

Exploring the potential role of diquarks in hadronization using SIDIS on nuclear targets

*2022 International Conference
on the Structure of Baryons*
9 November 2022

Will Brooks



Comprehensive review from last year

Progress in Particle and Nuclear Physics 116 (2021) 103835



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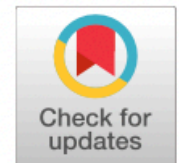
Progress in Particle and Nuclear Physics

journal homepage: www.elsevier.com/locate/ppnp



Review

Diquark correlations in hadron physics: Origin, impact and evidence



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C.D. Roberts^{18,19,*}, P. Rossi^{12,20}, G. Salmé²¹, E. Santopinto²², J. Segovia^{23,19},
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<https://doi.org/10.1016/j.ppnp.2020.103835>

<https://arxiv.org/abs/2008.07630>

Diquarks in theory	
2.1. Phenomenological quark models	
2.1.1. Diquark wave functions.....	
2.1.2. Diquark masses.....	
2.1.3. Light and heavy-light baryons in the diquark model..	
2.1.4. Compact tetraquarks in the diquark model.....	
2.1.5. Compact pentaquarks in the diquark model	
2.2. Continuum schwinger function methods.....	
2.2.1. Diquarks	
2.2.2. Insights from a contact interaction.....	
2.2.3. QCD-kindred formulation.....	
2.2.4. <i>Ab initio</i> approach	
2.2.5. Baryon distribution amplitudes.....	
2.3. Lattice-regularised QCD.....	
2.3.1. Effective masses of diquarks in Landau gauge	
2.3.2. Diquark correlations within baryons	
2.3.3. Bethe–Salpeter wave function approach.....	
2.3.4. Light-cone distribution amplitudes.....	

Diquarks in experiment and phenomenology	
3.1. Space-like nucleon form factors	
3.2. Time-like nucleon form factors.....	
3.3. Nucleon to resonance transition form factors.....	
3.4. Multidimensional structure of baryons.....	
3.4.1. Transverse momentum dependent parton distributions.....	
3.4.2. Generalised parton distributions.....	
3.5. Meson structure as a window onto diquark structure	
3.6. Exotic hadrons and their connection to diquarks	
3.6.1. Experimental status at a glance	
3.6.2. Theoretical tools for analyses of exotics	
3.6.3. Production of exotic states in pp and heavy-ion collisions ..	

**There are experimental indications of diquarks too,
but more limited than the theoretical evidence.**

How can we improve the experimental evidence?

SIDIS on Nuclear Targets!

A full-QCD lattice study of diquarks was carried out with lattice chiral fermions:

“Diquark mass differences from unquenched lattice QCD”

Yujiang Bi, Hao Cai, Ying Chen, Ming Gong, Zhaofeng Liu, Hao-Xue Qiao, Yi-Bo Yang

<https://iopscience.iop.org/article/10.1088/1674-1137/40/7/073106/pdf>

Table 2.3.3

Effective masses M_q of u, d quarks, M_s of the strange quark, and those of diquarks (m_{0+} and m_{1+}), computed in Landau gauge and extrapolated to the chiral limit.

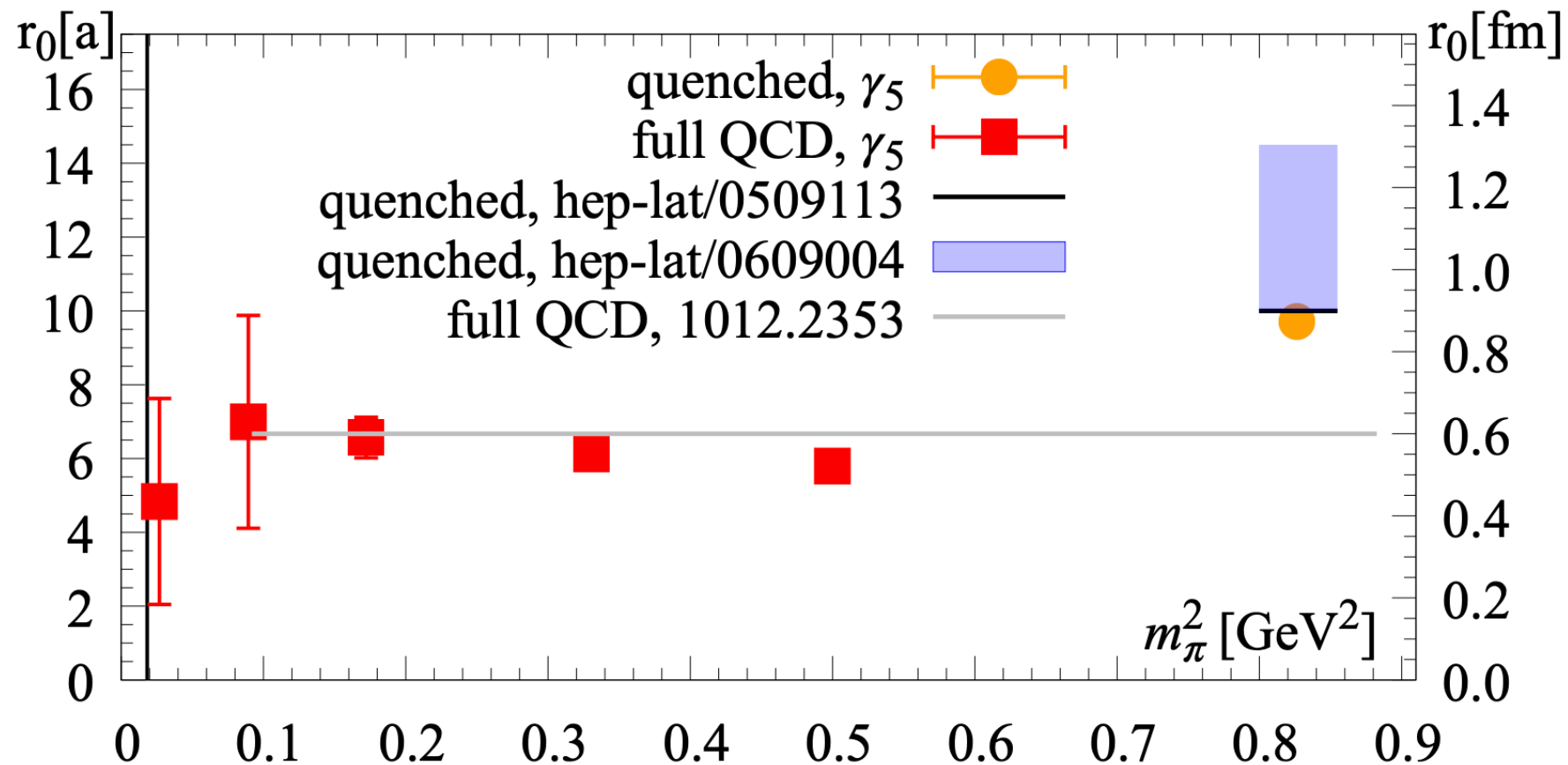
	M_q (MeV)	M_s (MeV)	m_{0+} (MeV)	m_{1+} (MeV)	$m_{1+} - m_{0+}$ (MeV)
c02	492(19)	575(23)	797(24)	1127(28)	330(35)
c005	427(25)	586(16)	725(20)	1022(44)	297(48)
f004	413(12)	603(15)	690(47)	990(60)	300(76)

The diquark mass can **exceed the proton mass (0.7-1.1 GeV)**.
Such large masses are found in models of diverse types.

“Diquark properties from full QCD lattice simulations”

Anthony Francis, Philippe de Forcrand, Randy Lewis, Kim Maltmane

[https://link.springer.com/article/10.1007/JHEP05\(2022\)062](https://link.springer.com/article/10.1007/JHEP05(2022)062)



Obtained in a *gauge-invariant* way in this work.

The **diquark shape** is estimated to be *spherical*.

Some diquarks have ‘good’ flavor, color and Dirac quantum numbers ($\bar{3}_F, \bar{3}_c, J^P = 0^+$).

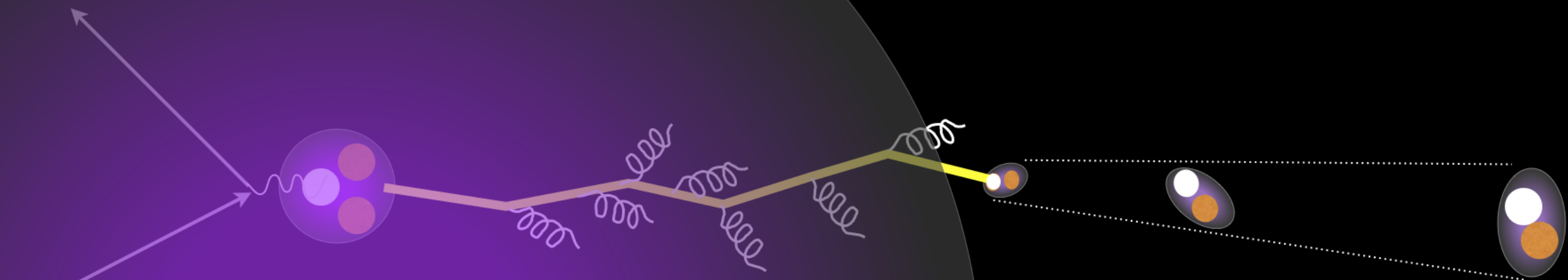
“Both one-gluon-exchange and instanton interactions are attractive in this channel.”

“Good” diquark size is estimated to be **0.6 fm**



By implanting the hadronization process within a nucleus, we gain new dynamical information at *femtometer distance scales*.

From the modifications of kinematic distributions for $A(e, e' h) X$ scattering, we can infer hadronization mechanisms for hadron h .



Important kinematic variables used here

Four-momentum transfer squared Q^2

Energy transfer ν ($=E-E'$ in the laboratory frame)

“Relative energy” $z = z_h = \frac{E_{hadron}}{\nu}$

Note: if the virtual photon is absorbed by a light object like a single quark, $z_h \leq 1.0$, but if it is absorbed by a heavy object, it can be **greater than 1.0**

Momentum transverse to the virtual photon direction p_T

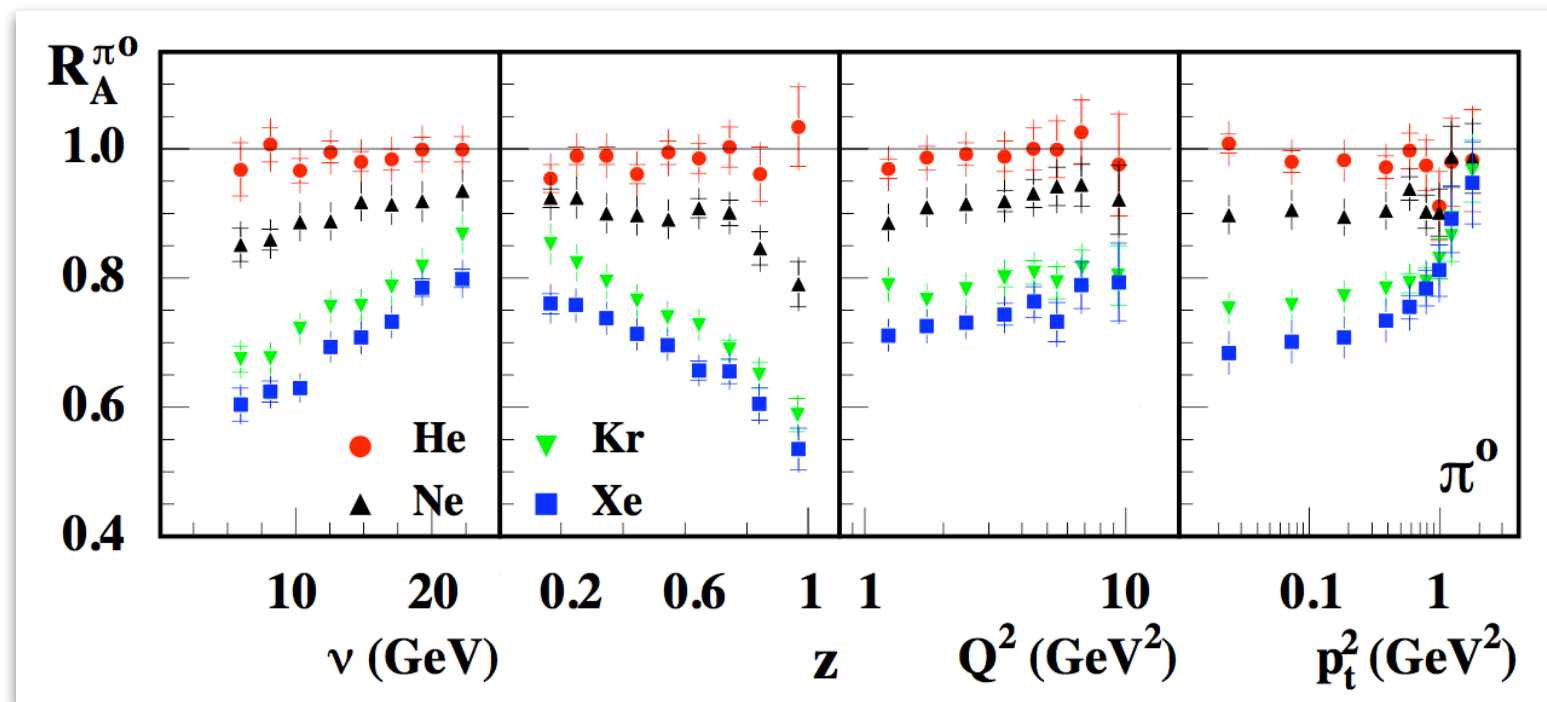
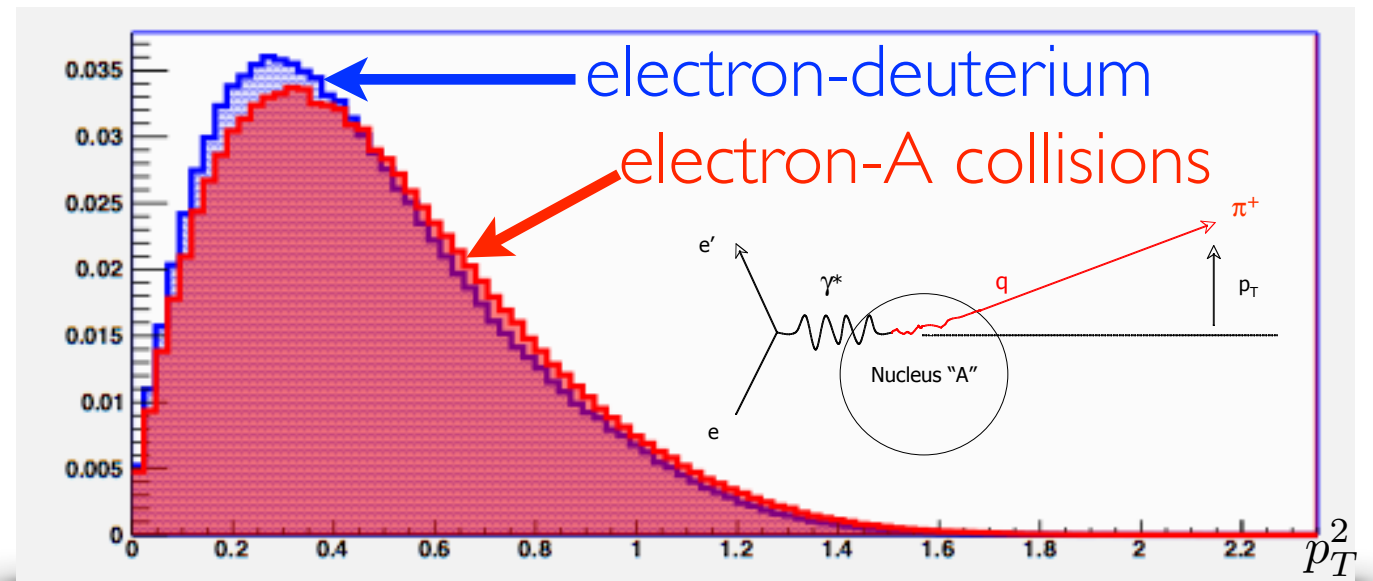
NB, what once was “hadronization” and then “hadron formation” is evidently now more popularly included as “Emergent Hadron Mass” (“EHM”)

EHM = EHM(time) in these studies, on the fm/c timescale

$$\Delta p_T^2(Q^2, \nu, z_h) \equiv \langle p_T^2(Q^2, \nu, z_h) \rangle |_A - \langle p_T^2(Q^2, \nu, z_h) \rangle |_D$$

Experimental
observables

Transverse momentum broadening



Hadronic
multiplicity ratio

$$R_M^h(Q^2, \nu, z_h, p_T) \equiv \frac{\frac{1}{N_e(Q^2, \nu)} \cdot N_h(Q^2, \nu, z_h, p_T)|_A}{\frac{1}{N_e(Q^2, \nu)} \cdot N_h(Q^2, \nu, z_h, p_T)|_D}$$



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Physics Letters B

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Estimating the color lifetime of energetic quarks

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^b Centro Científico Tecnológico de Valparaíso, Valparaíso, Chile

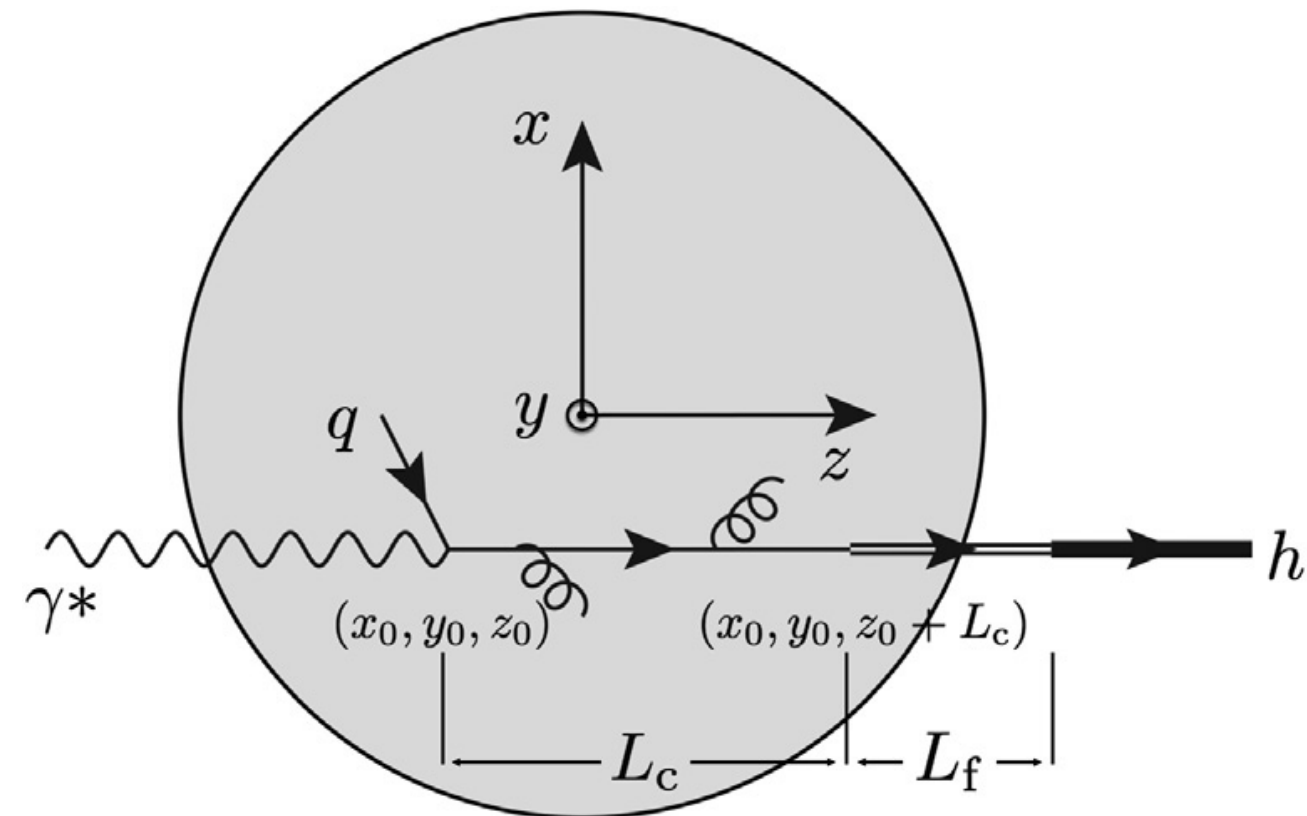
^c Department of Physics and Astronomy, University of New Hampshire, Durham NH, USA

^d Physikalisches Institut, Universität Heidelberg, Heidelberg, Germany

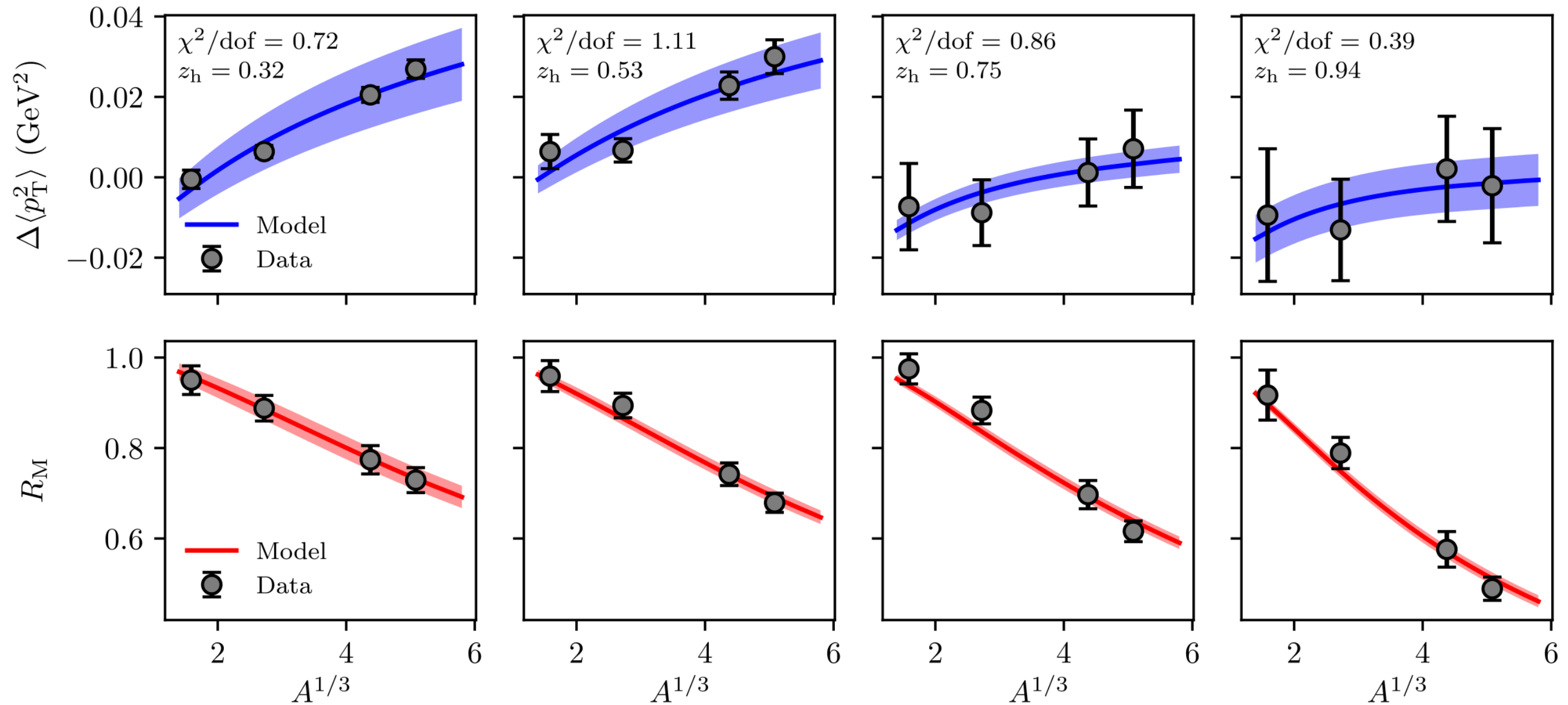


Struck quark moves a distance L_c as a **colored** object, then becomes a **hadron**. If the hadron forms **inside** the medium, it can interact with hadronic cross section.

