

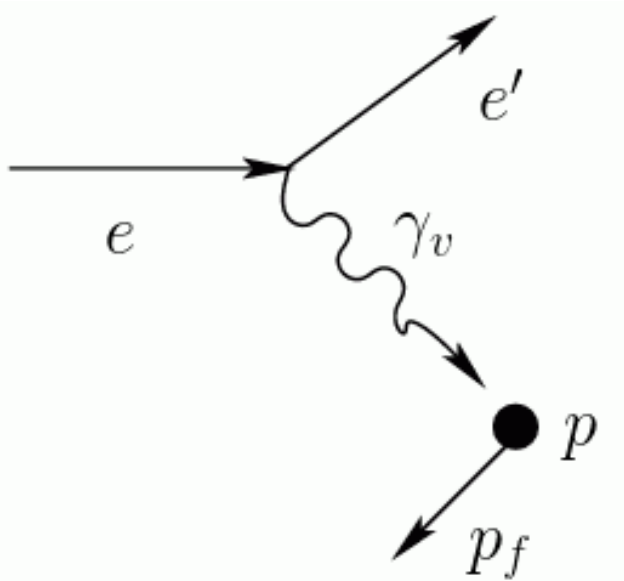
# **Investigation of Exclusive $\pi^+\pi^-$ Electroproduction off the Proton Bound in the Deuteron in the Resonance Region with CLAS**

**Speaker:** Iuliia Skorodumina  
(University of South Carolina)

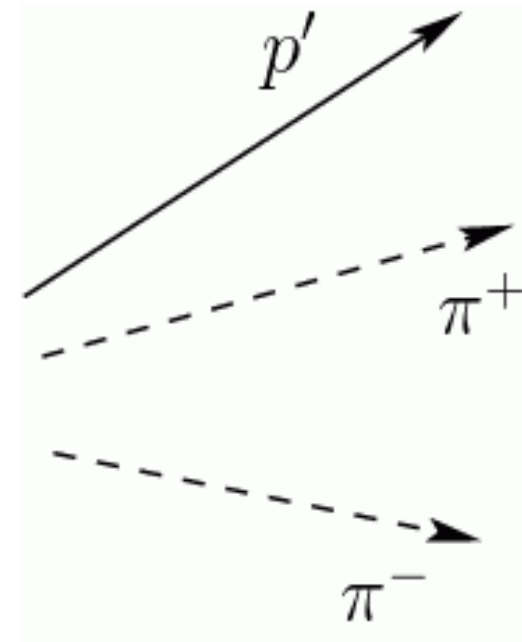
# CLAS Deuteron Target Experiment

( e1e run,  $E_{beam} = 2.039$  GeV)

$\gamma_v p(n)$



$p'(n')\pi^+ \pi^-$



# Final Goals

- To extract quasi-free integrated and single-differential cross sections of the reaction  $\gamma_v p(n) \rightarrow p'(n')\pi^+ \pi^-$  for  $W: [1.3, 1.825] \text{ GeV}$ ,  $Q^2: [0.45, 1] \text{ GeV}^2$
- To compare them with the cross sections of the analogous reaction on the free proton [1]

$$\frac{d^7 \sigma_e}{dW dQ^2 d^5 \tau} = \Gamma_v \frac{d^5 \sigma_v}{d^5 \tau}$$

$$d^5 \tau = dM_{\pi^+ p} dM_{\pi^+ \pi^-} d\Omega_{\pi^-} d\alpha_{[\pi^- p][\pi^+ p']}$$

# What is different from the free proton target experiment?

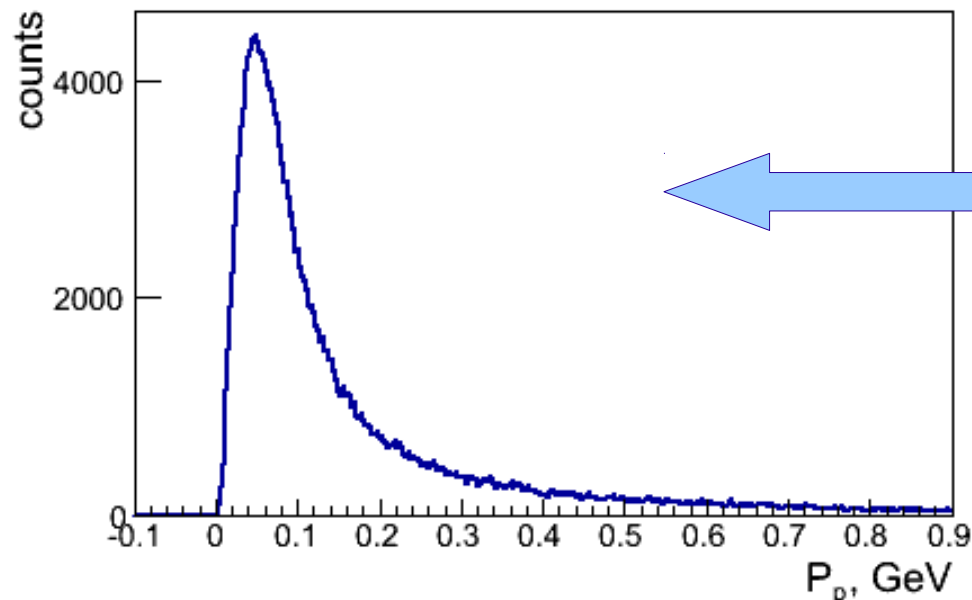
- 1) Considerably more complex effects of initial and final state interactions due to the presence of additional nucleon → lead to difficulties in exclusive event selection
- 2) Fermi motion of the target proton has the following consequences:
  - Smearing of kinematical quantities ( $W$ , missing mass, etc.) if not all final particles are registered
  - Different procedure of lab-to-cms transformation
  - Moving proton experiment with fixed beam energy is equivalent to that on the proton at rest with varying beam energy
- 3) Off-shellness of the target proton
- 4) Possible modification of reaction amplitudes

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# Event Generation with TWOPEG

- TWOPEG [2] is new double-pion event generator developed in the framework of the preparation of Hybrid Baryon Search proposal (approved by PAC44)
- Fermi motion was implemented according to the Bonn potential [3]
- In this analysis TWOPEG is successfully used for the first time for the efficiency evaluation



Generated momentum of the target proton

$$P_p = \left| \vec{P}_e - \vec{P}_{e'} - \vec{P}_{p'} - \vec{P}_{\pi^+} - \vec{P}_{\pi^-} \right|$$

where  $\vec{P}_i$  are the three-momenta of the particle  $i$ .



[2] CLAS12-NOTE-2017-001 (arXiv:1703.08081)

[3] R.Machleidt, K. Holinde, and C. Elster,  
Phys. Rept., vol. 149, pp. 1-89, 1987

# 2 $\pi$ Event Selection

Cuts	Data	Simulation
Fiducial	yes	yes
EC-cut	yes	yes
CC-cut	yes	no/yes
$\beta$ vs. $p$	yes	yes
$\theta$ vs. $p$	yes	yes
Electron momentum correction	yes	no
Proton energy loss correction	yes	yes
Exclusivity cut	yes	yes

# 2 $\pi$ Event Selection

Cuts	Data	Simulation
Fiducial	yes	yes
EC-cut  Electron identification	yes	yes
CC-cut	yes	no/yes
$\beta$ vs. $p$  Hadron identification	yes	yes
$\theta$ vs. $p$	yes	yes
Electron momentum correction	yes	no
Proton energy loss correction	yes	yes
Exclusivity cut	yes	yes



