

A Study of the ρ - ω Interference in the e^+e^- decay channel from $\gamma p \rightarrow e^+e^-X$

**M. Paolone¹, C. Djalali², M. Wood³, D. Weygand⁴
and the CLAS Collaboration.**

Brief history of ρ - ω interference

Motivation for studying ρ - ω interference on the proton

The g12 experiment in CLAS

Data reduction and analysis

Results and outlook

1 Temple University, Philadelphia, PA.

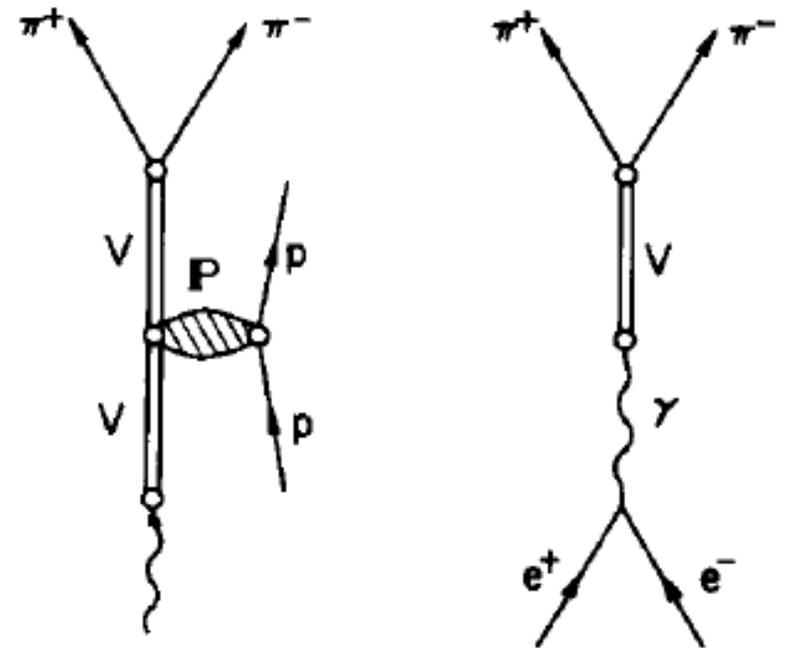
2 University of Iowa, Iowa City, IA.

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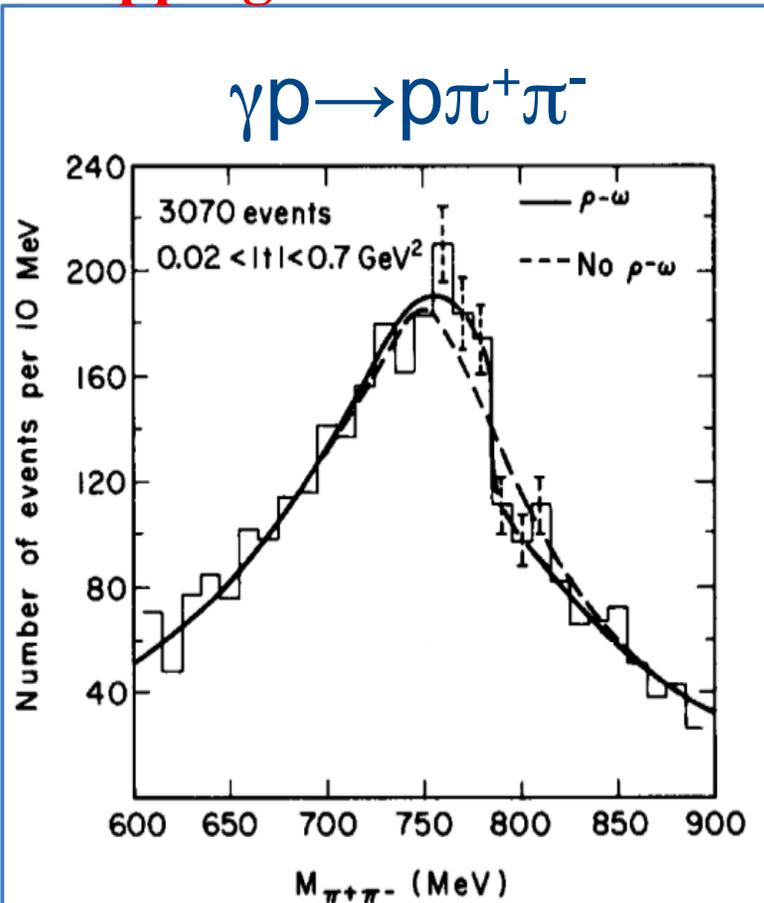
A brief history of ρ - ω interference.

- Quantum interference between the ρ and ω mesons was first proposed by S. Glashow (in 61) and became useful interpreting ρ - ω mass spectra reconstructed from detected pions in particle experiments of the 1960's.
- Results from e^+e^- annihilation required the study of the interference in both $\pi^+\pi^-$ and e^+e^- decay channels.



A brief history of ρ - ω interference.

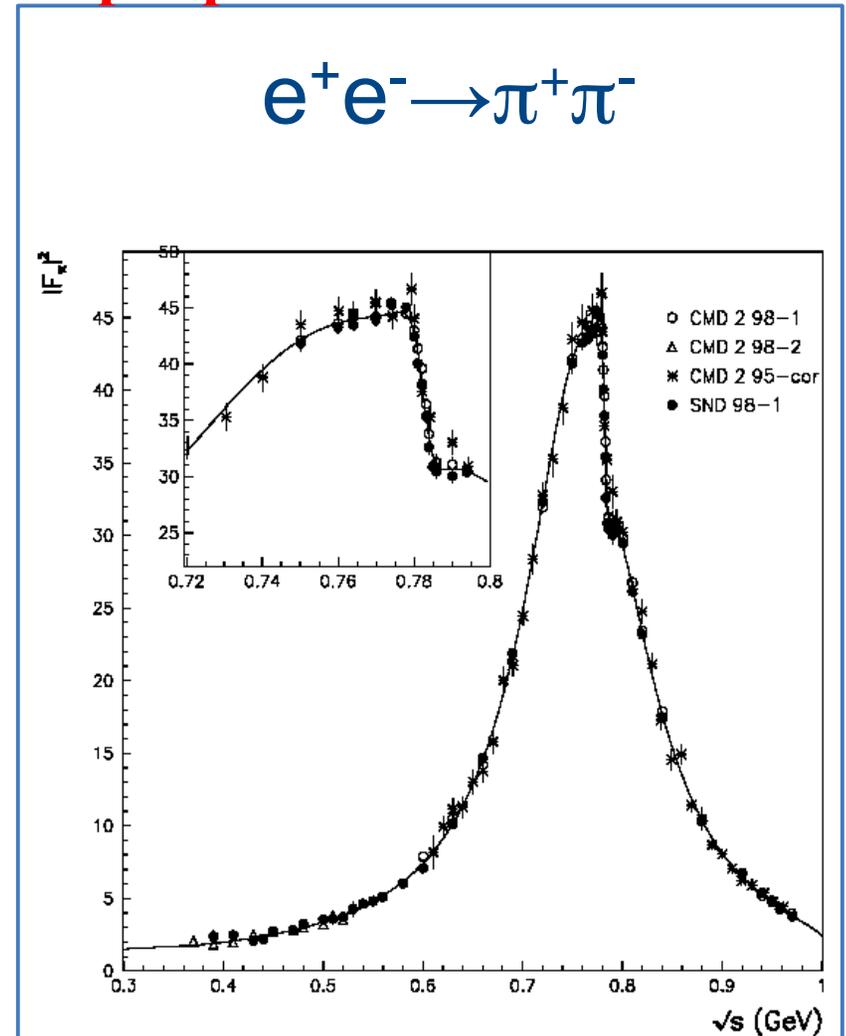
The interference between identical decay states can be seen in the overlapping mass distributions as a “sharp dip” or a “shoulder”.



5-
1

Fig. 2. The $\pi^+\pi^-$ mass distribution for events of the reaction $\gamma p \rightarrow \pi^+\pi^-p$. The curves give the results of maximum-likelihood fits with (—) and without (-----) $\rho^0 - \omega$ interference.

K.C. Moffeit *et al*, Nucl.Phys.B29 (1971)



Benayounet et al., Eur.Phys.J.C72, (2012)

Photoproduction and the hadronic decay channel.

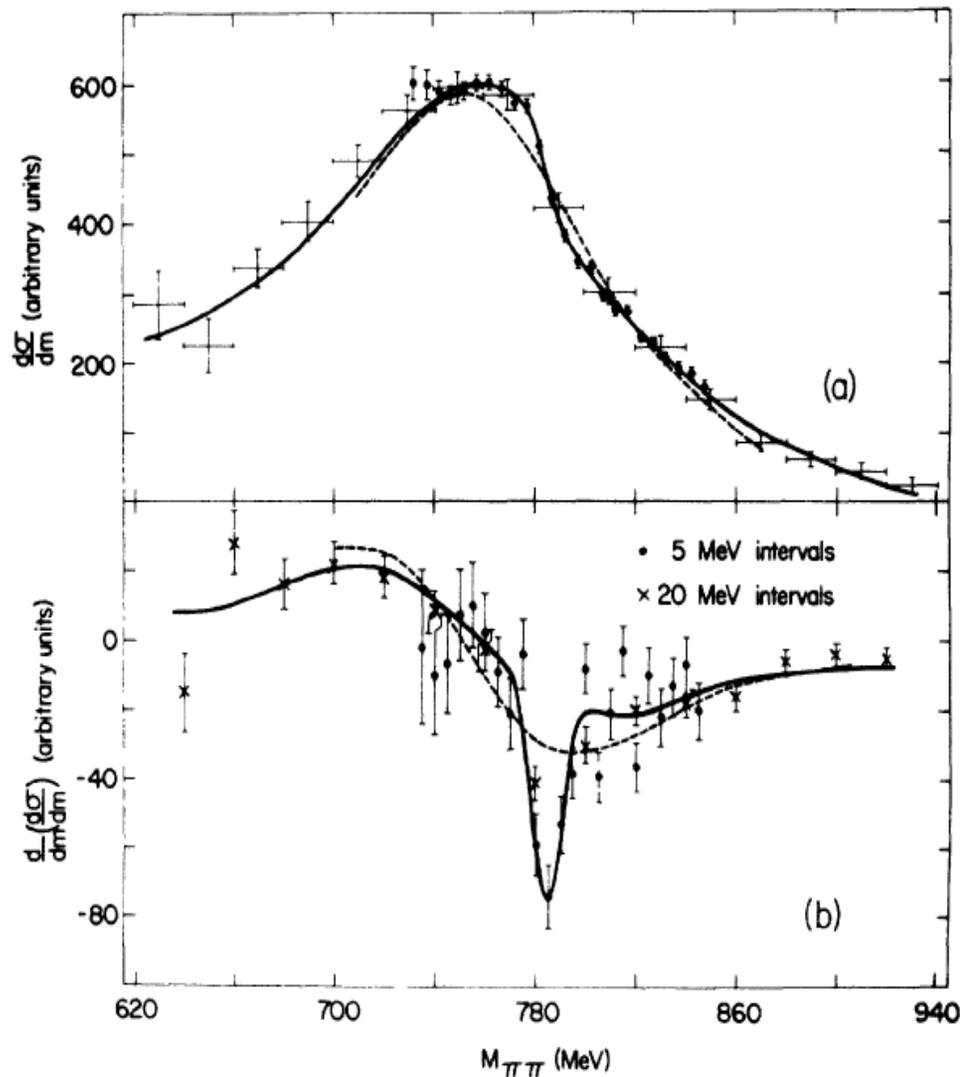


FIG. 2. (a) Mass spectrum and (b) first derivative of the mass spectrum of the π pairs photoproduced from carbon. The solid and dashed curves are fits with and without ρ^0 - ω interference.

$$\gamma A \rightarrow \pi^+ \pi^- A \quad A = \text{C, Al, Pb}$$

$$\phi_{\rho\omega} = (63 \pm 16)^\circ$$

Very little change with A

H. J. Behrend et al, Phys Rev Lett 27 (1971) 61

Photoproduction and the leptonic decay channel.