The color lifetime of the struck quark is distributed stochastically as a decaying exponential.

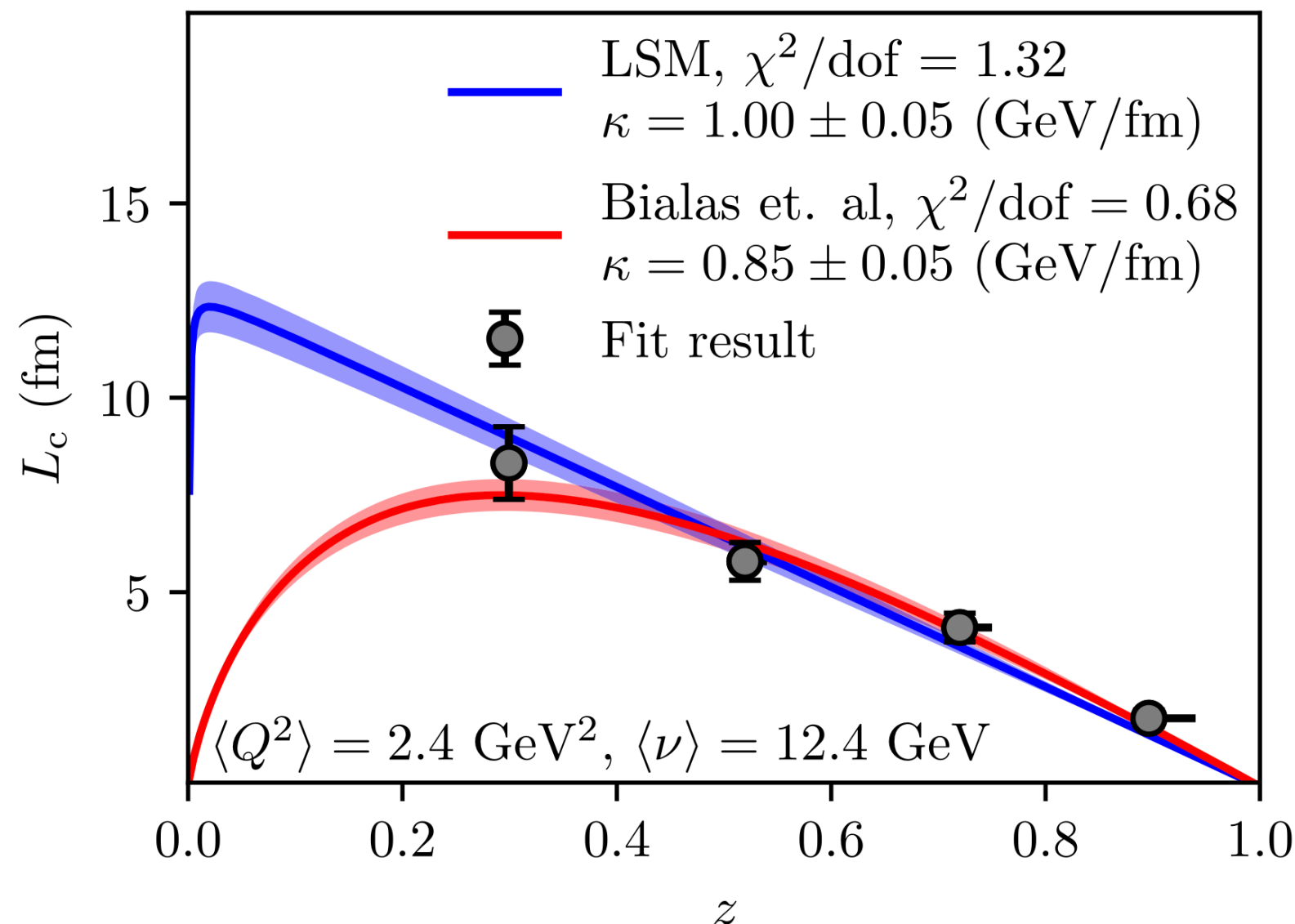


These are the results of the simultaneous fit to two observables



This **3-parameter space-time model** that fits **two observables simultaneously** gives the **semi-classical limit** of the true **quantum-mechanical** system

This is a fit of the color lifetime parameter L_c we find to the color lifetime calculated in the Lund String Model



The blue line only describes the **struck quark**

The red line describes the **struck quark and the residual quarks**

Independent determination of the string constant of the LSM!

Message: our space-time model is **consistent** with known **string fragmentation**, and for HERMES the **time range is 2-8 fm/c**.

We believe we have a correct physical picture for **pion formation**.

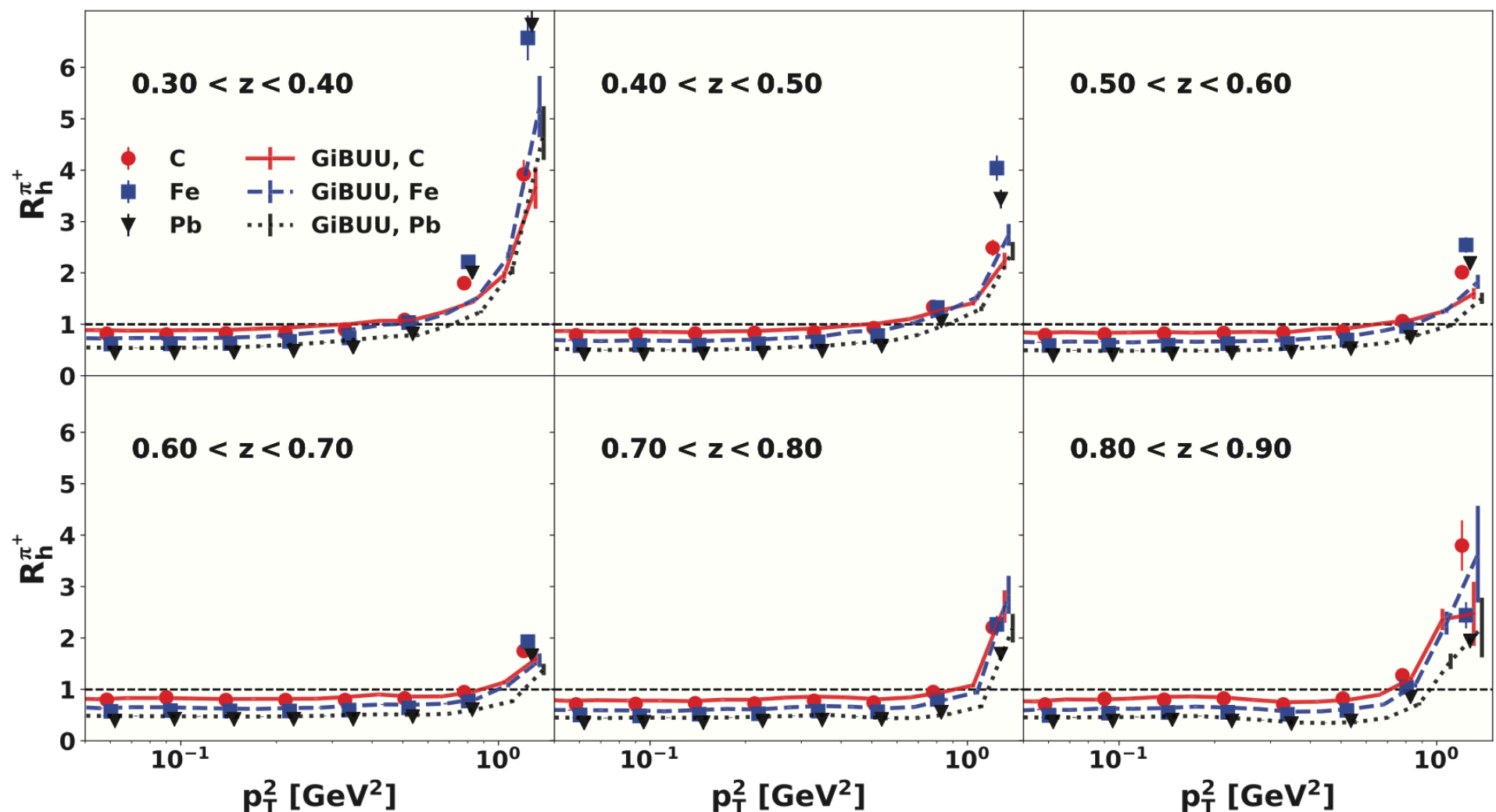
Measurement of charged-pion production in deep-inelastic scattering off nuclei with the CLAS detector

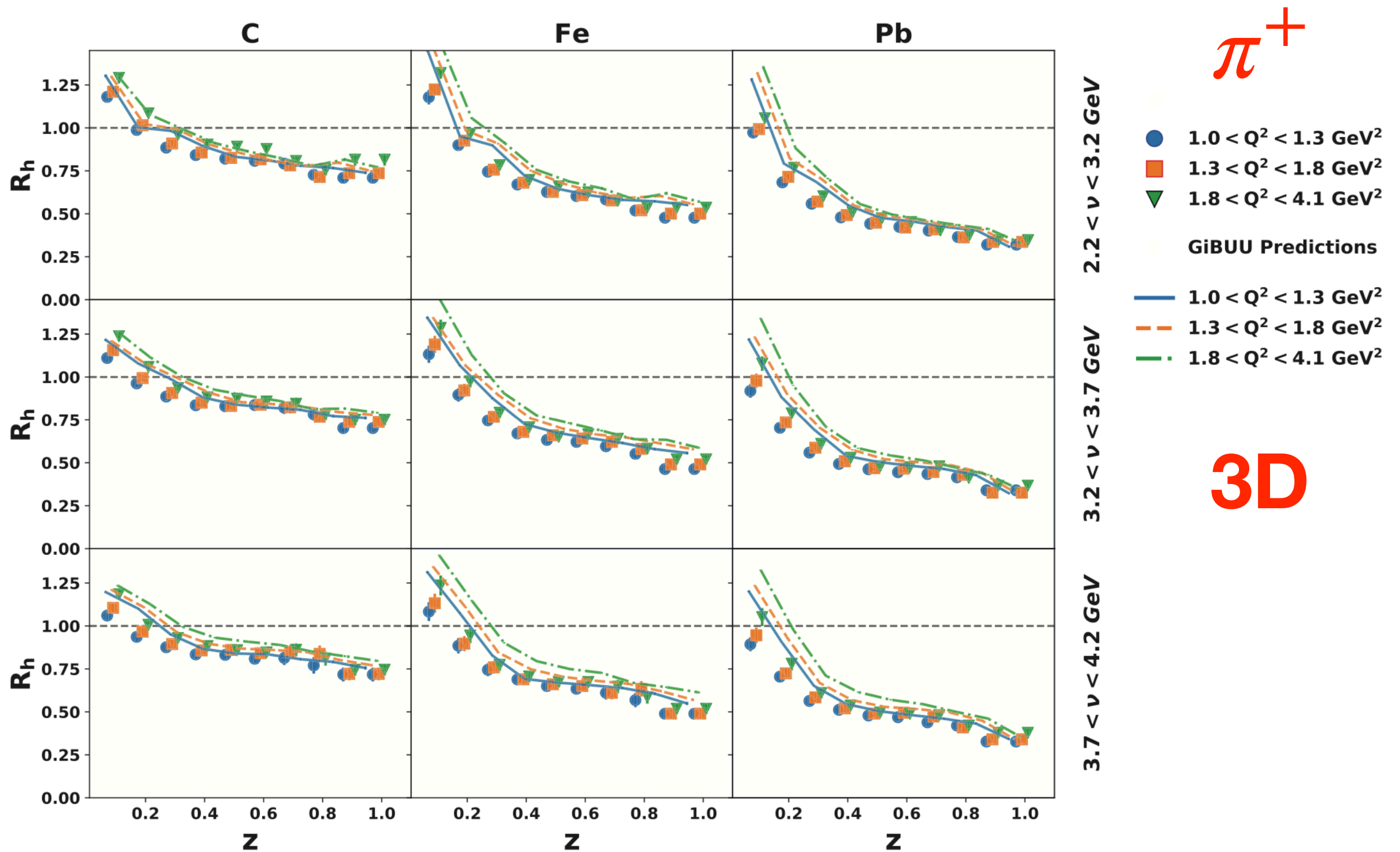
S. Morán,^{1,3} R. Dupre,² H. Hakobyan^{id},^{1,52} M. Arratia,³ W. K. Brooks,¹ A. Bórquez,¹ A. El Alaoui,¹ L. El Fassi,^{4,5} K. Hafidi,¹ R. Mendez,¹ T. Mineeva,¹ S. J. Paul,³ M. J. Amaryan,³⁶ Giovanni Angelini,¹⁹ Whitney R. Armstrong,⁵ H. Atac,⁴³

In this paper we compare high-precision CLAS data with the predictions of the **GiBUU** and **GK** models for charged pions in a *three dimensional analysis*, finding semi-quantitative **agreement**.

2D

Lines are
predictions from
the GiBUU event
generator with
standard
parameters





Lines are *predictions* from the GiBUU event generator with standard parameters

Phys. Rev. C 105, 015201 (2022)

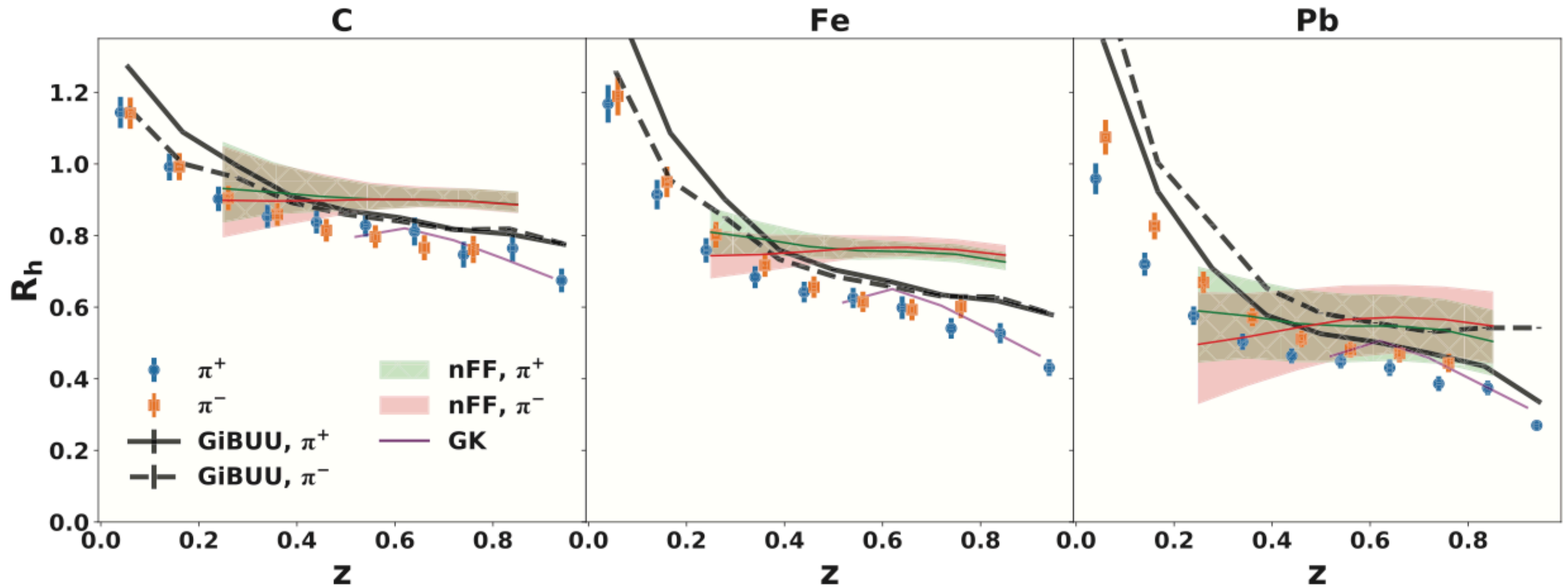
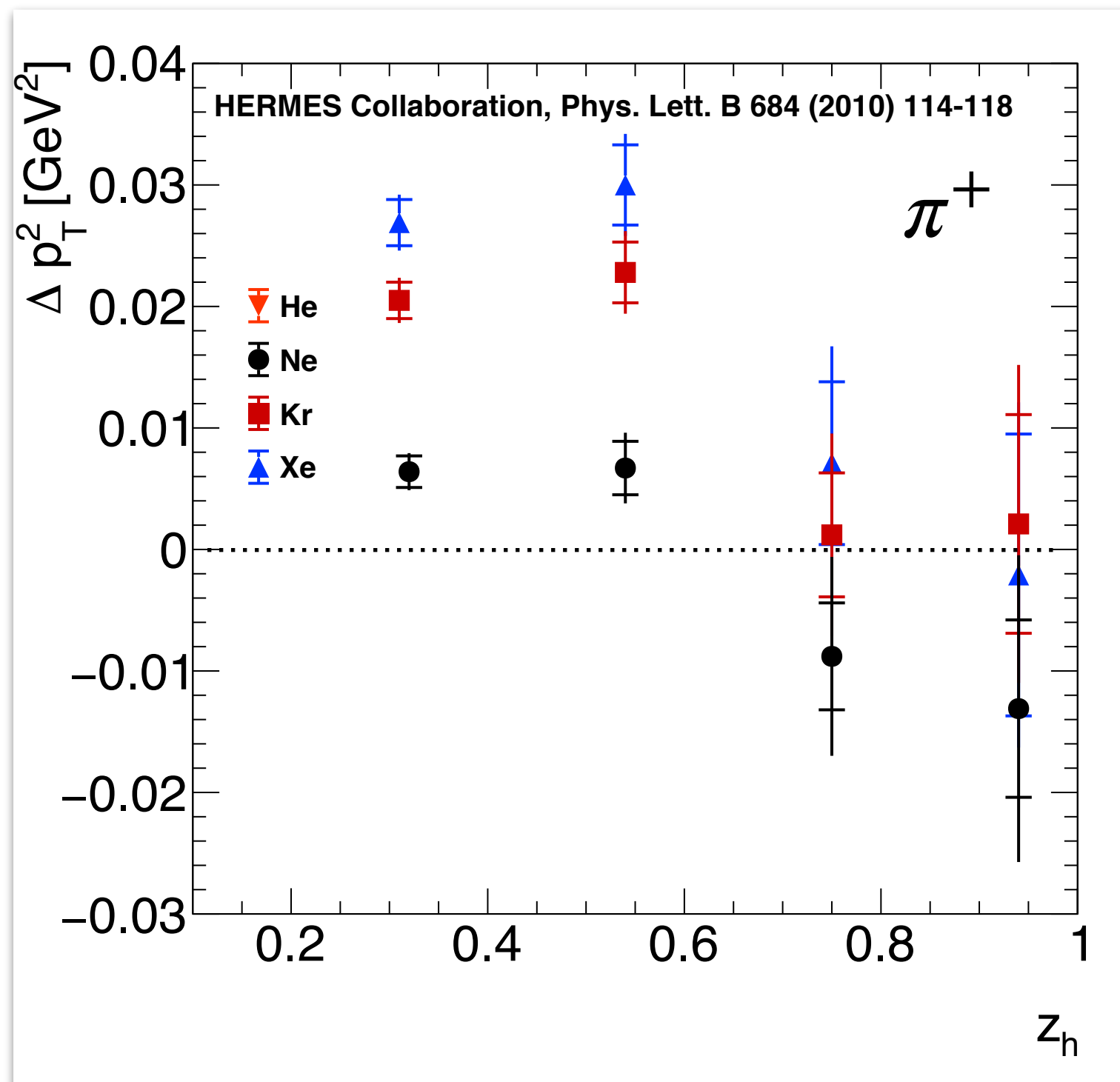


FIG. 1. Multiplicity ratio of π^+ and π^- as a function of z ; the three different panels show results for C, Fe, and Pb targets, respectively. The error bars represent the quadrature sum of systematic and statistical uncertainties, which is dominated by the systematic uncertainties that are partially correlated point to point. The points have a small horizontal shift for better visualization. The lines correspond to model calculations from GiBUU, GK, and the LIKEN21 nFFs. The bands represent the uncertainty of the LIKEN21 nFF set. The numerical values of the data points and associated errors of this figure are shown in Table II in the Appendix section of the article.

Message: GiBUU can describe up to **3D pion production**
We believe we have a correct physical picture.

