

Parton-hadron duality at high Q^2

Simona Malace

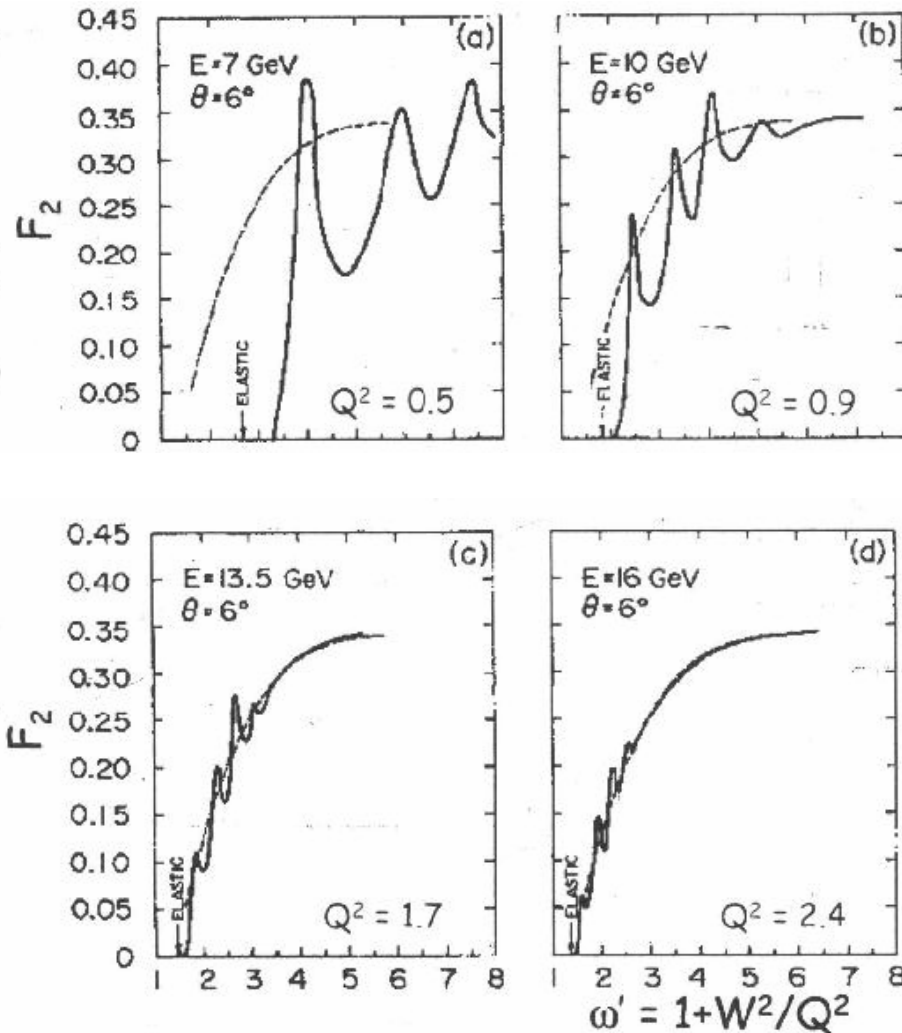
Hampton University/Bucharest University

Hall C Workshop, January 5-7, 2006

Outline

- ◆ **Quark-hadron duality**
- ◆ **Physics motivation for E00-116**
- ◆ **Analysis status for E00-116**
- ◆ **F_2^p and F_2^d at high x from E00-116 data**

Bloom-Gilman duality



'70- Bloom and Gilman observed that the prominent **resonances** in e-p scattering **do not disappear with increasing Q^2** relative to the “background” under them **but follow the DIS scaling limit curve** falling at roughly the same rate as any “background”.



Finite energy sum rule:

$$\frac{2M}{Q^2} \int_0^{\nu_m} \nu W_2(\nu, Q^2) d\nu = \int_1^{(2M\nu_m + m^2)/Q^2} \nu W_2(\omega') d\omega'$$

'76- A QCD based explanation by de Rujula Georgi and Politzer: in the **resonance regime** the **higher twist** effects are **small or cancel** → **duality**

Duality in the F_2 Structure Function

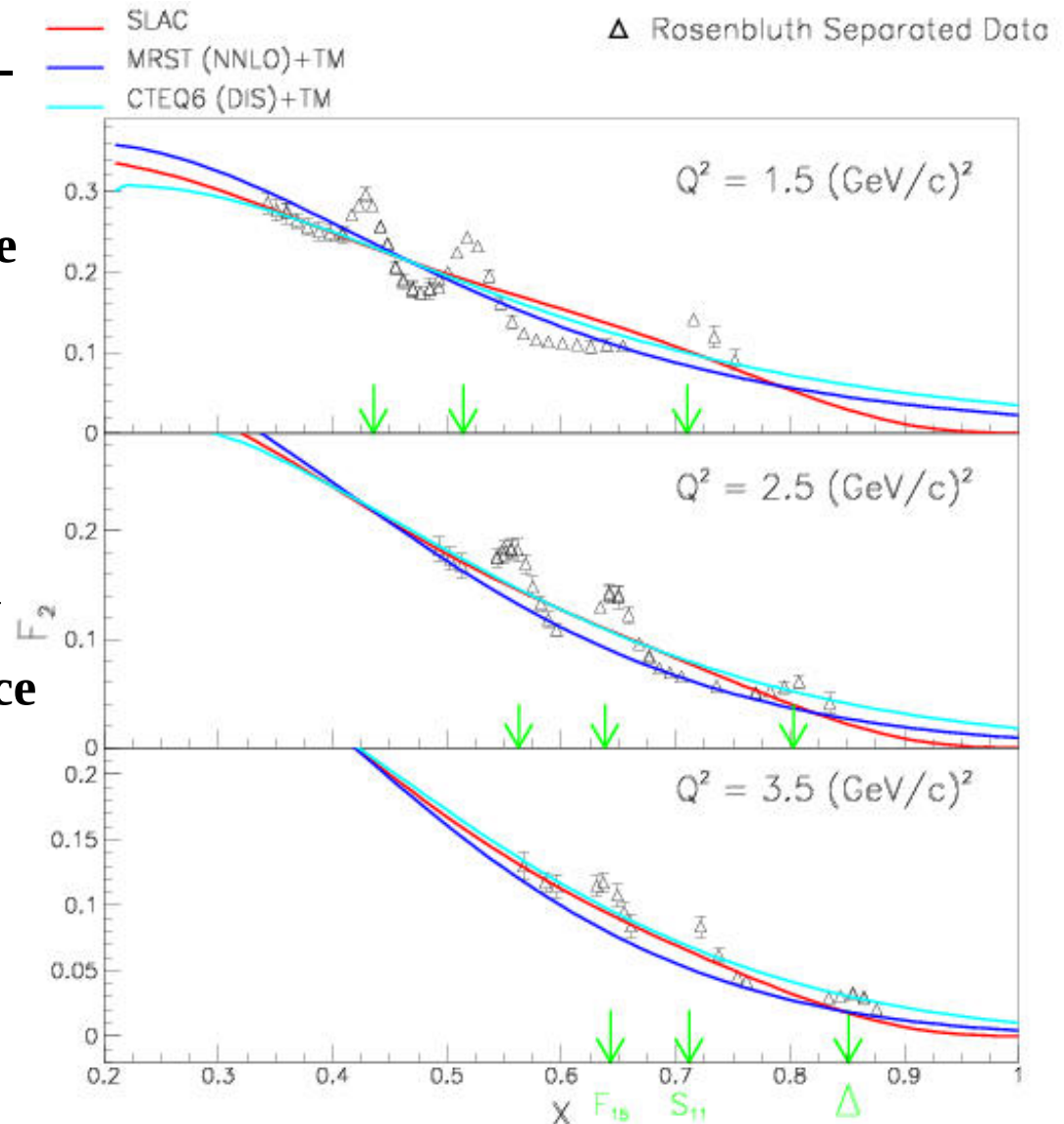
Use **Bjorken x** instead of Bloom-Gilman's ω'

Empirically, DIS region is where logarithmic scaling is observed: $Q^2 > 5 \text{ GeV}^2$, $W^2 > 4 \text{ GeV}^2$

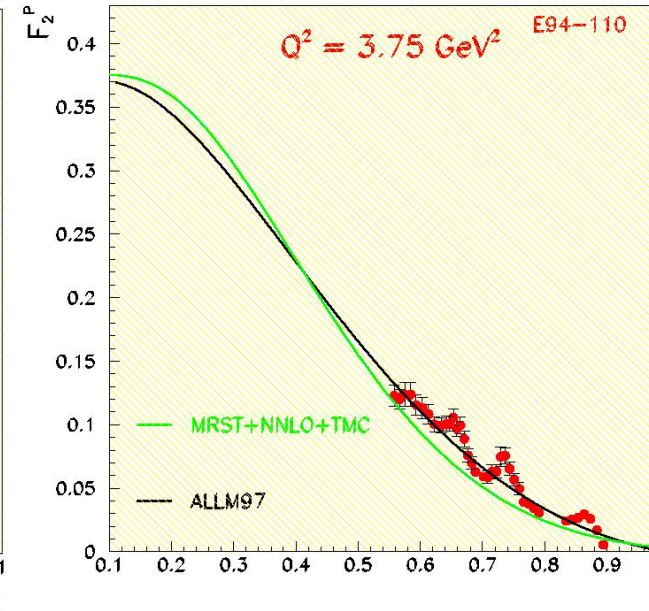
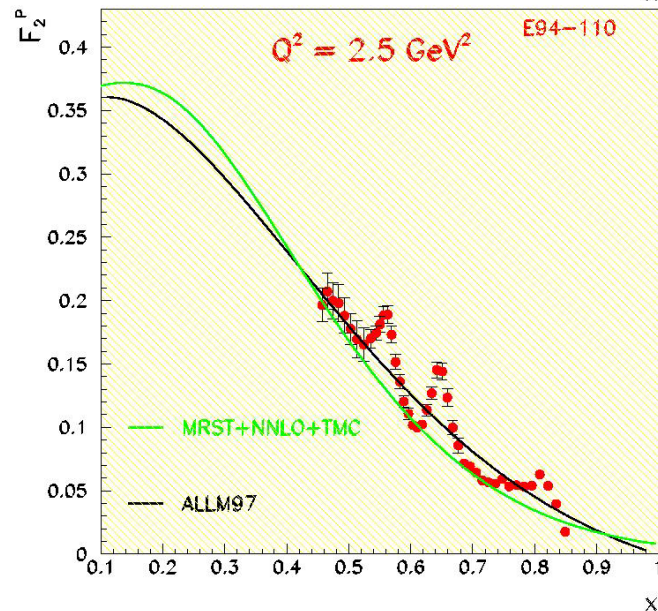
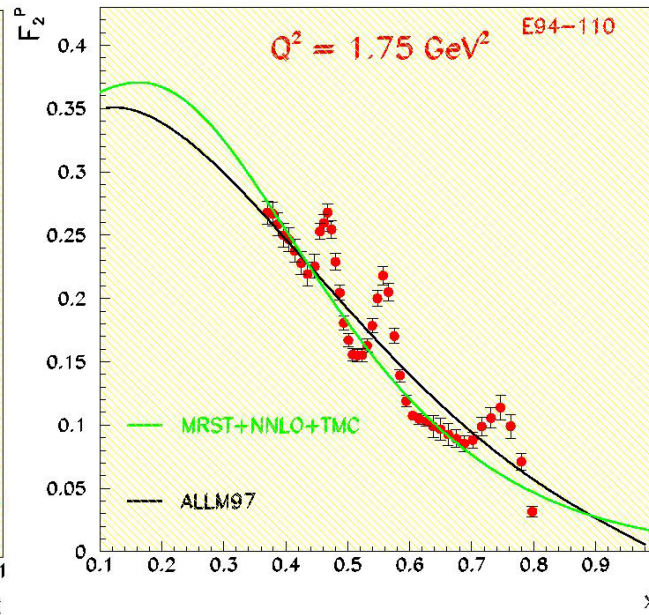
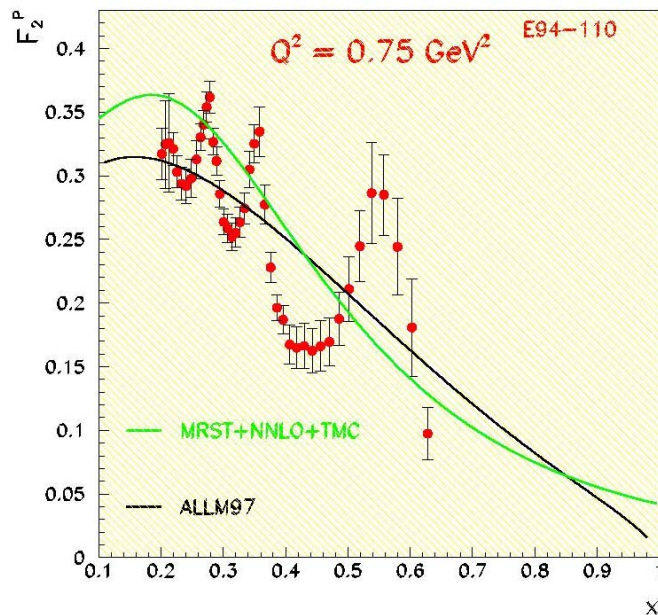
Duality: Averaged over W , logarithmic scaling observed to work also for $Q^2 > 0.5 \text{ GeV}^2$, $W^2 < 4 \text{ GeV}^2$, resonance regime

