

# Azimuthal distributions in unpolarized SIDIS

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# Outline

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- Motivation
- The Experiment
- Analysis
  - event selection & binning
  - acceptance studies
  - radiative corrections
- Results
- Comparison with higher energies
- Summary

# SIDIS kinematical plane

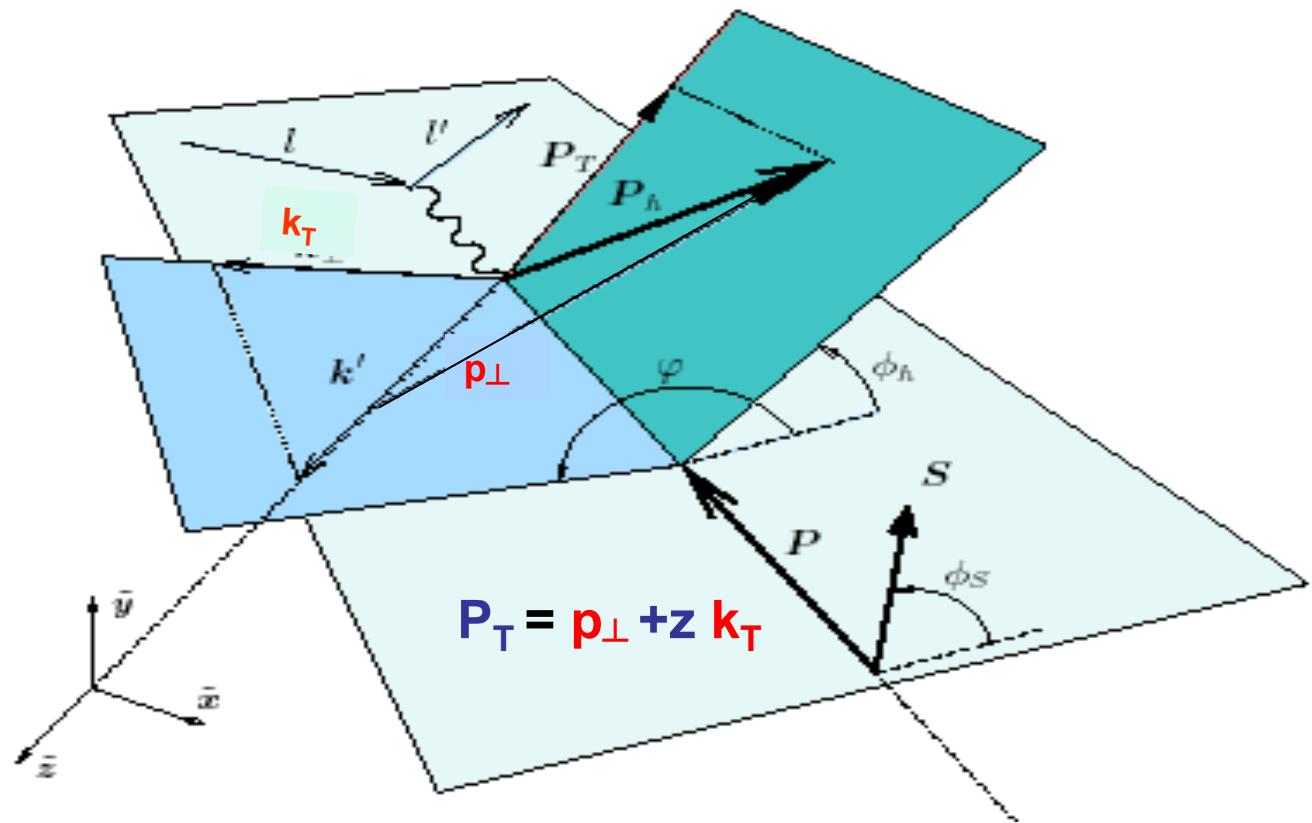
$$\nu = (qP)/M$$

$$Q^2 = (k - k')^2$$

$$y = (qP)/(kP)$$

$$x = Q^2/2(qP)$$

$$z = (qP_h)/(qP)$$



$$\sigma = \sigma_{UU} + \sigma_{UU}^{\cos \phi} \cos \phi + \sigma_{UU}^{\cos 2\phi} \cos 2\phi + \lambda \sigma_{LU}^{\sin \phi} \sin \phi + \dots$$

# SIDIS ( $\gamma^* p \rightarrow \pi X$ ) : $k_T$ -dependences

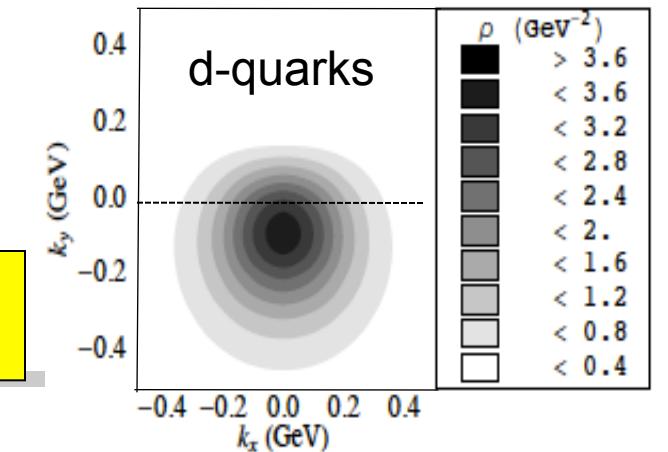
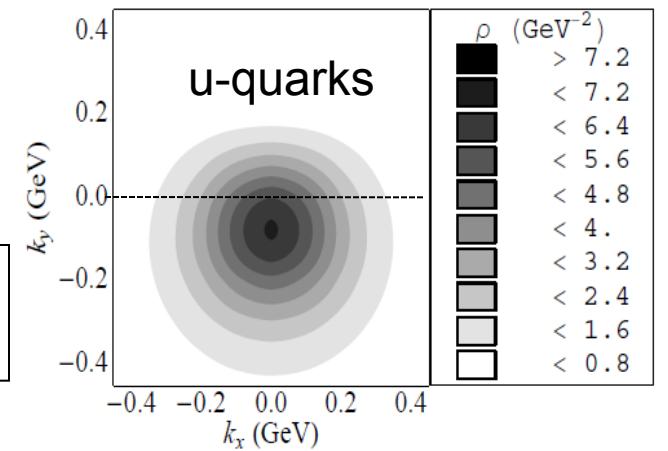
$$\frac{d\sigma}{dx_B dy d\psi dz d\phi_h dP_{h\perp}^2} = f_1 \otimes D_1 + h_1^\perp \otimes H_1^\perp + \text{HT} + \text{HT}$$

$$\frac{\alpha^2}{x_B y Q^2} \frac{y^2}{2(1-\varepsilon)} \left(1 + \frac{\gamma^2}{2x_B}\right) \left\{ F_{UU,T} + \varepsilon F_{UU,L} + \sqrt{2\varepsilon(1+\varepsilon)} \cos \phi_h F_{UU}^{\cos \phi_h} \right.$$

$$\left. + \varepsilon \cos(2\phi_h) F_{UU}^{\cos 2\phi_h} + \lambda_e \sqrt{2\varepsilon(1-\varepsilon)} \sin \phi_h F_{LU}^{\sin \phi_h} \right\},$$

N/q	U	L	T
U	$f_1$		$h_1^\perp$
L		$g_1$	$h_{1L}^\perp$
T	$f_{1T}^\perp$	$g_{1T}^\perp$	$h_1 h_{1T}^\perp$

Pasquini&Yuan(2010)



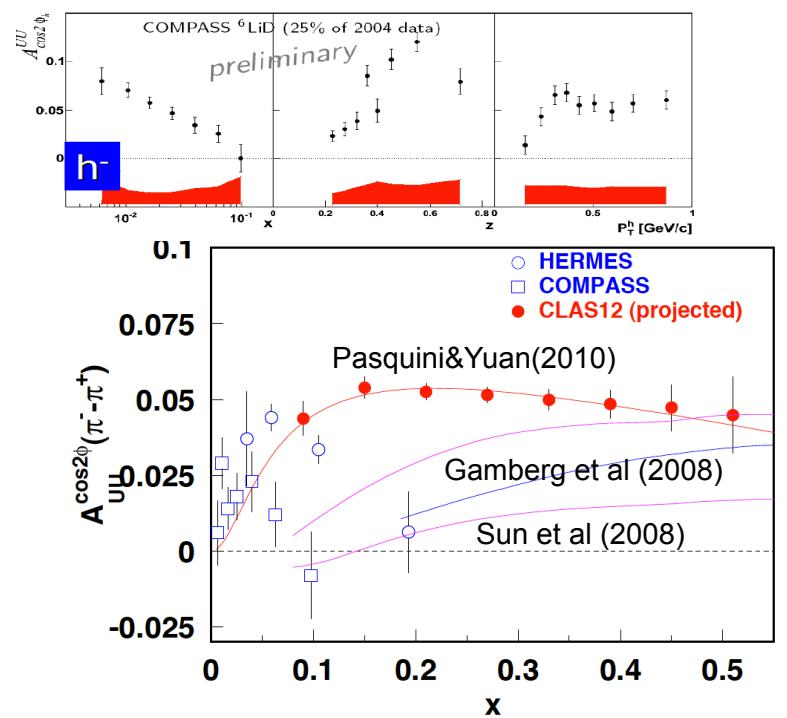
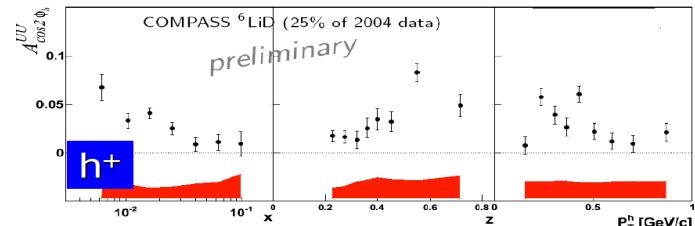
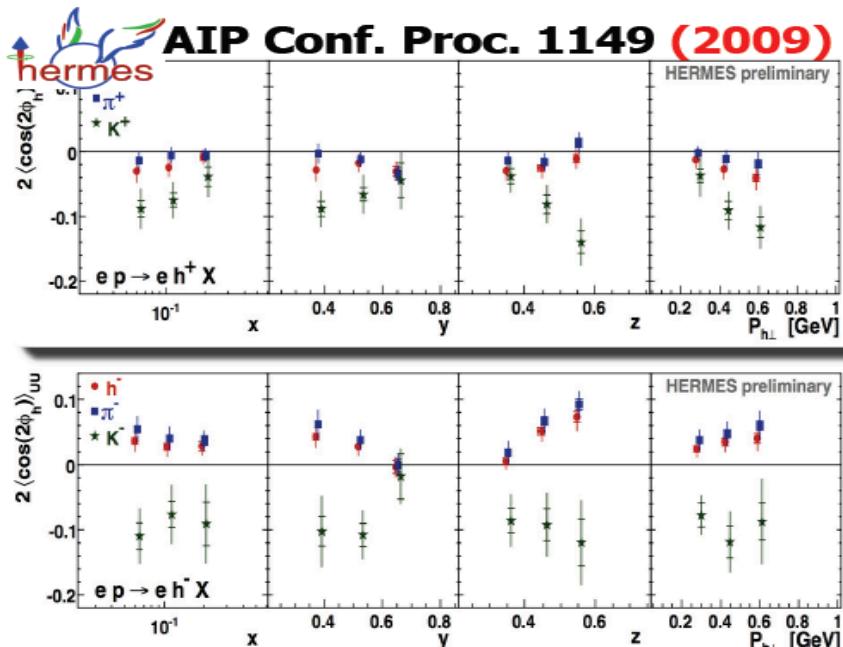
BM TMD (1998) describes correlation between the transverse momentum and transverse spin of quarks, requires FSI or ISI

$$f_{q/p}(x, k_\perp^2) = \frac{1}{2} [f_1^q(x, k_\perp^2) - h_1^{\perp q}(x, k_\perp^2) \frac{(\hat{P} \times k_\perp) \cdot S_q}{M}]$$

$$h_1^{\perp q}(\text{SIDIS}) = -h_1^{\perp q}(\text{DY})$$

BM TMD under intensive studies worldwide, including SIDIS and DY experiments, model calculations, lattice simulations.

