

Duality in Meson Electroproduction (E00-108)

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Outline

- The E00-108 Experiment
- Physics motivation
- Analysis status
- Simulation
- Current results
- Problems and what next to do.

The Experiment

- **HMS** was detecting hadrons , π^{\pm}
- **SOS** was set for electrons , e^{-}
- **DAQ** in coincidence mode
- 3 groups of measurement have been conducted:
 - I. Z-scan \rightarrow 8 different Z settings at fixed X_{Bj}
 - II. X-scan \rightarrow 5 different X_{Bj} settings at fixed Z
 - III. P_t -scan \rightarrow 5 different θ_{pq} settings at fixed Z and X_{Bj} .

$$X_{Bj} = \frac{Q^2}{2M\nu} \quad - \text{ Bjorken X}$$

$$Z = \frac{E_h}{\nu} \quad - \text{ part of energy taken by hadron.}$$

$$P_t \quad - \text{ transverse momentum of the meson relative to virtual photon.}$$

$$\theta_{pq} \quad - \text{ lab. angle between the virtual photon and outgoing meson.}$$

Quark-Hadron Duality

complementary between quark and hadron description

At high enough energy:

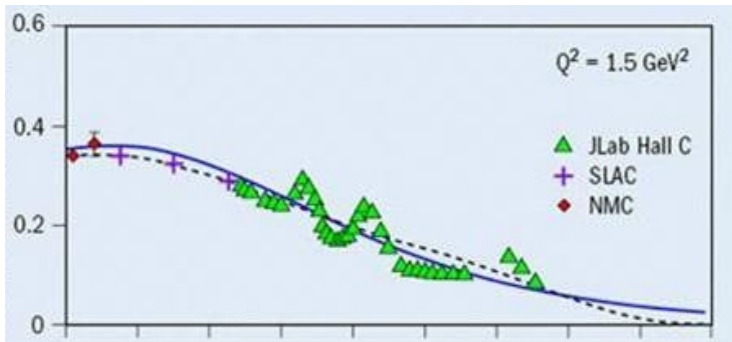
Hadronic Cross Sections
 averaged over appropriate
 energy range

Perturbative Quark-Gluon
 Theory

$$\Sigma_{\text{hadrons}} = \Sigma_{\text{quark+gluons}}$$

Can use either set of complete basis states to describe physical phenomena.
 But why also in limited local energy ranges?

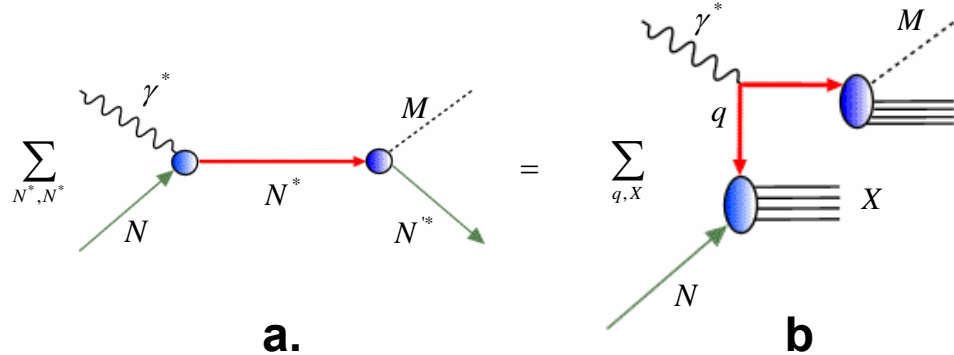
Duality works well.



Predicted to also appear in
 semi-inclusive scattering
 processes
 (Carlson et al, 1998)

Duality in Semi-inclusive Reactions

- Duality description of semi-inclusive ($eN \rightarrow ehX$) meson production in terms of **nucleon resonance excitation** (a), and **parton phenomenology** (b).



- Cross section is given by a product of **quark distribution** and **quark \rightarrow hadron fragmentation function**

$$\frac{d\sigma}{dx dz} \sim \sum_q e_q^2 q(x) D_{q \rightarrow h}(z) \quad \text{and a little bit more complicated}$$

$$\frac{\frac{d\Omega_e dE_e dx dP_{\perp}^2 d\phi}{d\sigma}}{\frac{d\Omega_e dE_e}{d\sigma}} = \frac{dN}{dz} b \exp(-bP_{\perp}^2) \frac{1 + A \cos \phi + B \cos 2\phi}{2\pi}$$

At high energies:

- No ϕ dependence
- Measured P_{\perp} dependence
- Cross section factorization

The Analysis Procedure

Factors taken into account:

- All efficiencies and dead times;
- Decayed pion loss (~ 20 %);
- FSI corrections for Deuterium target (~4 %);
- Radiative corrections made with SIMC checked with POLRAD /HAPRAD/ (typically 5-10 %);
- Exclusive events radiative “tail” subtractions;
- Scale off ρ^0 contribution;
- k^\pm - mesons subtraction (~2-9 %);
- Improved tracking pruning code and coincidence time path length correction.