(note: $x = Q^2/(W^2 - M^2 + Q^2)$)

JLab results: Works quantitatively to better than 10% at surprisingly low Q^2



E94-110 Rosenbluth separated data



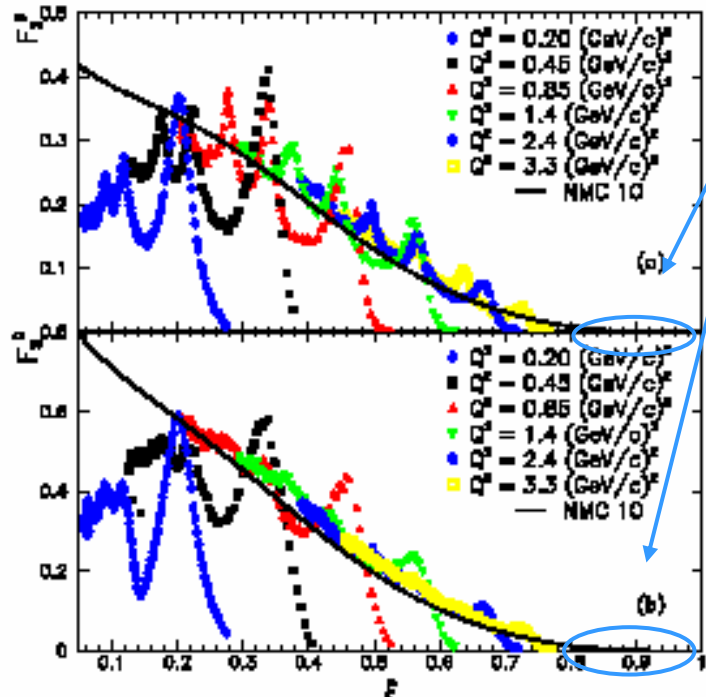
With increasing Q^2 the resonances slide towards higher x on ALLM97 curve while pdf curve MRST+NNLO+TMC starts undershooting the data.

Higher Q^2/x data needed to get more information ...

E00-116 physics motivation

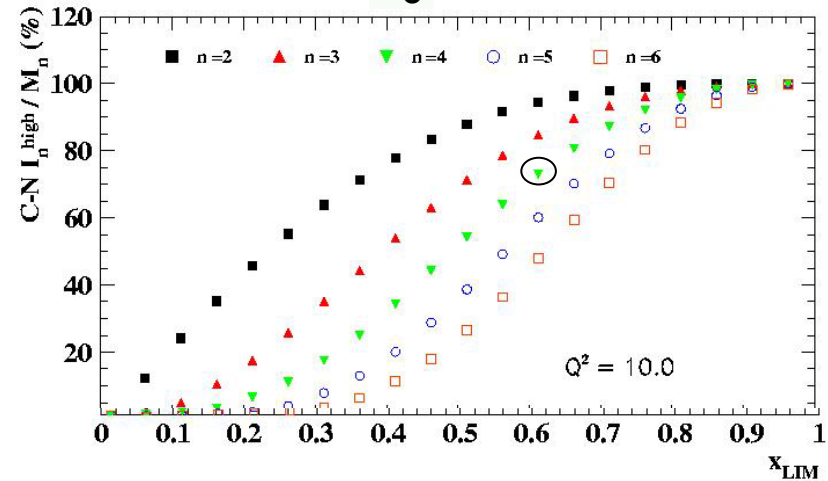
resonance data

high x

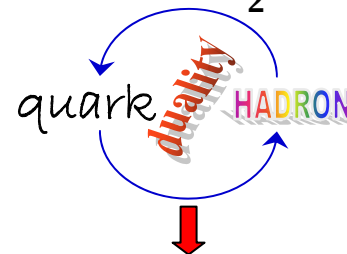


✚ Constrain higher moments

$$M_n(Q^2) = \int_0^1 dx \, x^{n-2} F(x, Q^2)$$

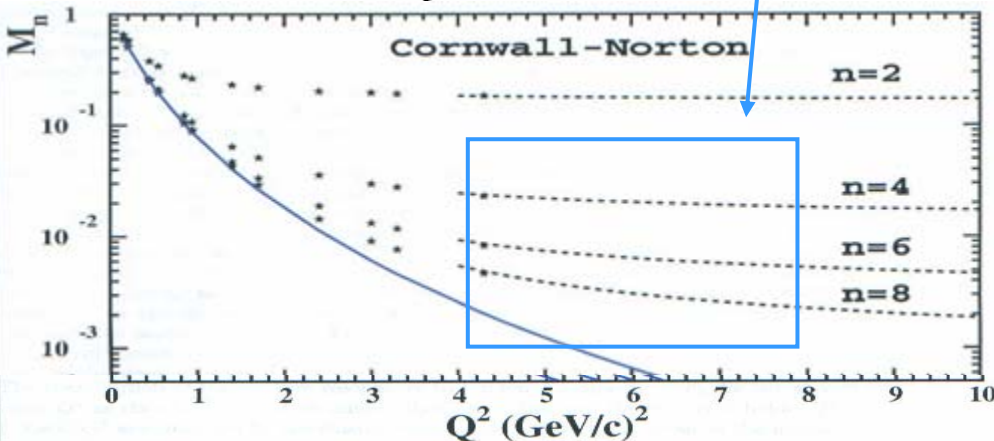


✚ Higher twist extraction
from both H₂ and D₂ data



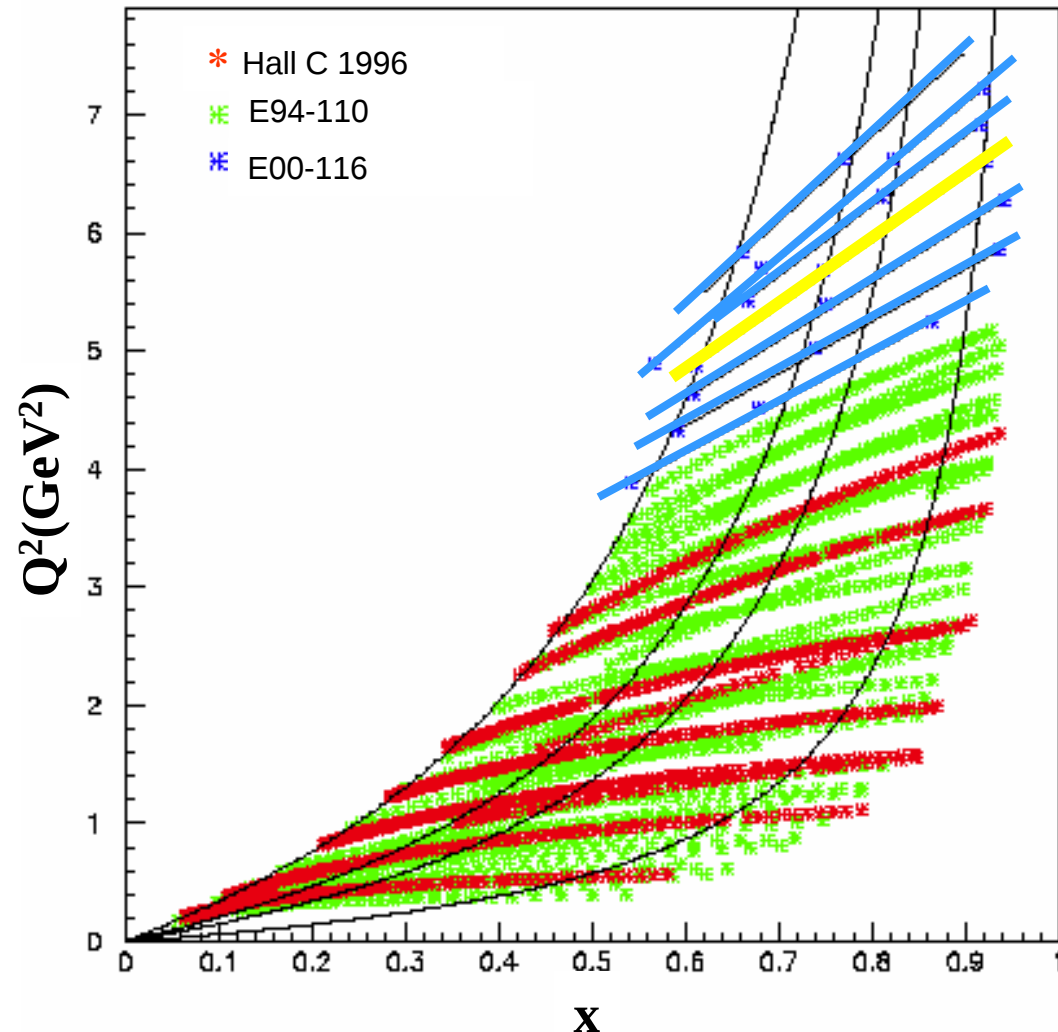
✚ High x pdf evolution

✚ F_2^d / F_2^p ratio at large x



E00-116 kinematics

$W^2=4$
 $W^2=2.82$
 $W^2=2.36$
 $W^2=1.52$



$$37.93^\circ \begin{cases} Q^2 \in (3.88 - 5.25) \\ x \in (0.54 - 0.87) \end{cases}$$

$$41^\circ \begin{cases} Q^2 \in (4.32 - 5.85) \\ x \in (0.59 - 0.94) \end{cases}$$

$$45^\circ \begin{cases} Q^2 \in (4.63 - 6.27) \\ x \in (0.61 - 0.94) \end{cases}$$

$$50^\circ \begin{cases} Q^2 \in (4.88 - 6.59) \\ x \in (0.61 - 0.92) \end{cases}$$

$$55^\circ \begin{cases} Q^2 \in (5.43 - 6.91) \\ x \in (0.67 - 0.92) \end{cases}$$

$$60^\circ \begin{cases} Q^2 \in (4.89 - 7.21) \\ x \in (0.56 - 0.92) \end{cases}$$

