

# ***E01-012: Spin Duality***

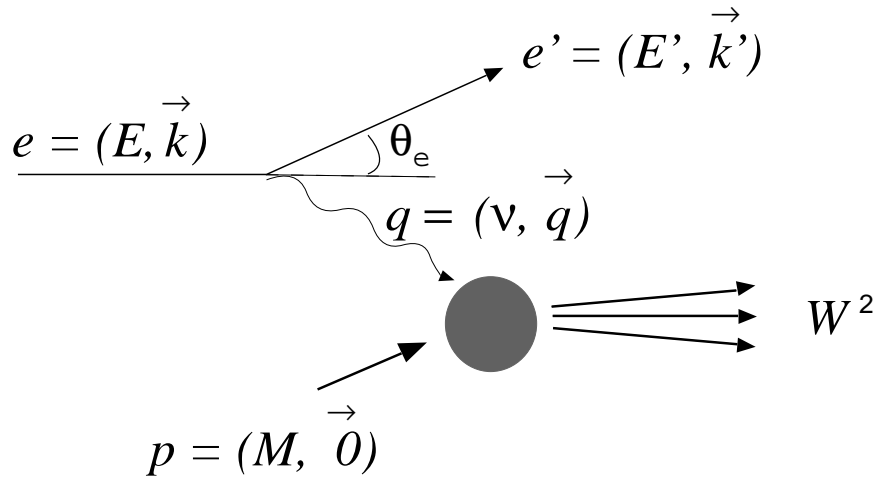
*Patricia Solvignon*

Temple University

Hall A Collaboration Meeting

December 5, 2005

# Inclusive scattering



Photon virtuality:

$$Q^2 = -q^2 = 4EE' \sin^2 \frac{\theta_e}{2}$$

Invariant mass squared:

$$W^2 = M^2 + 2M\nu - Q^2$$

Bjorken variable

$$x = \frac{Q^2}{2M\nu}$$

## Unpolarized case

$$\frac{d^2\sigma}{d\Omega dE'} = \sigma_{Mott} \left[ \frac{1}{\nu} F_2(x, Q^2) + \frac{2}{M} F_1(x, Q^2) \tan^2 \frac{\theta}{2} \right]$$

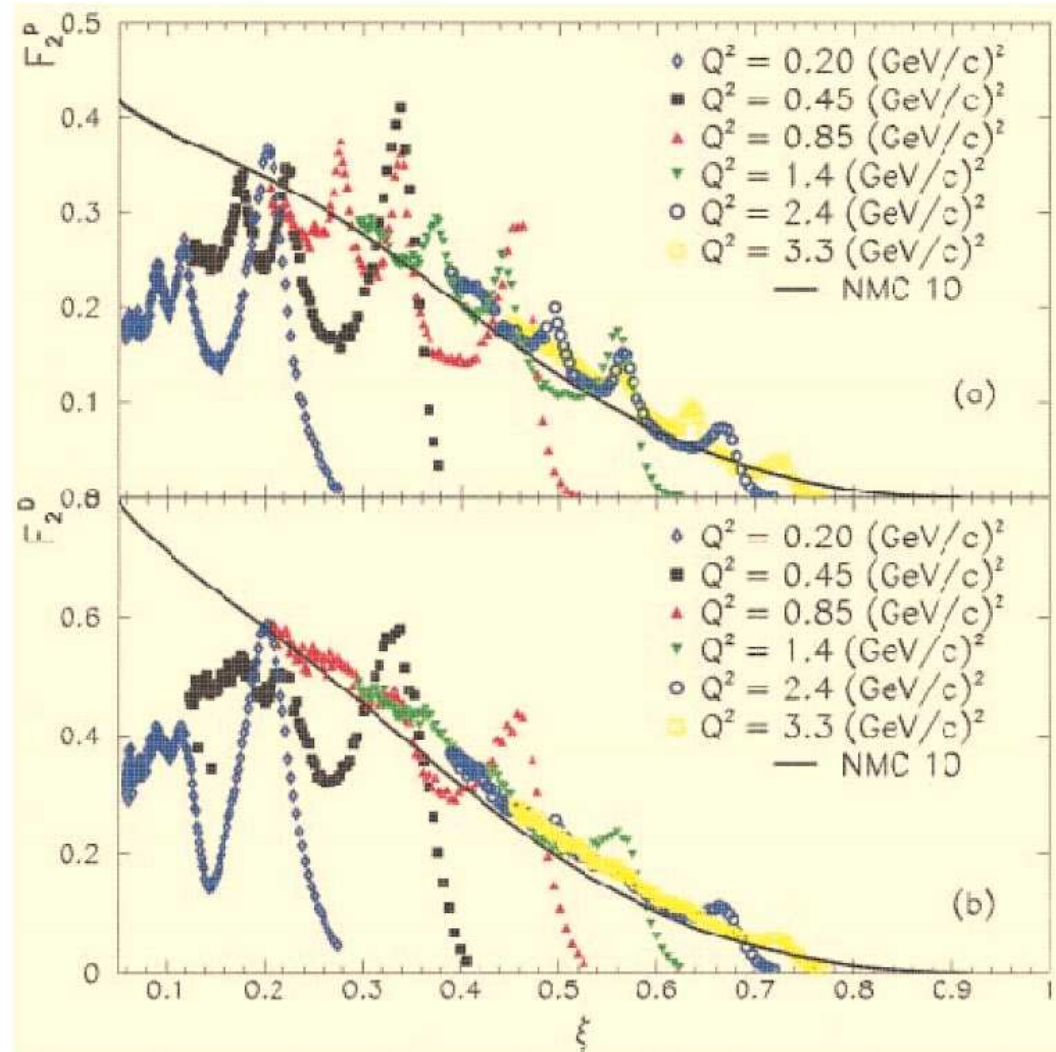
## Polarized case

$$\frac{d^2\sigma^{\uparrow\uparrow}}{d\Omega dE'} - \frac{d^2\sigma^{\uparrow\downarrow}}{d\Omega dE'} = \frac{4\alpha^2 E'}{\nu EQ^2} \left[ (E + E' \cos \theta) g_1(x, Q^2) - 2Mx g_2(x, Q^2) \right]$$

$$\frac{d^2\sigma^{\uparrow\Rightarrow}}{d\Omega dE'} - \frac{d^2\sigma^{\uparrow\Leftarrow}}{d\Omega dE'} = \frac{4\alpha^2 E'}{\nu EQ^2} \sin \theta \left[ g_1(x, Q^2) + \frac{2ME}{\nu} g_2(x, Q^2) \right]$$

# Quark-hadron duality

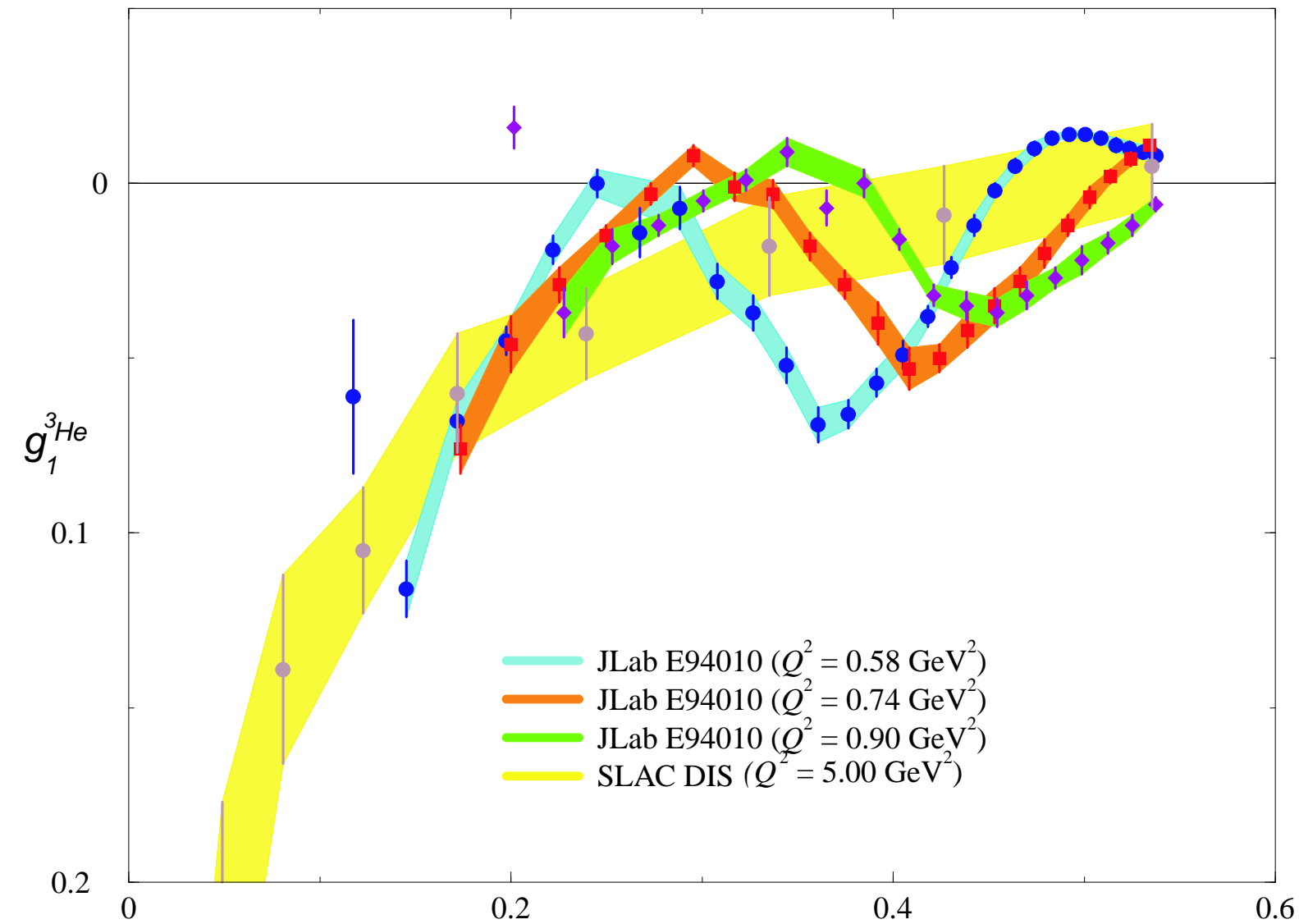
- First observed by Bloom and Gilman in the 1970's on  $F_2$
- Scaling curve seen at high  $Q^2$  is an accurate average over the resonance region at lower  $Q^2$
- Confirmed in Hall C  $\longrightarrow$
- Motivations:
  - Understand transition between quarks and hadrons