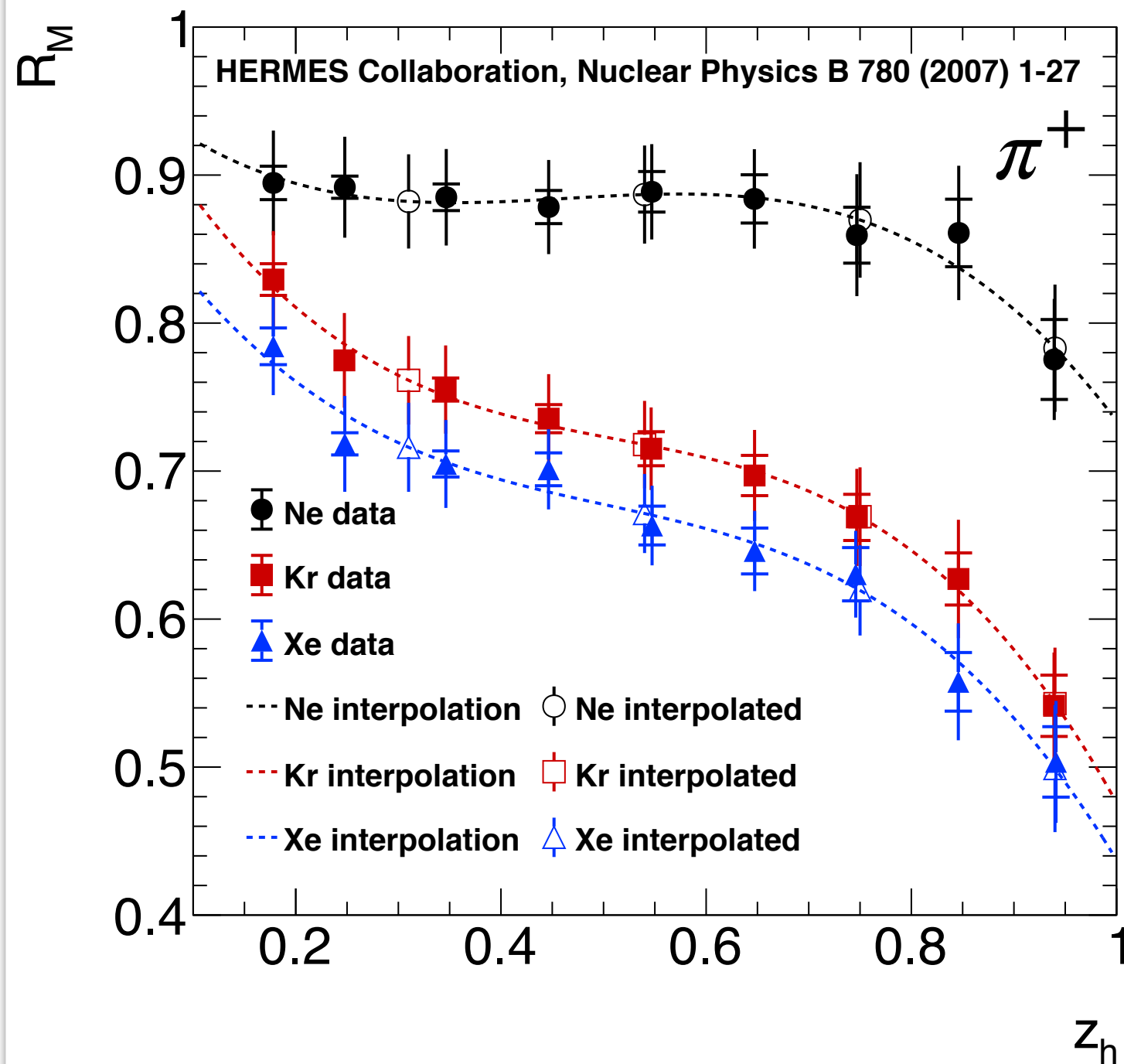
GiBUU uses hadronic degrees of freedom, it incorporates formation times, “prehadron” interactions,³ color transparency, and nuclear shadowing. These ingredients have been postulated to be necessary to describe nuclear modification of hadrons produced in DIS by the HERMES and EMC experiments. The default parameters of GiBUU 2019 are used.

Hermes data for p_T broadening vs. $z_h=E/\nu$



Note for later
discussion:
maximum is
0.03 GeV²

Hermes data, hadronic multiplicity ratio vs. $z_h = E/\nu$



Note for later discussion: **for this range in z_h ,**

$$R_M^\pi < 1$$

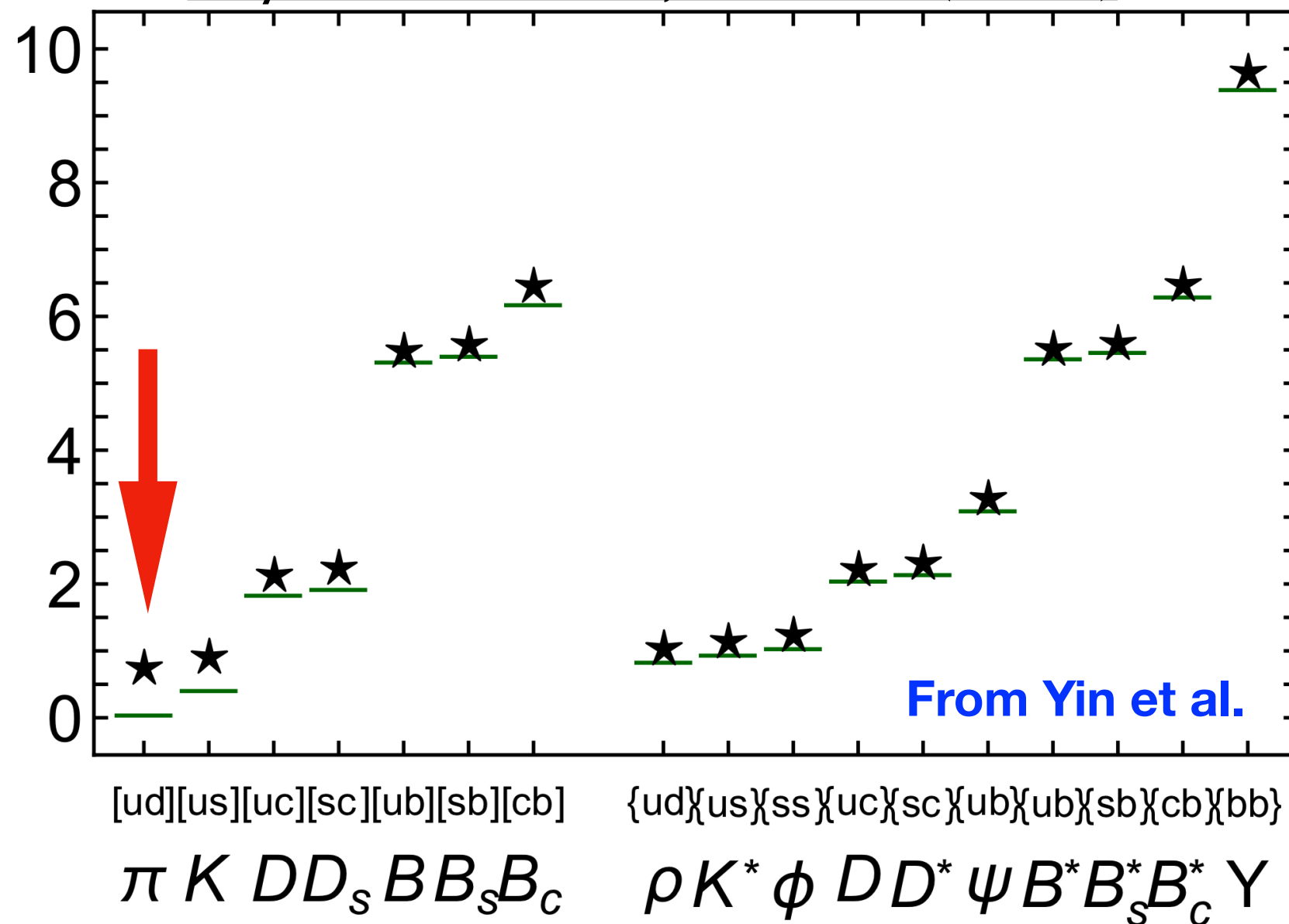
**Always
attenuation,
never
enhancement**

Masses of ground-state mesons and baryons, including those with heavy quarks

Pei-Lin Yin,^{1,*} Chen Chen,^{2,†} Gastão Krein,² Craig D. Roberts,^{3,‡} Jorge Segovia,⁴ and Shu-Sheng Xu¹

arXiv 1903.00160

Phys. Rev. D 100, 034008 (2019)



The ud diquarks are heavy, as seen previously in the lattice calculation.

FIG. 2. Comparison between computed masses of diquark correlations and their symmetry-related meson counterparts: diquarks – (black) stars and mesons – (green) bars.

Experimental **evidence** of **diquark scattering** from the HERMES data for SIDIS on nuclear targets

“Multidimensional study of hadronization in nuclei”

arXiv:1107.3496v3 [hep-ex] 13 Sep 2011

Eur. Phys. J. A47:113, 2011

Interpreting HERMES Nuclear DIS DATA: MESONS

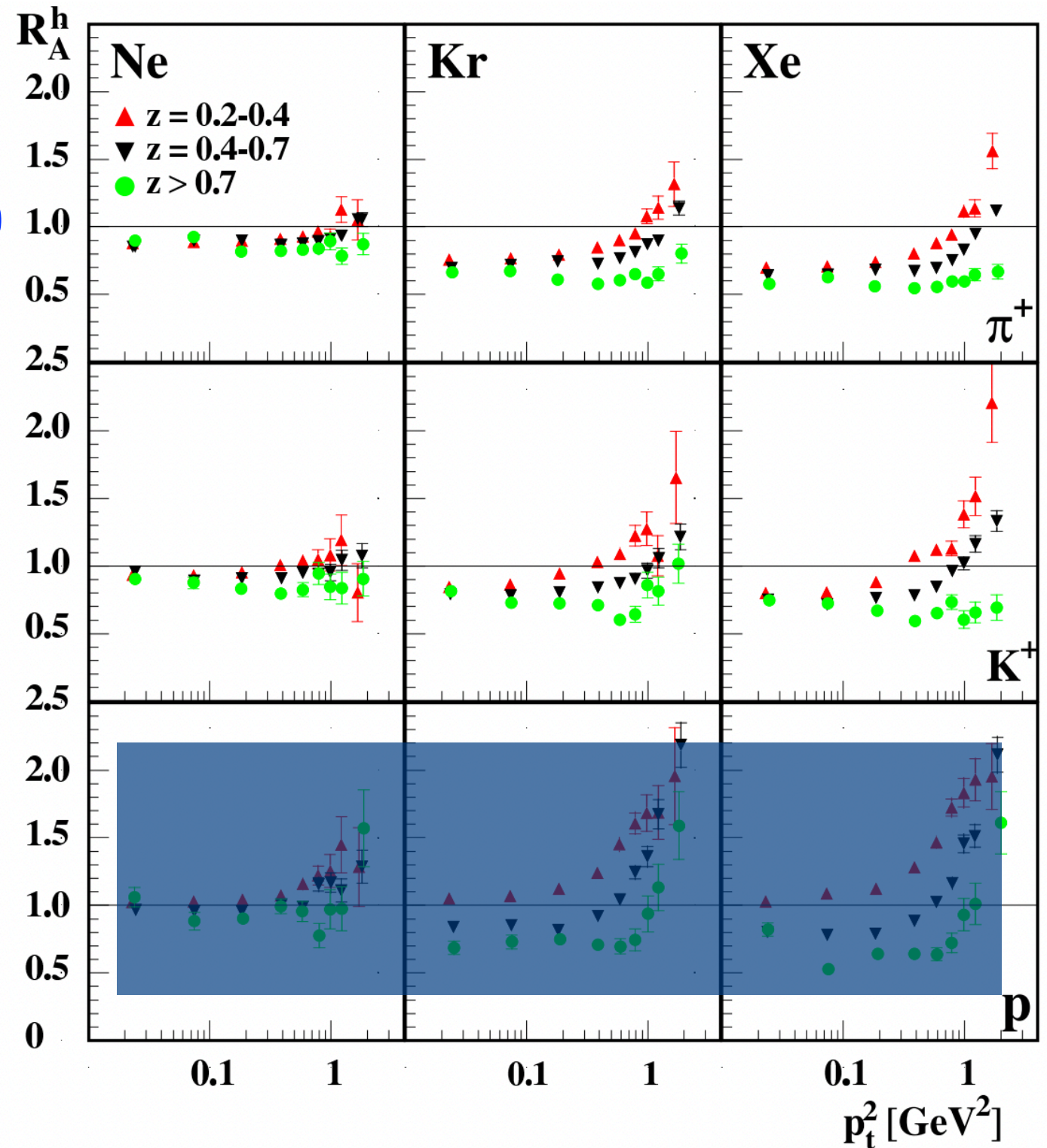
The multiplicity ratio measures effects of the nuclear medium.

“No nuclear effects” means $R=1.0$

$$R_A^h(\nu, Q^2, z, p_t^2) = \frac{\left(\frac{N^h(\nu, Q^2, z, p_t^2)}{N^e(\nu, Q^2)} \right)_A}{\left(\frac{N^h(\nu, Q^2, z, p_t^2)}{N^e(\nu, Q^2)} \right)_D}$$

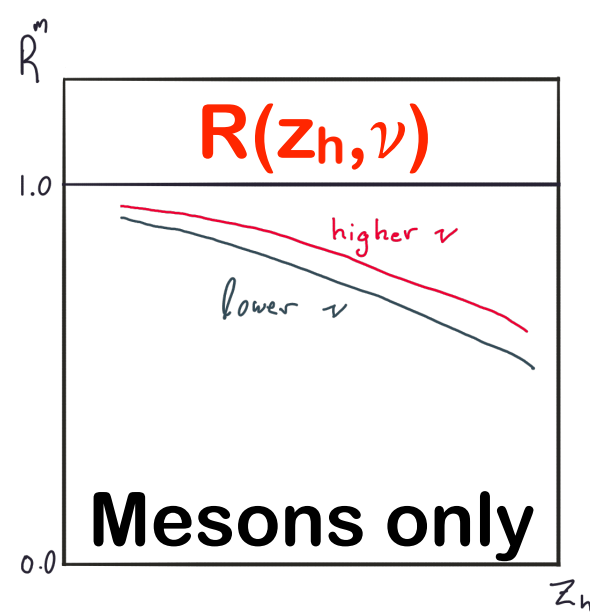
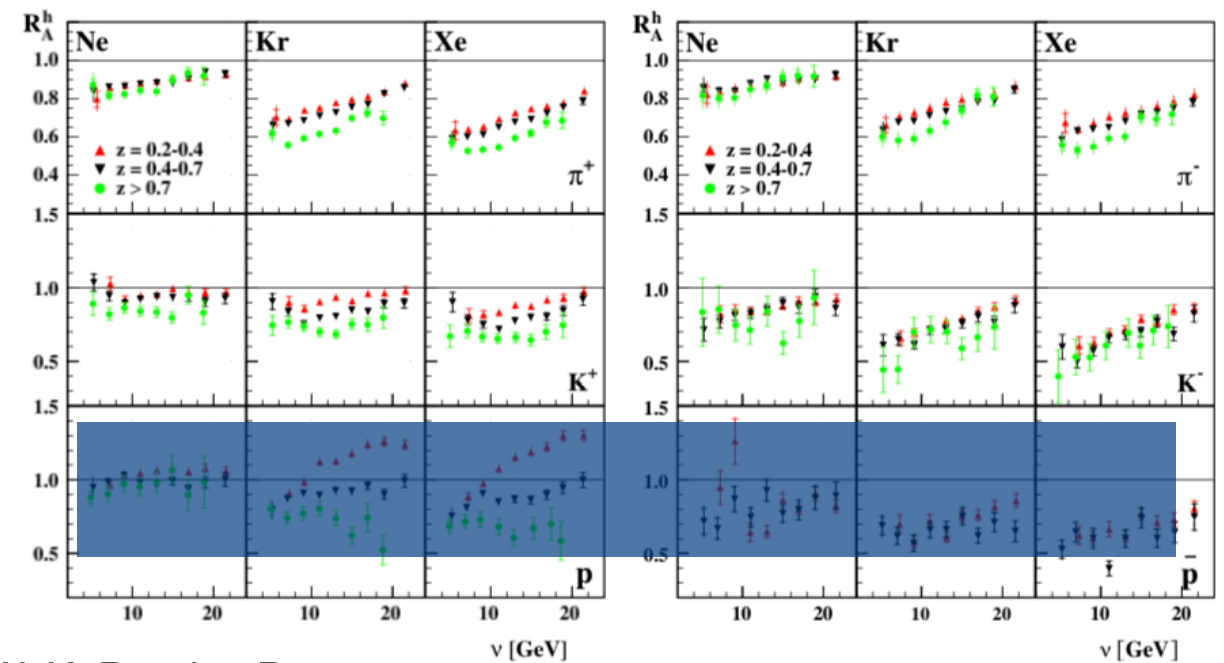
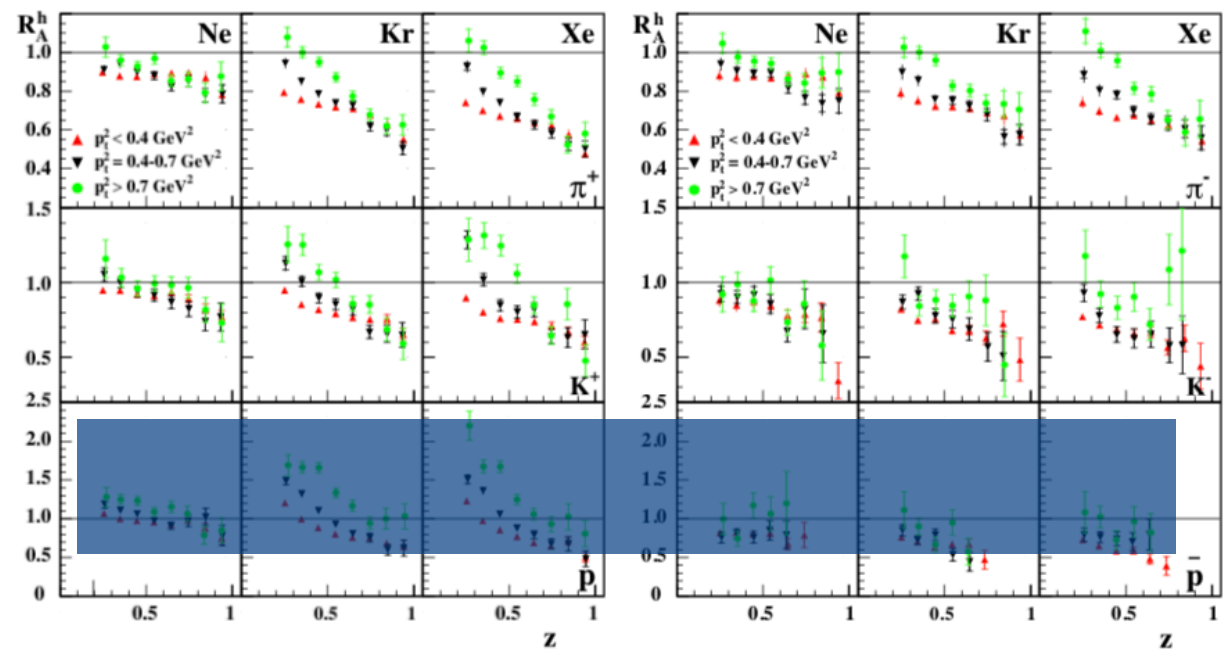
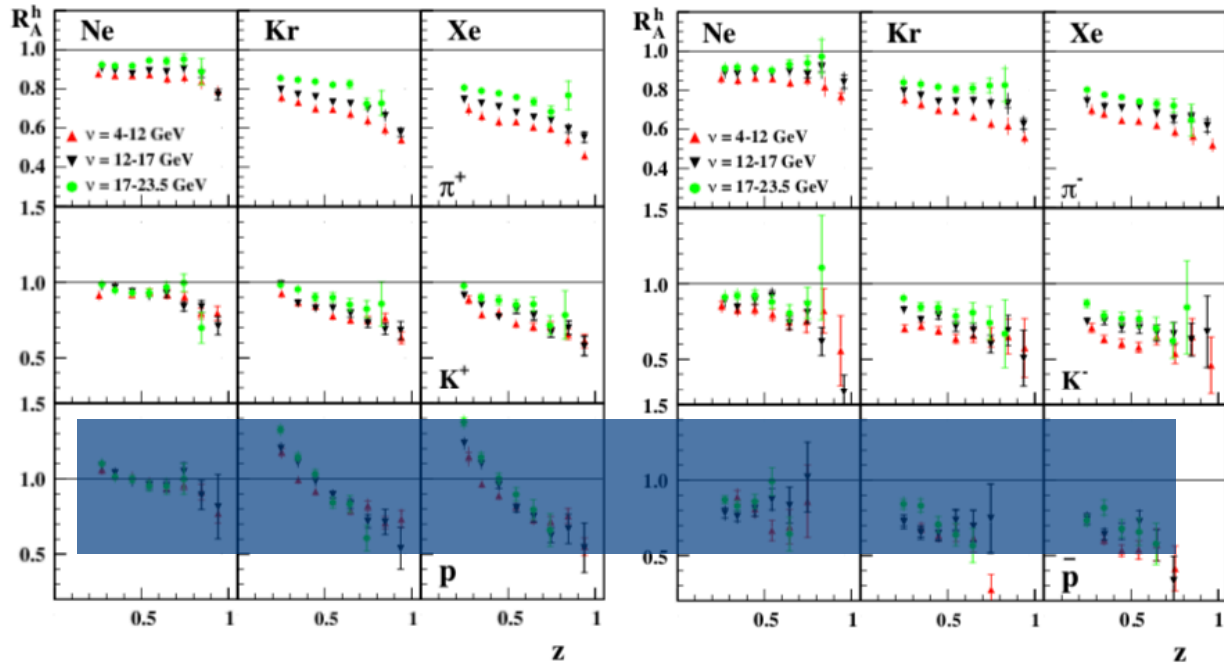
Most basic indicator is p_T dependence of multiplicity ratio.

$R > 1$ at high p_T because particles that interact with the medium acquire more p_T than those that don't interact as much.

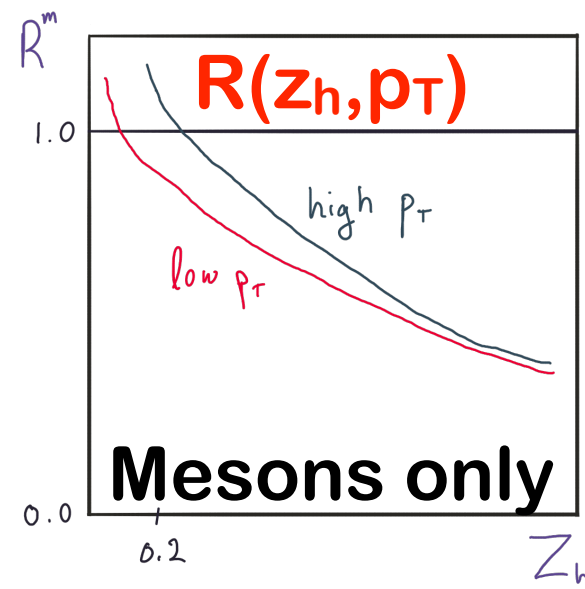


“Interact” = hadronic interaction + partonic multiple scattering

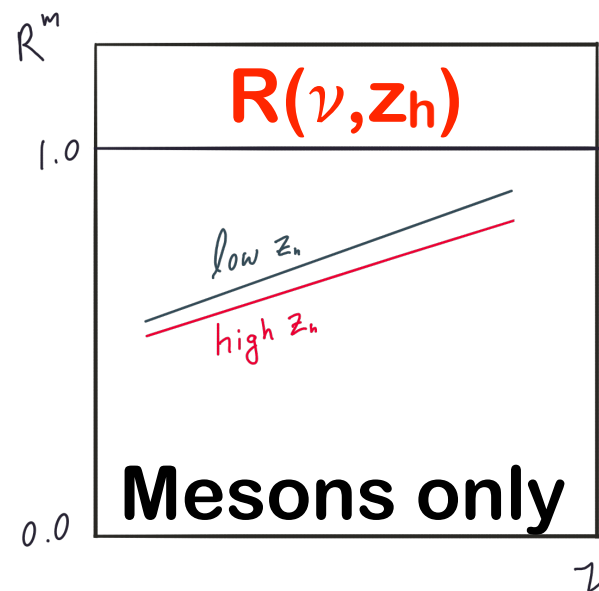
Empirically, from these plots, low- z mesons acquire more p_T than high- z .



Integrated over p_T ,
so always < 1 .
At higher ν , less
attenuation because
of time dilation of
color lifetime.



Not integrated over
 p_T , so can exceed 1.
Exceeds 1 faster for
higher p_T , so
crossing point is p_T
dependent.



Time dilation is
proportional to ν .
Slow approach to 1.0
at infinite ν . Color
lifetime goes to zero
at high z , so high z is
attenuated more.