- Two experiments:

- Alvensleben *et al.*, Nucl. Phys. B25 (1971):

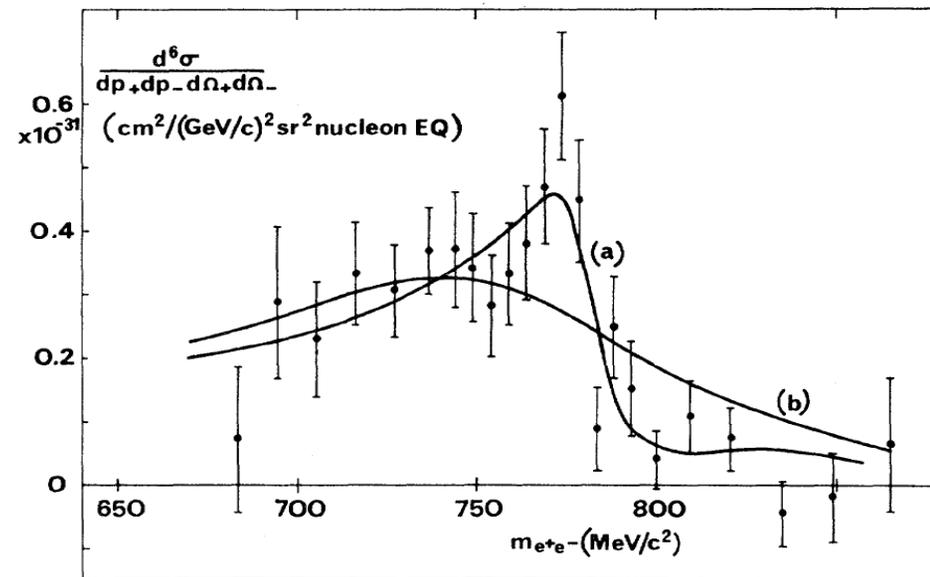
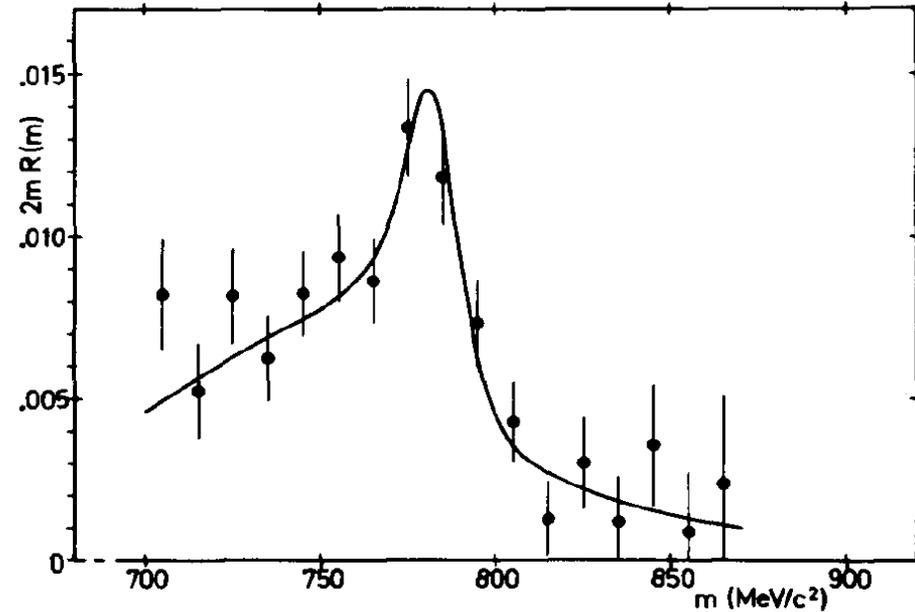
- $\gamma\text{Be} \rightarrow e^+e^-(X)$
- Published interference phase:

$$\phi_{\rho\omega} = (41 \pm 20)^\circ$$

- Biggs *et al.*, Phys. Rev. Lett. 24 (1970):

- $\gamma\text{C} \rightarrow e^+e^-(X)$
- Published interference phase:

$$\phi_{\rho\omega} = (100^{+38}_{-30})^\circ$$



Photoproduction and the leptonic decay channel.

- Two experiments:

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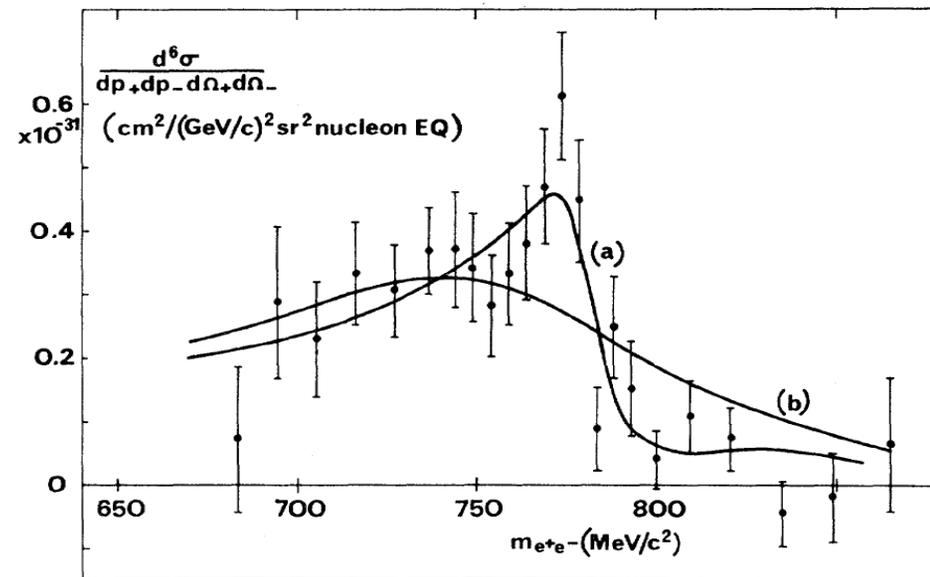
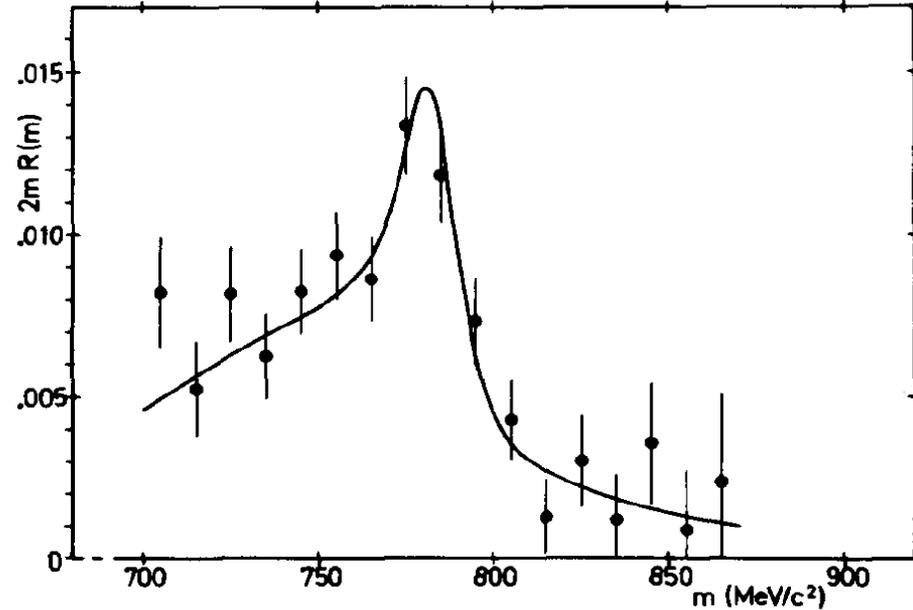
$$\phi_{\rho\omega} = (41 \pm 20)^\circ$$

→ Different phase angle

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Photoproduction and the leptonic decay channel.

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- $\gamma\text{Be} \rightarrow e^+e^-(X)$

$$\frac{Dm_\rho^4}{m^4} \left| \frac{1}{m_\rho^2 - m^2 - im_\rho\Gamma_\rho} + \frac{g_\rho^2 m_\omega^2}{g_\omega^2 m_\rho^2 m_\omega^2 - m^2 - im_\omega\Gamma_\omega} |R|e^{i\phi} \right|^2$$

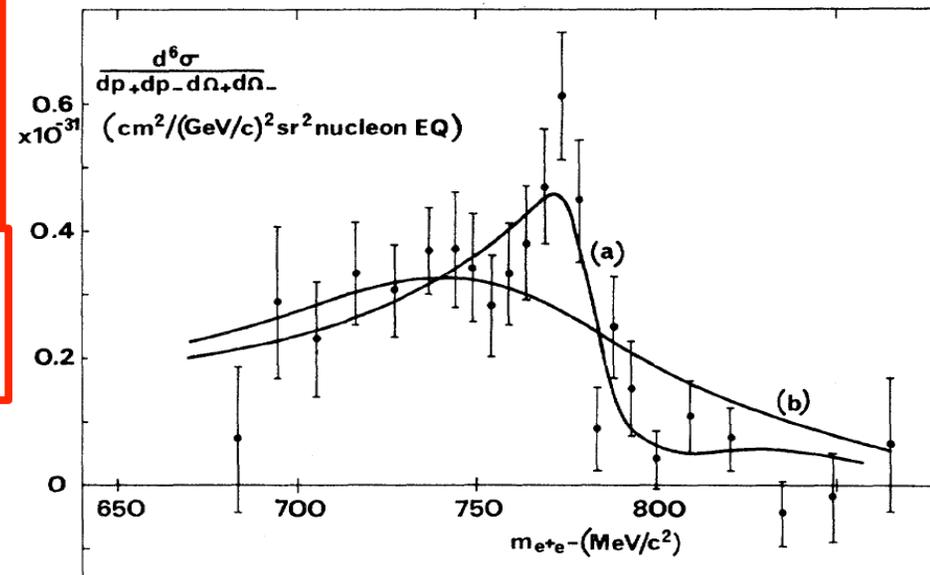
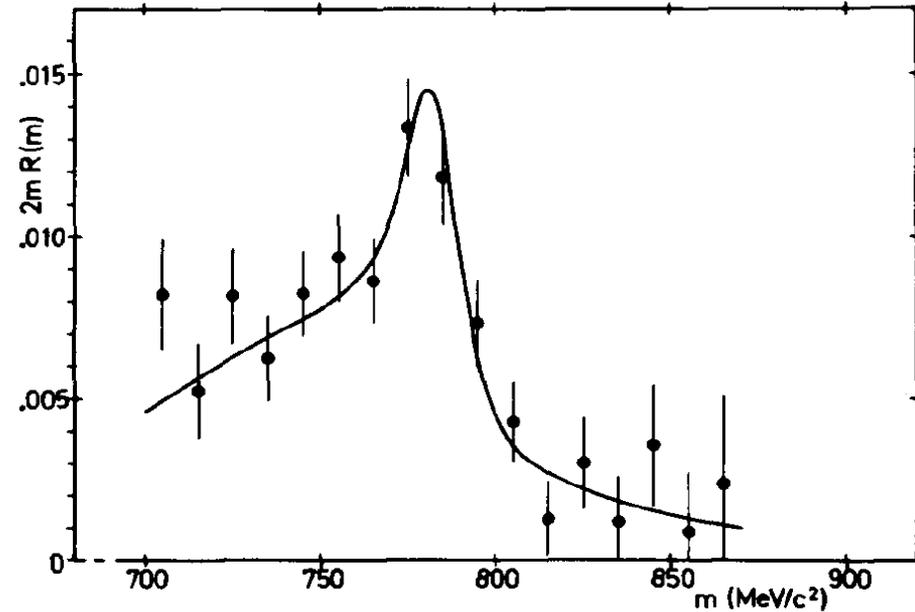


different
interference / fit formalism!!

- Biggs *et al.*, Phys. Rev. Lett. 24 (1970):

- $\gamma\text{C} \rightarrow e^+e^-(X)$

$$\frac{D}{m^2} \left| \frac{1}{m^2 - m_\rho^2 + im_\rho\Gamma_\rho} + \left(\frac{m_\omega}{m_\rho}\right)^4 \frac{\eta}{9} \frac{e^{i\phi}}{m^2 - m_\omega^2 + im_\omega\Gamma_\omega} \right|^2$$



ρ - ω interference phase in photoproduction experiments

Group	Data Sample	$\phi_{\rho\omega}$
Daresbury ('70) C	$\pi^+\pi^-$	$(104.0 \pm 5.1)^\circ$
Rochester-Cornell ('71) Al, Fe, Pb	$\pi^+\pi^-$	$(63 \pm 16)^\circ$
DESY-MIT ('71) Be	$\pi^+\pi^-$	$(96 \pm 15)^\circ$
Daresbury ('70) C	e^+e^-	$(100^{+38}_{-30})^\circ$
DESY-MIT ('70) Be	e^+e^-	$(41 \pm 20)^\circ$
FOCUS –FERMI LAB ('97) Be	$\mu^+\mu^-$	$(184.5 \pm 3.5 \pm 3.1)^\circ$

**Results quite inconsistent \rightarrow photoproduction phase in
leptonic decay considered undetermined.**

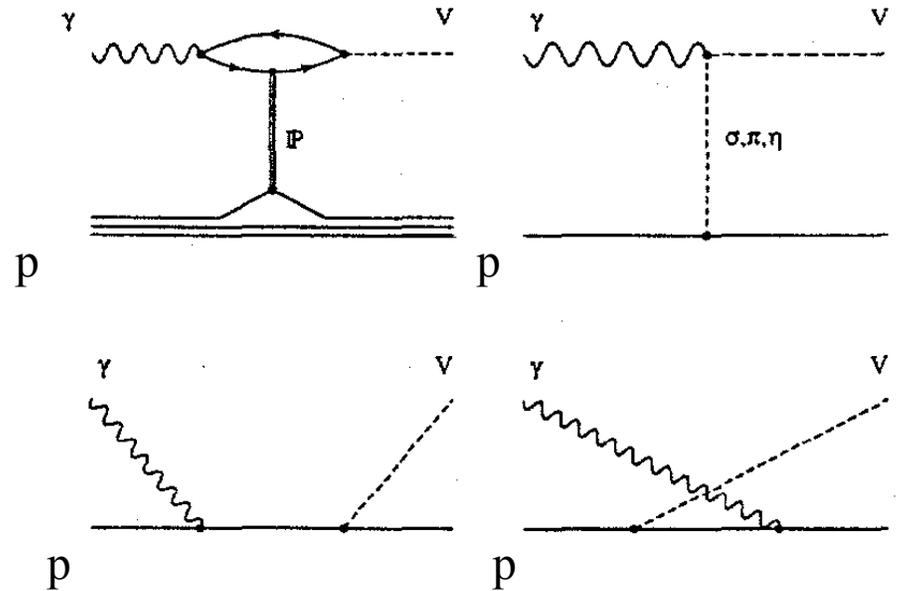
Experimental motivations for our study

- 1) Measure a high statistics data set $\gamma p \rightarrow e^+ e^- X$ at JLab energies (“baseline” for our studies in nuclei).
- 2) Extracting the Transparency ratios for the ω (CLAS g7 experiment) \rightarrow indication for ρ - ω interference. Not enough statistics.

