Proton Form Factor Ratio, G_{E}^{P}/G_{M}^{P} From Double Spin Asymmetries

Spin Asymmetries of the Nucleon Experiment (E07-003)

Analysis Updates





Anusha Liyanage HU Group Meeting (December 04, 2012)

Outline

- Introduction
- Physics Motivation
- Experiment Setup
 - BETA Detector
 - HMS Detector
 - Polarized Target
- Elastic Kinematic
- Data Analysis & MC/SIMC Simulation
- Conclusion



Introduction Nucleon Elastic Form Factors

- Defined in context of single-photon exchange.
- Describe how much the nucleus deviates from a point like particle.
- Describe the internal structure of the nucleons.
- Provide the information on the spatial distribution of electric charge (by electric form factor, G_E) and magnetic moment (by magnetic form factor, G_M) within the proton.
- Can be determined from elastic electron-proton scattering.
- They are functions of the four-momentum transfer squared, Q^2



The four-momentum transfer
squared,
$Q^2 = -q^2 = 4EE'\sin^2\left(\frac{\Theta}{2}\right)$
$E - E' = \frac{Q^2}{2M}$

General definition of the nucleon form factor is

$$\left\langle N(P') \Big| J^{\mu}_{EM}(0) \Big| N(P) \right\rangle = \overline{u} \left(P' \right) \left[\gamma^{\mu} F_1^N \left(Q^2 \right) + i \sigma^{\mu\nu} \frac{q_{\nu}}{2M} F_2^N \left(Q^2 \right) \right] u(P)$$

Sachs Form Factors
$$G_E = F_1 - \tau F_2$$
; $G_M = F_1 + F_2$; $\tau = \frac{Q^2}{4M^2}$

 F_1 – non-spin flip (Dirac Form Factor) describe the charge distribution F_2 – spin flip (Pauli form factor) describe the magnetic moment distribution

At low
$$|q^{2}|$$

 $G_{E}(q^{2}) \approx G_{E}(\vec{q}^{2}) = \int e^{i\vec{q}\cdot\vec{r}}\rho(\vec{r})d^{3}\vec{r}$
 $G_{M}(q^{2}) \approx G_{M}(\vec{q}^{2}) = \int e^{i\vec{q}\cdot\vec{r}}\mu(\vec{r})d^{3}\vec{r}$
At $q^{2} = 0$
 $G_{E}(0) = \int \rho(\vec{r})d^{3}\vec{r} = 1$
 $G_{M}(0) = \int \mu(\vec{r})d^{3}\vec{r} = \mu_{p} = +2.79$
Fourier transforms of the charge, $\rho(r)$
and magnetic moment, $\mu(r)$ distributions
in Breit Frame

Form Factor Ratio Measurements

1. Rosenbluth seperation method.

- Measured the electron unpolarized proton elastic scattering cross section at fixed Q² by varying the scattering angle, $\theta_{e.}$
- Strongly sensitive to the radiative corrections.

2. Polarization Transfer Technique.

- Measured the recoil proton polarization from the elastic scattering of polarized electron-unpolarized proton.
- Insensitive to absolute polarization, analyzing power.
- Less sensitive to radiative correction.

$$\frac{G_E}{G_M} = -\frac{P_T}{P_L} \frac{(E+E')\tan\left(\frac{\theta_e}{2}\right)}{2M_p}$$

E - Incoming going electron energy
E' - Out going electron energy
$$\theta_{e^-}$$
 Outgoing electron's scattering angle
 M_p - Proton mass

$$P_L = M_P^{-1}(E + E')\sqrt{\tau(1 + \tau)}G_M^2 \tan^2(\theta_e / 2) \longrightarrow \text{Polarization along } q$$

$$P_T = 2\sqrt{\tau(1+\tau)}G_E G_M \tan(\theta_e / 2)$$

 $P_N = 0$

- Polarization perpendicular to *q* (in the scattering plane)
- Polarization normal to scattering plane.

