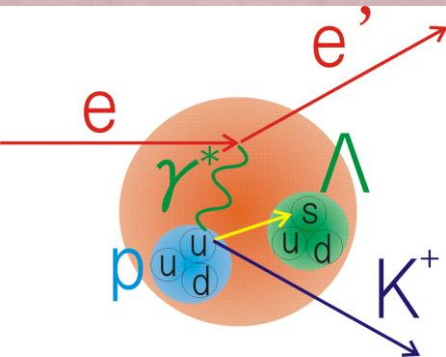


# Recent Spectroscopic Investigation of $\Lambda$ -Hypernuclei by the $(e,e'K^+)$ Reaction

-Analysis Status of E01-011 & E05-115-

Chunhua Chen  
Hampton University  
Nov. 05, 2013

# $\Lambda$ HYPERNUCLEAR SPECTROSCOPY VIA (e,e'K<sup>+</sup>)



## Merits of the (e,e'K<sup>+</sup>) experiment

- ☺ Large momentum transfer  
→ **Excitation of deeply-bound state**
- ☺ p to  $\Lambda$  reaction → **Mirror and Neutron-rich hypernuclei**
- ☺ Spin-flip/non-flip production
- ☺ High Energy Resolution due to CEBAF beam's quality

## 2005(E01-011) 2<sup>nd</sup> Experiment :

${}^7_{\Lambda}\text{He}$ ,  ${}^{12}_{\Lambda}\text{B}$ ,  ${}^{28}_{\Lambda}\text{Al}$

- ❖ Newly-constructed **HKS** for K<sup>+</sup> side
- ❖ Apply **"Tilt Method"** for e' side

## 2009(E05-115) 3<sup>rd</sup> Experiment:

${}^{12}_{\Lambda}\text{B}$ ,  ${}^7_{\Lambda}\text{He}$ ,  ${}^{10}_{\Lambda}\text{Be}$ ,  ${}^9_{\Lambda}\text{Li}$  and  ${}^{52}_{\Lambda}\text{V}$

- ❖ Beam Energy 1.8 → 2.344 GeV
- ❖ Brand-new e' spectrometer, HES

Calibration by the elementary process

$p(e,e'K^+)\Lambda$  or  $\Sigma$ : CH<sub>2</sub>

CEBAF Bird's-eye photo



# INTRODUCTION

## Physical Goals:

- To understand YN and YY interactions
- To explore and understand nuclear structure using  $\Lambda$  as a probe
  - **Model the baryonic many body system**
  - **Study the role of  $\Lambda$  in the nuclear medium**
- Shell Model with  $\Lambda$ -N Effective Potential ( $p_N s_\Lambda$ ) for p-shell hypernuclei

$$V_{\Lambda N} = \underbrace{V_0(r)}_{\vec{V}} + \underbrace{V_\sigma(r)}_{\Delta} \mathbf{s}_N \cdot \mathbf{s}_\Lambda + \underbrace{V_\Lambda(r)}_{S_\Lambda} L_{N\Lambda} \cdot \mathbf{s}_\Lambda + \underbrace{V_N(r)}_{S_N} L_{N\Lambda} \cdot \mathbf{s}_N + \underbrace{V_T(r)}_T S_{12}$$

Radial Integrals  
Coefficients of  
operators

- Additional Contribution:  $\Lambda$ - $\Sigma$  coupling

←  $V_{\Lambda\Sigma}$

Our results with precise  $B_\Lambda$  are important in helping to determine these parameters as well as to explore the full spectroscopy with unseen core states.



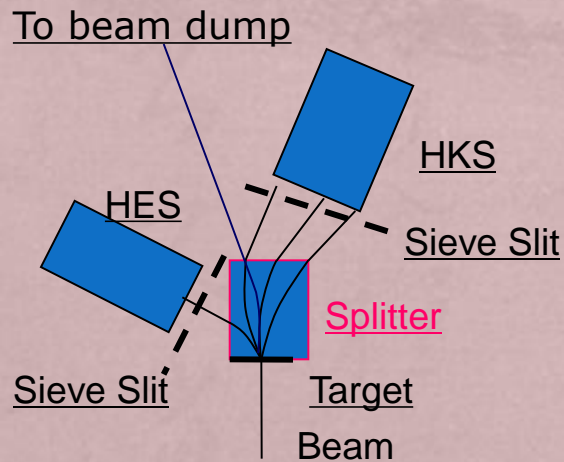
# Spectrometer System Calibration

Spectrometer system calibration: key to reach sub-MeV energy resolution

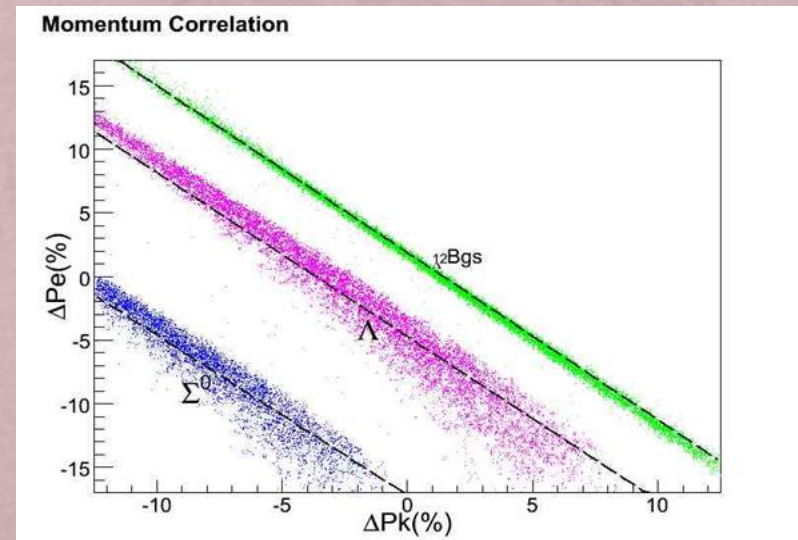
- Common splitter : Separated single arm calibration is impossible
- Technique: 2-arm coupled calibration for both kinematics and optics

Using known masses of  $\Lambda$ ,  $\Sigma^0$  from  $\text{CH}_2$  target and identified known hypernuclear bound states ( $^{12}_{\Lambda}\text{B}$  g.s.) for spectrometer calibration

