

Flavor separation at large x

Alberto Accardi

Hampton U. & Jefferson Lab

APS spring meeting
13-16 February 2010



Outline

Why large x (and low- Q^2)

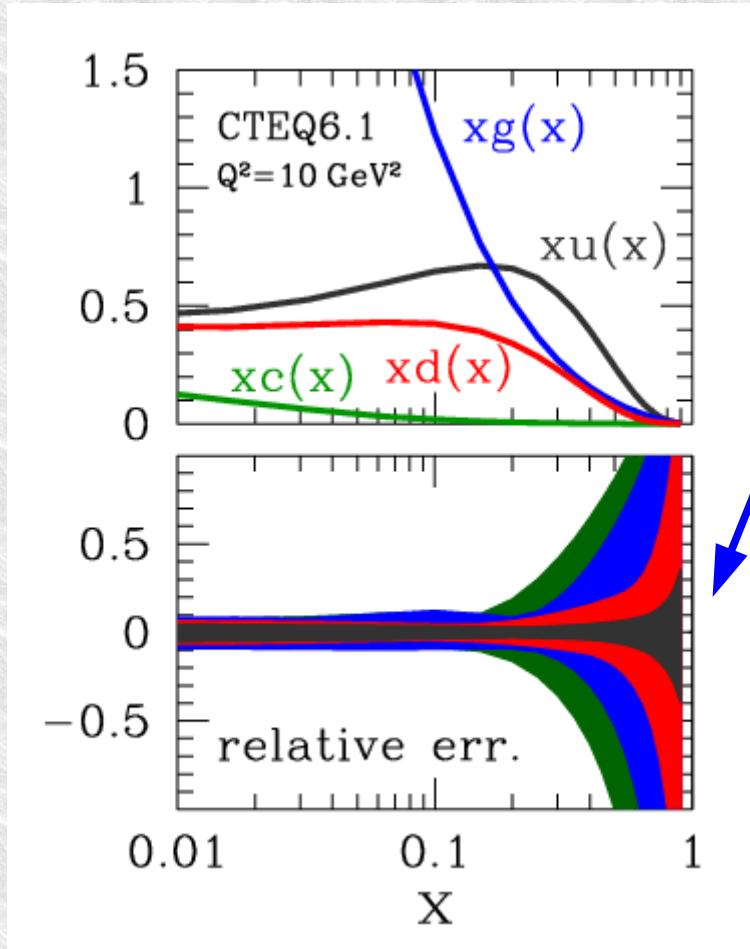
- ◆ Up and down: the CTEQ6X fit
- ◆ Gluons
- ◆ Intrinsic charm

Conclusions

Why large-x, low-Q²?

Why large x and low Q^2 ?

- Large uncertainties in quark and gluon PDF at $x > 0.4$ – e.g., CTEQ6.1



- PDF errors
 - propagation of exp. errors into the fit
 - statistical interpretation
 - reduced by enlarging the data set
- Theoretical errors
 - often poorly known
 - difficult to quantify
 - can be dominant

Why large x and low Q^2 ?

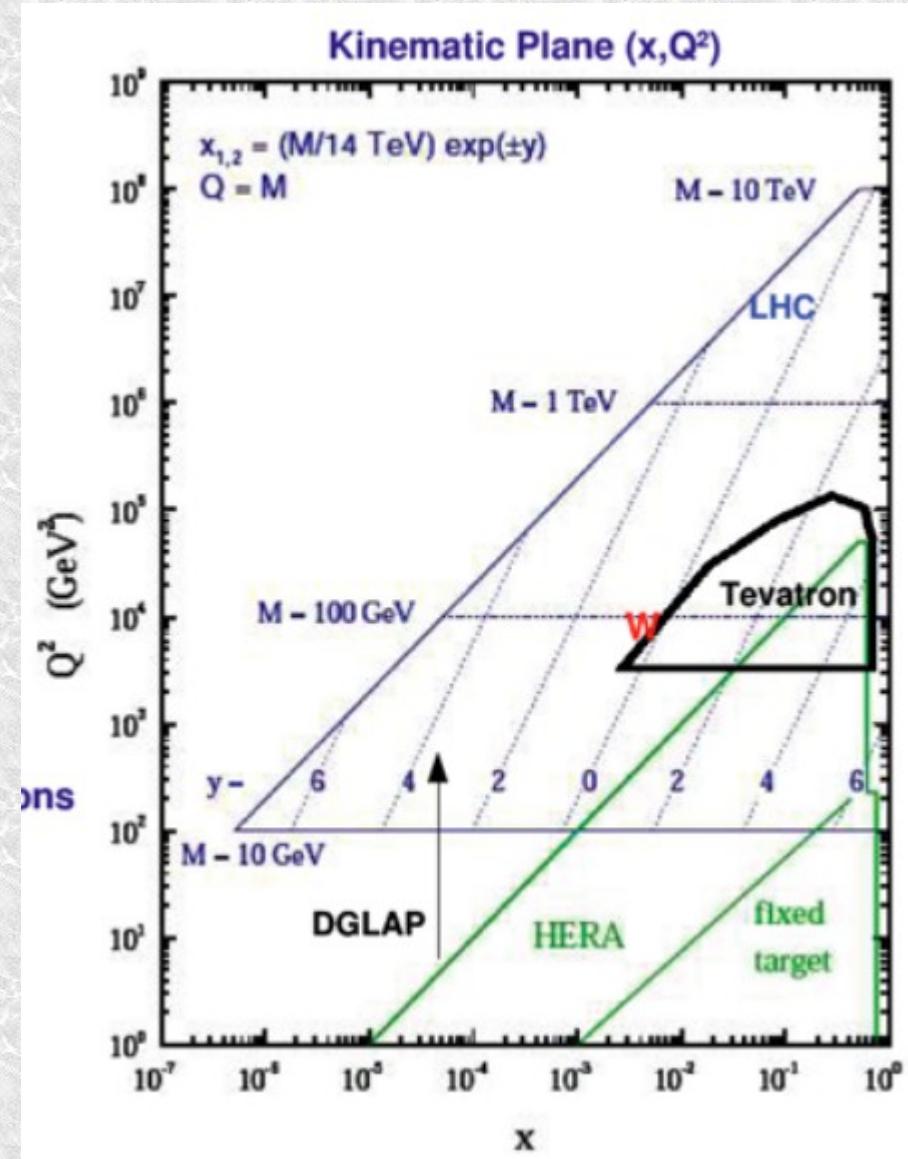
- ◆ Large uncertainties in quark and gluon PDF at $x > 0.4$
- ◆ Precise PDF at large x are needed, e.g.,
 - ◆ at LHC, Tevatron
 - 1) DGLAP evolution feeds large x , low Q^2 into lower x , large Q^2
 - 2) QCD background in high-mass new physics searches
 - ◆ Example: Z' production

$$M_{Z'} \gtrsim 200 \text{ GeV} \quad x = \frac{m_T}{\sqrt{s}} e^y$$

$$x \geq 0.02 \text{ (LHC)}, \quad 0.1 \text{ (Tevatron)}$$

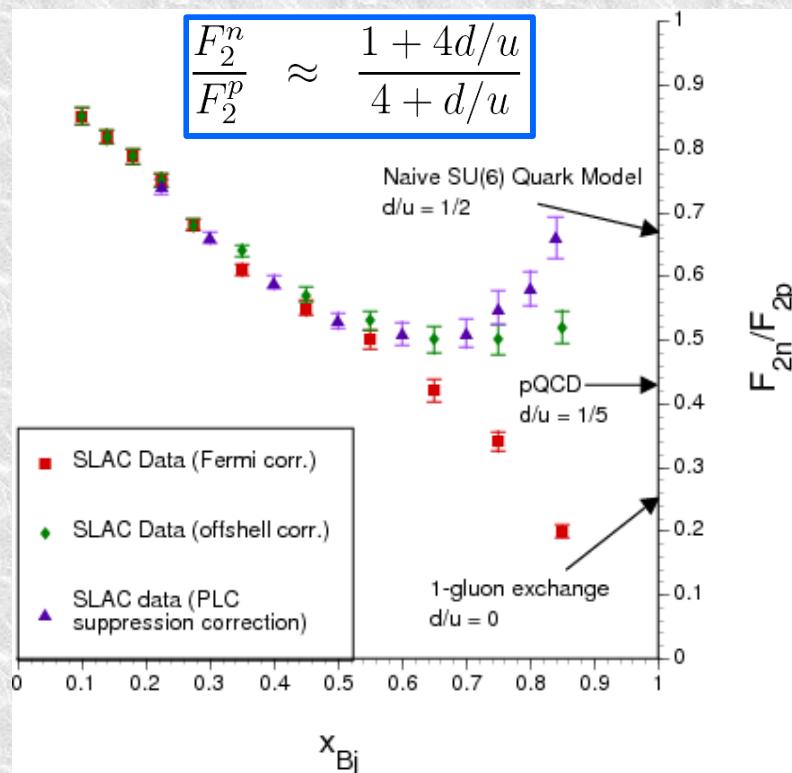
but recent work raises the bar:

$$M_{Z'} \gtrsim 900 \text{ MeV}$$



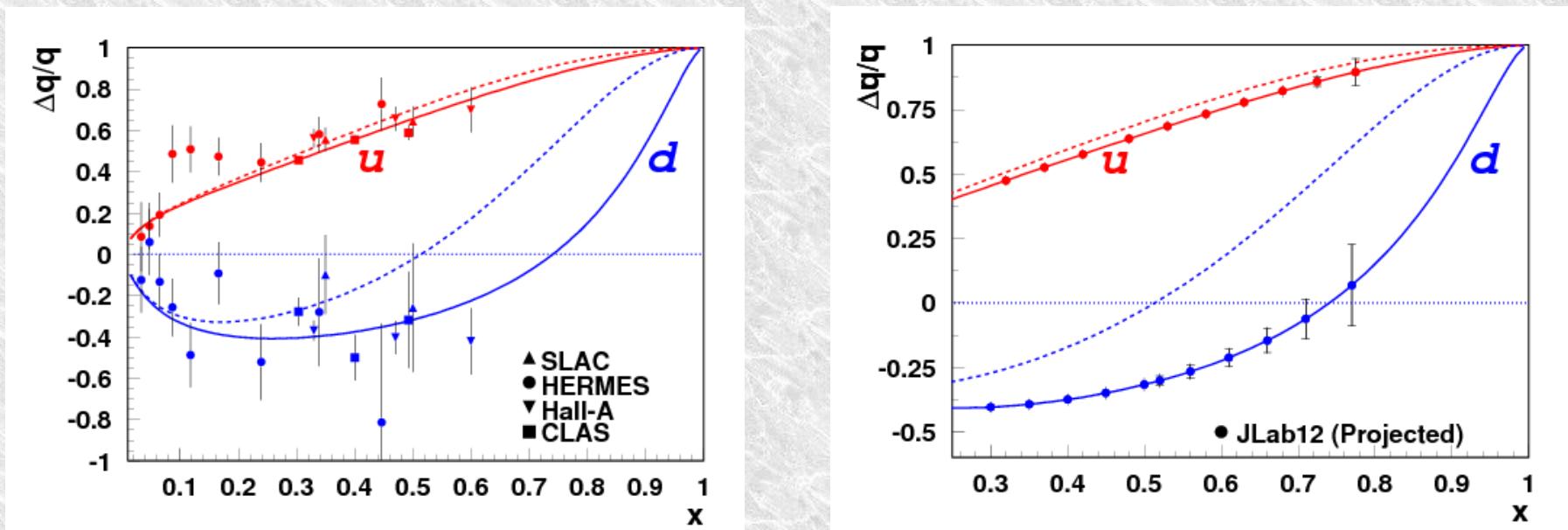
Why large x and low Q^2 ?

- Large uncertainties in quark and gluon PDF at $x > 0.5$
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 - at LHC, Tevatron
 - 1) New physics as excess in large p_T spectra \Leftrightarrow large x PDF
 - 2) QCD background in high-mass new physics searches
 - non-perturbative nucleon structure – e.g., d/u at $x \rightarrow 1$



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- ✚ Large uncertainties in quark and gluon PDF at $x > 0.5$
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 - ✚ at LHC, Tevatron
 - 1) New physics as excess in large p_T spectra \Leftrightarrow large x PDF
 - 2) QCD background in high-mass new physics searches
 - ✚ non-perturbative nucleon structure
 - ✚ spin structure of the nucleon *at small x* [see R.Seidl's talk]
 - ✚ neutrino oscillations

Why large x and low Q^2 ?

→ JLab and SLAC have precision DIS data at large x , BUT low Q^2

→ need of theoretical control over

- 1) higher twist $\propto \Lambda^2/Q^2$
 - 2) target mass corrections (TMC) $\propto x_B^{-2} m_N^{-2}/Q^2$
 - 3) heavy-quark mass corrections $\propto m_Q^{-2}/Q^2$
 - 4) nuclear corrections
- }
- this talk
-
- 5) jet mass corrections (JMC) $\propto m_j^{-2}/Q^2$
 - 6) large- x resummation
 - 7) large- x DGLAP evolution
 - 8) quark-hadron duality
 - 9) parton recombination at large x
 - 10) perturbative stability at low- Q^2
 - 11) ...