Study of higher twists

I. Niculescu et al, PRL 85 (2000) 1182

# Hint of duality



$$\xi = \frac{2x}{1 + \sqrt{1 + \frac{4M^2 x^2}{Q^2}}}$$

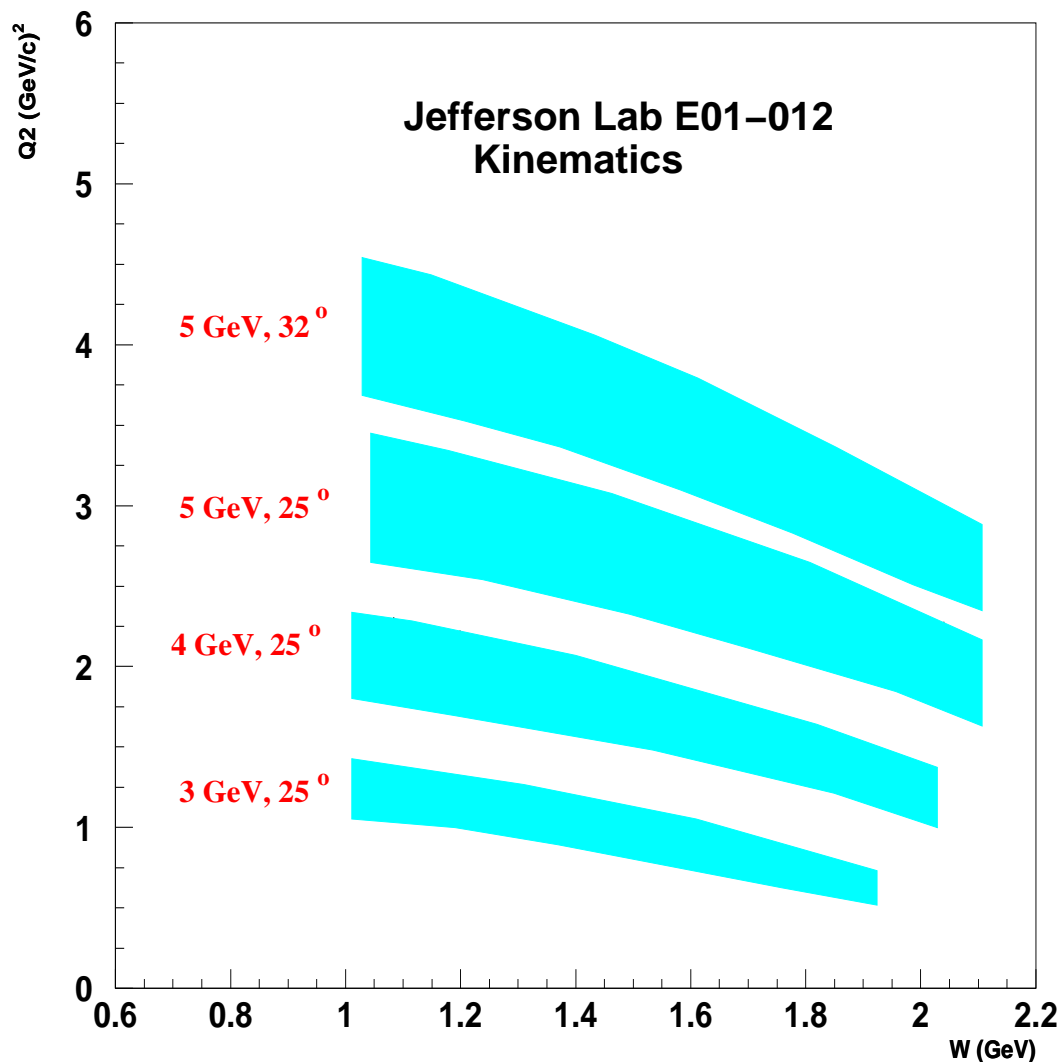
Figure from Seonho Choi

# The experiment E01-012

Spokepeople: N. Liyanage, J.-P. Chen, Seonho Choi

Graduate Student: P. Solvignon

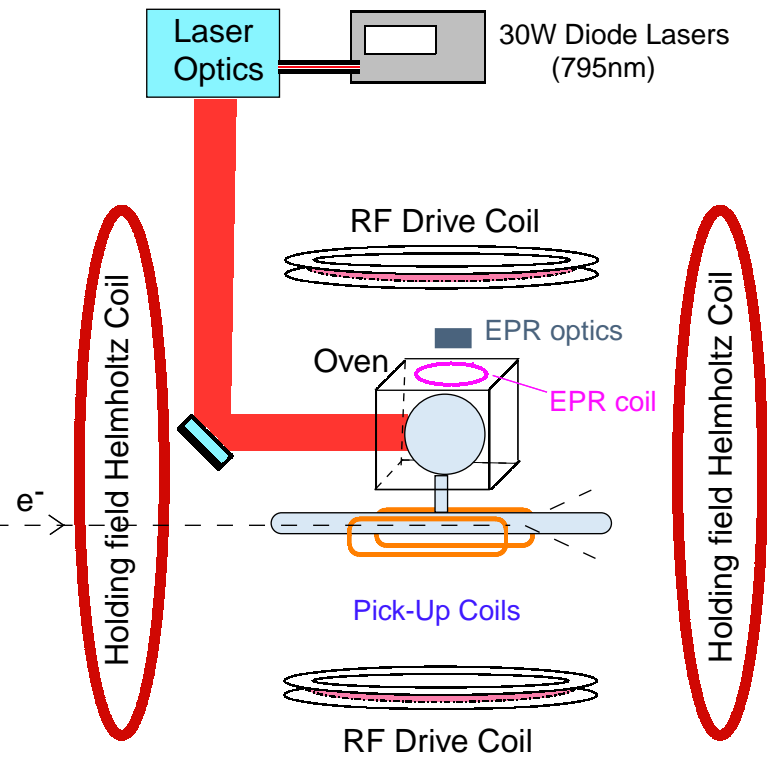
- Ran in January-February 2003
- Inclusive experiment:  ${}^3\vec{\text{H}}\text{e}(\vec{e}, e')X$
- Measured polarized cross section differences and asymmetries
- Form  $g_1$ ,  $g_2$ ,  $A_1$  and  $A_2$  for  ${}^3\text{He}$
- Test of spin duality on the neutron (and  ${}^3\text{He}$ )



# Analysis update

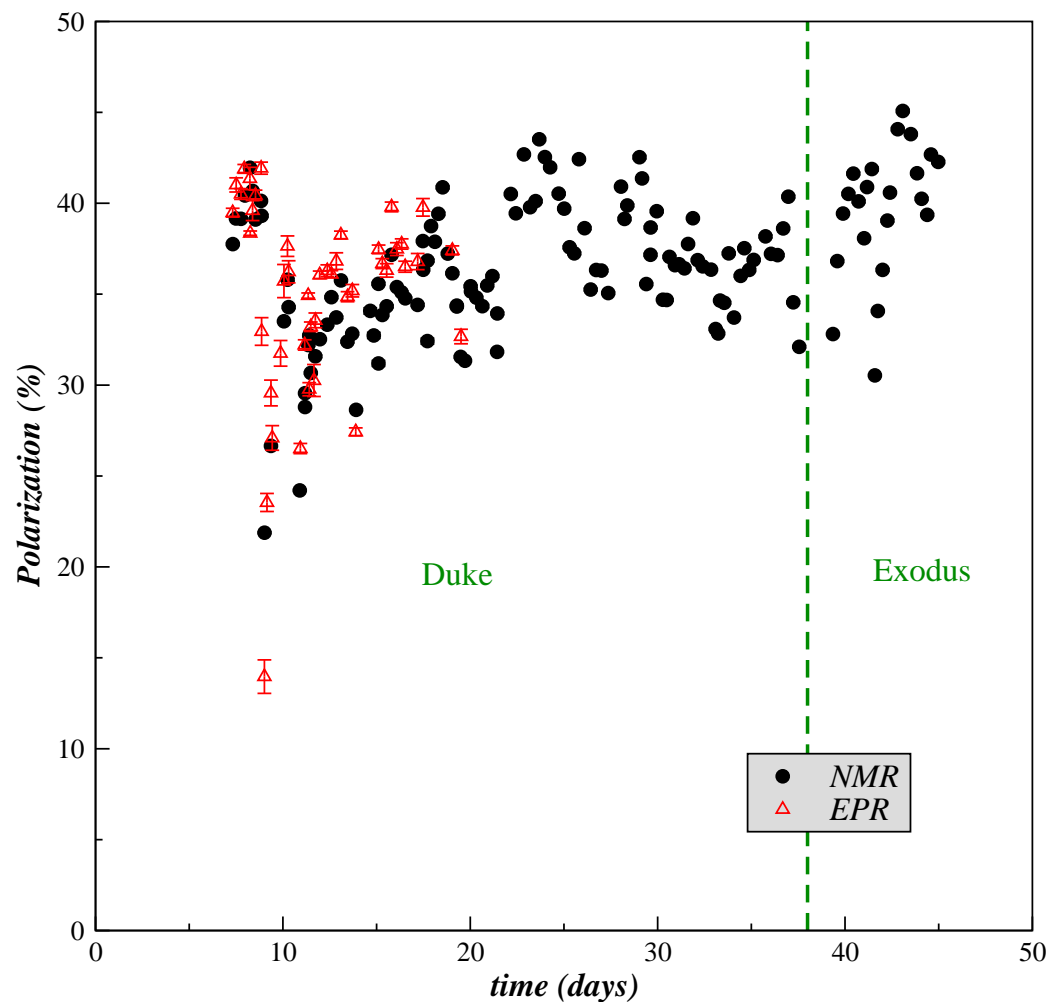
- Target polarimetry analysis in final stage (systematics).
- Detector analysis done.
- Cross sections and asymmetries near final.
- Detailed analysis of the  $N_2$  cross sections and dilution completed.
- First pass radiative corrections completed: used E94-010 data as input model.
- Preliminary results:  $g_1$ ,  $g_2$ ,  $A_1$  and  $A_2$  on  $^3\text{He}$ .
- Very preliminary results:  $\Gamma_1^n$  in the resonance region and test of global spin duality on the neutron.