# HT effects as background: Boer-Mulders distribution



Background contributions :  
 Higher twist azimuthal moments  
 kinematical HT (Cahn)  
 dynamical HT (Berger-Brodsky)  
 Radiative correction  
 Acceptance

} “flavor blind”

$$A_{UU}^{\cos 2\phi}(\pi^0) \approx A_{UU,Cahn}^{\cos 2\phi}$$

Wide range in  $Q^2$  and  $P_T$  accessible with CLAS12 are important for  $\cos 2\phi$  studies (all background contributions are HT)

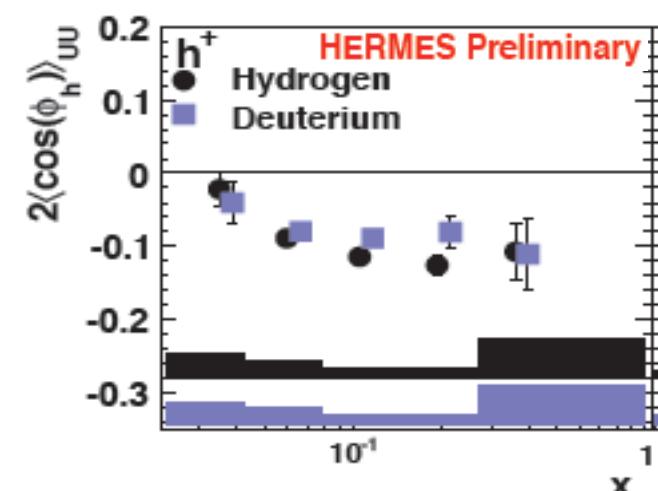
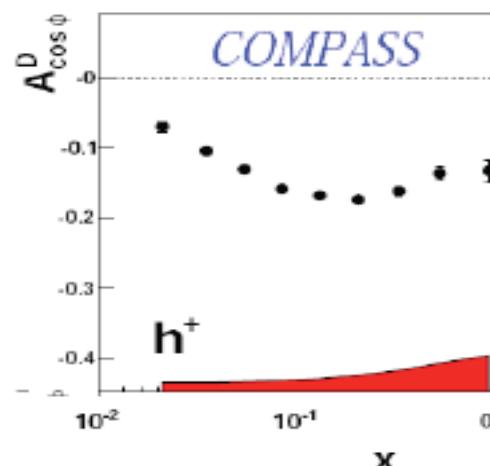
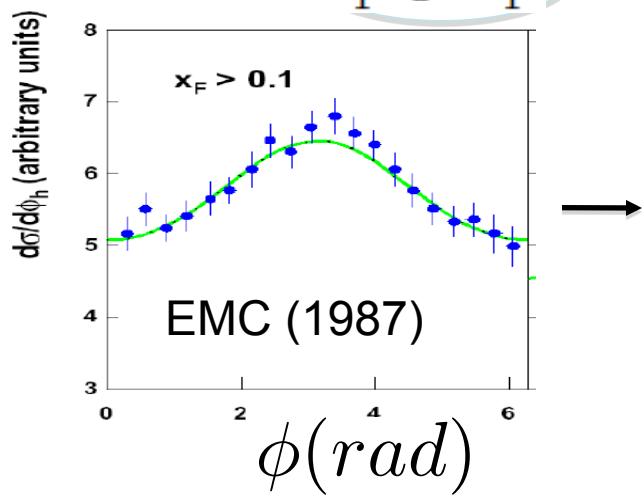
# Azimuthal distributions in SIDIS

$$\frac{d\sigma}{dx_B dy d\psi dz d\phi_h dP_{h\perp}^2} = f_1 \otimes D_1 + h.t. + h.t.$$

$$\frac{\alpha^2}{x_B y Q^2} \frac{y^2}{2(1-\varepsilon)} \left(1 + \frac{\gamma^2}{2x_B}\right) \left\{ F_{UU,T} + \varepsilon F_{UU,L} + \sqrt{2\varepsilon(1+\varepsilon)} \cos \phi_h F_{UU}^{\cos \phi_h} \right.$$

$$\left. + \varepsilon \cos(2\phi_h) F_{UU}^{\cos 2\phi_h} + \lambda_e \sqrt{2\varepsilon(1-\varepsilon)} \sin \phi_h F_{LU}^{\sin \phi_h} \right\},$$

$$h_1^\perp \otimes H_1^\perp + h.t.$$

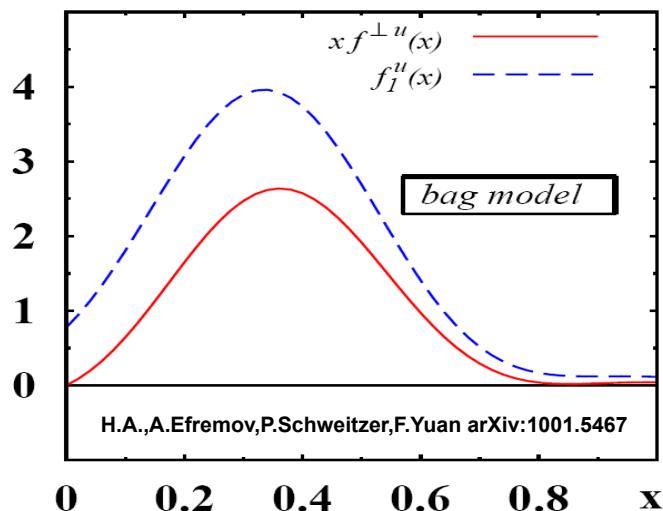


Large  $\cos\phi$  modulations observed by EMC were reproduced in electroproduction of hadrons in SIDIS with unpolarized targets at COMPASS and HERMES

# Model predictions for $\cos\phi$

$$F_{UU,T} + \varepsilon F_{UU,L} + \sqrt{2\varepsilon(1+\varepsilon)} \cos\phi_h F_{UU}^{\cos\phi_h}$$

$$F_{UU}^{\cos\phi_h} = \frac{2M}{Q} \mathcal{C} \left[ -\frac{\hat{h} \cdot \mathbf{k}_T}{M_h} \left( xh H_1^\perp + \frac{M_h}{M} f_1 \frac{\tilde{D}^\perp}{z} \right) - \frac{\hat{h} \cdot \mathbf{p}_T}{M} \left( xf^\perp D_1 + \frac{M_h}{M} h_1^\perp \frac{\tilde{H}}{z} \right) \right]$$



$$x f_{\perp}^{(q)} = x \tilde{f}_{\perp}^{(q)} + f_1^q$$

$\longleftrightarrow$   $F_{UU}^{\cos\phi} \propto f_{\perp}^{(q)} D_1^q$

"interaction dependent"

Models agree on a large HT distributions

# SIDIS cross-section

Expanding the contraction and integrating over  $\psi$  and the beam polarization, the cross-section for an unpolarized target can be written as

$$\frac{d^5\sigma}{dx dQ^2 dz d\phi_h dP_{h\perp}^2} = \frac{2\pi\alpha^2}{xyQ^2} \frac{y^2}{2(1-\epsilon)} \left(1 + \frac{\gamma^2}{2x}\right) (F_{UU,T} + \epsilon F_{UU,L}) \left\{ 1 + \frac{\sqrt{2\epsilon(1+\epsilon)} F_{UU}^{\cos \phi_h}}{(F_{UU,T} + \epsilon F_{UU,L})} \cos \phi_h + \frac{\epsilon F_{UU}^{\cos 2\phi_h}}{(F_{UU,T} + \epsilon F_{UU,L})} \cos 2\phi_h \right\}$$

$A_0$        $A_{UU}^{\cos \phi_h}$        $A_{UU}^{\cos 2\phi_h}$

According to the factorization theorem, structure functions can, in the Bjorken limit, be written as convolutions of TMDs and FFs  $F = \sum \text{TMD} \otimes \text{FF}$

Bjorken Limit:

$$Q^2 \rightarrow \infty$$

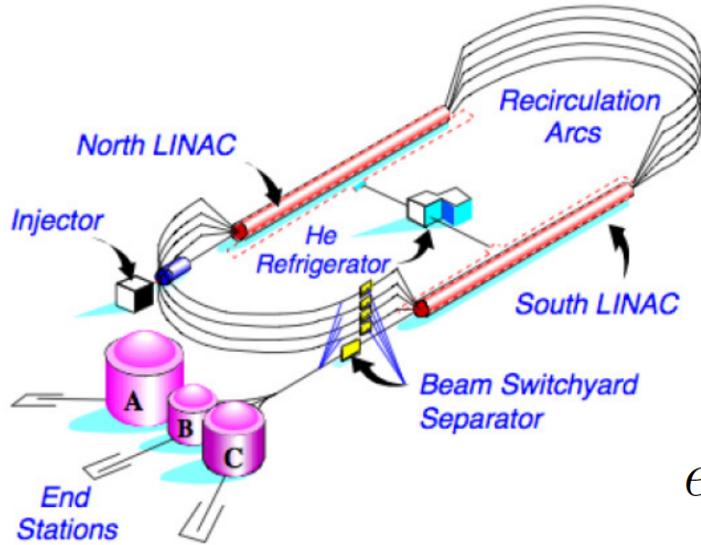
$$2P \cdot q \rightarrow \infty$$

$$P \cdot P_h \rightarrow \infty$$

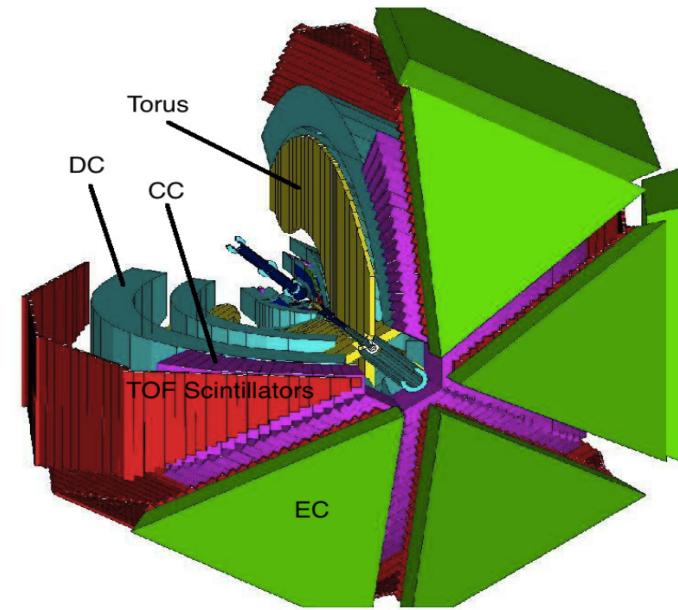
fixed

$$\begin{cases} x = Q^2 / 2P \cdot q \\ z = P \cdot P_h / P \cdot q \end{cases}$$

