

... for a brighter future

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New Results on the

³He and Deuteron

Resonance Spin Structure of



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Outline

- Srief introduction and motivations
- Experimental setups
- Results
 - > Sum rules
 - > Spin Duality
 - > Structure function g_2
 - > Virtual photon asymmetry A₁



Motivations

✦ Access to neutron spin structure functions

✦ Sum rules work for nuclei even when extra disintegration channels and nuclear excitation are added

- ✦ Test of sum rules without worrying of nuclear corrections
- ✦ Light nuclei measurements important to test EFT

True understanding of QCD means being able to describe nucleon and nuclei in terms of fundamental degrees of freedom



Implementations of QCD

Due to complexity of QCD we often employ approximations or effective theories



Inclusive electron scattering

 $e' = (E', \overline{k}')$

 $q = (v, \vec{q})$

<u>4-momentum transfer squared</u> $Q^2 = -q^2 = 4 EE' \sin^2 \frac{\theta}{2}$

Invariant mass squared

 $W^2 = M^2 + 2M\nu - Q^2$

 $\frac{\text{Bjorken variable}}{x = \frac{Q^2}{2M\nu}}$



e = (E, k)

 $p = (M, \vec{0})$

 $\frac{d^{2}\sigma^{\uparrow\uparrow}}{d\Omega dE'} - \frac{d^{2}\sigma^{\downarrow\uparrow}}{d\Omega dE'} = \frac{4\alpha^{2}E'}{vEQ^{2}} \Big[\Big(E + E'\cos\theta\Big)g_{1}(x,Q^{2}\Big) - 2Mxg_{2}g_{2}(x,Q^{2}) - 2Mxg_{2}(x,Q^{2}) - 2Mxg_{2}(x,Q^{2$ $-2Mxg_2(x,Q^2)$

W



GDH Sum Rule and extention to finite Q²





GDH Sum Rule and extention to finite Q²

Real Photon Scattering

$$\int_{\nu_0}^{\infty} \left(\sigma_{1/2} - \sigma_{3/2} \right) \frac{d\nu}{\nu} = -\frac{2\alpha\pi^2}{M^2} \kappa^2$$



Extension to finite Q²

$$S_1(0,Q^2) = \frac{8}{Q^2} \int_0^1 g_1(x,Q^2) dx$$

Ji and Osborne, J. Phys. <u>G27</u> (2001) 127

S₁ calculable (in principal)

Reduces to GDH sum rule as $Q^2 \rightarrow 0$





The g₂ structure function

Wandzura-Wilczek relation

PLB <u>72</u> (1977) 195

$$g_2^{WW}(x,Q^2) = -g_1(x,Q^2) + \int_x^1 \frac{g_1(y,Q^2)}{y} dy$$

Leading twist determined entirely by g₁

$$g_2 = g_2^{WW} + \overline{g_2}$$
 Higher twist



Burkhardt-Cottingham Sum rule

 $\int_{0}^{1} g_2(x, Q^2) dx = 0$

H.Burkhardt, and W.N. Cottingham Annals Phys. 56 (1970) 453.

Relies on the virtual Compton scattering amplitude S₂ falling to zero faster than 1/v as $v \rightarrow \infty$



Overview of available kinematic range at Jlab

Deuteron: Hall B Eg1b 6 CLAS Hall C RSS RSS E97-110 • Hall B Eg4 E94-010 5 E01-012 E99-117 E97-103 $Q^{2} (GeV^{2})$ **↔** ³He • Hall A E94-010 2 • Hall A E01-012 • Hall A E97-110 1 0.2 0.6 0.8 0.4 x

Uniquely positioned to provide data in transition region of QCD



Jlab Hall A: E94-010















g₁ and g₂ <u>Primary goal:</u> spin duality











³He: low Q² Structure functions and sum rules Hall A





Deuterium: Structure function g_1^d (per nucleon) Hall B





Deuterium: first moment



Hall B

Y. Prok et al., arXiv:0802.2232 (submitted to PRL)

Observation of turn over at low Q² as expected from GDH slope



Quark-hadron duality

First observed by Bloom and Gilman in the 1970's on F_2 :

Scaling curve seen at high Q^2 is an accurate average over the resonance region at lower Q^2

