

SOCRAT: a Software for Clas12 Reconstruction And Tracking

S. Procureur (CEA-Saclay)

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Outline

- Introduction
- The Kalman Filter algorithm
- Central tracking
- Forward tracking
- Miscellaneous (mini-stagger, energy loss)

Introduction

Goals:

- 1) Develop a track reconstruction software for CLAS12, taking into account realistic background (Geant4). This reconstruction is based on the Kalman Filter algorithm
- 2) Check that the design reaches the required performance
- 3) Optimize the design

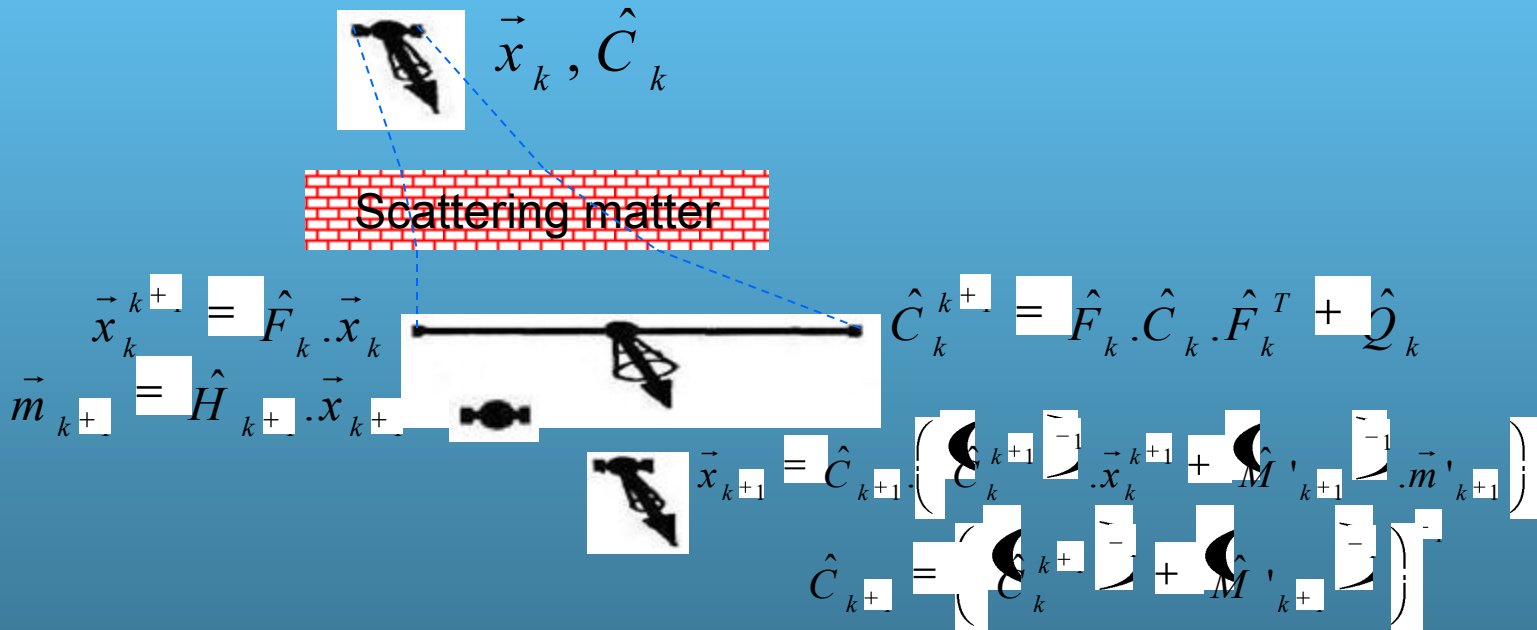
Key issues: charged particle reconstruction in the Forward DC system (~24k sense wires), and the Central Tracker (3x2 Silicon + 3x2 Micromegas)

Vertex: for accurate vertex reconstruction of forward tracks, e.g. for hyperon and cascades decays, the Forward Vertex Tracker (FVT) is also included

VID: not yet developed

Kalman Filter algorithm

- Starting point: a state vector and its covariance matrix
- Extrapolation to the next measurement:
- Update of the position (by minimizing the χ^2):



- Key issues:
- choice of \vec{x} (geometry)
 - initialization of \vec{x}_0 and C_0 (helix, torus Bdl param.)

Kalman Filter algorithm

- Central tracking:

- Measurement at \sim constant radius

$$\rightarrow \vec{x}^T = (\varphi, z, \vec{p})$$

- Homogeneous field (solenoid)

\rightarrow estimation of \vec{x}_0 with helical track

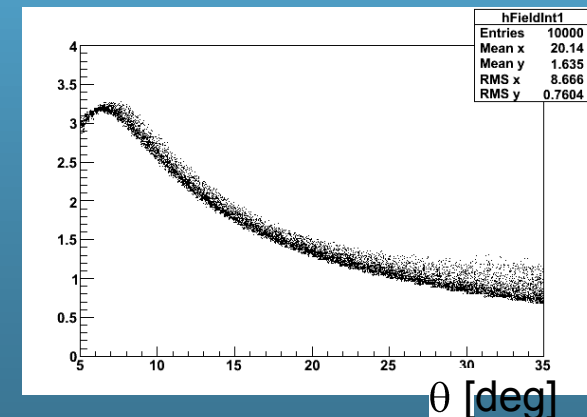
- Forward tracking:

- Measurement at \sim constant z

$$\rightarrow \vec{x}^T = (x, y, u_x, u_y, q / p)$$

- Toroidal field

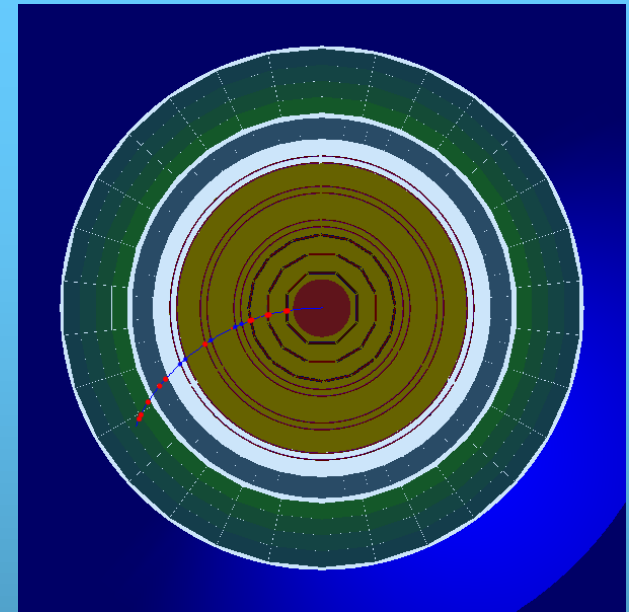
\rightarrow parameterization of $\int B dl$



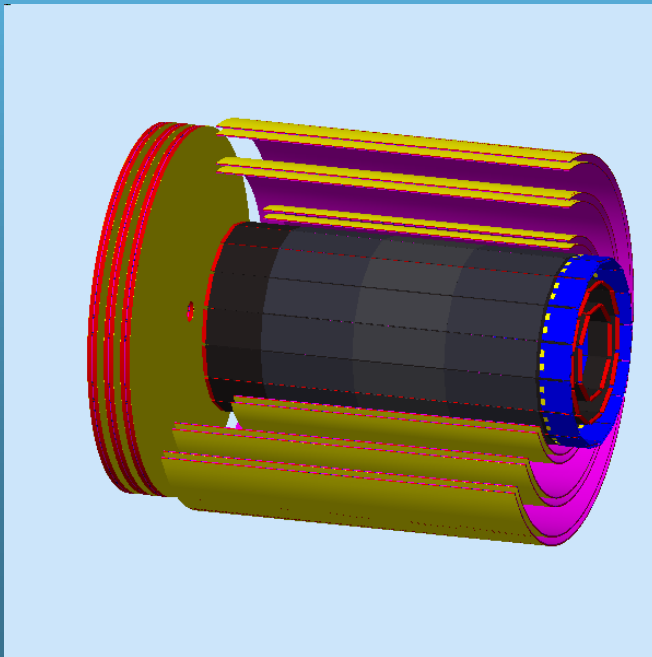
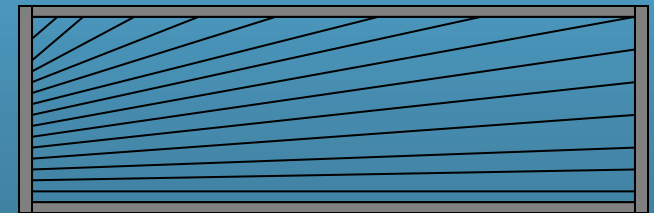
Central tracker (BVT)

Main features (up to now):

- 3x2 layers of Silicon
 - polygon structure
 - graded stereo angle: $0 \rightarrow 3^\circ$
- 3x2 layers of Micromegas
 - thin, cylindrical detectors
 - strip angle: 0 & 90°



Silicon strip layout:



Problems:

- Silicon design is still changing
- Micromegas are not yet fully official

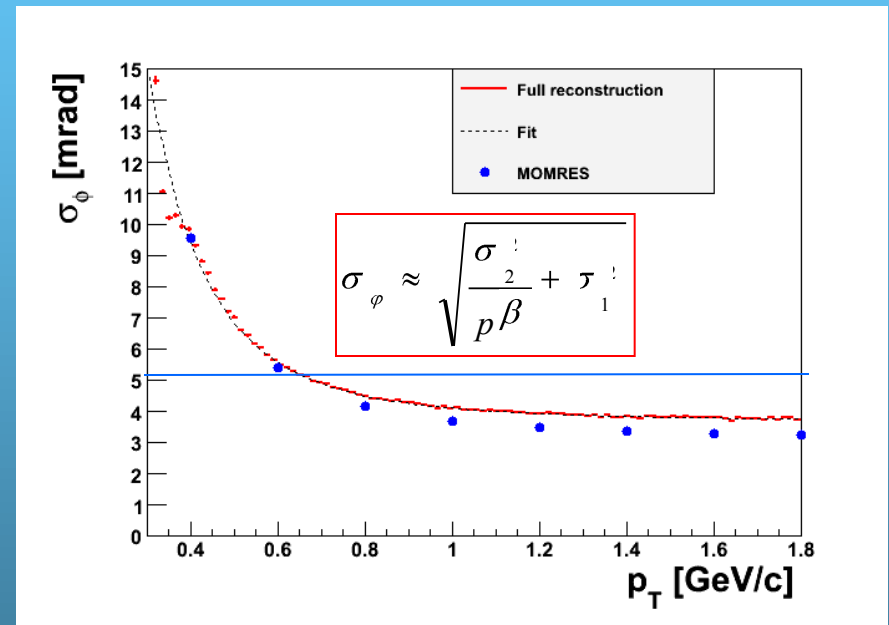
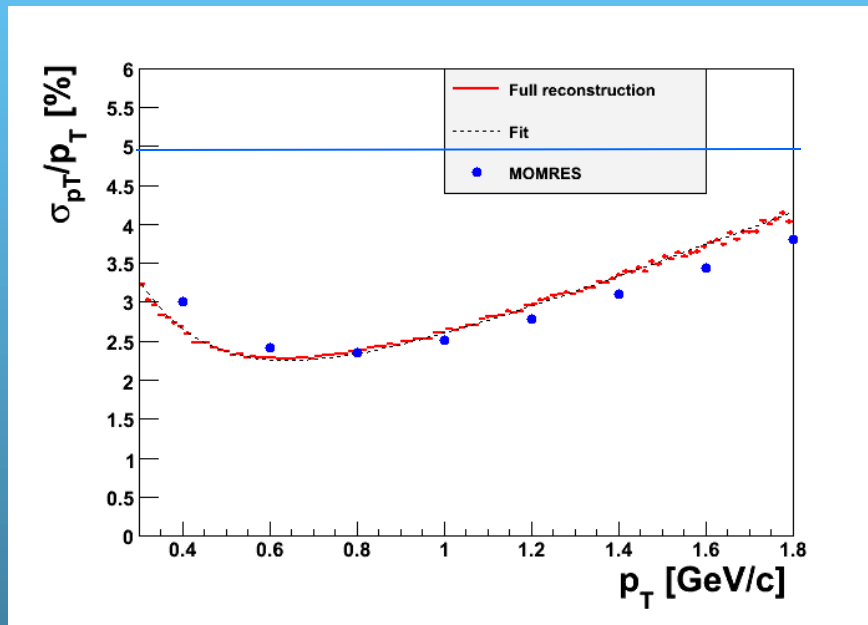
Central tracking - Performance

(using 4x2 layers of Silicon)

Track reconstruction requires at least 3 double layers

$$\langle \varepsilon \rangle \approx 91\%$$

Once a combination of hits has been found, it is sent to the KF for the final fit

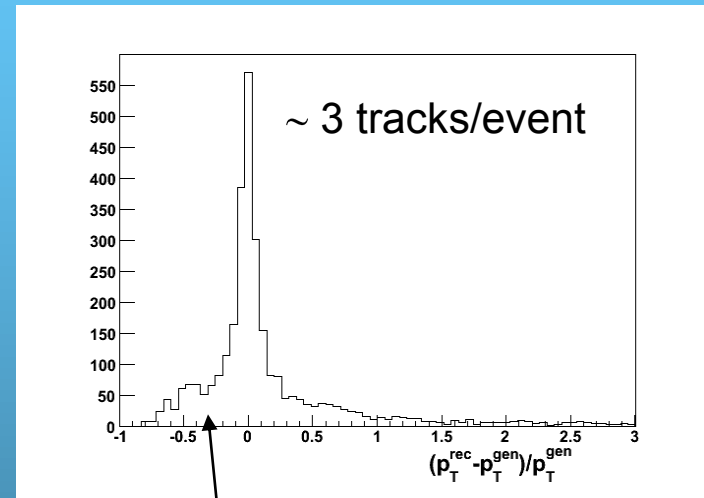
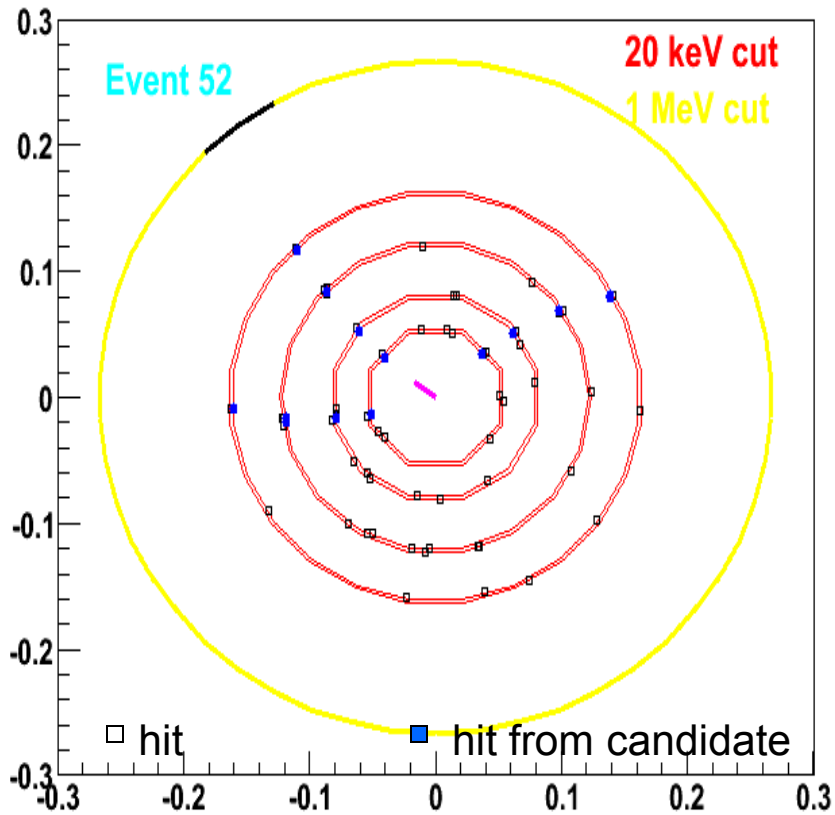


