

Precision Electron-Beam Polarimetry using Compton Scattering at 1 GeV

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We report on the highest precision yet achieved in the measurement of the polarization of a low energy, $\mathcal{O}(1)$ GeV, electron beam, accomplished using a new polarimeter based on electron-photon scattering, in Hall C at Jefferson Lab. A number of technical innovations were necessary, including a novel method for precise control of the laser polarization in a cavity and a novel diamond micro-strip detector which was able to capture most of the spectrum of scattered electrons. The data analysis technique exploited track finding, the high granularity of the detector and its large acceptance. The polarization of the 180 μ A, 1.16 GeV electron beam was measured with a statistical precision of $< 1\%$ per hour and a systematic uncertainty of 0.59%. This exceeds the level of precision required by the Q_{weak} experiment, a measurement of the vector weak charge of the proton. Proposed future low-energy experiments require polarization uncertainty $< 0.4\%$, and this result represents an important demonstration of that possibility. This measurement is also the first use of diamond detectors for particle tracking in an experiment.

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INTRODUCTION

High-precision physics experiments using polarized electron beams rely on accurate knowledge of beam polarization to achieve their ever improving precision. A parity-violating electron scattering experiment in Hall C at Jefferson Lab (JLab), known as the Q_{weak} experiment, is the most recent example [1, 2]. The Q_{weak} experiment aims to test the Standard Model of particle physics by providing a first precision measurement of the weak vector charge of the proton, from which the weak mixing angle will be extracted with the highest precision away from the Z^0 pole. With the Q_{weak} experiment proposed to obtain a statistical precision of 2.1% on the parity-violating asymmetry, the uncertainty goal for beam polarimetry was 1%. Two proposed future precision Standard Model tests at JLab, SOLID and MOLLER, have far more stringent polarimetry requirements of 0.4% [3, 4].

In order to meet this high-precision requirement, a new polarimeter based on electron-photon scattering (Compton scattering) was constructed in the experimen-

tal hall [2, 5]. This polarimeter could be operated without disrupting the electron beam, allowing for continuous polarization measurement during the Q_{weak} experiment. An existing polarimeter in Hall C, using a magnetized iron foil target to measure polarized e^-e^- scattering (Møller scattering), has previously reported a polarization measurement significantly better than 1% [6, 7]. However, the Møller measurement is destructive to the polarized beam and requires reduced beam current, and therefore the results must be extrapolated in beam current and interpolated in time between the dedicated measurements.

In this report we present the first measurement of electron beam polarization with the new Hall C Compton polarimeter, with the best precision ever achieved in this energy range (0.6%), and directly compare the result with the Hall C Møller polarimeter. With each polarimeter reporting precision better than 1%, a direct comparison of the two independent measurements provides a valuable cross-check of electron-beam polarimetry techniques. These results also suggest that the rigorous demands of future experiments can be met.

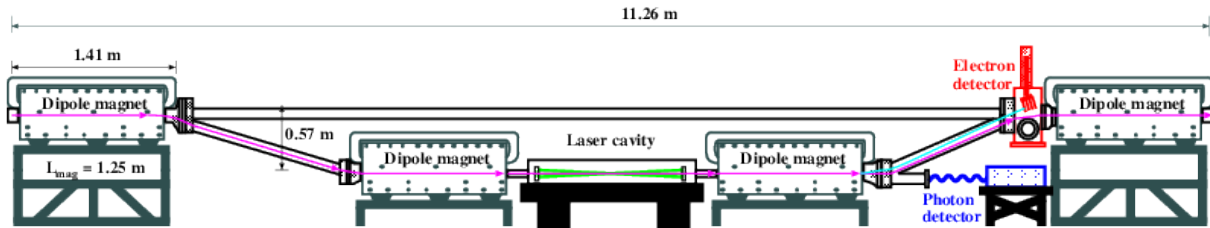


FIG. 1: Schematic diagram of the JLab Hall C Compton polarimeter. Four identical dipole magnets form a magnetic chicane that displaces the 1.16 GeV electron beam vertically downward by 0.57 m. An external low-gain Fabry-Pérot laser cavity provides a high intensity (~ 1.7 kW) beam of circularly polarized green (532 nm) photons. The laser light is focused at the interaction region ($\sigma_{\text{waist}} \sim 90 \mu\text{m}$), and it is larger than the electron beam envelope ($\sigma_{x/y} \sim 40 \mu\text{m}$). The photon detector was not used for these results.

