

Measurements of the $\text{Cos}\phi$ and $\text{Cos}2\phi$ Moments of the Unpolarized SIDIS π^+ Cross-section at CLAS12

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Presentation for the CLAS Collaboration

LinkedIn



Motivation

- Semi-Inclusive Deep Inelastic Scattering (SIDIS) experiments allow us to address questions about the 3D structure of nucleons
- Azimuthal modulations in unpolarized SIDIS cross-section for charged pion electroproduction can give access to the Cahn and Boer-Mulders effects
 - **Boer-Mulders Effect:** Sensitive to the correlation between the quark's transverse momentum and intrinsic transverse spin in an unpolarized nucleon
 - **Cahn Effect:** Sensitive to the transverse motion of quarks inside the nucleon
- A non-zero Boer-Mulders requires quark orbital angular momentum contributions to the proton spin (aspect of the proton missing spin puzzle)

SIDIS Cross-Section and Boer-Mulders

The lepton-hadron Unpolarized SIDIS Cross-Section:

$$\frac{d^5\sigma}{dx dQ^2 dz d\phi_h dP_{h\perp}^2} = \underbrace{\frac{2\pi\alpha^2}{xyQ^2} \frac{y^2}{2(1-\epsilon)} \left(1 + \frac{\gamma^2}{2x}\right) (F_{UU,T} + \epsilon F_{UU,L})}_{A_0} \left\{ 1 + \underbrace{\frac{\sqrt{2\epsilon(1+\epsilon)} F_{UU}^{\cos\phi_h}}{(F_{UU,T} + \epsilon F_{UU,L})}}_{A_{UU}^{\cos\phi_h}} \cos\phi_h + \underbrace{\frac{\epsilon F_{UU}^{\cos 2\phi_h}}{(F_{UU,T} + \epsilon F_{UU,L})}}_{A_{UU}^{\cos 2\phi_h}} \cos 2\phi_h \right\}$$

The Boer-Mulders and Cahn effects are present in the Structure Functions:

leading twist

$$F_{UU}^{\cos 2\phi_h} \propto C \left[\frac{2(\hat{P}_{h\perp} \cdot \vec{k}_T)(\hat{P}_{h\perp} \cdot \vec{p}_T) - \vec{k}_T \cdot \vec{p}_T}{MM_h} h_1^\perp H_1^\perp + \dots \right]$$

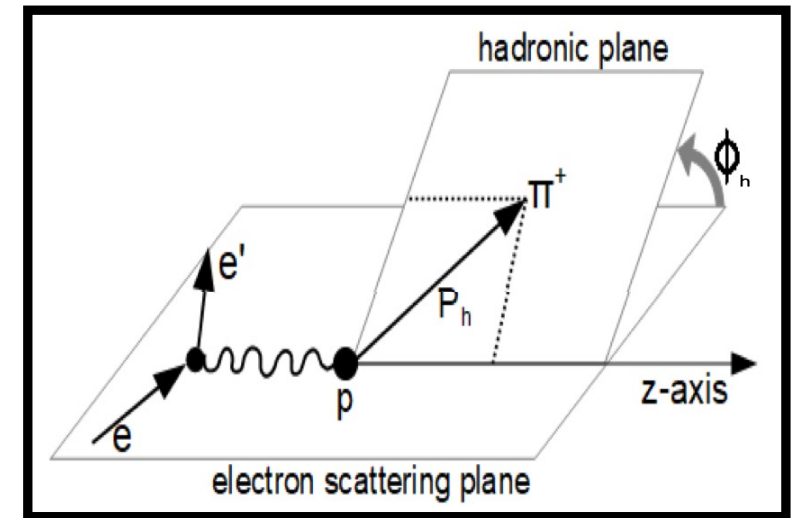
BOER-MULDERS EFFECT

next to leading twist

$$F_{UU}^{\cos\phi_h} \propto \frac{2M}{Q} C \left[-\frac{\hat{P}_{h\perp} \cdot \vec{k}_T}{M_h} x h H_1^\perp - \frac{\hat{P}_{h\perp} \cdot \vec{p}_T}{M} f_1 D_1 + \dots \right]$$

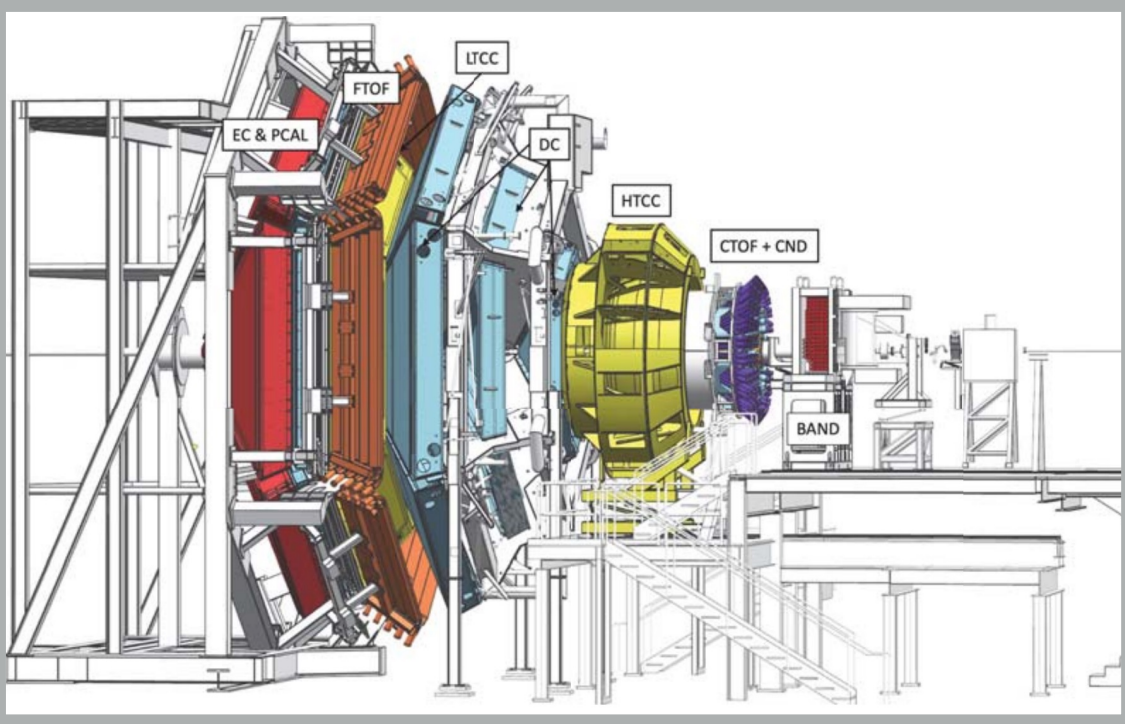
CAHN EFFECT

Interaction dependent terms neglected



Reaction Studied: $e p \rightarrow e \pi^+(X)$

Data Collection



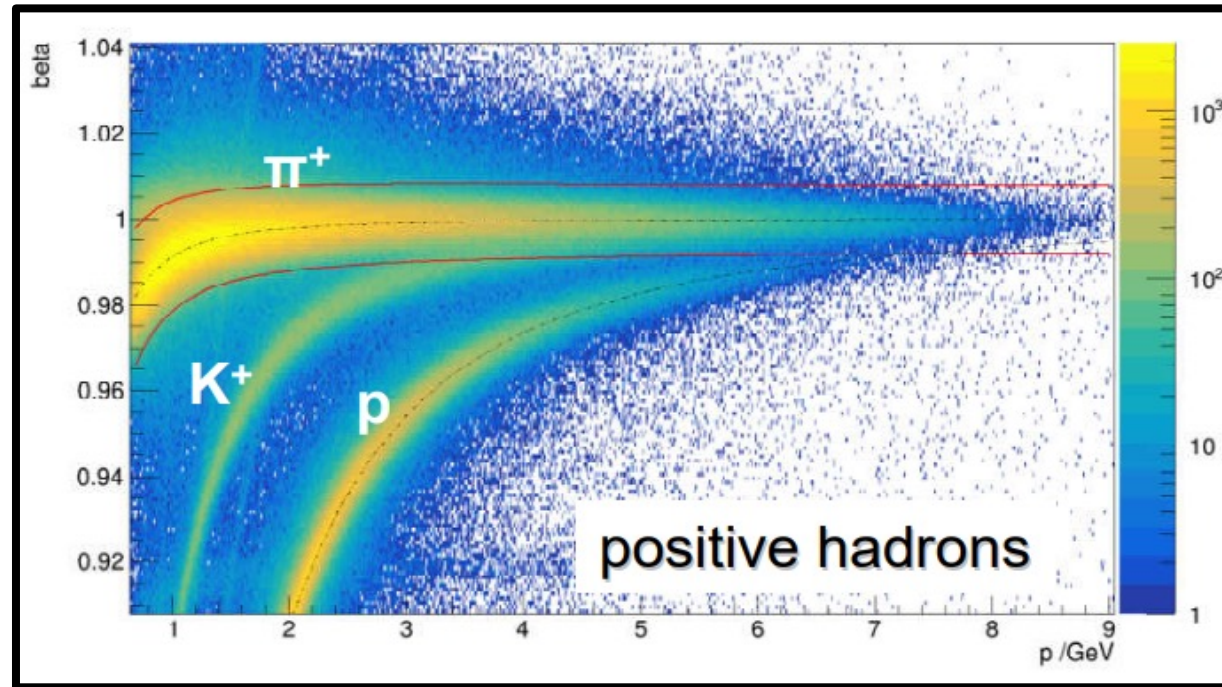
CLAS12 Detector

- CLAS12 detector in Hall B at Jefferson Lab
 - Upgrade from the CLAS detector
 - Enabled the higher energy and statistics for our experiments, not previously accessible
- Data from the Fall 2018 RG-A experiment
 - Used a 10.6 GeV polarized electron beam and unpolarized liquid hydrogen target
- Data presented uses forward tracking only

Event Selection

Particle ID (PID):

- **Electron ID:** Based on Electromagnetic Calorimeter (PCAL) and Cherenkov Counters (HTCC)
- **Hadron (π^+) ID:** Based on Time-Of-Flight Counters (TOF) and the correlation of velocity (β) and momentum



