

# *Hunting Traces of TeV-Scale Physics in Low-Energy Processes*

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Collider experiments probe new physics **directly**. Precision, low-energy measurements probe new physics **indirectly**, i.e., through the failure of robust Standard Model predictions.

## Some Basic Questions

- How do we know there is a “Beyond”?
- Why do we think there is new physics at the TeV scale?
- Why do we think we can probe TeV-scale physics in precision, low-energy experiments?
- Are indirect searches for new TeV-scale physics rendered obsolete by the LHC?

# How do we know there is a “Beyond”?

There is much theoretical “evidence” that the Standard Model is incomplete — *it leaves many questions unanswered.*

Here are a few.

- It does not explain dark matter, dark energy
- It does not explain the number of generations nor the large range of fermion masses
- It does not explain the weak mass scale (the “hierarchy” problem)
- It cannot explain the baryon asymmetry of the Universe

*Most notably, the Standard Model only explains 5% of the known Universe.*  
There is much observational evidence for dark matter.

Note, too, recent direct evidence from the “bullet” cluster:

[Clowe et al., astro-ph/0608407]



# How do we know there is a “Beyond”?

We have, moreover, direct empirical evidence from terrestrial experiments for physics beyond the Standard Model.

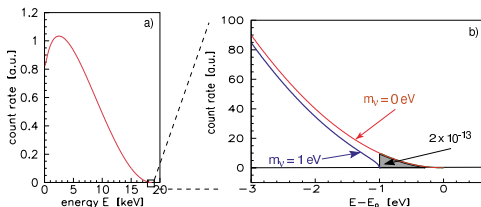
Empirical evidence for neutrino oscillations allows us to conclude  $\Delta m^2 \equiv m_i^2 - m_j^2 \neq 0$  with surety.

That is, neutrinos have mass.

We see then that the particle content of the Standard Model is incomplete: there is a  $\nu_R$ , which is “sterile” under Standard Model interactions.

This is not to say that the effects of neutrino mass are large.

Distortions in the shape of the electron energy spectrum in  ${}^3\text{H}$   $\beta$ -decay near its endpoint bound  $m_\nu^2$ . [KATRIN, loi]



# The Emergence of Physics Beyond the Standard Model

Why do we think there is new physics at  $\sim 1$  TeV?

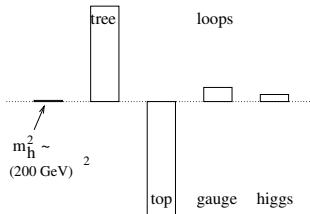
[Schmaltz, hep-ph/0210415]

Suppose we assume the Standard Model is valid for scales  $E \leq \Lambda$ , where  $\Lambda \sim \mathcal{O}(1\text{TeV})$ .

At one-loop level, we find large corrections to the tree-level Higgs mass  $m_{\text{tree}}$ .

All contributions must sum to  $m_H^2 \sim (200\text{GeV})^2$ , but each one  $\sim \Lambda^2$ !

At  $\Lambda = 10$  TeV,  $m_{\text{tree}}$  must be tuned to one part in 100!

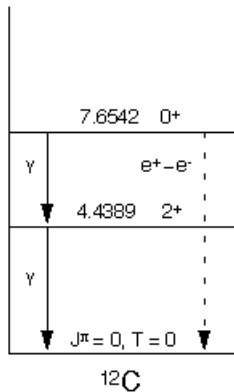


New physics at the TeV scale can enter to make the cancellations “natural.”

# “Fine-Tuning” does exist in Nature



$$\frac{7.2747}{3\alpha}$$



$$\frac{7.3666}{\alpha + {}^8\text{Be}}$$

[Hoyle, 1953; Cook, Fowler, Lauritsen, Lauritsen, 1957]

# Can we probe TeV-scale physics at low energies?

Yes. Let's illustrate this in a **toy model**.

