

# Study of Dimensional Scaling in Two- Body Photodisintegration of $^3\text{He}$

Yordanka Ilieva  
CLAS Collaboration

2011 Fall Meeting of the APS Division on Nuclear Physics Meeting  
Michigan State University  
October 26 - 29, 2011  
East Lansing, Michigan

# Dimensional Scaling Laws in Nuclear Physics

Brodsky, Farrar (1973): from dimensional analysis and perturbative QCD

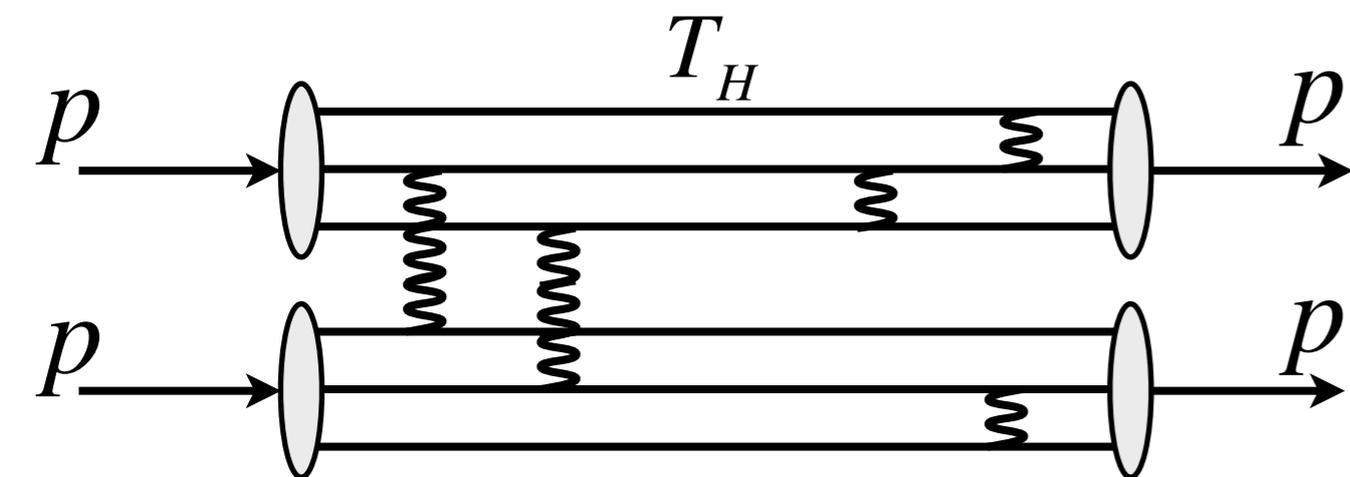
- At high  $t$  and high  $s$ , power-law behavior of the invariant cross section of an **exclusive process**  $A + B \rightarrow C + D$  at fixed CM angle:

$$\frac{d\sigma}{dt} = \frac{1}{s^{n-2}} f(t/s)$$

where  $n$  is the total number of the initial and final elementary fields.

- The energy dependence of the scattering amplitude given by the 'hard-scattering amplitude'  $T_H$  for scattering collinear constituents from the initial to the final state

$$pp \rightarrow pp \equiv 3q3q \rightarrow 3q3q$$



$$\frac{d\sigma}{dt} \sim \frac{|M|^2}{s^2},$$

$$\text{where } [M] = [T_H] = (\sqrt{s})^{4-n}$$

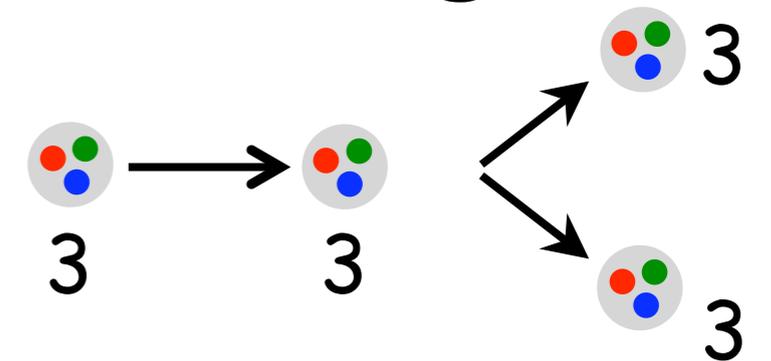
$$\frac{d\sigma}{dt} \sim \frac{1}{s^{n-2}}$$

S.J. Brodsky and G.R. Farrar, Phys. Rev. Lett **31**, 1153 (1973); S.J. Brodsky and J.R. Miller, Phys. Rev. C **28**, 475 (1983)