*Image provided by Stefan Diehl

π^+ Pion PID – β vs p

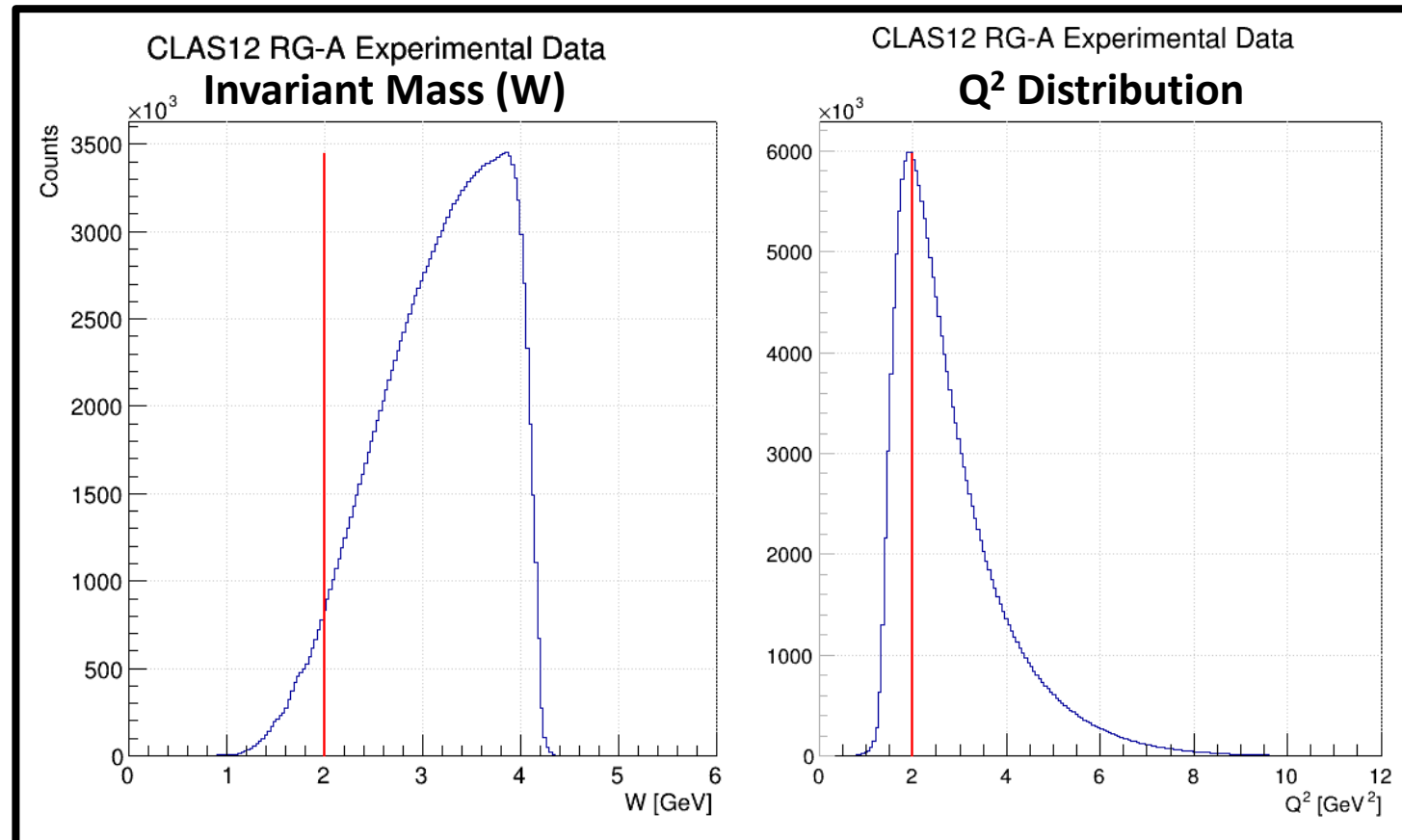
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Analysis Cuts:

- **SIDIS Cuts:**
 - $W > 2 \text{ GeV}$
 - $Q^2 > 2 \text{ GeV}^2$



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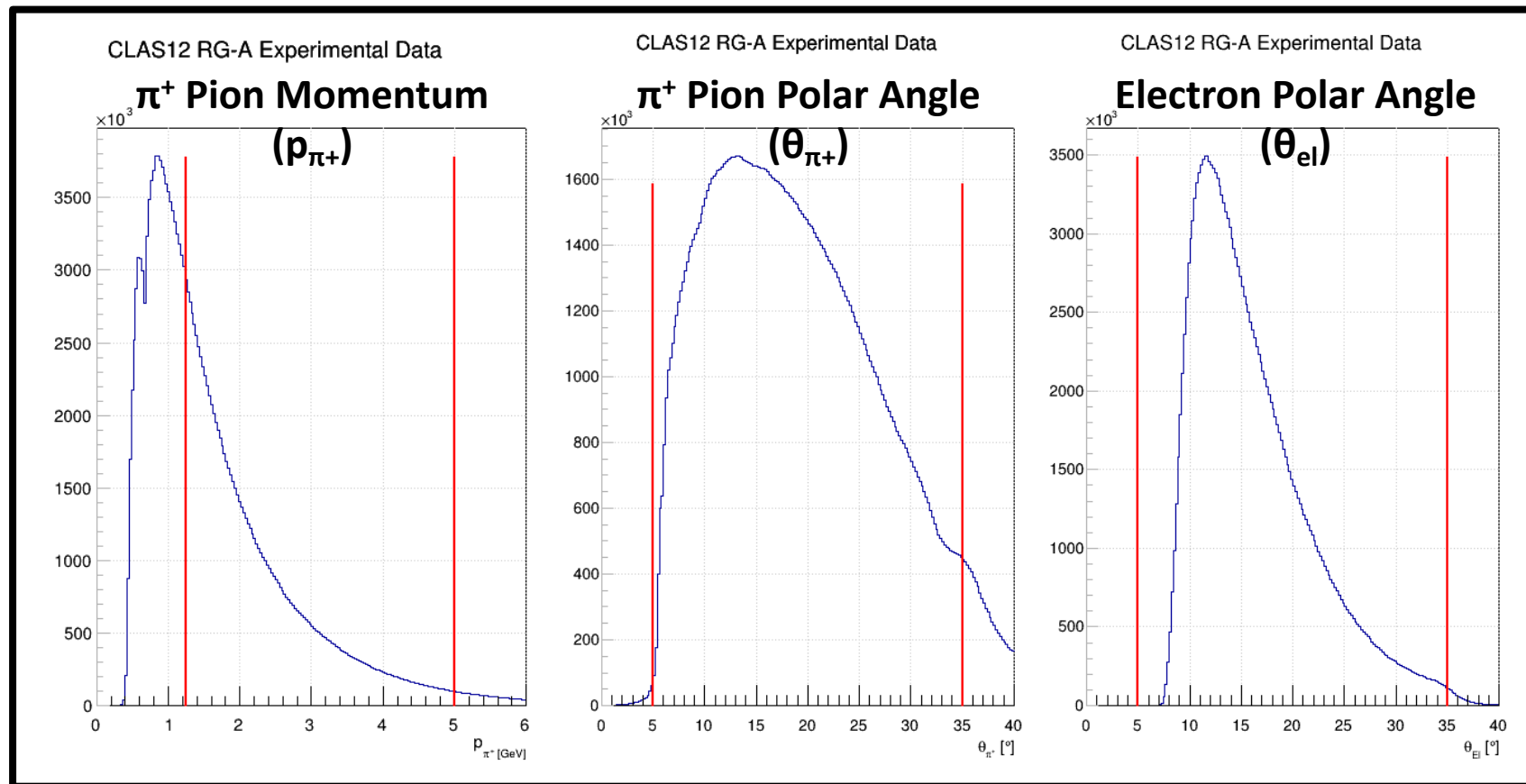
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- **Other Analysis Cuts:**

- p_{π^+} Cut: $1.25 \text{ GeV} < p_{\pi^+} < 5 \text{ GeV}$
- θ -angle Cut: $5^\circ < \theta_{\text{particle}} < 35^\circ$



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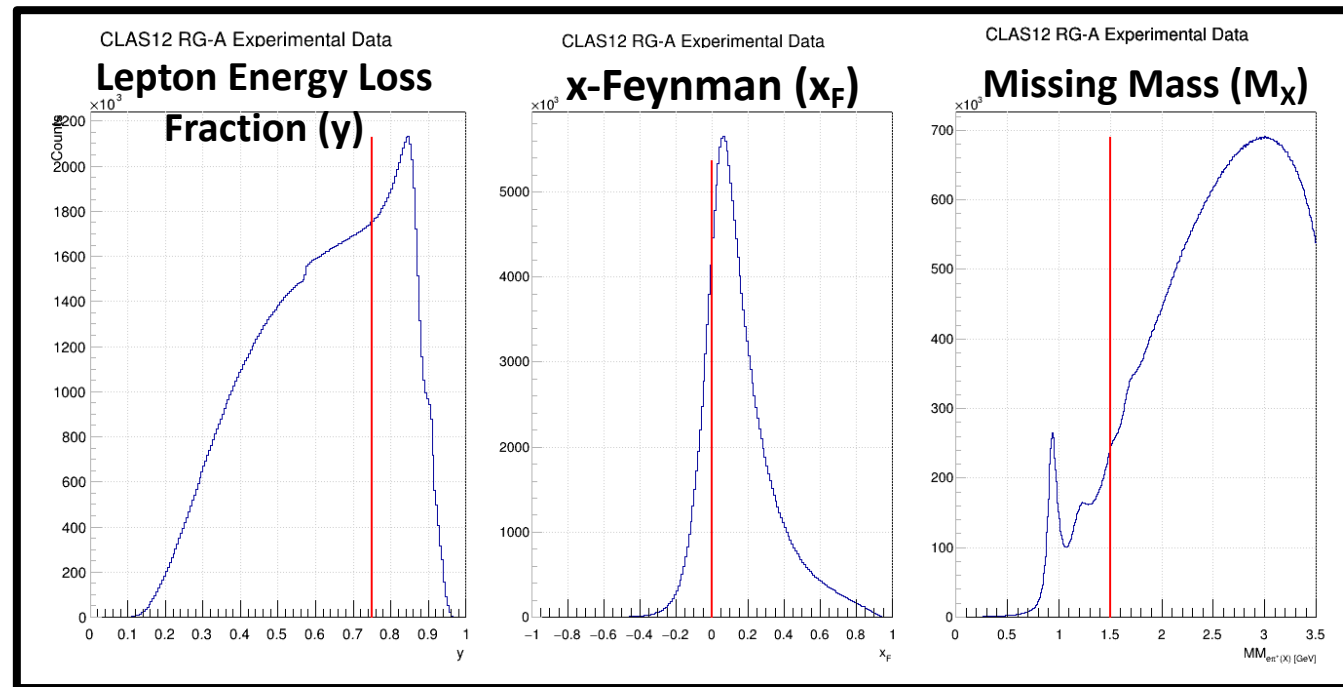
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- $y < 0.75$ (minimize other background processes)
- $x_F > 0$ (minimize contributions from target fragmentations)
- Missing Mass Cut: $M_x > 1.5 \text{ GeV}$ (limits contributions from exclusive events)



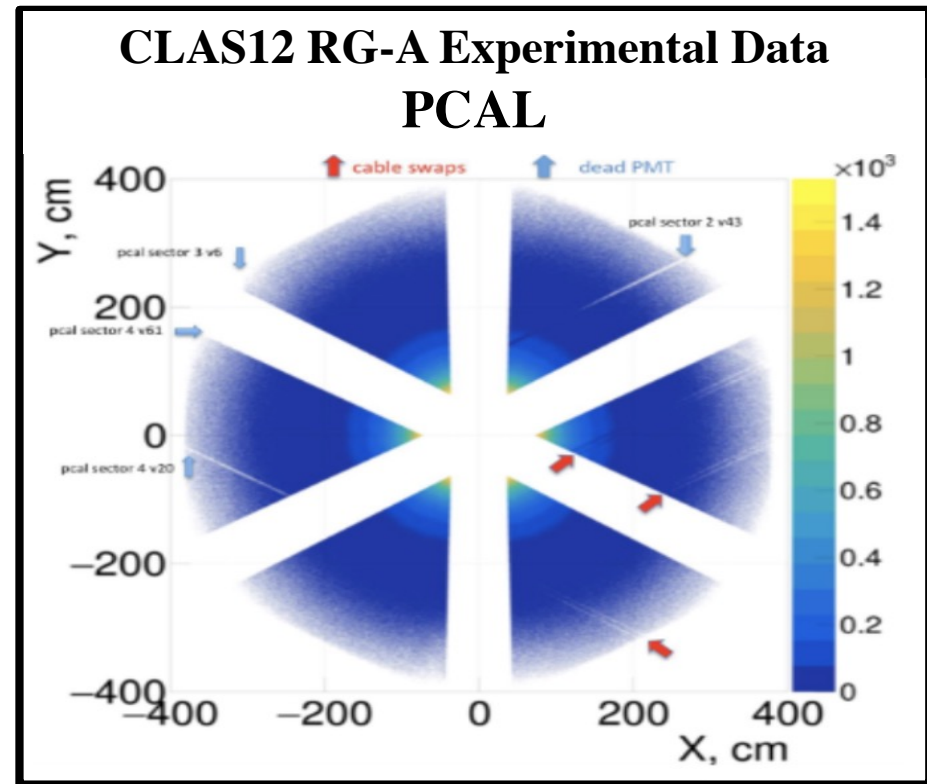
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 - Missing Mass Cut: $M_x > 1.5 \text{ GeV}$ (limits contributions from exclusive events)
 - Fiducial Cuts (e.g., accounts for bad channels present in data)