Consider the Gerasimov-Drell-Hearn sum rule:

[Gerasimov, 1966; Drell and Hearn, 1966.]

$$\frac{2\pi\alpha\kappa_i^2}{M^2} = \frac{1}{\pi} \int_{\omega_{\text{th}}}^{\infty} \frac{\Delta\sigma_i}{\omega} d\omega \equiv \frac{1}{\pi} \int_{\omega_{\text{th}}}^{\infty} \frac{(\sigma_{\text{Pi}}(\omega) - \sigma_{\text{Ai}}(\omega))}{\omega} d\omega$$

The photon and nucleon spins are aligned parallel (P) or anti-parallel (A).

A *linearized* sum rule also exists:

[Holstein, Pascalutsa, and Vanderhaeghen, 2005.]

$$\frac{4\pi\alpha\delta\kappa_i}{M^2} = \frac{1}{\pi} \int_{\omega_{\text{th}}}^{\infty} \frac{\Delta\tilde{\sigma}_i}{\omega} d\omega$$

where  $\Delta\tilde{\sigma} \equiv \partial\Delta\sigma/\partial\kappa_{0i}|_{\kappa_{0p}=\kappa_{0n}=0}$ . We can compute the contribution to  $\kappa_i$  from

$$\mathcal{L}_{\pi NN} = \frac{g}{2M} \bar{\psi} \gamma^\mu \gamma^5 \tau^a \psi \partial_\mu \pi^a$$

We thus determine the loop contribution to  $\kappa_i$  from a “pion” produced at some inelastic threshold  $\omega_{\text{New}}$  in  $\gamma - p$  scattering.

# Can we probe TeV-scale physics at low energies?

As  $\mu \equiv M_\pi/M \rightarrow \infty$  this yields

$$\begin{aligned}\delta\kappa_p &= \frac{g^2}{(4\pi)^2} (5 - 4 \ln \mu) \frac{1}{\mu^2} + \mathcal{O}(\mu^{-4}) \\ \delta\kappa_n &= \frac{g^2}{(4\pi)^2} 2(3 - 4 \ln \mu) \frac{1}{\mu^2} + \mathcal{O}(\mu^{-4})\end{aligned}$$

Thus if we choose  $M_\pi \sim 1$  TeV,  $\mu \sim 10^3$ , with  $g^2/4\pi = 13.5$ ,

$$\begin{aligned}\delta\kappa_p &= -2.4 \cdot 10^{-5} & \kappa_p^{\text{exp}} &= 1.792847351(28) \\ \delta\kappa_n &= -5.3 \cdot 10^{-5} & \kappa_n^{\text{exp}} &= -1.9130427(5)\end{aligned}$$

The effects of putative TeV-scale physics on the anom. mag. moments are appreciable.

The empirical anomalous magnetic moments are already sufficiently well-known to be impacted by TeV-scale physics, though these effects are obscured by non-perturbative QCD effects.

**A challenge to lattice QCD!**



# How do we probe new physics in low-energy experiments?

We control non-perturbative QCD effects by exploiting the symmetries of the Standard Model. **Some possibilities:**

## 1. Nuclear, neutron, pion, kaon $\beta$ -decay

Search for non- $V - A$  interactions. Tests of CKM unitarity.

## 2. The effective weak charge of an electron, proton, nucleus

Test the “running” of  $\sin^2(\theta_W(Q))$  away from the  $Z^0$ -pole.

## 3. Neutron, Atom, Molecular Electric Dipole Moments

The Standard Model produces **negligibly small** EDMs. A measurably non-zero EDM connotes the presence of physics beyond the Standard Model.