Up and down: the CTEQ6X fit

Accardi, Christy, Keppel, Melnitchouk, Monaghan, Morfín, Owens,
Phys. Rev. D 81, 034016 (2010)

CTEQ6X vs. CTEQ

- ◆ CTEQ

$$Q^2 \geq 4 \text{ GeV}^2 \quad W^2 \geq 12.25 \text{ GeV}^2$$

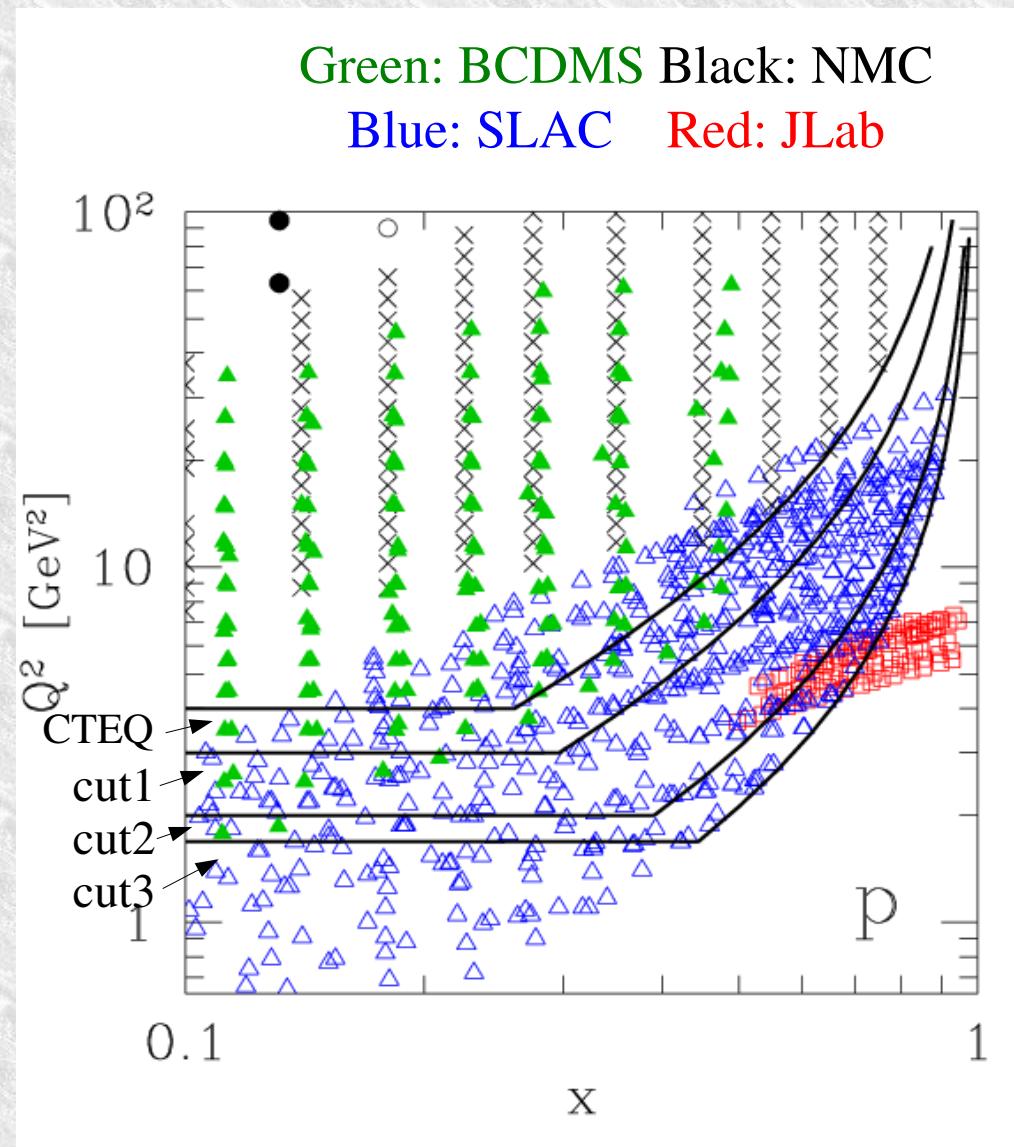
- + not so large x , not too low Q^2
- + hope $1/Q^2$ corrections not large

- ◆ CTEQ6X

- + TMC, HT, deuteron corrections
- + Progressively lower the cuts:

	Q^2 [GeV 2]	W^2 [GeV 2]
CTEQ \equiv cut0	4	12.25
cut1	3	8
cut2	2	4
cut3	1.69	3

- + Better large- x , low- Q^2 coverage



CTEQ6X vs. CTEQ

CTEQ

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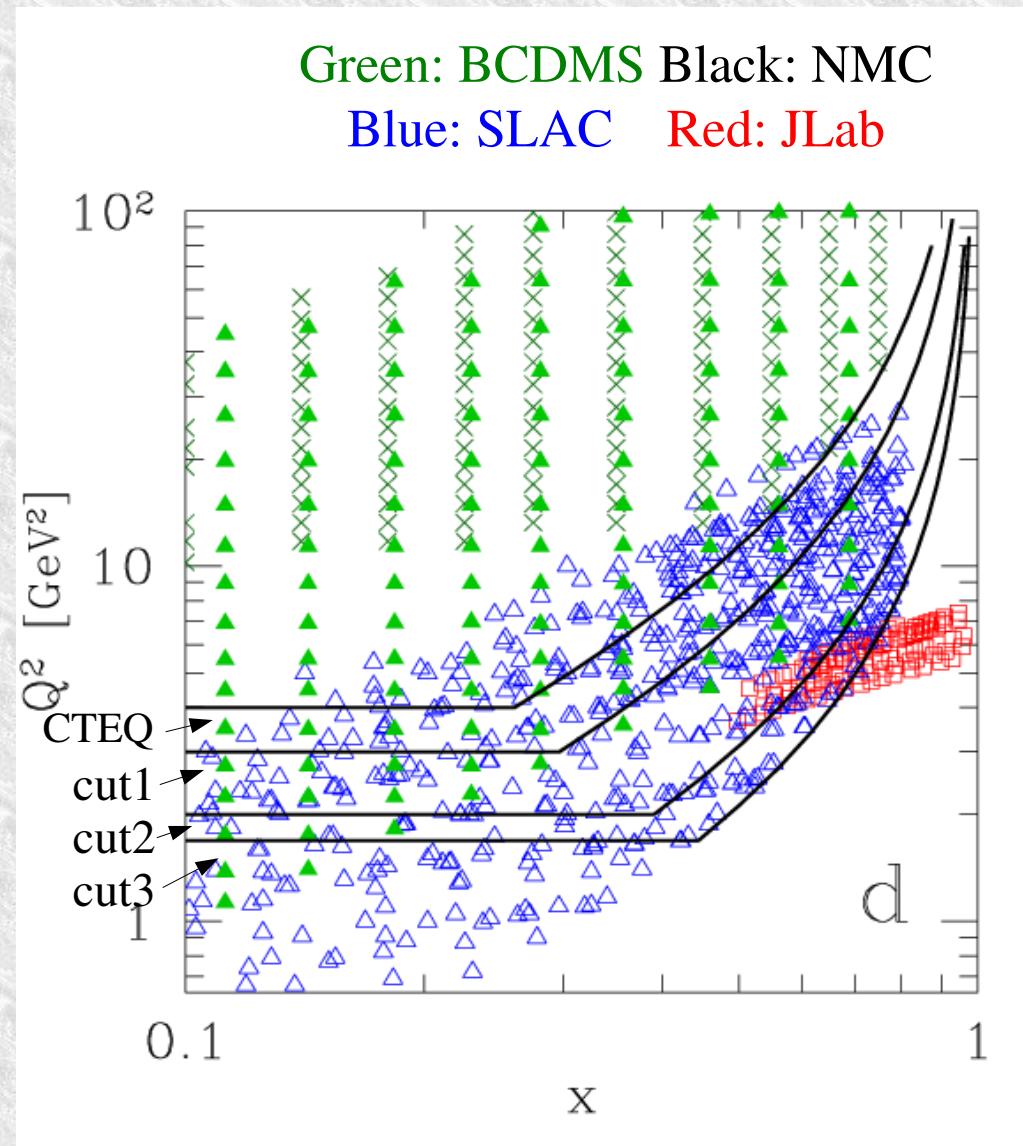
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CTEQ6X

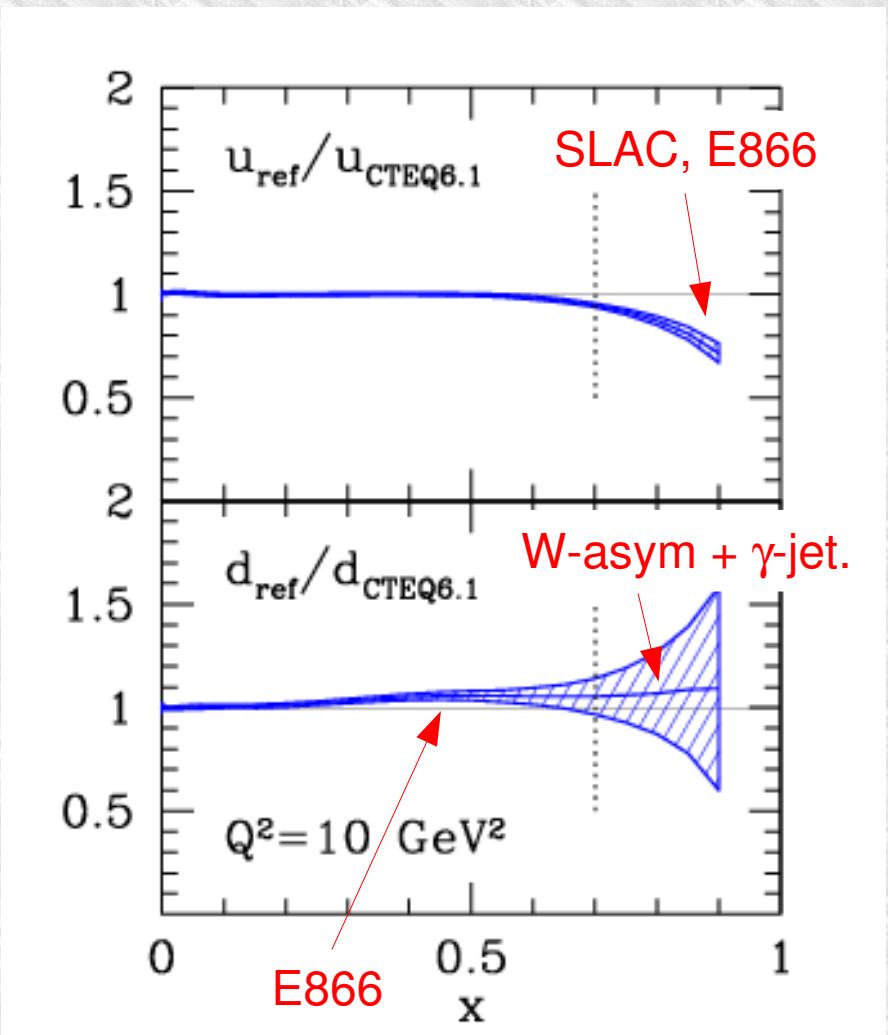
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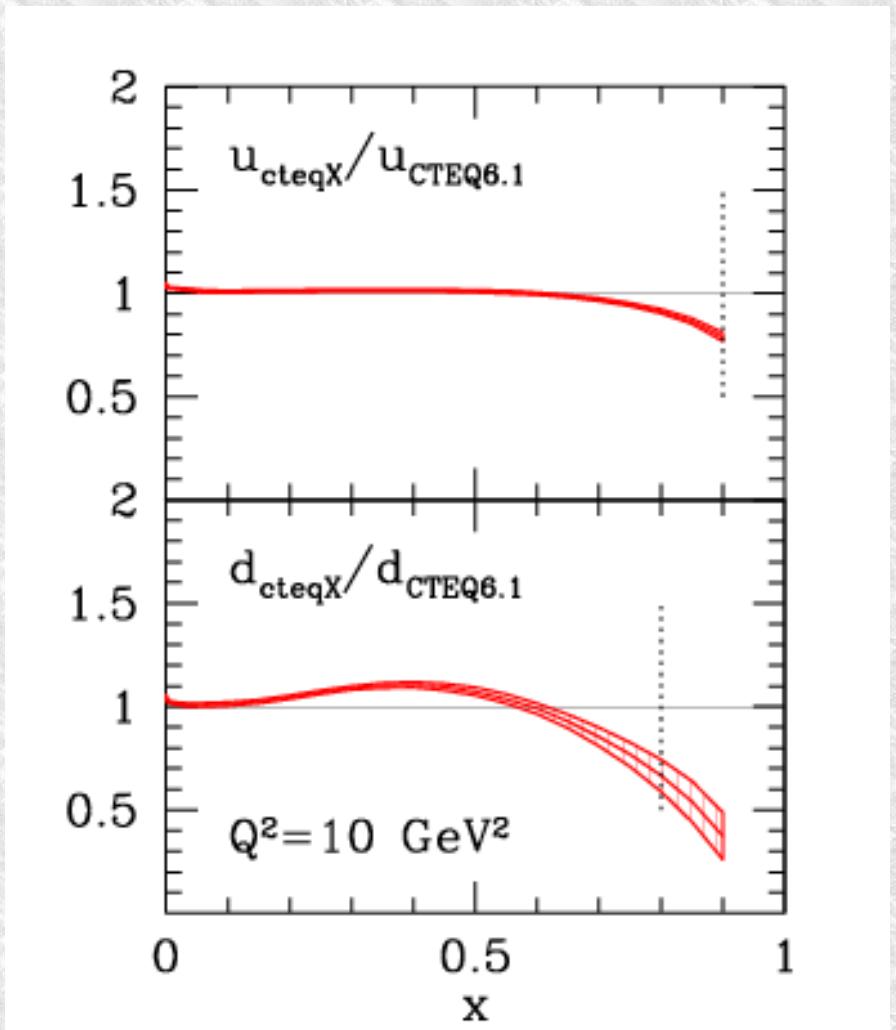
Reference fit vs. CTEQ6.1



