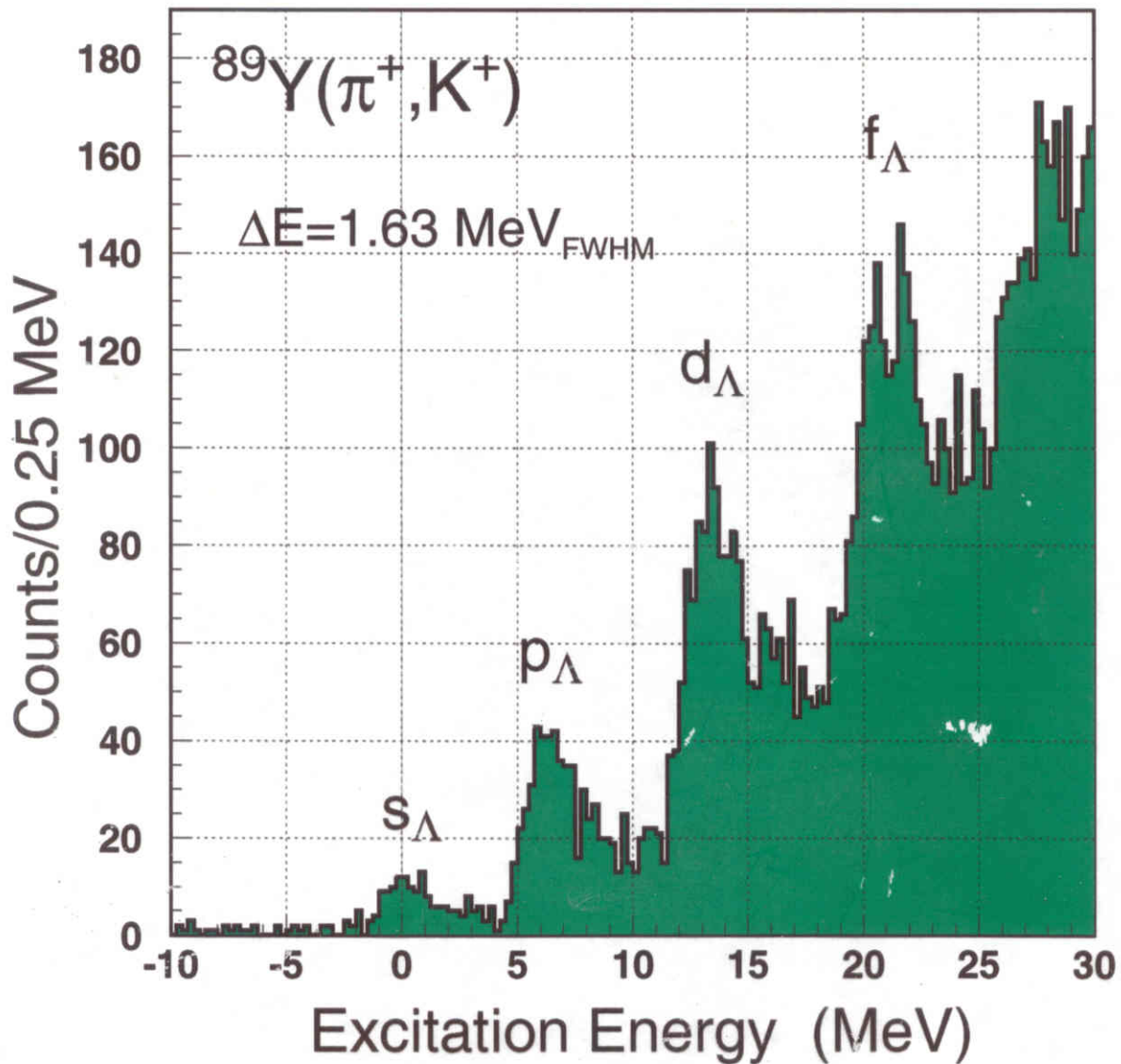


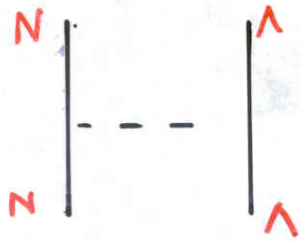
KEK E369



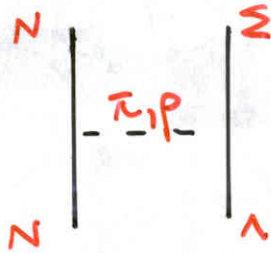
H. Hotochi et al., PRC 64 (2001) 044302

$S = -1 \quad T = 1/2$

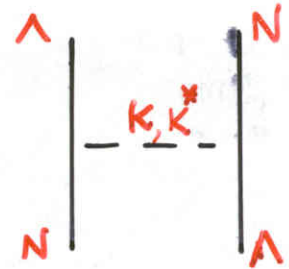
$\Lambda N - \Sigma N$



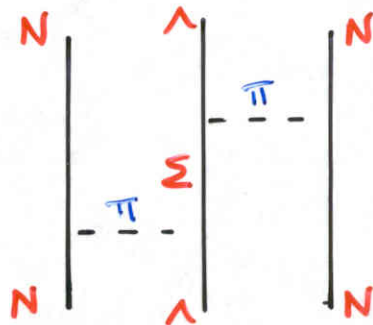
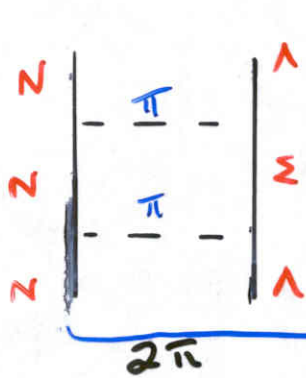
no π



1 π

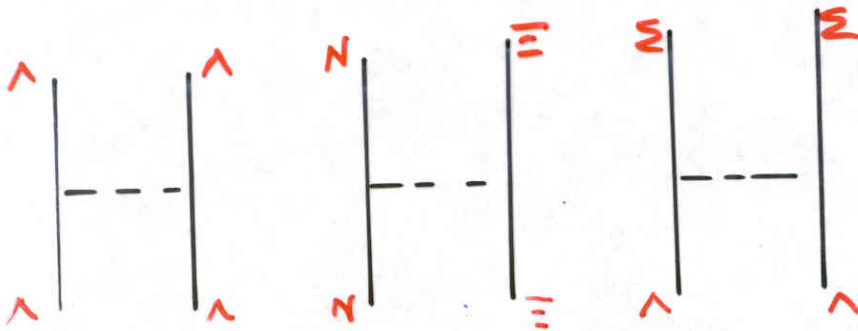


strange

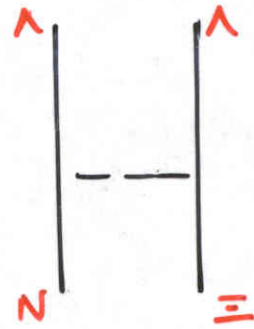


$S = -2 \quad T = 0$

$\Lambda \Lambda - \Xi N - \Sigma \Sigma$



Non-strange



strange

ΛN (YN) interaction parameters

$V_{N\Lambda}$	$s_N s_\Lambda$	$p_N s_\Lambda$	${}^7_\Lambda\text{Li}$ values MeV
V_0	I_0^e	$\bar{V} = \frac{1}{2}(I_0^e + I_1^o)$	(-1.22)
$V_\sigma s_N \cdot s_\Lambda$	I_0^e	$\Delta = \frac{1}{2}(I_0^e + I_1^o)$	0.480