# Dimensional Scaling Laws: The Findings

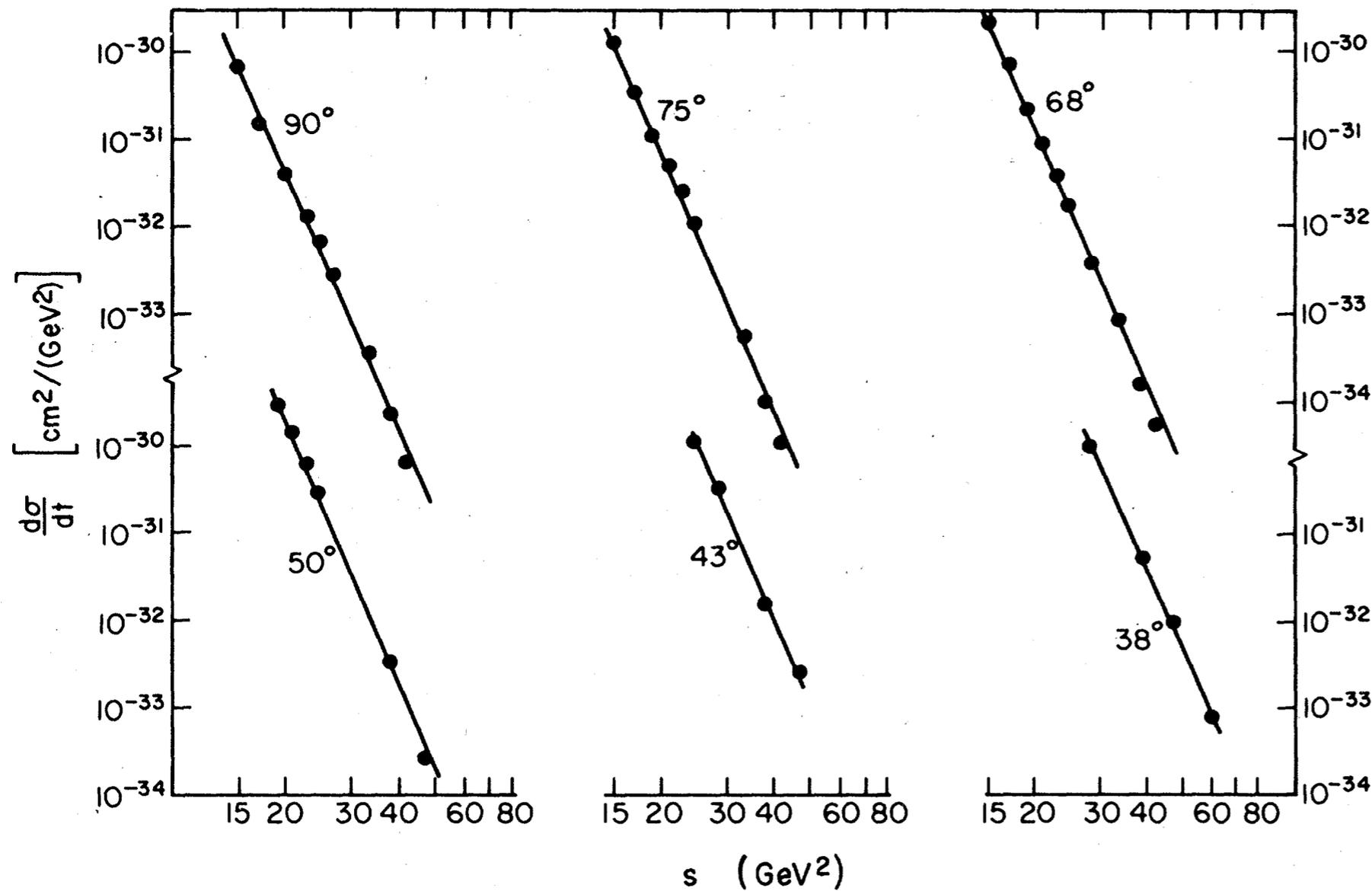
pp → pp

$$s^{10} \frac{d\sigma}{dt} \sim \text{const.}$$



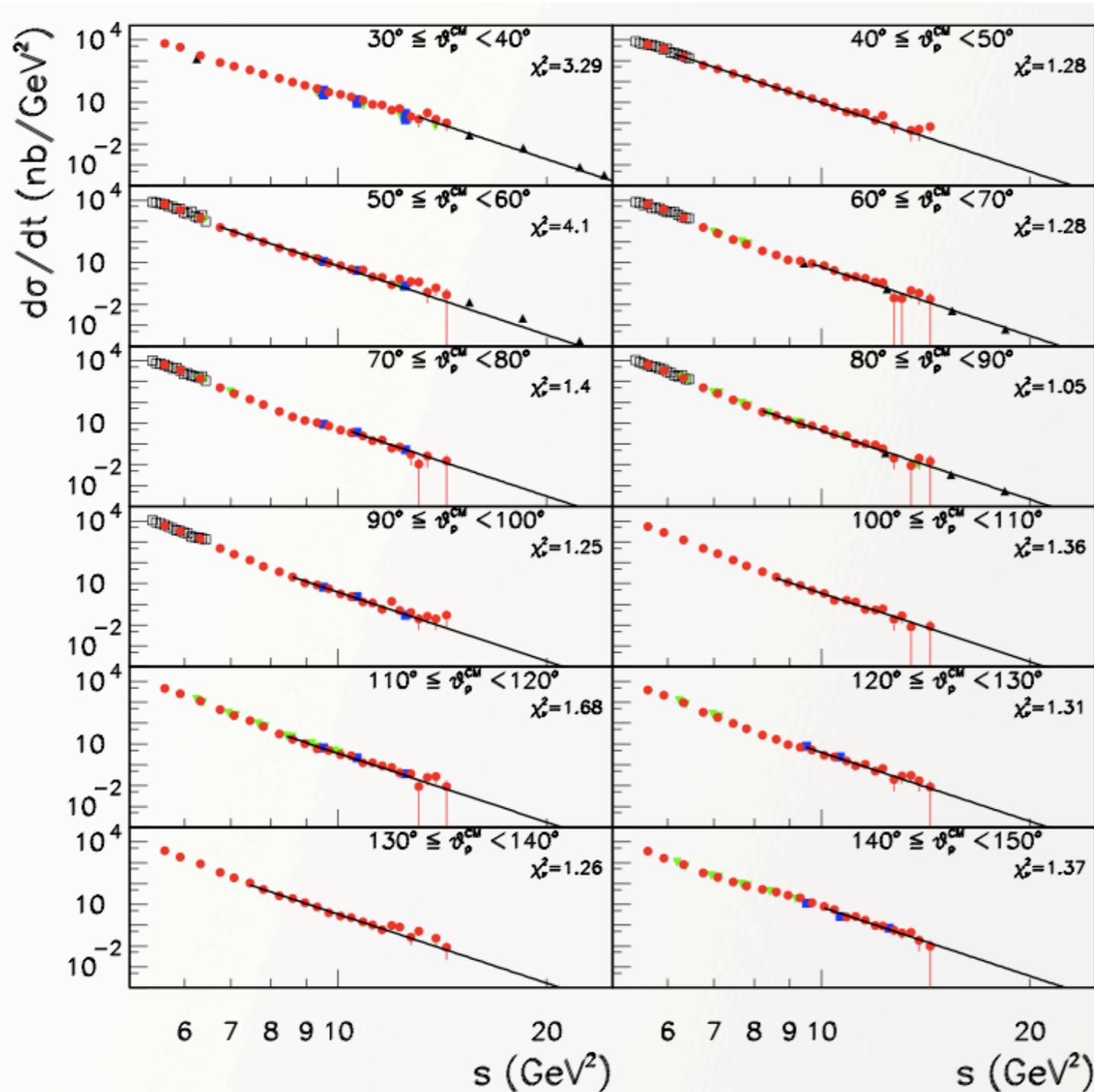
$$n - 2 = (4 \times 3) - 2 = 10$$

- Cross sections consistent with predicted scaling  $s^{-10}$  for a range of CM angles



# Dimensional Scaling Laws: The Findings

$\gamma d \rightarrow pn$



$$\frac{d\sigma}{dt} = \frac{1}{s^{11}} f(t/s)$$

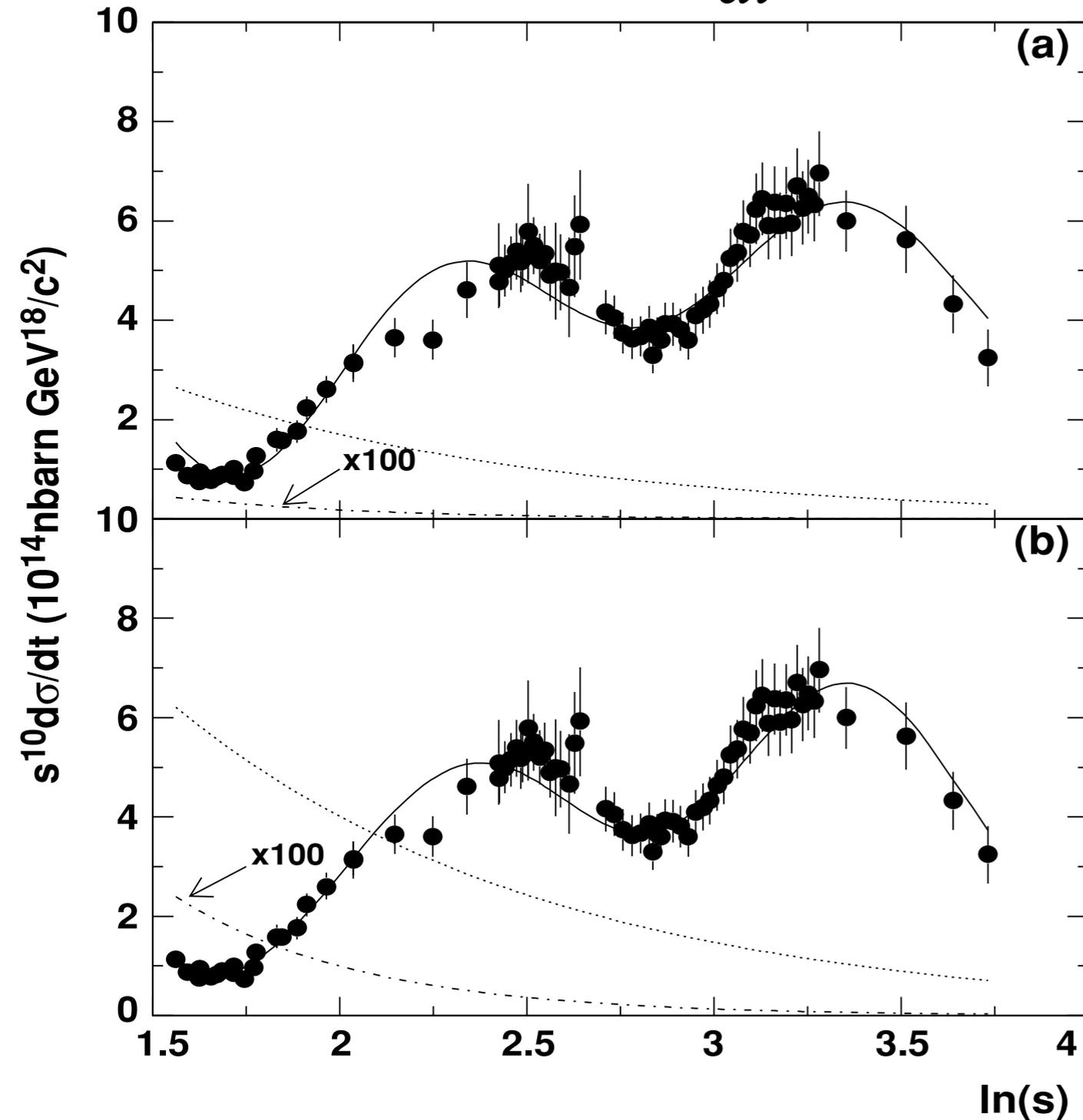
- Fits of  $d\sigma/dt$  data at  $p_T > 1.1$  GeV/c with  $As^{-11}$
- All but two fits have  $\chi^2 \leq 1.34$

P. Rossi et al., Phys. Rev. Lett. **94**, 012301 (2005)

# Dimensional Scaling Laws: The Anomalies

pp → pp

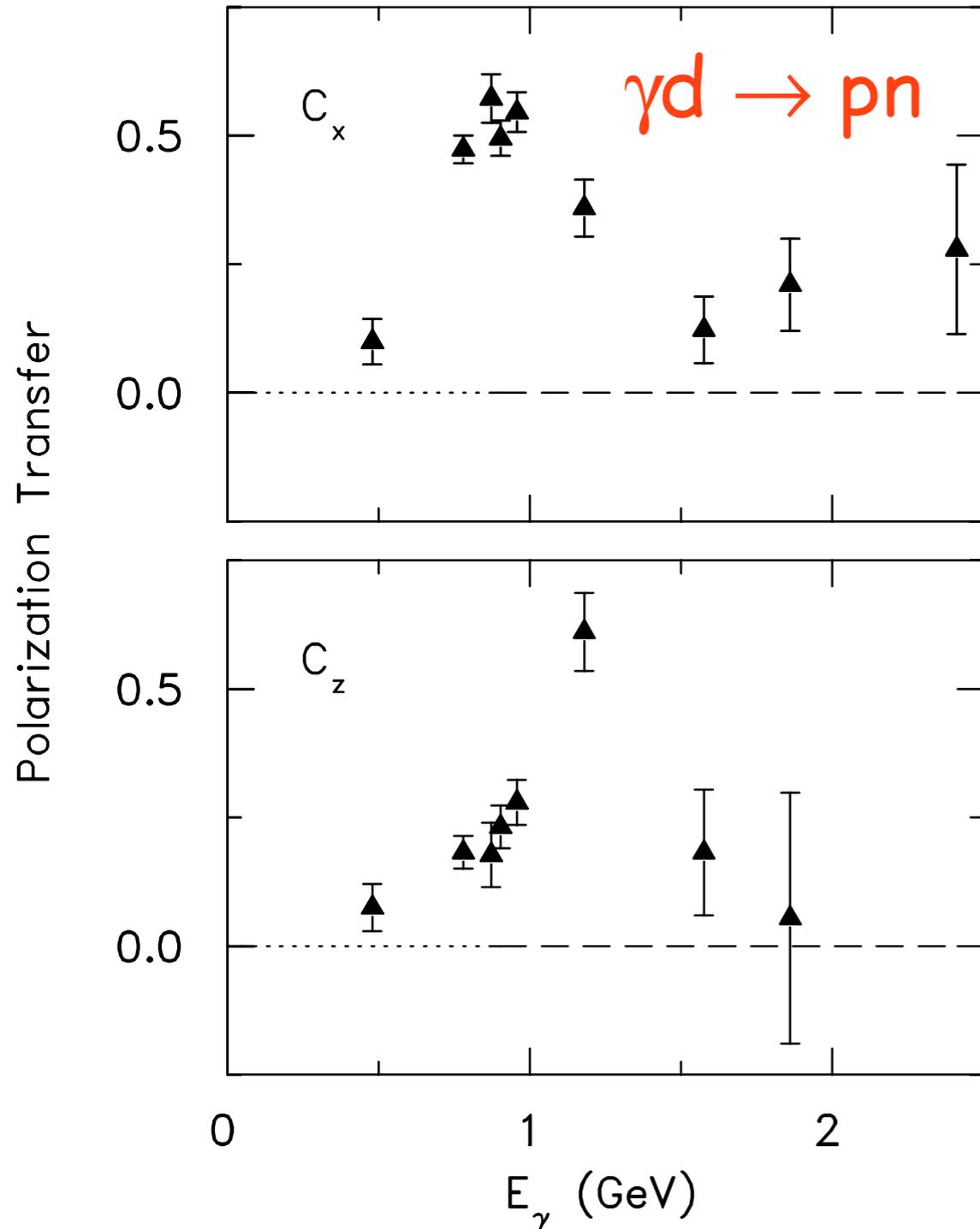
$$s^{10} \frac{d\sigma}{dt} \sim \text{const.}$$



- Oscillations of the scaled cross sections around the scaling value
- Various hypotheses for its origin
  - contributions from non-zero parton orbital angular momentum
  - long distance subprocesses
  - resonance excitations related to the opening of the charm threshold

# Dimensional Scaling Laws and pQCD: The Anomalies

pQCD prediction: **Hadron Helicity Conservation**



$$\lambda_d = \lambda_p + \lambda_n$$

- 12 helicity amplitudes
- 4 amplitudes conserve hadron helicity

$$F_{1+} = \langle 11 | T | +\frac{1}{2} + \frac{1}{2} \rangle$$

$$F_{3-} = \langle 1-1 | T | -\frac{1}{2} - \frac{1}{2} \rangle$$

$$F_{5+} = \langle 10 | T | +\frac{1}{2} - \frac{1}{2} \rangle$$

$$F_{5-} = \langle 10 | T | -\frac{1}{2} + \frac{1}{2} \rangle$$

# Dimensional Scaling Laws: What have we learned?

- Overwhelming experimental evidence for success at momentum transfer as low as 1 GeV
- Anomalies (can be related to resonance excitations)
- Some evidence that soft processes can mimic the predicted dimensional scaling behavior of cross sections
- Observed in a regime where pQCD is not applicable
  - not a feature of only pQCD?
  - manifestation of a more general symmetry?