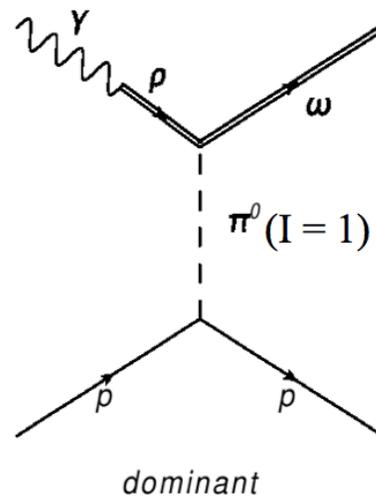
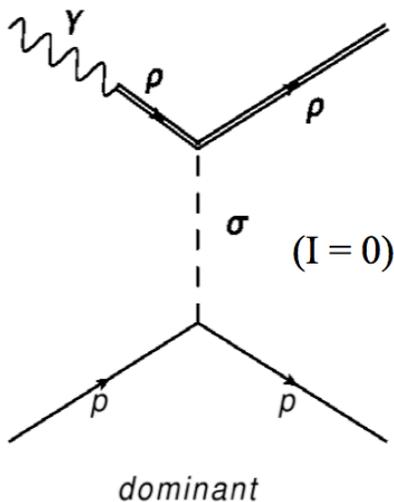
ρ, ω photoproduction on the proton

t-channel VM production:

- At high energies, Pomeron exchange
- Closer to threshold, meson exchange model (π, σ, η)

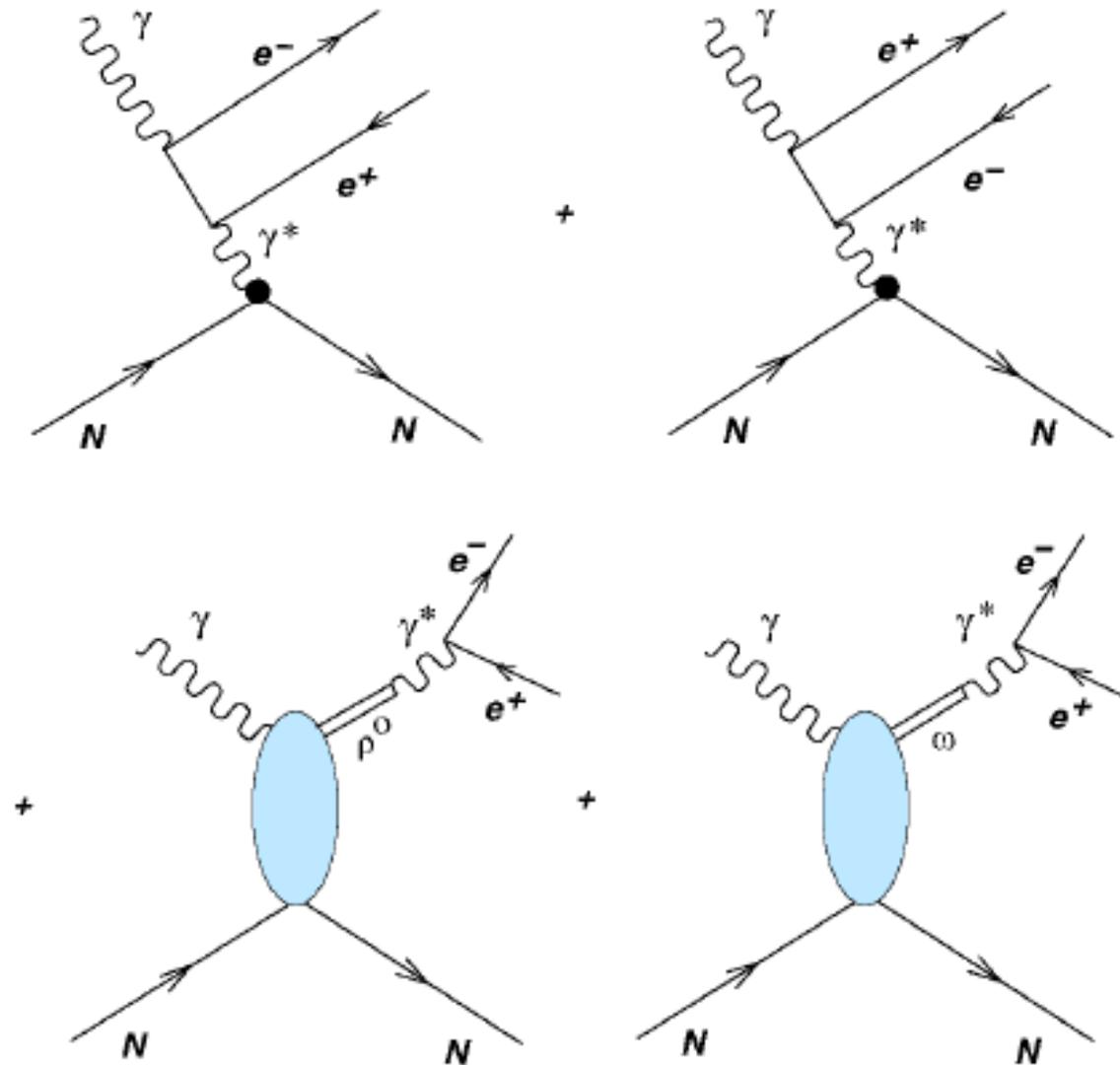


Friman and Soyeur model [NPA600, 477(1996)] at low energies:



The elementary reaction $\gamma p \rightarrow e^+ e^- p$

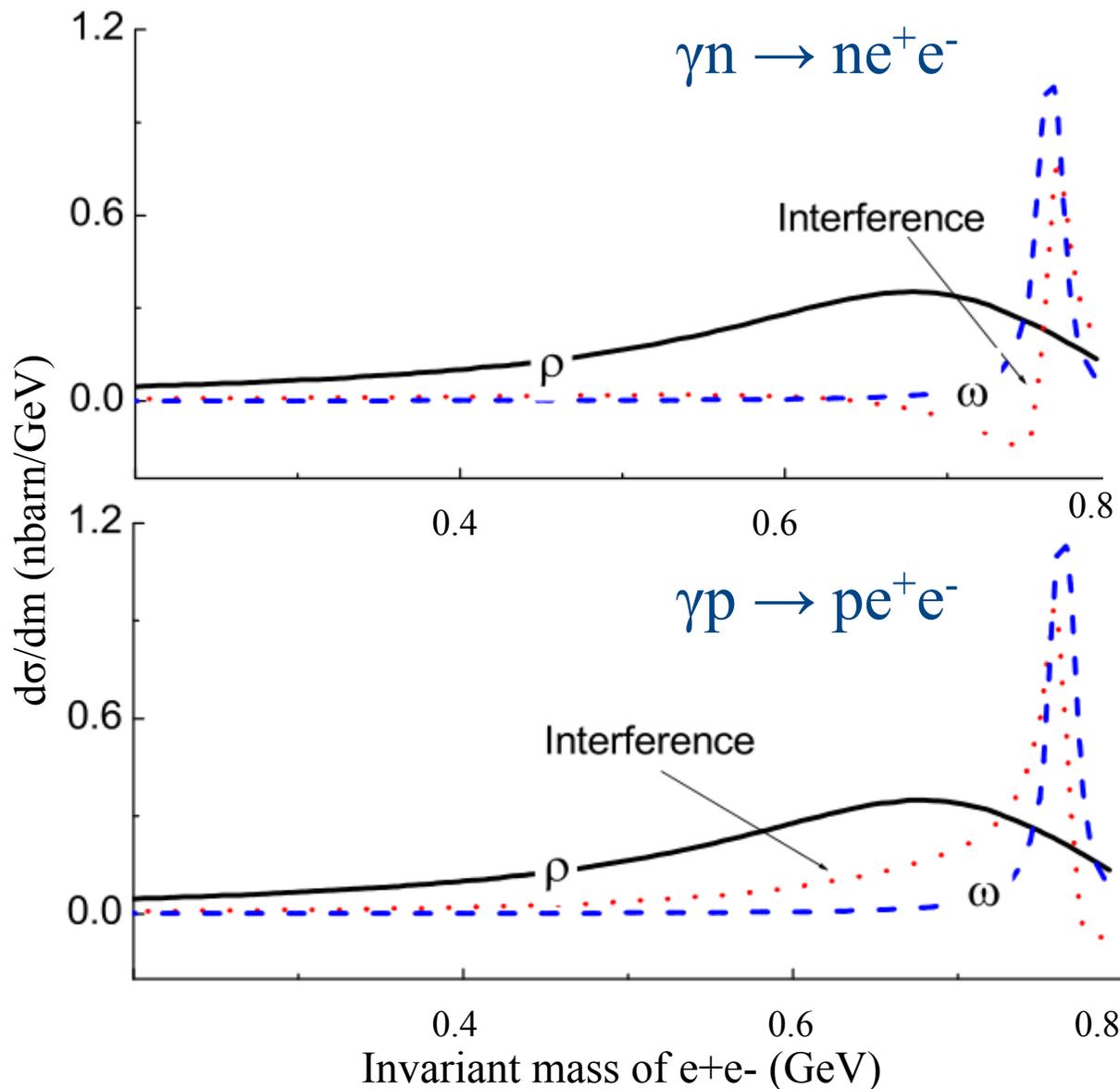
M.F.M Lutz and M.Soyeur, Nucl. Phys. A760 (2005) 85



Bethe-Heitler and vector meson decay contributions to the $\gamma N \rightarrow e^+ e^- N$ amplitude.

The elementary reaction $\gamma p \rightarrow e^+ e^- p$

M.F.M Lutz and M.Soyeur, Nucl. Phys. A760 (2005) 85



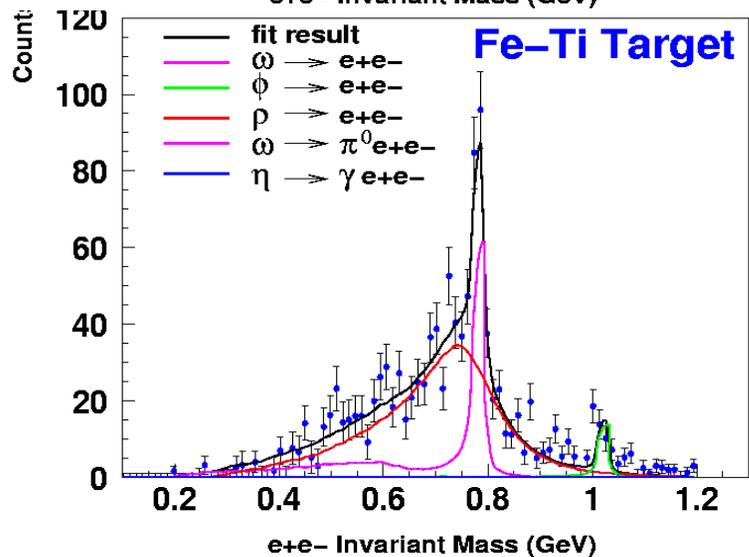
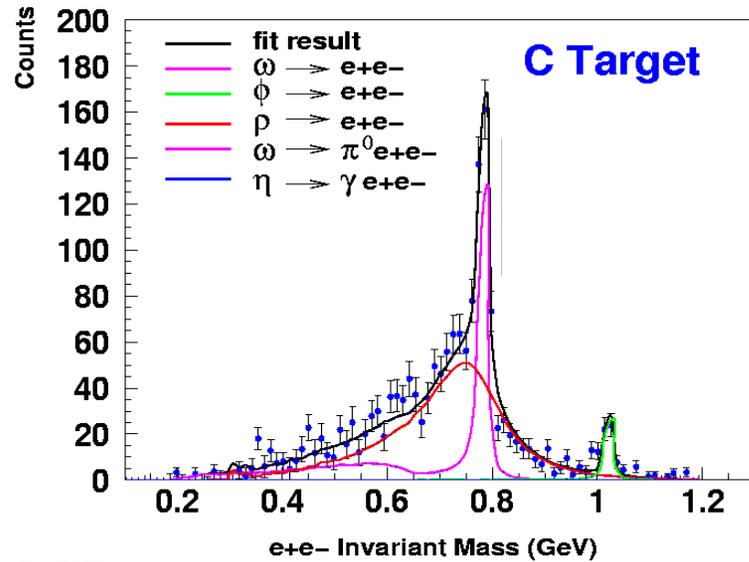
- Calculations predict the interference pattern to change depending on the target nucleon:
destructive on n

