

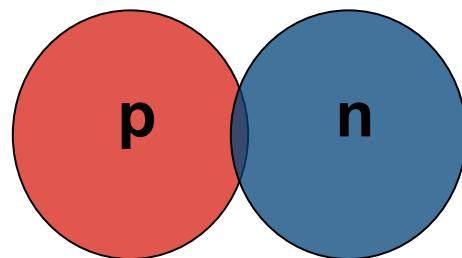
# Fitting (Semi) Inclusive Deuteron Data and Extraction of Neutron SF's

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**JLab Pizza Seminar**  
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# Outline

- Introduction
- Analysis
- Plans



# Motivation

- How well do we understand the deuteron? Need to understand how to model deuteron from proton and neutron;  $d =? p + n$
- How accurately can we describe the deuteron with in an independent nucleon impulse approximation?
- Extracting  $F_2^n$  from  $d, p$  DIS data.
- Fitting  $F_1^n, F_L^n$
- Confronting modeling with data:  $F_2^n$  from **BONuS\***
- More reliable extrapolation to  $\varepsilon = 1$ .

$$\varepsilon = \left[ 1 + 2 \left( 1 + \frac{\nu^2}{Q^2} \right) \tan^2 \frac{\theta}{2} \right]^{-1}$$

\*Barely Offshell Neutron Structure (E03-012)

# Analysis

- Fit Inclusive deuteron cross-sections;

$0.03 < Q^2 < 10.5 \text{ GeV}^2, 1.05 < W^2 < 11.5 \text{ GeV}^2$

- Compare fit to BONuS data:  $\sigma_{\text{tag}} / \sigma_{\text{untag}}$  ( $\rightarrow F_2^n/F_2^d @ \varepsilon = 1$ )
- Dependence of results on potential for deuteron wave function.
- Include BONuS result in fit and check consistency of model.

# Data Fitting

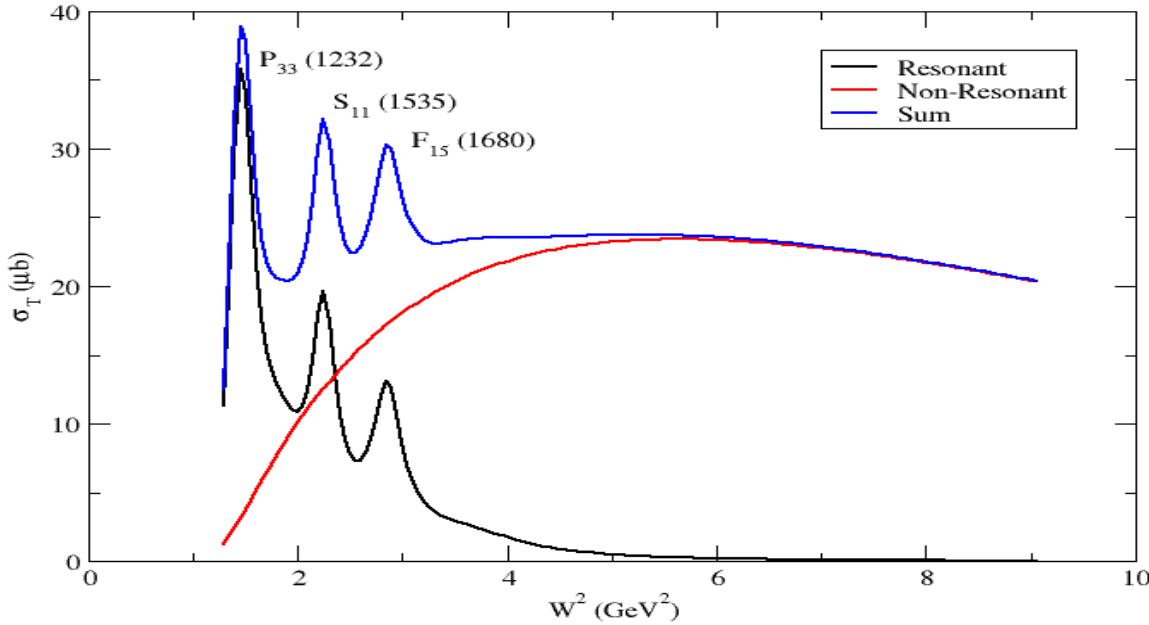
$$\sigma_{T,L}(W^2, Q^2) = \sigma_{T,L}^{Res}(W^2, Q^2) + \sigma_{T,L}^{NonRes}(W^2, Q^2)$$

*Fit Ingredients (Nucleon):*

$$\sigma_{T,L}^{Res}(W^2, Q^2) \propto BW_{T,L}(W^2) \cdot [A_{T,L}(Q^2)]^2$$

$$\sigma_T^{Non Res}(W^2, Q^2) \propto C(Q^2)x'(W - m_\pi)^{1/2}$$

Proton  $\langle Q^2 \rangle = 2.0 \text{ GeV}^2$



*So, what about SF's?*

$$\sigma_T \propto 2x F_I$$

$$\sigma_L \propto F_L$$

$$\sigma_T + \sigma_L \propto F_2$$

Resonance masses and widths fixed from proton result.

PRC 81, 055213 (Proton)

PRC 77, 065206 (Deuteron)

# Corrections: PWIA

- 3 Smear functions to describe  $xF_2, F_1, F_L$  *Convolution Model (Nucleus)*
- Using full AV18 potential for wave-function (includes 2-body forces).
- Theoretical smearing provided by W. Melnitchouk, J. Ethier.