In nuclei, the averaging is in part done by the Fermi motion. J. Arrington, et al., PRC73:035205 (2006)





Spin Duality

Bianchi, Fantoni and Liuti, PRD 69 014505 (2004)

- 1) Determine g_1^{res} at constant Q^2
- 2) Integrate over region of interest (local or global)
- 3) Compare to DIS result evolved to same Q²

$$\Gamma_1^{res}(Q^2) \equiv \int_{x\min}^{x\max} g_1^{res} dx \qquad \Gamma_1^{dis}(Q^2) \equiv \int_{x\min}^{x\max} g_1^{dis} dx$$

$$\Gamma_1^{res}(Q^2) = \Gamma_1^{dis}(Q^2) \Rightarrow Duality$$





Hall A

P. Solvignon et al., arXiv:0803.3845 (submitted to PRL)



Target mass corrections were applied on PDFs





Hall A P. Solvignon et al., arXiv:0803.3845





Target mass corrections were applied on PDFs







Spin duality on ³He

Hall A



Hall B

Spin Duality on deuterium



P. Bosted et al., PRC75 (2007) 035203







Hall C

Spin Duality on deuterium





Structure function g_2^{3He} at moderate Q^2



Early observation: above Q²≈ 1.8 GeV², qualitative good agreement in average with models

Comparison with g_2^{WW} will give an estimate of the size of the HT effects



Structure function g₂^d at moderate Q²



Early observation: qualitative good agreement in average with models



Virtual photon-nucleon asymmetry

$$A_{1}(x,Q^{2}) = \frac{g_{1}(x,Q^{2}) - \gamma^{2}g_{2}(x,Q^{2})}{F_{1}(x,Q^{2})} \quad \text{with} \quad \gamma^{2} = \frac{4M^{2}x^{2}}{Q^{2}}$$

In the parton model:

$$A_1 = \frac{g_1}{F_1}$$

If Q^2 dependence similar for g_1 and for $F_1 \Rightarrow$ weak Q^2 dependence of A_1





Hall A





A_1 for ³He



Hall A

P. Solvignon et al., arXiv:0803.3845 (submitted to PRL)

Large negative value in the $\Delta(1232)$ region



A_1 for ³He



Hall A

P. Solvignon et al., arXiv:0803.3845 (submitted to PRL)

Large negative value in the $\Delta(1232)$ region

Still large negative value in the $\Delta(1232)$ region



A_1 for ³He



Hall A

P. Solvignon et al., arXiv:0803.3845 (submitted to PRL)

Large negative value in the $\Delta(1232)$ region

Still large negative value in the $\Delta(1232)$ region

A₁ becomes positive in the Δ (1232) region due to the drop in the Δ FF and the rising of the DIS background



A₁ for ³He



Hall A

P. Solvignon et al., arXiv:0803.3845 (submitted to PRL)

Large negative value in the $\Delta(1232)$ region

Still large negative value in the $\Delta(1232)$ region

A₁ becomes positive in the Δ (1232) region due to the drop in the Δ FF and the rising of the DIS background

No strong Q²-dependence is now observed



A₁ for deuteron

Hall B



High W resonance data are in good agreement with the DIS data



A₁ for deuteron

Hall C



Good agreement between resonance and DIS data for W above the $\Delta(1232)$ region



Argonr







NALLABORATOR

Hall A

JLab Hall B: EG4

 $E_0 = 1.3, 2.0 \text{ GeV}$





JLab Hall B: EG4





Summary

Rich study of ³He spin structure in the resonance region for 0.04<Q²<4.0 GeV²

- Precision test of the extended GDH and BC sum rules
- \checkmark Observation of spin duality for Q² down to at least 1.8GeV²
- \checkmark A₁ shows no strong Q²-dependence above Q² \approx 2.0GeV²

Same coverage for the study of deuterium spin structure in the resonance region, except for the lack of coverage for the perpendicular data:

- \checkmark First moment of g_1 shows the turn over required by the GDH slope
- \checkmark Observation of spin duality for Q² down to at least 1.5GeV²
- \checkmark A₁ shows same trend as DIS data for W above the Δ (1232) region

All these results have the advantage to be free from nuclear corrections

