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# *The EMC Effect and The Quest for High $x$ Quark Distributions*

Patricia Solvignon

Argonne National Laboratory

*Nathan Isgur Distinguished Postdoctoral Fellowship Seminar*  
Jefferson Lab  
June 23, 2009

# Outline

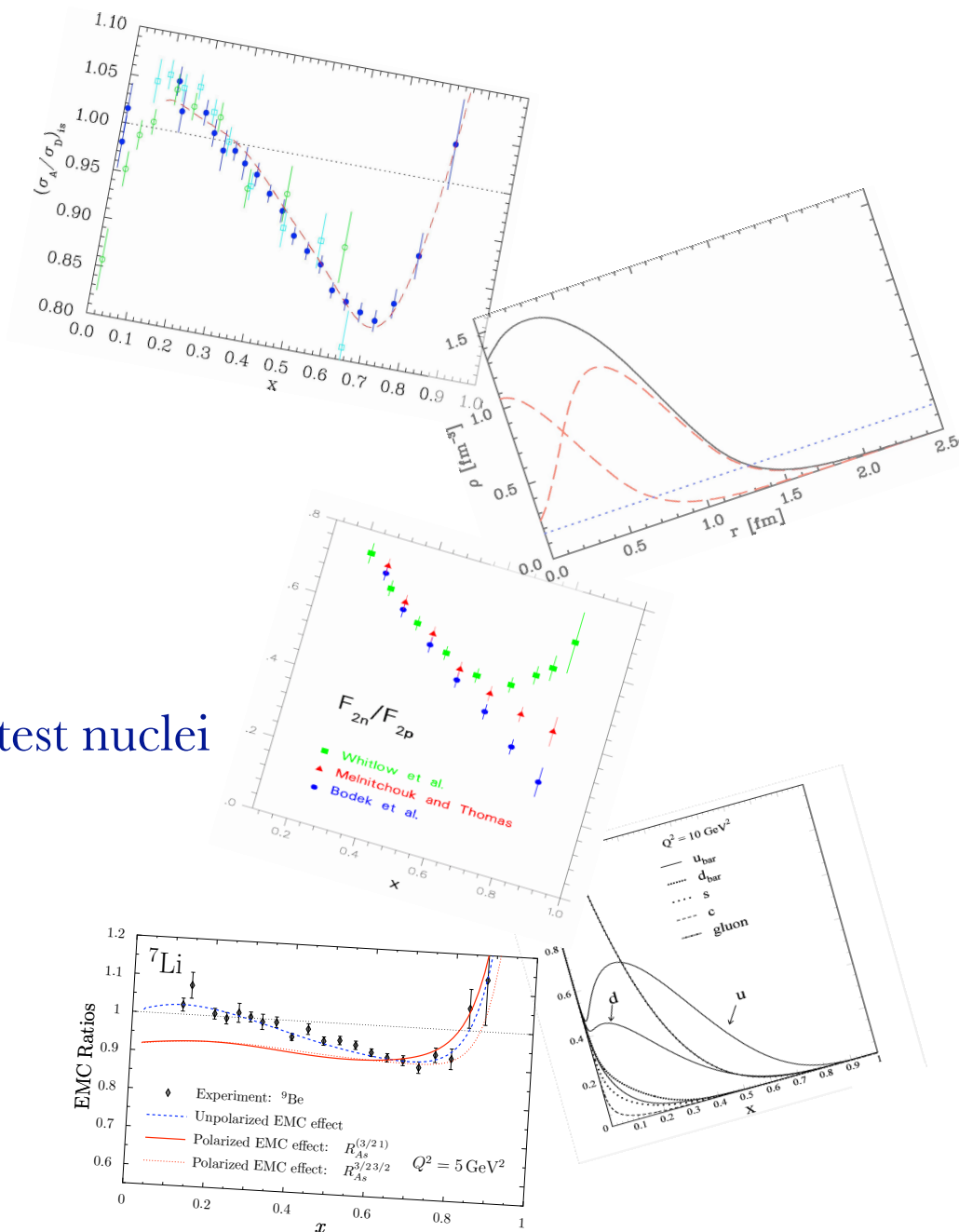
## □ The EMC effect

- Short introduction
- JLab Hall C E03-103 results:
  - ☉ *Light nuclei*
  - ☉ *Heavy nuclei and Coulomb distortion*

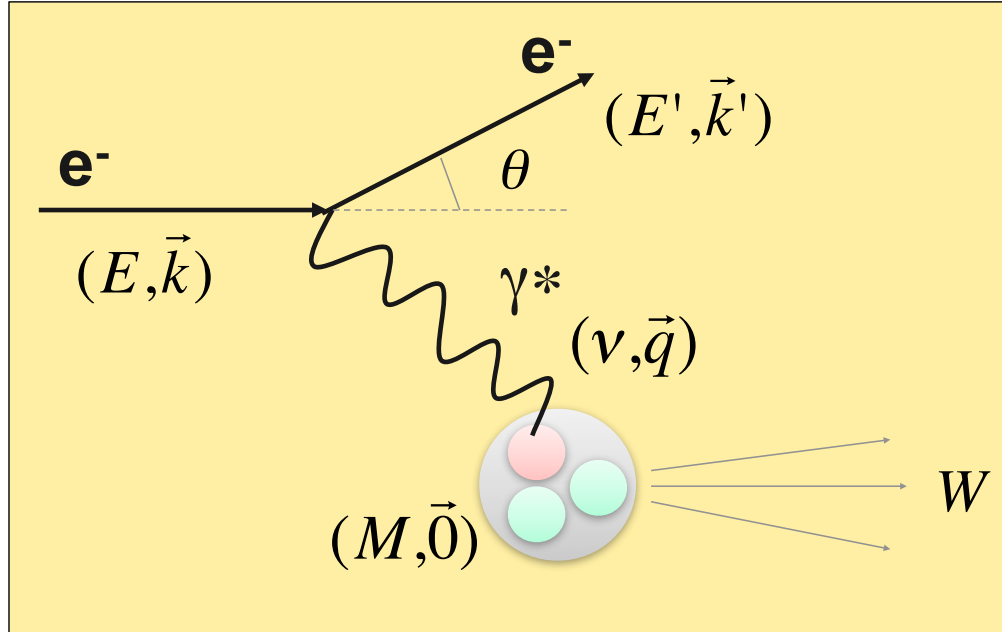
## □ What's next ?

- $F_2(^3\text{H})/F_2(^3\text{He})$ : EMC effect on lightest nuclei
- $F_{2n}/F_{2p}$  and  $d/u$  at high  $x$
- Polarized EMC effect

## □ Summary and Outlook



# Deep inelastic scattering



4-momentum transfer squared

$$Q^2 = -q^2 = 4EE' \sin^2 \frac{\theta}{2}$$

Invariant mass squared

$$W^2 = M^2 + 2M\nu - Q^2$$

Bjorken variable

$$x = \frac{Q^2}{2M\nu} = \text{quark momentum fraction}$$

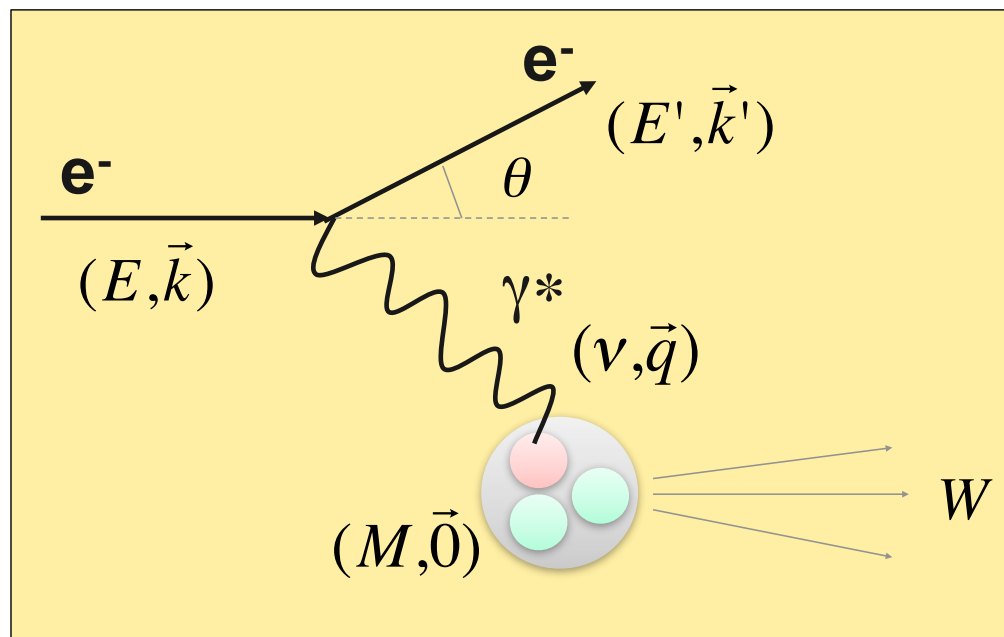
**DIS scattering measures structure function  $F_2(\mathbf{x})$**

$$\frac{d^2\sigma}{d\Omega dE'} = \sigma_{Mott} \left[ \frac{1}{\nu} F_2(x, Q^2) + \frac{2}{M} F_1(x, Q^2) \tan^2 \frac{\theta}{2} \right]$$

**In the parton model,**  $F_2(\mathbf{x})$  related to parton momentum distributions (pdfs)

$$F_1(x) = \frac{1}{2} \sum_i e_i^2 [q_i^\uparrow(x) + q_i^\downarrow(x)] = \frac{1}{2x} F_2(x)$$

# The quest for higher precision data

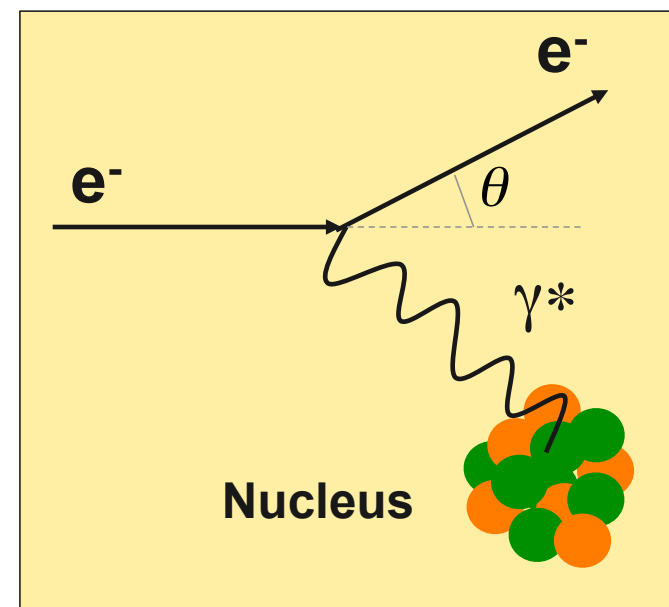


To increase the luminosity, physicists decided to use heavy nuclei to study the structure of the proton instead of a hydrogen target.

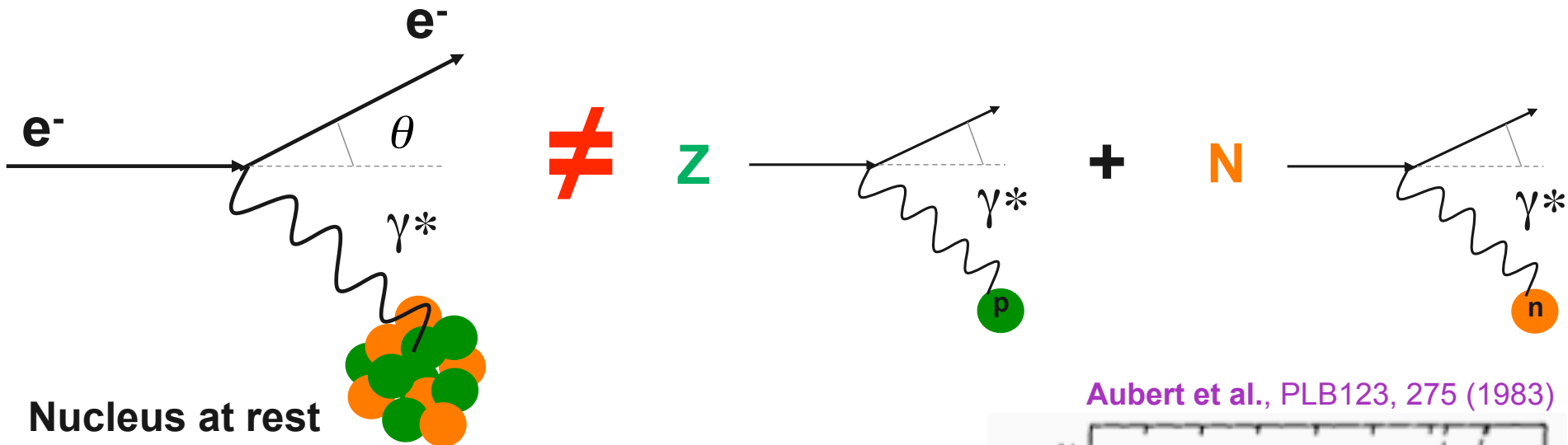
For nuclei,  
binding energies  $\ll$  energy  
scale of the probe

Expected

$$F_2^A(x) \approx Z F_2^p(x) + N F_2^n(x)$$



# The EMC effect

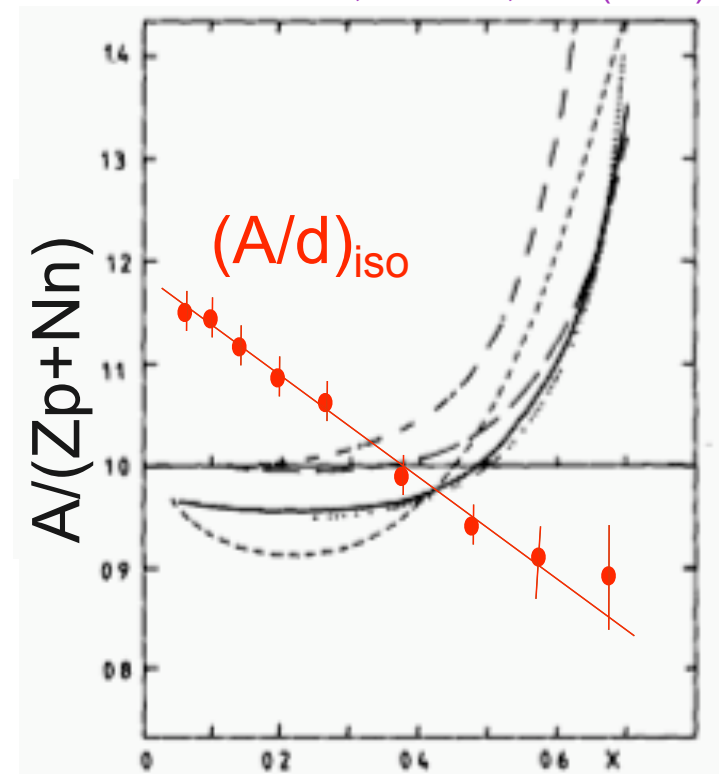


**Nucleus at rest**  
 ( $A$  nucleons =  $Z$  protons +  $N$  neutrons)

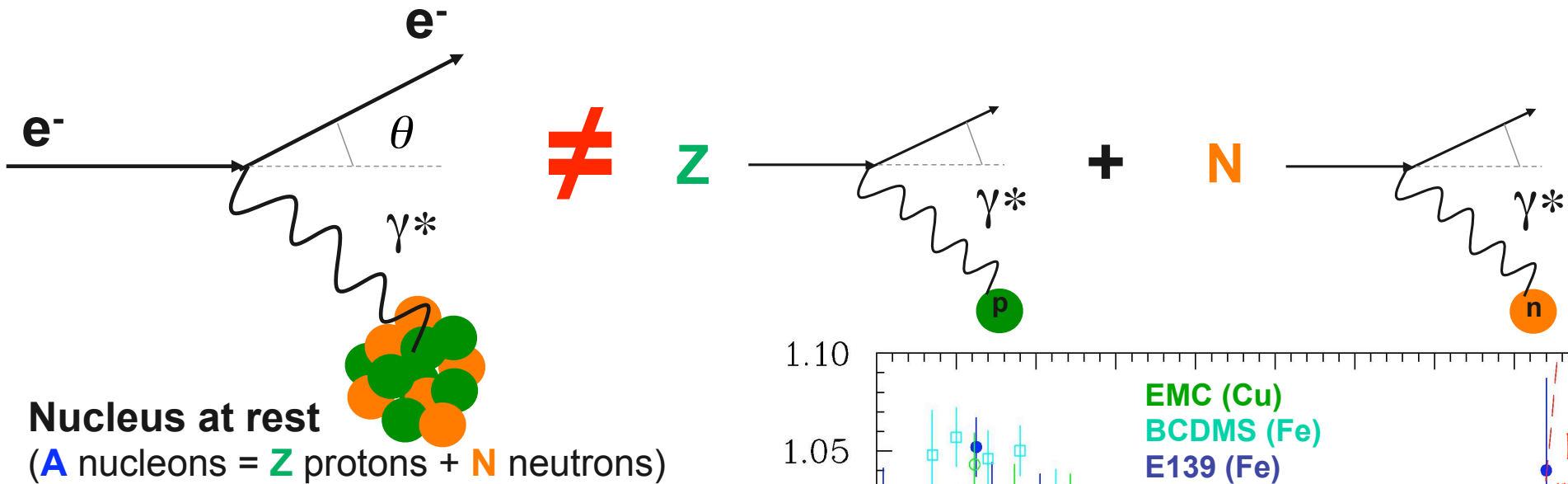
First measurement by the EMC collaboration (1983) found an **excess of low- $x$  quarks**, **deficit of high- $x$  quarks** in heavy nuclei

**Nuclear structure:** 
$$F_2^A \neq ZF_2^p + NF_2^n$$

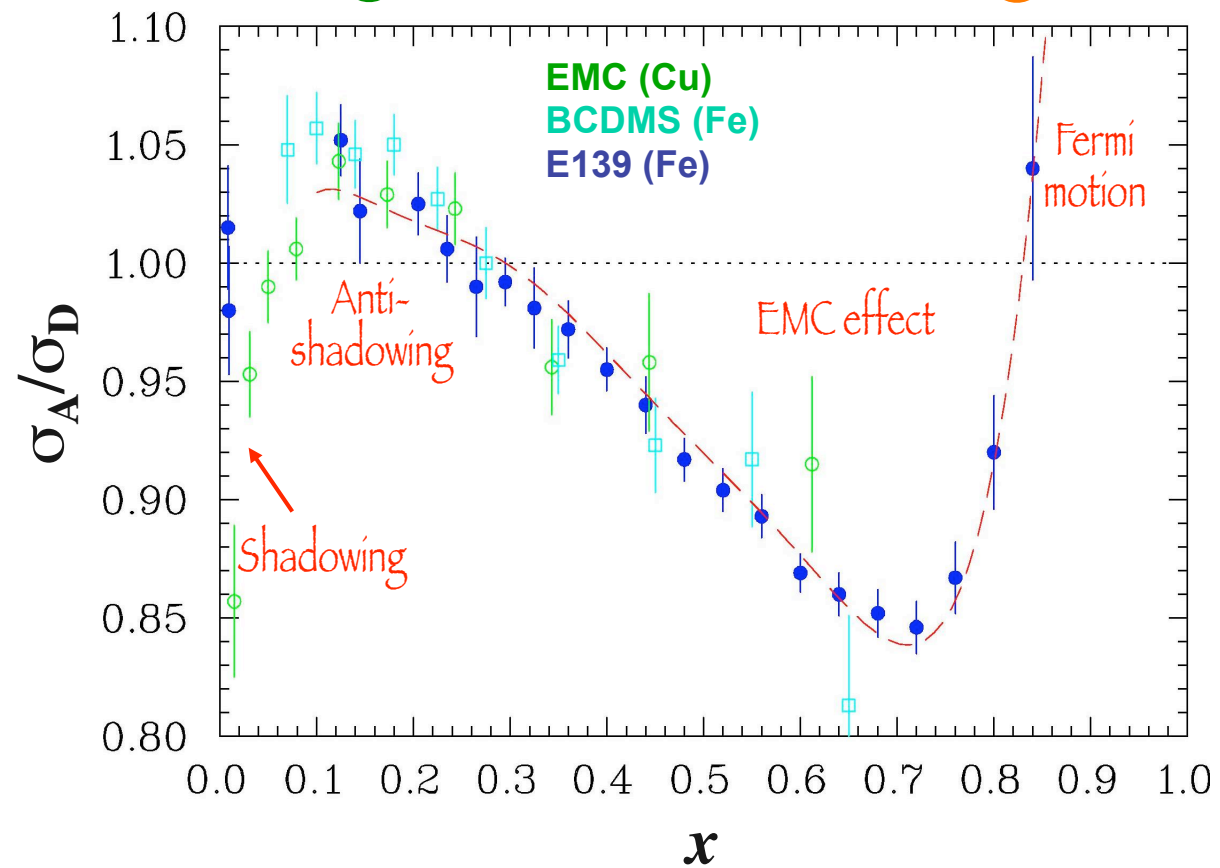
Aubert et al., PLB123, 275 (1983)



# The EMC effect



Effects found in  
several experiments  
at CERN, SLAC, DESY



# Nucleon only model

Assumptions on the nucleon structure function:

- not modified in medium
- the same on and off the energy shell

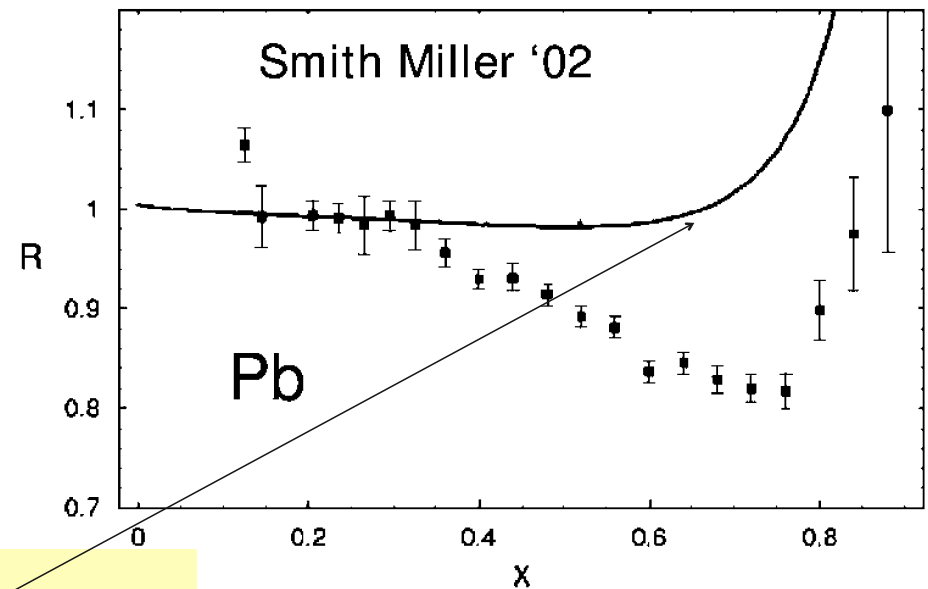
$$\frac{F_2^A(x_A)}{A} = \int_{x_A}^A dy \cdot f_N(y) F_2^N(x_A/y)$$

Fermi momentum  $\ll M_{\text{nucleon}}$

→  $f_N(y)$  is narrowly peaked and  $y \approx 1$

$$\frac{F_2^A}{A} \approx F_2^N \rightarrow \text{no EMC effect}$$

Smith & Miller,  
PRC 65, 015211 and 055206 (2002)



“... some effect not contained within the conventional framework is responsible for the EMC effect.” Smith & Miller, PRC 65, 015211 (2002)

# Nucleons and pions model

Pion field is enhanced and pions carry an excess of plus momentum:

$$P^+ = P_N^+ + P_\pi^+ = M_A$$

and using  $P_\pi^+ / M_A = 0.04$  is enough to reproduce the EMC effect.

But excess of nuclear pions



enhancement of the nuclear sea

However this enhancement was not seen in nuclear Drell-Yan reaction

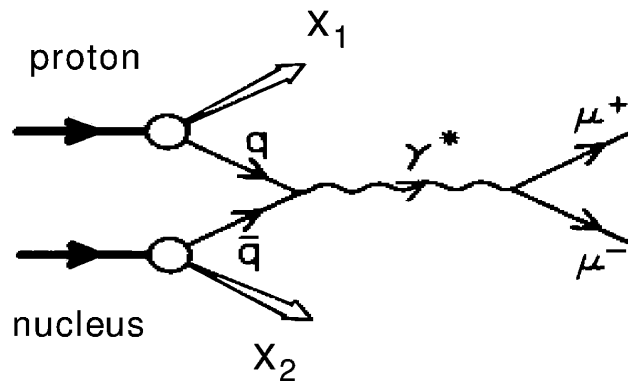
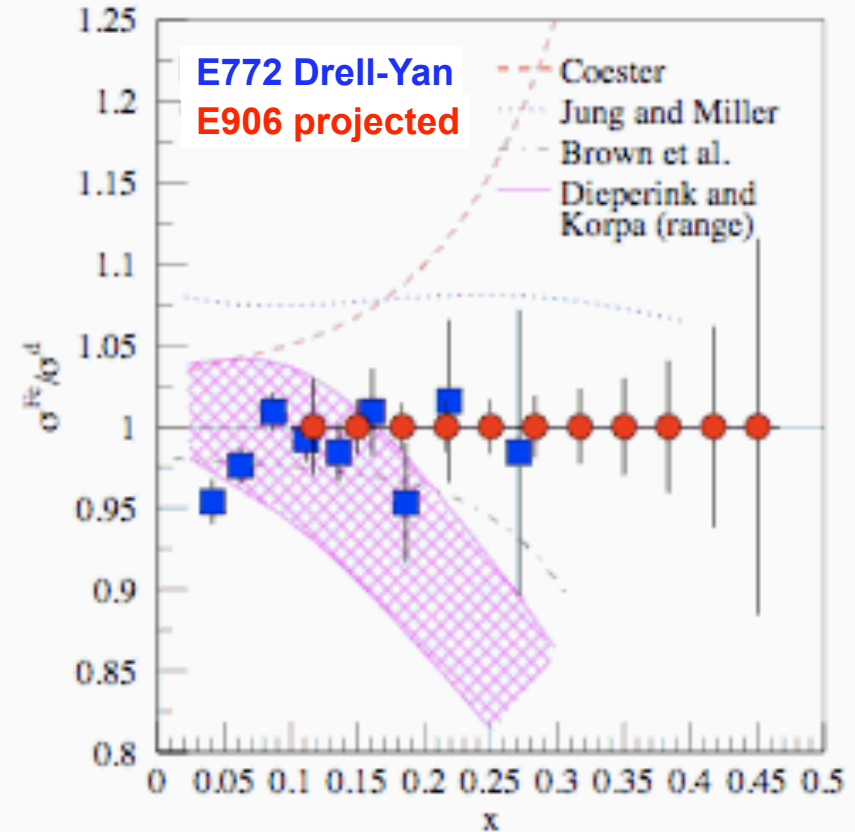


Fig from P. Reimer, Eur.Phys. J A31, 593 (2007)





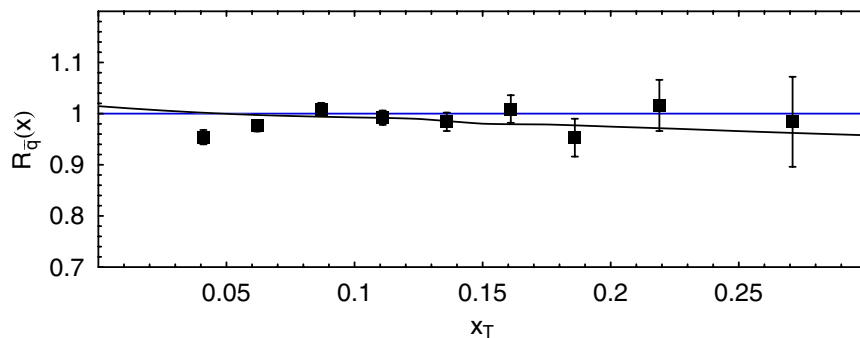
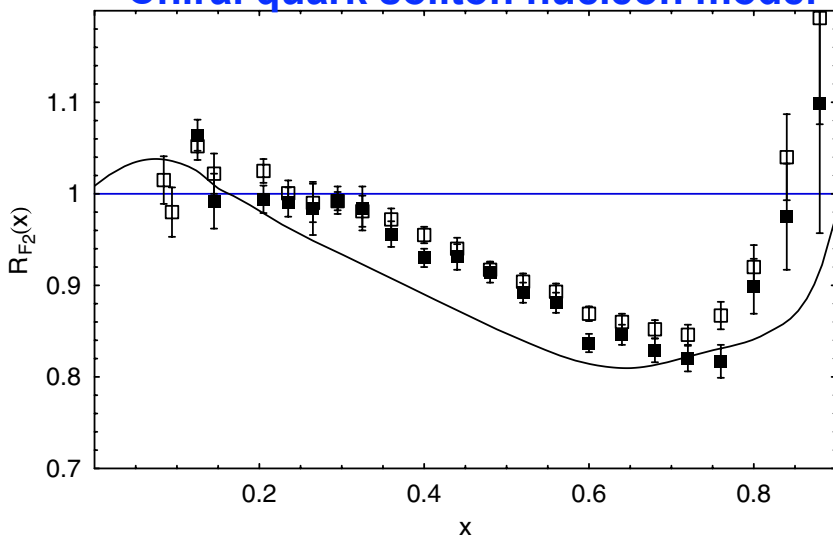
# Another class of models

## Interaction between nucleons

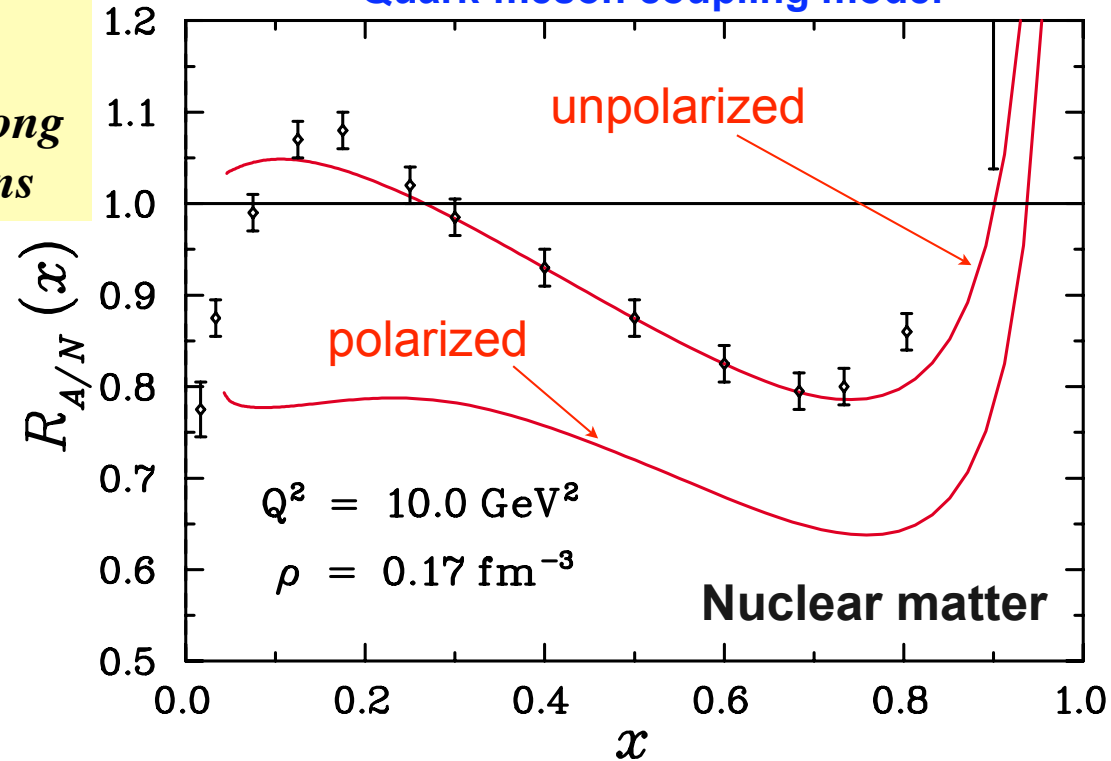
### Model assumption:

*nucleon wavefunction is changed by the strong external fields created by the other nucleons*

Smith & Miller, PRL 91, 212301 (2003)  
Chiral quark soliton nucleon model



Cloet, Bentz, and Thomas, PLB 642, 210 (2006)  
Quark-meson coupling model



### Model requirements:

- *Momentum sum rule*
- *Baryon number conservation*
- *Vanishing of the structure function at  $x < 0$  and  $x > A$*
- *Should describe the DIS and DY data*

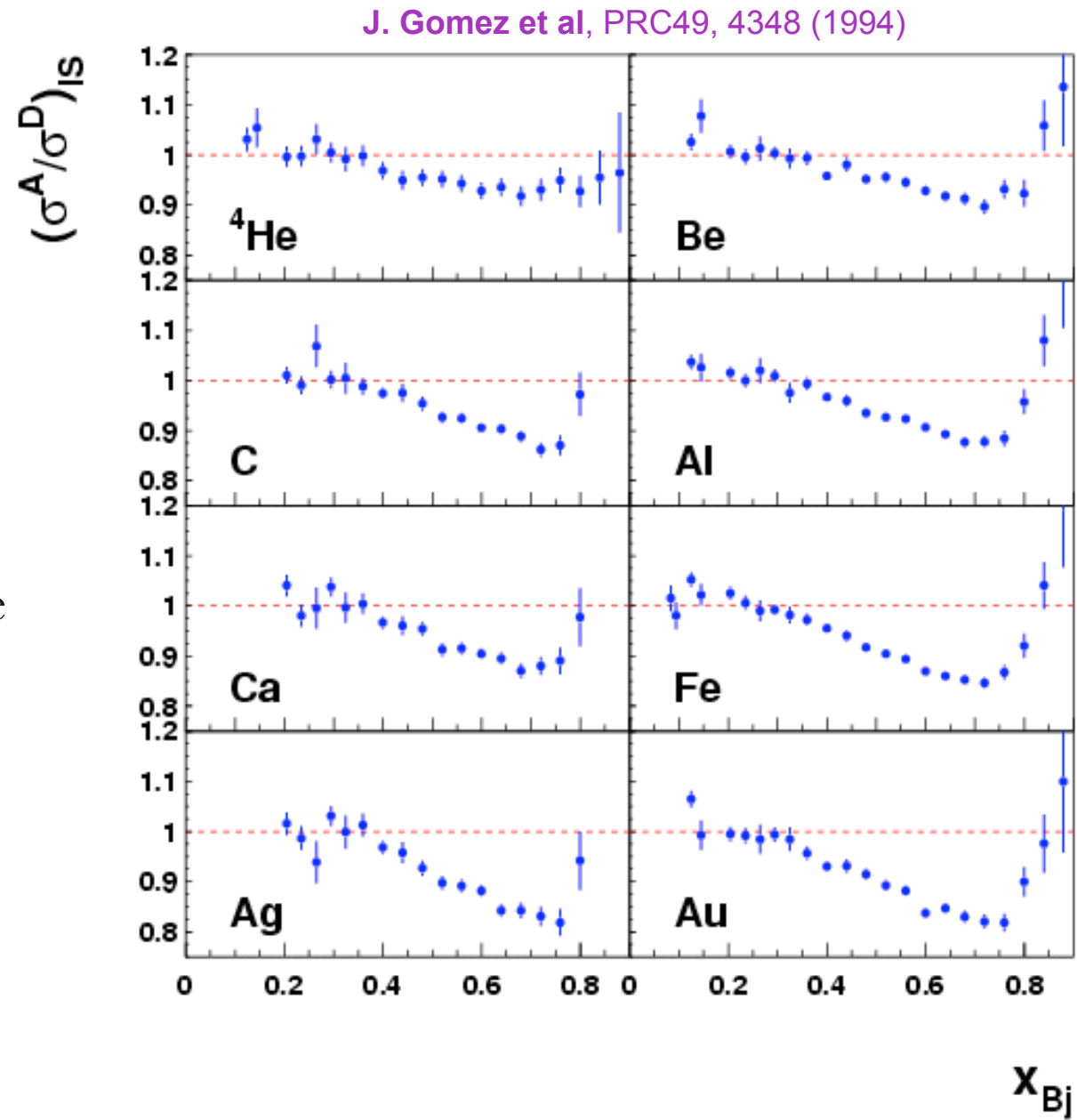
# Existing EMC Data

## SLAC E139:

- Most precise large x data
- Nuclei from A=4 to A=197

## Observations:

- Universal x-dependence shape



# Existing EMC Data

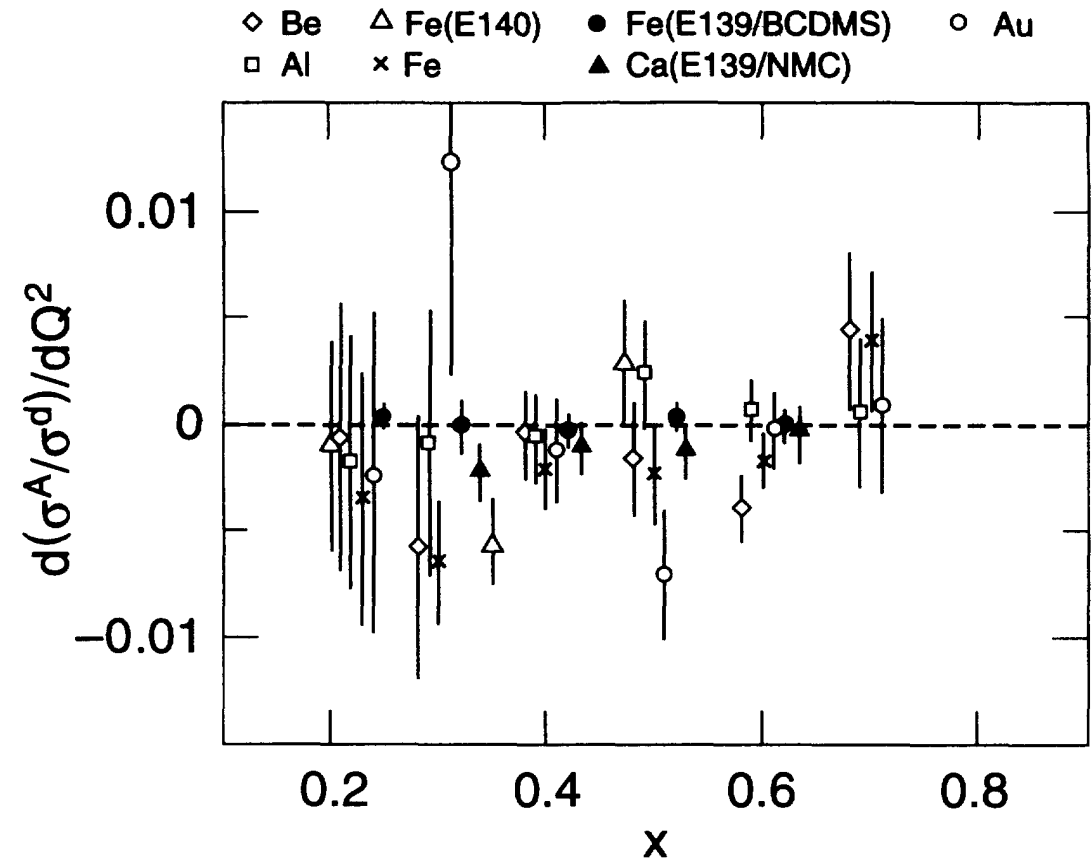
J. Gomez et al, PRC49, 4348 (1994)

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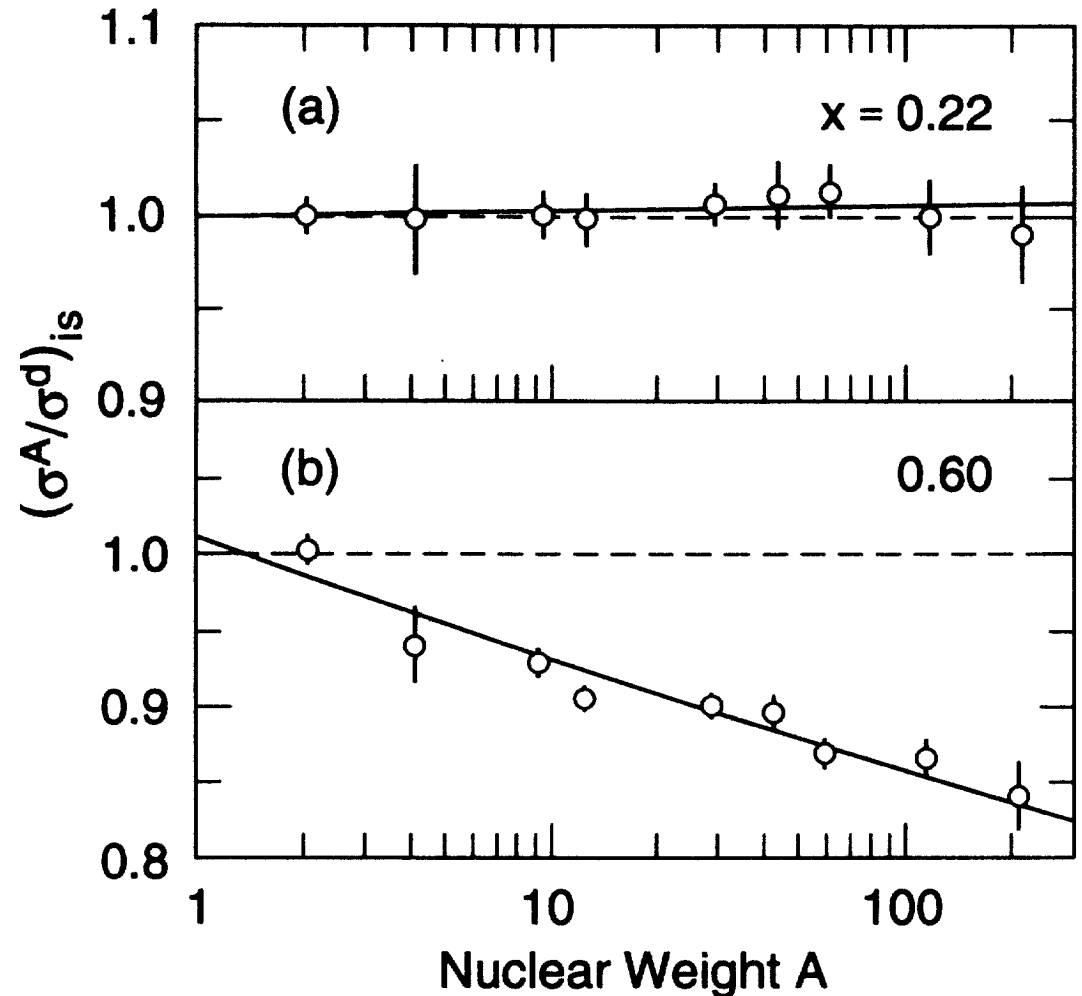
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  - Scale with  $A^{-1/3}$



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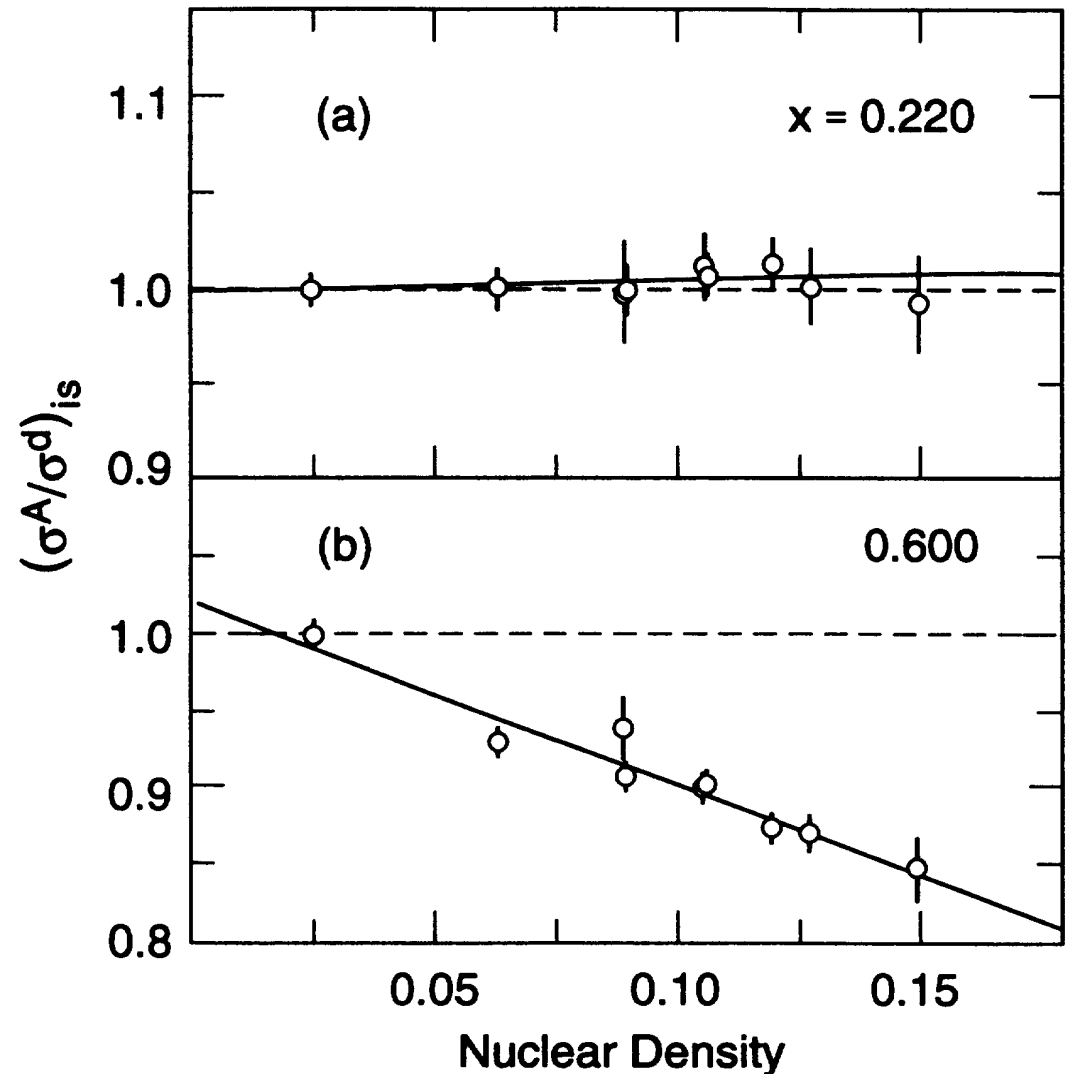
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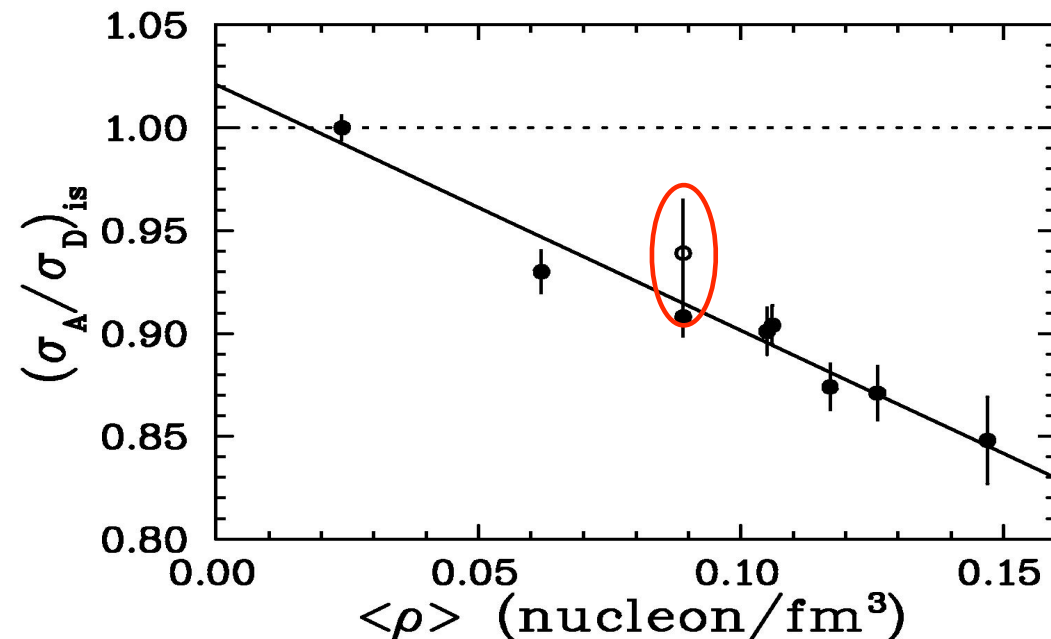
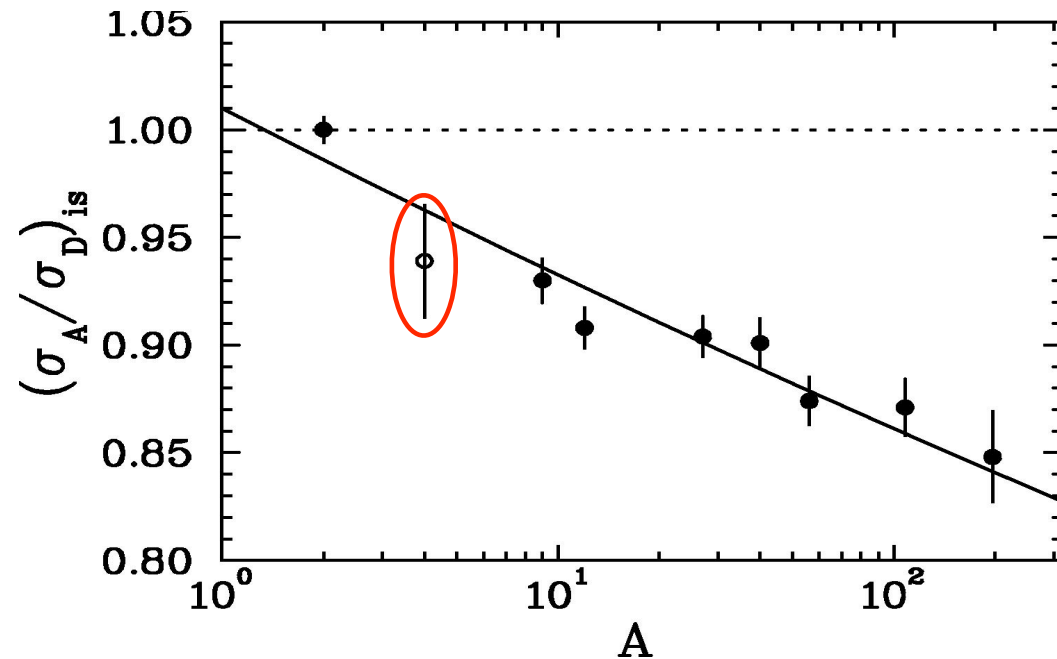
- Universal x-dependence shape
- $Q^2$ -independent
- Magnitude varies with A:
  - Scale with  $A^{-1/3}$
  - Scale with average density  
Density calculated assuming  
a uniform sphere of radius:  
 $R_e (r=3A/4\pi R_e^3)$

J. Gomez et al, PRC49, 4348 (1994)



# Limits of EMC Data

- ${}^4\text{He}$  much lighter than  ${}^{12}\text{C}$ , but has similar average density  
Compare  $A$  vs  $\langle\rho\rangle$
- ${}^3\text{He}$  has low  $A$  and low density; expect smaller EMC effect
- Both nuclei allow for precise, few-body calculations



# JLab Experiment E03-103

JLab E03-103, “EMC effect in few-body nuclei”

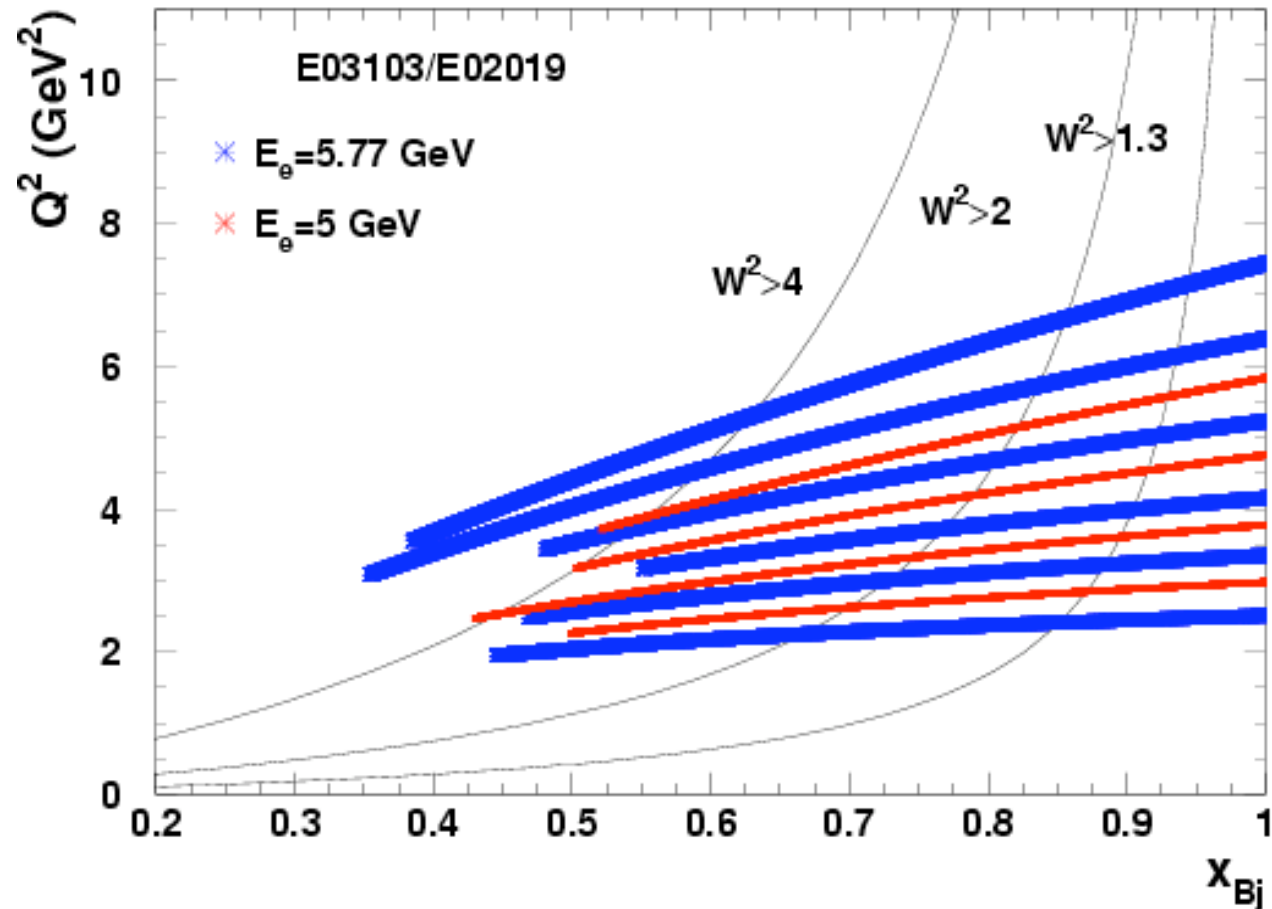
J. Arrington and D. Gaskell: spokespersons

J. Seely, A. Daniel, (N. Fomin): Ph.D. students

$A(e,e')$  at 5.0 and 5.8 GeV in Hall C

10 angles to measure  $Q^2$ -dependence

Targets: H,  $^2\text{H}$ ,  
 $^3\text{He}$ ,  $^4\text{He}$ ,  
 $^9\text{Be}$ ,  $^{12}\text{C}$ ,  
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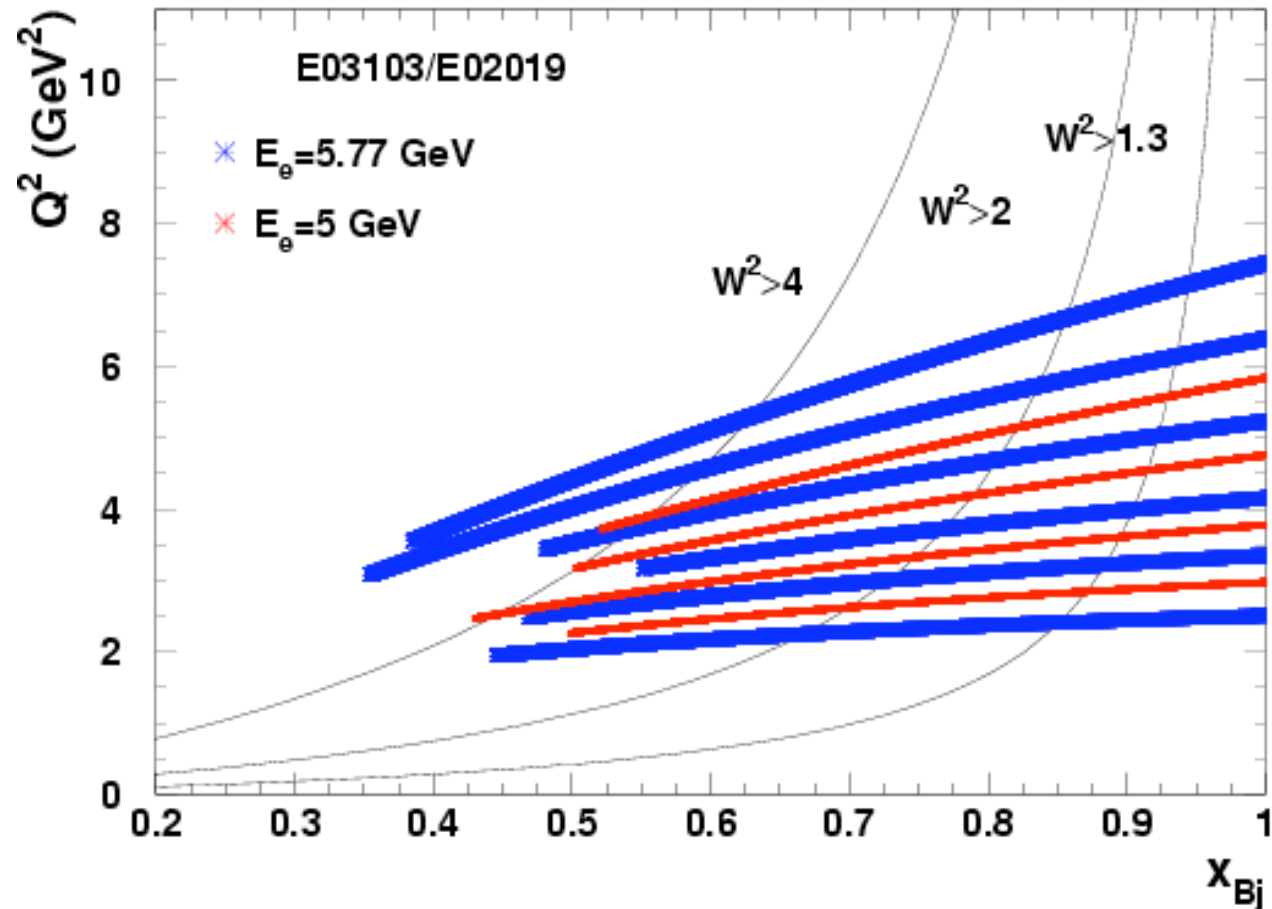
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*Isoscalar correction*