# Beyond “V-A” in Neutron $\beta$ -Decay

The search for non-V-A interactions continues...

$$\begin{aligned}\mathcal{H}_{int} = & (\bar{\psi}_p \psi_n)(C_S \bar{\psi}_e \psi_\nu + C'_S \bar{\psi}_e \gamma_5 \psi_\nu) + (\bar{\psi}_p \gamma_\mu \psi_n)(C_V \bar{\psi}_e \gamma^\mu \psi_\nu + C'_V \bar{\psi}_e \gamma^\mu \gamma_5 \psi_\nu) \\ & - (\bar{\psi}_p \gamma_\mu \gamma_5 \psi_n)(C_A \bar{\psi}_e \gamma^\mu \psi_\nu + C'_A \bar{\psi}_e \gamma^\mu \gamma_5 \psi_\nu) + (\bar{\psi}_p \gamma_5 \gamma_\mu \psi_n)(C_P \bar{\psi}_e \gamma_5 \psi_\nu + C'_P \bar{\psi}_e \psi_\nu) \\ & + \frac{1}{2}(\bar{\psi}_p \sigma_{\lambda\mu} \psi_n)(C_T \bar{\psi}_e \sigma^{\lambda\mu} \psi_\nu + C'_T \bar{\psi}_e \sigma^{\lambda\mu} \gamma_5 \psi_\nu) + h.c.\end{aligned}$$

[Lee and Yang, 1956; note also Gamow and Teller, 1936]

$C'_X$  denote parity-nonconserving interactions.

In polarized neutron (nuclear)  $\beta$ -decay one more correlation appears:  $b$

$$\begin{aligned}d^3\Gamma = & \frac{1}{(2\pi)^5} \xi E_e |\mathbf{p}_e| (E_e^{\max} - E_e)^2 \times \\ & [1 + a \frac{\mathbf{p}_e \cdot \mathbf{p}_\nu}{E_e E_\nu} + b \frac{m}{E_e} + \mathbf{P} \cdot (A \frac{\mathbf{p}_e}{E_e} + B \frac{\mathbf{p}_\nu}{E_\nu} + D \frac{\mathbf{p}_e \times \mathbf{p}_\nu}{E_e E_\nu})] dE_e d\Omega_e d\Omega_\nu\end{aligned}$$

[Jackson, Treiman, and Wyld, Phys. Rev. 106, 517 (1957)]

Note, e.g.,

$$b\xi = \pm 2\text{Re}[C_S C_V^* + C'_S C_V'^* + 3(C_T C_A^* + C'_T C_A'^*)]$$

If the electron polarization is also detected, more correlations enter.

# Limits from Nuclear $\beta$ -Decay

Recent limits on  $b$  come from nuclear  $\beta$ -decay:

- $b = +0.0001 \pm 0.0026$  ( $|C_S/C_V| \leq 0.0013$ )  
from survey of  $0^+ \rightarrow 0^+$  transitions in nuclei  
[Towner and Hardy, PRL 94, 092502 (2005)]
- $\tilde{a} \equiv a/(1 + bm_e/\langle E_e \rangle) = 0.9981 \pm 0.0030 \pm 0.0037$   
from  $0^+ \rightarrow 0^+$  pure Fermi decay of  $^{38m}\text{K}$   
[A. Gorelov et al., PRL 94, 142501 (2005)]

Both limits are consistent with the Standard Model.

Tests to this precision do not rely on the knowledge of nuclear structure in any way.

Ingredients: CVC hypothesis ( $g_V = (1 + \mathcal{O}(\alpha))V_{ud}$ ), recoil expansion ( $\mathcal{O}(E)/M \ll 1$ ).