# Topologies of $\gamma_{\nu} p(n) \rightarrow p'(n')\pi^+ \pi^-$

- All final particles are registered (10%) – fully exclusive topology
- $\pi^-$  is missing (70%)
- $\pi^+$  is missing (10%)  $\rightarrow$  misidentification with  $\gamma_{\nu} n(p) \rightarrow p'(n')\pi^-$  and  $\gamma_{\nu} n(p) \rightarrow p'(n')\pi^-\pi^0$  channels
- $p$  is missing (10%)  $\rightarrow$  misidentification with  $\gamma_{\nu} n(p) \rightarrow n'(p')\pi^+ \pi^-$  channel

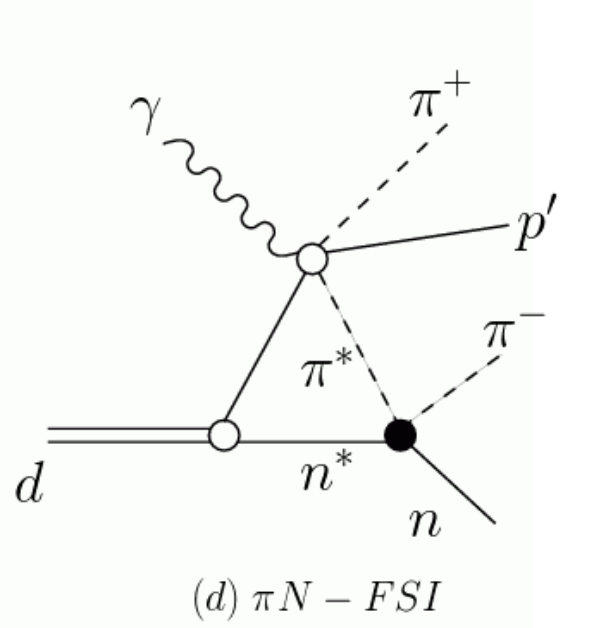
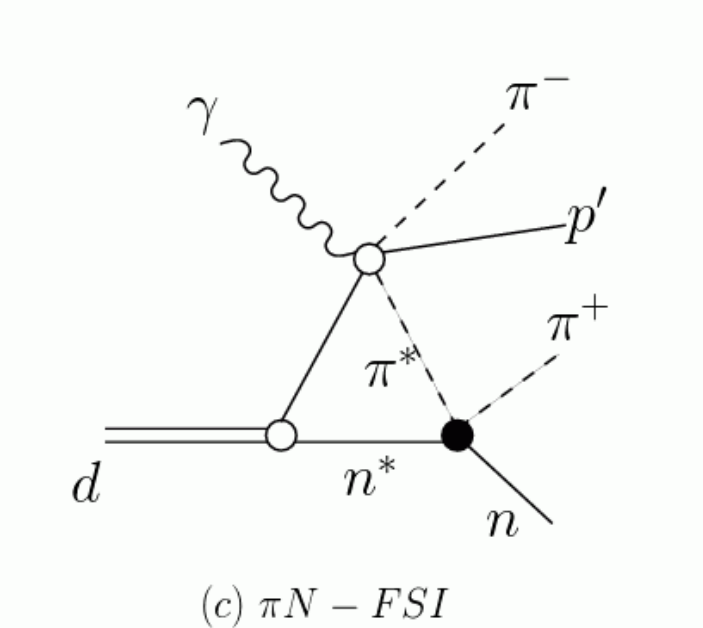
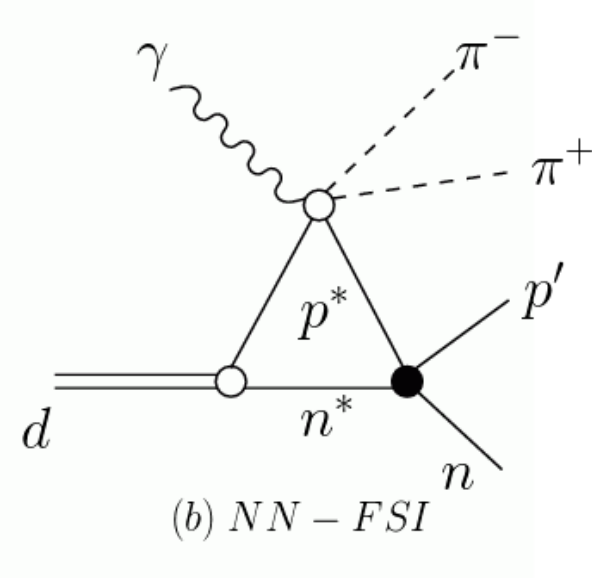
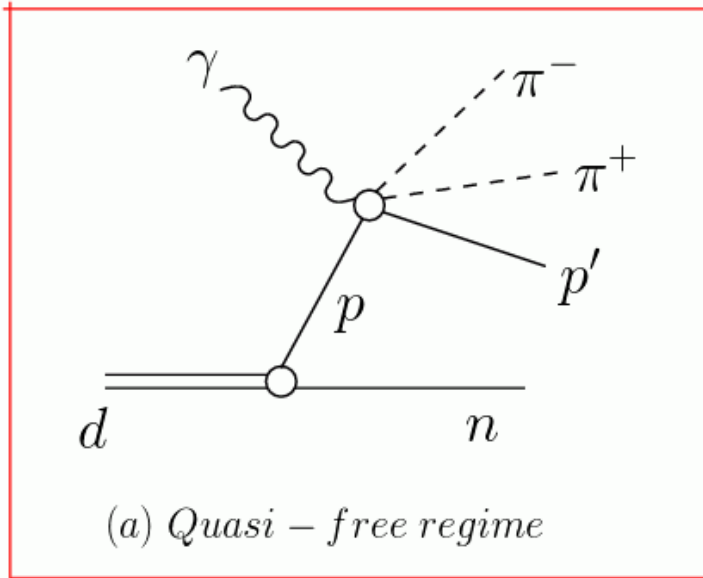
# Corrections to the Cross Sections

- *Correction due to FSI*
- Empty target subtraction
- Correction due to the filling cells with zero acceptance from the EG
- Radiative correction
- *Correction due to Fermi motion of the target proton*

# Final State Interactions

- Interaction of final hadrons with each other → rather small effect as it is known from  $2\pi$  production off the free proton
- Interaction of final hadrons with the additional nucleon (neutron) = rescattering under the influence of the strong interaction via resonant and/or non-resonant mechanisms → noticeable effect

# Quasi-Free Regime and FSI for $p(n)\pi^+ \pi^-$ Final State



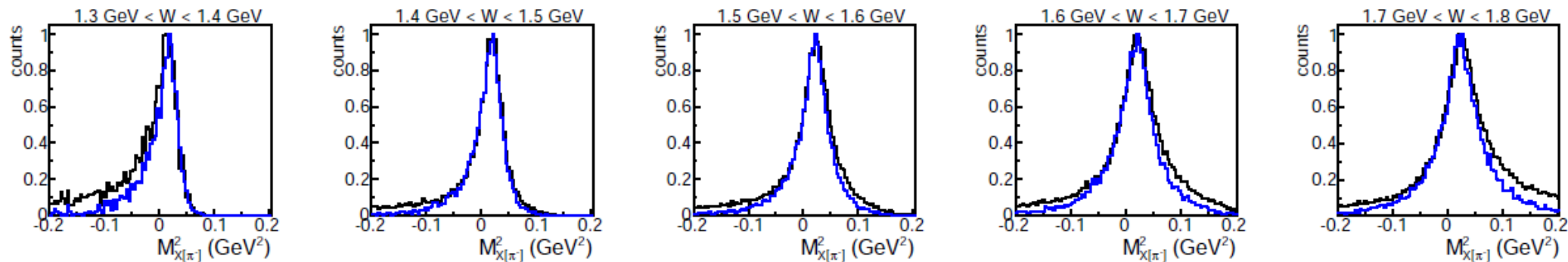
# FSI for $p(n)\pi^+\pi^-$ Final State

FSI strongly depend on:

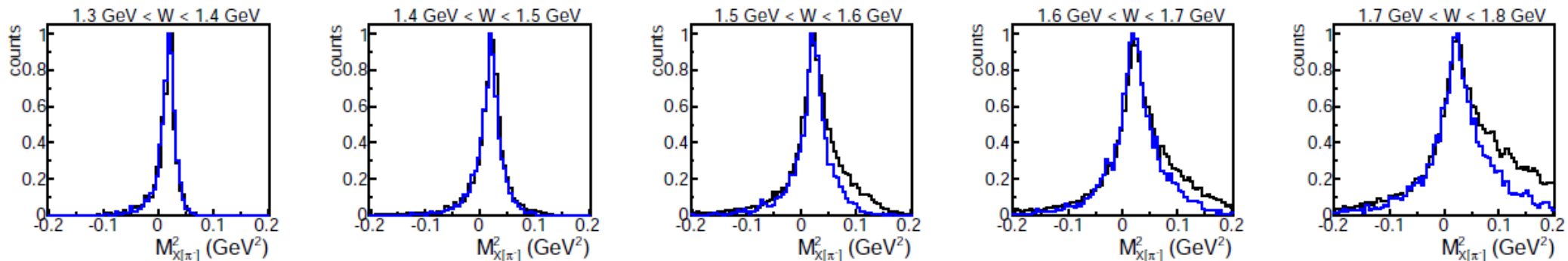
- Invariant mass of final hadron system ( $W$ )
- Scattering angles of final hadrons  $\rightarrow$  FSI are topology dependent!

$$M_{X[\pi^-]}^2 = [P_e^\mu + P_p^\mu - P_{e'}^\mu - P_{p'}^\mu - P_{\pi^+}^\mu]^2, \quad \text{where } P_i^\mu \text{ are the four-momenta of the particle } i.$$

## Fully exclusive topology

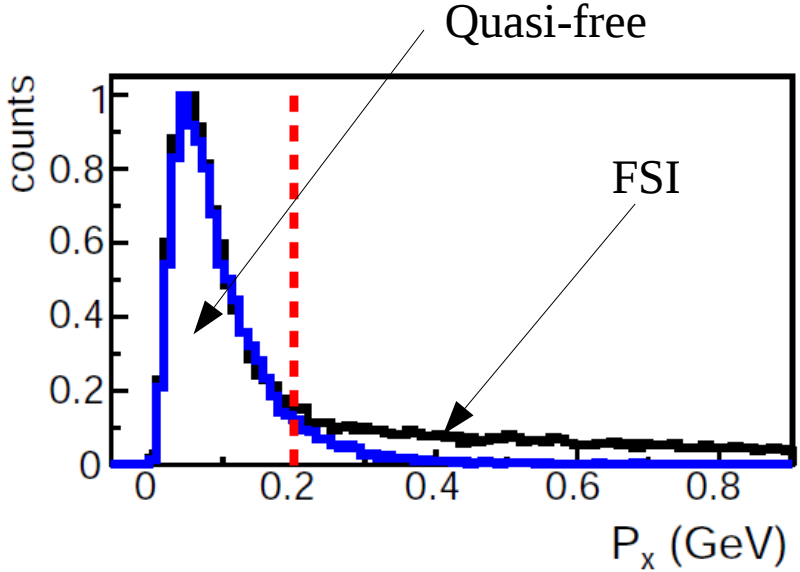


## $\pi^-$ missing topology



**Black curve** – data, **Blue curve** – simulation (FSI not included)

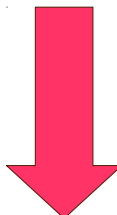
# Selection of Quasi-Free Events in Fully Exclusive Topology



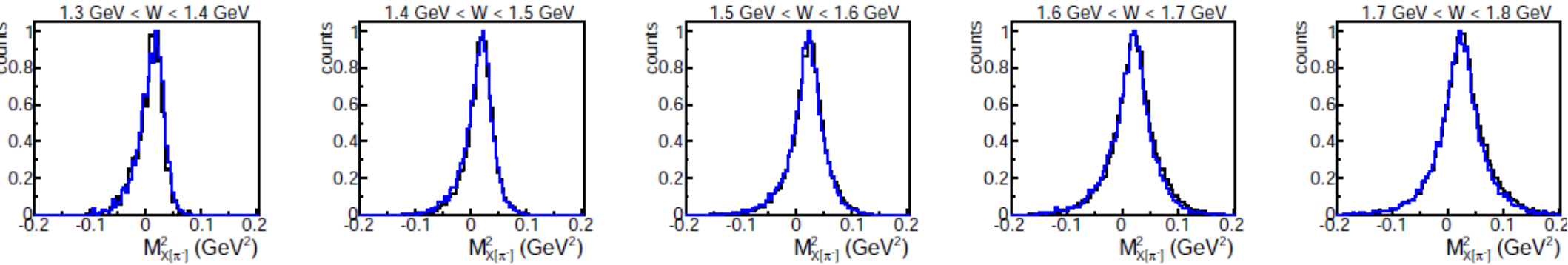
$$P_X = |\vec{P}_e - \vec{P}_{e'} - \vec{P}_{p'} - \vec{P}_{\pi^+} - \vec{P}_{\pi^-}|,$$

where  $\vec{P}_i$  are the three-momenta of the particle  $i$ .

Cut  $P_x = 0.2$  GeV selects quasi-free events.



After the cut.

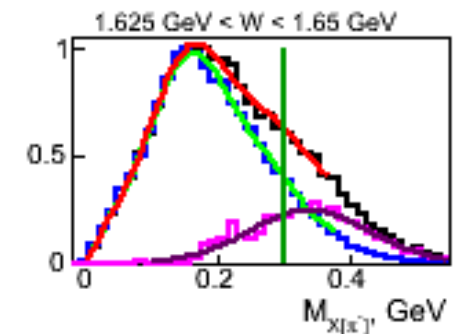
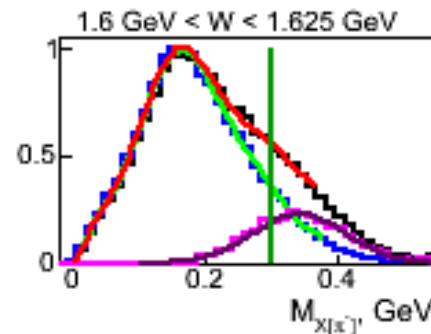
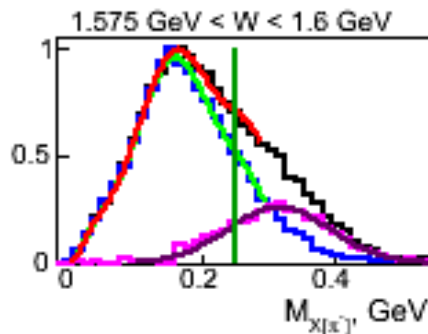


**Black curve** – data, **Blue curve** – simulation (FSI not included)

# Effective FSI Correction for $\pi$ Missing Topology

$$\frac{d^7 \sigma_{corrected}}{dW dQ^2 d^5 \tau} = \frac{d^7 \sigma_{not\ corrected}}{dW dQ^2 d^5 \tau} \times F_{fsi}(\Delta W)$$

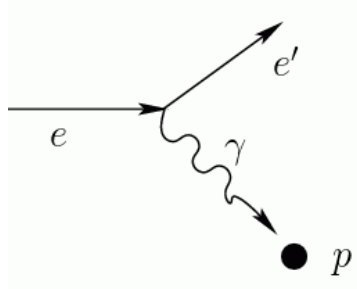
$$F_{fsi}(\Delta W) = \frac{\text{Area under green}}{\text{Area under red}}$$



**Black histogram** – experimental data, **Blue histogram** – simulation, **Purple histogram** – their difference.  
**Red curve** – fit to the data, **Green curve** – fit to the simulation, **Purple curve** – fit to the difference.