constructive on p

- The BH-mesons interference is shown to be negligible

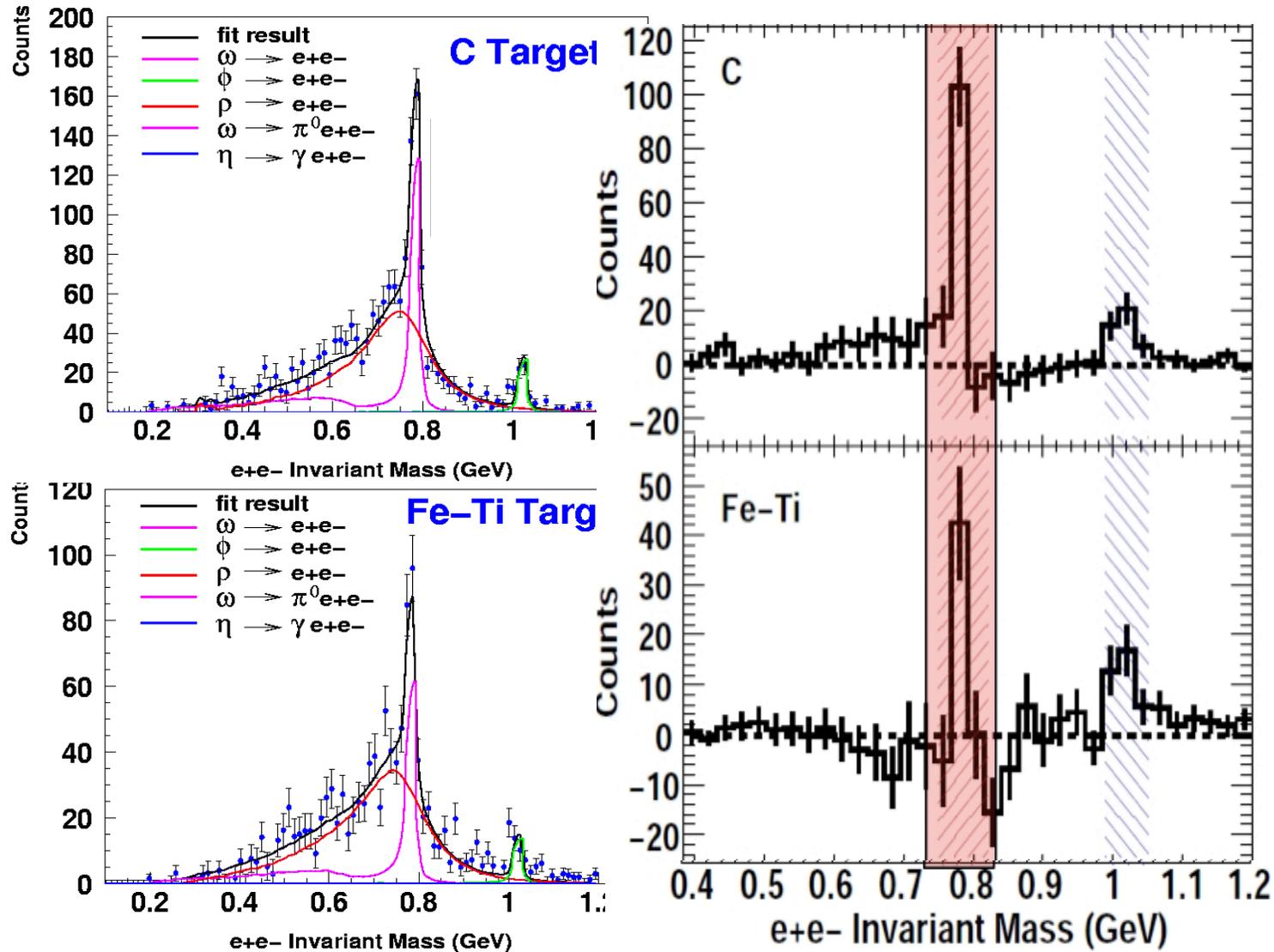
JLab g7: Possible ρ - ω Interference

After Background subtraction, mass spectra mainly ρ , ω and ϕ .



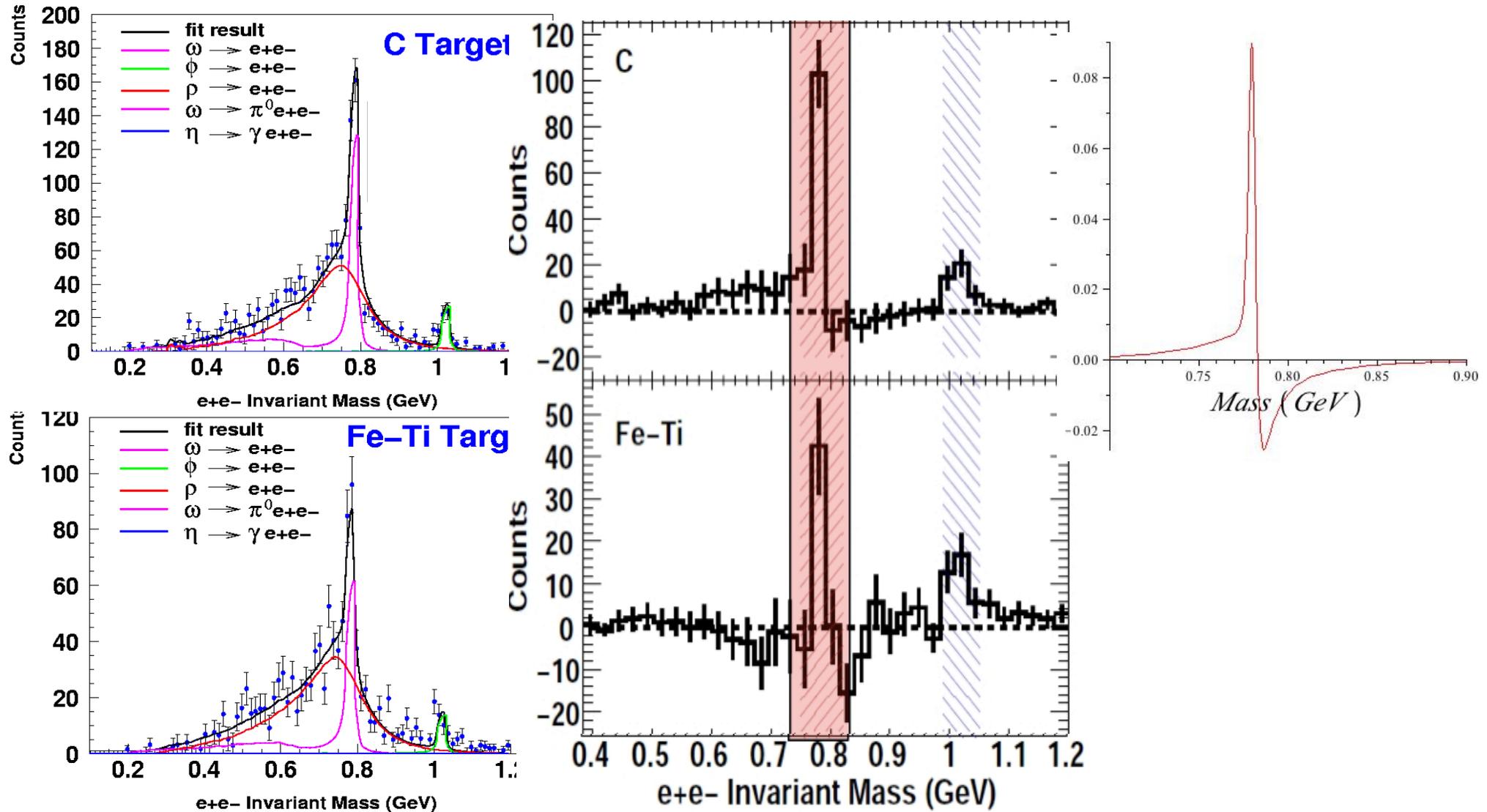
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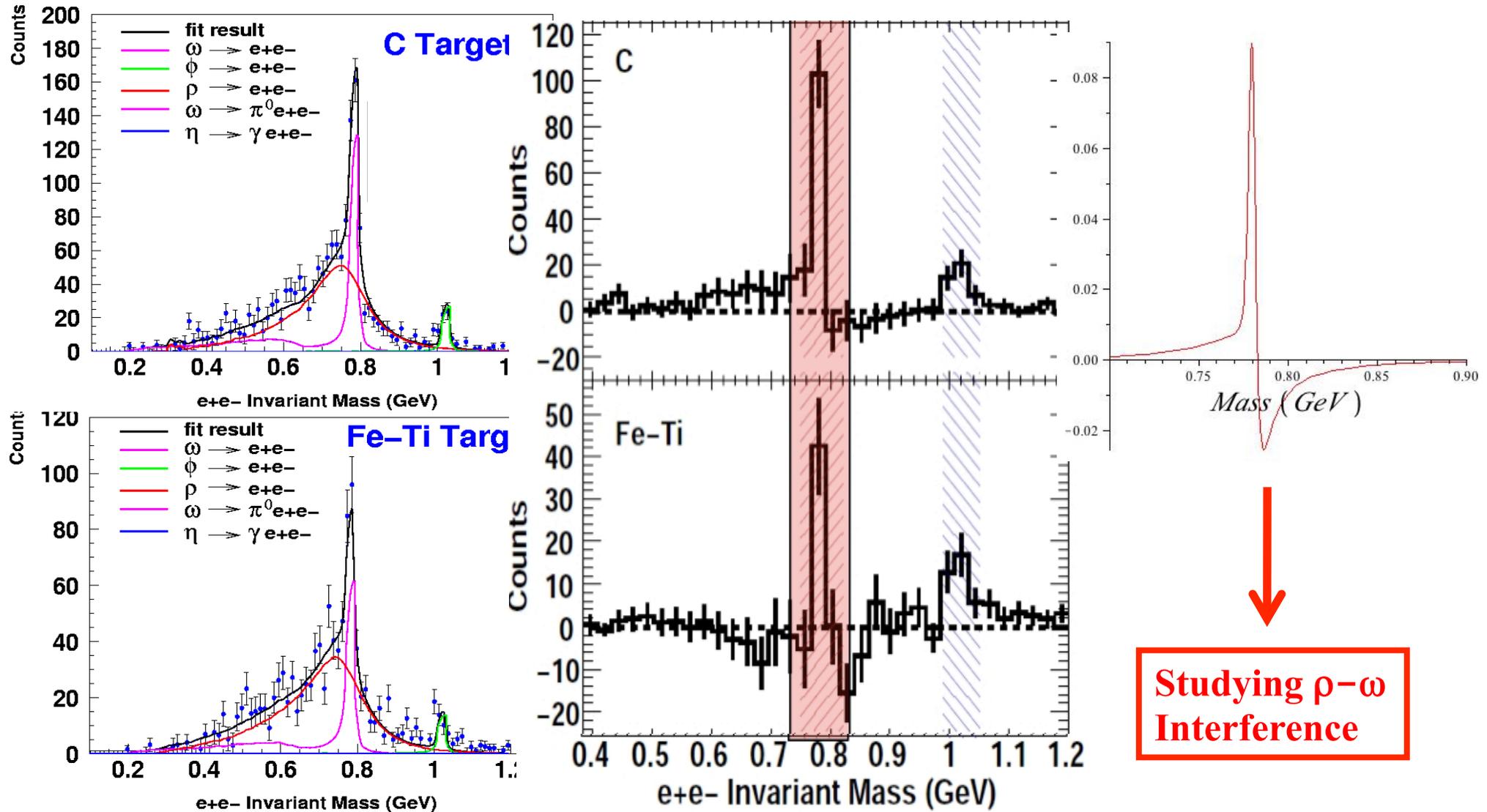
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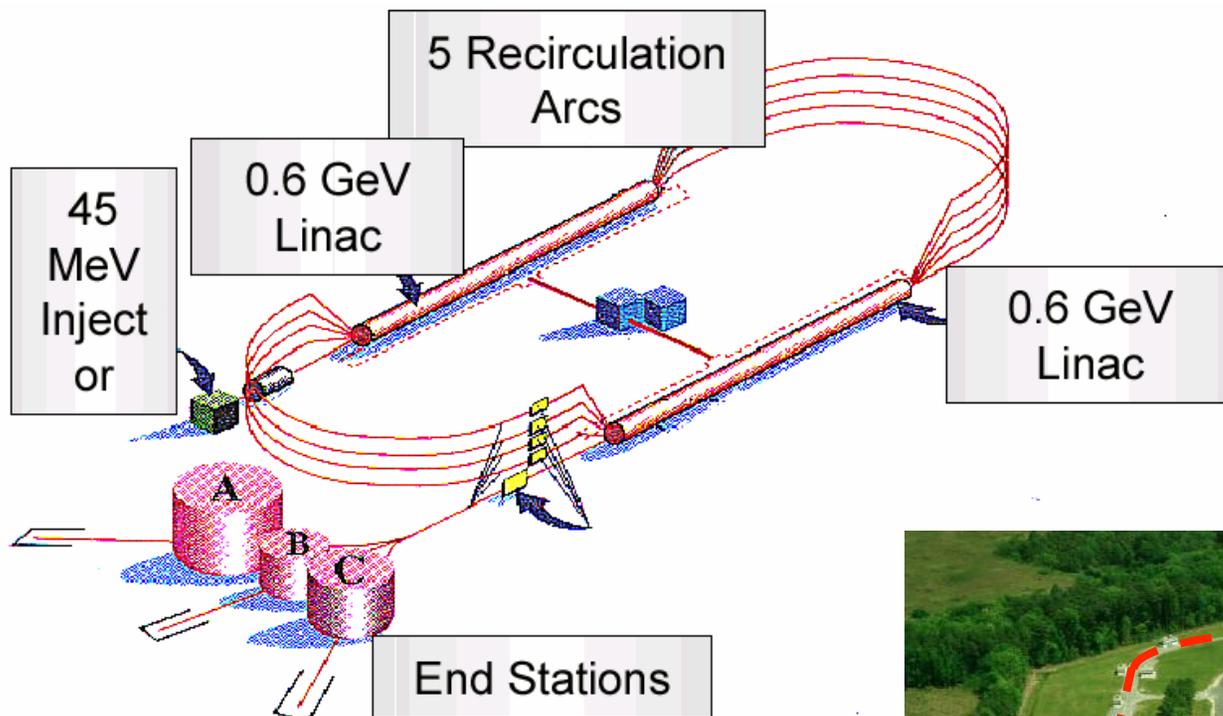