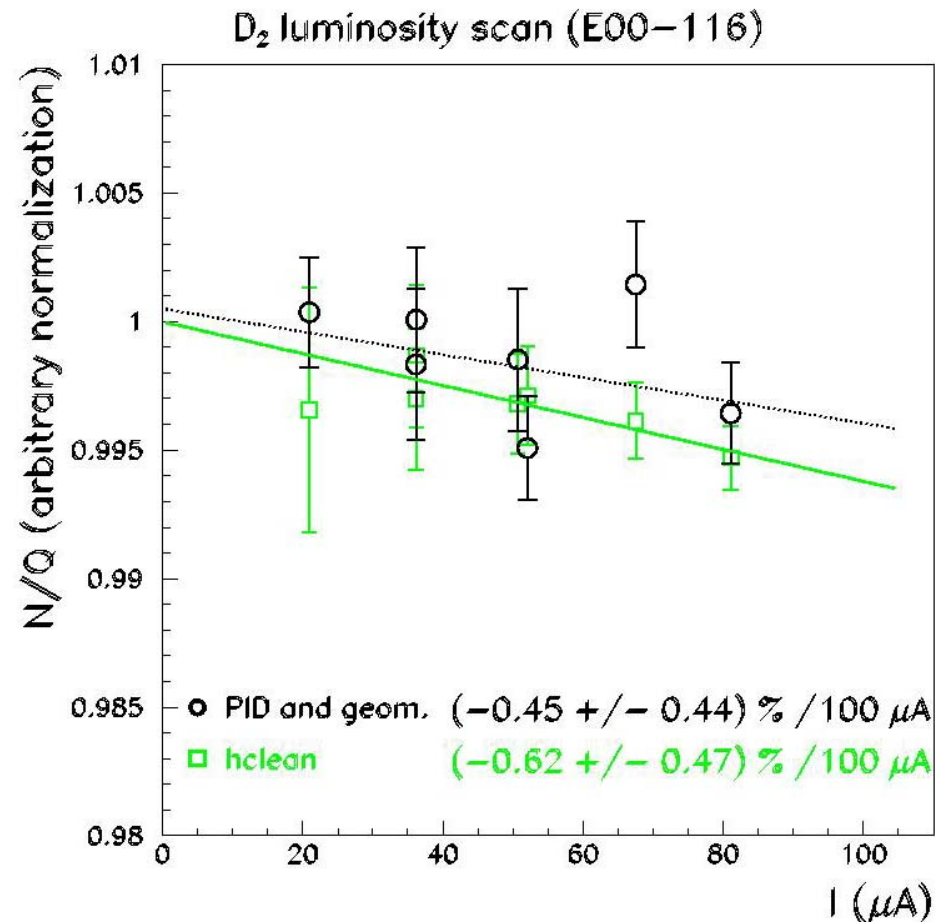
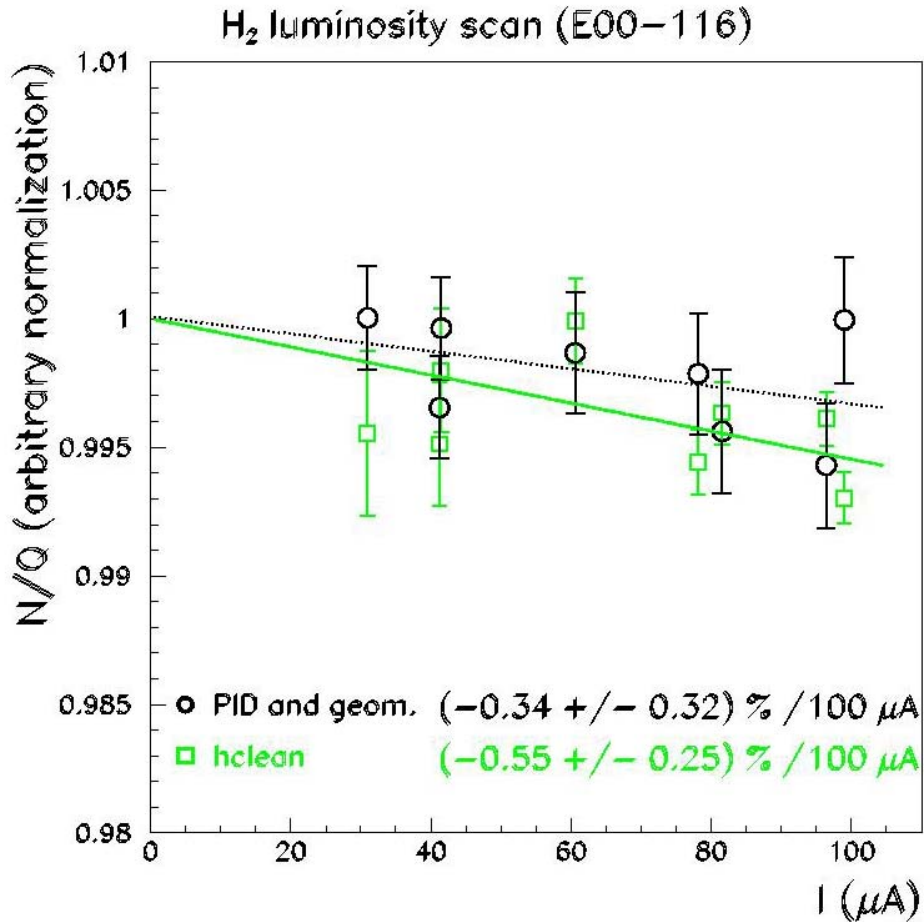
$$70^\circ \begin{cases} Q^2 \in (5.83 - 6.62) \\ x \in (0.66 - 0.77) \end{cases}$$

Analysis status for E00-116

- **Detector calibrations: done**
- **Luminosity studies: done**
- **BCM calibration: done**
- **Detector efficiencies checking: done**
- **Tracking efficiency checking: done**
- **Background estimation:**
 - pion contamination estimation: done**
 - charge symmetric background estimation: done**
- **Radiative corrections: need iteration**
- **Cross section extraction: final/iteration**
- **F_2^p and F_2^d extraction: preliminary**

Luminosity studies

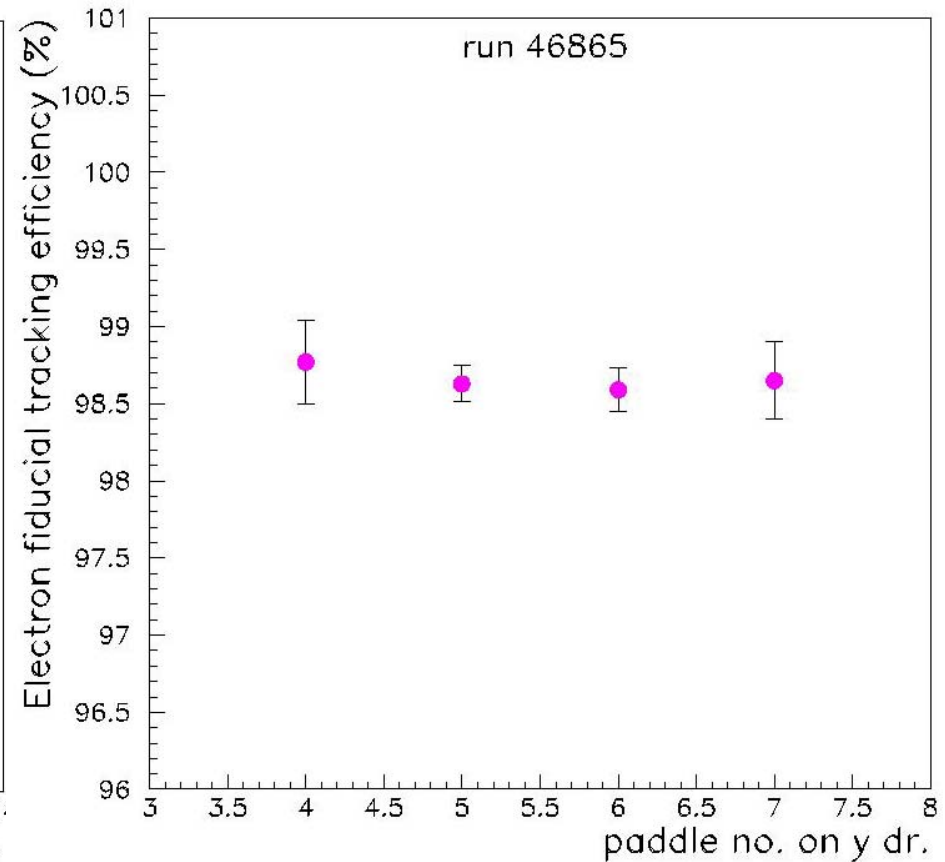
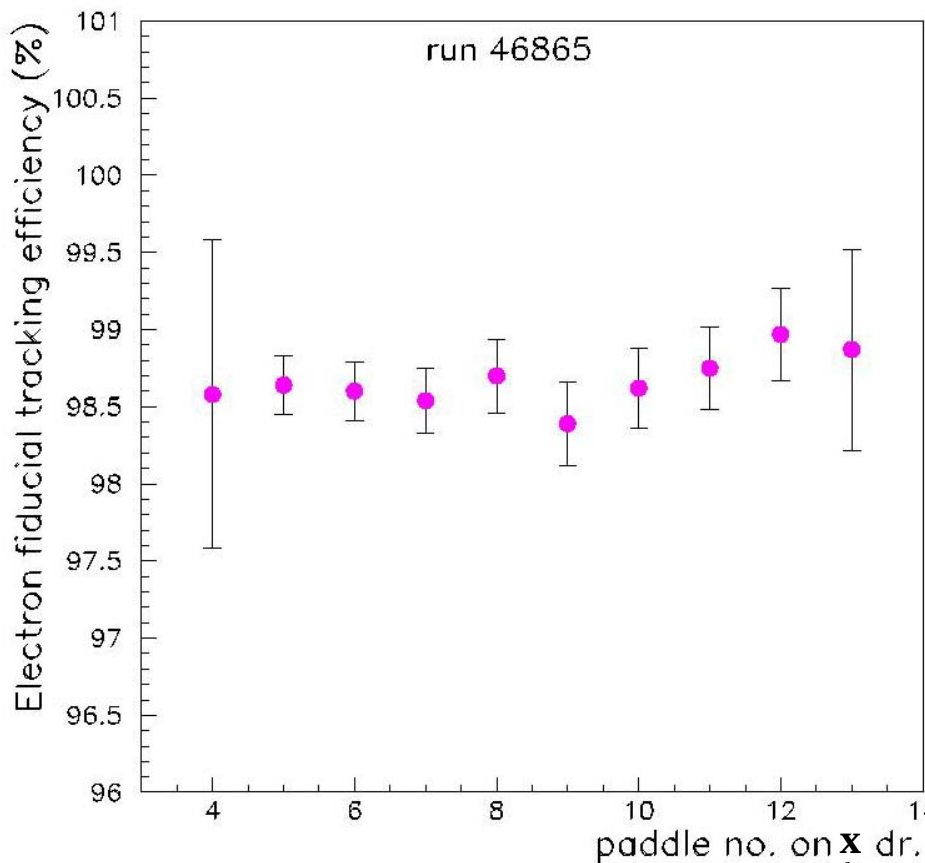
➡ We quantify the boiling effect in the targets with increasing current.



➡ On average, the scaler and tracking based studies reveal about 0.5 % correction with an error of about 0.3 %.

Tracking efficiency checks

- ➡ We are at low rates so we don't worry about the rate dependence of the tracking efficiency.
- ➡ But the tracking efficiency **could** have an angle dependence.



- ➡ We don't see any angle dependence in the tracking efficiency.

Background analysis

➡ Pion contamination:

We are at large angles so the (e, e^-) cross section is typically low.

We are at low momentum so we have high π/e ratio.
The typical PID cuts don't clean up all the pions.

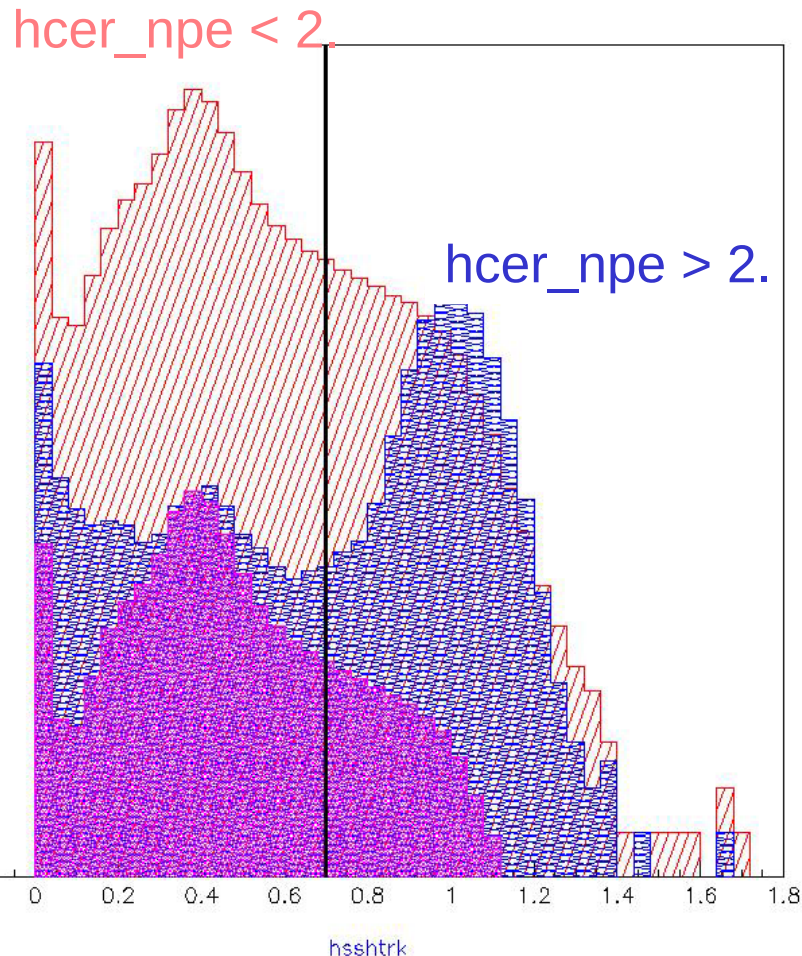
➡ Charge symmetric background:

We used **SOS** for H,D (e, e^+) measurement.

