

The APS Council has endorsed the establishment, contingent on funding, of the

## Herman Feshbach Prize in Nuclear Physics

To recognize and encourage outstanding research in theoretical nuclear physics. The prize will consist of \$10,000 and a certificate citing the contributions made by the recipient. The prize will be presented biannually or annually—depends on your contributions.

Herman Feshbach was a dominant force in Nuclear Physics for many years. He co-authored two seminal textbooks, provided the theoretical basis for nuclear reaction theory, and originated the “Feshbach resonance” used to control the interactions between atoms in ultracold gases. He also made many administrative contributions.

The establishment of this prize depends entirely on the contributions of institutions, corporations and individuals associated with Nuclear Physics. So far, significant pledges have been made by MIT, the DNP, Elsevier, ORNL/U.Tenn, JSA/SURA, LANL, TUNL, and many individuals. But the collection of contributions has begun. Please make a contribution by going online at <http://www.aps.org/> Look for the support banner and click APS member or non-member. Another way is to send a check, made out to “The American Physical Society”, with a notation indicating the purpose is the Feshbach Prize Fund, to

Darlene Logan  
Director of Development  
American Physical Society  
One Physics Ellipse  
College Park, MD 20740-3844

**If annual- number of experimentalists winning  
Bonner prize goes up by >50%**

If you have any questions please contact G. A. (Jerry) Miller UW, miller@uw.edu.

# Nucleon Electromagnetic Form Factors and Spin: is proton made of 3 quarks?

**Gerald A. Miller, UW**

Connection between elastic form factors and OAM through models

Model wave functions, compute form factors

OAM content of Models: elastic form factors imply that quark, pion OAM is large

# What is not in the talk

- Proton radius - new work
- Transverse densities - slope of  $G_E$  is not the real radius
- Transverse densities from dispersion relations:

PHYSICAL REVIEW D **83**, 013006 (2011)

**Pion transverse charge density from timelike form factor data**

G. A. Miller,<sup>1</sup> M. Strikman,<sup>2</sup> and C. Weiss<sup>3</sup>

PHYSICAL REVIEW C **84**, 045205 (2011)

**Realizing vector meson dominance with transverse charge densities**

G. A. Miller,<sup>1</sup> M. Strikman,<sup>2</sup> and C. Weiss<sup>3</sup>

Phys.Rev.Lett. **108** (2012) 232301

The Electromagnetic Self-Energy Contribution to  $M_p - M_n$   
and the Isovector Nucleon Magnetic Polarizability

André Walker-Loud,<sup>1,2</sup> Carl E. Carlson,<sup>3</sup> and Gerald A. Miller<sup>1,4</sup>

A lot of other stuff

**Review of all models is absent**

# History -Definitions

$$\bar{u}(p', \lambda') \Gamma^\mu u(p, \lambda) = \bar{u}(p', \lambda') [\gamma^\mu F_1(Q^2) + \frac{i\sigma^{\mu\nu} (p' - p)_\nu}{2M} F_2(Q^2)] u(p, \lambda)$$

$$G_E \equiv F_1 - \frac{Q^2}{4M} F_2, \quad G_M = F_1 + F_2$$

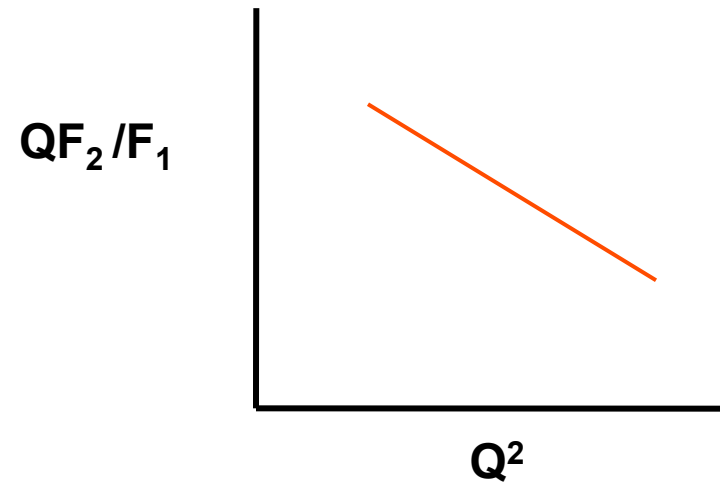
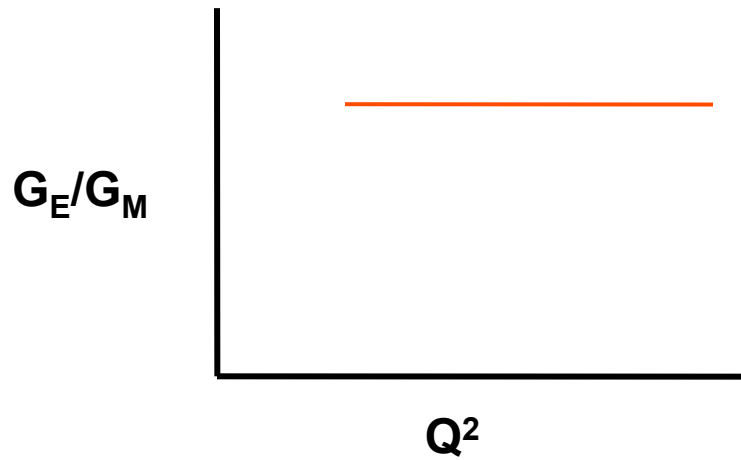
$F_1$  is light-front helicity non-flip,  $F_2$  is light-front helicity flip

old pQCD:

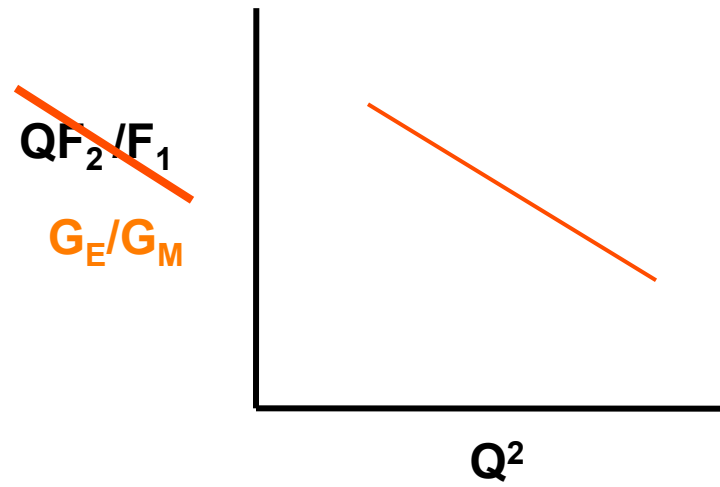
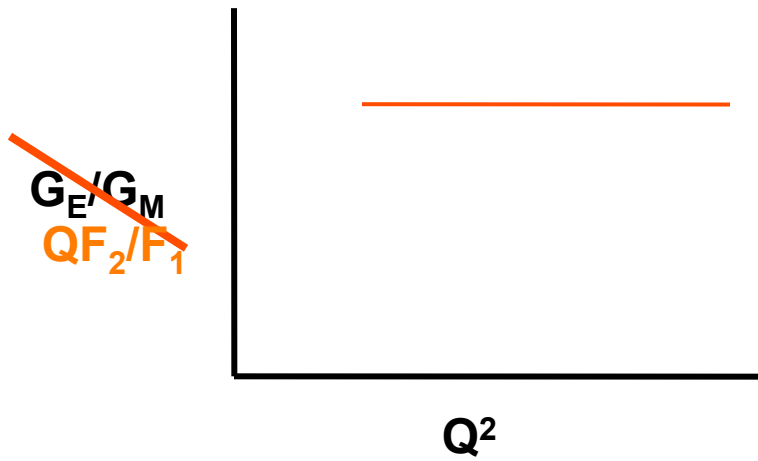
$$\frac{QF_2(Q^2)}{2M_N F_1} \sim \frac{m_{\text{quark}}}{Q} \rightarrow \frac{G_E}{G_M} = \text{const}$$