3. Double-Spin Asymmetry.

- Measured the cross section asymmetry between + and electron helicity states in elastic scattering of a polarized electron on a polarized proton.
- The systematic errors are different when compared to either the Rosenbluth technique or the polarization transfer technique.
- The sensitivity to the form factor ratio is the same as the Polarization Transfer Technique.

$$A_{p} = \frac{-br\sin\theta^{*}\cos\phi^{*} - a\cos\theta^{*}}{r^{2} + c}$$
$$\frac{G_{E}}{G_{M}} = -\frac{b}{2A_{p}}\sin\theta^{*}\cos\phi^{*} + \sqrt{\frac{b^{2}}{4A_{p}^{2}}}\sin^{2}\theta^{*}\cos^{2}\phi^{*} - \frac{a}{A_{p}}\cos\theta^{*} - c$$

Here,
$$r = G_E / G_M$$

 $a, b, c = kinematic factors$
 $\theta^*, \phi^* = pol. and azi. Angles between \vec{q} and \vec{S}
 $A_p = The beam - target asymmetry$$

Physics Motivation



- Dramatic discrepancy between Rosenbluth and recoil polarization technique.
- Multi-photon exchange considered the best candidate for the

explanation \Diamond

• Double-Spin Asymmetry is an Independent Technique to verify the discrepancy

Two-Photon Exchange

• Both Rosenbluth method and the polarization transfer technique account for radiative correction, but neither consider two photon exchange.

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is large chough to effect the extracted value of G_E .

Therefore, the extracted G_E/G_M for the Rosenbluth technique is reduced.

- The effect of TPE amplitude on the polarization components is small, though the size of the contribution change with \mathcal{E}
- The size of the TPE would measure by taking the \mathcal{E} dependence of the ratio of cross sections, R for elastic electron-proton scattering to positron-proton scattering at a fixed Q² and measuring the deviation from 1.

$$R = \frac{\sigma_{e+}}{\sigma_{e-}} = \frac{\left(A_{1\gamma} + A_{2\gamma}\right)^2}{\left(A_{1\gamma} - A_{2\gamma}\right)^2} \approx 1 + 4\operatorname{Re}\left(A_{2\gamma} / A_{1\gamma}\right)$$

Two-Photon Exchange: Exp. Evidence





Asymmetry measurements

$$\sigma = \sigma_0 + P_E P_T \Delta \sigma$$

$$\sigma_{++} = \sigma_0 + P_E P_T \Delta \sigma$$

$$\sigma_{+-} = \sigma_0 - P_E P_T \Delta \sigma$$

$$\frac{\sigma_{++} - \sigma_{+-}}{\sigma_{++} + \sigma_{+-}} = P_E P_T \cdot \frac{\Delta \sigma}{\sigma_0} = \frac{N_+ - N_-}{N_+ + N_-} = A_r$$
$$\frac{A_r}{P_E P_T} = \frac{\Delta \sigma}{\sigma_0} = A_p$$

 σ - Scattering cross section

- $\sigma_{\rm 0}\text{-}$ Scattering cross section at unpolarized target
- $\sigma_{\rm B}$ Scattering cross section from background
- $\Delta \sigma$ σ correction due to the spin
- P_E Beam polarization
- P_T Target polarization
- f Dilution factor

With background.... $\sigma_{++} = \sigma_0 + P_E P_T \Delta \sigma + \sigma_B$ $\sigma_{+-} = \sigma_0 - P_F P_T \Delta \sigma + \sigma_R$ $A_r = P_E P_T \cdot \frac{\Delta \sigma}{(\sigma_0 + \sigma_P)}$ $A_{r} = P_{E}P_{T} \cdot \frac{\Delta\sigma}{\sigma_{0}} \cdot \frac{\sigma_{0}}{(\sigma_{0} + \sigma_{B})} f$ $A_{P} = \frac{A_{r}}{fP_{E}P_{T}}$