Compton polarimetry is an established technique [8–15] which involves measuring a known QED double-spin asymmetry in electron scattering from a photon beam of known polarization. The scattering asymmetry varies with the fraction of electron beam energy transferred to the scattered photon, with the maximum asymmetry occurring at the kinematic limit for maximum backscattered photon energy. The Compton-scattered electrons and photons can be independently measured and analyzed to determine the polarization of the electron beam. Most Compton polarization measurements have primarily analyzed the scattered photons [8–14] and reliance on electron measurements has been less common [15, 16]. Both the maximum scattering asymmetry and the maximum fraction of beam energy transferred to the photon increase sharply with beam energy. For this reason, Compton scattering measurements are significantly more difficult at low beam energies.

The SLD Compton polarimeter [15] detected scattered electrons in a segmented gas Cerenkov detector with a reported precision of 0.5%—the only Compton polarimetry measurement more precise than this work. Operating at lower energies, the Compton polarimeter in Hall A at Jefferson Lab has reported a precision of $\sim 1\%$ by detecting the Compton scattered electrons in a silicon micro-strip detector [16] at a beam energy of 3 GeV and, in separate measurements, by integrating the total power of Compton scattered photons in a total-absorption GSO calorimeter [17] at 1–3 GeV [14, 18].

The Q_{weak} measurement presented new challenges to this established polarimetry technology. The very precise SLD result was achieved with a 532 nm laser at a beam energy of 46.5 GeV, providing a maximum asymmetry $A_{\text{exp}} \sim 0.75$ and a maximum photon energy of almost 60% of the electron beam energy. At the relatively low energy (1.16 GeV) of the electron beam for the Q_{weak} experiment, the maximum Compton asymmetry $A_{\text{exp}} \sim 0.04$ is significantly smaller, and only 5% of the electron energy can be transferred to the photon. The small asymmetry requires large luminosity to achieve sufficient statistical precision, while the lower kinematic limit implies that an electron detector must

be positioned close to the primary beam and have high spatial resolution to achieve suitable resolution on the scattered electron momentum.

The desired high luminosity was achieved by storing laser photons in a Fabry-Pérot cavity, although past measurements of the laser polarization have proven to be challenging in evacuated Fabry-Pérot cavities. An innovative technique for maximizing the laser polarization by analyzing the reflected light at the cavity entrance was employed for the first time during the Q_{weak} experiment.

The high signal count rate, expected background close to the beam, and proposed experimental run of 200 days required the selection of radiation-hard detection systems. A diamond micro-strip detector was selected for electron detection. The well-established radiation hardness of diamond [19, 20] and its insensitivity to synchrotron radiation were the most important considerations in this choice. While diamond micro-strip detectors have been demonstrated in test beams [21, 22], and other diamond detector configurations have been used in beam condition monitors [23–28], this is the first application of a diamond detector in an experiment as a particle tracking detector.

THE HALL C COMPTON POLARIMETER

A schematic of the Compton polarimeter in Hall C at JLab is shown in Fig. 1, and details can be found in Ref. [2, 5]. The electron beam was deflected vertically by two dipole magnets to where it could interact with the photon target. Circularly polarized 532-nm laser light was injected into a Fabry-Pérot optical cavity, in the beamline vacuum, with a gain of approximately 200. The injection laser, a Coherent Verdi [29] with an output of 10 W, was locked to the cavity. The 0.85 m long optical cavity crossed the electron beam at 1.3° .