How Can We Verify Factorization?

$$\frac{d\sigma}{dx dz} \sim \sum_q e_q^2 q(x) D_{q \rightarrow h}(z)$$

Neglect sea quarks and assume no p_T dependence to parton distribution functions

→ Fragmentation function dependence drops out in Leading Order

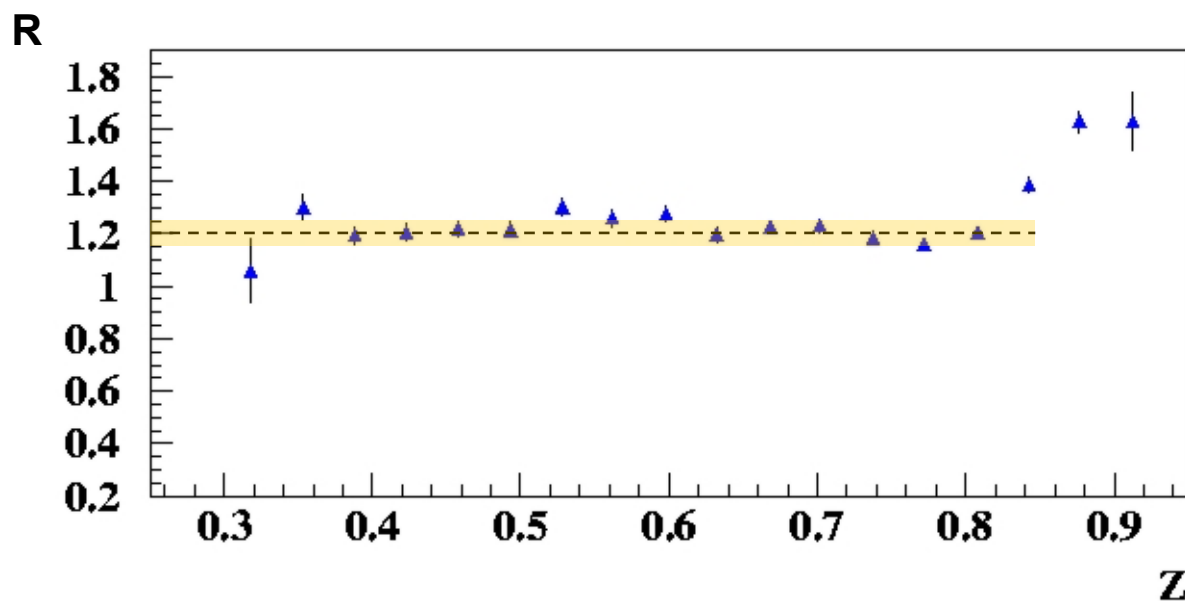
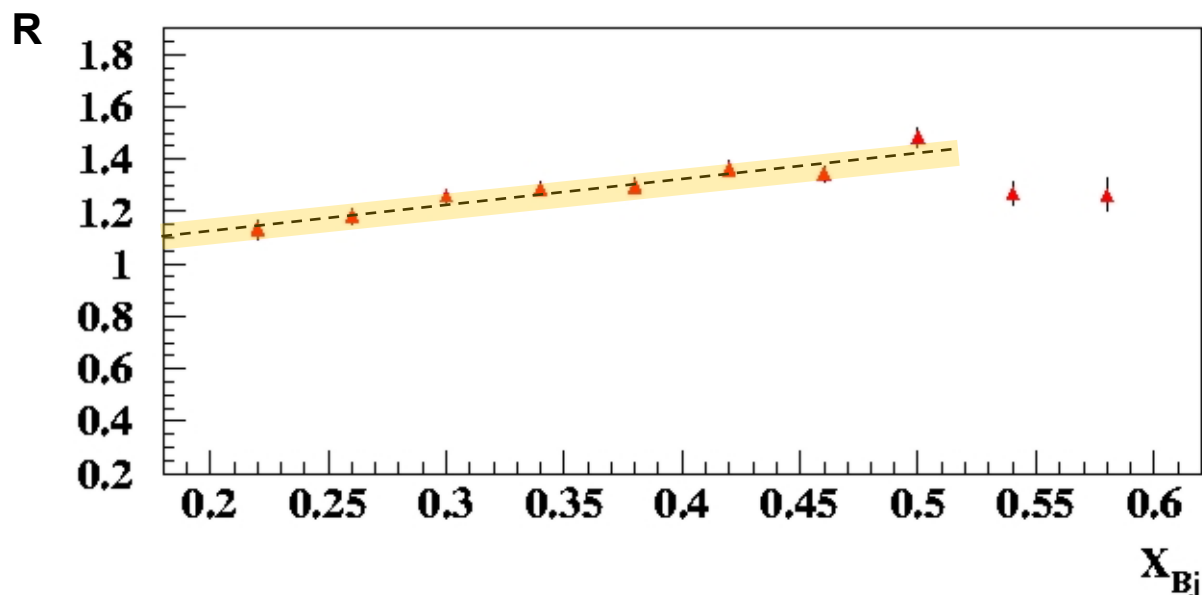
$$\begin{aligned} \rightarrow [\sigma_p(\pi^+) + \sigma_p(\pi^-)] / [\sigma_d(\pi^+) + \sigma_d(\pi^-)] \\ = [4u(x) + d(x)] / [5(u(x) + d(x))] \\ \sim \sigma_p / \sigma_d \quad \text{independent of } z \end{aligned}$$