Hence,

 $A_{p,}$ known as the physics asymmetry is the relative scattering cross section correction due to the spin. A_r is the raw asymmetry

Experiment Setup





Elastic (e, e'p) scattering from the polarized NH₃ target using a longitudinally polarized electron beam

(Data collected from Jan – March ,2009)



- BETA for coincidence electron detection
- \bullet Central scattering angle :40 $^{\circ}$
- Over 200 msr solid angle coverage



- HMS for the scattered proton detection
- Central angles are 22.3° and 22.0°
- Solid angle ~10 msr

Big Electron Telescope Array – BETA

Forward Tracker

• 3 planes of Bicron Scintillator provide early particle tracking



Cerenkov

- N₂ gas cerenkov
- Provides particle ID
- 8 mirrors and 8 PMTs

Lucite Hodescope

- 28 bars of 6cm wide Lucite
- Bars oriented horizontally for Y tracking
- PMTs on either side of bar provides X resolution



High Momentum Spectrometer – HMS

Drift Chambers

• Each plane has a set of alternating field and sense wires Filled with an equal parts Argon-Methane mixture





- Track particle trajectory by multiple planes.
- χ^2 fitting to determine a straight trajectory.

Hodescopes

- Each plane contains 10 to 16 Scintillator paddles with PMTs on both ends
- Each Paddle is 1.0 cm thick and 8.0 cm wide



- Fast position determination & triggering
- Time of Flight (TOF) = T2-T1 determines β ($\beta = L/c \times TOF$)



Gas Cerenkov

- Two mirrors (top & bottom) connected to two PMTs
- Used as a Particle ID

Lead Glass Calorimeter

- 4 layers of 10 cm x 10cm x70cm blocks stacked 13 high.
- Used as a Particle ID

Polarized Target





The Polarized Target Assembly

Polarized Target Magnetic Field



• Used only perpendicular magnetic field configuration for the elastic data

- Average target polarization is \sim 70 %
- Average beam polarization is $\sim73~\%$

Elastic Kinematics

(From HMS Spectrometer)

Spectrometer mode	Coincidence	Coincidence	Single Arm
HMS Detects	Proton	Proton	Electron
E Beam GeV	4.72	5.89	5.89
P _{HMS} GeV/c	3.58	4.17	4.40
Θ _{HMS} (Deg)	22.30	22.00	15.40
Q^2 (GeV/c) ²	5.17	6.26	2.20
Total Hours (h)	~40 (~44 runs)	~155 (~135 runs)	~12 (~15 runs)
Elastic Events	~113	~1200	-

Data Analysis

Electrons in HMS



By knowing, the incoming beam energy, E, scattered electron energy, E'and the scattered electron angle, θ

$$Q^2 = 4EE'\sin^2\left(\frac{\theta}{2}\right)$$

 $\vec{e} \vec{p} \rightarrow e^{-} p$

$$W^{2} = M^{2} - Q^{2} + 2M(E - E')$$

Momentum Acceptance



$$hsdelta = \begin{pmatrix} P - P_c \\ P_c \end{pmatrix} = \frac{\delta p}{p}$$

P -Measured momentum in HMS P_c -HMS central momentum

The elastic data are outside of the usual delta cut +/-8%

Because HMS reconstruction matrix elements work fine up to 10

Use -8% < hsdelta <10%

Perp. target magnetic field make some correlations....



- Introduced an 'azimuthal angle correction' which correct the target magnetic field in vertical direction in terms of the azimuthal angle. (First make the same correlations on MC/SIMC by applying the correction only for the forward direction and then use the correction on data)
- Different corrections for different detector angles.