- ◆ Reference fit:
 - ✚ cut0, no corrections
 - ✚ PDF errors with $\Delta\chi=1$

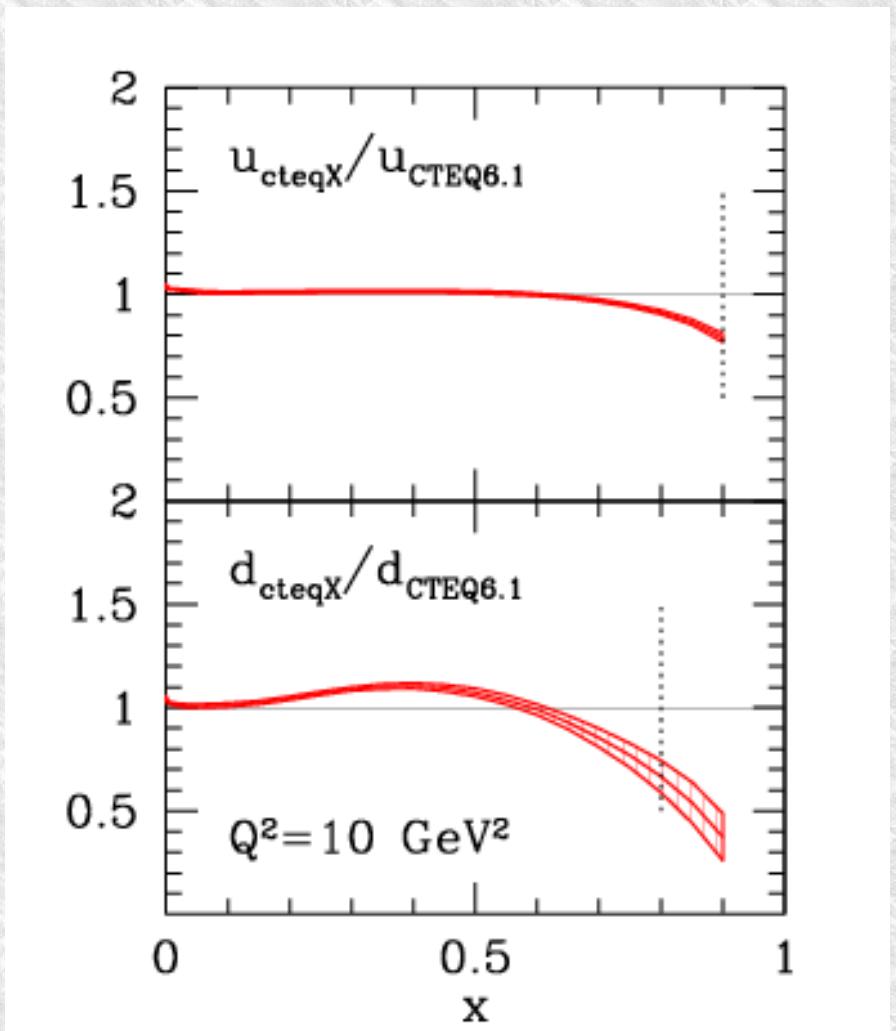
	data	CTEQ6.1
DIS	(JLab)	NO
	SLAC	NO
	NMC	✓
	BCDMS	✓
	H1	✓
	ZEUS	✓
DY	E605	✓
	E866	NO
W	CDF '98 (ℓ)	✓
	CDF '05 (ℓ)	NO
	D0 '08 (ℓ)	NO
	D0 '08 (e)	NO
	CDF '09 (W)	NO
jet	CDF	✓
	D0	✓
$\gamma+\text{jet}$	D0	NO

CTEQ6X vs CTEQ6.1



- ◆ CTEQ6X fit:
 - ✚ cut3, TMC+HT
 - ✚ deuteron corrections
- ◆ TMC, HT compensate each other
- ◆ u-quark:
 - ✚ almost unchanged
- ◆ d-quark suppressed
 - ✚ due to deuteron corrections
- ◆ Reduced PDF errors
 - ✚ about 30-50%

CTEQ6X vs CTEQ6.1



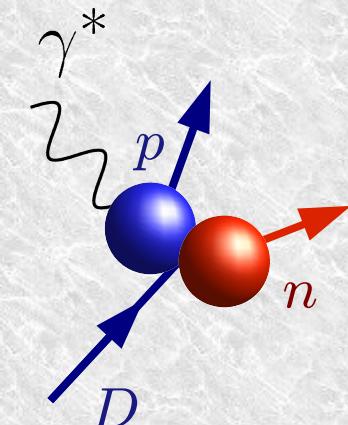
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- ◆ d-quark suppressed
 - + due to deuteron corrections
- ◆ Reduced PDF errors
 - + approx factor 2

Deuterium corrections

- ◆ Nuclear Smearing Model

[Kahn et al., PRC79(2009)
Accardi,Qiu,Vary, *in preparation*]

- ◆ nucleon Fermi motion and binding energy
- ◆ use non-relativistic deuteron wave-function
- ◆ **finite- Q^2 corrections** (very important!)

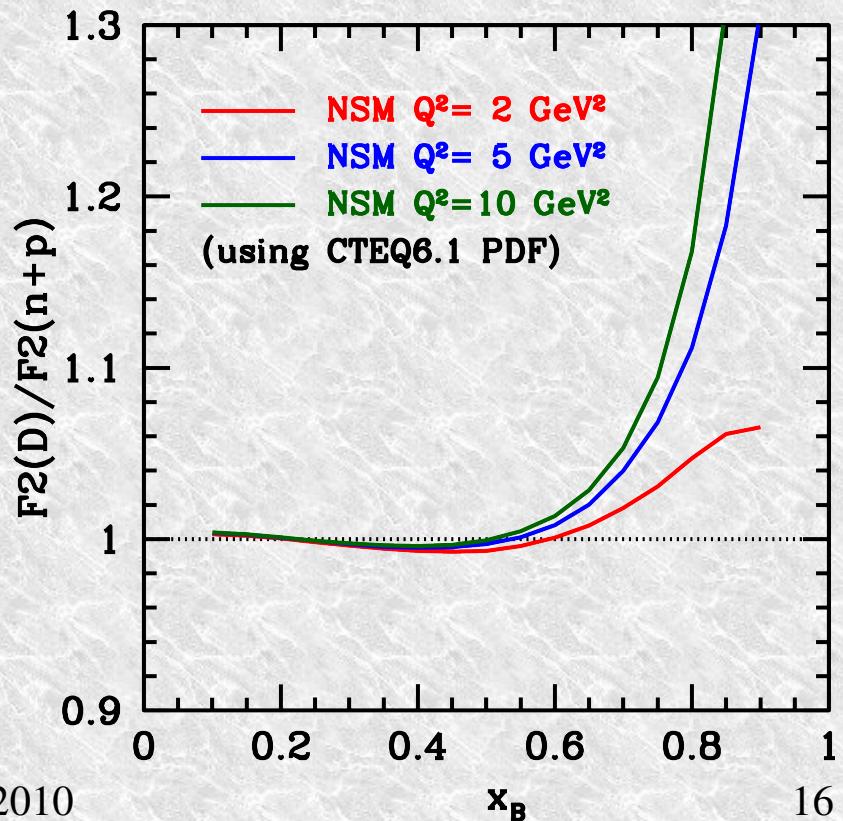


$$F_{2A}(x_B) = \int_{x_B}^A dy S_A(y, \gamma, x_B) F_2^{TMC}(x_B/y, Q^2)$$

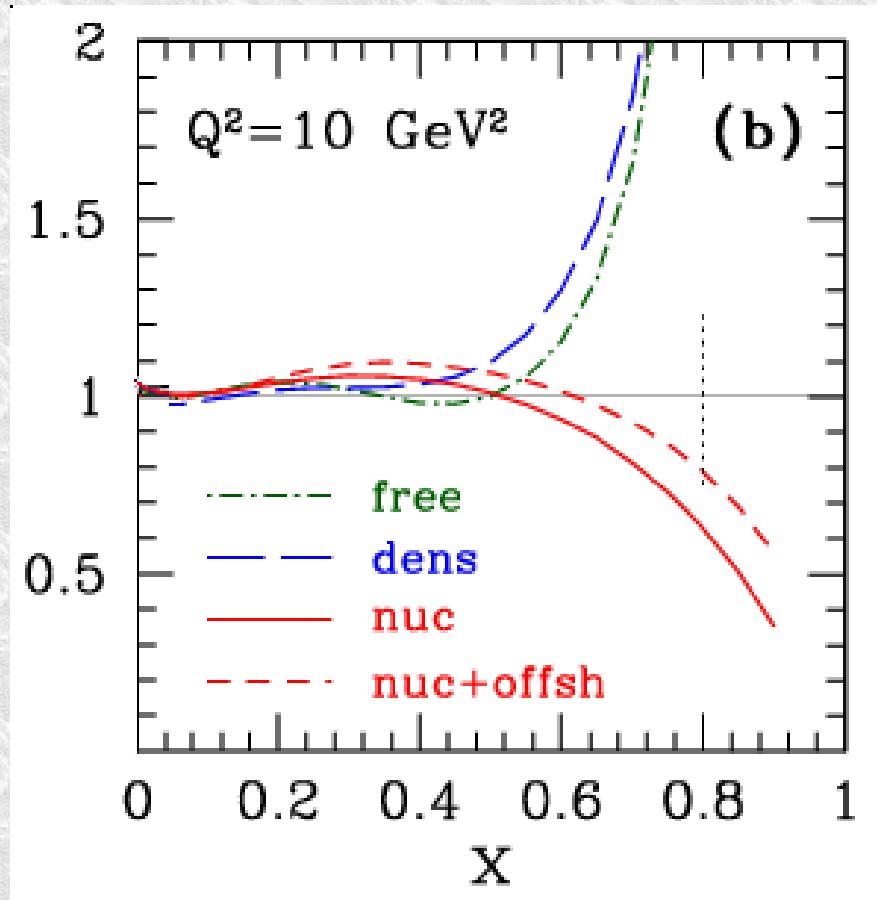
$$\gamma = \sqrt{1 + 4x_B^2 m_N^2 / Q^2}$$

$$\frac{x_B}{y} = -\frac{q^2}{2p_N \cdot q}$$

- ◆ off-shell effects can be included in S_A



Deuterium corrections



- ◆ d -quarks are very sensitive to deuterium corrections
- ◆ Off-shell corrections completely absorbed by the d -quark

free = free p+n
dens = density model corrections
nuc = WBA smearing model
offsh = off-shell corrections

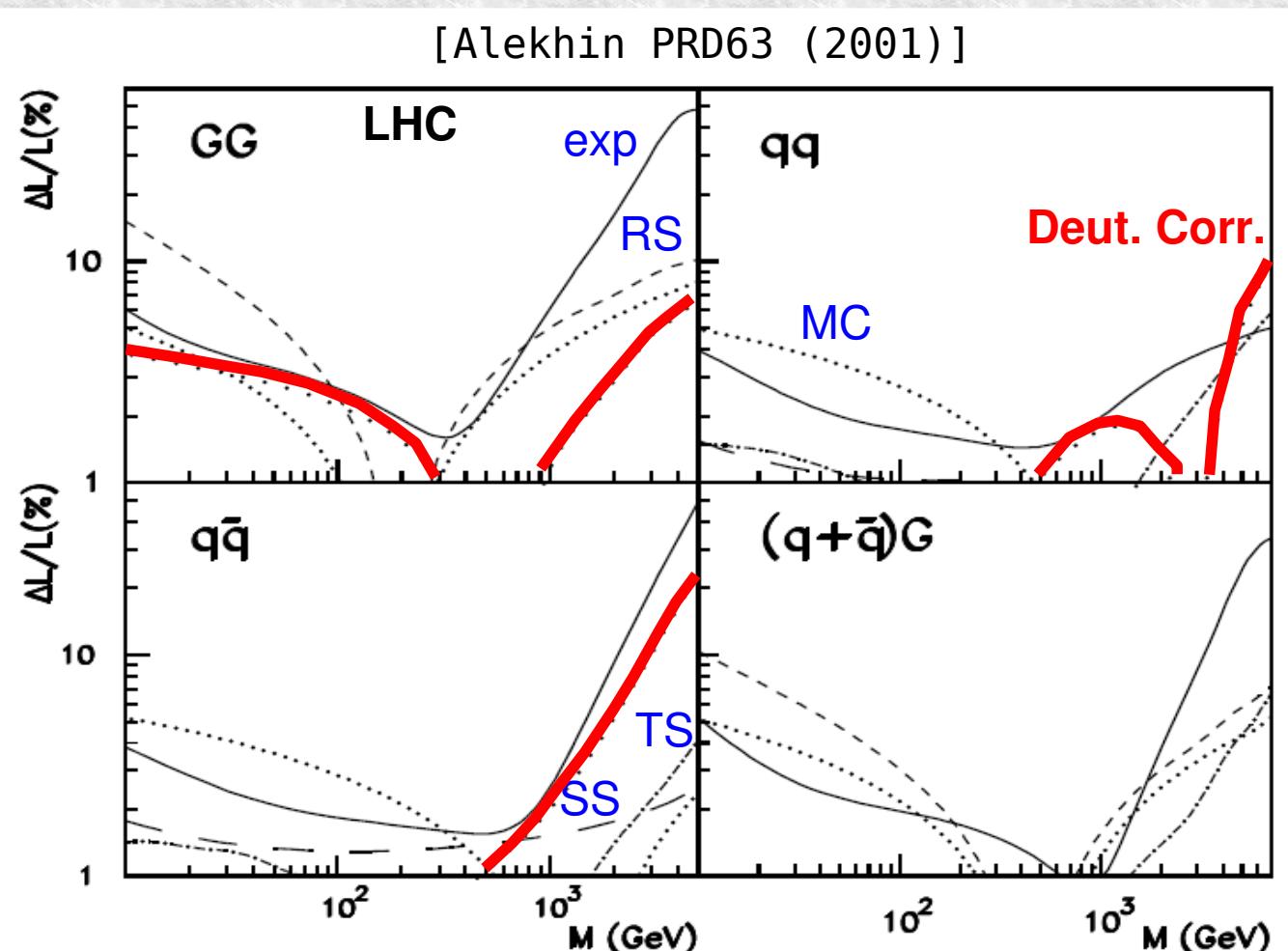
[Melnitchouk et al., '94]

Impact on LHC

- Parton luminosities

$$L_{i,j}(M) = \frac{1}{S} \int_{M^2/s}^1 \frac{dx}{x} q_i(x, M^2) q_j(M^2/(xs), M^2)$$

- Nuclear model uncertainty $\sim 10\%$ at large x :
 - dominates Z cross-sections used as luminosity monitor



d-quarks at large x

- ◆ Large theoretical uncertainties on d -quark at large x
 - ◆ coming from deuteron corrections
(no deuteron $\Rightarrow d$ unconstrained at large x)
 - ◆ unavoidable at the moment: model dependent
- ◆ How to progress?
 - ◆ Avoid them
 - Free nucleon targets \hookrightarrow not enough data so far
 - ◆ Constrain them
 - Q^2 dependence of D/p ratios at large x
 - Use quasi-free nucleon targets
 - Use ratio of ${}^3\text{He}$ - ${}^3\text{H}$ mirror nuclei