Analysis Procedure

Experimental extraction of cross-section

$$\frac{d^5\sigma}{dQ^2 dx_B dP_T dz d\varphi_h} = \frac{1}{(\Delta Q^2 \Delta x_B \Delta P_T \Delta z \Delta \varphi_h)} \frac{N}{R \cdot BC \cdot \eta \cdot N_0} \frac{1}{(N_A \cdot \rho \cdot t / A_w)}$$

Where:

Bin Volume Target Number Density

- R = Radiative Correction
- η = **Acceptance Correction** → **Requires Monte Carlo (MC) Simulation**
- N = Bin Yields
- N_0 = Life-time corrected incident electron flux
- BC = factor which evolves bin-averaged differential cross-section

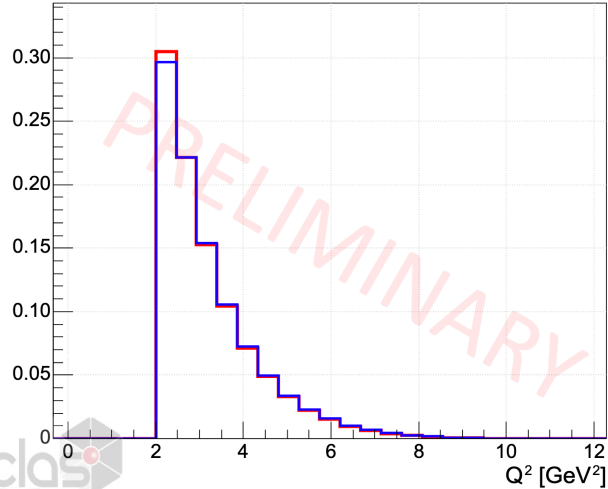
SIDIS MC are generated with LEPTO event generator

(220) Simulated Files Available Here:

`cache/clas12/rg-a/production/montecarlo/clasdis/fall2018/torus-1/v1/bkg45nA_10604MeV/`

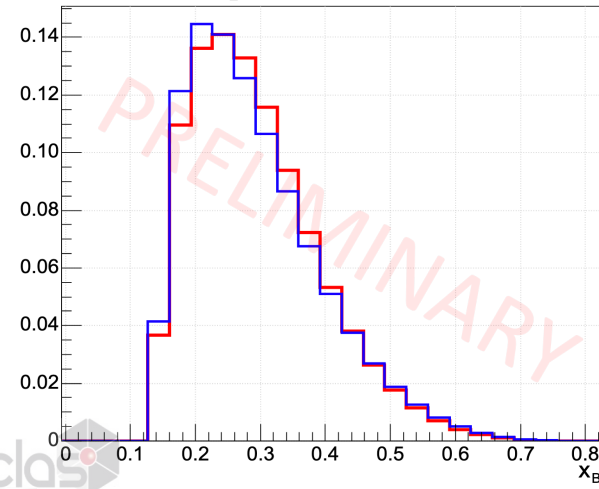
Data and Monte Carlo Comparison

Normalized Comparison of Data and Simulated Q^2



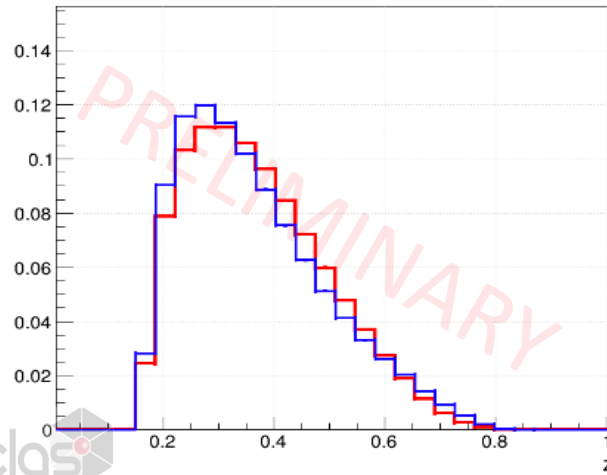
Q^2 Comparison

Normalized Comparison of Data and Simulated x_B



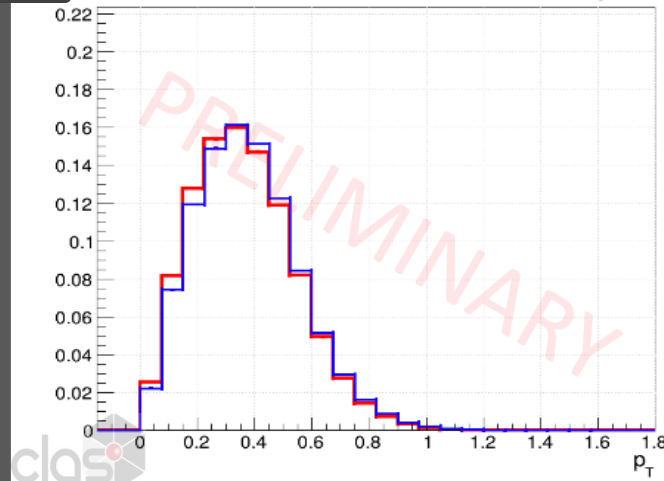
x_B Comparison

Normalized Comparison of Real and Simulated z



z Comparison

Normalized Comparison of Real and Simulated p_T



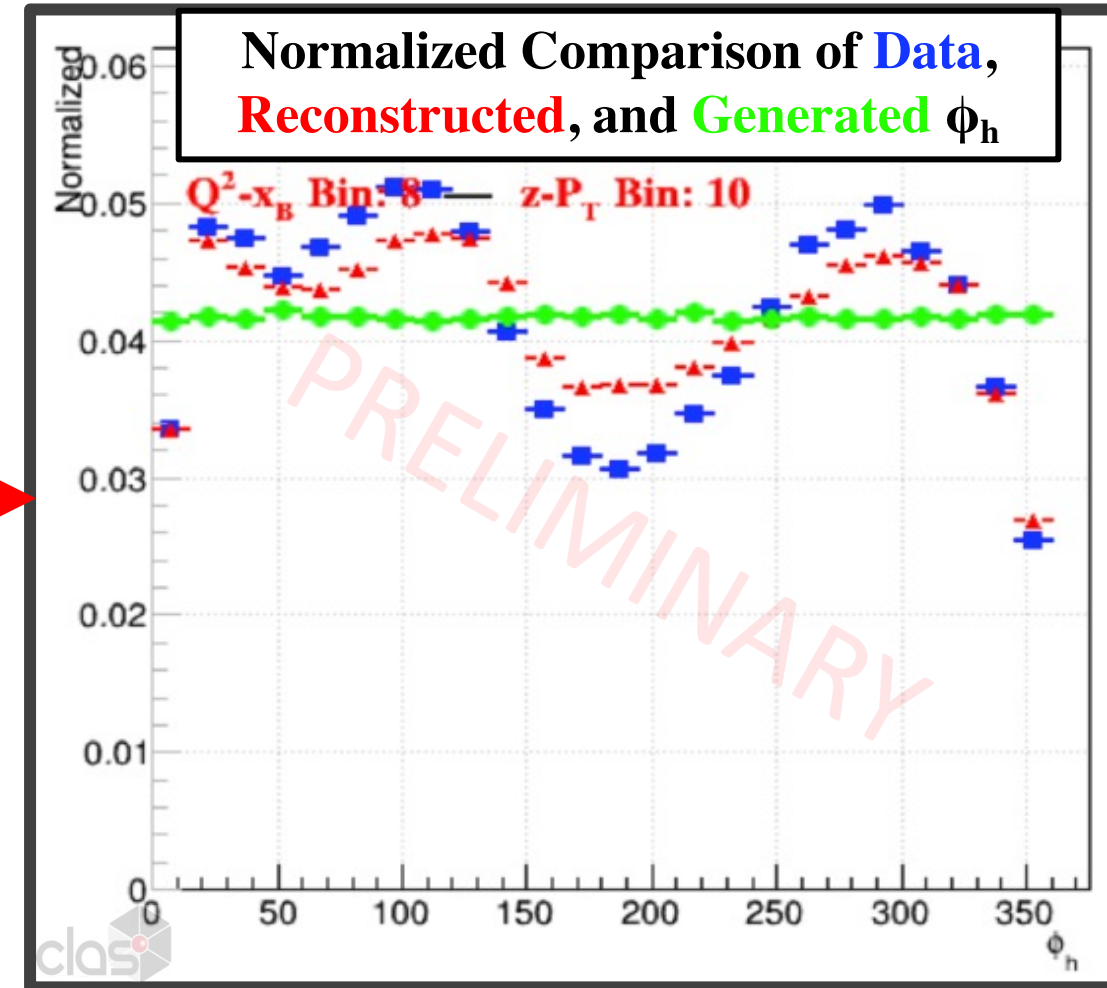
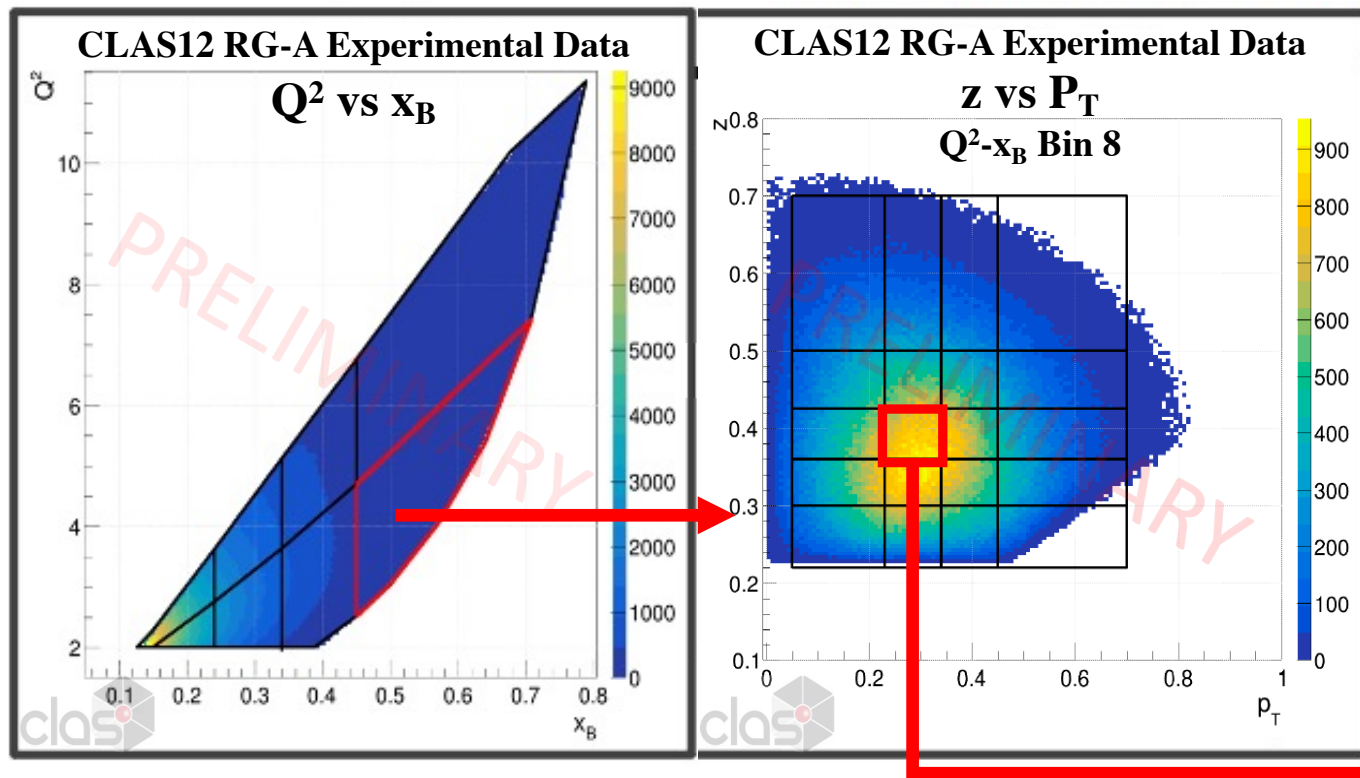
p_T Comparison