# CLAS: e1f data set



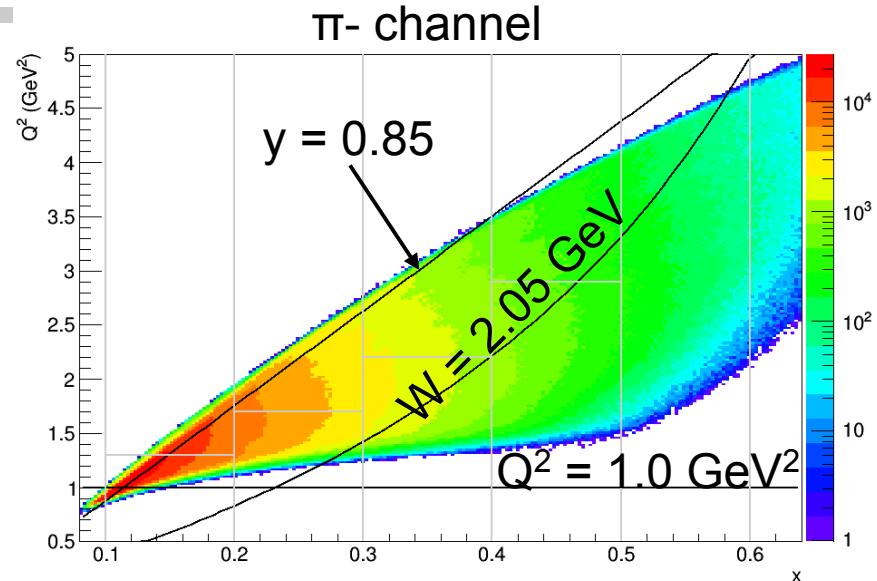
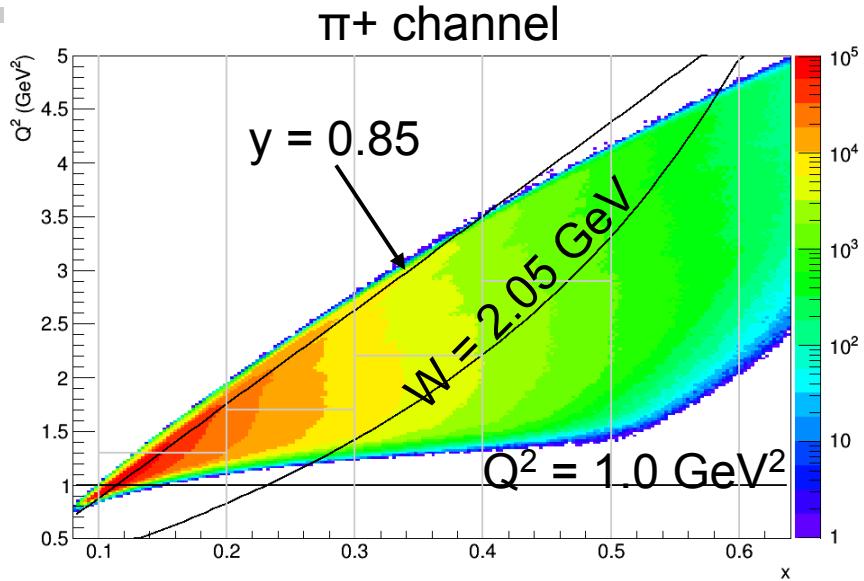
$$ep \rightarrow e\pi^\pm X$$



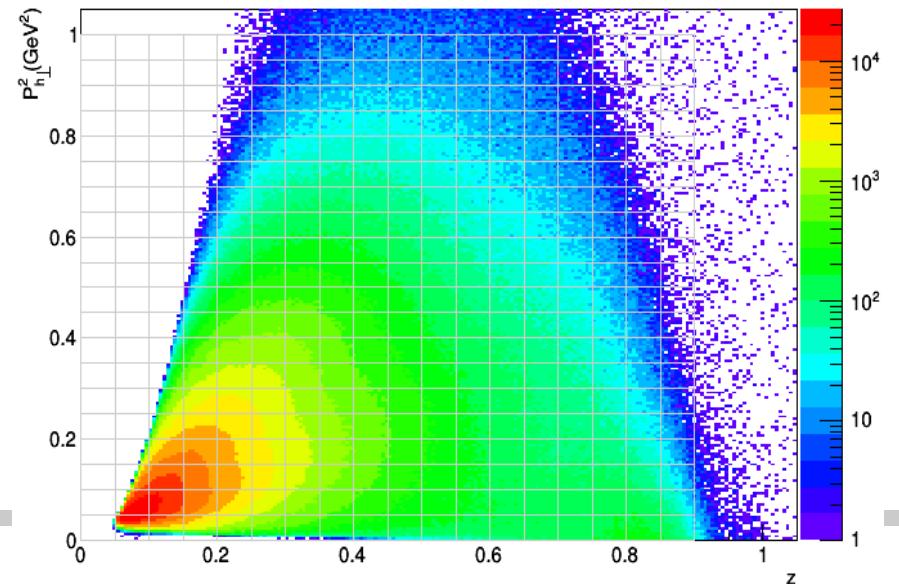
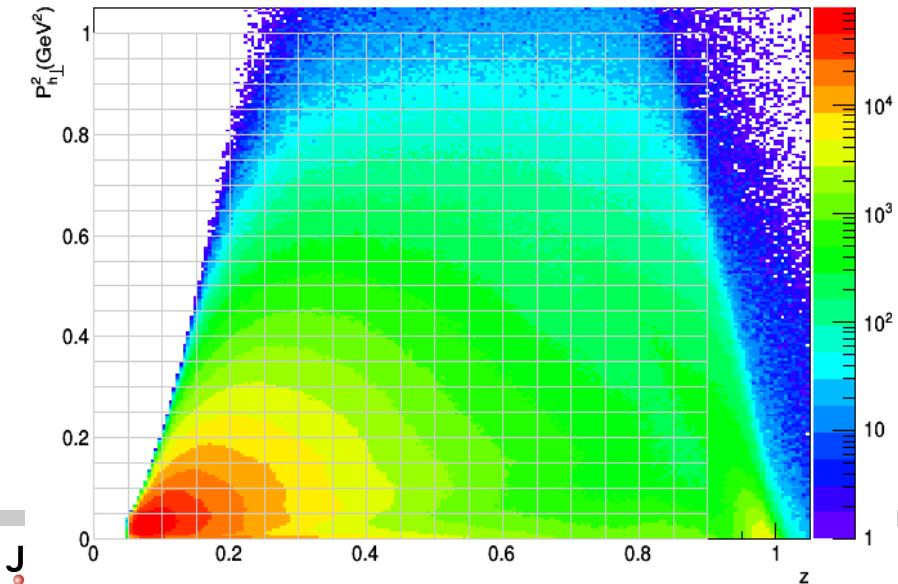
- Two 0.4 GeV linear accelerators.
- Nine recirculation arcs for five loops around the track.
- Continuous, polarized electron beam up to 6 GeV delivered simultaneously to 3 experimental halls.
- High luminosity of  $0.5 \times 10^{34} (\text{cm}^2 \text{ s})^{-1}$
- E1-f run: 5.498 GeV electron beam with ~75% polarization (averaged over for this analysis); unpolarized liquid hydrogen target; about 2 billion events; broad and comparable kinematic range for two channels:

- Electromagnetic Calorimeter (EC) and Čerenkov Counter (CC) used in electron identification.
- Drift Chamber (DC) (3 regions) and time of flight Scintillators (SC) record position and timing information for each charged track.
- **Torus** magnet creates toroidal magnetic field which causes charged tracks to curve while preserving the  $\varphi_{\text{lab}}$  angle.

# SIDIS Cuts and Binning

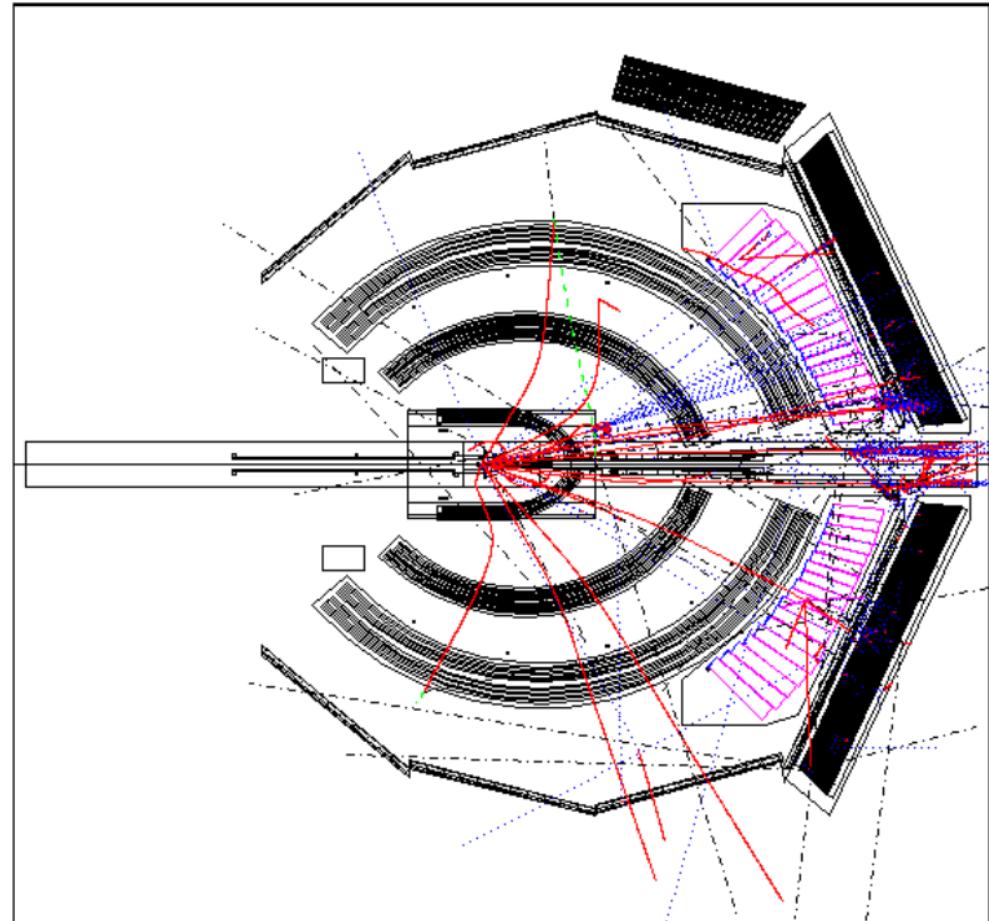


The DIS region is defined as  $Q^2 > 1.0$  GeV $^2$  and  $W > 2.05$  GeV.