$$\begin{aligned} \rightarrow [\sigma_p(\pi^+) - \sigma_p(\pi^-)] / [\sigma_d(\pi^+) - \sigma_d(\pi^-)] \\ = [4u(x) - d(x)] / [3(u(x) + d(x))] \end{aligned}$$

*independent of z ,
but more sensitive to assumptions*

$$R = \frac{\sigma_p(\pi^+) + \sigma_p(\pi^-)}{\sigma_d(\pi^+) + \sigma_d(\pi^-)}$$

Expected x dependence

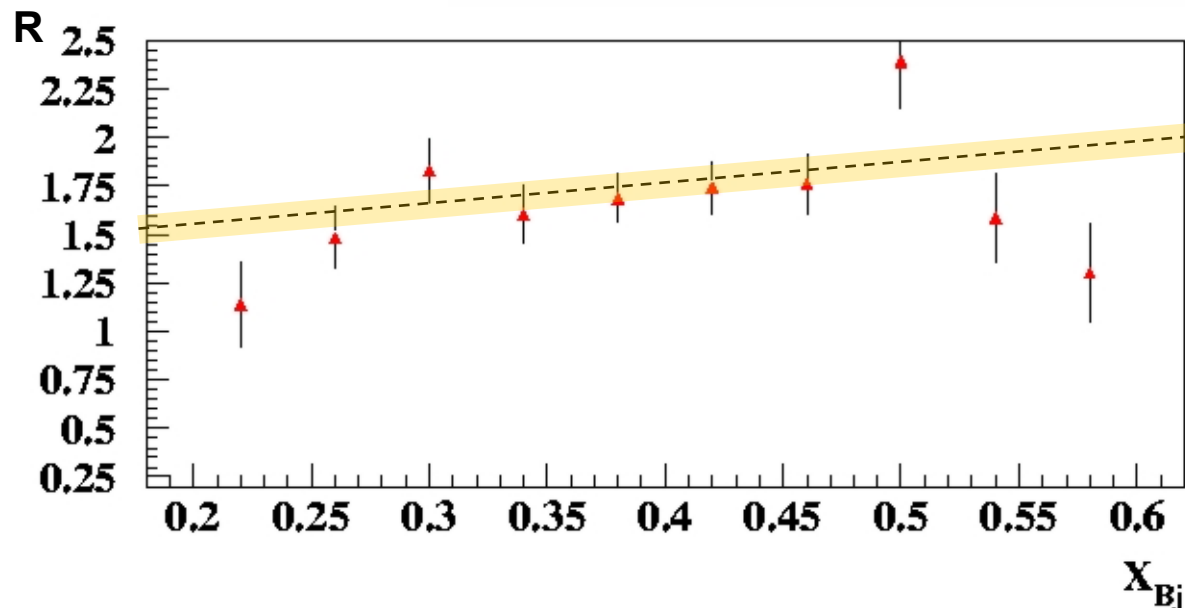


independent of z

- Dotted line is LUND Monte-Carlo.