So far, we have a reasonable **qualitative** interpretation for **mesons** that explains multi-dimensional behavior.

Let's see if we can understand HERMES **baryon** data!

Interpreting HERMES Nuclear DIS DATA: MESONS

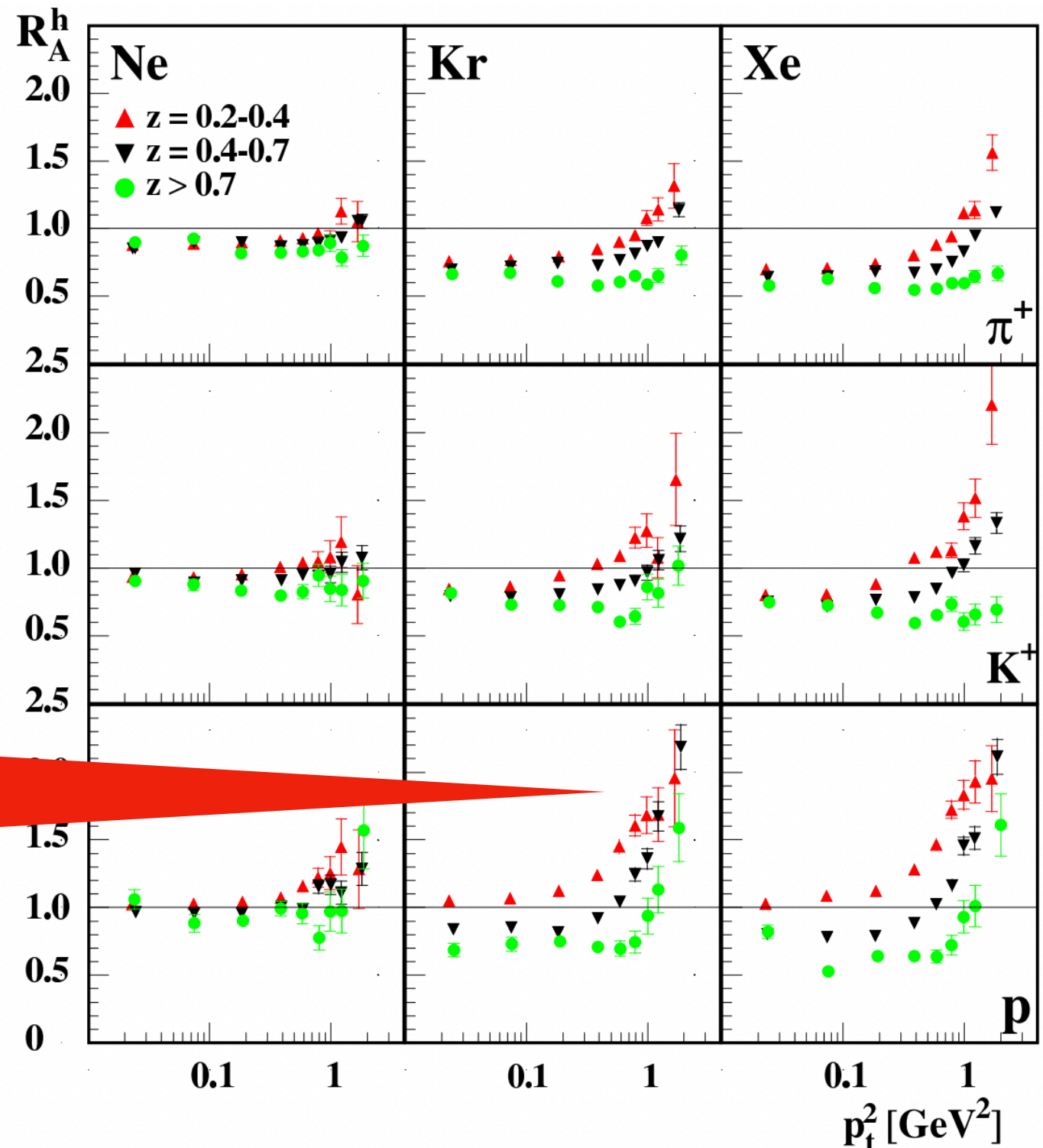
The multiplicity ratio measures effects of the nuclear medium.

“No effects” means $R=1.0$

$$R_A^h(\nu, Q^2, z, p_t^2) = \frac{\left(\frac{N^h(\nu, Q^2, z, p_t^2)}{N^e(\nu, Q^2)} \right)_A}{\left(N^h(\nu, Q^2, z, p_t^2) \right)}$$

The ordering in z seen for mesons *disappears* at high p_T for protons.

A strong interaction occurs at all values of z at high p_T .

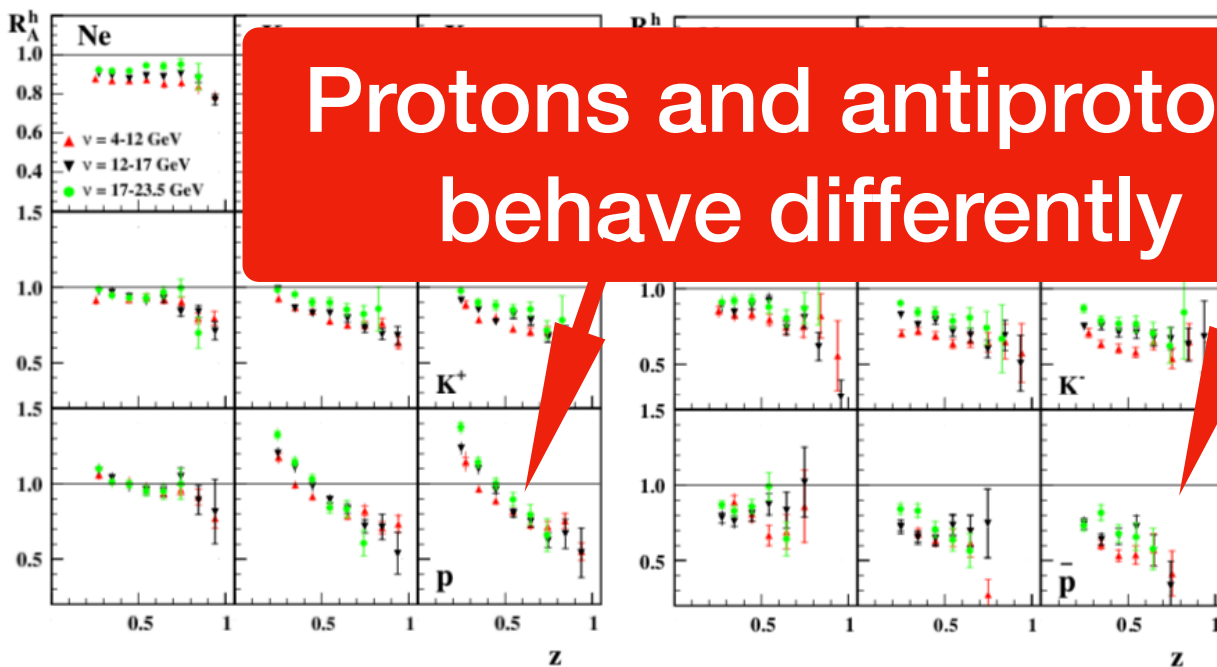


Interact — hadronic interaction of forming hadrons, + quark energy loss.

Empirically, from these plots, low- z mesons acquire more p_T than high- z .

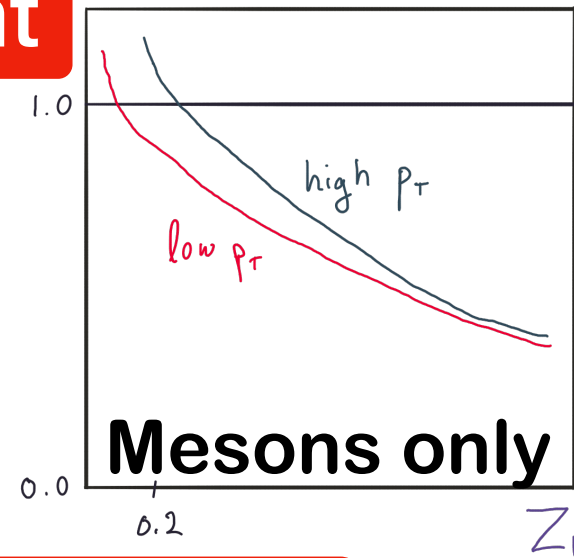
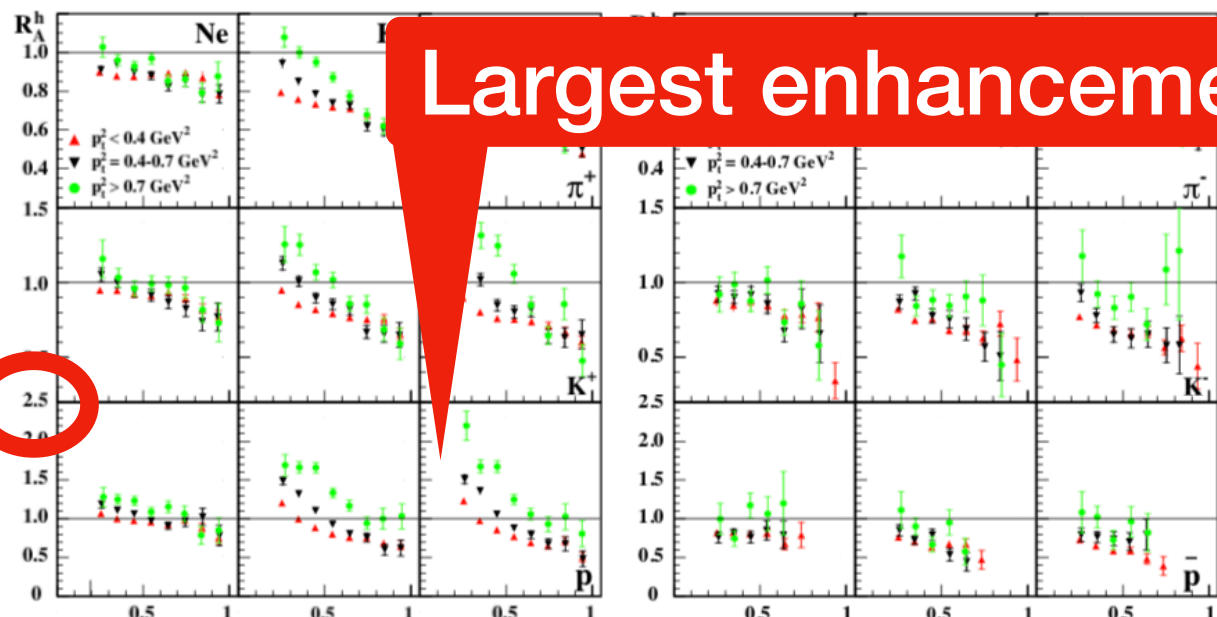
Enhancement at high p_T mostly caused by hadronic interactions at low z .

Protons and antiprotons
behave differently



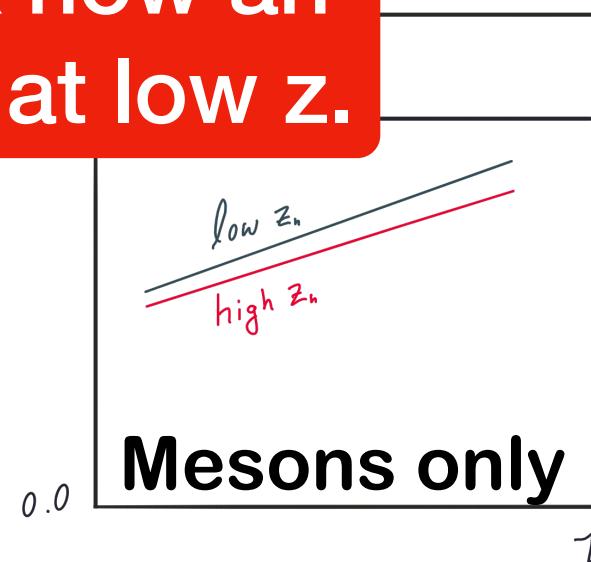
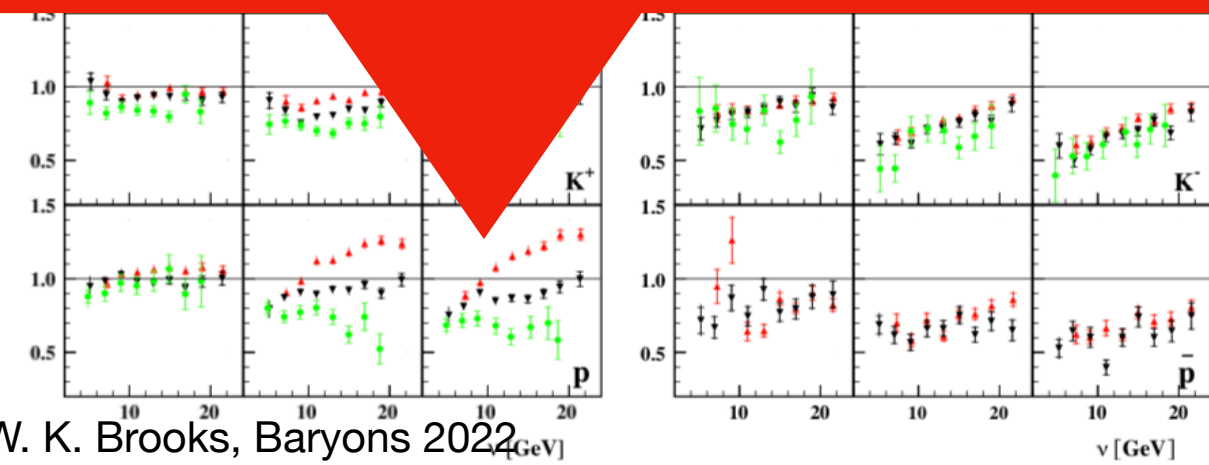
Integrated over p_T ,
so always < 1 .
At higher ν , less
attenuation because
of time dilation of
color lifetime

Largest enhancement



Not integrated over
 p_T , so can exceed 1.
Exceeds 1 faster for
higher p_T , so
crossing point is p_T
dependent.

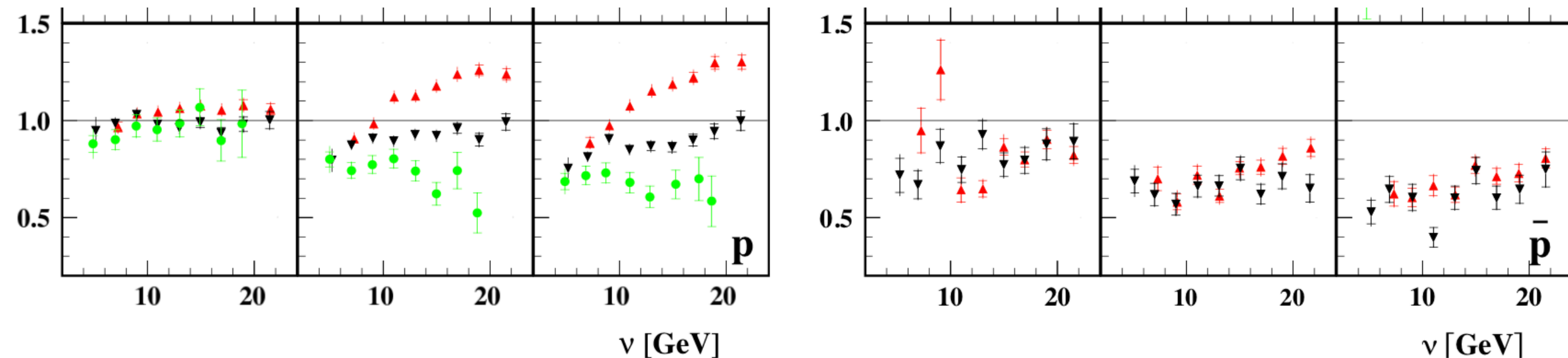
Time dilation of a single quark now an
infeasible interpretation: $R \gg 1$ at low z .



Time dilation is
proportional to ν .
Slow approach to 1.0
at infinite ν . Color
lifetime goes to zero
at high z , so high z is
attenuated more.

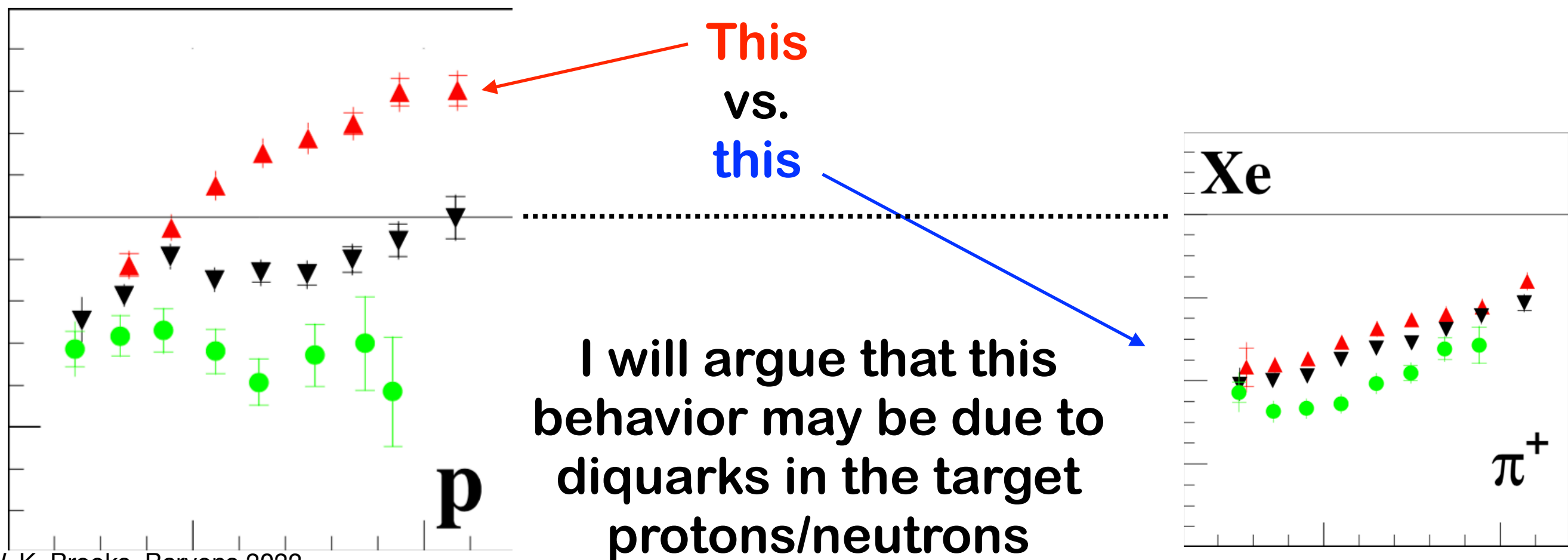
HERMES Proton Multiplicity Ratios

▲ $z = 0.2-0.4$
 ▼ $z = 0.4-0.7$
 ● $z > 0.7$



proton (left) and antiproton (right) are totally different

Proton multiplicity ratios qualitatively different from mesons.



CLAS6 nuclear DIS data for Lambda Baryons

$A(e, e' \Lambda)X$ in DIS Kinematics, with $A = D, C, Fe, Pb$

“First Measurement of Λ Electroproduction off Nuclei in the Current and Target Fragmentation Regions”

T. Chetry, L. El Fassi, W.K. Brooks, R. Dupré, A. El Alaoui, K. Hafidi et al. (CLAS Collaboration)

<https://doi.org/10.48550/arXiv.2210.13691>

Analysis Team from Mississippi State University:

Prof. Lamiaa El Fassi

Dr. Taya Chetry

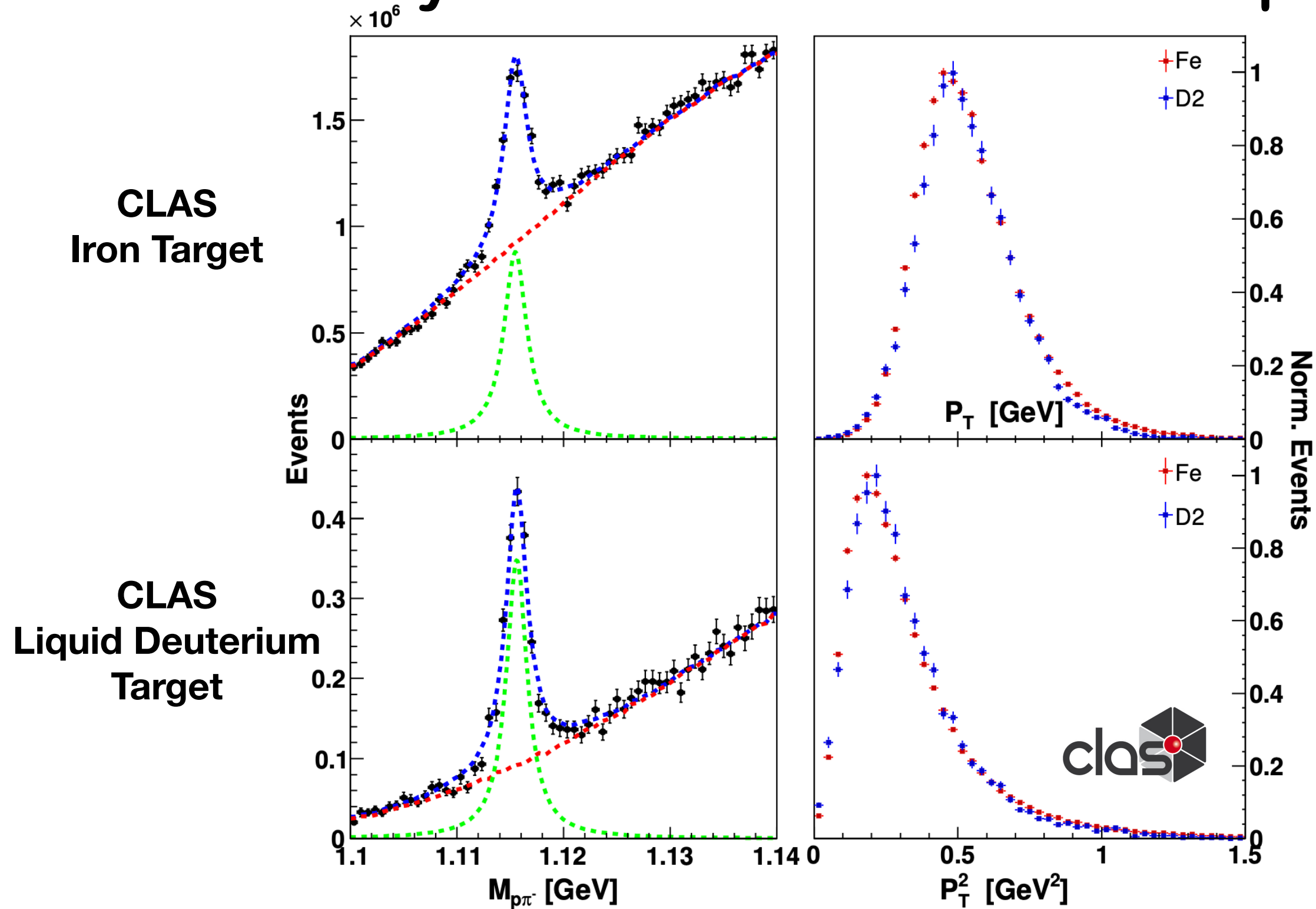
Dr. Latif-ul Kabir

Analysis Contributions from U. Técnica Fed. Santa María:

Dr. Ahmed El Alaoui

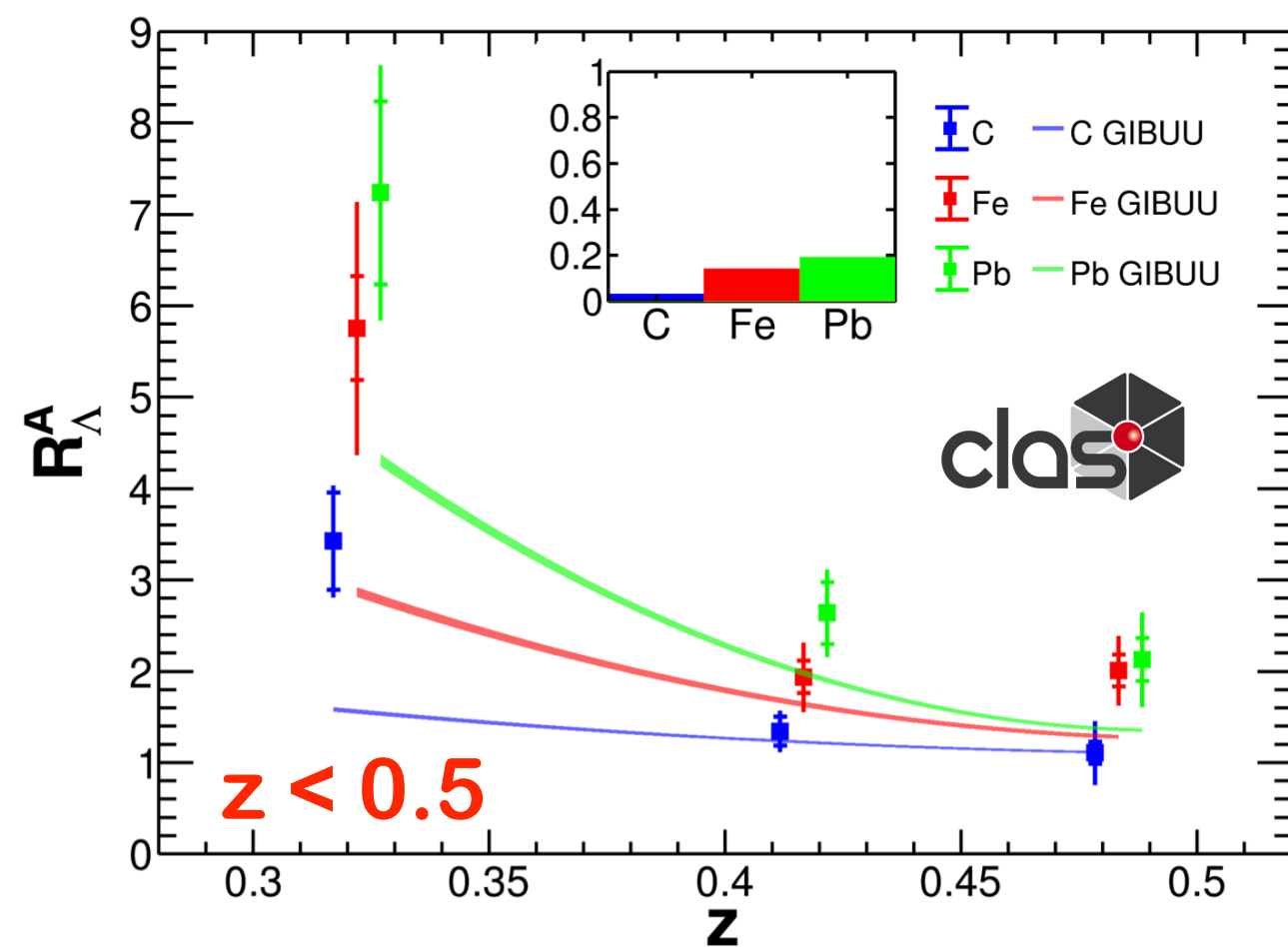
Initial work performed at ANL.

Lambda Baryons are well-identified in π -p channel

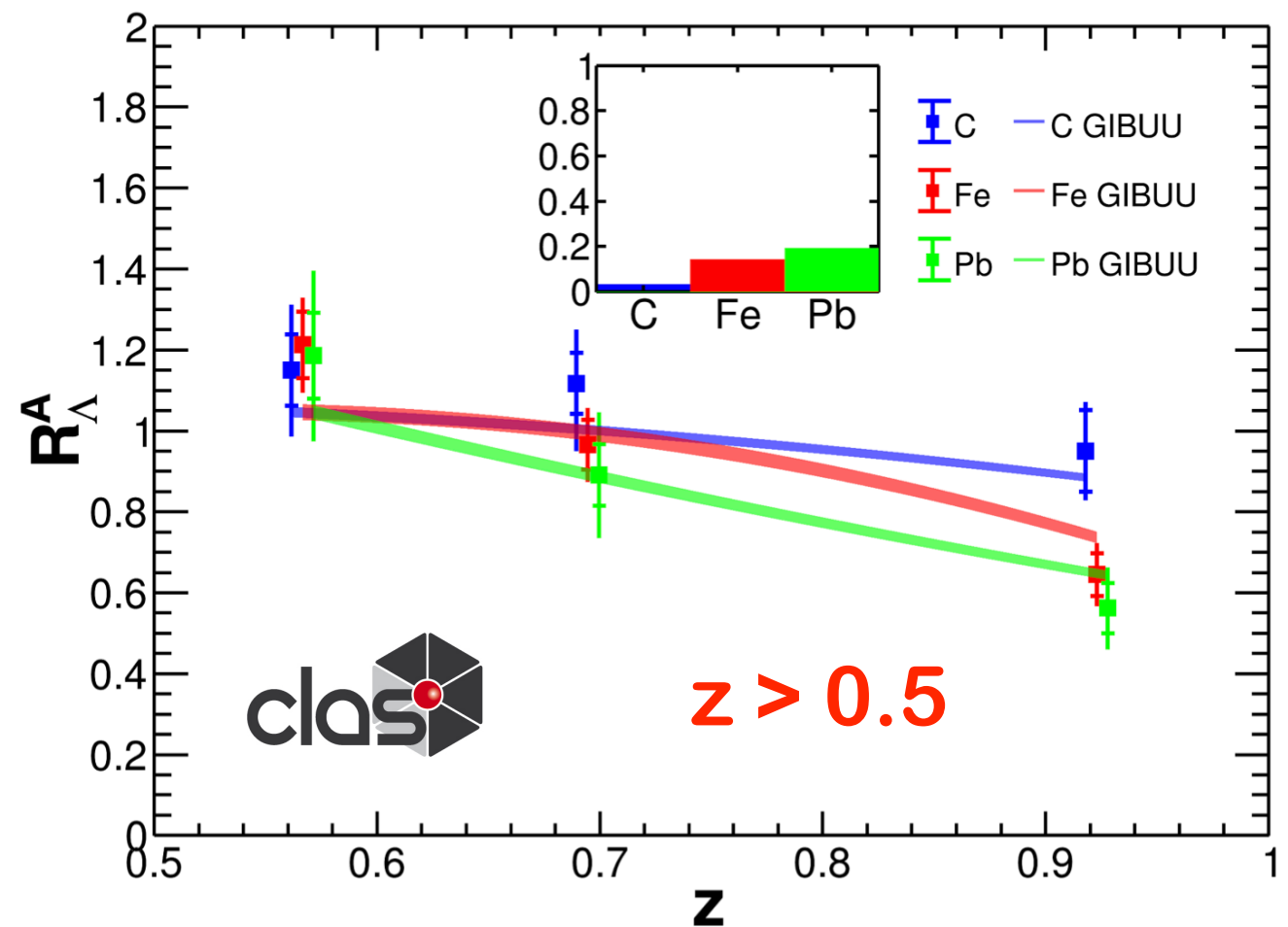


Backgrounds are under control - three different extraction methods agree.
 p_T broadening is easily visible by eye.

<https://doi.org/10.48550/arXiv.2210.13691>

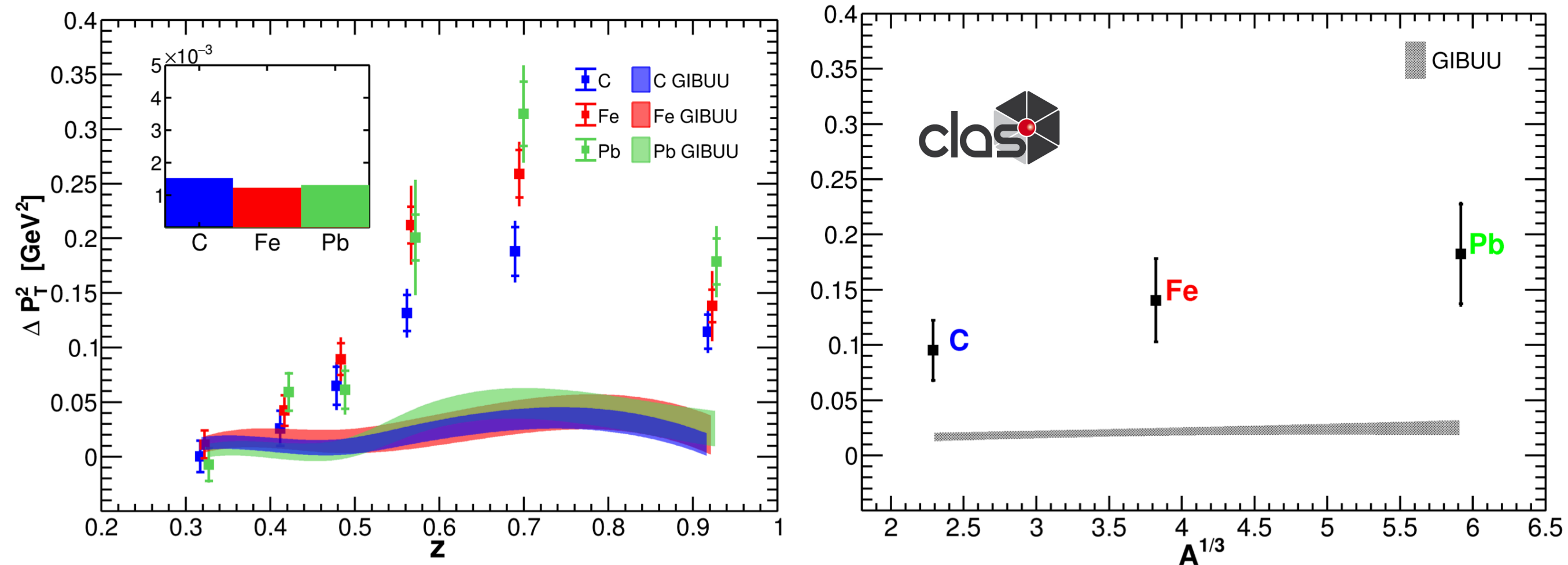


“Pile-up” of events at low z -
huge compared to pion
 production: 7.5 vs. ~ 1.0
 Underpredicted by GiBUU.



At higher z , there is
 relatively little attenuation.
 Agrees with GiBUU
 prediction for high z .

Lambda Transverse Momentum Broadening



Maximum is 0.3 GeV²

Compare to maximum for pions of 0.03 GeV²!

The **object passing through the medium is disruptive!**

E.g., it is “large” (has an extended color field).

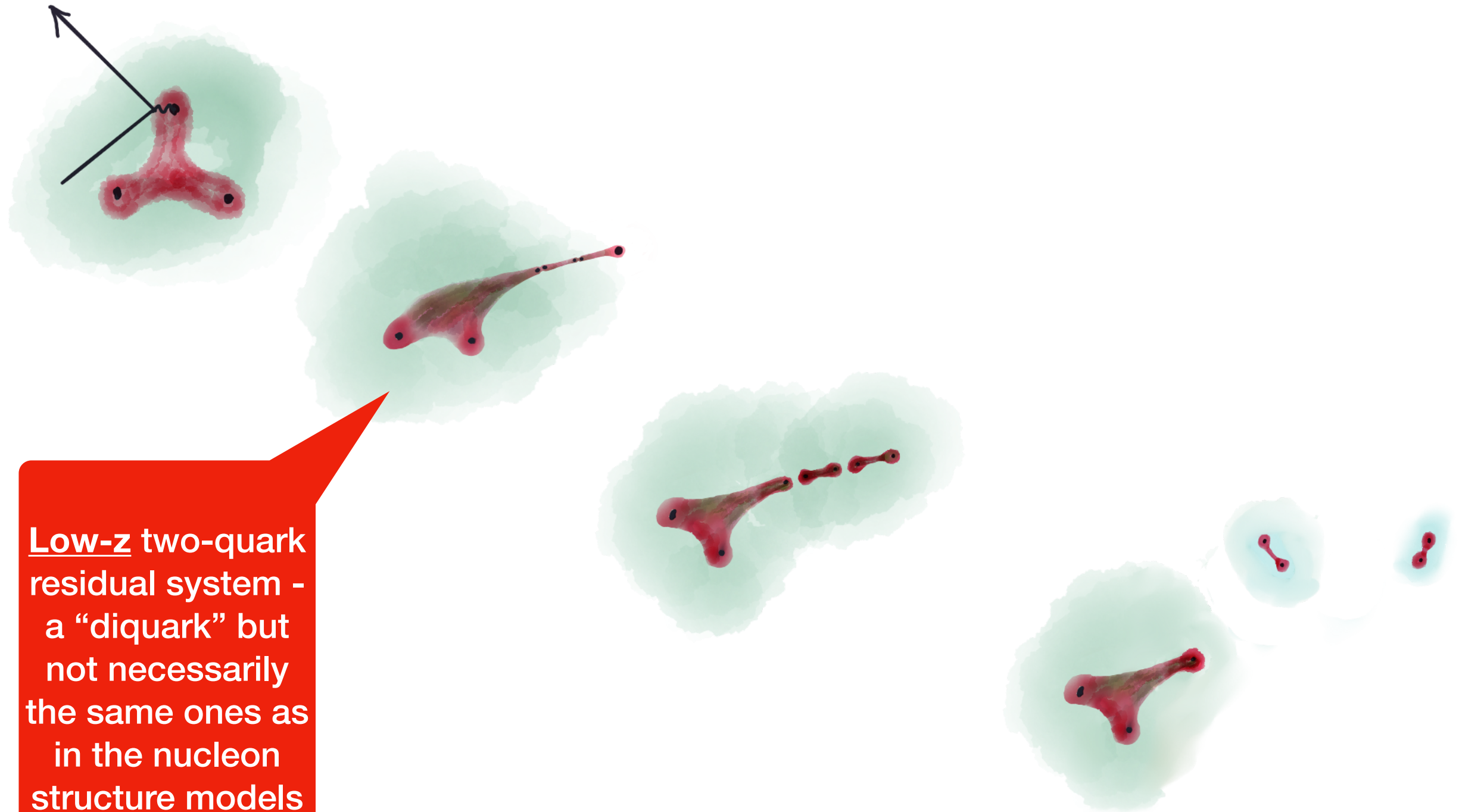
Unlike for pions, GiBUU cannot predict this observable.

We apparently do not have the correct physical picture in the case of baryon hadronization.

Could it be possible that the **virtual photon is sometimes absorbed by a diquark?**

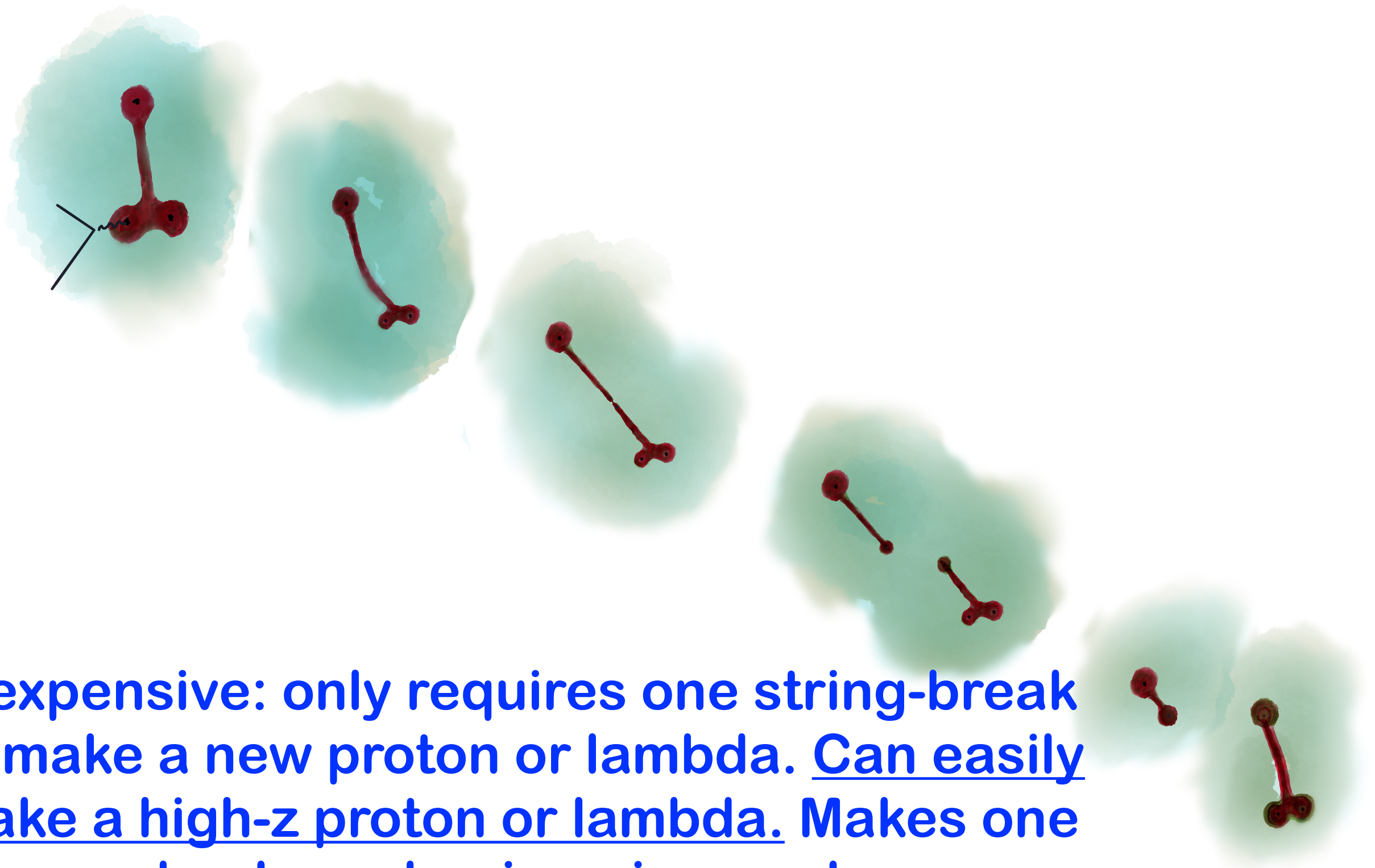
Let's call this Direct Diquark Scattering (**DDS**)

Traditional picture of particle production from proton with string fragmentation: Single Quark Scattering



Low-z two-quark residual system - a “diquark” but not necessarily the same ones as in the nucleon structure models

Alternative picture of particle production from proton: Direct Diquark Scattering



**Inexpensive: only requires one string-break
to make a new proton or lambda. Can easily
make a high-z proton or lambda. Makes one
or more backward-going pions or kaons.**

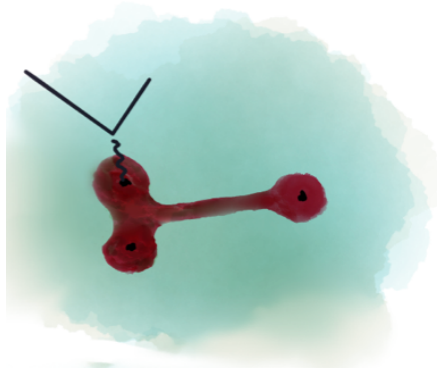
DDS mechanism makes it much easier to form a proton or a lambda baryon.

Especially true for these low energies.