# Dimensional Scaling Laws: Where do we stand?

- A comprehensive theoretical description of exclusive processes in the non-perturbative regime has proved difficult (pQCD, models).
- Overwhelming evidence for dimensional scaling, yes, but we do not know how to interpret it.

# Dimensional Scaling Laws: Where do we stand?

- A comprehensive theoretical description of exclusive processes in the non-perturbative regime has proved difficult (pQCD, models).
- Overwhelming evidence for dimensional scaling, yes, but we do not know how to interpret it.

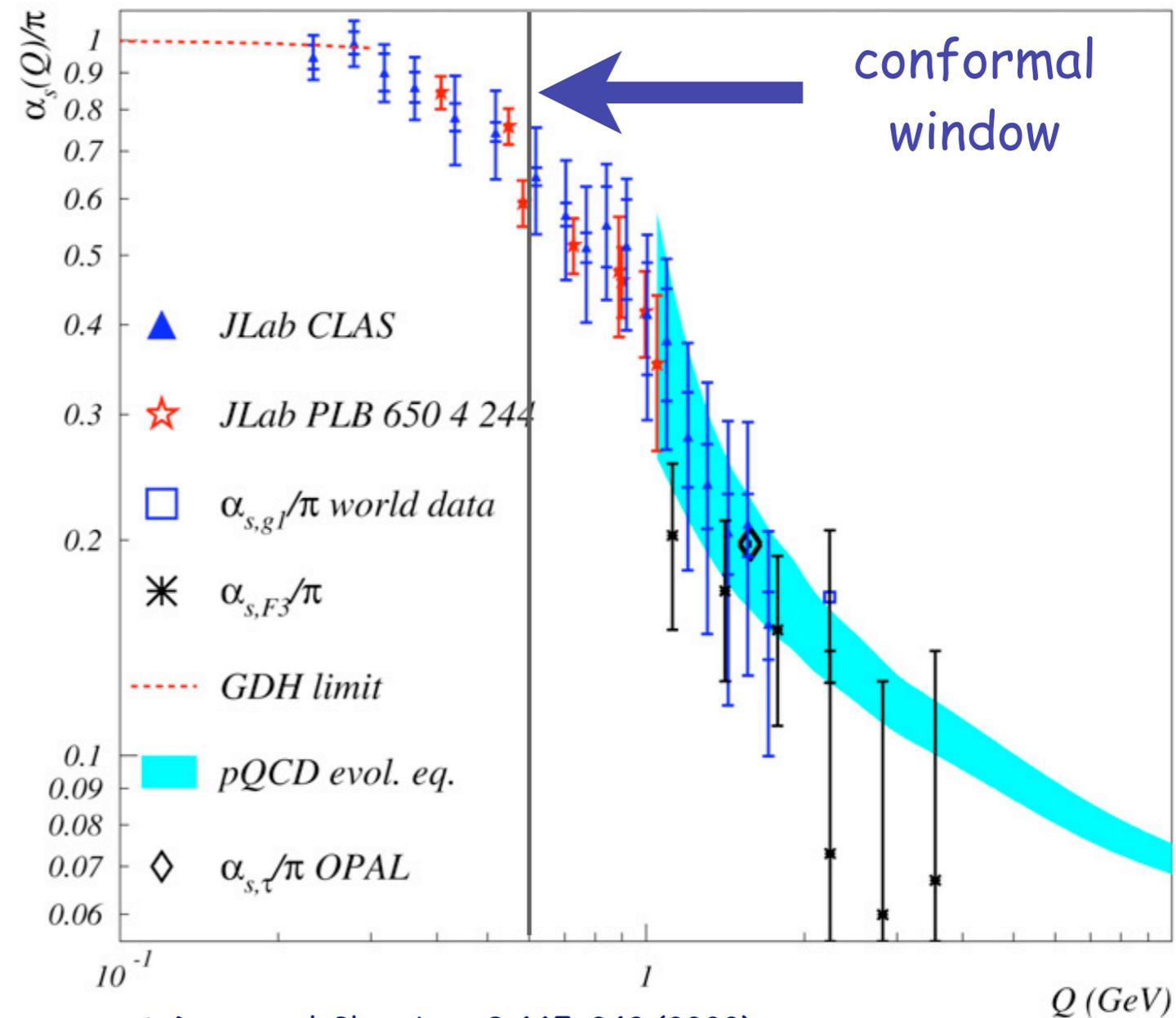
**What is the origin of the scale-invariance of the underlying non-perturbative dynamics in the regime of confinement?**

# Dimensional Scaling Laws: A New Insight

- QCD is not conformal, however it has manifestations of a scale-invariant theory (dimensional scaling, Bjorken scaling)
- AdS/CFT Correspondence between string theories in Anti de Sitter space-time and conformal field theories in physical space-time
- Allows to treat confinement at large distances and conformal symmetry at short distances
- **Non-perturbative derivation of Dimensional Scaling Laws!**

# Dimensional Scaling Laws: A New Insight

- At **short distances**, dimensional scaling laws reflect the scale independence of  $\alpha_s$  (**asymptotic freedom**)
- At **large distances**, dimensional scaling laws reflect the existence of infrared fixed point of QCD:  $\alpha_s$  is large but **scale-independent**
- Scale-invariance is **broken** in the **transition** between these two dynamical regimes



# Dimensional Scaling Laws: Our Approach

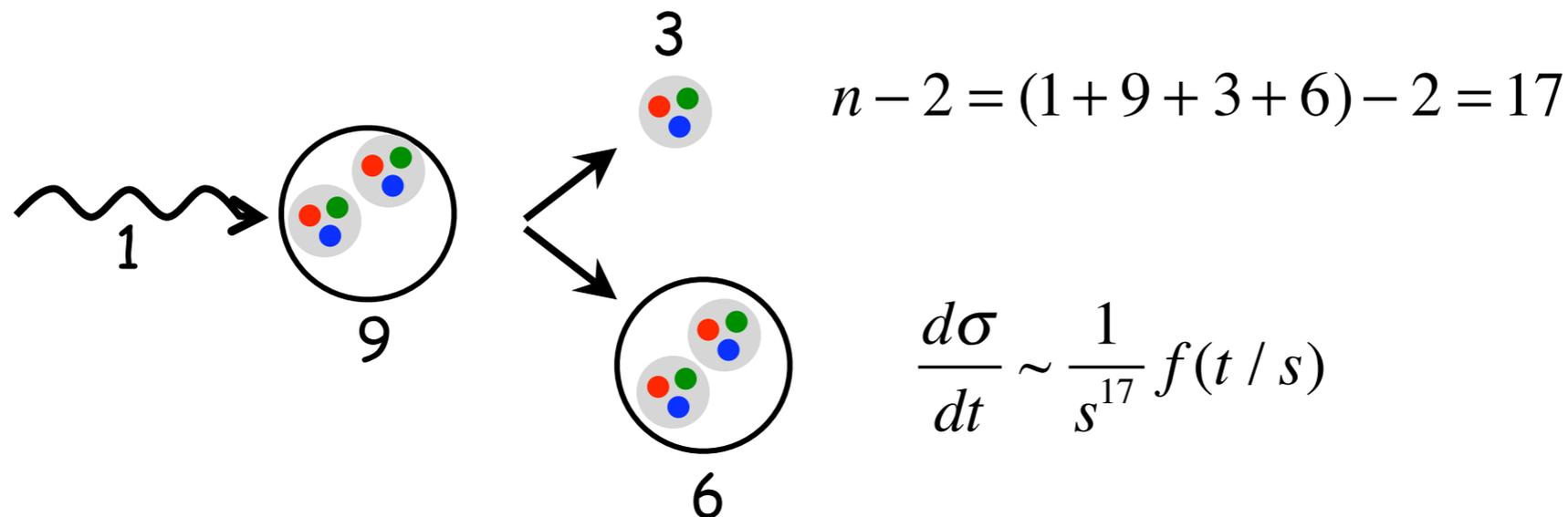
- Dimensional Scaling Laws probe two very **different dynamical regimes**: interpretation depends on the **average momentum transfer** to each hadron constituent.
- In order to test the predictions of the novel AdS/CFT approach, we need to rigorously probe **dimensional scaling** in exclusive processes at **small momentum transfer**.
- We need to look at reactions in which the **momentum transfer is shared** among many constituents.
- We need to look for reactions that are **not dominated by resonance** excitation at low energies.
- The **nucleus** is an **ideal laboratory**.