Agreement between Kalman Filter & MOMRES

All physics requirements met, but upper limit for θ

Effect of the background

Example of DVCS events at full luminosity (from Geant4): $e+p \rightarrow e+p+\gamma$

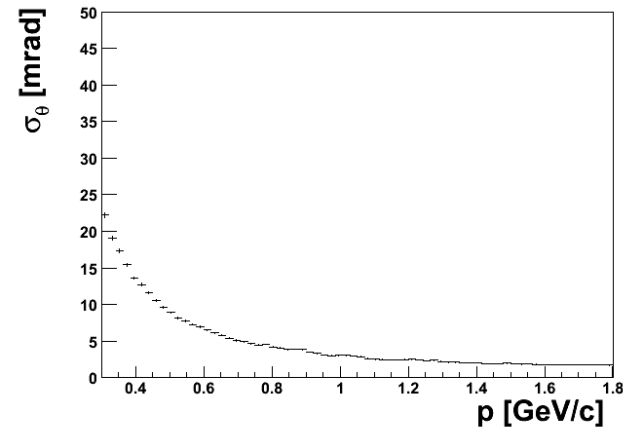
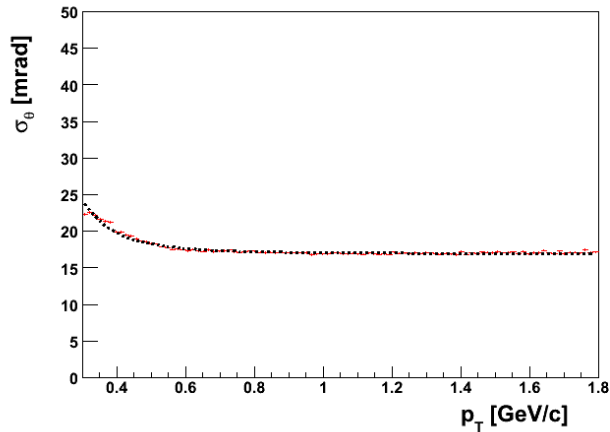
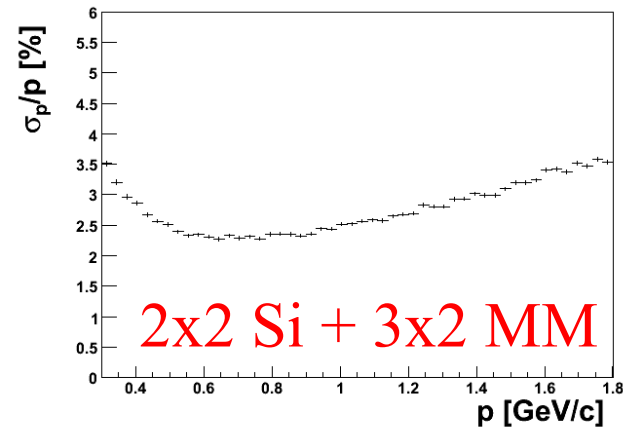
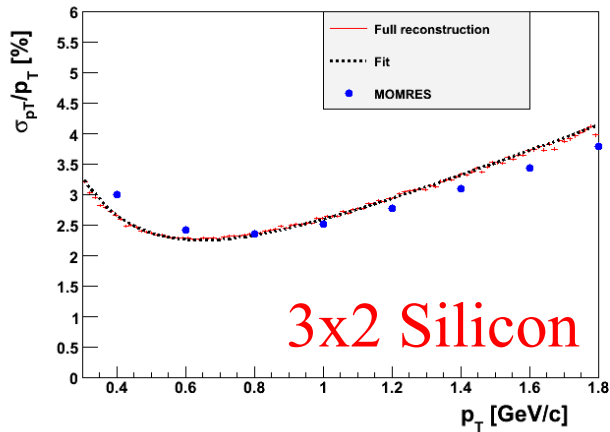


The few remaining fakes can be rejected using the CTOF

Small fraction of fake tracks (mainly « sister » tracks), $\epsilon_{\text{tracking}} > 95\%$

Effect of the Micromegas

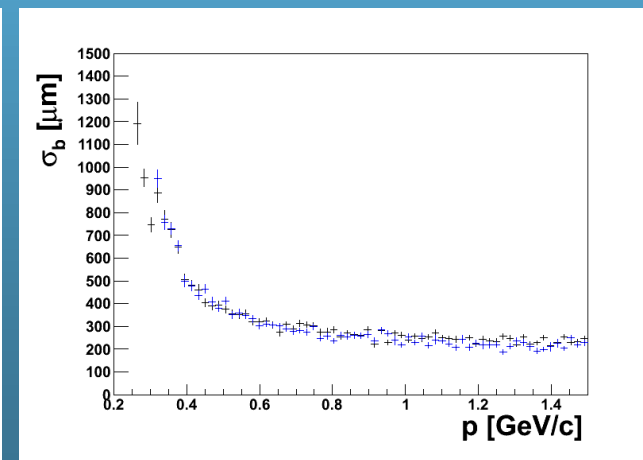
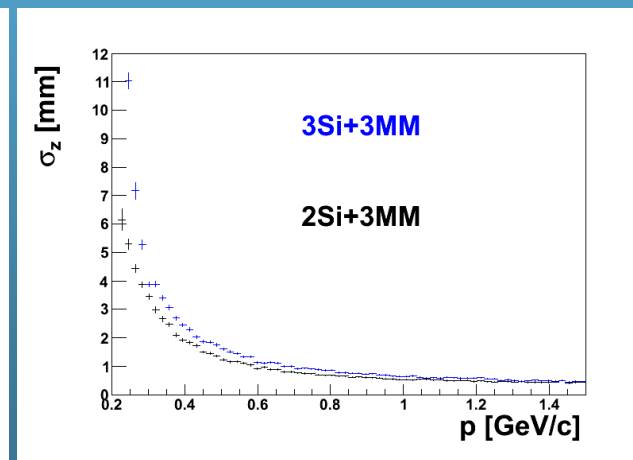
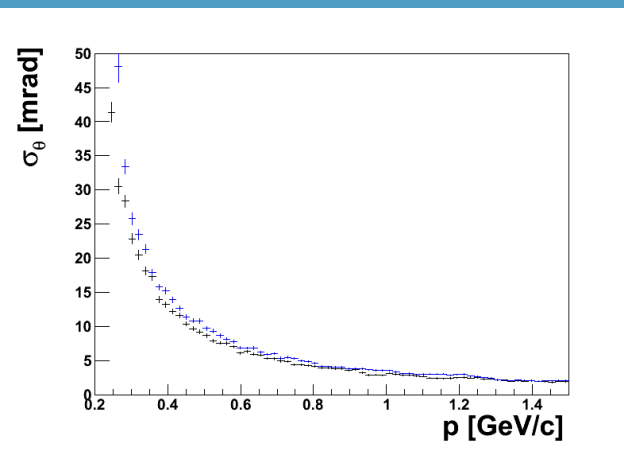
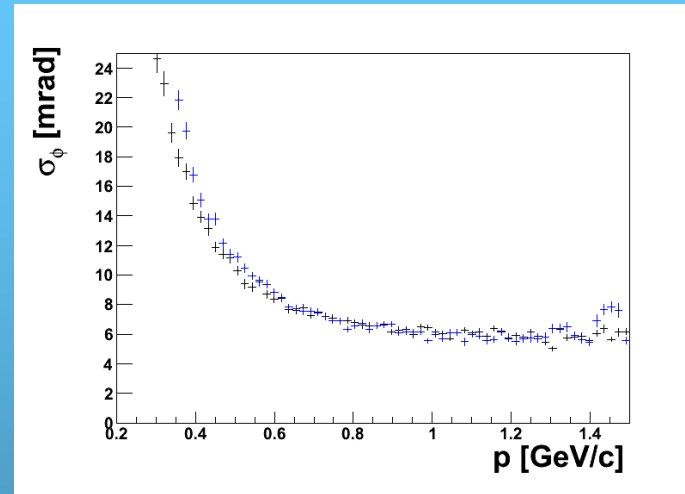
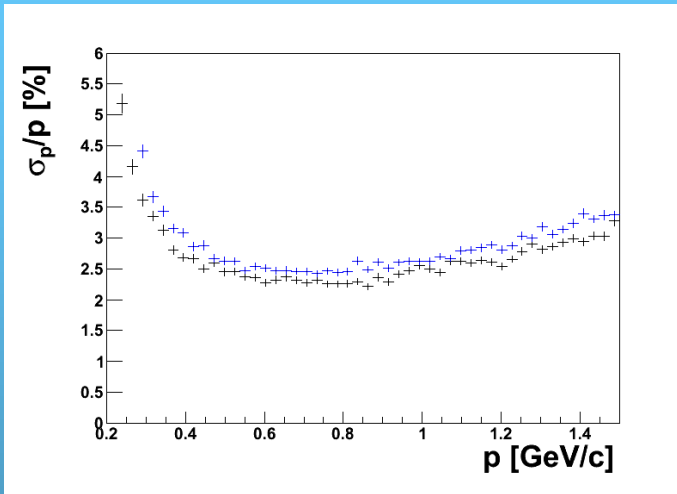
Comparison between Silicon and Silicon+Micromegas designs:



⇒ Much better θ resolution, as expected by previous simulations

Central Tracking

Effect of the number of Silicon layers in the tracking



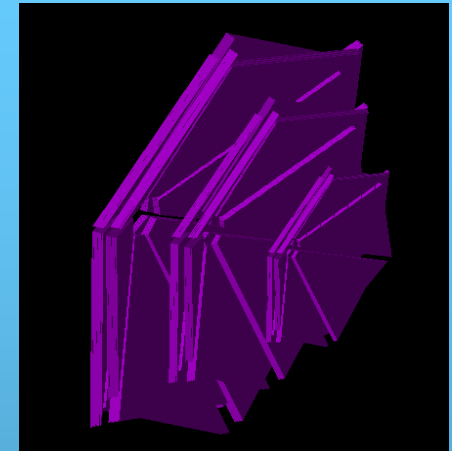
more multiple scattering, but limited effect

Forward tracker (DC, FVT)

Main features:

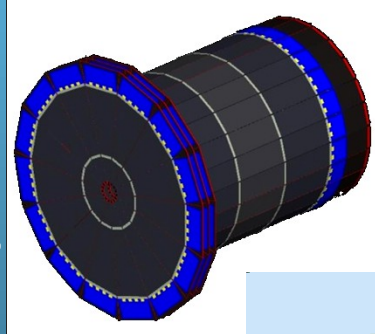
DC

- 3 regions, 3x2 superlayers, 3x2x6 planes
- 6 sectors of 60°
- 6° stereo angle
- plane tilted by 25° wrt the beam axis
- acceptance: 5° °



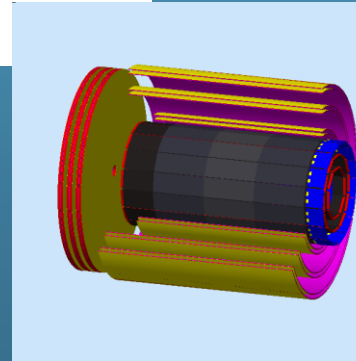
FST

- 3x2 layers
- trapezoidal tiles
- 12° stereo angle
- acceptance: 5° °



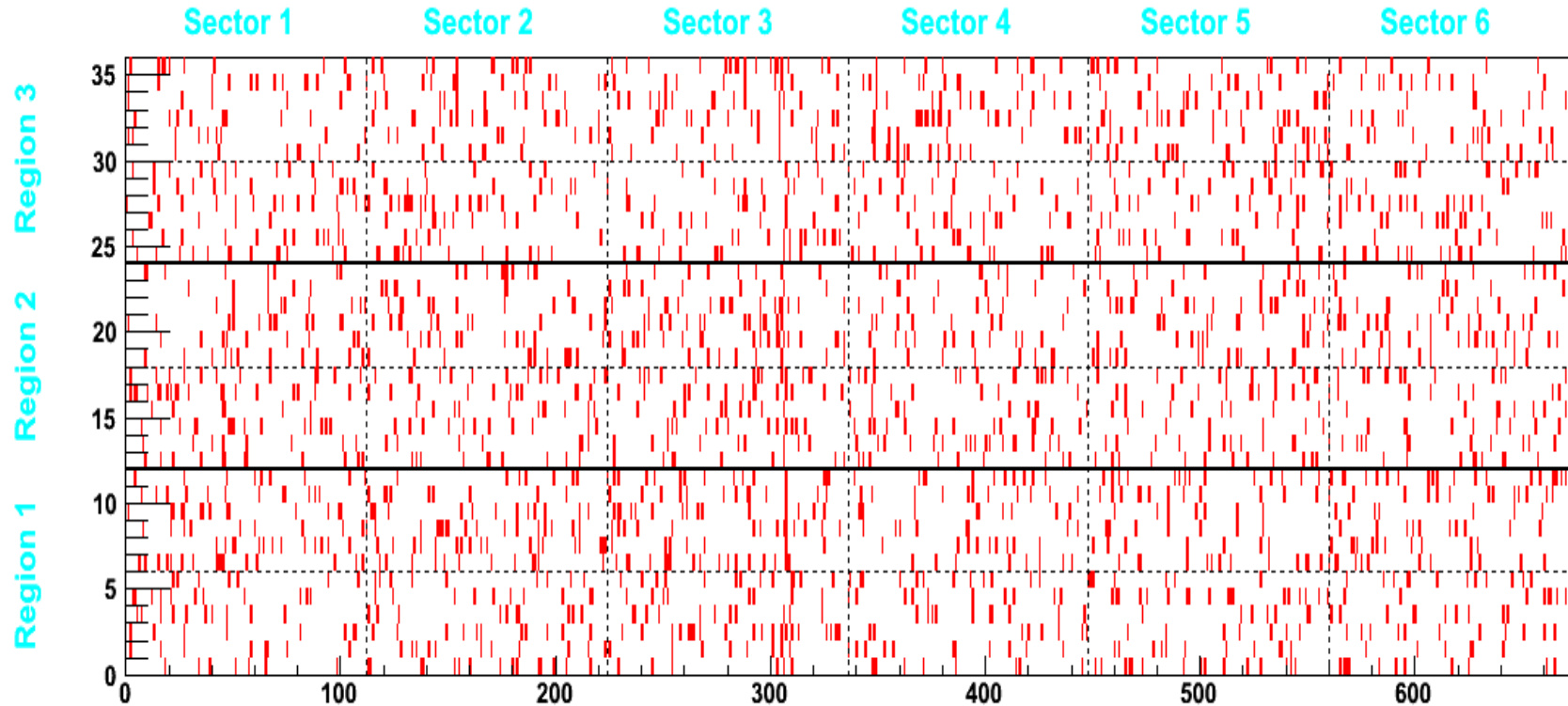
FMT

- 3x2 layers
- circular detectors
- 24 to 45° stereo angle
- acceptance: 5 (2?)° °