Multidimensional Analysis Procedures

Multidimensional Kinematic Binning (5 Dimensions)

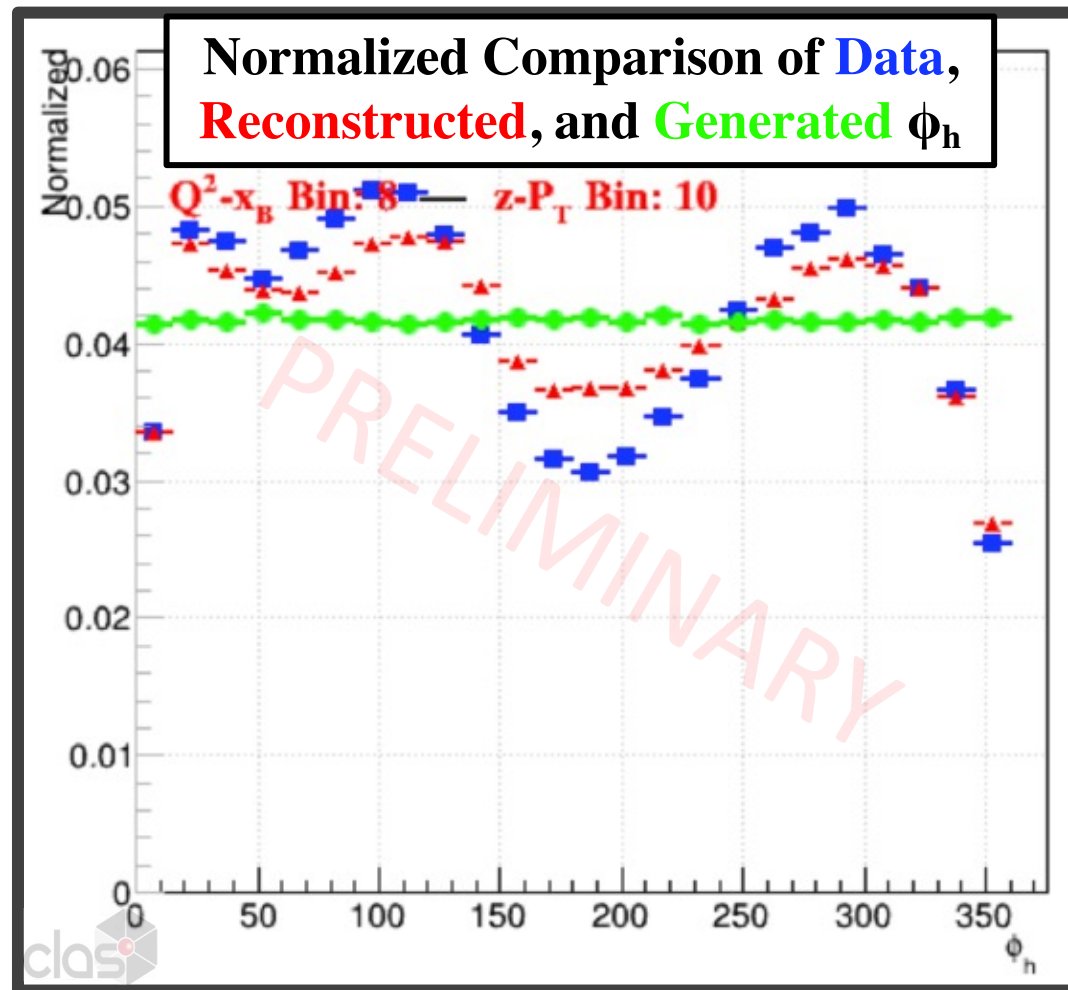
8 Q^2 - x_B Bins Total – 20-49 z - P_T Bins (per Q^2 - x_B bin)

ϕ_h distribution for the Q^2 - x_B - z - P_T bin shown in red



Unfolded Multidimensional Analysis Procedures

Multidimensional Kinematic Binning (5 Dimensions)



Apply
Multidimensional
Acceptance
Corrections and
convert to a
cross-section
measurement

ϕ_h fit for
every bin

$A(1 + B \cos(\phi_h) + C \cos(2\phi_h))$
Where the parameters A, B, C
give the cross-section moments

$$A_{UU}^{\cos \phi_h} = B \quad A_{UU}^{\cos 2\phi_h} = C$$

Methods used for Acceptance Corrections:

- **Bin-by-bin Correction**
 - Simple method which just needs the 1D plots shown here
- **(SVD) Singular Value Decomposition**
- **Bayesian Unfolding**
 - Both the SVD and Bayesian Unfolding Methods use Acceptance Matrices to correct the data

Acceptance Corrections and Bin Migration Study

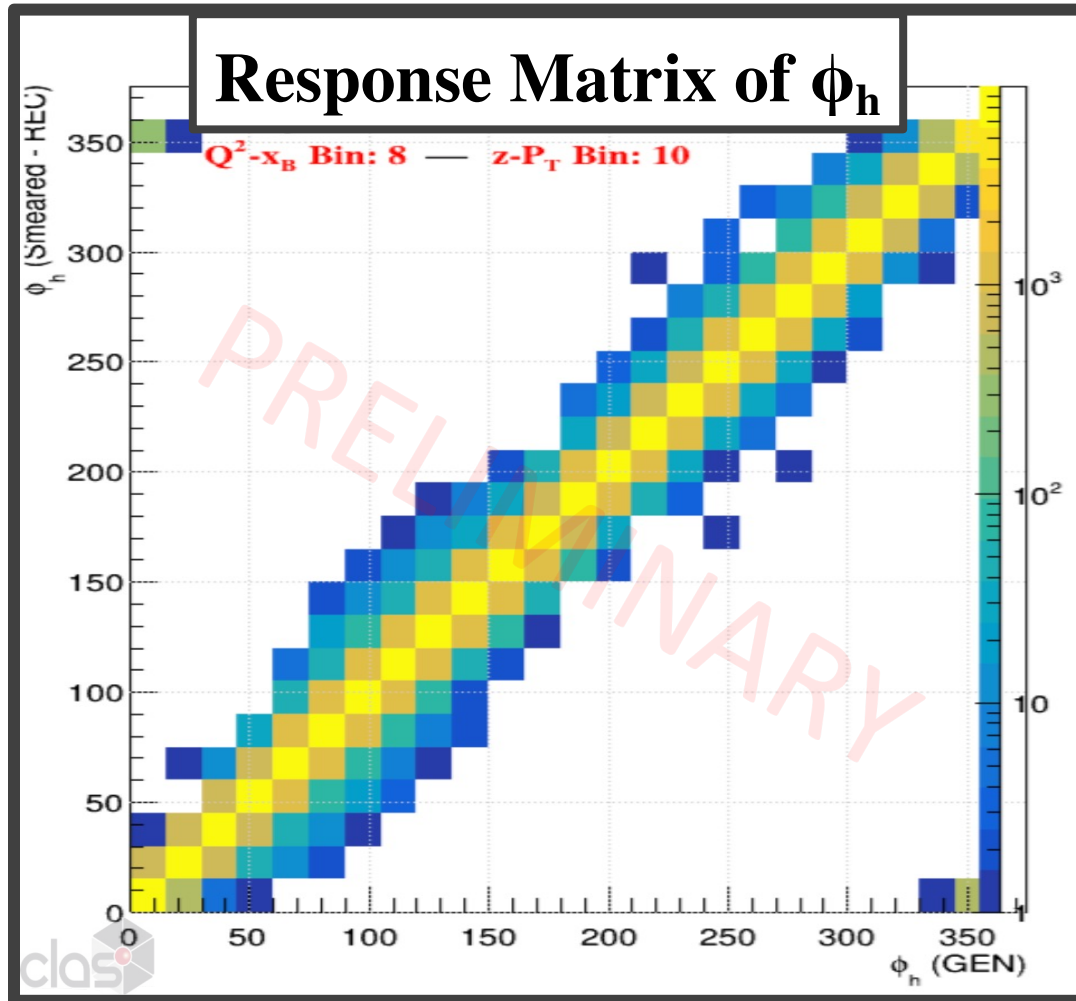
- **Acceptance Matrix:** $A_{(i,j)}$ describes both Acceptance (including geometric acceptance and detector efficiency) and Bin Migration
- $A_{(i,j)} = \frac{\text{Number of Events Generated in bin } j \text{ but Reconstructed in bin } i}{\text{Total Number of Events Generated in the } j\text{th bin}}$
- Acceptance Unfolding: $Y_i = A_{(i,j)} X_j \Leftrightarrow X_j = A_{(i,j)}^{-1} Y_i$

where:

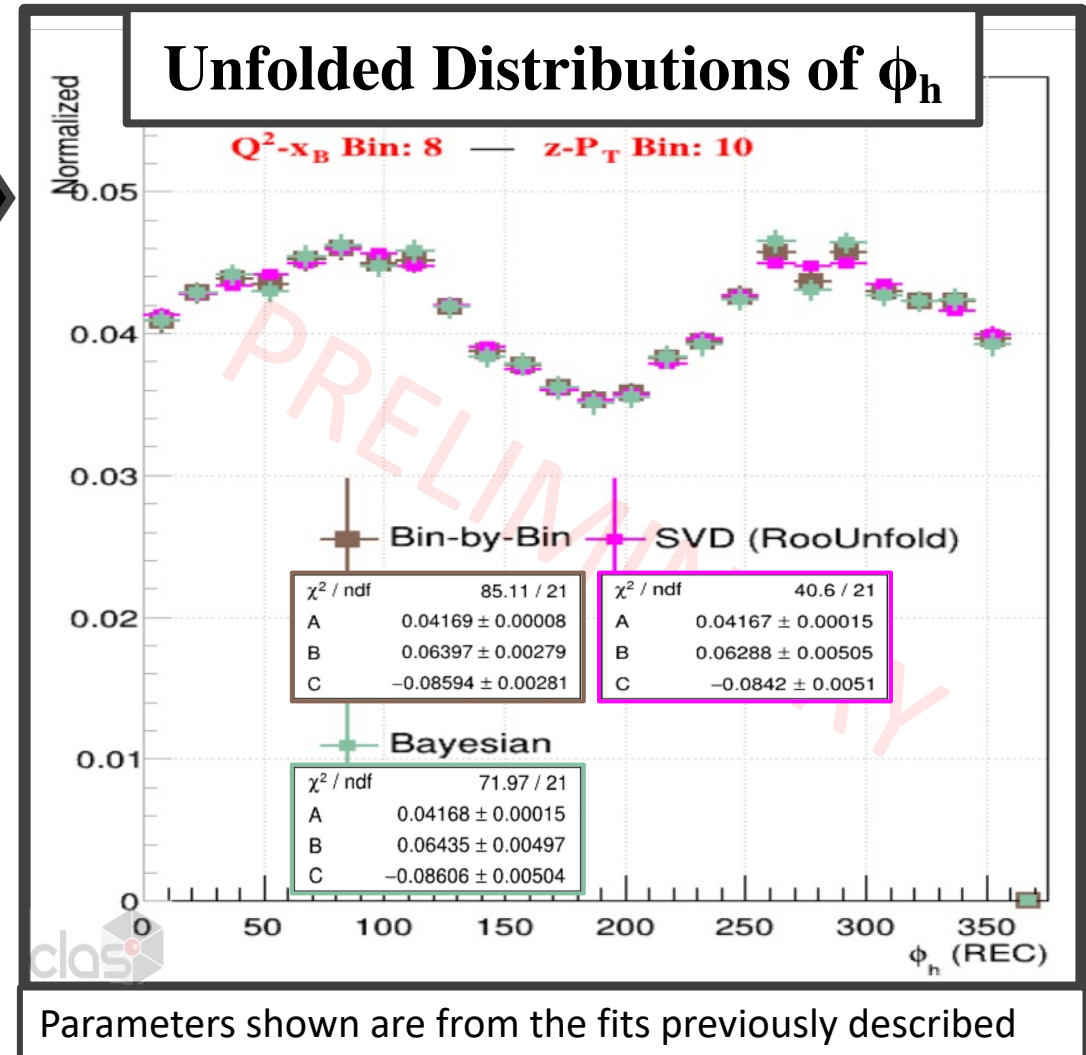
- Y_i = Number of events experimentally measured in the i -th bin
- X_j = Number of acceptance-corrected events in the j -th bin

Example of Unfolding Procedure

Using the Multidimensional Kinematic Bin from prior example



Unfolding
Procedures



Outlook

- Working on Multidimensional Acceptance Corrections for the simultaneous unfolding of Q^2 , x_B , z , P_T , and ϕ_h variables
- Efforts towards more realistic MC simulations, both on the detector response description and physics process
- Include Radiative and BC Corrections to analysis
- Long-term goals:
 - Extraction of multiplicity ($F_{UU,T} + \varepsilon F_{UU,L}$), $F_{UU}^{\cos \varphi_h}$, and $F_{UU}^{\cos 2\varphi_h}$ in terms of in Q^2 , x_B , z , and P_T for the π^+ for all CLAS12 RG-A data

Thank you

For more information and updates, see the following web page:

https://userweb.jlab.org/~richcap/Interactive_Webpage_SIDIS_richcap/Interactive_Unfolding_Page.html

Questions?

Acknowledgements

- Contributions made by other members of the CLAS Collaboration
- This work is supported by the U.S. Department of Energy, Office of Science, Office of Nuclear Physics under contract number DE-AC02-06CH11357



Backup Slides

Event Selection (Full PID)

The RG-A Analysis Overview and Procedures note goes into detail about the common particle identification scheme used for RG-A

(See: https://clas12-docdb.jlab.org/DocDB/0009/000949/001/RGA_Analysis_Overview_and_Procedures-08172020.pdf)

Electron PID Criteria:

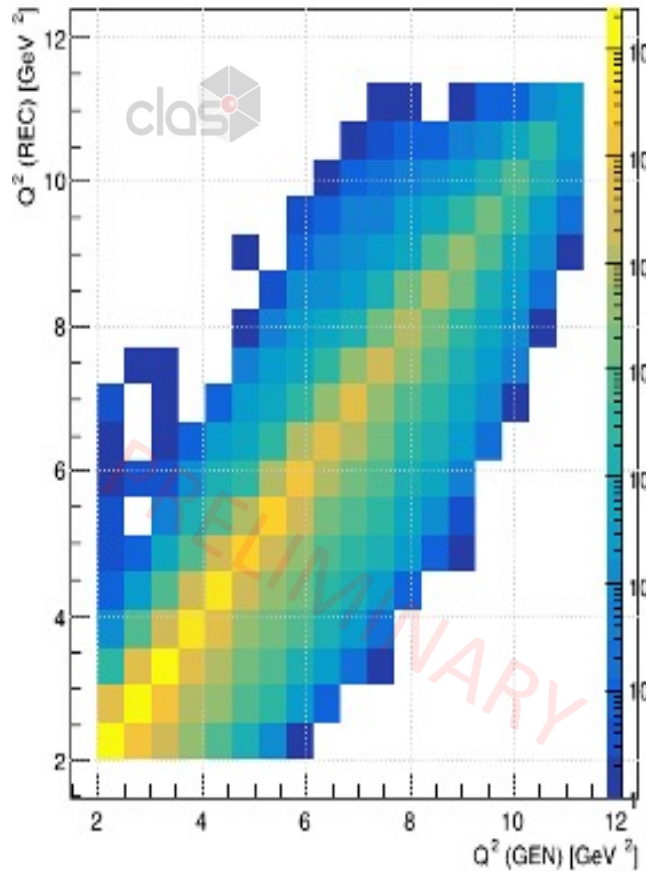
- Detected in Forward Detector
- > 2 photoelectrons detected in the HTCC
- > 0.07 GeV energy deposited in the PCAL
- Sector dependent sampling fraction cut
- “Diagonal cut” for electrons above 4.5 GeV (HTCC threshold)
- $y < 0.75$, not strictly an “electron cut”, but sets the min electron energy approximately > 2.4 GeV

Pion PID Criteria:

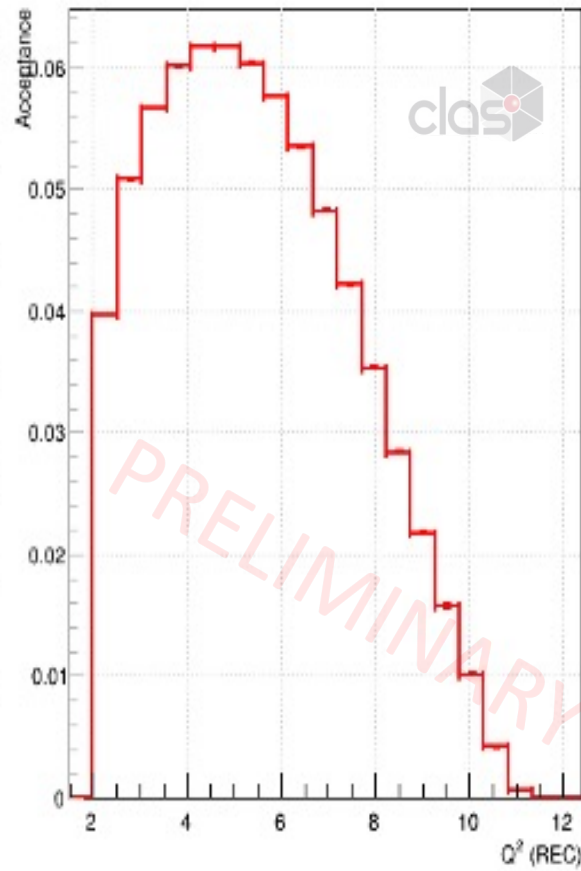
- Detected in Forward Detector
- $p > 1.25$ GeV
- Refined chi2pid cuts

Example of Unfolding (Q^2)