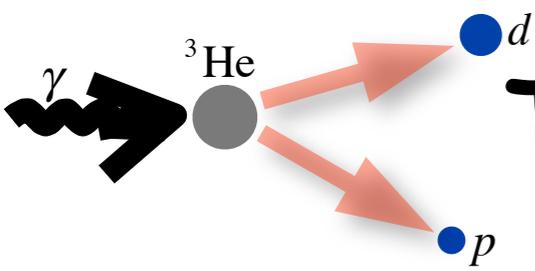
# Dimensional Scaling Laws: Our Approach

- We study the reaction  $\gamma^3\text{He} \rightarrow pd$  in the energy range 0.4 - 1.4 GeV
- Advantages
  - prior evidence that **re-scattering** mechanisms play significant role (ideal tool for sharing the momentum among many constituents so that the average momentum transfer per constituent is small).
  - low-energy studies show that the cross sections are **not** dominated by **resonance** excitation.

# Dimensional Scaling Laws: Our Approach

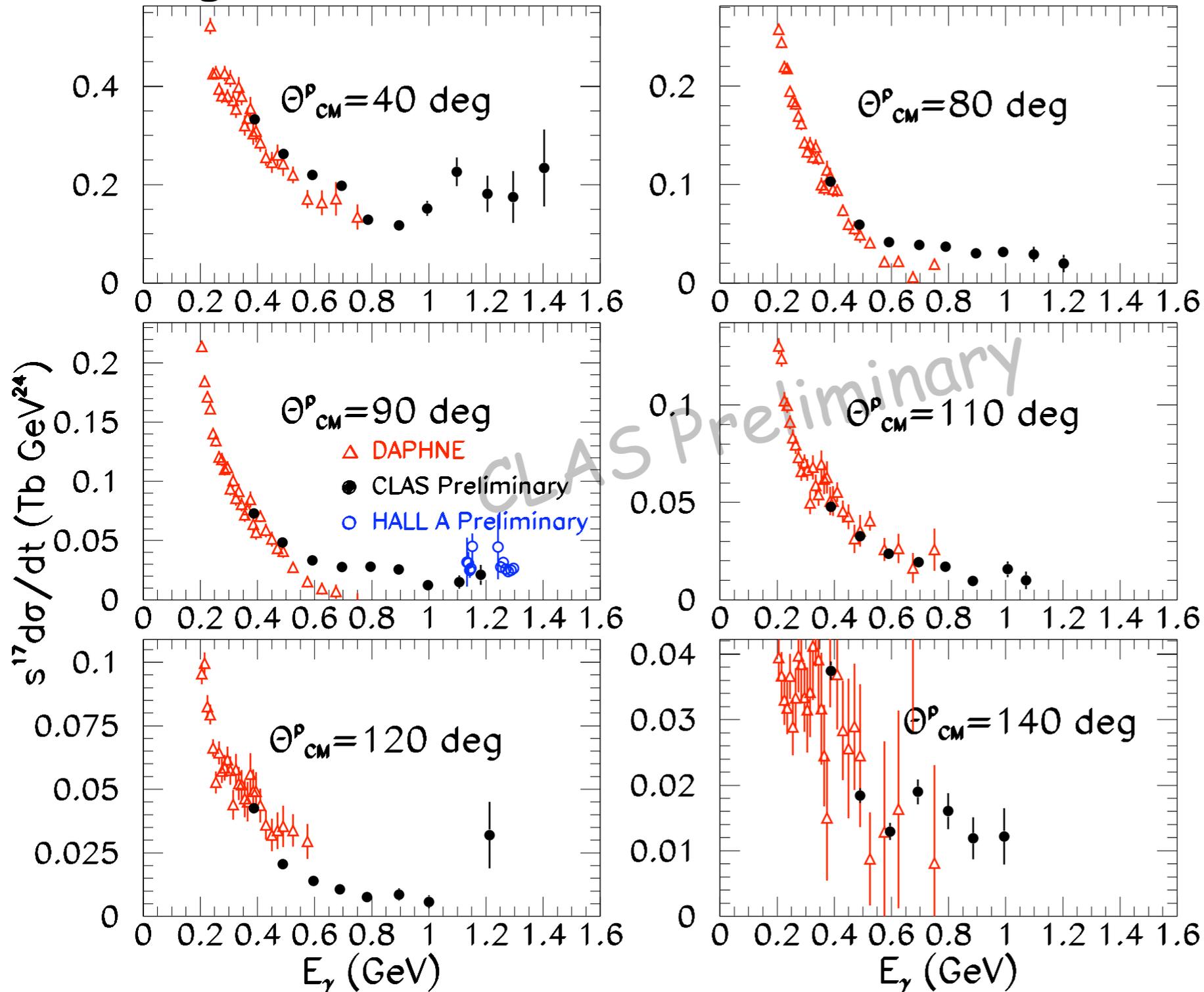
- We study the reaction  $\gamma^3\text{He} \rightarrow pd$  in the energy range **0.4 - 1.4 GeV**
- Advantages
  - prior evidence that **re-scattering** mechanisms play significant role (ideal tool for sharing the momentum among many constituents so that the average momentum transfer per constituent is small).
  - low-energy studies show that the cross sections are **not** dominated by **resonance** excitation.





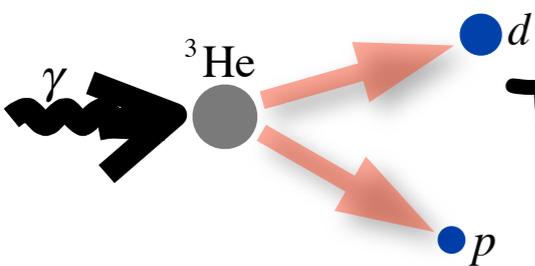
# Two-Body Photodisintegration of $^3\text{He}$

## Scaling of invariant cross sections



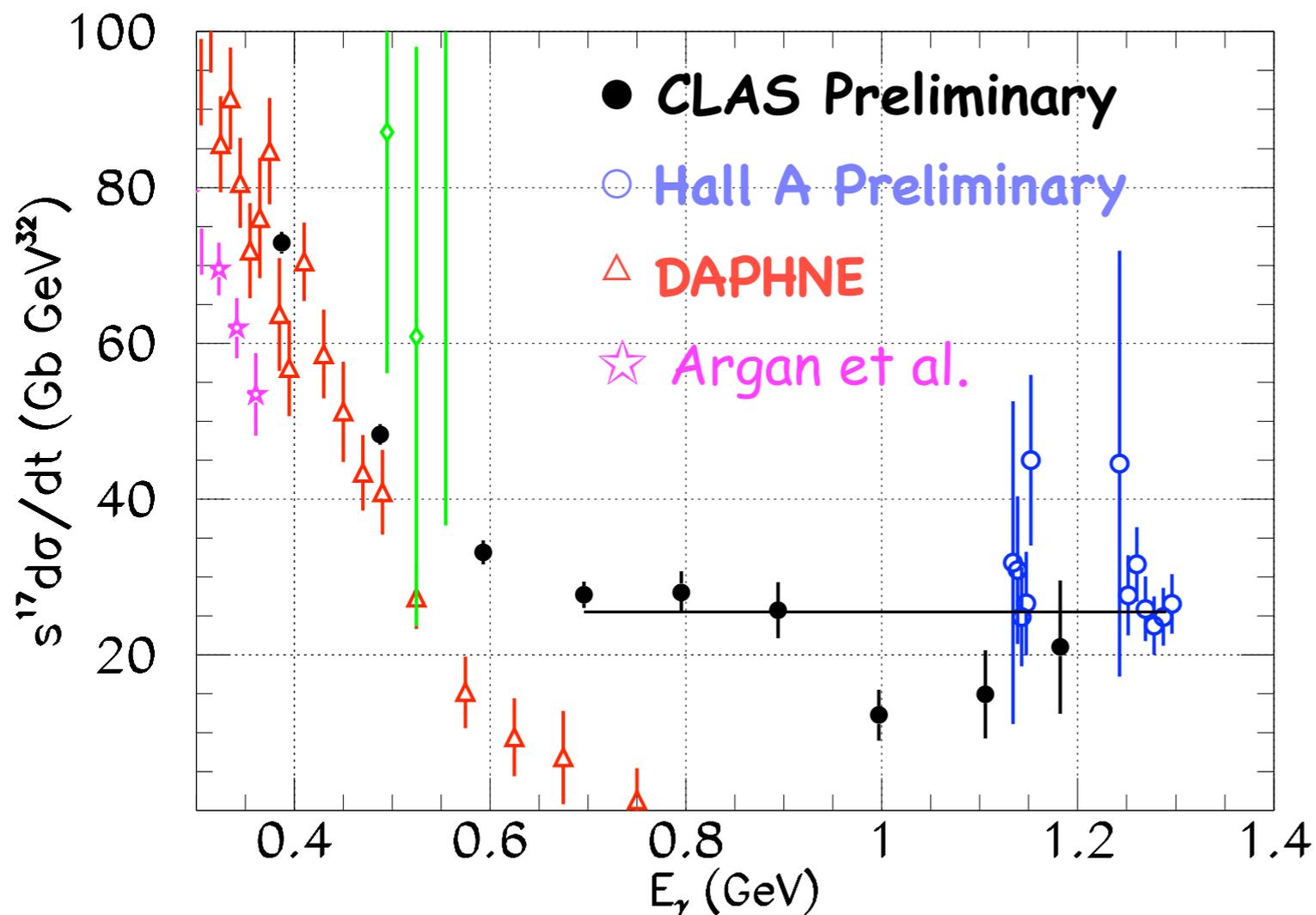
$$s^{17} \frac{d\sigma}{dt} \sim \text{const.}$$

- Dimensional Scaling Predicts  $n-2=17$
- Indication that above  $\sim 0.7 \text{ GeV}$  data consistent with scale invariance for all *CM* angles
- Consistent with the AdS/CFT hypothesis



# Two-Body Photodisintegration of $^3\text{He}$

Scaling of invariant cross sections at  $90^\circ$



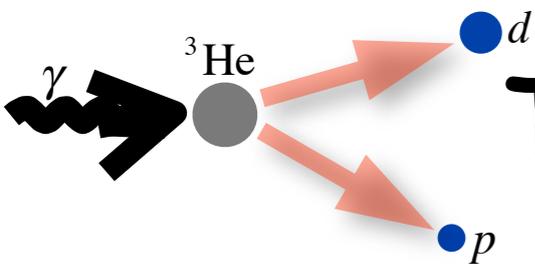
Data fitted by:  $\frac{d\sigma}{dt} = A s^{-N}$