## HES spectrometer system

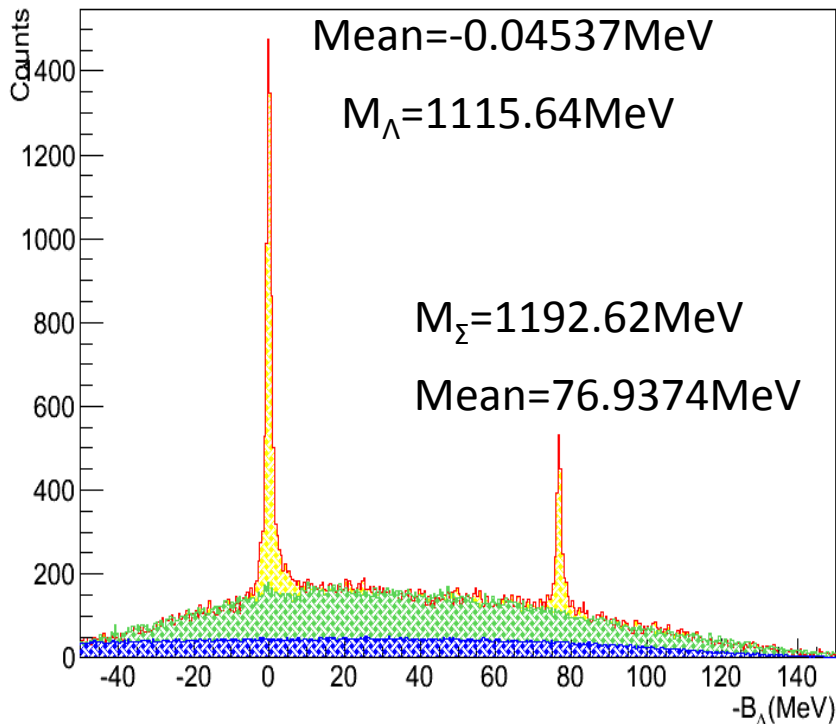


## Kinematics coverage



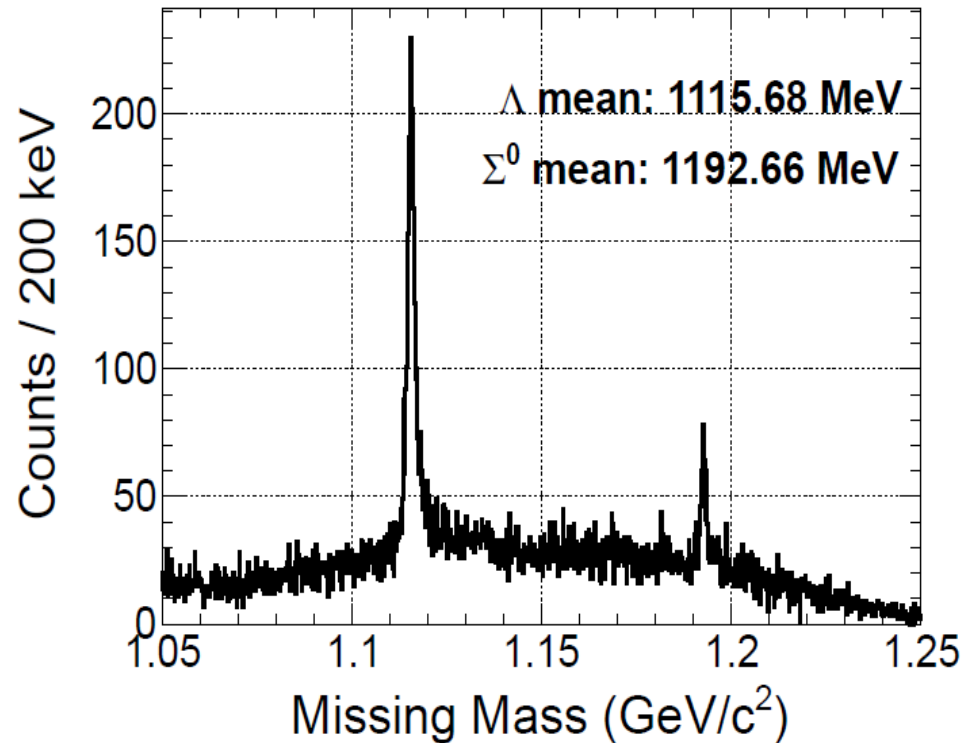
# CALIBRATION DATA RESULT

MM FROM CH2



**E05-115**

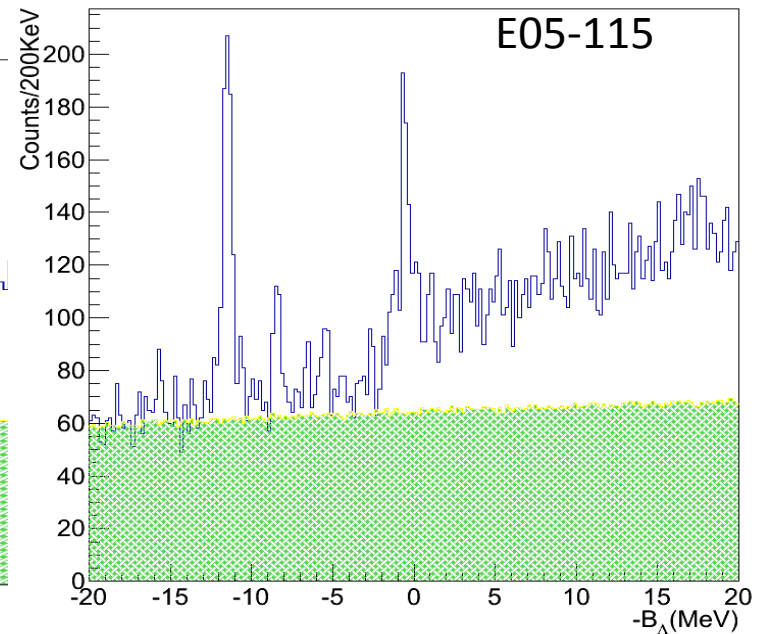
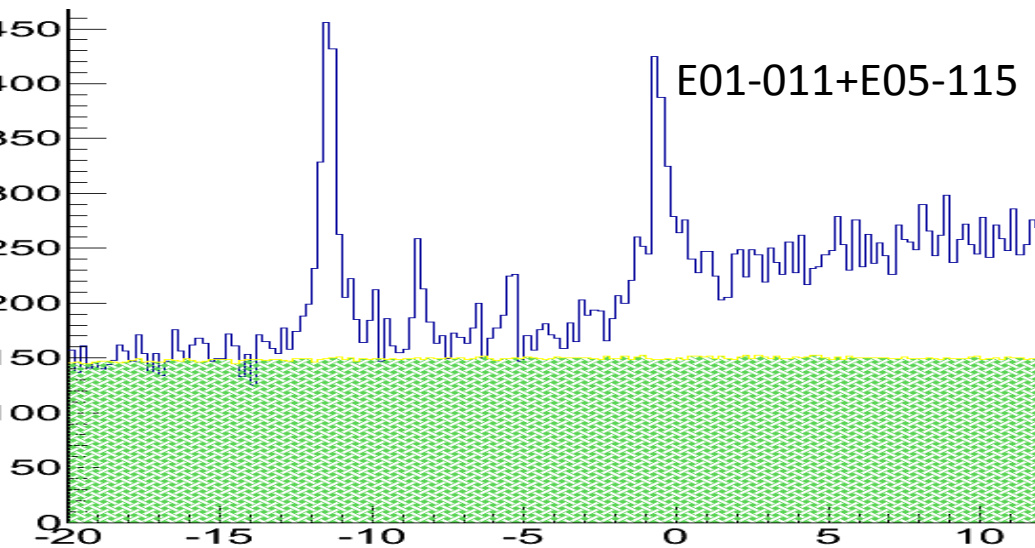
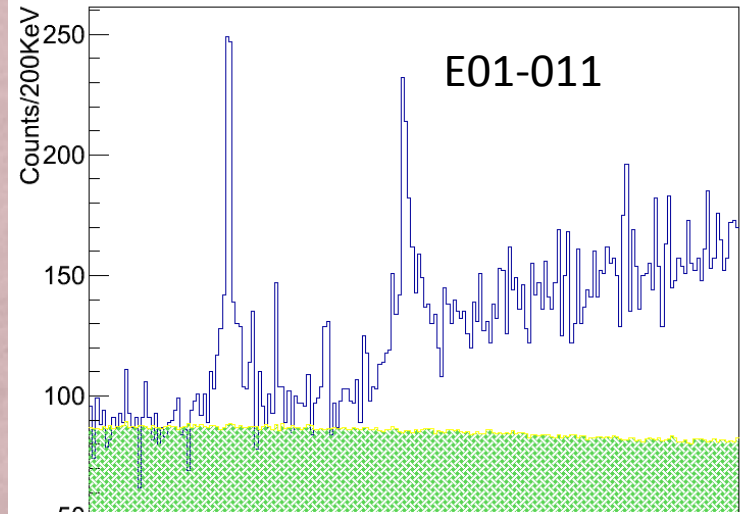
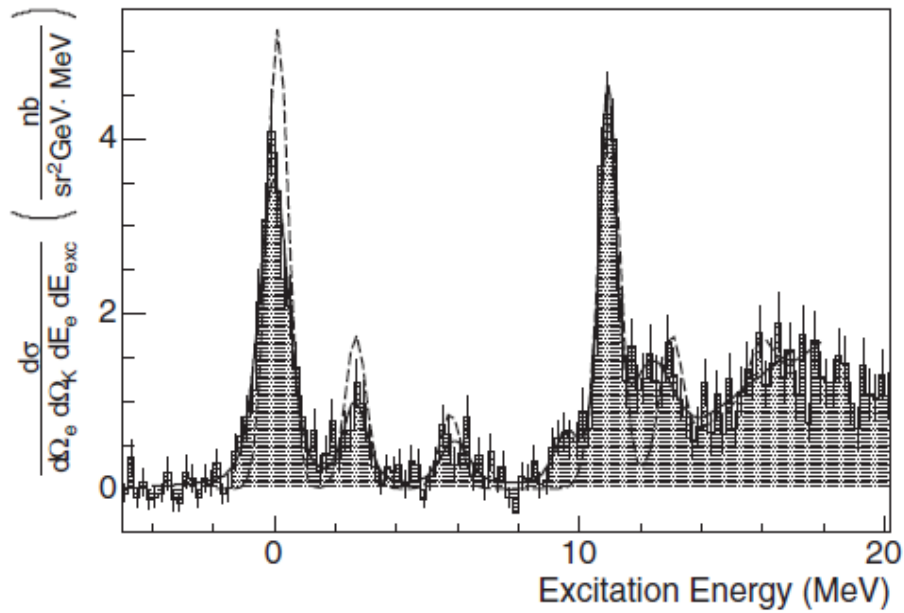
CH2 Target E01-011



**E01-011**

# $^{12}_{\Lambda}\text{B}$

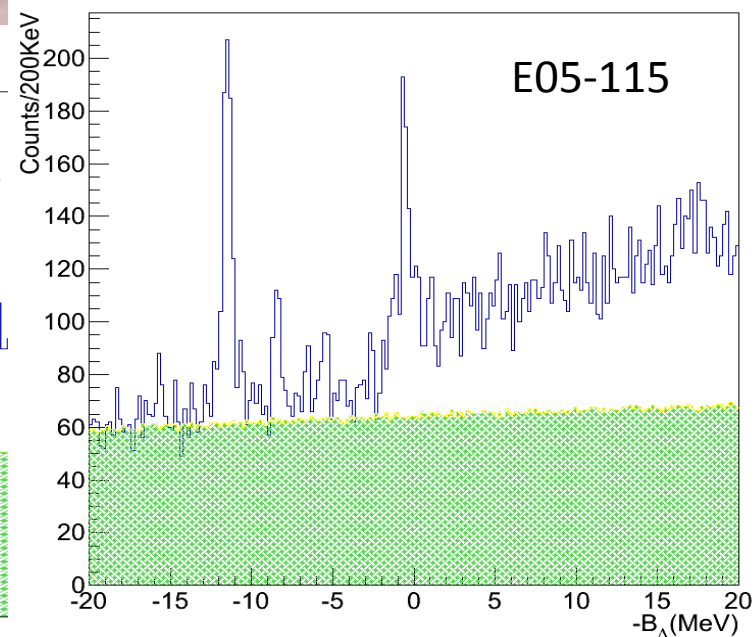
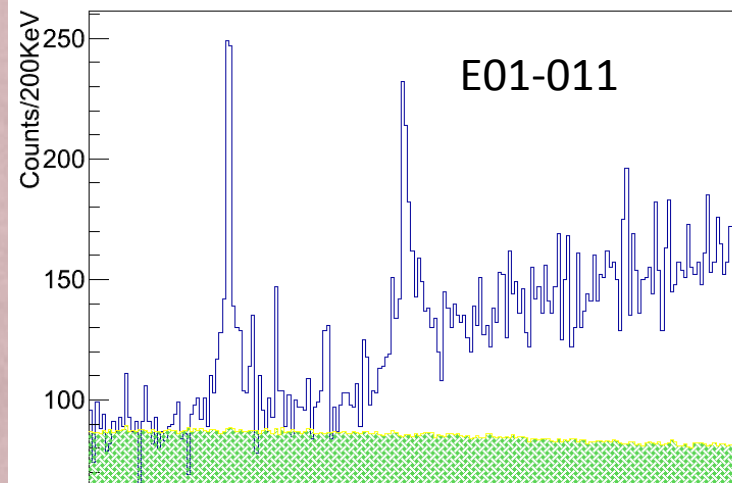
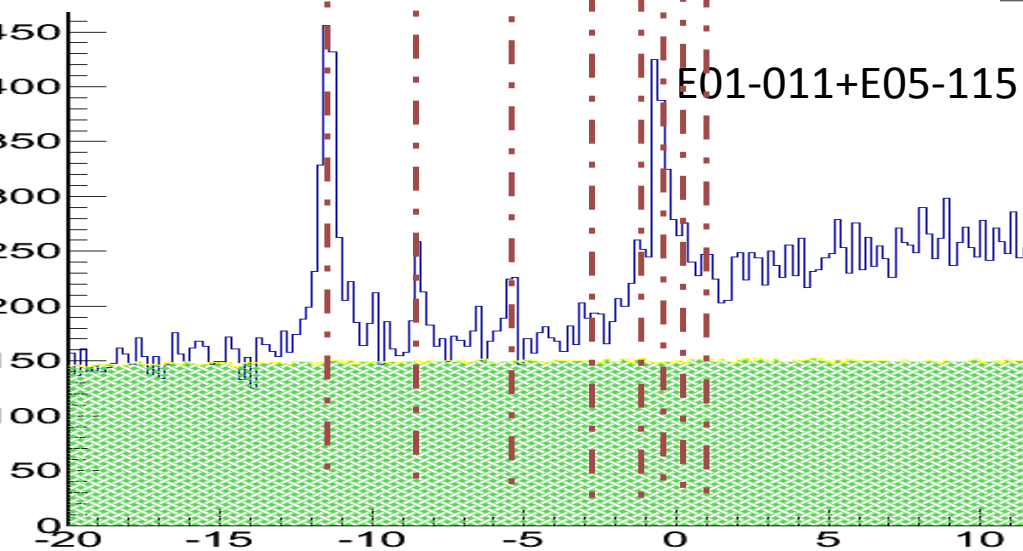
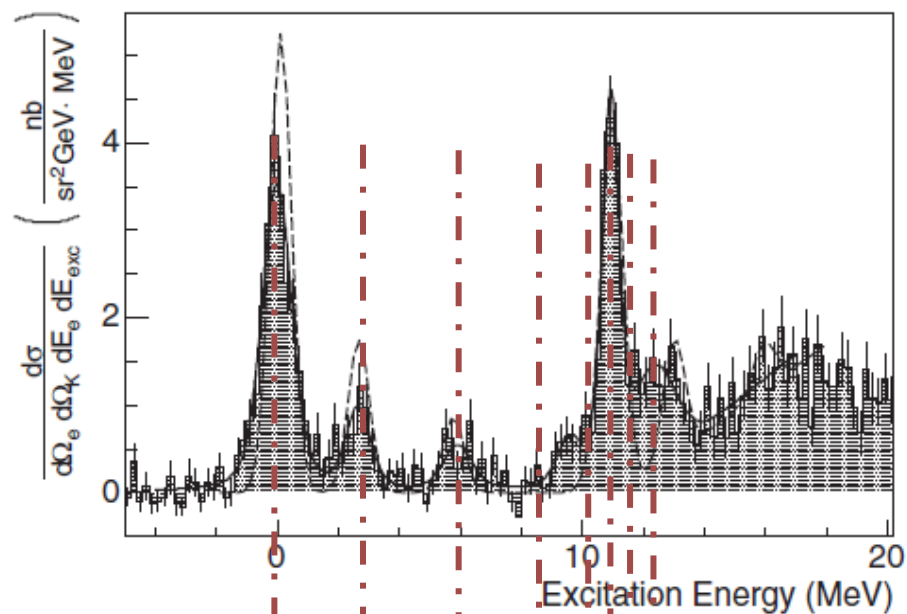
Phys. Rev. Lett. 99, 052501 (2007) (HallA data)