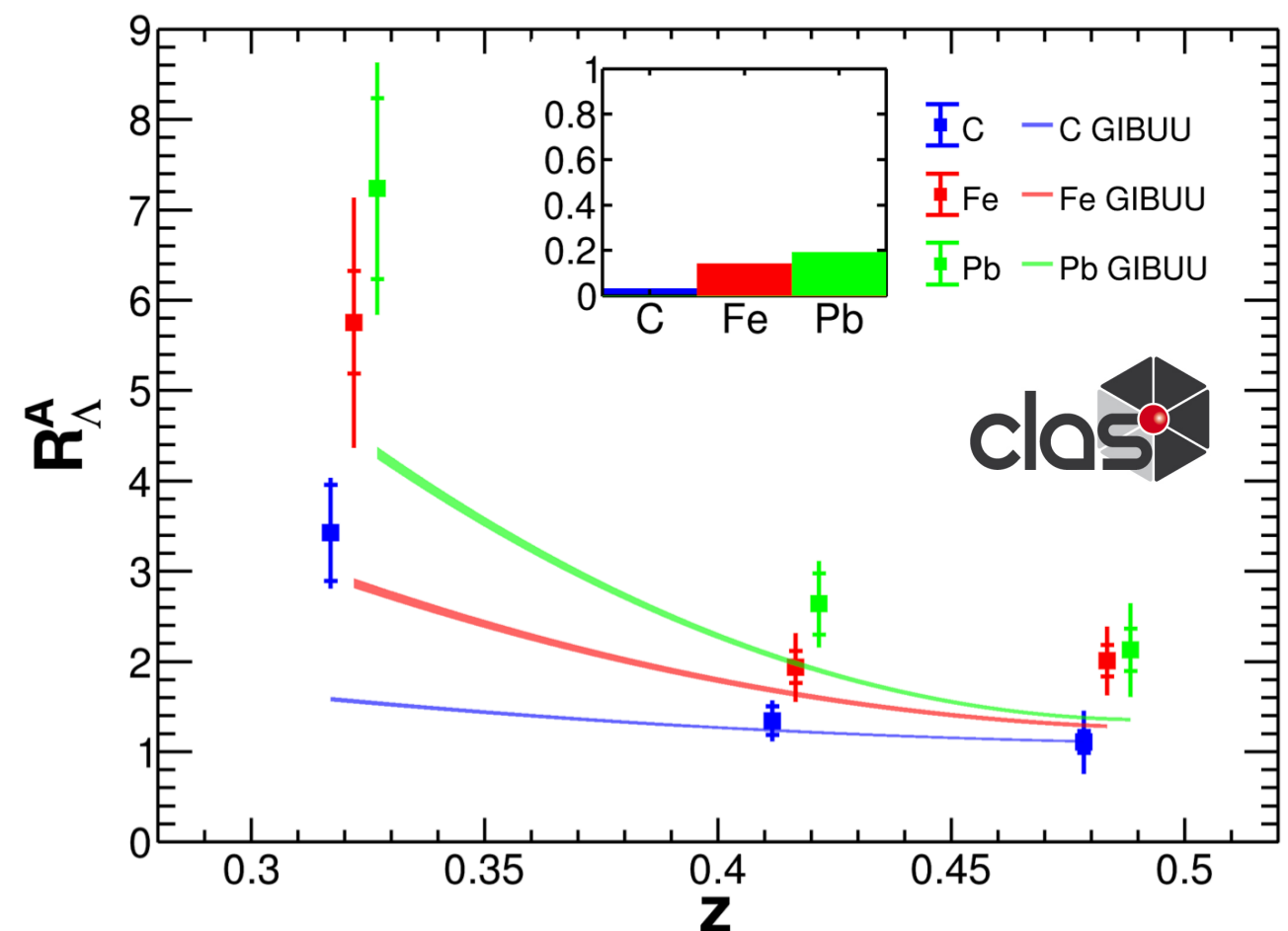
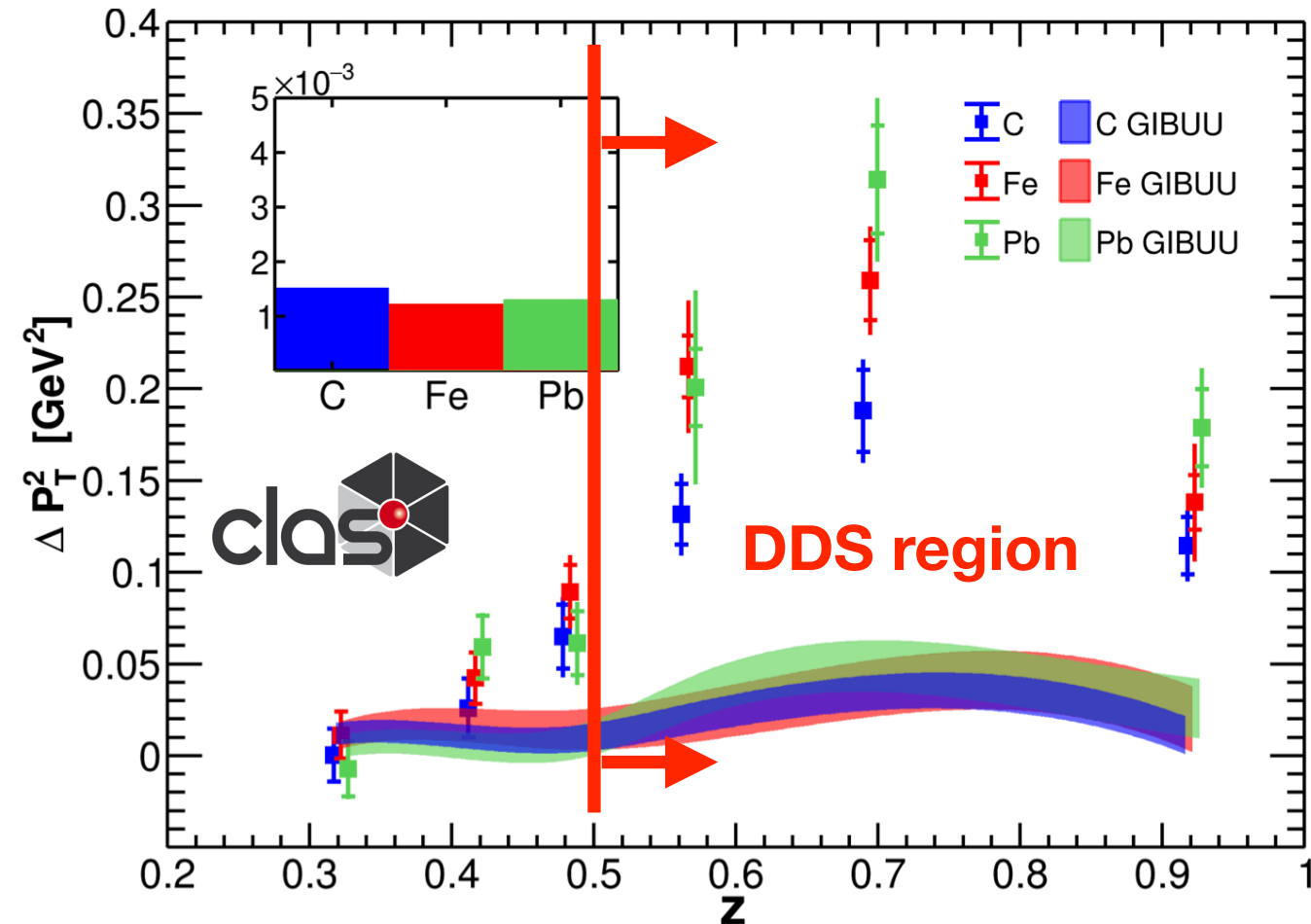
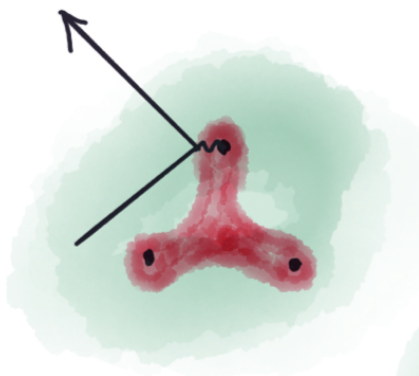
With nuclear DIS baryon production, we will be able to gather substantial evidence to test this idea.

Multiplicity ratio, p_T broadening, and correlations between hadrons will provide the evidence.

If DDS occurs, it will appear for $z > 0.5$, where the observed hadron is very likely to contain the struck object (quark or diquark).



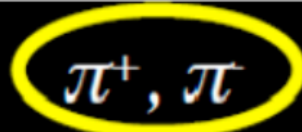







Low- z production of lambdas will naturally occur via the traditional mechanism of single-quark scattering.



Future tests of the Direct Diquark Scattering hypothesis with CLAS12 nuclear DIS on nine baryons

 **Actively underway with existing 5 GeV data**

<i>meson</i>	$c\tau$	mass	flavor content	<i>baryon</i>	$c\tau$	mass	flavor content
 π^0	25 nm	0.13	$u\bar{u}d\bar{d}$	 p	stable	0.94	ud
 π^+, π^-	7.8 m	0.14	$u\bar{d}, d\bar{u}$	\bar{p}	stable	0.94	$\bar{u}\bar{d}$
 η	170 pm	0.55	$u\bar{u}d\bar{d}s\bar{s}$	 Λ	79 mm	1.1	uds
 ω	23 fm	0.78	$u\bar{u}d\bar{d}s\bar{s}$	$\Lambda(1520)$	13 fm	1.5	uds
η'	0.98 pm	0.96	$u\bar{u}d\bar{d}s\bar{s}$	Σ^+	24 mm	1.2	us
ϕ	44 fm	1.0	$u\bar{u}d\bar{d}s\bar{s}$	 Σ^-	44 mm	1.2	ds
f_1	8 fm	1.3	$u\bar{u}d\bar{d}s\bar{s}$	Σ^0	22 pm	1.2	uds
 K^0	27 mm	0.50	$d\bar{s}$	Ξ^0	87 mm	1.3	us
K^+, K^-	3.7 m	0.49	$\bar{u}s, \bar{u}s$	Ξ^-	49 mm	1.3	ds

Masses of ground-state mesons and baryons, including those with heavy quarks

Pei-Lin Yin,^{1,*} Chen Chen,^{2,†} Gastão Krein,² Craig D. Roberts,^{3,‡} Jorge Segovia,⁴ and Shu-Sheng Xu¹

arXiv 1903.00160

Phys. Rev. D 100, 034008 (2019)

Baryon	$M^{e/l}$	M^{CI}	dom. corr.
p (B.5a)	0.94	0.94	$[ud]u$ ●
Λ (B.5b)	1.12	1.06	$[ud]s$ ●
Σ (B.5c)	1.19	1.20	$[us]u$
Ξ (B.5d)	1.32	1.24	$[us]s$
Λ_c (B.5e)	2.29	2.50	$[uc]d - [dc]u$
Σ_c (B.5f)	2.45	2.53	$\{uu\}c$? almost
Ξ_c (B.5g)	2.47	2.66	$[uc]s - [sc]u$
Ξ'_c (B.5h)	2.58	2.68	$\{us\}c$
Ω_c (B.5i)	2.70	2.83	$\{ss\}c$

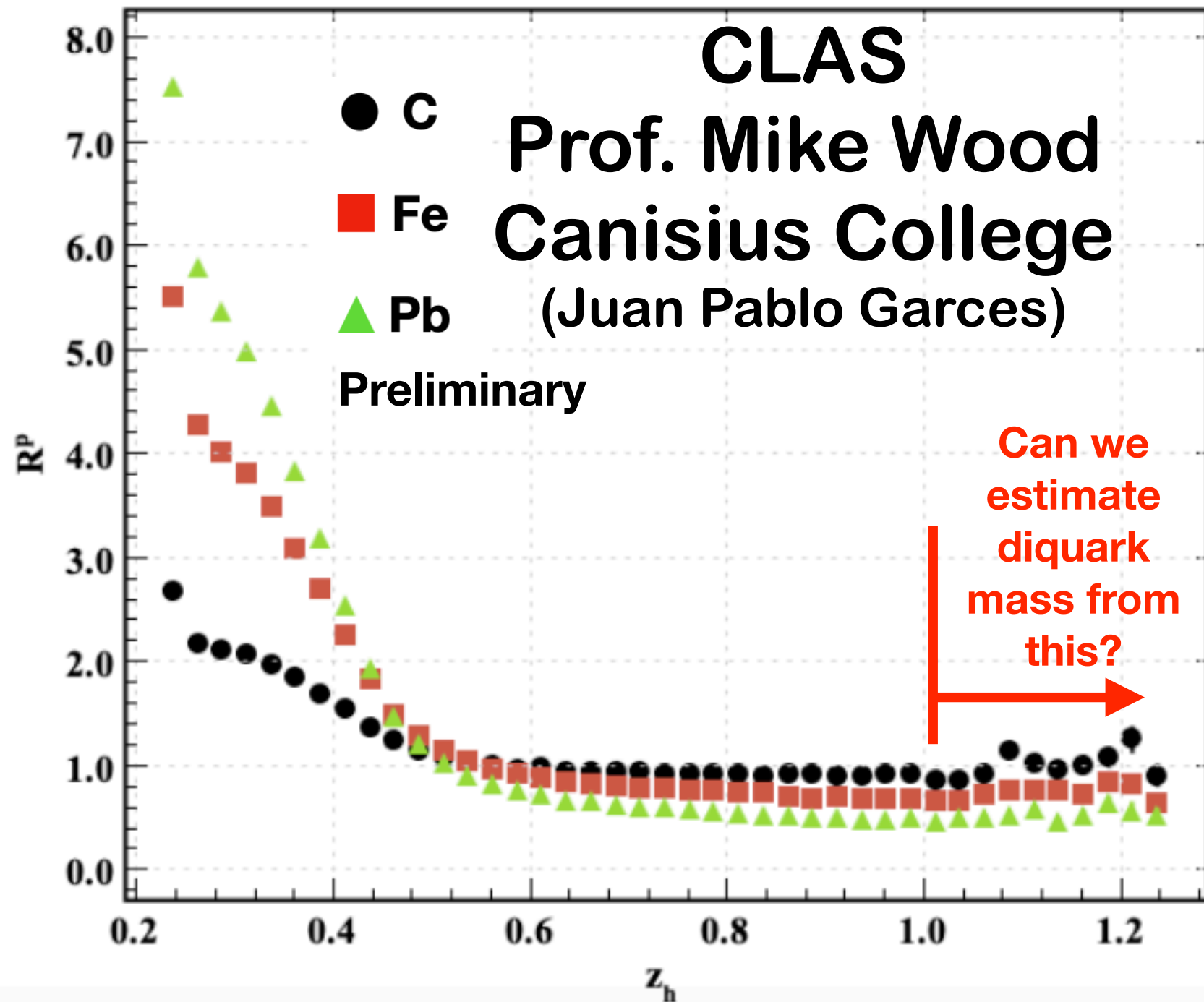
**This suggests
a specific behavior
for DDS.**

**Only p, n, lambda
can easily be formed
by DDS.**

**Prediction: proton
(neutron) and lambda
will behave similarly;
the others will be
different.**

**We can test this prediction already, with our new
preliminary data on the proton!**

Proton multiplicity ratio

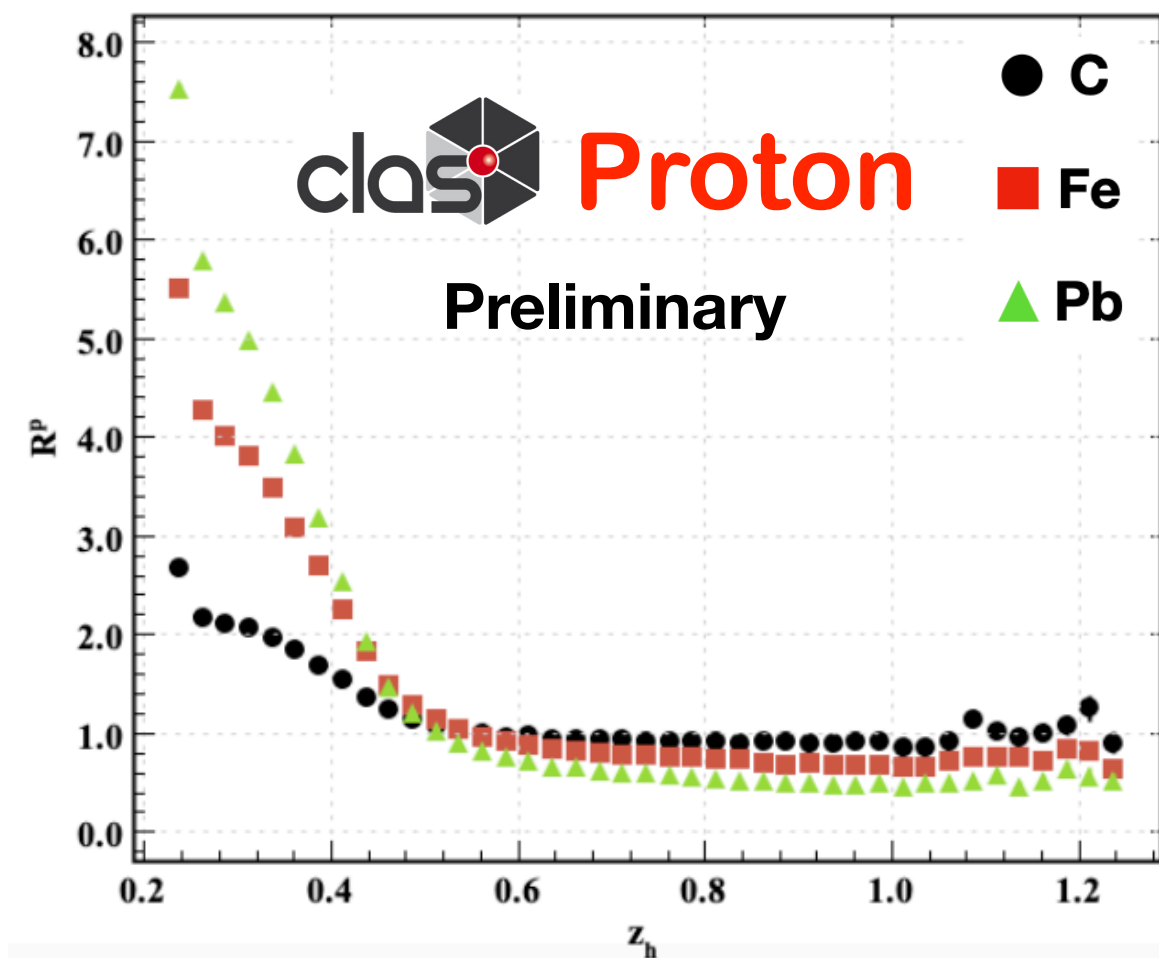
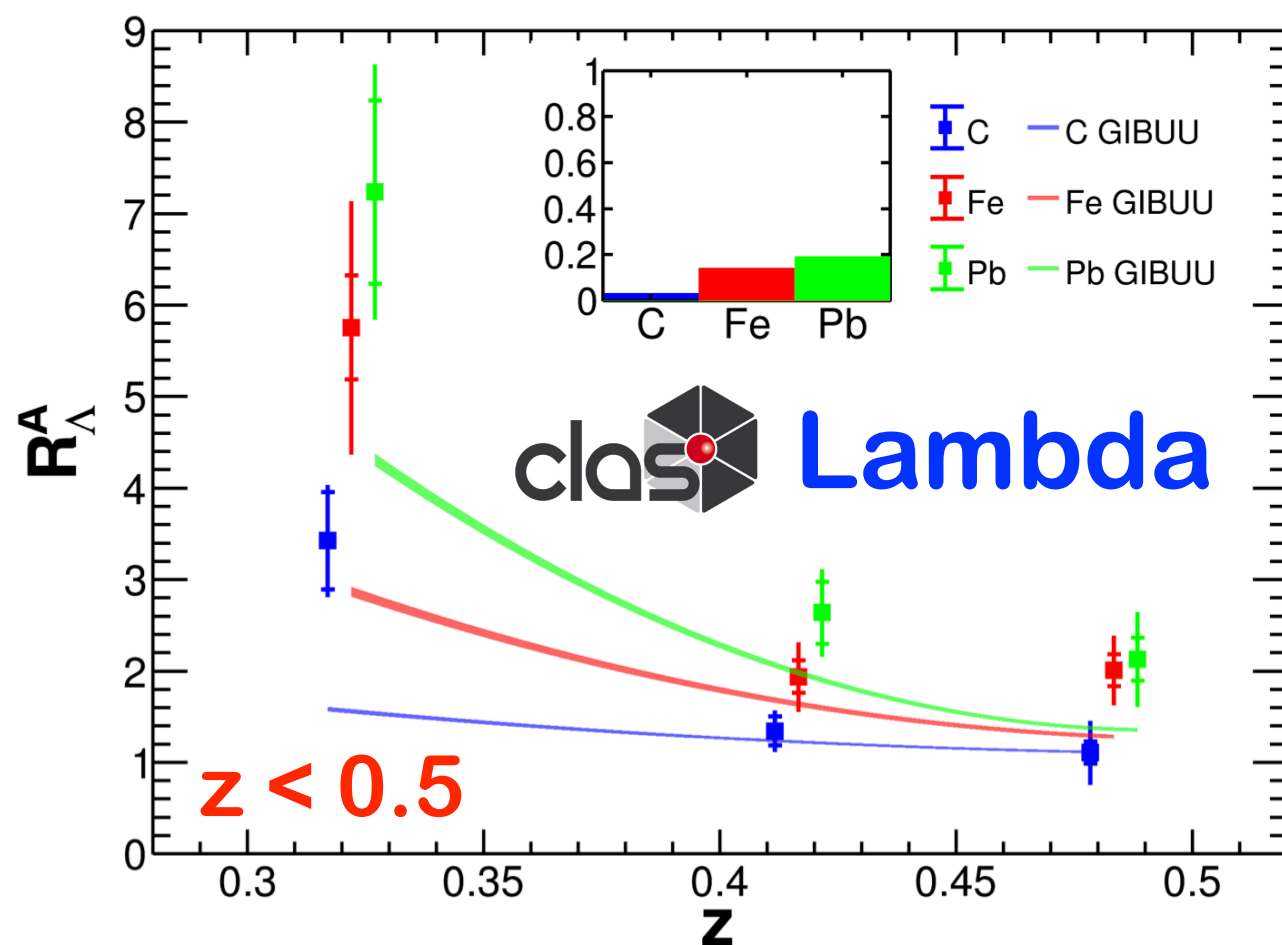


Maximum value 7.5

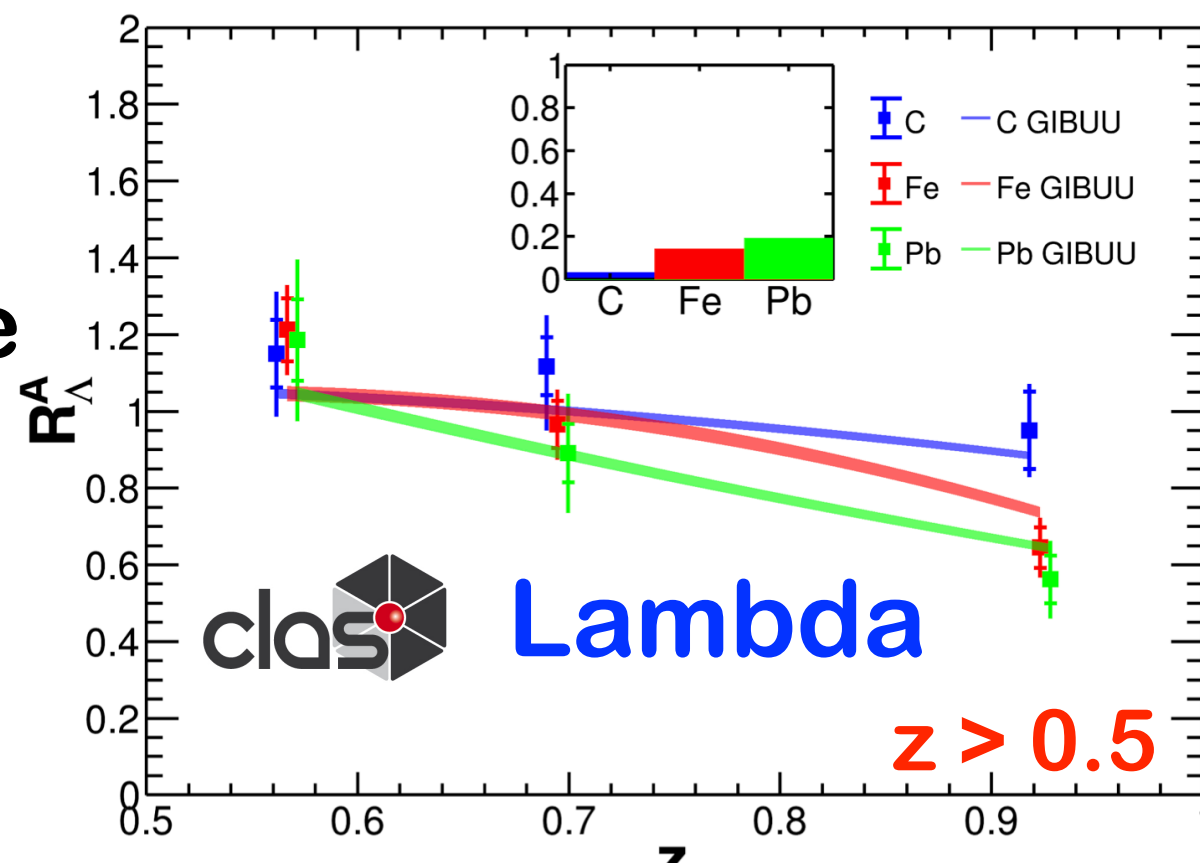
The **same number** as for the lambda!