In COIN BETA data



Extract the electrons

- Used only Electron selection cuts. # of Cerenkov photoelectrons > 2 $E_{sh}/E' > 0.7$ $\left(P - P_{c}/P_{c}\right) < 10 \text{ and } \left(P - P_{c}/P_{c}\right) > -8$
- Here,
- P/E' Detected electron momentum/ energy at HMS
 - P_c Central momentum of HMS
- E_{sh} Total measured shower energy of a chosen electron track by HMS Calorimeter

- Cerenkov cut
- Calorimeter cut
- HMS Momentum Acceptance cut



Extracted the Asymmetries

The raw asymmetry, A_r

$$=\frac{N^{+}-N^{-}}{N^{+}+N^{-}} \qquad \Delta A_{r} = \frac{2\sqrt{N^{+}}\sqrt{N^{-}}}{(N^{+}+N^{-})\sqrt{(N^{+}+N^{-})}}$$

 N^+ / N^- = Charge and life time normalized counts for the +/- helicities $\Delta A_r = Error \text{ on the raw asymmetry}$ $P_{R}P_{T}$ = Beam and Target polarization

 $N_{\rm c} = A$ correction term to eliminates the contribution from quasi-elastic ¹⁵N scattering under the elastic peak

The Asymmetries



Need

dilution factor, f in order to determine the physics asymmetry,



and G_{F}^{P}/G_{M}^{P}

MC for C run



MC with NH3

- Generated N, H and He separately.
- Added Al come from target end caps and 4K shields as well.
- Calculated the MC scale factor using the data/MC luminosity ratio for each target type.
- Added all targets together by weighting the above MC scale factors.
- Used 60% packing fraction.
- Adjust acceptance edges in Ytar and yptar from adjusting the horizontal beam position.
- Adjust the vertical beam position to bring the W peak to 0.938 GeV

Packing Fraction.

- Packing Fraction is the actual amount of target material used.
- Determined by taking the ratio of data to MC as a function of W.
- Need to determine the packing fractions for each of the NH3 loads used during the data taking.

Determine the Packing Fraction

- Looked data to SIMC comparison for the NH3 target for 3 different Packing Fractions.
- Normalized MC_NH3 by 0.93 which is the factor that brings C data/MC ratio to 1.

- Determined the packing fraction which brings Data/MC ratio to 1 from the plot.
- Packing Fraction=56.3 %

Pf (%)	50	60	70
Data/MC Ratio	1.00	0.88	0.78
Data/MC Ratio/0.93	1.075	0.95	0.84

Determination of the Dilution Factor

What is the Dilution Factor ?

The dilution factor is the ratio of the yield from scattering off free protons(protons from H in NH_3) to that from the entire target (protons from N, H, He and Al)

MC Background contributions (Only He+N+Al)

- Calculate the ratio of Yield_{Data}/Yield_{MC} for the W region 0.7 < W <0.85 and MC is normalized
 - with this new scaling factor.
- Used the polynomial fit to N+ He+Al in MC and
- Subtract the fit function from data

The relative Dilution Factor (Preliminary)

Dilution Factor, $F = \frac{Yield_{Data} - Yield_{MC(N+He)}}{Yield_{Data}}$

- We have taken data using both NH3 targets, called NH3 top and NH3 bottom.
- NH3 crystals are not uniformly filled in each targets which arise two different packing fractions and hence two different dilution factors.

Beam / Target Polarizations

• The beam - target asymmetry,
$$A_p$$

$$A_p = \frac{-br \sin \theta^* \cos \phi^* - a \cos \theta^*}{r^2 + c}$$

$$\frac{G_E}{G_M} = -\frac{b}{2A_p} \sin \theta^* \cos \phi^* + \sqrt{\frac{b^2}{4A_p^2} \sin^2 \theta^* \cos^2 \phi^* - \frac{a}{A_p} \cos \theta^* - c}}{Using the exeperiment data at Q^2 = 2.2 (GeV/c)^2 \qquad 0.125 \qquad 0.100 \qquad 0.125 \qquad 0.125 \qquad 0.150 \qquad 0.150 \qquad 0.150 \qquad 0.125 \qquad 0.150 \qquad 0.125 \qquad 0.150 \qquad 0.1$$