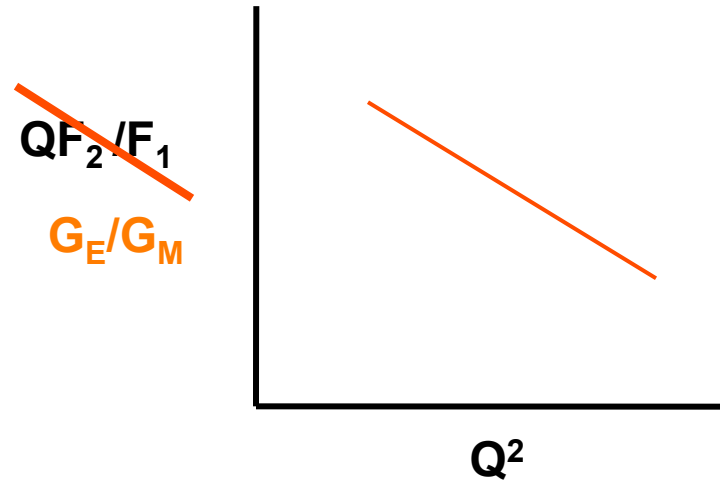
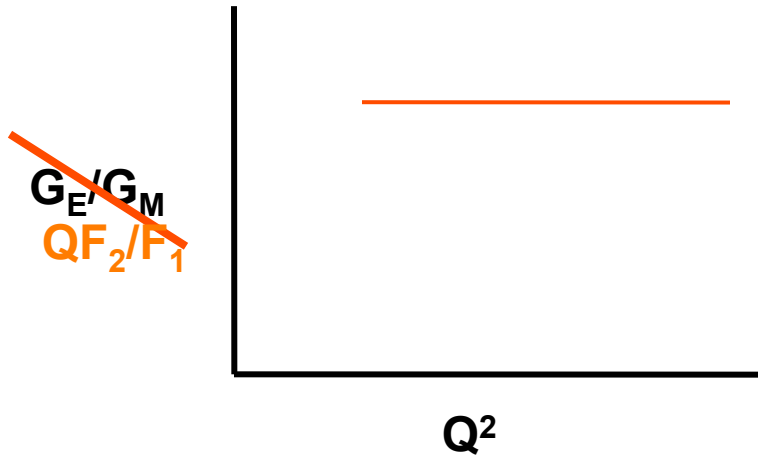
Same as non-relativistic

# Expectations- Pre Jlab



# Expectations- Pre Jlab





# Relativistic Wave function

Frank, Jennings, Miller PR C54, 920 (1996)  
Relativistic model for color transparency

- 3 quark anti-symmetric
- relative variables, frame independent **Light front variables**
- eigenstate of spin operator- rotational invariant
- reduces to non-relativistic if  $m \rightarrow \infty$

$$\Psi = \Phi(M_0^2) u(p_1) u(p_2) u(p_3 = K) \psi(s_i, t_i) \text{ Terentev, Coester}$$

spatial dist **DIRAC SPINORS** spin-ispin color amp

Schlumpf Mom space wf  $\Phi(M_0) = N / (M_0^2 + \beta^2)^\gamma$

$$\beta = 0.607 \text{ GeV} \quad \gamma = 3.5 \quad m = 0.267 \text{ GeV}$$



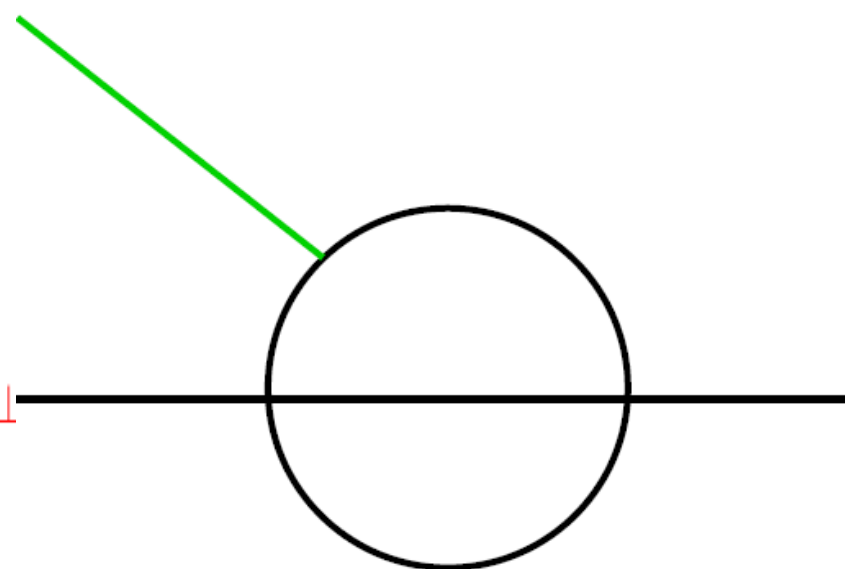
# Impulse Approximation

Model proton wave function  $\Psi(\mathbf{k}_\perp, \mathbf{K}_\perp, \xi, \eta)$

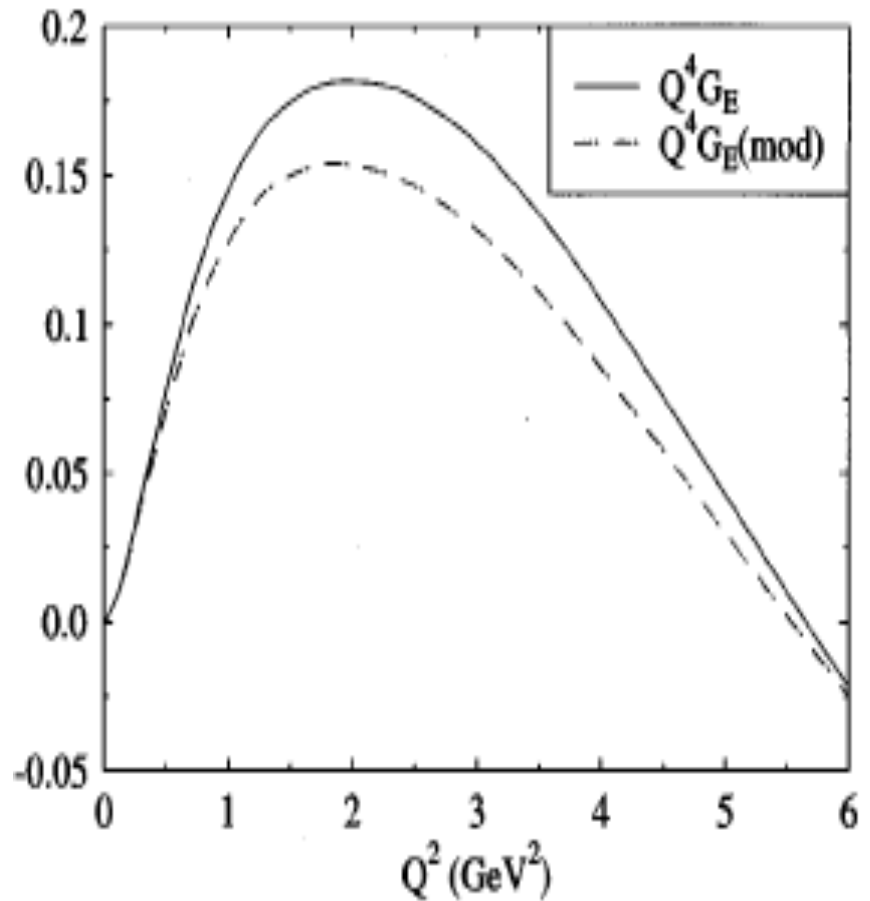
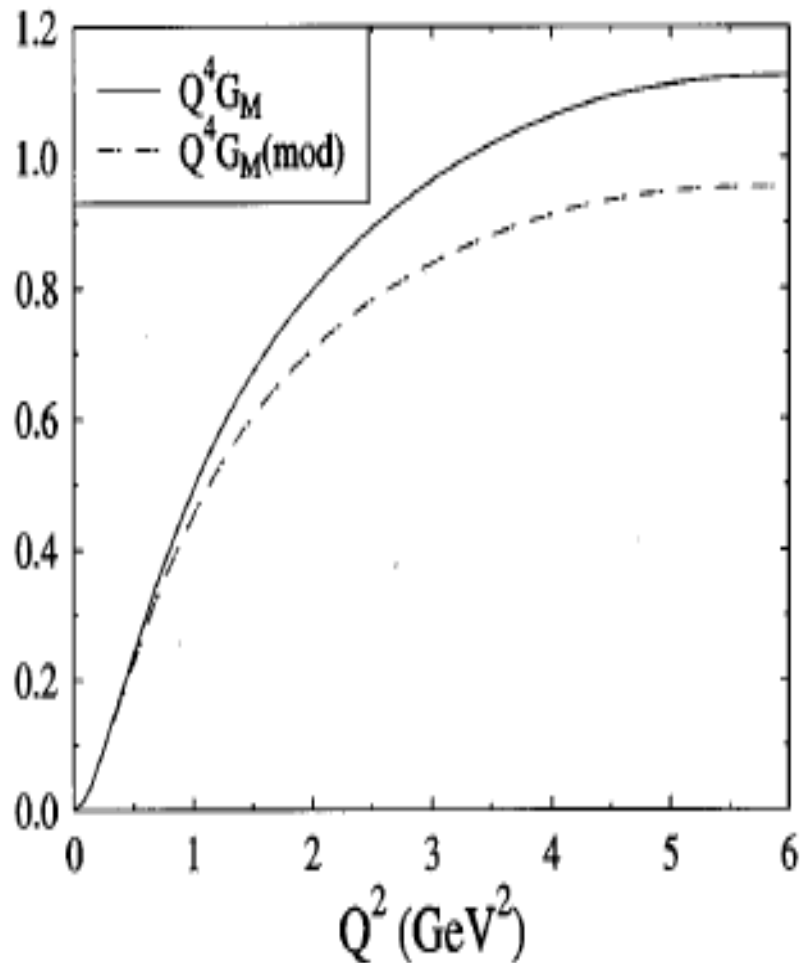
Poincare invariant