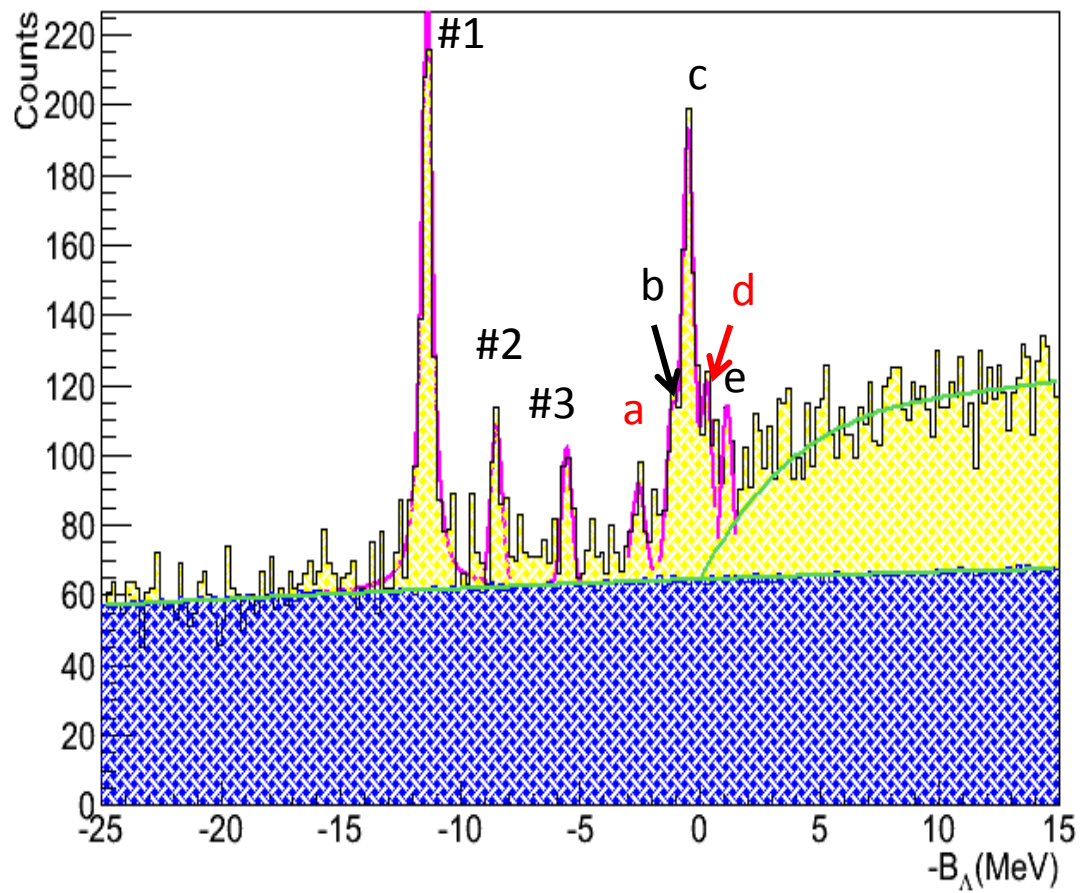
# $^{12}_{\Lambda}\text{B}$

Phys. Rev. Lett. 99, 052501 (2007) (HallA data)



# $^{12}_{\Lambda}\text{B}$

$^{12}_{\Lambda}\text{B}$  Missing Mass



peak	Mean (MeV)	$\sigma$ (KeV)
1	-11.41	265
2	-8.48	231
3	-5.54	210
<b>a</b>	<b>-2.539</b>	<b>281</b>
b	-1.164	240
c	-0.485	240
<b>d</b>	<b>0.295</b>	<b>240</b>
e	1.146	234

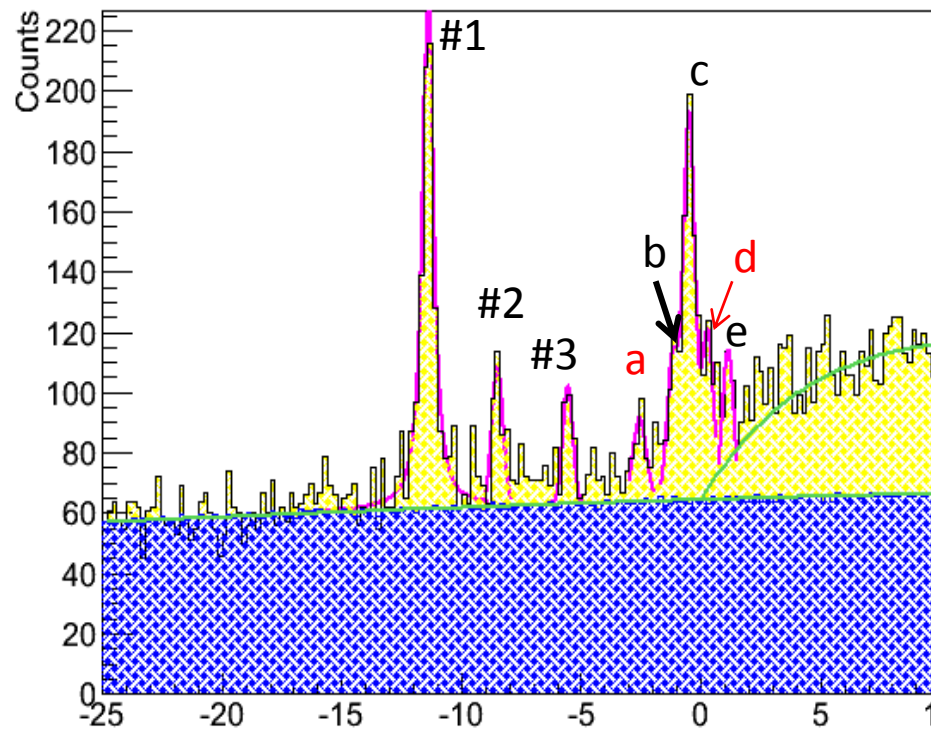
**Resolution:**

$\sigma = \sim 240 \text{ keV}$  or  $\sim 565 \text{ keV FWHM}$



# $^{12}_{\Lambda}\text{B}$

$^{12}_{\Lambda}\text{B}$  Missing Mass



e	$2^+/1^+$	1.146	—
c	$2^+/3^+$	-0.485	- - -
b	$2^+/1^+$	-1.164	—
a			- - -

$s^4p^6(sd) \otimes s_{\Lambda}$

#3  $2^-$  -5.54 —

#2  $1^-$  -8.48 —

#1 -11.41 —

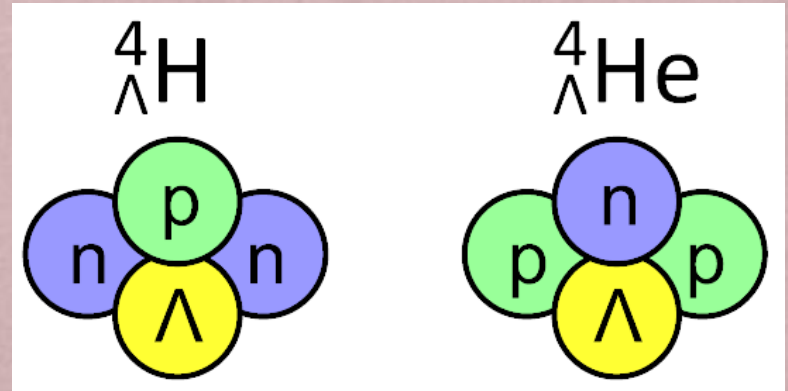
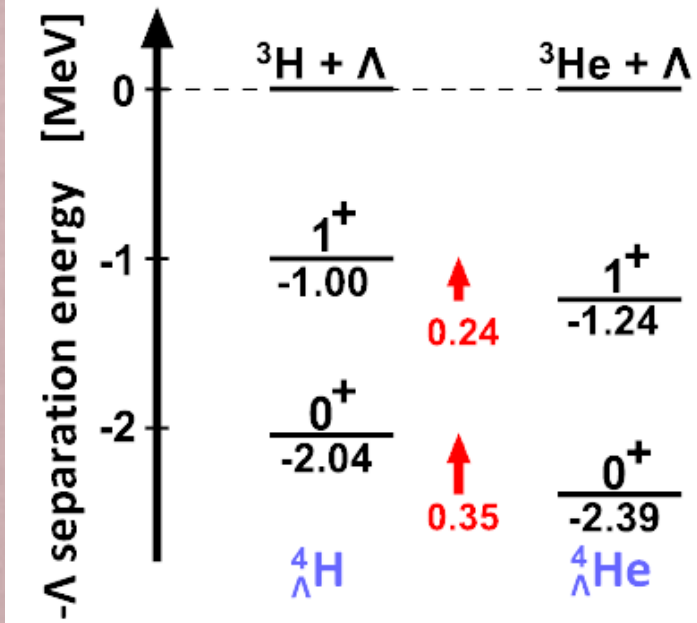
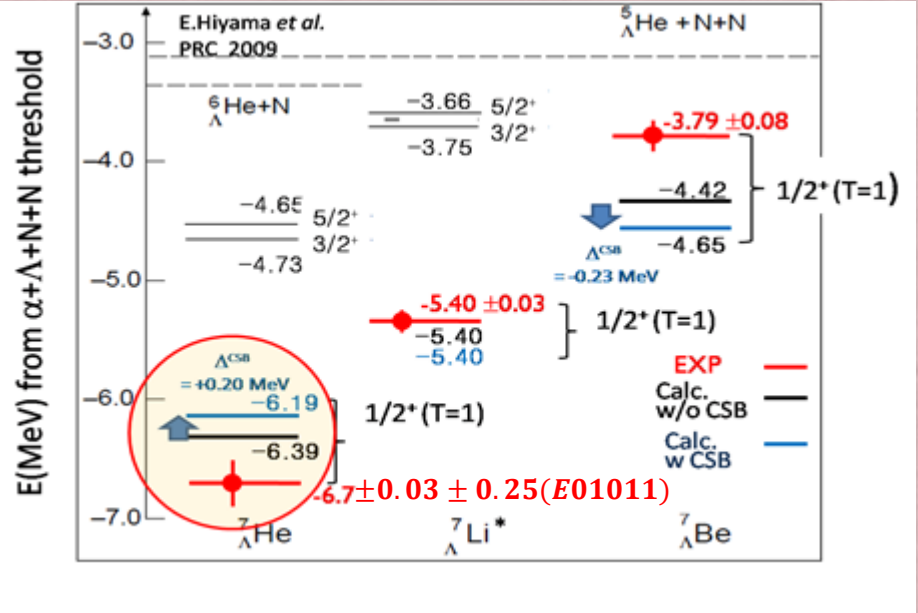
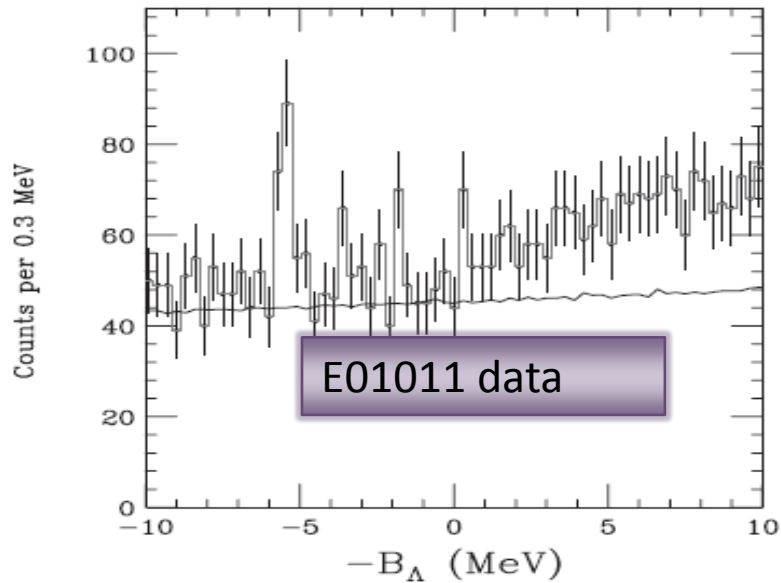
**E05115**  
Fitting  
w/ (3:1)