# Target performance



→ 2 independent polarimetries:  
NMR and EPR

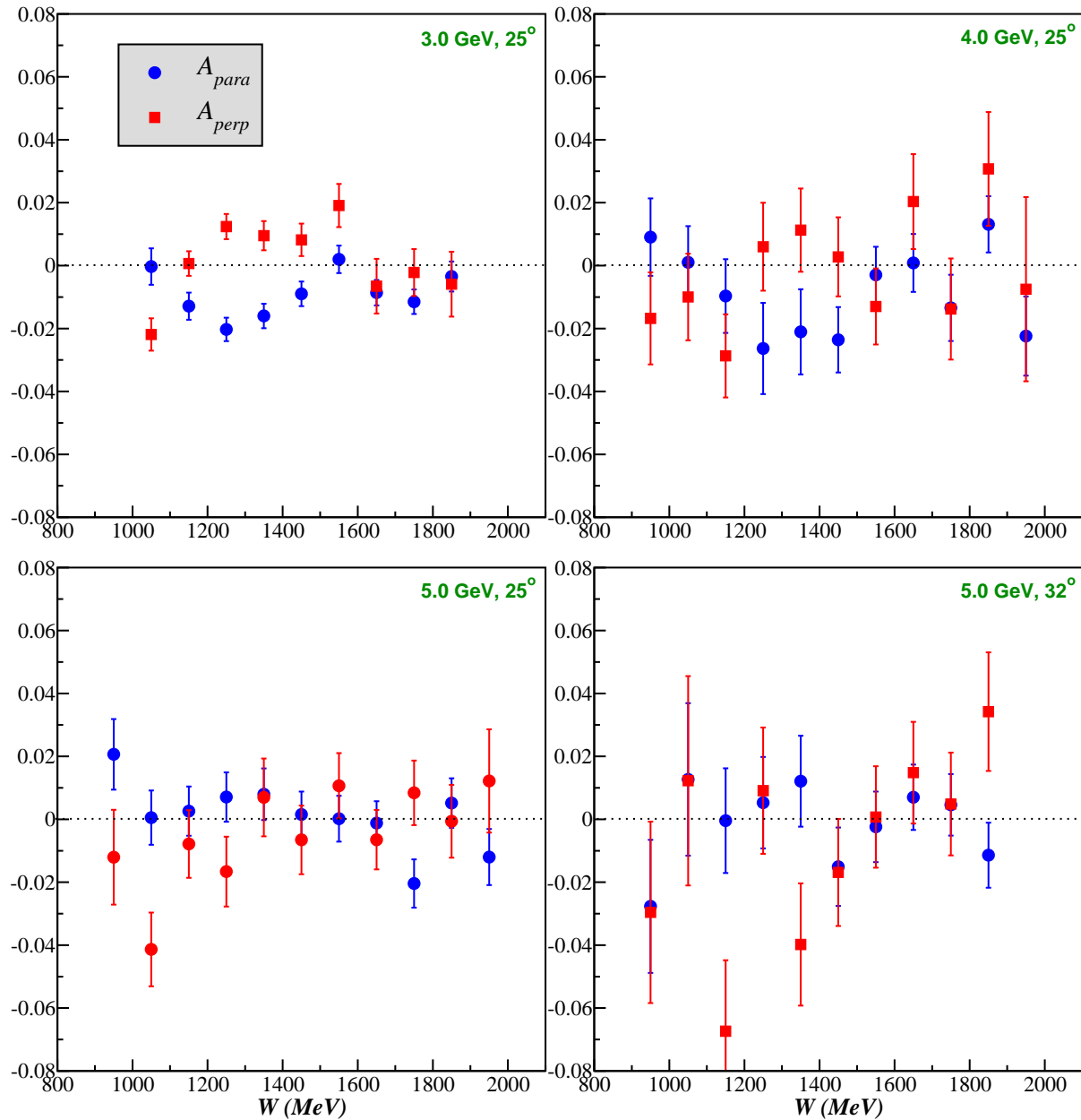
→ Longitudinal and transverse  
polarizations



NMR analysis completed (Vince Sulkosky)

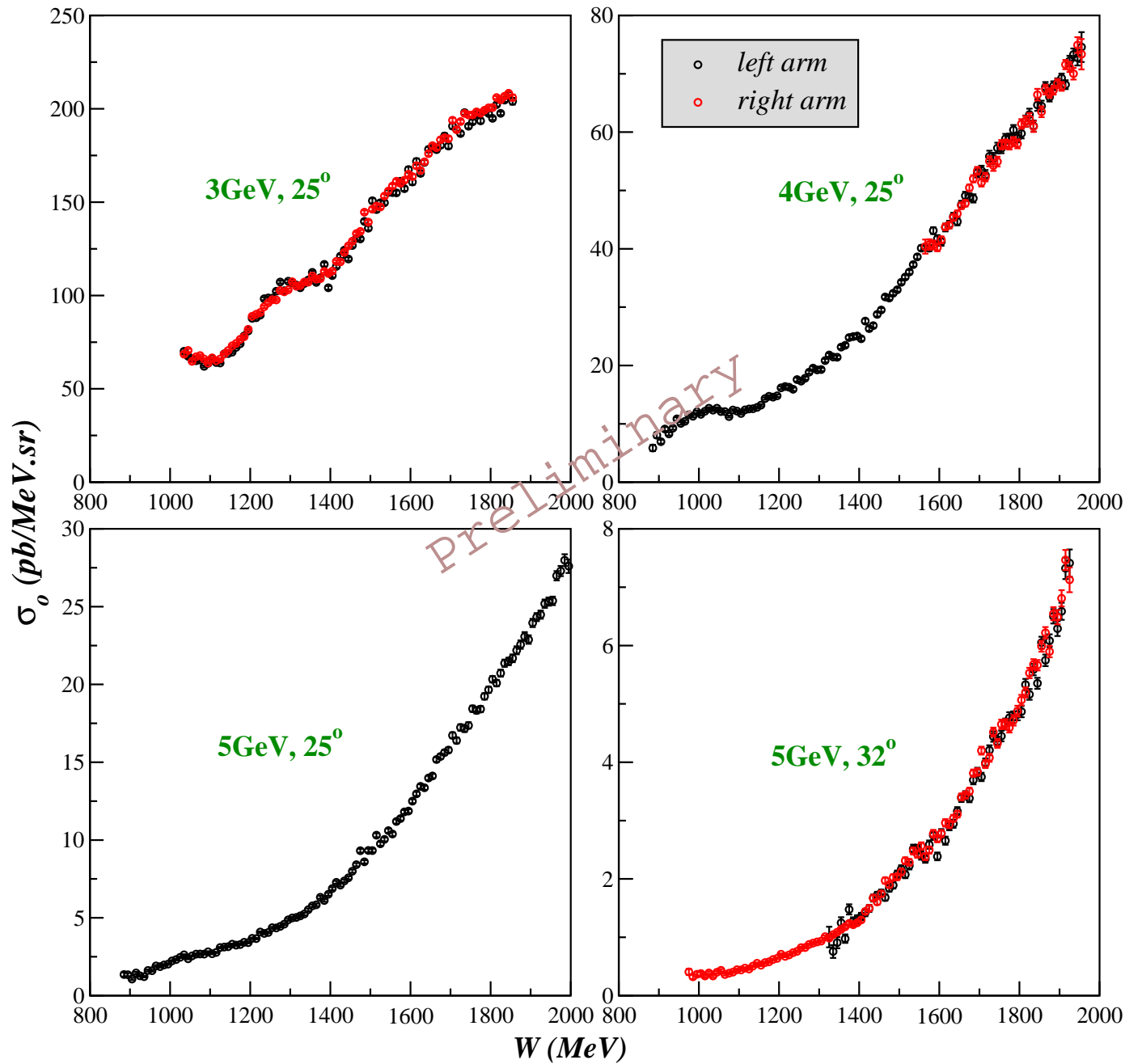
EPR analysis almost completed:  
still have to estimate the systematic error.

# Asymmetries



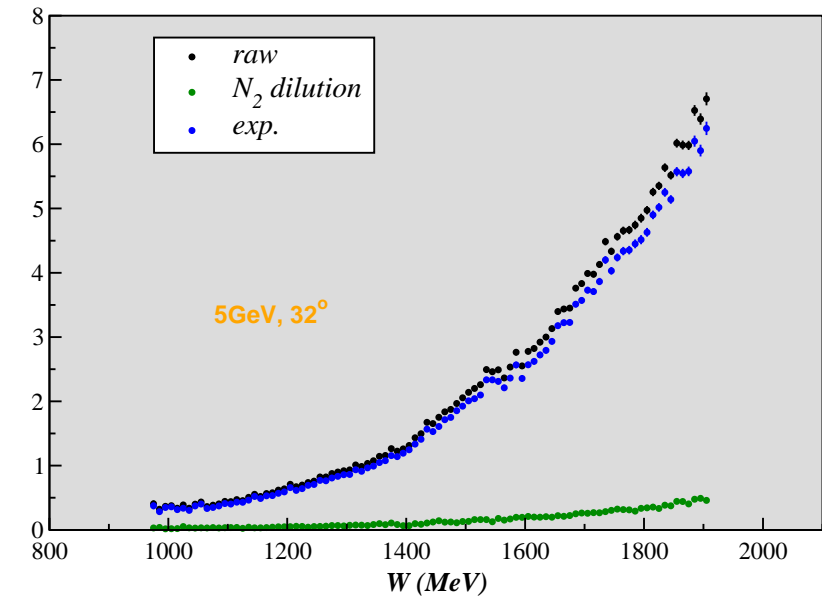
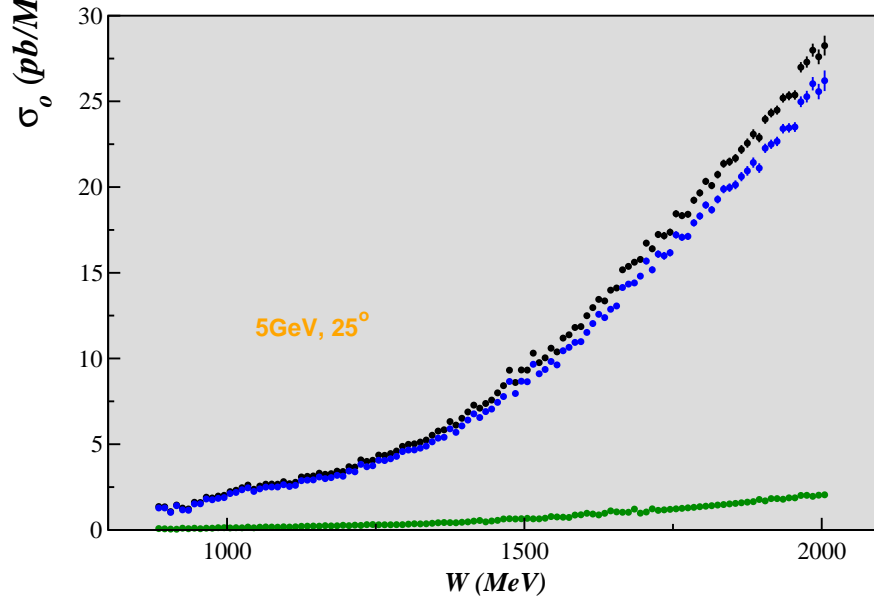
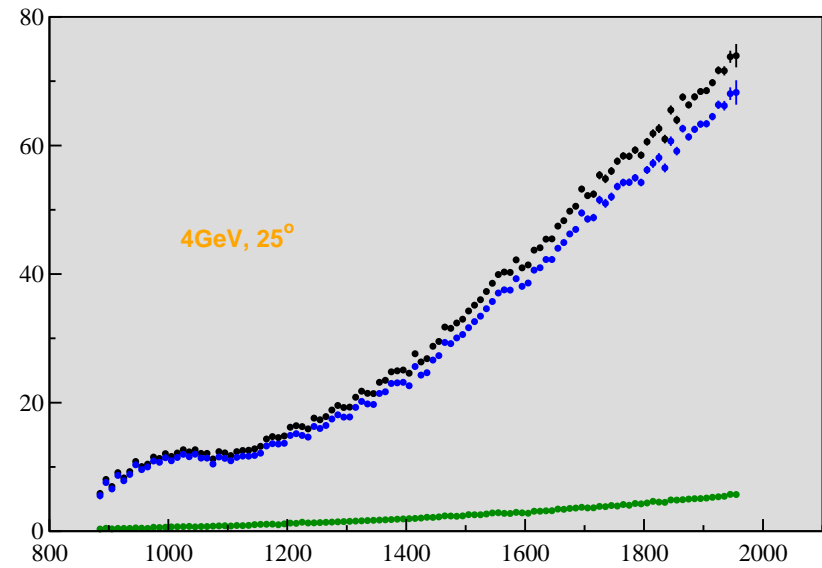
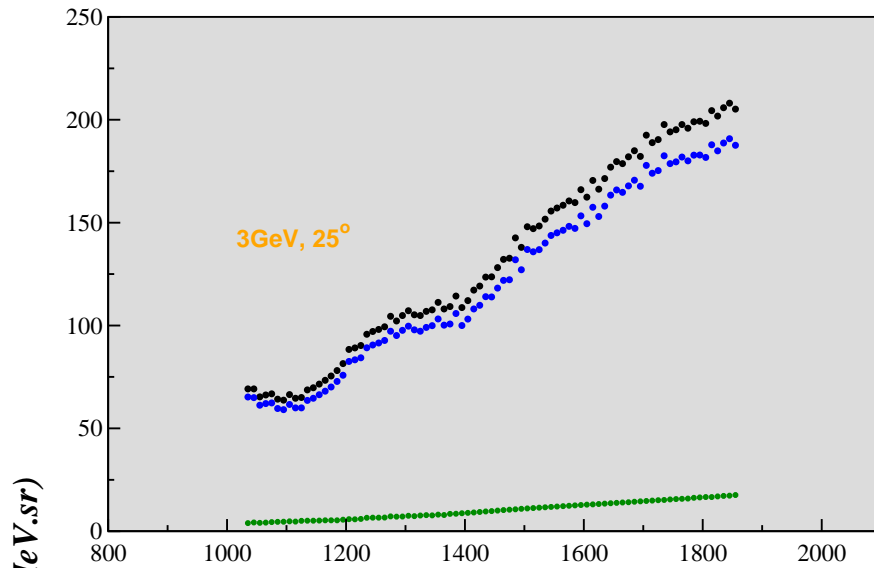