Light front variables for boost:  $\mathbf{K} \rightarrow \mathbf{K} + \eta \mathbf{q}_\perp$

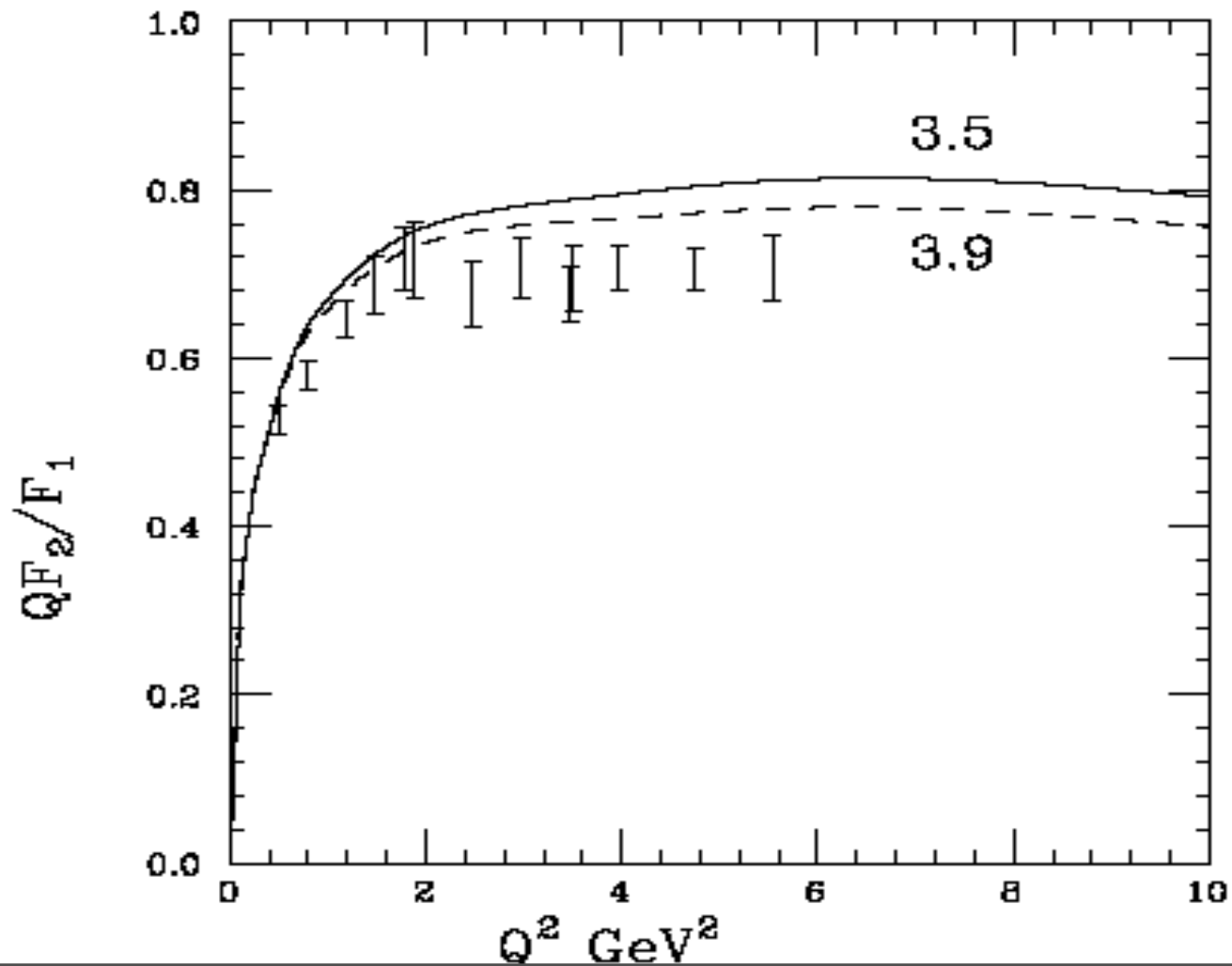
Dirac spinors



# 1995 Frank, Jennings, Miller



# Ratio of Pauli to Dirac Form Factors 1995



# Relativistic Explanation

$J^+$  acts on third quark, other two have 0 spin

$$u(K, s) = \begin{pmatrix} (E(K) + m)|s\rangle \\ \boldsymbol{\sigma} \cdot \mathbf{K}|s\rangle \end{pmatrix}$$

$\sigma_y|s\rangle$ : quark spin  $\neq$  proton ang mom

lower components  $\equiv L_z \neq 0$

$$\bar{u}(K', s')\gamma^+u(K, s) \sim \langle s'|K^+ + i\sigma_y Q|s\rangle \text{ Large } Q$$

spin non-flip  $F_1(Q^2) = \int \dots Q\Phi\Phi$ , flip  $QF_2 = \int \dots Q\Phi\Phi$

$$\frac{QF_2}{F_1} \sim \text{Constant}$$

Miller, Frank **Phys.Rev. C65 (2002) 065205**

# Relativistic Explanation

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$$u(K, s) = \begin{pmatrix} (E(K) + m)|s\rangle \\ \boldsymbol{\sigma} \cdot \mathbf{K}|s\rangle \end{pmatrix} \quad \text{Large OAM associated with relativistic effects}$$

$\sigma_y|s\rangle$ : quark spin  $\neq$  proton ang mom

lower components  $\equiv L_z \neq 0$

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$$\frac{QF_2}{F_1} \sim \text{Constant}$$

Miller, Frank *Phys.Rev. C65* (2002) 065205

# Spin content - OAM

$$s_{\mu} \Delta q = \langle N, s | \bar{q} \gamma_{\mu} \gamma_5 q | N, s \rangle$$

$$\Sigma = \Delta u + \Delta d + \Delta s$$

**75 % of proton angular momentum carried by quark spin**

Textbook relativistic effect that reduces calculated axial vector coupling constant below NRQM value 5/3

Neutron: Need  $\pi$  cloud effect at low  $Q^2$

## Cloudy Bag Model 1980

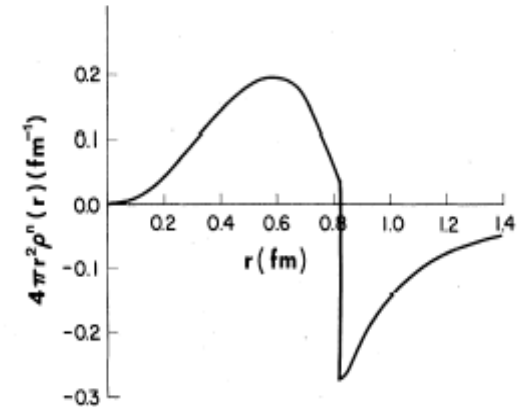
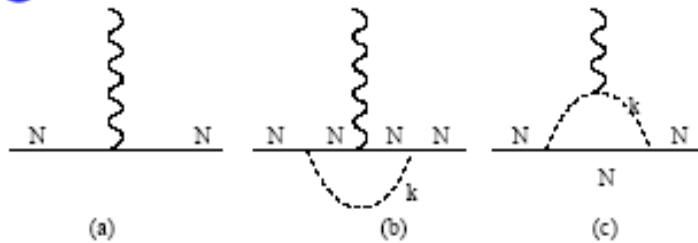


FIG. 11. Neutron charge density.