Free nucleon targets

- ◆ Constraints on large- x d -quarks from

- ◆ $p+p(\bar{p})$: DY at large x_F

$$pp(\bar{p}) \longrightarrow \mu^+ \mu^- X$$

- ◆ $p+p(\bar{p})$: W-asymmetry at large rapidity [D0 and ZEUS]

$$pp(\bar{p}) \longrightarrow W^\pm X$$

- ◆ $\nu+p$ and $\nu\bar{p}+p$

- WA21 already has data
(but hard to reconstruct cross-sections
from published “quark distributions”)
 - MINERvA with a hydrogen target

$$\nu(\bar{\nu}) p \longrightarrow l^\pm X$$

- ◆ Parity Violating DIS *

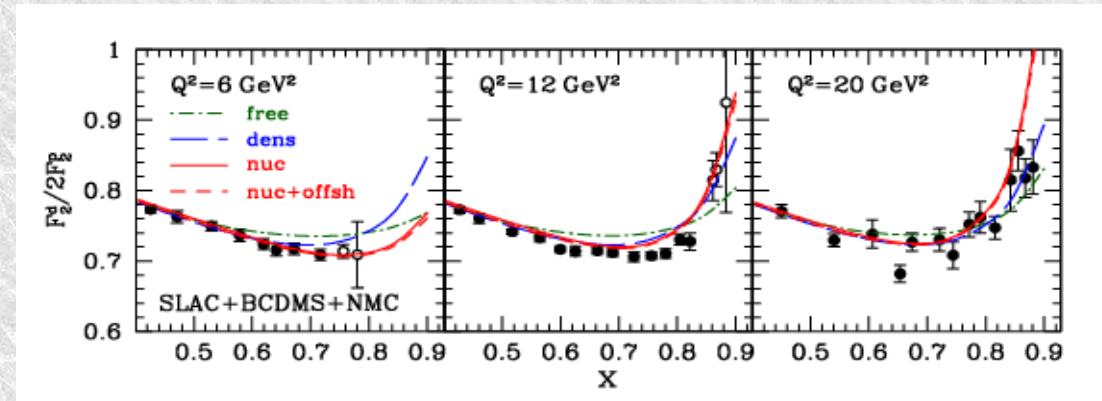
- L/R electron asymmetry $\Rightarrow \gamma/Z$ interference $\propto d/u$

$$\vec{e}_L(\vec{e}_R) p \longrightarrow e X$$

* planned for Jlab at 12 GeV

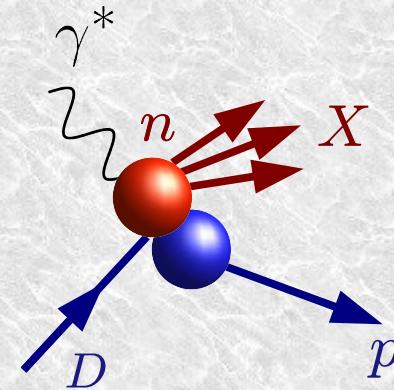
Constraining the nuclear corrections

- ◆ Q^2 dependence of D/p ratios at large x



- ◆ Quasi-free nucleon targets ^{*}
[BONUS, E94-102 and EG6 at JLab 6 GeV]

$$e A \rightarrow e (A - 1) X$$



- ◆ ${}^3\text{He} - {}^3\text{H}$ mirror nuclei ^{*}

$$\frac{{}^3\text{H}}{{}^3\text{He}} \approx \frac{n}{p} \frac{2 + p/n}{2 + n/p}$$

^{*} planned for Jlab at 12 GeV

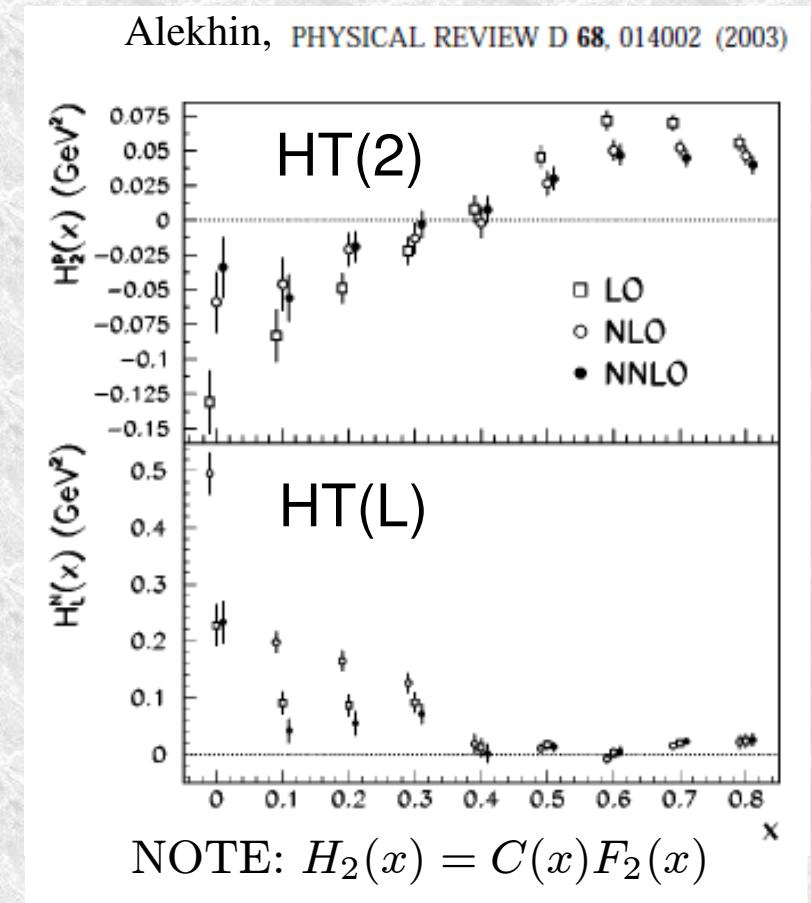
Gluons

Observables for gluons

- ◆ Jets in $p+p$ collision – CT09
 - ✚ limited statistics
 - ✚ only very large Q^2 , and smallish x
- ◆ $dF_2 / d(\ln Q^2)$
 - ✚ indirect
 - ✚ little leverage at large x , large errors
- ◆ Longitudinal F_L
 - ✚ directly sensitive to gluons
 - ✚ so far not many data points
 - ✚ JLab / JLab12 will improve large- x coverage, but low Q^2

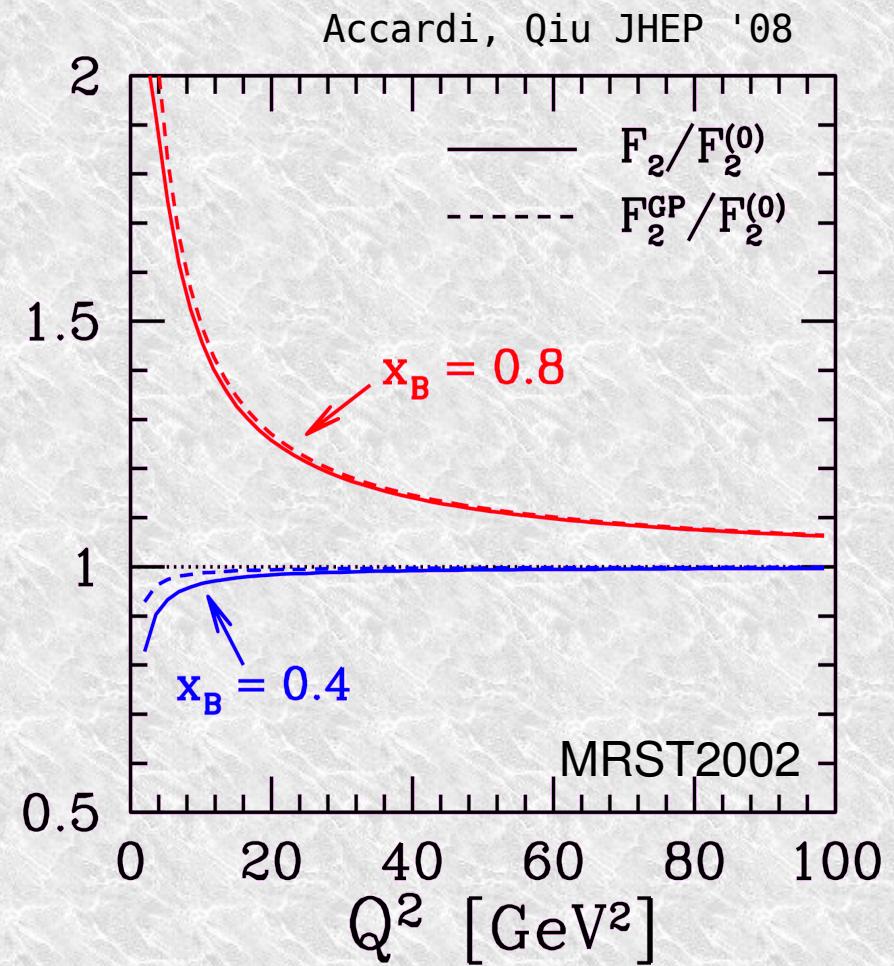
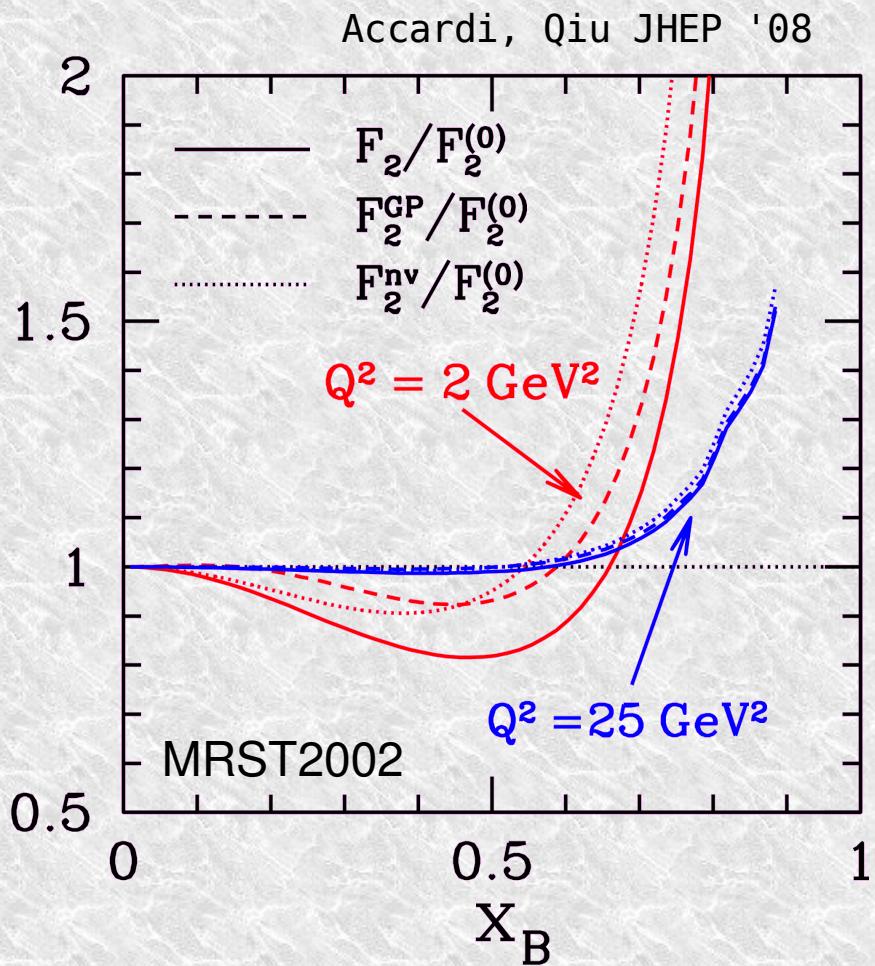
F_L – HT and perturbative stability

- HT for F_L have little constraints from theory, some guidance from renormalon calculations
 - Perturbatively unclear at large x
 - When fitted, large at NLO, decrease at NNLO
- “The high x and low Q^2 domain is ‘dangerous’. This is another reason, along with target mass, to avoid fitting data in this region”*
[Martin, Stirling, Thorne, PLB635(06)]
- Should we dare more?
[see e.g., Alekhin et al., arXiv:0710.0124]