After interacting with the photon target, the electron beam was deflected back to the nominal beamline with a second pair of dipole magnets. The Compton scattered photons passed through an aperture in the third magnet and were detected in an array of PbWO_4 crystals. The

analysis of the detected photons were used as a crosscheck of the electron analysis. The third chicane magnet bent the primary beam by 10.1° , also separating the Compton scattered electrons from the primary beam by up to 17 mm before the fourth dipole. Here the scattered electrons were incident on the electron detector, a set of four planes of diamond micro-strip detectors. Remote actuation allowed the detector distance to the primary beam to be varied. Data were taken with the innermost strip a mere 5 mm from the beam, with routine operation at 7 mm from the beam. This range allowed the detection of most of the Compton electron spectrum, including the zero-crossing of the asymmetry 8.5 mm from the primary beam.

The electron detectors were made from $21 \times 21 \times 0.5$ mm³ plates of synthetic diamond grown using chemical vapor deposition (CVD) [30]. A novel Ti-Pt-Au metalization was used to deposit electrodes on the diamond plates. Each diamond plate has 96 horizontal metalized electrode strips with a pitch of 200 μ m (180 μ m of metal and 20 μ m of gap) on one side. The Compton spectrum is spread over 50 – 60 strips allowing a precise measurement of the shape. The strips were read out using custom low noise amplifiers and discriminators, grouped together with 48 channels in a single module [31]. A schematic of a single detector plane is shown in Fig 2.

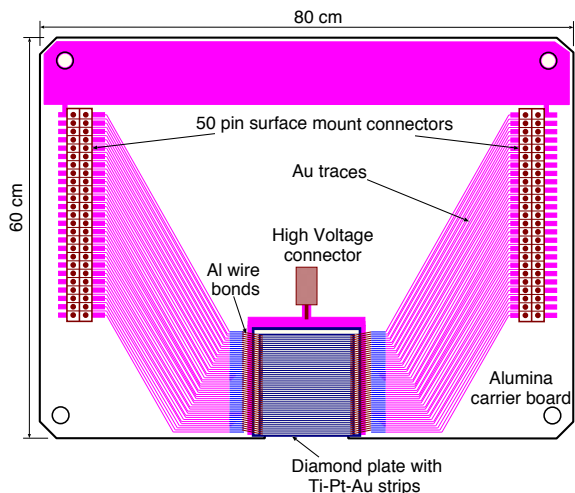


FIG. 2: A schematic diagram of the CVD diamond plate mounted on an alumina frame which forms a single detector plane. There were 96 Ti-Pt-Au strips deposited on the front face of the diamond plate which was attached to the frame using a silver epoxy. The strips were connected to Au traces on the alumina frame with aluminum wire bonds. The traces terminated on two 50 pin connectors. A high voltage (HV) bias of ~ -300 V was applied to the back side of the diamond plate via a miniature HV connector.

The data acquisition (DAQ) system employed a set of field programmable gate array (FPGA) based logic modules [32] to implement a track-finding algorithm, which

generated a trigger when a strip in the same cluster of 4 adjacent strips was identified in multiple active planes. Three detector planes were used during the experiment, and the typical trigger condition required 2 out of 3 planes. Untriggered hits were also recorded and were used for studying DAQ dead-time and trigger inefficiencies. In the triggered mode, electronic noise was suppressed by a factor of 100 – 200 compared to the untriggered mode, which led to a significantly better signal-to-background ratio in the triggered mode, but at the cost of a few percent in trigger efficiency.

For a beam current of 180 μ A and a laser intensity of 1.7 kW, the total untriggered rate in the detector was 70 – 90 kHz. The well tuned electron beam, low-noise electronics and the insensitivity of diamond to synchrotron radiation contributed to a signal-to-background ratio of $\mathcal{O}(10)$. The detector efficiency was estimated to be 70% by comparing the expected to the observed rates. The small signal sizes, large distance between the detector and the readout electronics, and a threshold to reduce noise led to the inefficiency. Over the 2 year running period of the Q_{weak} experiment, the detectors were exposed to a radiation dose of 100 kGy from electrons (synchrotron radiation not included). No degradation of the detector performance was observed, demonstrating the intended radiation hardness.