Relativistic treatment needed Feynman graphs,  $\int dk^-$

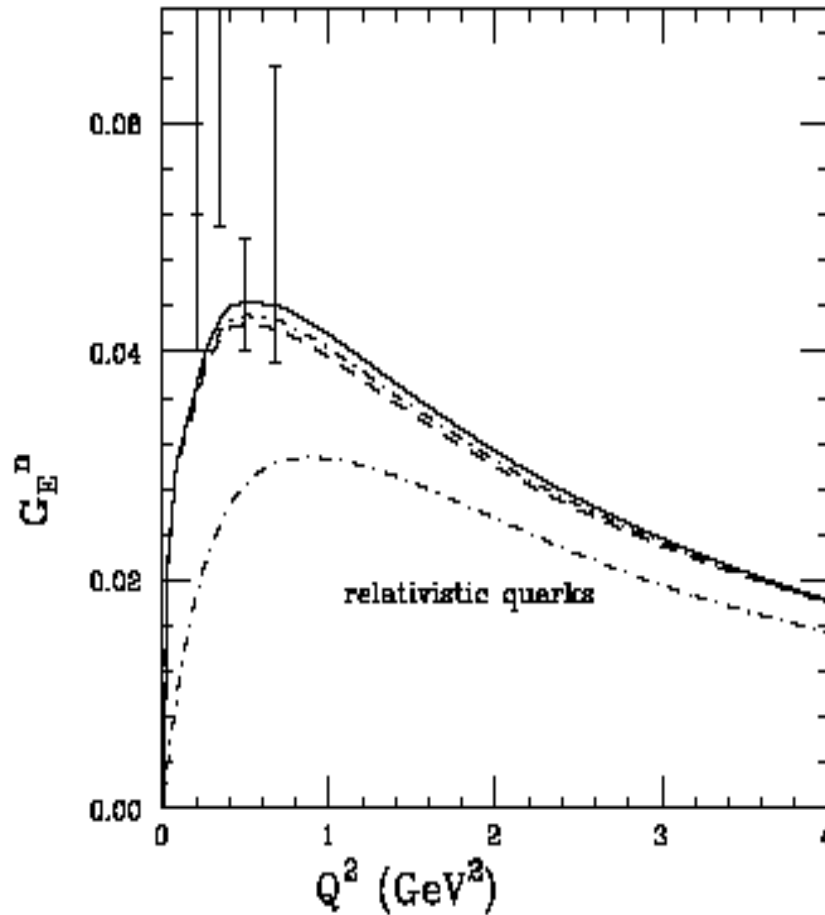
Light front cloudy bag model LFCBM 2002

Miller Phys.Rev. C66 (2002) 032201

- $\gamma N$  form factors from model (our model)
- rel.  $\pi N$  form factor  $\Lambda_{\pi N}$
- Model parameters:  $m, \beta, \gamma, \Lambda_{\pi N}$

Consistent with leading non-analytic terms in chiral expansion

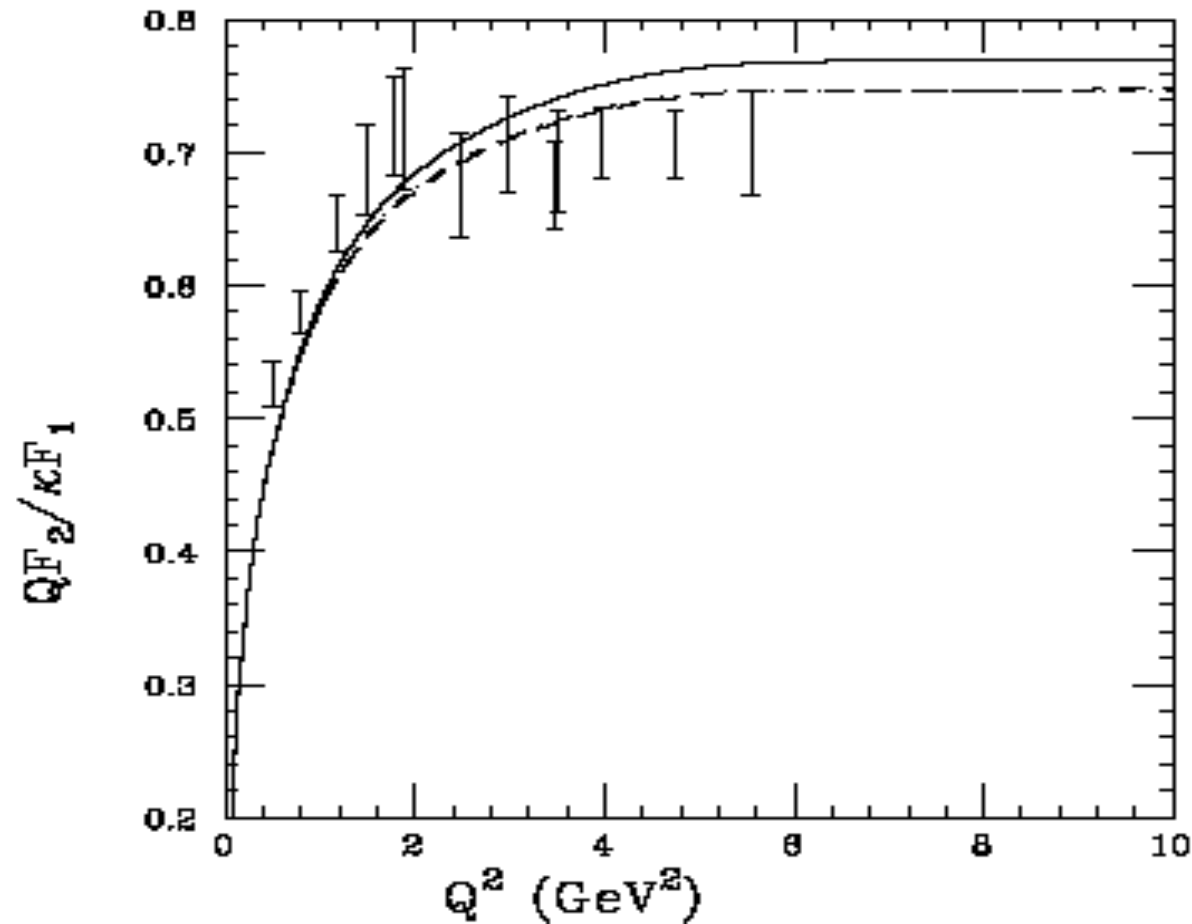
# Neutron Electric Form Factor



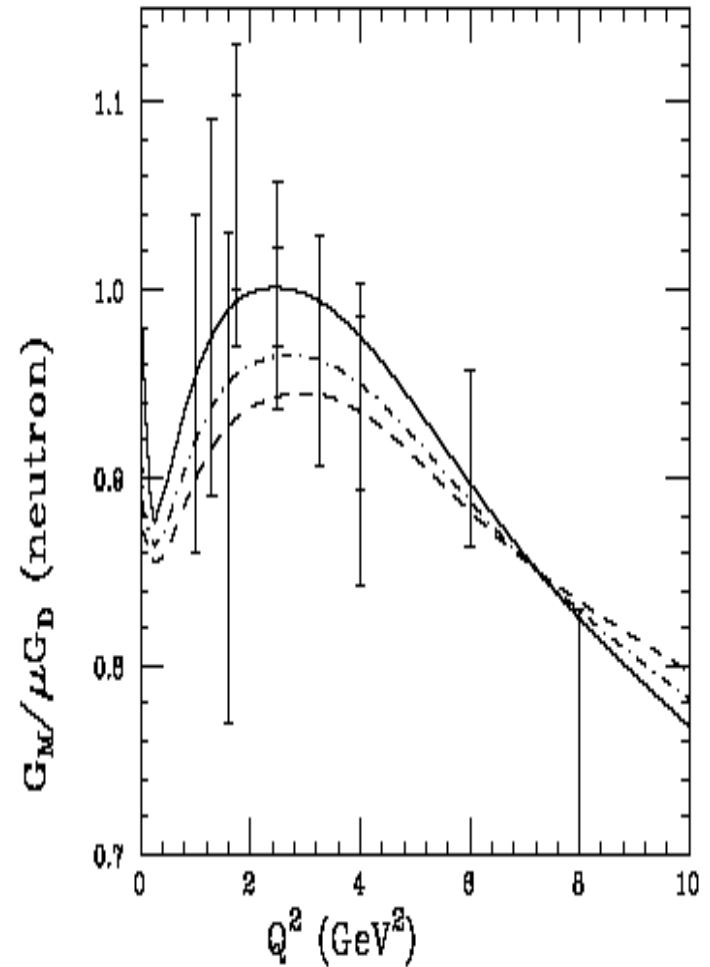
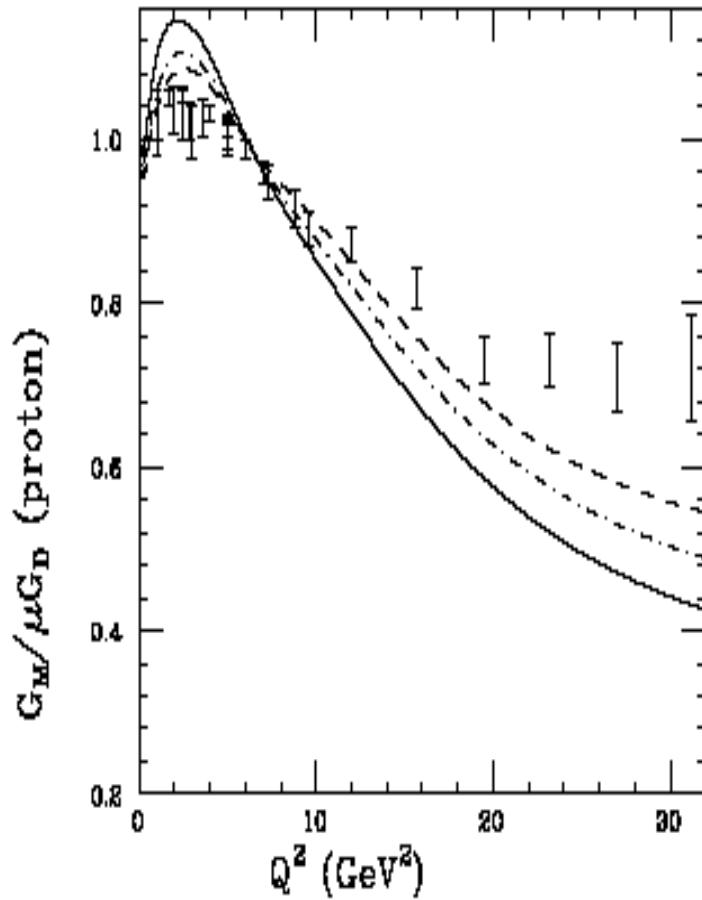
LFCBM 2002- much  
better data now



