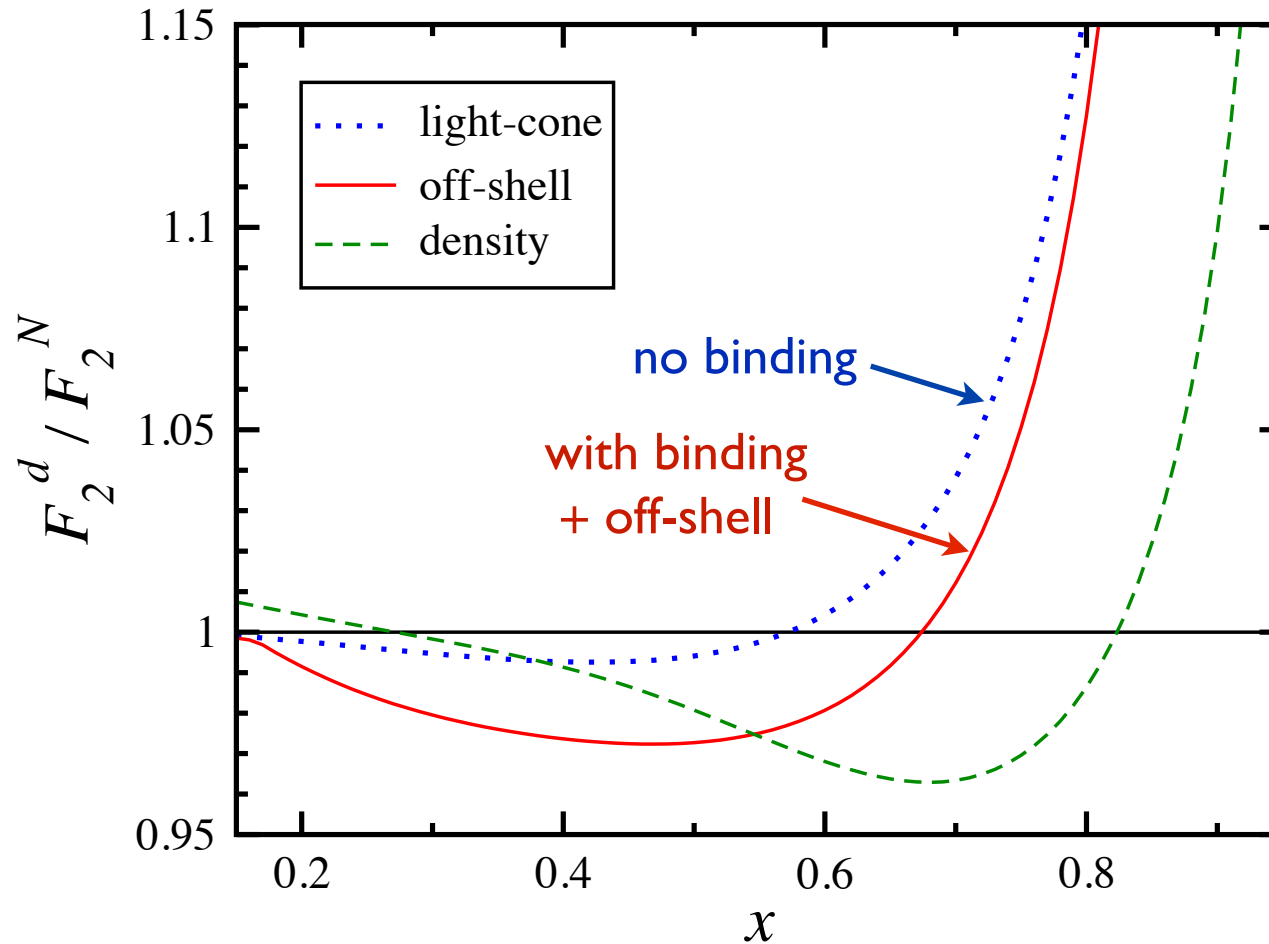
■ Absence of free neutron targets

→ use *deuterons* (weakly bound state of p and n)



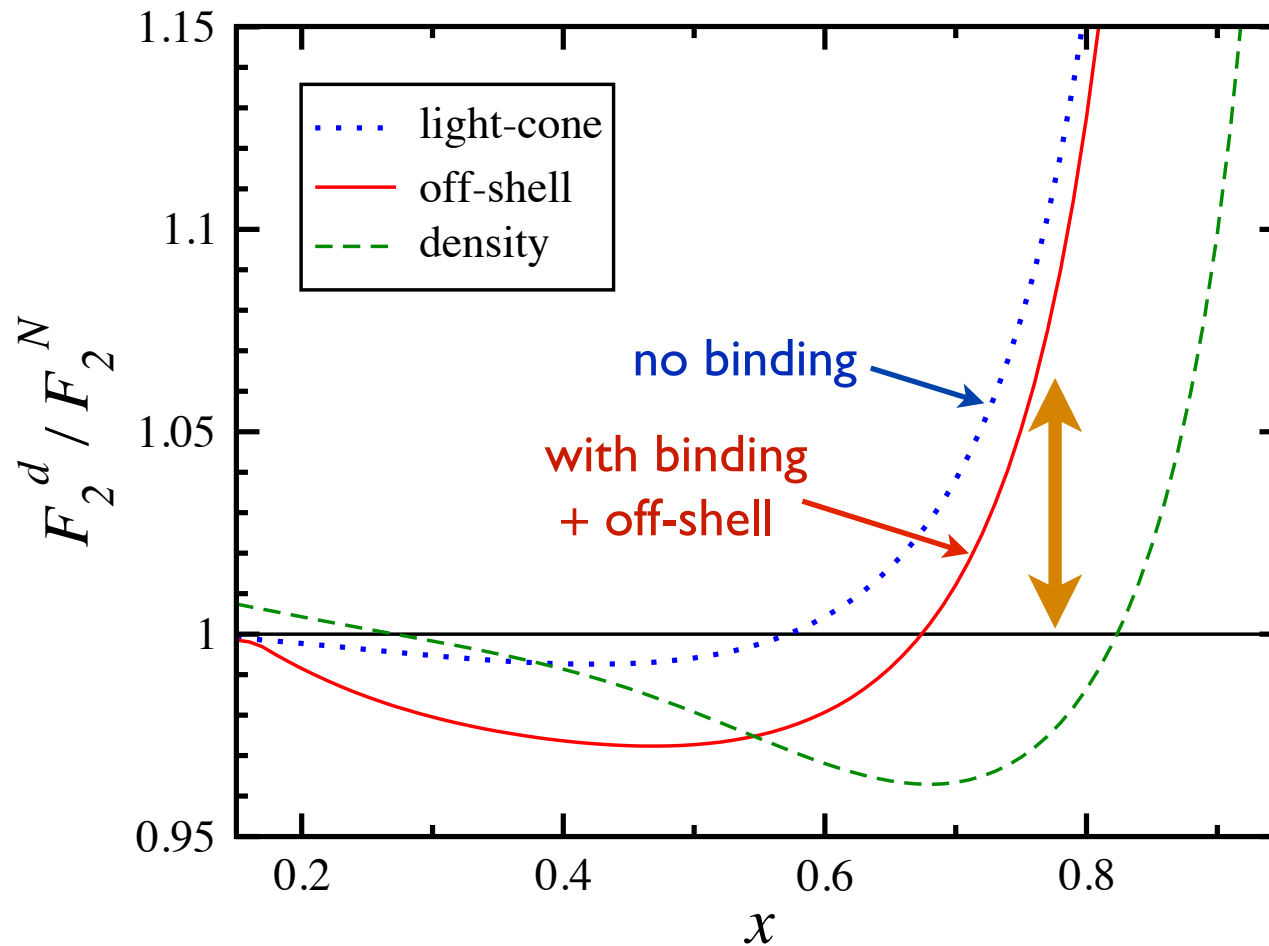
→ deuteron model dependence obscures free neutron structure information at large x

Deuteron corrections



- $\sim 2\text{--}3\%$ reduction of F_2^d / F_2^N at $x \sim 0.5\text{--}0.6$ with steep rise for $x > 0.6\text{--}0.7$
- larger EMC effect at $x \sim 0.5\text{--}0.6$ with binding + off-shell corrections *cf.* light-cone

Deuteron corrections



- using off-shell model, will get *larger* neutron *cf. light-cone* model
- but will get *smaller* neutron *cf. no nuclear effects* or *density* model

New global PDF analysis: CTEQ-JLab collaboration

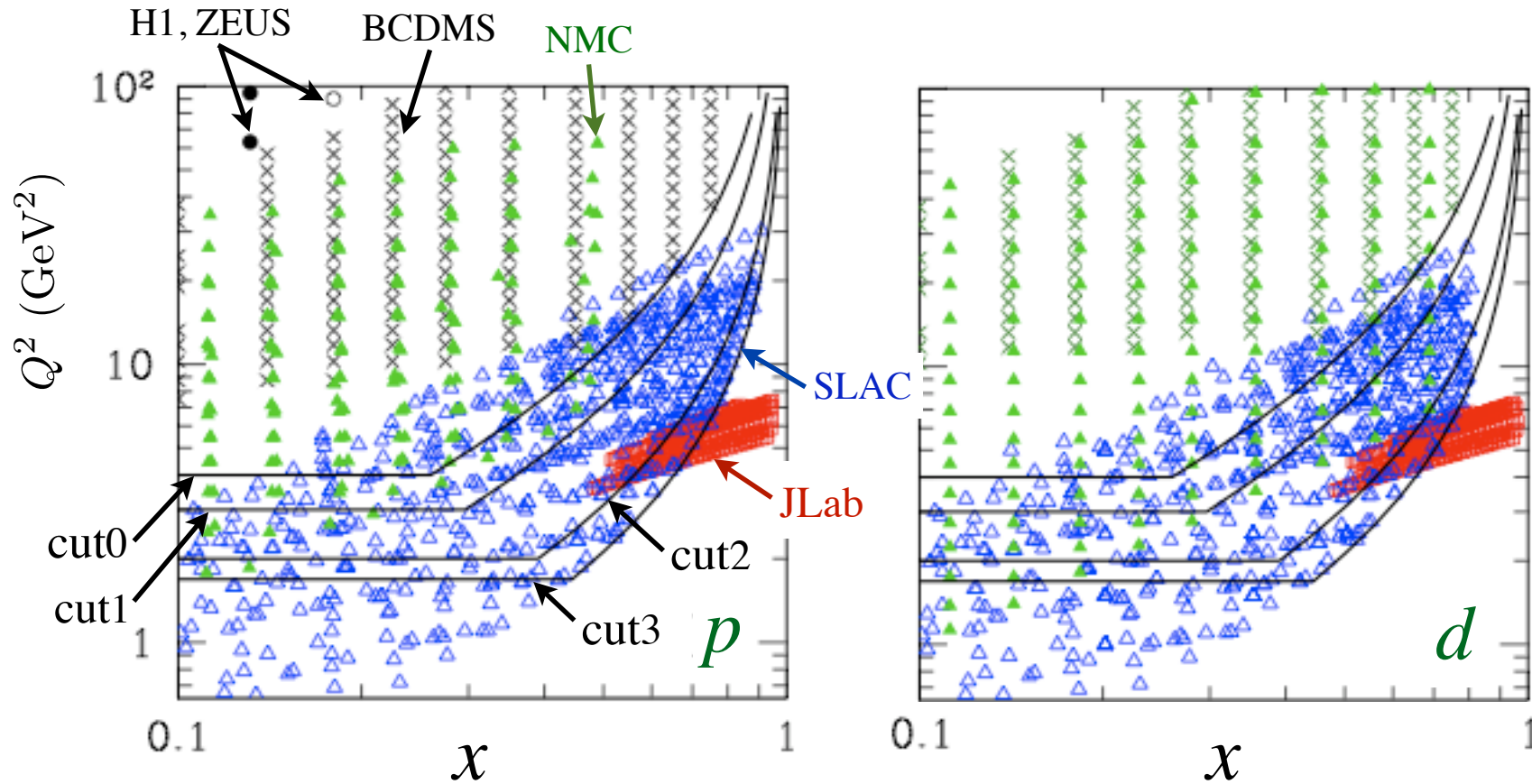
A. Accardi, E. Christy, C. Keppel,
W. Melnitchouk, P. Monaghan, J. Owens, L. Zhu