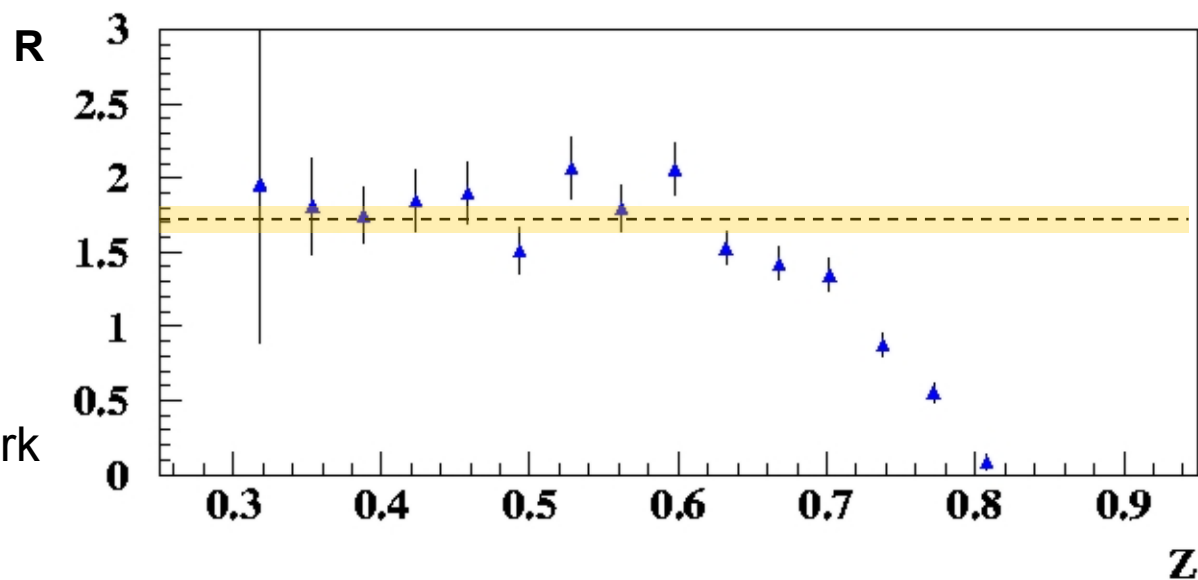
$$R = \frac{\sigma_p(\pi^+) - \sigma_p(\pi^-)}{\sigma_d(\pi^+) - \sigma_d(\pi^-)}$$

Expected x dependence



independent of z

Difference clearable more sensitive, but seems to work from $z < 0.65$



Simulation

- For the simulation the standard SIMC package has been used with an addition of semi-inclusive cross section:

$$\sigma_{e,e'\pi x} \approx \sigma_{e,e'x} \frac{dN}{dz} (1 + A \cos \varphi + B \cos 2\varphi) b e^{-bP_t^2} \quad \text{where}$$