*Inelastic:*

$$\int_x dy f_2(y, \gamma) F_2\left(\frac{y}{x}, \gamma\right) = F_2^{smear}(x, Q^2)$$

$$\gamma = \left[ 1 + \frac{4m^2 x^2}{Q^2} \right]^{1/2}$$

$$\int_x dy f_{11}(y, \gamma) \frac{2x}{y} F_1\left(\frac{y}{x}, \gamma\right) + f_{12}(y, \gamma) F_2\left(\frac{y}{x}, \gamma\right) = F_1^{smear}(x, Q^2)$$

$$F_L^{smear} = \gamma^2 F_2^{smear} - 2x F_1^{smear}$$

*Elastic:*

$$F_1 = \frac{G_M^2}{2} \delta(1-x)$$

$$F_2 = \frac{\tau G_M^2 + G_E^2}{1 + \tau} \delta(1-x)$$

$$\tau = \frac{Q^2}{4M^2}$$

$$G_{M,E}^2 = (G_M^p)^2 + (G_M^n)^2$$

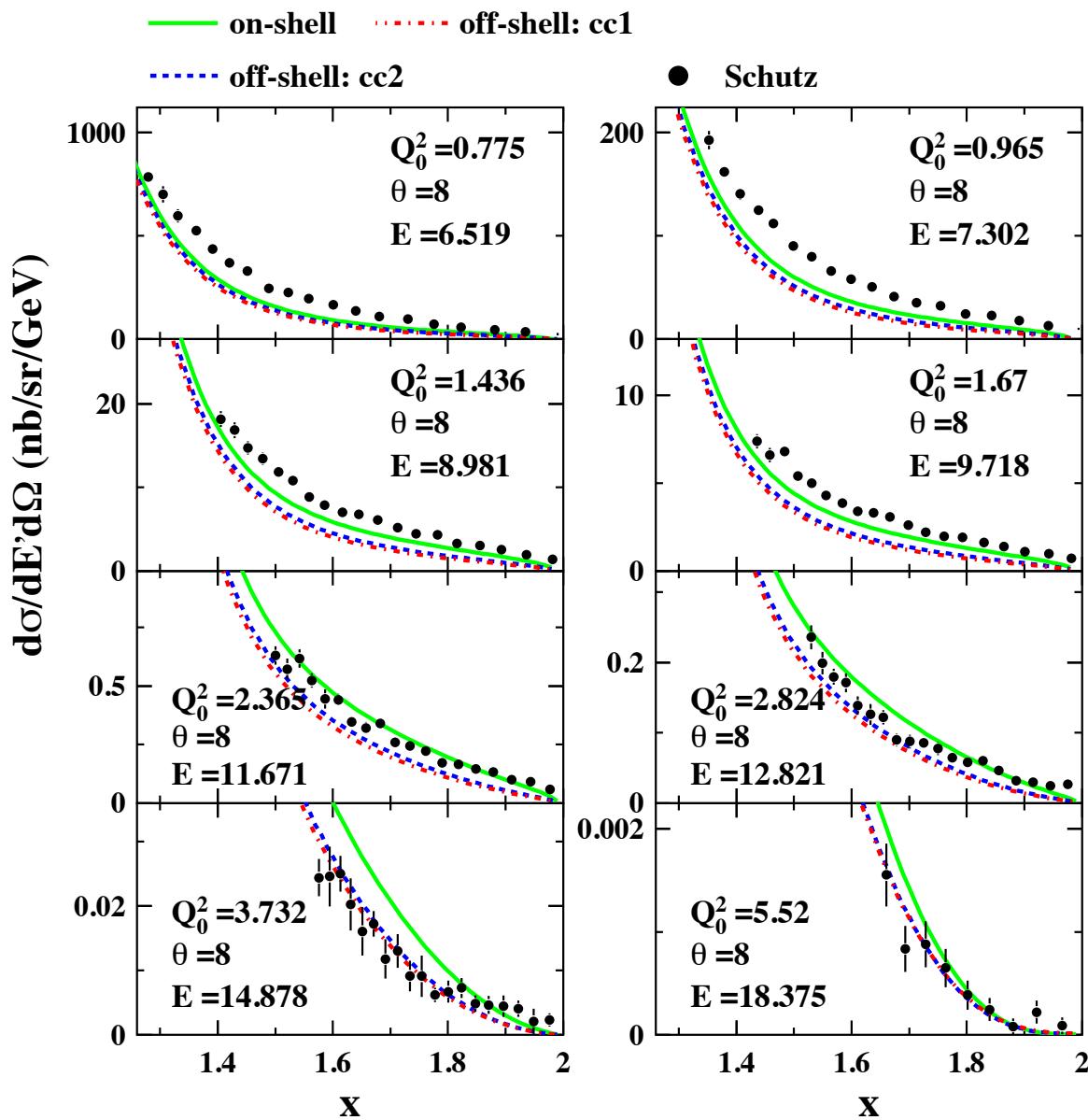
- Expressions above are for on-shell
- Used CJ12 for inelastic off-shell correction:  
assumed ~1.5% change in  $d_2$  nucleon radius