Accardi et al., Phys. Rev. D 81, 034016 (2010) “CJ10”

Accardi et al., Phys. Rev. D 84, 014008 (2011) “CJ11”

- Next-to-leading order (NLO) analysis of expanded set of *proton* and *deuterium* data, including large- x , low- Q^2 region
 - also include new CDF & D0 W -asymmetry, and E866 DY data
- Systematically study effects of Q^2 & W cuts
 - as low as $Q \sim m_c$ and $W \sim 1.7$ GeV
- Include subleading $1/Q^2$ corrections
 - target mass corrections & dynamical higher twists
- Correct for *nuclear* effects in the deuteron (binding + off-shell)
 - most global analyses assume *free* nucleons; some use density model, a few assume Fermi motion only

Kinematic cuts



cut0: $Q^2 > 4 \text{ GeV}^2$, $W^2 > 12.25 \text{ GeV}^2$

cut1: $Q^2 > 3 \text{ GeV}^2$, $W^2 > 8 \text{ GeV}^2$

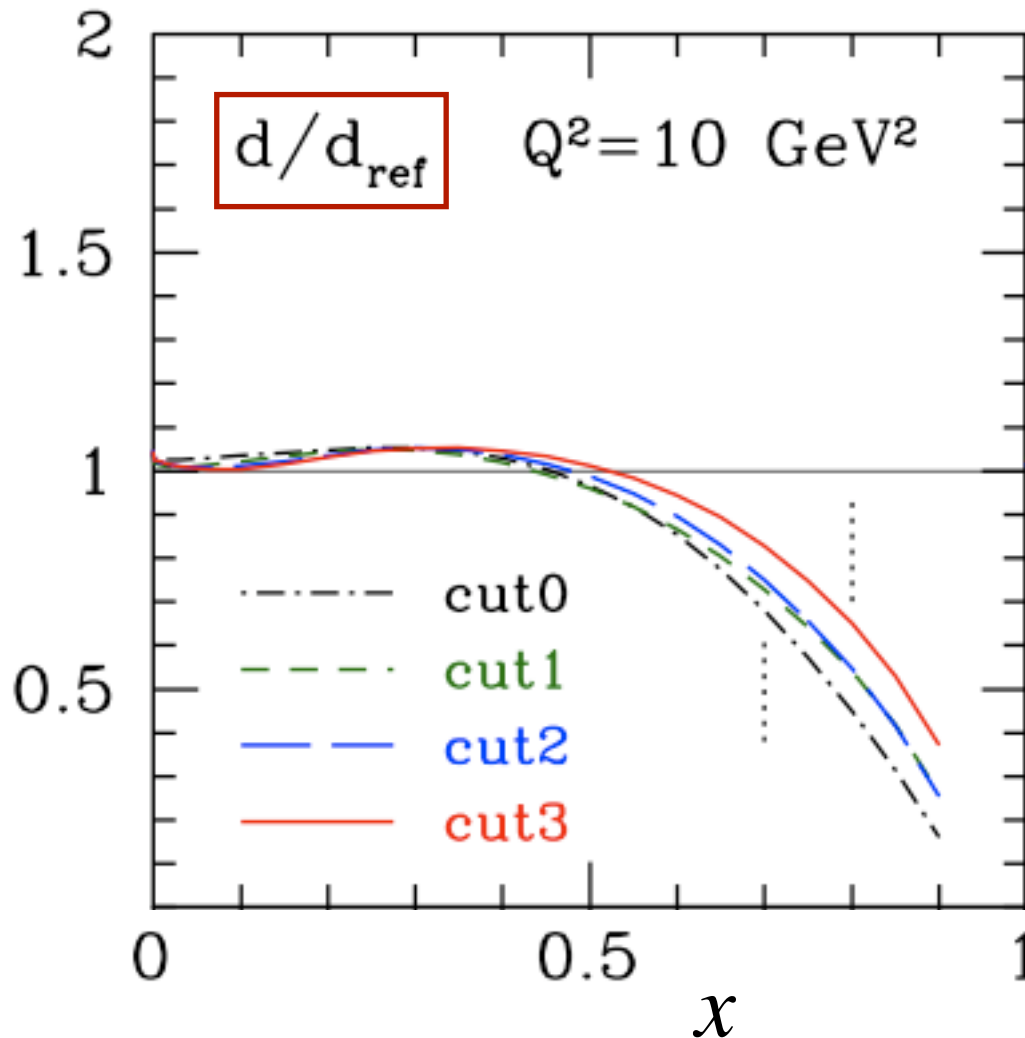
cut2: $Q^2 > 2 \text{ GeV}^2$, $W^2 > 4 \text{ GeV}^2$

cut3: $Q^2 > m_c^2$, $W^2 > 3 \text{ GeV}^2$

factor 2 increase
in DIS data from
cut0 \rightarrow cut3

Effect of Q^2 & W cuts

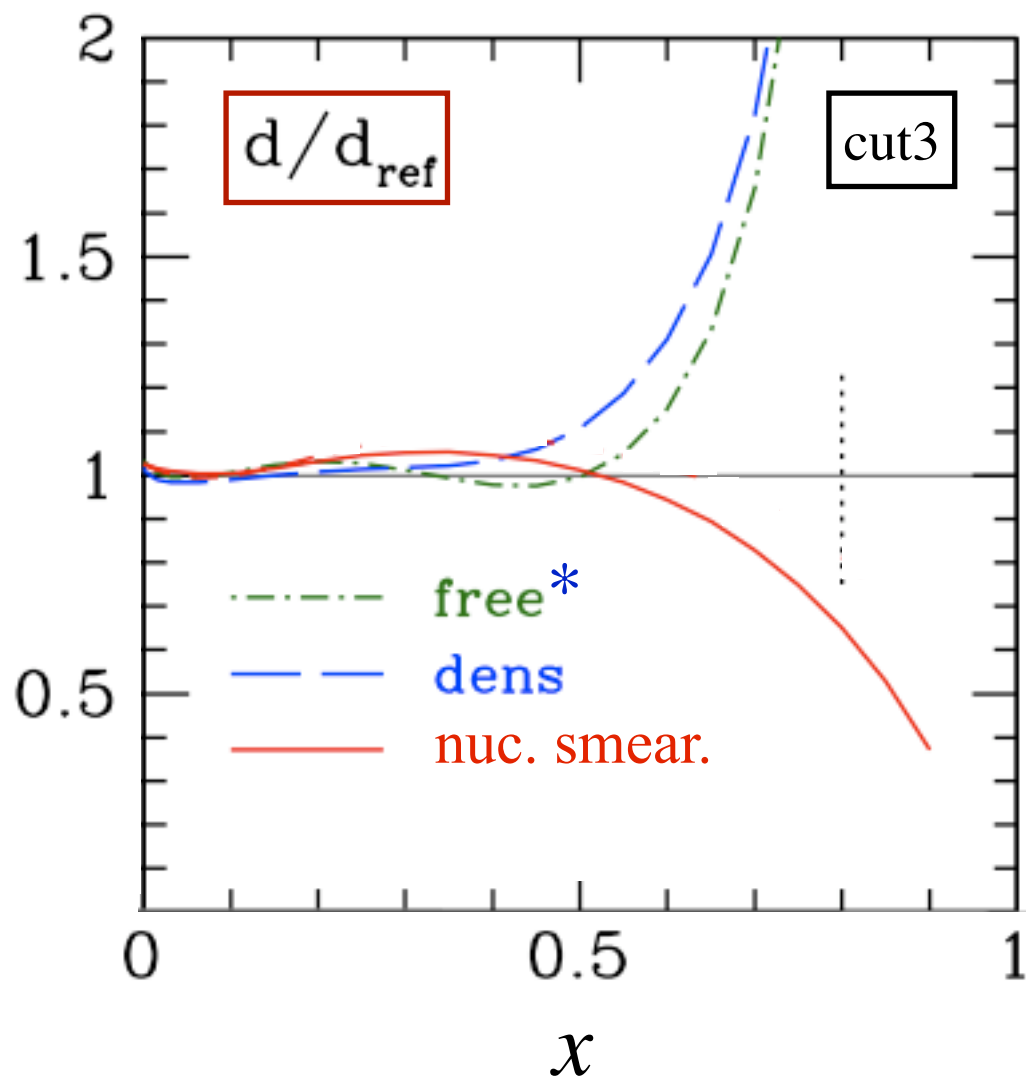
- Systematically reduce Q^2 and W cuts
- Fit includes TMCs, HT term, nuclear corrections



→ *stable* with respect to cut reduction

→ *d* quark suppressed by $\sim 50\%$ for $x > 0.5$ (driven by nuclear corrections)

Nuclear corrections



* assumes $F_2^d = F_2^p + F_2^n$ as in CTEQ6.1 and most other global fits

→ increased d quark for
no nuclear effects
(compensates for nuclear smearing
in deuteron → increased F_2^d)