It is possible to test the CVC hypothesis (and more) in neutron  $\beta$ -decay through comparison of the  $a$  and  $A$  correlation coefficients. [SG, Chi Zhang, 2001]

# The Cabibbo-Kobayashi-Maskawa (CKM) Matrix

$$\begin{pmatrix} d' \\ s' \\ b' \end{pmatrix}_{\text{weak}} = V_{\text{CKM}} \begin{pmatrix} d \\ s \\ b \end{pmatrix}_{\text{mass}} ; \quad V_{\text{CKM}} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$

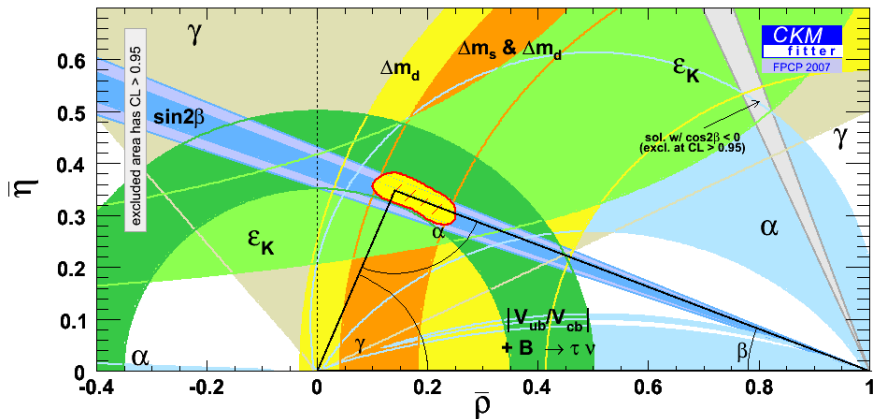
In the **Wolfenstein parametrization (1983)**

$$V_{\text{CKM}} = \begin{pmatrix} 1 - \frac{\lambda^2}{2} & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \frac{\lambda^2}{2} & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix} + \mathcal{O}(\lambda^4)$$

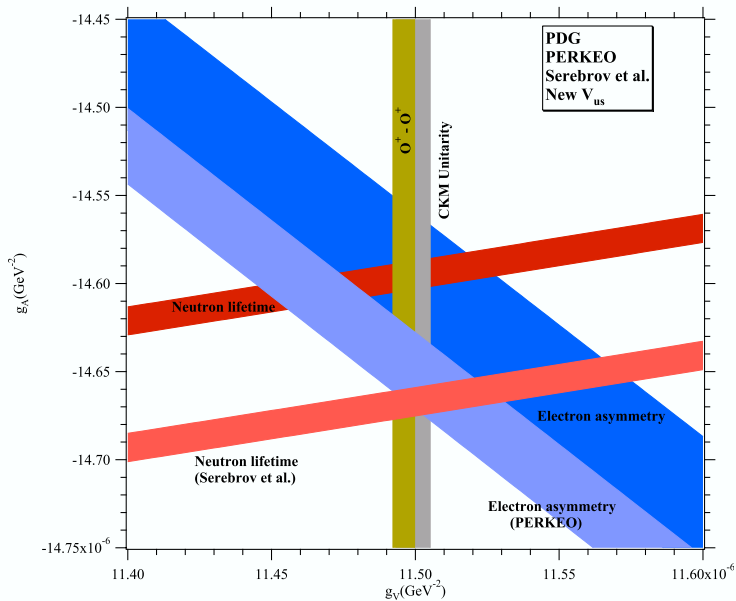
where  $\lambda \equiv |V_{us}| \simeq 0.22$  and is thus “small”.  $A, \rho, \eta$  are real.

- There are three “generations” of particles.  
Thus, the CKM matrix is unitary [  $V_{\text{CKM}}^\dagger V_{\text{CKM}} = 1$  ]
- The unitarity of the CKM matrix and the structure of the weak currents implies that four parameters capture the CKM matrix.
- A real, orthogonal  $3 \times 3$  matrix contains three parameters. The fourth parameter ( $\eta$ ) must make  $V_{\text{CKM}}$  complex.
- All CP-violating phenomena are encoded in  $\eta$ .