# Unpolarized cross sections



Good agreement between the two HRS.

# Nitrogen dilution



N<sub>2</sub> dilution is an 8% effect

# Spin duality on Neutron and $^3\text{He}$

→ Used method defined by N. Bianchi, A. Fantoni and S. Liuti on  $g_1^p$   
PRD 69 (2004) 014505

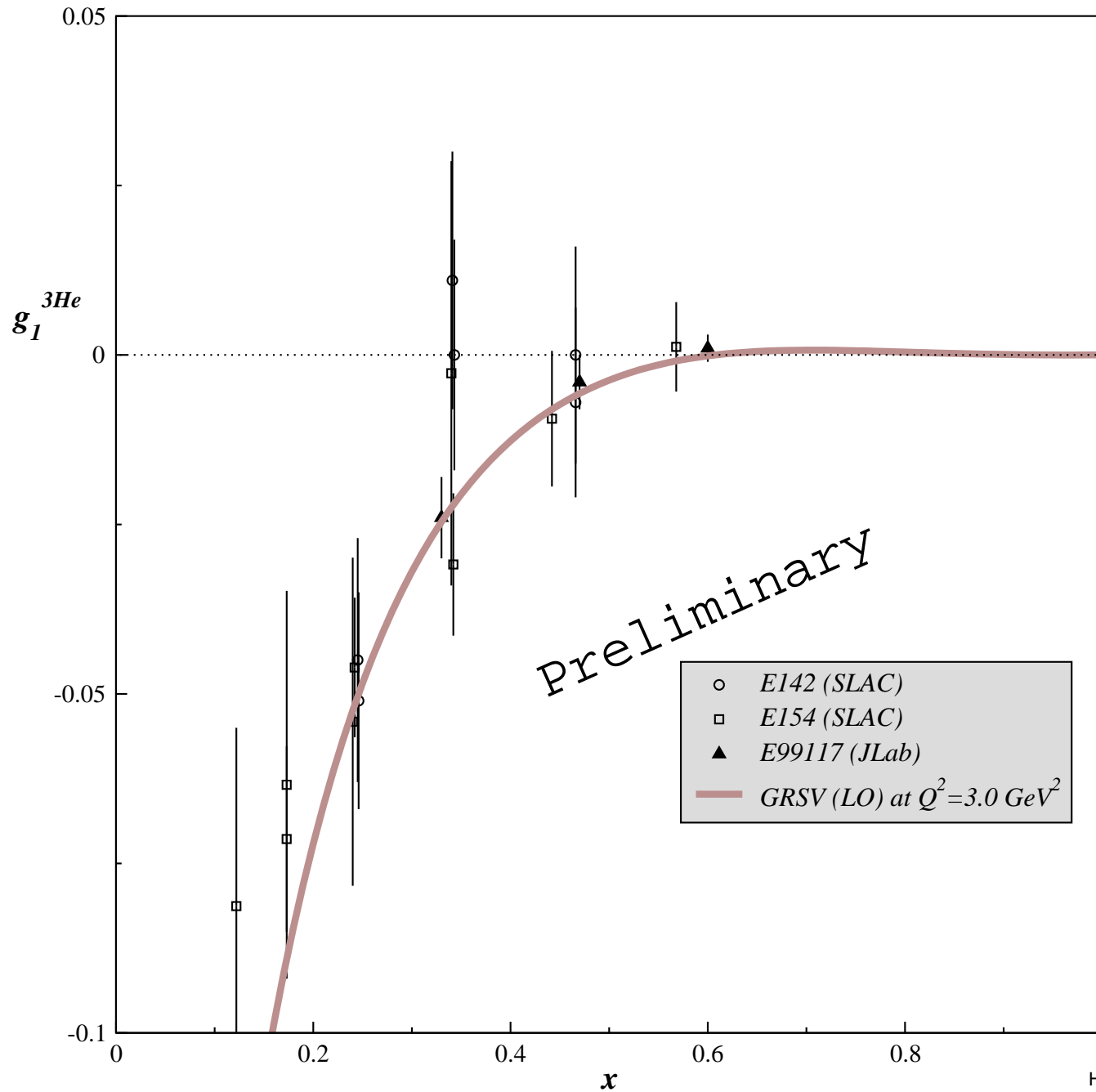
- Get  $g_1$  at constant  $Q^2$
- Define integration range in the resonance region in function of  $W$
- Integrate  $g_1^{res}$  and  $g_1^{dis}$  over the same  $x$ -range and at the same  $Q^2$

$$\tilde{\Gamma}_1^{res} = \int_{x_{min}}^{x_{max}} g_1^{res}(x, Q^2) dx \quad \text{and} \quad \tilde{\Gamma}_1^{LT} = \int_{x_{min}}^{x_{max}} g_1^{LT}(x, Q^2) dx$$

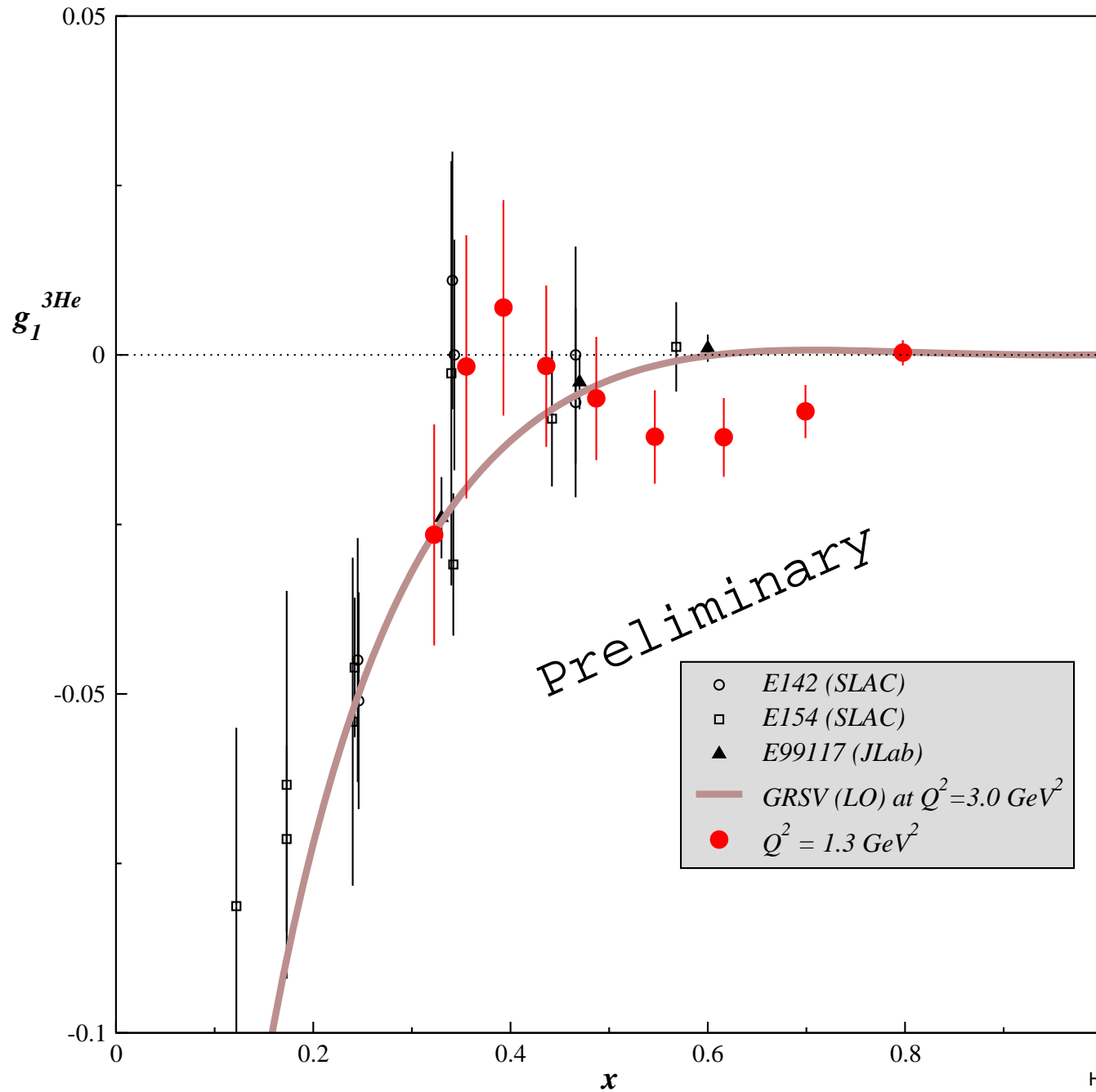
$$R^{LT} = \frac{\tilde{\Gamma}_1^{res}}{\tilde{\Gamma}_1^{LT}} \quad \text{if unity} \Rightarrow \text{duality is verified.}$$

⇒ Depending of the  $W$ -range chosen: test of global or local duality.