→ decreased d quark for
nuclear smearing models

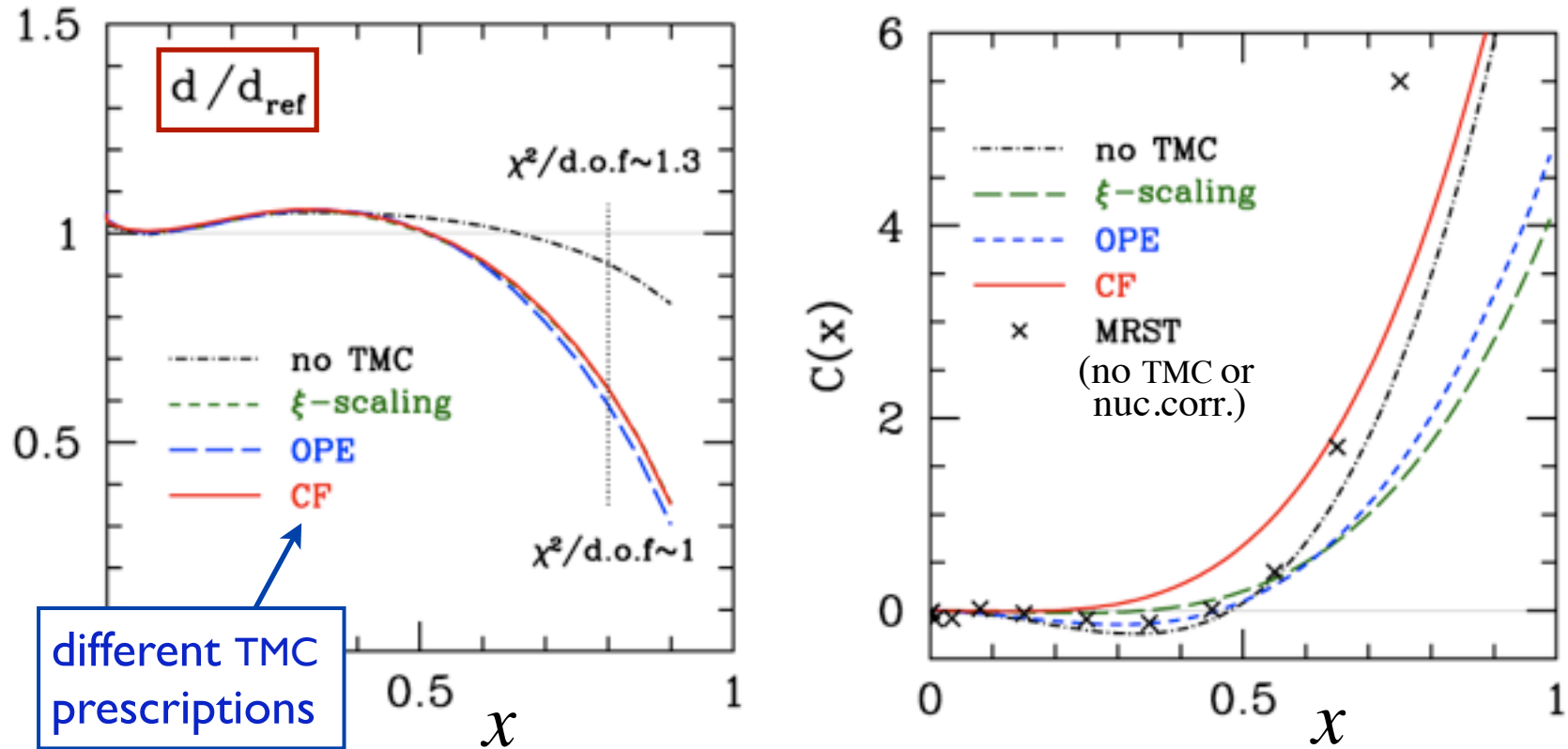


$F_2^d / F_2^N > 1$ for $x \sim 0.6-0.8$
while $F_2^d / F_2^N < 1$ for “free”
and “density” models

$$F_2^d / F_2^N \uparrow \longleftrightarrow F_2^n / F_2^p \downarrow$$

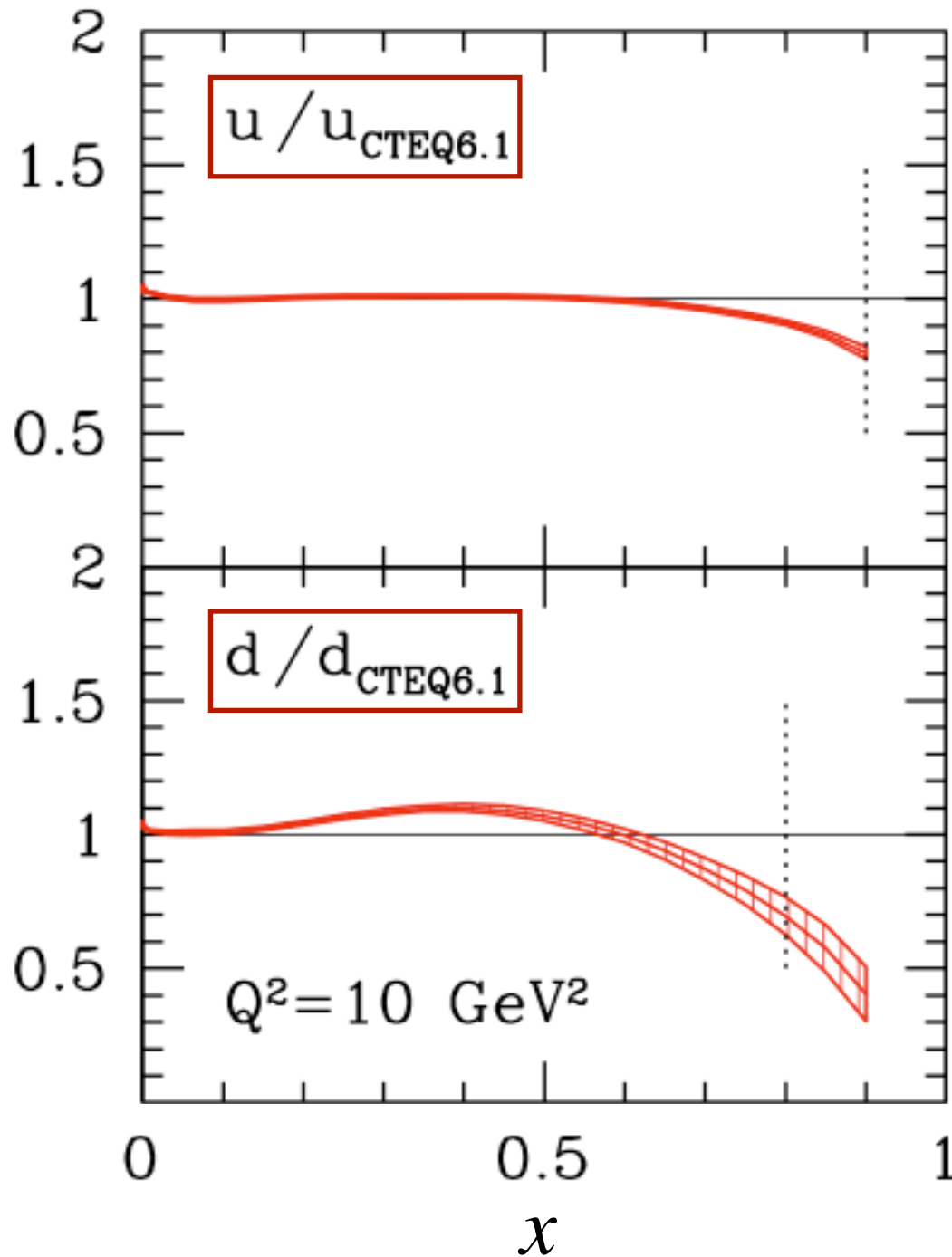
$$\longleftrightarrow d/u \downarrow$$

Effect of $1/Q^2$ corrections



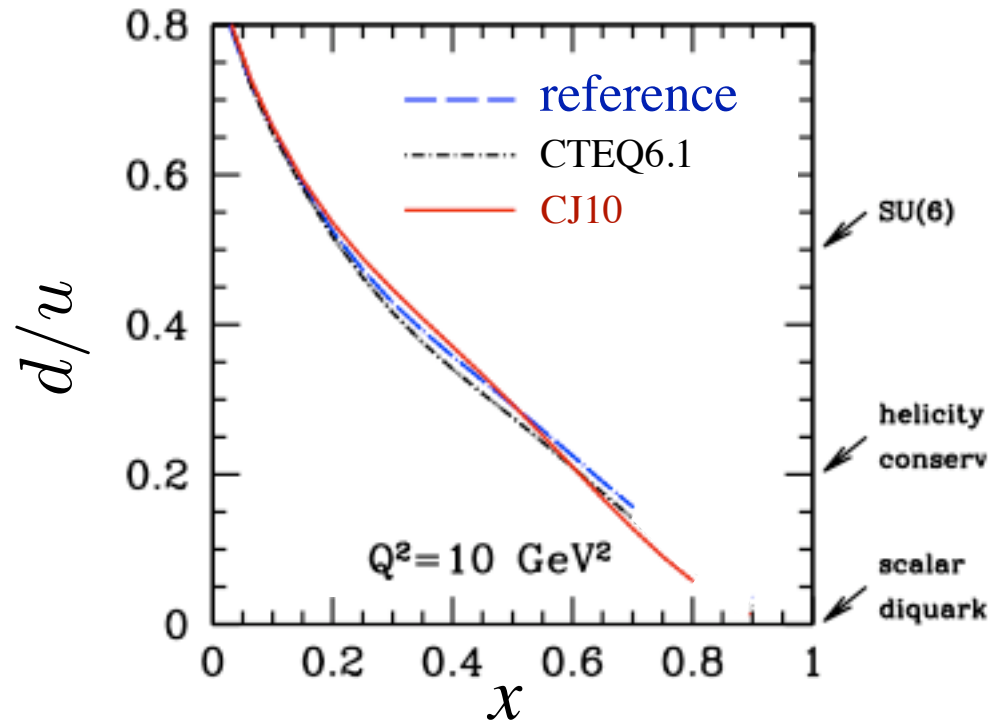
- $1/Q^2$ correction $F_2 = F_2^{\text{LT}} \left(1 + \frac{C(x)}{Q^2} \right)$, $C(x) = c_1 x^{c_2} (1 + c_3 x)$
- important interplay between TMCs and higher twist:
HT alone *cannot* accommodate full Q^2 dependence
- stable leading twist when both TMCs and HTs included