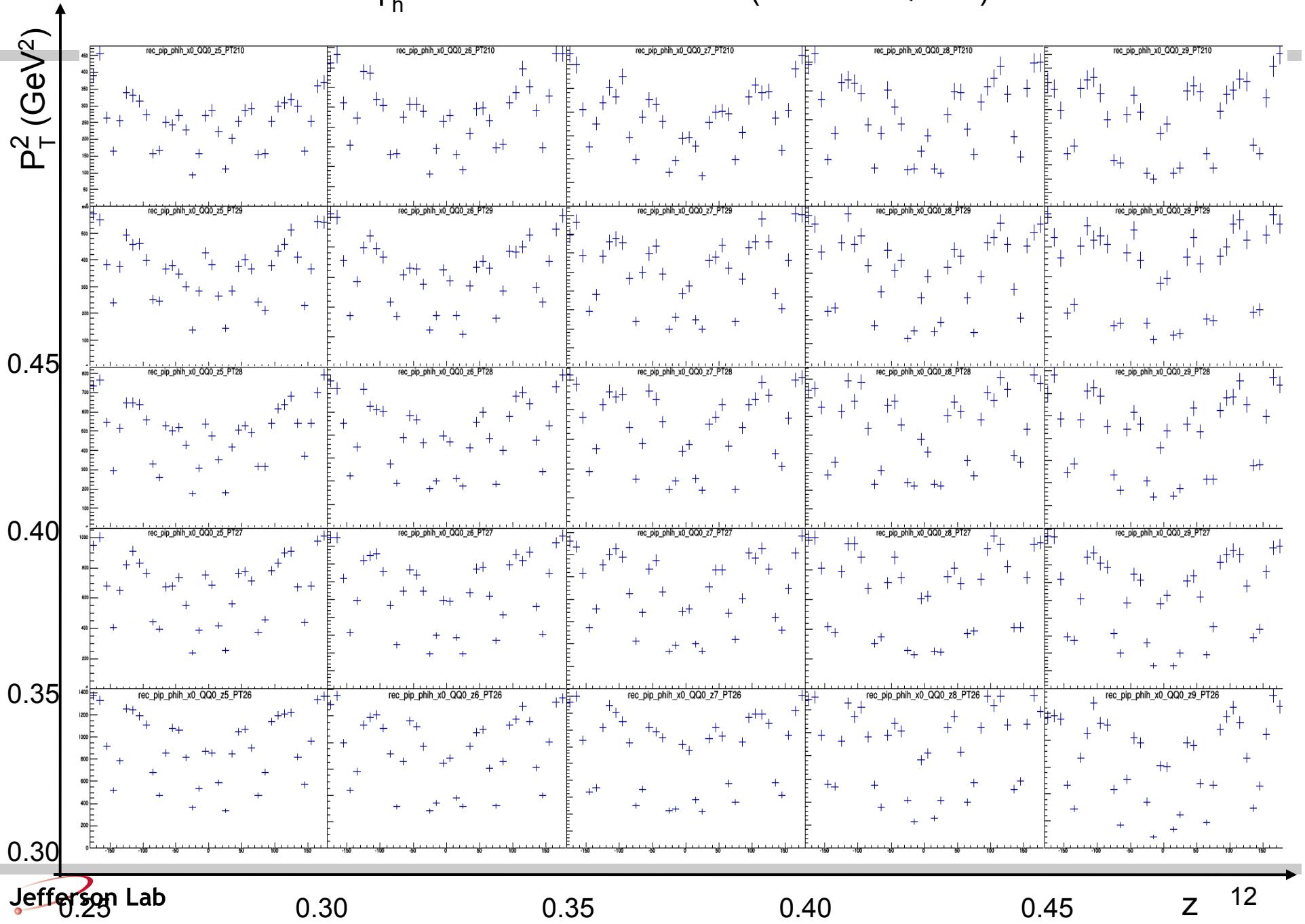
# Simulation

- 1B SIDIS events are generated with a PYTHIA based event generator.
- 3 different models were used to study model dependence.
- Generated events are put into a GEANT based Monte Carlo simulation of the CLAS detector (GSim).
- Smearing and inefficiencies are introduced to the simulation to make it more realistic.
- The simulated data is then “cooked”, processed, and analyzed in the same way as the E1-f data set.



Above: Five generated events being reconstructed by GSim. Charged tracks are shown in red, neutral tracks in gray.

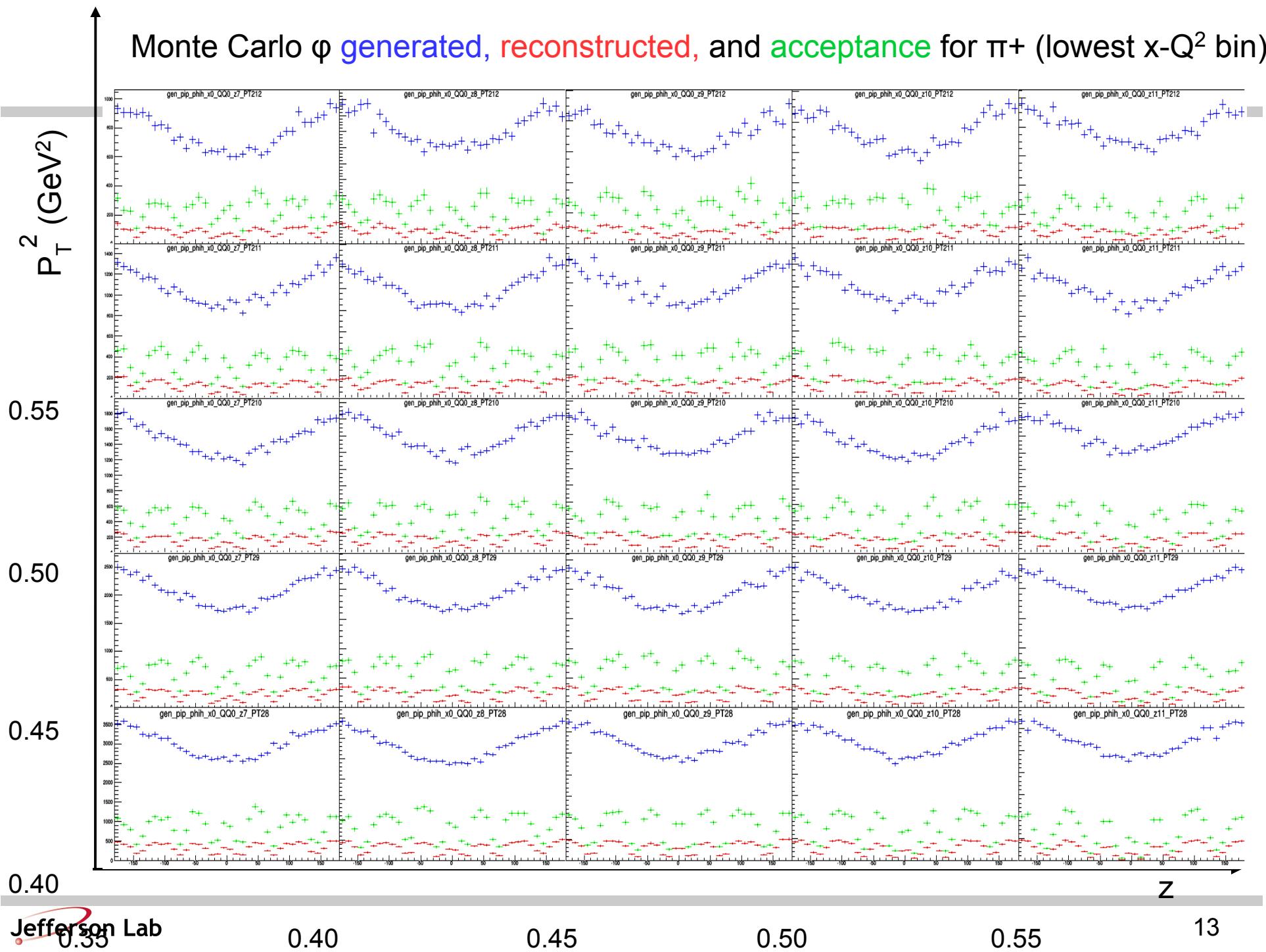
# $\phi_h$ distributions - raw data (lowest x-Q<sup>2</sup> bin)