JLab g7: Possible ρ - ω Interference

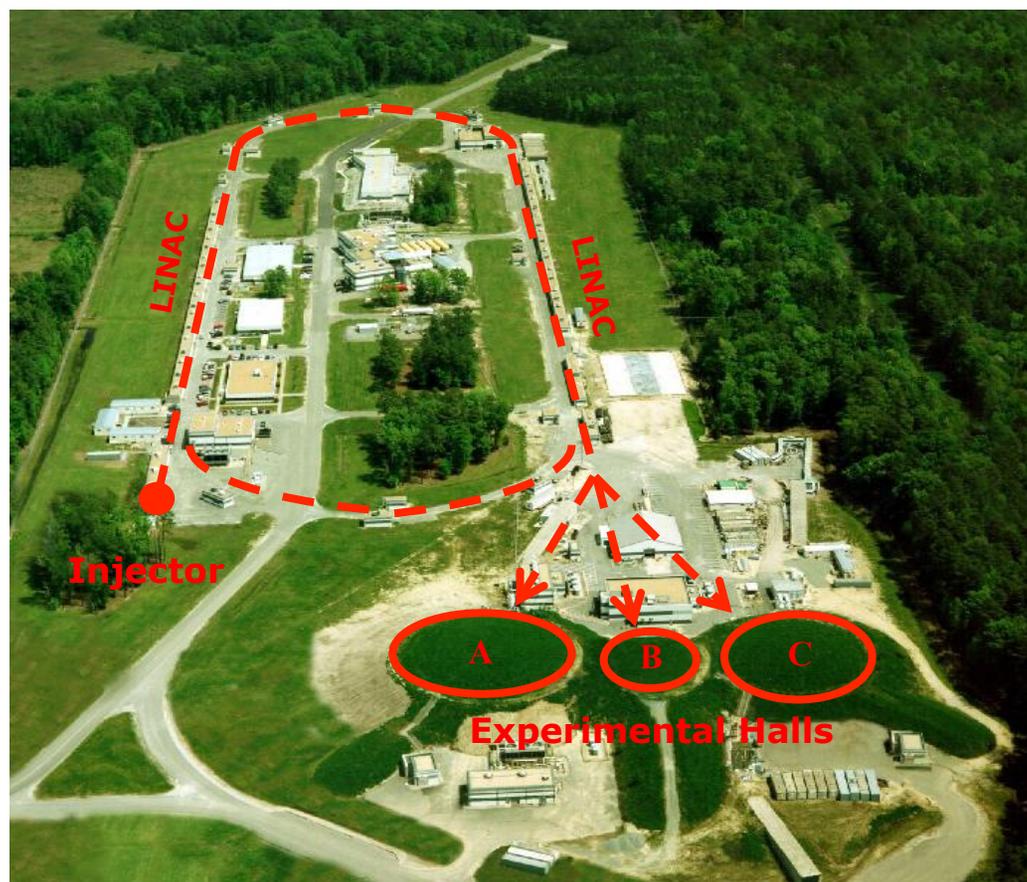
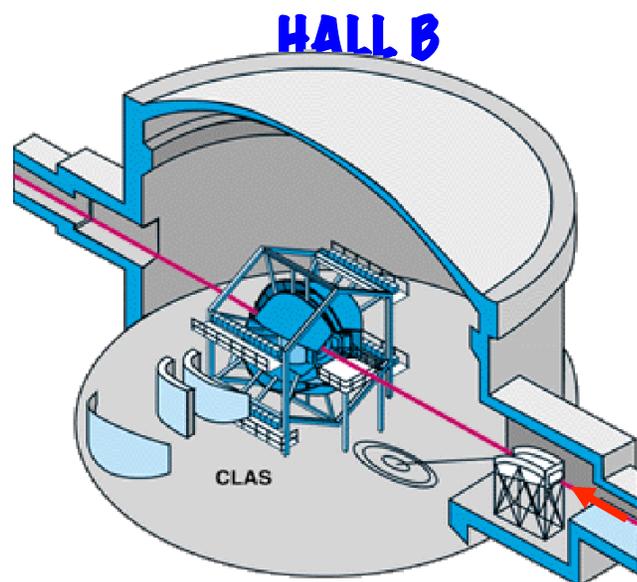
After Background subtraction, mass spectra mainly ρ , ω and ϕ .



Jlab "6GeV": The "old" 6 GeV Accelerator



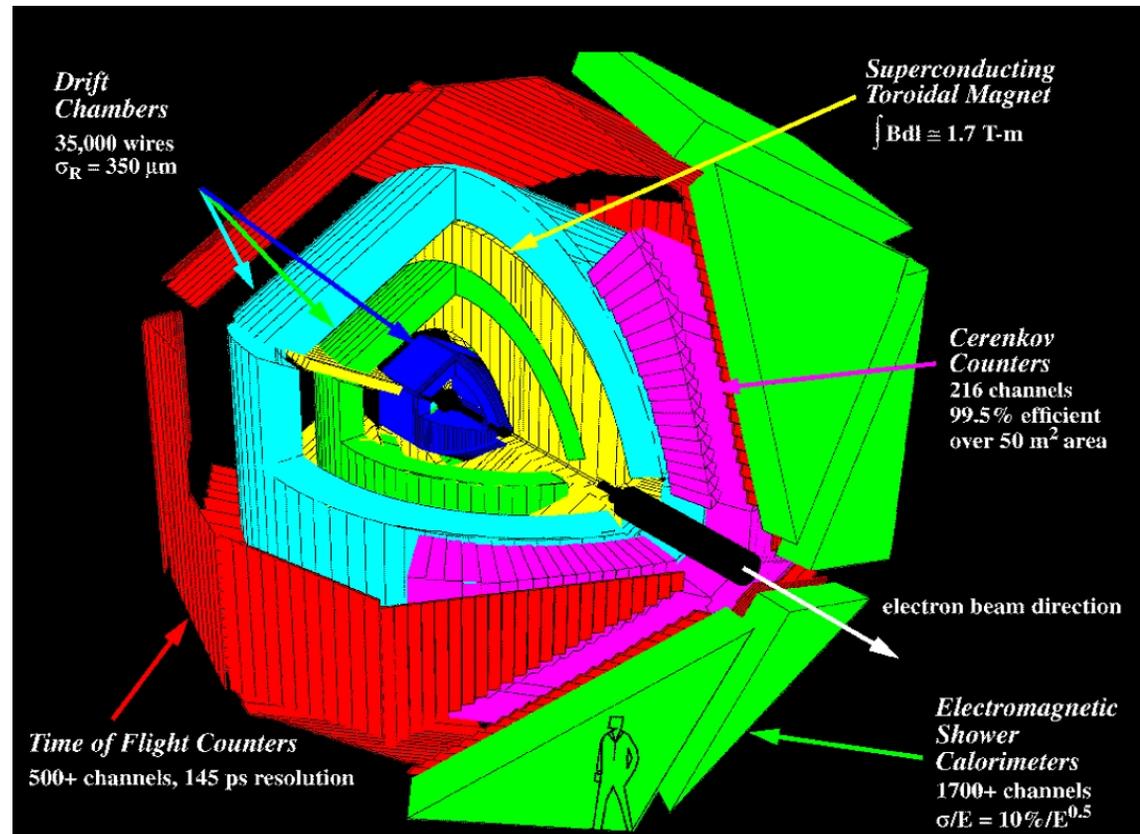
E_{\max}	$\sim 6 \text{ GeV}$
I_{\max}	$\sim 200 \mu\text{A}$
Duty Factor	$\sim 100\%$
σ_E/E	$\sim 2.5 \cdot 10^{-5}$
Beam P	$\sim 80\%$
$E_g(\text{tagged})$	$\sim 0.8- 5.5 \text{ GeV}$



CLAS Experiment g12

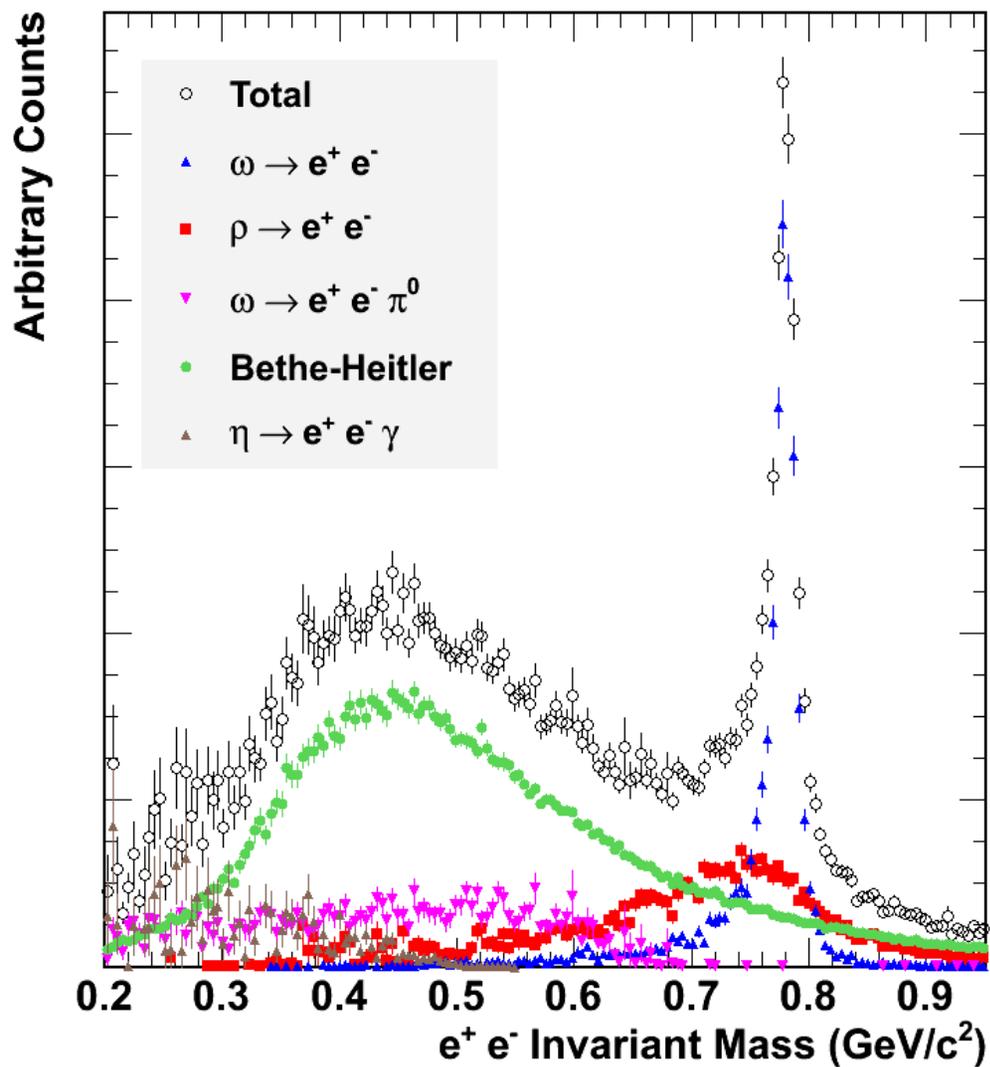
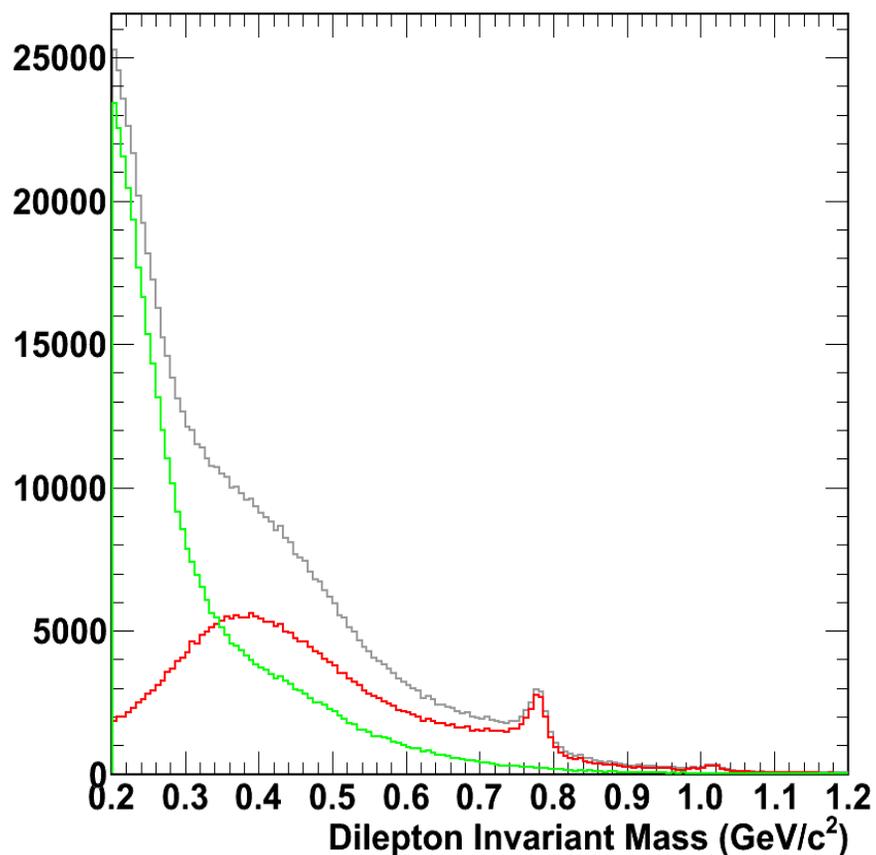
$\gamma p \rightarrow e^+ e^- X$ channel, parallel trigger

- Hall-B houses the CLAS detector, ideal for photoproduction and lepton identification.
- g12 in CLAS
 - ✓ 44 days of beam
 - ✓ Tagged Photons E_γ [1.1 to 5.5 GeV] incident on a LH_2 target
 - ✓ 26.2×10^9 production triggers (3 x 10^6 di-lepton triggers)
 - ✓ EC and CC combine to provide an e/π rejection factor better than 10^{-6} for di-lepton pairs.
 - ✓ LH_2 target placed 90 cm upstream