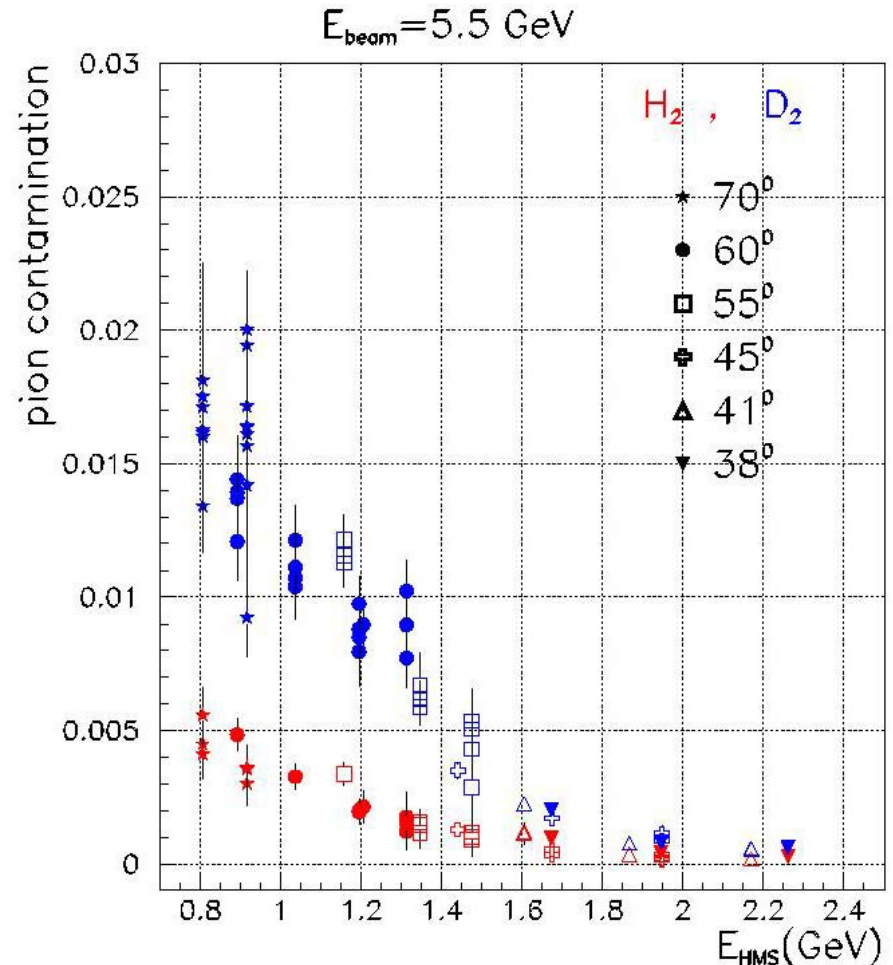
SOS has a larger acceptance than HMS. (e, e^+) cross section is varying strongly as a function of θ and E' .
Therefore we need to disentangle θ and E' dependence in order to do the subtraction.

Pion contamination estimation

- ➡ We assume that for $\text{hcer_npe} < 2$ we have only pions and for $\text{hcer_npe} > 2$ still some pion contamination → we “scale” the pion spectrum to subtract pions.

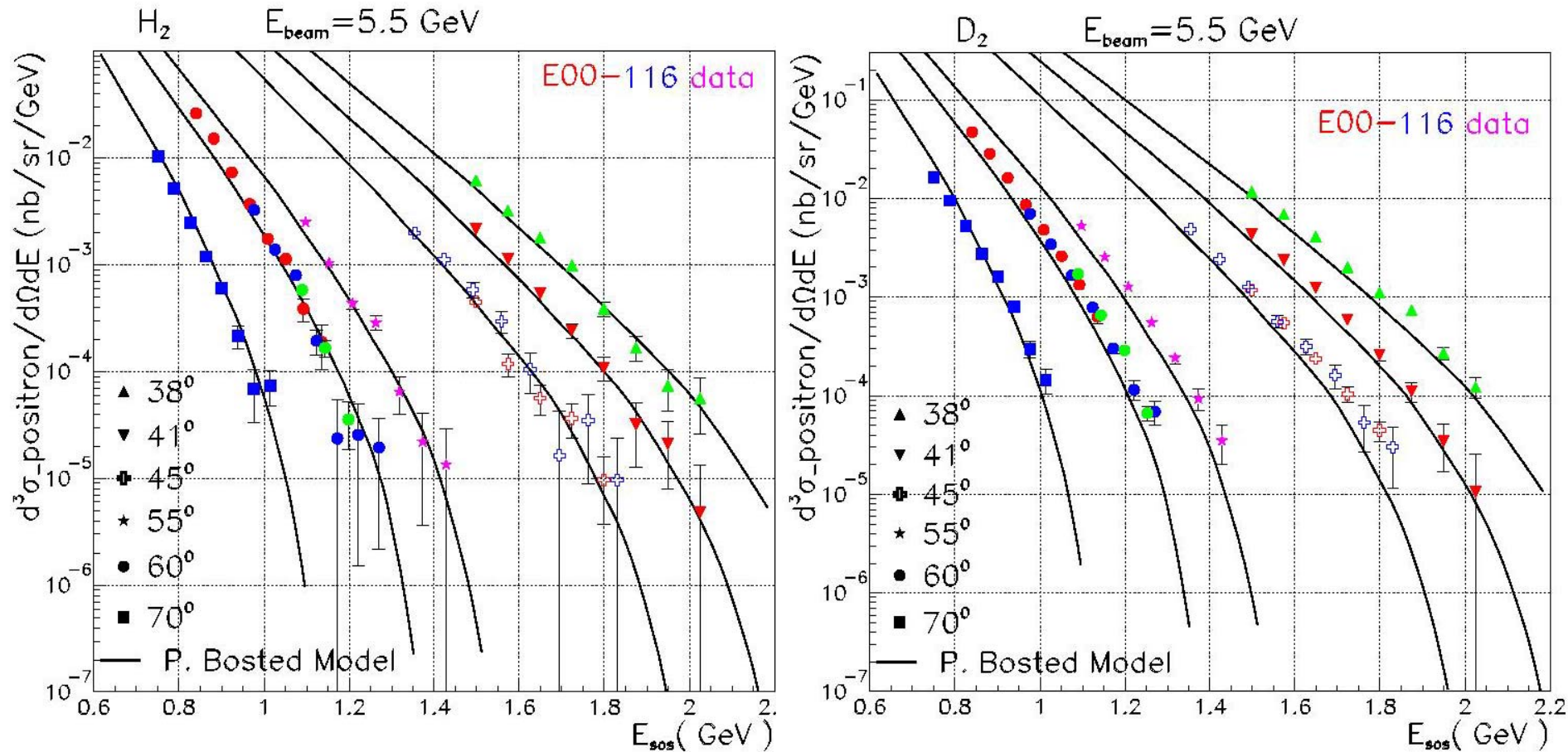


- ➡ The pion contamination is parameterized as a function of momentum and the fit is used for subtraction.



Charge symmetric background estimation

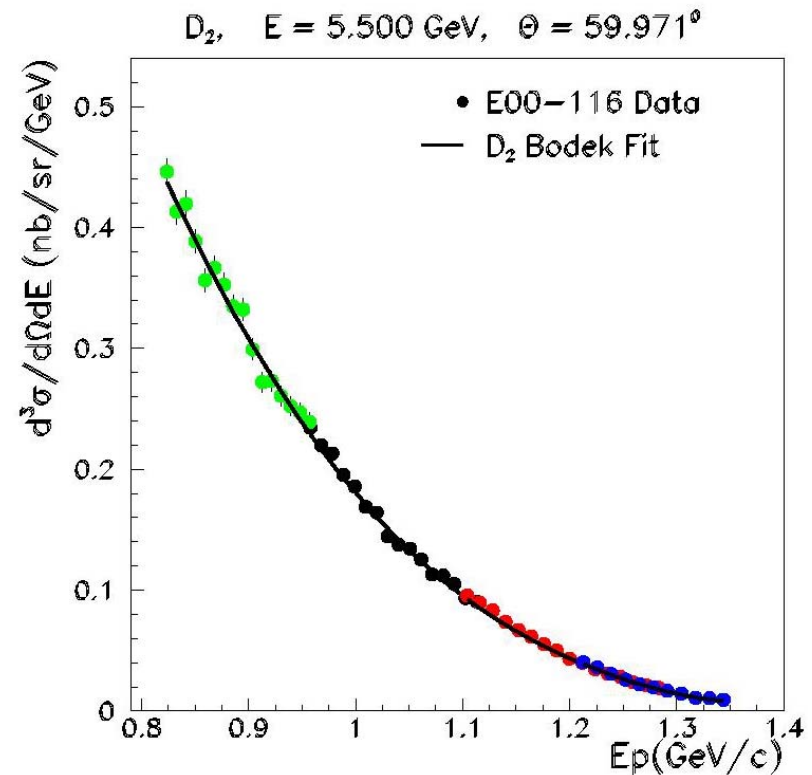
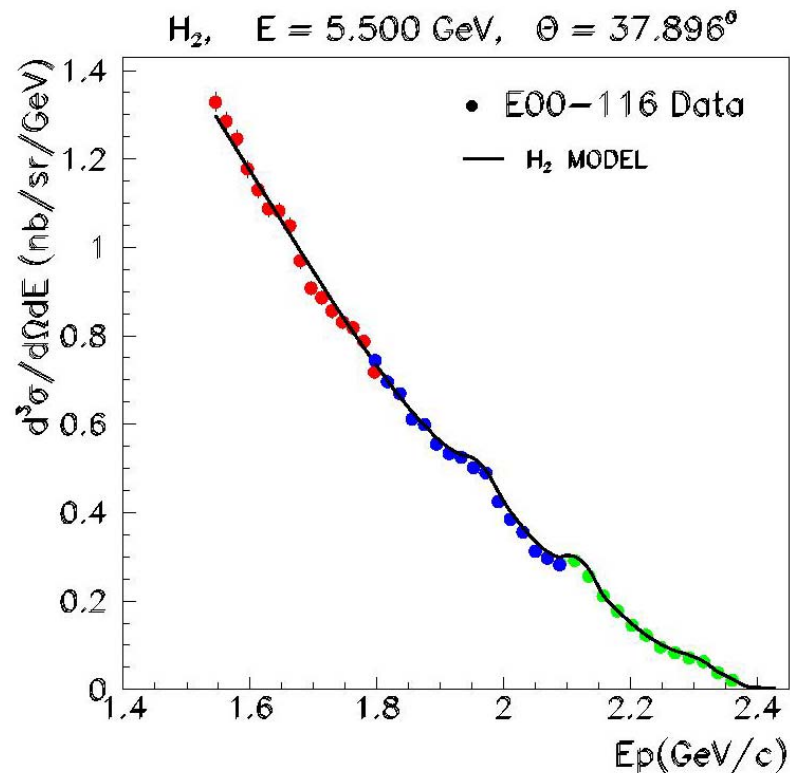
- ➡ For **positron cross section calculation**, spectrometer **acceptance corrections** were applied and **P. Bosted model**(based on **Wiser π^+, π^- production data**) was used for **bin centering correction**.



- ➡ The background was subtracted on a theta/momentum grid.

Cross sections extraction

➡ For H_2 target all corrections are final and two iterations were performed.



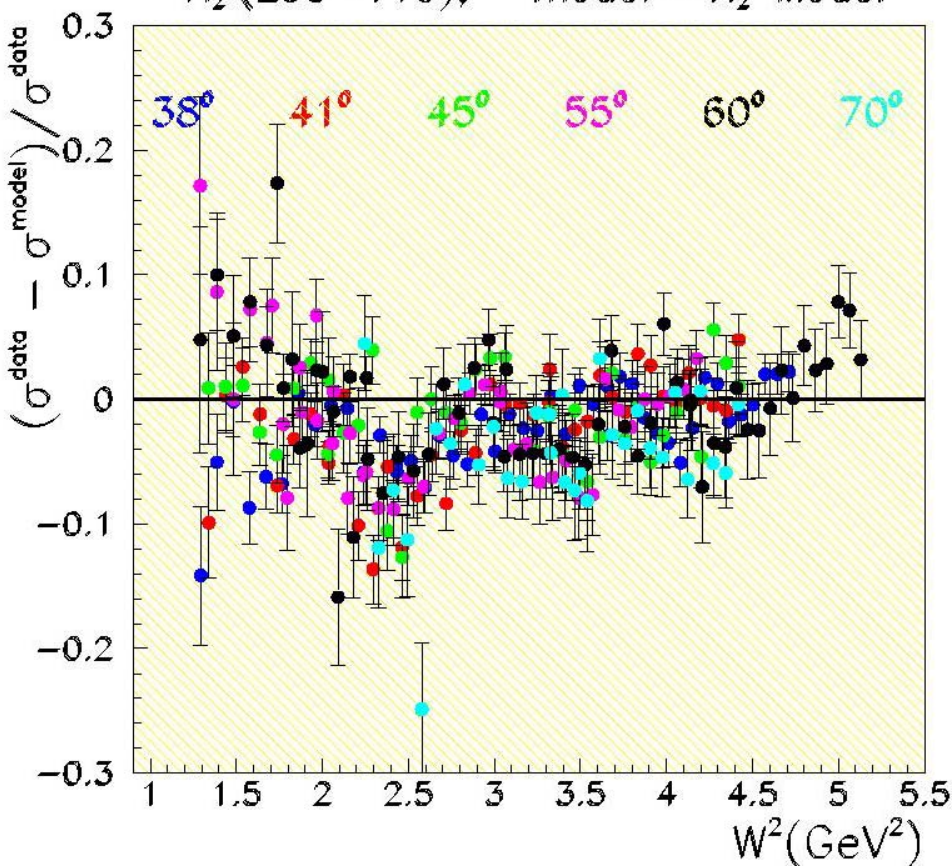
➡ For D_2 target, the born inelastic cross section was obtained by subtracting the radiated elastic and quasielastic contributions and correcting for the radiative effects.

H_2 cross sections

➡ We still need to iterate the radiative corrections.