PRD 69, 114009 (2004), Sec. III

PRC 79, 035205 (2009), Sec. II

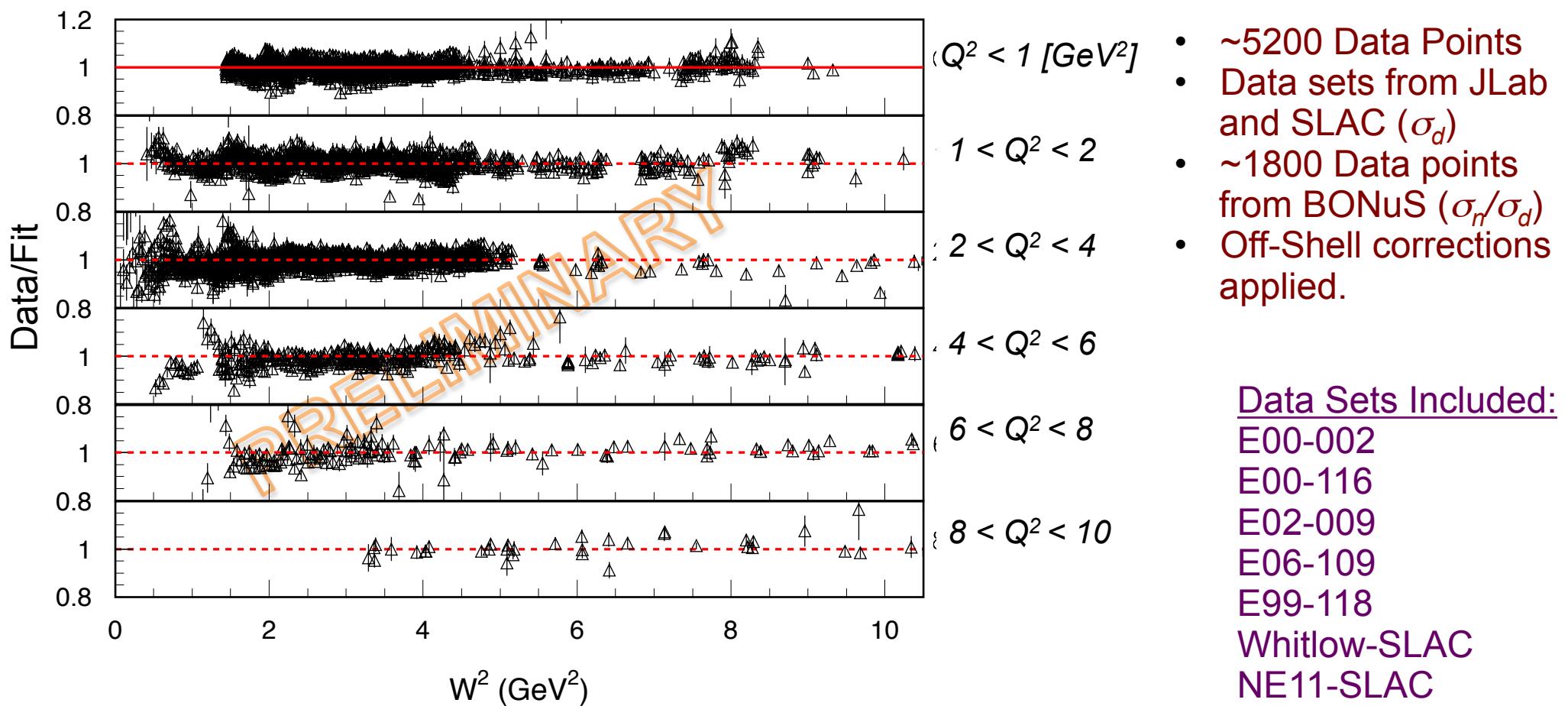
PRD 84, 014008 (2011), Sec. II

# (Quasi)Elastic Corrections

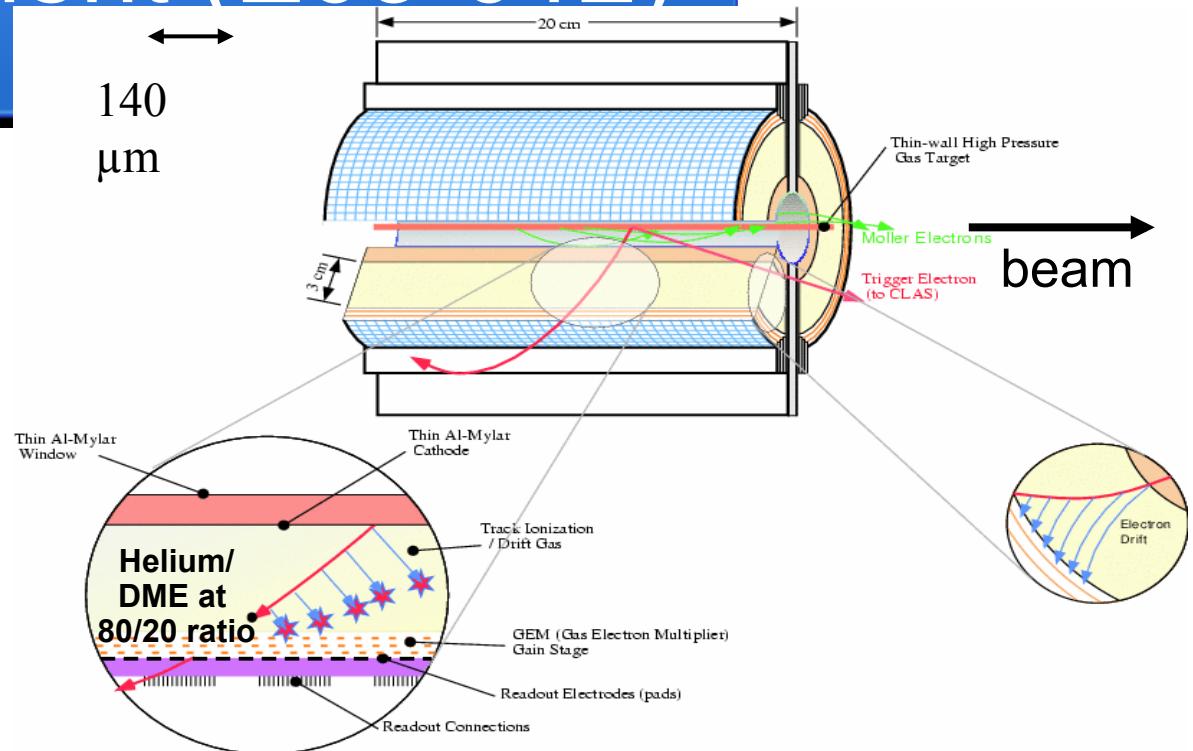
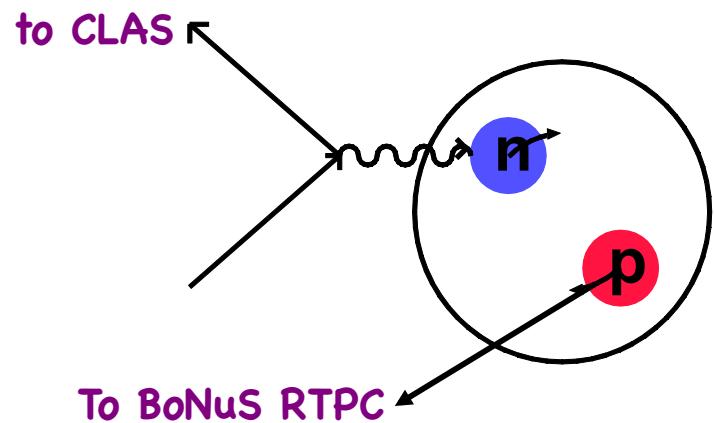