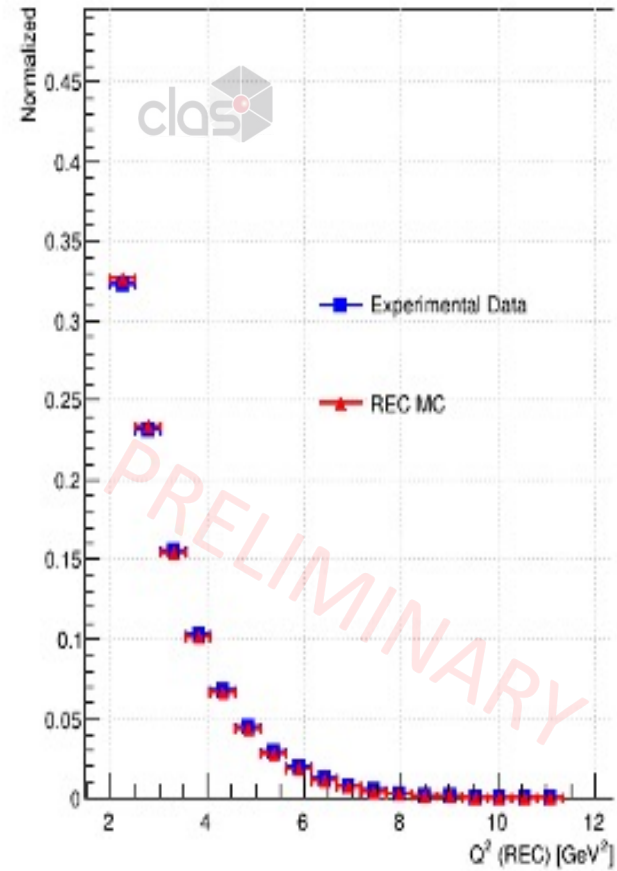
Response Matrix of Q^2



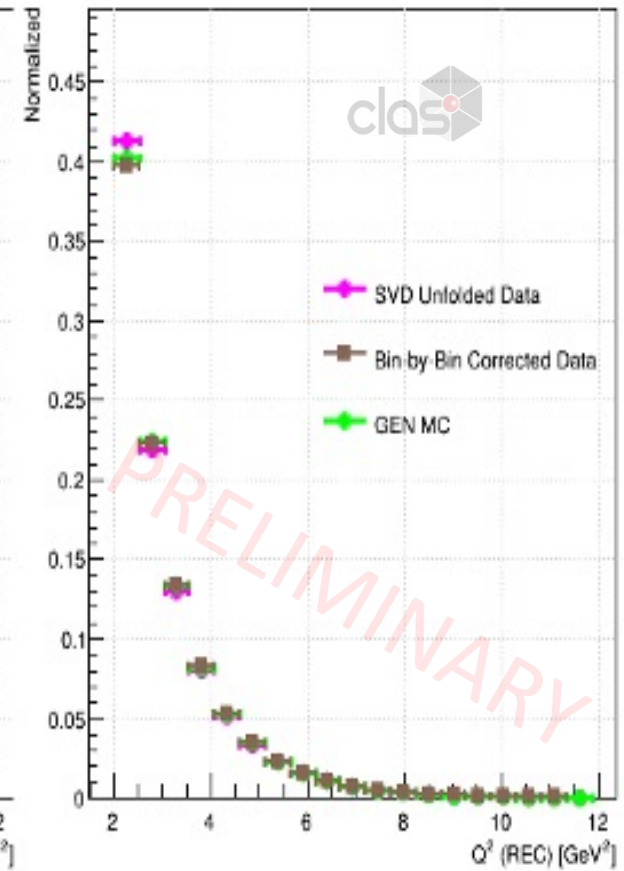
Acceptance Correction of Q^2



Reconstructed Distribution of Q^2

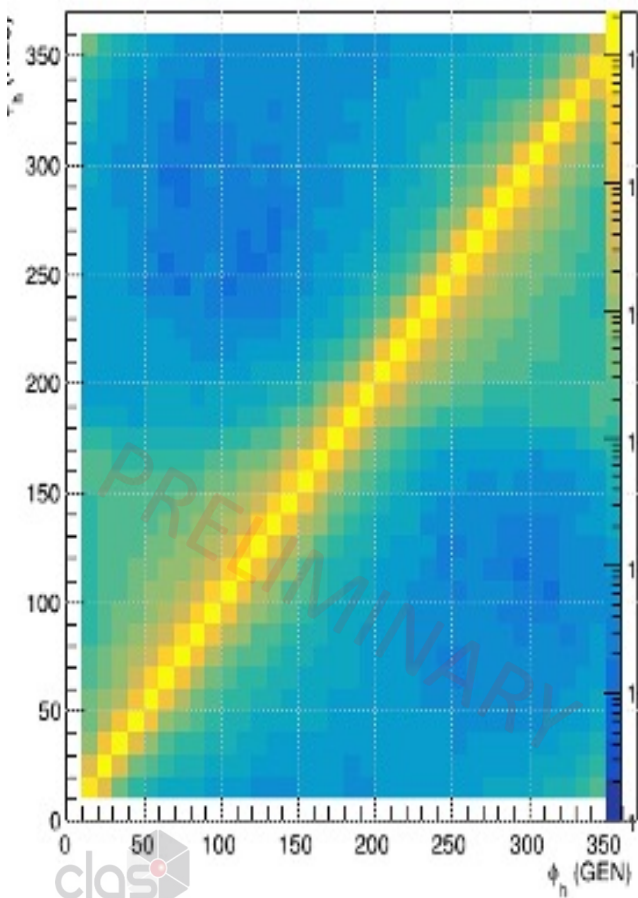


Unfolded Distribution of Q^2

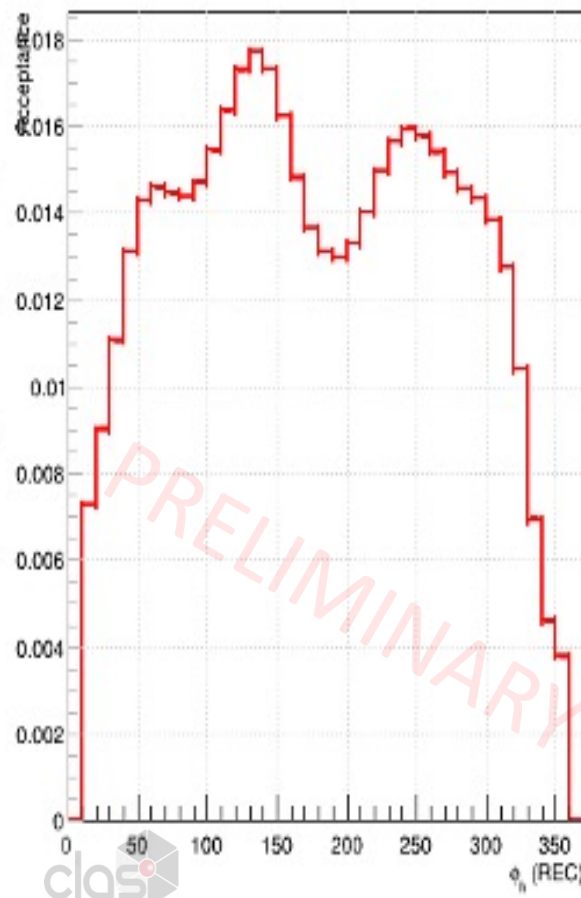


Example of Unfolding (ϕ_h)

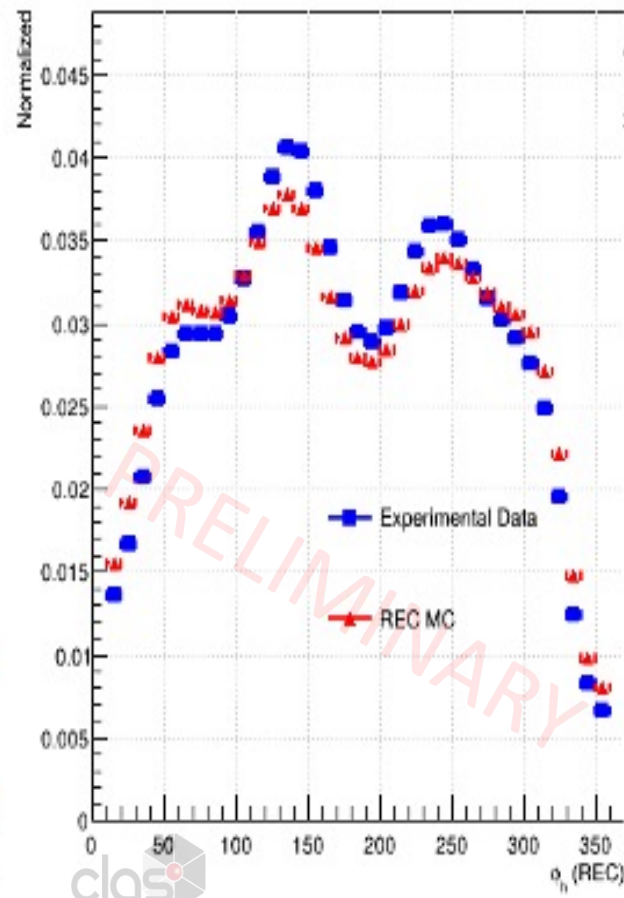
Response Matrix of ϕ_h



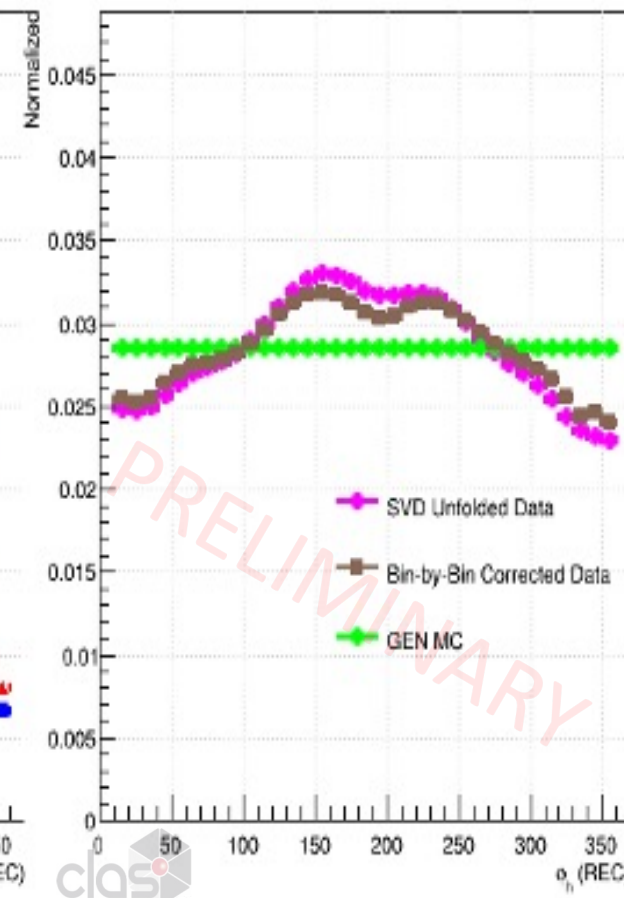
Acceptance Correction of ϕ_h



Reconstructed Distribution of ϕ_h



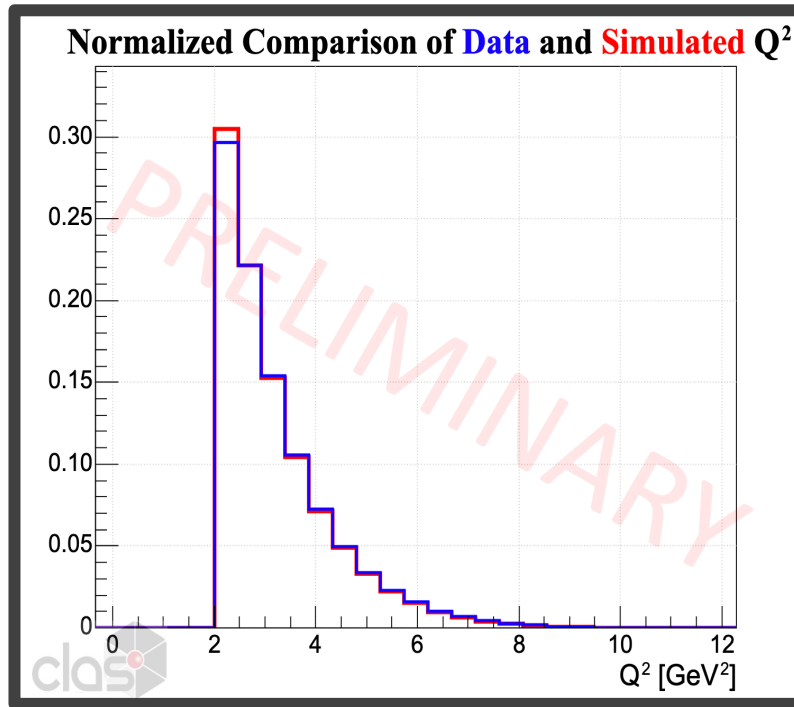
Unfolded Distribution of ϕ_h



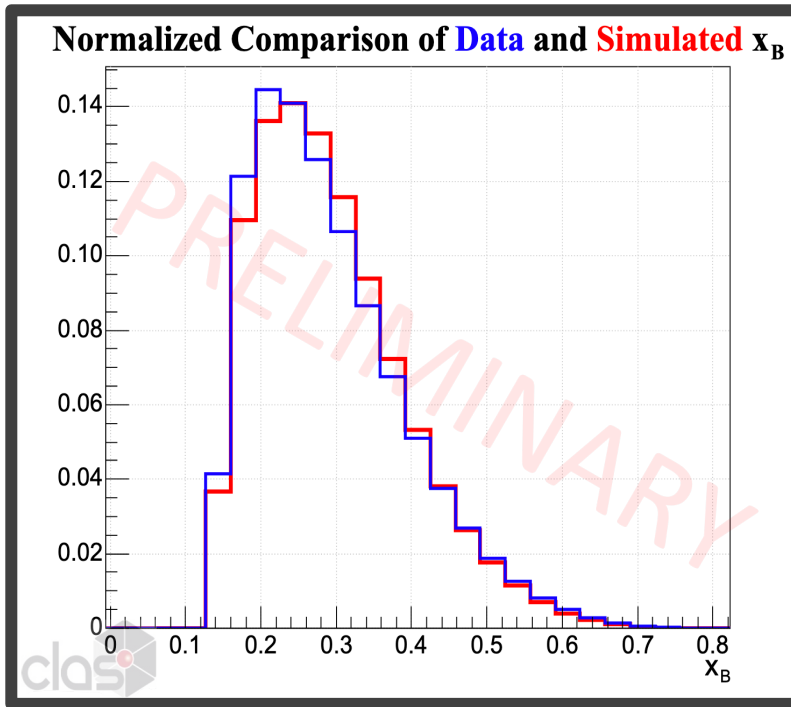
Kinematic Binning and Data-MC Comparison