- Extracted value from fits to data:

$$N = 17 \pm 1$$

- $|t|_{\text{thr}}$  and  $p_{\perp\text{thr}}$  are too low to support hard scattering hypothesis:  
 $|t|_{\text{thr}} = 0.64 (\text{GeV}/c)^2$   
 $p_{\perp\text{thr}} = 0.95 \text{ GeV}/c$

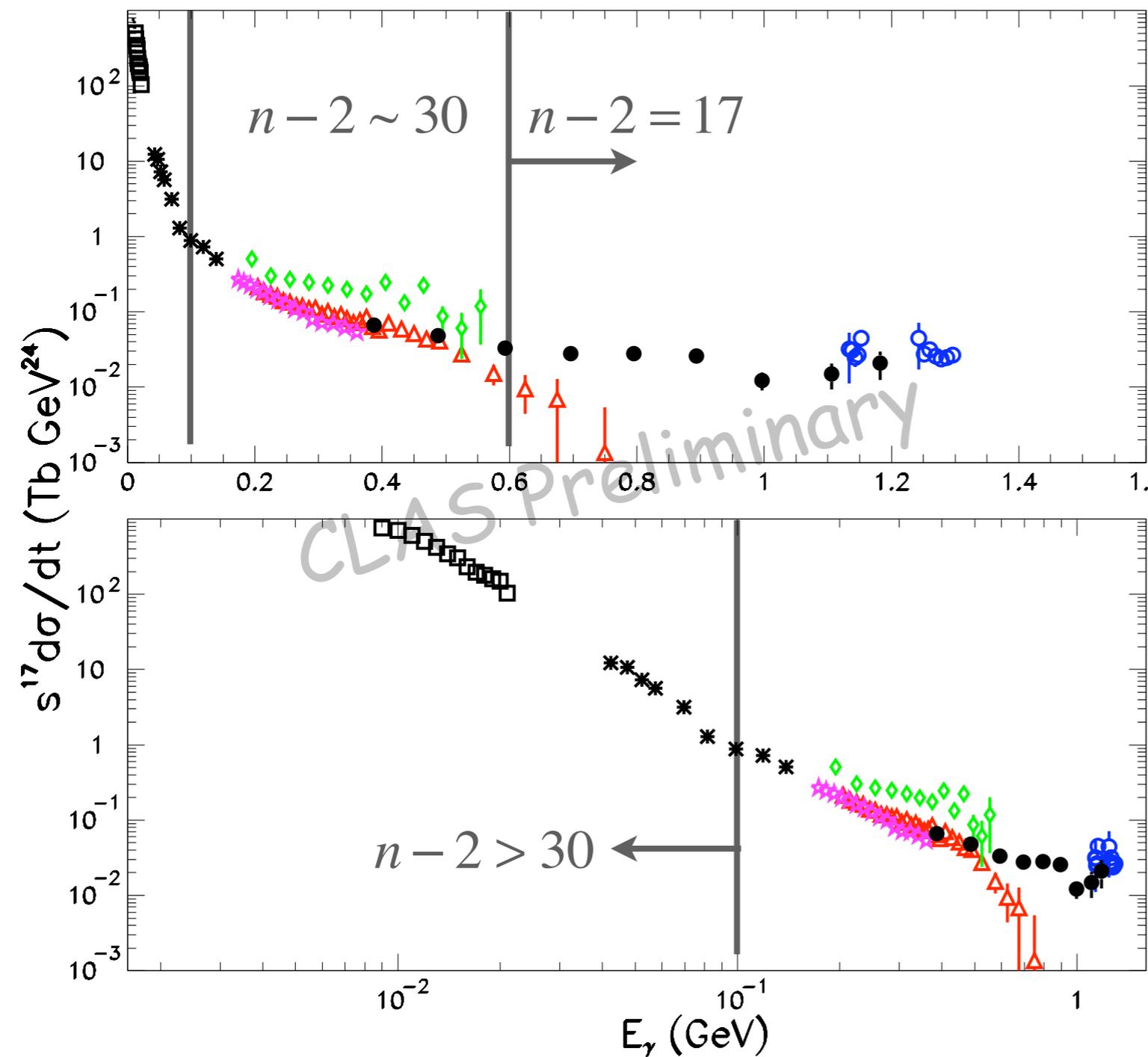
- Our data are consistent with the hypothesis of conformal window from AdS/CFT



# Two-Body Photodisintegration of $^3\text{He}$

Scaled invariant cross sections at  $90^\circ$

$$s^{17} \frac{d\sigma}{dt} \sim \text{const.}$$



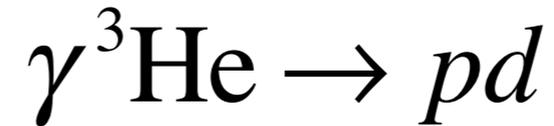
- Dimensional Scaling Predicts  $n-2=17$
- For energies  $\sim(0.1 - 0.6)$  GeV data scale with  $n-2 \sim 30$ .
- Below  $\sim 0.1$  GeV: parton picture break down (?)

# Summary and Perspectives

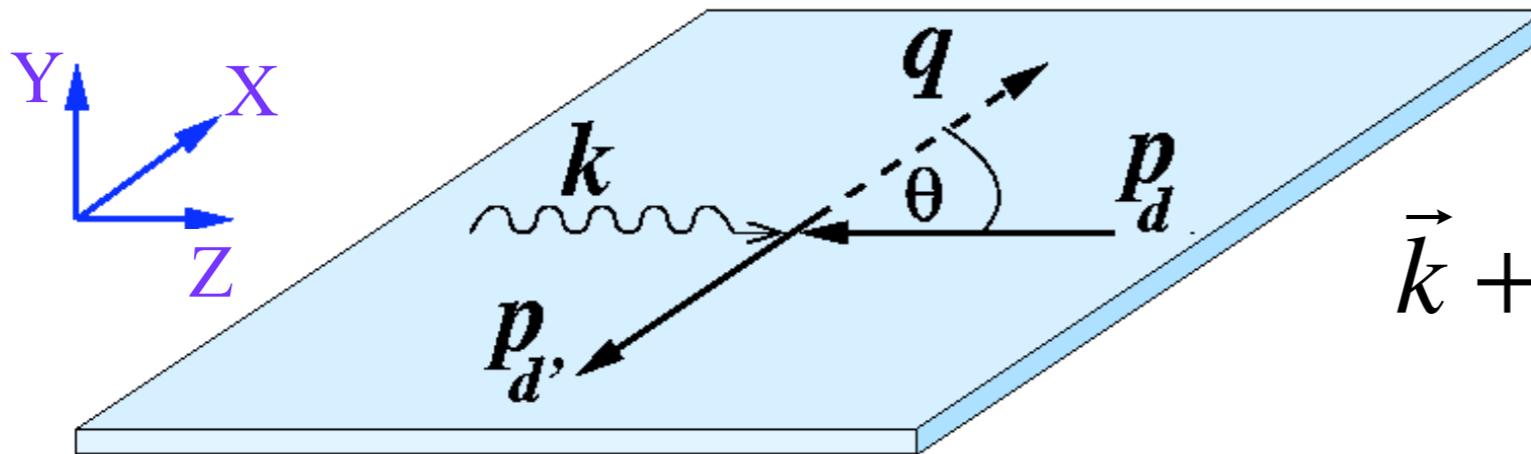
- First systematic study of **dimensional scaling** of an exclusive nuclear process,  $\gamma^3\text{He} \rightarrow \text{pd}$  at **low  $s$  and  $t$** .
- Results currently under CLAS analysis review.
- Solid experimental **evidence** for onset of **dimensional scaling** at CM angles of  **$90^\circ$** .
- Indication for onset of **dimensional scaling** at other CM **angles**.
- Observed scaling is qualitatively **consistent** with the hypothesis of **conformal window** at very low momentum transfer.
- **Not understood** what is the origin of scaling in other exclusive processes: dominance of hard re-scattering or conformal window scale invariance
  - Polarization measurement of  $\gamma d \rightarrow \text{pn}$  (g13 data at JLab)
  - Exclusive kaon photoproduction at JLab 12 GeV (LOI-11-107)

**The END**

# Kinematics of Exclusive Processes



Center-of-Mass Reference Frame (CM):