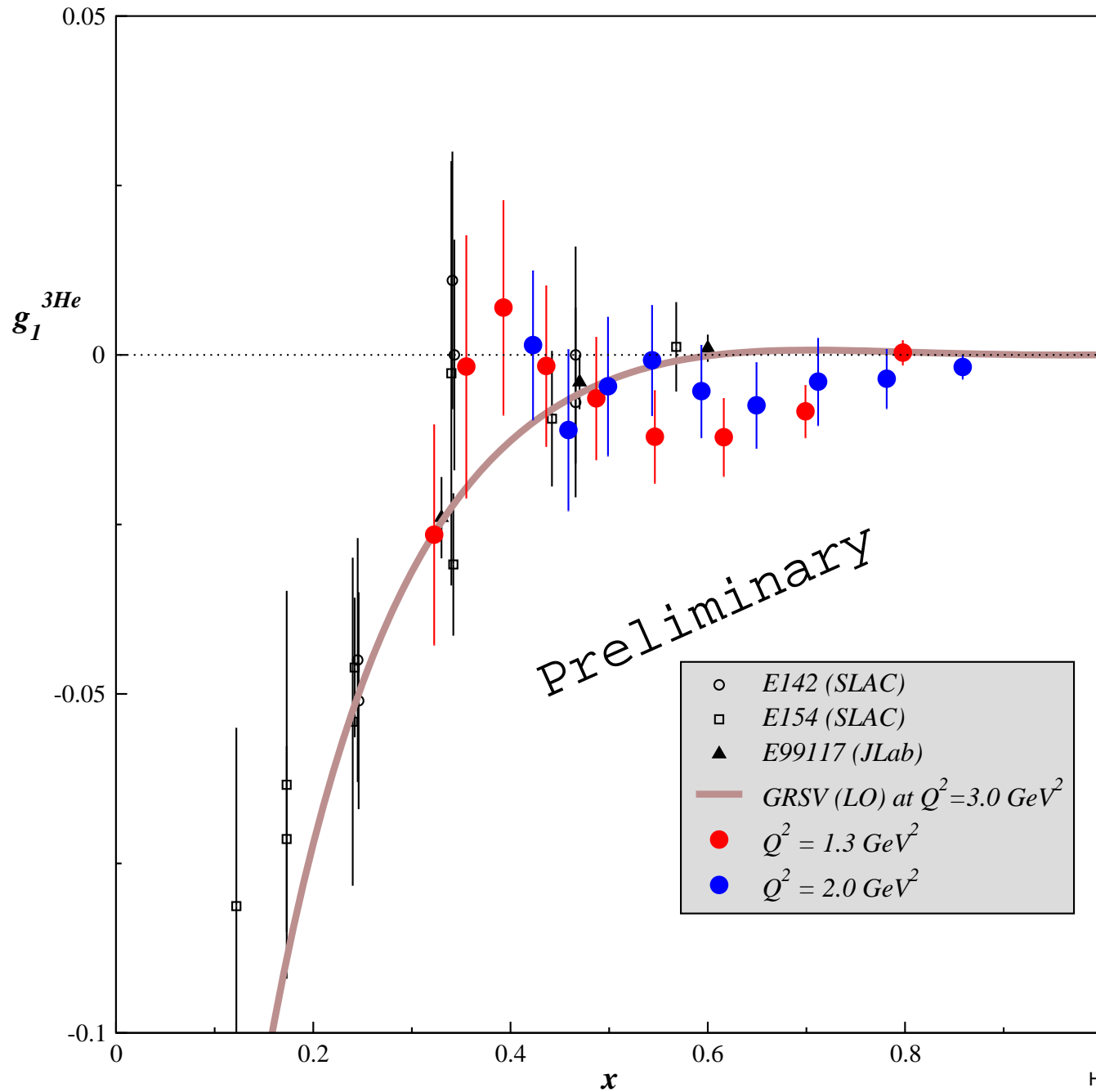
# $g_1^{3\text{He}}$ at constant $Q^2$



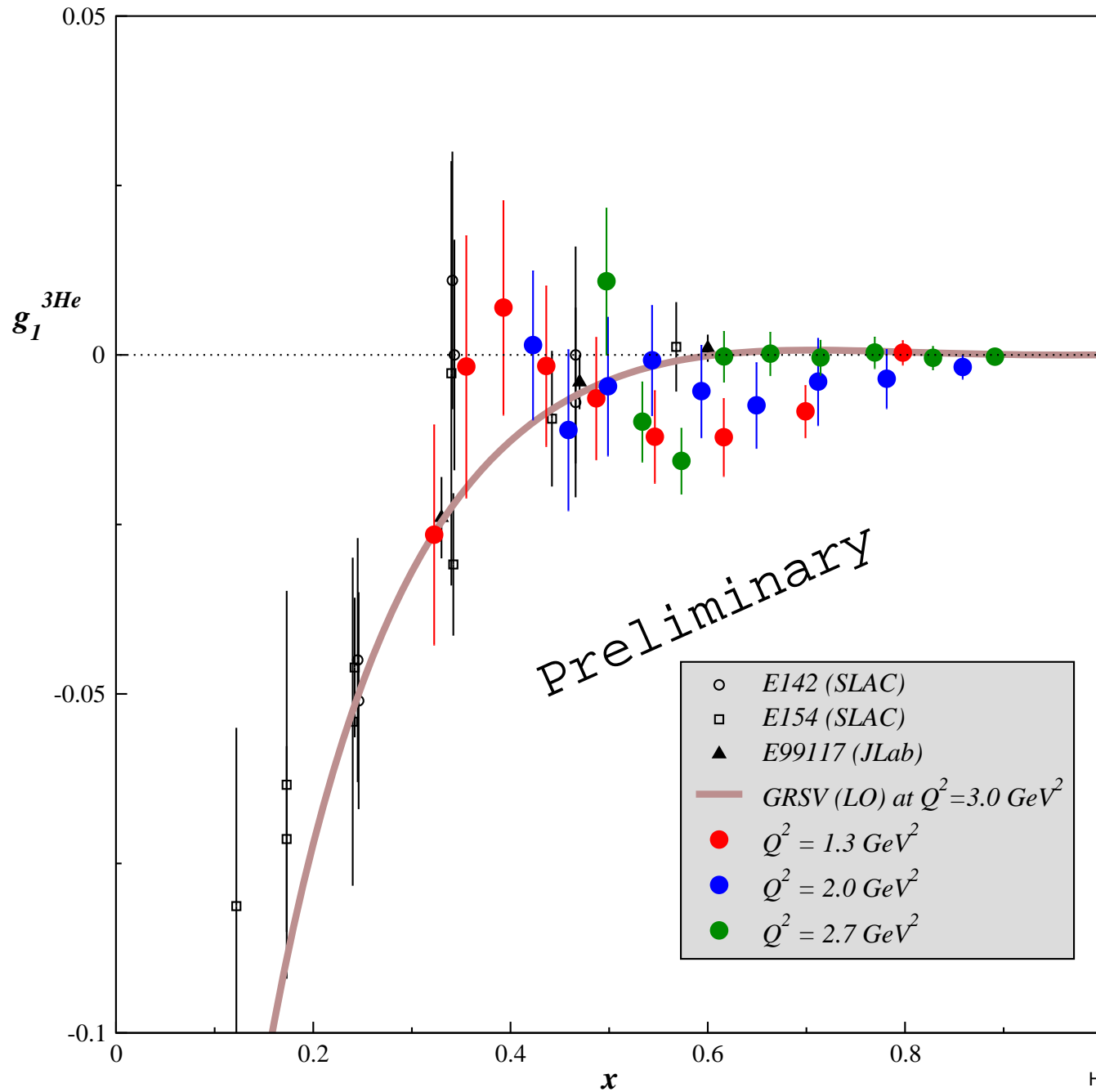
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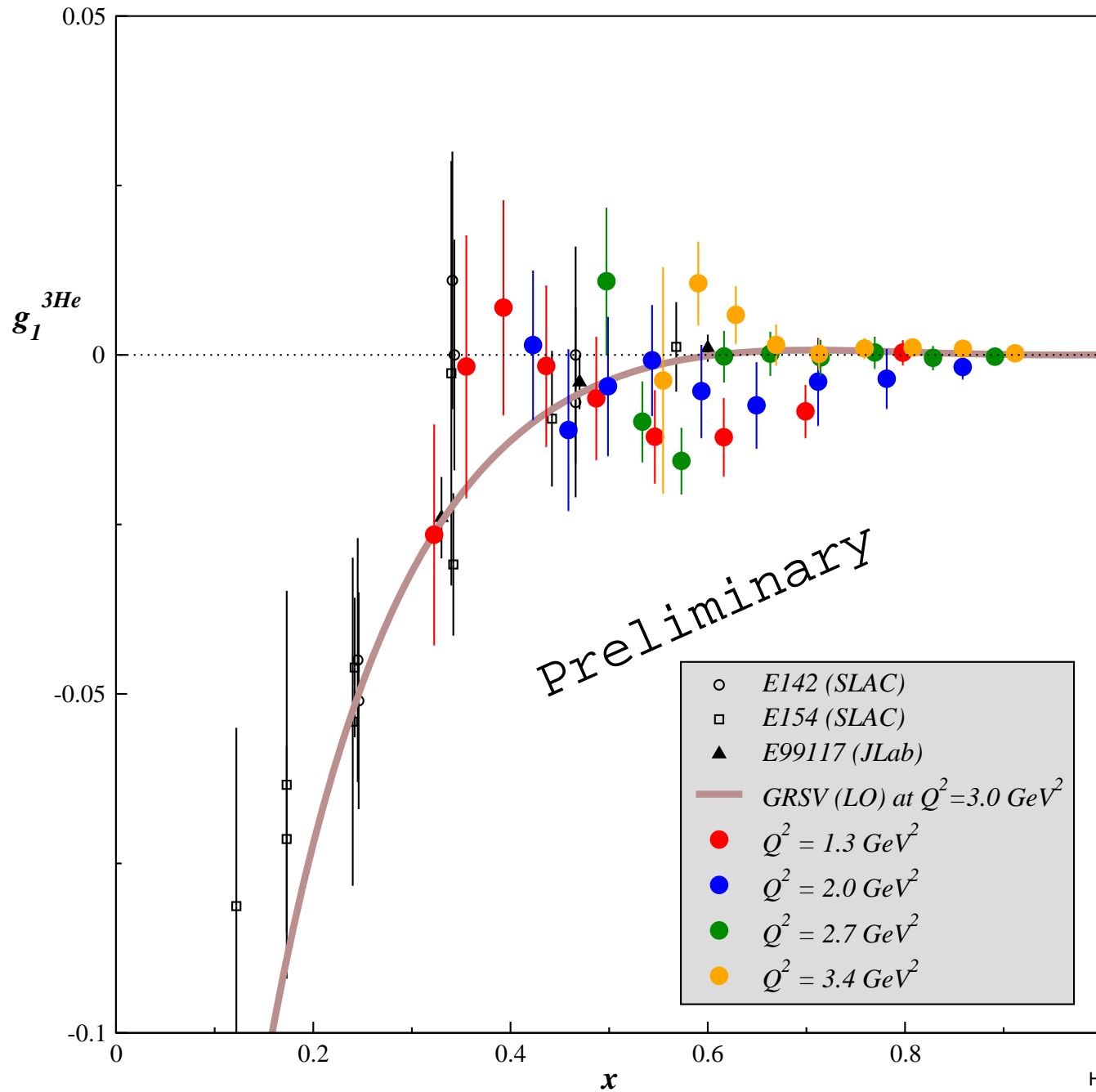
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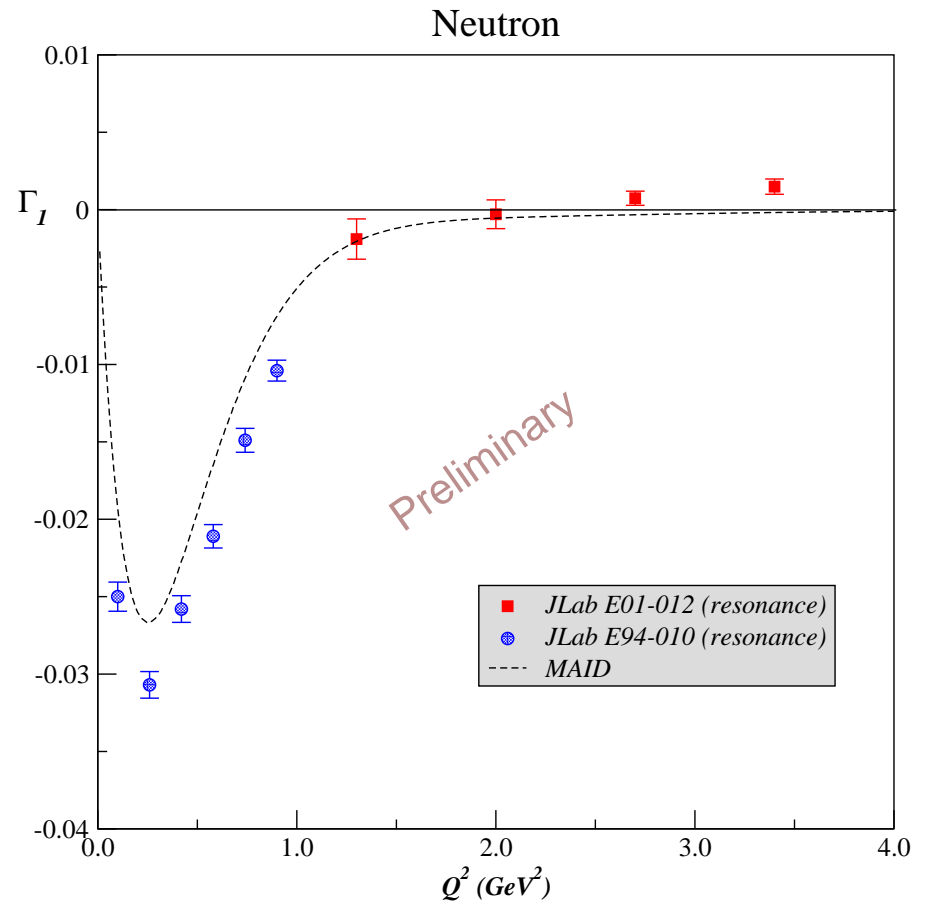
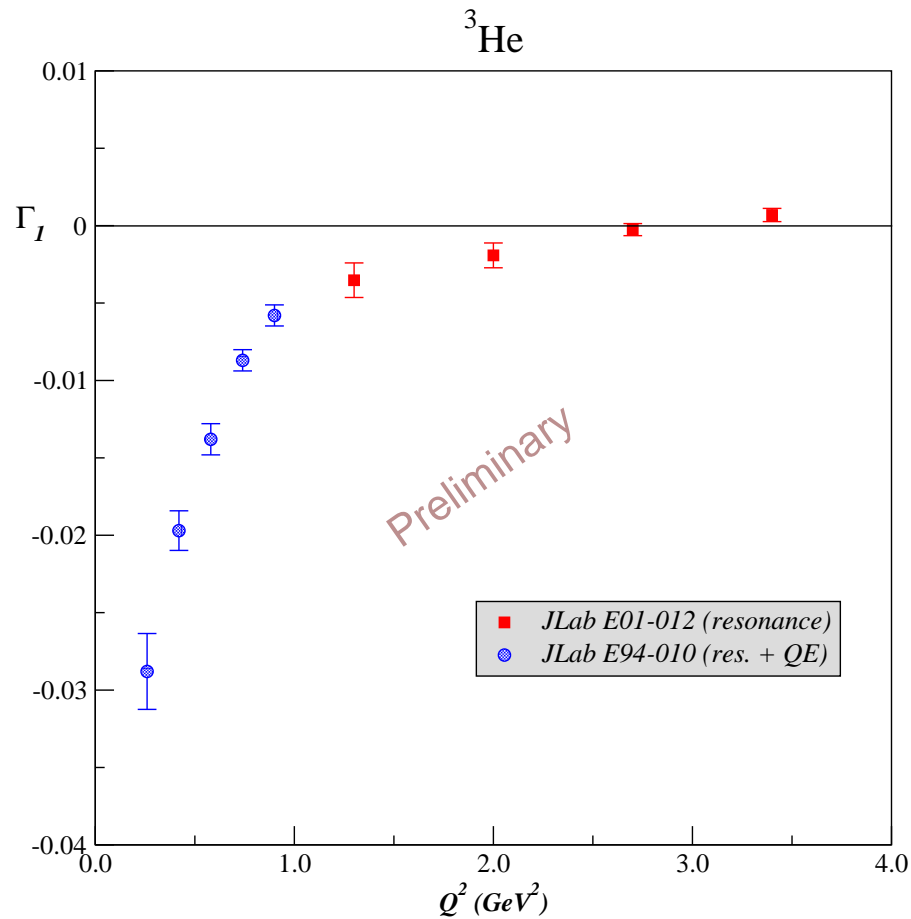