CJ10 PDF results



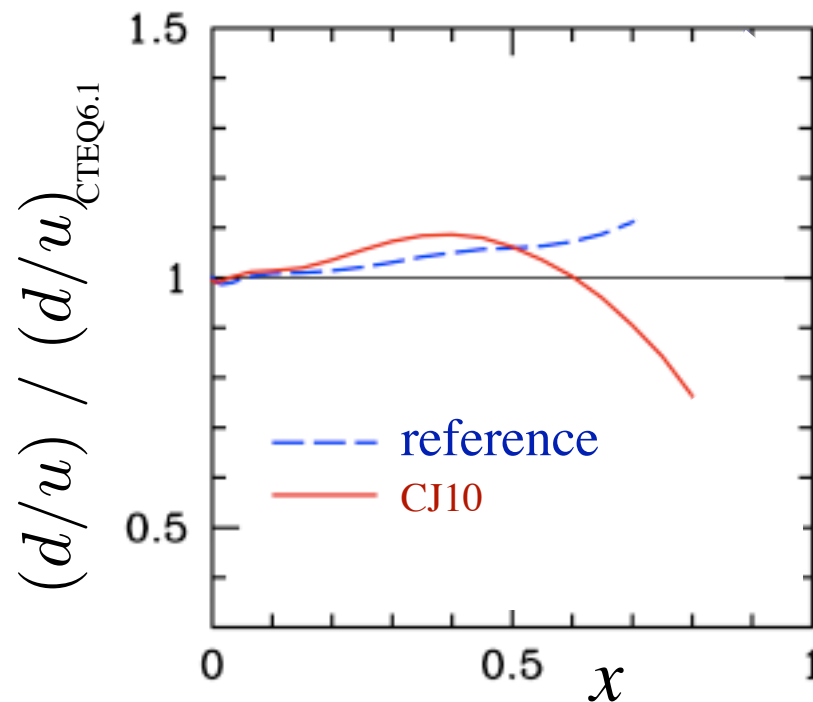
→ full fits favors
smaller d/u ratio

CJ10 PDF results

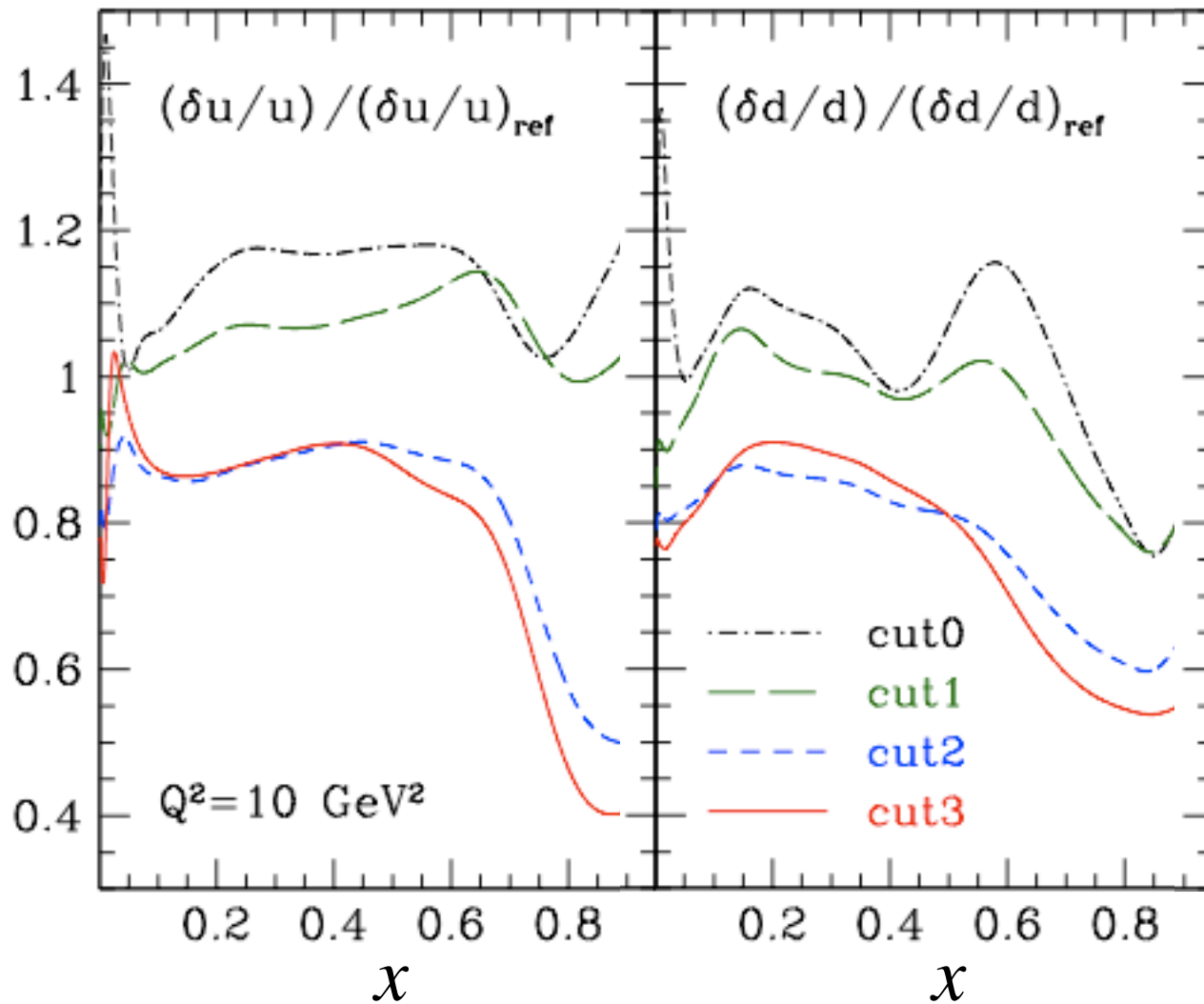


→ full fits favors smaller d/u ratio

→ dominance of non-pQCD physics (*cf.* hard g exchange)



CJ10 PDF results



→ full fits favors smaller d/u ratio

→ dominance of non-pQCD physics (*cf.* hard g exchange)

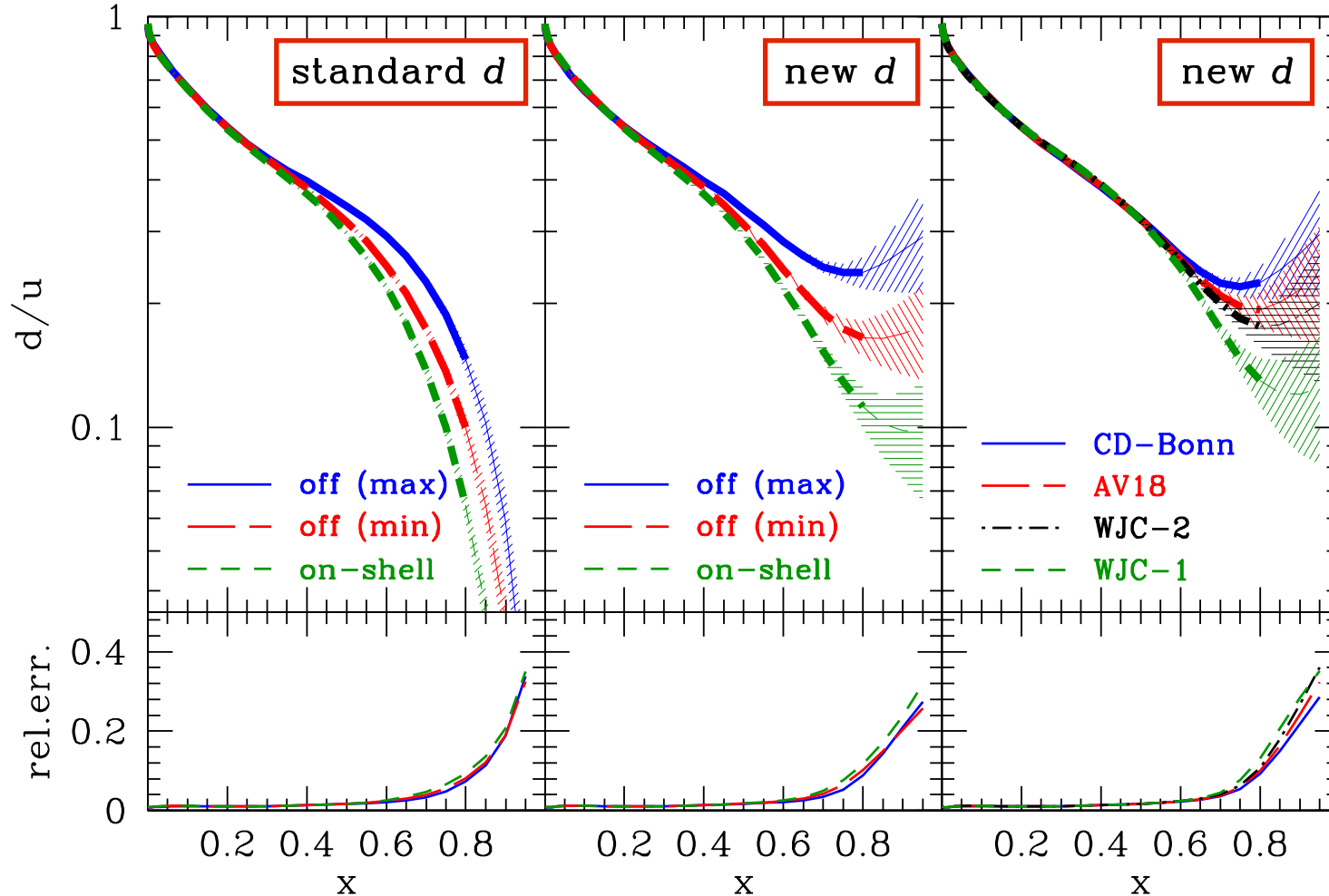
→ significantly reduced errors with weaker cuts