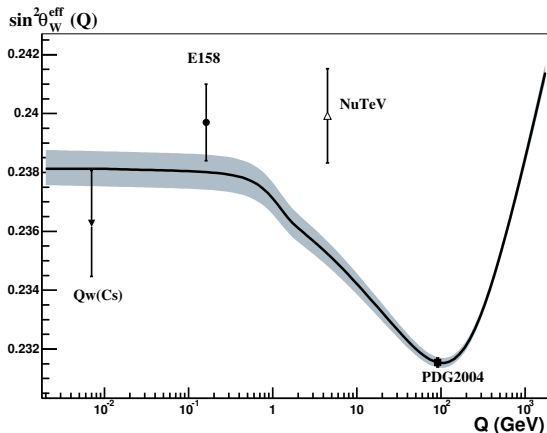
# Testing CKM Unitarity – “the” Unitarity Triangle



[CKMfitter: hep-ph/0104062, hep-ph/0406184 ; <http://ckmfitter.in2p3.fr> – June, 2007 update]



# The Effective Weak Charge



[E158, Anthony et al, PRL 95 (2005) 081601]

[Theory: Czarnecki and Marciano, 1996, 2000; Erler and Ramsey-Musolf, 2005]

**Future experimental studies should yield much sharper tests.**

# The Electric Dipole Moment - A Primer

The electric dipole moment  $d$  of a particle with spin  $S$  is defined via

$$\mathcal{H} = -d \frac{\mathbf{S}}{S} \cdot \mathbf{E}$$

$d \neq 0$  violates both  $T$  and  $P$ .

E. M. Purcell and N. F. Ramsey, "On the Possibility of Electric Dipole Moments for Elementary Particles and Nuclei," Phys. Rev. 78, 807 (1950):

The argument against electric dipoles, in another form, raises the question of parity.... But there is no compelling reason for excluding this possibility....

Context: Dirac (1949) – A magnetic monopole violates  $P$ ,  $T$ .

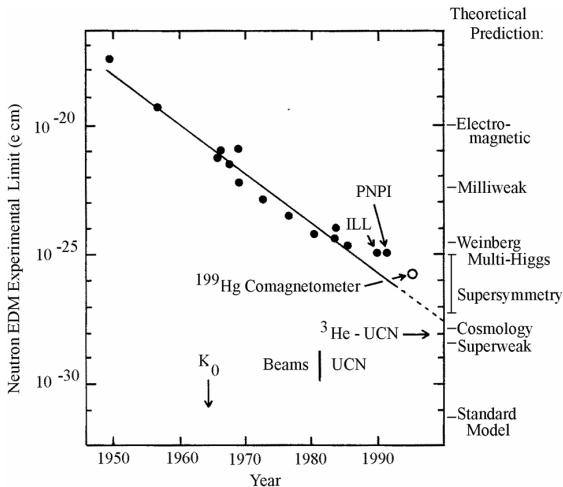
A experimental strategy for  $d$ :

$$\mathcal{H} = -\mu \frac{\mathbf{S}}{S} \cdot \mathbf{B} - d \frac{\mathbf{S}}{S} \cdot \mathbf{E}$$

Limit set by neutron density, observation time, and the strength of the applied electric field.



# Neutron EDM Timeline – The “Model Killer”



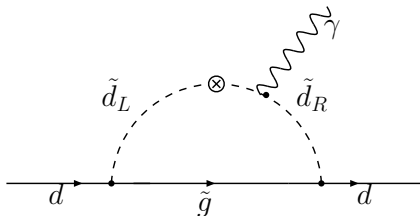
[S. Lamoreaux (Yale)]

# Electric Dipole Moments

EDM measurements exist on neutrons, paramagnetic atoms ( $^{205}\text{Tl}$ : “ $d_e$ ”), and diamagnetic atoms.

Supersymmetric models naturally “overproduce” electric dipole moments – picking parameters at random invariably lead to EDMs at odds with experiment, the “SUSY CP problem”.