# Ratio of Pauli to Dirac Form



# Two More Form Factors Needed



# OAM content of light front cloudy bag model

$$\Sigma \rightarrow \left( Z - \frac{1}{3} P_{N\pi} + \frac{5}{3} P_{\Delta\pi} \right) \Sigma$$

Schreiber, Thomas PLB215, 141(88)

$$LFCBM : P_{N\pi} \approx .25, P_{\Delta\pi} = 0$$

$$\Sigma \rightarrow \frac{2}{3} \Sigma \sim \frac{2}{3} \frac{3}{4} = \frac{1}{2}$$

Can now include



Alberg, Miller PRL 108 (2012) 172001

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# 2011 Update model

- In LFCBM  $G_E/G_M$  falls too fast with  $Q^2$
- New data -slower fall, flavor decomposition not good Cates et al  
*Phys.Rev.Lett.* 106 (2011) 252003
- get smaller quark spin?
- Many invariant forms of nucleon wave function
- Cloet & Miller [arXiv:1204.4422](https://arxiv.org/abs/1204.4422) quark di-quark model:
- uses other invariant wave functions

(Brodsky, Hiller, Karmanov, Hwang PRD 2001)

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# Cloet Miller 2011-12

Scalar diquark

$$\Phi_{\lambda_q \lambda_D}^{\lambda_N}(k, p) = \bar{u}(k, \lambda_q) \left[ \varphi_1^s + \frac{M}{p^+} \gamma^+ \varphi_2^s \right] u_N(p, \lambda_N) \\ + \bar{u}(k, \lambda_q) \varepsilon_\nu^*(q, \lambda_D) \gamma^\nu \gamma_5 \left[ \varphi_1^a + \frac{M}{p^+} \gamma^+ \varphi_2^a \right] u_N(p, \lambda_N)$$

Axial vector diquark

$$|p\rangle = \frac{1}{\sqrt{2}} |u S_0\rangle + \frac{1}{\sqrt{6}} |u T_0\rangle - \frac{1}{\sqrt{3}} |d T_1\rangle, \\ \varphi_1 = \frac{1}{(M_0^2 + \beta^2)^\gamma}, \quad \varphi_2 = c \frac{(M_0 - M)}{2M} \varphi_1.$$

**Plus pion cloud- 9 parameters**

$\chi^2$	$m$	$M_s$	$M_a$	$c_s$	$\beta_s$	$\gamma_s$	$c_a$	$\beta_a$	$\gamma_a$	$\Lambda$	$\mu_p (\mu_N)$	$\mu_n (\mu_N)$
0.078516	0.191	0.414	0.167	1.509	1.226	5.719	0.008	1.104	8.586	1.035	2.794	-1.849

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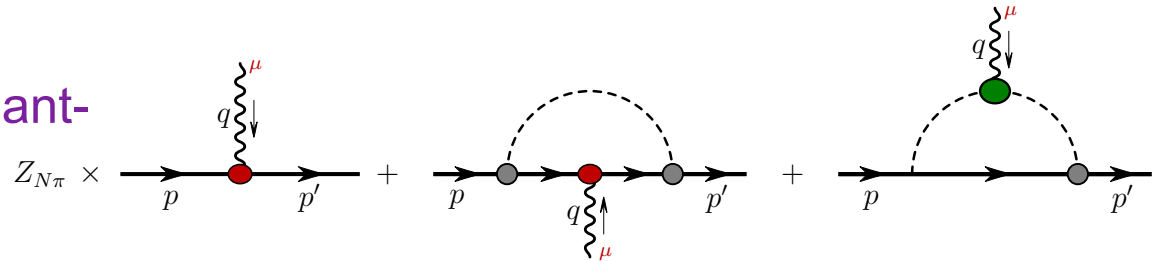
**Plus pion cloud- 9 parameters**

$\chi^2$	$m$	$M_s$	$M_a$	$c_s$	$\beta_s$	$\gamma_s$	$c_a$	$\beta_a$	$\gamma_a$	$\Lambda$	$\mu_p (\mu_N)$	$\mu_n (\mu_N)$
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# Cloet & Miller '11-'12

Model proton wave function: quark-diquark

Lorentz and rotationally invariant-different forms!



Light front variables

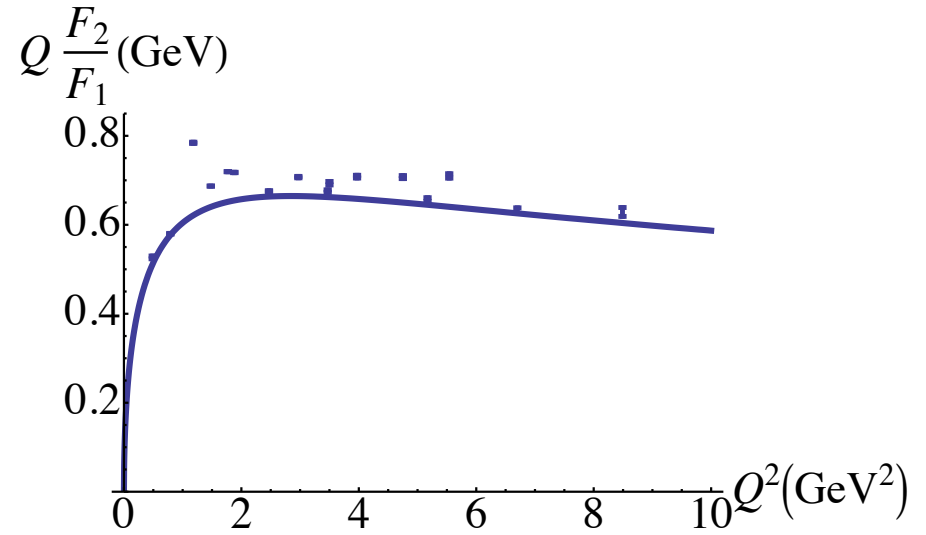
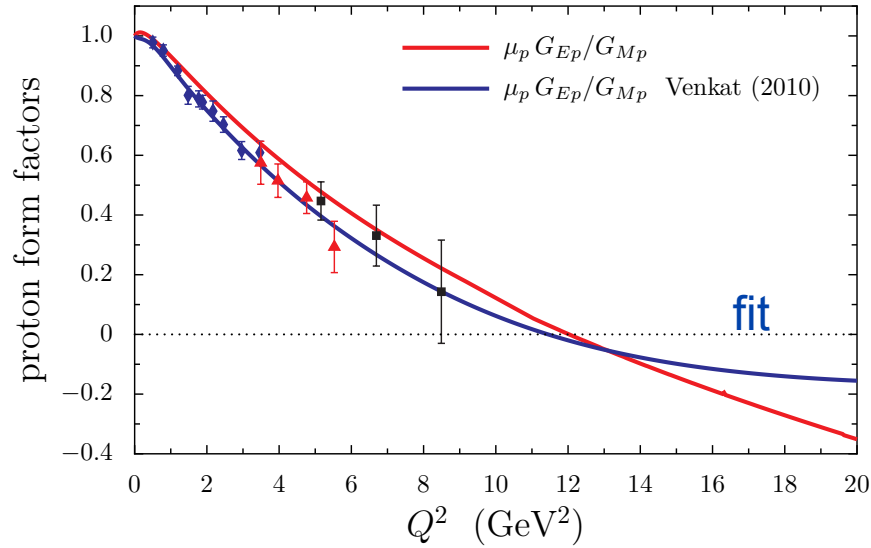
Dirac spinors-orbital angular momentum