New CJ11 PDF analysis

- Explore dependence of PDF fits on deuteron wave functions and nucleon off-shell corrections
 - use only “high-precision” wave functions (AV18, CD-Bonn, WJC-1, WJC-2)
 - model nucleon off-shell correction with reasonable range of parameters
- Dependence of d/u ratio on d quark parametrization
 - allow for finite, nonzero ratio in $x = 1$ limit

$$d(x, Q^2) \rightarrow d(x, Q^2) + a x^b u(x, Q^2)$$

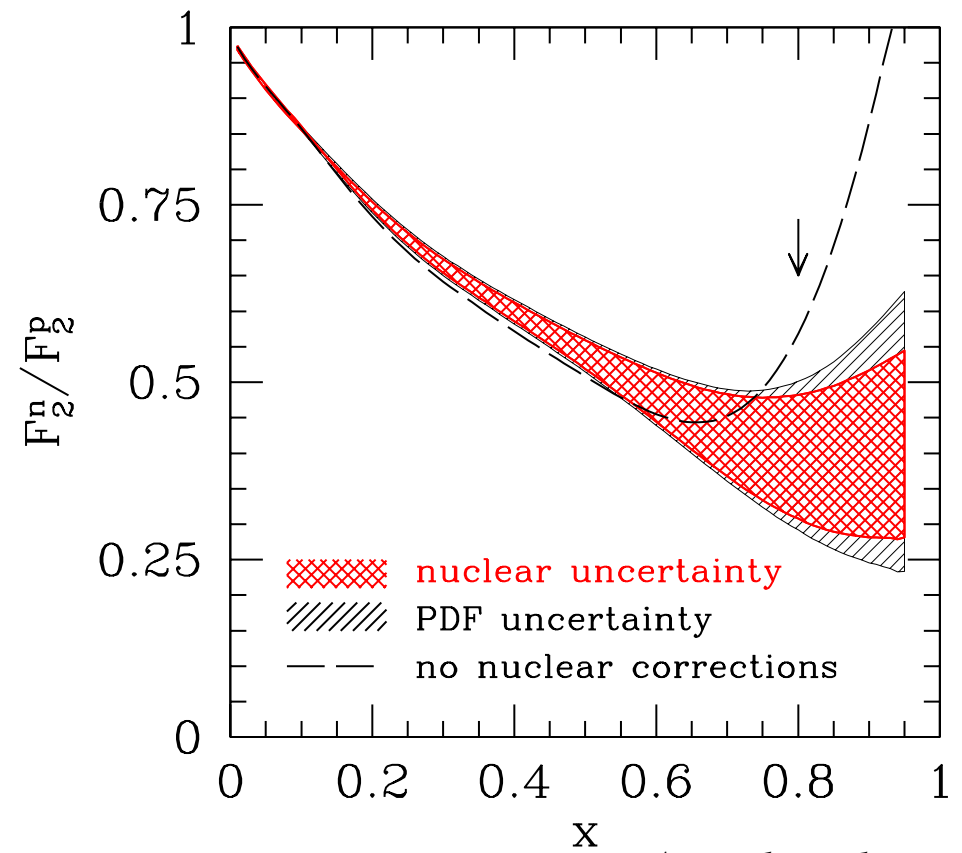
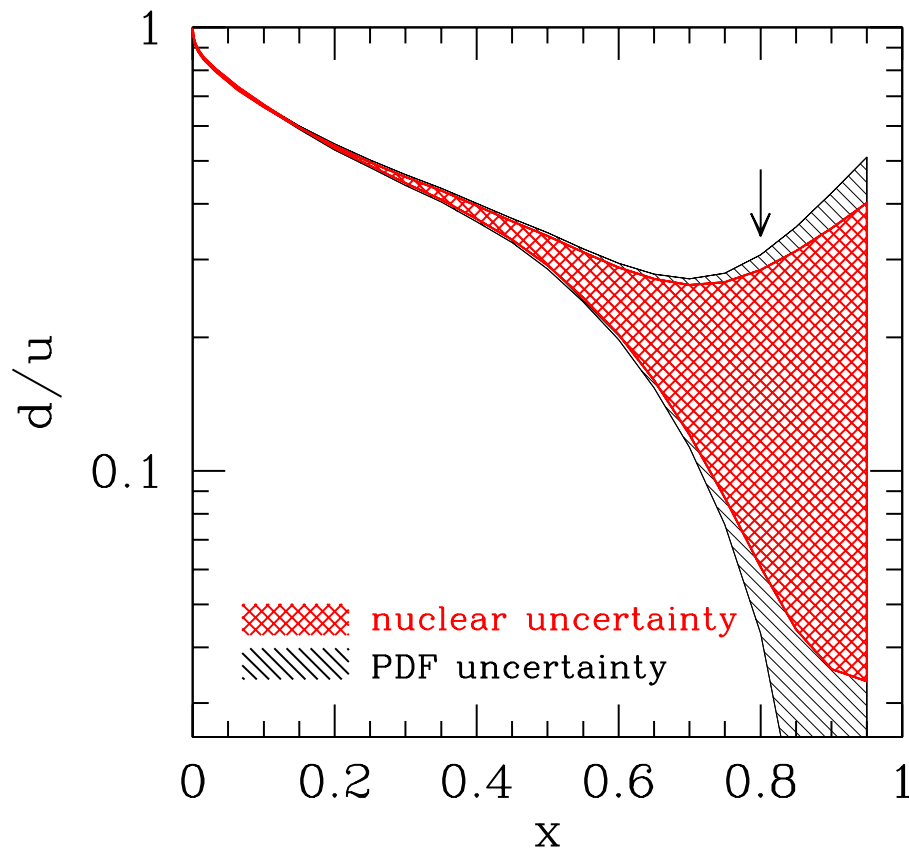
New CJ11 PDF analysis



Accardi et al.
PRD 84, 014008 (2011)

→ dramatic increase in d PDF in $x \rightarrow 1$ limit
 with more flexible parametrization

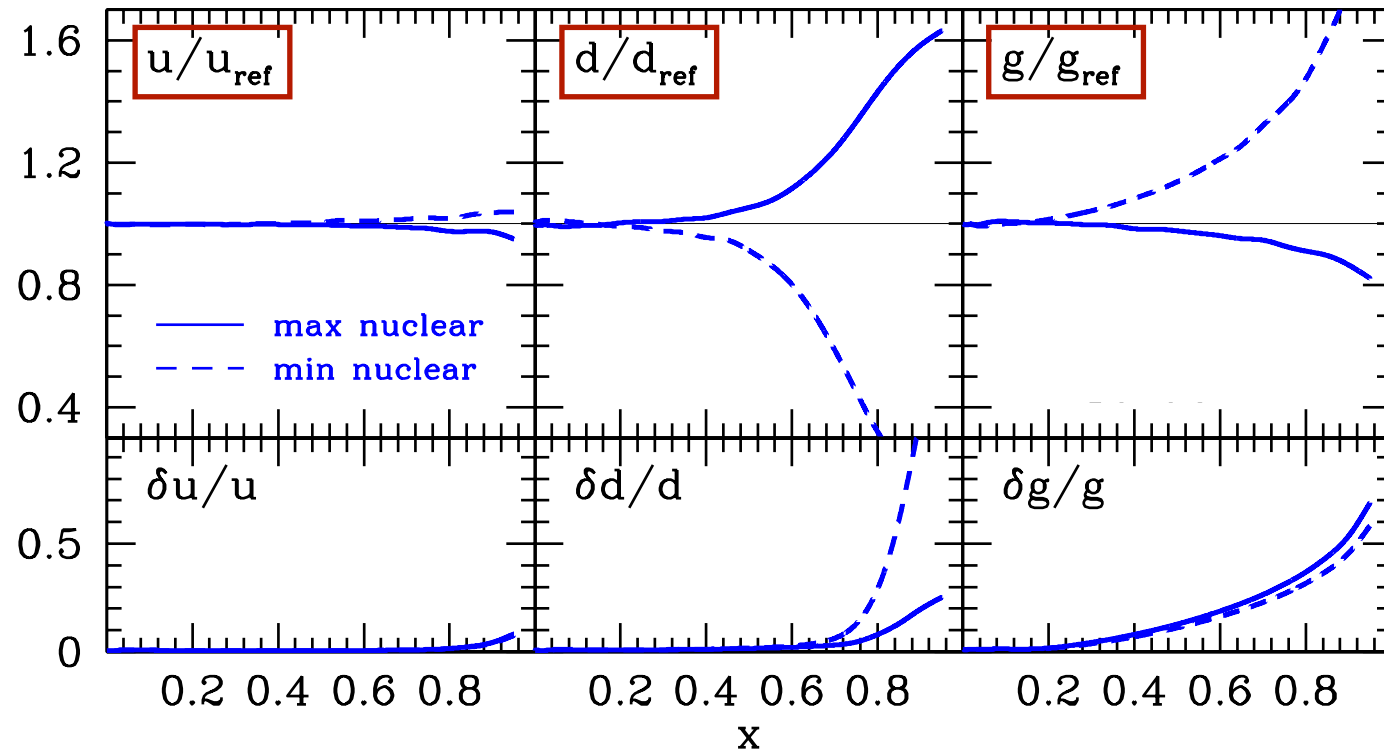
New CJ11 PDF analysis



Accardi et al.
PRD 84, 014008 (2011)

- combined nuclear correction uncertainties sizable at $x > 0.5$
- $x \rightarrow 1$ limiting value depends critically on deuteron model
- n/p ratio smaller at large x *cf.* no nuclear corrections fit

New CJ11 PDF analysis



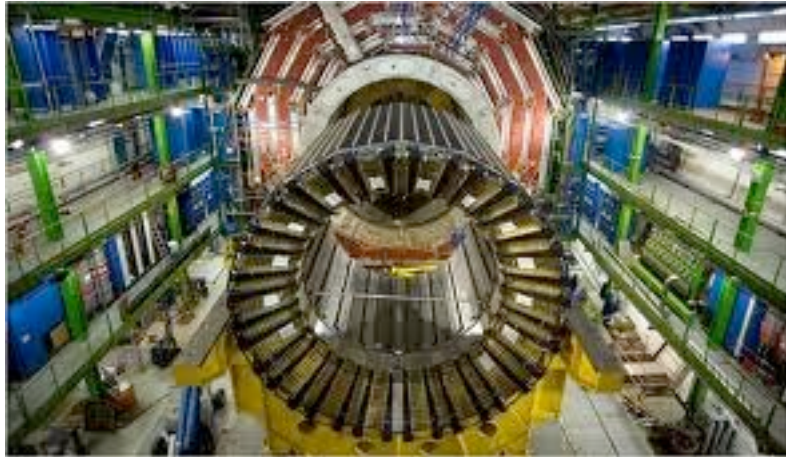
Accardi et al.
PRD 84, 014008 (2011)

- **very little effect on u quark PDF**
(tightly constrained by DIS & DY proton data)
- **gluon PDF anticorrelated with d quark**
(g compensates for smaller d quark contribution in jet data)
- **uncertainty in d feeds into larger uncertainty in g at high x**