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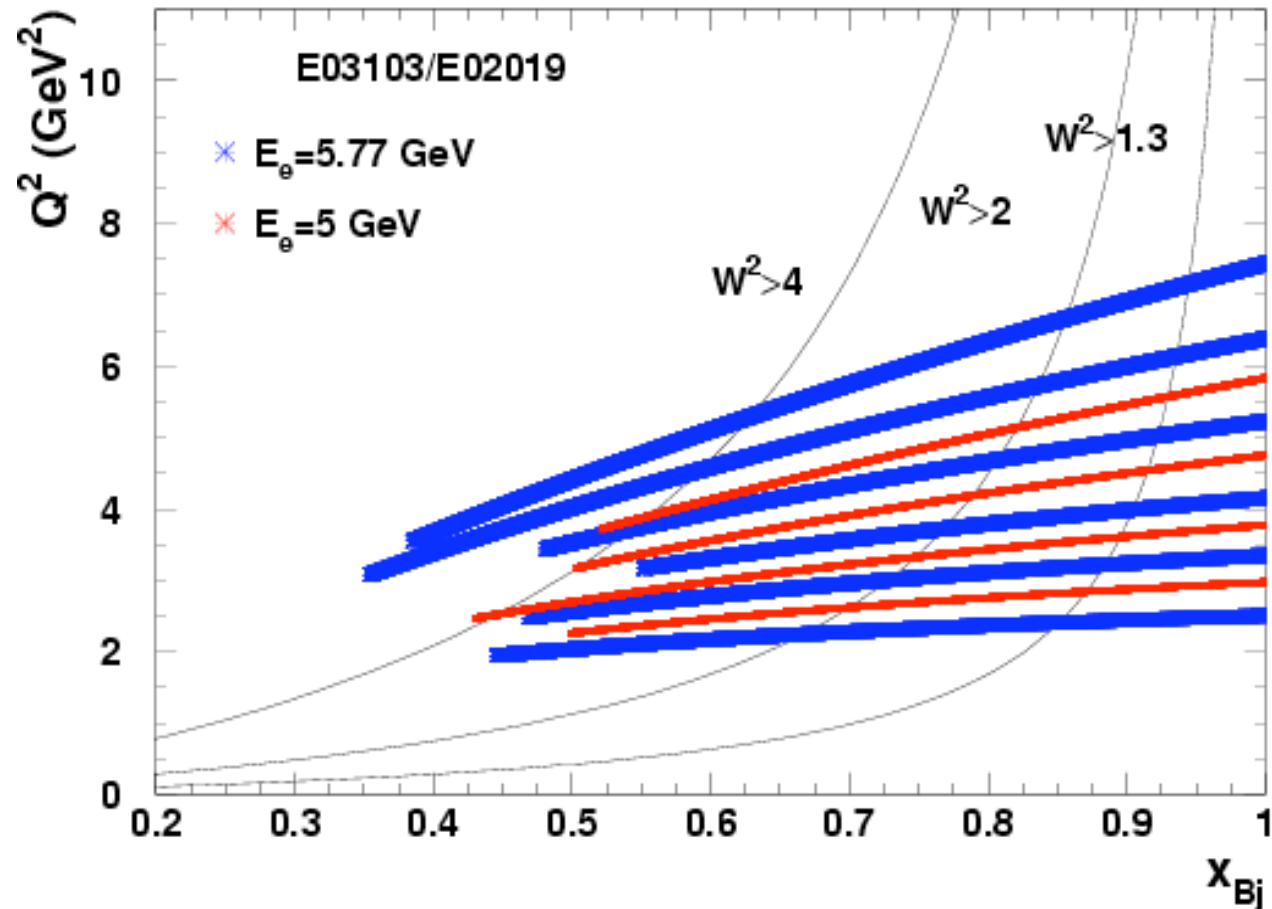
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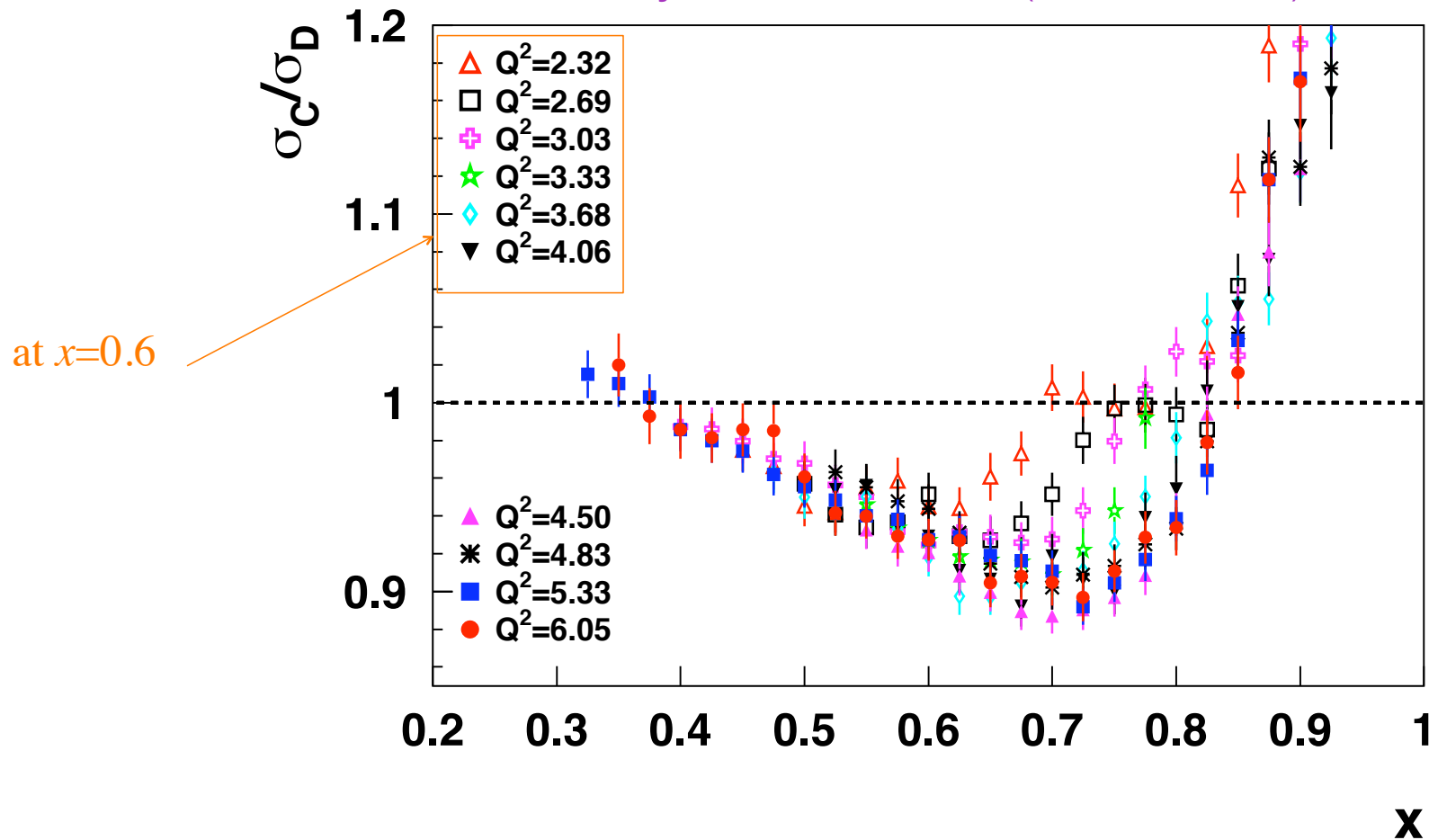
*Isoscalar correction*

*Coulomb correction*



# E03-103: Carbon EMC ratio and $Q^2$ -dependence

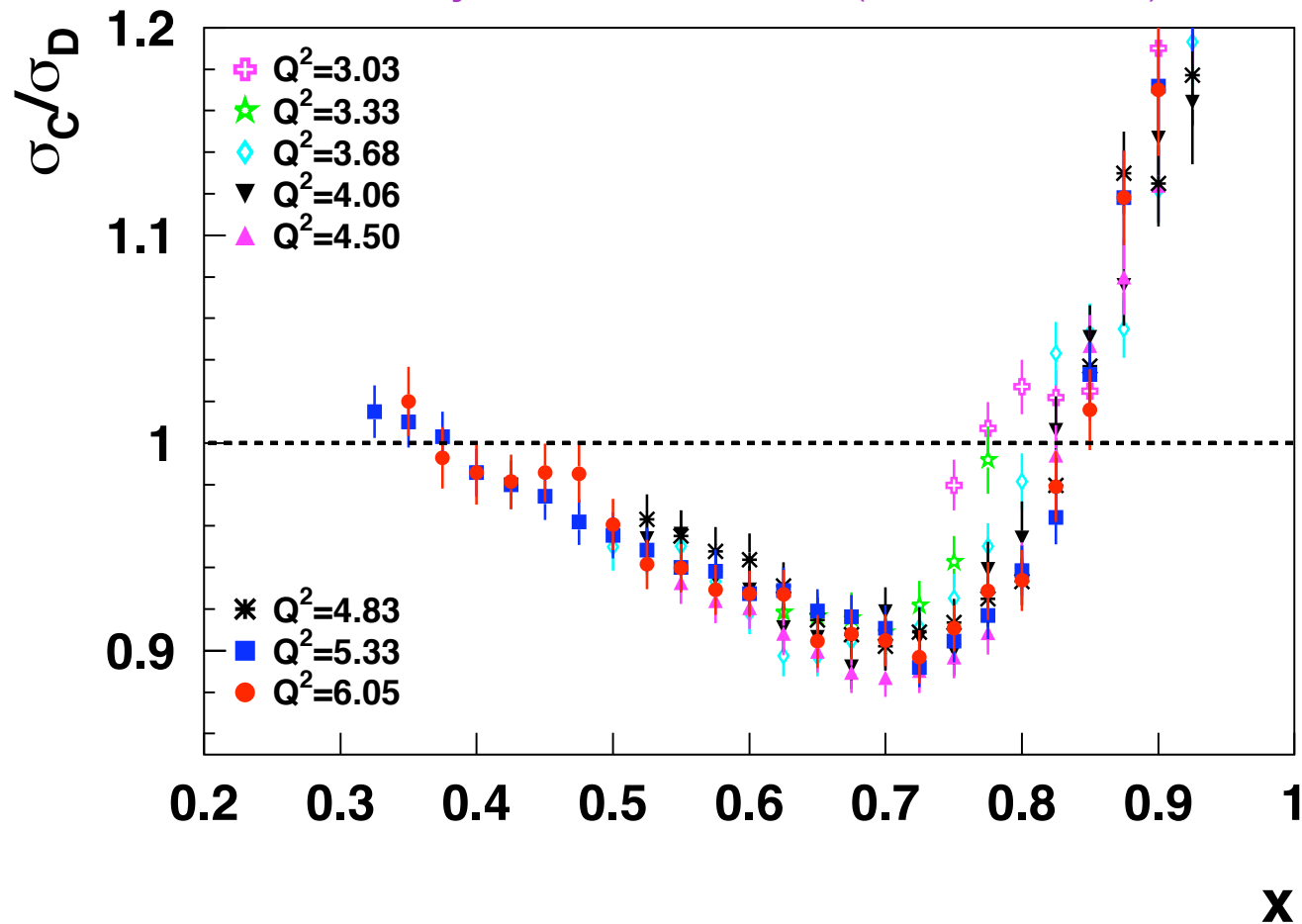
J. Seely et al, arXiv:0904.4448 (submitted to PRL)



Small angle, low  $Q^2 \rightarrow$  clear **scaling violations** for  $x > 0.6-0.7$

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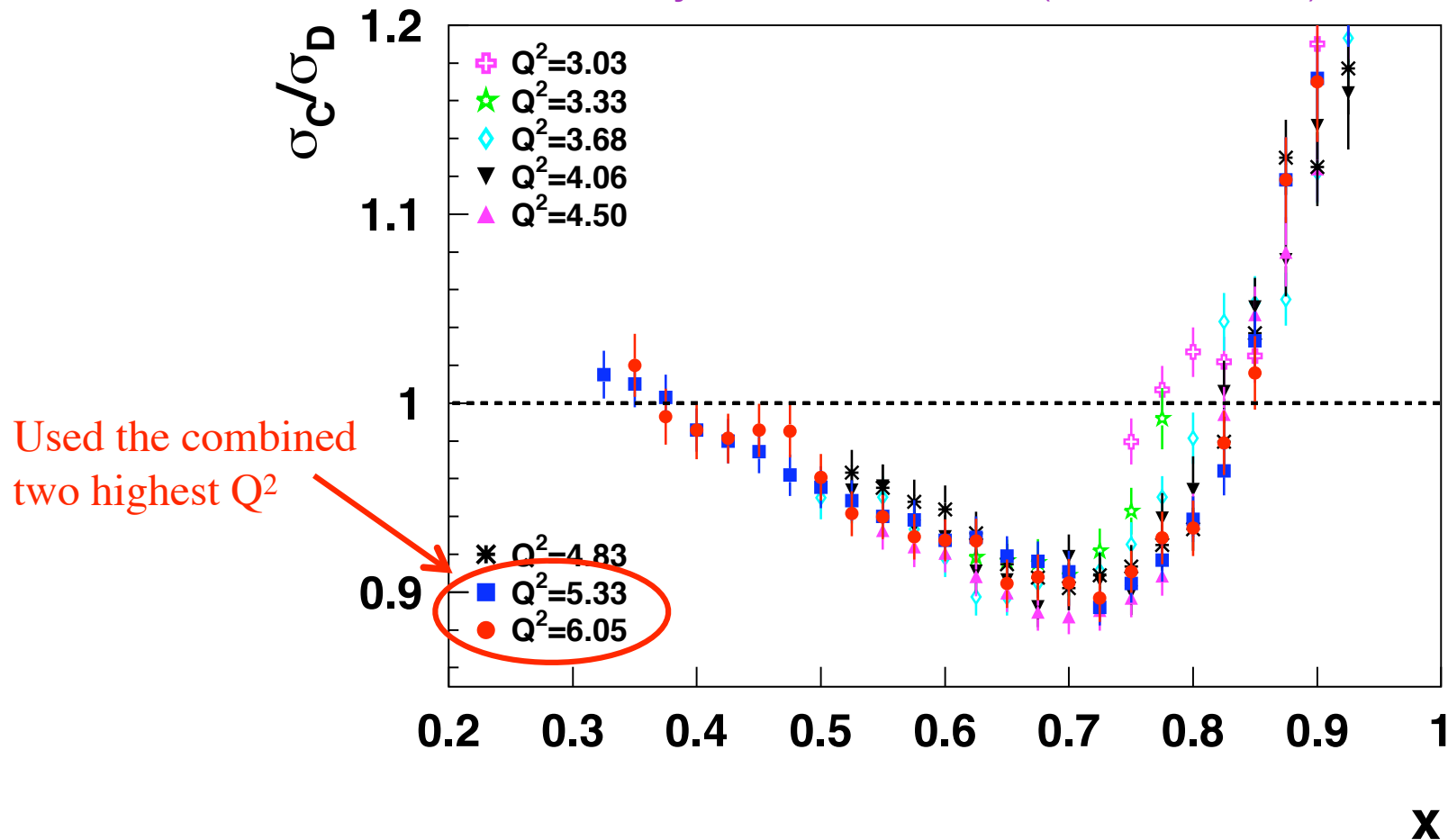
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At larger angles  $\rightarrow$  indication of **scaling** to very large  $x$

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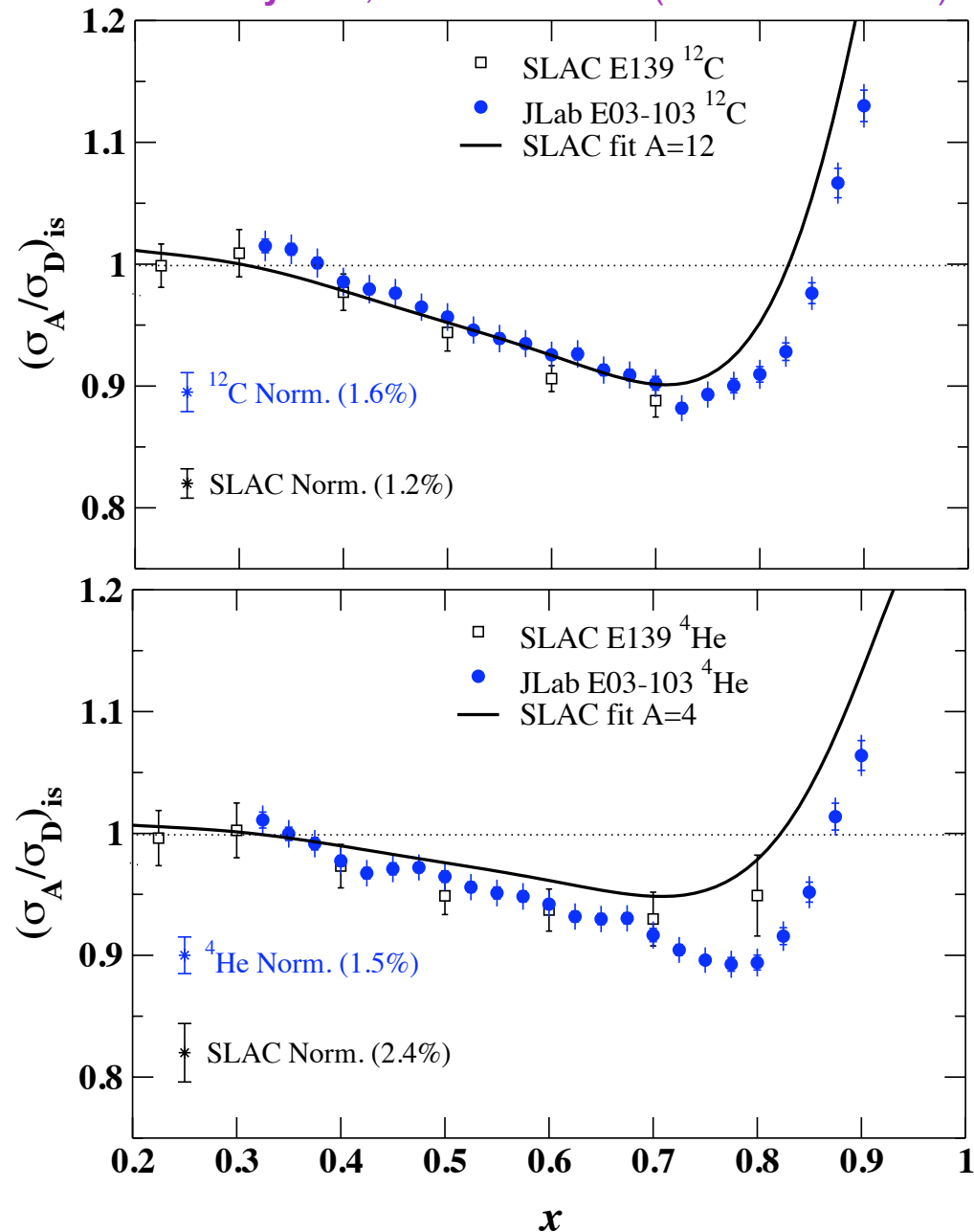
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# E03-103: $^{12}\text{C}$ and $^4\text{He}$ EMC ratios

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JLab results consistent with  
SLAC E139

→ Improved statistics and  
systematic errors



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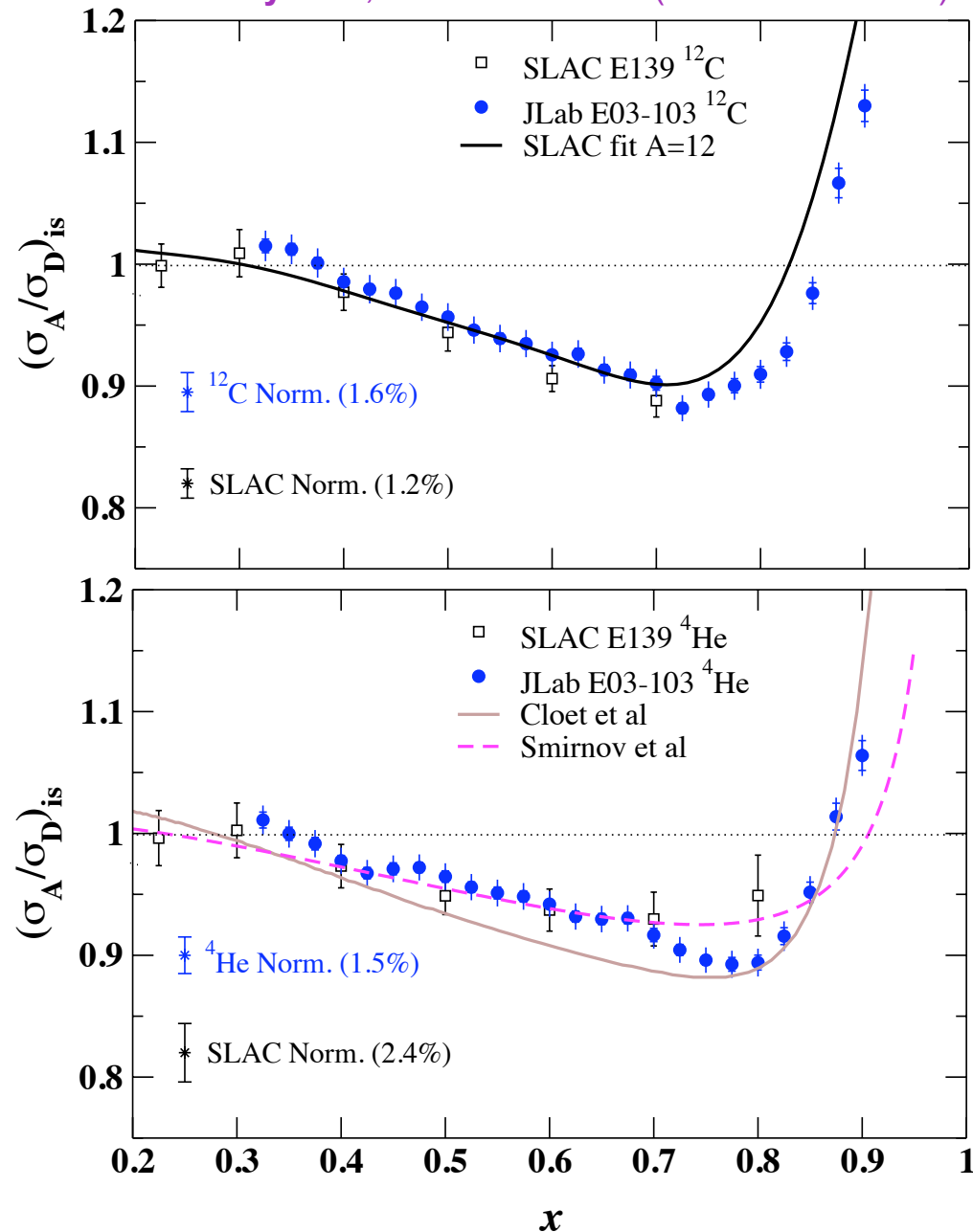
J. Seely et al, arXiv:0904.4448 (submitted to PRL)

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→ Improved statistics and  
systematic errors

Models shown do a reasonable job  
describing the data.

But very few real few-body calculations  
(most neglect structure, scale NM)



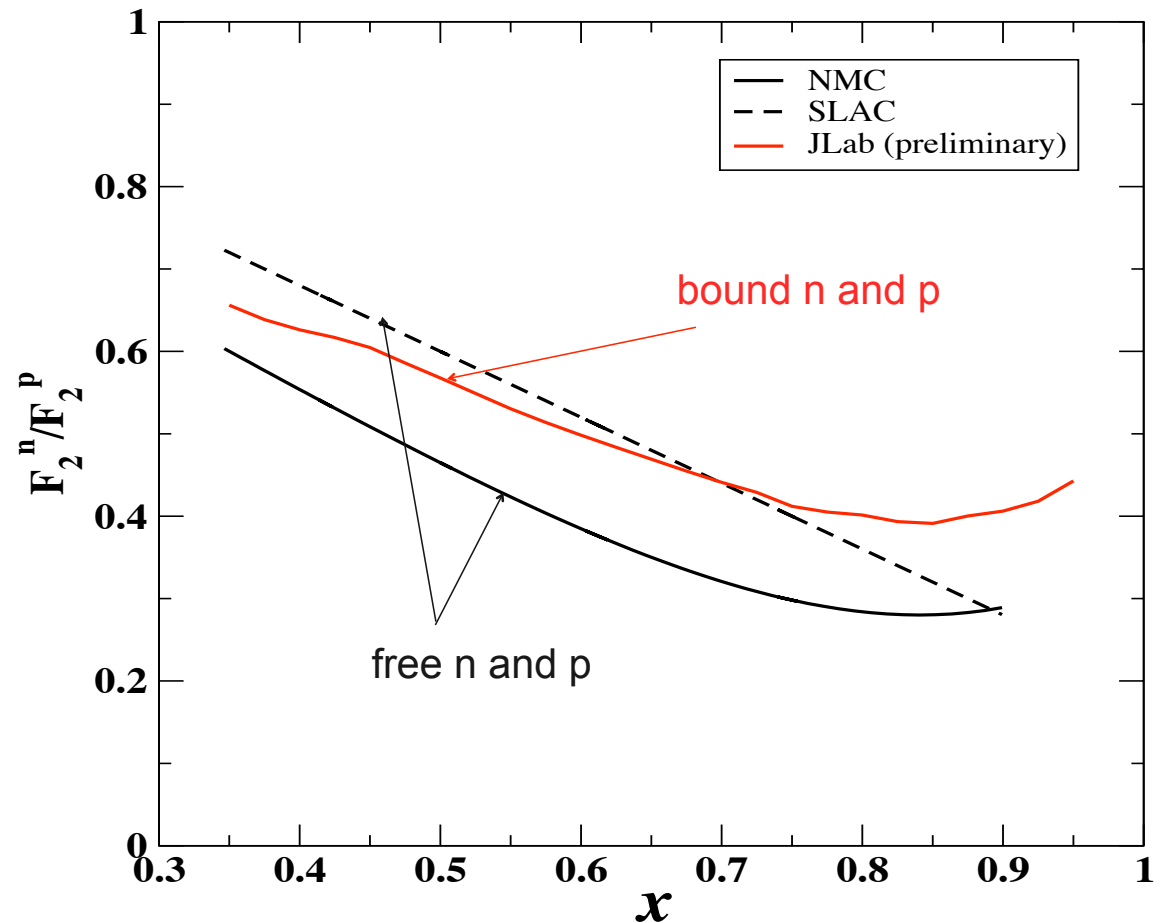
# Isoscalar correction

$$Zp + Nn \rightarrow A/2(p+n)$$

**Smeared n/p** at the kinematics of the experiment

vs.

**high  $Q^2$  free n/p**

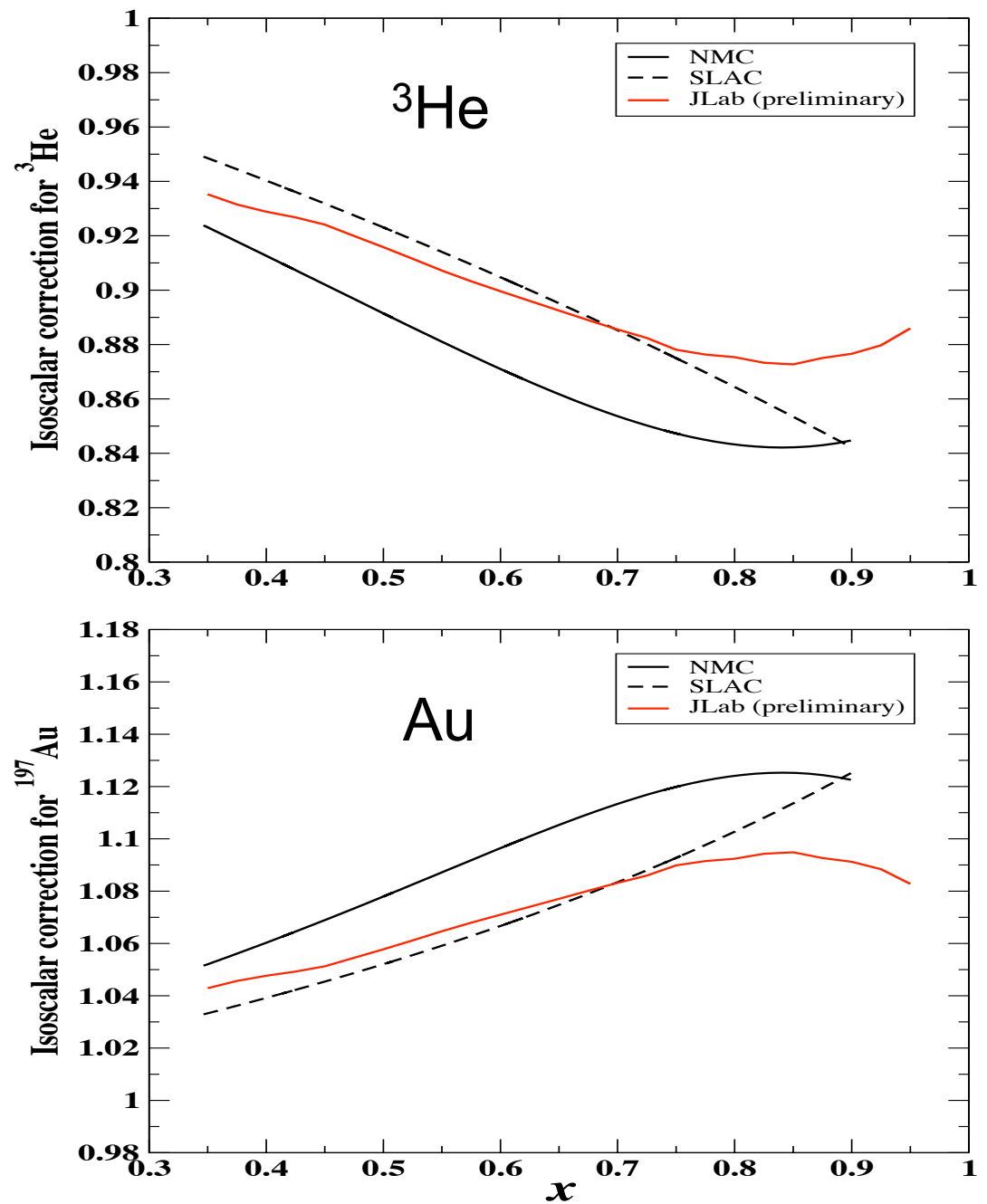


J. Arrington, F. Coester, R.J. Holt, T.-S.H. Lee, J.Phys.G36, 025005 (2009)

# Isoscalar correction

$$R_{EMC} = \frac{\sigma_2^A / A}{\sigma_2^D / 2} \cdot \frac{(p+n)/2}{(Zp + Nn)/A}$$

Isoscalar correction

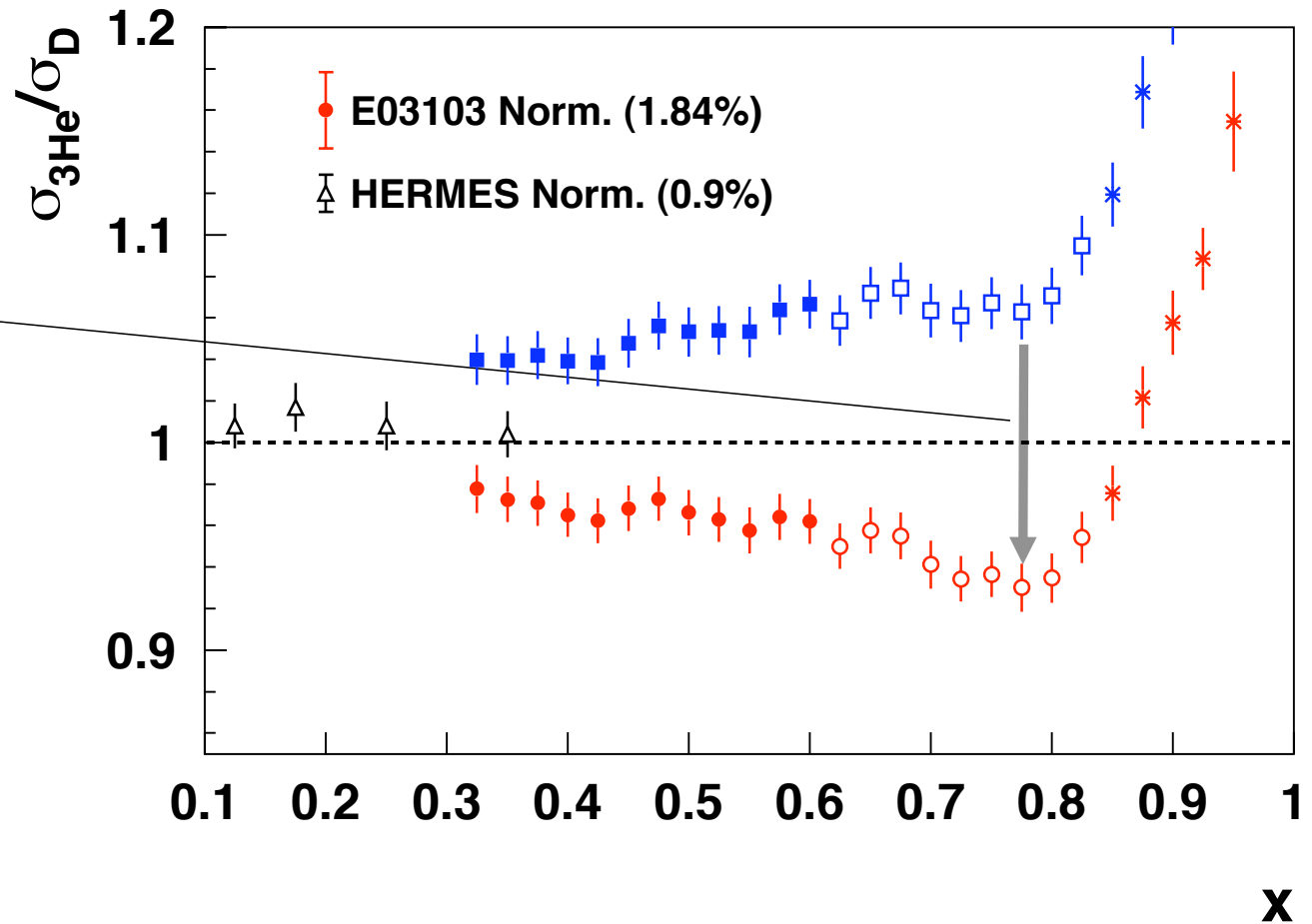




# E03-103: $^3\text{He}$ EMC ratio

J. Seely et al, arXiv:0904.4448 (submitted to PRL)

Large proton excess  
correction



Isoscalar correction  
done using ratio of  
bound neutron to bound  
proton at E03-103  
kinematics