Preliminary

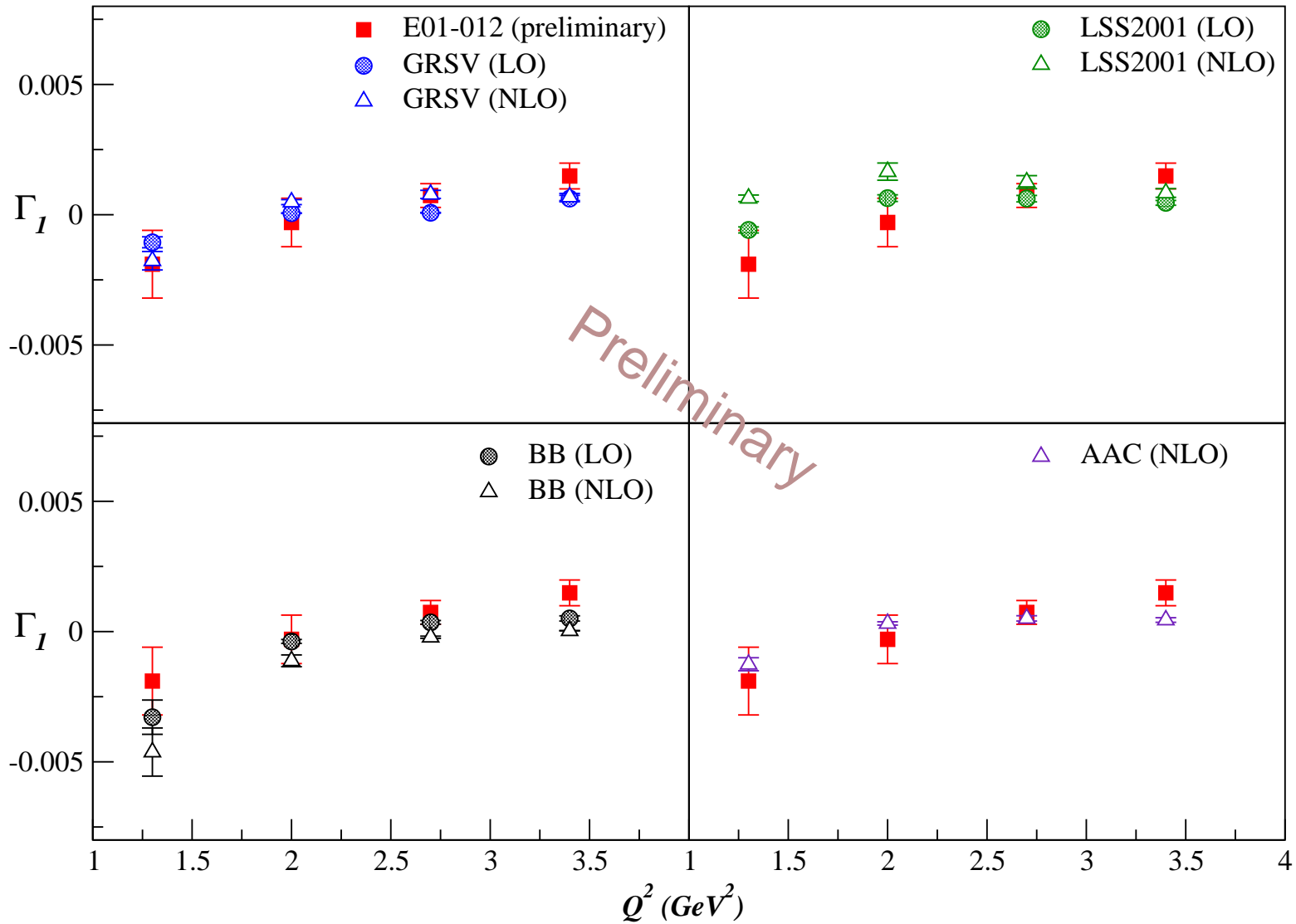


# $\Gamma_1^n$ in the resonance region

- Interpolate  $g_1^{3\text{He}}$  to constant  $Q^2$ .
- Integrate  $g_1^{3\text{He}}$  over the resonance region.
- Extract  $\tilde{\Gamma}_1^n$  from  $\tilde{\Gamma}_1^{3\text{He}} = P_n \tilde{\Gamma}_1^n + 2.0 P_p \tilde{\Gamma}_p$