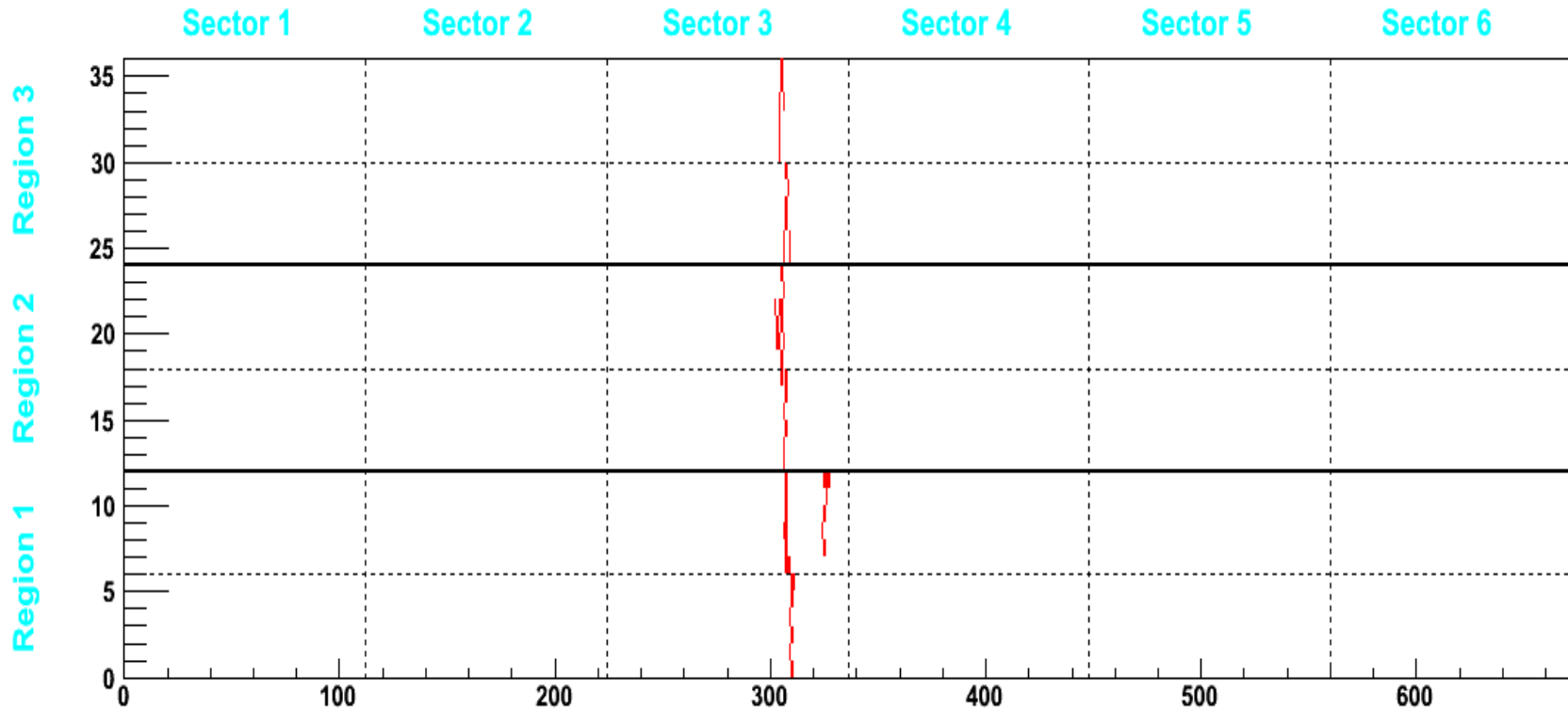
Reconstruction in DC

Starting point (uncorrelated background, just for illustration):



- 1) Find track candidates (patterns)
- 2) Find road(s) in each cluster
- 3) Fit of the track candidates (KF)

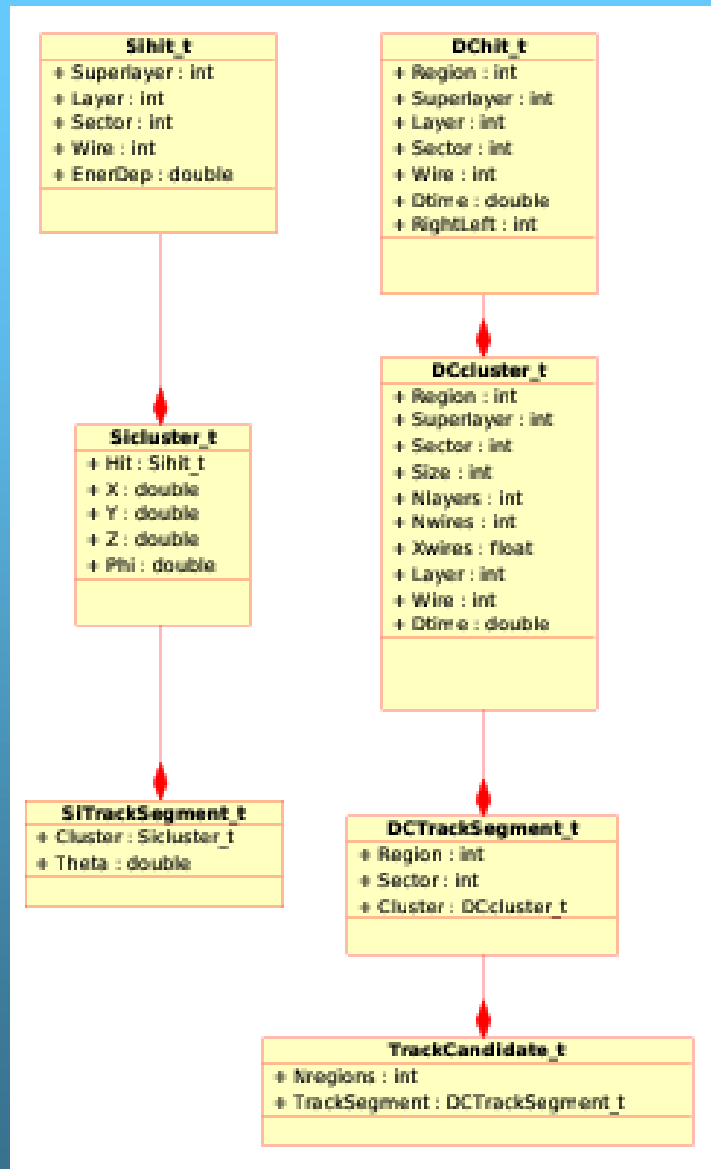
Track finding



- 1) Find clusters (in each superlayer)
- 2) Find track segments (in each region)
- 3) Find track candidates (3 regions)

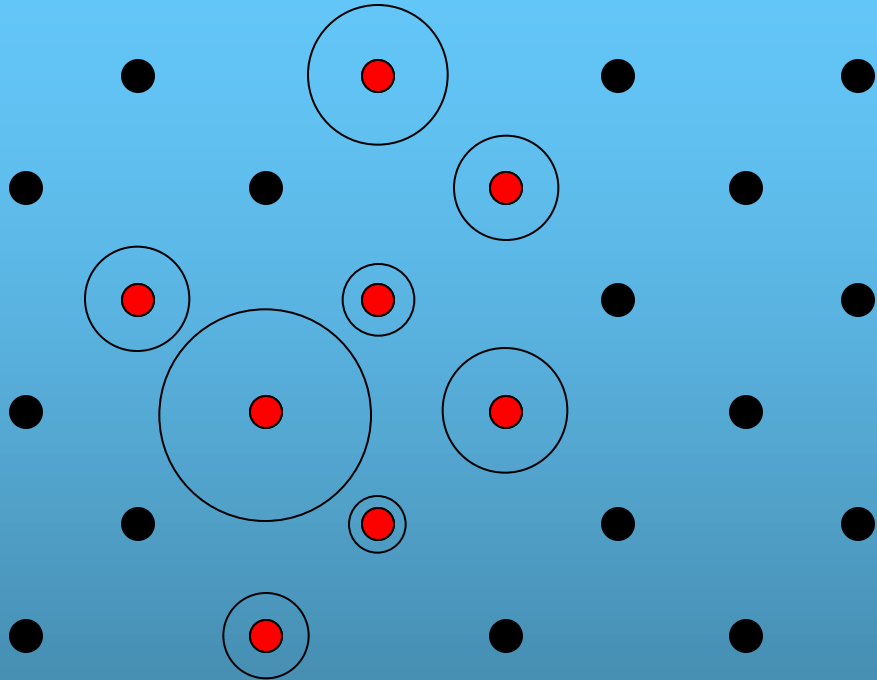
*Corresponding structures in Socrat:
DChit, DCcluster, DCTrackSegment,
DCTrackCandidate*

Structures in Socrat



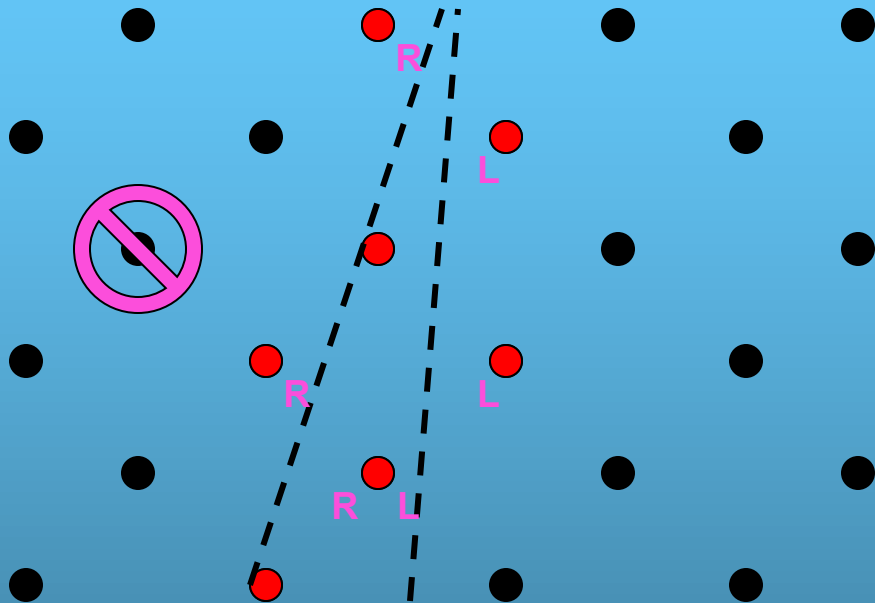
Find roads in clusters

Starting point:



● : wire with signal

Find roads in clusters

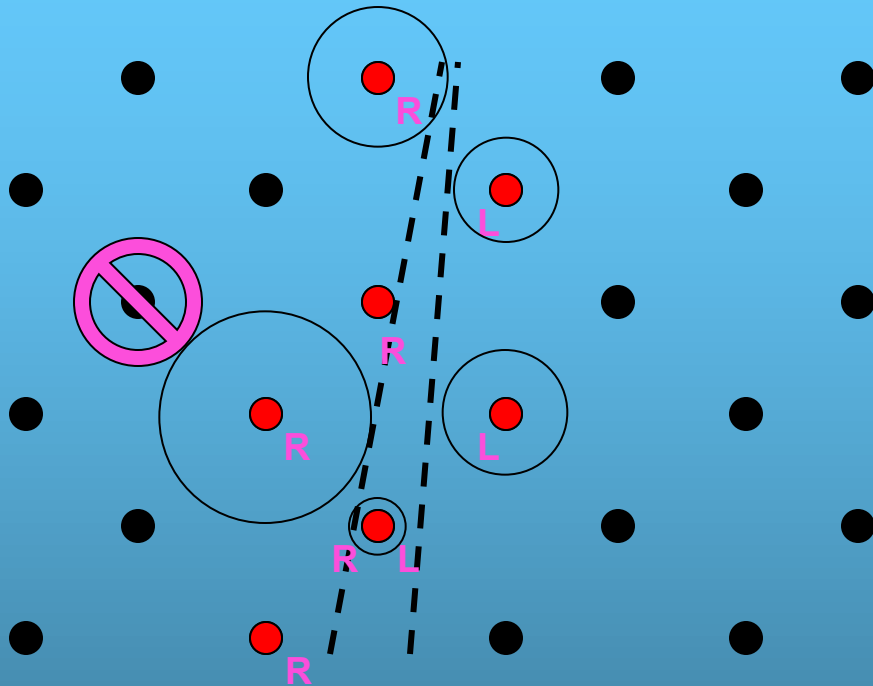


Step 0: fit using wires only
(and large errors)