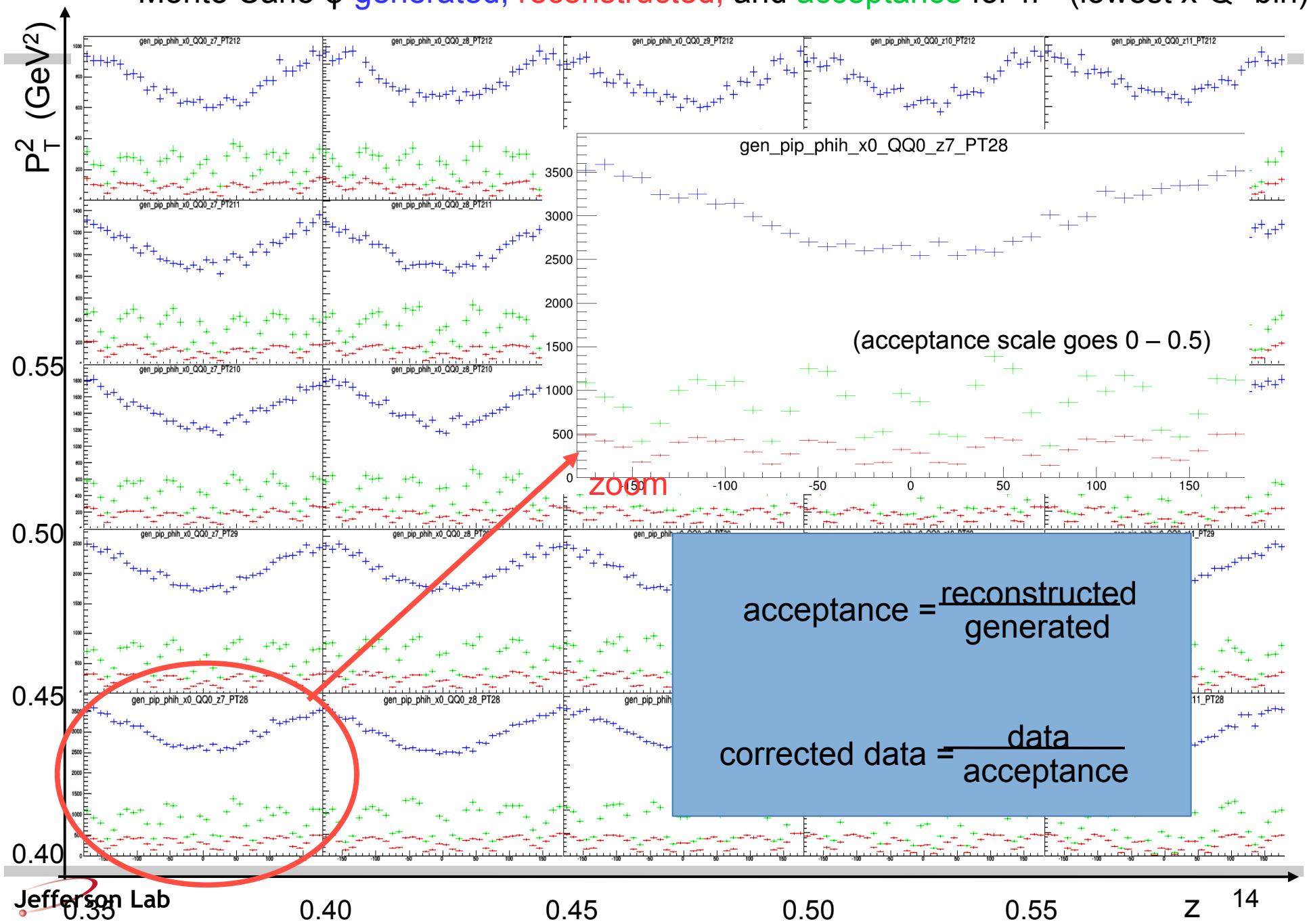
Jefferson Lab  
0.25

12

# Monte Carlo $\varphi$ generated, reconstructed, and acceptance for $\pi^+$ (lowest x-Q<sup>2</sup> bin)



# Monte Carlo $\varphi$ generated, reconstructed, and acceptance for $\pi^+$ (lowest $x$ - $Q^2$ bin)

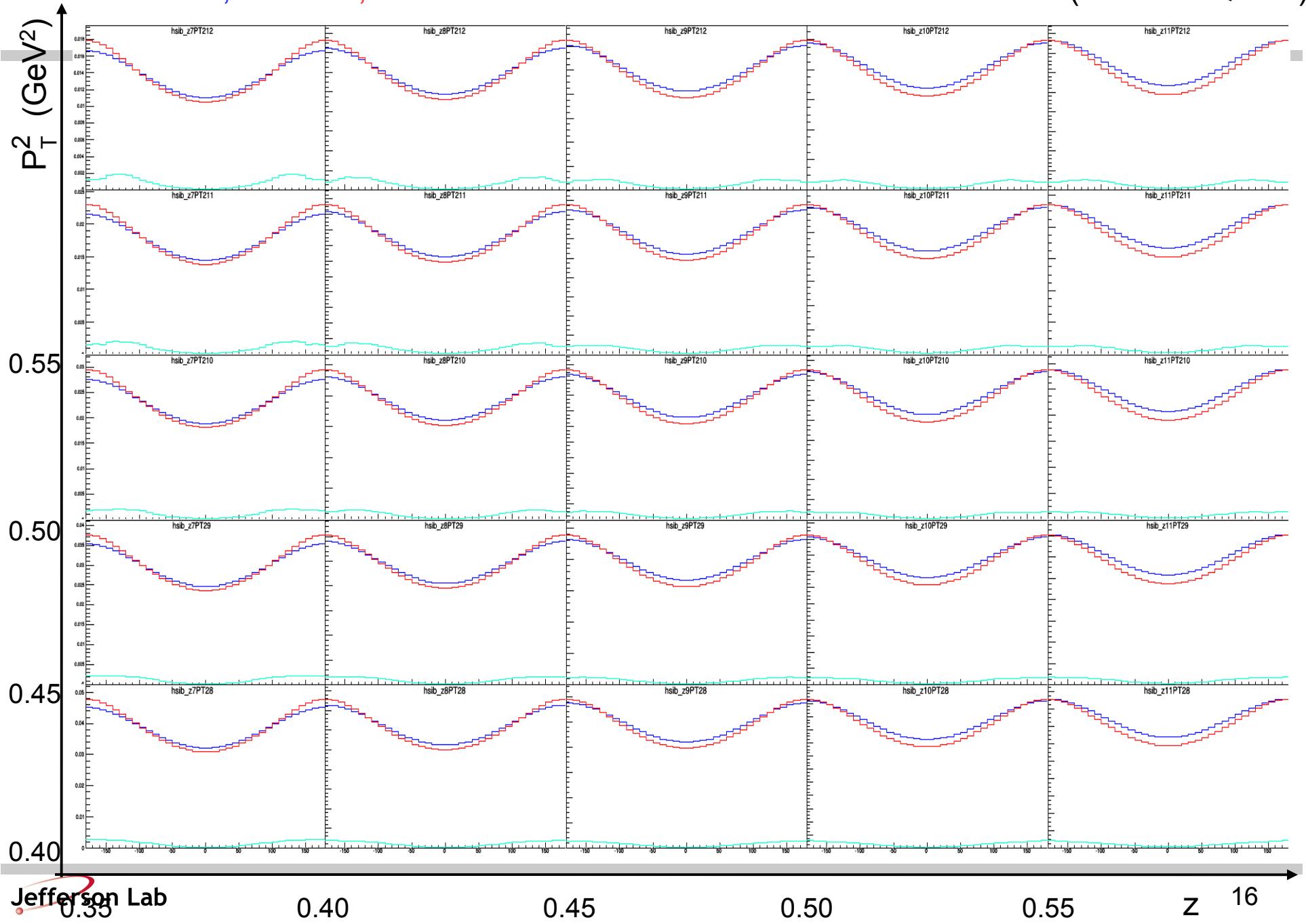


# Radiative Corrections

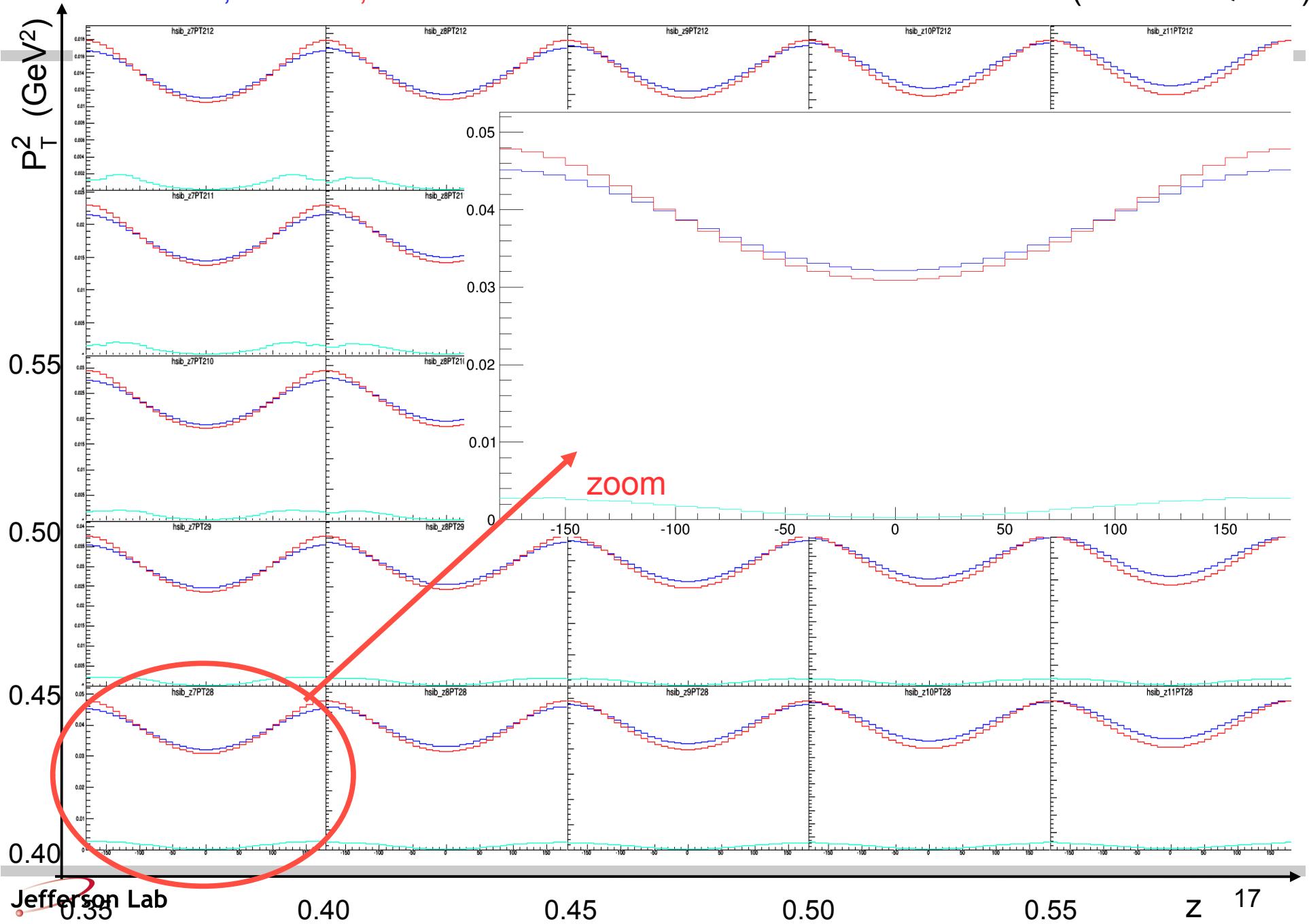
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- Radiative effects, such as the emission of a photon by the incoming or outgoing electron, can change all five SIDIS kinematic variables.
- Furthermore, exclusive events can enter into the SIDIS sample because of radiative effects (“exclusive tail”).
- HAPRAD 2.0 is used to do radiative corrections.
  - For a given  $\sigma_{Born}(x, Q^2, z, P_{h\perp}^2, \phi_h)$  (obtained from a model), HAPRAD calculates  $\sigma_{rad+tail}(x, Q^2, z, P_{h\perp}^2, \phi_h)$ . The correction factor is then: 
$$RC\ factor = \frac{\sigma_{rad+tail}(x, Q^2, z, P_{h\perp}^2, \phi_h)}{\sigma_{Born}(x, Q^2, z, P_{h\perp}^2, \phi_h)}$$
- 3 different models were used to study model dependence.