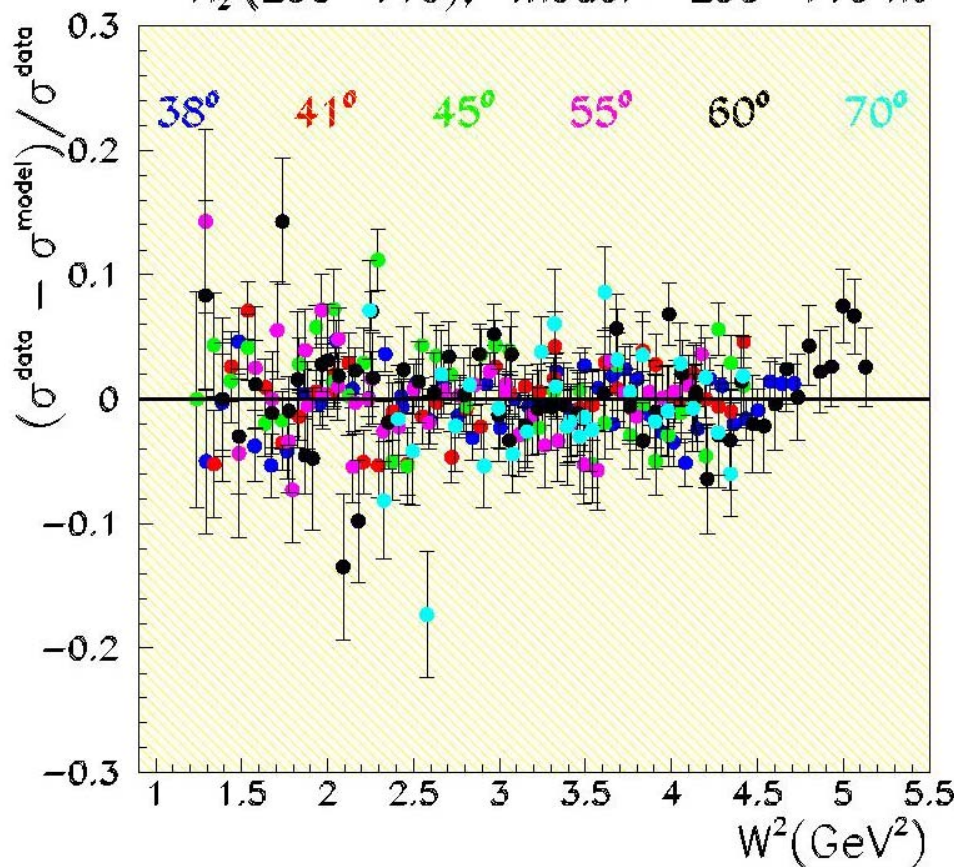
Before iteration

H_2 (E00-116), model = H_2 Model



After two iterations

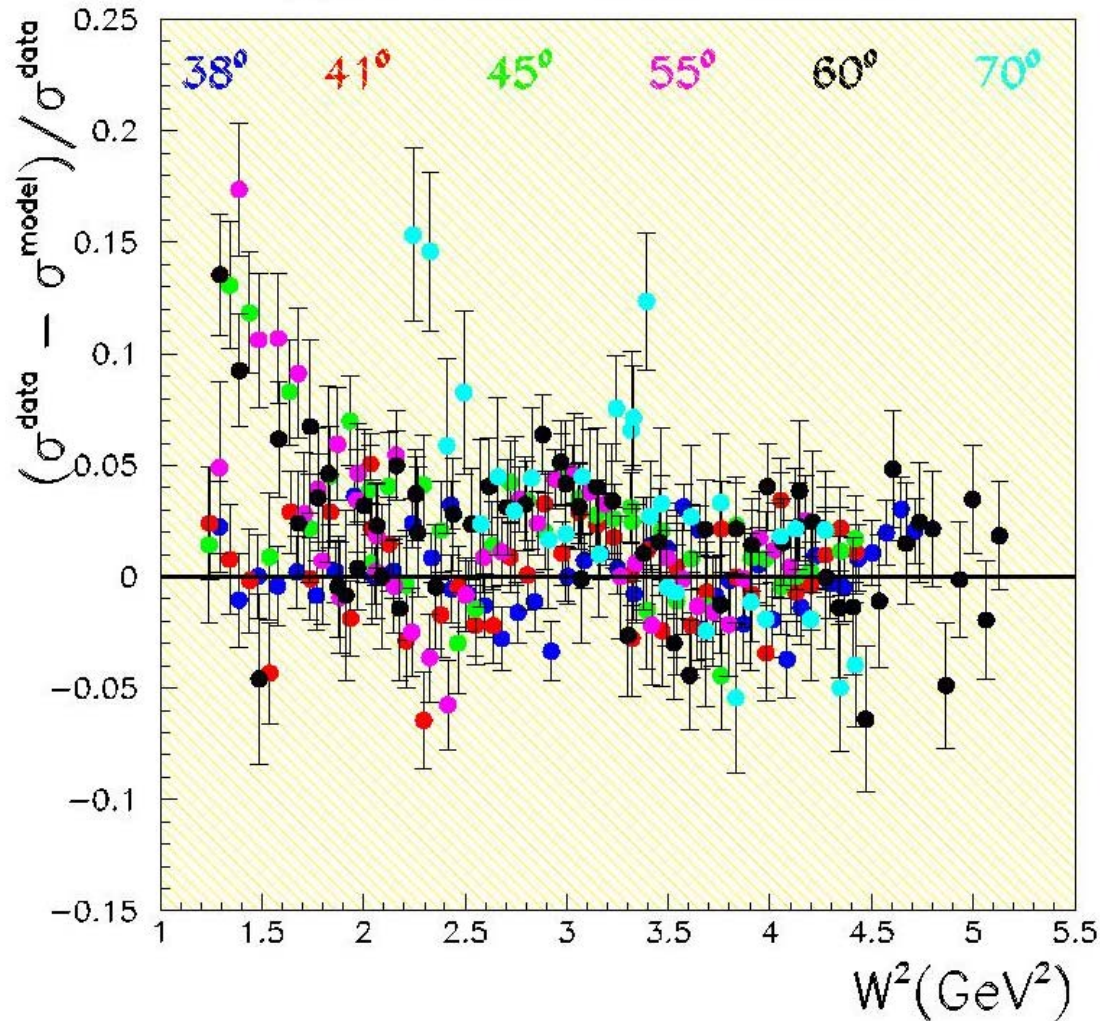
H_2 (E00-116), model = E00-116 fit



➡ The new fit will be used for bin centering and to get radiative corrections.

D_2 cross sections

D_2 (E00-116), model = Bodek fit



- ➡ Up to now no iteration was performed on D_2 data.
- ➡ There seem to be small systematic fluctuations so we will try get a better fit.

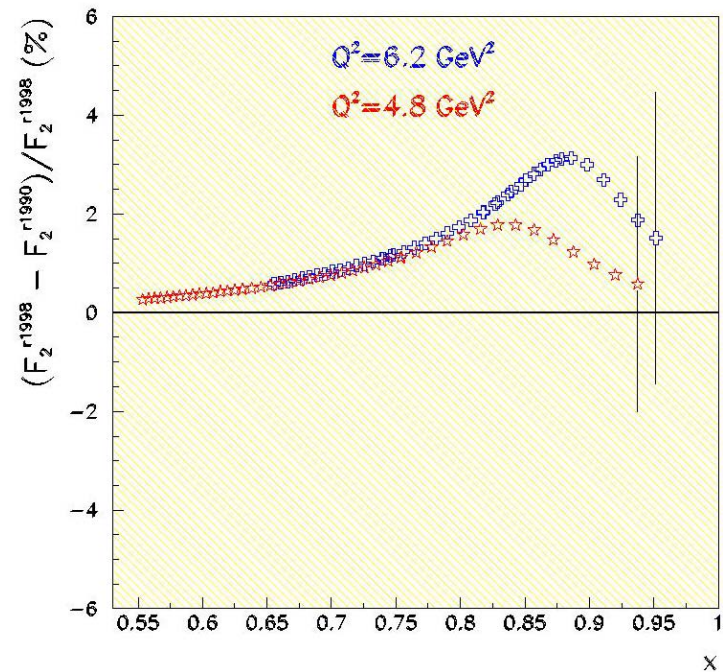
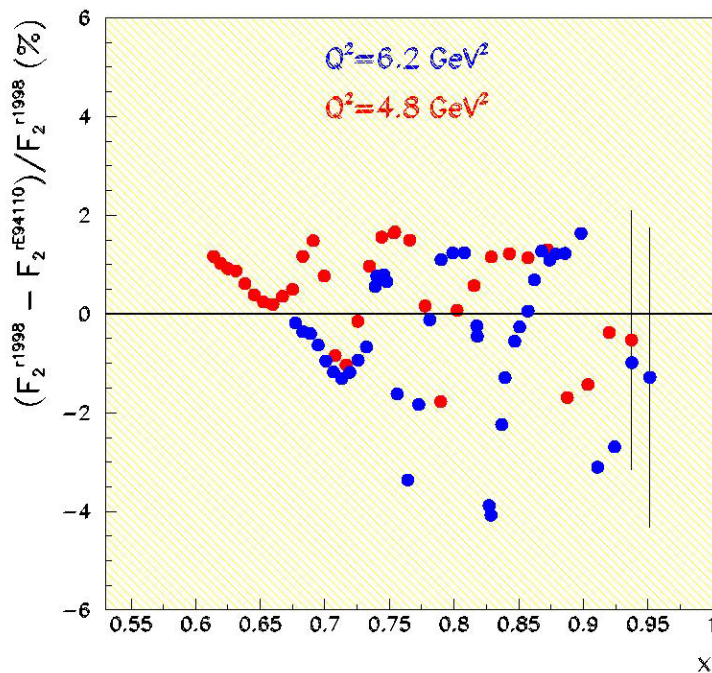
F_2 extraction

$$F_2 = \frac{d^3\sigma}{d\Omega dE'} \frac{1+R}{1+R\varepsilon} \frac{K\nu}{4\pi^2\alpha} \frac{1}{\Gamma} \frac{1}{1+\nu^2/Q^2}$$

➡ E00-116 measures

We wish to construct F_2 but have not measured R .

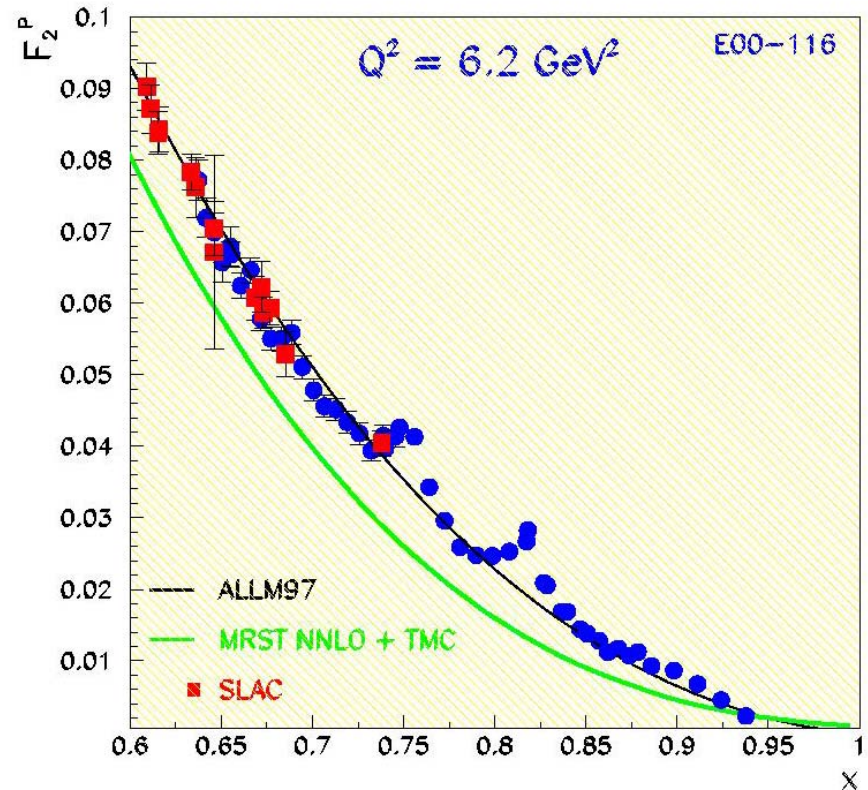
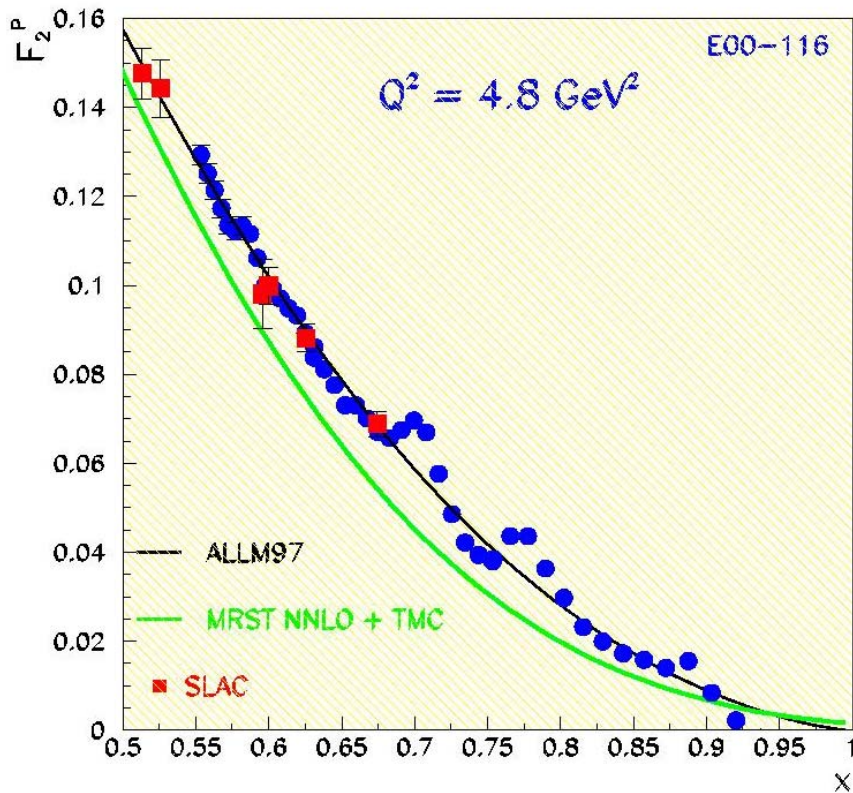
➡ For F_2 extraction R1998 was used.



