# Proton Form Factor Ratio, $G_{E}^{P}/G_{M}^{P}$ From Double Spin Asymmetries

Spin Asymmetries of the Nucleon Experiment (E07-003)

**Analysis Updates** 





Anusha Liyanage HU Group Meeting (December 04, 2012)

# Outline

- Introduction
- Physics Motivation
- Experiment Setup
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  - HMS Detector
  - Polarized Target
- Elastic Kinematic
- Data Analysis & MC/SIMC Simulation
- Conclusion



# Introduction Nucleon Elastic Form Factors

- Defined in context of single-photon exchange.
- Describe how much the nucleus deviates from a point like particle.
- Describe the internal structure of the nucleons.
- Provide the information on the spatial distribution of electric charge (by electric form factor,  $G_E$ ) and magnetic moment ( by magnetic form factor,  $G_M$ ) within the proton.
- Can be determined from elastic electron-proton scattering.
- They are functions of the four-momentum transfer squared,  $Q^2$



The four-momentum transfer
squared,
$Q^2 = -q^2 = 4EE'\sin^2\left(\frac{\Theta}{2}\right)$
$E - E' = \frac{Q^2}{2M}$

General definition of the nucleon form factor is

$$\left\langle N(P') \Big| J^{\mu}_{EM}(0) \Big| N(P) \right\rangle = \overline{u} \left( P' \right) \left[ \gamma^{\mu} F_1^N \left( Q^2 \right) + i \sigma^{\mu\nu} \frac{q_{\nu}}{2M} F_2^N \left( Q^2 \right) \right] u(P)$$

Sachs Form Factors 
$$G_E = F_1 - \tau F_2$$
;  $G_M = F_1 + F_2$ ;  $\tau = \frac{Q^2}{4M^2}$ 

 $F_1$  – non-spin flip (Dirac Form Factor) describe the charge distribution  $F_2$  – spin flip (Pauli form factor) describe the magnetic moment distribution

At low 
$$|q^{2}|$$
  
 $G_{E}(q^{2}) \approx G_{E}(\vec{q}^{2}) = \int e^{i\vec{q}\cdot\vec{r}}\rho(\vec{r})d^{3}\vec{r}$   
 $G_{M}(q^{2}) \approx G_{M}(\vec{q}^{2}) = \int e^{i\vec{q}\cdot\vec{r}}\mu(\vec{r})d^{3}\vec{r}$   
At  $q^{2} = 0$   
 $G_{E}(0) = \int \rho(\vec{r})d^{3}\vec{r} = 1$   
 $G_{M}(0) = \int \mu(\vec{r})d^{3}\vec{r} = \mu_{p} = +2.79$   
Fourier transforms of the charge,  $\rho(r)$   
and magnetic moment,  $\mu(r)$  distributions  
in Breit Frame

### Form Factor Ratio Measurements

## 1. Rosenbluth seperation method.

- Measured the electron unpolarized proton elastic scattering cross section at fixed Q<sup>2</sup> by varying the scattering angle,  $\theta_{e.}$
- Strongly sensitive to the radiative corrections.

## 2. Polarization Transfer Technique.

- Measured the recoil proton polarization from the elastic scattering of polarized electron-unpolarized proton.
- Insensitive to absolute polarization, analyzing power.
- Less sensitive to radiative correction.

$$\frac{G_E}{G_M} = -\frac{P_T}{P_L} \frac{(E+E')\tan\left(\frac{\theta_e}{2}\right)}{2M_p}$$

E - Incoming going electron energy  
E' - Out going electron energy  
$$\theta_{e^-}$$
 Outgoing electron's scattering angle  
 $M_p$  - Proton mass

$$P_L = M_P^{-1}(E + E')\sqrt{\tau(1 + \tau)}G_M^2 \tan^2(\theta_e / 2) \longrightarrow \text{Polarization along } q$$

$$P_T = 2\sqrt{\tau(1+\tau)}G_E G_M \tan(\theta_e / 2)$$

 $P_N = 0$ 

- Polarization perpendicular to *q* (in the scattering plane)
- Polarization normal to scattering plane.