# Test of duality



# Spin asymmetries

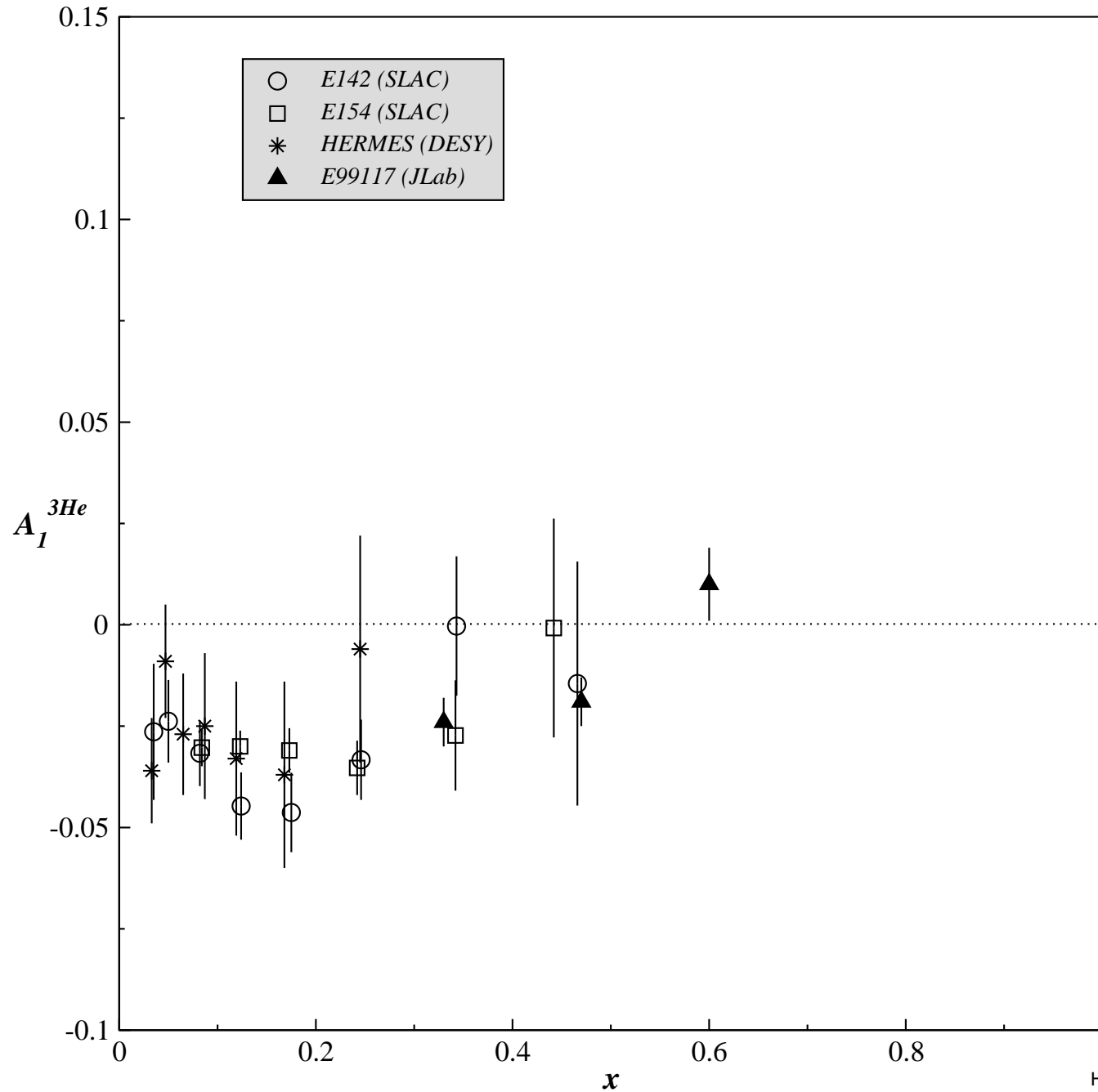
$$A_1(x, Q^2) = \frac{g_1(x, Q^2) - \gamma^2 g_2(x, Q^2)}{F_1(x, Q^2)}$$

$$A_2(x, Q^2) = \frac{\gamma [g_1(x, Q^2) + g_2(x, Q^2)]}{F_1(x, Q^2)}$$

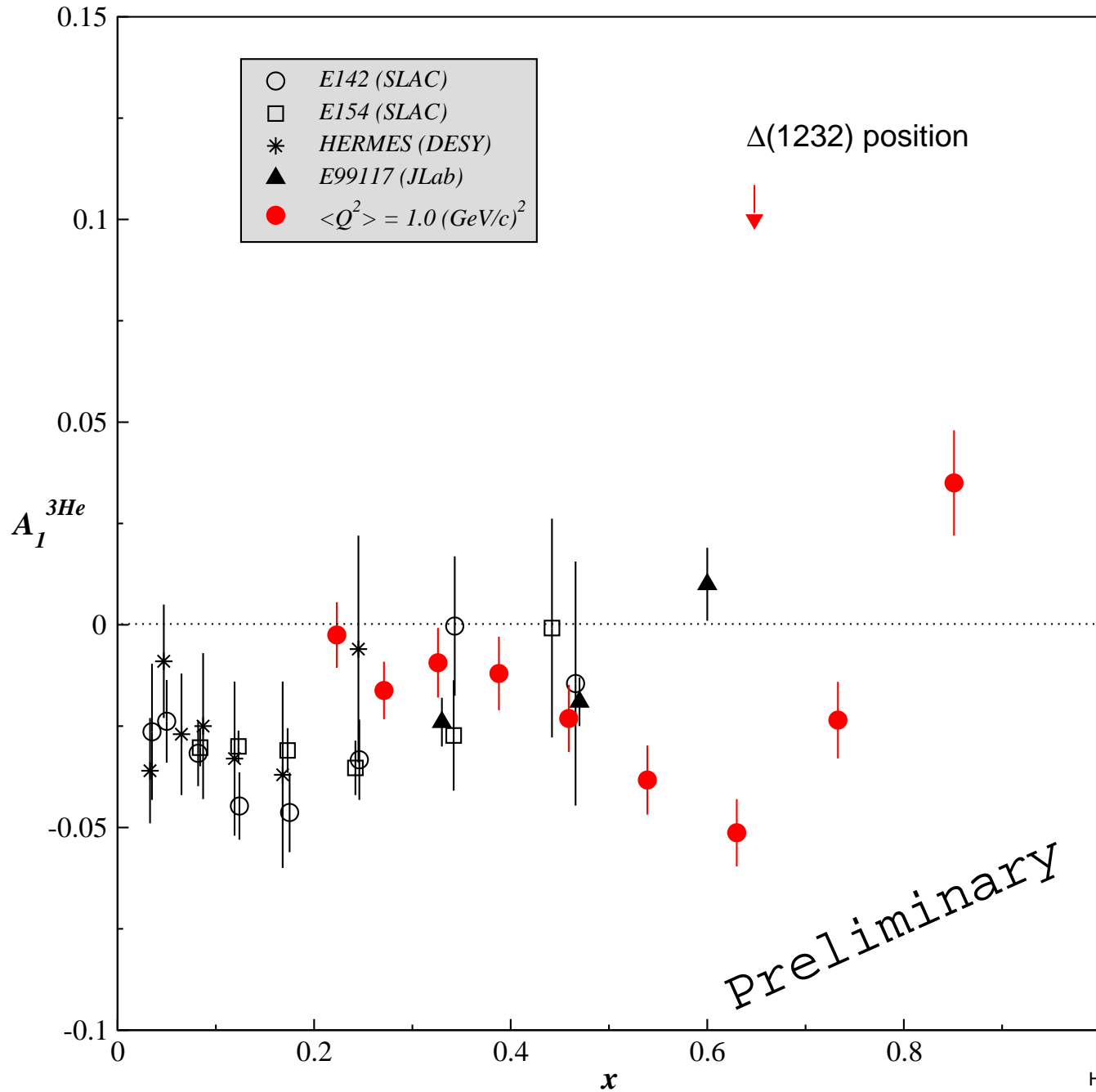
with  $\gamma^2 = \frac{Q^2}{\nu^2}$ .

Need model of  $F_1$  for  $^3\text{He}$  and neutron.