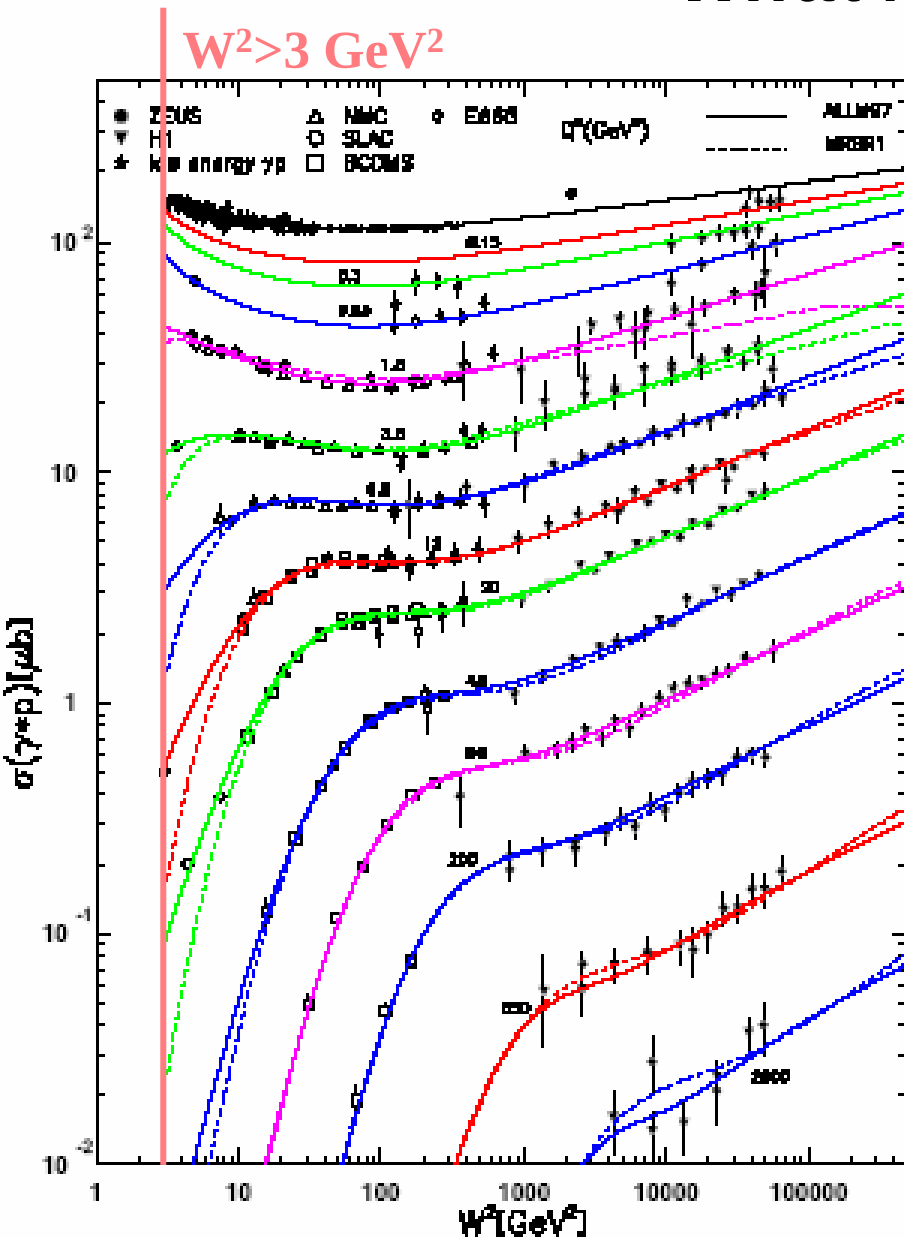
➡ Estimated uncertainty on F_2 originating from the R parameterization used is about 2%.

F_2^p from E00-116 data

- ➡ As observed from E94-110, MRST pdf evolution curve undershoots the data at intermediate Q^2 , high x .
- ➡ ALLM97 fit behaves as a “scaling curve” for the resonance data.



What is ALLM97 ?



ALLM97 (Abramowicz, Levin, Levy, Maor) is a fit to a wide range of γ^*p scattering data (all existing data by 1997) with $W^2 > 3 \text{ GeV}^2$ including also photoproduction data (γp).

The fit form assumed for F_2 is the product of:

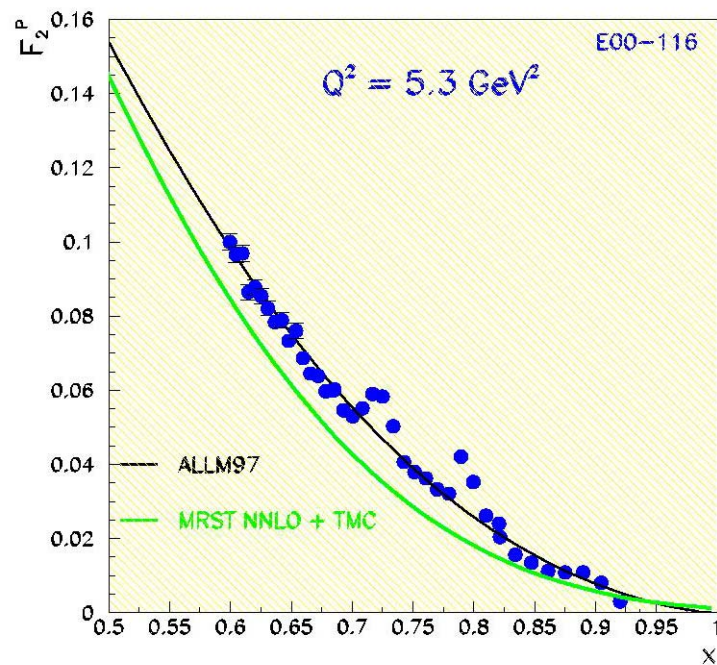
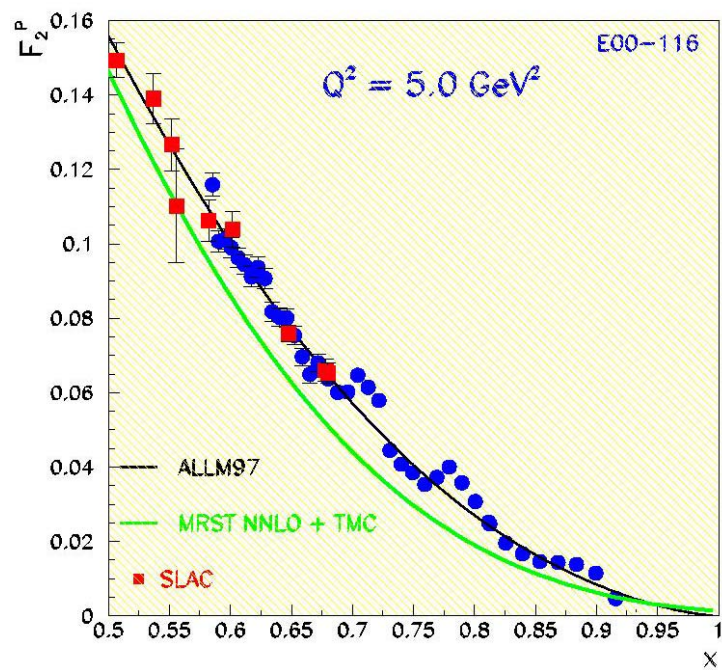
$$\rightarrow Q^2/(Q^2 + m_0^2)$$

$$\rightarrow c_{P,R}(t) * x_{P,R}^{a_{P,R}(t)} * (1-x)^{b_{P,R}(t)}$$

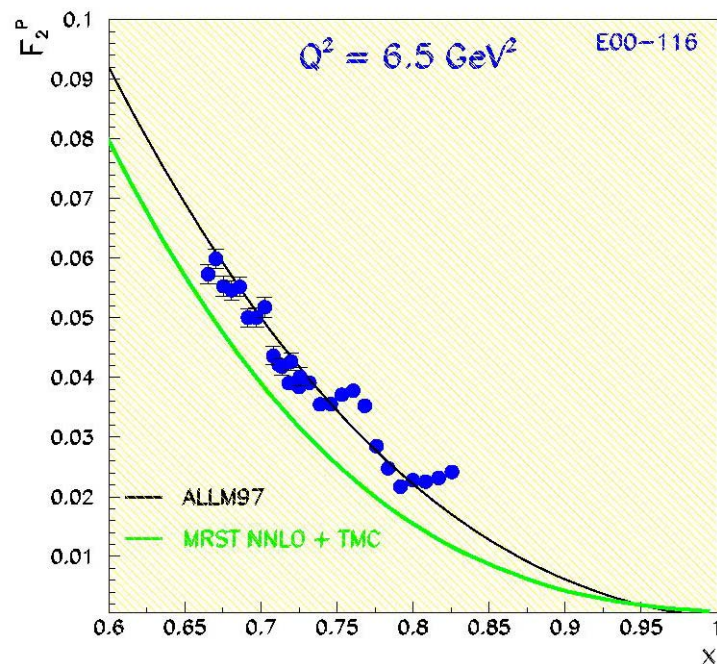
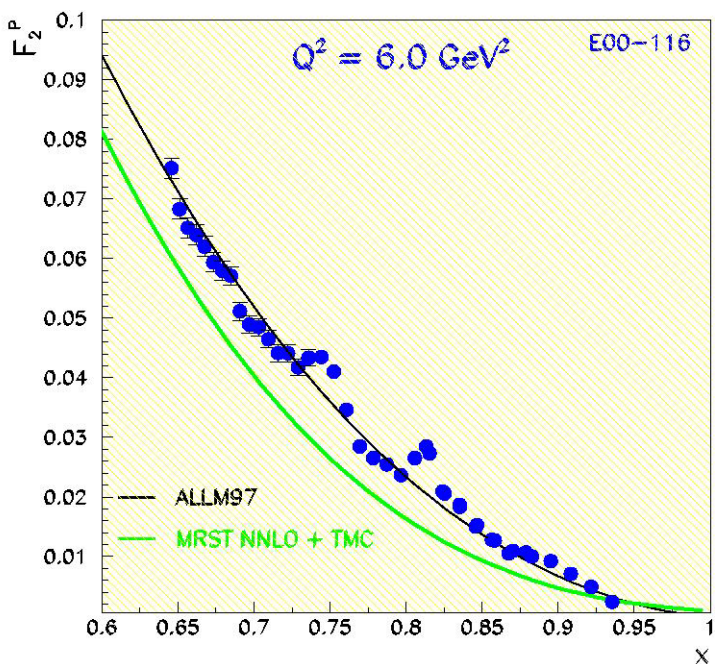
$$\text{where } t = \ln \left\{ \frac{\ln[(Q^2 + Q_0^2)/\Lambda^2]}{\ln(Q_0^2/\Lambda^2)} \right\}$$