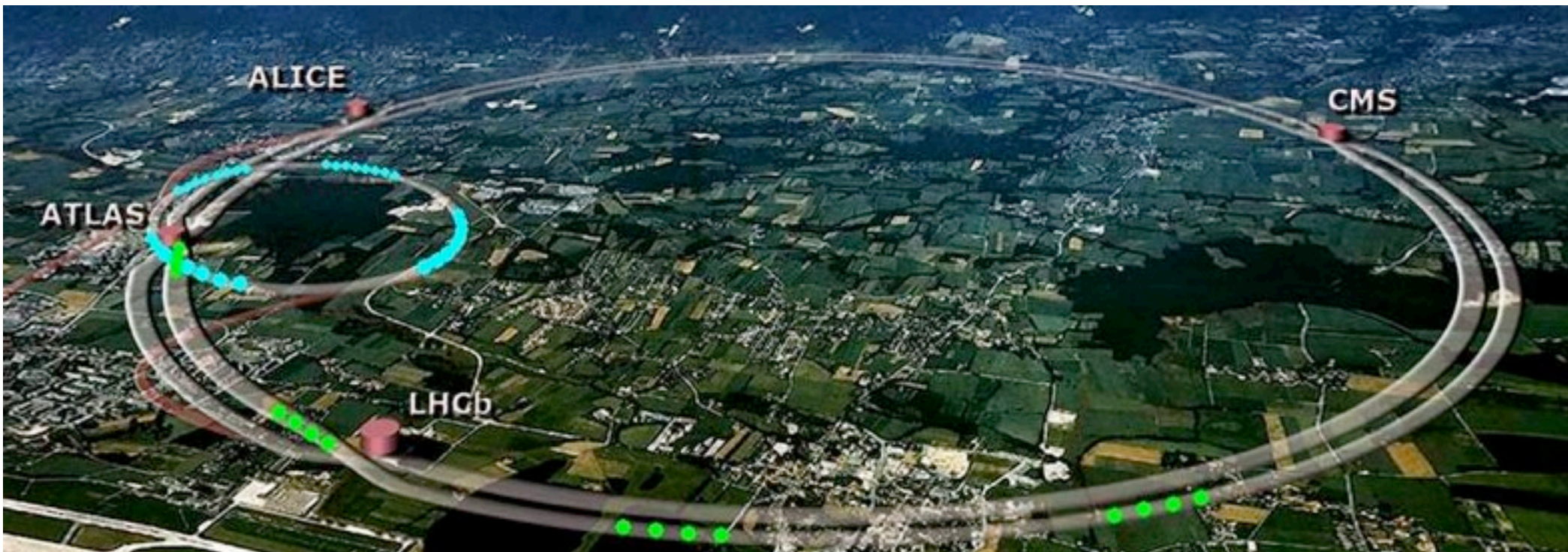
Implications for high-energy colliders

(Tevatron, LHC)

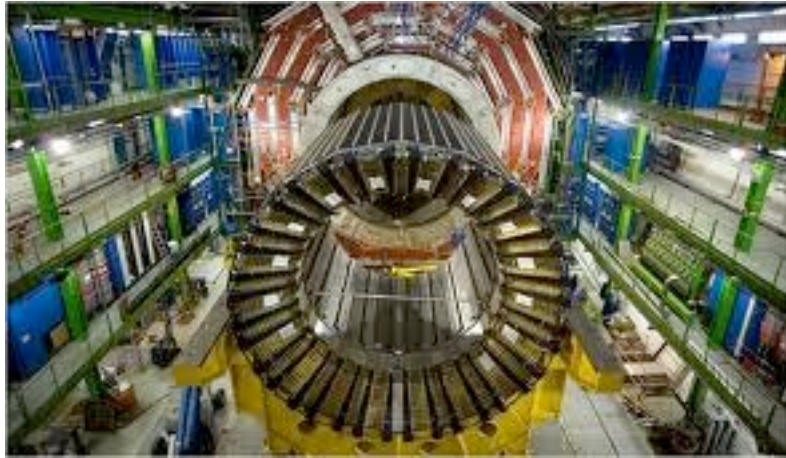
Large Hadron Collider (CERN): discovery of *Higgs boson*,
new physics beyond
the Standard Model?



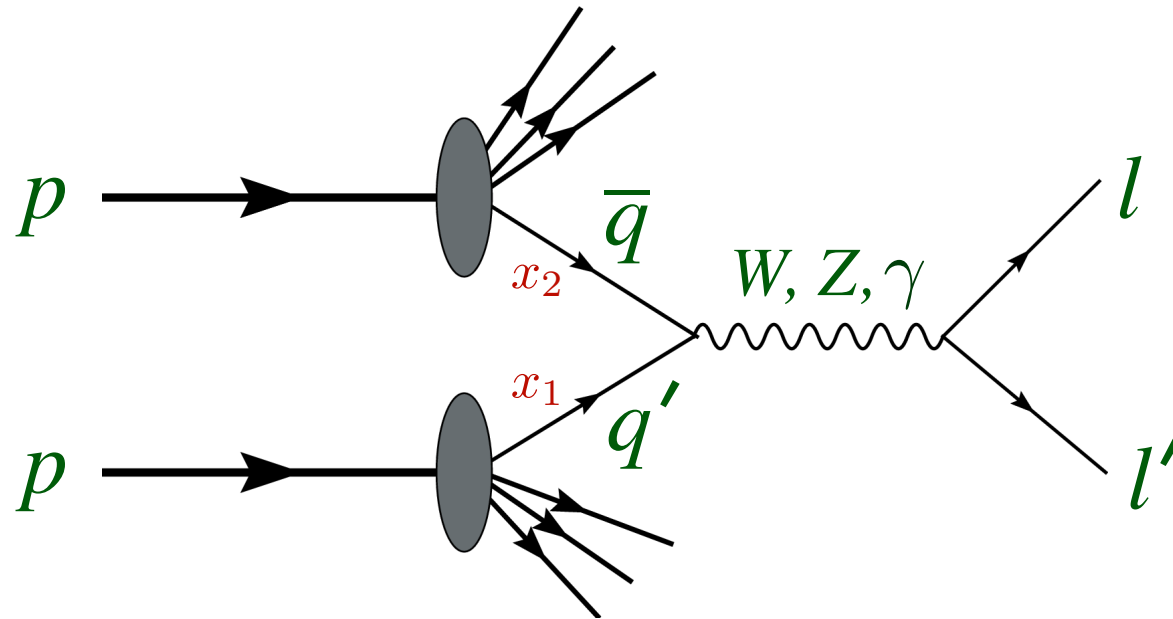
→ pp collisions at $\sqrt{s} = 7$ TeV



Large Hadron Collider (CERN): discovery of *Higgs boson*, new physics beyond the Standard Model?



→ pp collisions at $\sqrt{s} = 7$ TeV



W boson asymmetries

- Large- x PDF uncertainties affect observables at large rapidity y , defined as

$$x_{1,2} = \frac{M}{\sqrt{s}} e^{\pm y}$$

e.g. W^{\pm} asymmetry

$$A_W(y) = \frac{\sigma_{W^+} - \sigma_{W^-}}{\sigma_{W^+} + \sigma_{W^-}} \approx \frac{d(x_2)/u(x_2) - d(x_1)/u(x_1)}{d(x_2)/u(x_2) + d(x_1)/u(x_1)} \quad [x_1 \gg x_2]$$

where

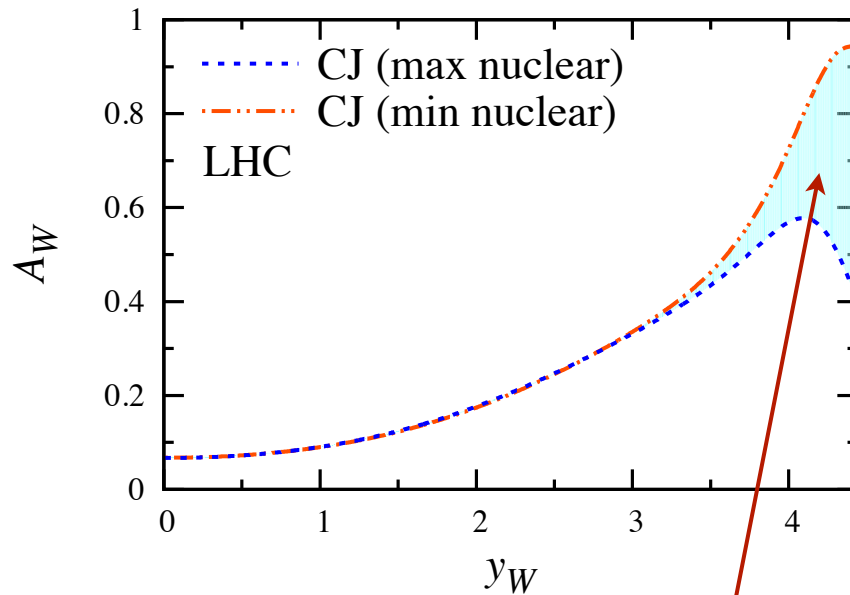
$$\sigma_{W^+} \equiv \frac{d\sigma}{dy}(pp \rightarrow W^+ X) = \frac{2\pi G_F}{3\sqrt{2}} x_1 x_2 (u(x_1)\bar{d}(x_2) + \dots)$$

W boson asymmetries

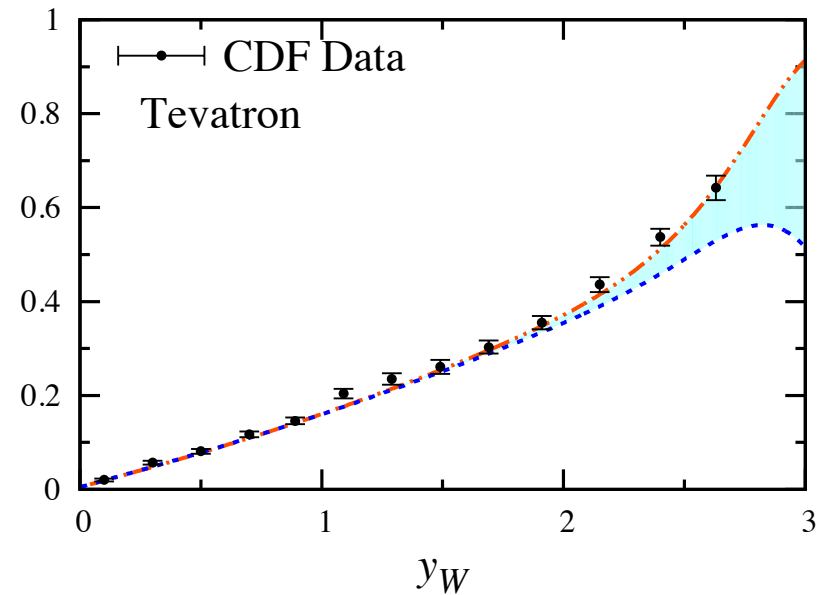
- Large- x PDF uncertainties affect observables at large rapidity y , defined as

$$x_{1,2} = \frac{M}{\sqrt{s}} e^{\pm y}$$

e.g. W^{\pm} asymmetry



sensitive to
 d at high x



Brady, Accardi, WM, Owens (2011)