- reject some hits
- solve some L/R ambiguities

● : wire with signal

Find roads in clusters



● : wire with signal

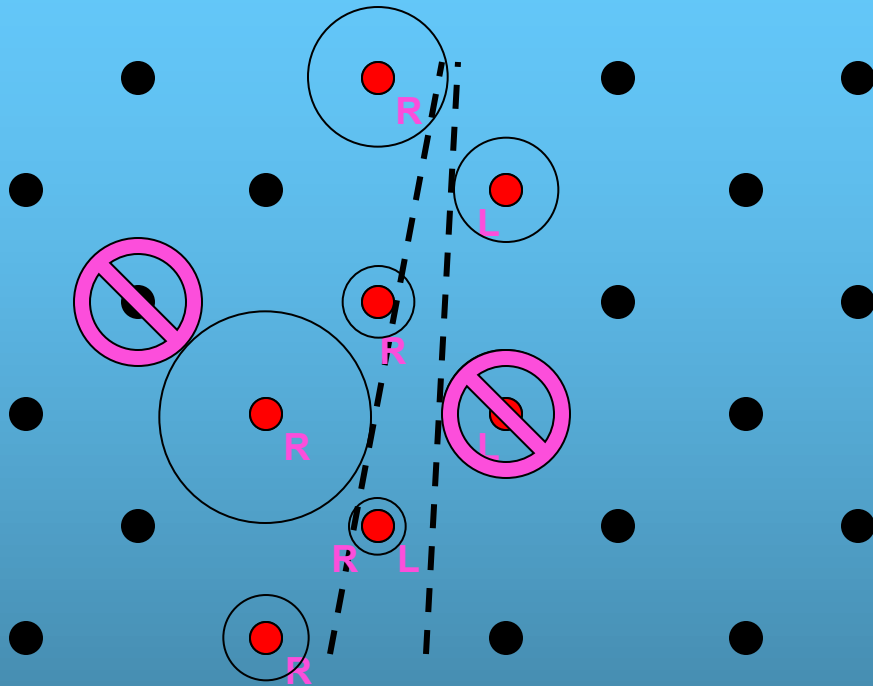
Step 0: fit using wires only
(and large errors)

- reject some hits
- solve some L/R ambiguities

Step i: fit using wires, or
drift dist. if L/R solved

- solve more L/R ambiguities

Find roads in clusters



● : wire with signal

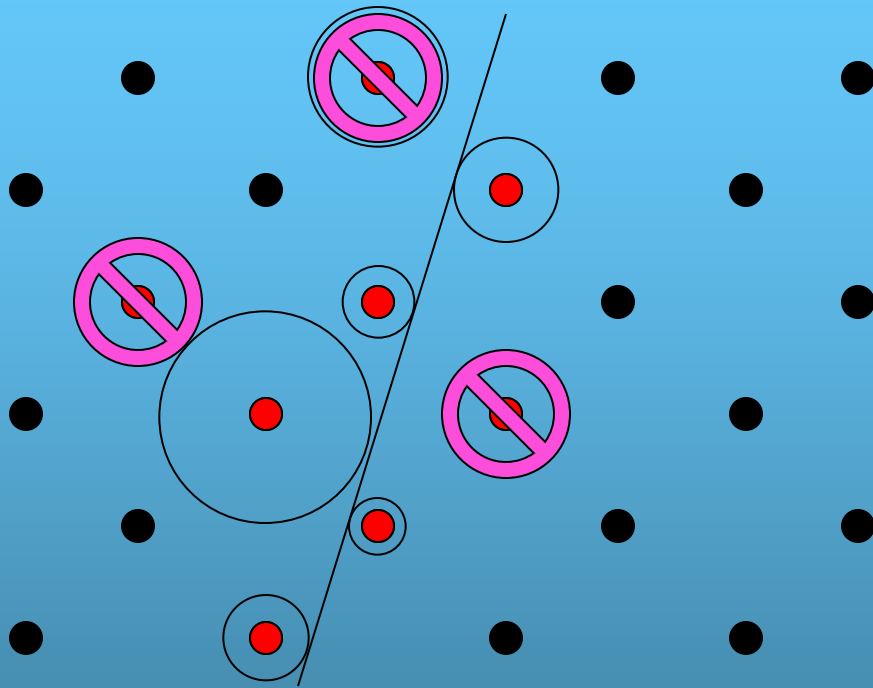
Step 0: fit using wires only
(and large errors)

- reject some hits
- solve some L/R ambiguities

Step i: fit using wires, or
drift dist. if L/R solved

- solve more L/R ambiguities

Find roads in clusters



● : wire with signal

Step 0: fit using wires only
(and large errors)

→ reject some hits
→ solve some L/R ambiguities

Step i: fit using wires, or
drift dist. if L/R solved

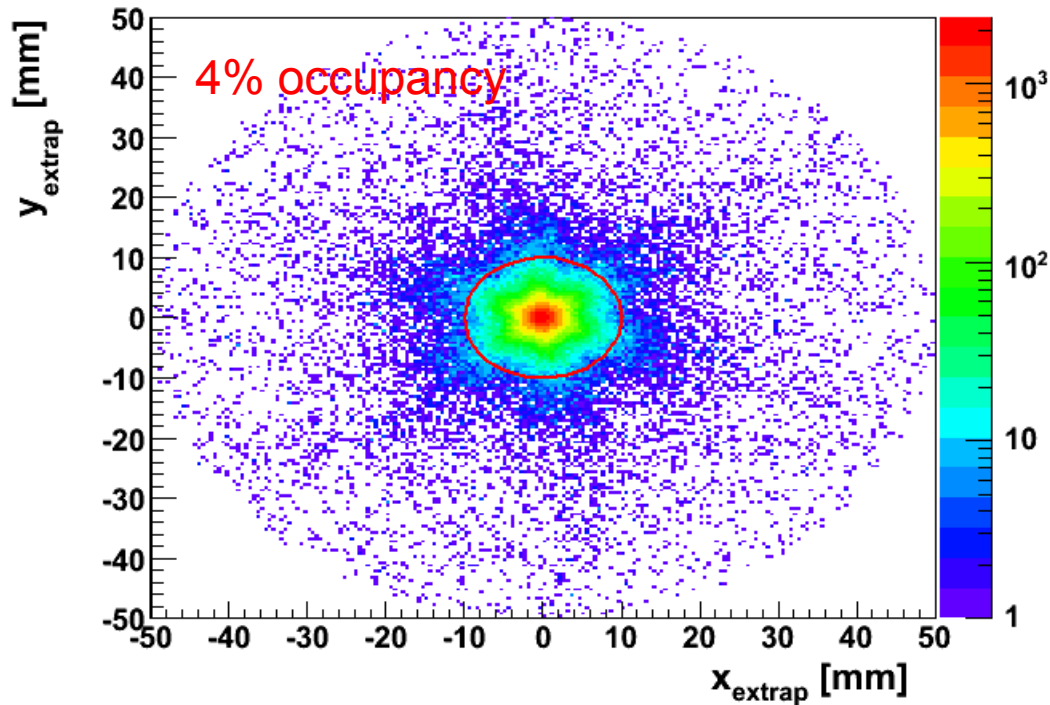
→ solve more L/R ambiguities

Step N(=4): reject bad hits,
solve all L/R

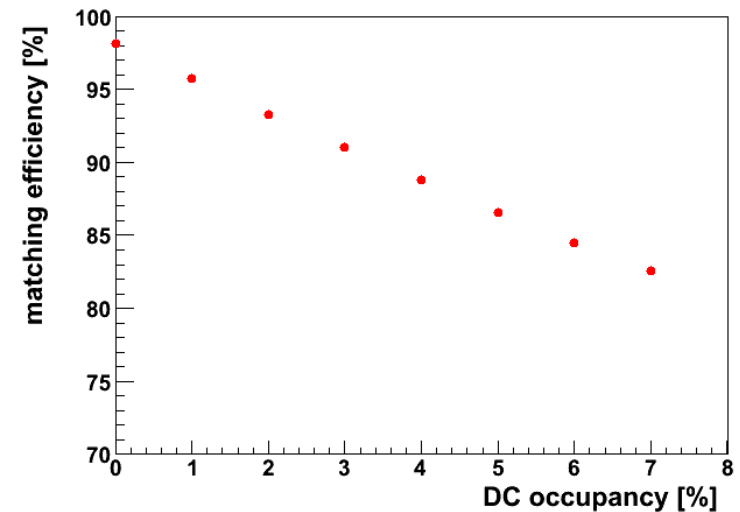
Small probability of mistake (~10%), increase with background

Matching tracks with the FVT

The track obtained in the DC is extrapolated back to the last layer of the FVT. The algorithm then looks for a FVT track segment around this extrap. position ($R=1\text{cm}$)



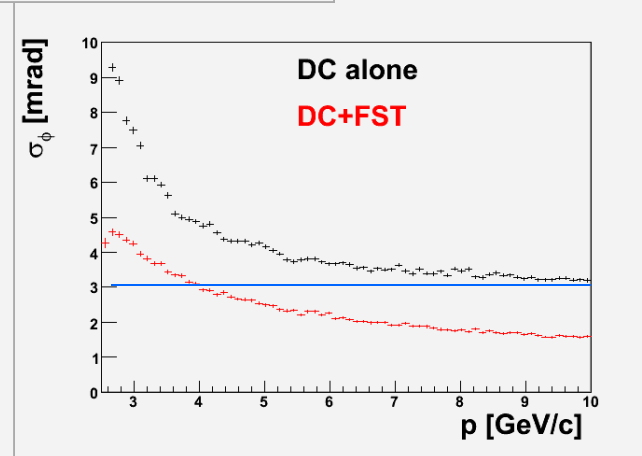
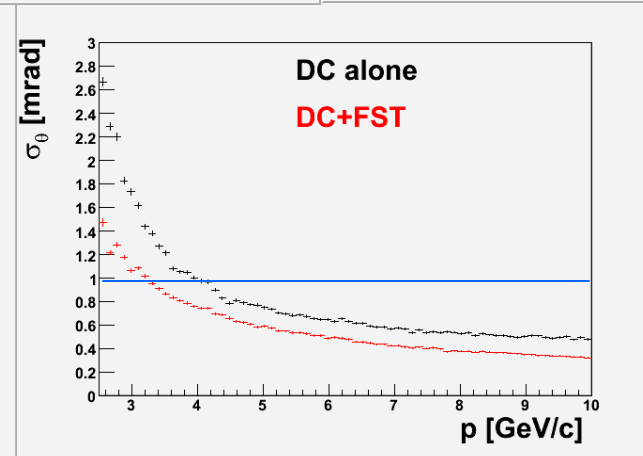
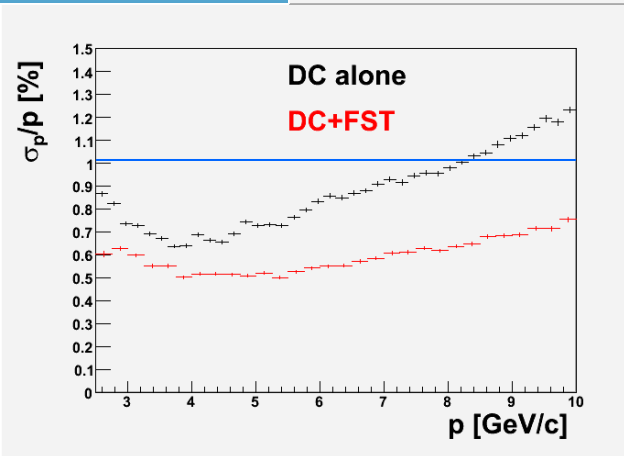
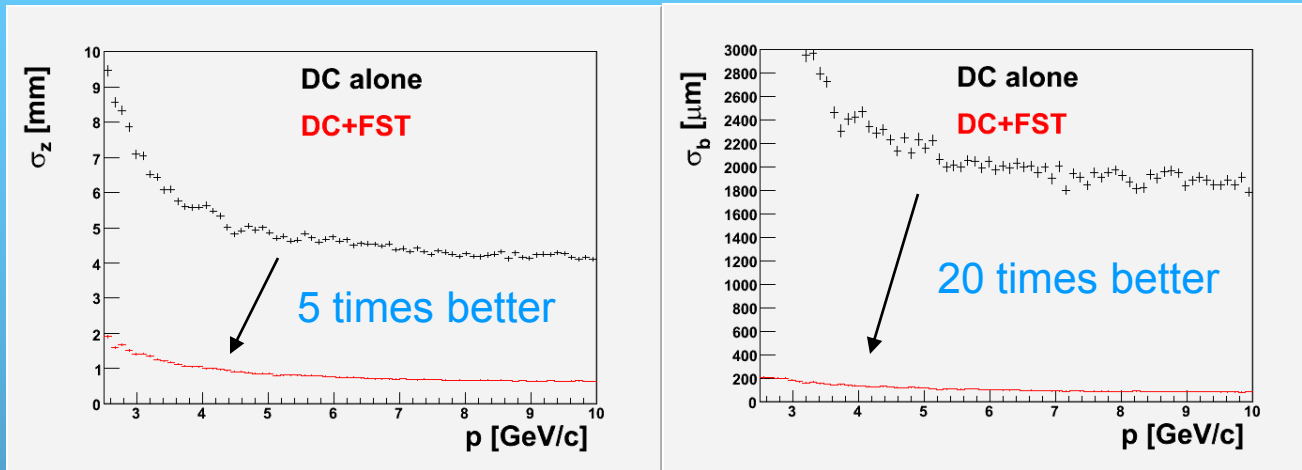
(protons at $\theta = 15^\circ$)