# Invariant Mass of Final Hadronic System

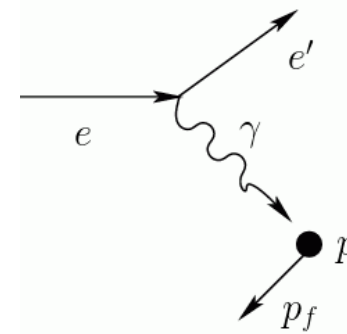
Proton at rest



$$P_p^{at\ rest} = (0, 0, 0, m_p)$$

$$W_{true} = \sqrt{(P_p^{at\ rest} + P_{\gamma v})^2}$$

Moving proton



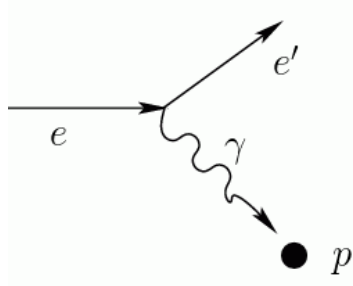
$$P_p^{moving} = (p_{fx}, p_{fy}, p_{fz}, \sqrt{m_p^2 + p_f^2})$$

$$W_{true} = \sqrt{(P_p^{moving} + P_{\gamma v})^2}$$



# Invariant Mass of Final Hadronic System

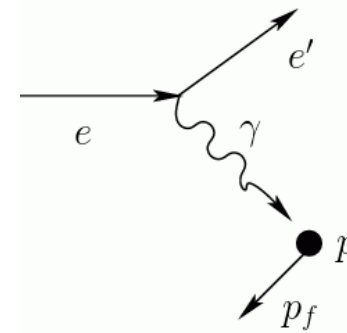
Proton at rest



$$P_p^{at\ rest} = (0, 0, 0, m_p)$$

$$W_{true} = \sqrt{(P_p^{at\ rest} + P_{\gamma\nu})^2}$$

Moving proton



$$P_p^{moving} = (p_{fx}, p_{fy}, p_{fz}, \sqrt{m_p^2 + p_f^2})$$

$$W_{true} = \sqrt{(P_p^{moving} + P_{\gamma\nu})^2}$$

$P_f$  is unknown if  $\pi$  is missing

In target-at-rest assumption



$$W_{fsm} = \sqrt{(P_p^{at\ rest} + P_{\gamma\nu})^2}$$

# Correcting the Effects of Fermi Motion on the Cross Sections

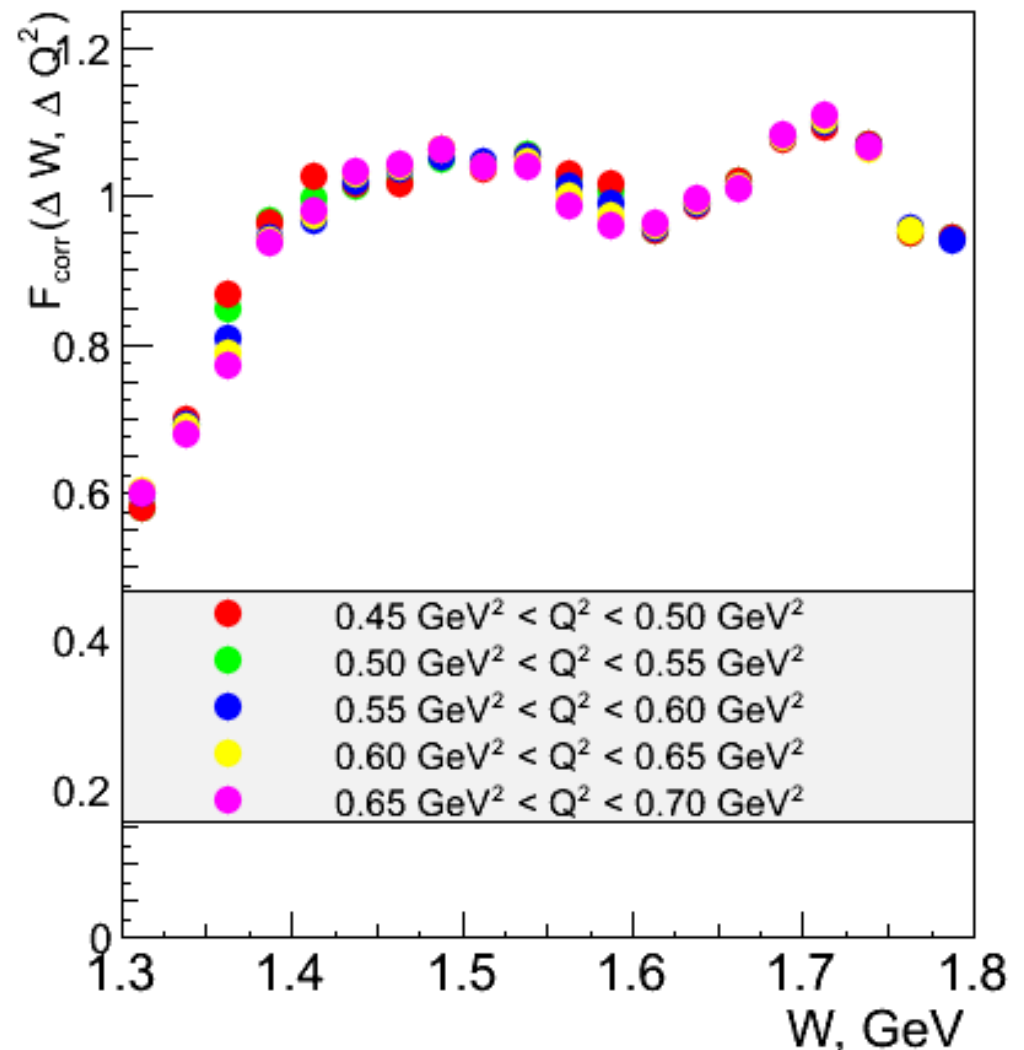
$$\frac{d^7 \sigma_{corrected}}{dW_{true} dQ^2 d^5 \tau} = \frac{d^7 \sigma_{not\ corrected}}{dW_{fsm} dQ^2 d^5 \tau} \times F_{corr}(\Delta W, \Delta Q^2, \Delta \tau)$$