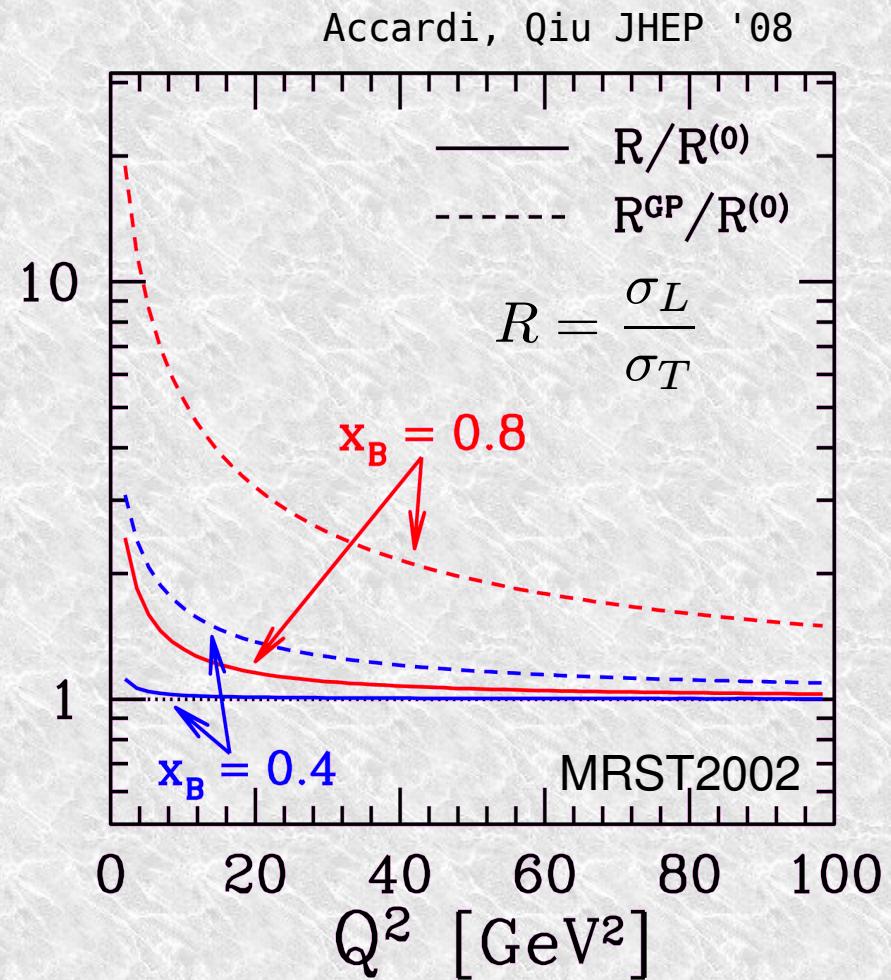
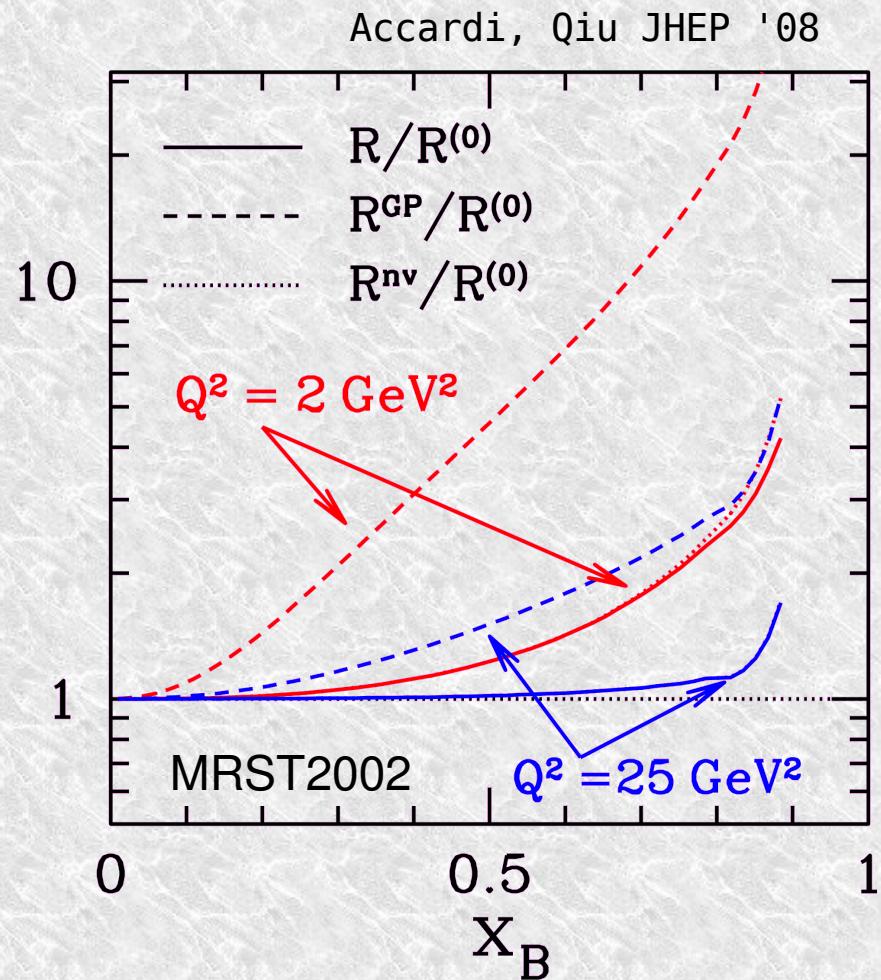
Target Mass Corrections

- ◆ Difference between Coll. Fact. [Accardi,Qiu] and OPE [Georgi,Politzer] for F_2
- ◆ different slope in $Q^2 \Rightarrow$ different gluons from $dF_2/d(\ln Q^2)$!



Target Mass Corrections

- ◆ Very different F_L correction
- ◆ Can the differences be absorbed in HT terms ?
- ◆ Play F_L and F_2 off each other \Rightarrow can differentiate TMC method ??



Intrinsic charm

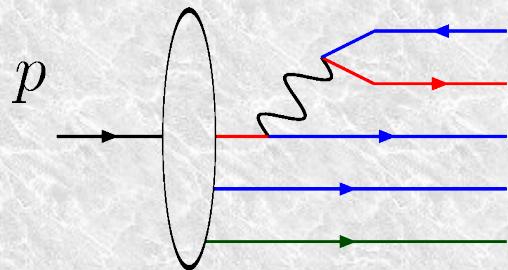
Intrinsic vs. radiative charm

- Usual assumption in global fits: at threshold

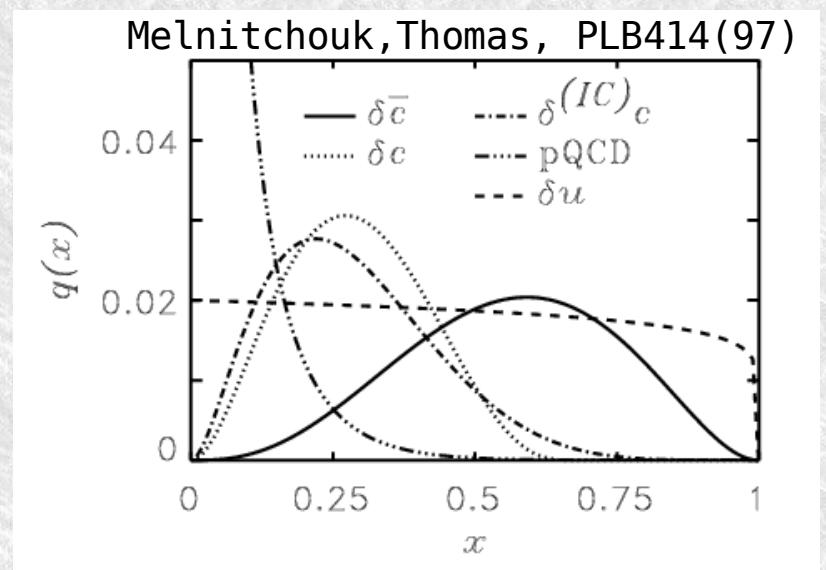
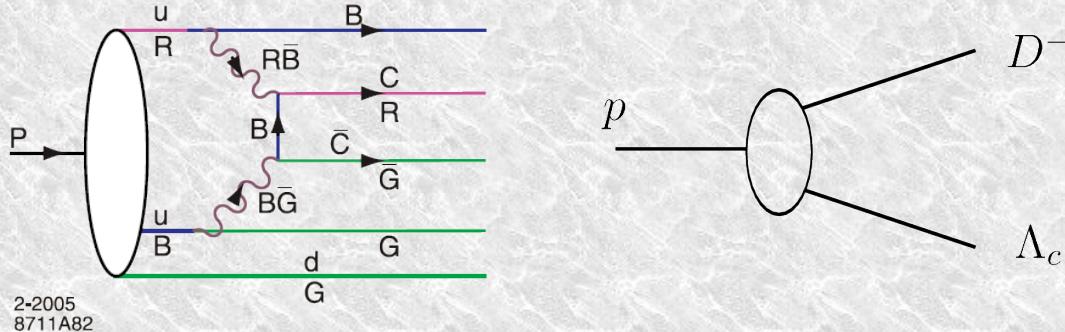
$$c(x, Q_c \approx m_c) = 0$$

Pumplin, PRD73(06),
Brodsky et al., PRD73(06)
+ references therein

- charm generated during DGLAP evolution



- but QCD predicts intrinsic charm



- a c - \bar{c} pair fluctuation already exists, peaked at large $x \sim 0.4$
- fully participates in DGLAP evolution
- $c, c\bar{c}$ asymmetry: small @ NLO (pQCD) or large (nonpert. models)

Indications from global fits

[Pumplin, Lai, Tung, PRD75(07)]

- 3 models at $\mu = m_c$
[see Pumplin PRD 73(06) for review of models]

- 1) Brodsky-Hoyer-Peterson-Sakai [PLB 93 (80)]

$$\begin{aligned} c(x) &= \bar{c}(x) \\ &= A x^2 [6x(1+x) \ln x + (1-x)(1+10x+x^2)] \end{aligned}$$

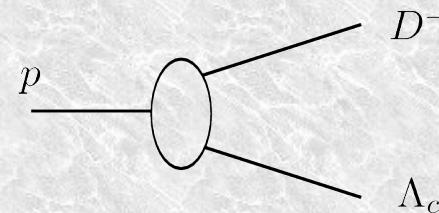
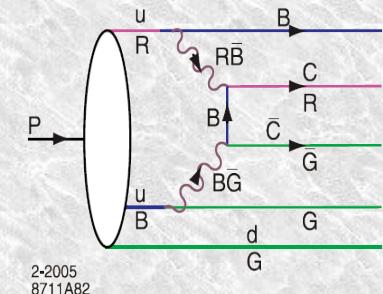
- 2) meson-cloud model

[Navarra et al '96, '98;
Melnitchouk, Steffens, Thomas '97, '99]

$$\begin{aligned} c(x) &= Ax^{1.897}(1-x)^{6.095} \\ \bar{c}(x) &= \bar{A}x^{2.511}(1-x)^{4.929} \end{aligned}$$

- 3) phenomenological “sea-like”

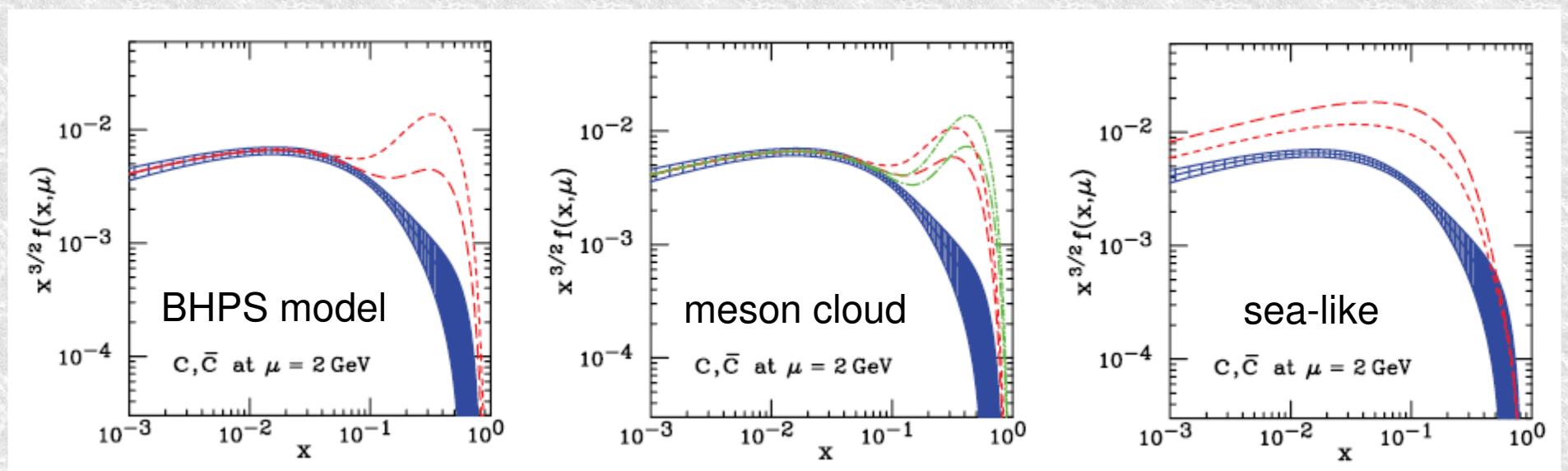
$$c(x) = \bar{c}(x) \propto \bar{d}(x) + \bar{u}(x)$$



Indications from global fits

[Pumplin, Lai, Tung, PRD75(07)]

- All models allow IC = 0-3% intrinsic charm
 - Evolution redistributes IC to lower x , but large- x peak persists
 - sea-like spread out over x