[Pospelov and Ritz, 2005]

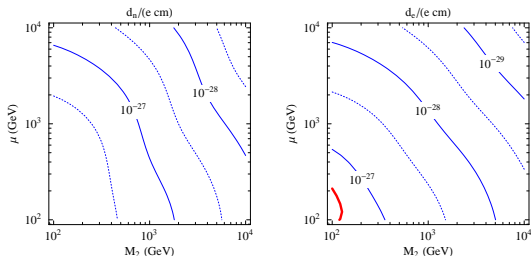


Can resolve by making scalars heavy or CP-violating parameters small.

# Electric Dipole Moments

Models with “split” supersymmetry (heavy scalars!) can still produce significant EDMs at two-loop order:

[Giudice and Romanino, 2006]



The red shows current limit on  $d_e$ .

Both  $d_e$  and  $d_n$  are expected to improve.

$|d_n| \leq 3 \cdot 10^{-26}$  e-cm [Baker et al., ILL, hep-ex/0602020] to  $10^{-28}$  e-cm [LANL/SNS EDM expt]

$|d_e| \leq 1.6 \cdot 10^{-27}$  e-cm [Regan, Commins, Schmidt, DeMille, PRL 88, 071805 (2002)]

to  $10^{-29(31)}$  e-cm [DeMille]

# Electric Dipole Moments

Estimates of hadronic electric dipole moments depend on the hadron's non-perturbative structure.

For example, in the SM (CKM mechanism of CP violation), long-distance effects ( $\pi$ -loop) give for the neutron

$$d_n^{\text{KM}} \simeq 10^{-32} \text{e-cm} \quad [\text{Gavela et al., PLB 1982; Khriplovich \& Zhitnitsky, PLB 1982}]$$

whereas a LL computation in three-loops yields

$$d_d^{\text{KM}} \simeq 10^{-34} \text{e-cm}. \quad [\text{Czarnecki \& Krause, PRL 1997}]$$

cf. QCD sum rules w/  $\dim \leq 5$  CP-violating ops. give  $d_n$  to  $\sim 50\%$

[Pospelov & Ritz, PRL 1999]

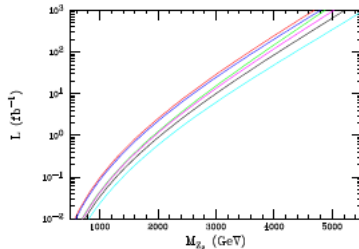
Evaluating  $d_n$  and  $d_p$  is also important to interpreting the  $^2\text{H}$  EDM.

[Lebedev et al., PRD 2004]

The quality of the nucleon matrix element computations needed to extract bounds on fundamental Lagrangian parameters can be tested by confronting the empirical anomalous moments. [Brodsky, SG, Hwang, 2006]

The Lesson of the  $Z'$ . Note  $5\sigma$  discovery reach:

The LHC should accumulate  $10\text{fb}^{-1}$  in  $L$  *each year*.



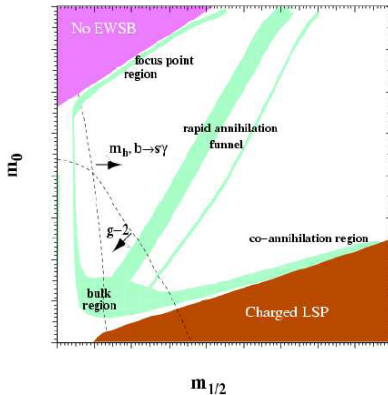
[T. Rizzo (SLAC), TASI 06]

The LHC should quickly find a  $Z'$  of a few TeV in mass — and eventually determine its spin.

But is it *really* a  $Z'$ ? For that, determining its couplings to SM fermions are essential... and low-energy experiments can play a crucial role.

# Complementarity

In supersymmetric models with restricted parameter space (note the “CMSSM”), the constraints of the superpartner masses from cosmological and low-energy data are severe. **Caveat Emptor!**



[M. Schmitt (Northwestern), SSI 2007, after J. Feng, astro-ph/0511043 and refs. therein]

Major ticks are separated by 100 GeV.

We look forward to an era of discovery!