2<sup>-</sup> -11.356  
—  
1<sup>-</sup> -11.535  
↓ **179KeV**

Preliminary  
simulation

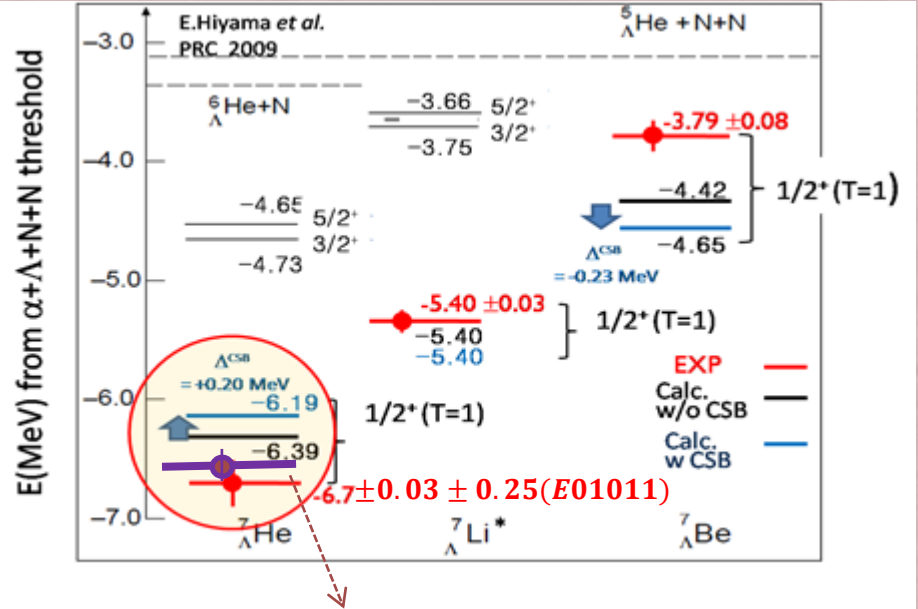
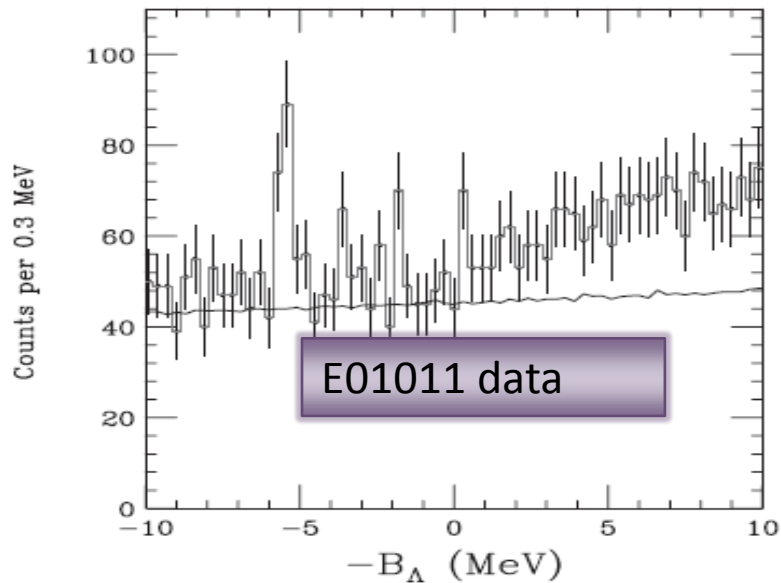
# ${}^7_{\Lambda}\text{He}$

PRL 110, 012502 (2013)

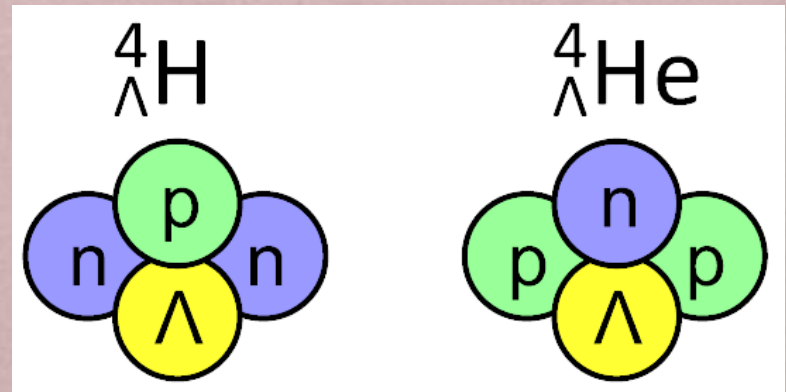
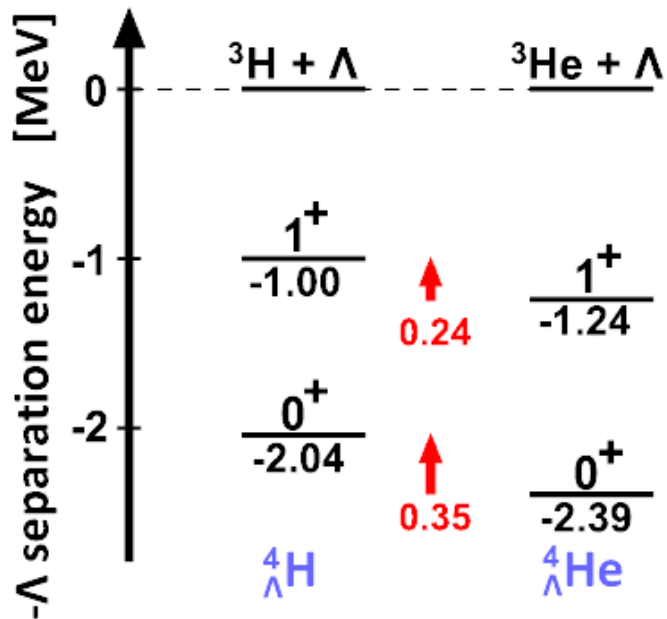


# ${}^7_{\Lambda}\text{He}$

PRL 110, 012502 (2013)



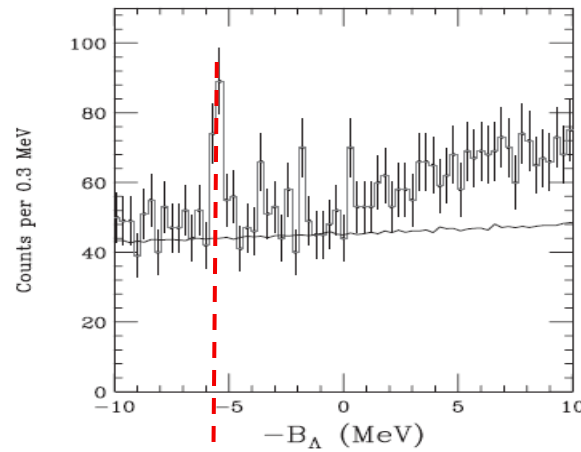
E05-115 with 4 time more statistics and better precision



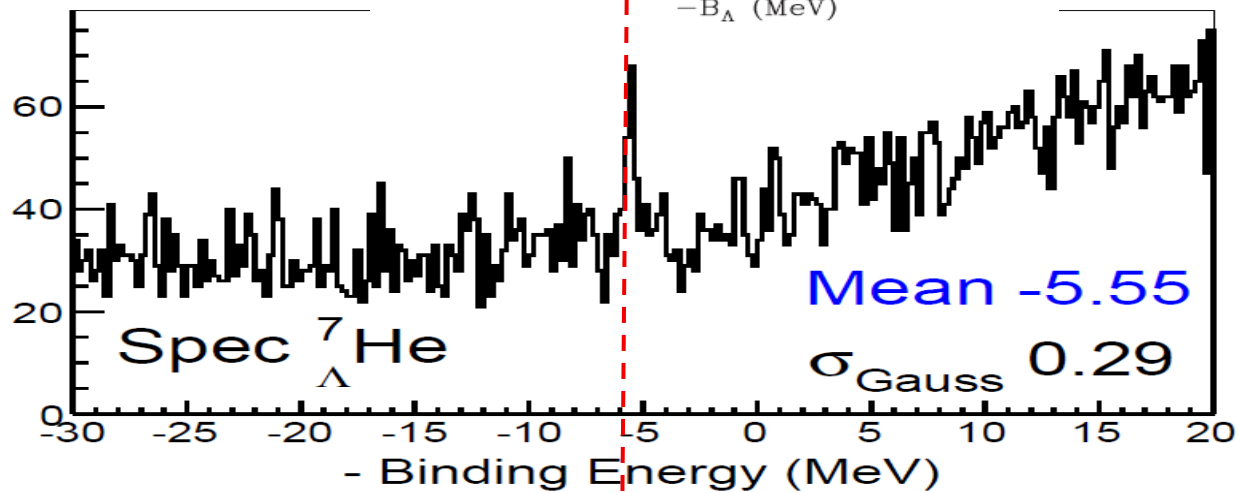


${}^7_{\Lambda}\text{He}$

PRL 110, 012502 (2013)

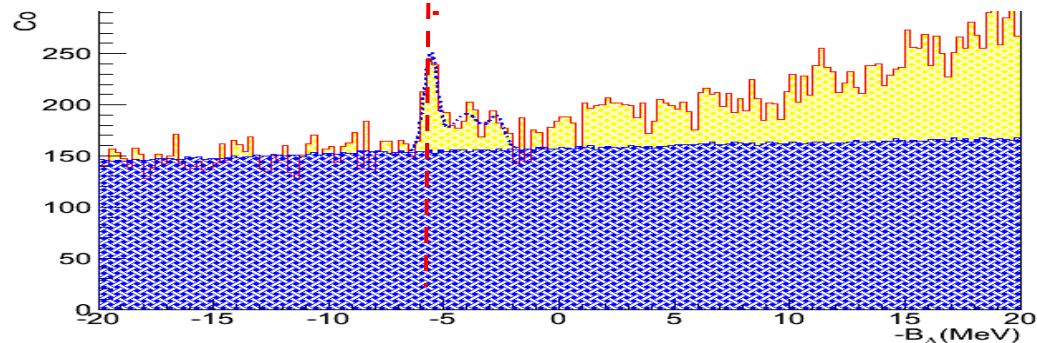


Counts / 0.2 MeV



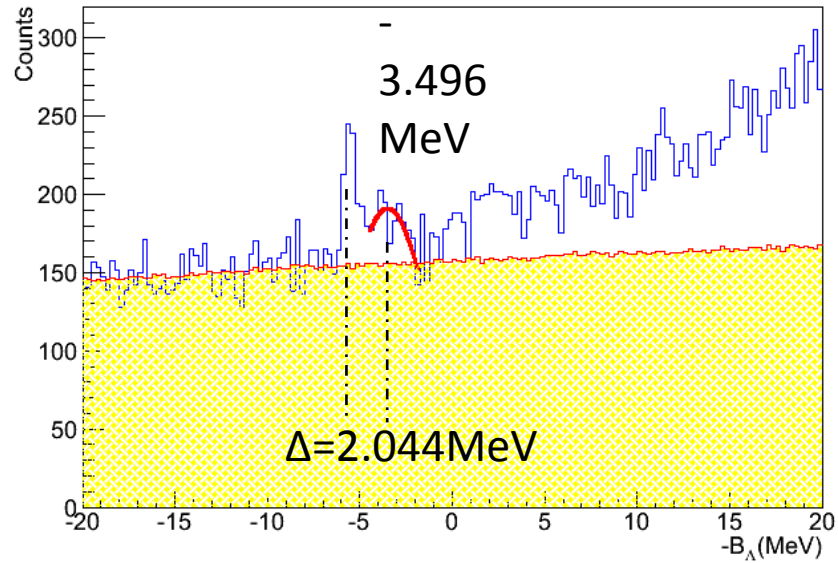
E01-011  
reanalyzed

E05-115

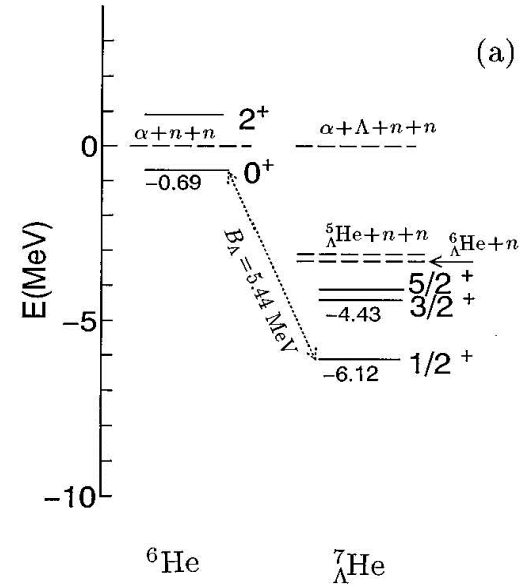
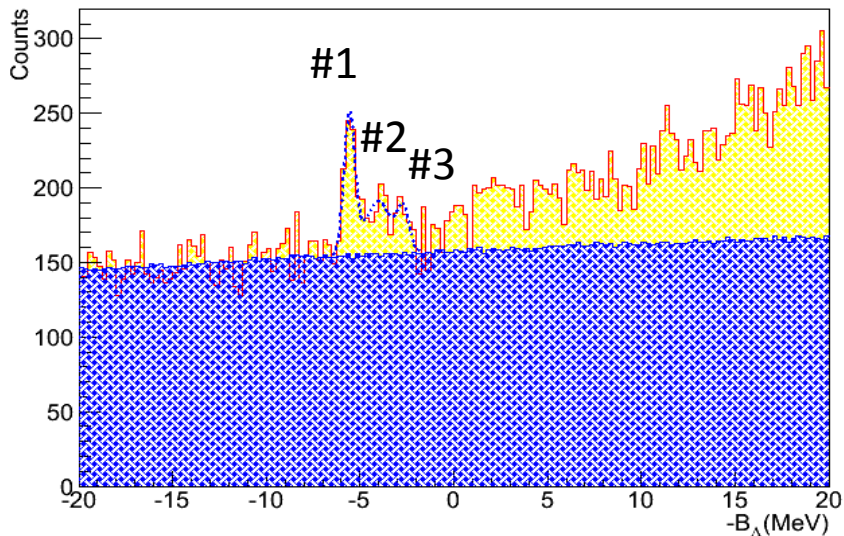