$$\vec{k} + \vec{p}_{^3\text{He}} = \vec{p}_d + \vec{p}_p = 0$$

Center of mass energy,  $s$ , and momentum transfers,  $t$  and  $u$

$$s = (\tilde{p}_\gamma + \tilde{p}_{^3\text{He}})^2 = s(E_\gamma)$$

$$t = (\tilde{p}_d - \tilde{p}_{^3\text{He}})^2 = t(E_\gamma, \theta)$$

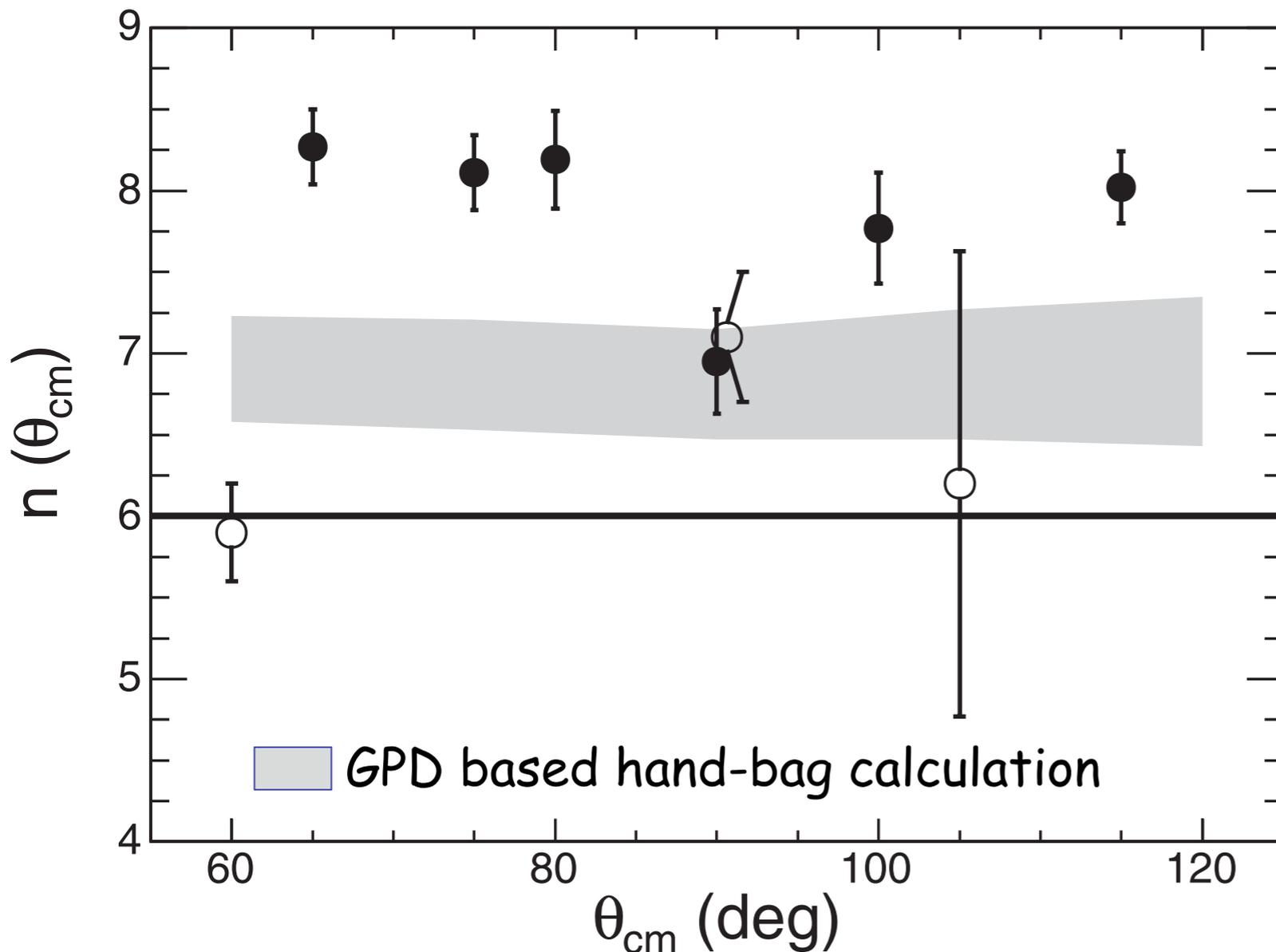
$$u = (\tilde{p}_p - \tilde{p}_{^3\text{He}})^2 = u(E_\gamma, \theta)$$

At large energies, the cross section is a simple function of  $s$ . 18

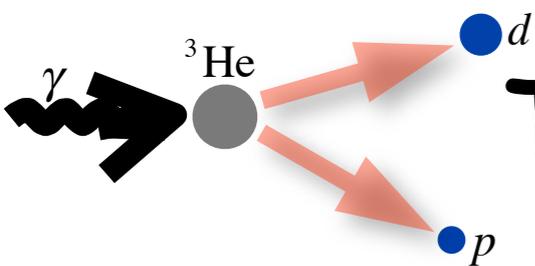
# Dimensional Scaling Laws: The Anomalies

$\gamma p \rightarrow \gamma p$

$$s^6 \frac{d\sigma}{dt} \sim \text{const.}$$

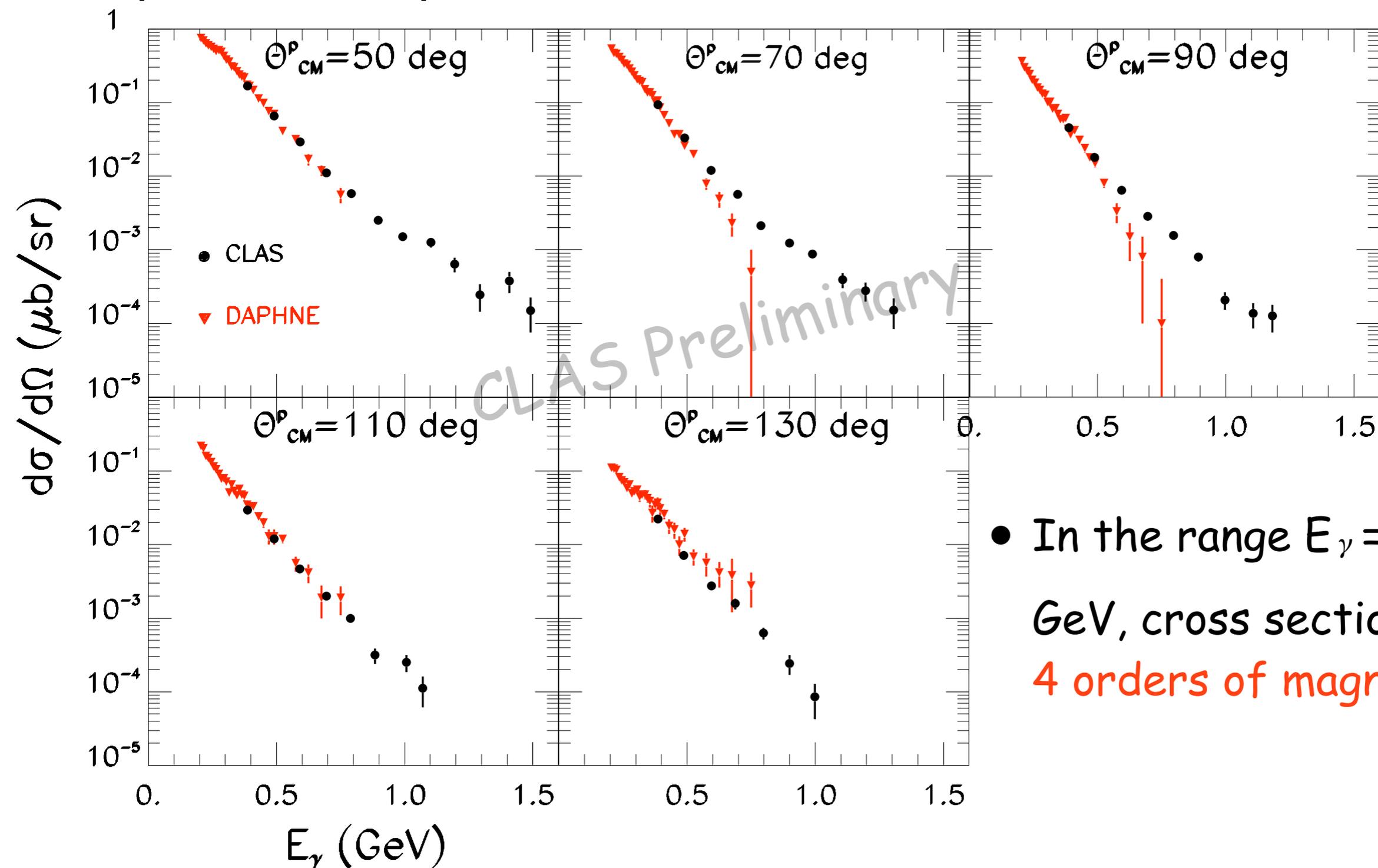


- Cross sections inconsistent with predicted scaling power
- Some theoretical studies suggest the process is dominated by soft subprocesses
- $n \sim 8$  due to the vector-meson component of the real photon?



# Two-Body Photodisintegration of $^3\text{He}$

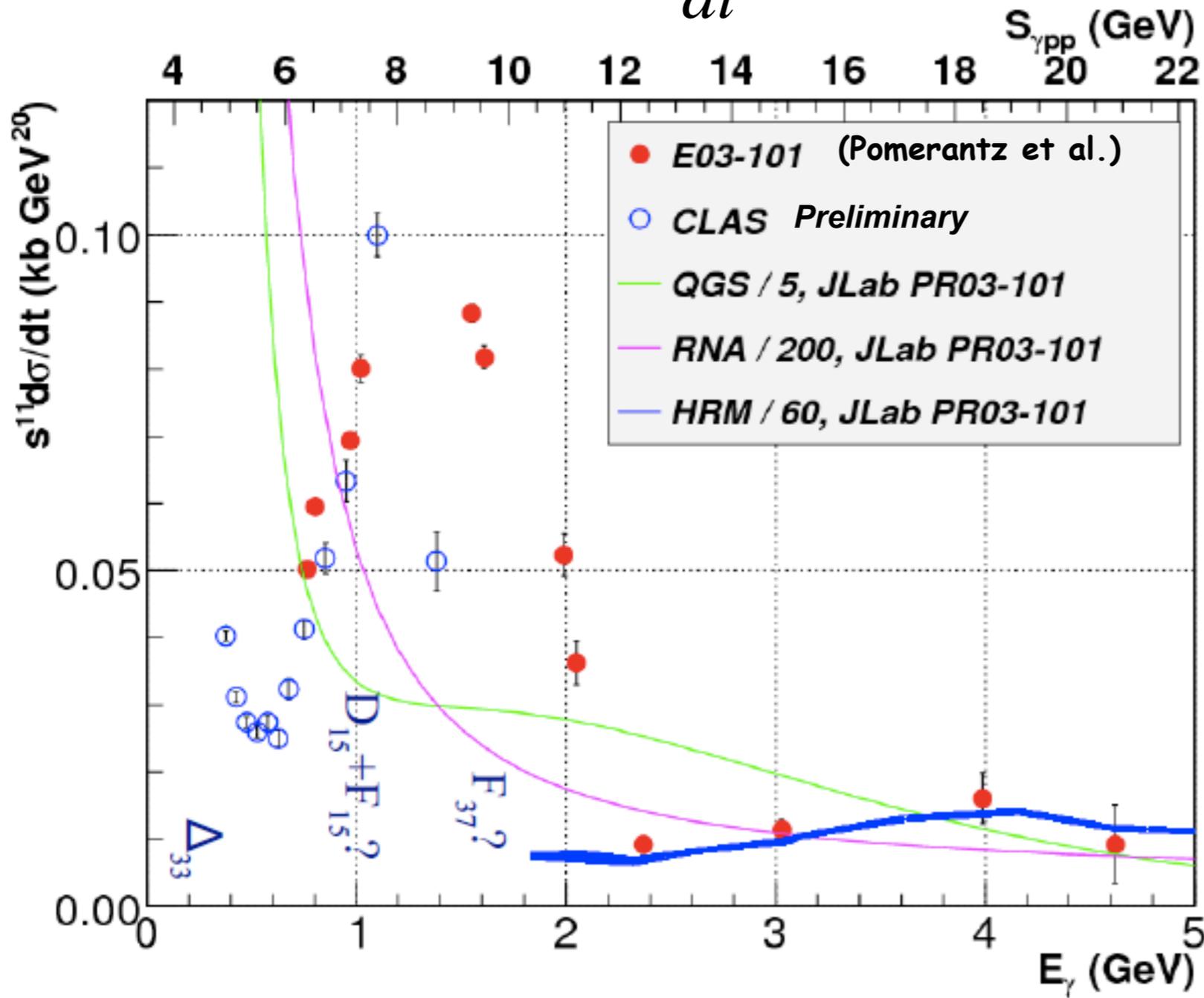
Comparison with previous measurements



- In the range  $E_\gamma = 0.2 - 1.5$  GeV, cross sections drop 4 orders of magnitude.