- QE Off-Shell and smearing in De Forest cc1,2 formalism
- Worked out and provided by W. Melnitchouk, J. Ethier. [arXiv:1402.3910]

# Comparison of Data/Fit



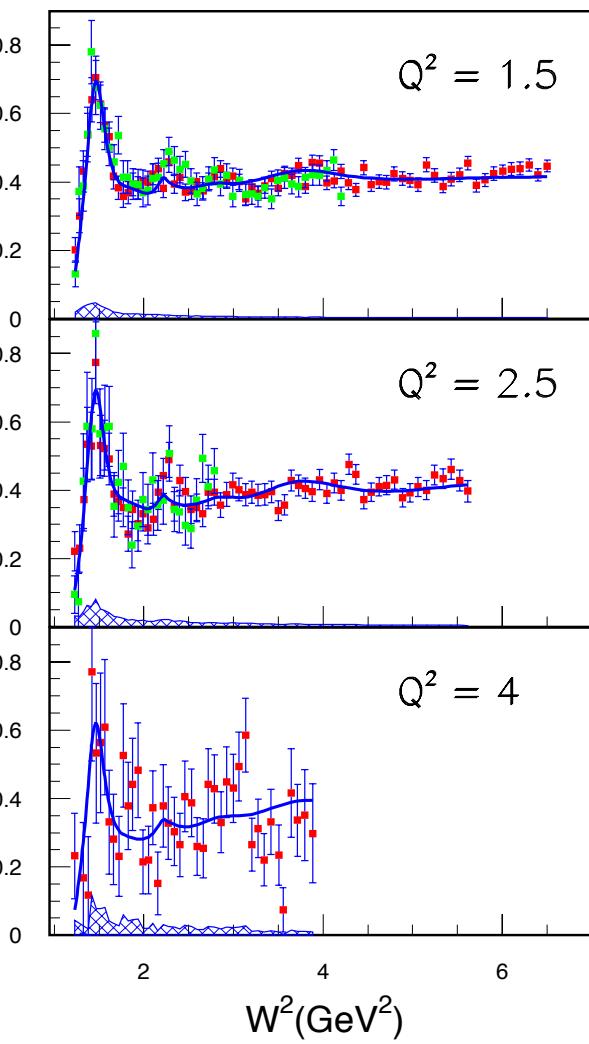
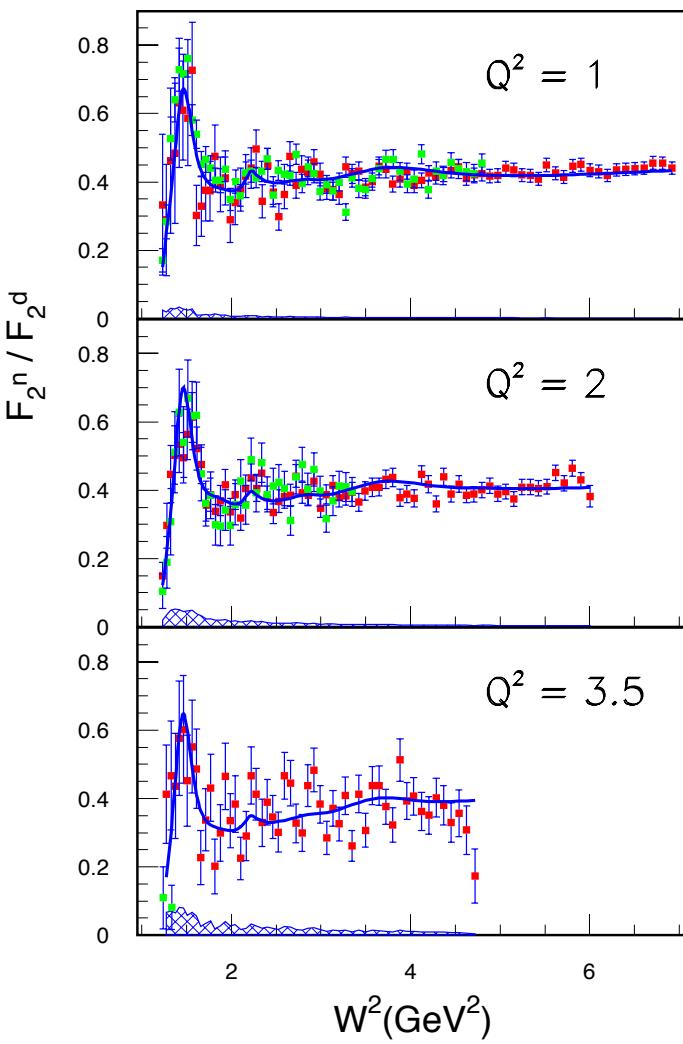
# BONUS Experiment (E03-012)



Thin walled deuterium gas target (7 atm) with 2, 4, and 5 GeV e-beam.