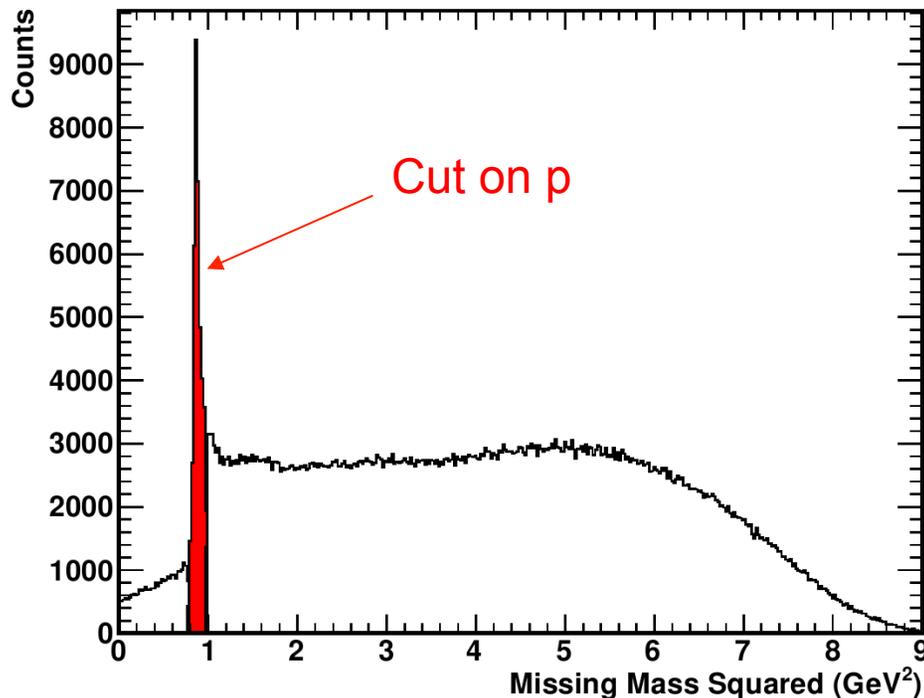
Signal and Background

- Looking for $\rho \rightarrow e^+ e^-$ and $\omega \rightarrow e^+ e^-$
 - ✓ Bethe-Heitler is significant and must be accounted for. The upstream location of the target increases the small angle acceptance. (angle cut)

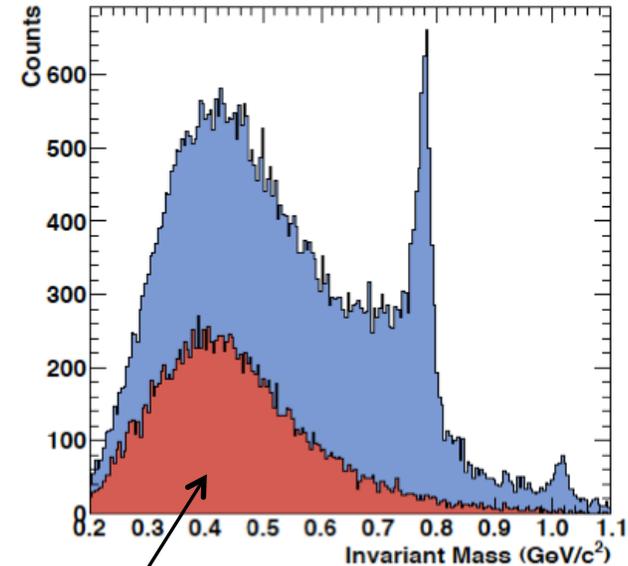


Selecting an Outgoing Proton

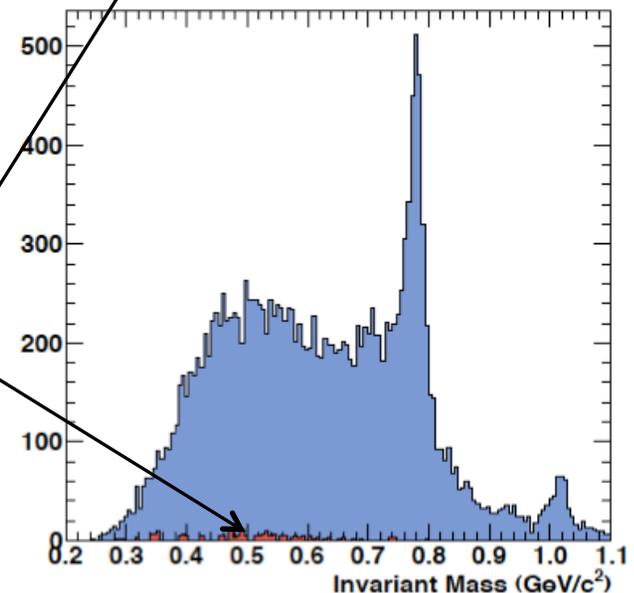
- Initial cuts must be made on the missing mass to isolate a proton in the final state.



- ✓ Uncorrelated lepton pairs are also eliminated by tight missing mass cuts on the proton.



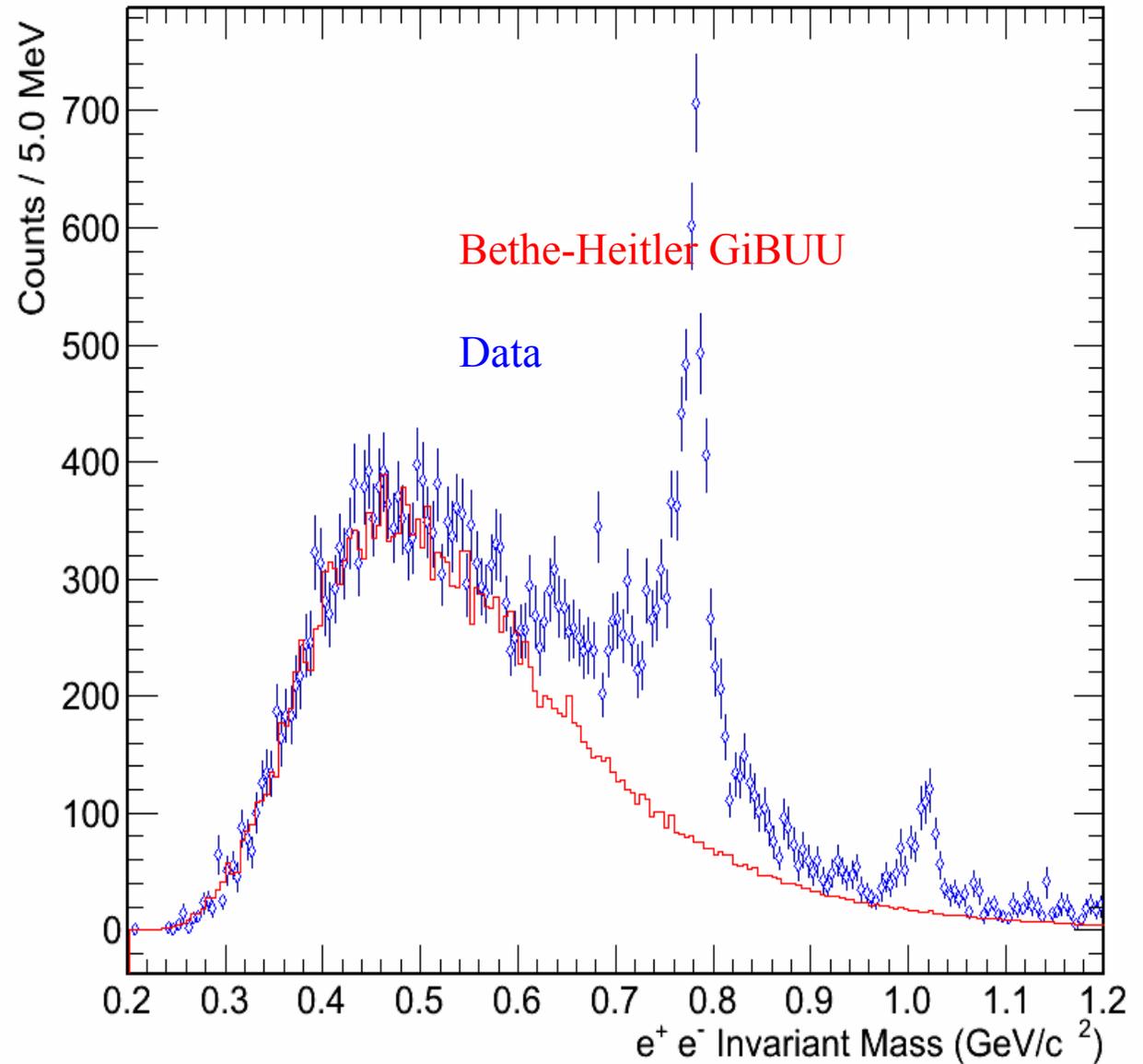
No cut



cut

BH subtraction

After lepton acceptance correction, missing proton selection, timing, and vertex cuts, the Bethe-Heitler is calculated by GiBUU and subtracted



The ρ - ω invariant mass spectrum is now ready for the fit

Interference Formalism, cont.

- The a phase is then introduced, accounting for the cross amplitudes and mass term:

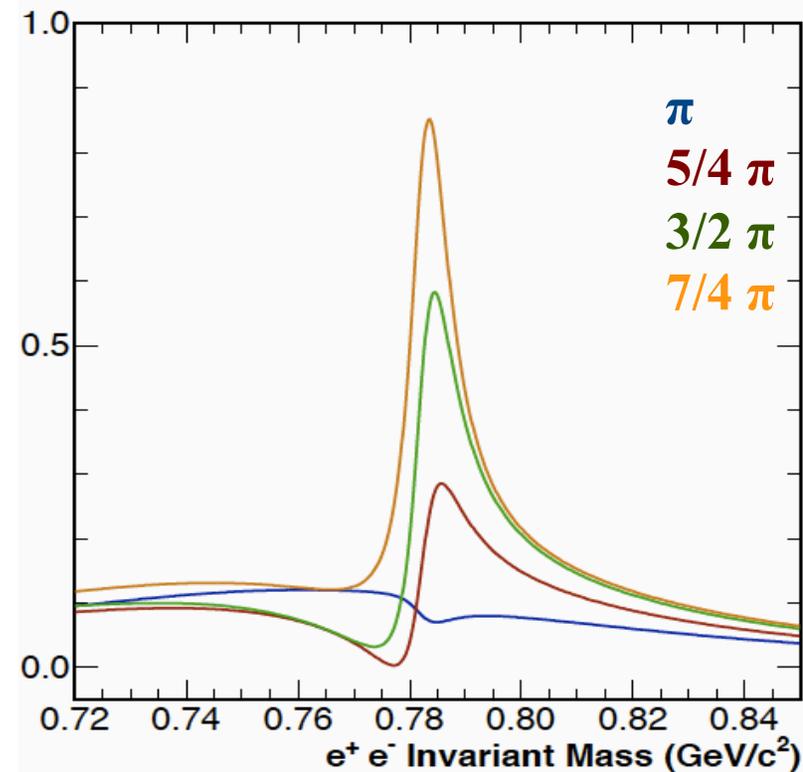
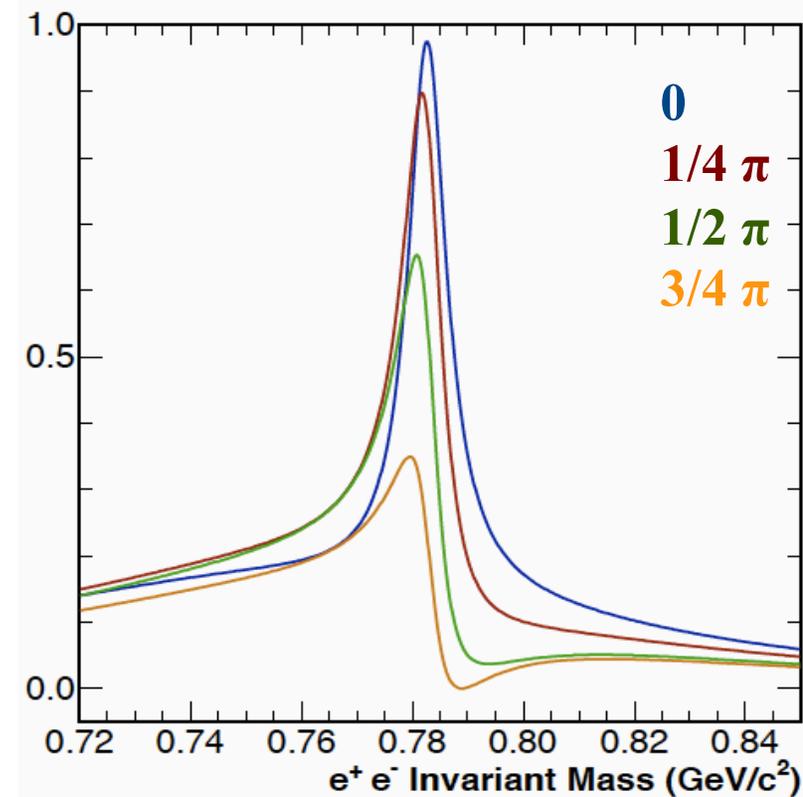
$$1 - ie^{i\phi_\rho} = -\frac{\delta}{M_\rho} \left(\frac{T_\rho A_\omega + T_\omega A_\rho}{T_\omega A_\omega} \right)$$

- The amplitude is then rewritten as a combination of the meson amplitudes with a complex phase term:

$$F = f_\rho + ie^{i\phi_\rho} f_\omega$$

- When squared, the amplitude takes the form:

$$F^2 = f_\rho^2 + f_\omega^2 - \frac{2a}{b^2 + c^2} (b \sin \phi_\rho + c \cos \phi_\rho)$$