Unlike the lambda, we have **tiny statistical uncertainties**

So we can probe the **multidimensional behavior**



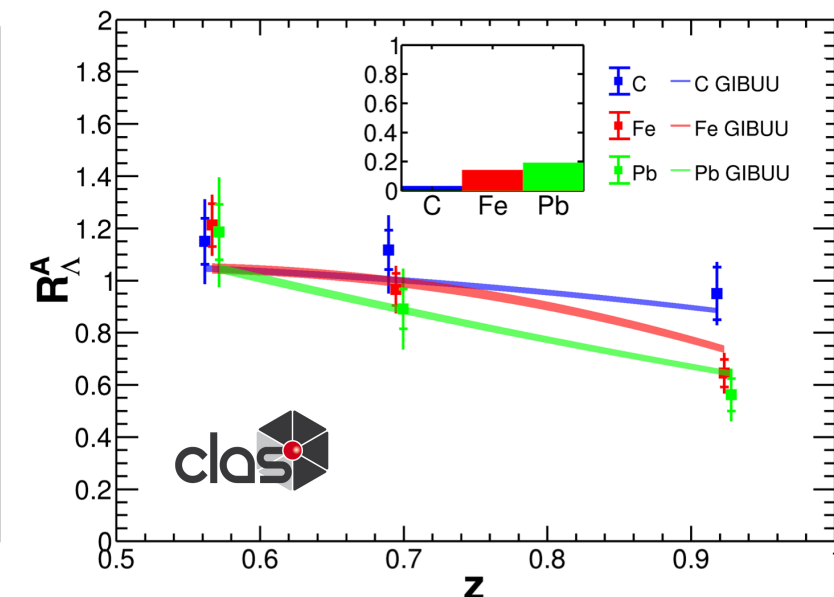
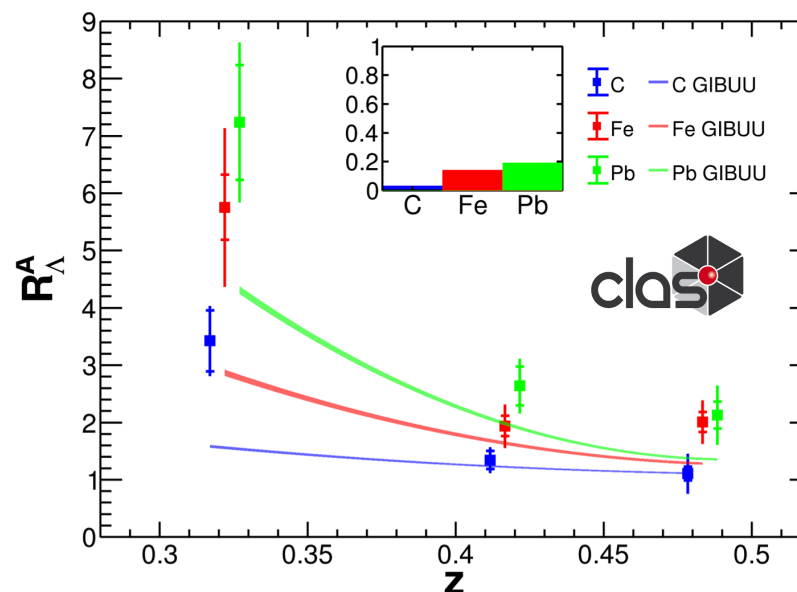
The multiplicity ratio for the **lambda** and the **proton** have the same magnitude and the same pattern of ordering.



Next Steps

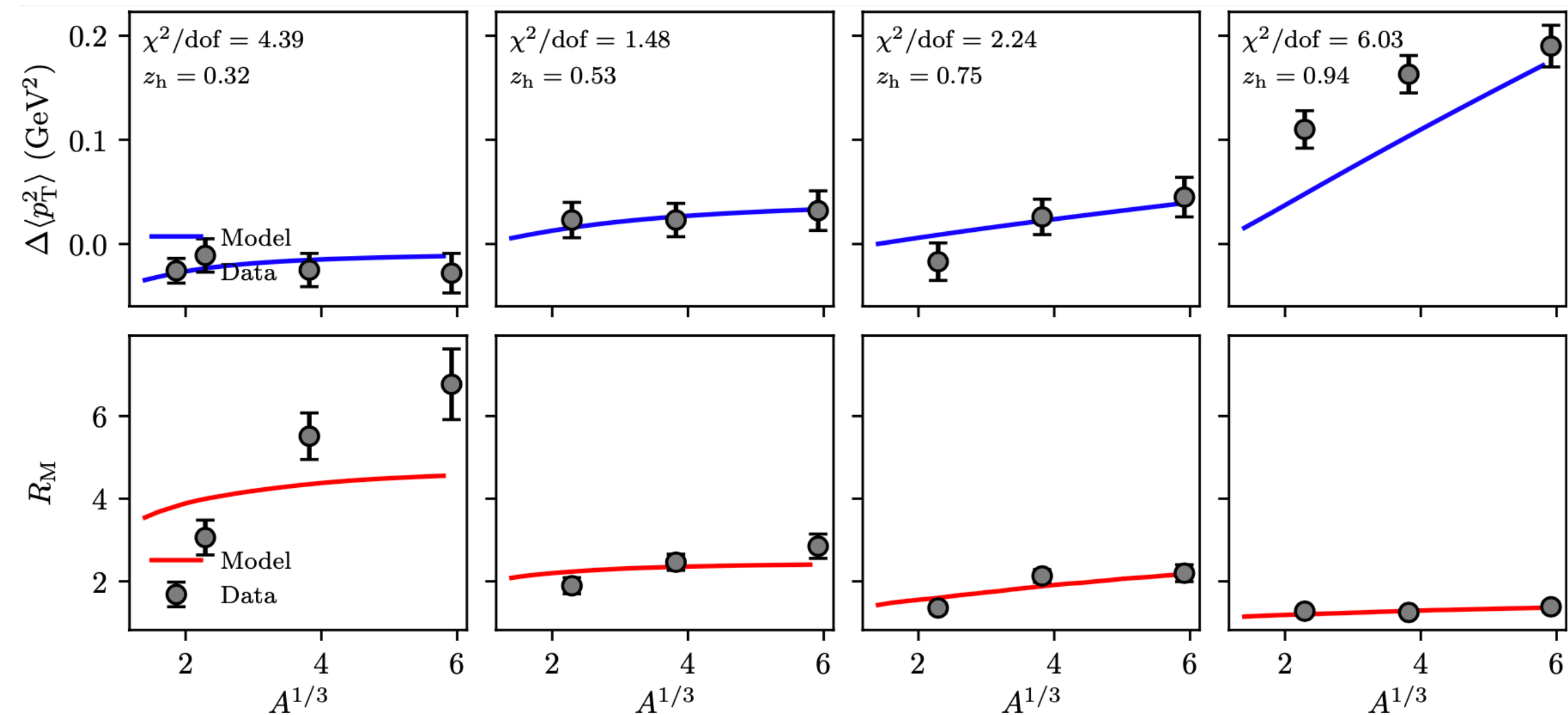
- Build a semi-classical space-time **model** for baryon hadronization like our meson model
- Make a two-observable **fit**, as with the mesons
- **New ingredients:**
 1. Two independent mechanisms are needed because the enhancement at low z is **far too big** to explain by the attenuation at high z
 2. A diquark-medium effective **cross section** σ_{qqA} and **transport coefficient** \hat{q}_{qqA} will be needed

- Test the model on all baryons with two observables



One-mechanism model does not give good results

Discrepancy is biggest for the multiplicity ratio at low z and for p_T broadening at high z



Conclusions

- Baryon nDIS data from HERMES and CLAS behave **qualitatively differently** from mesons, in multiplicity ratios and in transverse momentum broadening.
- The hypothesis is that **Direct Diquark Scattering** may be one mechanism for formation of protons and lambdas, for $z > 0.5$. **Protons, neutrons and lambdas** should **behave the same** if this is actually a valid mechanism, based on advanced models of diquarks. **Two mechanisms** are needed.
- More **theoretical work** is needed to determine the feasibility and plausibility of this interpretation, and distinguish it from, e.g., **color recombination** hadronization
- The planned and approved CLAS12 **Color Propagation** program is ideal for testing these ideas: access to production of **nine long-lived baryons**.

Acknowledgments

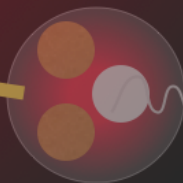
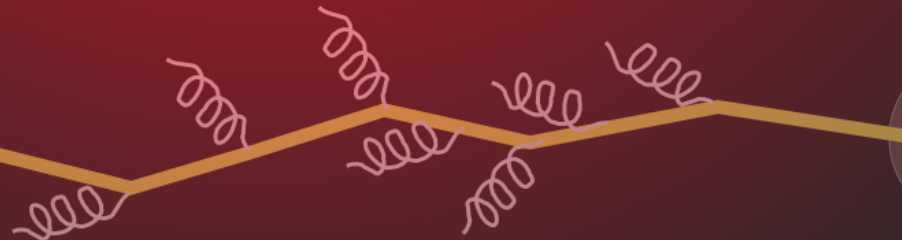
This work was funded in part by:

[ANID PIA/APOYO AFB180002 \(Chile\)](#) - Center for Science and Technology of Valparaíso (CCTVal).

[ANID - Millennium Science Initiative Program - ICN2019 044 \(Chile\)](#) - Millennium Institute for SubAtomic Physics at the High energy frontier (SAPHIR).

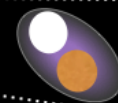
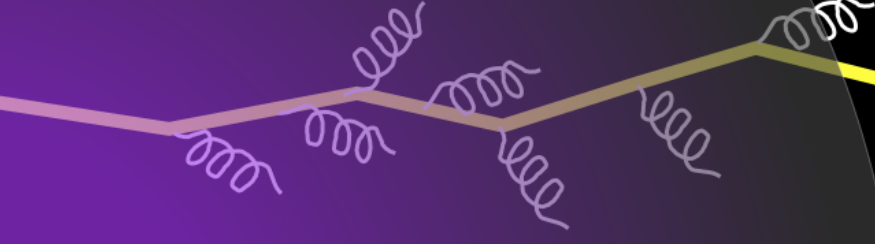
[Universidad Técnica Federico Santa María \(Technical University of Federico Santa Maria\)](#), Valparaíso, Chile.

Backup slides



A space-time model for propagation of **QCD color** through **strongly interacting systems**

Will Brooks and Jorge López
(UTFSM) (Heidelberg)





Estimating the color lifetime of energetic quarks

William K. Brooks^{a,b,c,*}, Jorge A. López^{b,d}

^a Departamento de Física, Universidad Técnica Federico Santa María, Valparaíso, Chile

^b Centro Científico Tecnológico de Valparaíso, Valparaíso, Chile

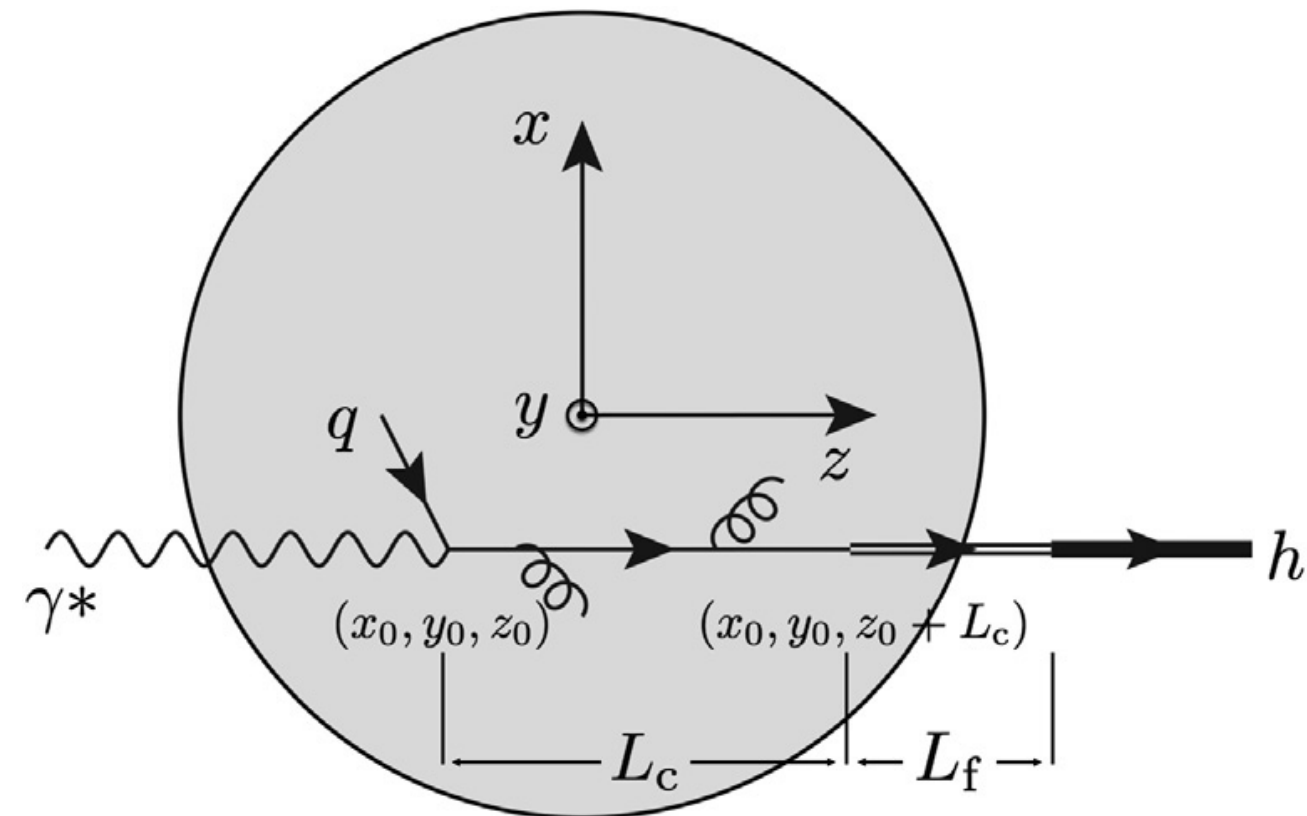
^c Department of Physics and Astronomy, University of New Hampshire, Durham NH, USA

^d Physikalisches Institut, Universität Heidelberg, Heidelberg, Germany



Struck quark moves a distance L_c as a **colored** object, then becomes a **hadron**. If the hadron forms **inside** the medium, it can interact with hadronic cross section.

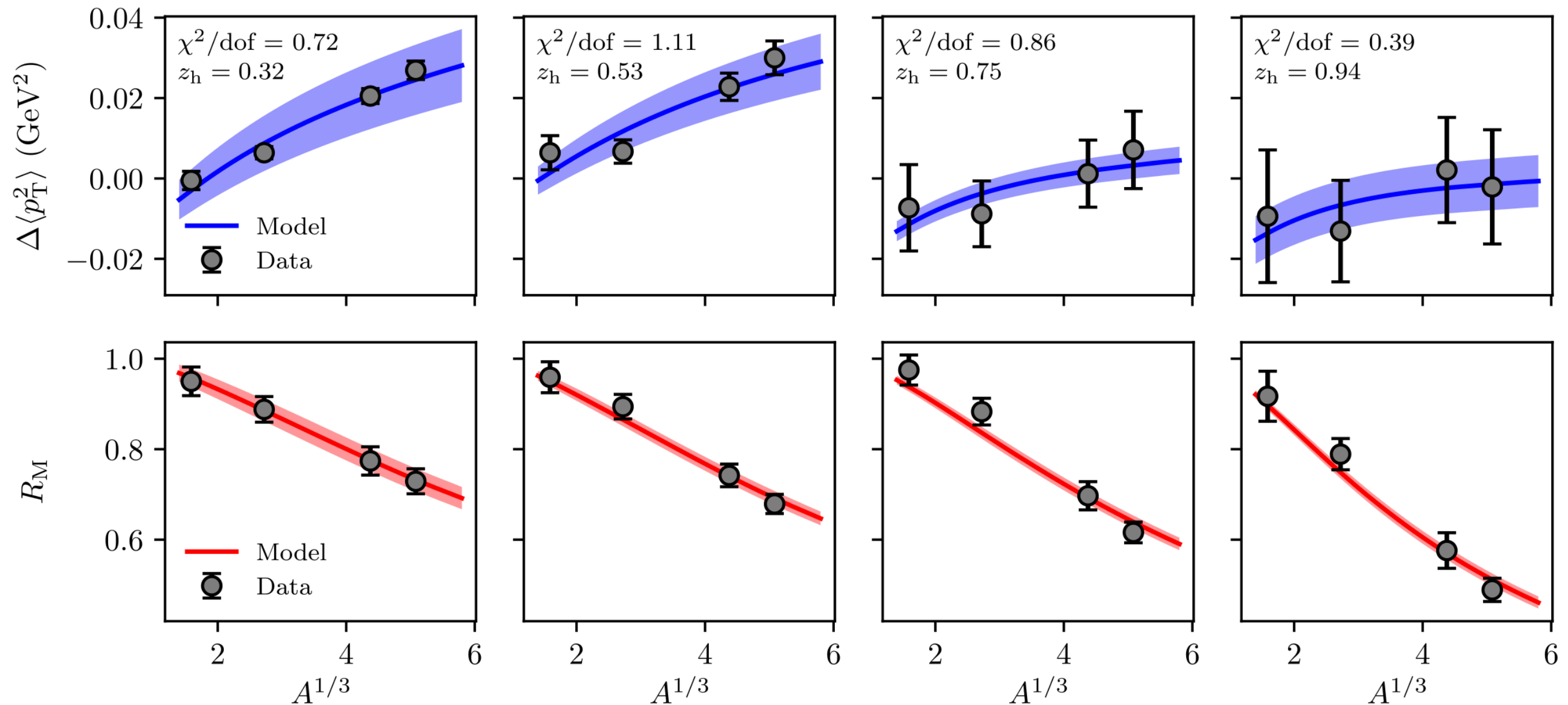
The color lifetime of the struck quark is distributed stochastically as a decaying exponential.



About this model

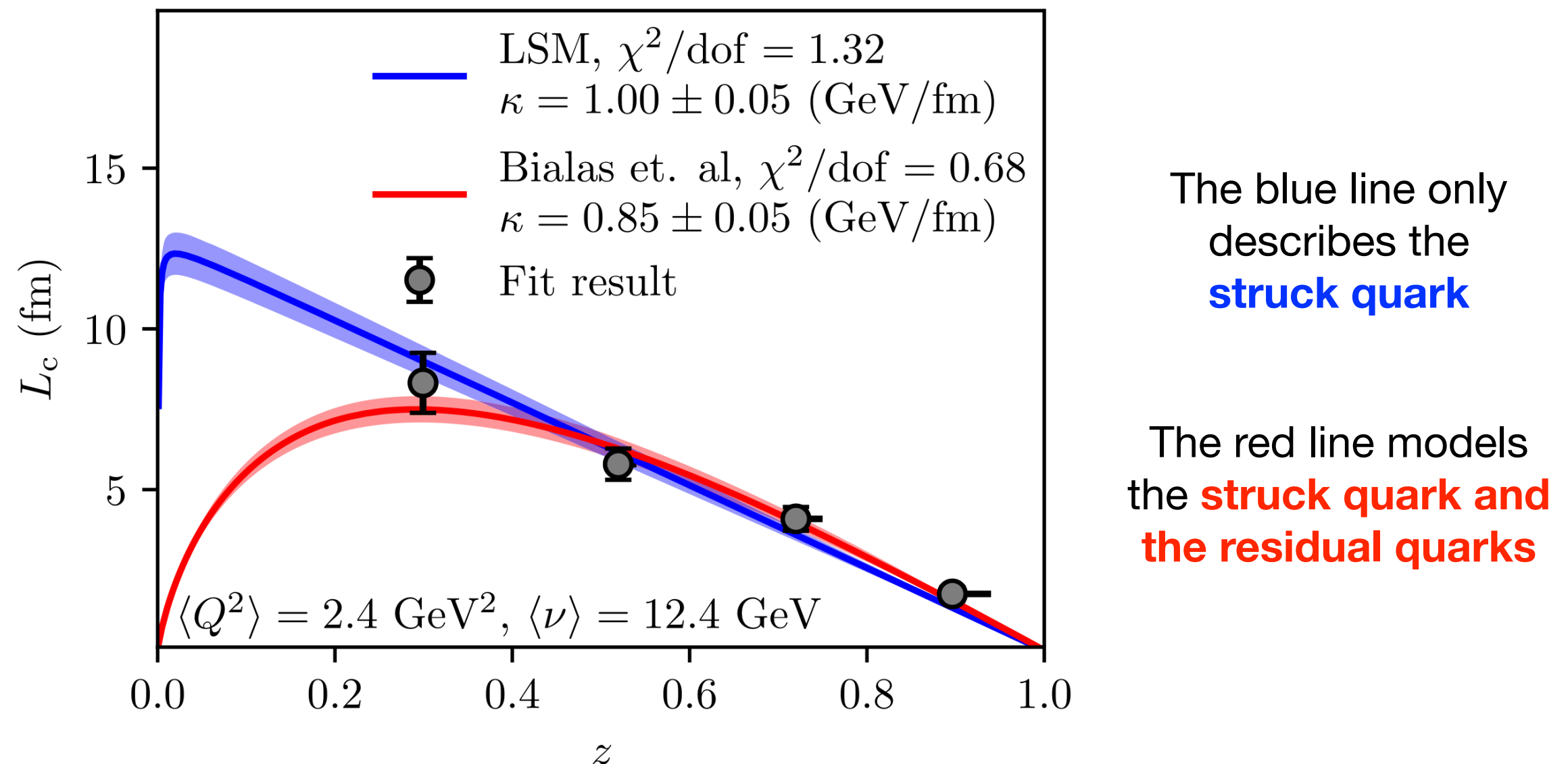
- A **new analysis** of two published HERMES measurements. We isolate the roles of **quark energy loss and pre-hadron formation** in describing the data.
- **Two observables** are fitted **simultaneously**.
- The primary ingredient is the **well-known density distribution** in nuclei.
- A second ingredient is the measured pi-N cross section
- Only **3** parameters

These are the results of the simultaneous fit to two observables



Message: we *believe* we understand pion hadronization well, in a simple space-time picture

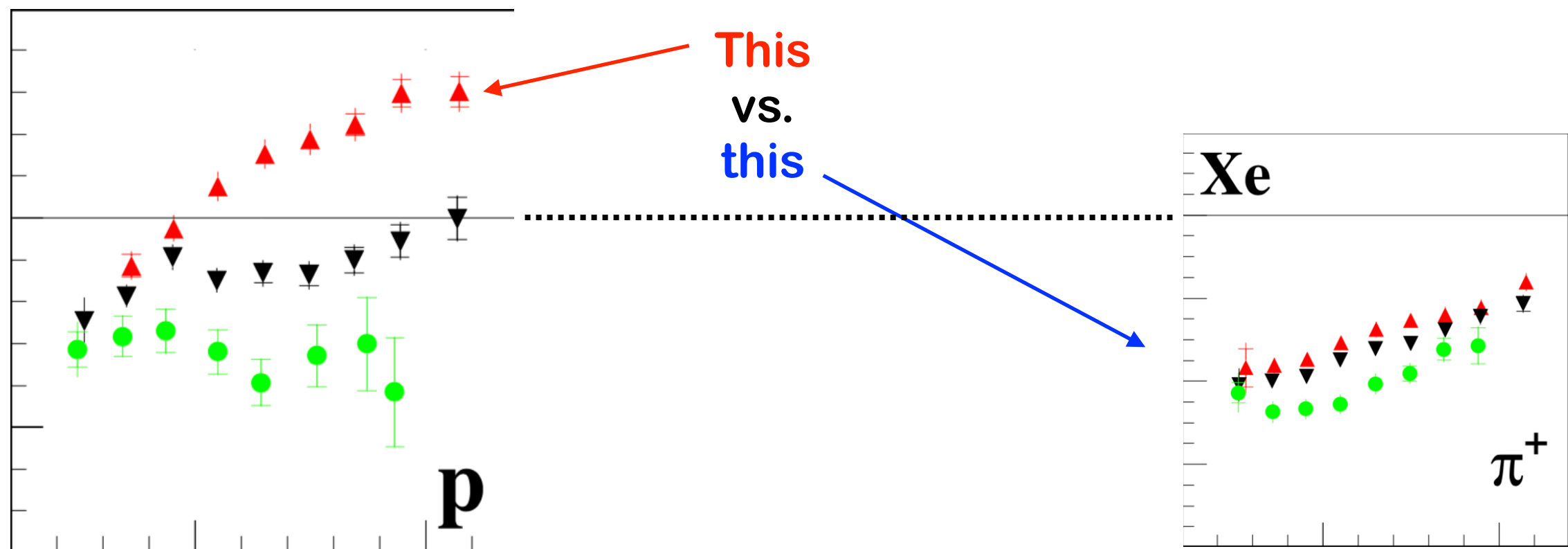
This is a fit of the color lifetime parameter L_c we find to the color lifetime calculated in the Lund String Model



Independent determination of the string constant of the LSM!