$$F_{corr}(\Delta W, \Delta Q^2, \Delta \tau) =$$

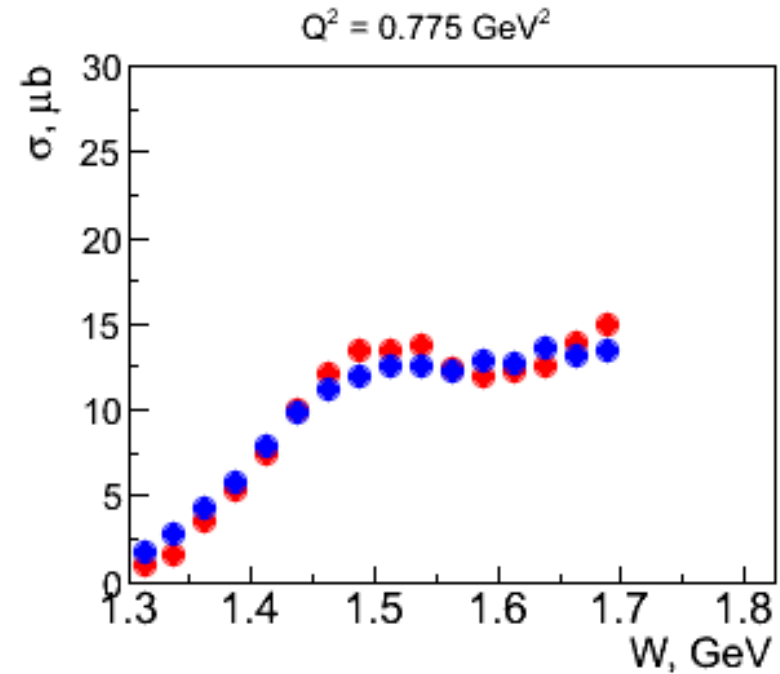
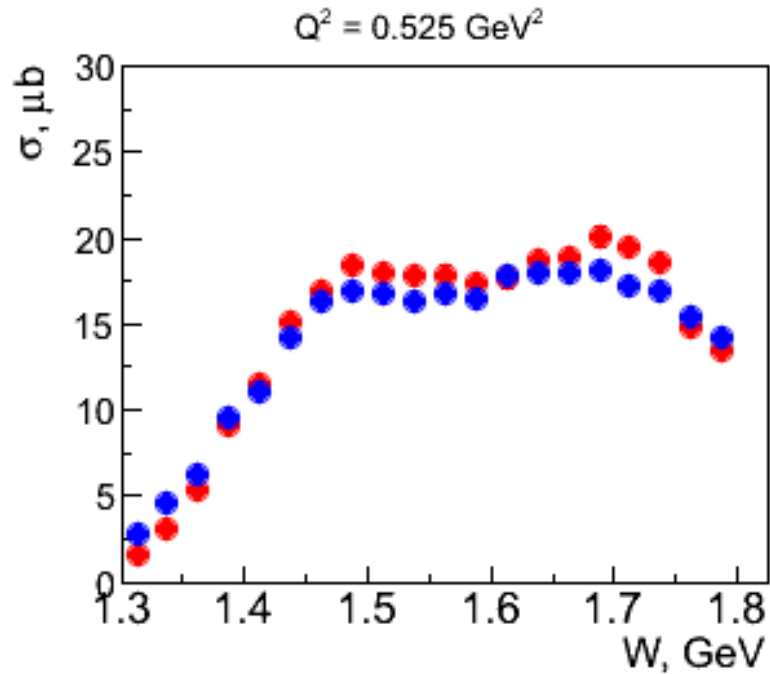
$$\frac{N_{nofermi}(\Delta W, \Delta Q^2, \Delta \tau)}{N_{fermi}(\Delta W, \Delta Q^2, \Delta \tau)}$$

$N_{nofermi}$  – from TWOPEG on free proton

$N_{fermi}$  – from TWOPEG on moving proton



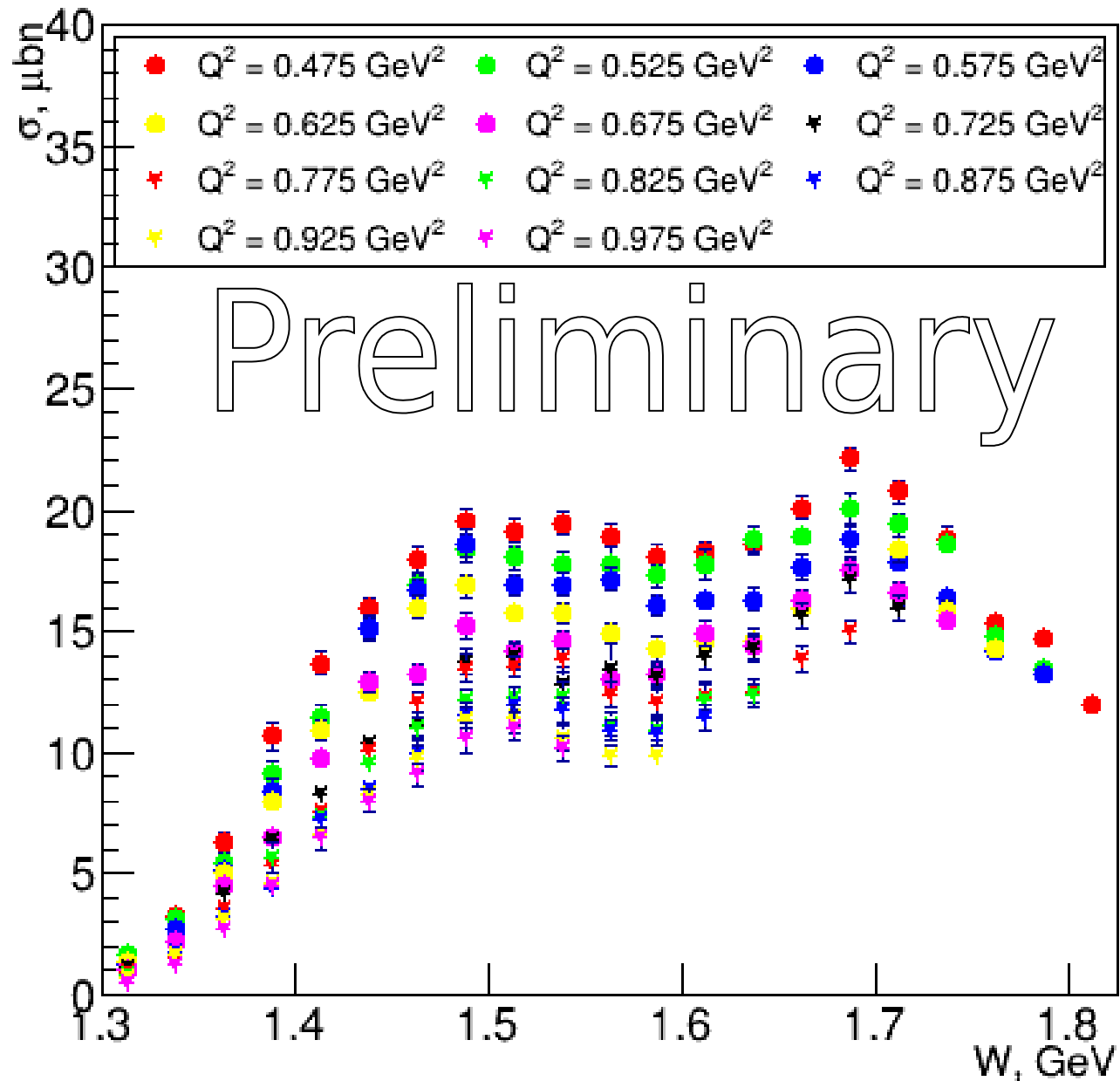
# Comparison of the Integral Cross Section with and without Fermi Correction (preliminary)