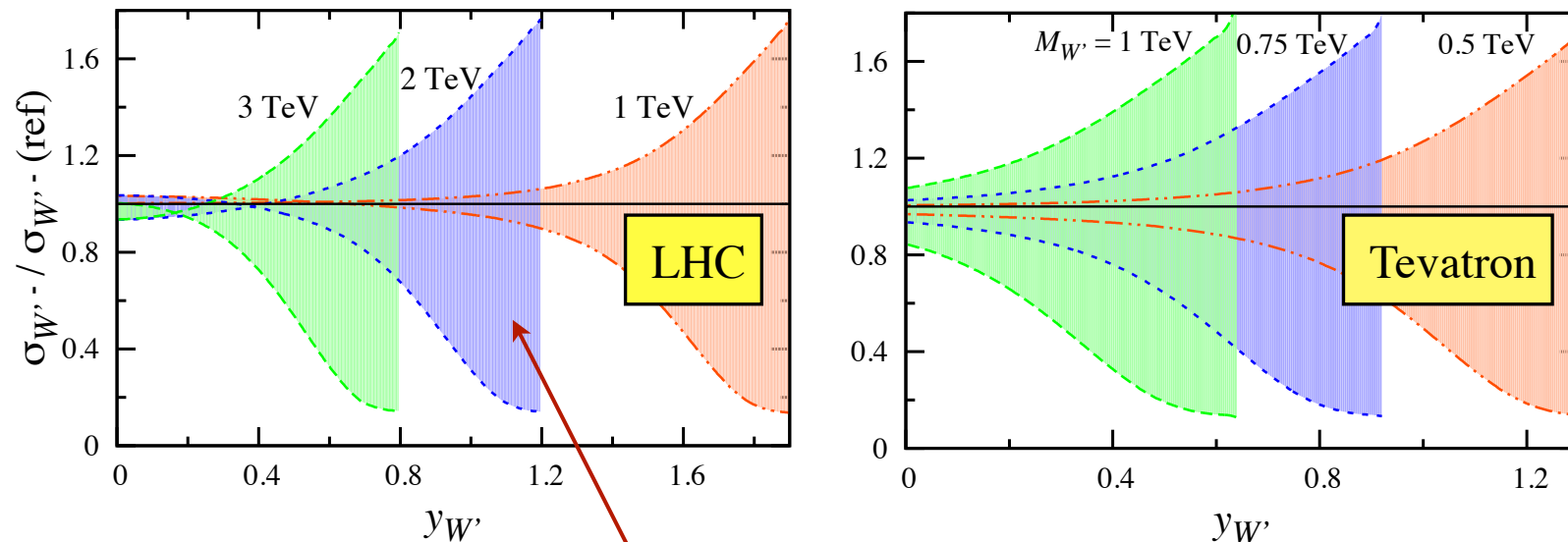
Heavy W' , Z' boson production

- Some extensions of Standard Model predict heavy versions of W , Z bosons
 - current limits $M_{W'} > 2.15 \text{ TeV}$, $M_{Z'} > 1.83 \text{ TeV}$
(assuming Standard Model couplings)

Heavy W' , Z' boson production

- Some extensions of Standard Model predict heavy versions of W , Z bosons
- Observation of new physics signal requires accurate determination of QCD backgrounds, which depend on PDFs!

e.g. for W'^- production

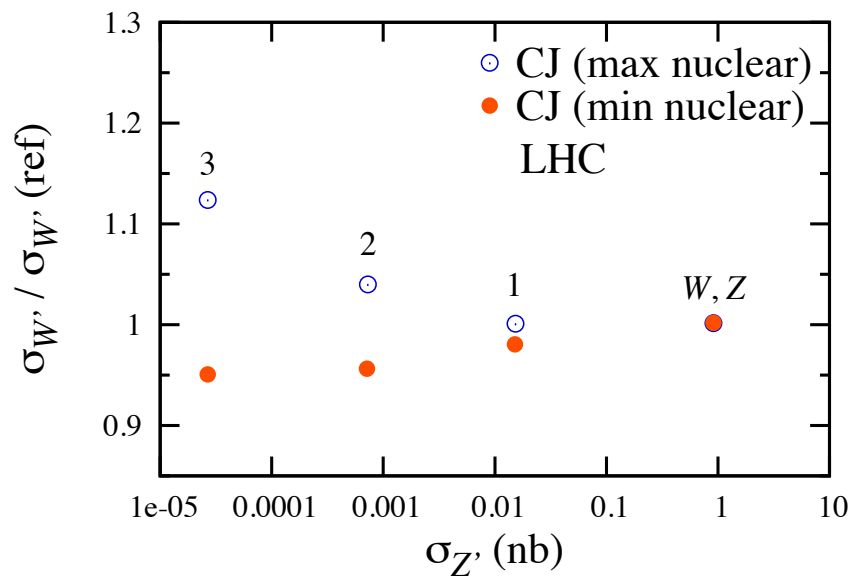


increasing uncertainty at large y

Heavy W' , Z' boson production

- Some extensions of Standard Model predict heavy versions of W , Z bosons
- Observation of new physics signal requires accurate determination of QCD backgrounds, which depend on PDFs!

e.g. integrated W' cross section



uncertainties in high- x PDFs
could affect interpretation
of experiments searching
for new particles

Future plans

Future plans for determining d/u

- $e d \rightarrow e p_{\text{spec}} X^*$
“BoNuS”

semi-inclusive DIS from d
→ tag “spectator” protons

- $e {}^3\text{He}({}^3\text{H}) \rightarrow e X^*$
“MARATHON”

${}^3\text{He}$ -tritium mirror nuclei

- $e p \rightarrow e \pi^\pm X^*$

semi-inclusive DIS as flavor tag

- $e^\mp p \rightarrow \nu(\bar{\nu}) X$
 $\nu(\bar{\nu}) p \rightarrow l^\mp X$
 $p p(\bar{p}) \rightarrow W^\pm X, Z^0 X$
 $\vec{e}_L(\vec{e}_R) p \rightarrow e X^*$
“PVDIS / SOLID”

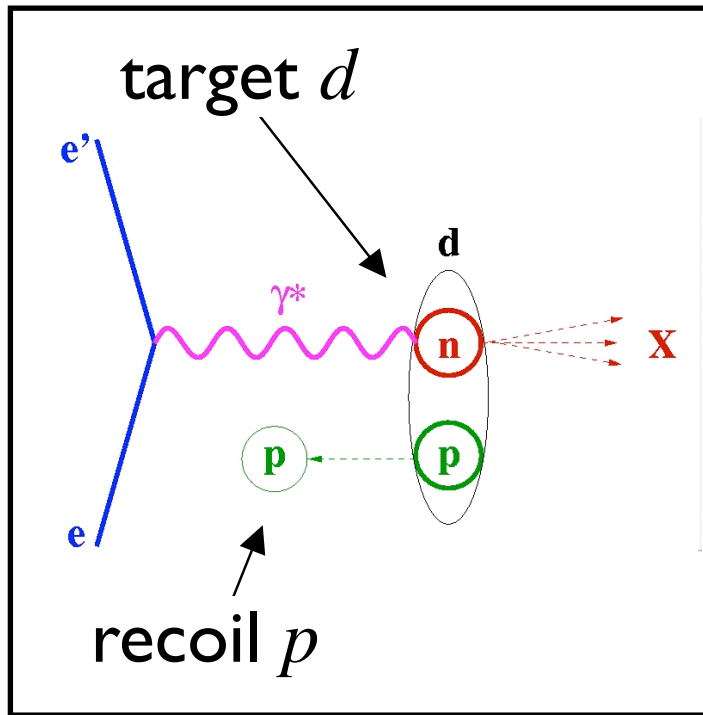
}

weak current
as flavor probe

*planned for JLab at 12 GeV

BoNuS: slow spectator tagging

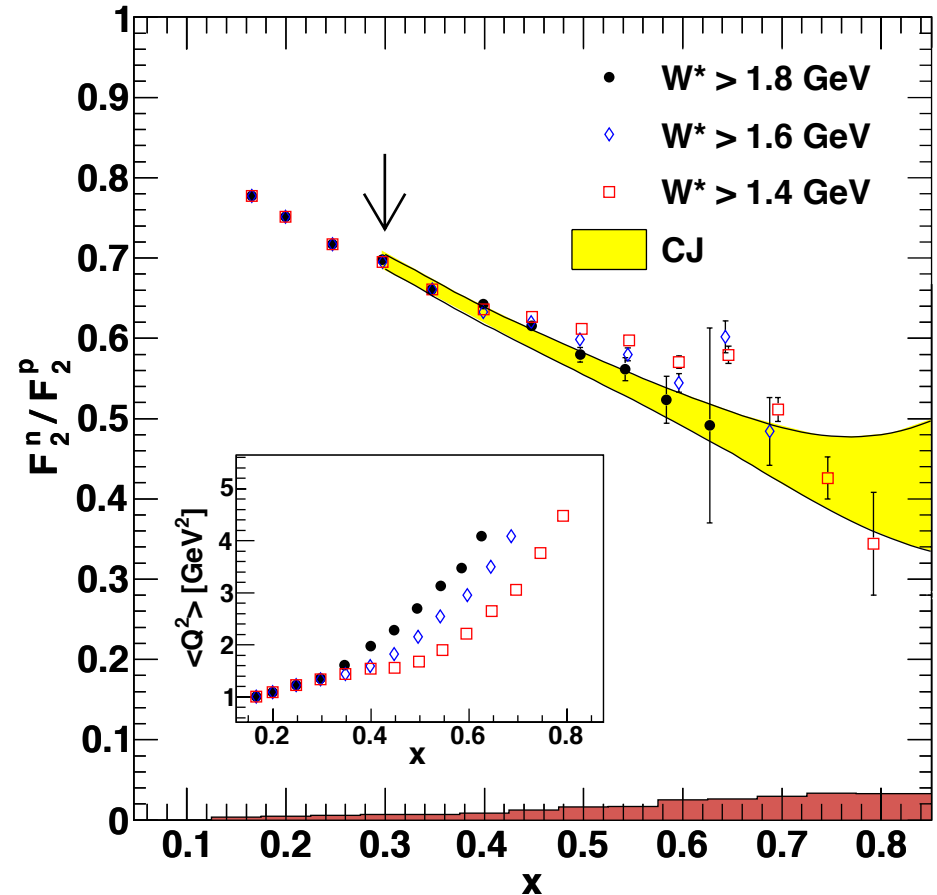
$$e d \rightarrow e p X$$



slow backward p

- neutron nearly on-shell
- minimize rescattering

“6 GeV” JLab data



Baillie et al., arXiv:1110.2770

- 12 GeV experiment will extend range to $x \sim 0.8$

Bueltmann et al., Expt. E12-10-102

MARATHON: DIS from ^3He / ^3H

- Extract n/p ratio from measured ^3He / ^3H ratio

$$\frac{F_2^n}{F_2^p} = \frac{2\mathcal{R} - F_2^{^3\text{He}}/F_2^{^3\text{H}}}{2F_2^{^3\text{He}}/F_2^{^3\text{H}} - \mathcal{R}}$$