ANALYSIS AND RESULTS

The electron beam helicity was reversed at a rate of 960 Hz in a pseudo-random sequence. The Compton laser was operated in 90 second cycles (60 s on and 30 s off). The laser-off data were used to measure the background, which was subtracted from the laser-on yield for each electron helicity state. The signal-to-background ratio was 5–20, depending on the strip. The measured asymmetry was built from the yields using,

$$A_{\text{exp}} = \frac{Y^+ - Y^-}{Y^+ + Y^-}, \quad (1)$$

where $Y^\pm = N_{\text{on}}^\pm / Q_{\text{on}}^\pm - N_{\text{off}}^\pm / Q_{\text{off}}^\pm$ is the charge normalized Compton yield for each detector strip, $N_{\text{on/off}}^\pm$ is the number of detected counts, and $Q_{\text{on/off}}^\pm$ the beam charge, accumulated during the laser (on/off) period for the (\pm) electron helicity state. A statistical precision of $< 1\%$ per hour was routinely achieved. Typical yield spectra for the laser-on and laser-off periods are shown in Fig. 3 (top). Consistent results were obtained subtracting the background over 1 laser cycle (90 s) and also over ~ 900 s. A typical spectrum for an hour long run is shown in Fig. 3. The background asymmetry is consistent with zero within the statistical uncertainties.

The electron beam polarization P_e was extracted by fitting the measured asymmetry to the theoretical Comp-

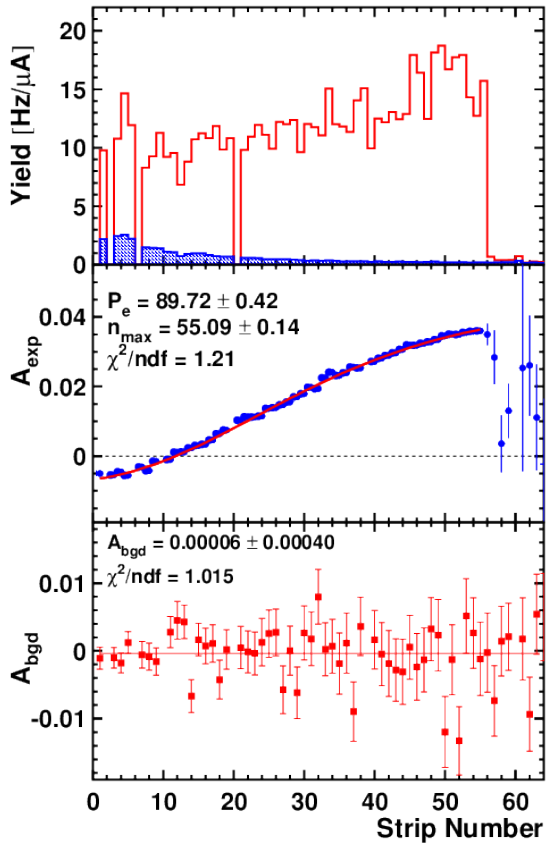


FIG. 3: Yield and asymmetry data from a single detector plane plotted versus detector strip number, for a typical hour-long run. Statistical uncertainties only. (top) The charge normalized yield at a beam current of $180 \mu\text{A}$ and laser intensity of 1.7 kW . The laser-on yield is shown in red and laser-off (background) yield is shown in shaded blue. (middle) The measured Compton asymmetry (background-subtracted). The solid red line is a fit to Eq. 2. (bottom) The background asymmetry from the laser-off period. The solid red line is a fit to a constant value.

ton asymmetry, using

$$A_{\text{exp}}^n = P_e P_\gamma A_{\text{th}}^n, \quad (2)$$

where P_γ is the polarization of the photon beam and A_{th}^n is the $\mathcal{O}(\alpha)$ theoretical Compton asymmetry for fully polarized electrons and photon beams in the n -th strip. The theoretical Compton asymmetry $A_{\text{th}}(\rho)$ was calculated as a function of the dimensionless variable

$$\rho = \frac{E_\gamma}{E_\gamma^{\text{max}}} \approx \frac{E_e^{\text{beam}} - E_e}{E_e^{\text{beam}} - E_e^{\text{min}}}, \quad (3)$$

where E_γ the energy of a back-scattered photon, E_γ^{max} is the maximum allowed photon energy, and E_e , E_e^{min} , and E_e^{beam} are the scattered electron energy, its minimum value, and the electron beam energy, respectively. A_{th}^n

was related to $A_{\text{th}}(\rho)$ by mapping ρ to the strip number using knowledge of the magnetic field in the third dipole, the geometry of the chicane, the strip pitch and n_{max} , the position of the kinematic end point (Compton edge) expressed as a strip position. An initial estimate of the kinematic end-point, n_{max} , was determined from the edge of the yield spectrum. It was observed to vary slowly as the electron beam angle drifted by up to $\pm 0.5 \text{ mrad}$.