# 3. Double-Spin Asymmetry.

- Measured the cross section asymmetry between + and electron helicity states in elastic scattering of a polarized electron on a polarized proton.
- The systematic errors are different when compared to either the Rosenbluth technique or the polarization transfer technique.
- The sensitivity to the form factor ratio is the same as the Polarization Transfer Technique.

$$A_{p} = \frac{-br\sin\theta^{*}\cos\phi^{*} - a\cos\theta^{*}}{r^{2} + c}$$
$$\frac{G_{E}}{G_{M}} = -\frac{b}{2A_{p}}\sin\theta^{*}\cos\phi^{*} + \sqrt{\frac{b^{2}}{4A_{p}^{2}}}\sin^{2}\theta^{*}\cos^{2}\phi^{*} - \frac{a}{A_{p}}\cos\theta^{*} - c$$

Here, 
$$r = G_E / G_M$$
  
 $a, b, c = kinematic factors$   
 $\theta^*, \phi^* = pol. and azi. Angles between  $\vec{q}$  and  $\vec{S}$   
 $A_p = The beam - target asymmetry$$ 

# Physics Motivation



- Dramatic discrepancy between Rosenbluth and recoil polarization technique.
- Multi-photon exchange considered the best candidate for the

explanation  $\Diamond$ 

• Double-Spin Asymmetry is an Independent Technique to verify the discrepancy

# **Two-Photon Exchange**

• Both Rosenbluth method and the polarization transfer technique account for radiative correction, but neither consider two photon exchange.

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is large chough to effect the extracted value of  $G_E$ .

Therefore, the extracted  $G_E/G_M$  for the Rosenbluth technique is reduced.

- The effect of TPE amplitude on the polarization components is small, though the size of the contribution change with  $\mathcal{E}$
- The size of the TPE would measure by taking the  $\mathcal{E}$  dependence of the ratio of cross sections, R for elastic electron-proton scattering to positron-proton scattering at a fixed Q<sup>2</sup> and measuring the deviation from 1.

$$R = \frac{\sigma_{e+}}{\sigma_{e-}} = \frac{\left(A_{1\gamma} + A_{2\gamma}\right)^2}{\left(A_{1\gamma} - A_{2\gamma}\right)^2} \approx 1 + 4\operatorname{Re}\left(A_{2\gamma} / A_{1\gamma}\right)$$

# **Two-Photon Exchange: Exp. Evidence**





# Asymmetry measurements

$$\sigma = \sigma_0 + P_E P_T \Delta \sigma$$

$$\sigma_{++} = \sigma_0 + P_E P_T \Delta \sigma$$

$$\sigma_{+-} = \sigma_0 - P_E P_T \Delta \sigma$$

$$\frac{\sigma_{++} - \sigma_{+-}}{\sigma_{++} + \sigma_{+-}} = P_E P_T \cdot \frac{\Delta \sigma}{\sigma_0} = \frac{N_+ - N_-}{N_+ + N_-} = A_r$$
$$\frac{A_r}{P_E P_T} = \frac{\Delta \sigma}{\sigma_0} = A_p$$

 $\sigma$  - Scattering cross section

- $\sigma_{\rm 0}\text{-}$  Scattering cross section at unpolarized target
- $\sigma_{\rm B}$  Scattering cross section from background
- $\Delta \sigma$   $\sigma$  correction due to the spin
- $P_E$  Beam polarization
- P<sub>T</sub> Target polarization
- f Dilution factor