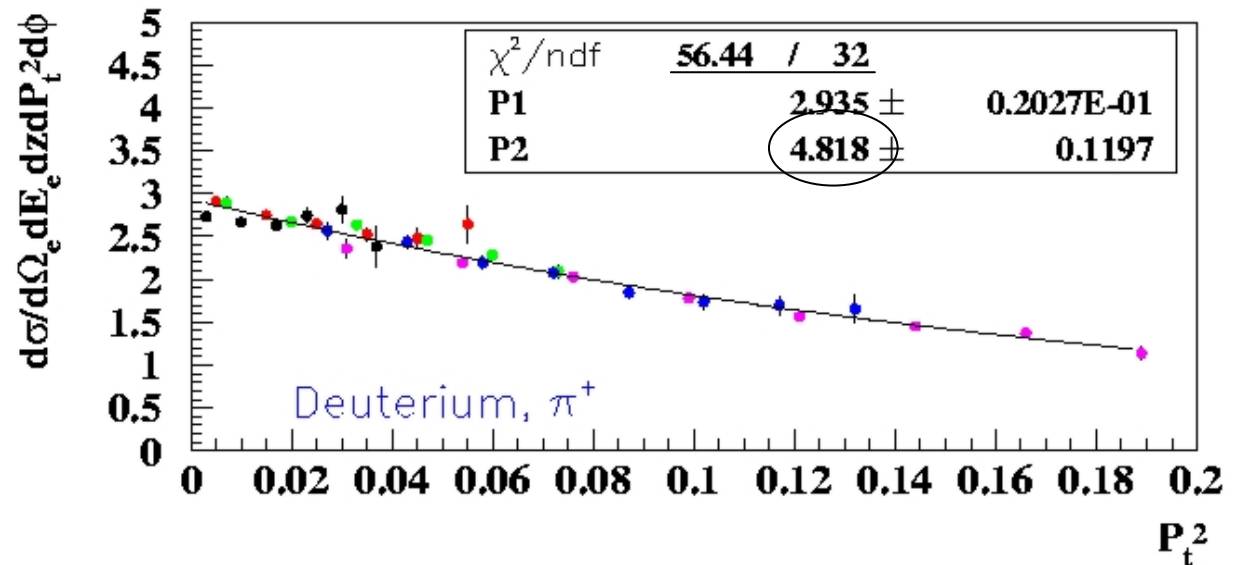
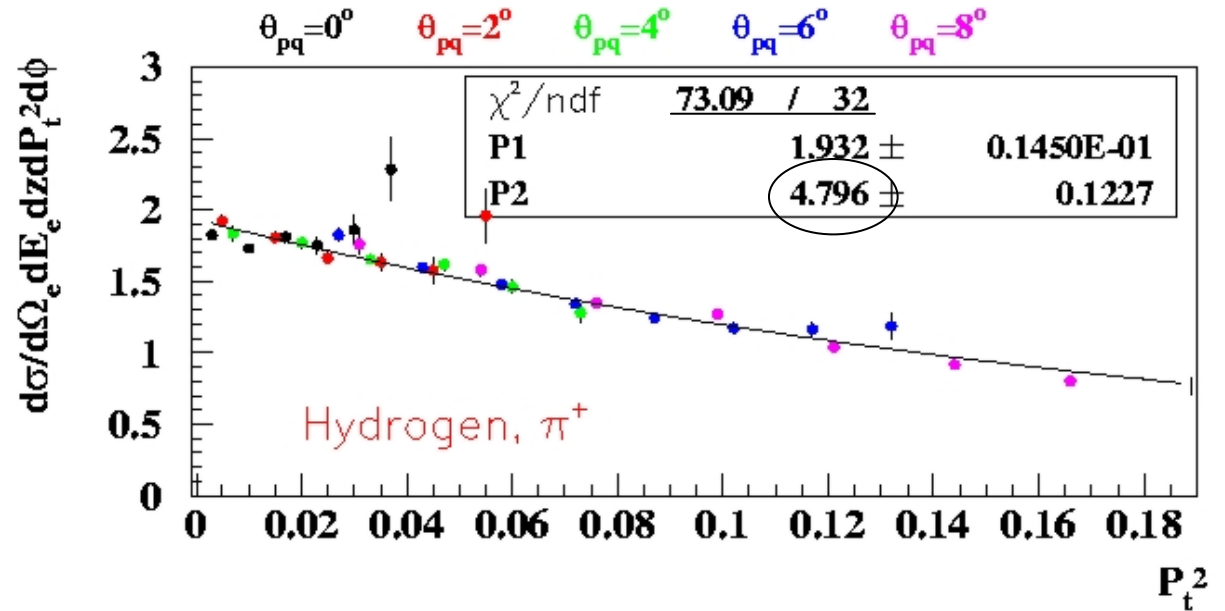
$$\frac{dN}{dz} \rightarrow \frac{\sum_i q_i^2 U_i(x, Q^2) D_i(z, Q^2)}{\sum_i q_i^2 U_i(x, Q^2)}$$

- CTEQ5 parametrization for parton distributions.
- BKK parametrization for the fragmentation functions.
- To separate favored and unfavored fragmentation functions a parametrizations of D⁺/D⁻ from HERMES is used.
- DIS cross section was calculated through F₁ and F₂ structure functions.
- Explicit φ and P_t^2 dependences are added in model.
- Q² dependence is included in the model to better describe experimental data