$x_{P,R}$ = modified Bjorken x

$$1/x_{P,R} = 1 + (W^2 - M^2)/(Q^2 + m_{P,R}^2)$$

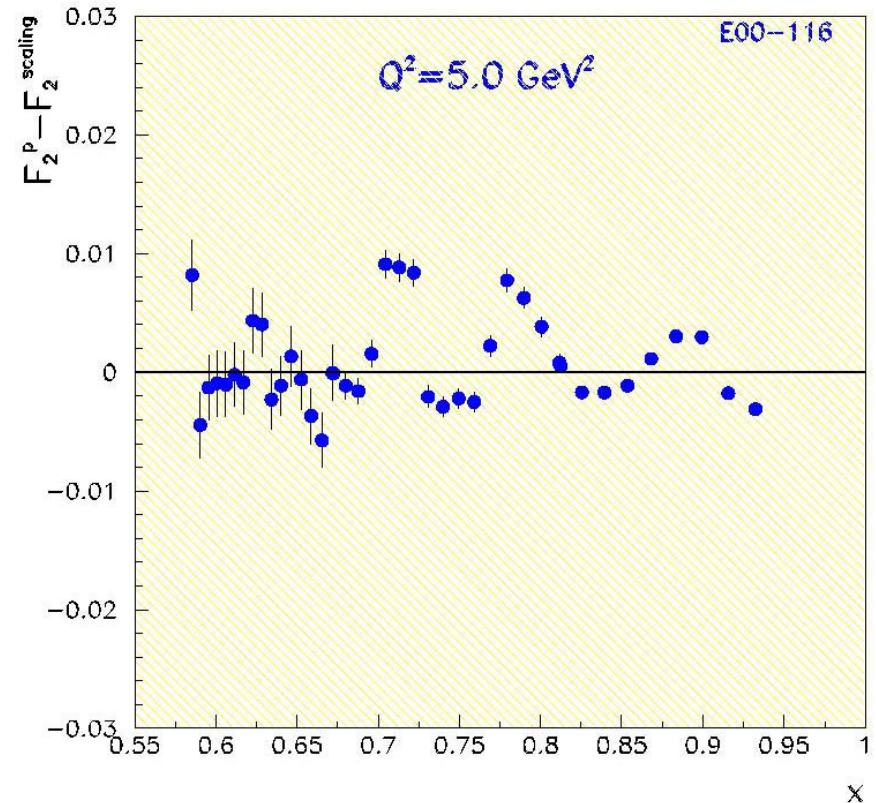
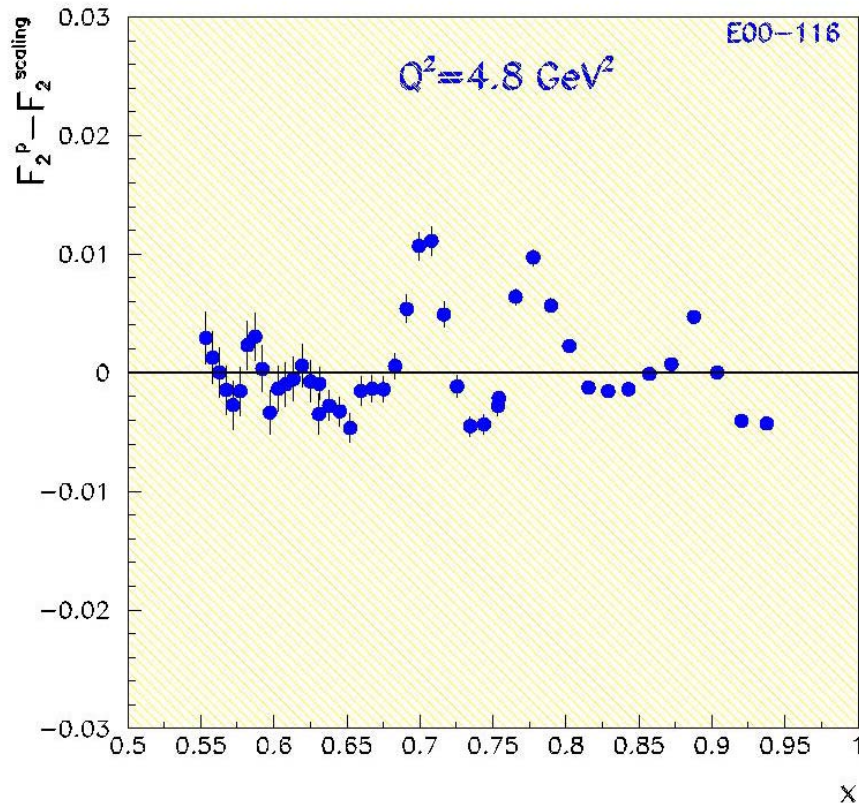


*Remaining
spectra of
 F_2^p*



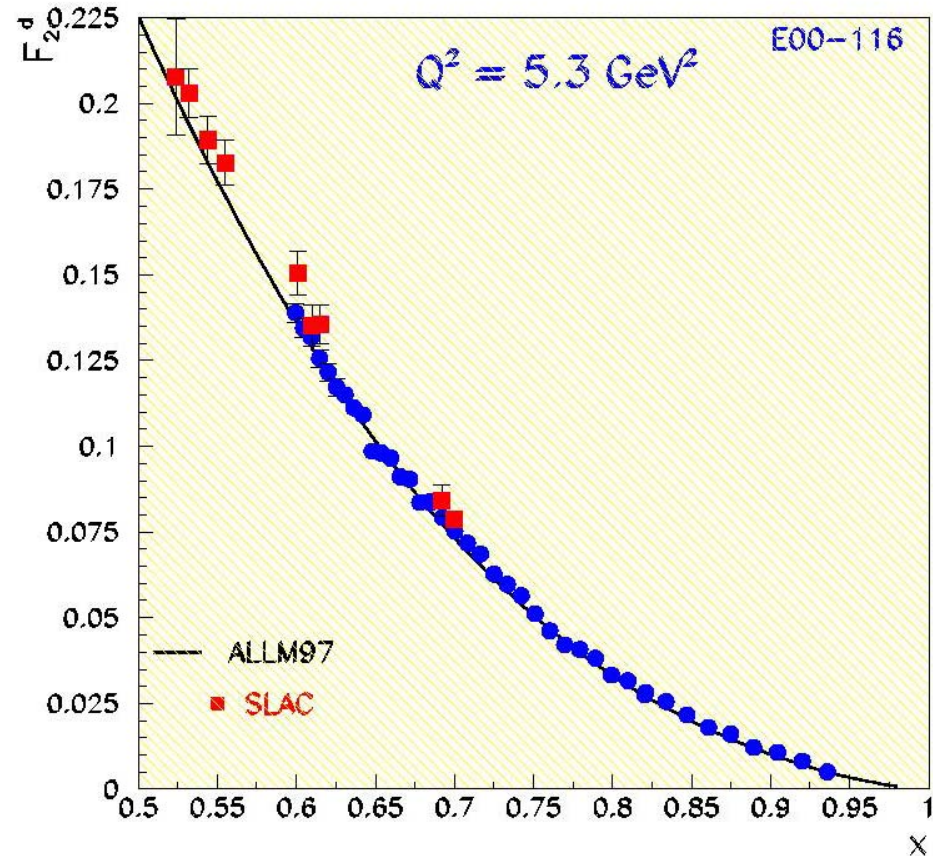
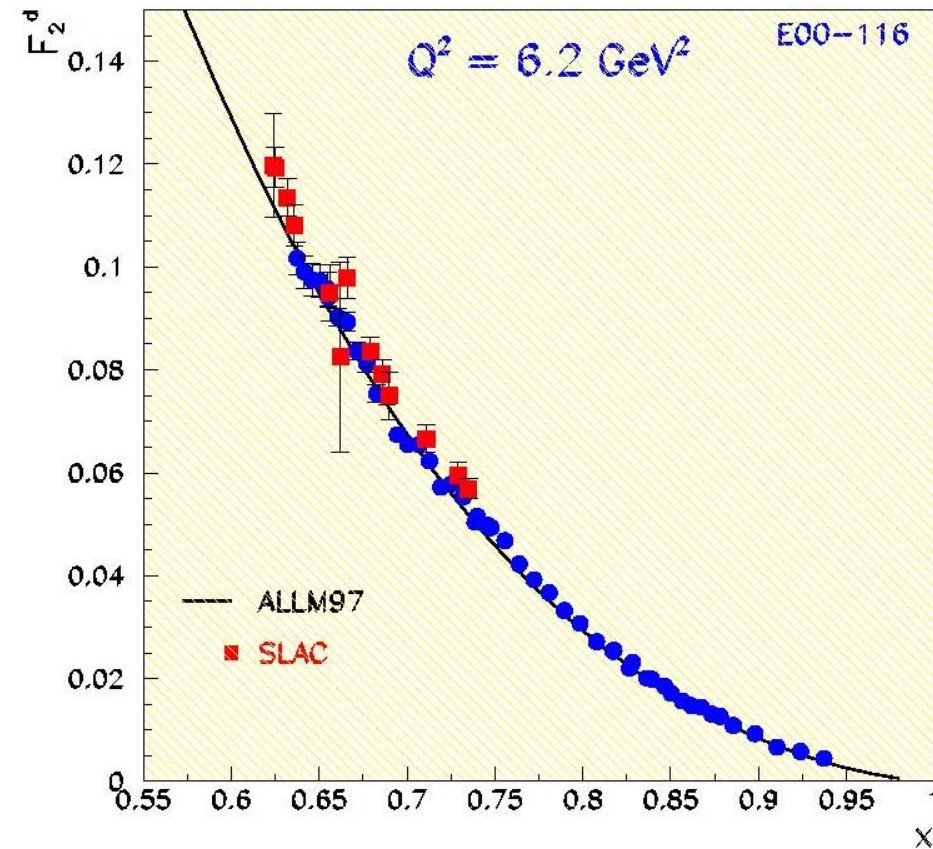
How well ALLM97 describes the H_2 data ?

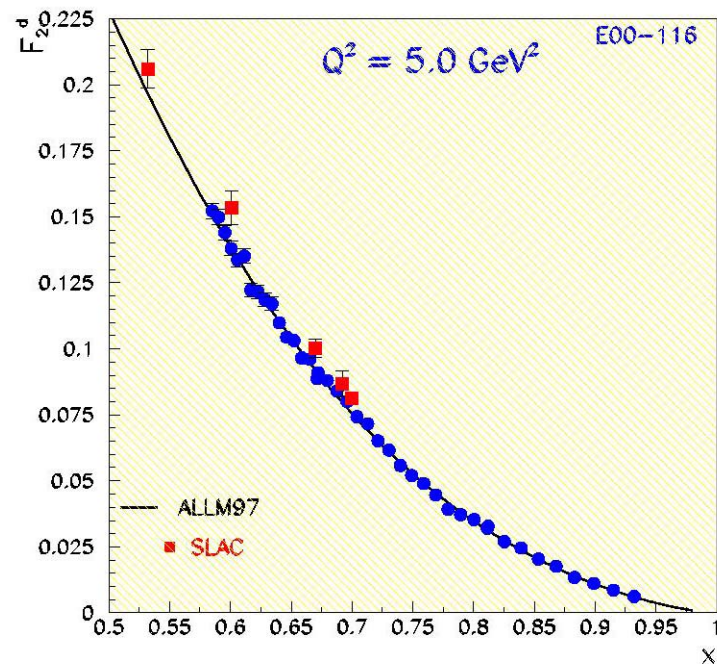
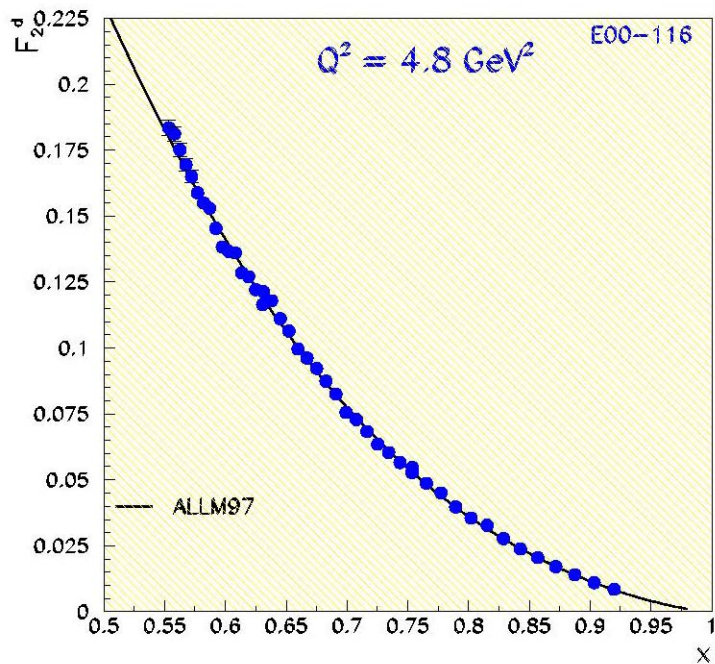
- ➡ **Global duality** studies revealed that when integrating over the entire spectrum - resonance + DIS region – with **ALLM97** as **scaling curve**, **duality** holds up to **2%**.