- Large acceptance spectrometer (CLAS) together with new detector capable of detecting spectator protons surrounding the target.
- Obtain virtually free neutron by tagging spectator protons with low momenta (66-200 MeV/c) and large scattering angles ( $> 90$  deg.); **minimize FSI + Off-shell effects**
- Physics from (semi) inclusive and exclusive channels.

$$F_2^n/F_2^d$$

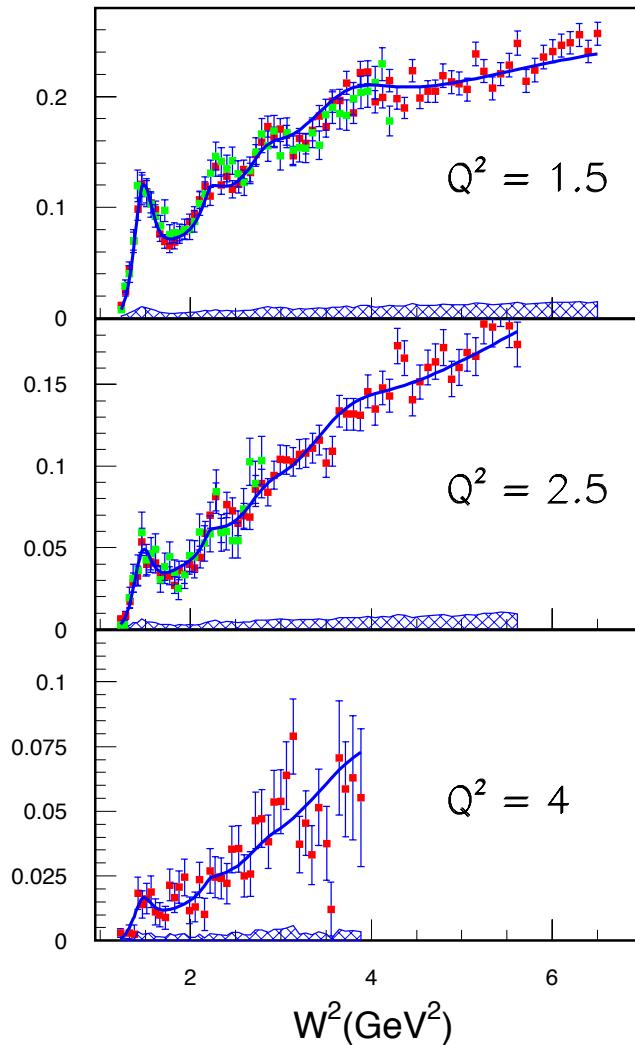
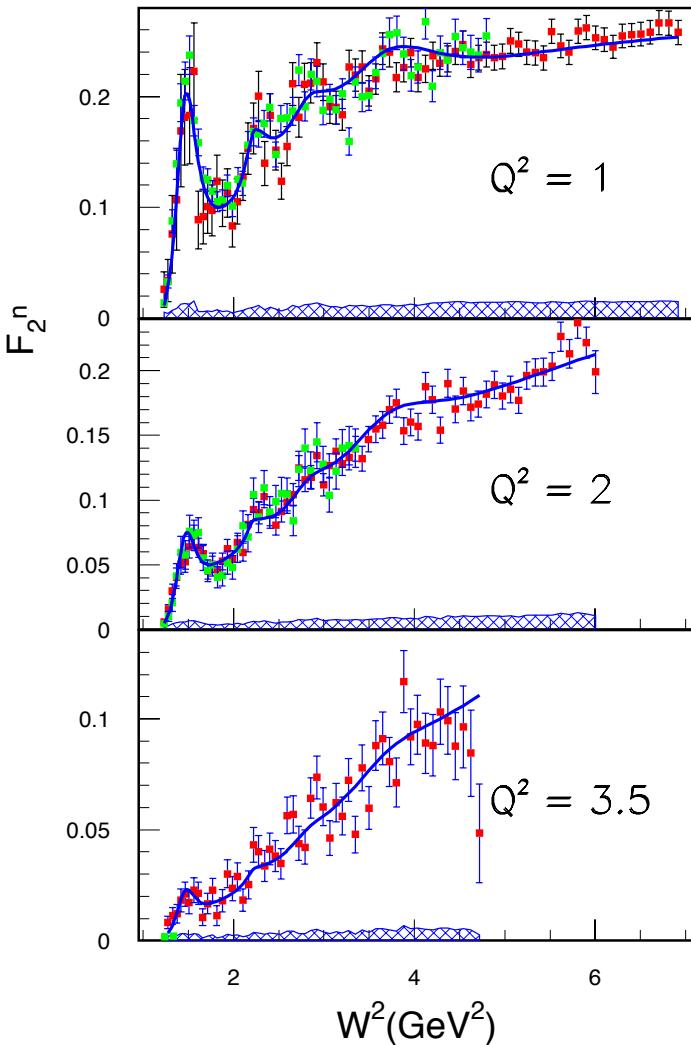


- Compare (normalized) BONuS result to fit
- Blue curve prediction from fit
- 5 GeV in red, 4 GeV in green.

PRC 89, 045206 (2014)

# $F_2^n$

$$(F_2^n/F_2^d)_{\text{BONuS}} \times (F_2^d)_{\text{fit}} \rightarrow F_2^n$$



- Compare (normalized) BONuS result to fit
- Blue curve prediction from fit
- 5 GeV in red, 4 GeV in green.