HERMES $\rightarrow b=4.69$

SLAC $\rightarrow b=4.61$

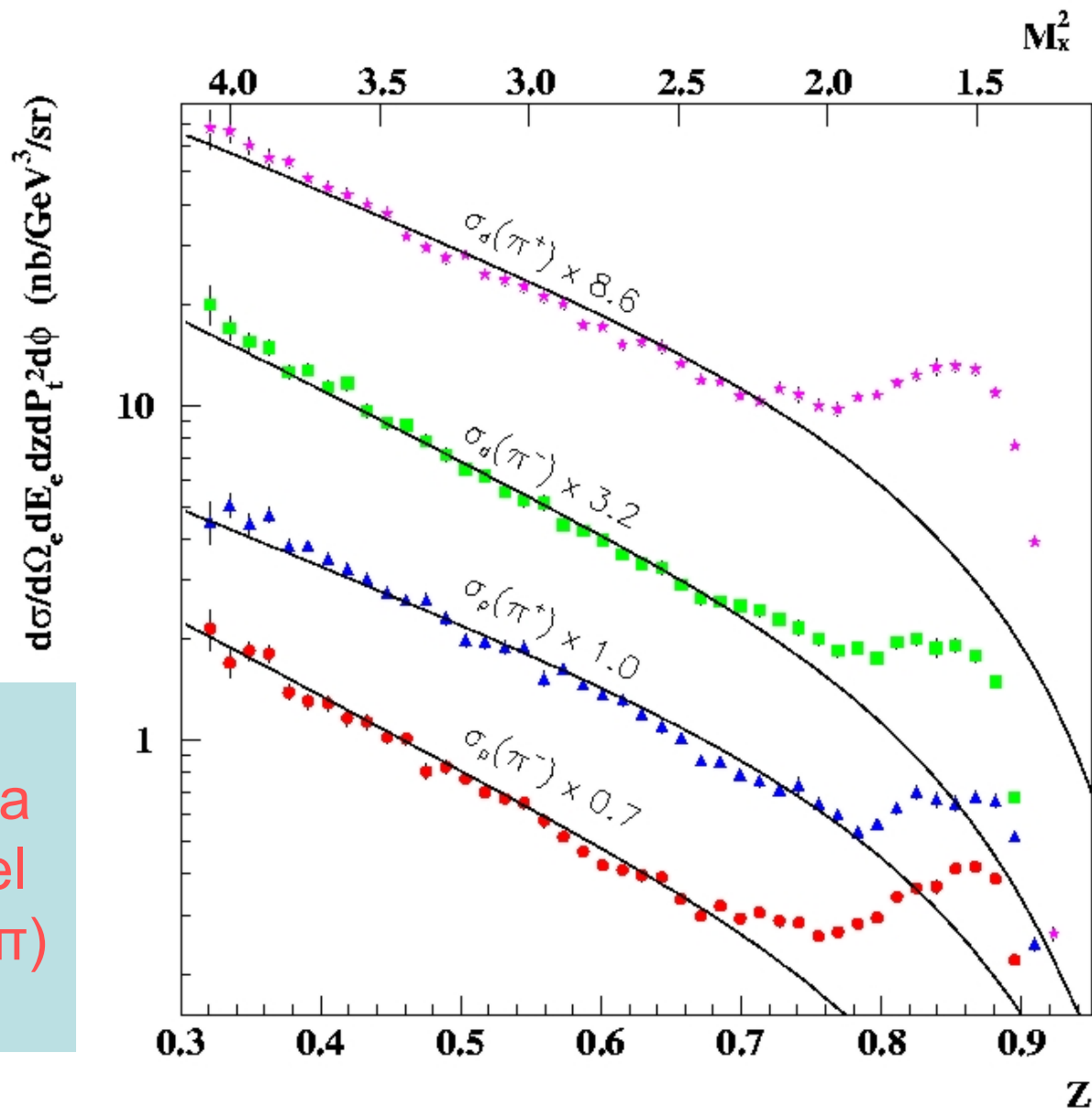
- Almost final $\pm 10\%$



- Solid curves SIMC

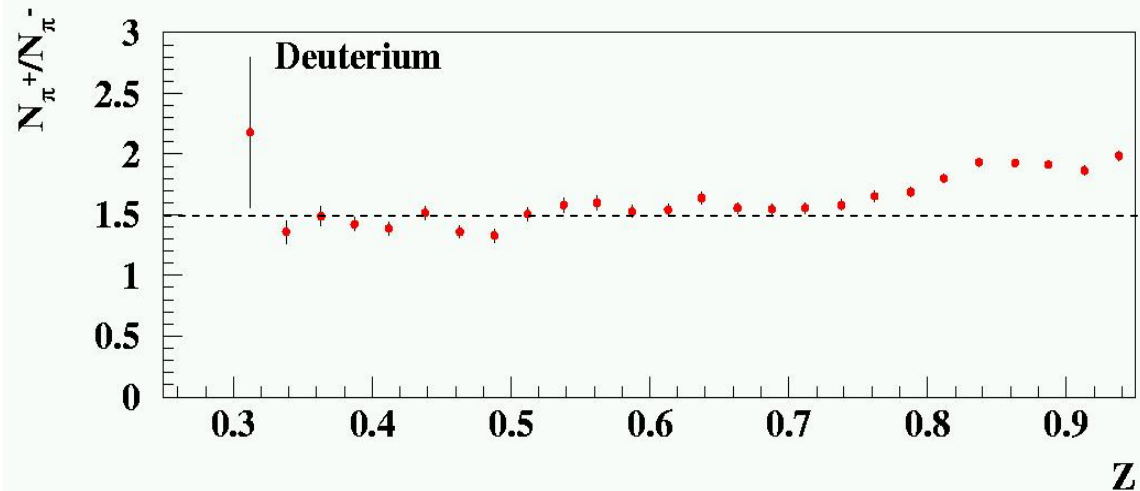
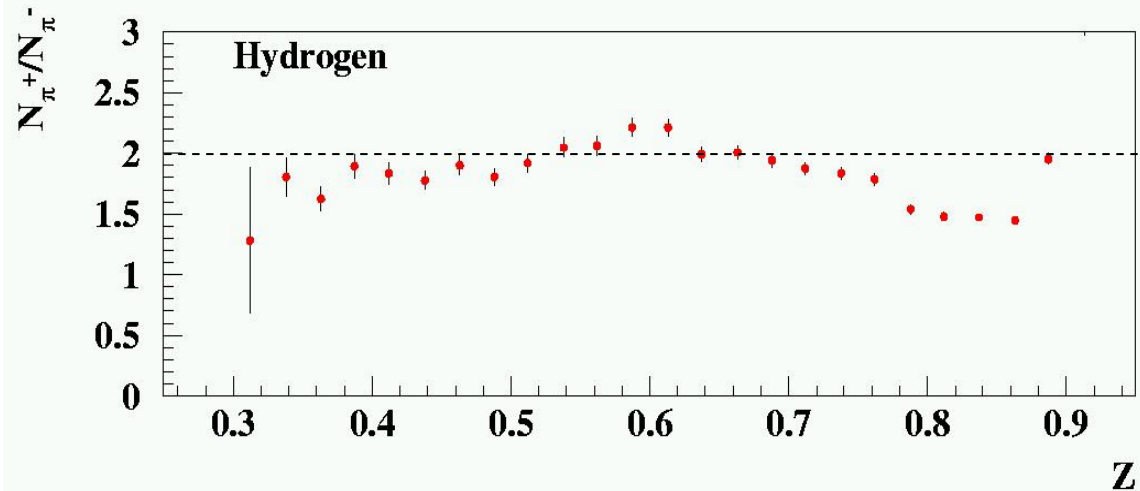
$$\sigma_{\text{exp}} = \frac{Y_{\text{exp}}}{Y_{MC}} \sigma_{mc}$$

