

# **$Q^2$ -Dependence of the Spin Structure Functions of the Proton and the Deuteron**

The data obtained in the Stanford Linear Accelerator Center (SLAC) experiment E155 cover a large range in  $Q^2$ , improving the available experimental data on the  $Q^2$ -dependence of the spin structure functions. We present the latest results of our analysis.

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# **Overview**

## ***Introduction***

Phenomenological Study of  $Q^2$ -Dependence of  $A_1$

## ***Motivation***

Calculation of E155 Radiative Corrections

## ***Procedure***

Details of the Study

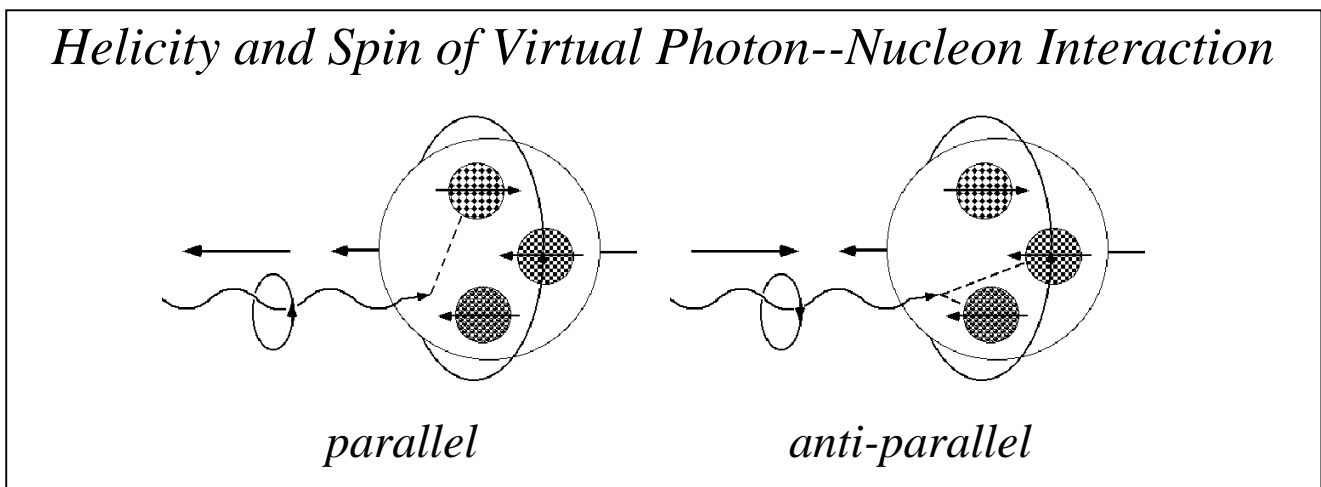
## ***Results***

Evidence of  $Q^2$ -Dependence of  $A_1^p$

## ***Summary***

## Introduction

Phenomenological Study of  $Q^2$ -Dependence of Virtual Photon  
Asymmetry  $A_1(x_{Bjorken}, Q^2)$



$$A_1(x_{Bj}, Q^2) = \frac{\left( g_1(x_{Bj}, Q^2) - \gamma^2 g_2(x_{Bj}, Q^2) \right)}{F_1(x_{Bj}, Q^2)}$$

$$g_2^{WW}(x_{Bj}, Q^2) = -g_1(x_{Bj}, Q^2) + \int_{x_{Bj}}^1 \frac{g_1(y, Q^2)}{y} dy$$

## Motivation

Calculation of E155 Radiative Corrections  
Requires Model of  $A_1(x_{\text{Bjorken}}, Q^2)$  as Input

$\Rightarrow$  New Model (Fit), incl. E155 Data

$g_1$  and  $F_1$  have Well-Established  
 $Q^2$ -Dependence, but Prior to E155, no  
Conclusive Answer if  $A_1$  is  $Q^2$ -Dependent

$$A_1 \approx \frac{g_1(x_{Bj}, Q^2)}{F_1(x_{Bj}, Q^2)}$$

## Procedure

Calculation of Radiative Corrections Based on  
Recipe of *T. V. Kuchto* and *N. M. Shumeiko*  
*Nucl. Phys. B219(1983) 412-436*

Use  $A_1$  Model and  $g_2^{\text{ww}}$  (Derived from  $A_1$ )

$A_1$  Model is Fit to Data via Iterative Process

Model Fine-Tuned with Direct Fit to Raw Asymmetries

Best Fit Requires Largest Data Set, Kinematic Coverage

⇒ Use All Available Data and Maximize Data Set:

Simultaneous Fits to  $A_1^p$ ,  $A_1^n$  &  $A_1^d$  Data Using  
Parameterization of  $A_1^p$  and  $A_1^n$  and

$$g_1^d = \frac{1}{2} \left( 1 - \frac{3}{2} \omega_D \right) \left( g_1^p + g_1^n \right)$$

( $\omega_D$  = D-State Probability)

## Procedure

*Form of General Parameterization of  $A_1^p$  and  $A_1^n$ :*

$$A_1 = x^\alpha (a + bx + cx^2) (1 + d \cdot f(Q^2))$$

*Forms of  $f(Q^2)$  Examined:*

$1/Q^2$ ,  $1/Q$ ,  $\log Q^2$ , None,  
Others, Combinations

### *Data Set*

*(only points with  $Q^2 > 1.0 \text{ GeV}^2$ , not in Resonance Region)*

#### **Proton (N=268)**

E155, E143, E130, E80, Hermes, SMC, EMC

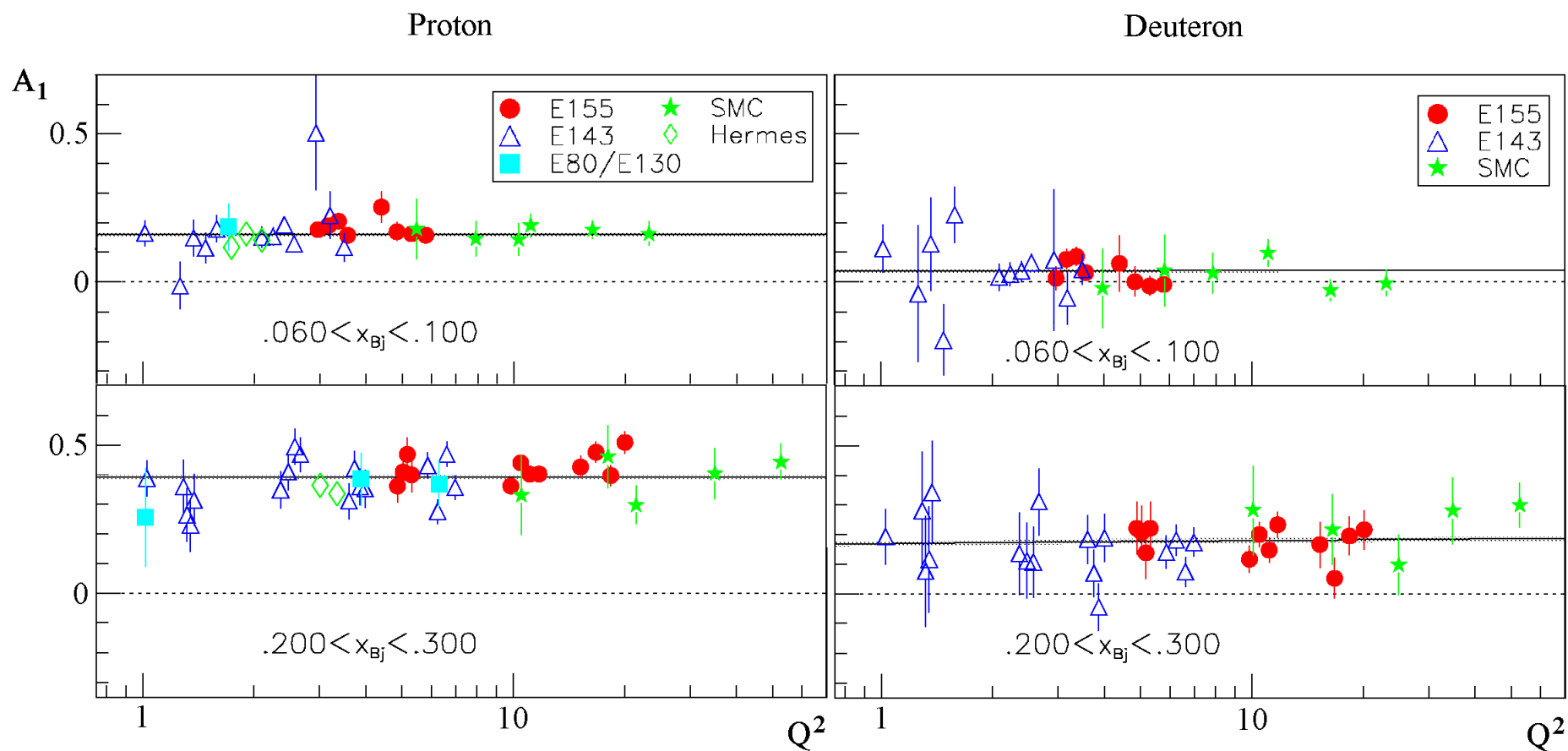
#### **Deuteron (N=224)**

E155, E143, SMC

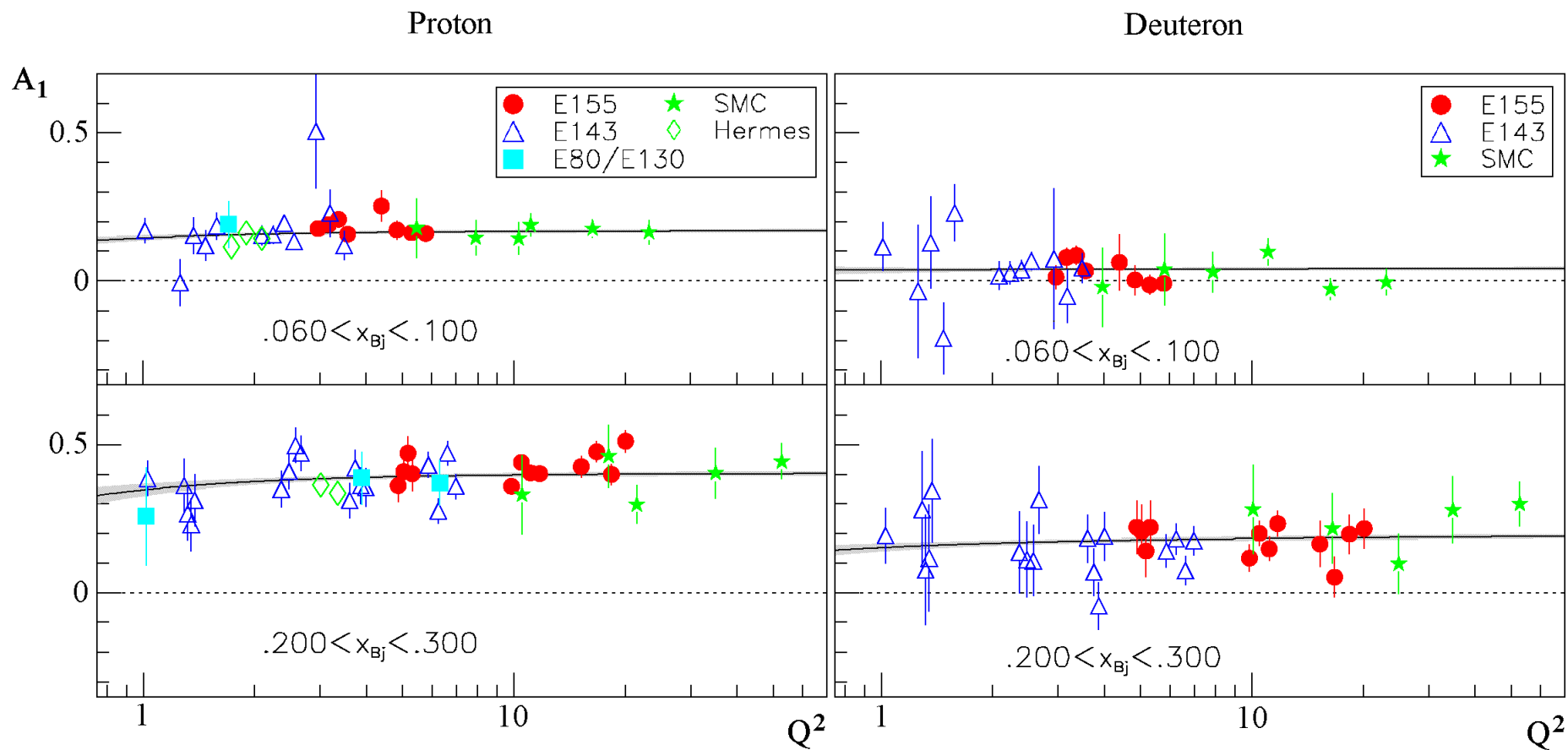
#### **Neutron (N=35)**

E154, E142, Hermes

# $A_1$ vs. $Q^2$ — No $Q^2$ -Dependent Term

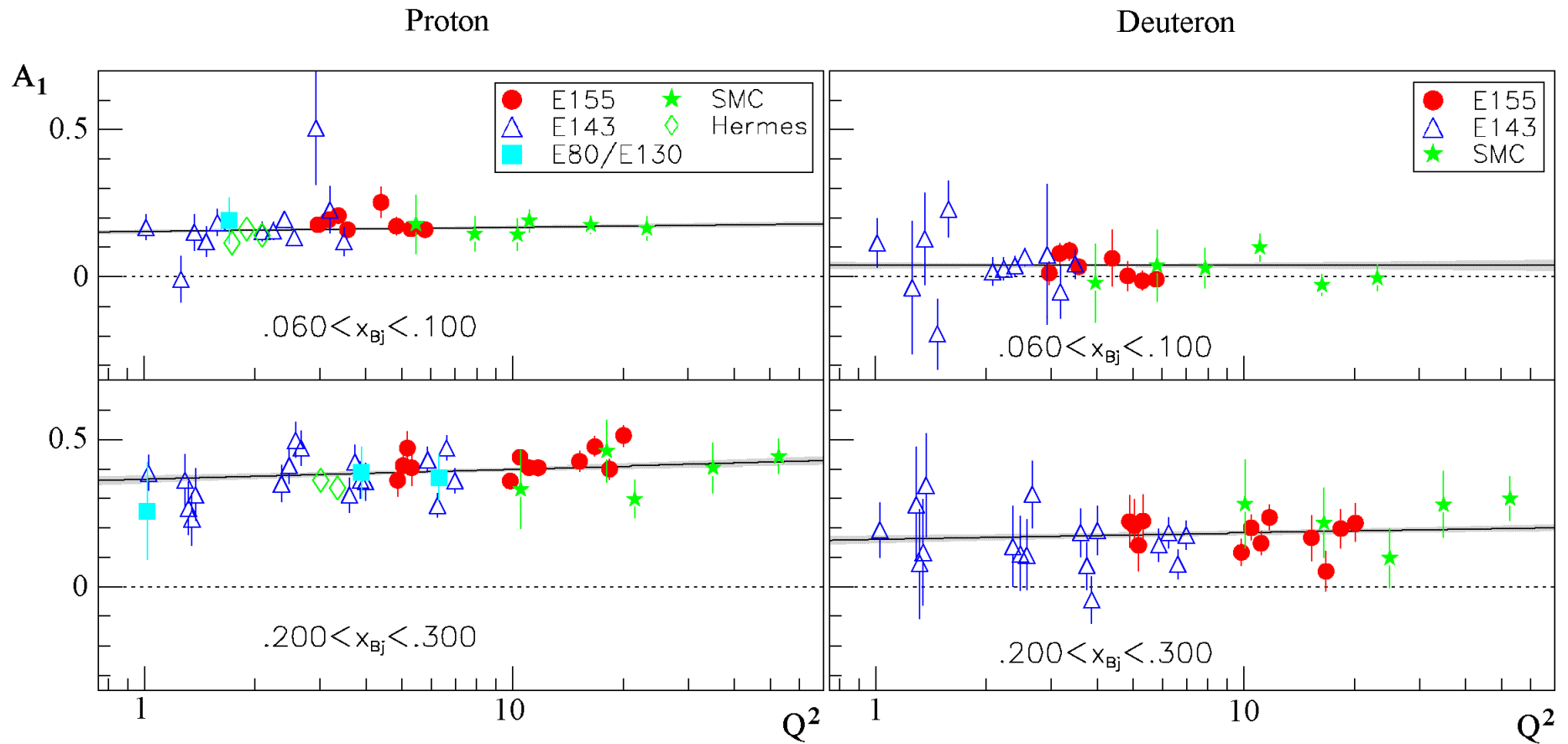


# $A_1$ vs. $Q^2 \rightarrow 1/Q^2$





# $A_1$ vs. $Q^2$ — $\log Q^2$



## Results

### $\chi^2$ of Fits

	$A_1^p$	$A_1^d$
$N$	268	224
None	273.5	256.3
$1/Q^2$	266.9	256.8
$\log Q^2$	266.1	256.7

### Change to $A_1^p$ Due to $1+d \cdot f(Q^2)$

$Q^2$	1	10	100
$1/Q^2$	-14%	-1%	0
$\log Q^2$	0	9%	18%

## Summary

For  $Q^2 > 1 \text{ GeV}^2$  and Based on Currently Available Data,  $1/Q^2$  Form Improves  $\chi^2$  of Fit to  $A_1^p$  by  $\sim 2.5\sigma$ , Compared to No  $Q^2$  Term

Below  $Q^2 = 1 \text{ GeV}^2$ , Strong  $Q^2$  Dependence, as Expected

No Significant  $Q^2$  Dependence of  $A_1^d$  Evident

Newly Obtained Global Fit to World  $A_1$  Data with Overall  $\chi^2$  of 539.0 for 527 Data Points Provides Good Model for RC Calculation