Good DC/FVT matching efficiency, but depends on DC occupancy

Resolutions with DC+FVT

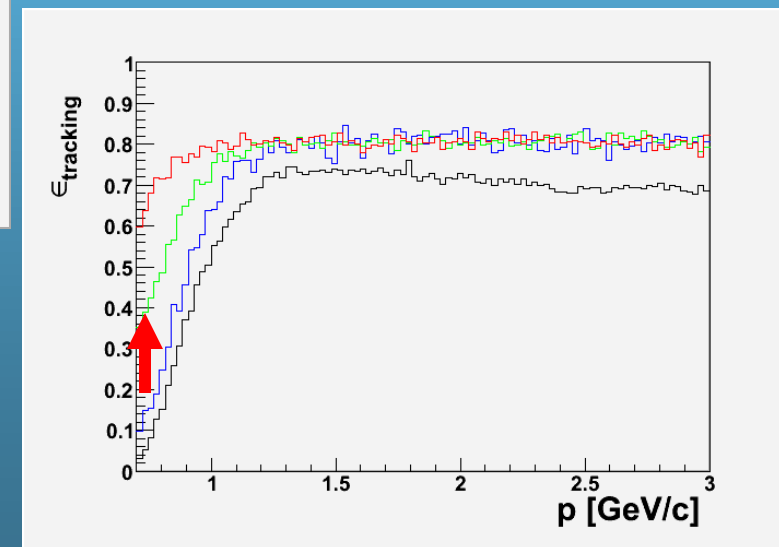
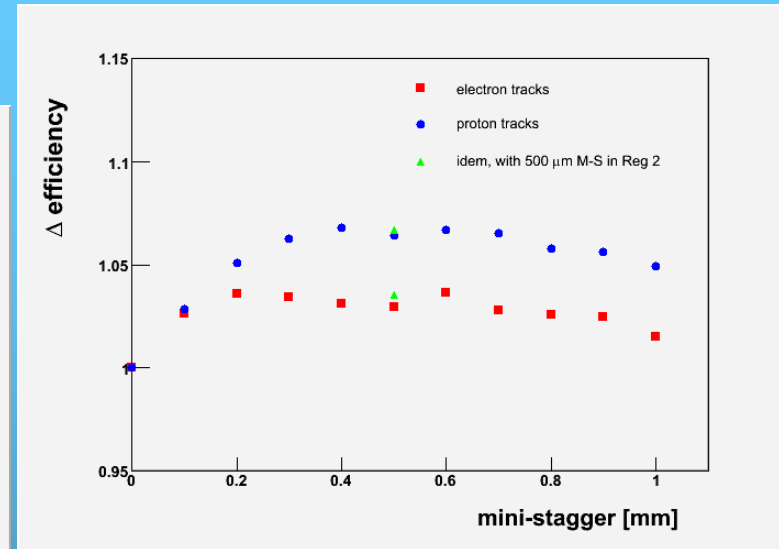
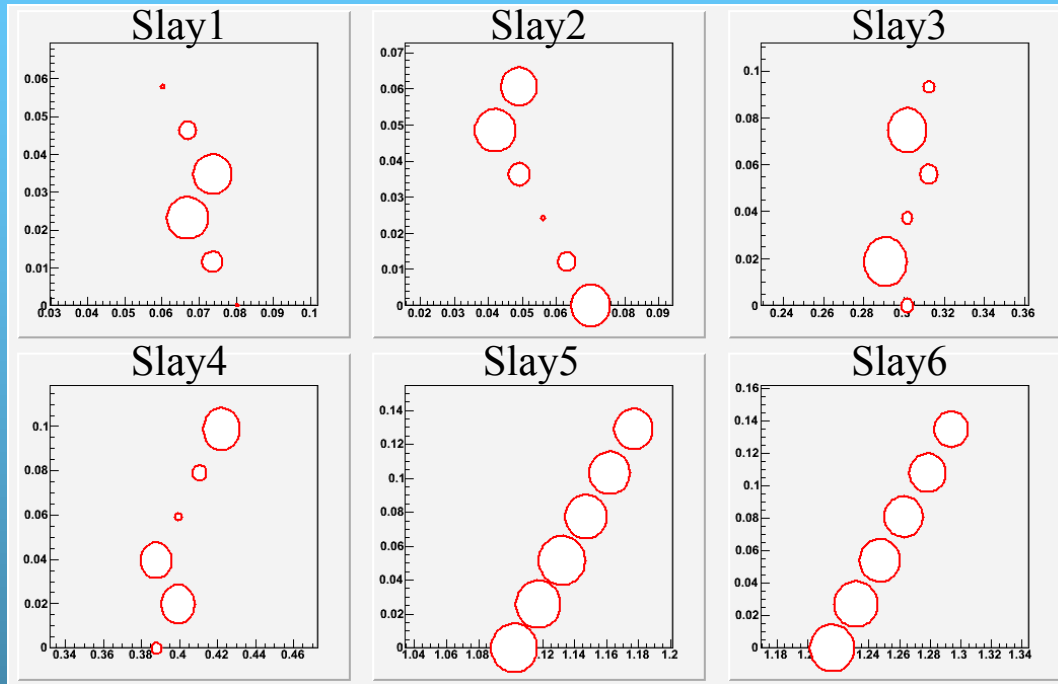
(electrons at $\theta = 15^\circ$, tracks from GEMC):



FVT largely improves the vertex resolution, ϕ , θ and p

Mini-stagger in Region 3

A proton track in DC...



Significant increase of efficiency
at small momentum

Momentum bias and energy loss

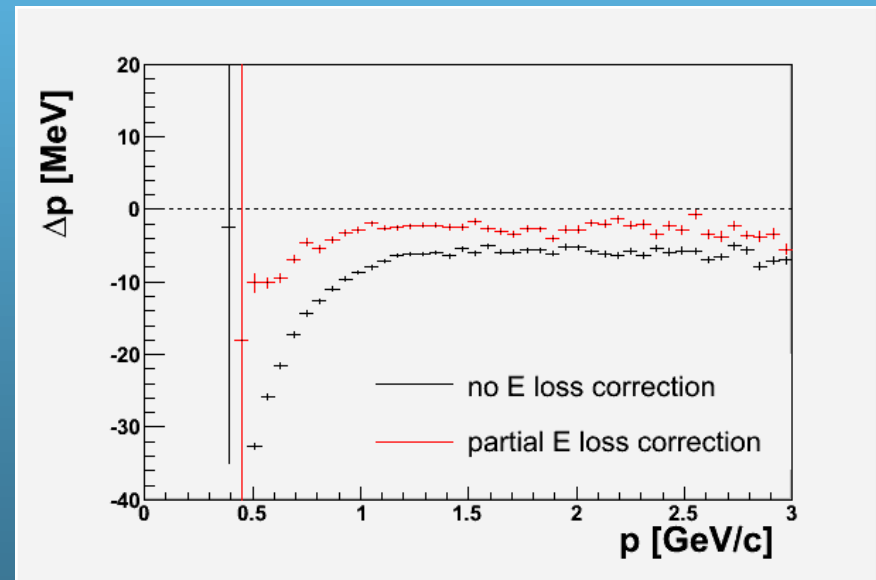
Energy loss through material is well known...

$$-\frac{dE}{dx} = K Z^2 \frac{1}{A \beta} \left(\frac{1}{2} \ln \left(\frac{2 m_e c^2 \beta \gamma^2 T_{\max}}{I^2} \right) - \beta \right) \quad (\text{Bethe-Bloch})$$

... and can be easily taken into account step by step in the Kalman Filter.

So far:

- DC (argon gas)
- Air
- FST (silicon+carbon fibers)
- Target (LH2)



Conclusion

helped the design of several detectors:

- strip layout of the BST (zigzag to graded stereo angle)
- mini-stagger in DC Region 3 (300 microns)
- geometry of the Micromegas FVT at small acceptance (in progress)

code available on svn

see CLAS note 2008-015 for more details

runs with Geant4 events (or internal track generator)

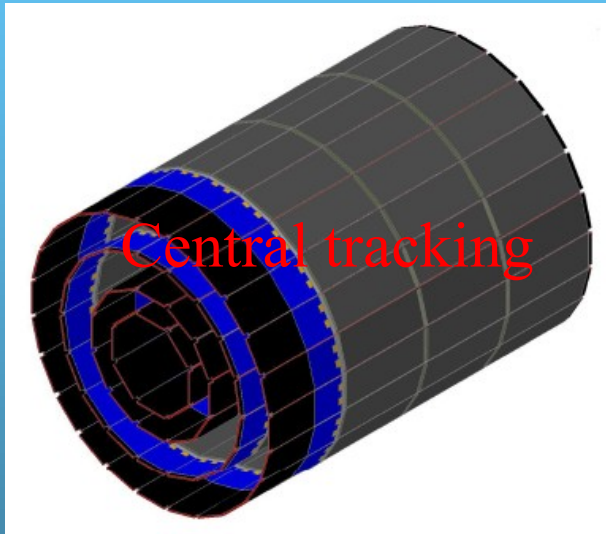
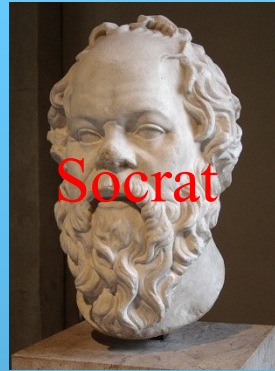
user friendly script to run Gemc+Socrat on the batch (Simu.pl)

two (unwanted) sons with the same algorithms translated in different languages:

- JSocrat
- Scrat

. but work is still needed on the algorithms!

Additional slides



Central tracking - backup

Acceptance

Stereo angle

Overlap setup

Acceptance
optimization

Uncertainty
on B field

Background



Forward tracking - backup

FST alone

FST spacing

FST
background

DC – resol &
background

DC – L/R
ambiguity

FST
fake tracks

DC+FST –
p resolutions

FST
acceptance



Kalman Filter - backup

Initialization

Multiple
scattering



Socrat - backup

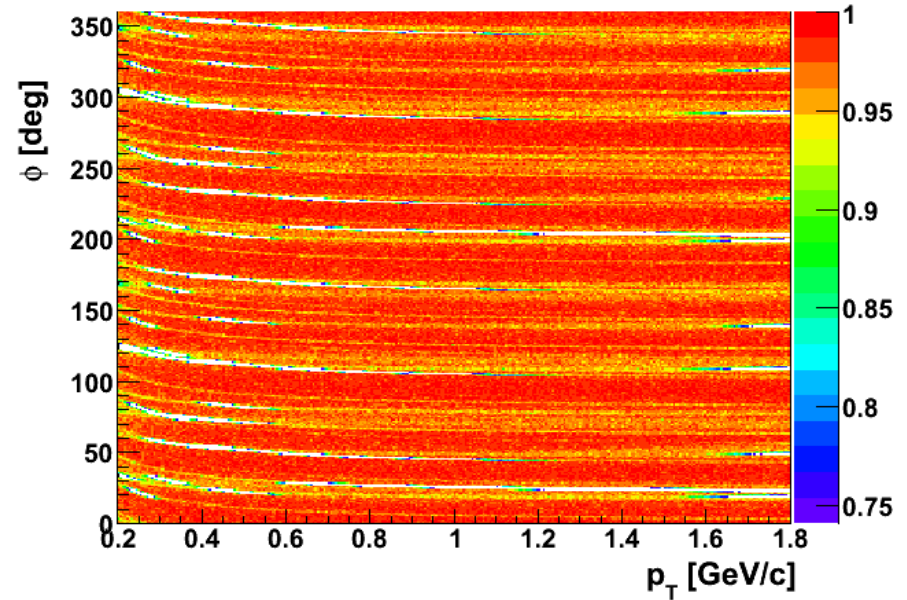
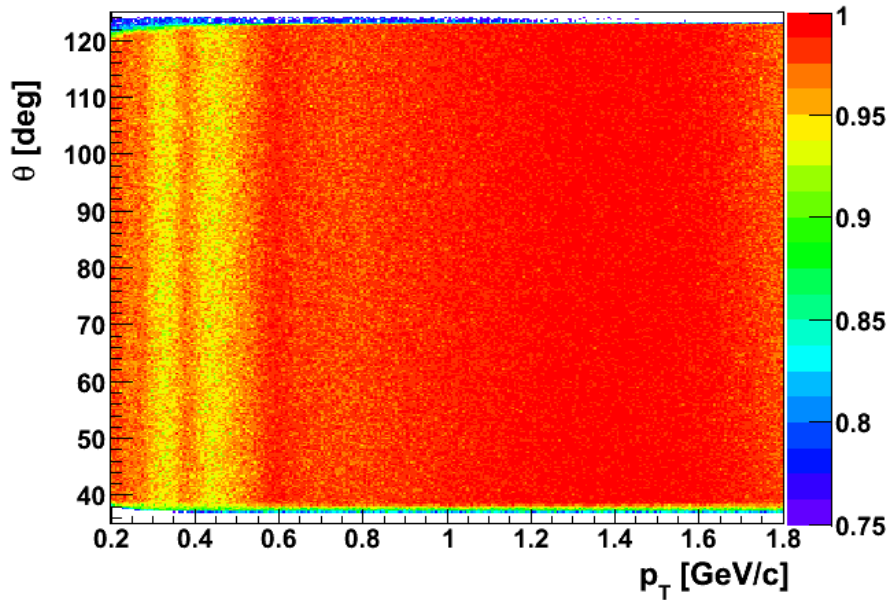
Misalignments

Generation
routine



BST - acceptance

Track reconstruction requires at least 3 (out of 4) superlayers



$$\langle \varepsilon \rangle \approx 94 \%$$

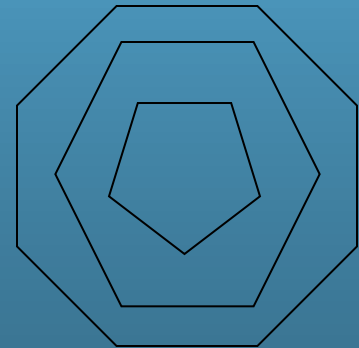
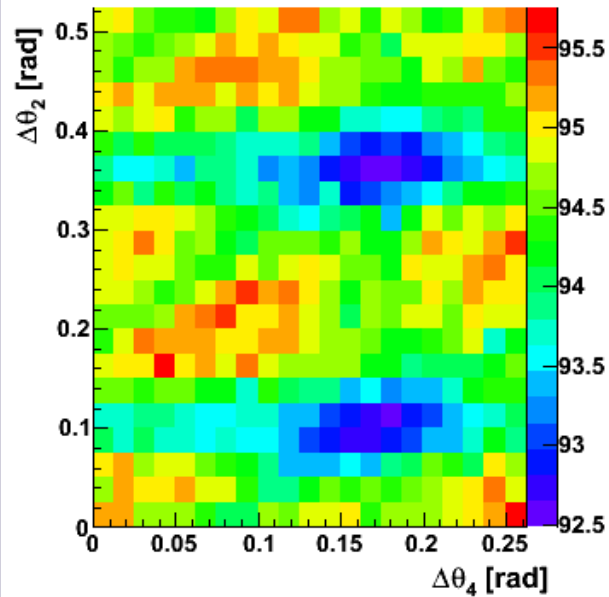
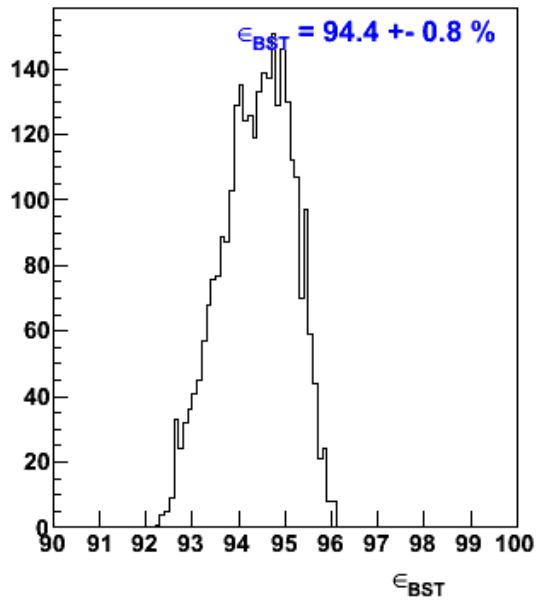
(thin target)



BST – acceptance optimization

One can increase the acceptance efficiency by rotating the different double layers