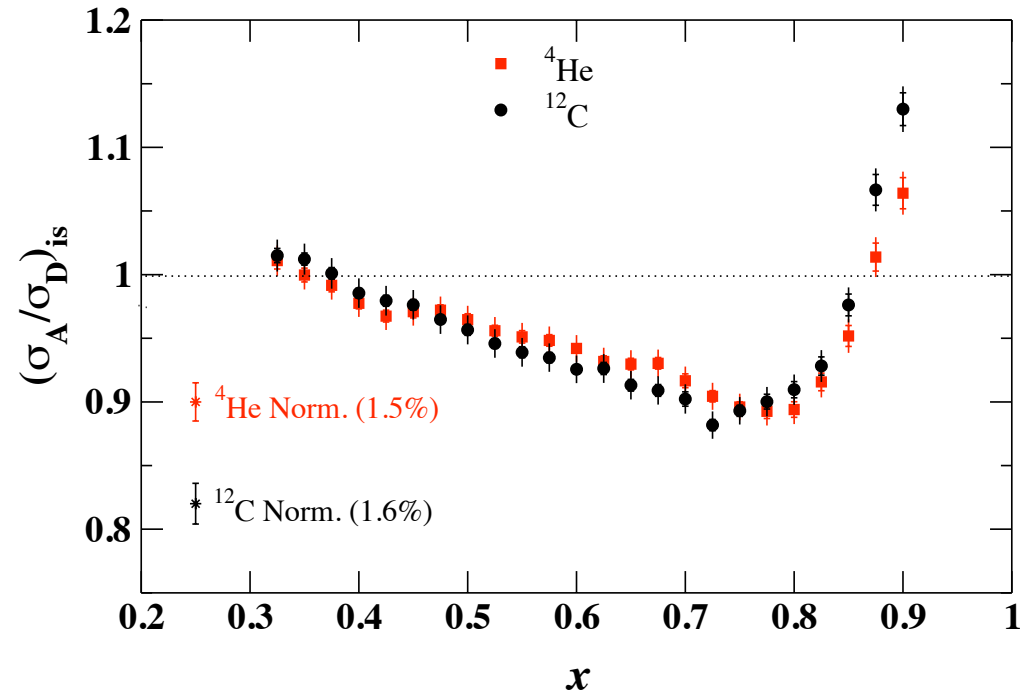
# *A or $\rho$ -dependence ?*

Magnitude of the EMC effect for C and  $^4\text{He}$  very similar, and

$$\rho(^4\text{He}) \sim \rho(^{12}\text{C})$$

$^4\text{He}$  suggests  $\rho$ -dependent

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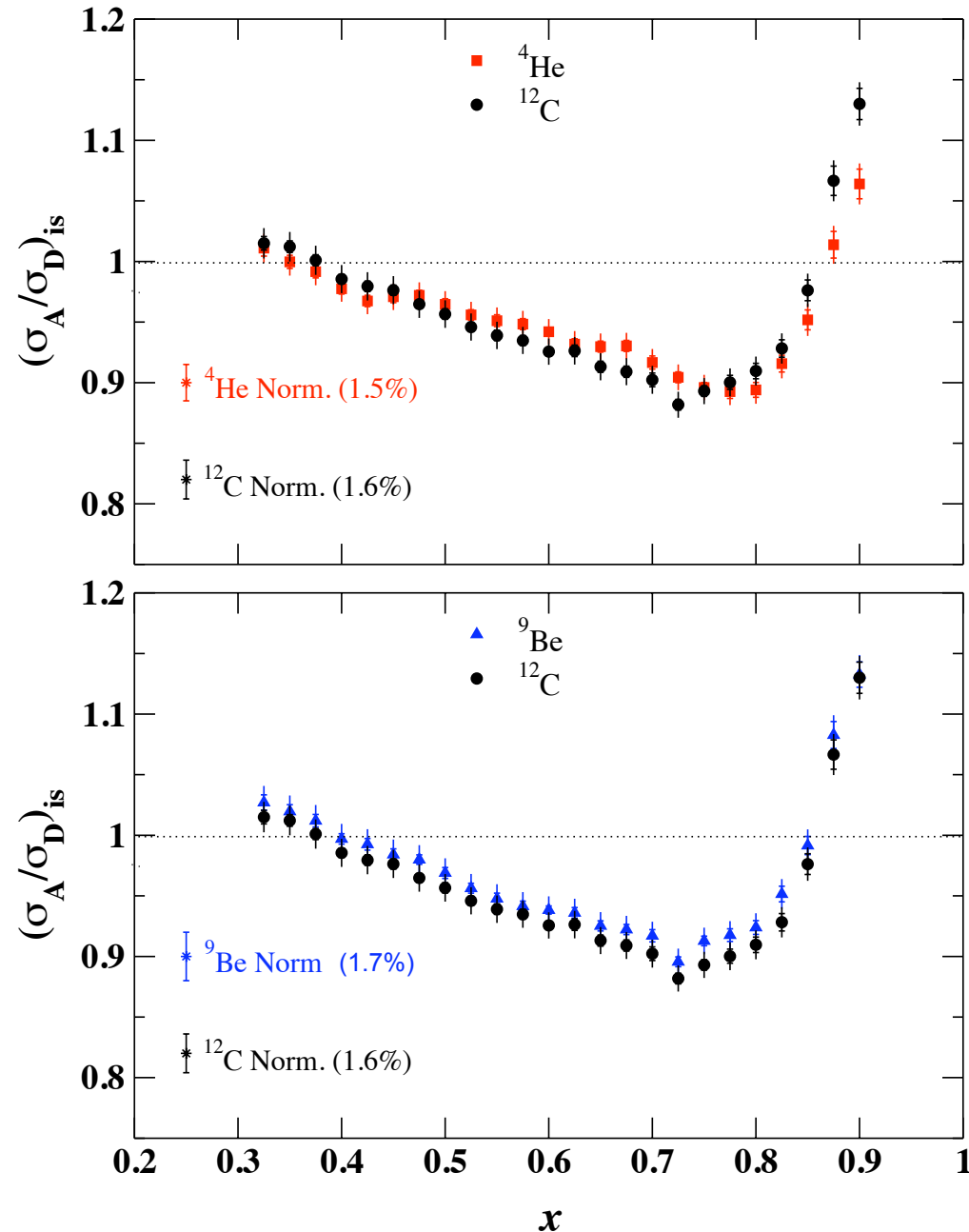
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Magnitude of the EMC effect for C and  $^9\text{Be}$  very similar, but

$$\rho(^9\text{Be}) \ll \rho(^{12}\text{C})$$

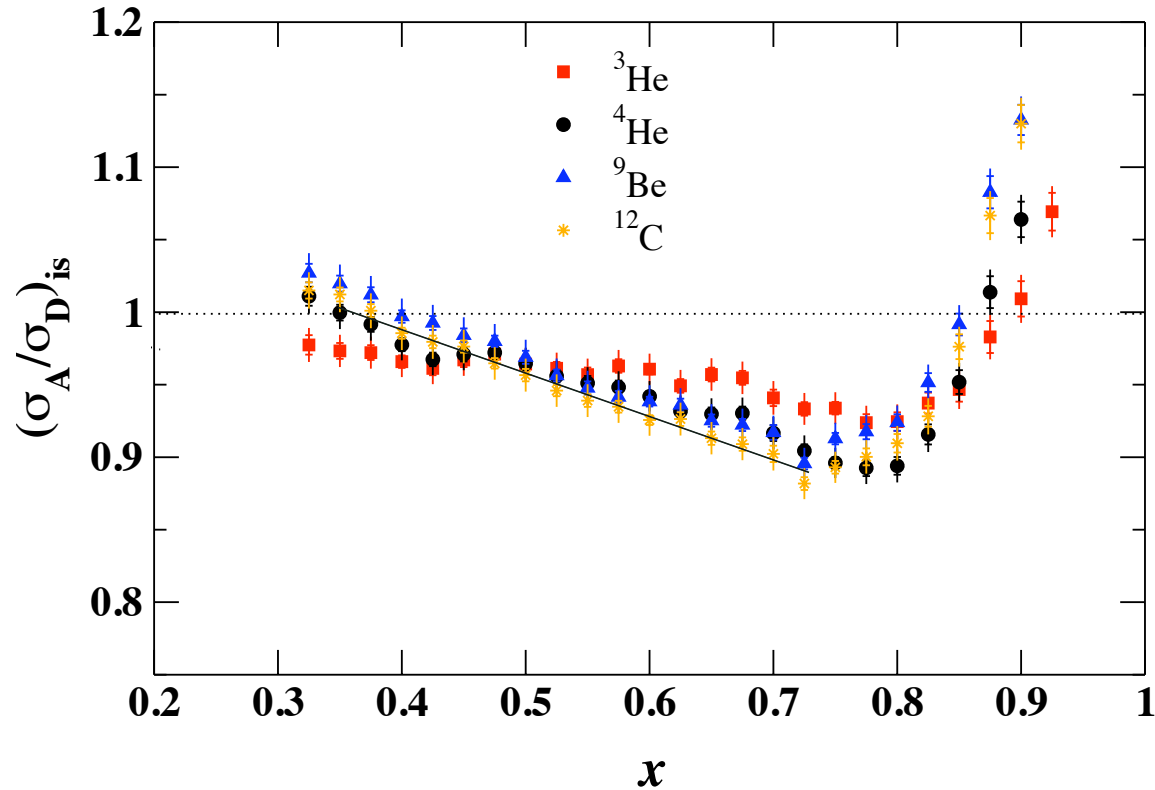
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J. Seely et al, arXiv:0904.4448 (submitted to PRL)



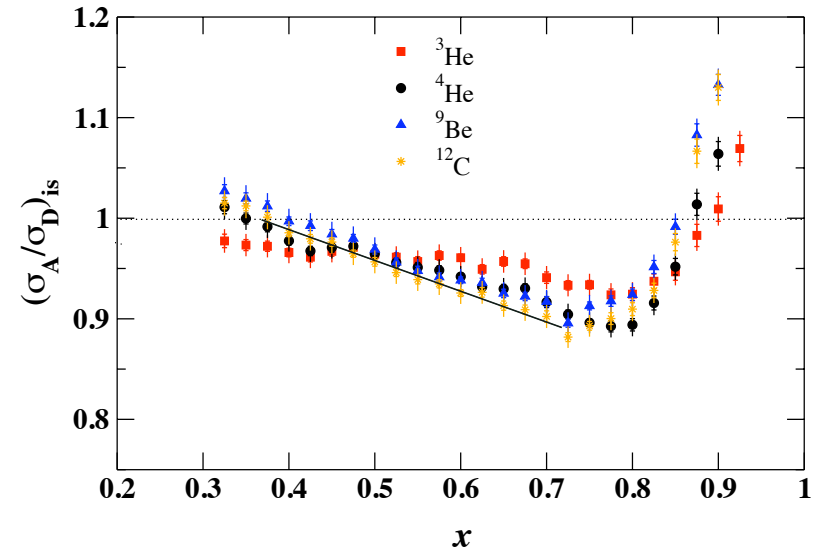
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Fit of the EMC ratio for  $0.35 < x < 0.7$  and look at A- and density dependence of the slope

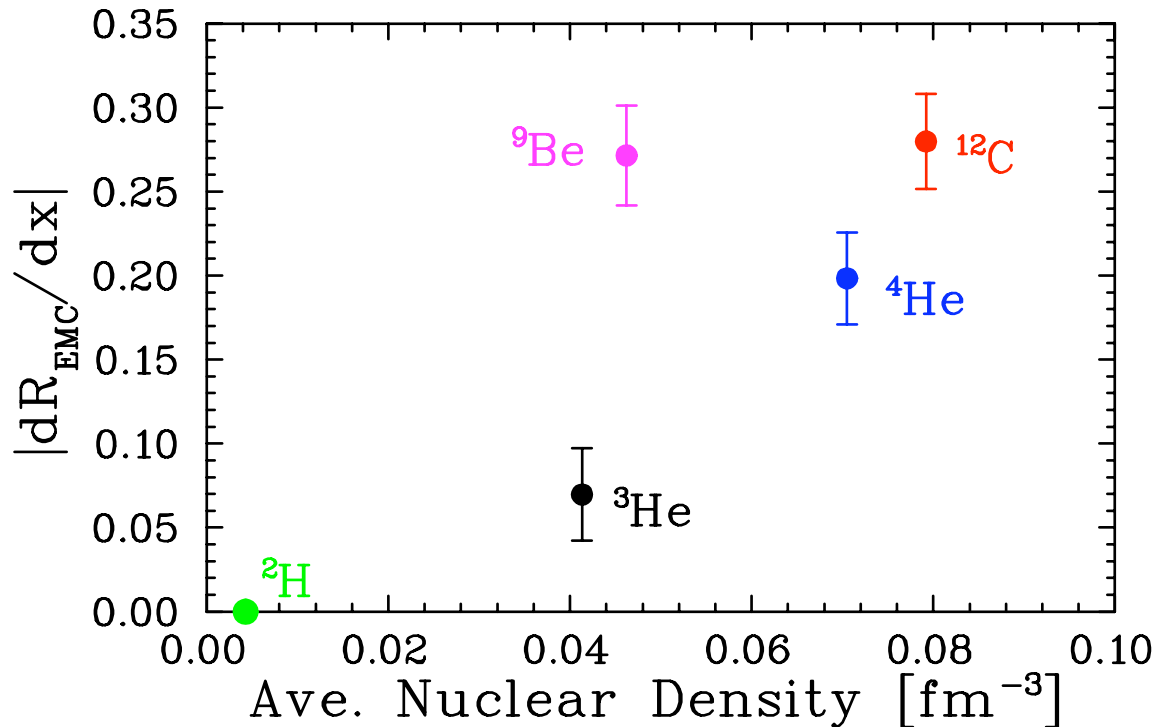


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J. Seely et al, arXiv:0904.4448 (submitted to PRL)



Density determined from ab initio few-body calculation

S.C. Pieper and R.B. Wiringa,  
Ann. Rev. Nucl. Part. Sci 51, 53 (2001)

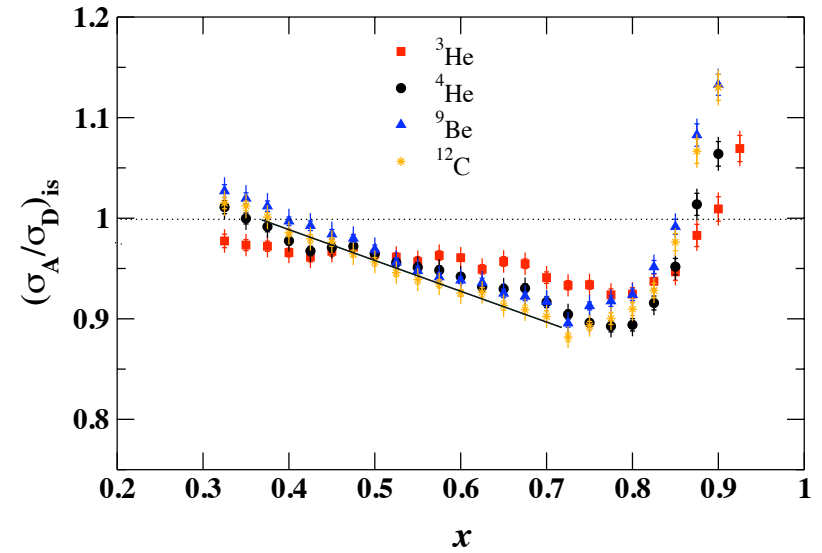
To remove struck nucleon's contribution, scale density by  $(A-1)/A$

Data show smooth behavior as density increases...

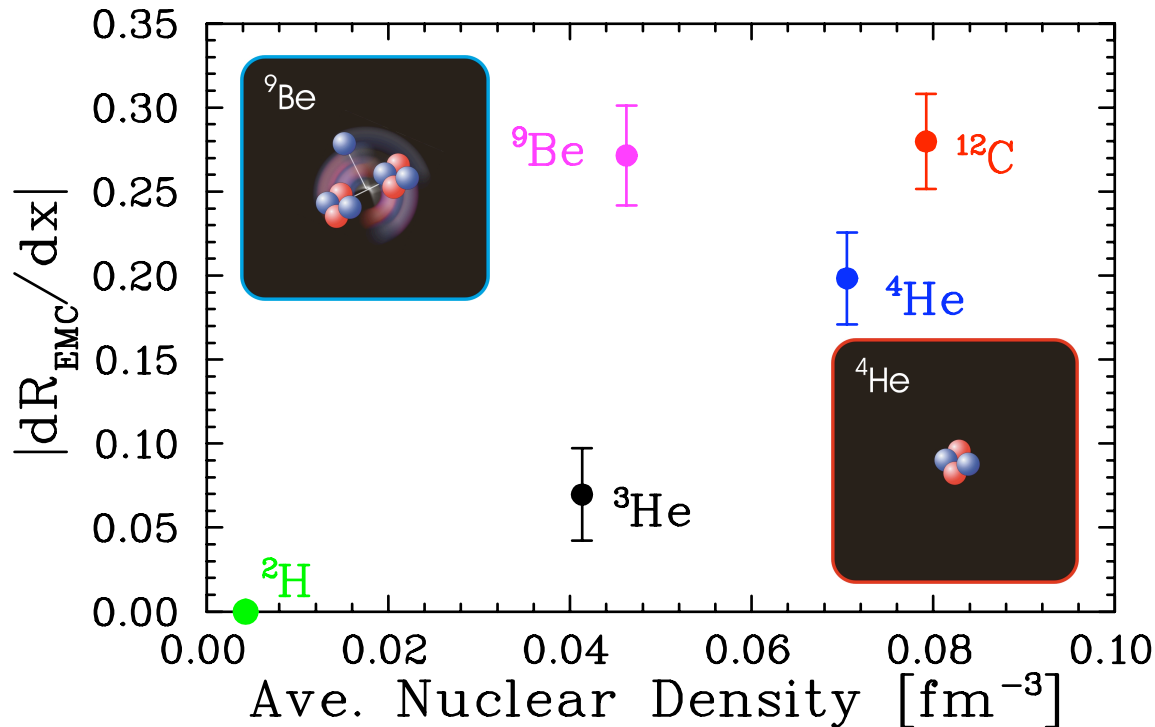
**except for  $^9\text{Be}$**

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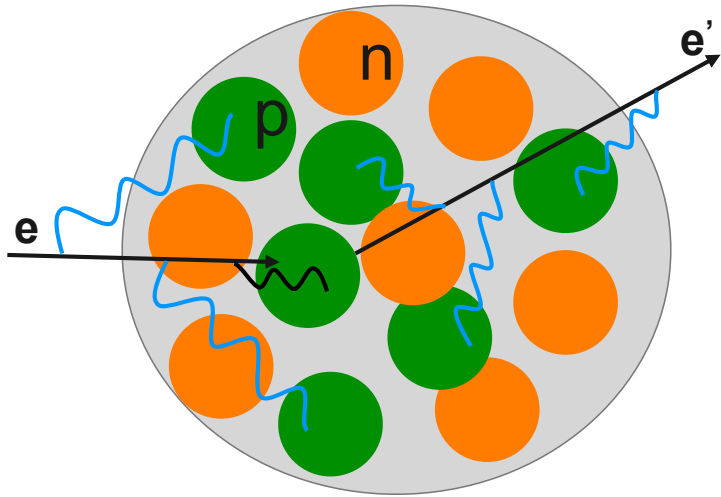
J. Seely et al, arXiv:0904.4448 (submitted to PRL)



$^9\text{Be}$  has low average density, but large component of structure is  $2\alpha+n$  most nucleons in tight,  $\alpha$ -like configurations

*Heavy nuclei  
and  
Coulomb distortion*

# Coulomb distortion



Exchange of one or more (soft) photons with the nucleus, in addition to the one hard photon exchanged with a nucleon

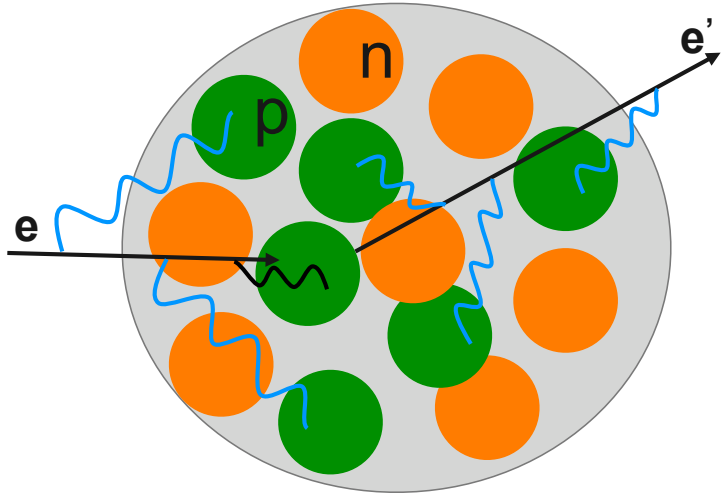
**Incident (scattered) electrons are accelerated (decelerated) in the Coulomb well of the nucleus.**

Opposite effect with positrons

$$\sigma_{tot}^{PWBA} = \sigma_{Mott} S_{tot}^{PWBA}(|\vec{q}|, \omega, \theta)$$



# Coulomb distortion



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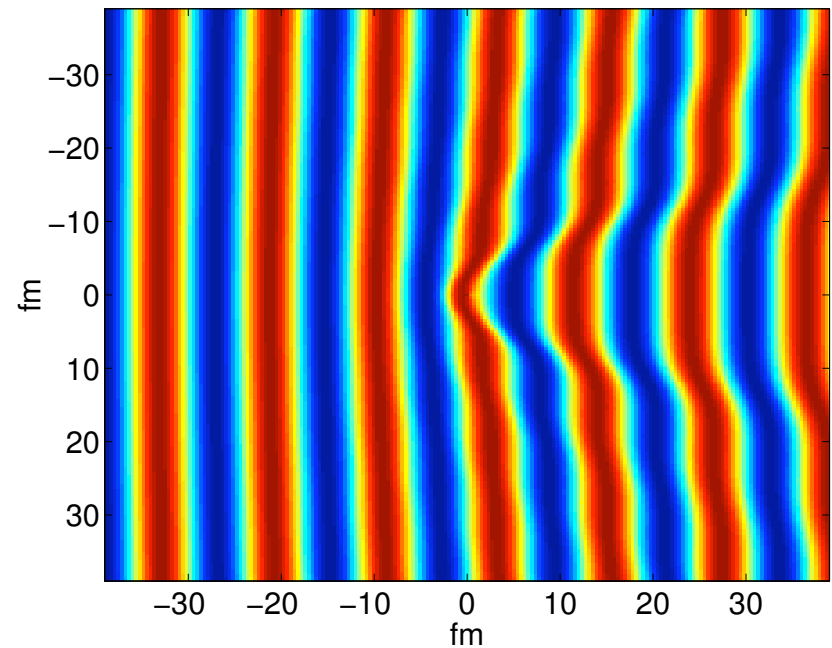
Fig. from A. Aste at Mini-Workshop on Coulomb Distortion, JLab May 2005

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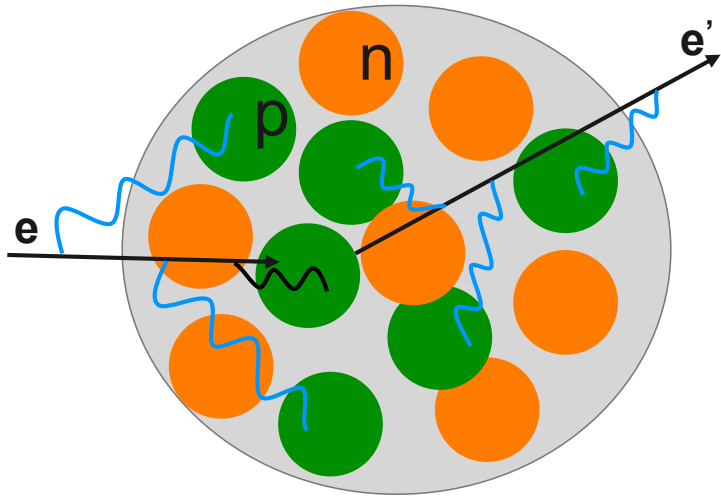


$$\sigma_{tot}^{DWBA}$$

- Focusing of the electron wave function
- Change of the electron momentum



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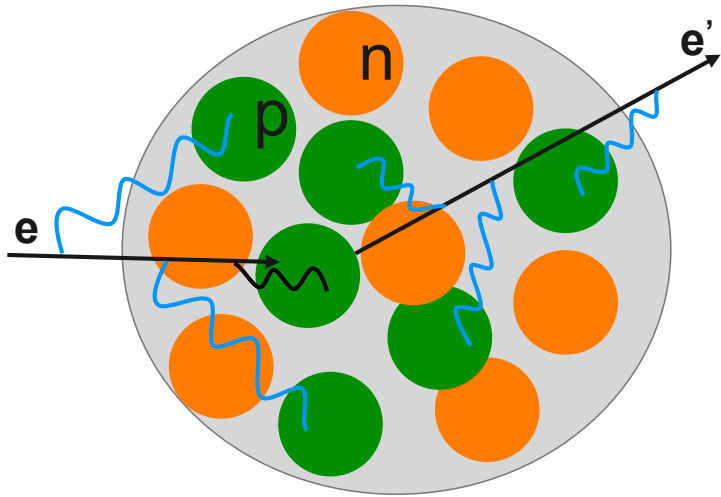
Opposite effect with positrons

## Effective Momentum Approximation (EMA)

$$\left. \begin{array}{l} E \rightarrow E + \bar{V} \\ E_p \rightarrow E_p + \bar{V} \end{array} \right\} Q_{eff}^2 = 4(E + \bar{V})(E_p + \bar{V}) \sin^2\left(\frac{\theta}{2}\right)$$

Aste and Trautmann, Eur. Phys. J. A26, 167-178(2005)

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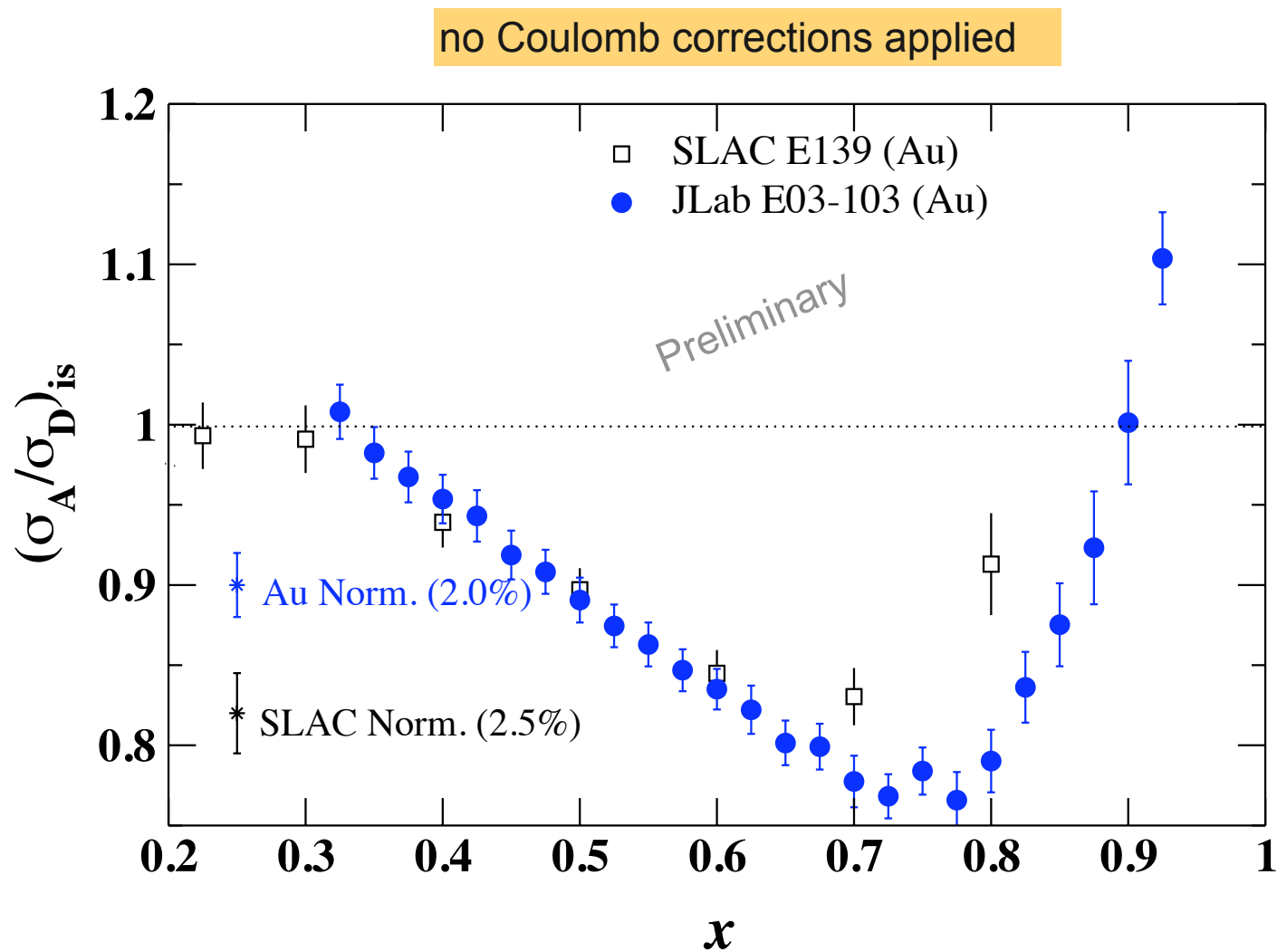
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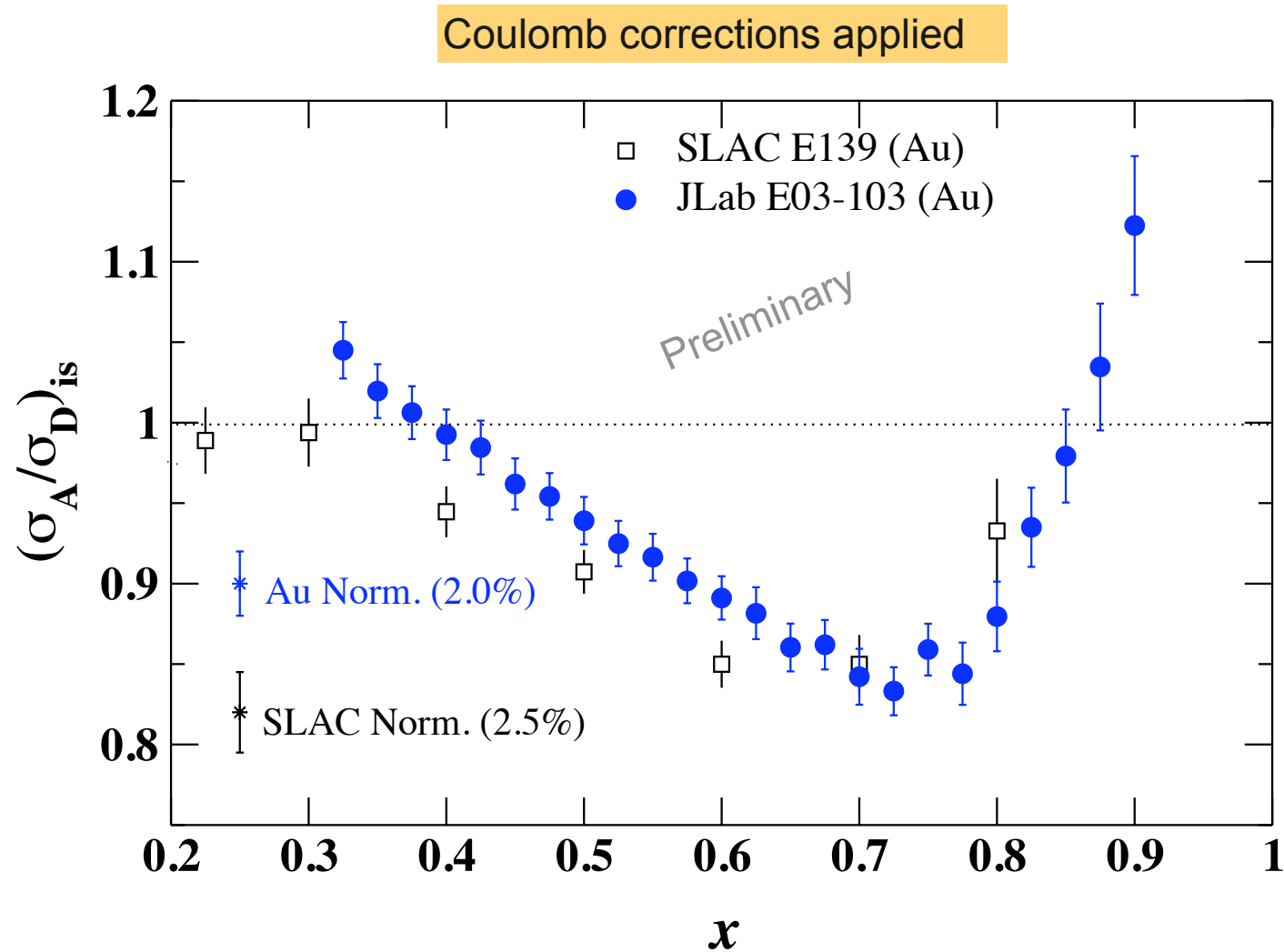
One-parameter model depending only on the effective potential seen by the electron on average.