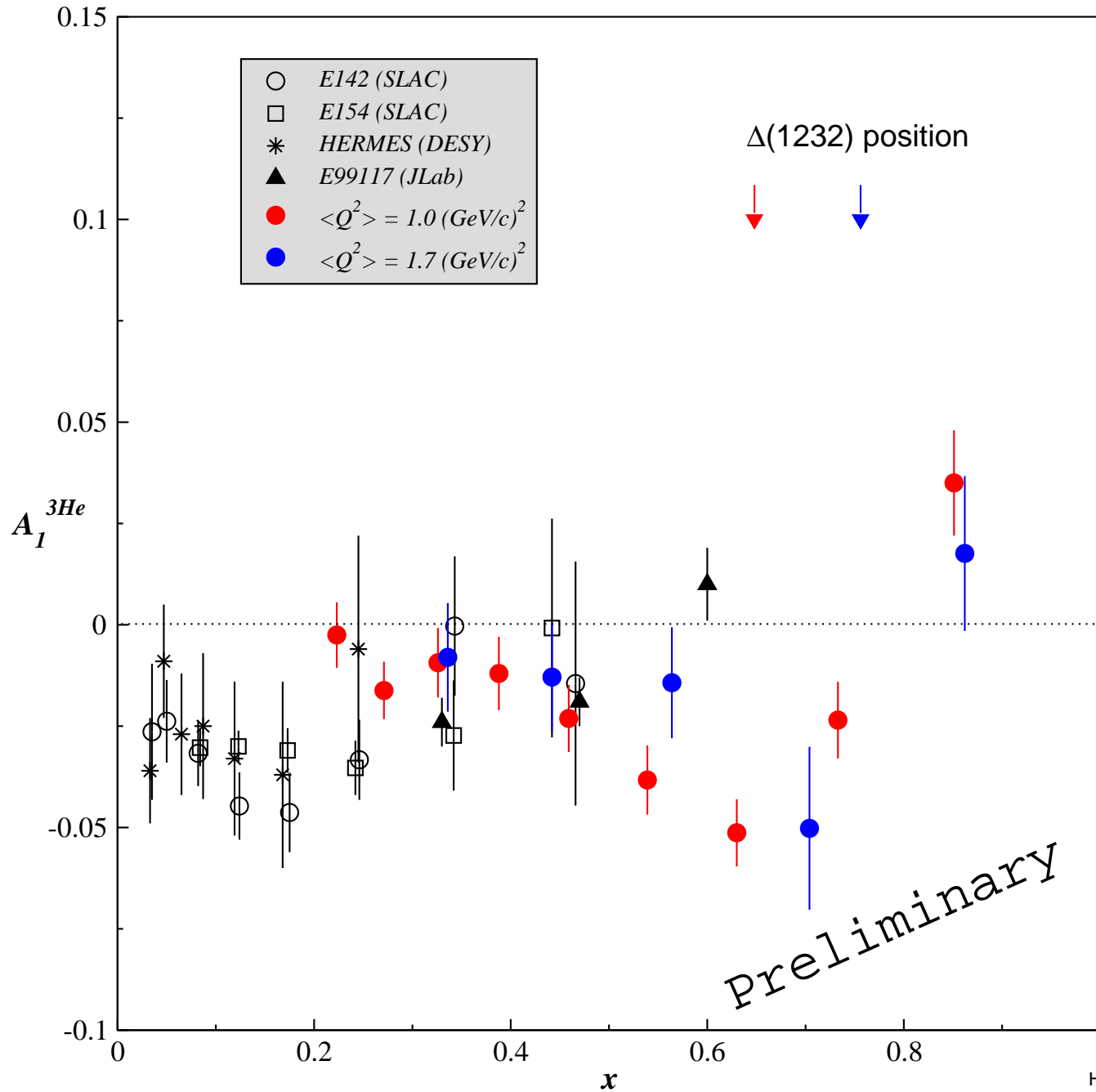
# Spin asymmetry $A_1$



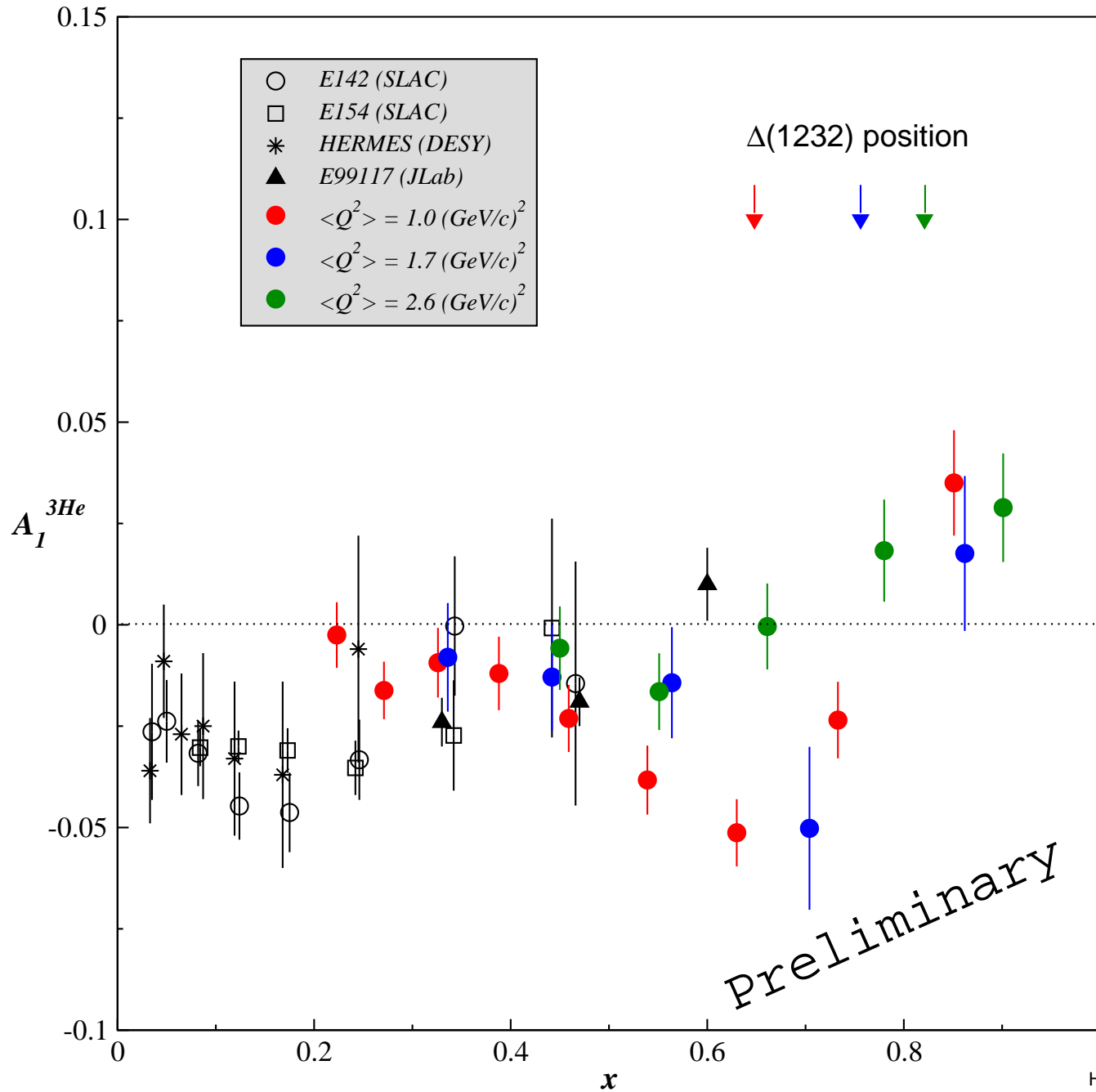
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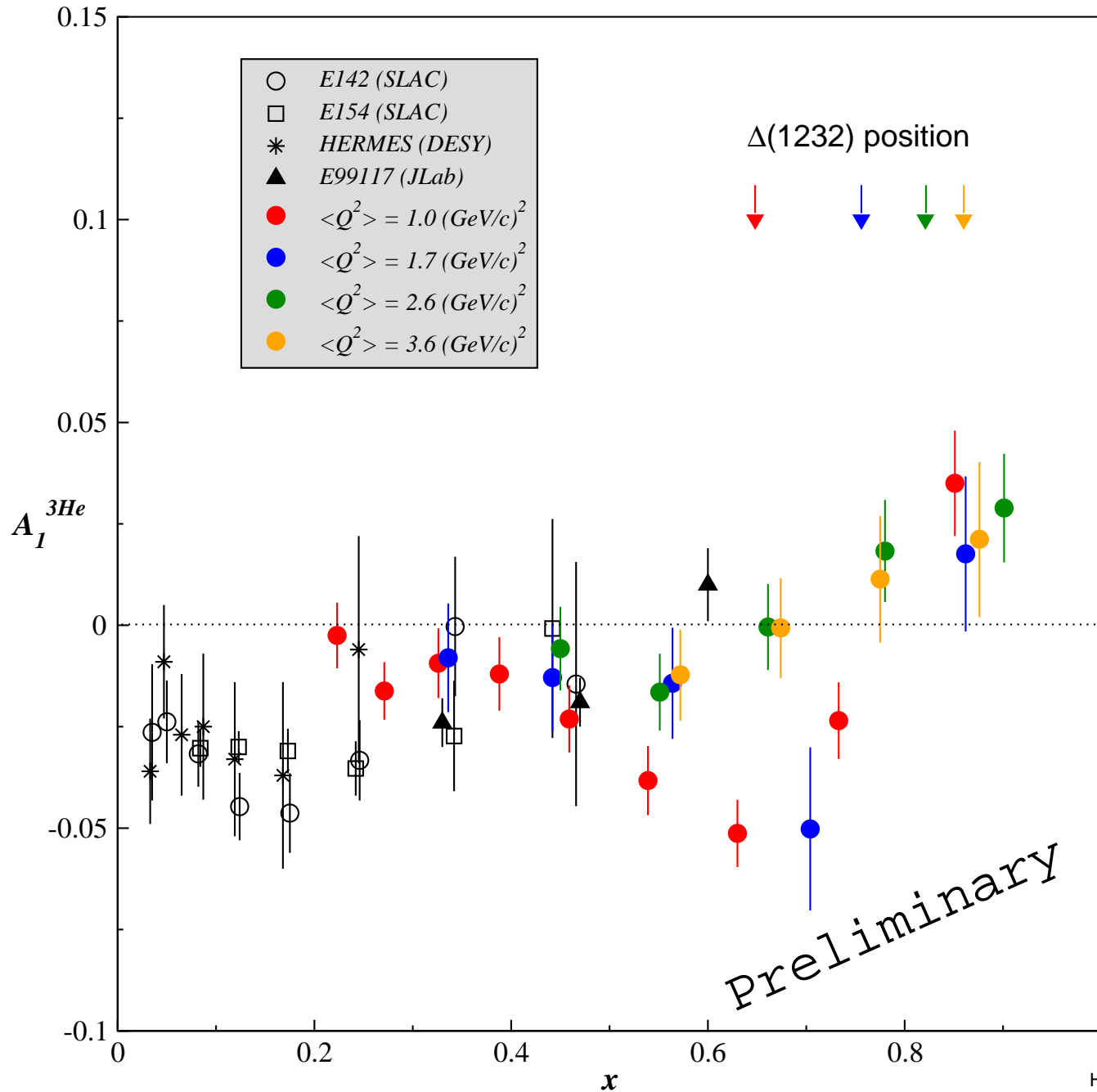
# Spin asymmetry $A_1$



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# Spin asymmetry $A_1$





# *Still to do*

- Finalize radiative corrections
- Neutron spin structure functions extraction from convolution approach
- Test of global and local spin duality on neutron and  $^3\text{He}$
- Extract moments of structure functions.
- Systematics errors