Pion cloud of Light Front Cloudy Bag Model -GAM PRC 66 (2002) 032201

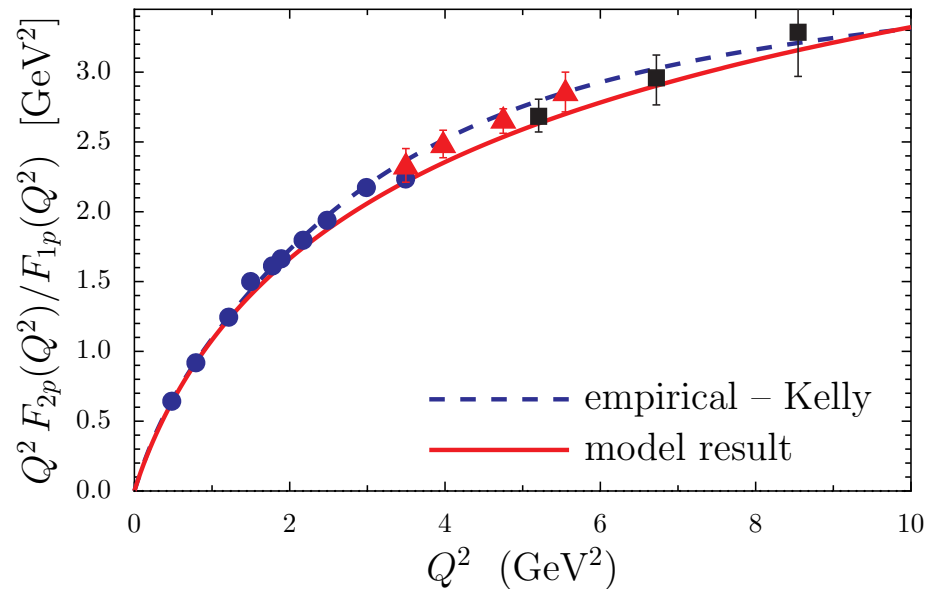
Could be improved according to Alberg Miller **Phys.Rev.Lett.** 108 (2012) 172001



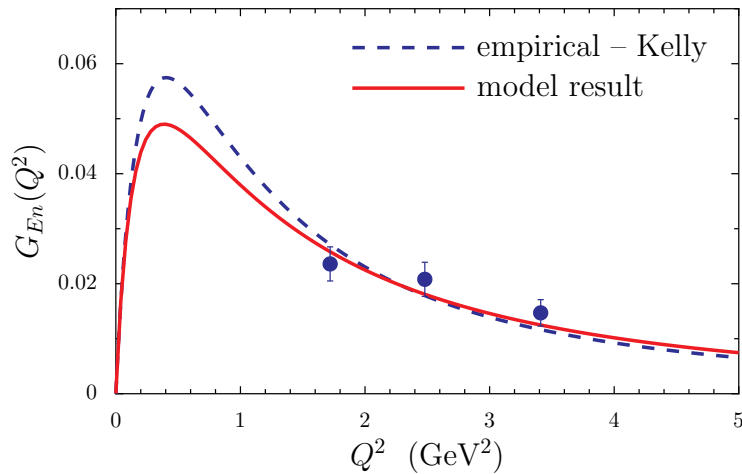
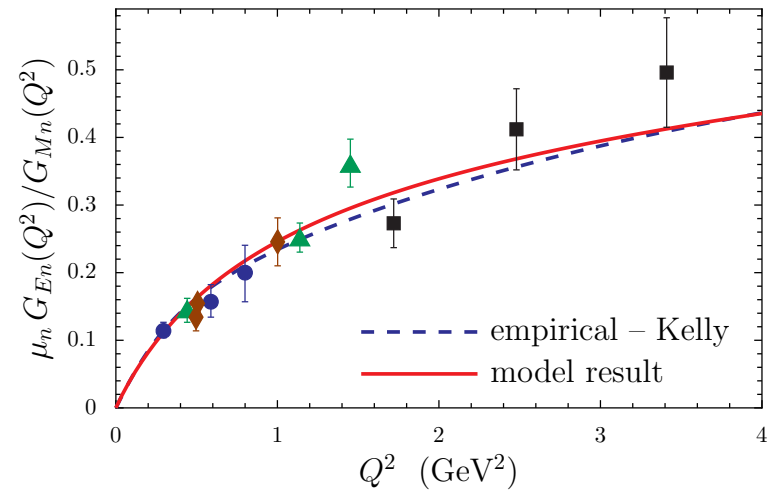
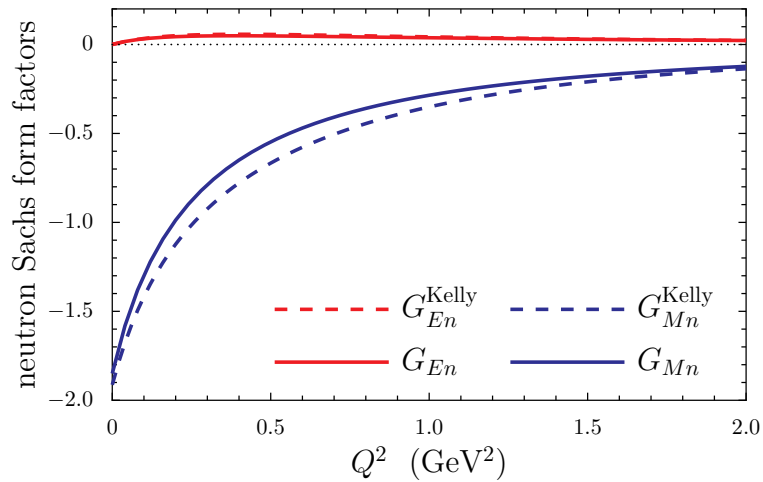
# Cloet & Miller '11-'12-proton results



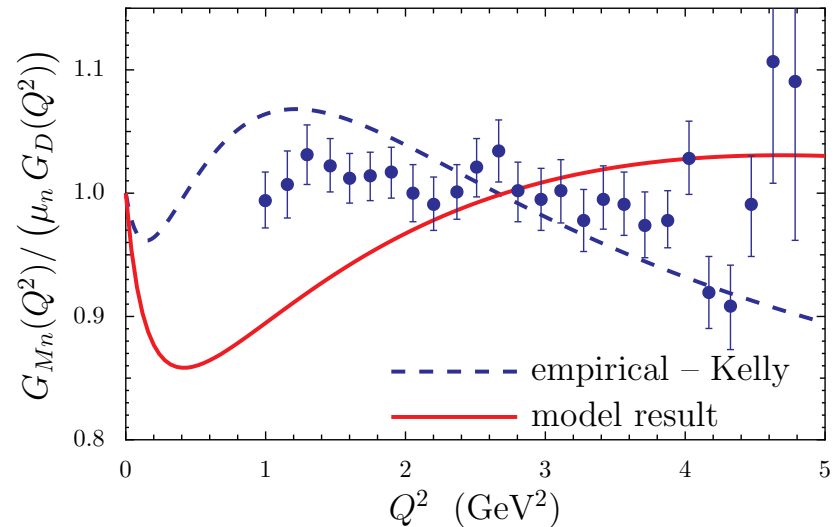
Data Jones, Gayou,  
Puckett, Perdrisat,  
Punjabi etc