SIMC assume factorization and is a simple parton model assumption of $(e, e' \pi)$ process



- Acceptance, kinematic and bin centering corrections are canceled in π^+/π^- ratios.

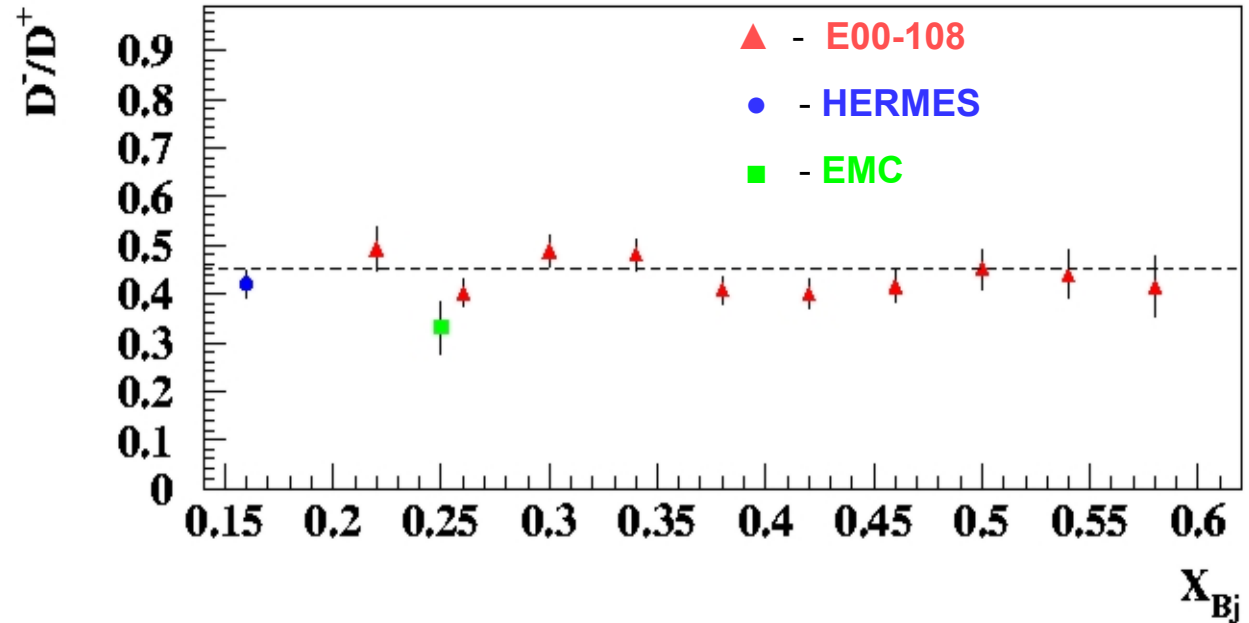
- π^+/π^- ratio expected to be flat in Z at the fixed X_{Bj} according to the previous experiments (SLAC, Cornell, DESY).