$V_\Lambda l_{N\Lambda} \cdot s_\Lambda$		$S_\Lambda = \frac{1}{2}I_1^o$	-0.010
$V_N l_{N\Lambda} \cdot s_N$		$S_N = \frac{1}{2}I_1^o$	-0.400
$V_T S_{12}$		$T = \frac{1}{3}I_1^o$	0.021

Free-Space YN Interactions

- Spin-spin interaction (Δ) is basically undetermined
- Similarly for odd-state central interaction
- Similarly for strength of $\Lambda - \Sigma$ coupling
- NSC97 models - Th.A. Rijken, V.J.G. Stoks, and Y. Yamamoto
Phys. Rev. C 59 (1999) 21
- NSC97a,b,c $\Delta < 0$, NSC97d,e,f $\Delta > 0$; models e and f favored on these grounds

S-Shell Λ Hypernuclei

Hypernucleus	$J^\pi(gs)$	B_Λ MeV	J^π	E_x MeV
${}^3_\Lambda\text{H}$	$1/2^+$	0.13(5)		
${}^4_\Lambda\text{H}$	0^+	2.04(4)	1^+	1.04(5)
${}^4_\Lambda\text{He}$	0^+	2.39(3)	1^+	1.15(4)
${}^5_\Lambda\text{He}$	$1/2^+$	3.12(2)		