With background....  $\sigma_{++} = \sigma_0 + P_E P_T \Delta \sigma + \sigma_B$  $\sigma_{+-} = \sigma_0 - P_F P_T \Delta \sigma + \sigma_R$  $A_r = P_E P_T \cdot \frac{\Delta \sigma}{(\sigma_0 + \sigma_P)}$  $A_{r} = P_{E}P_{T} \cdot \frac{\Delta\sigma}{\sigma_{0}} \cdot \frac{\sigma_{0}}{(\sigma_{0} + \sigma_{B})} f$  $A_{P} = \frac{A_{r}}{fP_{E}P_{T}}$ 

Hence,

 $A_{p,}$  known as the physics asymmetry is the relative scattering cross section correction due to the spin.  $A_r$  is the raw asymmetry

# **Experiment Setup**





Elastic (e, e'p) scattering from the polarized NH<sub>3</sub> target using a longitudinally polarized electron beam

(Data collected from Jan – March ,2009)



- BETA for coincidence electron detection
- $\bullet$  Central scattering angle :40  $^{\circ}$
- Over 200 msr solid angle coverage



- HMS for the scattered proton detection
- Central angles are 22.3° and 22.0°
- Solid angle ~10 msr

# Big Electron Telescope Array – BETA

#### Forward Tracker

• 3 planes of Bicron Scintillator provide early particle tracking



#### Cerenkov

- N<sub>2</sub> gas cerenkov
- Provides particle ID
- 8 mirrors and 8 PMTs

### Lucite Hodescope

- 28 bars of 6cm wide Lucite
- Bars oriented horizontally for Y tracking
- PMTs on either side of bar provides X resolution



# High Momentum Spectrometer – HMS

#### Drift Chambers

• Each plane has a set of alternating field and sense wires Filled with an equal parts Argon-Methane mixture





- Track particle trajectory by multiple planes.
- $\chi^2$  fitting to determine a straight trajectory.

#### Hodescopes

- Each plane contains 10 to 16 Scintillator paddles with PMTs on both ends
- Each Paddle is 1.0 cm thick and 8.0 cm wide



- Fast position determination & triggering
- Time of Flight (TOF) = T2-T1 determines  $\beta$ ( $\beta = L/c \times TOF$ )



### Gas Cerenkov

- Two mirrors (top & bottom) connected to two PMTs
- Used as a Particle ID

#### Lead Glass Calorimeter

- 4 layers of 10 cm x 10cm x70cm blocks stacked 13 high.
- Used as a Particle ID

# **Polarized Target**





#### The Polarized Target Assembly

## Polarized Target Magnetic Field

![](_page_15_Figure_1.jpeg)

• Used only perpendicular magnetic field configuration for the elastic data

- Average target polarization is  $\sim$  70 %
- Average beam polarization is  $\sim73~\%$

# **Elastic Kinematics**

( From HMS Spectrometer )

Spectrometer mode	Coincidence	Coincidence	Single Arm
HMS Detects	Proton	Proton	Electron
E Beam GeV	4.72	5.89	5.89
P <sub>HMS</sub> GeV/c	3.58	4.17	4.40
Θ <sub>HMS</sub> (Deg)	22.30	22.00	15.40
$Q^2$ (GeV/c) <sup>2</sup>	5.17	6.26	2.20
Total Hours (h)	~40 (~44 runs)	~155 (~135 runs)	~12 (~15 runs)
Elastic Events	~113	~1200	-

# Data Analysis

## **Electrons in HMS**

![](_page_17_Picture_2.jpeg)

By knowing, the incoming beam energy, E, scattered electron energy, E'and the scattered electron angle,  $\theta$ 

$$Q^2 = 4EE'\sin^2\left(\frac{\theta}{2}\right)$$

 $\vec{e} \vec{p} \rightarrow e^{-} p$ 

$$W^{2} = M^{2} - Q^{2} + 2M(E - E')$$

#### Momentum Acceptance

![](_page_18_Figure_1.jpeg)

$$hsdelta = \begin{pmatrix} P - P_c \\ P_c \end{pmatrix} = \frac{\delta p}{p}$$

P -Measured momentum in HMS  $P_c$ -HMS central momentum

The elastic data are outside of the usual delta cut +/-8%

Because HMS reconstruction matrix elements work fine up to 10

Use -8% < hsdelta <10%

## Perp. target magnetic field make some correlations....

![](_page_19_Figure_1.jpeg)

- Introduced an 'azimuthal angle correction' which correct the target magnetic field in vertical direction in terms of the azimuthal angle. (First make the same correlations on MC/SIMC by applying the correction only for the forward direction and then use the correction on data)
- Different corrections for different detector angles.