Message: our space-time model is consistent with known string fragmentation.

We believe we have a correct [simplified] physical picture.



HERMES paper explanation: FSI are “knocking out protons.” **Maybe.**
 But, at high W and Q^2 , if virtual photon strikes **one** quark: need to
 make an energetic pion in-medium to knock out a proton.

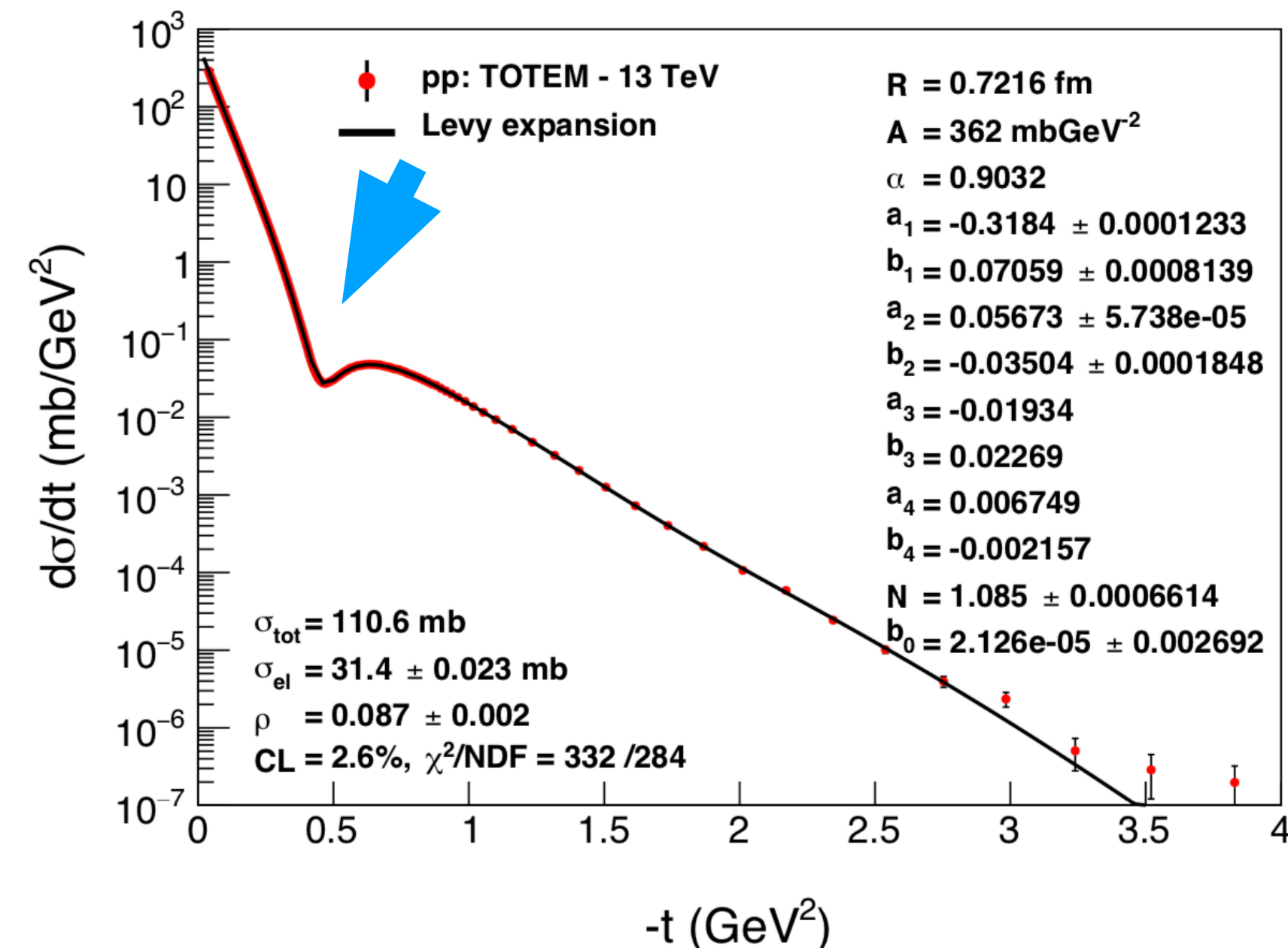
But maybe it could be diquarks knocking them out.
 Diquark “size” must be similar to proton (0.6 fm in LQCD)
 = diquark color field much more extended in space

**Test this hypothesis: CLAS new nDIS data for
Lambda Baryons**

Diquarks have been invoked for hadron beam scattering

“Convergence properties of Lévy expansions: implications for Odderon and proton structure,”

T. Csörgő, R. Pasechnik, A. Ster,
<https://arxiv.org/pdf/1903.08235>



Having only one minimum
implies there are only two
internal substructures,
such as quark-diquark.

<https://arxiv.org/abs/1903.08235>

<https://arxiv.org/abs/1902.00109>

<https://arxiv.org/abs/1811.08913>

<https://arxiv.org/abs/1807.02897>

Diquarks have been invoked for hadron beam scattering

To explain anomalies in proton production!

Breakstone et al. (following 2 slides) 1985 ISR data

<http://cds.cern.ch/record/158001/files/198503162.pdf>



EUROPEAN ORGANIZATION FOR NUCLEAR RESEARCH

CERN/EP 85-30

5 March 1985

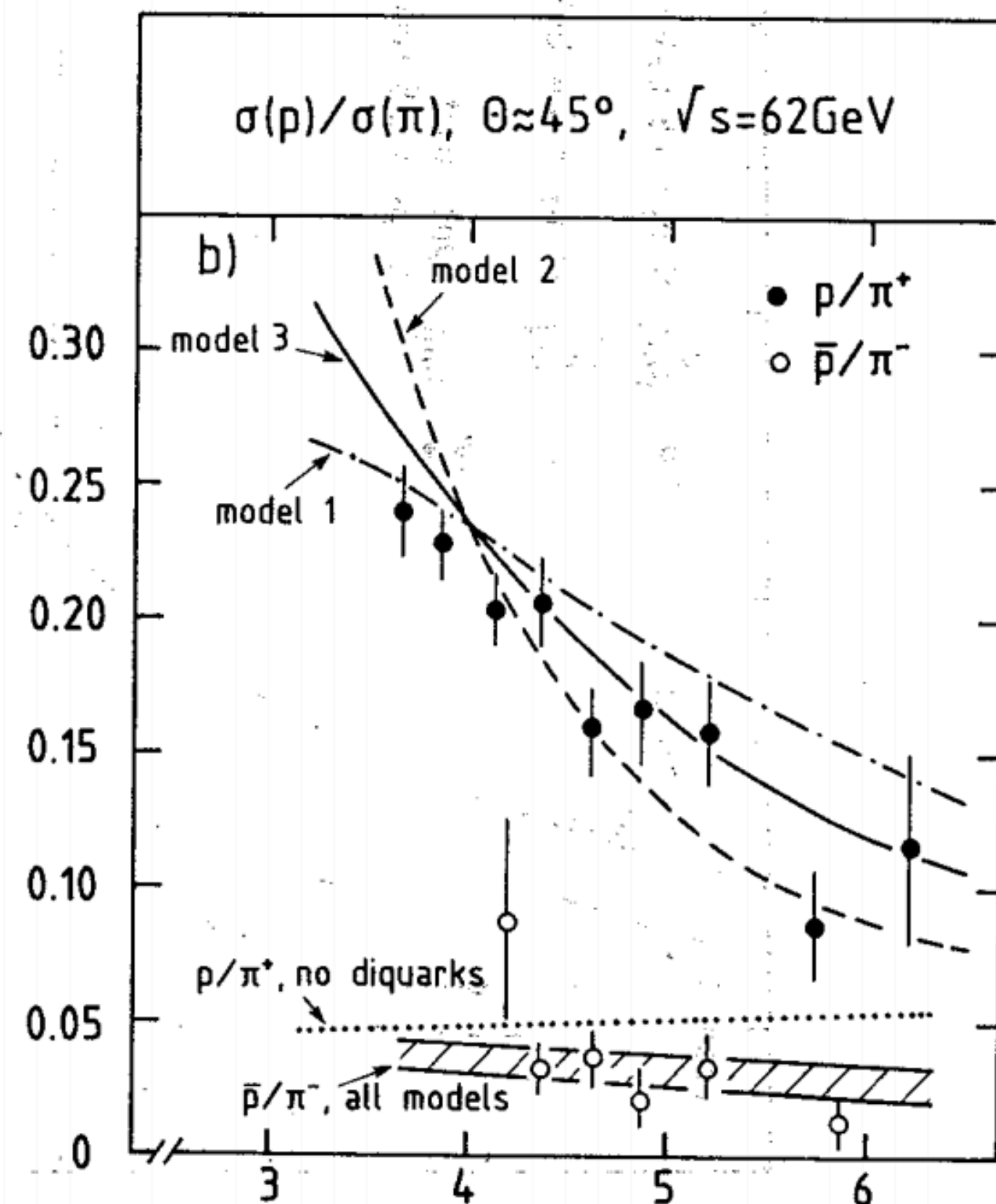
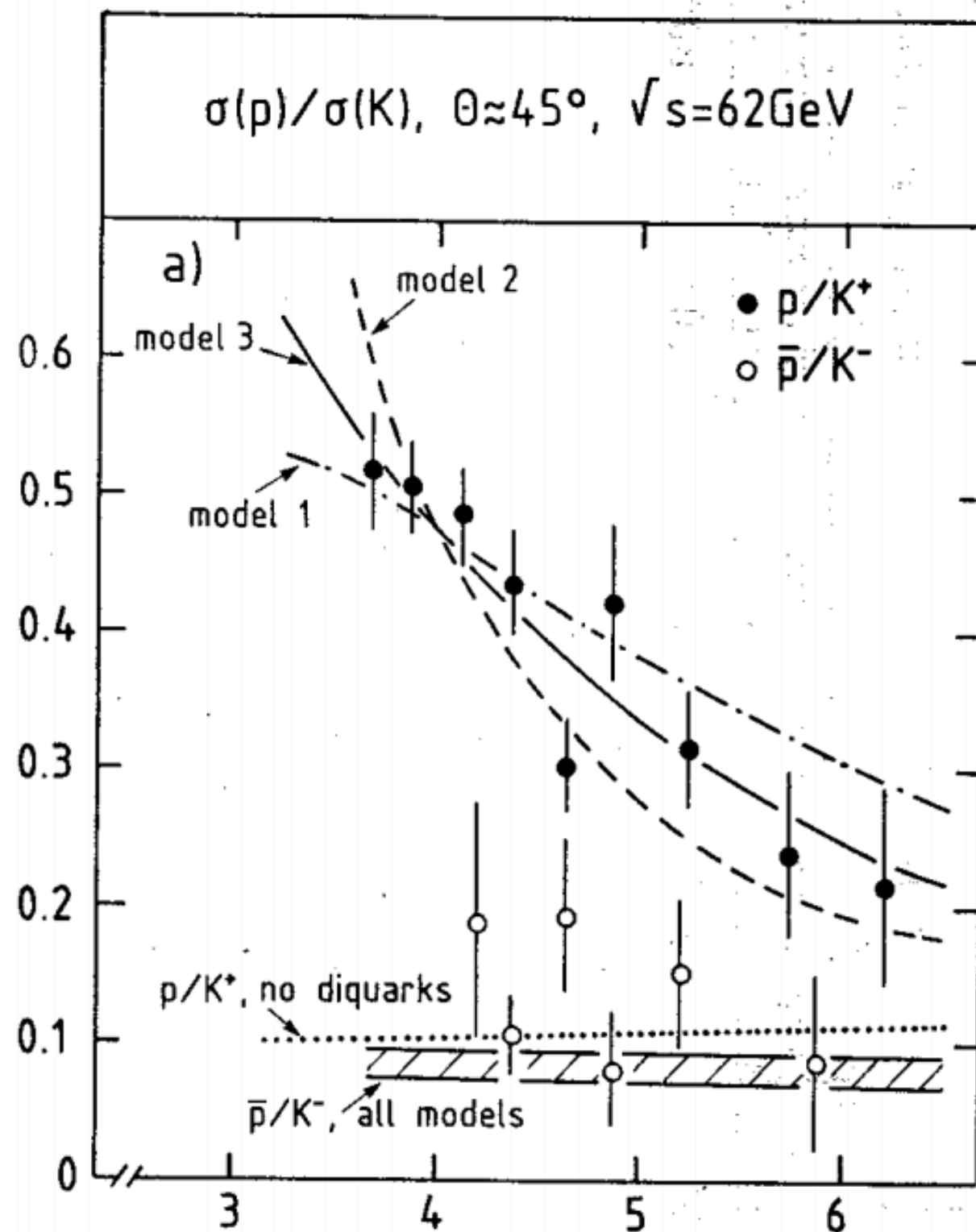
A DIQUARK SCATTERING MODEL FOR HIGH p_T PROTON PRODUCTION IN pp
COLLISIONS AT THE ISR

Ames-Bologna-CERN-Dortmund-Heidelberg-Warsaw Collaboration

A. Breakstone¹⁽⁺⁾, H.B. Crawley¹, G.M. Dallavalle⁵, K. Doroba⁶, D. Drijard³,
F. Fabbri³, A. Firestone¹, H.G. Fischer³, H. Frehse^{3(*)}, W. Geist^{3(**)},
G. Giacomelli², R. Gokieli⁶, M. Gorbics¹, P. Hanke⁵, M. Heiden^{3(**)},
W. Herr⁵, E.E. Kluge⁵, J.W. Lamsa¹, T. Lohse⁴, R. Mankel⁴, W.T. Meyer¹,
T. Nakada^{5(***)}, M. Panter³, A. Putzer⁵, K. Rauschnabel⁴, B. Rensch⁵,
F. Rimondi², M. Schmelling⁴, G. Siroli², R. Sosnowski⁶, M. Szczekowski³,
O. Ullaland³ and D. Wegener⁴

Breakstone et al.

<http://cds.cern.ch/record/158001/files/198503162.pdf>



p_T [GeV/c]

Breakstone et al.

<http://cds.cern.ch/record/158001/files/198503162.pdf>

Fig. 1

P_T broadening for positive pions in CLAS

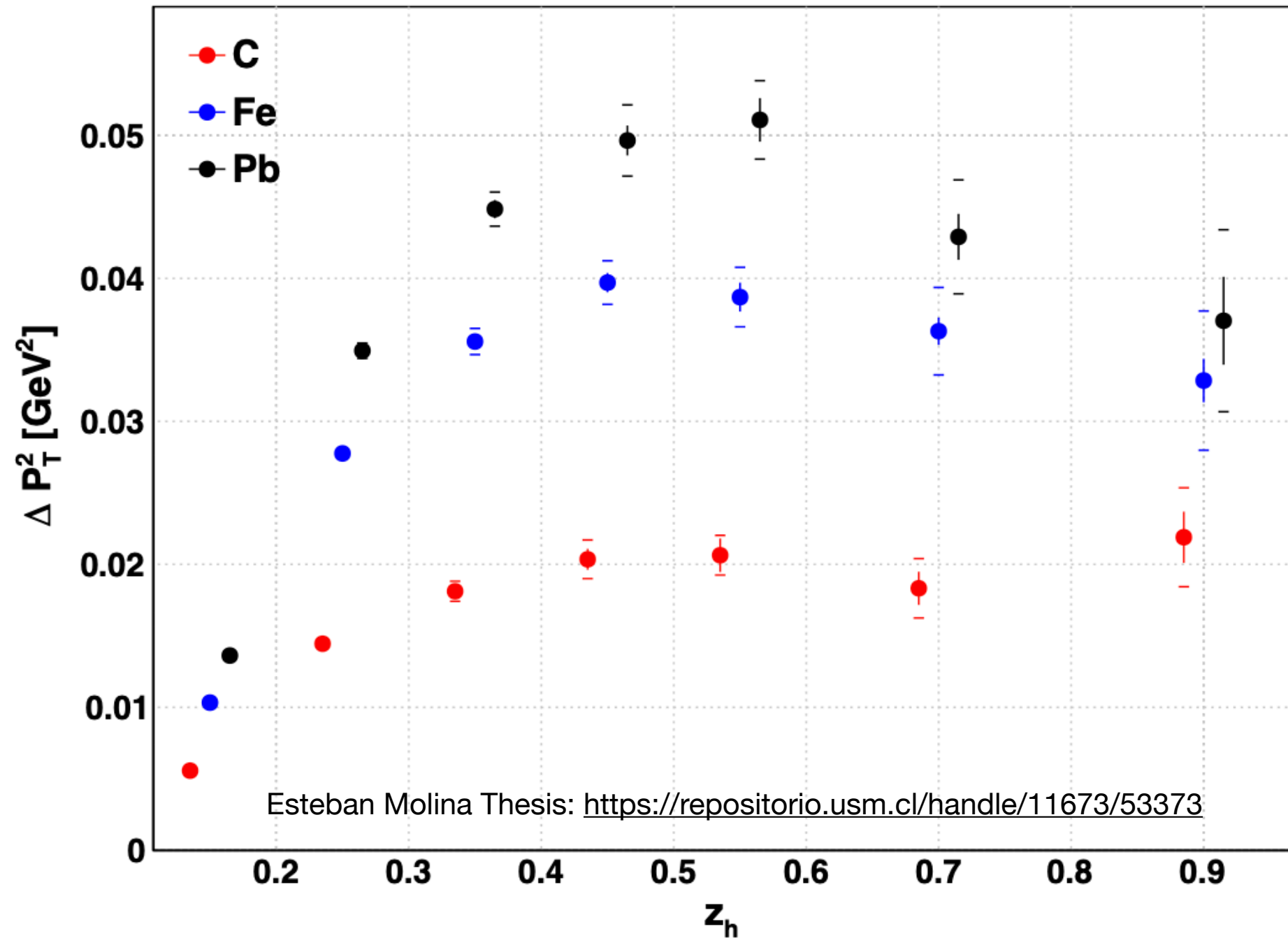


Figure B.63: ΔP_T^2 with all variables integrated except z_h .

P_T broadening for positive pions in CLAS

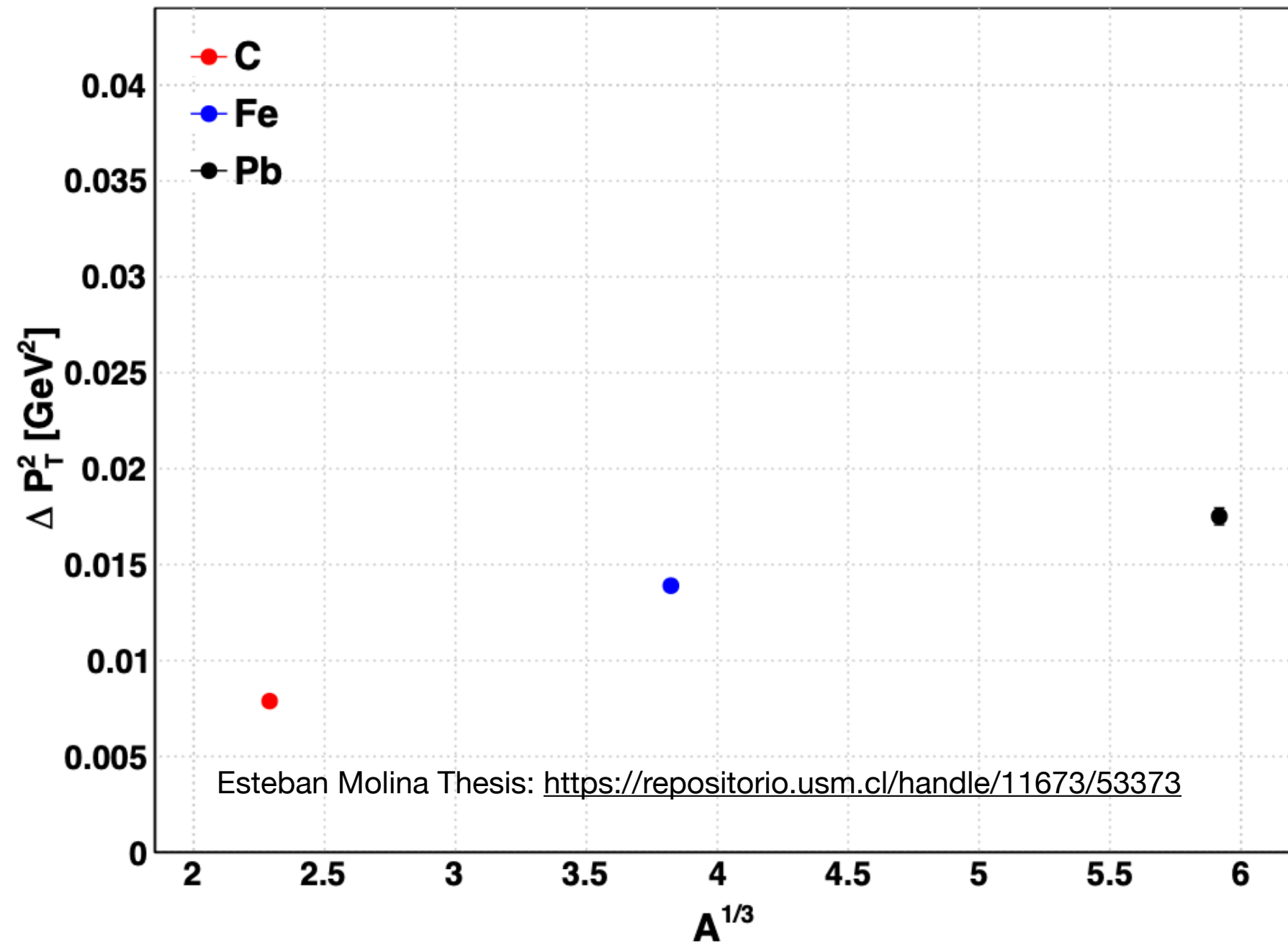


Figure B.59: ΔP_T^2 with all variables integrated and no x_f cut.