Using the exeperiment data at $Q^2=2.2$ (GeV/c)² and by knowing the Ap=-0.201,

$$r = \left(\frac{G_E}{G_M}\right) = 0.2416$$

$$\mu r = \mu \left(\frac{G_E}{G_M}\right) = 0.674$$

Where , μ – Magnetic Moment of the Proton=2.79

Error propagation from the experiment

$$A_P = \frac{-b\sin\theta^*\cos\phi^*r}{c} - \frac{a\cos\theta^*}{c}$$

$$\Delta r = \Delta \left(\frac{G_E}{G_M}\right) = \left|\frac{c}{b\sin\theta^*\cos\varphi^*}\right| \Delta A_p$$

By knowing the Δ Ap=0.017,

$$\Delta(\mu r) = \Delta\left(\mu \frac{G_E}{G_M}\right) = 0.13$$

Coincidence Data (Electrons in BETA and Protons in HMS)

Definitions :

- X/Yclust Measured X/Y positions on the BigCal
- *X* = horizontal / in-plane coordinate
- Y = vertical / out of plane coordinate
- Eclust Measured electron energy at the BigCal

By knowing the energy of the polarized electron beam, E_B and the scattered proton angle, Θ_P

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Fractional momentum difference

 P_{HMS} – Measured proton momentum by HMS

- $P_{cal}~$ Calculated proton momentum by knowing the beam energy, E and the proton angle, $\pmb{\Theta}$
- $P_{cent} HMS$ central momentum

X/Y position difference

X position difference

Elastic Events

5.89 GeV data

4.72 GeV data

Extract the Raw Asymmetries

Raw yields are normalized with

- Total Charge
- charge average +/- life times

Need dilution factor, f in order to determine the physics asymmetry,

$$A_p = \frac{A_r}{fP_BP_T} + N_C$$

and G_{E}^{P}/G_{M}^{P}

- Get the ratio of data/SIMC_C for the region of 0.03 < dpel_hms < 0.08. (ratio=2.73893)
- Normalized the SIMC_C with that ratio (2.73893) for the region of -0.1 < dpel_hms < 0.1 and added SIMC_H3 to it. Compare with the data. Data/SIMC(H3+2.73893*C) = 0.991536
- Used the Gaussian fit for the SIMC_C (normalized with 2.73893) and subtract it from the data
- Get the relative dilution factor by taking the ratio of SIMC_C substracted data to data. the relative df. = (data-SIMC_C)/data

Get The Relative Dilution Factor

The Relative Dilution Factors For

Bottom Target

The Relative Dilution Factor (Used the Integration Method)

- Because of the law statistics, It is hard to correct the raw asymmetry for the df as a function of dpel_hms
- Just integrate over the dpel_hms region of +/- 0.02 for the top and bottom.

Beam and Target Polarizations

- Used the runs of beam polarization > 60 % and abs(target polarization) > 55 %
- Used the charge average target and beam polarizations to calculate the physics asymmetries

Extract the Physics Asymmetries

To Do

• Determine the new dilution factor, raw/physics asymmetries and hence the form factor ratio, G_F/G_M using the new packing fraction of 56.3% for the single arm electron data. •Estimate the systematic errors for both single arm electron and coincidence data

Conclusion

- Measurement of the beam-target asymmetry in elastic electron-proton scattering offers an independent technique of determining the G_E/G_M ratio.
- This is an 'explorative' measurement, as a by-product of the SANE experiment.
- Extraction of the G_E/G_M ratio from single-arm electron and Coincidence data are shown.
- The preliminary data point at $2.2 (GeV/c)^2$ is very consistent with the recoil polarization data (falls even slightly below it)
- The preliminary weighted average data point of the coincidence data at 5.72 $(GeV/c)^2$ consistent with the recoil polarization data within it's 3 σ error.

SANE Collaborators:

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