- From the simple quark count and SU(6) symmetry, ratio over ratio for **Hydrogen** should be at the level ~ 2 , and for **Deuterium** $3/2$.

$$\frac{d\sigma}{dx dz} \sim \sum_q e_q^2 q(x) D_{q \rightarrow h}(z)$$

$$\frac{D^-}{D^+} = \frac{4 - \frac{N_{\pi^+}}{N_{\pi^-}}}{4 * \left(\frac{N_{\pi^+}}{N_{\pi^-}} \right) - 1}$$



D^- is the “favored” and D^+ is the “unfavored” fragmentation functions

- Strange quark contribution neglected.

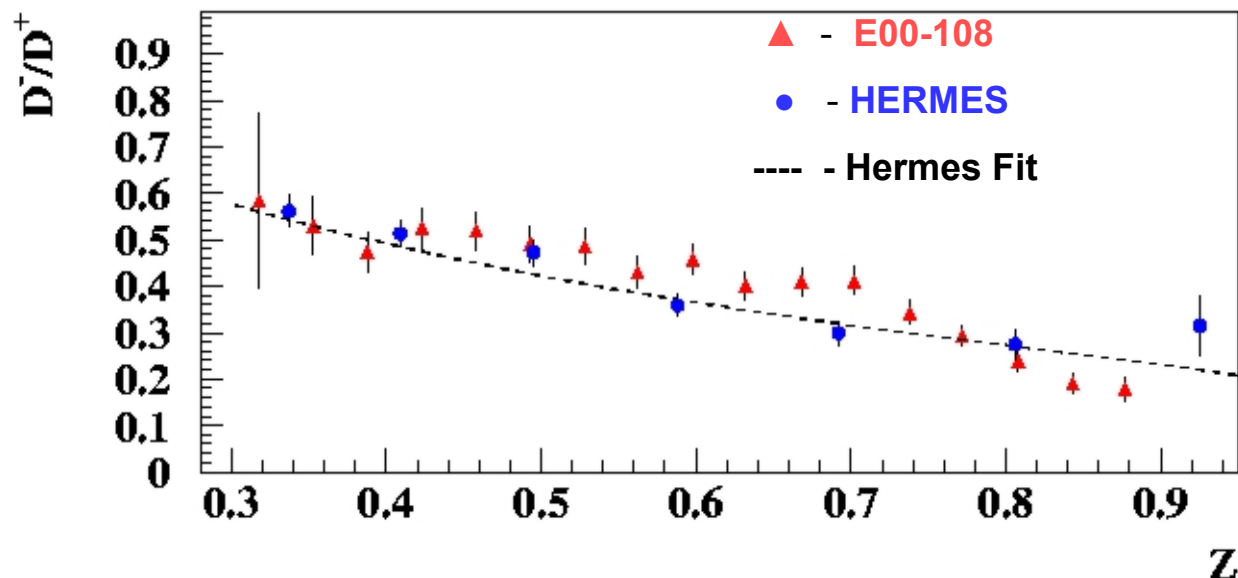


D^-/D^+ ratio should be independent from X_{Bj}

but

$$\frac{D^-}{D^+} = \frac{4-R}{4 \cdot R - 1}$$

where $R = \frac{N_{\pi^+}}{N_{\pi^-}}$



→ ... should depend on Z

Similar slope versus Z at HERMES

Conclusion

- ***Data indicate a surprisingly smooth transition from “Quark model physics” to “Parton Model Physics” at low Q^2***
- Evidence of cross-section factorization.
- Data seem to confirm the high energy physics predictions.
- Results are close to the data from experiments at higher energies.

What next ?

- Iterate the model.
- Calculate cross-sections.
- Estimate systematic errors.