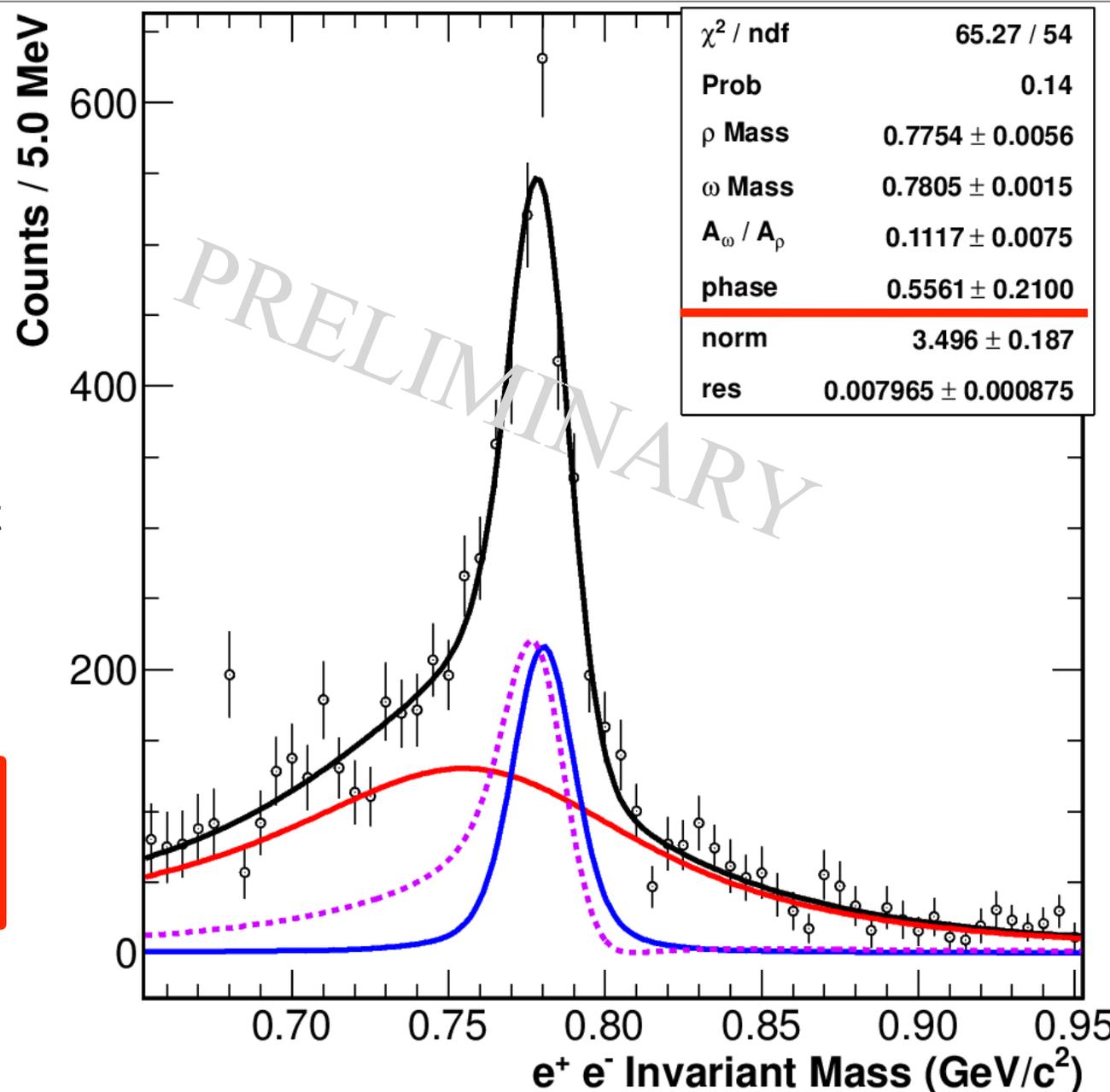
Preliminary Results

- Two Relativistic Breit-Wigner functions
- Interference term
- Gaussian convolution

- The ρ and ω widths are set to the PDG value.
- $\chi^2/\text{ndf} = 1.21$
- Interference phase of:

$$\phi_{\rho\omega} = (32 \pm 12)^\circ$$

Stat uncertainties only



Fits of g12 data using Biggs' function

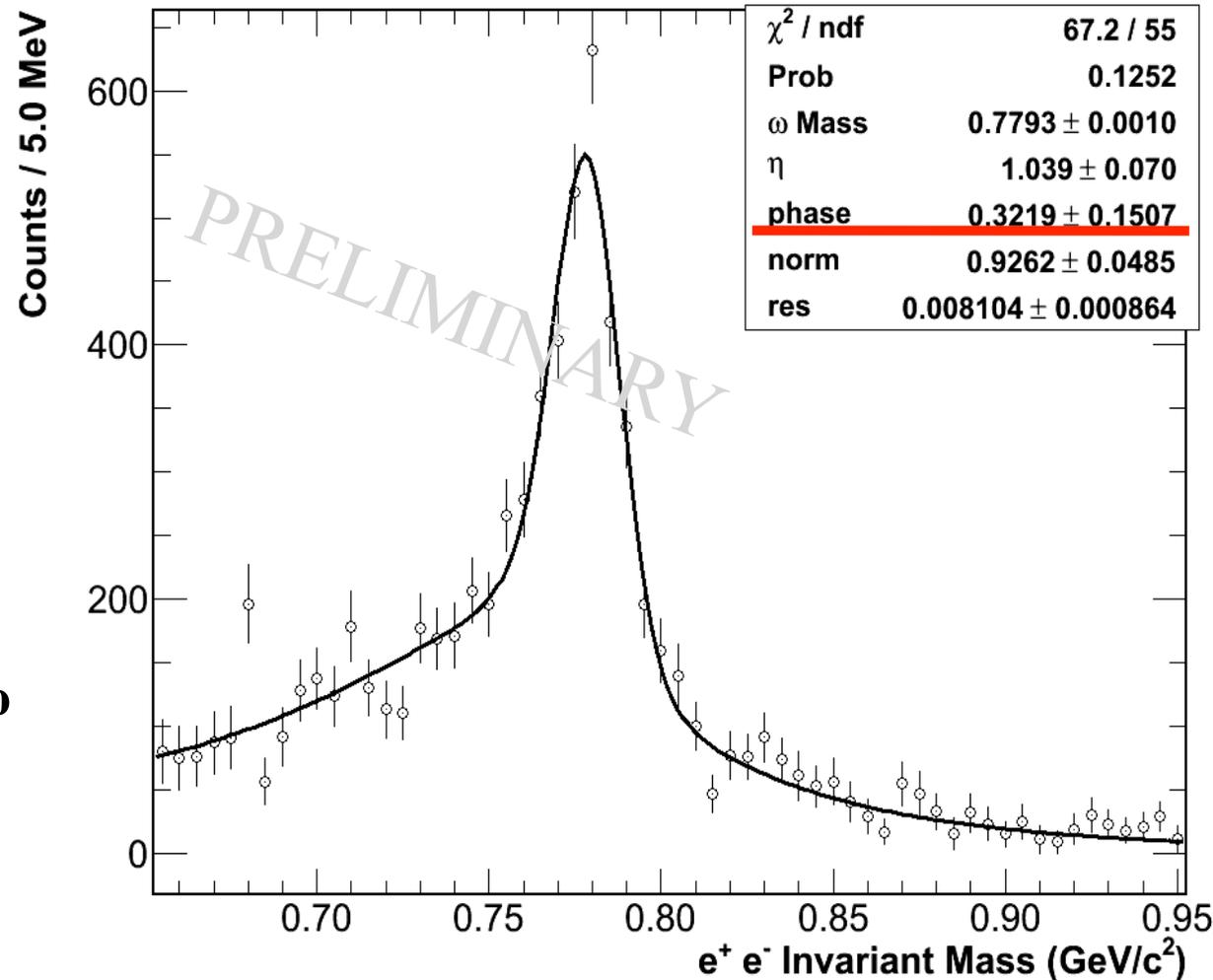
Biggs Function

- The ρ and ω widths are set to the PDG value.
- $\chi^2/\text{ndf} = 1.22$
- Interference phase of:

$$\phi_{\rho\omega}^{\text{H}} = (18.5 \pm 8.6)^\circ$$

This phase on H can be compared to the one measured on C:

$$\phi_{\rho\omega}^{\text{C}} = (100^{+38}_{-30})^\circ$$



Phases are very different. Target dependence?

Summary and outlook

- ◆ The CLAS g12 experiment at JLab has generated large statistics data in the $\gamma p \rightarrow e^+e^-X$ channel.
- ◆ Vector mesons clearly seen. After subtracting the Bethe-Heitler “background”, the fit to the ρ - ω mass region clearly shows an interference in the di-lepton channel.

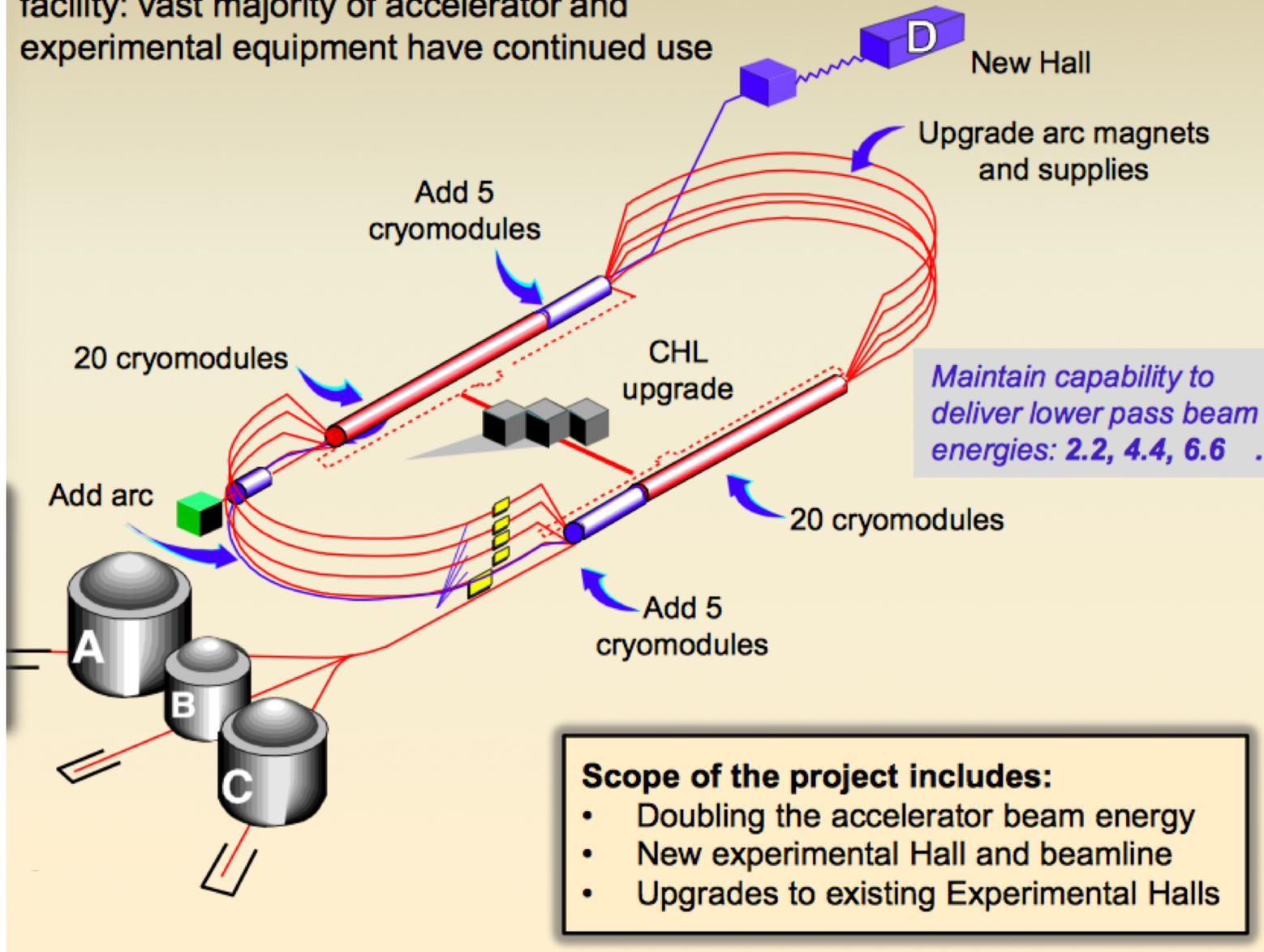
preliminary result : $\phi_{\rho\omega} = (32. \pm 12.)^\circ$ **(stat)**

- ◆ Careful when comparing with other published results
- ◆ Systematic uncertainties being determined, PRL draft ready.
- ◆ Target/Medium dependence of interference phase?
- ◆ Extension of studies with CLAS12?

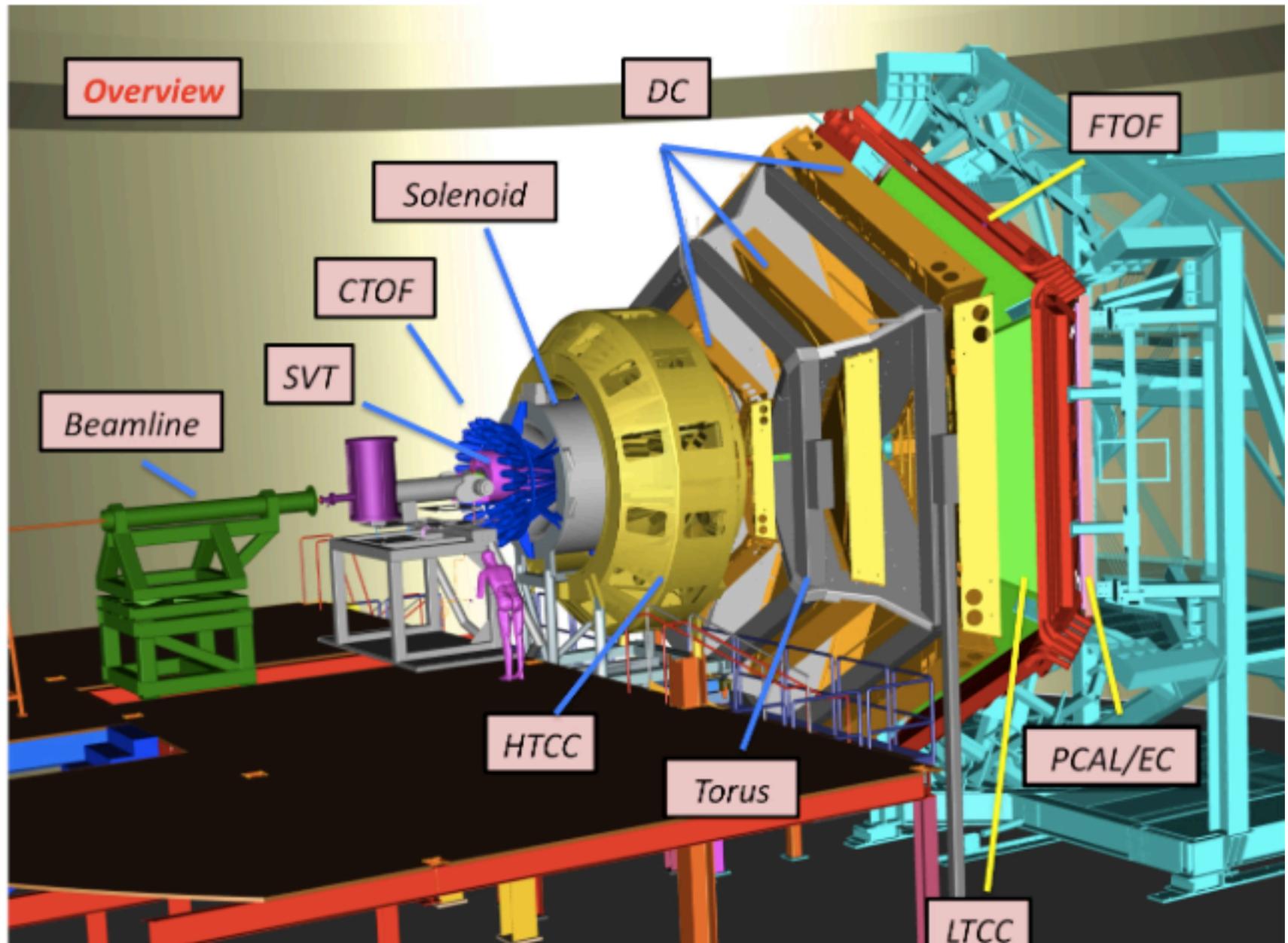
Backup Slides

Jlab "12GeV": The "new" 12 GeV Accelerator Coming very soon!