Recent “Exact” Calculations

- $A = 3, 4$ A. Nogga et al., PRL 88 (2002) 172501
Faddeev and Faddeev-Yakubovsky
- $A = 4$ E. Hiyama et al., PRC 65 (2002) 011301(R)
Jacobi-coordinate Gaussian basis
- $A = 3, 4, 5$ H. Nemura et al., PRL 89 (2002) 142504
Stochastic variation with correlated Gaussians

$\Lambda - \Sigma$ coupling for ${}^4_{\Lambda}\text{H}$ and ${}^4_{\Lambda}\text{He}$

Y. Akaishi, T. Harada, S. Shinmura, and Khin Swe Myint
 PRL 84 (2000) 3539

$$|{}^4_{\Lambda}\text{He}(T = 1/2)\rangle = \alpha s^3 s_{\Lambda} + \beta s^3 s_{\Sigma}$$

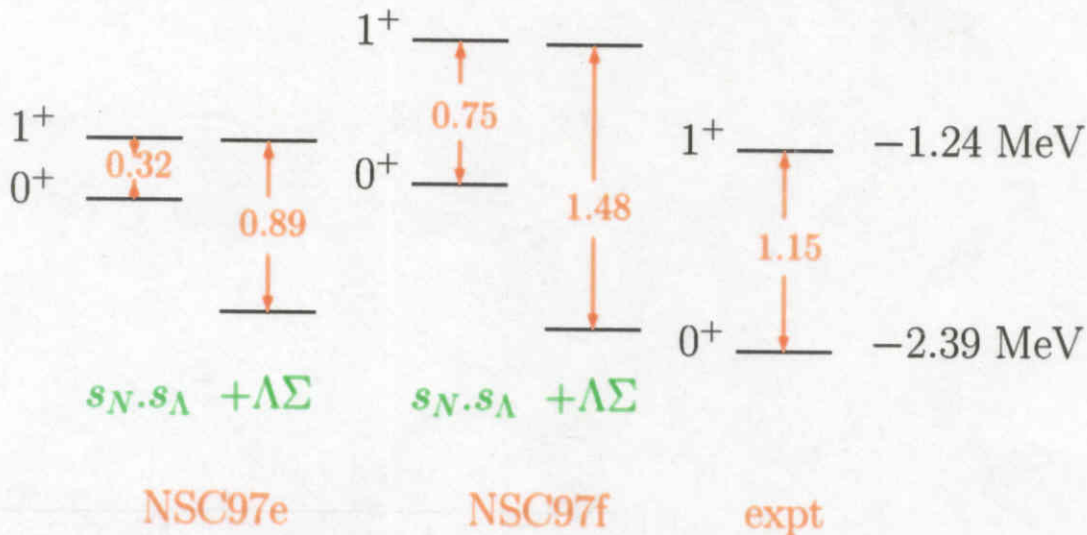
From $\Lambda\text{N} - \Sigma\text{N}$ g matrix for $0s$ orbits

$$v = \langle s^3 s_{\Lambda} | g | s^3 s_{\Sigma} \rangle, \quad \Delta E \sim 80 \text{ MeV}$$

$$0^+ \quad v = \frac{3}{2} {}^3g_{ss} - \frac{1}{2} {}^1g_{ss} \quad \text{Admixture} \sim v/\Delta E$$