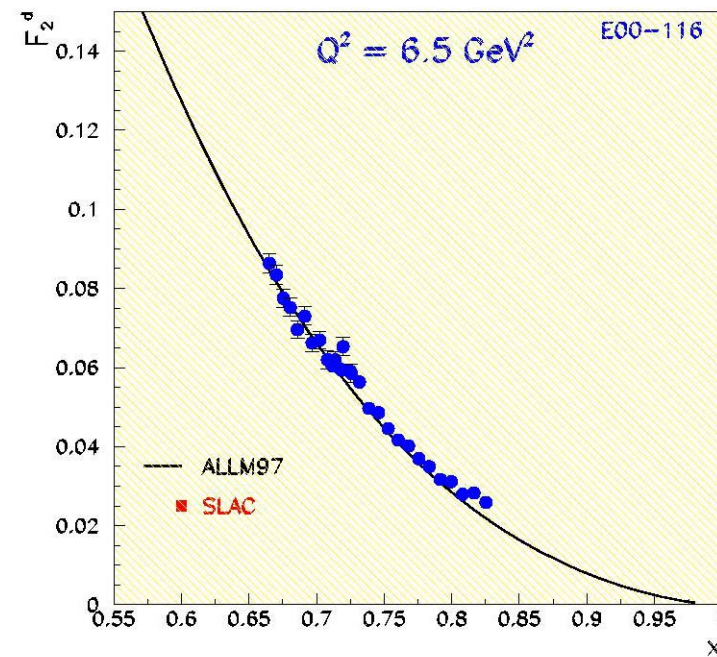
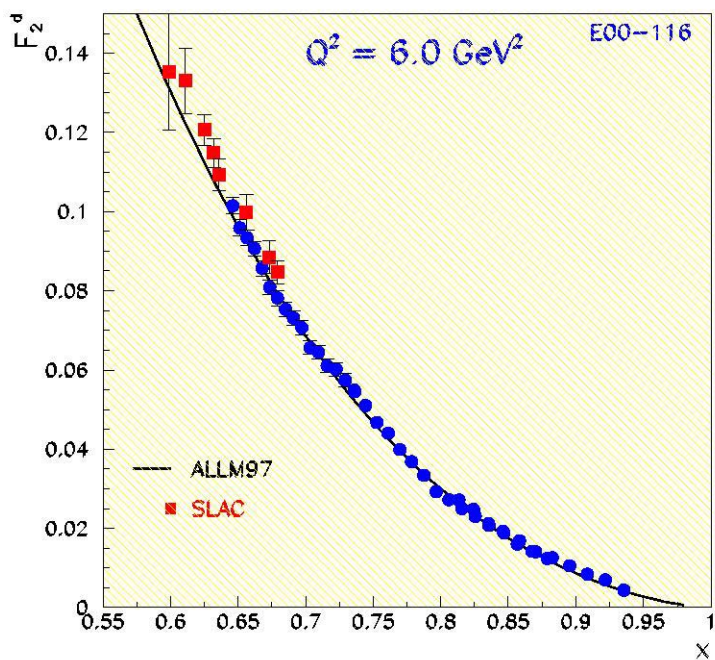
F_2^d from E00-116 data

➡ ALLM97 for D_2 is: (the fit to world dis F_2^p) X (parameterization of F_2^d/F_2^p as a function of x from world data)





*Remaining
spectra of
 F_2^d*

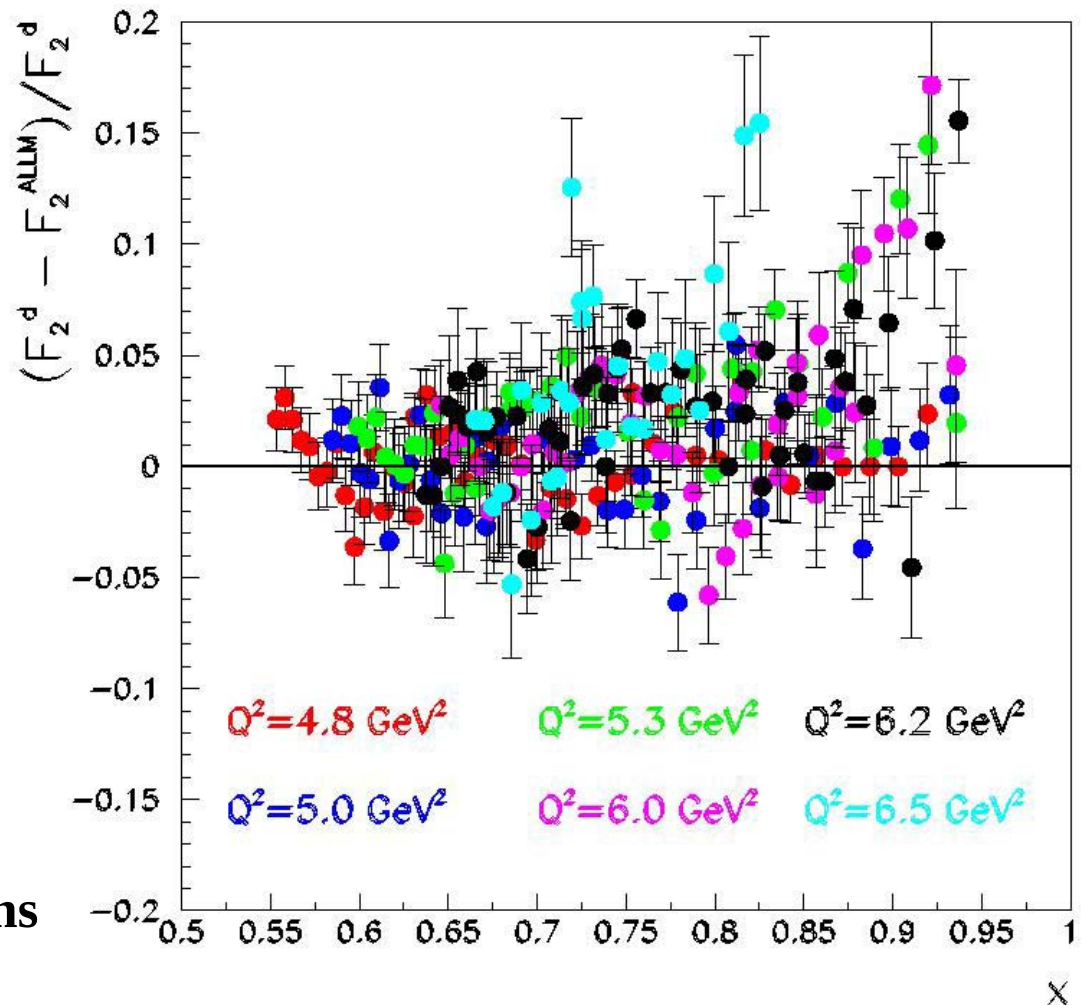


How well ALLM97 describes the D_2 data ?

➡ Overall, ALLM97 D_2 is about 1.5 % lower than E00-116 data , the discrepancy getting bigger at high x .

➡ E00-116 data seem few percent lower than SLAC data.

...but D_2 data still need iteration(for both cross sections and radiative corrections)...

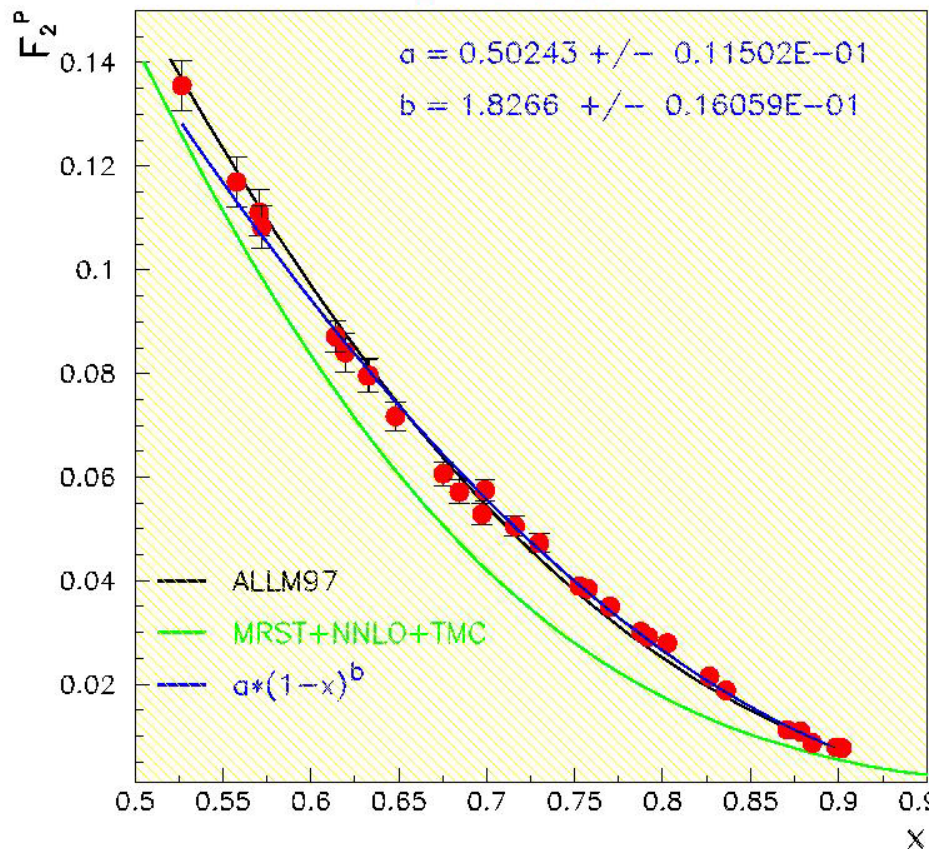


$$F_2(x) |_{Q^2=\text{const.}} \sim (1-x)^b$$

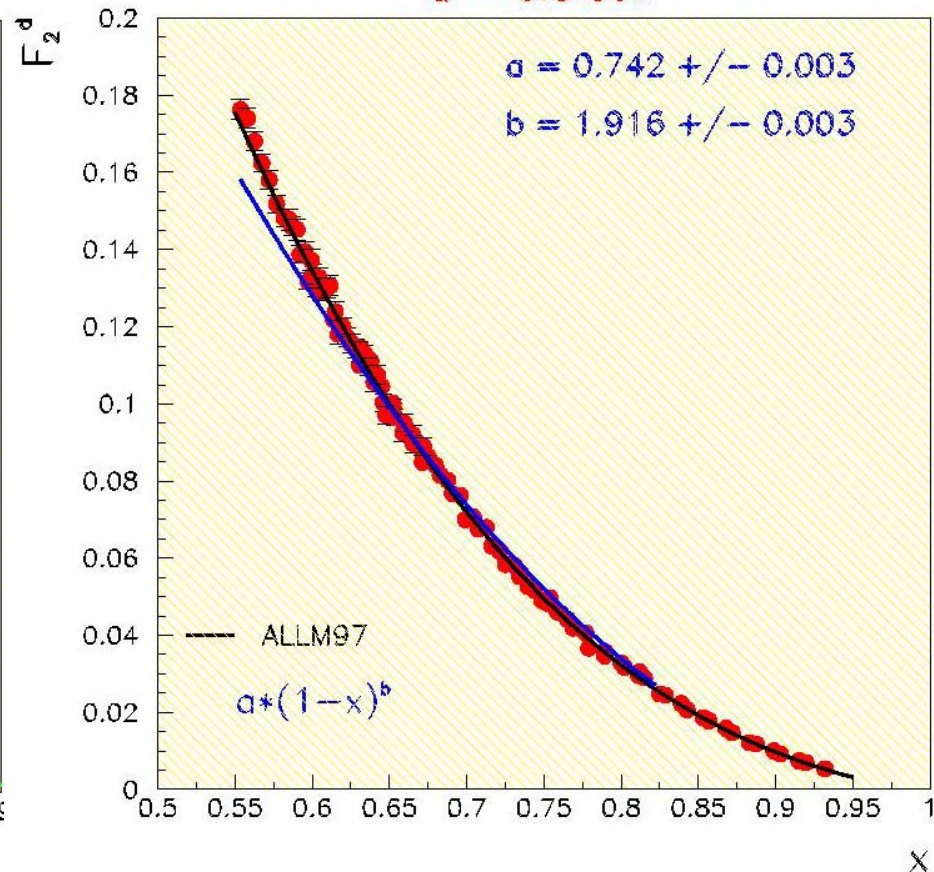
➡ For a fixed Q^2 ,
the F_2 dependence of x goes like $(1-x)^b$.

➡ E00-116 F_2^p and F_2^d “points” were centered at a fixed $Q^2 = 5.5 \text{ GeV}^2$
and the x dependence of F_2^p was fitted.

$Q^2 = 5.5 \text{ GeV}^2$



$Q^2 = 5.5 \text{ GeV}^2$



Summary

- ◆ F_2^p extracted from E00-116 resonance data were shown. With increasing Q^2/x they slide on ALLM97 curve but are becoming systematically higher than MRST+NNLO+TMC curve.
- ◆ F_2^p dependence of Q^2/x for E00-116 data were checked against world data, ALLM97 fit and MRST+NNLO+TMC. E00-116 data follow the Q^2 / x behavior of ALLM97 fit.
- ◆ Preliminary F_2^d were shown against “ALLM97” fit and available SLAC data but D_2 data still need iteration.