Upgrade is designed to build on existing facility: vast majority of accelerator and experimental equipment have continued use



CLAS 12 Detector



Interference Formalism

- The ρ - ω interference can be described by constructing a complex and symmetric mass matrix:

$$M = \begin{bmatrix} M_\rho & -\delta \\ -\delta & M_\omega \end{bmatrix} \quad M_a = (m^2 - m_a^2 + im\Gamma_a)/m\Gamma_a$$

- The propagator can then be constructed as:

$$P = |M|^{-1} = \frac{1}{M_\rho M_\omega - \delta^2} \begin{bmatrix} M_\omega & +\delta \\ +\delta & M_\rho \end{bmatrix} \approx \begin{bmatrix} 1/M_\rho & \delta/M_\rho M_\omega \\ \delta/M_\rho M_\omega & 1/M_\omega \end{bmatrix}$$

- And the amplitude then takes the form:

$$F(e^+e^-) = [T(\rho \rightarrow e^+e^-) \quad T(\omega \rightarrow e^+e^-)]P \begin{bmatrix} A(\gamma p \rightarrow \rho) \\ A(\gamma p \rightarrow \omega) \end{bmatrix}$$

- Combining to make:

$$F(e^+e^-) = \frac{T_\rho A_\rho}{M_\rho} + \frac{T_\omega A_\omega}{M_\omega} + \frac{\delta(T_\rho A_\omega + T_\omega A_\rho)}{M_\omega M_\rho}$$

Fitting Procedure

- The ρ - ω invariant mass spectrum is fitted with:
 - Two Relativistic Breit-Wigner functions

$$\frac{m^2}{(m^2 - m_a^2)^2 + \Gamma_a^2 m^2}$$

- With a mass dependent ρ width:

$$\Gamma_\rho(m, m_{\rho 0}, \Gamma_{\rho 0}) = \Gamma_{\rho 0} \left(\frac{m_{\rho 0}}{m} \right) \left(\frac{m^2 - 4m_\pi^2}{m_{\rho 0}^2 - 4m_\pi^2} \right)^{3/2}$$

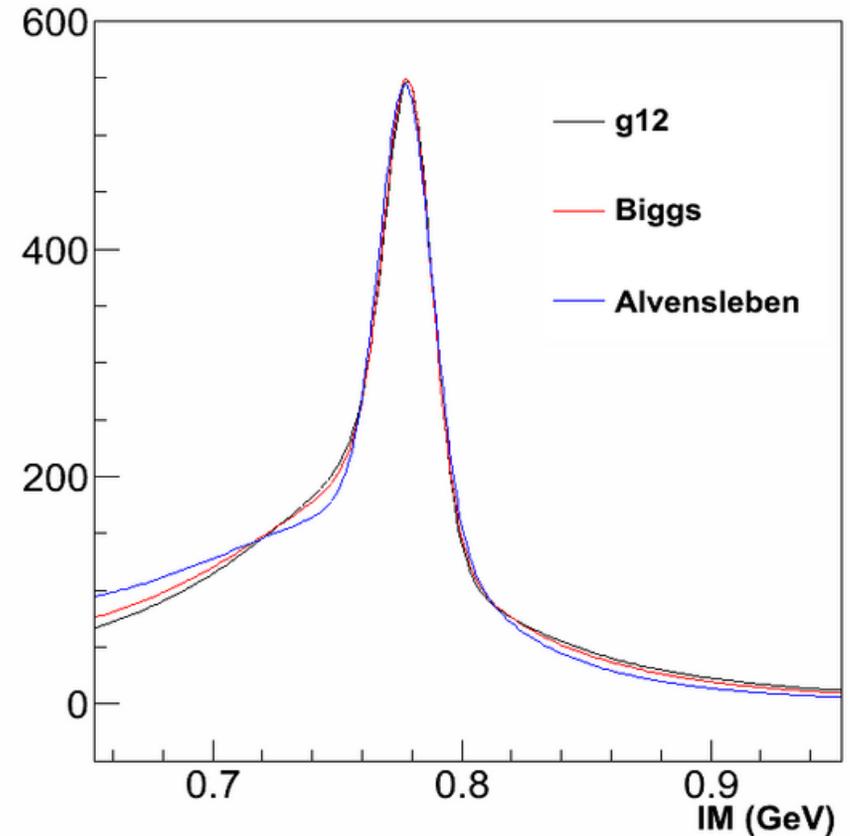
- Interference term
- Gaussian convolution

Different functional forms for ρ , ω and interference

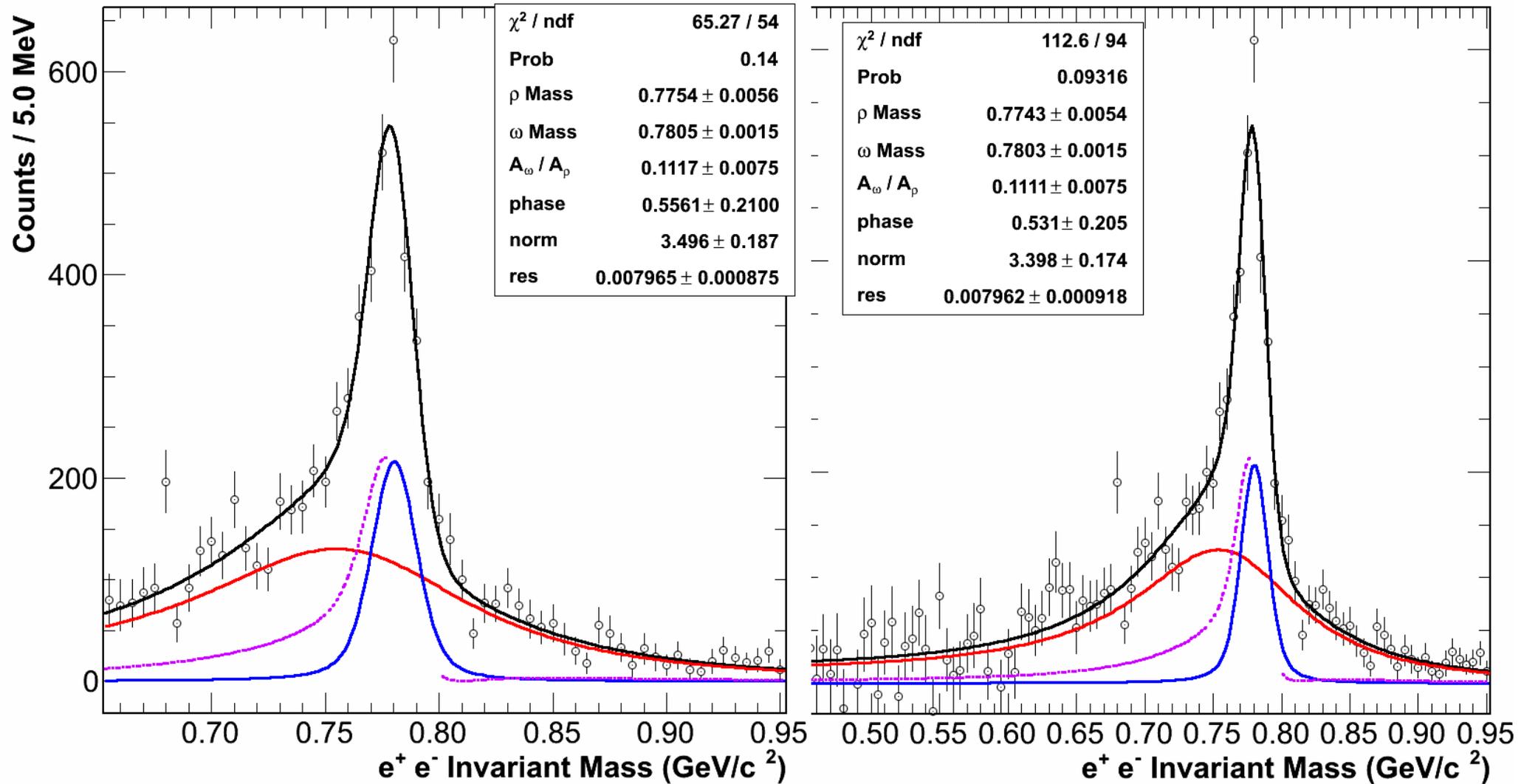
$$F_{g12}^2 = \frac{D A_\rho^2 m_\rho^4}{m} \left| \frac{1}{(m_\rho^2 - m^2) + im_\rho \Gamma_\rho} + \frac{A_\omega m_\omega^2}{A_\rho m_\rho^2} \frac{e^{i\phi}}{(m_\omega^2 - m^2) + im_\omega \Gamma_\omega} \right|^2$$

$$F_{Biggs}^2 = \frac{D}{m^2} \left| \frac{1}{m^2 - m_\rho^2 + im_\rho \Gamma_\rho} + \left(\frac{m_\omega}{m_\rho} \right)^4 \frac{\eta}{9} \frac{e^{i\phi}}{m^2 - m_\omega^2 + im_\omega \Gamma_\omega} \right|^2$$

$$F_{Alvensleben}^2 = \frac{D m_\rho^4}{m^4} \left| \frac{1}{m_\rho^2 - m^2 - im_\rho \Gamma_\rho} + \frac{g_\rho^2 m_\omega^2}{g_\omega^2 m_\rho^2} \frac{|R| e^{i\phi}}{m_\omega^2 - m^2 - im_\omega \Gamma_\omega} \right|^2$$

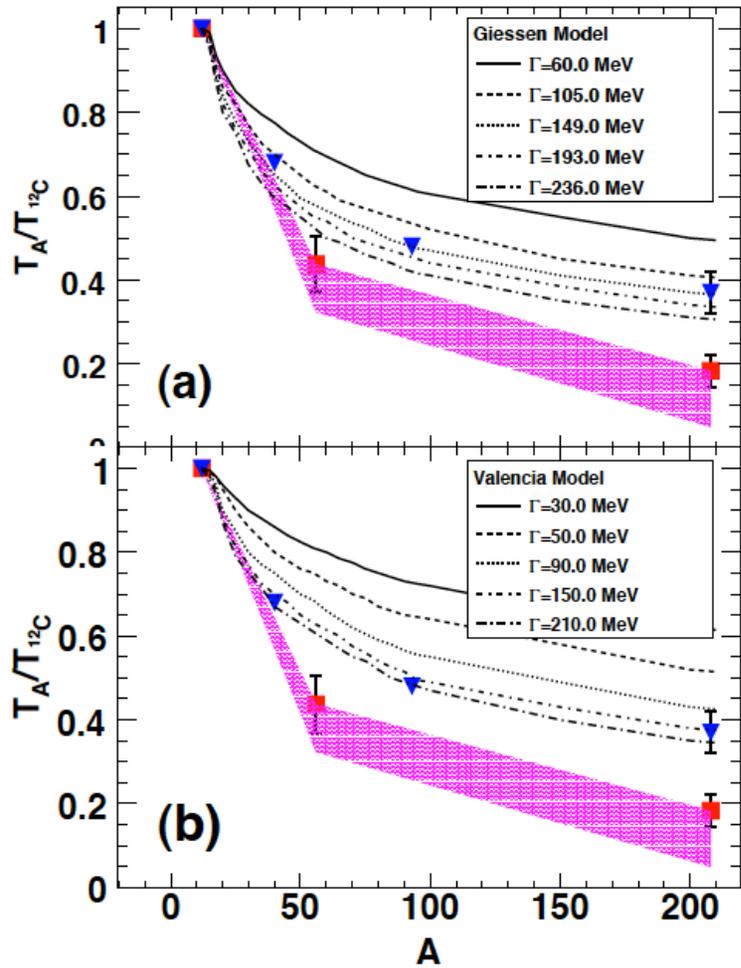


Systematic uncertainties (effect of range of MM)



Jlab Transparency ratios for ω

$$\gamma A \rightarrow e^+ e^- (X)$$



$$\omega \rightarrow e^+ e^-$$

Wood *et al*, Phys. Rev. Lett. 105 2010

- Transparency ratios in the dilepton decay channel indicate a very large in-medium width for the ω

$$(\Gamma_{\omega} > 200 \text{ MeV})$$

- Once ρ meson is subtracted, the “negative yield” on the high invariant mass side of the ω -peak is indicative of ρ - ω interference.