Radiative corrections to the Compton asymmetry were calculated to leading order with a low energy approximation applicable for few GeV electrons [33]. The radiative correction to the asymmetry was $< 0.3\%$ in all strips.

Equation 2 was fit to the measured asymmetries with P_e and n_{max} as the two free parameters. No systematic deviation of the shape of the asymmetry was observed. A typical fit is shown in Fig. 3. The χ^2 per degree-of-freedom of the fit, considering statistical uncertainties only, ranges between 0.8 and 1.5 for 50 – 60 degrees of freedom. The detection of a large fraction of the Compton electron spectrum, spanning both sides of the zero crossing of the Compton asymmetry, significantly improved the robustness of the fit. The fit quality was validated using the simulation discussed below.

The systematic uncertainty in the determination of P_e is summarized in Table I. In previous polarimeters using a laser system based on a Fabry-Pérot cavity, knowledge of the laser polarization was a significant source of uncertainty. Pressure induced birefringence in the vacuum window can lead to large changes in laser polarization which cannot be directly measured in the evacuated beamline. In this work we use an optical reversibility theorem [34], that relates the polarization ellipticity at the output of an optical system to the polarization of the retro-reflected light at the input, in order to maximize the circular polarization in the cavity. The technique works by analyzing the light reflected from the entrance mirror of the cavity, exploiting the fact that circular polarization reverses sign on reflection while linear polarization is unchanged. A linear polarizer, followed by a half-wave-plate and quarter-wave-plate, was used to create an arbitrary polarization state at the entrance to the vacuum system. Minimizing the back-reflected light that is transmitted through the polarizer (Polarization Signal) maximizes the degree-of-circular-polarization (DOCP) at the cavity entrance mirror.

To determine the uncertainty in the photon polarization, this DOCP maximization technique was directly tested *in situ*. With the vacuum enclosure removed, the intra-cavity DOCP was measured simultaneously with the Polarization Signal while scanning over input polarization states, with a concentration of points near the maximum DOCP, as in Fig. 4, demonstrating a very close and robust correlation. The uncertainty on the laser polarization is estimated to be 0.18%, which is dominated by our ability to bound, through direct measurement, effects that might alter the polarization over the numerous

reflections within the Fabry-Pérot cavity. Effects of depolarization or spatial polarization gradients are bound by the degree of extinction in the Polarization Signal, and are included in the quoted laser polarization uncertainty.

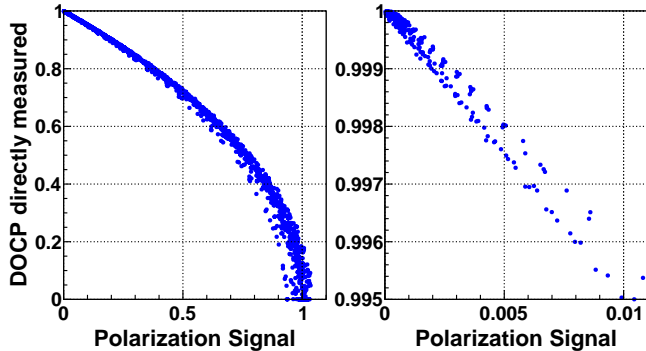


FIG. 4: Direct test of laser polarization maximization technique. The correlation between the laser DOCP directly measured after the cavity mirror and the Polarization Signal extracted from the reflected light. The left panel shows the full range while the right panel is a zoom of the region of maximum DOCP.