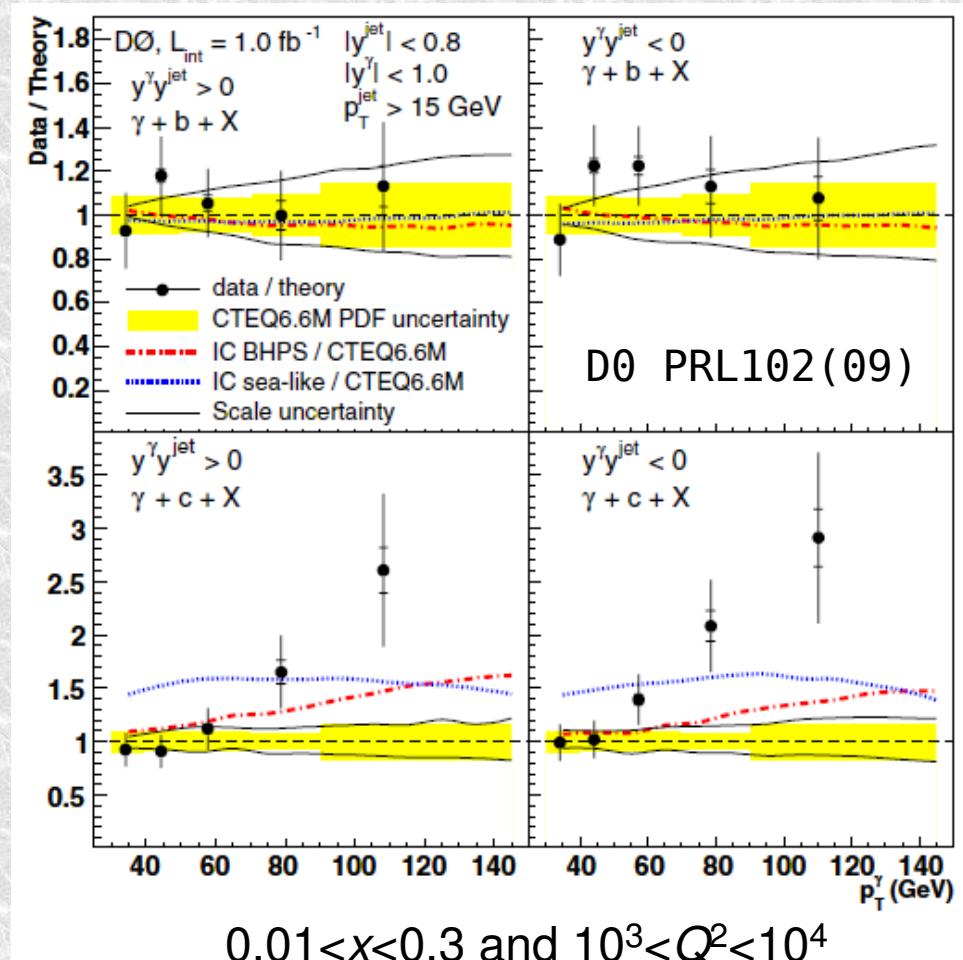
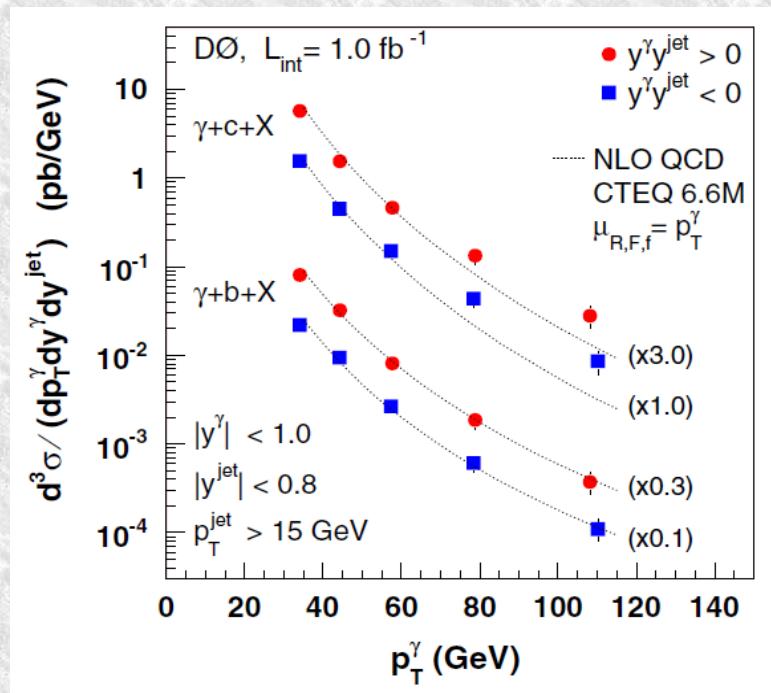


Experimental evidence - D0

- D0 measured excess of $\gamma + \text{charm}$ jets compared CTEQ6.6 [D0, PRL102(09)]

$$g + Q \rightarrow \gamma/Z + Q$$

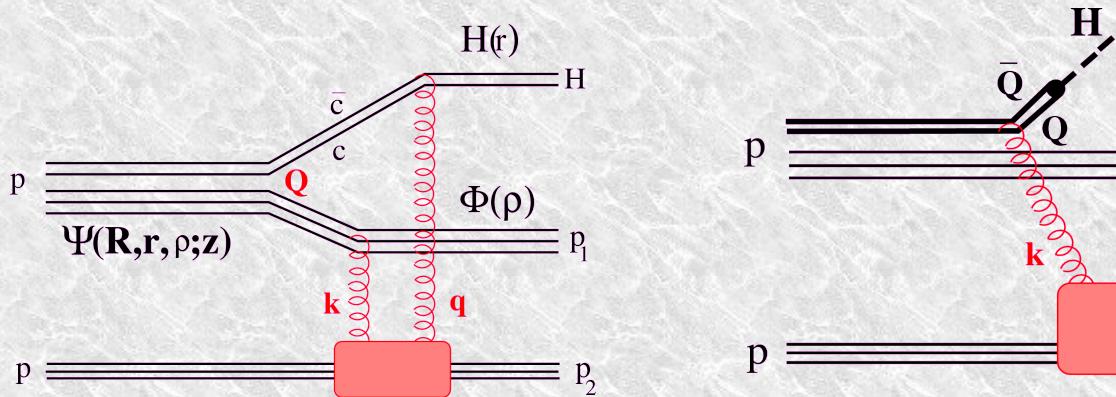
$$q + \bar{q} \rightarrow \gamma/Z + g \rightarrow \gamma/Z + Q\bar{Q}$$



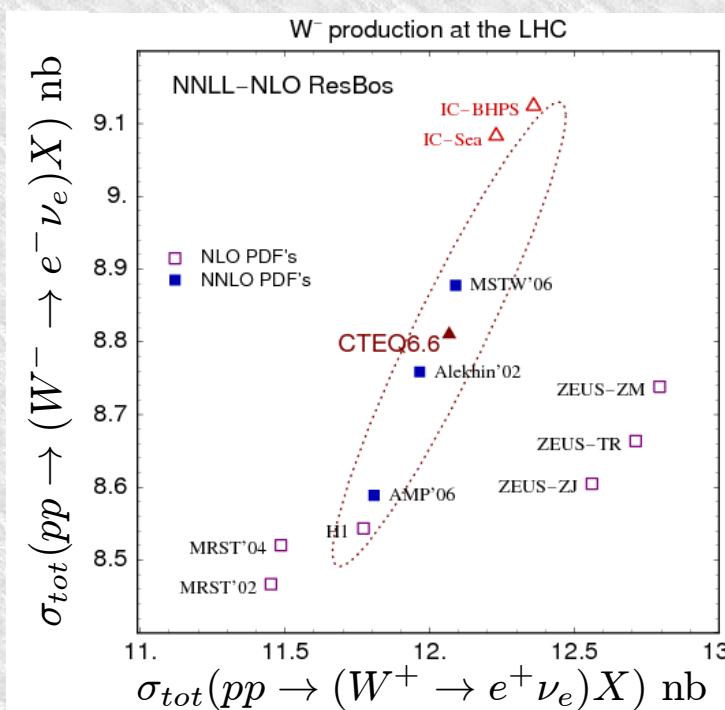
- Difference due to
 - intrinsic charm?
 - underestimate of $g \rightarrow c\bar{c}$?

Phenomenological implications

- ◆ SM and beyond at Tevatron and LHC
- ◆ Higgs and single top production sensitive to heavy quarks
- ◆ Novel Higgs production mechanisms at large $x_F \approx 0.7\text{-}0.9$ [Brodsky et al. PRD73(06), NPB907(09)]



- ◆ W production



[Nadolsky et al. PRD78(08)]

How to measure – hadronic collisions

→ $\gamma/Z + \text{charm jet}$

- sensitive to $g + Q \rightarrow \gamma/Z + Q$ and $q + \bar{q} \rightarrow \gamma/Z + g \rightarrow \gamma/Z + Q\bar{Q}$
- $y_\gamma y_{jet} > 0$ and $y_\gamma y_{jet} < 0$ sensitive to different x_1, x_2
- allows constraints on Q , $Q\bar{q}$, and gluons
- angular dependence to distinguish above sub-processes

→ Also,

- High x_F $pp \rightarrow J/\psi X$
- High x_F $pp \rightarrow J/\psi J/\psi X$
- High x_F $pp \rightarrow \Lambda_c X$
- High x_F $pp \rightarrow \Lambda_b X$
- High x_F $pp \rightarrow \Xi(ccd)X$ (SELEX)

How to measure – DIS

- ◆ HERA charm and bottom events
 - already included in the fits
 - most data at small x , where $\gamma g \rightarrow c\bar{c}$ dominates over $\gamma c \rightarrow cX$
 - needs larger x
- ◆ F_L/F_2 ratio [Ivanov, NPB814(09)]
- ◆ JLAB 6/12
 - Ideally placed across the charm threshold
 - D+ vs. D- sensitive to c/cbar asymmetry
- ◆ EIC (LHeC ??)
 - jet measurements are possible
 - larger Q^2 range

Target and heavy-quark mass corrections

- DIS in collinear factorization: [Accardi, Qiu JHEP '08]

$$F_{T,L}(x_B, Q^2, m_N) = \sum_f \int_{x_f^{min}}^{x_f^{max}} \frac{dx}{x} h_{T,L}^f\left(\frac{\xi_f}{x}, Q^2\right) \varphi_f(x, Q^2)$$

f parton mass Nachtmann variable

$$\xi_f = \xi \left[1 - \frac{\xi^2}{x^2} \frac{m_f^2}{Q^2} \right]^{-1} \xrightarrow[m_f \rightarrow 0]{ } \xi \quad \xrightarrow[M_N \rightarrow 0]{ } x_B$$

$$x_f^{min} = \xi \frac{Q^2 + (c-1)m_f^2 + \Delta[m_f^2, -Q^2, cm_f^2]}{2Q^2} \quad \xrightarrow[m_f \rightarrow 0]{ } \xi \quad \xrightarrow[M_N \rightarrow 0]{ } x_B$$

$$x_f^{max} = \xi \frac{Q^2/x_B + 3m_f^2 + \Delta[m_f^2, -Q^2, Q^2(1/x_B - 1)]}{2Q^2} \quad \xrightarrow[m_f \rightarrow 0]{ } \xi/x_B \quad \xrightarrow[M_N \rightarrow 0]{ } 1$$

$$\Delta[a, b, c] = \sqrt{a^2 + b^2 + c^2 - 2(ab + bc + ca)} \quad \xi = 2x_B / (1 + \sqrt{1 + 4x_B^2 M_N^2 / Q^2})$$

Conclusions

★ Flavor separation at large x important

- to understand the nucleon structure
- for phenomenological applications

★ but needs theoretical corrections

- target/quark mass, HT, nuclear corrections, ...

★ u, d quarks

- CTEQ6X reveals d-quark suppression compared to CTEQ / MRST fits
- Essential to control nuclear corrections, or use free nucleon target

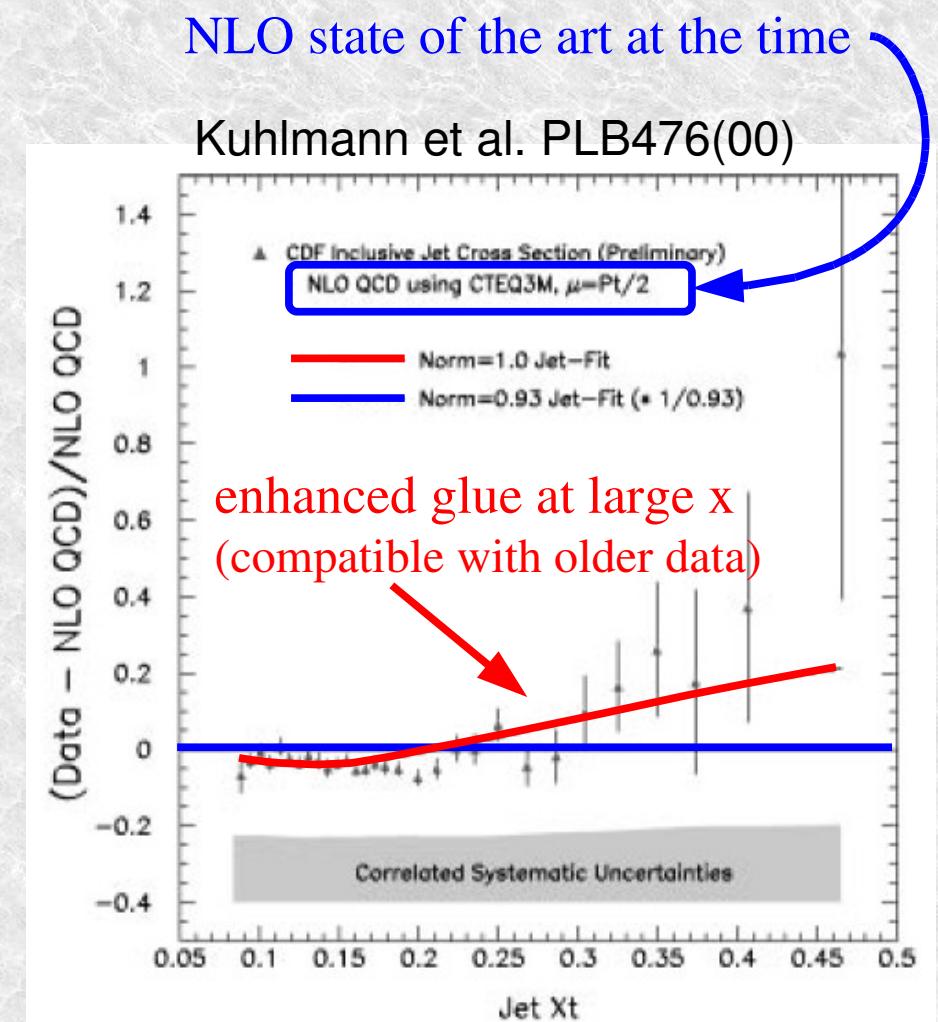
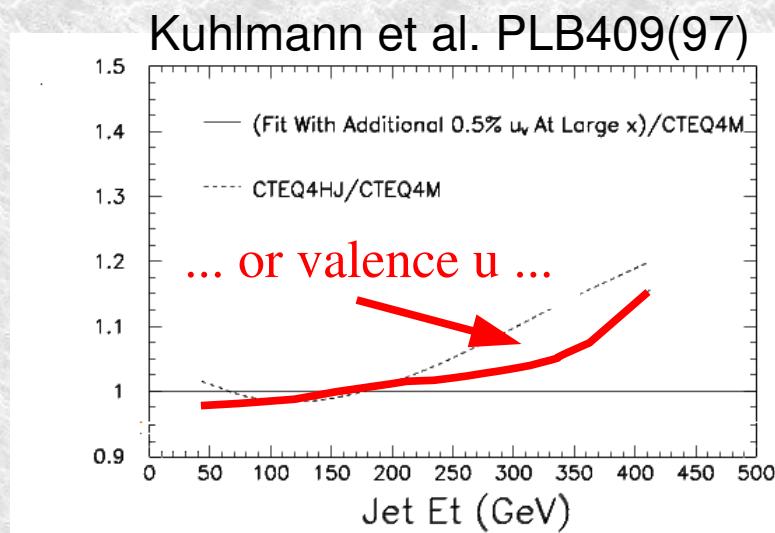
★ Gluons: will be included in the CTEQ6X global fit

★ Intrinsic charm: interesting direction for the future

BACKUP SLIDES

Why large x_B and low Q^2 ?