# Neutron form factors



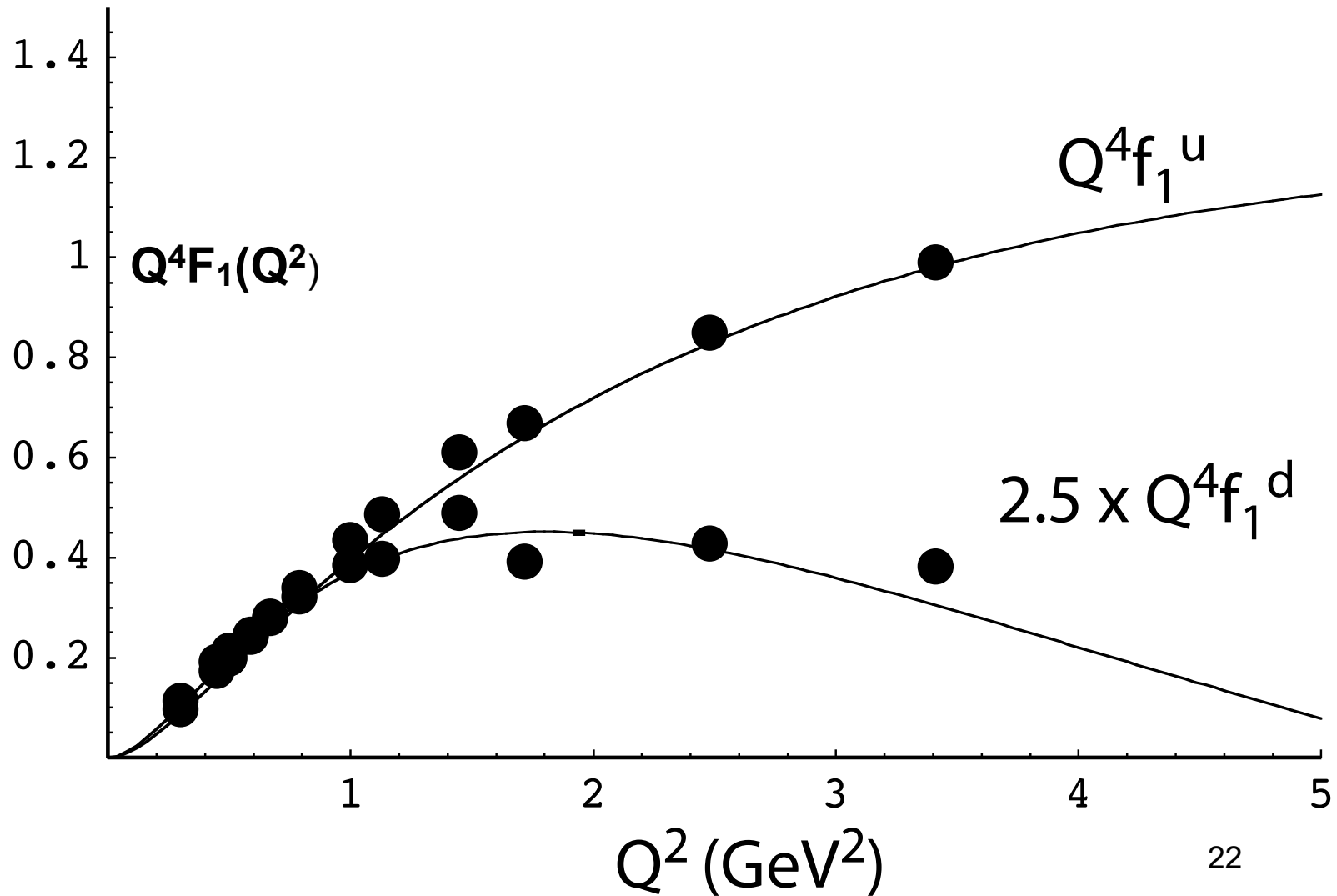
Riordan et al data



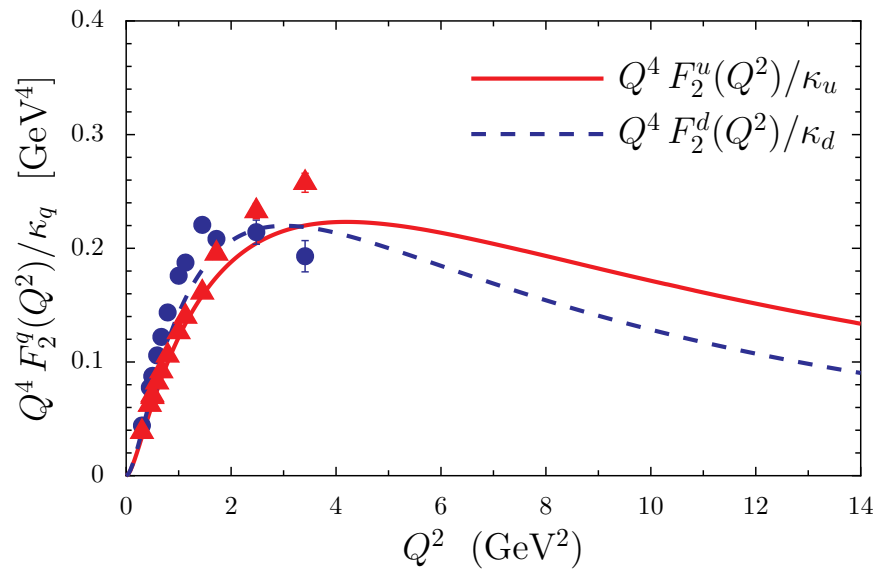
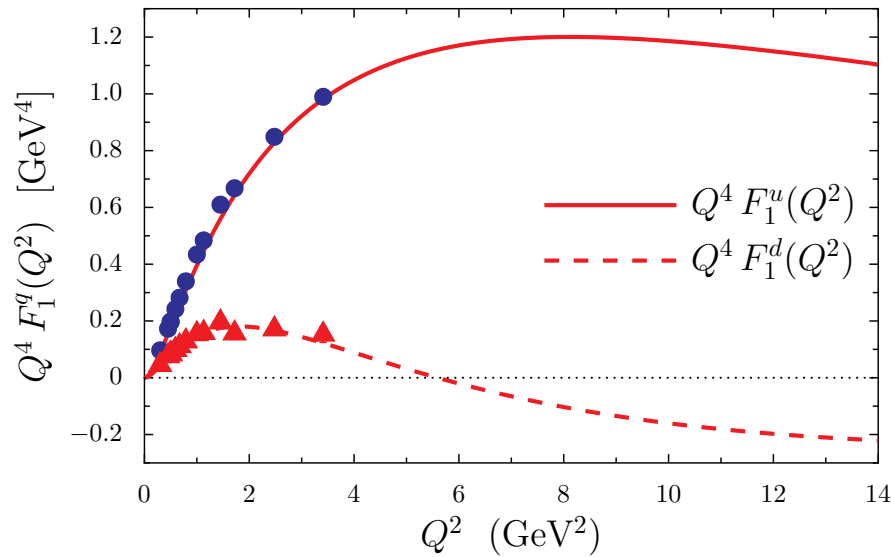
Data Lachniet et al

# Flavor separation: Cates, de Jager, Riordan, Wojtsekhowski

PRL 106,252003

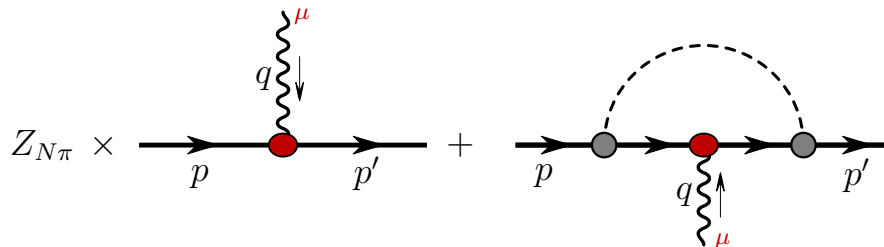


# More flavor separation



Data  
Cates et al  
Jones et al  
Gayou et al  
Gayou et al  
Puckett et al  
Riordan et al  
Zhu et al  
Bermuth et al  
Warren et al  
Glazier et al  
Plaster et al

# Quark-Diquark model -spin content



$$\Delta q = q_+(x) - q_-(x), \quad \Delta\Sigma = \Delta u + \Delta d, \quad \text{NRQM } \Delta u = 4/3, \quad \Delta d = -1/3$$

$$\Delta u = \frac{3}{2}\Delta q_s + \frac{1}{2}\Delta q_a, \quad \Delta d = \Delta q_a = -0.424$$

$$\Delta q_s = 0.754, \quad \Delta u = 0.921, \quad \Delta\Sigma = 0.497 \text{ no pion cloud}$$

$$\Delta\Sigma_\pi = (Z_{N\pi} + \Delta q_N^\pi)(\Delta u + \Delta d) = (0.706 + \underline{0.281})(0.497) = 0.365$$

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No gluons, so effects of quark orbital angular momentum