# ${}^7_{\Lambda}\text{He}$

${}^7_{\Lambda}\text{He}$  Missing Mass

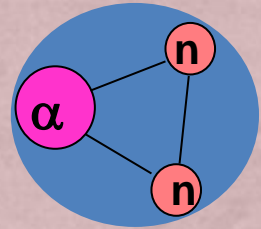


${}^7_{\Lambda}\text{He}$  Missing Mass



E. Hiyama, et al., PRC53 2078 (1996)

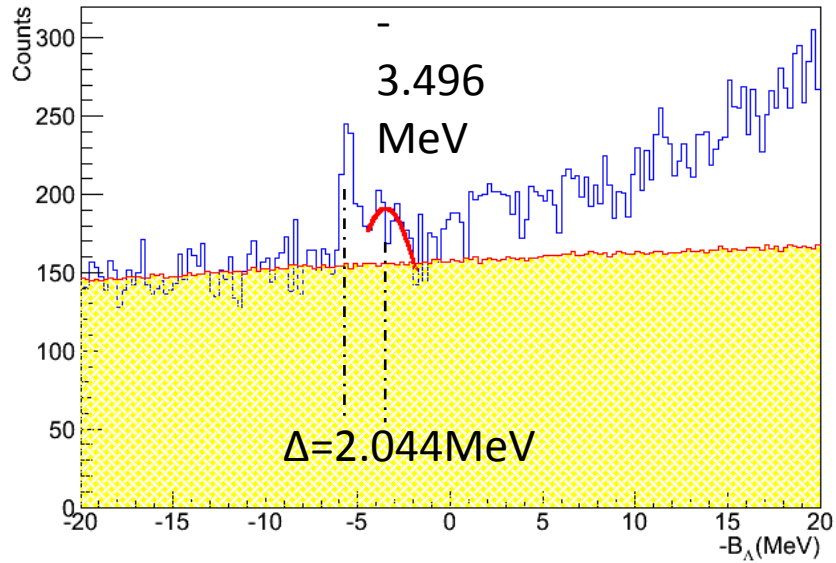
${}^6\text{He}$  core



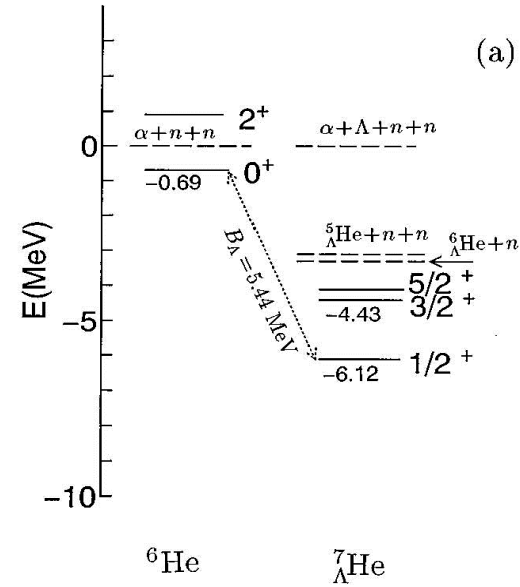
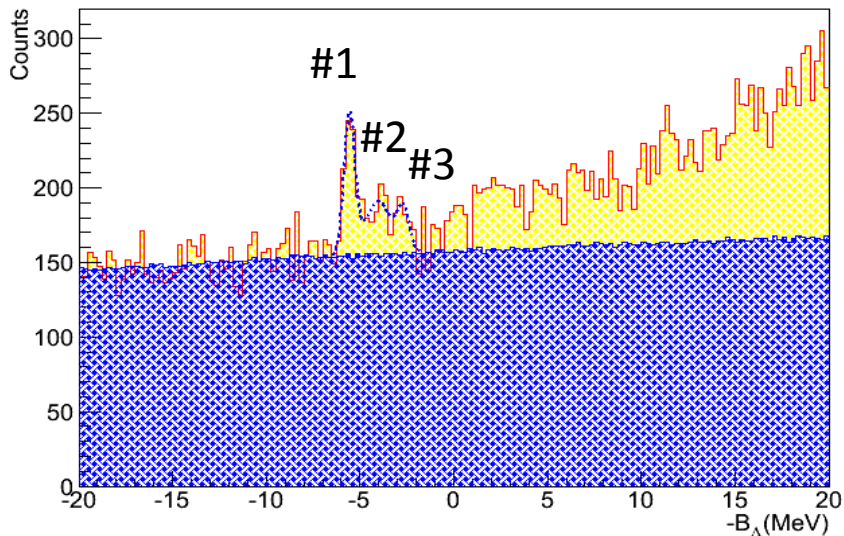
peak	Mean(Me v)	$\sigma \text{ (KeV)}$
1	-5.54	253
2	-4.01	379
3	-2.97	375

# ${}^7_{\Lambda}\text{He}$

${}^7_{\Lambda}\text{He}$  Missing Mass

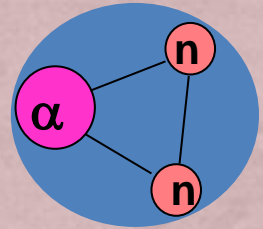


${}^7_{\Lambda}\text{He}$  Missing Mass



E. Hiyama, et al., PRC53 2078 (1996)

${}^6\text{He}$  core



peak	Mean(Me v)	$\sigma(\text{KeV})$
1	-5.54	253
2	-4.01	379
<b>3</b>	<b>-2.97</b>	<b>375</b>

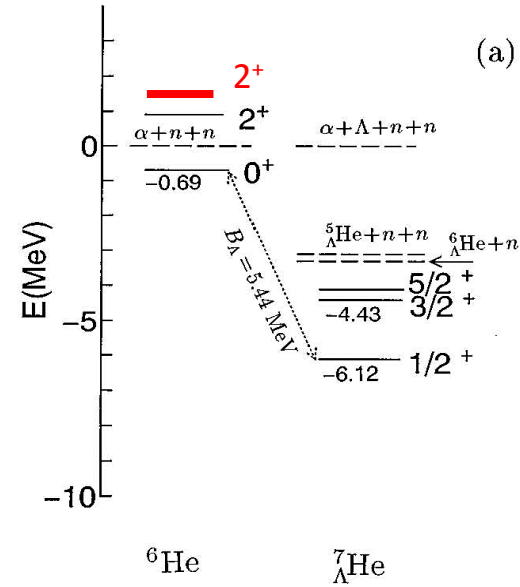
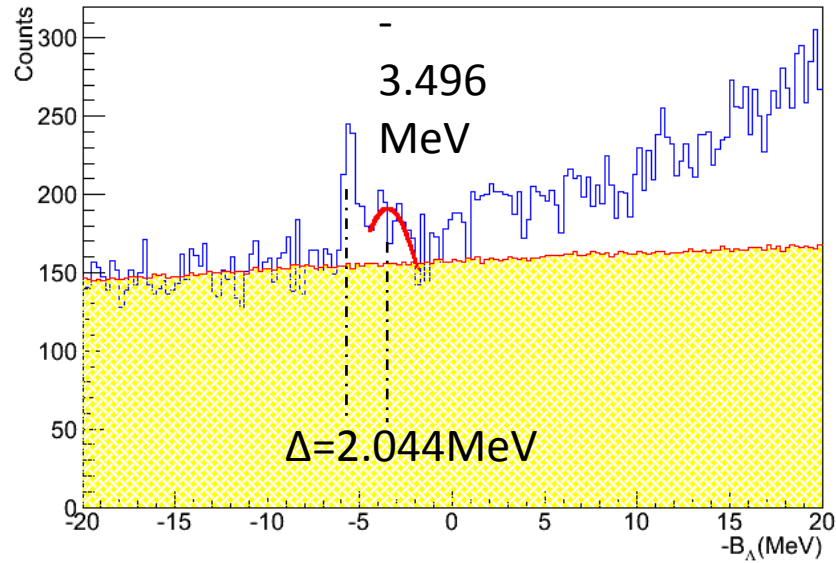
$\Delta E_{\Lambda} \sim 130 \text{ keV}$