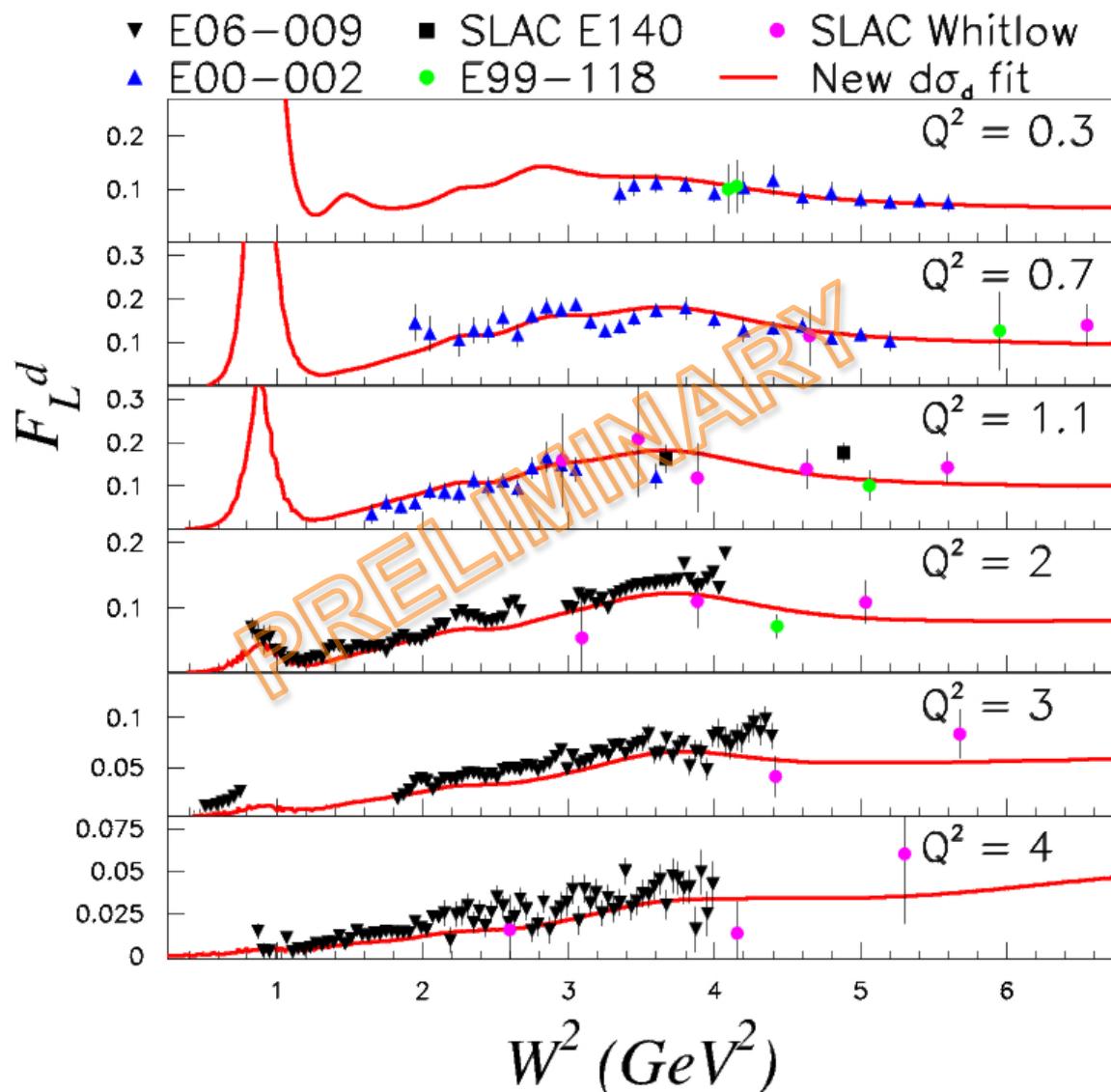
PRC 89, 045206 (2014)

# $F_2^n$

From  $(F_2^n/F_2^d)_{\text{BONuS}} \times (F_2^d)_{\text{fit}} \rightarrow F_2^n$

- Quark-Hadron Duality & Moments: [arXiv: 1501.02203 ]
- Study EMC effect for deuteron:  $F_2^d/(F_2^n + F_2^p)$ , under study
- ...

# Comparison of Data/Fit: $F_L^d$



- Reasonable global consistency within uncertainties.
- All sets shown are included in fit.
- Finalizing E06-009 (ROSEN07); use fit to redo RCs