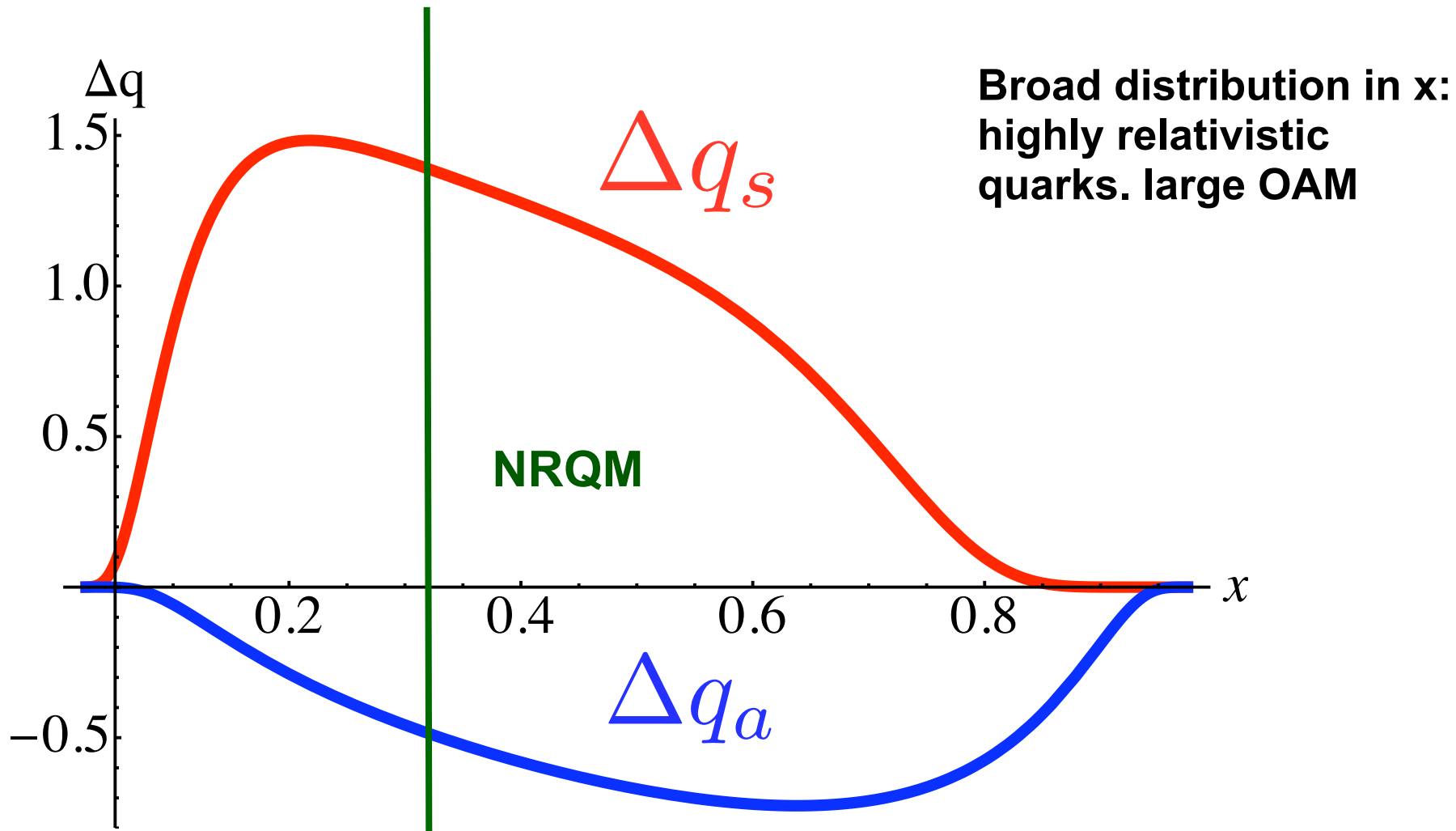
Changes to naive quark model are modest, not revolutionary

# Understanding Parameters and spin content

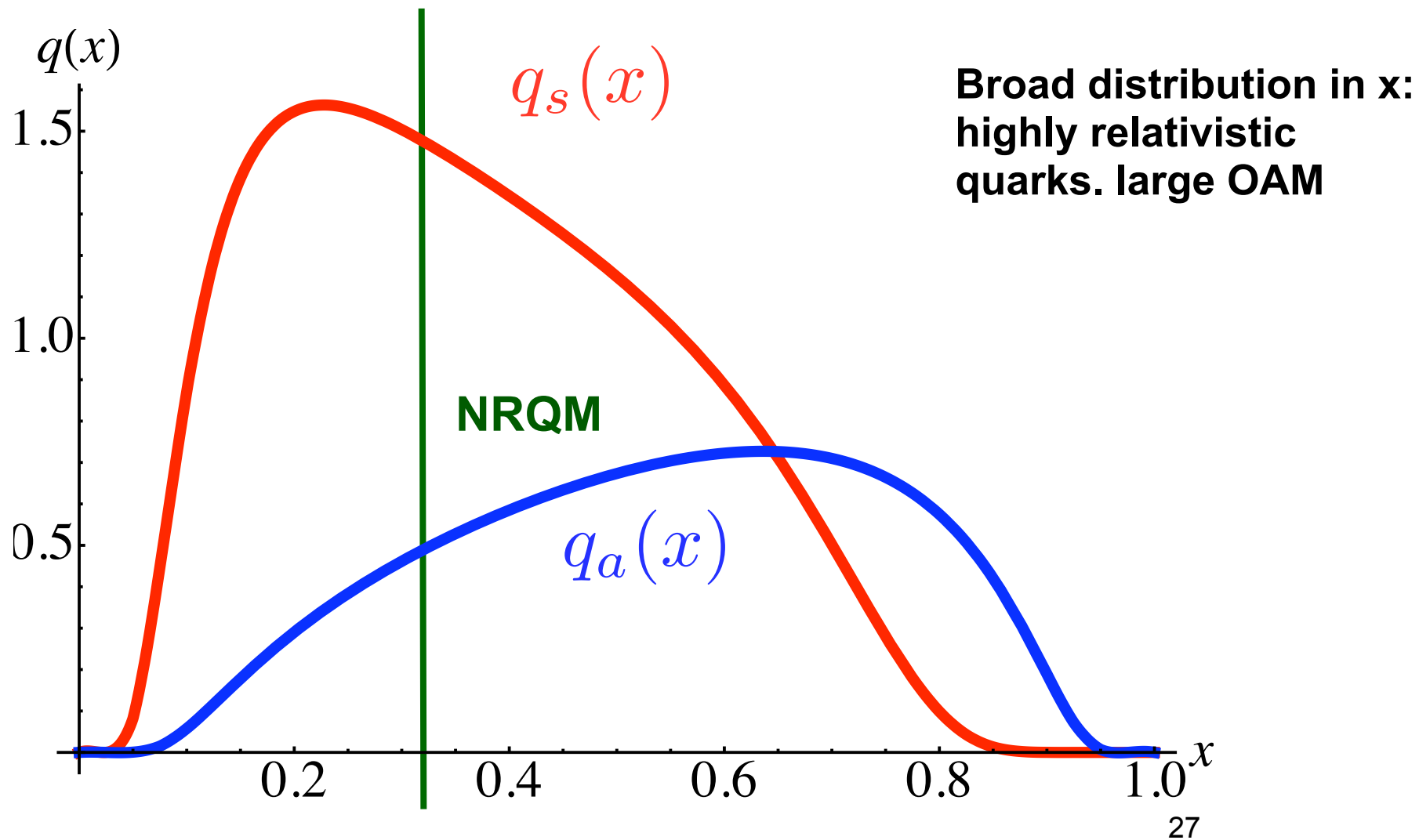
$\chi^2$	$m$	$M_s$	$M_a$	$c_s$	$\beta_s$	$\gamma_s$	$c_a$	$\beta_a$	$\gamma_a$	$\Lambda$	$\mu_p (\mu_N)$	$\mu_n (\mu_N)$
0.078516	0.191	0.414	0.167	1.509	1.226	5.719	0.008	1.104	8.586	1.035	2.794	-1.849

- Lighter quark mass 191 vs 267 MeV
- Relativistic effects are larger than in earlier models, therefore more OAM
- Axial vector di-quark has enhanced components with quark spin opposing proton spin, signature of OAM

# Integrands for spin content



# Quark distribution $q(x)$ -non evolved





# Summary

- Relativistic light front quark model with pion cloud can reproduce nucleon form factors
- Flavor separation works and is testable in the future
- Model quark spin is 36.5 % of total angular momentum, quark OAM is important
- (Relativistic) quark model alive and well, proton is made mainly of three quarks