$$\frac{3^+}{2} / \frac{5^+}{2}$$

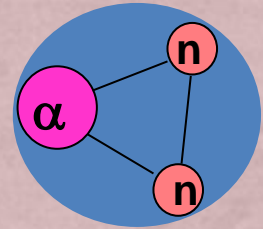


# ${}^7_{\Lambda}\text{He}$

${}^7_{\Lambda}\text{He}$  Missing Mass

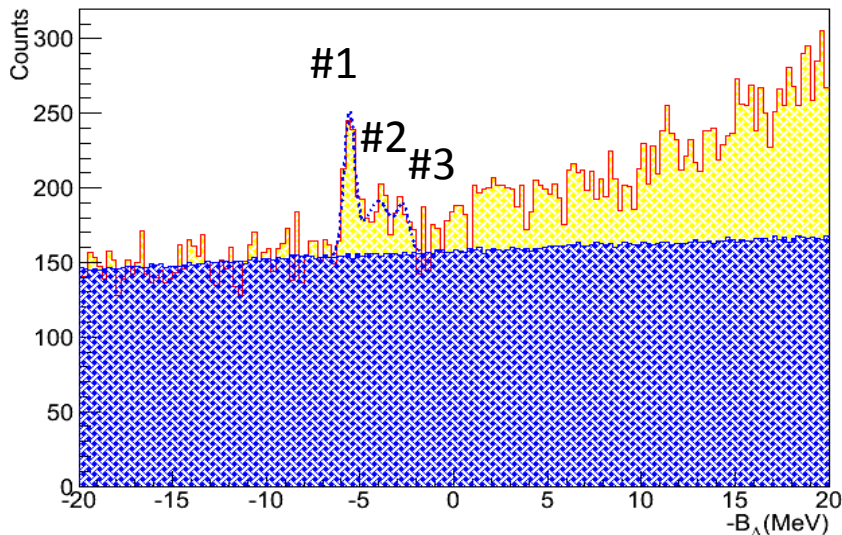


${}^6\text{He}$  core



E. Hiyama, et al., PRC53 2078 (1996)

${}^7_{\Lambda}\text{He}$  Missing Mass



peak	Mean(MeV)	$\sigma \text{ (KeV)}$
1	-5.54	253
2	-4.01	379
3	-2.97	375

$\Delta E_{\Lambda} \sim 130 \text{ keV}$

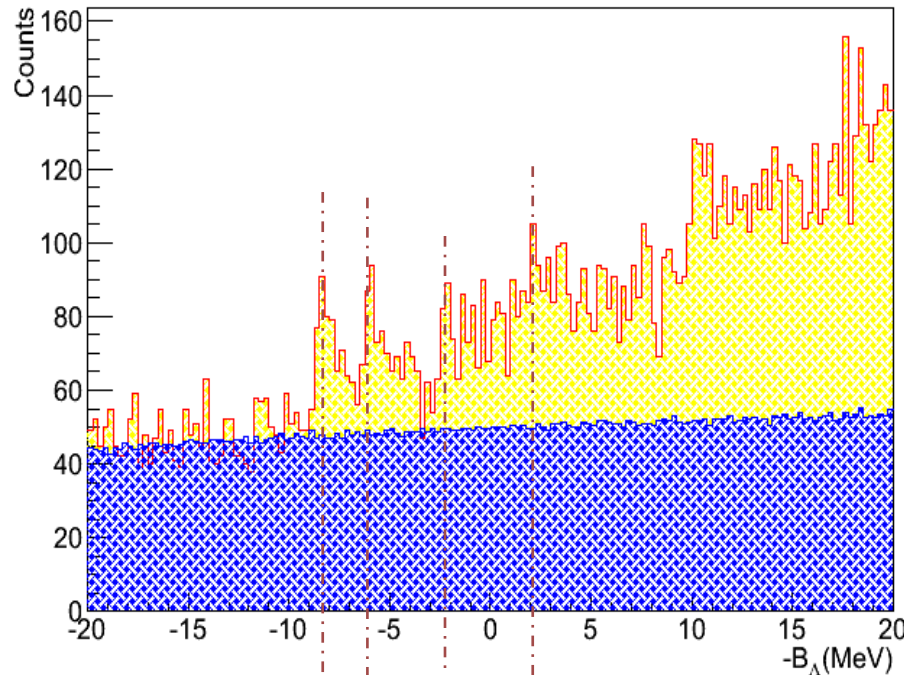
$\frac{3^+}{2} / \frac{5^+}{2}$

Possibility :  
Additional  $2^+$   
core state

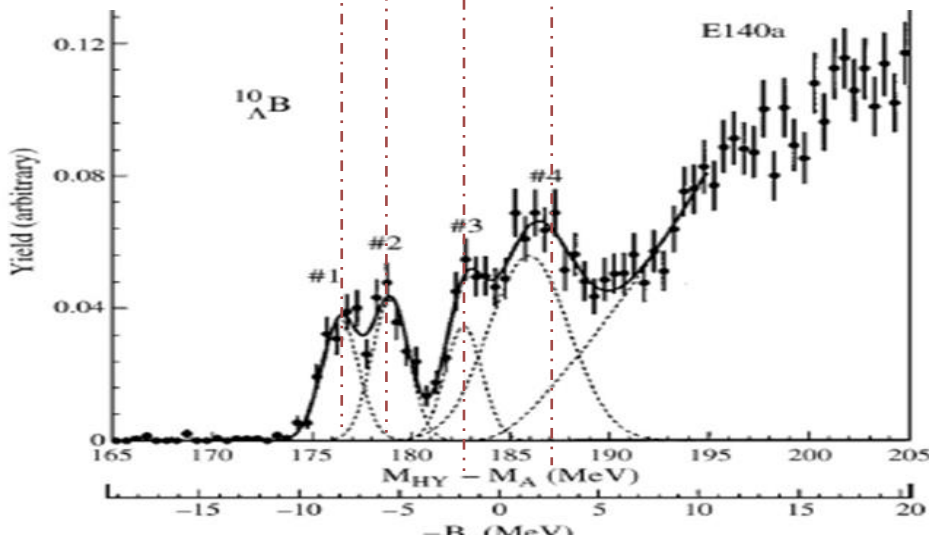
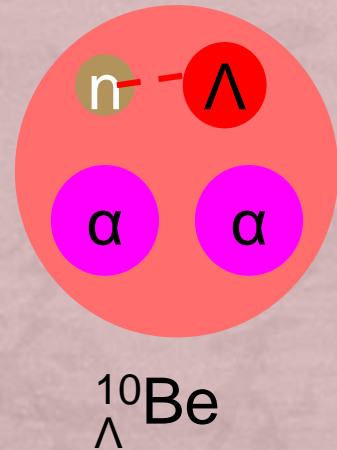
A resonance state

# PRELIMINARY RESULT – $^{10}_{\Lambda}\text{Be}$

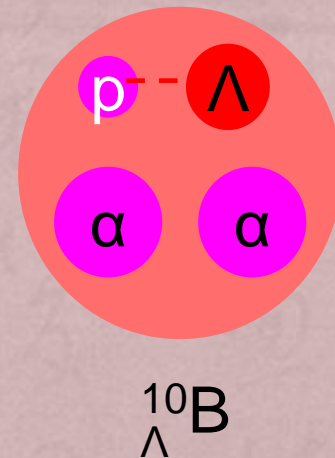
$^{10}_{\Lambda}\text{Be}$  Missing Mass



E05-115

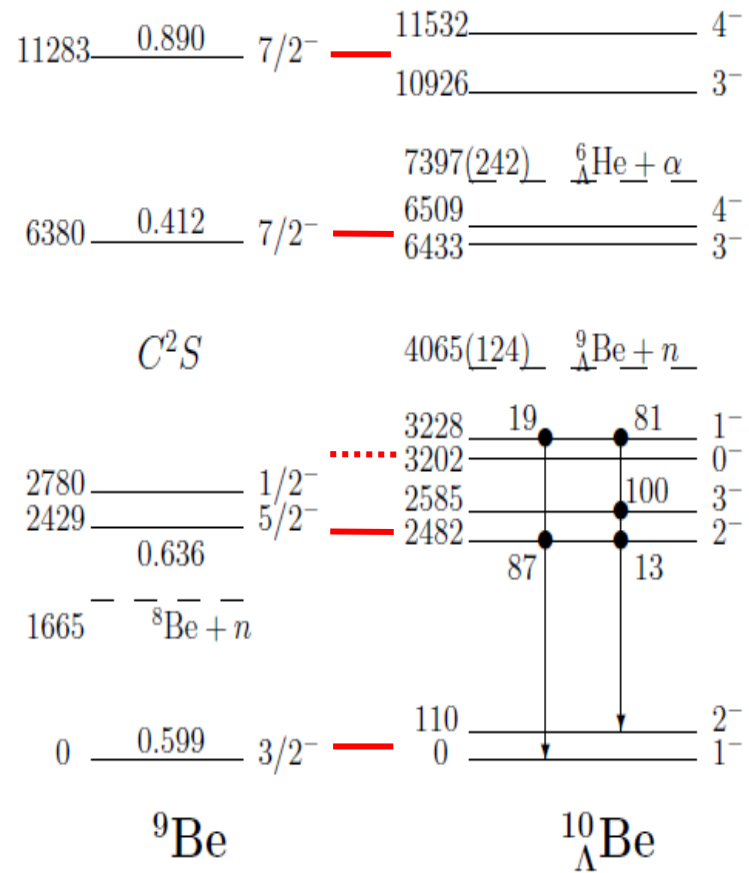
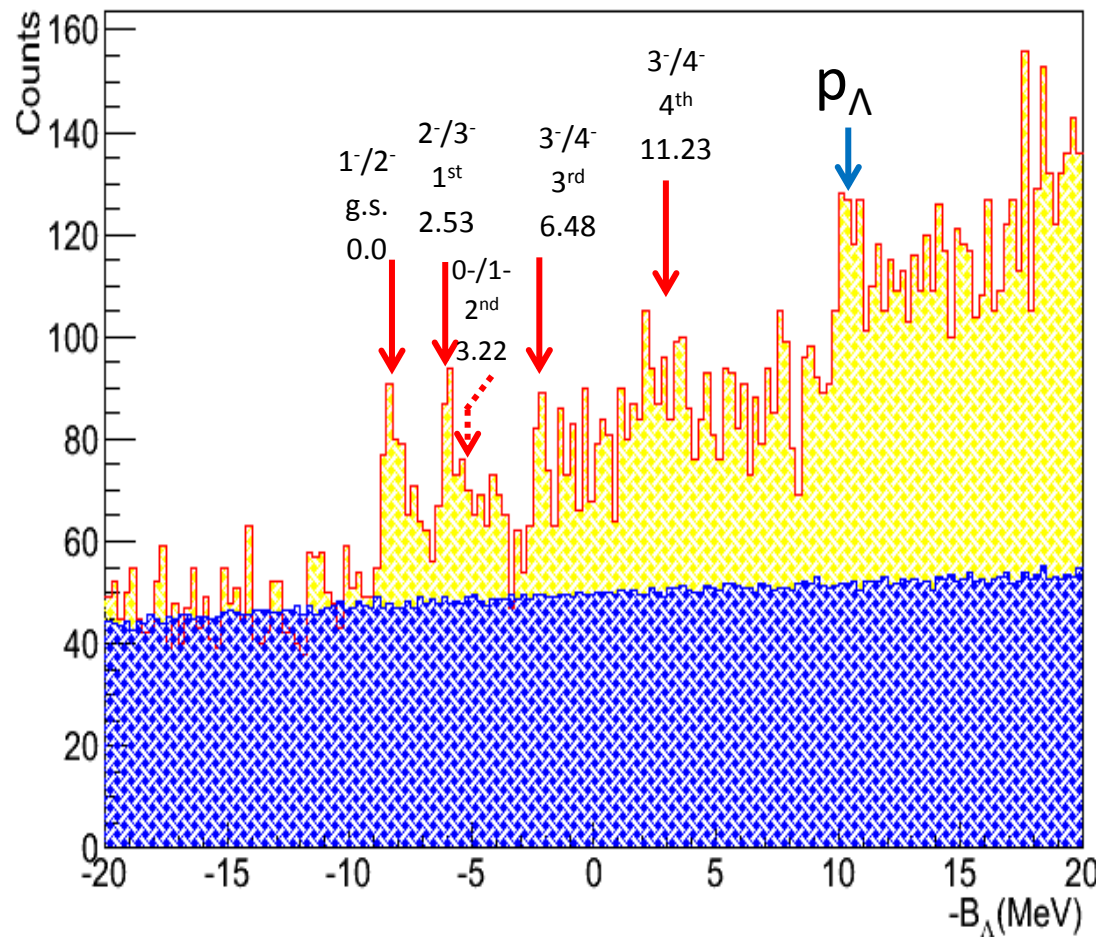