The uncertainties in the measured asymmetry were studied using a Monte Carlo simulation of the Compton polarimeter, which was coded using the GEANT3 [35] detector simulation package. In addition to Compton scattering, the simulation included backgrounds from beam-gas interactions and beam halo interactions in the chicane elements. It also incorporated the effects of detector efficiency, the track-finding trigger, and electronic noise. A typical simulated strip-hit spectrum (ideal, with noise, and with noise and efficiency), and the asymmetry extracted from it, are shown in Fig. 5. The simulation was used to study the analysis procedure and the statistical quality of the fits that were used to extract the beam polarization. It was demonstrated that the central value of the polarization fit parameter was typically insensitive to small distortions to the electron spectrum such as a few missing or noisy strips, and the observed strip-to-strip variation in efficiency. The simulation was also used to study a variety of sources of systematic uncertainties. For each source, the relevant parameter was varied within the expected range of uncertainty, and the range of variation of the extracted polarization was listed as its contribution to the systematic uncertainty.

The MC simulation demonstrated that secondary particles knocked out by the Compton scattered electron passing through the first detector plane produced a 0.4% change in the extracted polarization in the subsequent planes, consistent with observation. A correction for the second and third planes could be made but at the cost of a slightly higher systematic uncertainty and hence only the results from the first detector plane are quoted here. Although all three planes were used in the tracking trig-

ger, the results from the first detector plane were shown by the simulation to be insensitive to this effect.

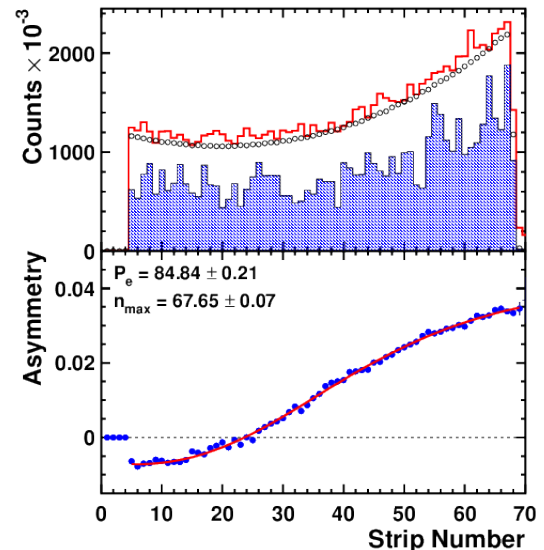


FIG. 5: (top) Typical Monte Carlo simulated Compton spectra for a single detector plane; ideal (black open circles), with noise (red) and with detector efficiency (blue, shaded). (bottom) The Compton asymmetry extracted from the simulated spectrum including detector efficiency (blue circles), and a two parameter fit to the calculated asymmetry (red line). The input asymmetry was 85%.

There were several sources of rate-dependent efficiency associated with the DAQ system, such as the algorithm used to identify electron tracks and form the trigger, and the dead-time due to a busy (hold off) period in the DAQ. A digital logic simulation platform, Modelsim [36], was used to model the DAQ system. Simulated Compton events, backgrounds, and noise signals were processed with this model, which made a detailed accounting of the logic and delays from the internal signal pathways in the FPGA modules and the external electronic chain.

These results were used to determine a correction to the detector yields, for each hour-long run, based on the detector rates during the run. This correction is calculated and applied for each beam helicity state independently. An estimate of the systematic uncertainty due to this correction was determined from the variation of the ratio of the polarizations extracted from the corrected, triggered data to those obtained from the untriggered data over a wide range of signal rates and several difference trigger conditions. The DAQ efficiency correction resulted in $< 1\%$ change in the extracted polarization.

The extracted beam polarization for the entire second running period of the Q_{weak} experiment is shown in Fig. 6. Changes at the electron source, indicated by the dashed and solid vertical lines, led to discontinuities in the beam polarization. Each point is shown with system-

TABLE I: Systematic Uncertainties

Source	Uncertainty	$\Delta P/P\%$
Laser Polarization	0.18%	0.18
helicity correl. beam	5 nm, 3 nrad	< 0.07
Plane to Plane	secondaries	0.00
magnetic field	0.0011 T	0.13
beam energy	1 MeV	0.08
detector z position	1 mm	0.03
trigger multiplicity	1-3 plane	0.19
trigger clustering	1-8 strips	0.01
detector tilt (x, y and z)	1 degree	0.06
detector efficiency	0.0 - 1.0	0.1
detector noise	up to 20% of rate	0.1
fringe field	100%	0.05
radiative corrections	20%	0.05
DAQ efficiency correction	40%	0.3
DAQ efficiency pt.-to-pt.		0.3
Beam vert. pos. variation	0.5 mrad	0.2
spin precession in chicane	20 mrad	< 0.03
Electron Detector Total		0.56
Grand Total		0.59

atic uncertainties that may vary for each measurement, while a common systematic uncertainty of 0.42% applies to all points together.