Other Comparisons

All Events



Q^2 Comparison



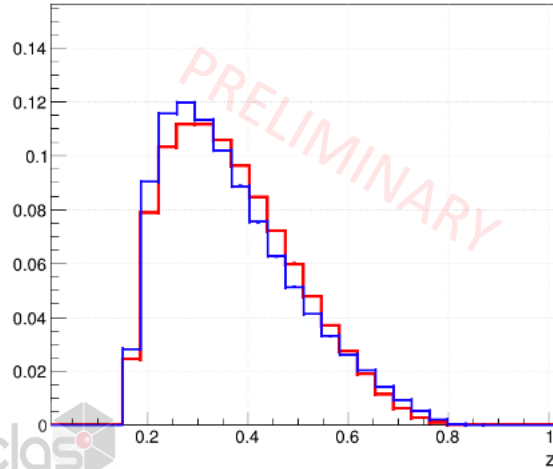
x_B Comparison

Kinematic Binning and Data-MC Comparison

Other Comparisons

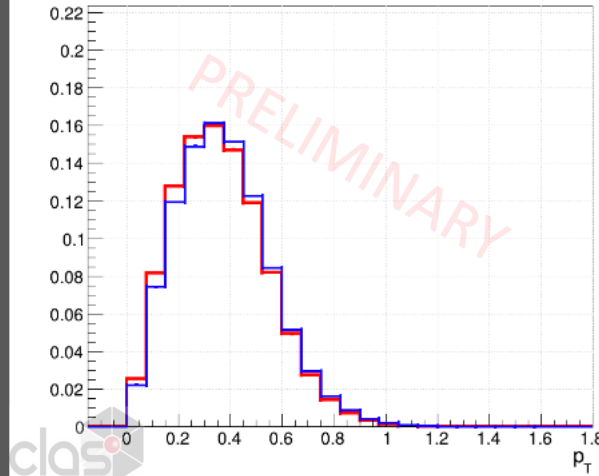
All Events

Normalized Comparison of Real and Simulated z



z Comparison

Normalized Comparison of Real and Simulated p_T

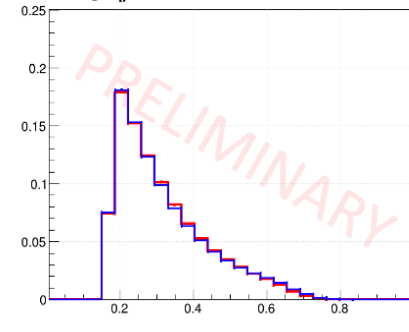


p_T Comparison

Q^2-x_B Bin 1

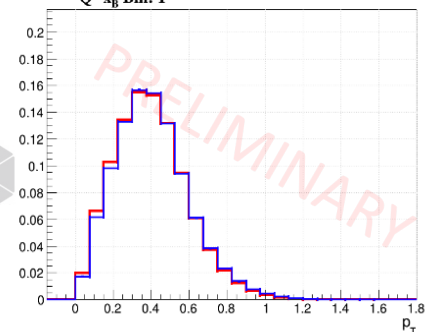
z Comparison

Normalized Comparison of Real and Simulated z
 Q^2-x_B Bin: 1



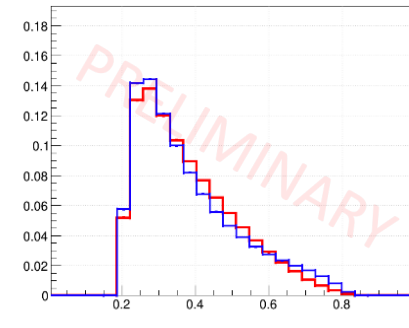
p_T Comparison

Normalized Comparison of Real and Simulated p_T
 Q^2-x_B Bin: 1

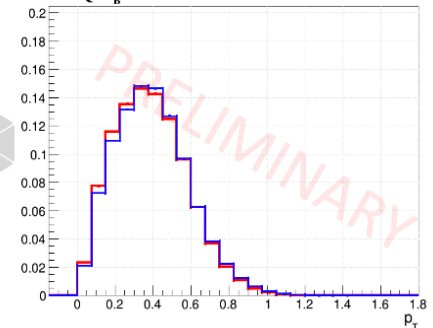


Q^2-x_B Bin 2

Normalized Comparison of Real and Simulated z
 Q^2-x_B Bin: 2



Normalized Comparison of Real and Simulated p_T
 Q^2-x_B Bin: 2



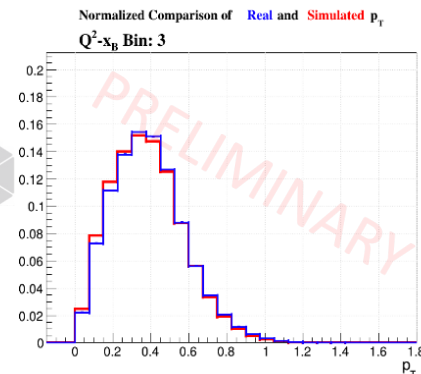
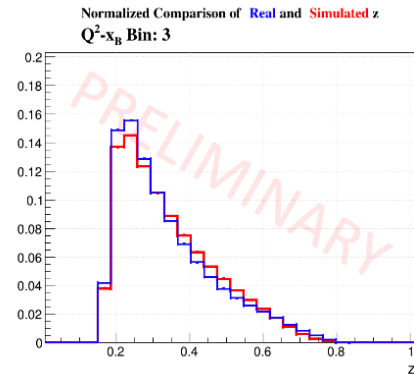
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Other Comparisons

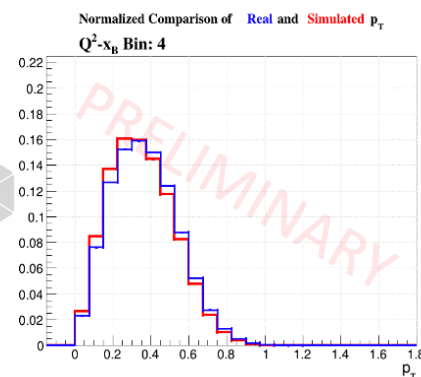
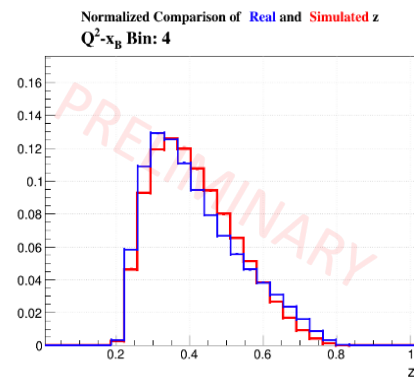
z Comparison

P_T Comparison

Q^2-x_B
Bin 3



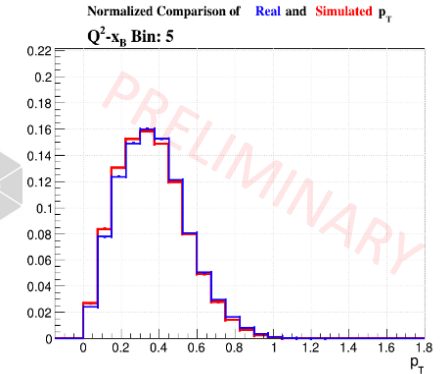
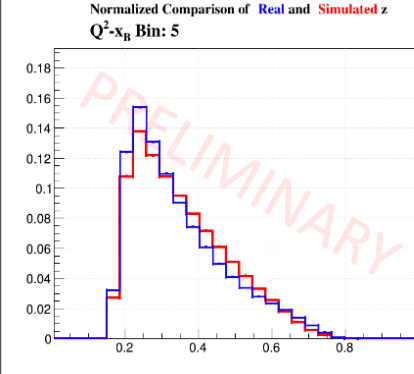
Q^2-x_B
Bin 4



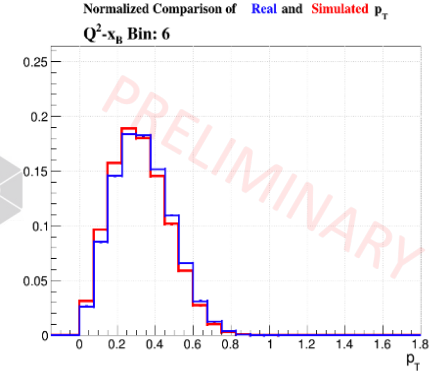
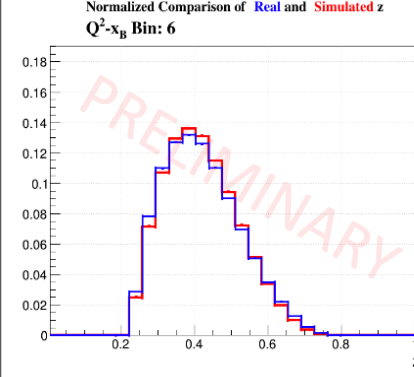
Q^2-x_B
Bin 5