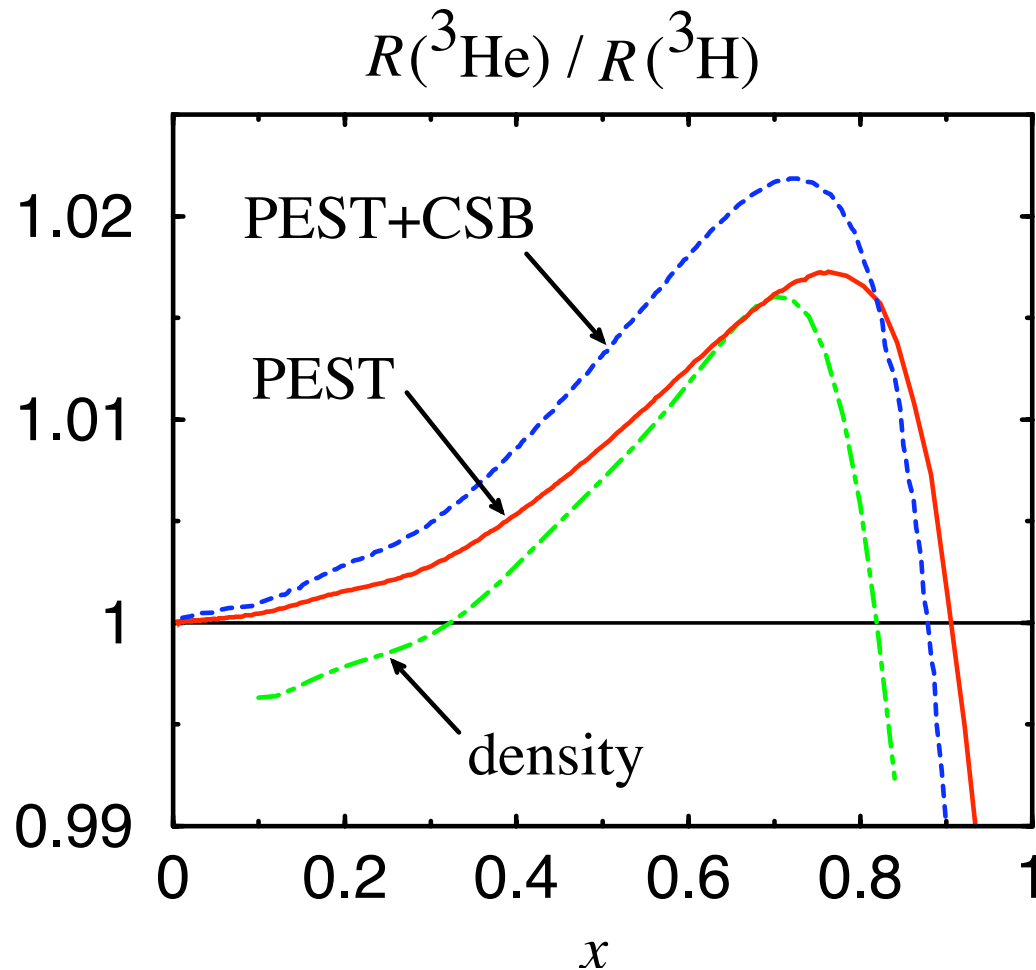
where ratio of “EMC ratios” $\mathcal{R} = \frac{R(^3\text{He})}{R(^3\text{H})}$

$$R(^3\text{He}) = \frac{F_2^{^3\text{He}}}{2F_2^p + F_2^n} ; \quad R(^3\text{H}) = \frac{F_2^{^3\text{H}}}{F_2^p + 2F_2^n}$$

→ main theoretical input

MARATHON: DIS from ${}^3\text{He} / {}^3\text{H}$

- Extract n/p ratio from measured ${}^3\text{He} / {}^3\text{H}$ ratio

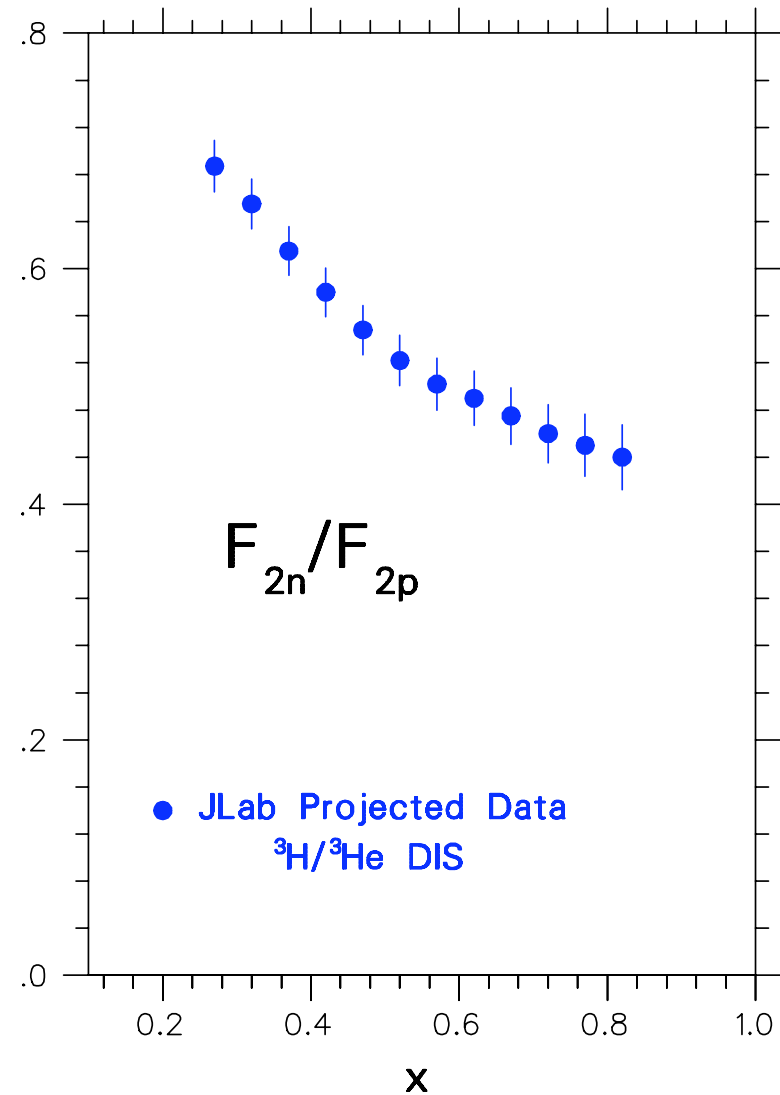
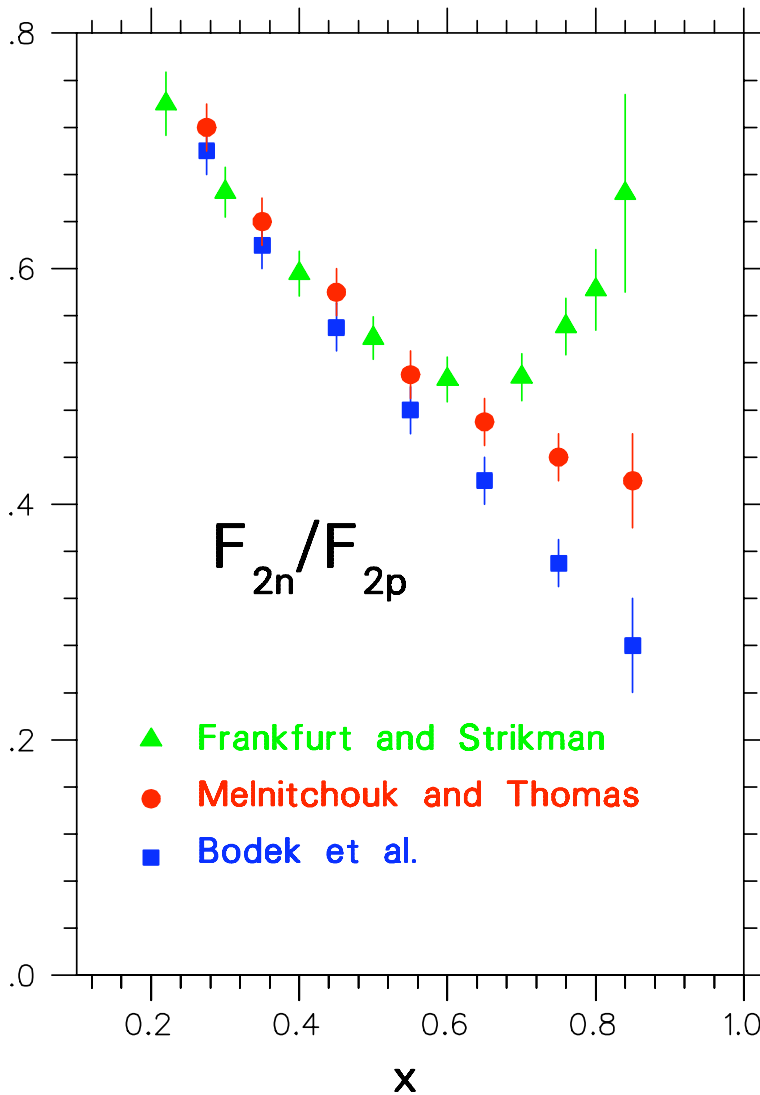


Afnan et al., PRC 68, 035201 (2003)

→ nuclear effects
cancel to $< 1\%$

MARATHON: DIS from ^3He / ^3H

■ Expected uncertainties of 12 GeV experiment



Petratos et al., Expt. E12-10-103

Summary

- New frontiers explored at large momentum fractions x
 - dedicated global PDF analysis by CJ collaboration
- Current large uncertainties on d quark PDF
 - impede knowledge about quark-gluon dynamics at large x
 - affect possible signals of new physics at colliders
- Model independent constraints expected from new experiments at 12 GeV uniquely sensitive to d quarks
- Plan extension to *spin-dependent* global PDF analysis
 - dedicated JLab (theory/experiment) postdoc from Jan. 2012 (Pedro Jimenez-Delgado)

The End