**Red symbols** – experimental integral cross section *with* Fermi correction

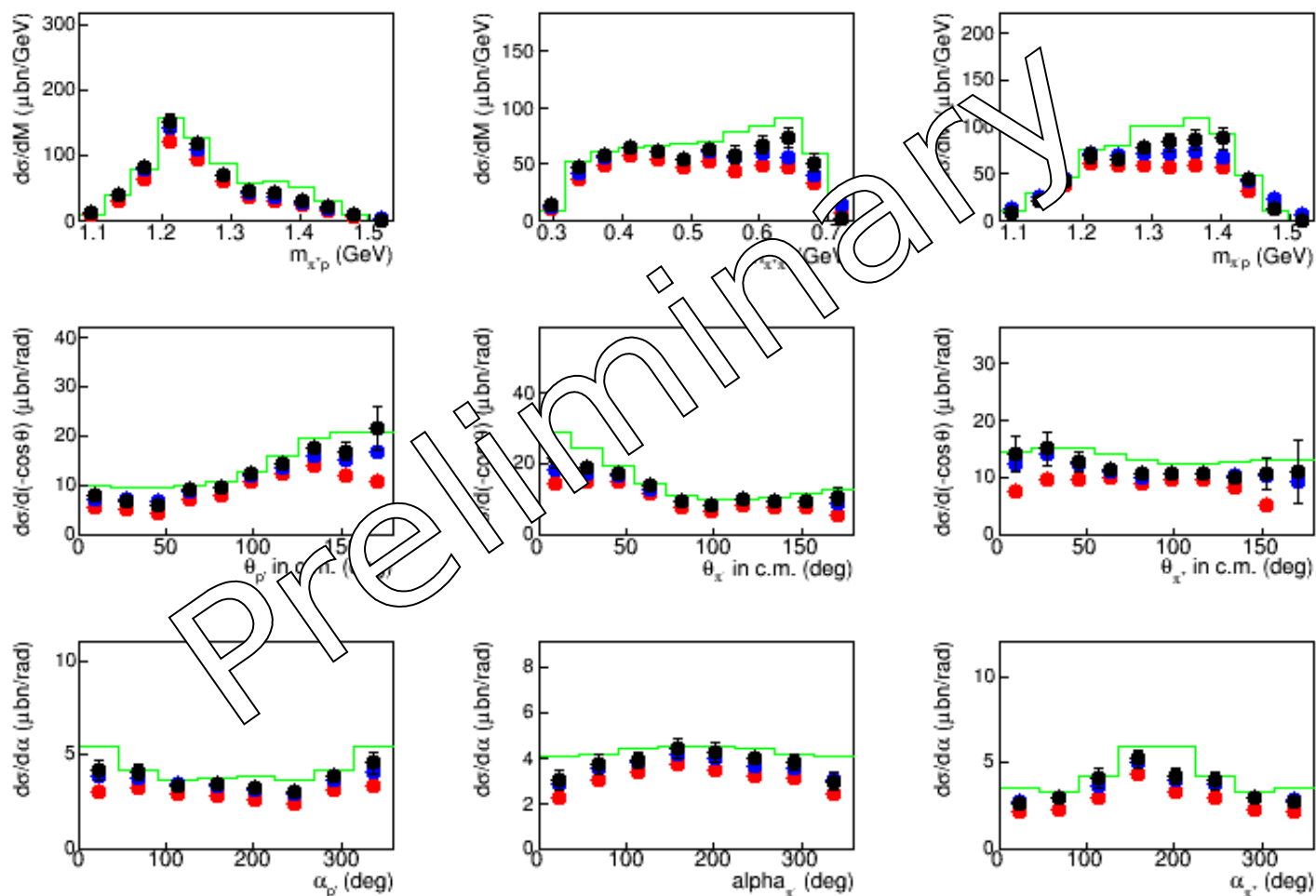
**Blue symbols** – experimental integral cross section *without* Fermi correction

# Integrated Cross Sections (Preliminary)



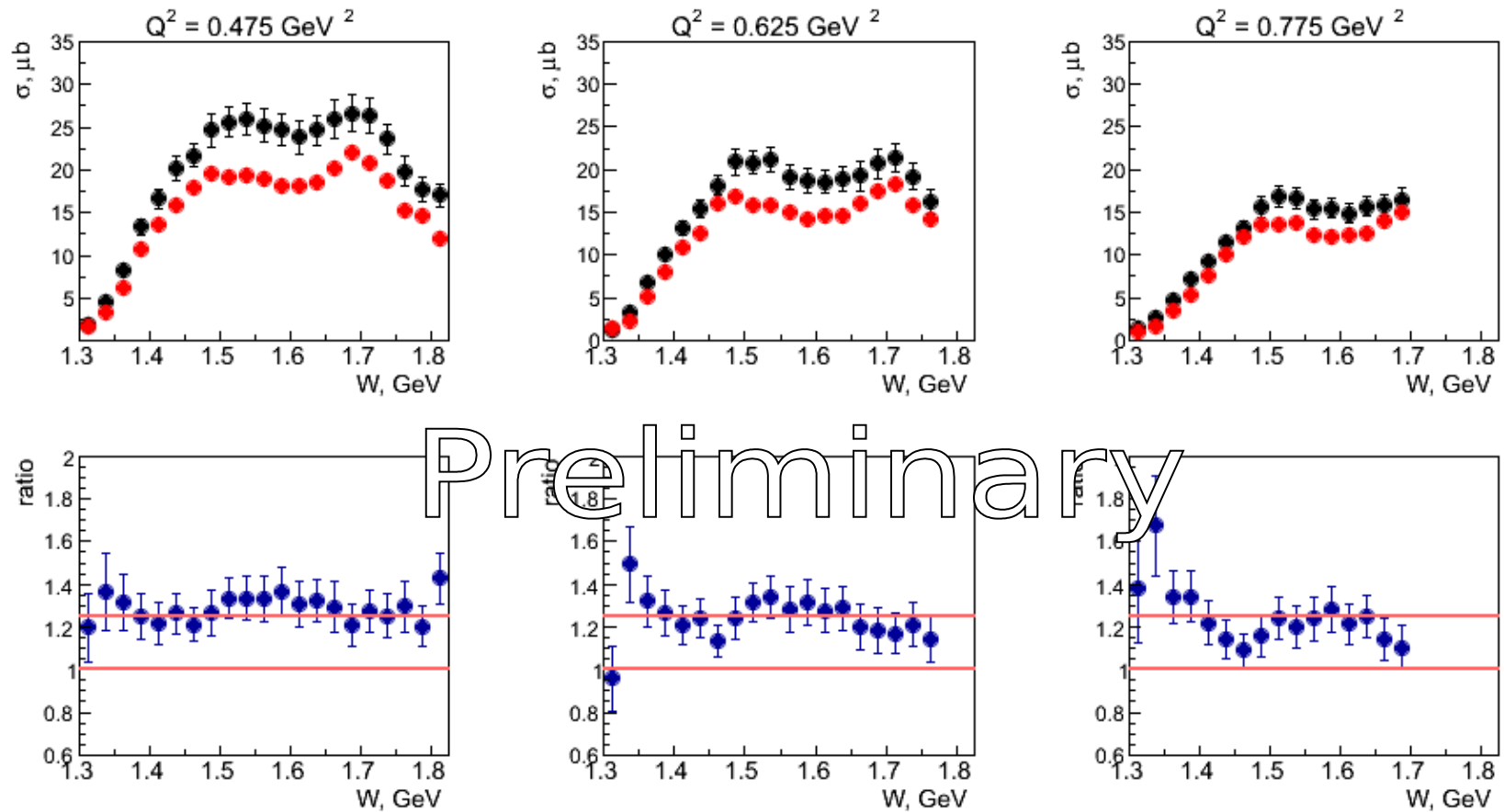
# Differential Cross Sections (Preliminary)

$$W = 1.6375 \text{ GeV}, Q^2 = 0.475 \text{ GeV}^2$$



**Red symbols** – empty cells are NOT filled    **Blue symbols** – empty cells are filled  
**Black symbols** – Fermi correction is applied    **Green curve** – from EG off the free proton 21

# Comparison with Free Proton Cross Sections



**Black symbols** – free proton cross sections ( $e1e$ ,  $E_{beam} = 2.039 \text{ GeV}$ ) [1],  
error bars show both *statistical* and *systematical* uncertainties

**Red symbols** – quasi-free cross sections on proton in deuteron ( $e1e$ ,  $E_{beam} = 2.039 \text{ GeV}$ ),  
error bars show *statistical* uncertainty only