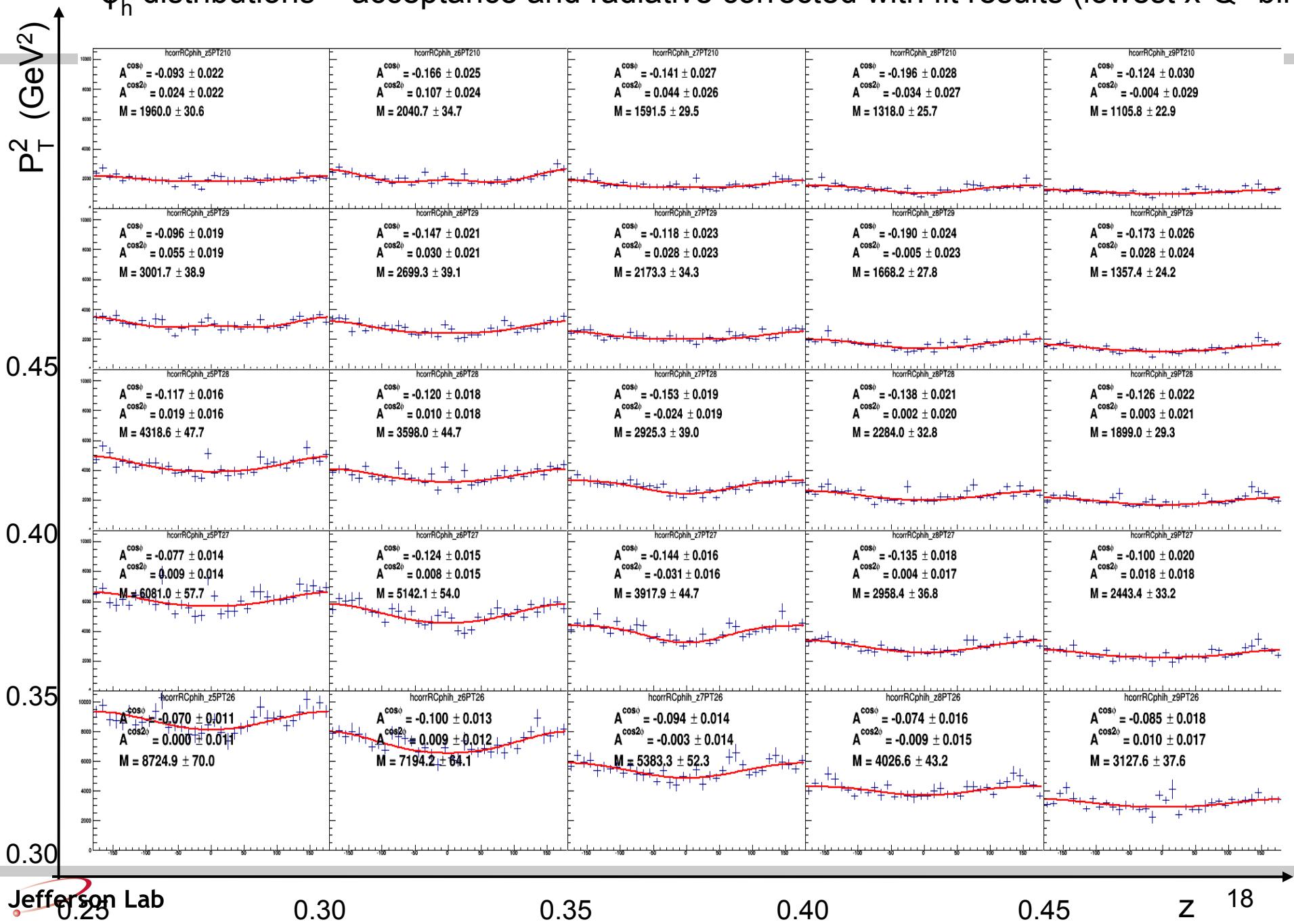
# Born, radiated, and exclusive tail cross-sections from HAPRAD (lowest x-Q<sup>2</sup> bin)



# Born, radiated, and exclusive tail cross-sections from HAPRAD (lowest x-Q<sup>2</sup> bin)



# $\varphi_h$ distributions – acceptance and radiative corrected with fit results (lowest x-Q<sup>2</sup> bin)

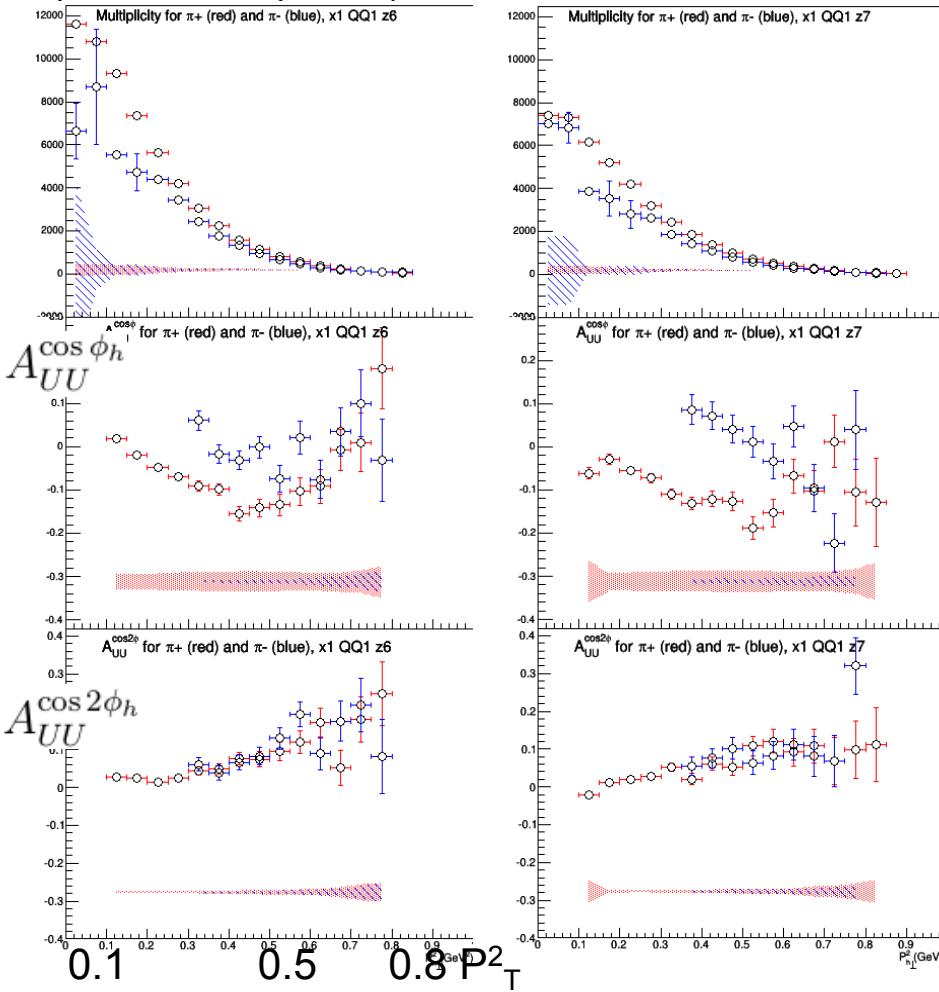


Jefferson Lab  
0.25

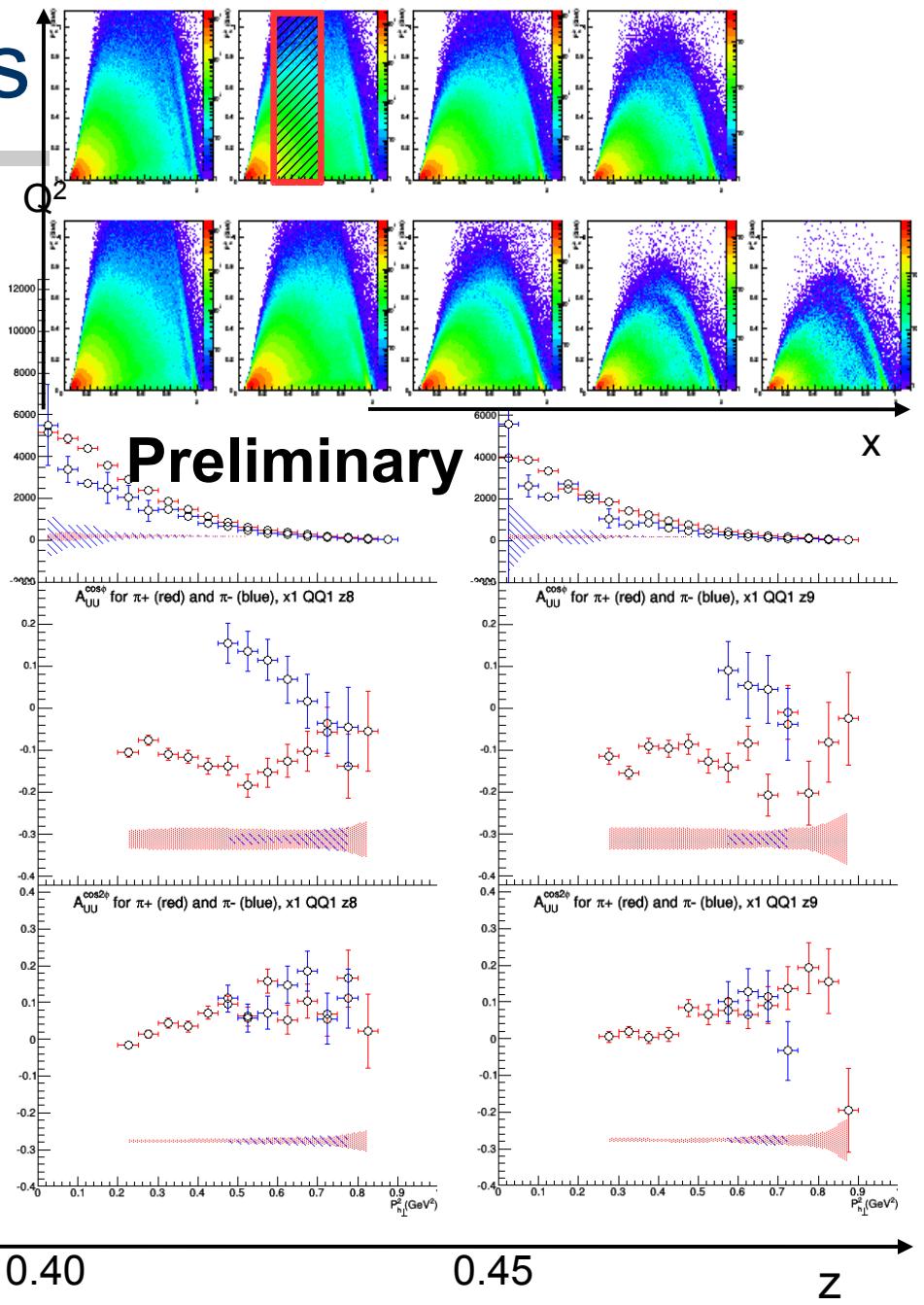
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# Representative Results

$A_0$  (top row),  $A_{UU}^{\cos \phi_h}$  (middle row), and  $A_{UU}^{\cos 2\phi_h}$  (bottom row) vs  $P_T^2$  for  $\pi^+$  and  $\pi^-$