z Comparison

P_T Comparison



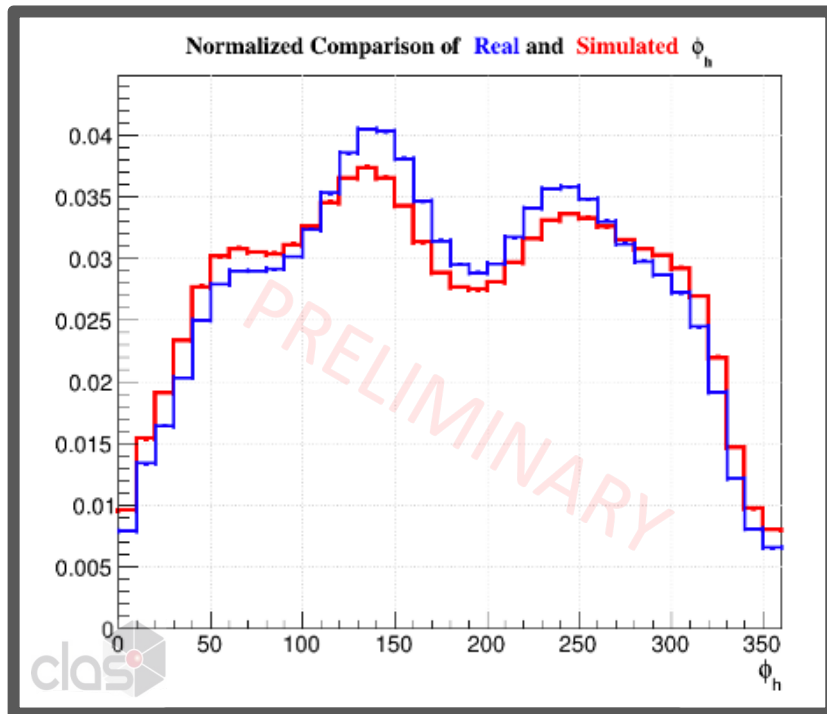
Q^2-x_B
Bin 6



Kinematic Binning and Data-MC Comparison

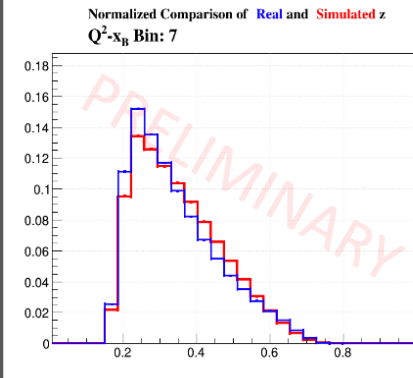
Other Comparisons

All Events



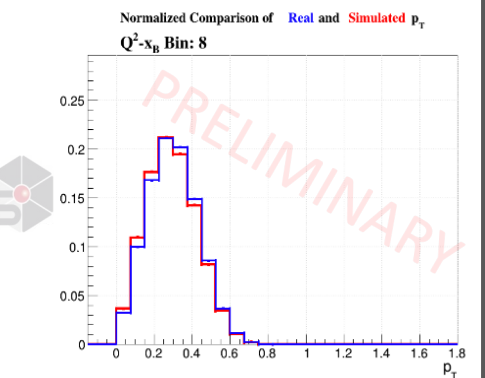
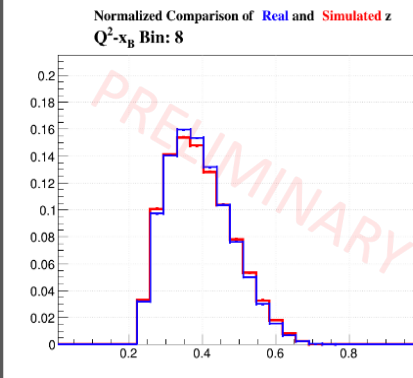
z Comparison

Q^2-x_B
Bin 7



P_T Comparison

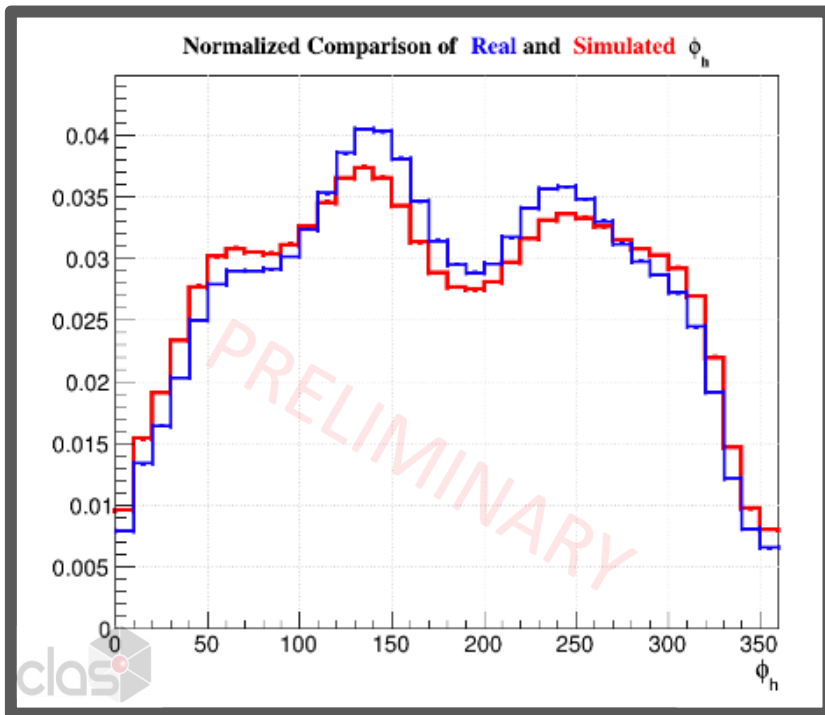
Q^2-x_B
Bin 8



Kinematic Binning and Data-MC Comparison

Other Comparison

All Events



ϕ_h Comparison

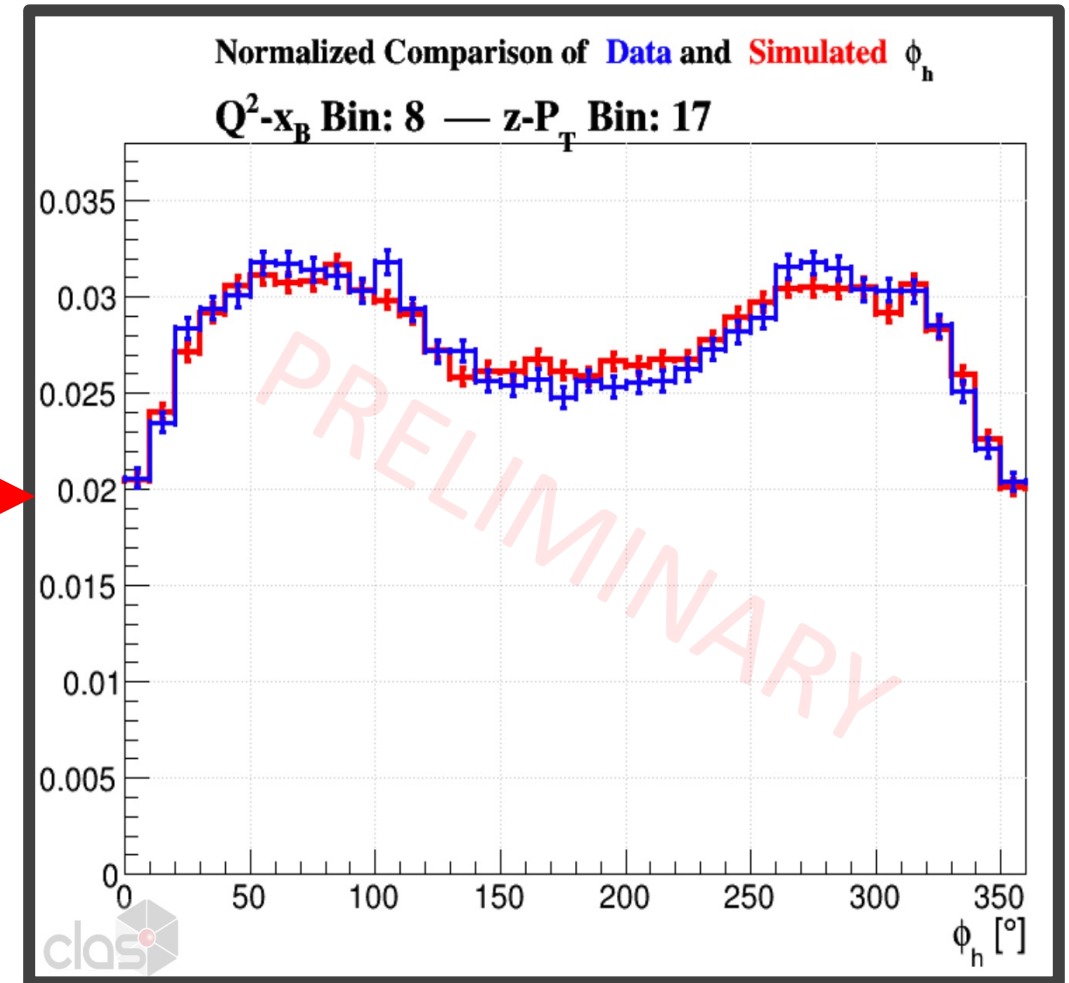
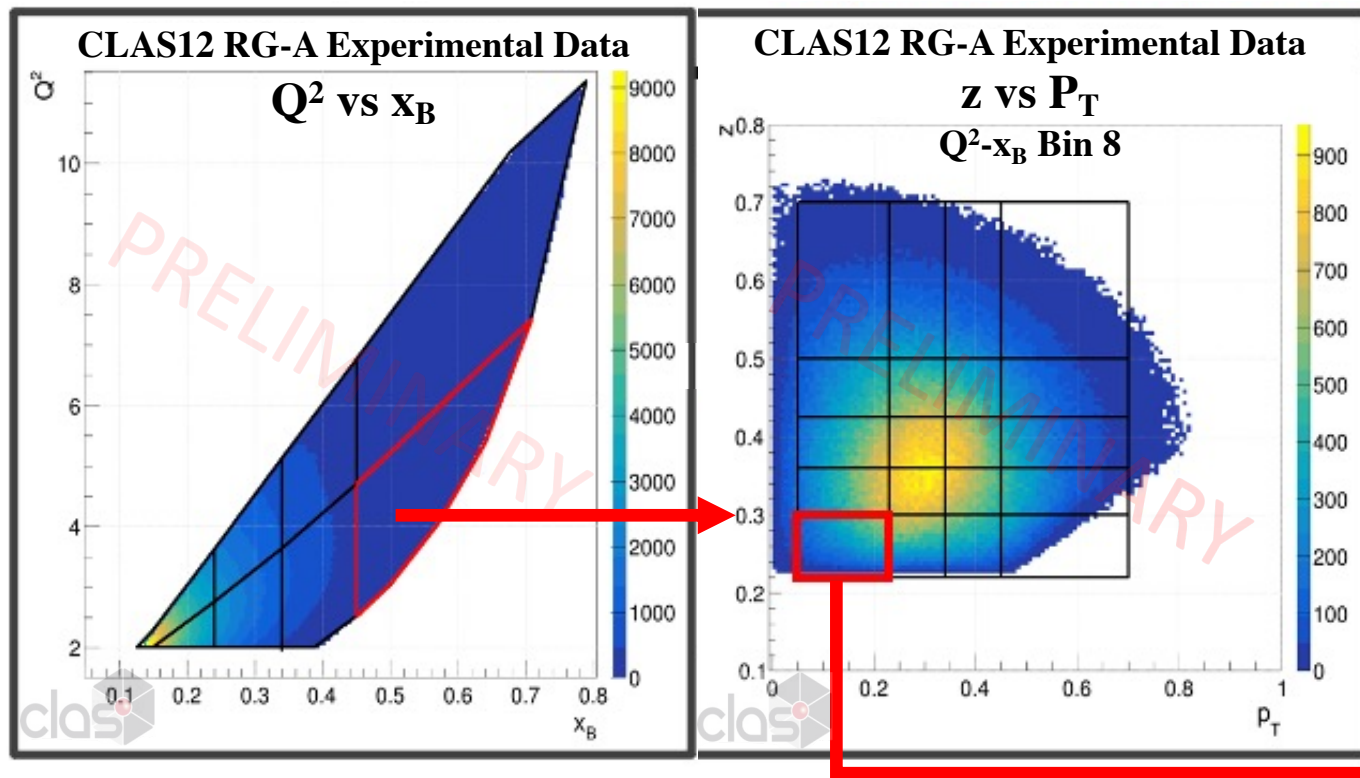
- Some differences between the ϕ_h distributions are expected
- **Reason:** The Monte Carlo Simulation is not initialized with any ϕ_h modulations yet
 - i.e., the ϕ_h distribution is completely flat before reconstruction
- Initial calculations of the $\cos\phi$ and $\cos 2\phi$ moments will be used to 'update' the simulation in an iterative fashion

Multidimensional Analysis Procedures

Multidimensional Kinematic Binning (5 Dimensions)

8 Q^2 - x_B Bins Total – 20-49 z - P_T Bins (per Q^2 - x_B bin)

ϕ_h distribution for the Q^2 - x_B - z - P_T bin shown in red



EXTRA EXAMPLE