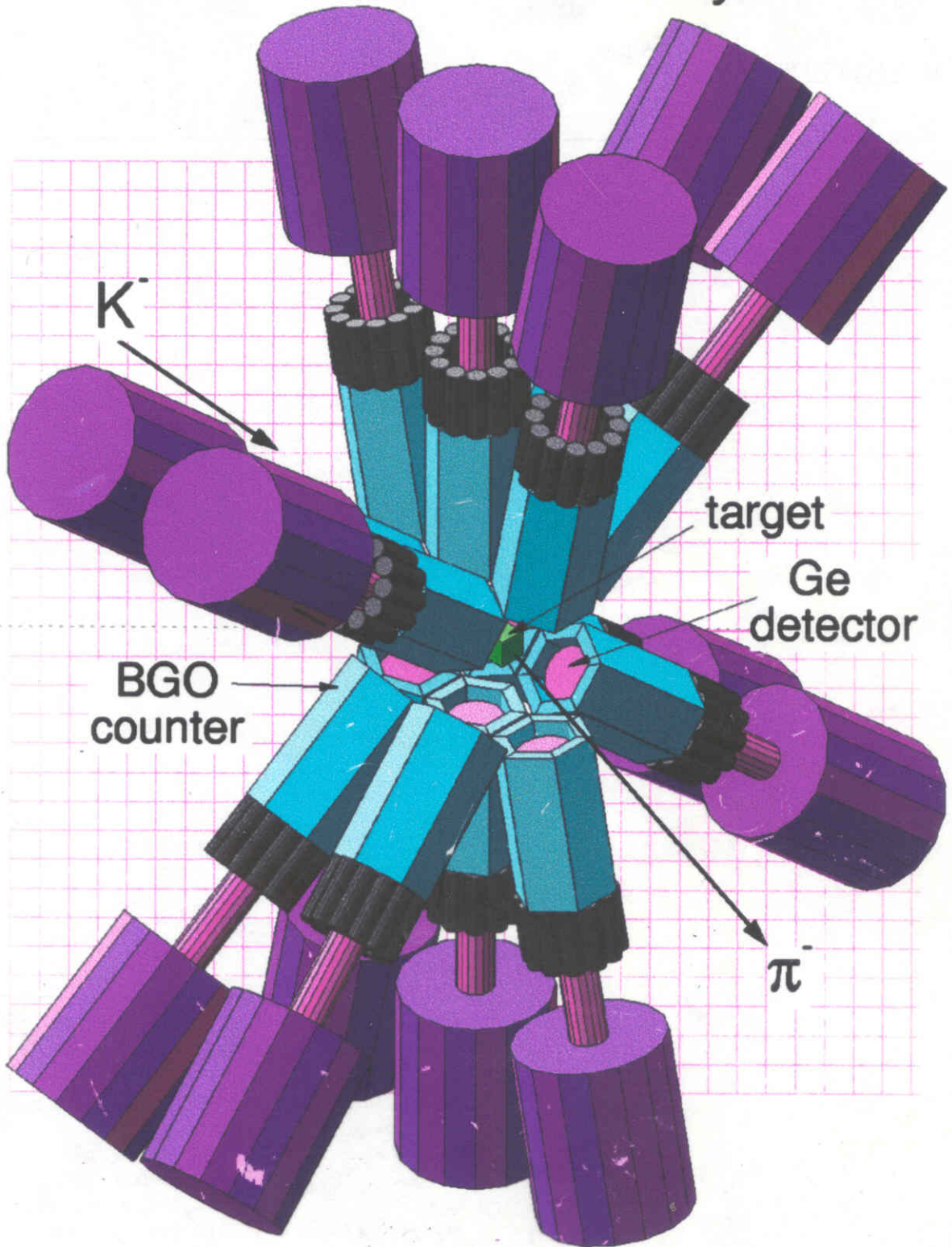
$$1^+ \quad v = \frac{1}{2} {}^3g_{ss} + \frac{1}{2} {}^1g_{ss} \quad E^{shift} \sim v^2/\Delta E$$

$$\text{NSC97f: } v \sim 7.6 \text{ MeV} \Rightarrow E^{shift} \sim 0.72 \text{ MeV}$$