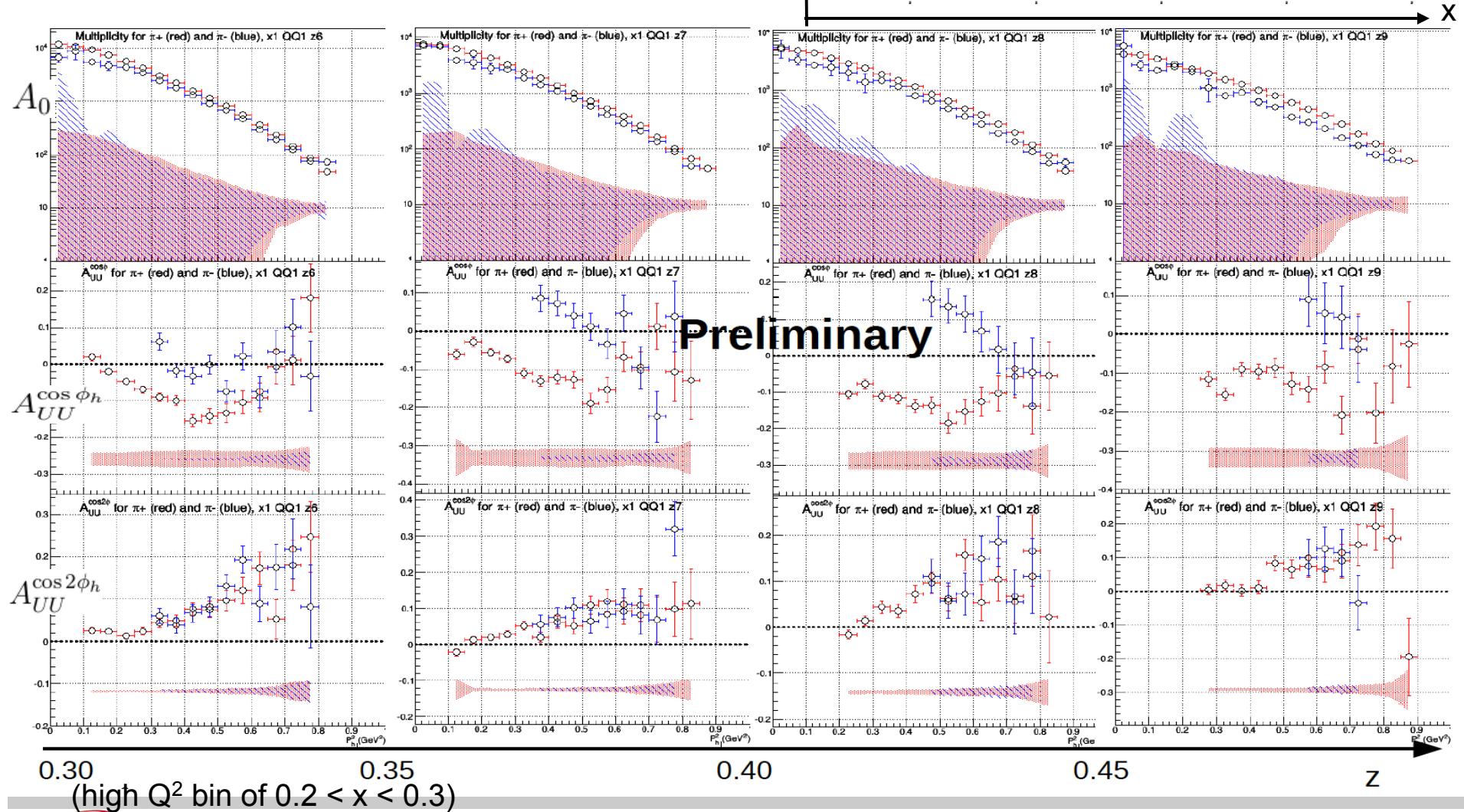
0.30  
(high  $Q^2$  bin of  $0.2 < x < 0.3$ )



Preliminary

# Representative Results

$A_0$  (top row),  $A_{UU}^{\cos \phi_h}$  (middle row), and  $A_{UU}^{\cos 2\phi_h}$  (bottom row) vs  $P_T^2$  for  $\pi^+$  and  $\pi^-$



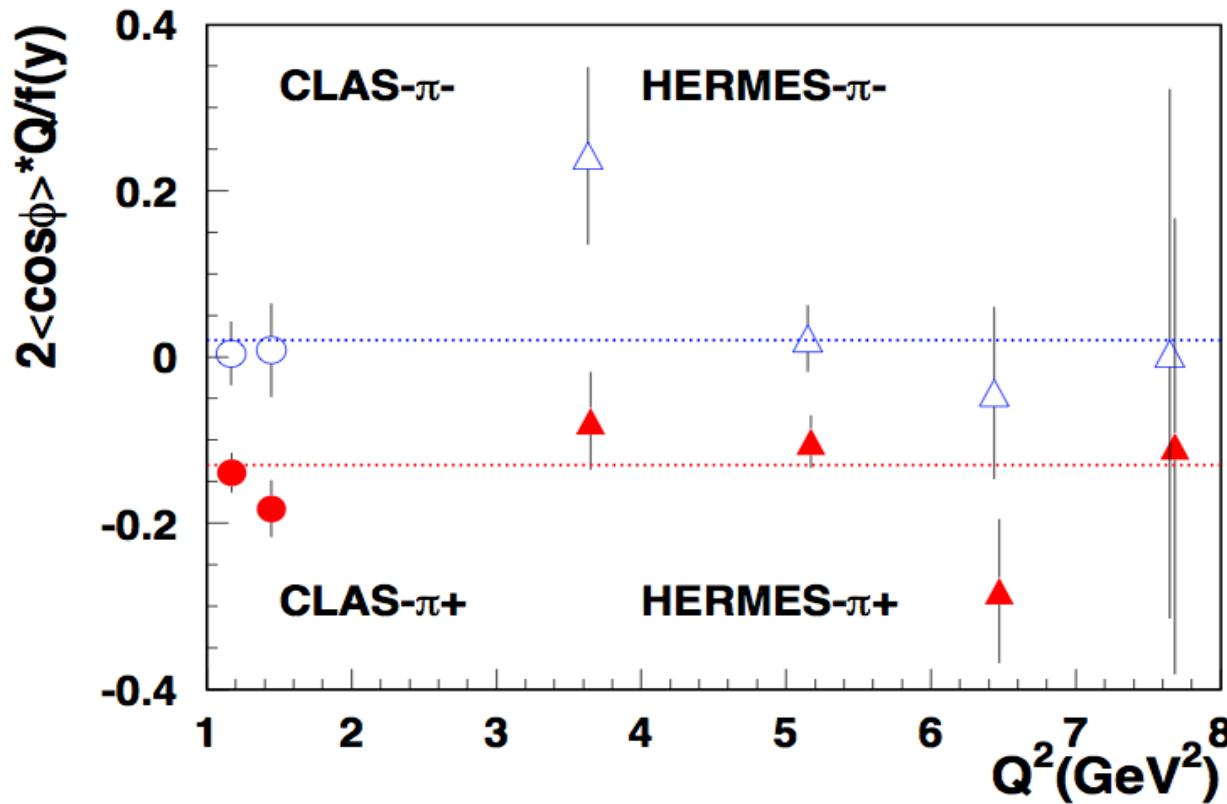
Preliminary

# Comparing with HERMES

$$F_{UU,T} + \varepsilon F_{UU,L} + \sqrt{2\varepsilon(1+\varepsilon)} \cos \phi_h F_{UU}^{\cos \phi_h}$$

$$F_{UU}^{\cos \phi_h} = \frac{2M}{Q} \mathcal{C} \left[ -\frac{\hat{h} \cdot \mathbf{k}_T}{M_h} \left( xh H_1^\perp + \frac{M_h}{M} f_1 \frac{\tilde{D}^\perp}{z} \right) - \frac{\hat{h} \cdot \mathbf{p}_T}{M} \left( xf^\perp D_1 + \frac{M_h}{M} h_1^\perp \frac{\tilde{H}}{z} \right) \right]$$

**x=0.19, z=0.45, P<sub>T</sub>=0.42 GeV**



CLAS data consistent  
with HERMES (27.5 GeV)

# Summary

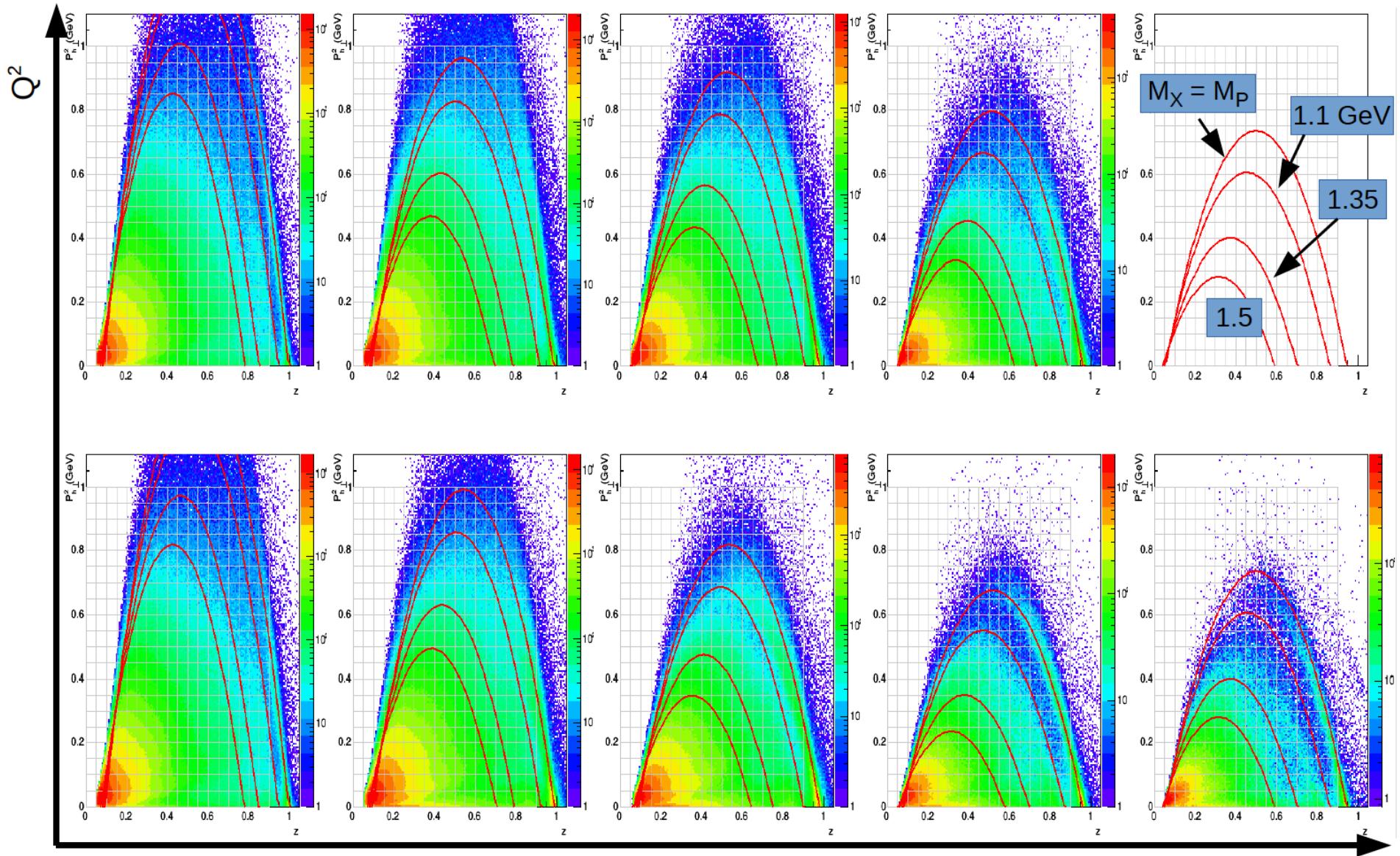
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- The multiplicity,  $\cos\varphi_h$  moment, and  $\cos 2\varphi_h$  moment of the unpolarized SIDIS cross-section have been measured for both charged pion channels in a fully differential way with good statistics and well controlled systematics over a wide kinematic range.
- The  $\cos\varphi_h$  and  $\cos 2\varphi_h$  modulations are significant, depend on flavor, and their understanding is important for interpretation of spin-azimuthal asymmetries
- Comparison of azimuthal moments with HERMES, supports the higher twist nature of the  $\cos\varphi_h$  moment (Cahn effect).