**Coulomb potential established in Quasi-elastic scattering regime !**

# Coulomb distortion effect on E03-103

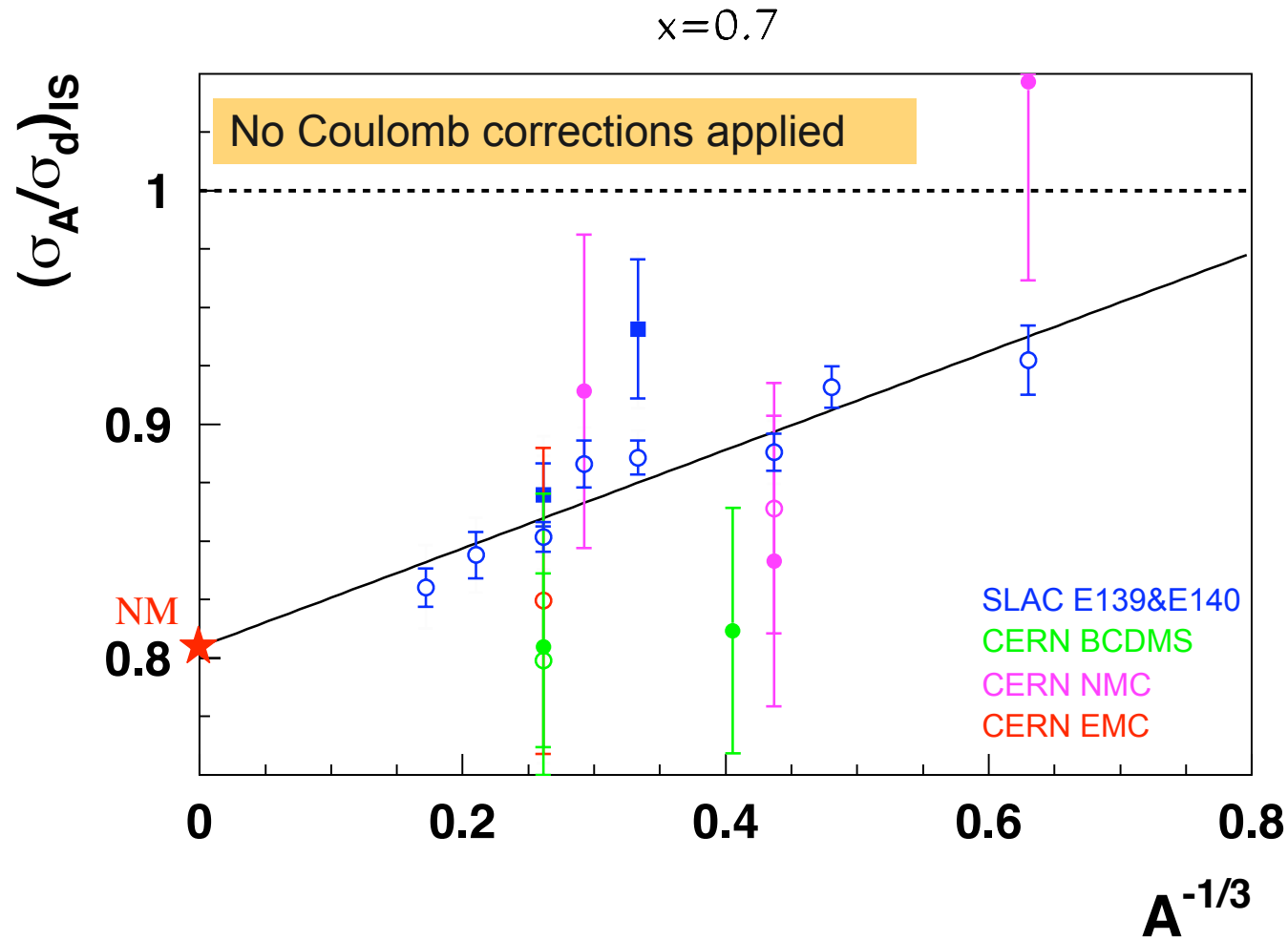


# Coulomb distortion effect on E03-103



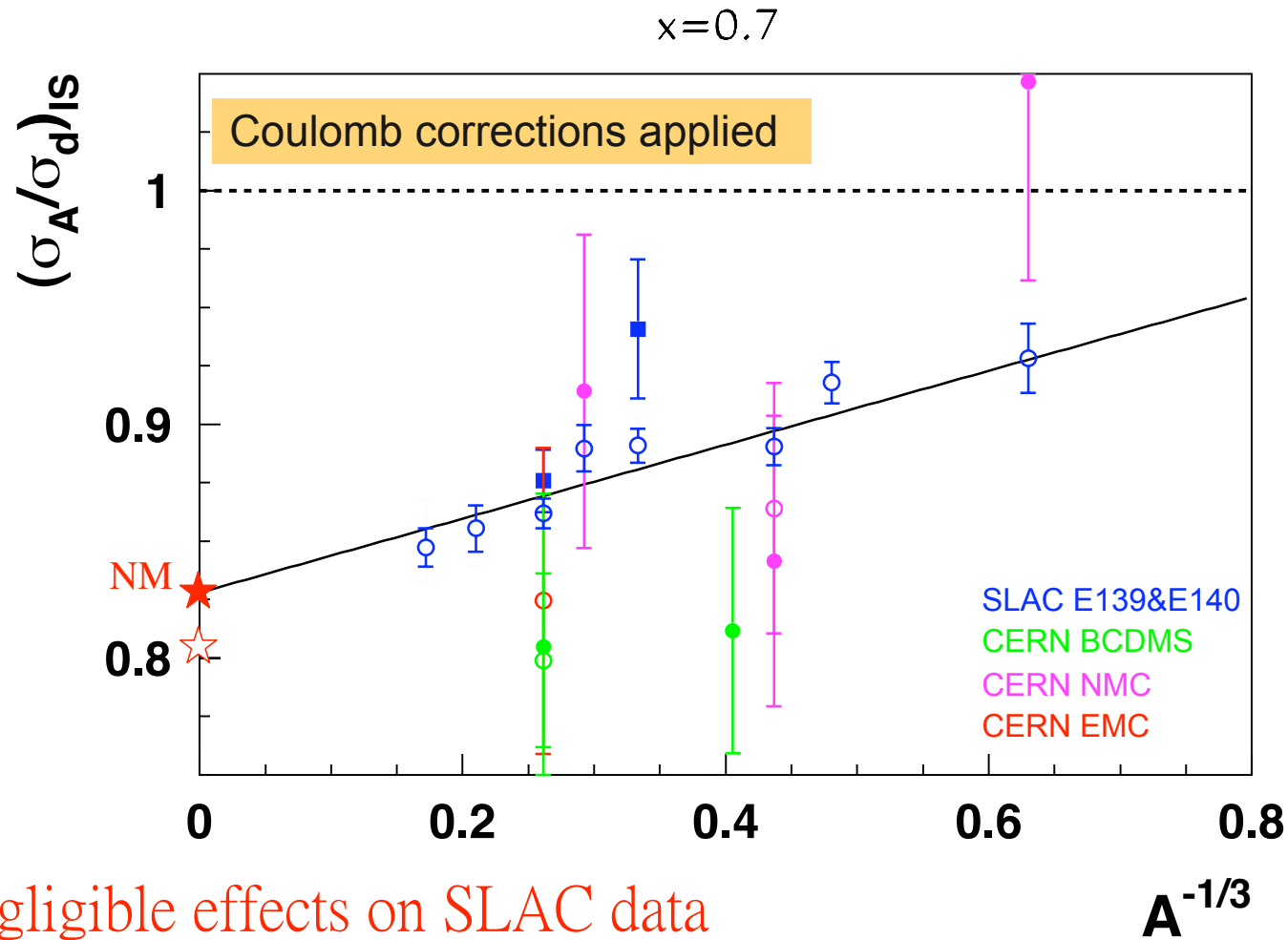
# Extrapolation to nuclear matter

Exact calculations of the EMC effect exist for light nuclei and for nuclear matter.



# Extrapolation to nuclear matter

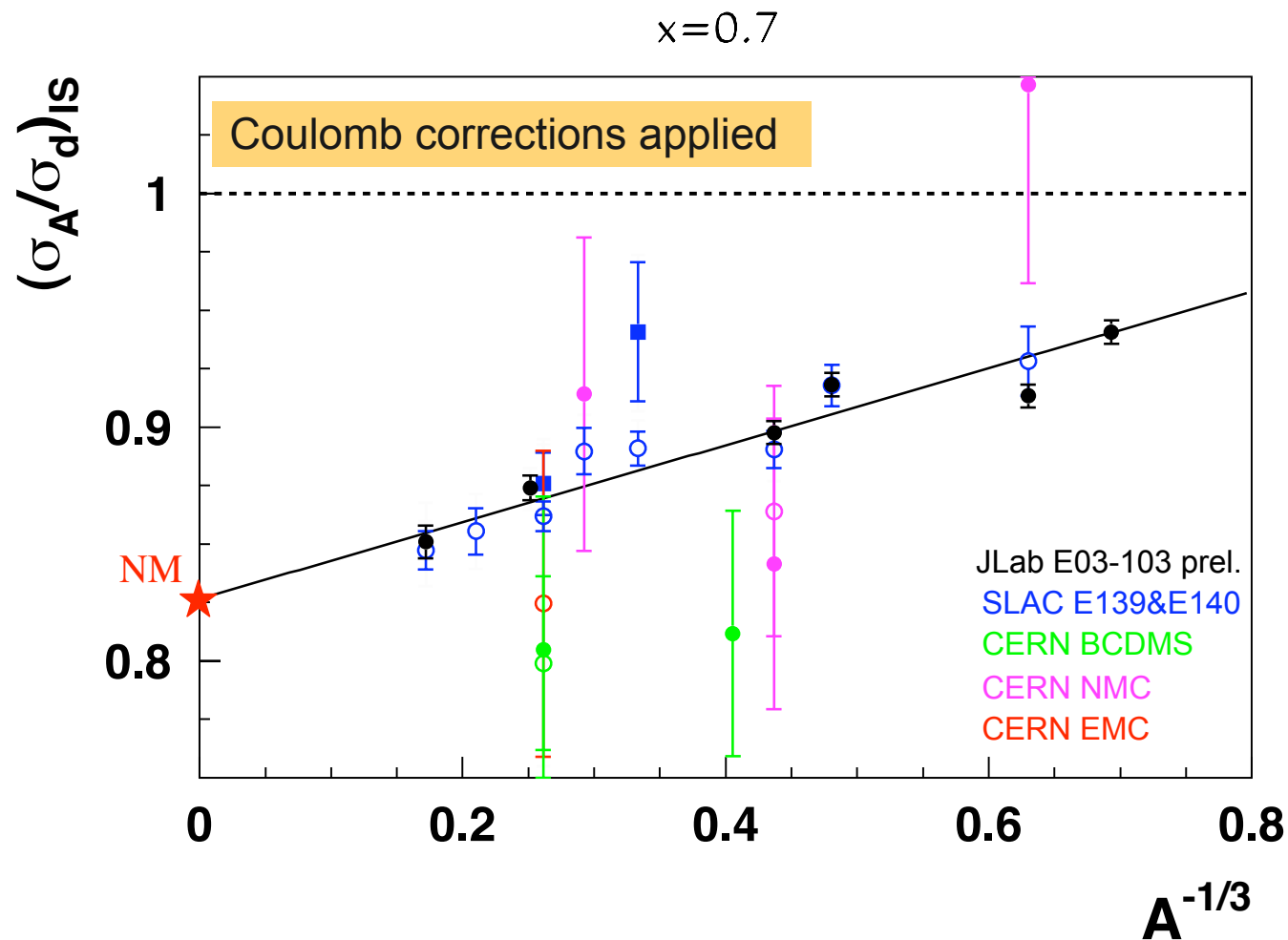
Exact calculations of the EMC effect exist for light nuclei and for nuclear matter.



Non-negligible effects on SLAC data

# Extrapolation to nuclear matter

Exact calculations of the EMC effect exist for light nuclei and for nuclear matter.





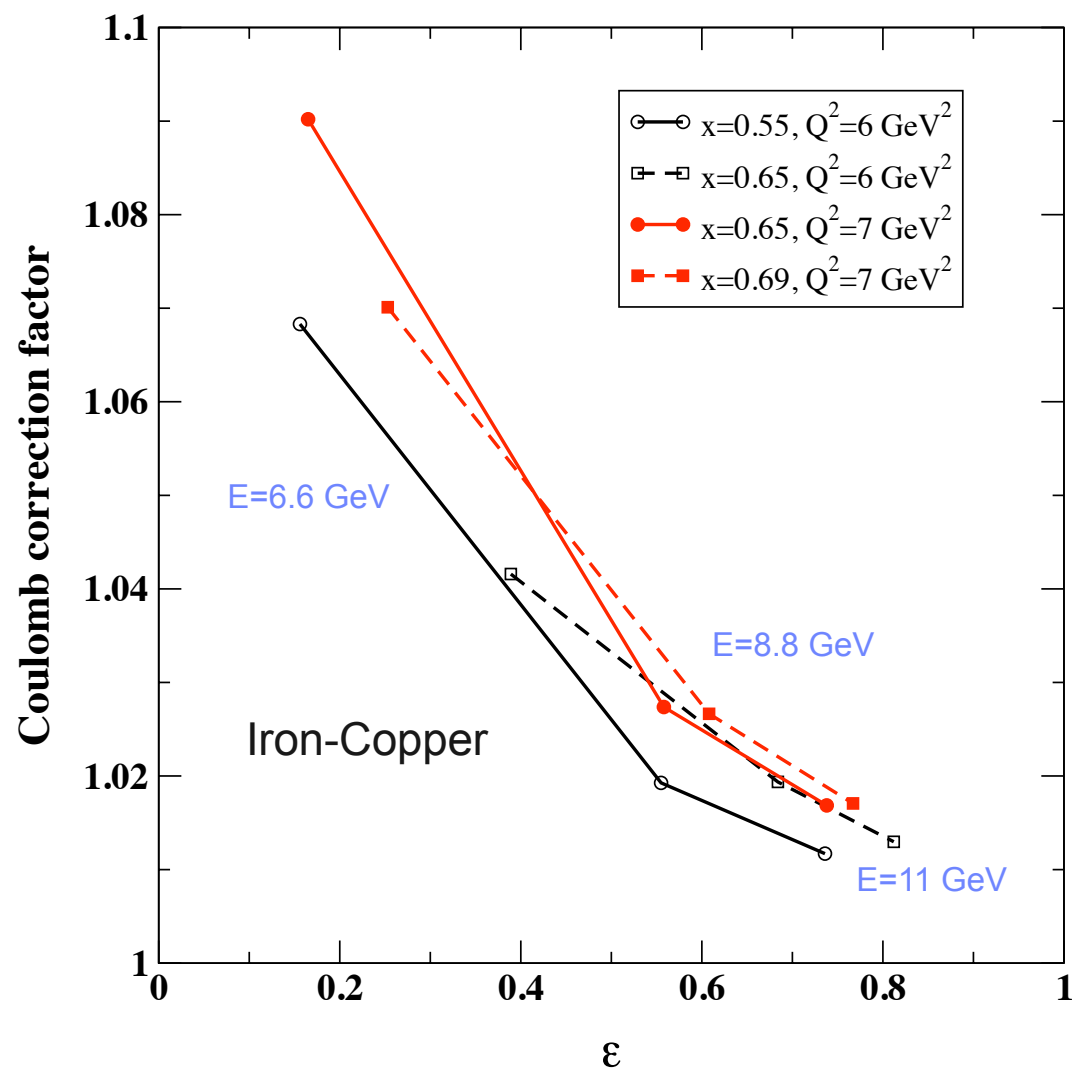
# Coulomb distortion: $\epsilon$ -dependence

The  $\epsilon$ -dependence of the Coulomb distortion has effect on the extraction of  $R$  in nuclei.

$$\epsilon = \frac{1}{1 + 2 \left[ 1 + \frac{\nu^2}{Q^2} \tan^2\left(\frac{\theta}{2}\right) \right]}$$

$$\theta = 0^\circ \rightarrow \epsilon = 1$$

$$\theta = 180^\circ \rightarrow \epsilon = 0$$



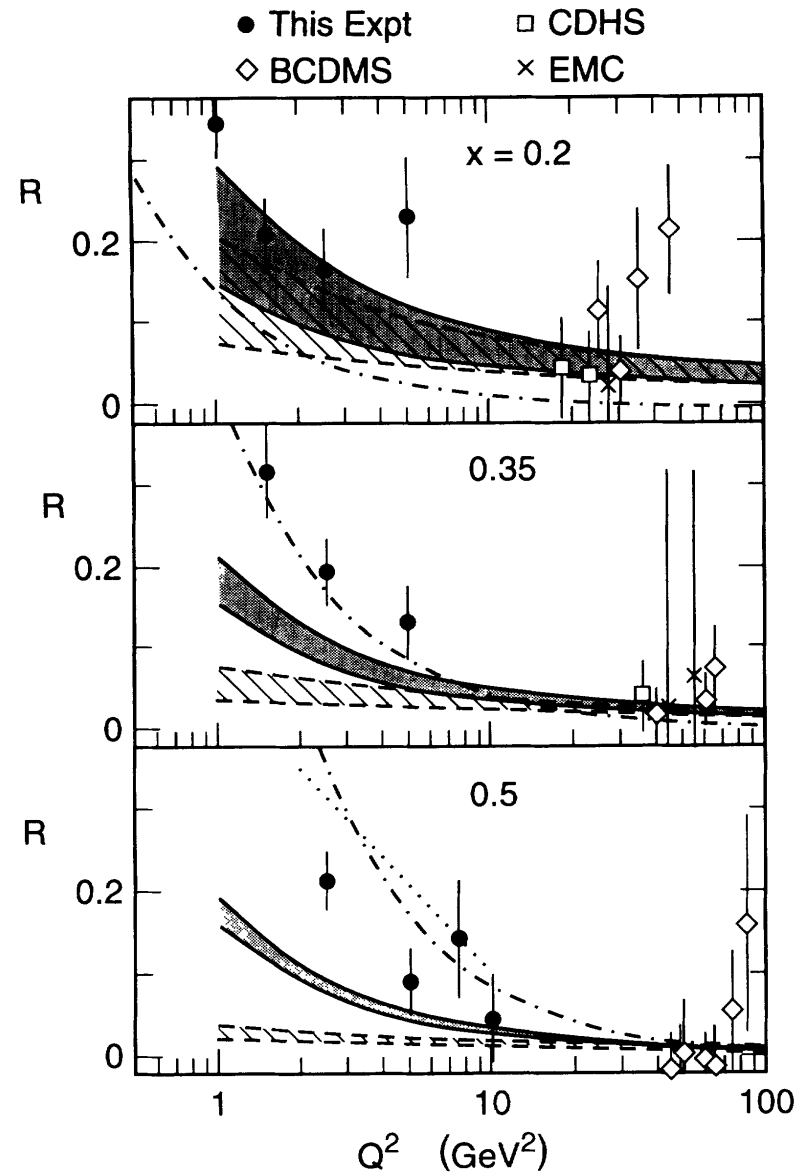
# $R(x, Q^2)$

$$\frac{d\sigma}{d\Omega dE'} = \Gamma \left[ \sigma_T(x, Q^2) + \varepsilon \sigma_L(x, Q^2) \right]$$

$$R(x, Q^2) = \frac{\sigma_L(x, Q^2)}{\sigma_T(x, Q^2)}$$

In a model with:

- a) **spin-1/2 partons**: R should be **small** and **decreasing rapidly with  $Q^2$**
- b) **spin-0 partons**: R should be **large** and **increasing with  $Q^2$**



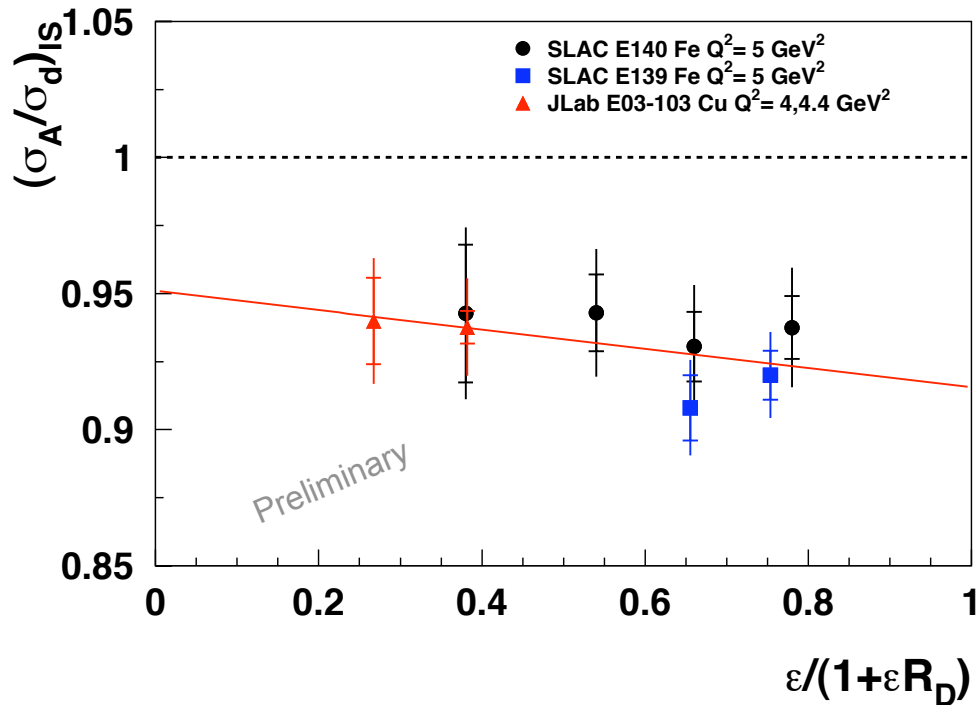
Dasu et al., PRD49, 5641(1994)

# Access to nuclear dependence of $R$

## Iron-Copper

No Coulomb corrections applied

$x=0.5$



slopes  $\Rightarrow R_A - R_D$

$$R_A - R_D = 0 \Rightarrow$$

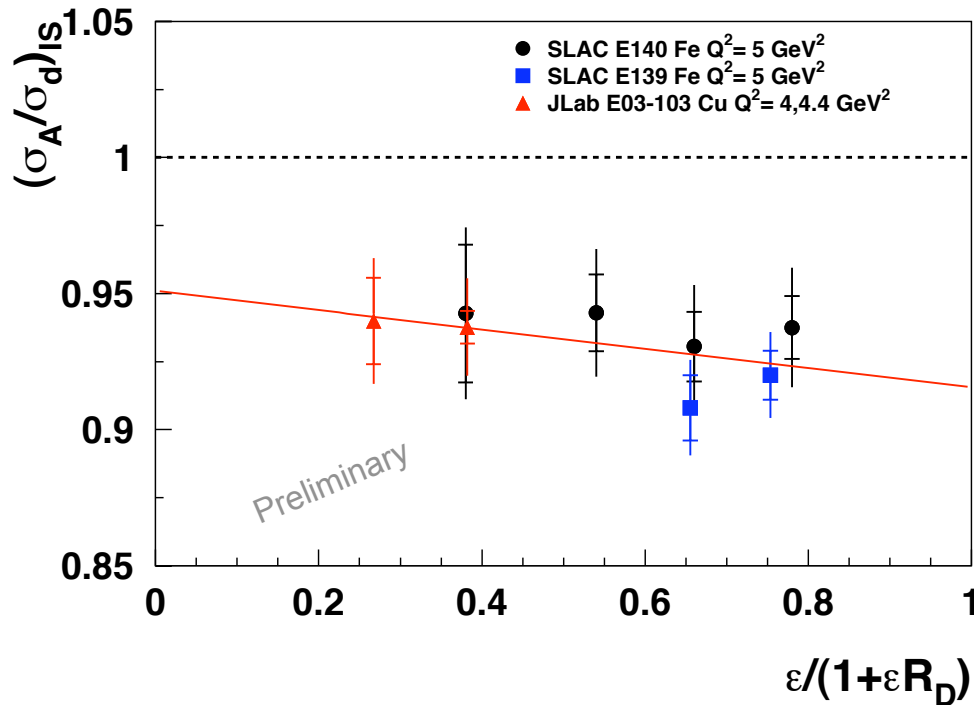
Nuclear higher twist effects and spin-0 constituents in nuclei: same as in free nucleons

# Access to nuclear dependence of $R$

## Iron-Copper

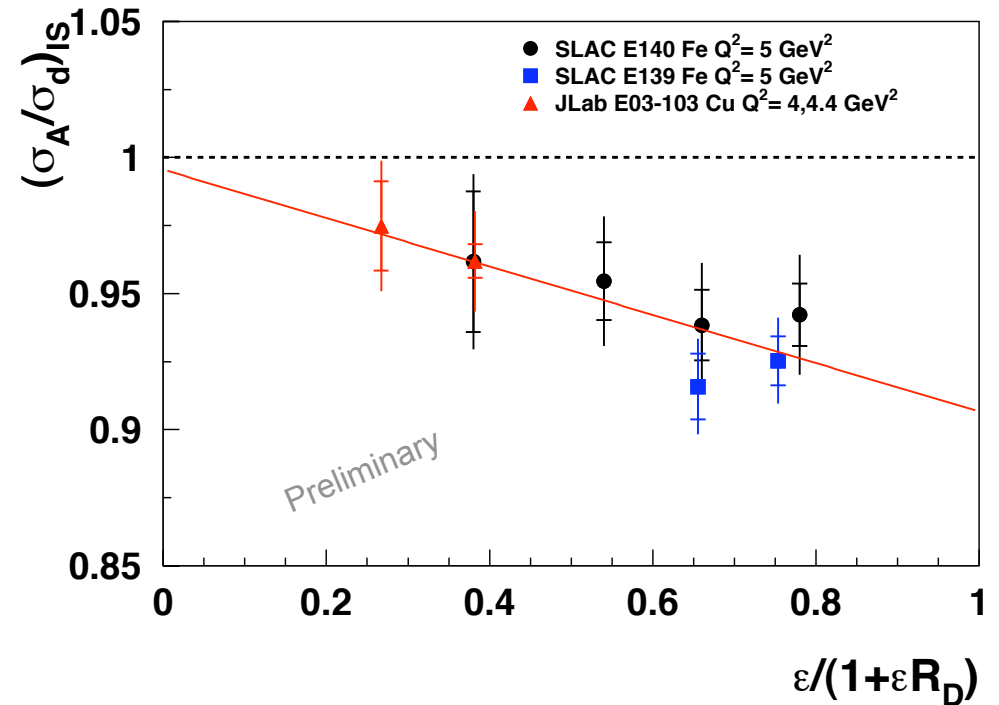
No Coulomb corrections applied

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Coulomb corrections applied

$x=0.5$



**New data from JLab E03-103: access to lower  $\epsilon$**

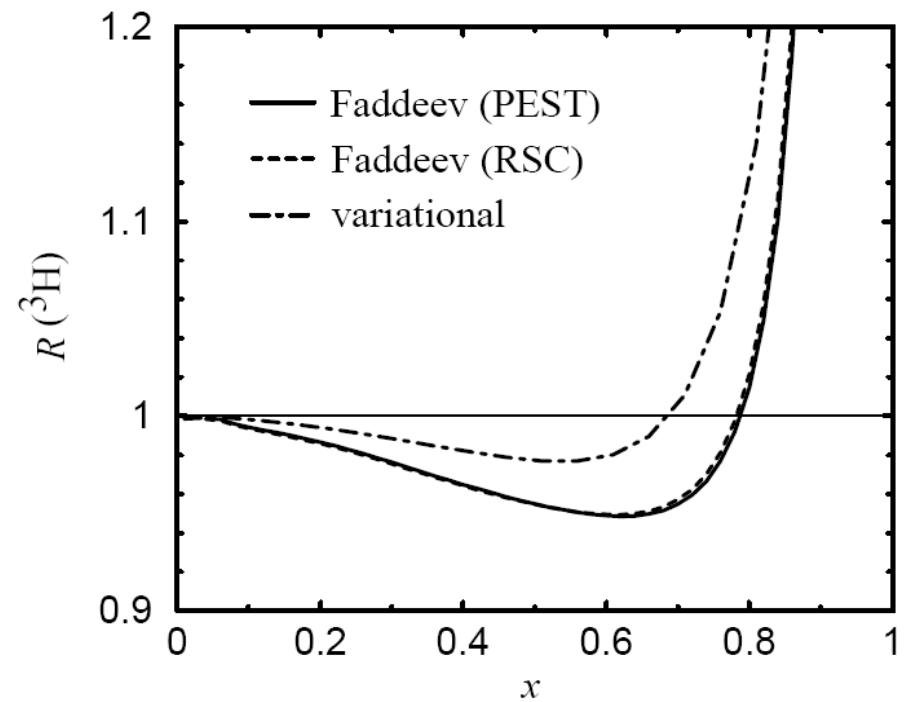
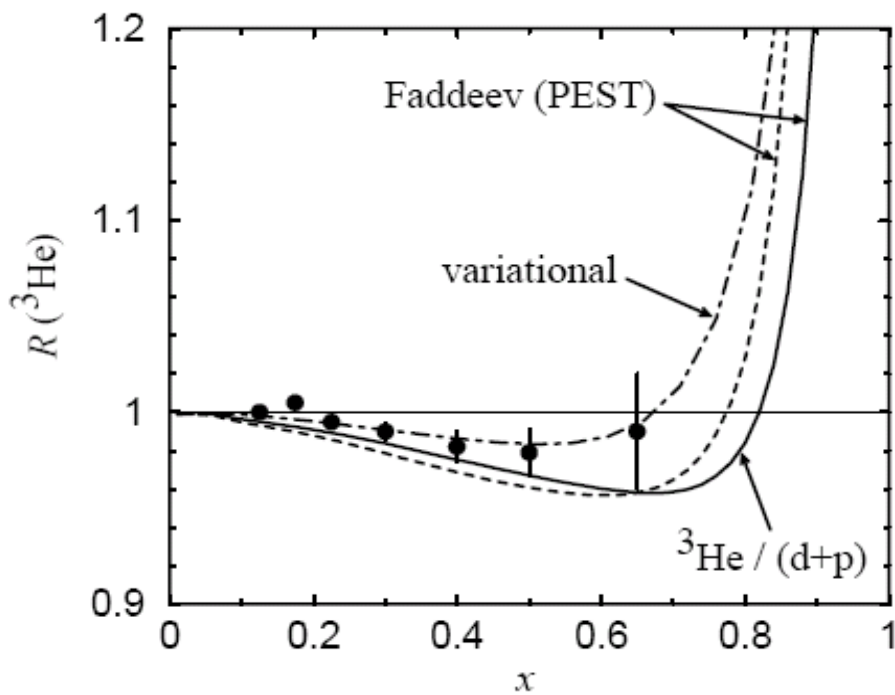
After coulomb corrections:  $R_A - R_D = -0.08 \pm 0.04$