In COIN BETA data

![](_page_19_Figure_5.jpeg)

## Extract the electrons

- Used only Electron selection cuts. # of Cerenkov photoelectrons > 2  $E_{sh}/E' > 0.7$  $\left(P - P_{c}/P_{c}\right) < 10 \text{ and } \left(P - P_{c}/P_{c}\right) > -8$
- Here,
- P/E' Detected electron momentum/ energy at HMS
  - P<sub>c</sub> Central momentum of HMS
- $E_{sh}$  Total measured shower energy of a chosen electron track by HMS Calorimeter

- Cerenkov cut
- Calorimeter cut
- HMS Momentum Acceptance cut

![](_page_20_Figure_9.jpeg)

## Extracted the Asymmetries .....

## The raw asymmetry, A<sub>r</sub>

$$=\frac{N^{+}-N^{-}}{N^{+}+N^{-}} \qquad \Delta A_{r} = \frac{2\sqrt{N^{+}}\sqrt{N^{-}}}{(N^{+}+N^{-})\sqrt{(N^{+}+N^{-})}}$$

 $N^+$  /  $N^-$  = Charge and life time normalized counts for the +/- helicities  $\Delta A_r = Error \text{ on the raw asymmetry}$  $P_{R}P_{T}$  = Beam and Target polarization

 $N_{\rm c} = A$  correction term to eliminates the contribution from quasi-elastic <sup>15</sup>N scattering under the elastic peak

#### The Asymmetries

![](_page_21_Figure_6.jpeg)

# Need

dilution factor, f in order to determine the physics asymmetry,

![](_page_21_Figure_9.jpeg)

and  $G_{F}^{P}/G_{M}^{P}$ 

## MC for C run

![](_page_22_Figure_1.jpeg)

# MC with NH3

- Generated N, H and He separately.
- Added Al come from target end caps and 4K shields as well.
- Calculated the MC scale factor using the data/MC luminosity ratio for each target type.
- Added all targets together by weighting the above MC scale factors.
- Used 60% packing fraction.
- Adjust acceptance edges in Ytar and yptar from adjusting the horizontal beam position.
- Adjust the vertical beam position to bring the W peak to 0.938 GeV

![](_page_23_Figure_8.jpeg)

# Packing Fraction.

- Packing Fraction is the actual amount of target material used.
- Determined by taking the ratio of data to MC as a function of W.
- Need to determine the packing fractions for each of the NH3 loads used during the data taking.

![](_page_24_Figure_4.jpeg)

## Determine the Packing Fraction

- Looked data to SIMC comparison for the NH3 target for 3 different Packing Fractions.
- Normalized MC\_NH3 by 0.93 which is the factor that brings C data/MC ratio to 1.

![](_page_25_Figure_3.jpeg)

- Determined the packing fraction which brings Data/MC ratio to 1 from the plot.
- Packing Fraction=56.3 %

Pf (%)	50	60	70
Data/MC Ratio	1.00	0.88	0.78
Data/MC Ratio/0.93	1.075	0.95	0.84

### **Determination of the Dilution Factor**

#### What is the Dilution Factor ?

The dilution factor is the ratio of the yield from scattering off free protons(protons from H in  $NH_3$ ) to that from the entire target (protons from N, H, He and Al)

![](_page_26_Figure_3.jpeg)

### MC Background contributions (Only He+N+Al)

![](_page_27_Figure_1.jpeg)