BST - acceptance efficiency

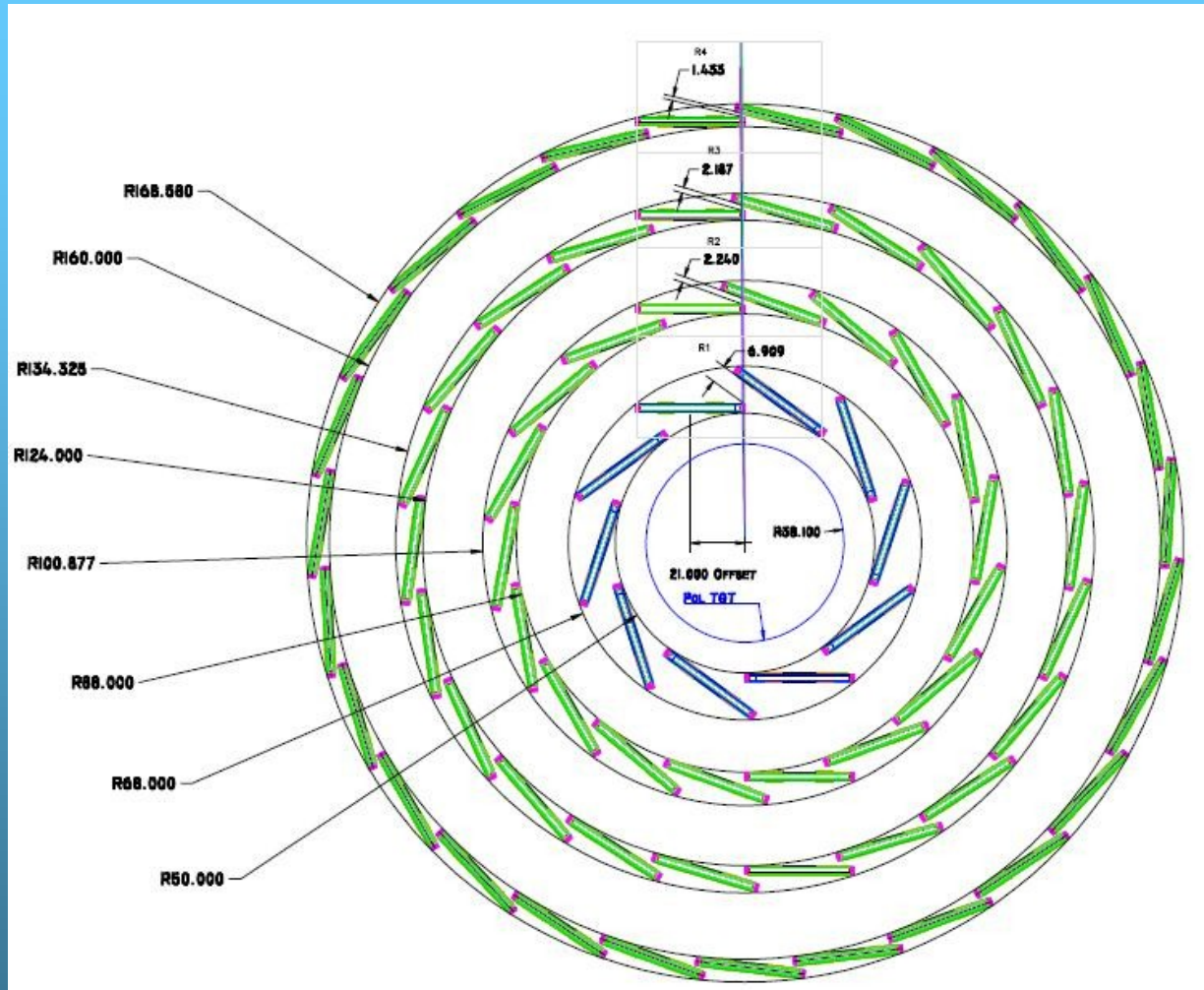


BST – stereo angle

α_S	$\sigma_1(p_T, \%)$	$\sigma_1(\varphi, \text{mrad})$	$\sigma_1(\theta, \text{mrad})$	$\sigma_1(z, \text{mm})$	Track cand / event
3°	2.69	4.50	18.9	2.35	2.95
6°	3.04	5.09	12.0	1.43	4.49
9°	3.26	5.48	9.77	1.12	5.85
15°	4.05	6.66	8.74	0.93	6.55



BST – overlap design



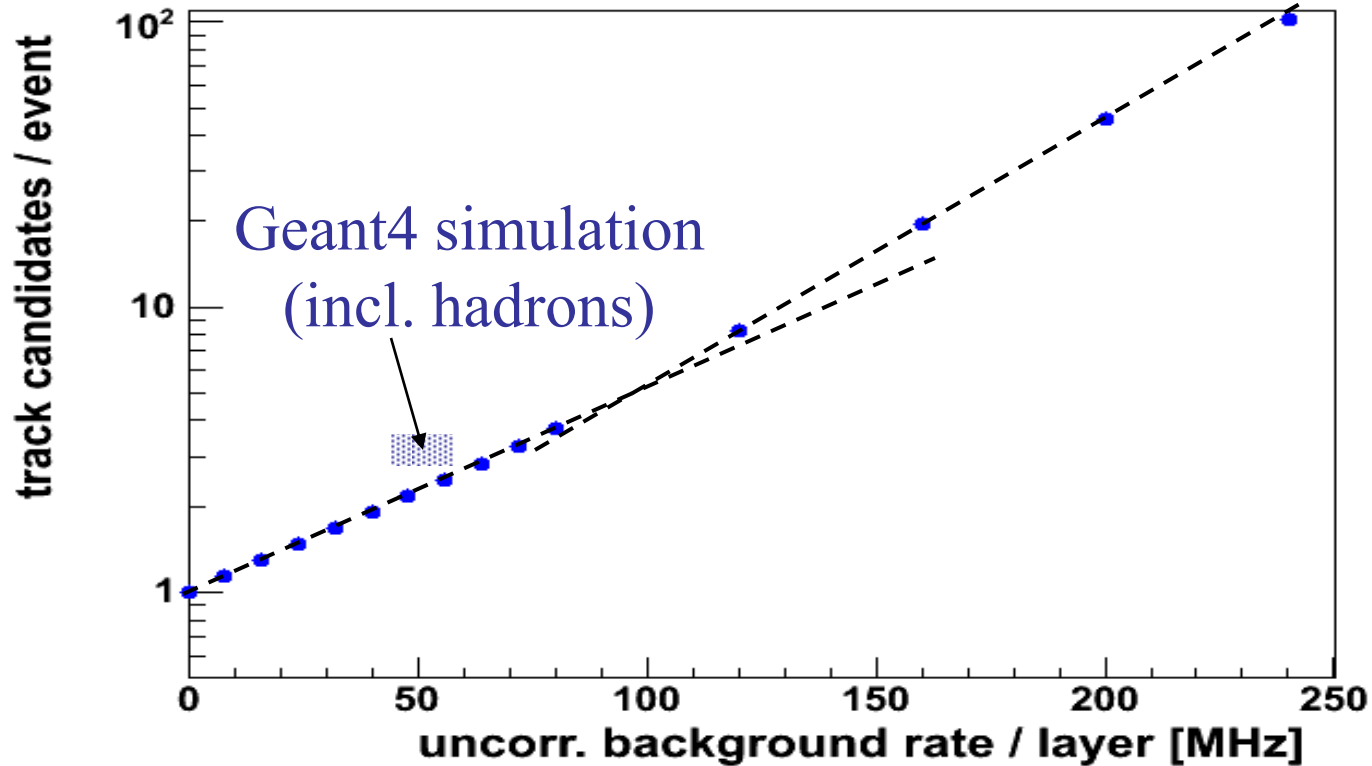
BST – uncertainty on B field

B field	σ_1 (p_T ,%)	σ_1 (φ ,mrad)	σ_1 (θ ,mrad)	σ_1 (z,mm)
0.99%	2.71	4.67	19.1	2.41
1.00%	2.69	4.50	18.9	2.35
1.01%	2.83	4.69	19.1	2.41



BST – background studies

(using the uncorrelated background from the tracking code)