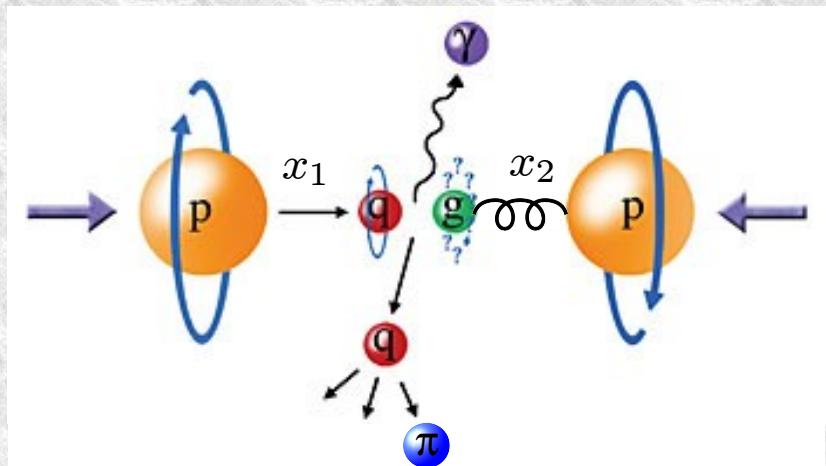
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- ✚ Precise PDF at large x are needed, e.g.,
 - ✚ at LHC, Tevatron
 - 1) DGLAP evolution feeds large x , low Q^2 into lower x , large Q^2
 - 2) New physics as excess in large- p_T spectra \Leftrightarrow large x PDF
- ✚ Example 2: 1996 CDF p_T excess



Why large x_B and low Q^2 ?

- Large uncertainties in quark and gluon PDF at $x > 0.5$
- Precise PDF at large x are needed, e.g.,
 - at LHC, Tevatron
 - New physics as excess in large p_T spectra \Leftrightarrow large x PDF
 - DGLAP evolution feeds large x , low Q^2 into lower x , large Q^2
 - non-perturbative nucleon structure
 - spin structure of the nucleon – most spin at large- x , but also, e.g.,

$$\sigma(p\vec{p} \rightarrow \pi^0 X) \propto \Delta q(x_1) \Delta g(x_2) \hat{\sigma}^{qg \rightarrow qg} \otimes D_q^{\pi^0}(z)$$

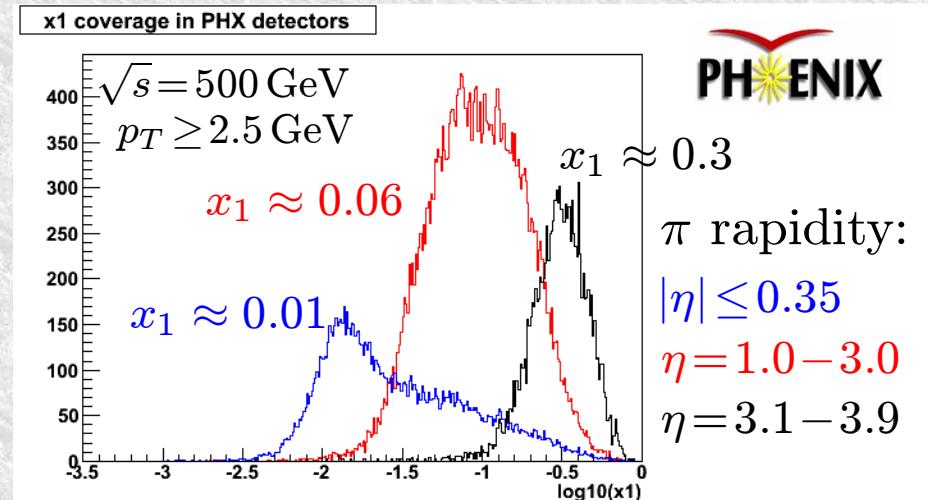
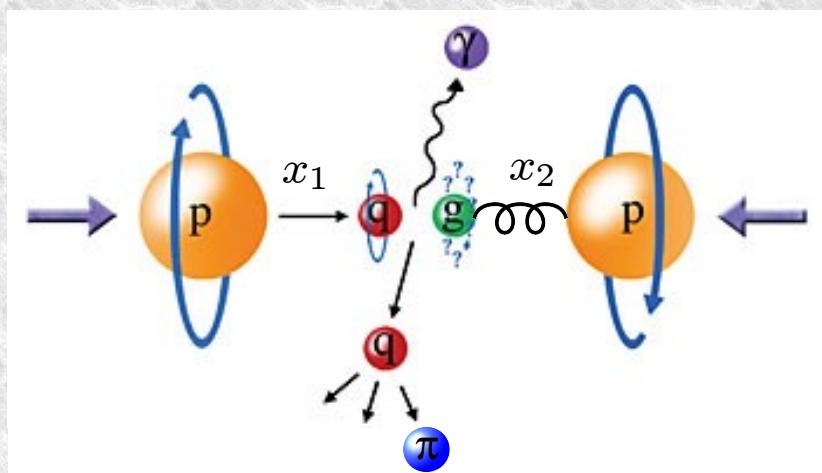


$$x_1 \sim \frac{p_T}{\sqrt{s}} e^y$$
$$x_2 \sim \frac{p_T}{\sqrt{s}} e^{-y}$$

Why large x and low Q^2 ?

- ✚ Large uncertainties in quark and gluon PDF at $x > 0.5$
- ✚ Precise PDF at large x are needed, e.g.,
 - ✚ at LHC, Tevatron
 - 1) New physics as excess in large p_T spectra \Leftrightarrow large x PDF
 - 2) DGLAP evolution feeds large x , low Q^2 into lower x , large Q^2
 - ✚ non-perturbative nucleon structure
 - ✚ spin structure at small x

$$\sigma(p\vec{p} \rightarrow \pi^0 X) \propto \Delta q(x_1) \Delta g(x_2) \hat{\sigma}^{qg \rightarrow qg} \otimes D_q^{\pi^0}(z)$$



Target mass corrections

- ✚ Nachtmann variable: $\xi = \frac{2x_B}{1 + \sqrt{1 + 4x_B^2 m_N^2 / Q^2}} < 1$ at $x_B = 1$
- ✚ Standard Georgi-Politzer (OPE)
[Georgi, Politzer 1976; see review by Schienbein et al. 2007]
 - ✚ leads to non-zero structure functions at $x_B > 1$ (!)
- ✚ Collinear factorization [Accardi, Qiu, JHEP 2008; Accardi, Melnitchouk 2008]
Structure fns as convolutions of parton level structure fns and PDF

$$F_{T,L}(x_B, Q^2, m_N) = \sum_f \int_\xi \frac{\xi}{x_B} \frac{dx}{x} h_{T,L}^f\left(\frac{\xi}{x}, Q^2\right) \varphi_f(x, Q^2)$$

- ✚ respects kinematic boundaries
- ✚ ξ -scaling, uses $x_{\max} = 1$ [Aivazis et al '94; Kretzer,Reno '02]

$$F_{T,L}^{nv}(x_B, Q^2, m_N) \equiv F_T^{(0)}(\xi, Q^2)$$

- ✚ leads to non-zero structure functions at $x_B > 1$ (!)

“Higher-Twists” parametrization

- Parametrize by a multiplicative factor:

$$F_2(\text{data}) = F_2(\text{TMC}) \times \left(1 + \frac{C(x_B)}{Q^2}\right)$$

with

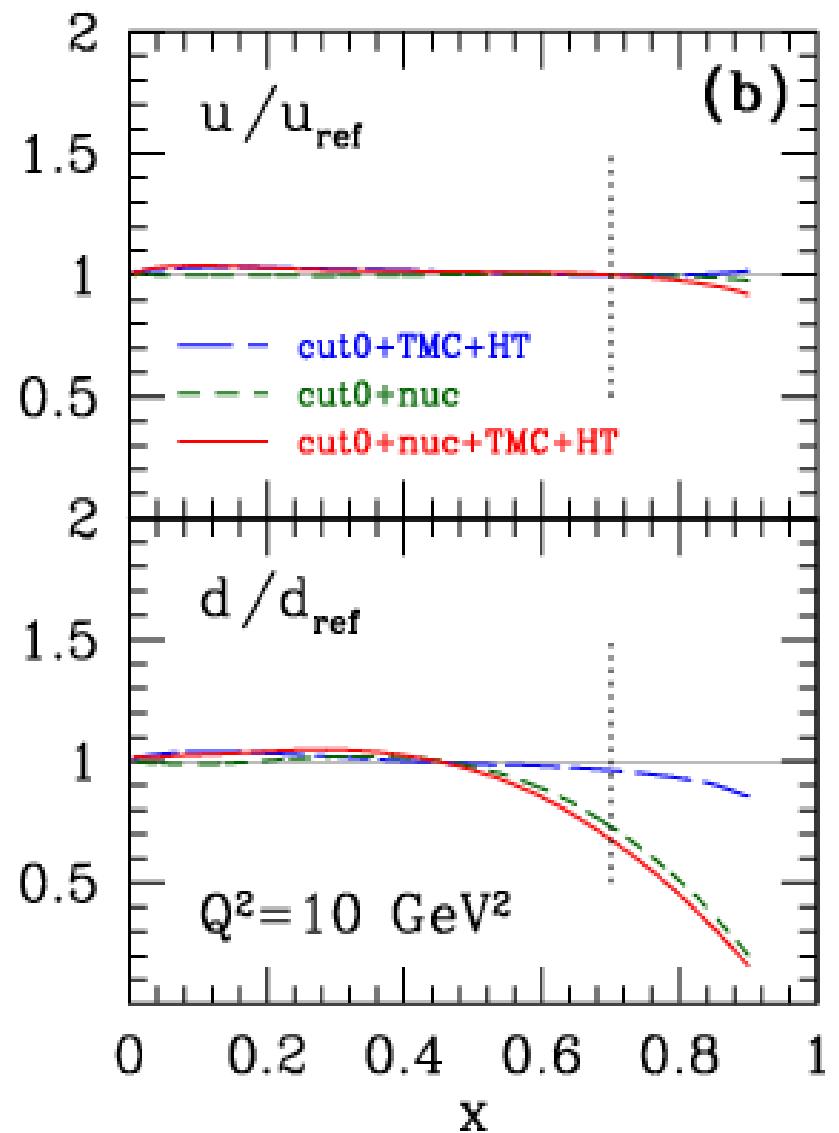
$$C(x_B) = a x^b (1 + c x)$$

- parametrization is sufficiently flexible to give good fits to data
- c parameter allows negative HT at small x_B

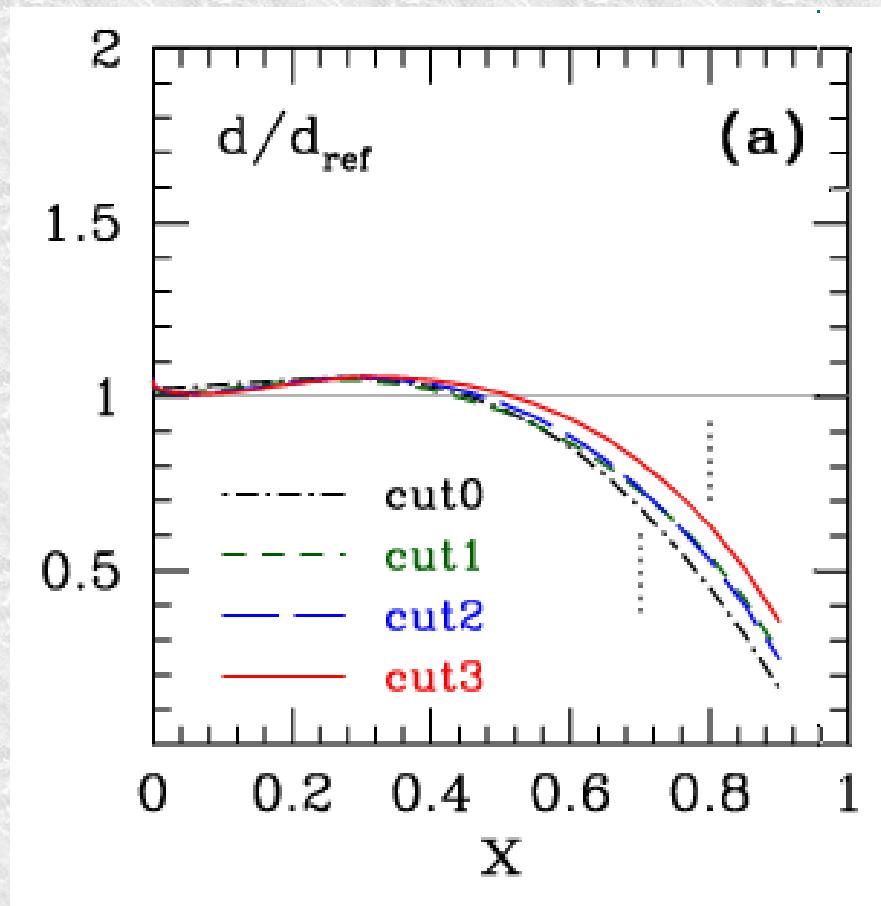
- Important:** $C(x_B)$ includes
 - dynamical higher-twists (parton correlations)
 - all uncontrolled power corrections, e.g.,
 - ✓ TMC model uncertainty, Jet Mass Corrections
 - ✓ NNLO corrections (power-like at small Q)