- Calculate the ratio of Yield<sub>Data</sub>/Yield<sub>MC</sub> for the W region 0.7 < W <0.85 and MC is normalized
  - with this new scaling factor.
- Used the polynomial fit to N+ He+Al in MC and
- Subtract the fit function from data

# The relative Dilution Factor (Preliminary)

Dilution Factor,  $F = \frac{Yield_{Data} - Yield_{MC(N+He)}}{Yield_{Data}}$ 

- We have taken data using both NH3 targets, called NH3 top and NH3 bottom.
- NH3 crystals are not uniformly filled in each targets which arise two different packing fractions and hence two different dilution factors.

![](_page_28_Figure_4.jpeg)

### Beam / Target Polarizations

![](_page_29_Figure_1.jpeg)

![](_page_29_Figure_2.jpeg)

![](_page_30_Figure_0.jpeg)

• The beam - target asymmetry, 
$$A_p$$
  

$$A_p = \frac{-br \sin \theta^* \cos \phi^* - a \cos \theta^*}{r^2 + c}$$

$$\frac{G_E}{G_M} = -\frac{b}{2A_p} \sin \theta^* \cos \phi^* + \sqrt{\frac{b^2}{4A_p^2} \sin^2 \theta^* \cos^2 \phi^* - \frac{a}{A_p} \cos \theta^* - c}}{Using the exeperiment data at Q^2 = 2.2 (GeV/c)^2 \qquad 0.125 \qquad 0.100 \qquad 0.125 \qquad 0.125 \qquad 0.150 \qquad 0.150 \qquad 0.150 \qquad 0.125 \qquad 0.150 \qquad 0.125 \qquad 0.150 \qquad 0.1$$

Using the exeperiment data at  $Q^2=2.2$  (GeV/c)<sup>2</sup> and by knowing the Ap=-0.201,

$$r = \left(\frac{G_E}{G_M}\right) = 0.2416$$

$$\mu r = \mu \left(\frac{G_E}{G_M}\right) = 0.674$$

Where ,  $\mu$  – Magnetic Moment of the Proton=2.79

Error propagation from the experiment

$$A_P = \frac{-b\sin\theta^*\cos\phi^*r}{c} - \frac{a\cos\theta^*}{c}$$

$$\Delta r = \Delta \left(\frac{G_E}{G_M}\right) = \left|\frac{c}{b\sin\theta^*\cos\varphi^*}\right| \Delta A_p$$

By knowing the  $\Delta$  Ap=0.017,

$$\Delta(\mu r) = \Delta\left(\mu \frac{G_E}{G_M}\right) = 0.13$$

![](_page_33_Figure_0.jpeg)

# Coincidence Data (Electrons in BETA and Protons in HMS)

#### Definitions :

- X/Yclust Measured X/Y positions on the BigCal
- *X* = horizontal / in-plane coordinate
- Y = vertical / out of plane coordinate
- Eclust Measured electron energy at the BigCal

By knowing the energy of the polarized electron beam, E<sub>B</sub> and the scattered proton angle, Θ<sub>P</sub>

![](_page_34_Picture_7.jpeg)

## Elastic Kinematics

#### (From HMS Spectrometer)

Spectrometer mode	Coincidence	Coincidence	Single Arm
HMS Detects	Proton	Proton	Electron
E Beam GeV	4.72	5.89	5.89
P <sub>HMS</sub> GeV/c	3.58	4.17	4.40
Θ <sub>HMS</sub> (Deg)	22.30	22.00	15.40
$Q^2$ (GeV/c) <sup>2</sup>	5.17	6.26	2.20
Total Hours (h)	~40 (~44 runs)	~155 (~135 runs)	~12 (~15 runs)
e-p Events	~113	~1200	-

## Fractional momentum difference

![](_page_36_Figure_1.jpeg)