KEK-E140a  
 $^{10}_{\Lambda}\text{B}$



# PRELIMINARY RESULT – $^{10}_{\Lambda}\text{Be}$

$^{10}_{\Lambda}\text{Be}$  Missing Mass

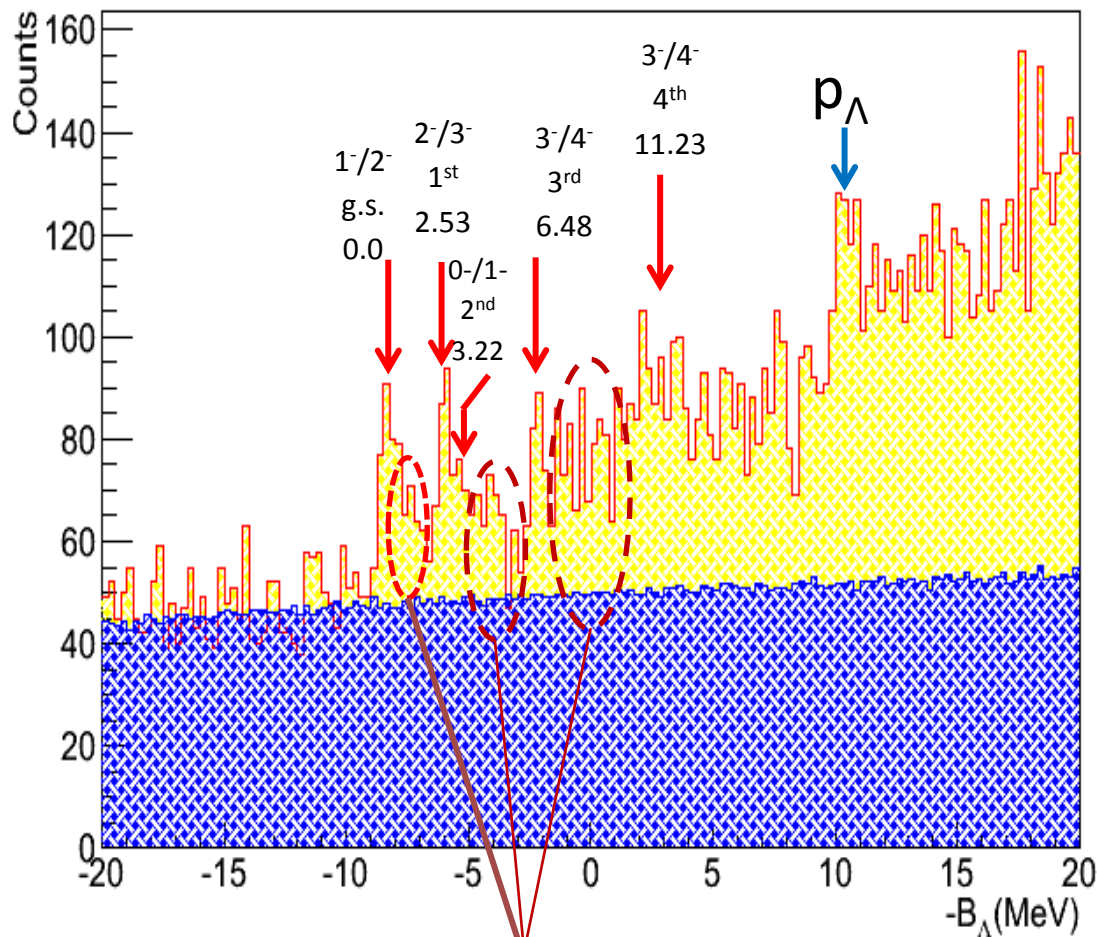


Calculated by D.J. Millener



# PRELIMINARY RESULT – $^{10}_{\Lambda}\text{Be}$

$^{10}_{\Lambda}\text{Be}$  Missing Mass

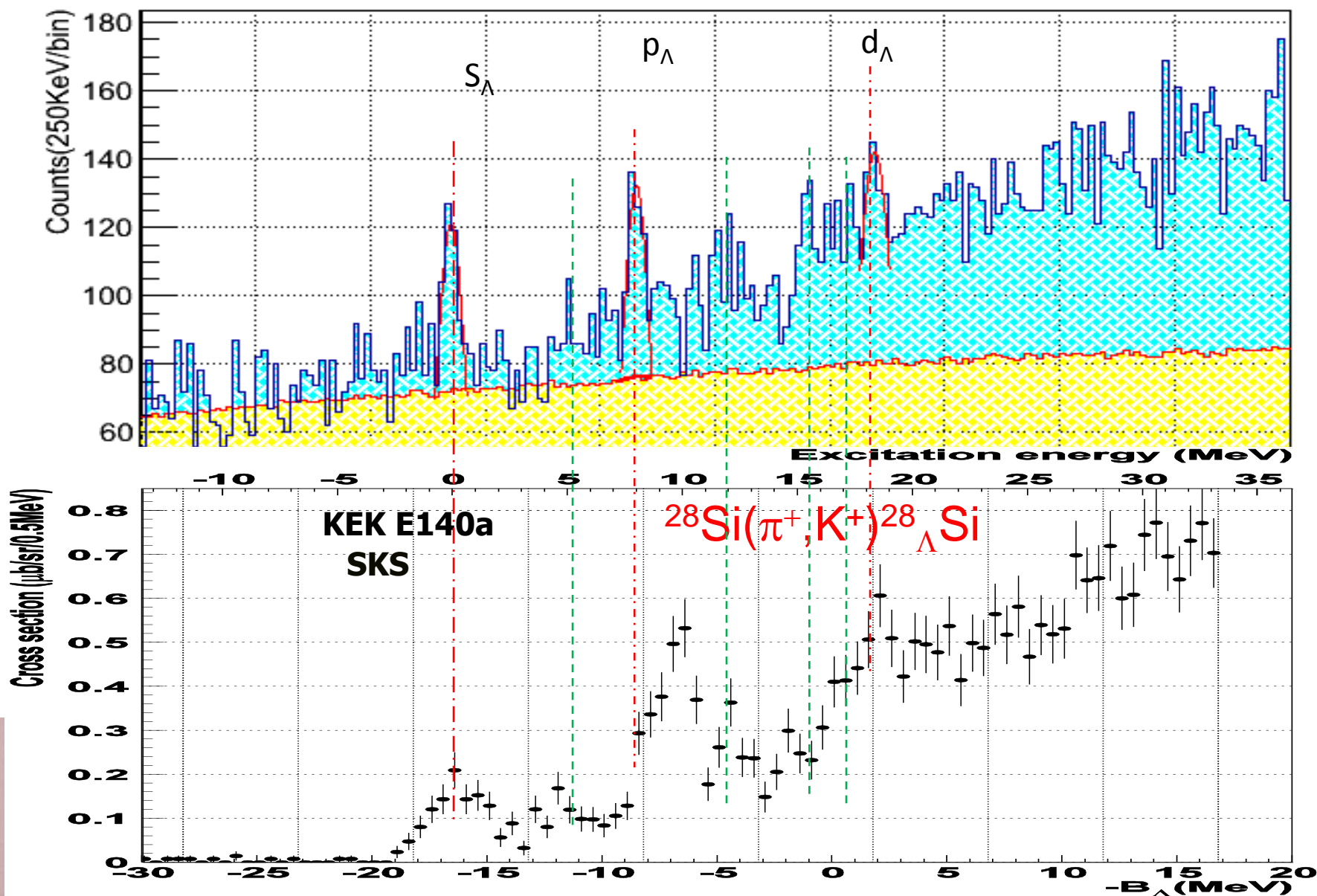


Positive parity core states

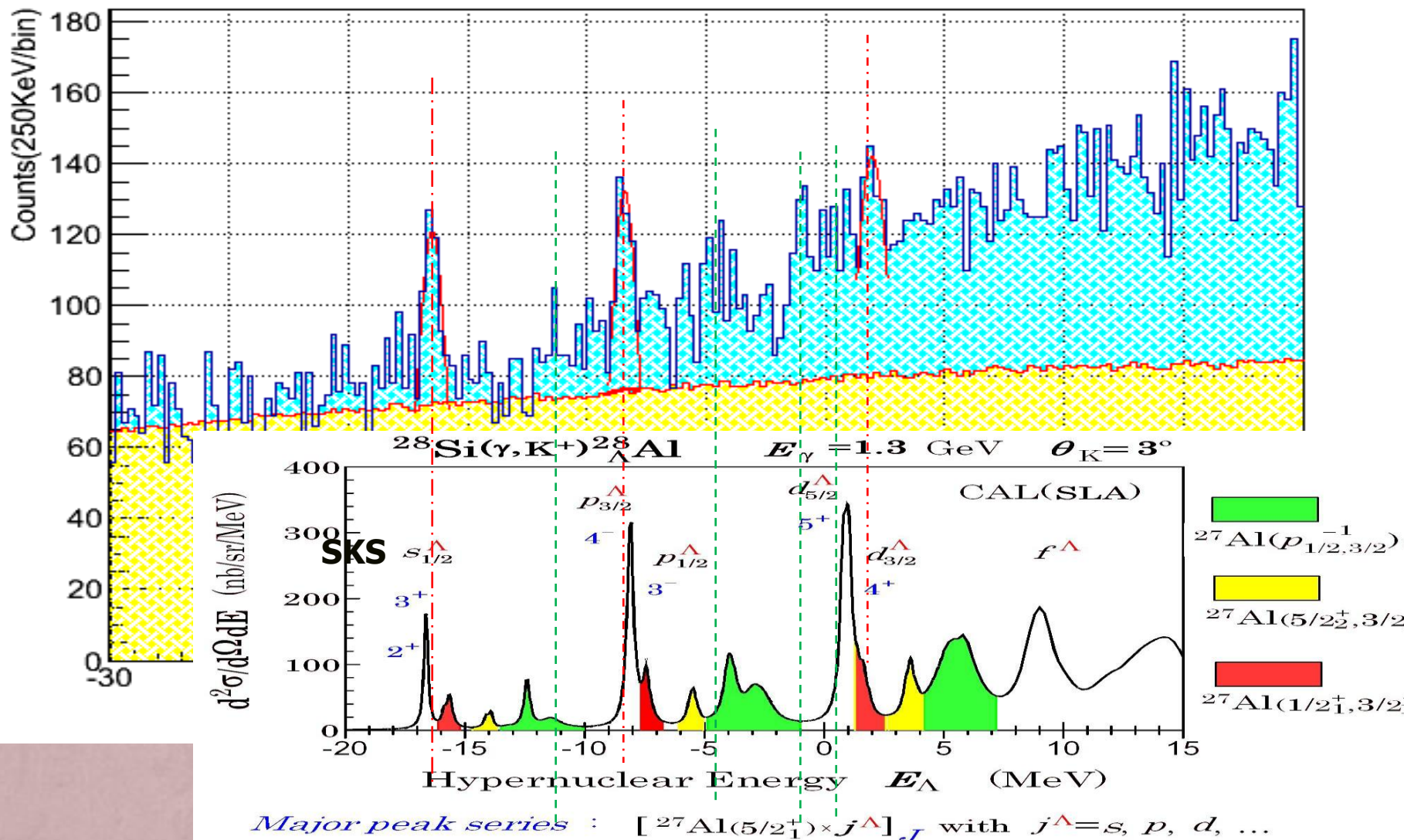
Mirror states ( $T = \frac{1}{2}$ ) in  $A = 9$  nuclei<sup>a</sup>

$^9\text{Be}$	
$E_x$ (MeV)	$J^{\pi}$
0	$\frac{3}{2}^-$
1.684	$\frac{1}{2}^+$
2.429	$\frac{5}{2}^-$
2.78	$\frac{1}{2}^-$
3.049	$\frac{5}{2}^+$
4.704	$(\frac{3}{2})^+$
5.59	$(\frac{3}{2})^-$
6.38 <sup>d</sup>	$\frac{7}{2}^-$
6.76	$\frac{9}{2}^+$
7.94	$(\frac{5}{2})^-$
11.283	$(\frac{7}{2})^-$
11.81	$\frac{5}{2}^-$

# Preliminary Status – $^{28}_{\Lambda}\text{Al}$



# Preliminary Status – $^{28}_{\Lambda}\text{Al}$





# SUMMARY

- Our systematic calibration is almost completed;
- The precise level structure of p-shell  $\Lambda$  hypernuclei ( ${}^7_{\Lambda}\text{He}$ ,  ${}^{10}_{\Lambda}\text{Be}$ , and  ${}^{12}_{\Lambda}\text{B}$ ) are evidential and encouraging;
- There is stronger evidence for sd-shell nuclei from spectroscopy of  ${}^{12}_{\Lambda}\text{B}$  and  ${}^{28}_{\Lambda}\text{Al}$ ;
- ${}^{52}_{\Lambda}\text{V}$  spectroscopy is coming soon.