# Dimensional Scaling Laws: The Anomalies

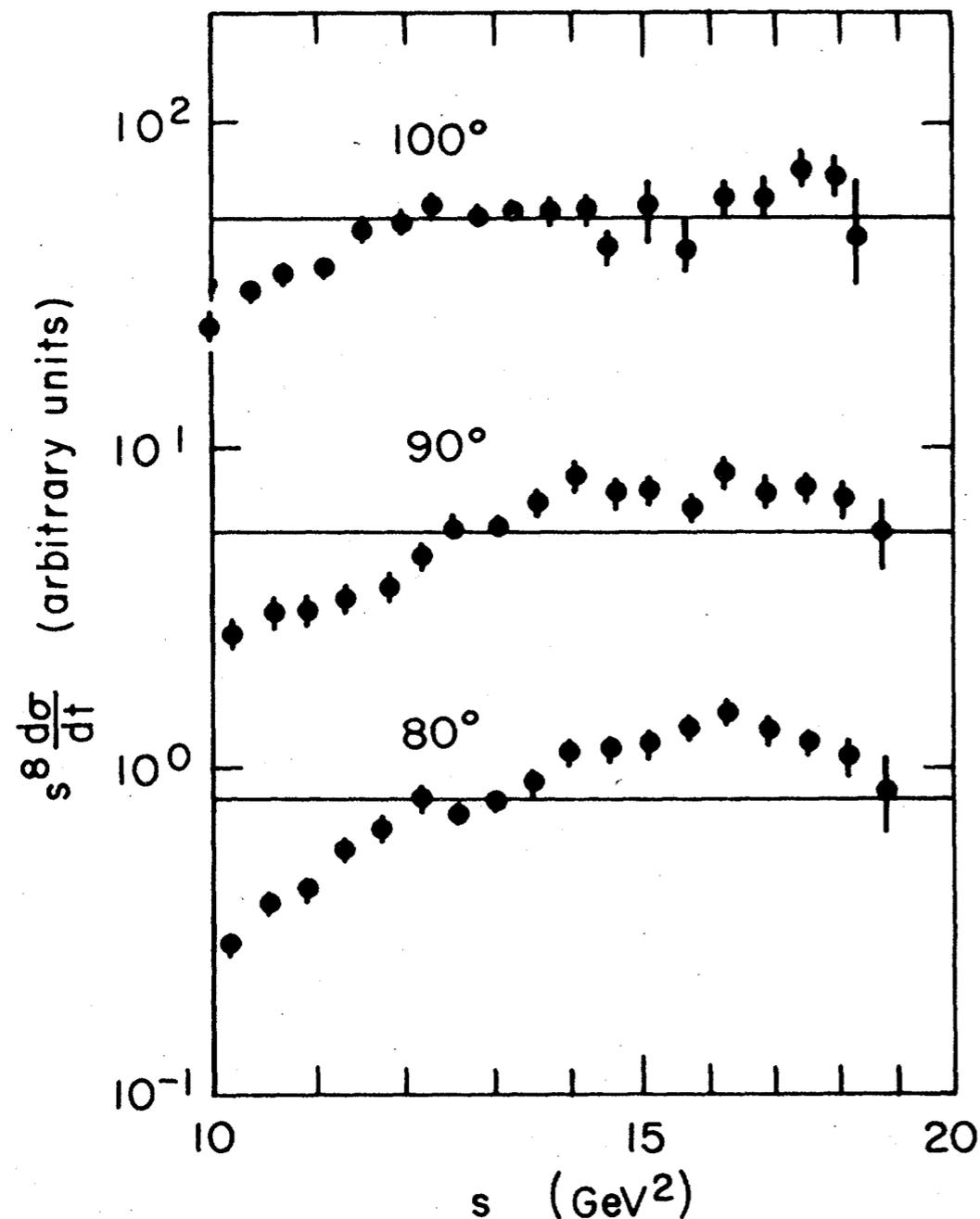
$$\gamma p p(n) \rightarrow p p(n) \quad s^{11} \frac{d\sigma}{dt} \sim \text{const.}$$



- Large resonance-like structure below 2 GeV, not observed in deuteron photodisintegration
- Various models describe equally well the shape of scaled cross section above 2 GeV
  - Quark-Gluon String M
  - Hard Rescattering M
  - Reduced Nuclear Amplitudes

# Dimensional Scaling Laws: The Findings

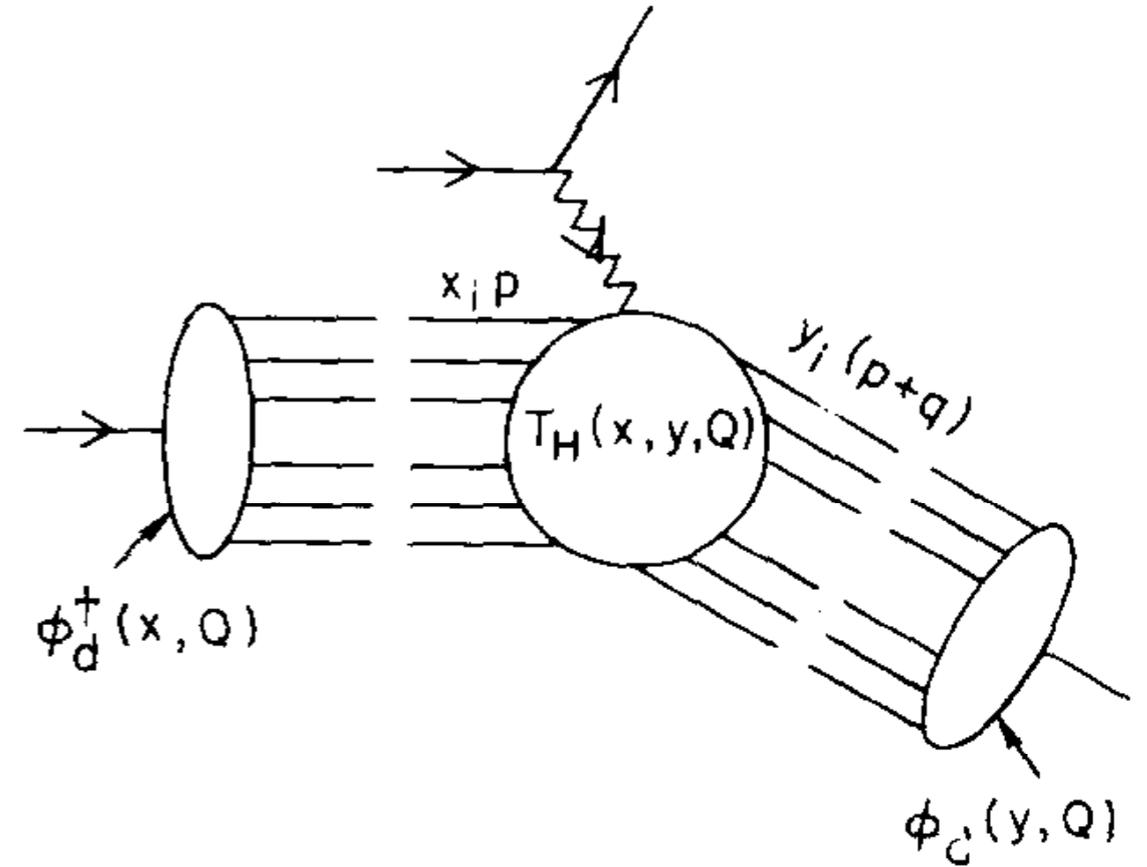
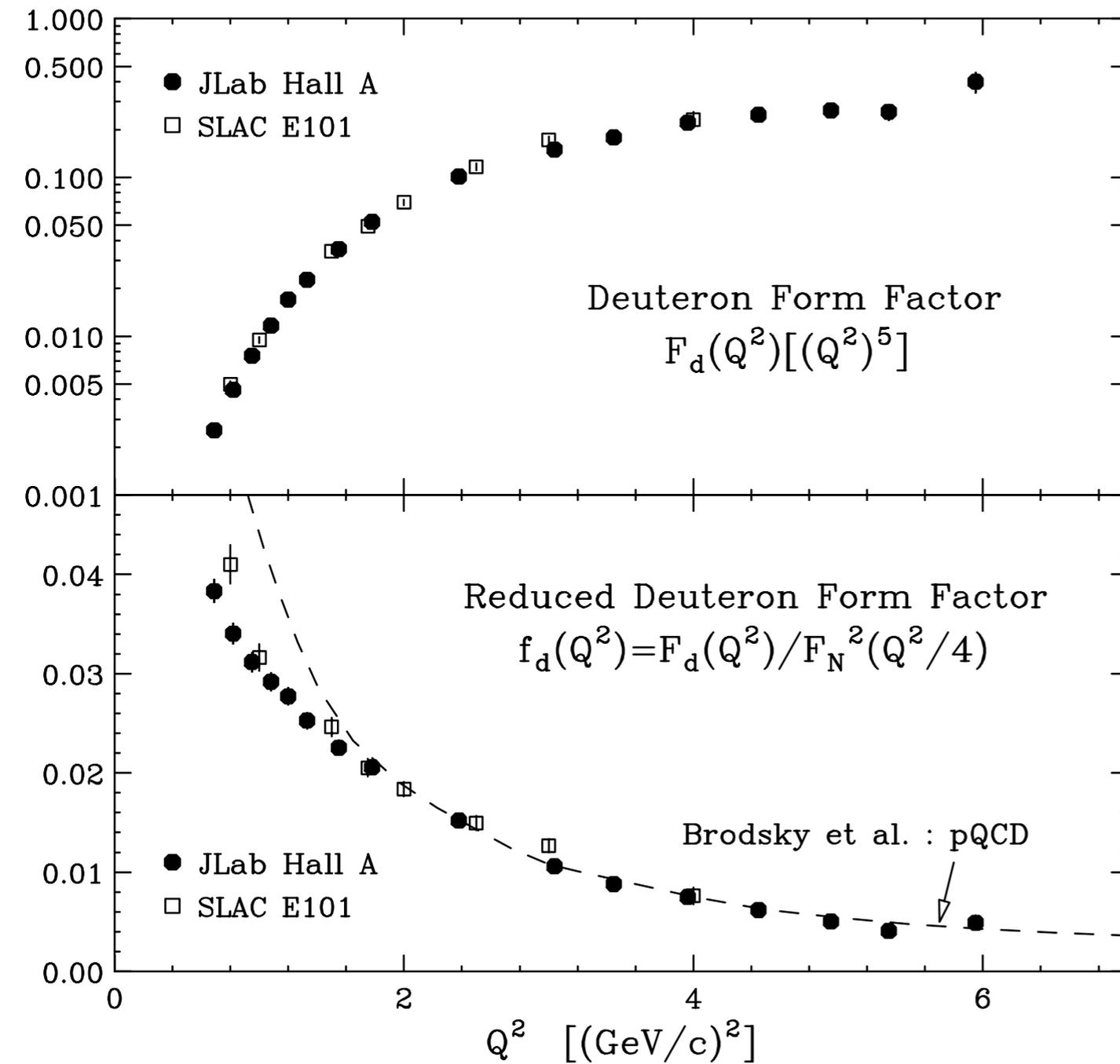
$$\pi^- p \rightarrow \pi^- p \quad s^8 \frac{d\sigma}{dt} \sim \text{const.}$$