*What's next ?*

# The EMC effect in ${}^3\text{H}$ and ${}^3\text{He}$

$$R({}^3\text{He}) = \frac{F_2^{3\text{He}}}{2F_2^p + F_2^n}$$

$$R({}^3\text{H}) = \frac{F_2^{3\text{H}}}{F_2^p + 2F_2^n}$$



I. Afnan et al, PRC 68 (2003)

# Ratio of ${}^3\text{He}$ , ${}^3\text{H}$ : JLab E12-06-118

A way to get access to  $F_2^n$

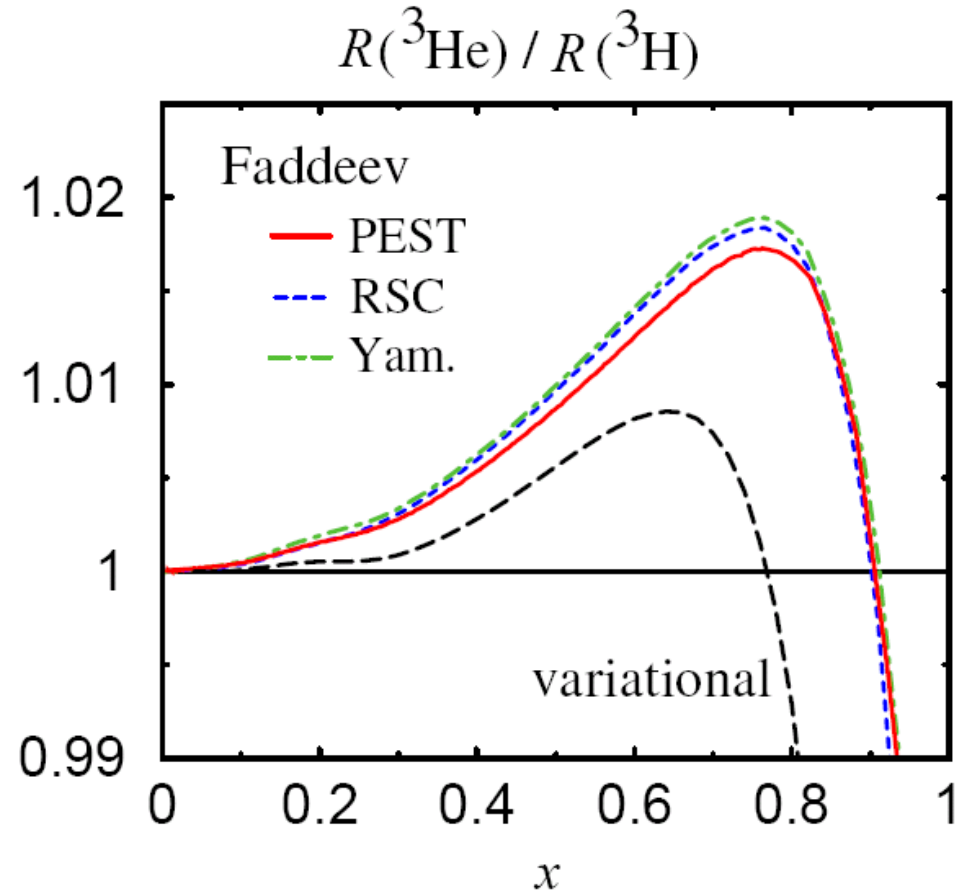
- Measure  $F_2$ 's and form ratios:

$$R({}^3\text{He}) = \frac{F_2^{3\text{He}}}{2F_2^p + F_2^n}, \quad R({}^3\text{H}) = \frac{F_2^{3\text{H}}}{F_2^p + 2F_2^n}$$

- Form “super-ratio”,  $r$ , then

$$\frac{F_2^n}{F_2^p} = \frac{2r - F_2^{3\text{He}}/F_2^{3\text{H}}}{2F_2^{3\text{He}}/F_2^{3\text{H}} - r}$$

where  $r \equiv \frac{R({}^3\text{He})}{R({}^3\text{H})}$



I. Afnan et al, PRC 68 (2003)

# Why is the $F_2^n/F_2^p$ ratio so interesting?

**SU(6)-symmetric wave function** of the proton in the quark model (spin up):

$$|p \uparrow\rangle = \frac{1}{\sqrt{18}} (3u \uparrow [ud]_{S=0} + u \uparrow [ud]_{S=1} - \sqrt{2}u \downarrow [ud]_{S=1} - \sqrt{2}d \uparrow [uu]_{S=1} - 2d \downarrow [uu]_{S=1})$$

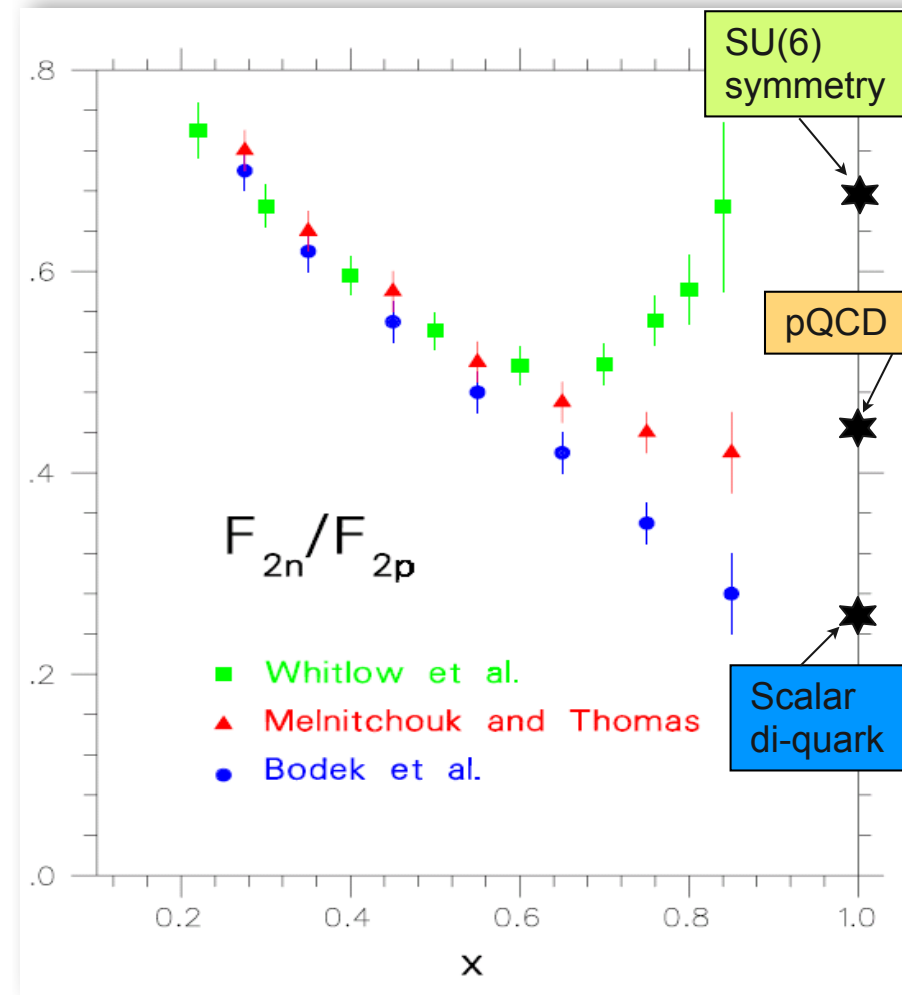
- *u and d quarks identical, N and Δ would be degenerate in mass.*
- *In this model:  $d/u = 1/2$ ,  $F_2^n/F_2^p = 2/3$ .*

**pQCD: helicity conservation** ( $q \uparrow \uparrow p$ )

$$\Rightarrow d/u = 2/(9+1) = 1/5, F_2^n/F_2^p = 3/7 \text{ for } x \rightarrow 1$$

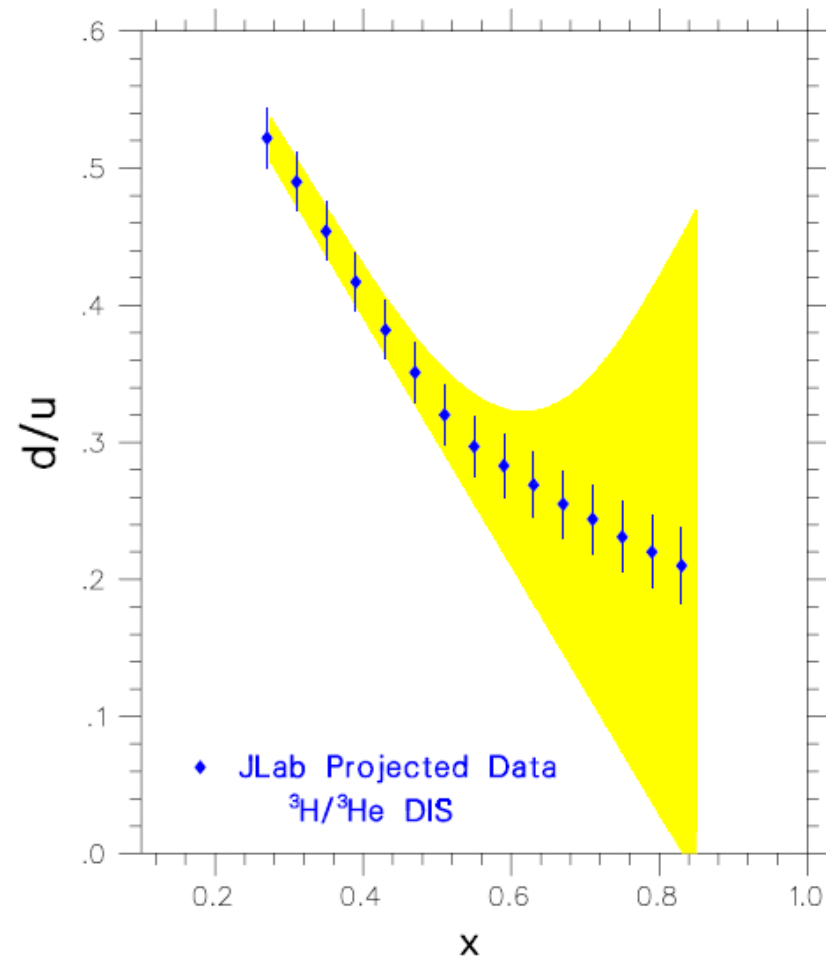
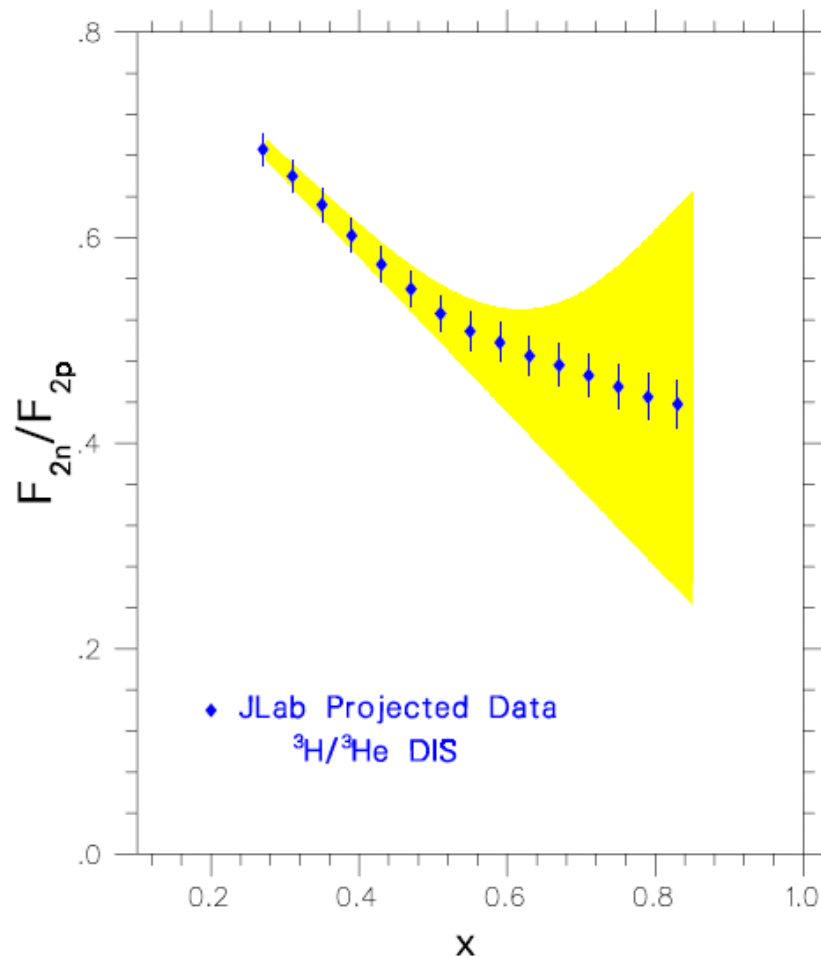
**SU(6) symmetry is broken: N-Δ Mass Splitting**

- *Mass splitting between  $S=1$  and  $S=0$  diquark spectator.*
  - *symmetric states are raised, antisymmetric states are lowered ( $\sim 300$  MeV).*
  - *$S=1$  suppressed*
- $$\Rightarrow d/u = 0, F_2^n/F_2^p = 1/4, \text{ for } x \rightarrow 1$$





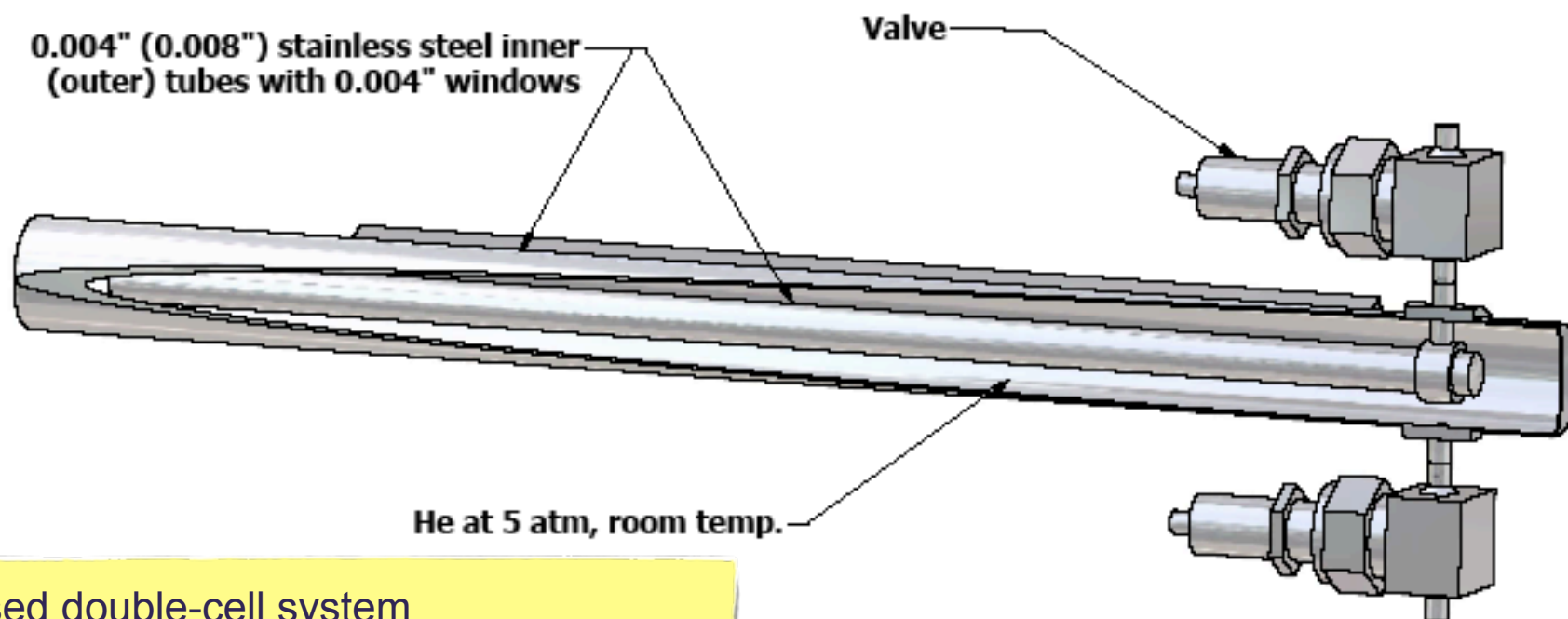
# E12-06-118 Projected Results



- PAC30: “conditionally approved”
- 5000 Ci T target, 31 days
- JLab E12-06-118, G. Petratos, J. Gomez, R. J. Holt, R. Ransome *et al*

# The tritium target conceptual design

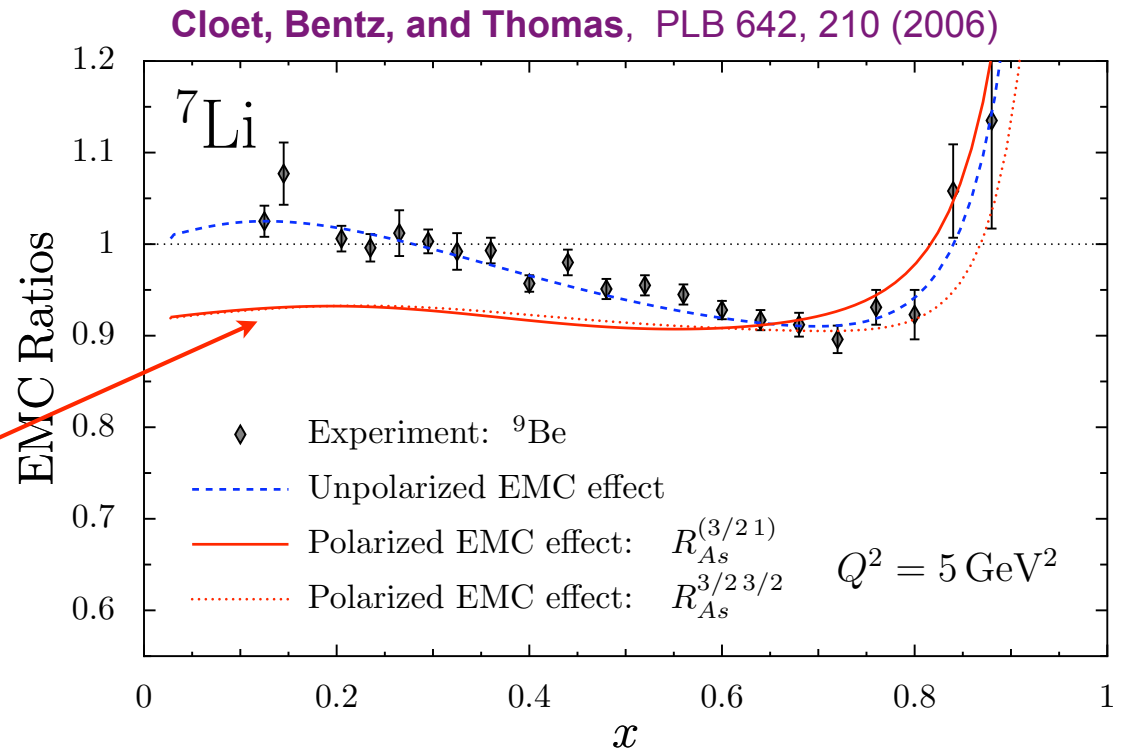
E. J. Beise (U. of Maryland), R. J. Holt (Argonne), W. Korsch (U. of Kentucky),  
T. O'Connor (Argonne), G. G. Petratos (Kent State U.), R. Ransome (Rutgers U.),  
P. Solvignon (Argonne), and B. Wojtsekhowski (Jefferson Lab)  
**Tritium Target Task Force**



- ❖ Closed double-cell system
- ❖ Density: 2.5mg/cm<sup>3</sup>
- ❖ Target length/diameter: 40cm/1.25cm
- ❖ Activity ~ 1500 Ci
- ❖ He for heat conduction

# Polarized EMC effect

- Best target to do this type of measurement would be polarized tritium
- Most probable measurement will be with  ${}^7\text{Li}$  at this time
- Calculation on the size of the effect exists in the modified NJL model.
- State-of-the-art calculation from GFMC are available for  ${}^7\text{Li}$

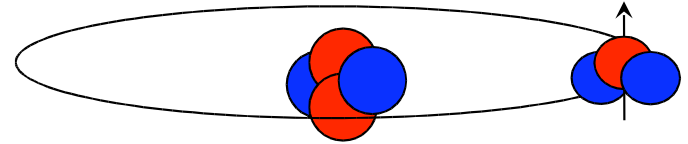


*Different sensitivity to the components of the valence quark wave function  $\Rightarrow$  could bring promising insights in the origin of the EMC effect*

# Polarized EMC effect

- From cluster model:  ${}^7\text{Li} = \alpha + \text{triton}$

“ ${}^7\text{Li}$  is most of the time in the cluster configuration.” *R. Wiringa, Private Comm.*

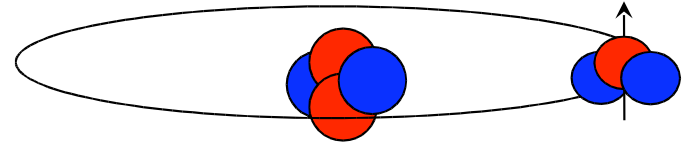


- From JLab E03-103 results on light nuclei ( $A \leq 12$ ), EMC effect depends on the local density:
  - ➔ the polarized proton “feels” dominantly the two neutrons part of the same cluster
  - ➔ the  $\alpha$  cluster dilutes the asymmetries
  - ➔ at first approximation, polarized  ${}^7\text{Li}$  could be seen as an effective polarized tritium target !

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- ➔ the  $\alpha$  cluster dilutes the asymmetries
- ➔ at first approximation, polarized  ${}^7\text{Li}$  could be seen as an effective polarized tritium target !

- Therefore the use of polarized  ${}^7\text{Li}$  could be handy for several physics goal:

- ➔ the polarized EMC effect in  ${}^7\text{Li}$
- ➔ If cluster model assumptions are right: access to the polarized EMC effect in triton and also the Bjorken Sum Rule for mirror nuclei:

$$\Gamma_1^{(3\text{H})} - \Gamma_1^{(3\text{He})} = \frac{g_A^{\text{tri}}}{6} \cdot C_{\text{NS}}(\alpha_s)$$

axial vector coupling constant of the triton measured in tritium decay

R. Jaffe & A. Manohar, Nucl. Phys. B321, 343 (1989)

# Summary

JLab experiment E03-103 brings a wealth of new results:

## □ Light nuclei:

- *contain key information on the EMC effect*
- *hint of **local density dependence** of the EMC effect*
- *can be compared to **realistic calculations***

## □ Heavy nuclei and Coulomb distortion:

- *affects the extrapolation to **nuclear matter** which is key for comparison with theoretical calculations*
- *has a real impact on the **A-dependence of R**: clear  $\epsilon$ -dependence*
- *need a measurement of the amplitude of the effect in the inelastic regime*

# Outlook

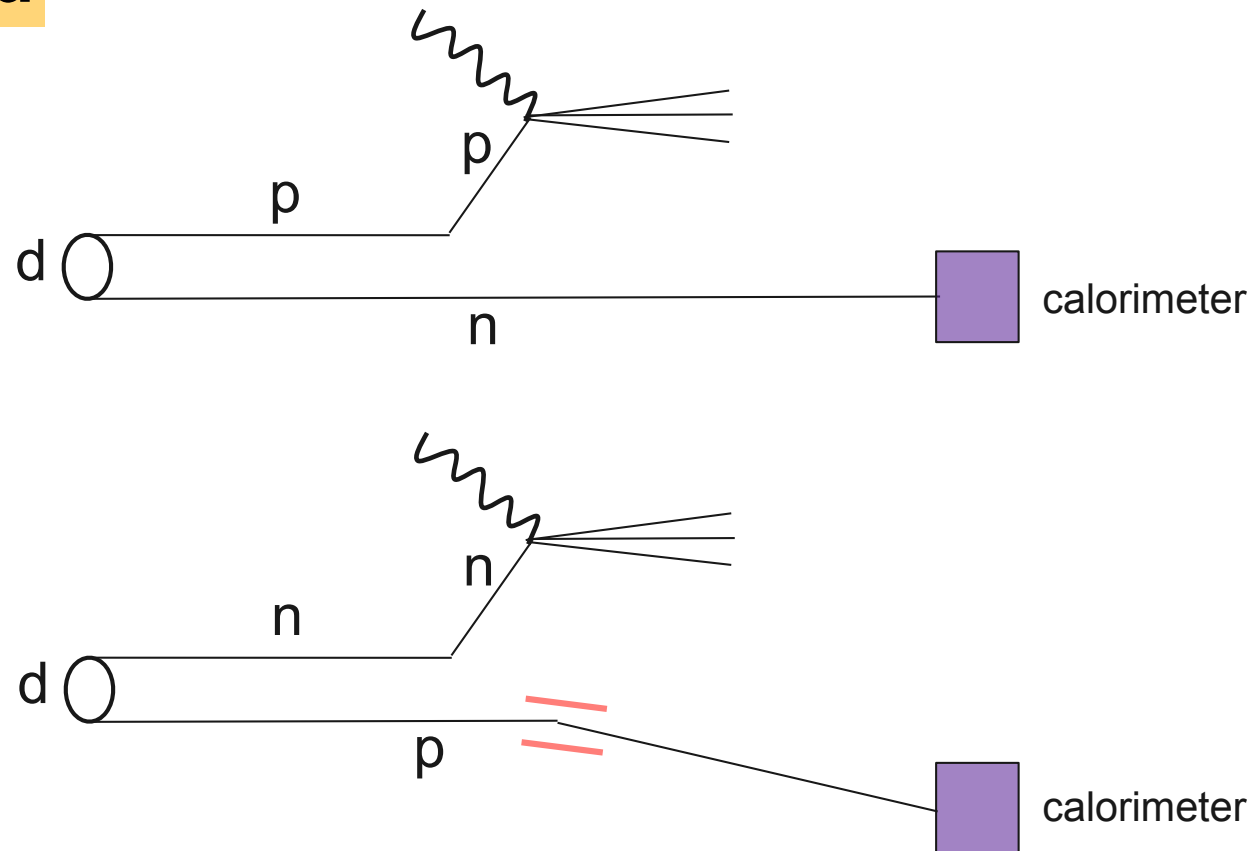
- $F_2(^3\text{He})/F_2(^3\text{H})$ : Hall A E12-06-118 (*conditionally approved*)
  - EMC effect in light nuclei
  - n/p at high x in DIS
  - getting to the d-quark distribution
  
- Coulomb distortion measurement in DIS (*require a positron beam*)
  
- Precision measurement of R in medium weight nuclei in DIS (*proposal in preparation*)
  
- Polarized EMC (*discussion-stage about a possible proposal*)
  
- (Short-range correlations and super-fast quarks: *approved measurements*)
  
- EIC ...