**BACK UP**

# CALIBRATION PROCEDURE

$$MM = f(E_{beam}, P_k, xt'_k, yt'_k, P_{e'}, xt'_{e'}, yt'_{e'})$$

$$= f(E_{beam_0} + \Delta E_{beam_0}, P_{k0} + \Delta P_{k0}, xt'_k, yt'_k, P_{e'0} + \Delta P_{e'0}, xt'_{e'}, yt'_{e'})$$

$$P = P_0(1 + \delta/100)$$

$$\begin{pmatrix} xt' \\ yt' \\ \delta \end{pmatrix} = (M) \begin{pmatrix} xf' \\ xf' \\ yf' \\ yf' \end{pmatrix}$$

$$= \begin{pmatrix} M_{angle} \\ M_{momentum} \end{pmatrix} \begin{pmatrix} xf' \\ xf' \\ yf' \\ yf' \end{pmatrix}$$

## ❖ Field Map Correction Real Optics

- ✓ Agreement between Simulation data and Real SS data
- ✓ Independence of invariant mass to reconstructed kinematical parameters. ( $\Lambda \& \Sigma$ ;  $P, xt', yt'$ )

Initial  
Matrices

## ❖ Mathematical optimization by **Nonlinear Least Chi<sup>2</sup> fitting**

- a. Central kinematics scan ( $m_{\Lambda}, m_{\Sigma}, \Delta m_{\Lambda \Sigma}$ )
- b. Angular matrices ( $m_{\Lambda}, m_{\Sigma}, \sigma$ )
- c. Momentum matrices ( $^{12}_{\Lambda} Bgs$ )
- d. Iteration

# Kinematics of the E05-115 Experiment

Electron beam

Momentum:  $2.344\text{GeV}/c$

Target nucleus

Scattered electron

Momentum:  $0.844\text{GeV}/c \pm 17\%$   
Angular acceptance:  $3^\circ \sim 9^\circ$

Coincidence measurement

$\gamma + p \rightarrow \Lambda + K^+$

$1.5\text{GeV}$

$\gamma$

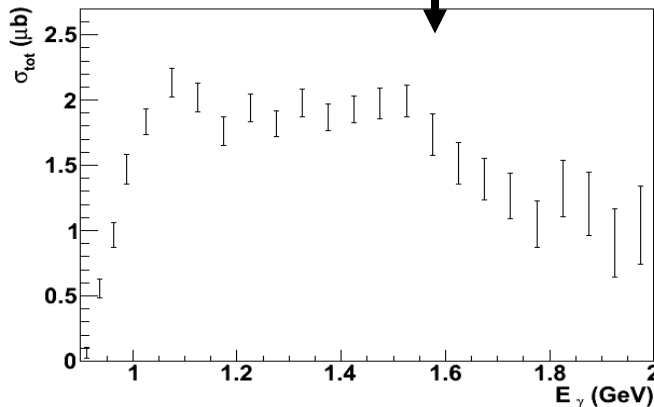
$p$

$\Lambda$

$K^+$

Momentum:  $1.2\text{GeV}/c \pm 12.5\%$

Angular acceptance :  $1^\circ \sim 13^\circ$





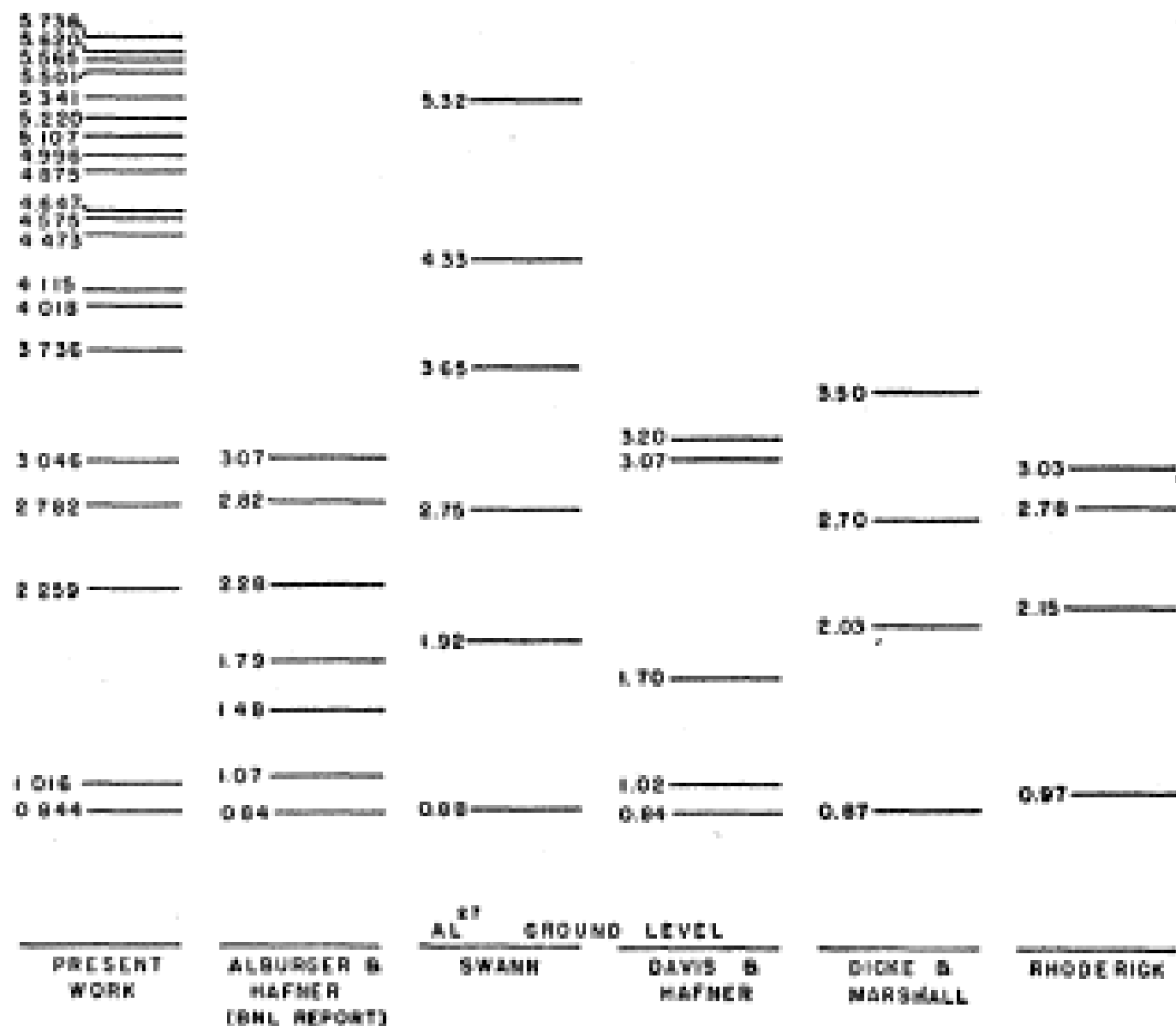
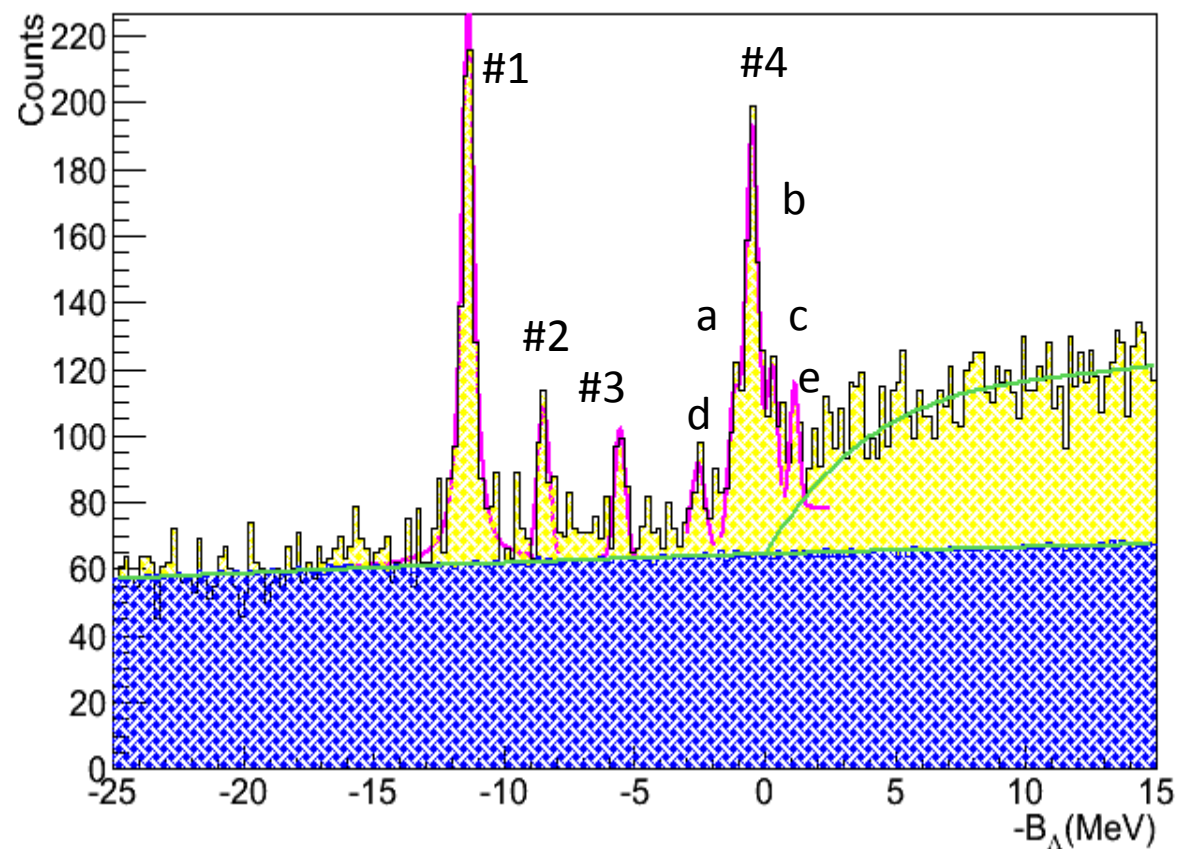


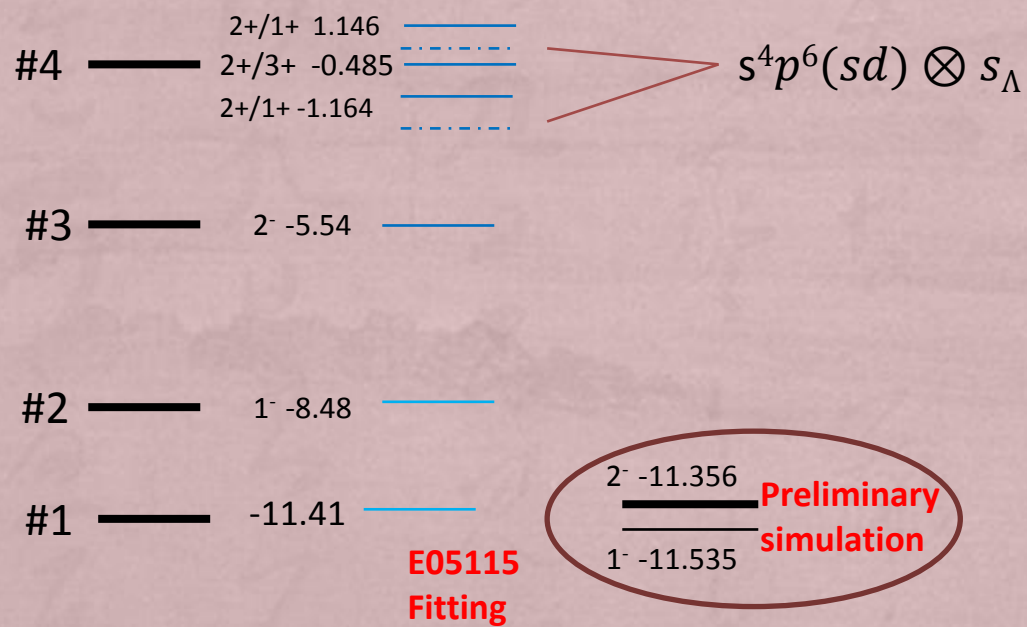
FIG. 2. Energy level scheme for  $Al^{27}$ .

# $^{12}_{\Lambda}\text{B}$

$^{12}_{\Lambda}\text{B}$  Missing Mass



peak		Mean(Me v)	$\sigma$ (KeV)
4	1	-11.41	265
	2	-8.48	231
	3	-5.54	210
	a	-1.164	240
	b	-0.485	
	c	0.295	
	d	-2.539	
	e	1.146	172



peak		Mean(MeV)	$\sigma$ (KeV)
1		-11.41	265
2		-8.48	231
3		-5.54	210
4	a	-1.164	240
	b	-0.485	
	c	0.295	
	d	-2.539	281
	e	1.146	234