These results are quantitatively compared to results [2] from the Møller polarimeter by examining periods of stable polarization between changes in the polarized source. Previous cross-comparisons between polarimeters in this energy range have uncovered significant discrepancies between various polarimeters [37]. The ratio of Compton to Møller measurements, when averaged over these stable periods using statistical and point-to-point systematic uncertainties, was 1.007 ± 0.003 . The results are compatible within the total relative normalization uncertainty of 0.77%. This is the first direct comparison of two independent polarimeters with better than 1% precision.

Future experiments will require a polarimetry precision of 0.4% with beam energies between 6 and 11 GeV. Our results indicate that these goals are within reach of Compton polarimetry. Recent results using integrating photon detection [14] have demonstrated that uncertainties in the photon analysis (excluding the laser polarization) are at the level of 0.5%. Such a measurement could be combined with an independent electron analysis as demonstrated here, with a precision approaching 0.5%, with the dominant systematic error in common between the two analyses being the uncertainty on intra-cavity laser polarization (< 0.2%). It is worth noting that fur-

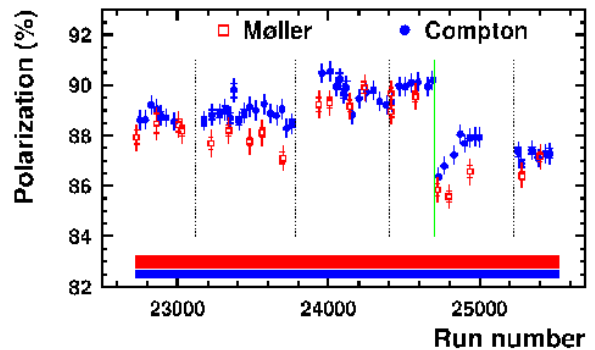


FIG. 6: The extracted beam polarization for the 1.16 GeV, 180 μ A electron beam, as a function of run-number and averaged over 30 hour long periods, during the second run period of the Q_{weak} experiment (blue, solid circle). Also shown are the results from the intermittent measurements with the Møller polarimeter [2] (red, open square). The inner error bars show the statistical uncertainty while the outer error bar is the quadrature sum of the statistical and point-to-point systematic uncertainties. The solid bands show the additional normalization/scale type systematic uncertainty (0.42% Compton and 0.65% Møller). The dashed and solid (green) vertical lines indicate changes at the electron source.

ther gains are possible: the dominant errors in the electron analysis relate to rate-dependent DAQ inefficiencies, which would undoubtedly be reduced through refinement of the logic and timing parameters, while improvements in gain stability and linearity measurements would further improve the photon measurements. The increased beam energies for planned future measurements are also more favorable to Compton polarimetry.

CONCLUSIONS

The polarization of a 1.16 GeV electron beam was measured with a systematic uncertainty of 0.59%. The interacting photon polarization was maximized and the uncertainty reduced using a novel technique based on the reflected incident light. We used diamond micro-strip detectors for the first time as tracking detectors and demonstrated their ability to withstand a high radiation dose. The high granularity of the detectors and the measurement of a large fraction of the Compton electron spectrum, spanning the asymmetry zero crossing, coupled with a robust analysis technique and rigorous simulations of the polarimeter and the DAQ system, produced a reliable, high precision measurement of the polarization in a high radiation environment. Due to these technical advances, the uncertainty goal was significantly surpassed. These results suggest that even more precise electron beam polarization measurements, such as required for the future parity-violation measurements SOLID and MOLLER, will be achievable through Comp-

ton polarimetry.

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