- Cross sections consistent with predicted scaling  $s^{-8}$  for large CM angles and  $s > 12 \text{ GeV}^2$

# Dimensional Scaling Laws: The Findings

## Deuteron Form Factor



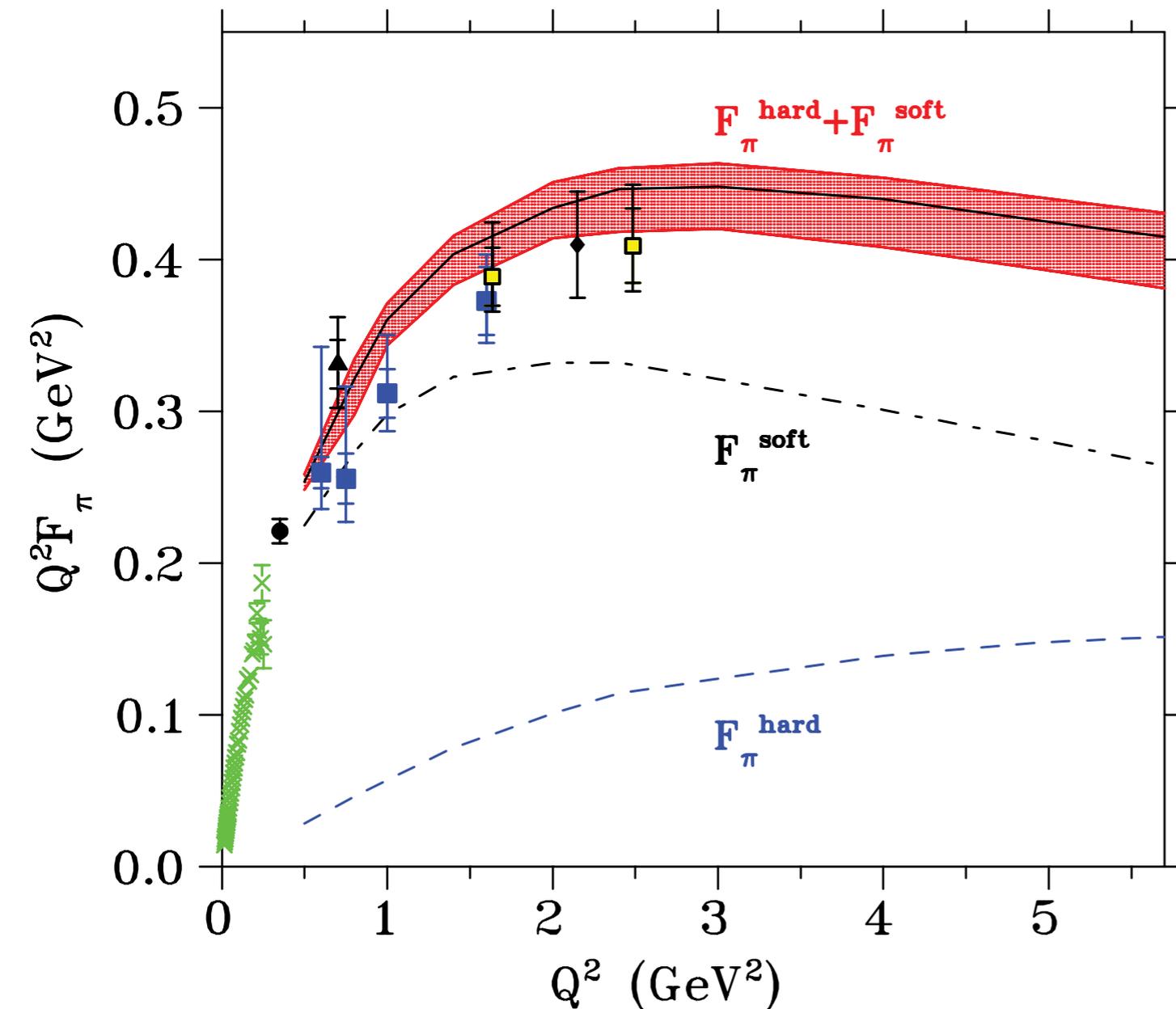
$$T_H^{6q+\gamma^* \rightarrow 6q} = \left[ \frac{\alpha_s(Q^2)}{Q^2} \right]^5 t(x, y) [1 + O(\alpha_s(Q^2))]$$

$$F_d(Q^2) \sim \frac{1}{Q^{10}}$$

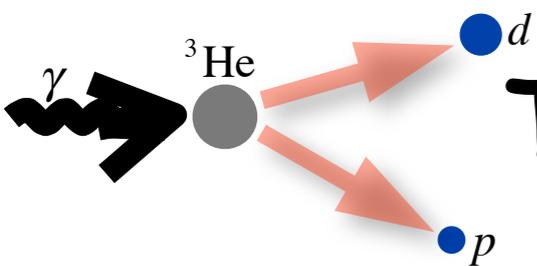
$$Q^{10} F_d(Q^2) \sim \text{const.}$$

# Dimensional Scaling Laws and pQCD: The Anomalies

Pion Form Factor  $Q^2 F_\pi \sim \text{const.}$

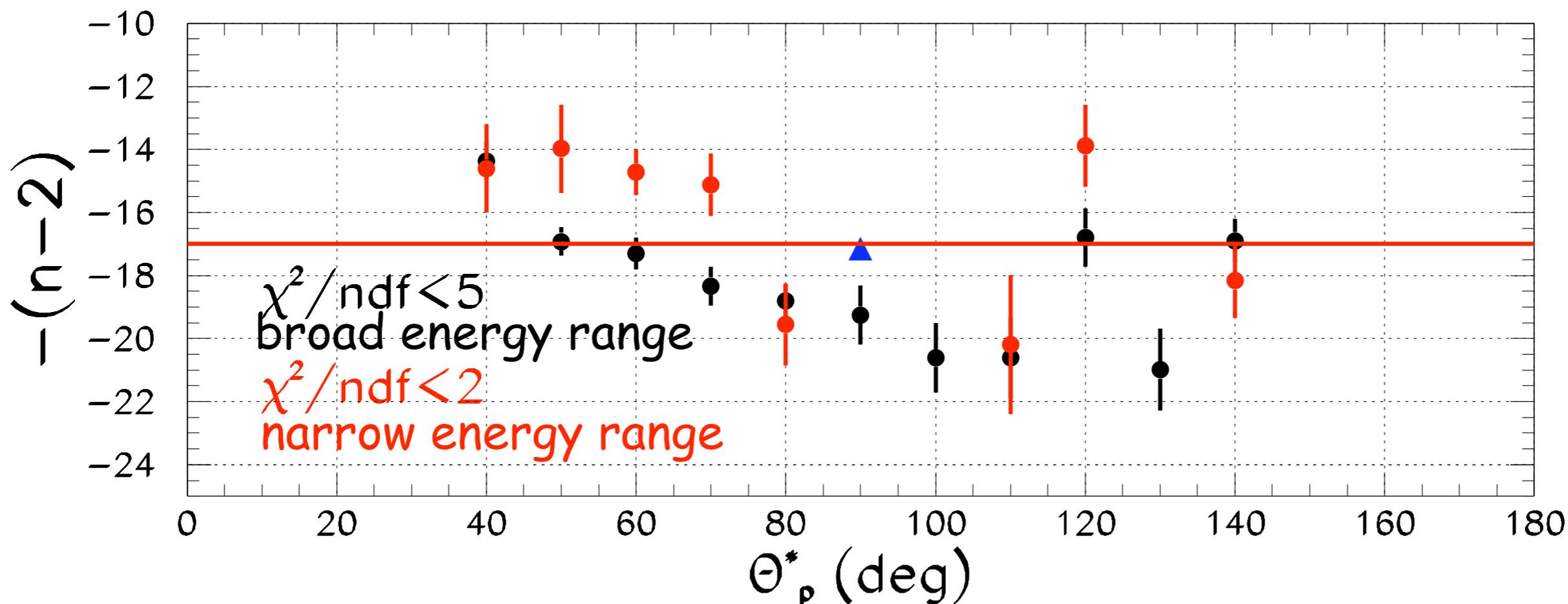


- Data show indications of approaching scaling behavior
- Data are far above the pQCD prediction
- Non-perturbative contributions dominate in the kinematic range of measured data.



# Two-Body Photodisintegration of $^3\text{He}$

Can we make quantitative statements at other angles?



- Difficulty: lack of good statistics data in the higher-energy end
- $\chi^2/\text{ndf}$  may not be a **reliable criterion** to conclude about scaling
- With limited energy coverage, a minimum length of fitted energy range may be needed.
- Using only CLAS data, it is difficult to make conclusive statements.