**Blue symbols** – their ratio

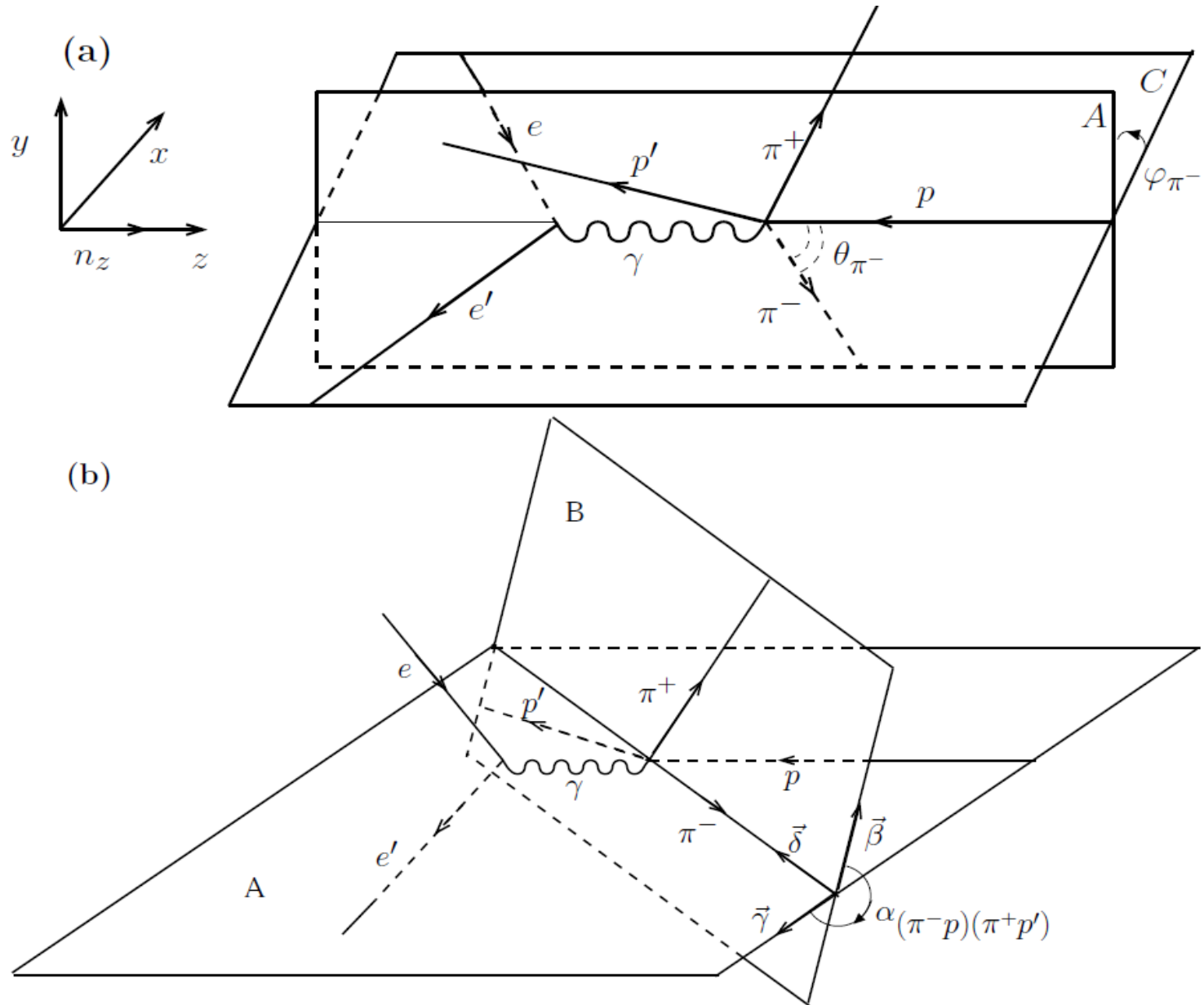
# Conclusion

- Integral and single-differential cross sections of the reaction  $\gamma_{\nu} p(n) \rightarrow p'(n')\pi^+ \pi^-$  in quasi-free regime are extracted for the first time
- The procedure of correcting the cross section distortion due to the Fermi motion is developed and applied
- The procedure of selecting events in quasi-free kinematics is developed
- TWOPEG was tested and for the first time used for the efficiency evaluation

Thank you!

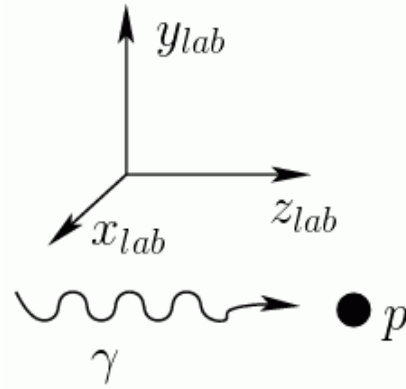


# $2\pi$ Kinematics



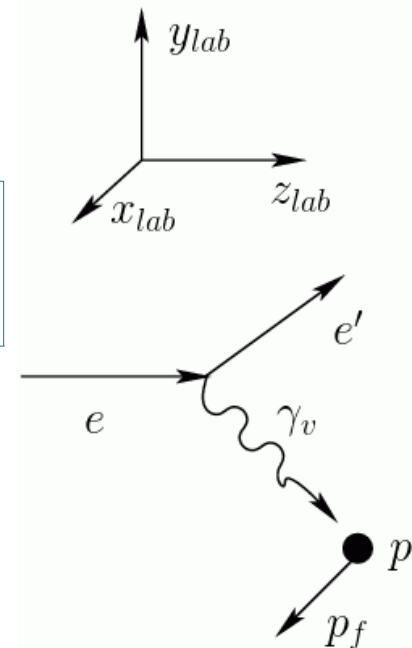
# Lab-to-CMS Transformation

## Photoproduction off the free proton



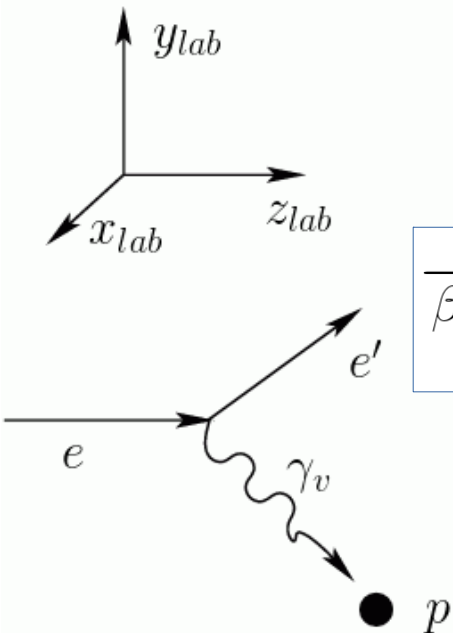
$$\vec{\beta} = \left( 0, 0, \frac{|\vec{q}_\gamma|}{E_\gamma + m_p} \right)$$