# What about a measurement at the EIC ?

$F_{2n}/F_{2p}$  at EIC:

high  $W$  so no need to worry about target mass correction

$e^- \rightarrow \leftarrow d$





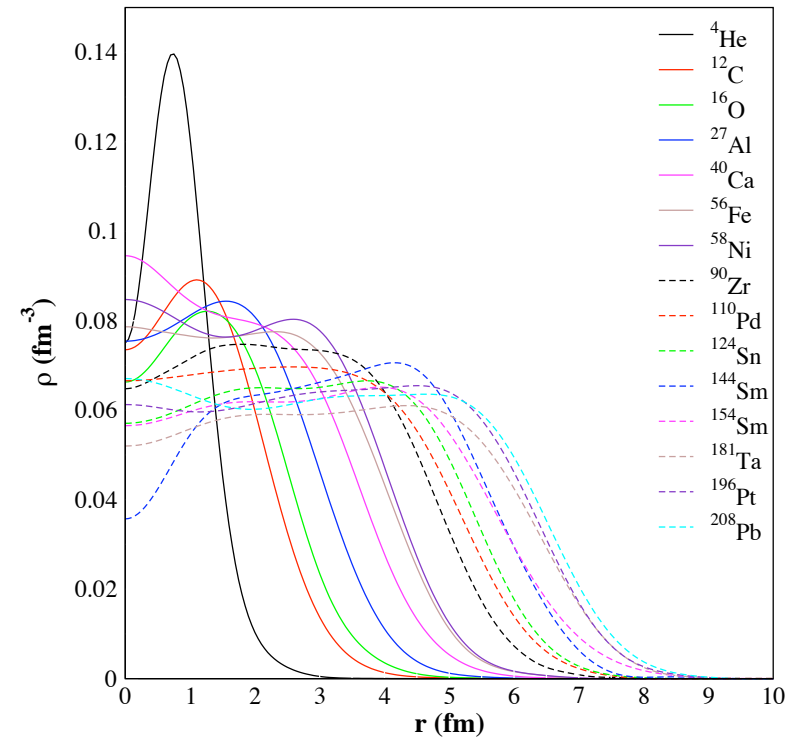
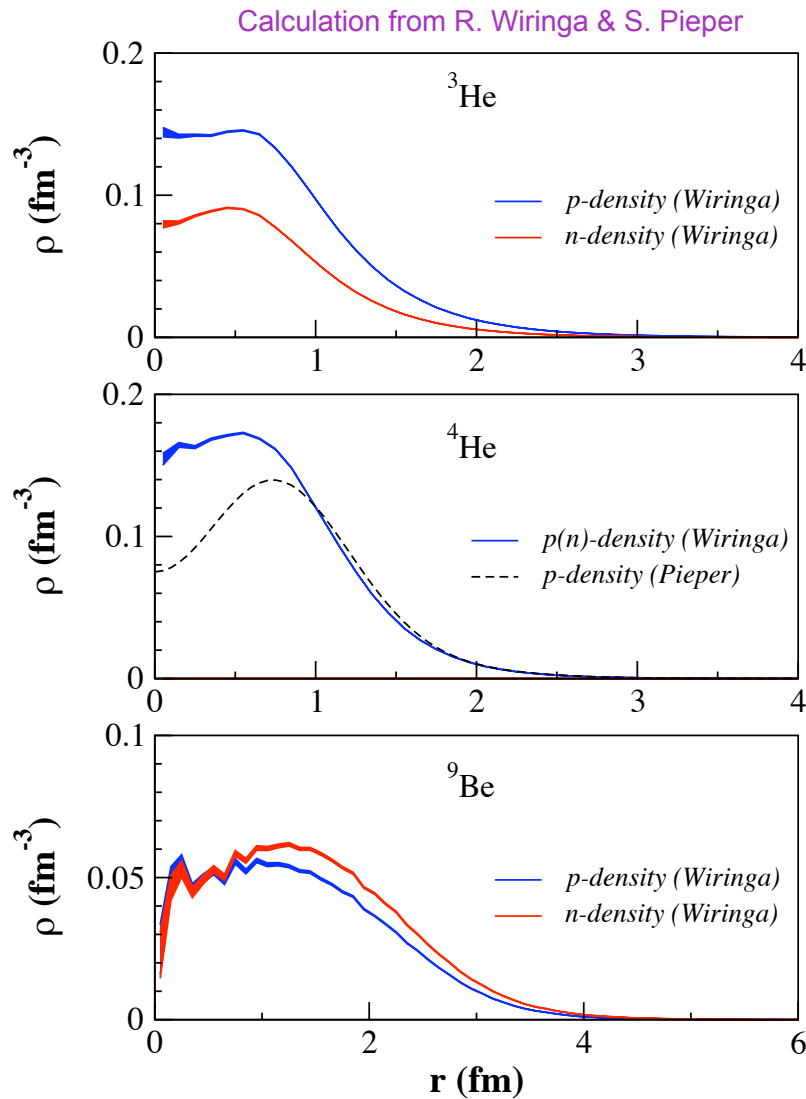
*Extra slides*

# World data re-analysis

Experiments	E (GeV)	A	x-range	Pub. 1 <sup>st</sup> author
CERN-EMC	280	56	0.050-0.650	Aubert
		12,63,119	0.031-0.443	Ashman
CERN-BCDMS	280	15	0.20-0.70	Bari
		56	0.07-0.65	Benvenuti
CERN-NMC	200	4,12,40	0.0035-0.65	Amaudruz
	200	6,12	0.00014-0.65	Arneodo
SLAC-E61	4-20	9,27,65,197	0.014-0.228	Stein
SLAC-E87	4-20	56	0.075-0.813	Bodek
SLAC-E49	4-20	27	0.25-0.90	Bodek
SLAC-E139	8-24	4,9,12,27,40,56,108,197	0.089-0.8	Gomez
SLAC-E140	3.7-20	56,197	0.2-0.5	Dasu
DESY-HERMES	27.5	3,14,84	0.013-0.35	Airapetian

# Density calculations

Calculation from S. Pieper



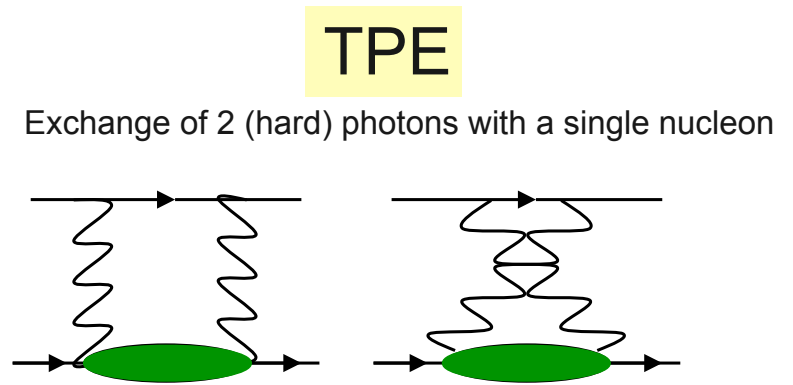
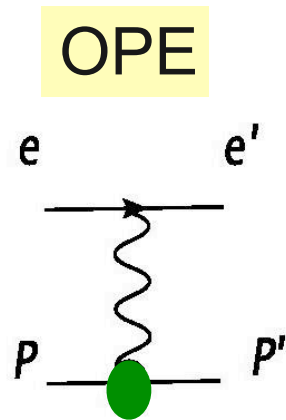
Average density:

$$\langle \rho_{n,p} \rangle = \frac{\int \rho_{n,p}^2 d^3 r}{\int \rho_{n,p} d^3 r}$$

$$\langle \rho_p \rangle + \langle \rho_n \rangle = \langle \rho_A \rangle \xrightarrow{\text{finite proton size correction}} \langle \rho_A \rangle \cdot \left( \frac{\langle r \rangle}{r_{\text{eff}}} \right)^3$$

$$\text{with } r_{\text{eff}} = \sqrt{\langle r \rangle^2 + 0.9^2}$$

# Coulomb distortion and two-photon exchange

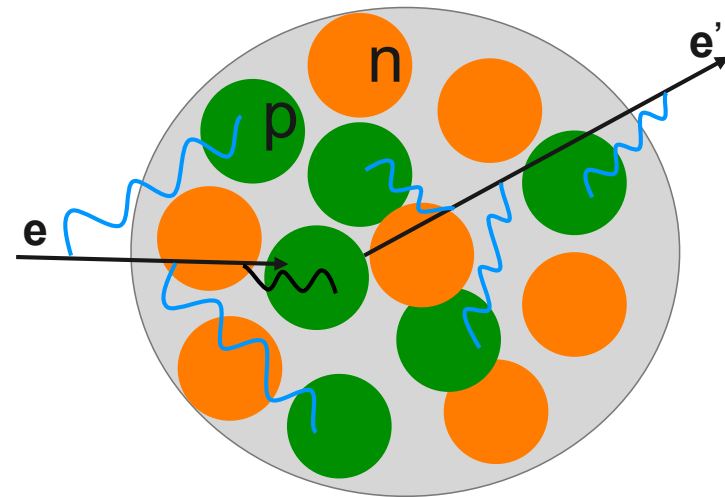


Incident (scattered) electrons are accelerated (decelerated) in the Coulomb well of the nucleus.

Opposite effect with positrons

## Coulomb distortion

Exchange of one or more (soft) photons with the nucleus, in addition to the one hard photon exchanged with a nucleon



# How to correct for Coulomb distortion ?

~~$$\sigma_{tot}^{PWBA} = \sigma_{Mott} S_{tot}^{PWBA}(|\vec{q}|, \omega, \theta)$$~~


$$\sigma_{tot}^{DWBA}$$

- Focusing of the electron wave function
- Change of the electron momentum

Effective Momentum Approximation (EMA)

Aste and Trautmann, Eur. Phys. J. A26, 167-178(2005)

$$\left. \begin{array}{l} E \rightarrow E + V^- \\ E_p \rightarrow E_p + V^- \end{array} \right\} Q_{eff}^2 = 4(E + \bar{V})(E_p + \bar{V}) \sin^2\left(\frac{\theta}{2}\right)$$

1<sup>st</sup> method

$$S_{tot}^{PWBA}(|\vec{q}|, \omega, \theta) \longrightarrow S_{tot}^{PWBA}(|\vec{q}_{eff}|, \omega, \theta)$$

2<sup>nd</sup> method

$$S_{tot}^{PWBA}(|\vec{q}|, \omega, \theta) \longrightarrow S_{tot}^{PWBA}(|\vec{q}_{eff}|, \omega, \theta)$$

$$\sigma_{Mott}^{eff} = 4\alpha^2 \cos^2(\theta/2)(E_p + \bar{V})^2 / Q_{eff}^4$$

$$F_{foc}^i = \frac{E + \bar{V}}{E}$$

$$\sigma_{tot}^{CC} = \sigma_{Mott} \cdot S_{tot}^{PWBA}(|\vec{q}_{eff}|, \omega, \theta)$$



$$\sigma_{tot}^{CC} = (F_{foc}^i)^2 \cdot \sigma_{Mott}^{eff} \cdot S_{tot}^{PWBA}(|\vec{q}_{eff}|, \omega, \theta)$$

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$S_{tot}^{PWBA}$  One-parameter model depending only on the effective potential seen by the electron on average.

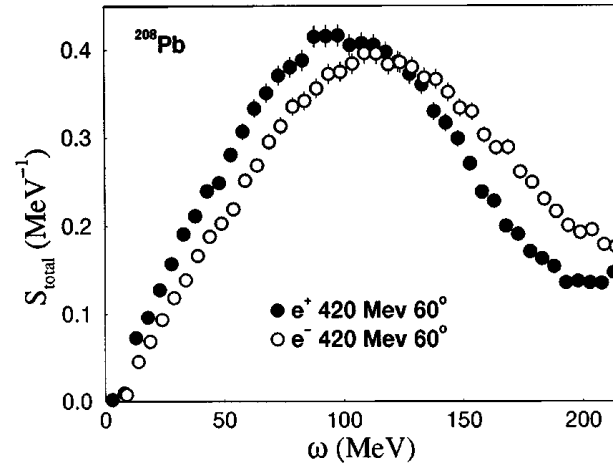
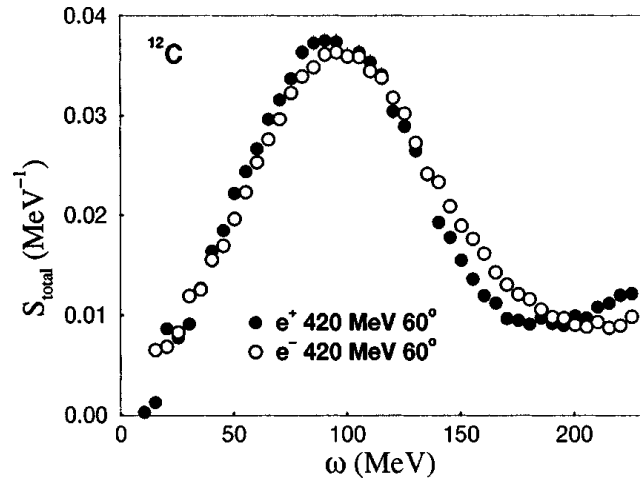
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# Coulomb distortion measurements in quasi-elastic scattering



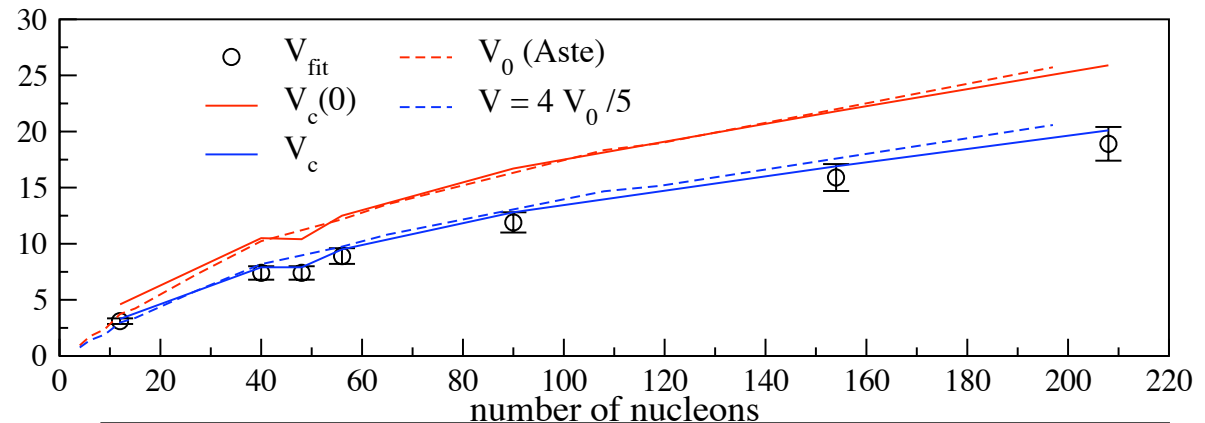
Gueye et al., PRC60, 044308 (1999)

$$\tilde{k} = k - V(z)$$

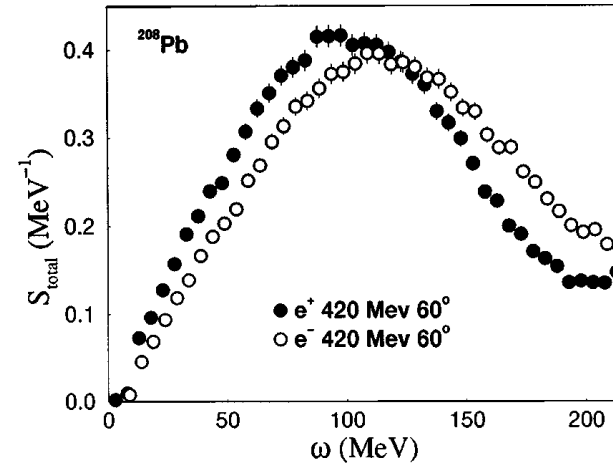
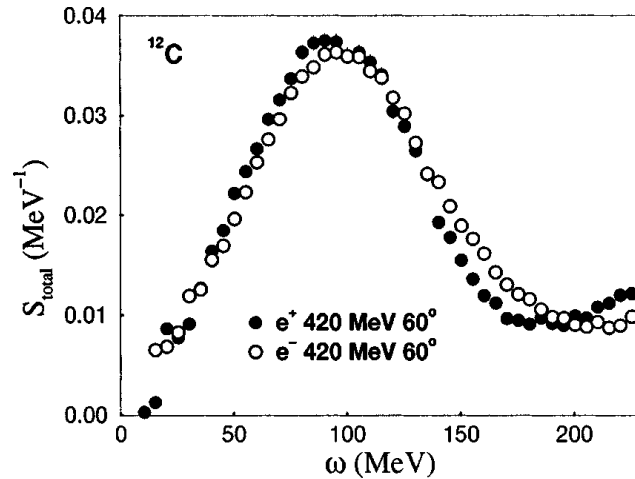
$$V(r) = -\frac{3\alpha(Z-1)}{2R} + \frac{\alpha(Z-1)}{2R} \left(\frac{r}{R}\right)^2$$

$$R = 1.1A^{1/3} + 0.86A^{-1/3}$$

Aste and Trautmann, Eur. Phys. J. A26, 167-178(2005)



# Coulomb distortion measurements in quasi-elastic scattering



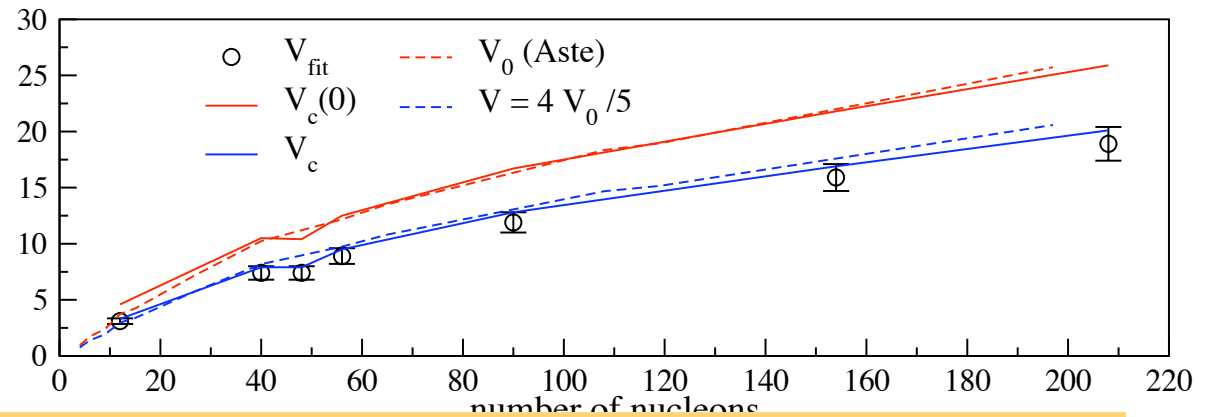
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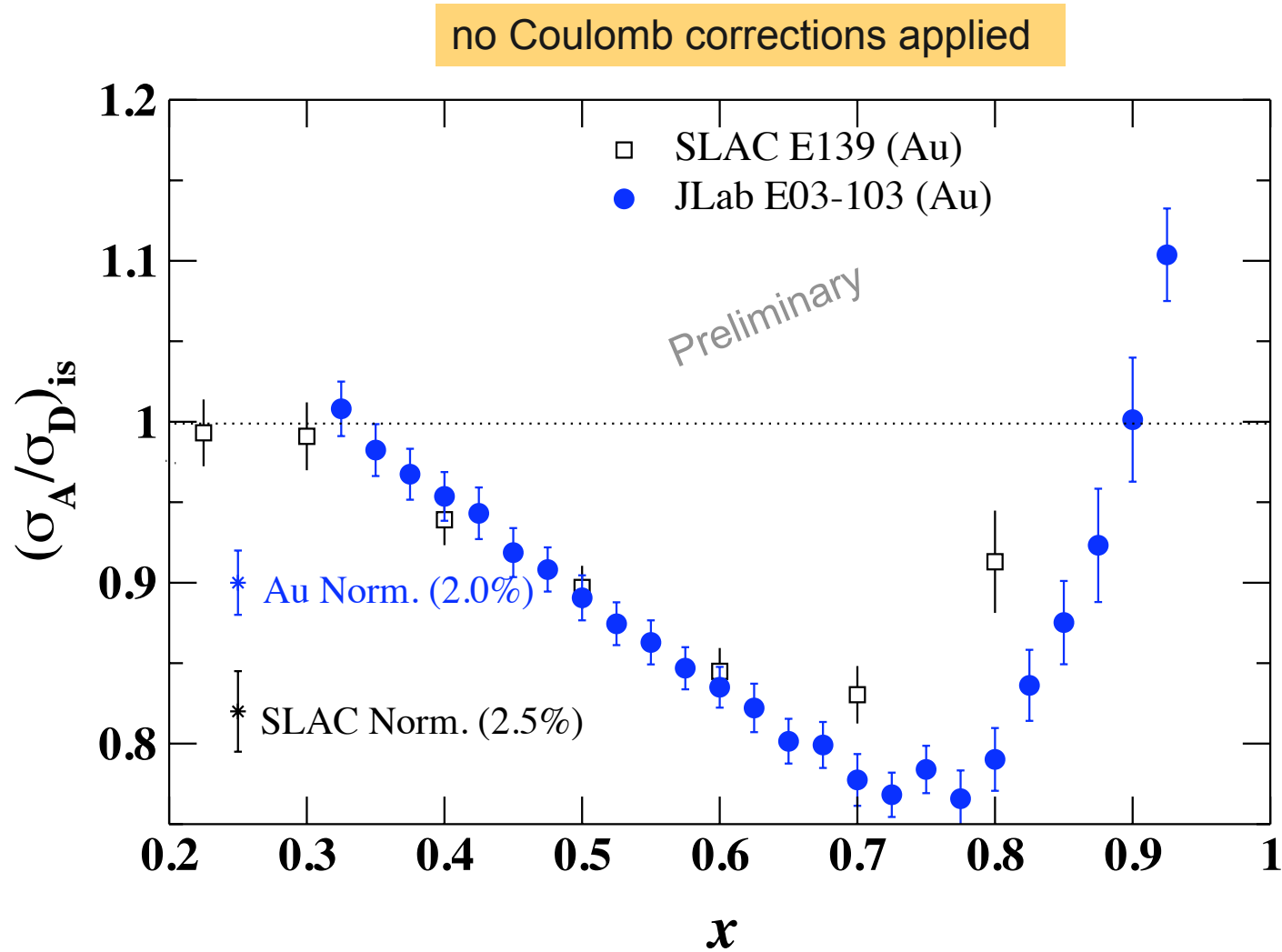
Aste and Trautmann, Eur. Phys. J. A26, 167-178(2005)



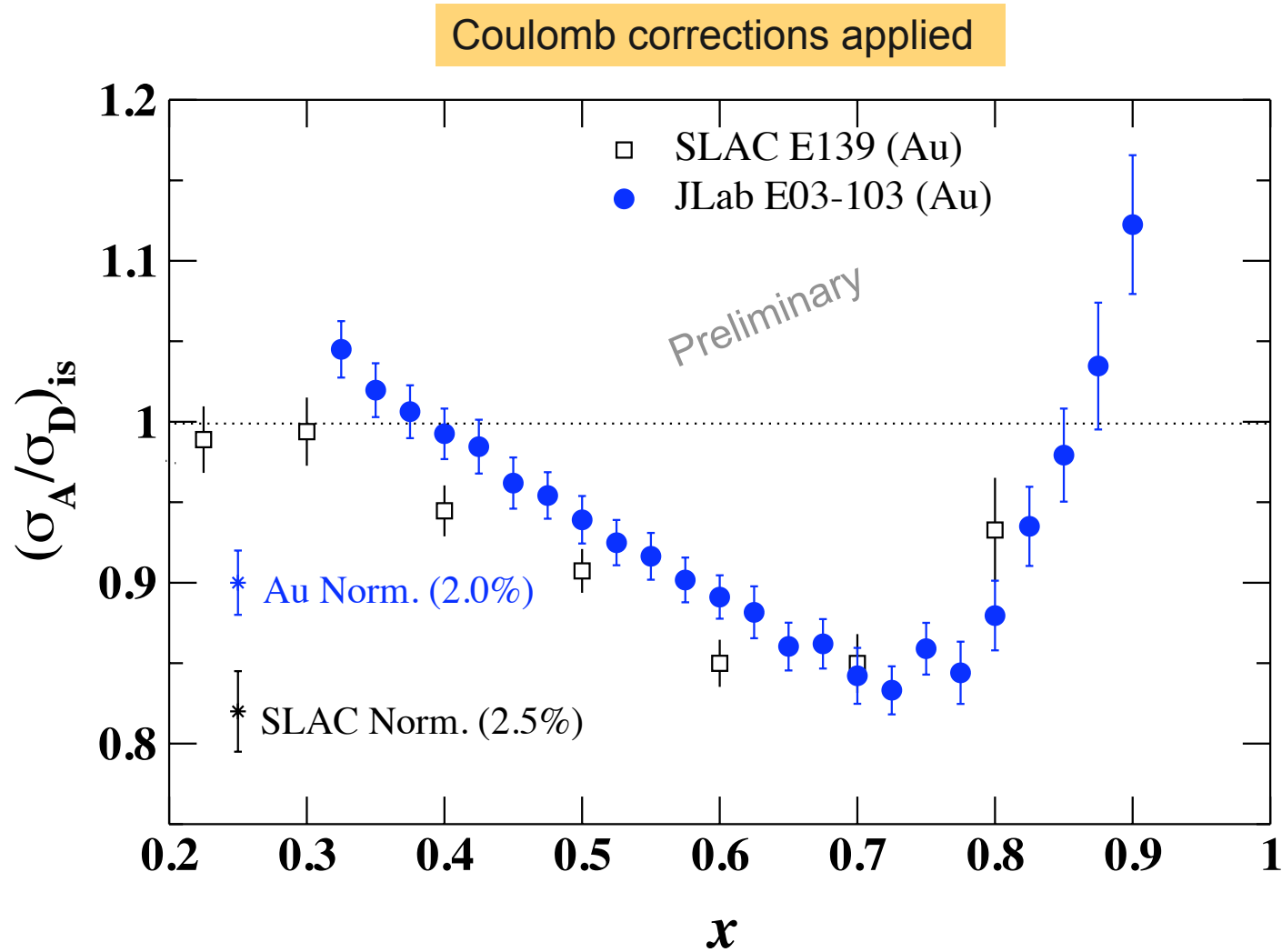
Coulomb potential established in Quasi-elastic scattering regime !



# *E03-103 heavy target results*



# *E03-103 heavy target results*



# $R(x, Q^2)$

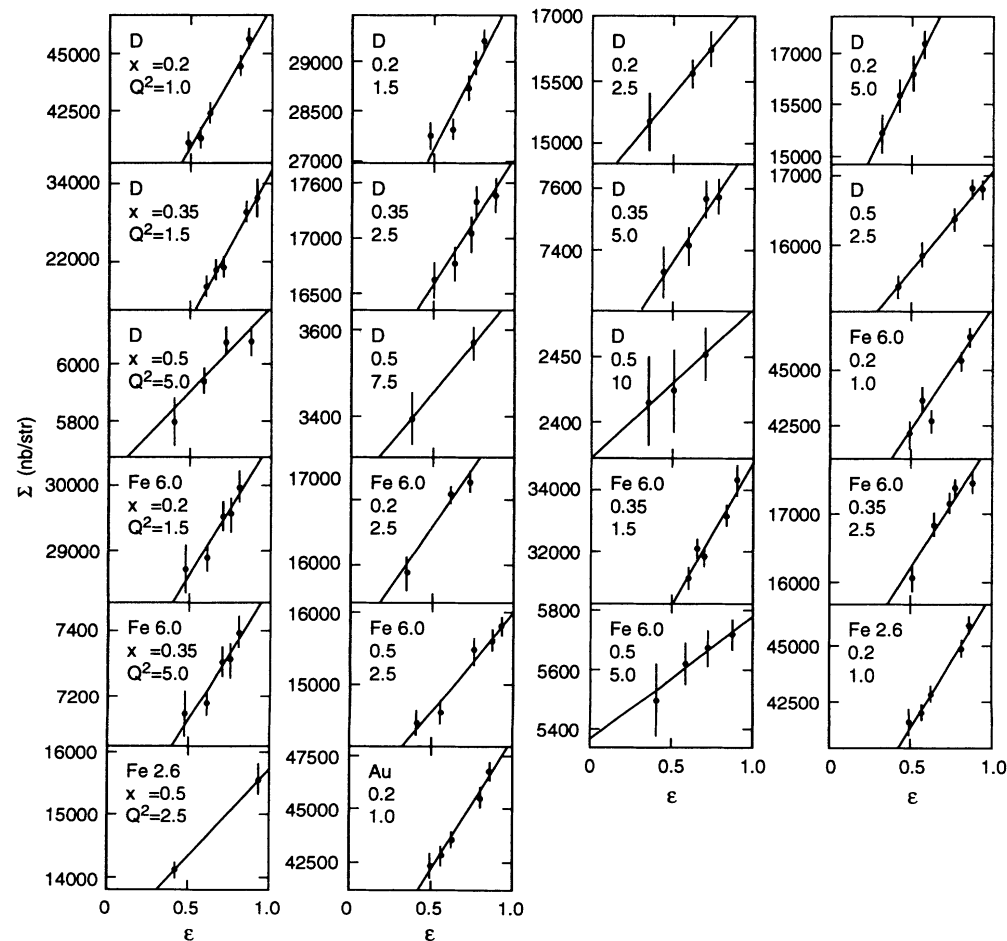
$$\frac{d\sigma}{d\Omega dE'} = \Gamma [\sigma_T(x, Q^2) + \varepsilon \sigma_L(x, Q^2)]$$

$$R(x, Q^2) = \frac{\sigma_L(x, Q^2)}{\sigma_T(x, Q^2)}$$

TPE can affect the  $\varepsilon$  dependence (talk of E. Christy on Thursday)

Coulomb Distortion could have the same kind of impact as TPE, but gives also a correction that is A-dependent.

Dasu et al., PRD49, 5641(1994)

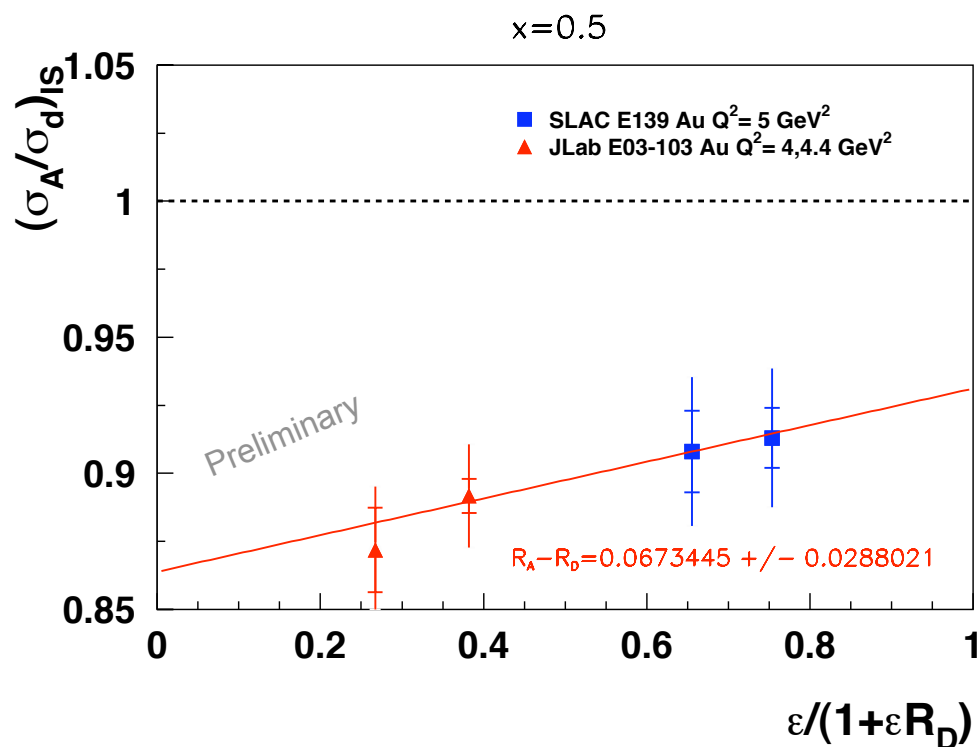


# Access to nuclear dependence of $R$

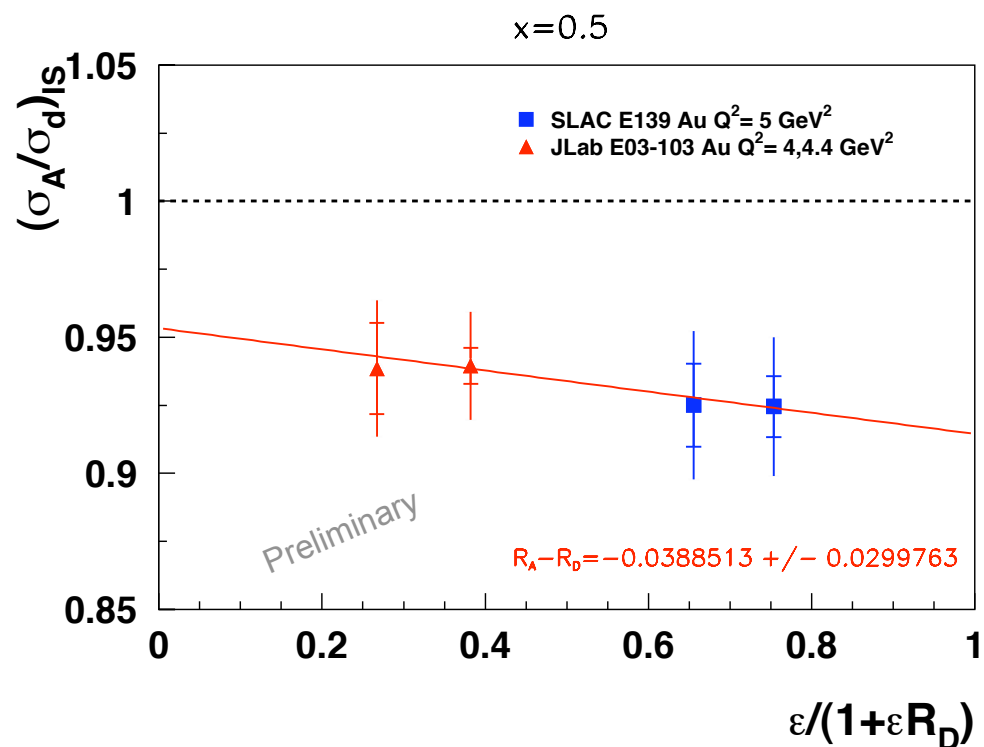
New data from JLab E03-103: access to lower  $\varepsilon$

## Gold

No Coulomb corrections applied



Coulomb corrections applied



# Why don't we know the ratio at high $x$ ?

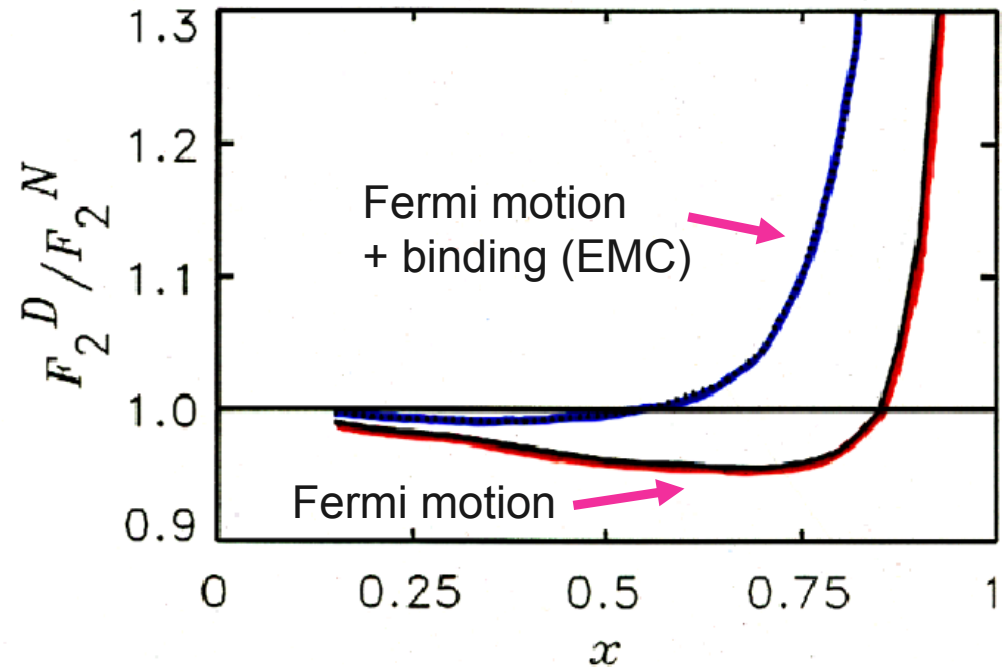
The deuteron is used as “poor person’s” neutron target.

$$F_2^D = \frac{1}{2} \sum_N \int_x^{M_D/M} dy \rho(y) F_2^N \left( \frac{x}{y}, Q^2 \right) + \delta^{off} F_2^D$$

Probability of N of momentum  $y$   
( Fermi smearing + binding)

Off-shell

- Subtract off-shell corr from deuteron data
- Smear the proton data and subtract
- Remainder is smeared neutron struc fn.
- Unsmear the neutron structure function



$$F_2^n = S_n (F_2^{D(conv)} - \tilde{F}_2^p)$$

- Iterate

A. W. Thomas and W. Melnitchouk, NP A 631 (1998) 296

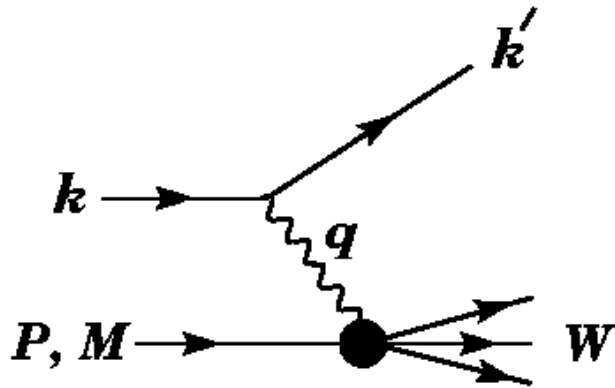
# *Large $x$ is essential for particle physics*

- **Parton distributions at large  $x$  are important input into simulations of hadronic background at colliders, eg the LHC.**
  - High  $x$  at low  $Q^2$  evolves into low  $x$  at high  $Q^2$ .
  - Small uncertainties at high  $x$  are amplified.
  