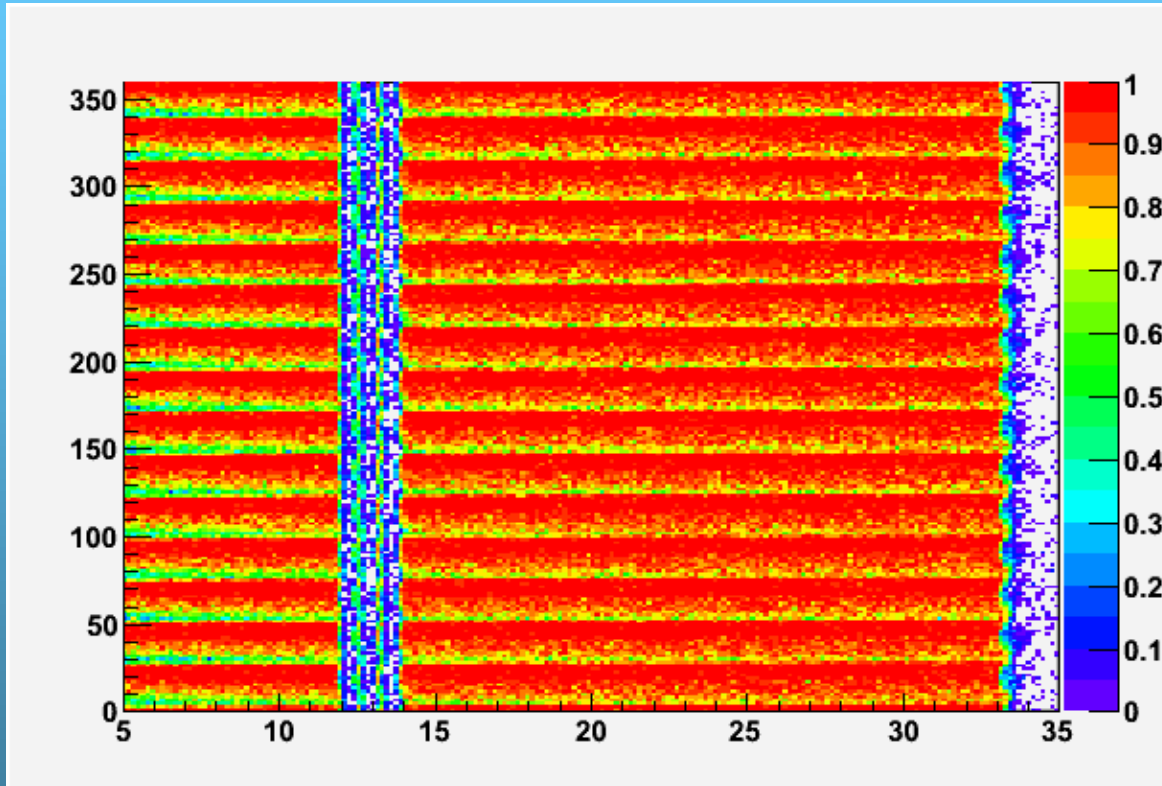


Good agreement with Geant4 background, gives the behaviour with the rate



FST - acceptance

Track reconstruction requires 3 out of 3 superlayers

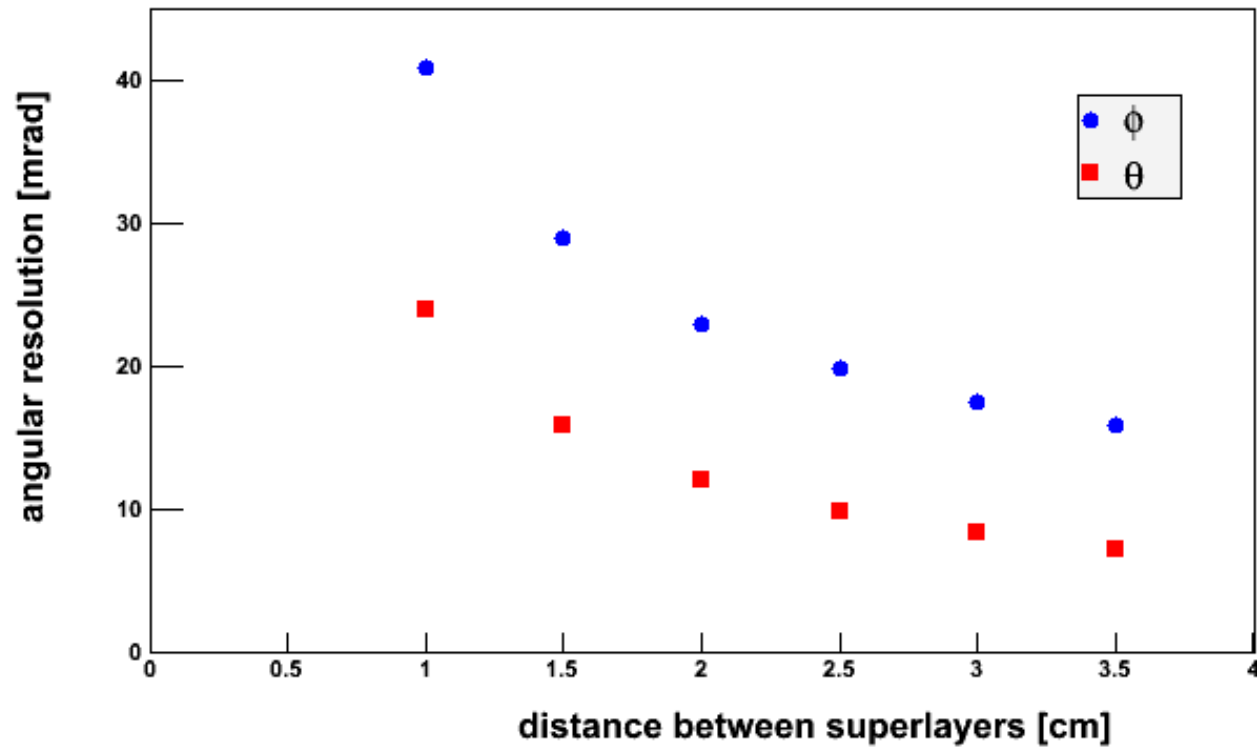


$$\langle \varepsilon \rangle \approx 32 \%$$

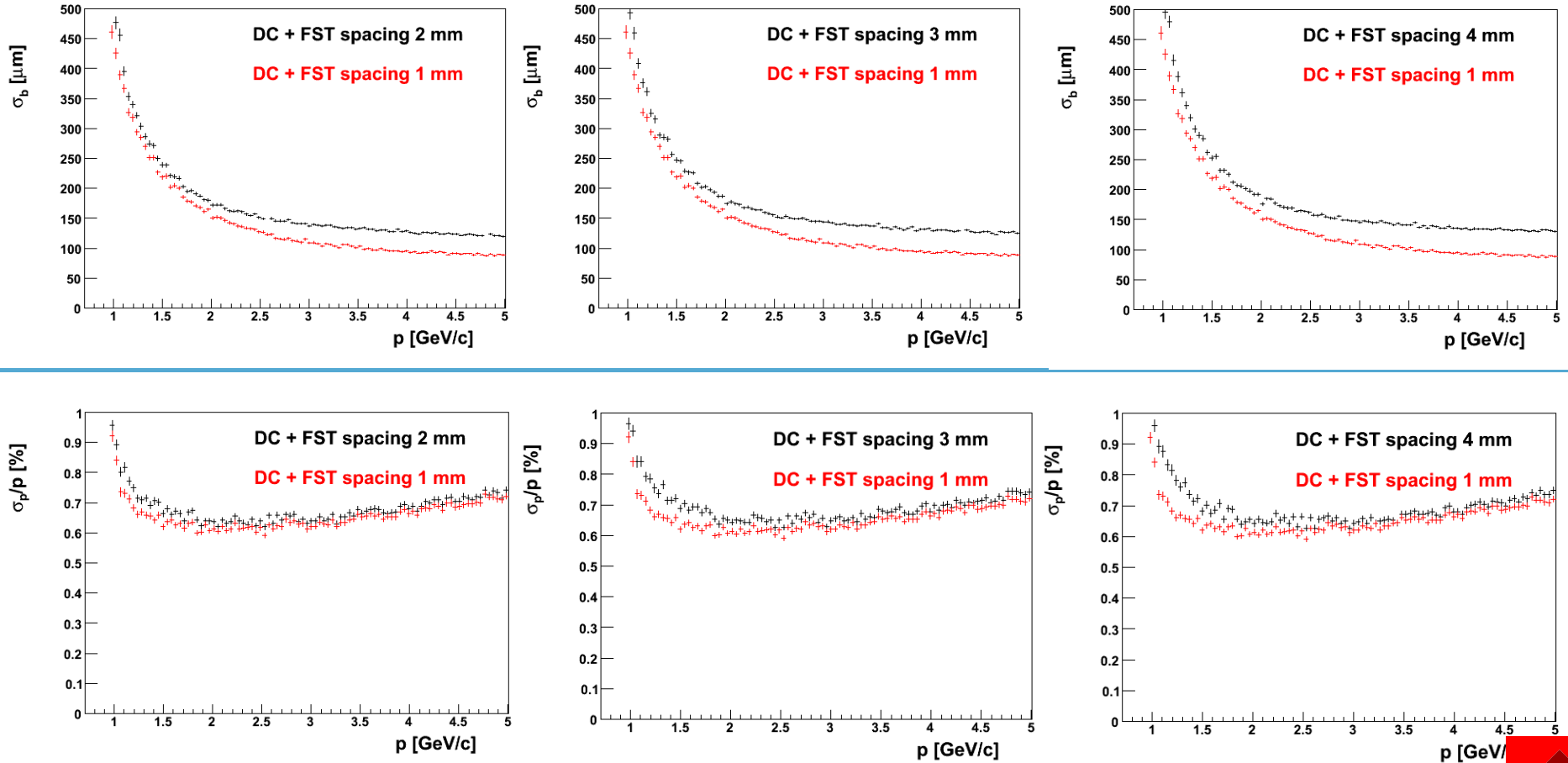
(thin target)



FST alone



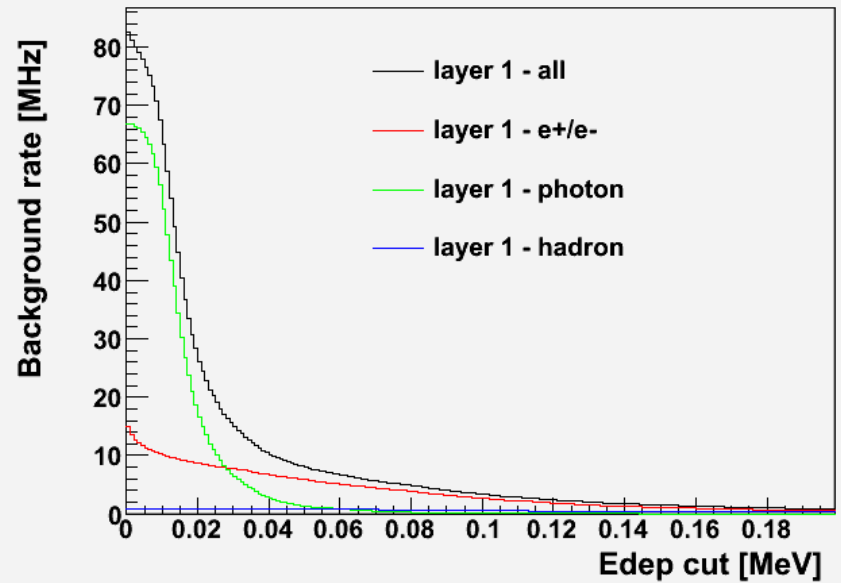
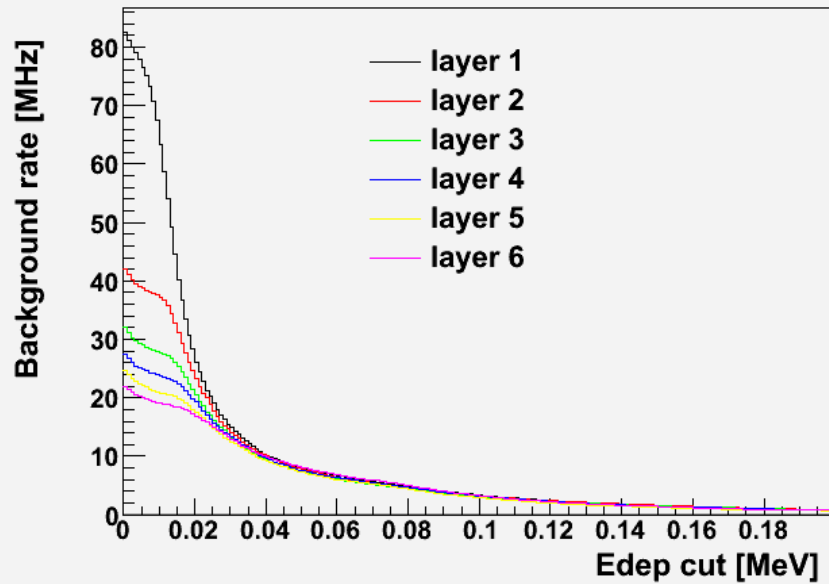
FST – spacing of superlayers



→ Better to have small distance between the superlayers

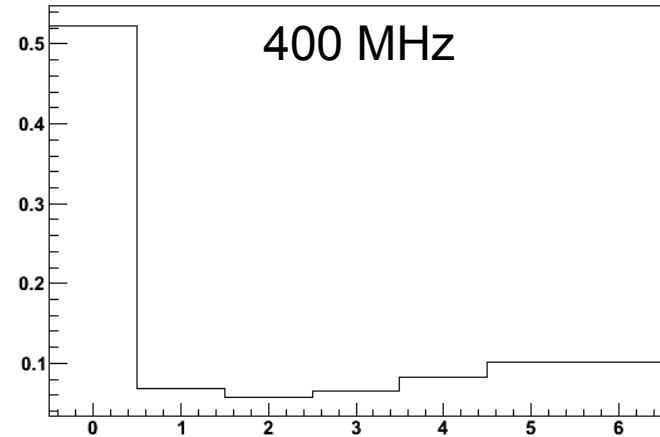
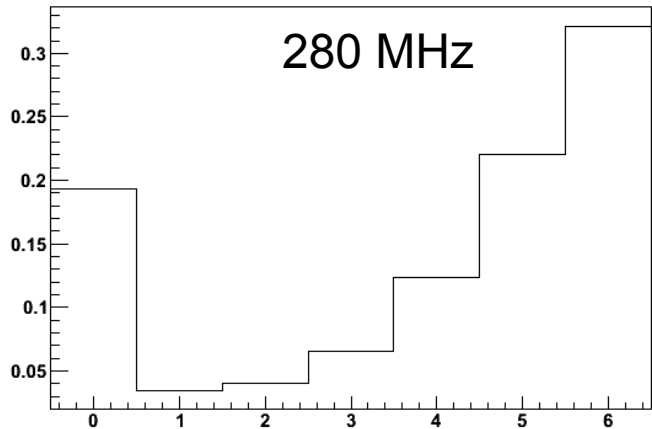
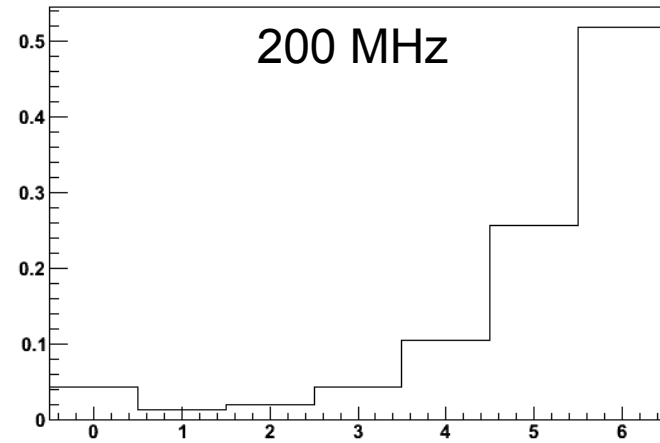
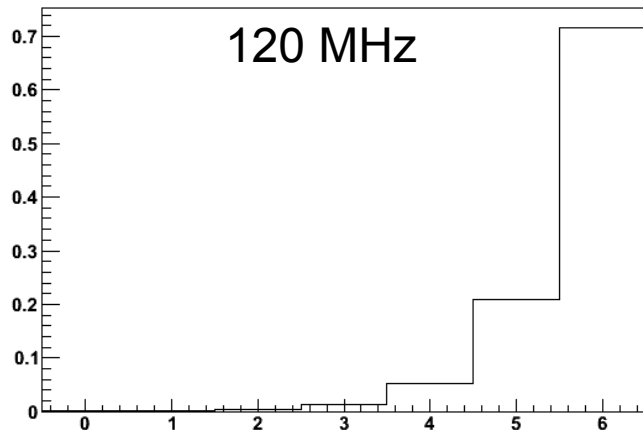


FST – background



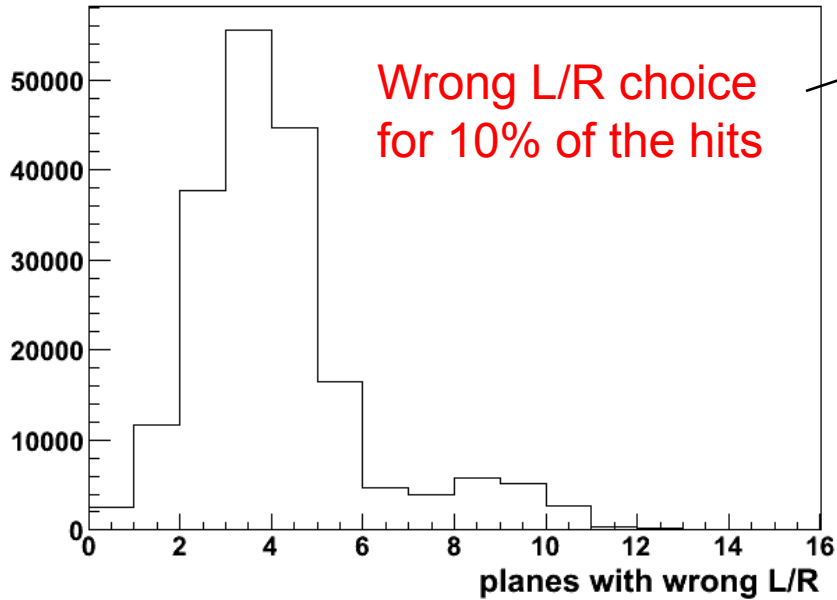
FST - fake tracks

Number of common hits of track candidates with the real track:

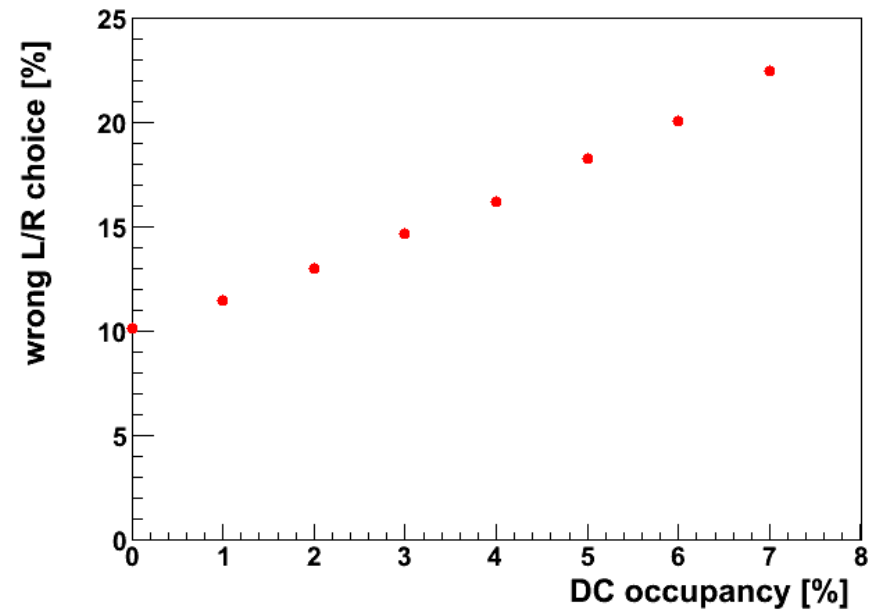


DC – L/R ambiguity

Results (protons at $\theta = 15^\circ$):



Almost no effect on the resolution

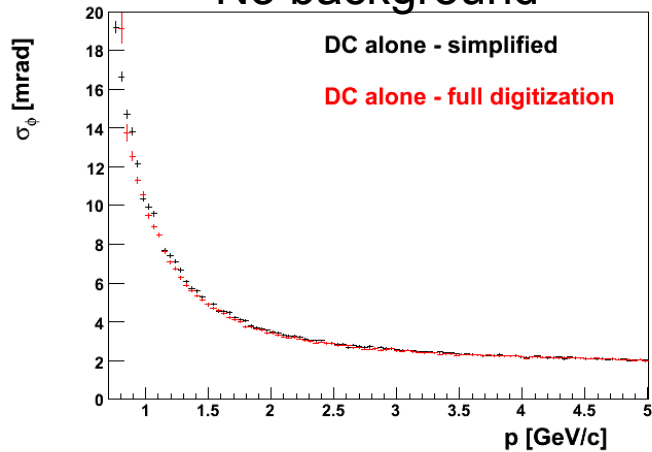


Occupancy degrades the L/R determination (expected!)