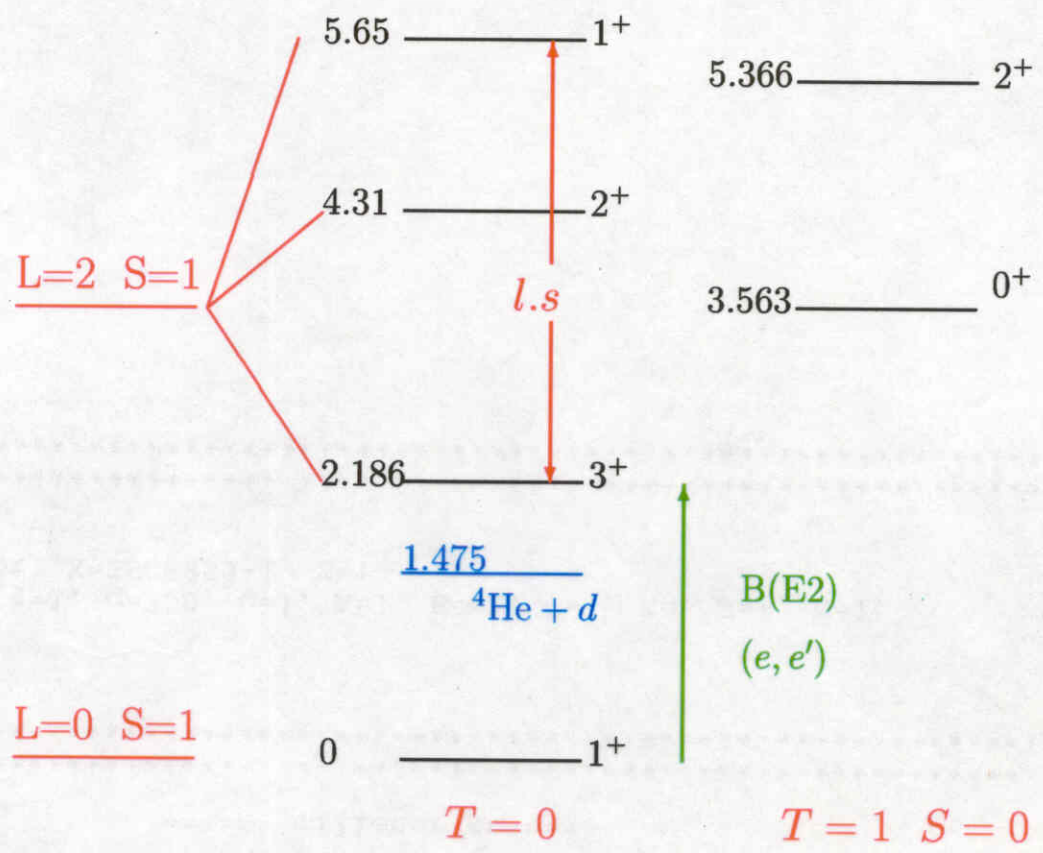
E. Hiyama et al., nucl-th/0106070, obtain similar results using a large model space for the 4-body calculation and the free YN interaction.

Germanium detector system



SNP99-3

${}^6\text{Li}$ core for ${}^7_\Lambda\text{Li}$



$${}^6\text{Li}(\text{gs}) = \alpha {}^3\text{S}_1 + \beta {}^3\text{D}_1 + \gamma {}^1\text{P}_1$$

CK616	0.9576	-0.2777	-0.0761
DJM	0.9873	-0.0422	-0.1532

$$Q({}^6\text{Li}) = e^0 \sqrt{2/5} (\sqrt{8}\alpha\beta + \sqrt{5/2}\gamma^2 - 7/2\sqrt{10}\beta^2) b^2 \quad (\text{Elliott, 1953})$$

$$Q = -0.083 \text{ fm}^2 \quad \text{Experiment}$$

$$Q = -0.126 \text{ fm}^2 \quad \text{DJM} \quad Q = -1.26 \text{ fm}^2 \quad \text{CK616}$$