- **HERA anomaly: (1996): excess of neutral and charged current events at  $Q^2 > 10,000 \text{ GeV}^2$** 
  - Leptoquarks
  - $\sim 0.5\%$  larger  $u(x)$  at  $x > 0.75$   
S. Kuhlmann et al, PLB 409 (1997)



LHC era is approaching.

# Why do we need high energy electrons?



$$Q^2 > 1 \text{ GeV}^2$$

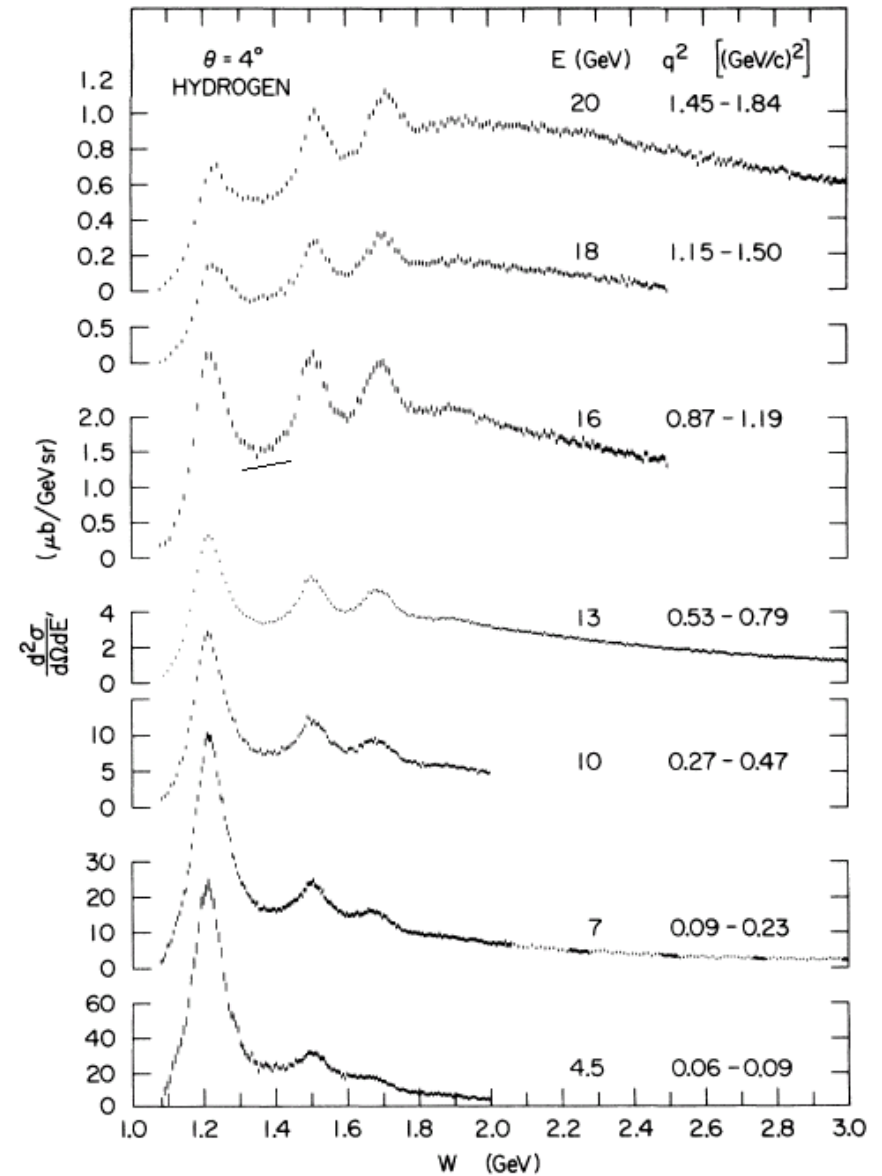
$$W > 2 \text{ GeV}$$

$$W^2 = (p + q)^2 = M^2 + 2M\nu - Q^2$$

$$W^2 = M^2 + \frac{1-x}{x}Q^2$$

eg. if  $x = 0.9$ , then  $Q^2 = 27 \text{ GeV}^2$

Practical limit at JLab12:  $x = 0.8$



S. Stein *et al*, PRD 12 (1975)

# Ratio: Neutron to Proton Structure Function

- Proton structure function:

$$F_2^p = x \left[ \frac{4}{9}(u + \bar{u}) + \frac{1}{9}(d + \bar{d}) + \frac{1}{9}(s + \bar{s}) \right]$$

- Neutron structure function (isospin symmetry):  $u_p(x) = d_n(x) \equiv u(x)$

$$F_2^n = x \left[ \frac{4}{9}(d + \bar{d}) + \frac{1}{9}(u + \bar{u}) + \frac{1}{9}(s + \bar{s}) \right]$$

- Ratio:

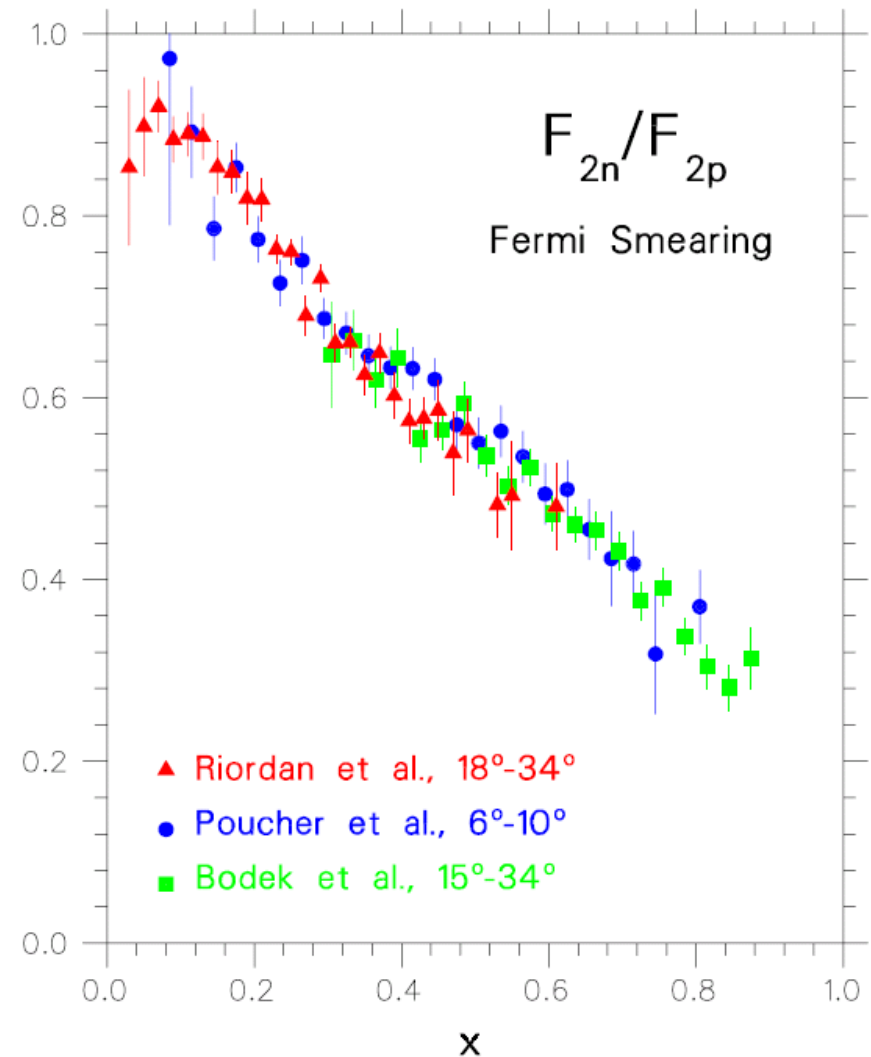
$$\frac{F_2^n}{F_2^p} = \frac{u + \bar{u} + 4(d + \bar{d}) + s + \bar{s}}{4(u + \bar{u}) + d + \bar{d} + s + \bar{s}}$$

- Nachtmann inequality:

$$\frac{1}{4} \leq \frac{F_2^n}{F_2^p} \leq 4$$

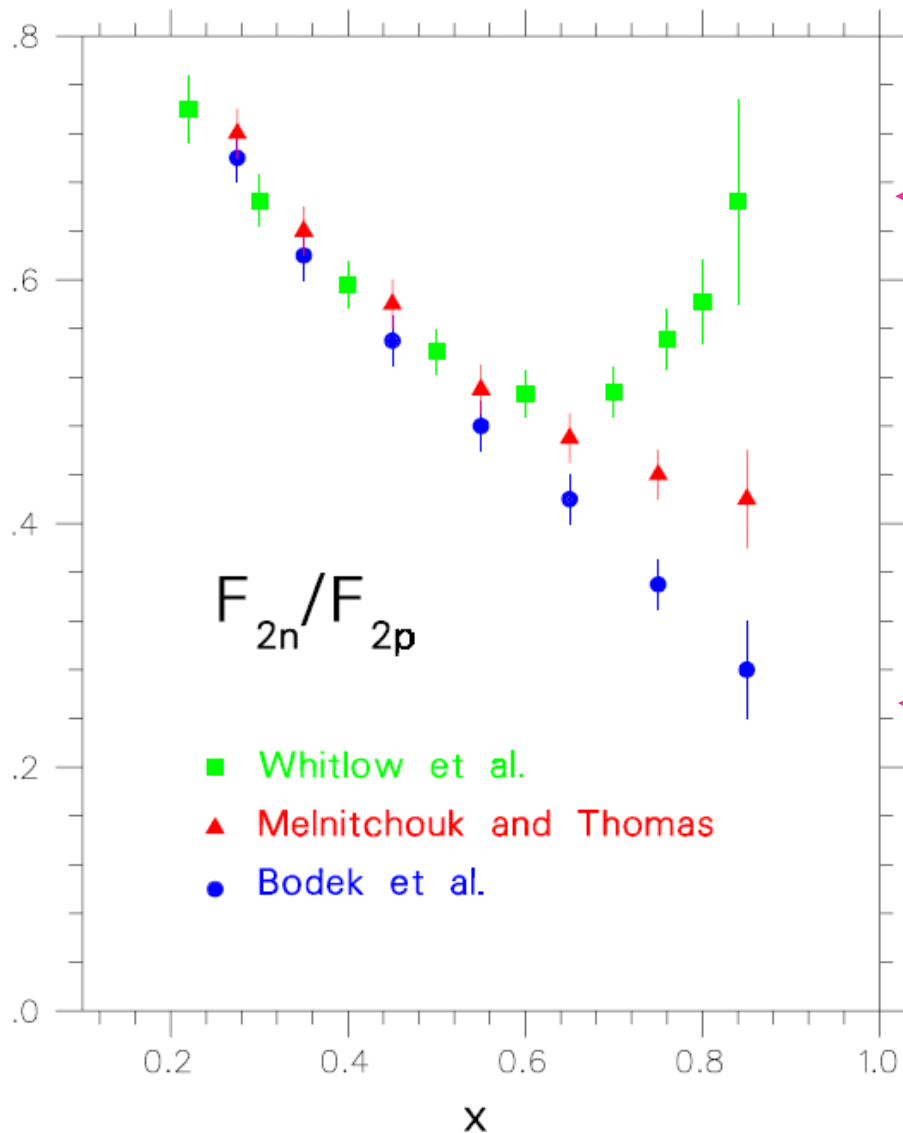
- Focus on high x:

$$\frac{F_2^n}{F_2^p} = \frac{[1 + 4(d/u)]}{[4 + (d/u)]}$$





# Structure Function Ratio



← SU(6) symmetry

← pQCD

← Scalar di-quark

Reviews:

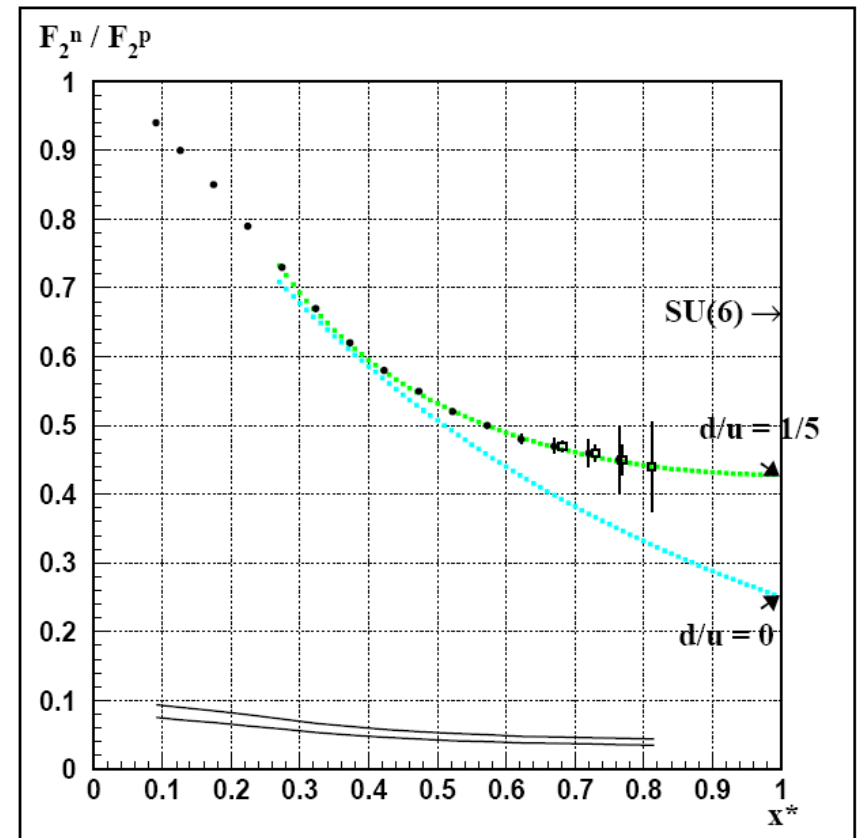
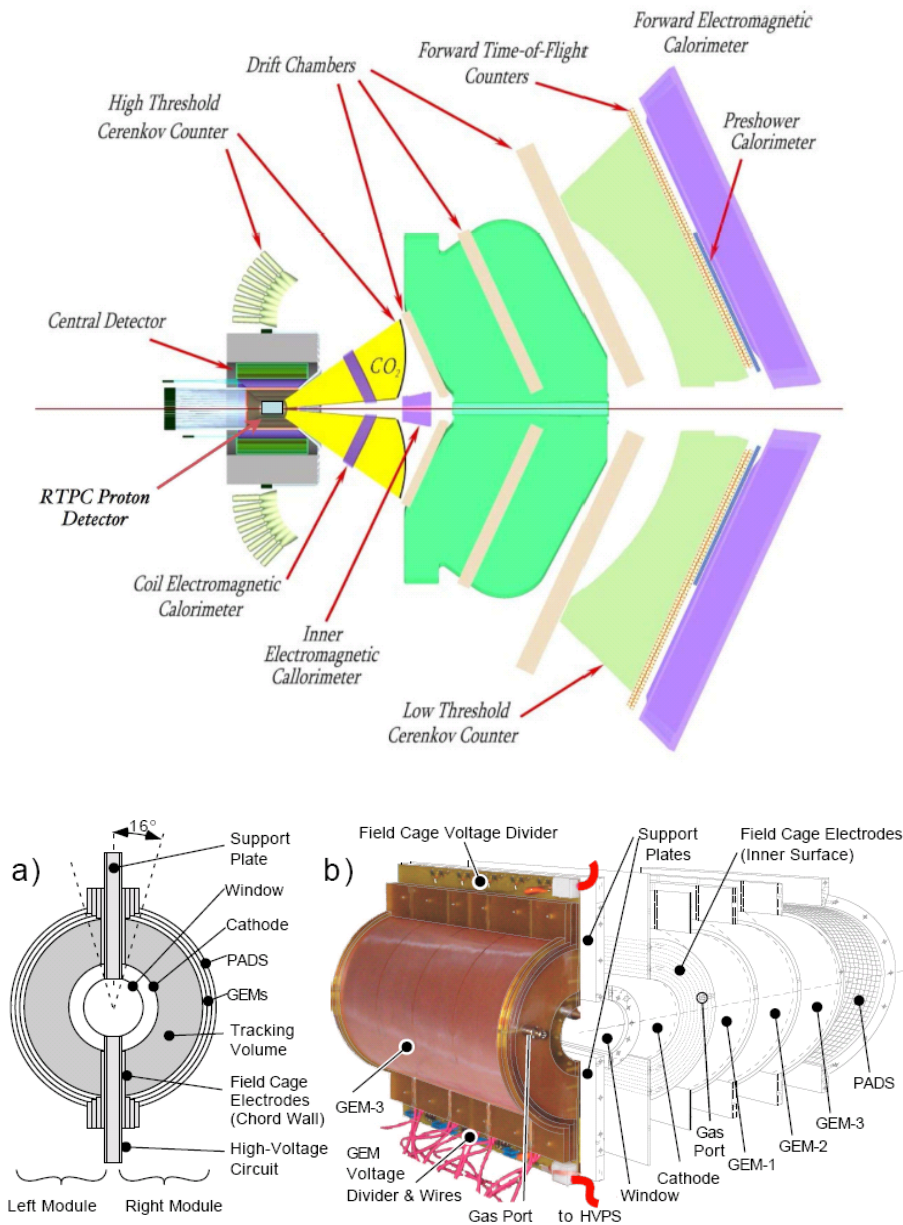
N. Isgur, PRD **59** (1999),

S Brodsky et al NP **B441** (1995),

W. Melnitchouk and A. Thomas PL **B377** (1996) 11.

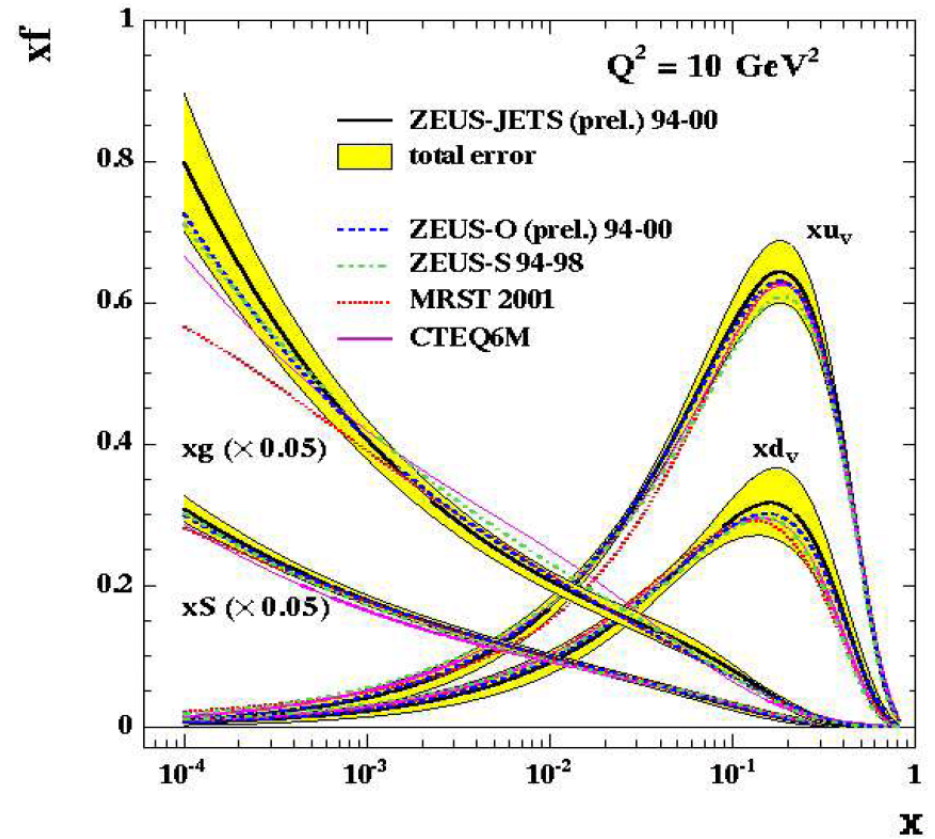
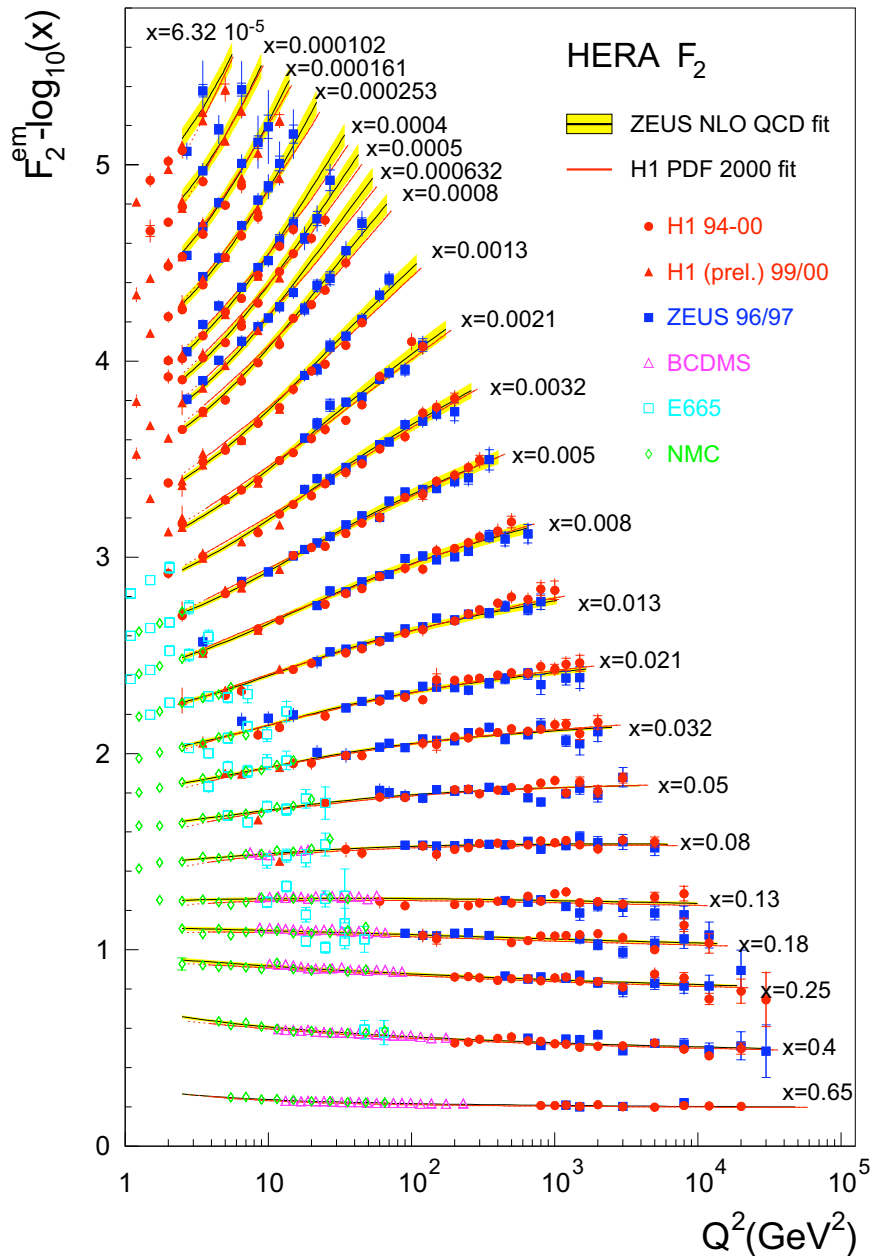
Craig Roberts: “a top priority”

# Tagged Neutron in the Deuteron – BONUS + CLAS12

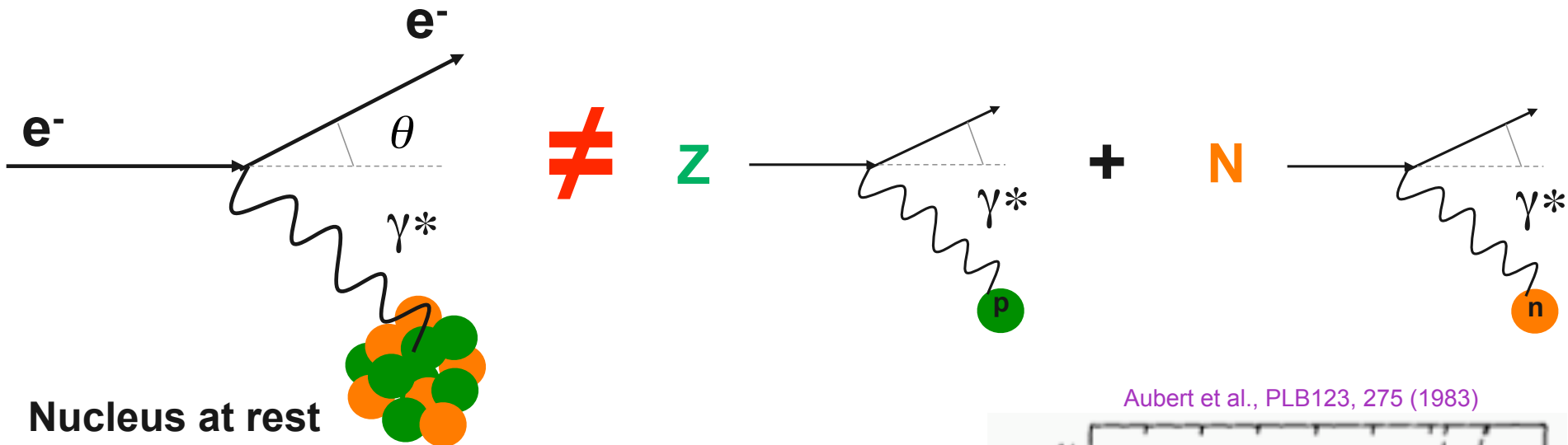


- PAC30: “conditionally approved”
- JLab E12-06-113, S. Bultmann, H. Fenker, M. Christy, C. Keppel *et al*

# F2p and parton distributions



# The EMC effect



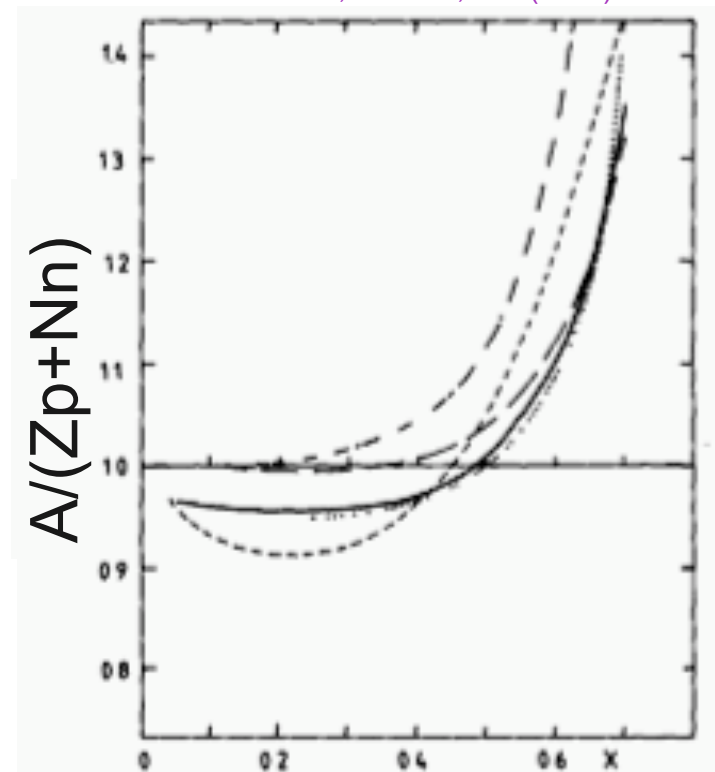
**Nucleus at rest**  
 ( $A$  nucleons =  $Z$  protons +  $N$  neutrons)

Theoretical prediction:

$$F_2^A = ZF_2^p + (A - Z)F_2^n$$

after corrections due to the motion of the nucleons in the nucleus (slowly moving nucleons weakly bound)

Aubert et al., PLB123, 275 (1983)



# *Polarized EMC effect*

- ◆ Why is it important to measure it ?
- ◆ Experimental requirements for a baseline measurement
- ◆ Will the extraction of  $g_1(7\text{Li})/g_1p$  be model independent ?
- ◆ A1n extraction only considered unpolarized EMC effect. Need calculation of  $g_1(3\text{He})/g_1n$ .
- ◆ ...