 $P_{HMS}$  – Measured proton momentum by HMS

- $P_{cal}~$  Calculated proton momentum by knowing the beam energy, E and the proton angle,  $\pmb{\Theta}$
- $P_{cent} HMS$  central momentum

### X/Y position difference

X position difference

![](_page_37_Figure_2.jpeg)

![](_page_38_Figure_0.jpeg)

### Elastic Events

5.89 GeV data

#### 4.72 GeV data

![](_page_39_Figure_2.jpeg)

### Extract the Raw Asymmetries

![](_page_40_Figure_1.jpeg)

Raw yields are normalized with

- Total Charge
- charge average +/- life times

Need dilution factor, f in order to determine the physics asymmetry,

$$A_p = \frac{A_r}{fP_BP_T} + N_C$$

and  $G_{E}^{P}/G_{M}^{P}$ 

![](_page_41_Figure_0.jpeg)

- Get the ratio of data/SIMC\_C for the region of 0.03 < dpel\_hms < 0.08. (ratio=2.73893)
- Normalized the SIMC\_C with that ratio (2.73893) for the region of -0.1 < dpel\_hms < 0.1 and added SIMC\_H3 to it. Compare with the data. Data/SIMC(H3+2.73893\*C) = 0.991536
- Used the Gaussian fit for the SIMC\_C (normalized with 2.73893) and subtract it from the data
- Get the relative dilution factor by taking the ratio of SIMC\_C substracted data to data. the relative df. = (data-SIMC\_C)/data

### Get The Relative Dilution Factor

![](_page_42_Figure_1.jpeg)

### The Relative Dilution Factors For

![](_page_43_Figure_1.jpeg)

**Bottom Target** 

![](_page_43_Figure_3.jpeg)

![](_page_43_Figure_4.jpeg)

# The Relative Dilution Factor (Used the Integration Method)

- Because of the law statistics, It is hard to correct the raw asymmetry for the df as a function of dpel\_hms
- Just integrate over the dpel\_hms region of +/- 0.02 for the top and bottom.

![](_page_44_Figure_3.jpeg)

### **Beam and Target Polarizations**

![](_page_45_Figure_1.jpeg)

- Used the runs of beam polarization > 60 % and abs(target polarization) > 55 %
- Used the charge average target and beam polarizations to calculate the physics asymmetries

## Extract the Physics Asymmetries

![](_page_46_Figure_1.jpeg)

![](_page_47_Figure_0.jpeg)

# To Do

• Determine the new dilution factor, raw/physics asymmetries and hence the form factor ratio,  $G_F/G_M$  using the new packing fraction of 56.3% for the single arm electron data. •Estimate the systematic errors for both single arm electron and coincidence data

# Conclusion

- Measurement of the beam-target asymmetry in elastic electron-proton scattering offers an independent technique of determining the  $G_E/G_M$  ratio.
- This is an 'explorative' measurement, as a by-product of the SANE experiment.
- Extraction of the  $G_E/G_M$  ratio from single-arm electron and Coincidence data are shown.
- The preliminary data point at  $2.2 (GeV/c)^2$  is very consistent with the recoil polarization data (falls even slightly below it)
- The preliminary weighted average data point of the coincidence data at 5.72  $(GeV/c)^2$  consistent with the recoil polarization data within it's 3  $\sigma$  error.

#### **SANE Collaborators:**

Argonne National Laboratory, Christopher Newport U., Florida International U., Hampton U., Thomas Jefferson National Accelerator Facility, Mississippi State U., North Carolina A&T State U., Norfolk S. U., Ohio U., Institute for High Energy Physics, U. of Regina, Rensselaer Polytechnic I., Rutgers U., Seoul National U., State University at New Orleans, Temple U., Tohoku U., U. of New Hampshire, U. of Virginia, College of William and Mary, Xavier University of Louisiana, Yerevan Physics Inst.

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![](_page_50_Picture_3.jpeg)

![](_page_50_Picture_4.jpeg)