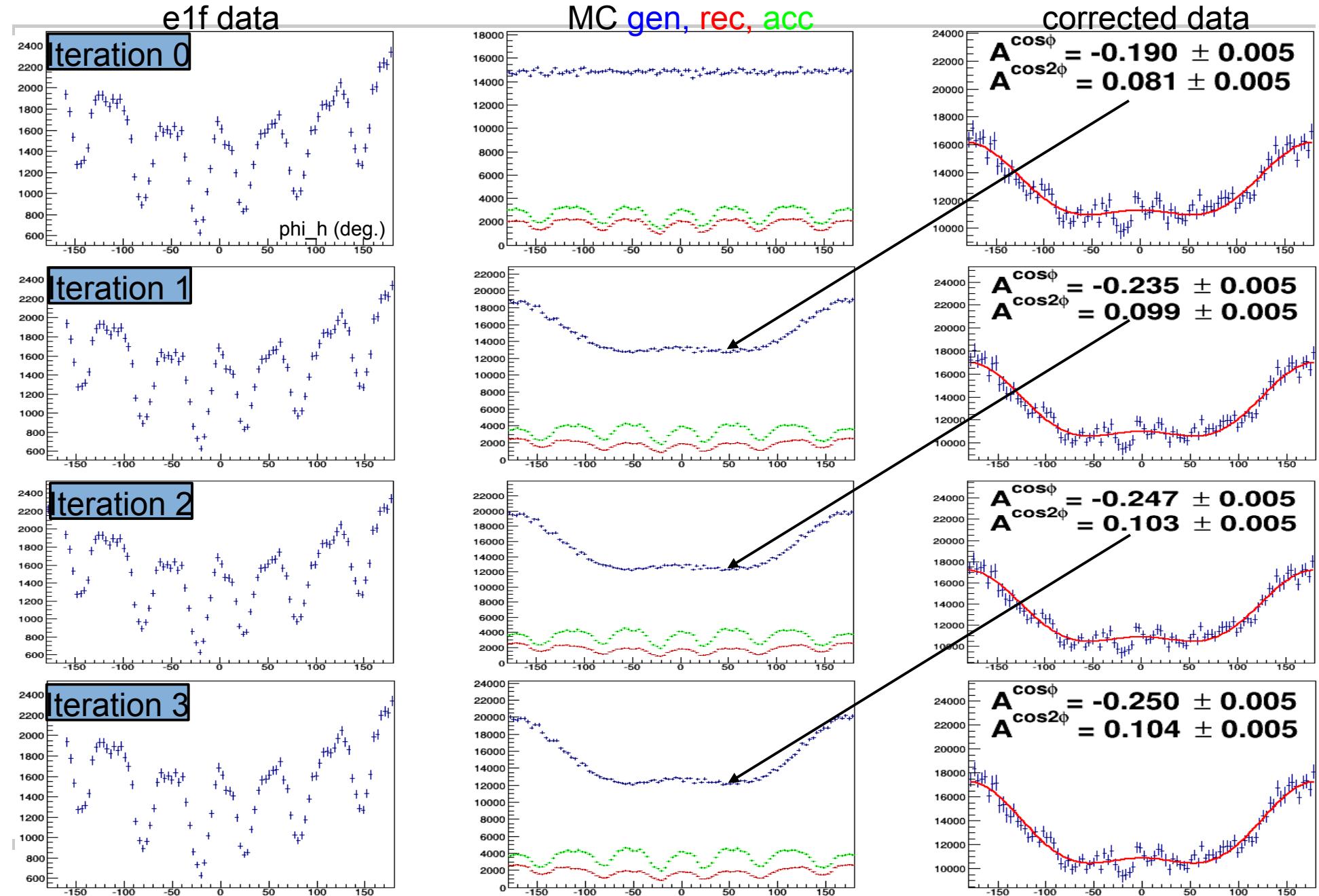
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# Support slides....

# $\pi^+ P_{h\perp}^2$ vs z for each x-Q<sup>2</sup> bin



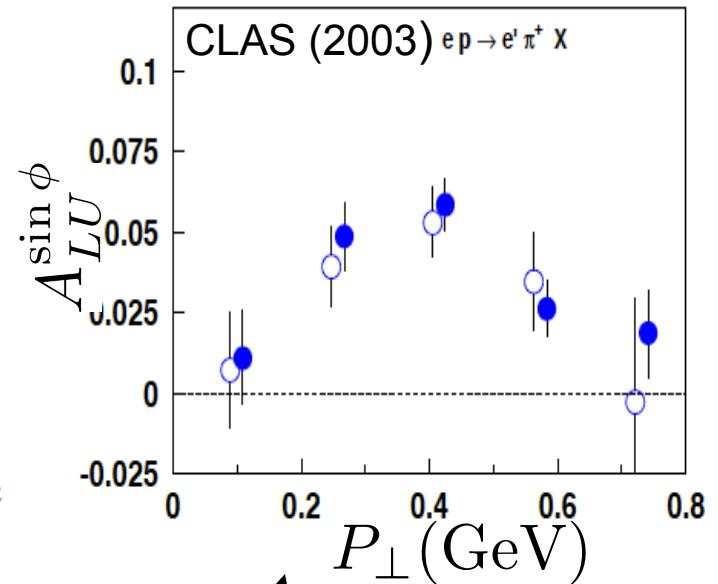
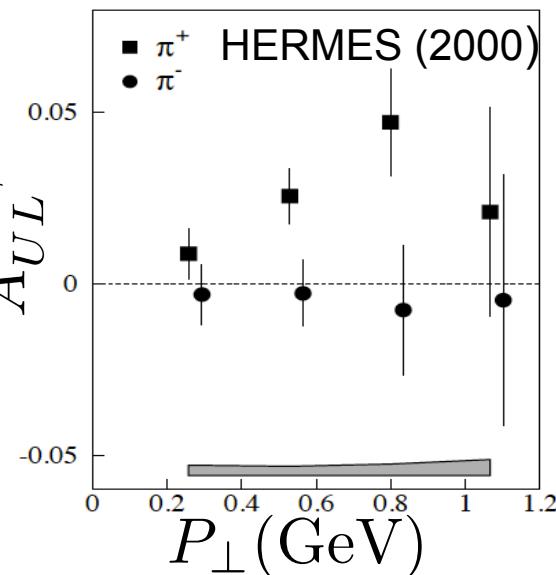
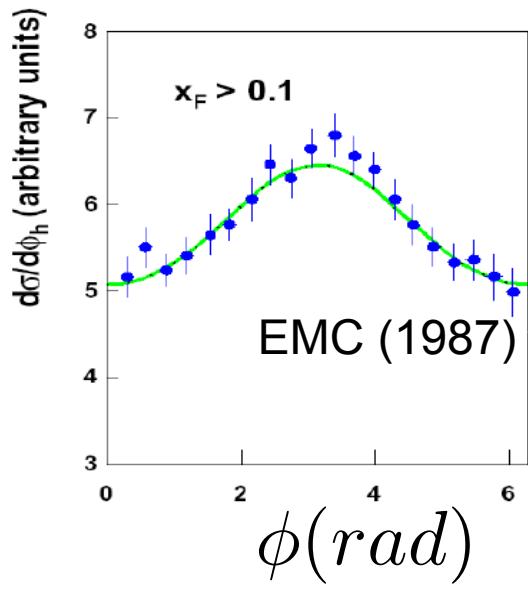
# Effects of the shape of the generated $\phi$ distribution



# Measurements of SS azimuthal asymmetries in SIDIS

$$\sigma = \sigma_{UU}(1 + P_B A_{LU}^{\sin \phi} \sin \phi + P_T A_{UL}^{\sin \phi} \sin \phi + P_T A_{UT}^{\sin \phi - \phi_S} \sin(\phi - \phi_S) + \dots)$$

Large  $\cos\phi$  and  $\sin\phi$  modulations have been observed in electroproduction of hadrons in SIDIS with polarized and unpolarized targets



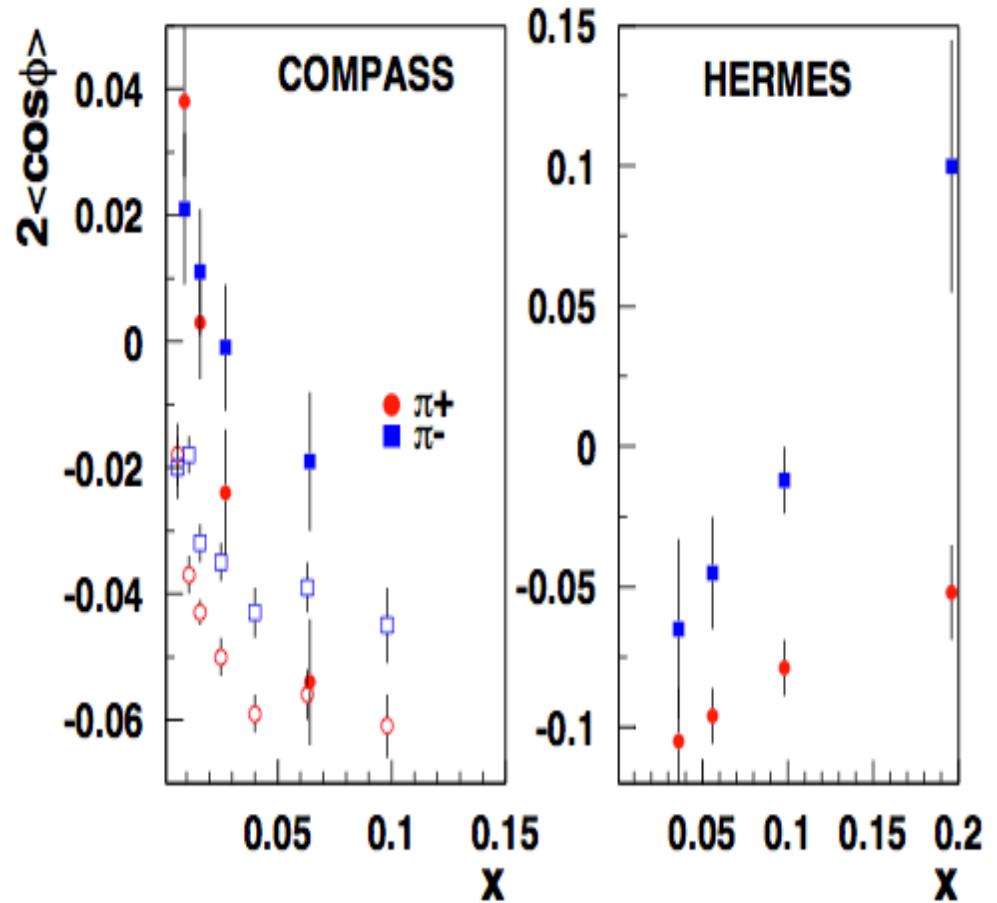
Related to spin-orbit correlations in fragmentation?

# $A_{UU}^{\cos\phi}$ : From measurements to interpretation

N/q	U	L	T
U	$f_U^\perp$	$g_L^\perp$	$h, e$
L	$f_L^\perp$	$g_L^\perp$	$h_L, e_L$
T	$f_T, f_T^\perp$	$g_T, g_T^\perp$	$h_T, e_T, h_T^\perp, e_T^\perp$

q/h	U	L	
U	$D_1$		
L		$G_{1L}$	
T	$H_1^\perp$	$H_{1L}^\perp$	H

$$A_{UU}^{\cos\phi} \propto f^\perp D_1 + h H_1^\perp$$



$\pi^0$  SSA less sensitive polarized fragmentation effects (Collins function suppressed)