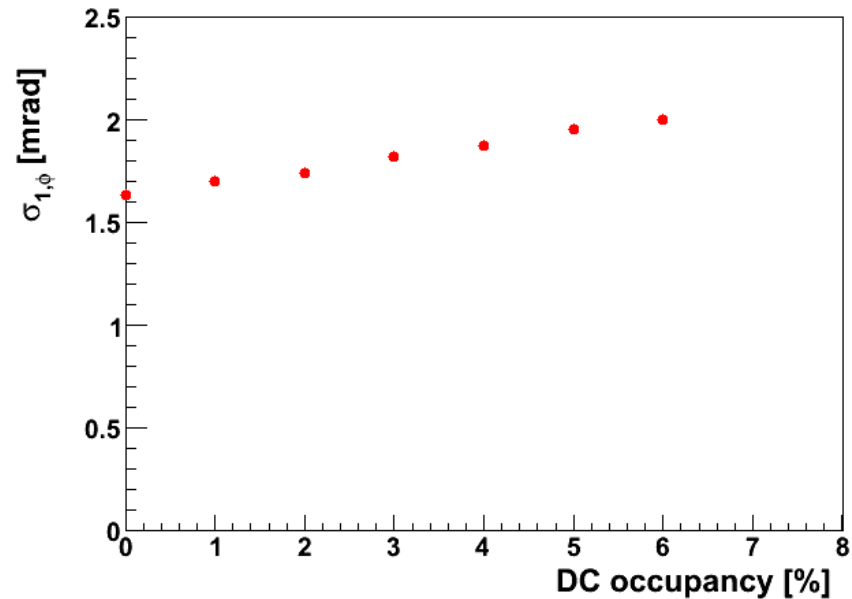


DC – resolution & background

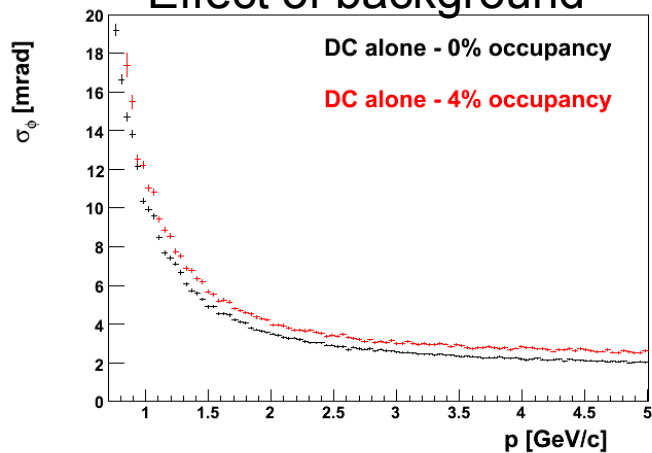
No background



10% mistake on L/R
has indeed no impact



Effect of background

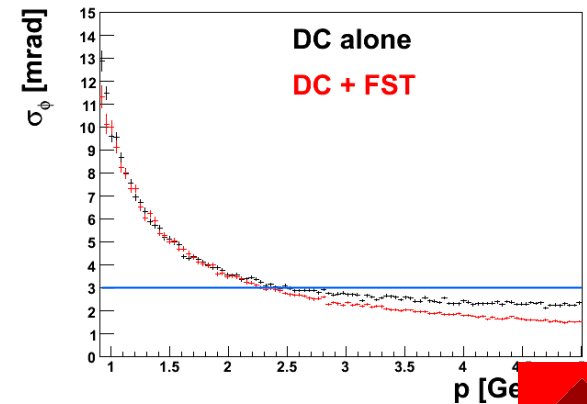
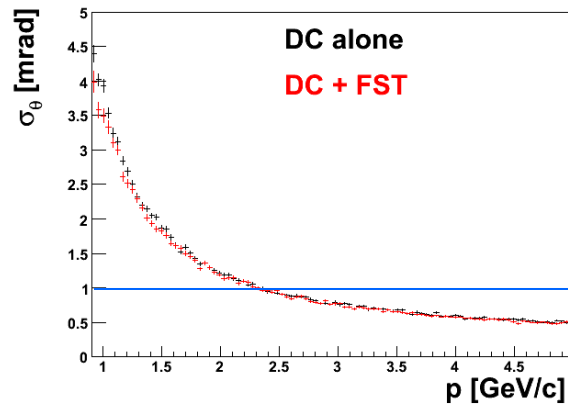
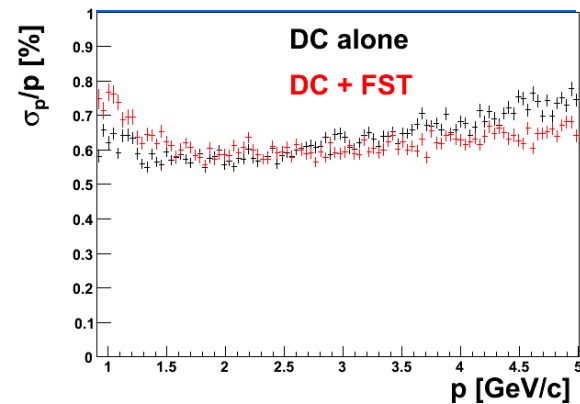
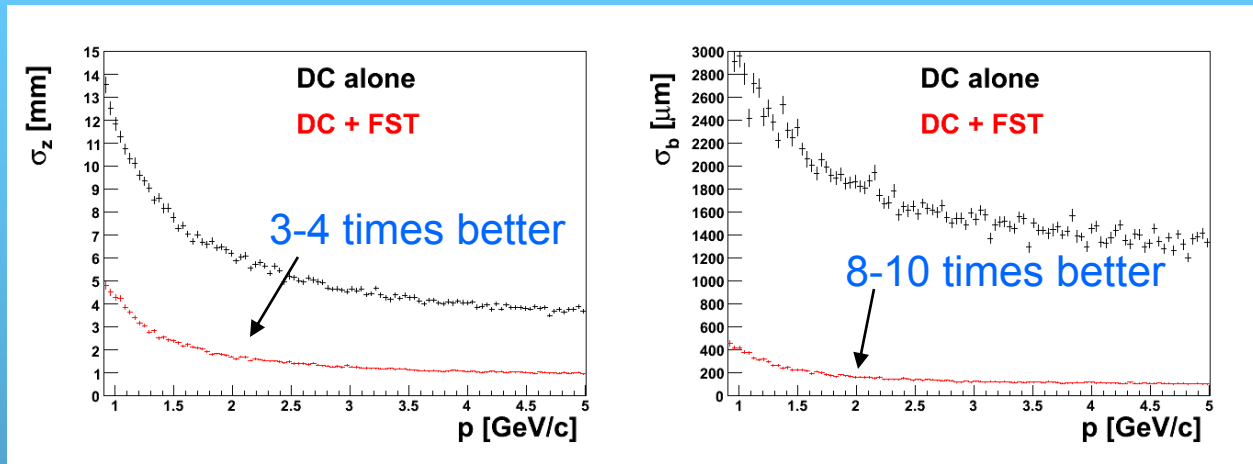


4% occupancy degrades the resolution by $\sim 15\%$



DC+FST – resolution with protons

(protons at $\theta = 15^\circ$):



Much better vertex resolution with FST (and ϕ resolution at high p)



KF - initialization

- Central tracking:

- Measurement at \sim constant radius

$$\rightarrow \vec{r}^T = (\varphi, z, \vec{p})$$

- Homogeneous field (solenoid)

\rightarrow estimation of \vec{x}_0 with helical track

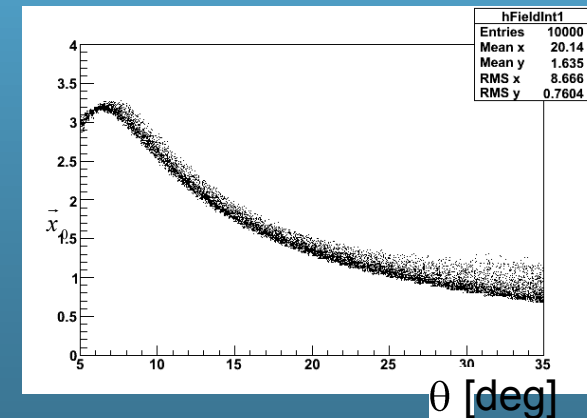
- Forward tracking:

- Measurement at \sim constant z

$$\rightarrow \vec{r}^T = (x, y, u_x, u_y, q / p)$$

- Toroidal field

\rightarrow parameterization of $\int B dl$



KF – multiple scattering

The multiple scattering can be « easily » taken into account in the KF:

$$\hat{C}_k^{k+} = \hat{F}_k \cdot \hat{C}_k \cdot \hat{F}_k^T + \hat{Q}_k$$

$$\hat{Q}_{i,j} = \sigma^2(\theta) * \left(\frac{\partial x_i}{\partial \theta} \frac{\partial x_j}{\partial \theta} + \frac{\partial x_i}{\partial \theta} \frac{\partial x_j}{\partial \theta} \right)$$

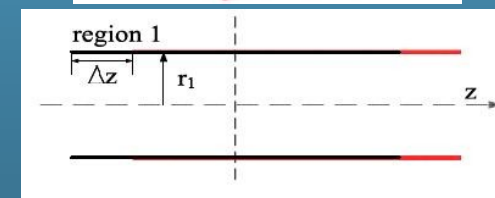
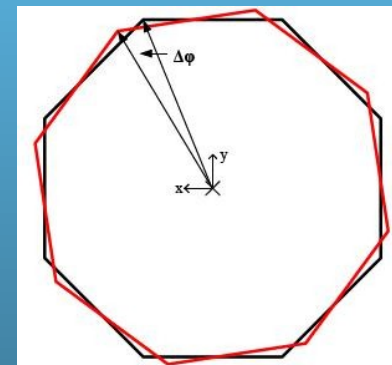
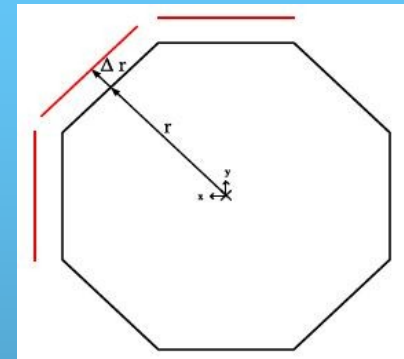
$$\hat{Q} = \sigma^2(\theta) \begin{pmatrix} 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & (1+x'^2) & x'y' & 0 \\ 0 & 0 & x'y' & (1+y'^2) & 0 \\ 0 & 0 & 0 & 0 & 0 \end{pmatrix} \quad \hat{Q} = \sigma^2(\theta) \begin{pmatrix} 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & p_y^2 + p_z^2 & -p_x p_y & -p_x p_z \\ 0 & 0 & -p_x p_y & p_x^2 + p_z^2 & -p_y p_z \\ 0 & 0 & -p_x p_z & -p_y p_z & p_x^2 + p_y^2 \end{pmatrix}$$



Socrat - Misalignments

Socrat allows the study of misalignments in various parameters

- For each DC region:
 - * Distance to the target ($\sim \Delta z$)
 - * Tilt around the x_i axis (nominal: 25°)
 - * Position of the 1st wire ($\sim \Delta x$)
- For each FST superlayer:
 - * Azimuthal position ($\Delta\phi$)
 - * Position along the beam axis (Δz)
- For each magnet (solenoid & torus):
 - * Position in space ($\Delta x, \Delta y, \Delta z$)
- For each BST superlayer:
 - * Distance to the beam axis (ΔR)
 - * Azimuthal position ($\Delta\phi$)
 - * Position along the beam axis (Δz)



Socrat – Generation routine

The tracking code has a routine to generate its own events:

- taking into account the Mult. Scat. (not from air)
- using the available field maps
- with full digitization (for Si and DC)
- with **uncorrelated** background
- in case of central & forward tracking, tracks are generated at the same vertex position

much faster than Geant4 (no physics!)



Misalignment studies

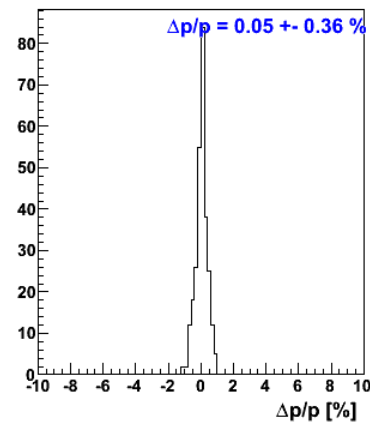
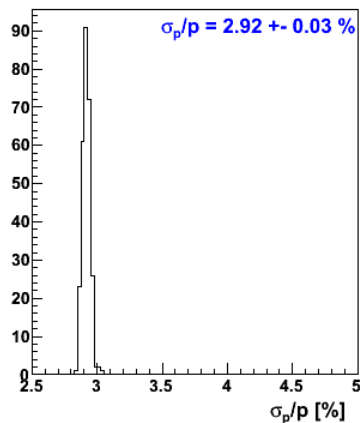
Socrat can generate misalignments in BST, FST, DC, magn. fields

Ex: effect of BST misalignments on momentum

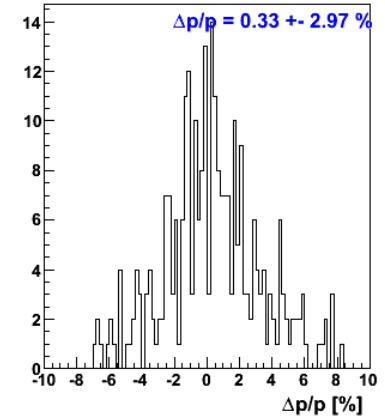
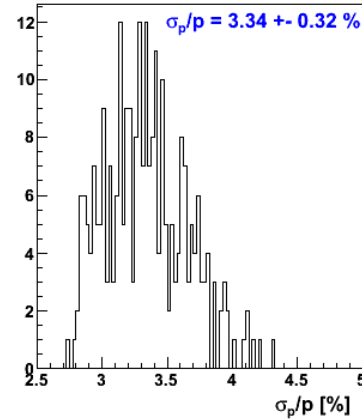
$\Delta R=50$ microns, $\Delta z=20$ microns, $\Delta\phi=0.1$ mrad

$\Delta R=200$ microns, $\Delta z=100$ microns, $\Delta\phi=1$ mrad

BST - $\sigma_R = 50$ microns - $\sigma_z = 20$ microns - $\sigma_\phi = 0.1$ mrad -



BST - $\sigma_R = 200$ microns - $\sigma_z = 100$ microns - $\sigma_\phi = 1$ mrad -



⇒ Give constraints on the accuracy of detectors alignment