## Electroproduction off the moving proton

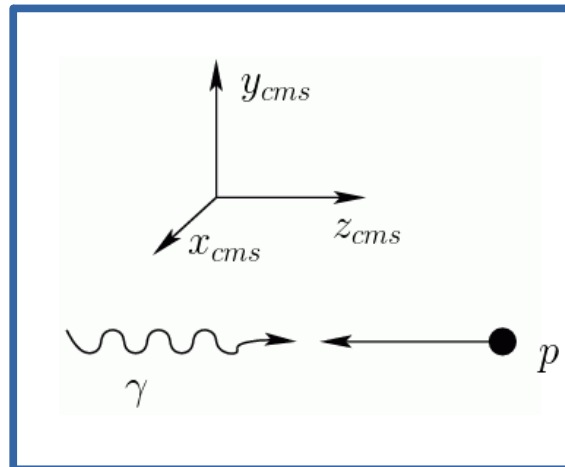


$$\vec{\beta} = \frac{\vec{q}_\gamma + \vec{p}_f}{E_\gamma + E_p}$$

## Electroproduction off the free proton



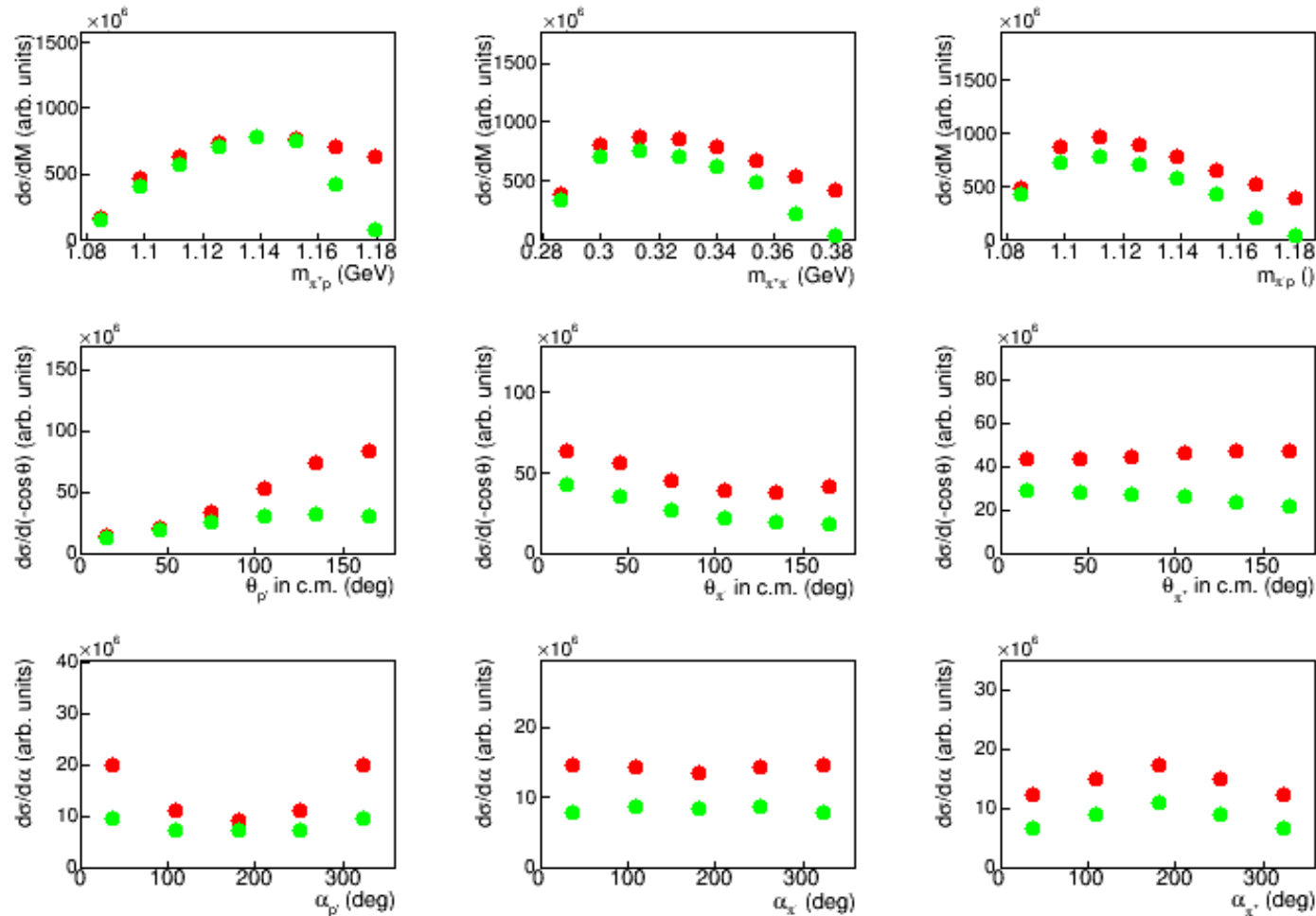
$$\vec{\beta} = \frac{\vec{q}_\gamma}{E_\gamma + m_p}$$



CMS

# Fermi Correction

$$W = 1.3125 \text{ GeV}, Q^2 = 0.475 \text{ GeV}^2$$

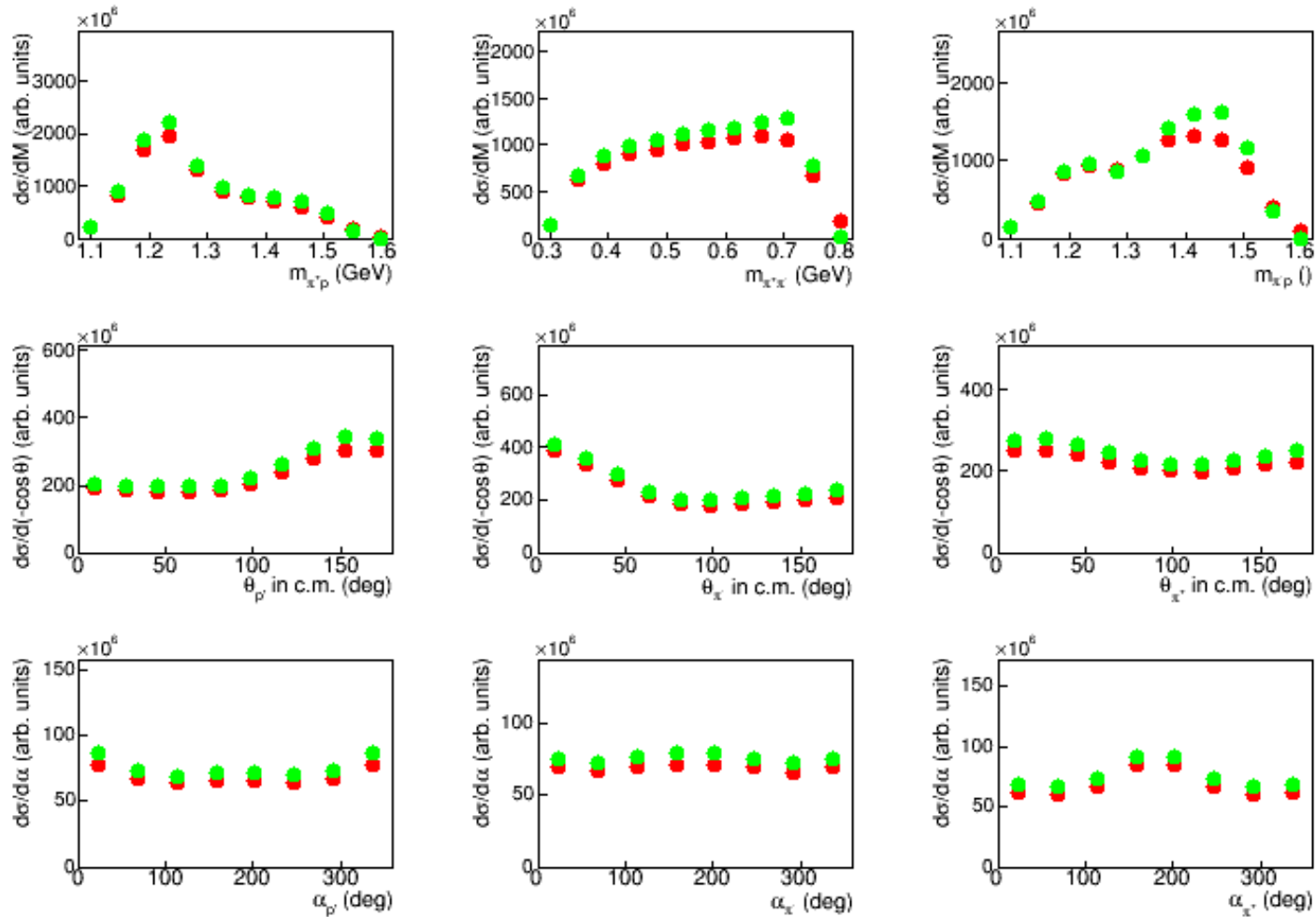


**Red symbols** – from EG for the moving proton

**Green symbols** – from EG for the free proton

# Fermi Correction

$$W = 1.7125 \text{ GeV}, Q^2 = 0.475 \text{ GeV}^2$$



**Red symbols** – from EG for the moving proton

**Green symbols** – from EG for the free proton