# Remaining

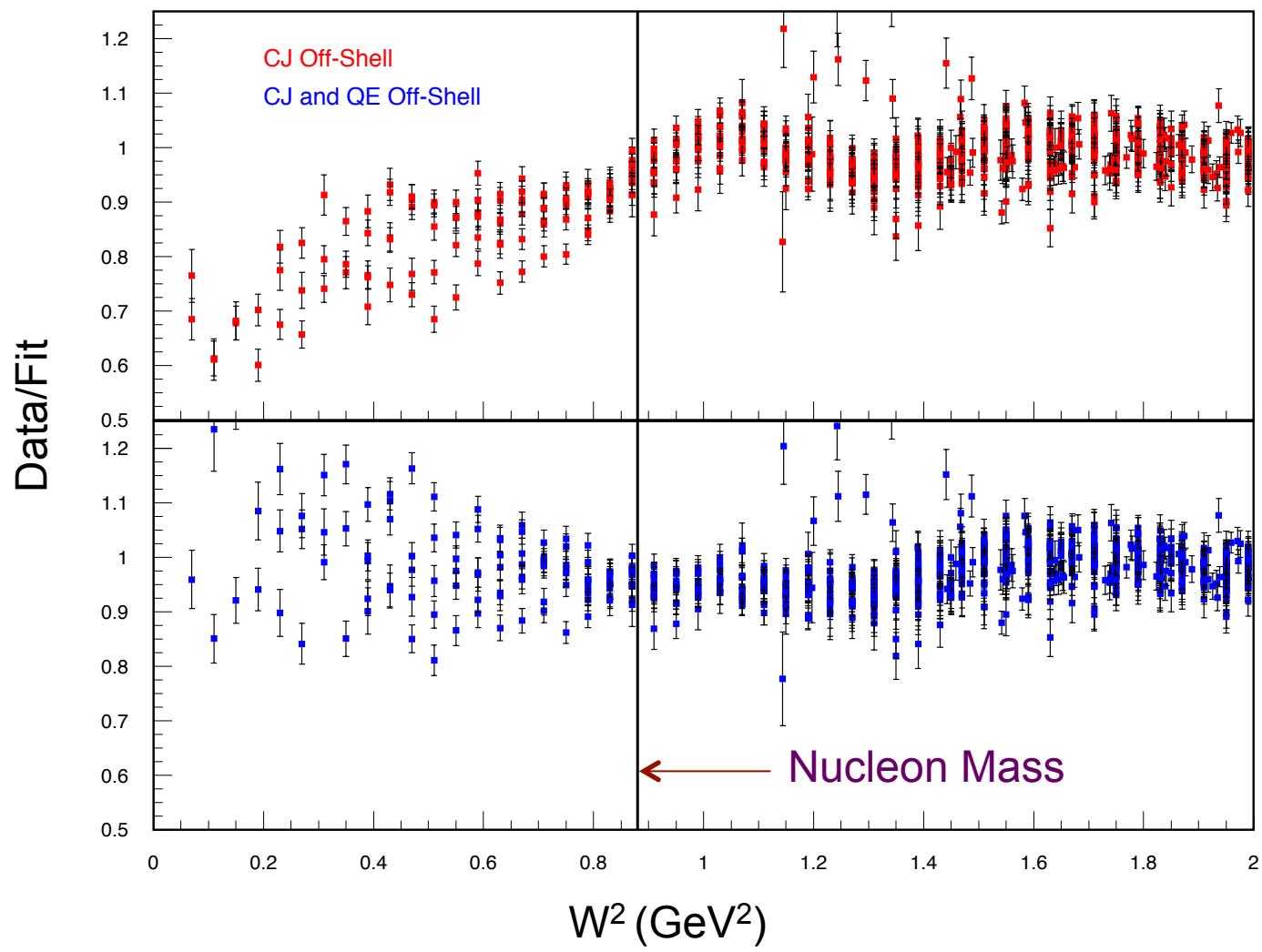
*After current iteration:*

- Include finalized ROSEN07 ( $F_L$ ) and Jan05 data
- Check helicity amplitudes.
- Check dependence on wave-function –i.e. compare answer from AV18 to what other wv-fn's would say

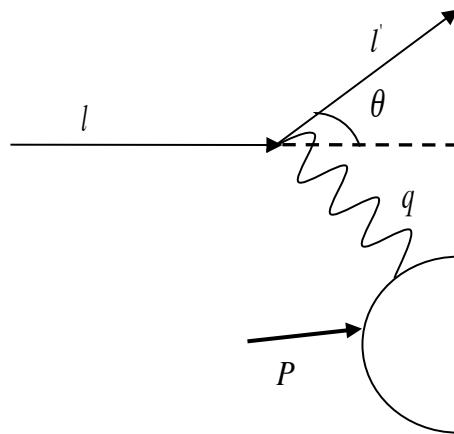
# Summary

- Updating fit to deuteron, utilizing proton information, and including several more deuteron data sets.
- Including more deuteron. Replacing previous smear with convolution prescription.
- New QE off-shell correction.
- Using fit to model deuteron and extract  $F_2^n$ .
- Fit includes neutron (BONuS) data.

# Comparison of Data/Fit



# Lepton Scattering



$$l = (E, \vec{l})$$

$$l' = (E', \vec{l}')$$

$$q = l - l'$$

$$Q^2 = (-q)^2 = 4EE' \sin^2 \frac{\theta}{2}$$

$$x = \frac{Q^2}{2M\nu}$$

$$\nu = E - E'$$

$$y = \frac{\nu}{E}$$

$$W^2 = M^2 + 2M\nu - Q^2$$

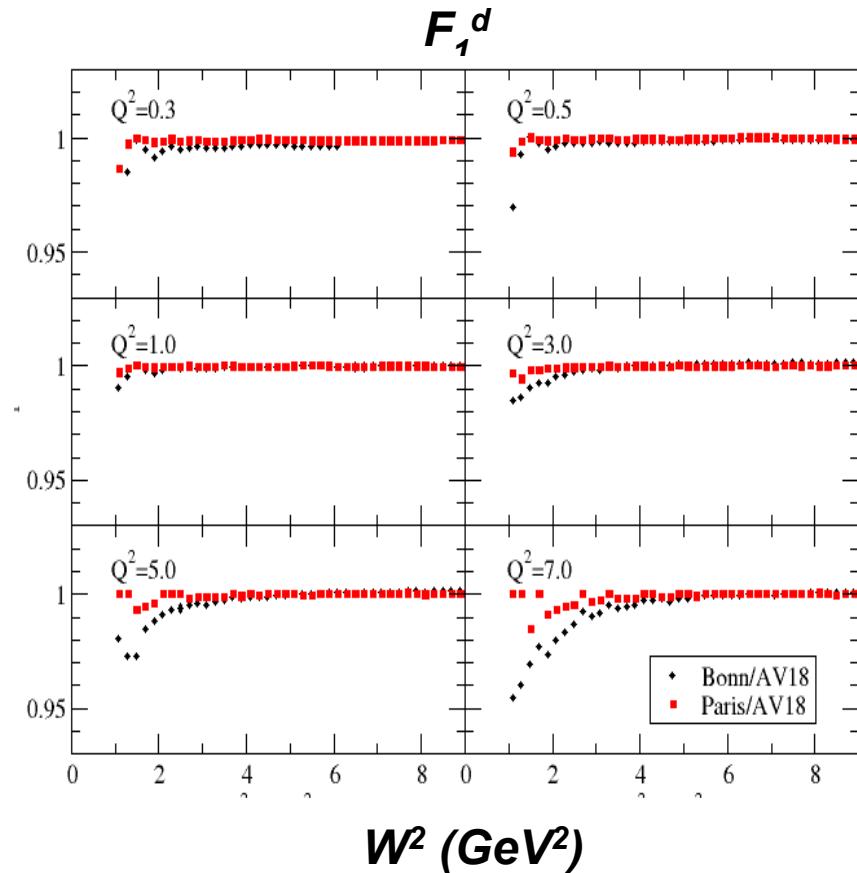
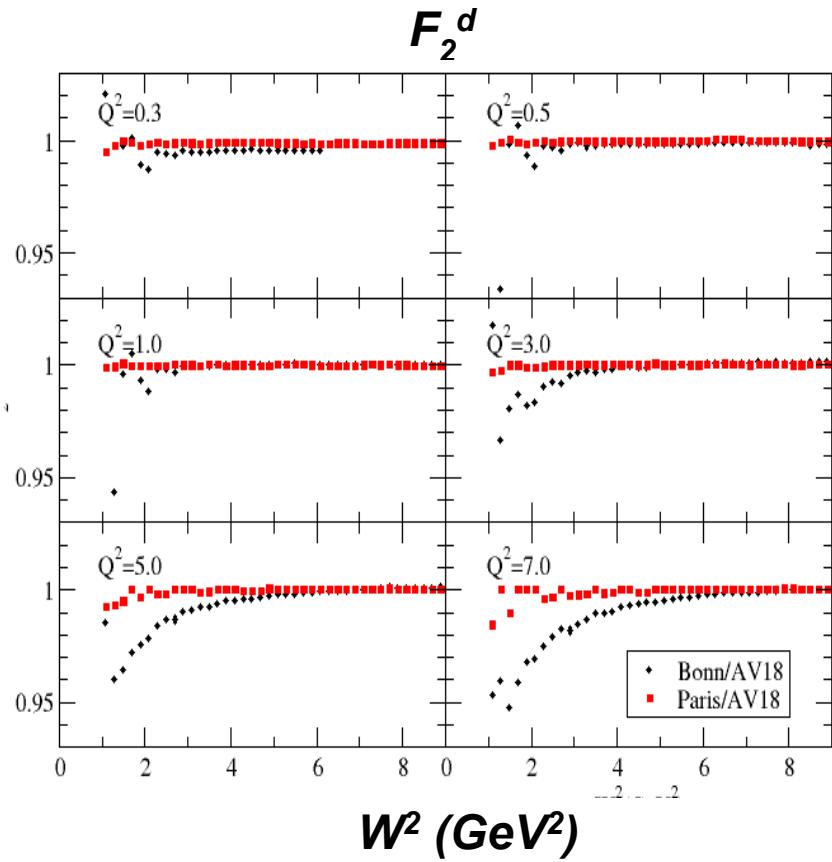
$$\Gamma = \frac{\alpha E' (W^2 - M^2)}{4\pi^2 Q^2 M E (1 - \varepsilon)}$$