Effects of corrections on reference fit

- Apply the theoretical corrections one at a time
- 2 important lessons:
 - cut0 removes TMC+HT (as desired)**
 - nuclear corrections are large starting from $x > 0.5$!!**
("safe cuts" aren't safe everywhere)

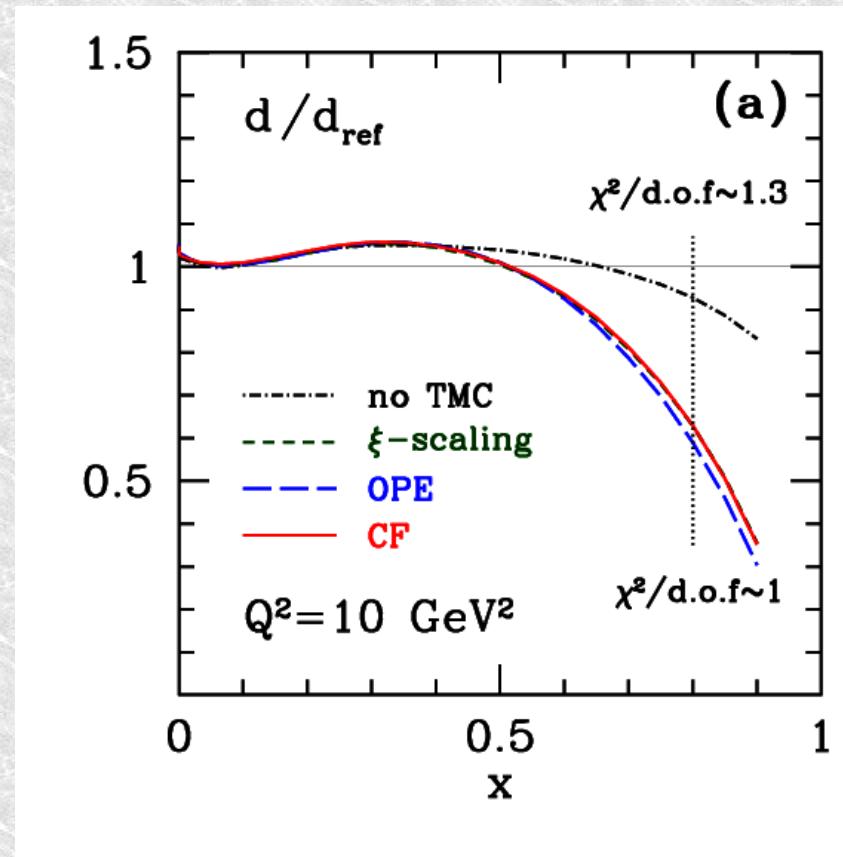


Stability of the d-quark fit



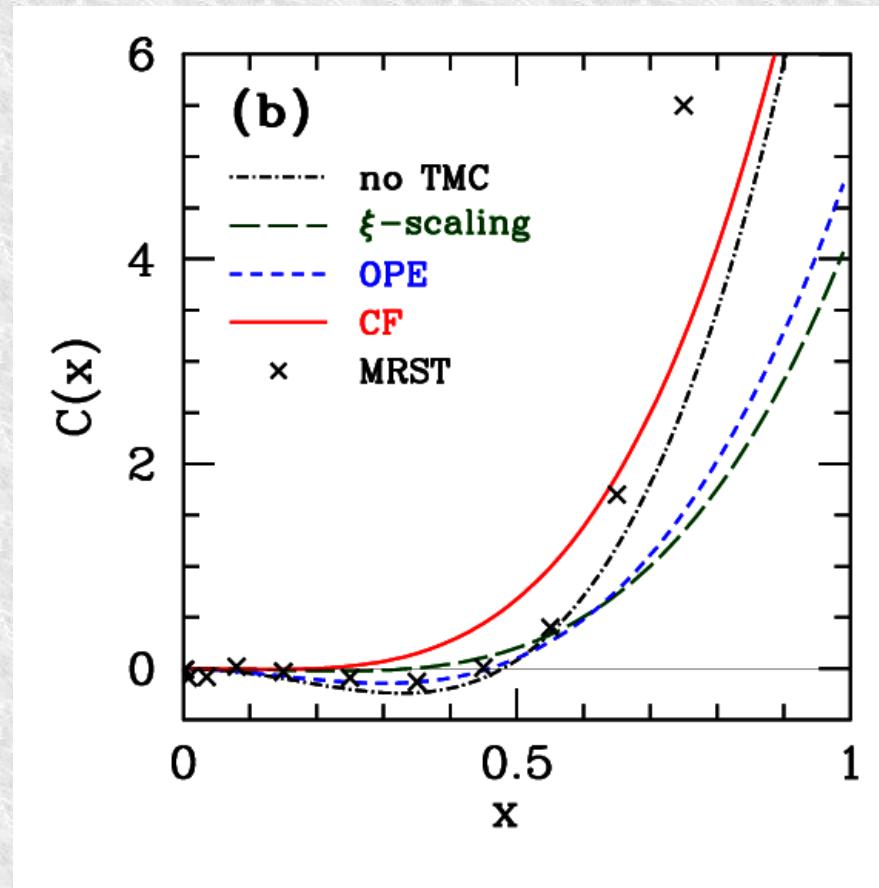
- ➔ Relatively stable against kinematic cuts, but
 - ➔ the d-quark suppression is lessened by the less restrictive cuts
 - ➔ effect still sizable at $x=0.5$ – 0.7 in the nominal range of validity of cut0

TMC vs HT



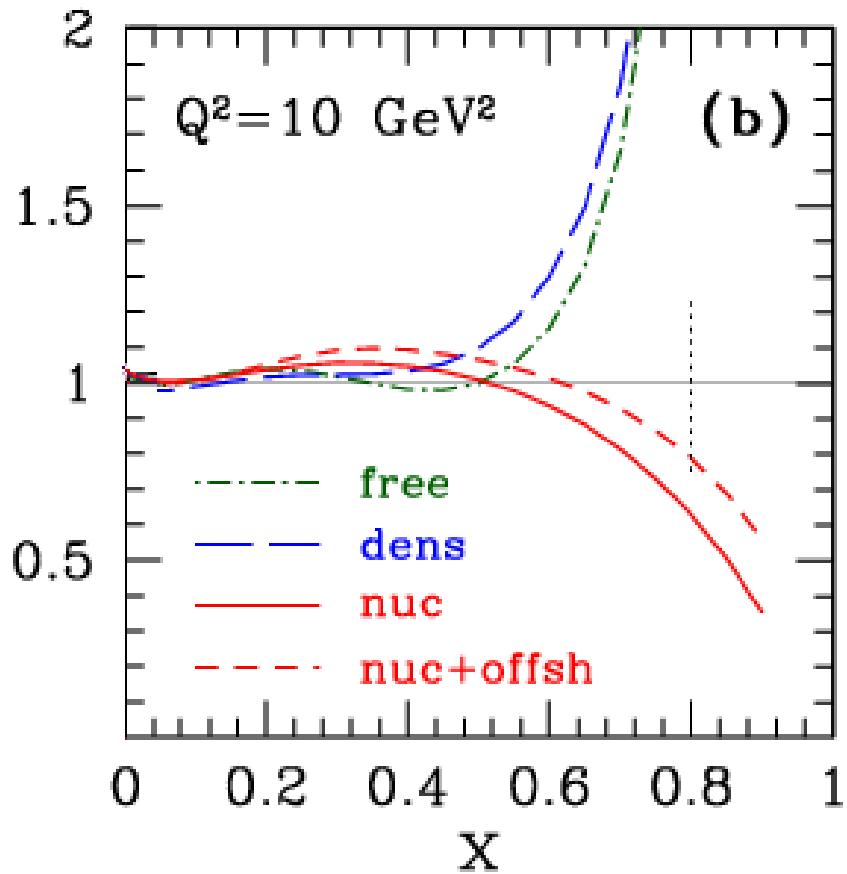
- Extracted twist-2 PDF much less sensitive to choice of TMC
 - fitted HT function compensates the TMC
 - except when no TMC is included
- Inclusion of TMC allow for economical HT parametrization (3 params)

TMC vs HT



- Extracted higher-twist term depends on the type of TMC used
 - $Q^2 > 1.69 \text{ GeV}^2$ and $W^2 > 3 \text{ GeV}^2$ (referred to as “cut03”)
 - lower cuts $\Rightarrow x_B < 0.85$ compared to $x_B < 0.7$ in CTEQ/MRST
 - No evidence for negative HT

Off-shell corrections



$$F_2^p = \frac{4}{9}x u \left(1 + \frac{d}{4u}\right) \quad \text{no corrections}$$

$$F_2^d = \frac{5}{9}x u \left(1 + \frac{d}{u}\right). \quad \text{O.S. corrections}$$

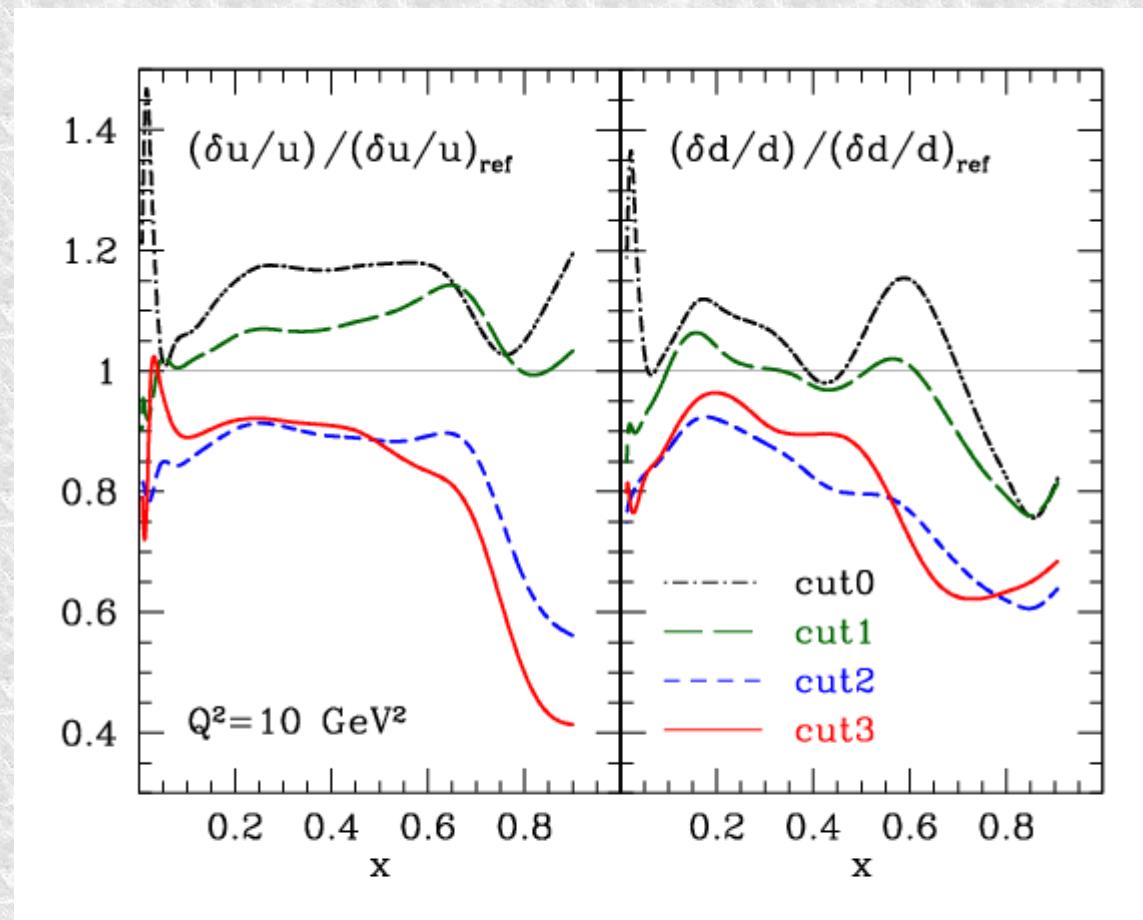
$$\frac{\delta d}{d} = \frac{4}{3} \frac{\delta F_2^d}{F_2^d} \left(1 + \frac{1}{d/u}\right).$$

1.5% on $F_2^d \Rightarrow 40\%$ on d -quark !!!

- ◆ d-quark is strongly correlated to choice of Off-Shell correction !
- ◆ on-shell or mild off-shell correction \Rightarrow d-quark suppression
- ◆ might as well be enhanced...
- ◆ Need to constrain the models ! – see later

Experimental uncertainties: PDF errors

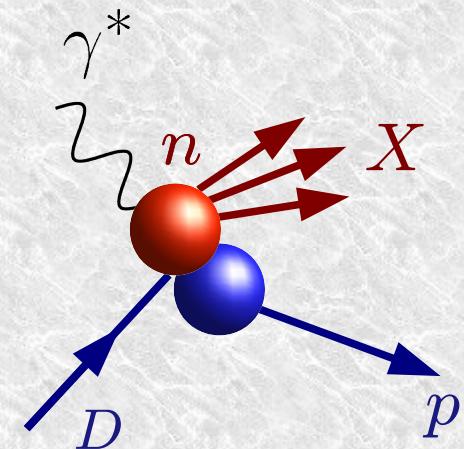
- PDF errors at large x are reduced by lowering the cuts
 - Note: these are exp. errors propagated in the fit
 - nuclear correction uncertainty for d-quarks likely larger than this!



Quasi-free nucleon targets

BONUS and E94-102 experiments at JLab

- ◆ DIS on deuterium with tagged proton
- ◆ tagged proton momentum is measured
- ◆ neutron off-shellness can be reconstructed



- ◆ Study the off-shell dependence of $F_2(n)$ and quark PDFs

$$q \equiv q_D(x, Q^2, p^2)$$

- ◆ Extrapolate to a free neutron target $p^2 \rightarrow M_n^2$

D/p ratios

- Strong Q^2 dependence of nuclear smearing
- use fixed x_B data up to larger Q^2
- needs resonance region \Rightarrow quark-hadron duality
- off-shell corrections can't be constrained