$$\frac{d^2\sigma}{d\Omega dE'} = \Gamma [\sigma_T(W^2, Q^2) + \varepsilon \sigma_L(W^2, Q^2)]$$

$$\varepsilon = \left[ 1 + 2 \left( 1 + \frac{\nu^2}{Q^2} \right) \tan^2 \frac{\theta}{2} \right]^{-1}$$

$$\sigma_{Reduced} = \frac{1}{\Gamma} \frac{d^2\sigma}{d\Omega dE'} = \sigma_T(W^2, Q^2) + \varepsilon \sigma_L(W^2, Q^2)$$

# Comparison of Potentials

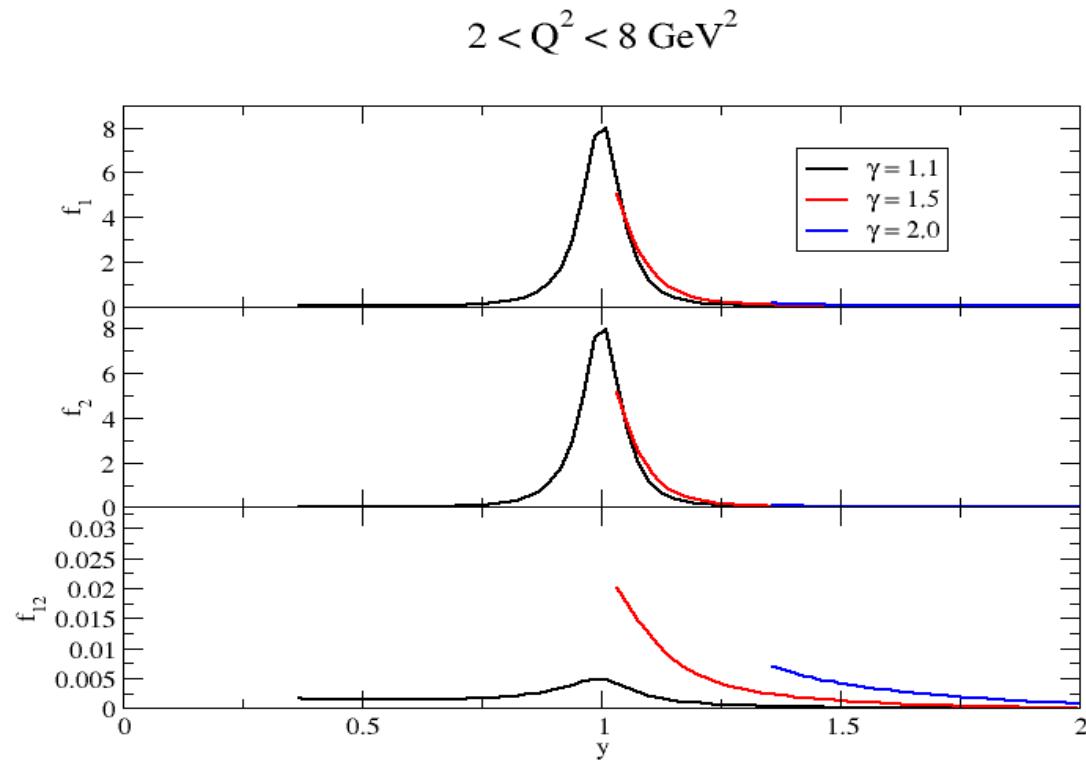


- Gives range of uncertainties from wave-function.
- Using AV18 in fit.
- AV18 more consistent with Paris than Bonn.
- QE region is included.

# Plane Wave Impulse Approximation

- 3 Smear functions to describe and 2 of  $xF_2, F_1, F_L$
- Using AV18 potential for wave-function.
- Theoretical smearing and off-shell calculations provided by W. Melnitchouk, J. Ethier.

*Convolution Model (Nucleus)*



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