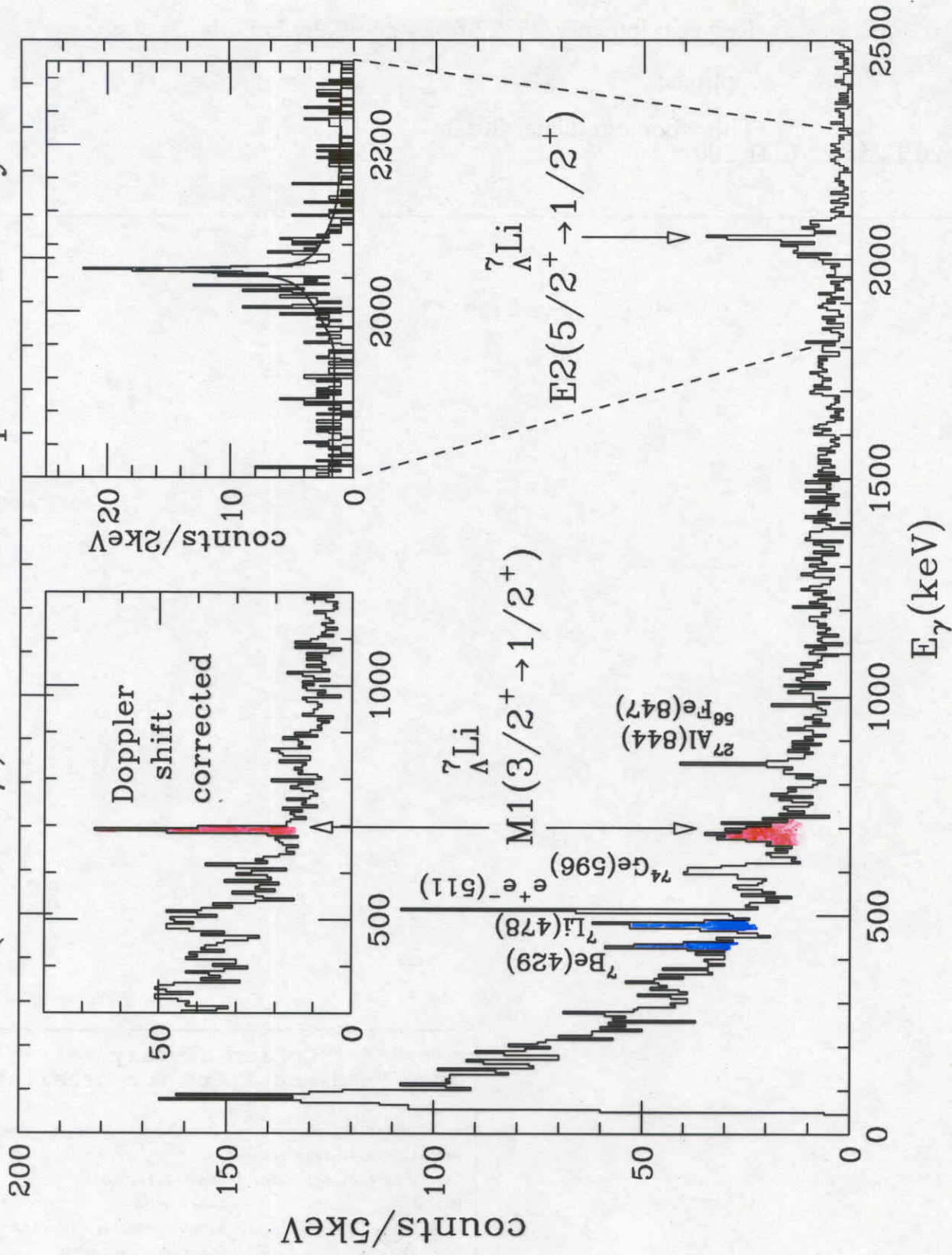
$\Lambda N - \Sigma N$ Coupling for $\langle p_N s_\Lambda | V | p_N s_\Sigma \rangle$

Can use the same parametrization as for ΛN

$$|\bar{V}| = 1.45 \text{ MeV} \quad |\Delta| = 3.04 \text{ MeV}$$

${}^7\text{Li}(\pi^+, \text{K}^+ \gamma)$

E419 preliminary



K. TANIDA

H. TAMURA (PANIC99)

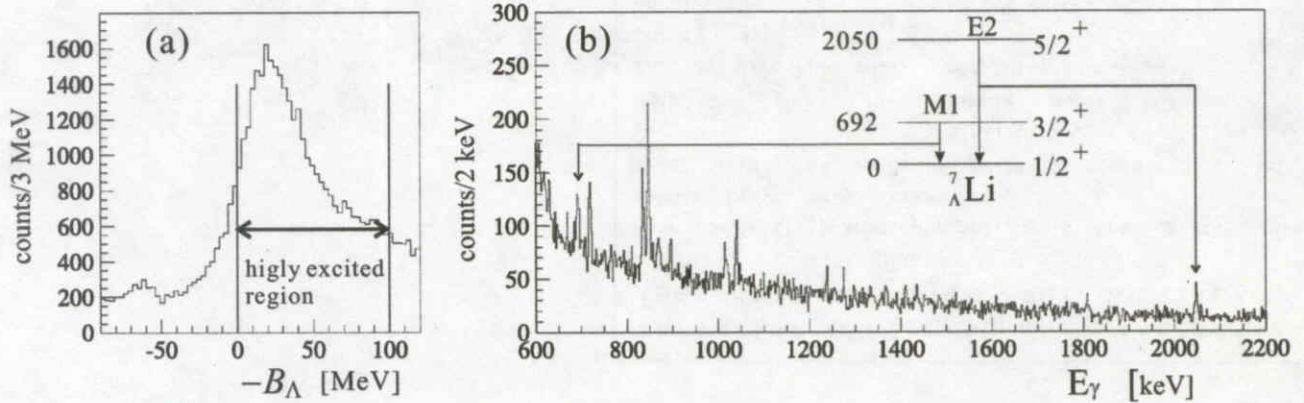


FIG. 1: (a) Mass spectrum of $^{10}_{\Lambda}\text{B}$

(b) γ -ray spectrum for the mass region shown in (a).

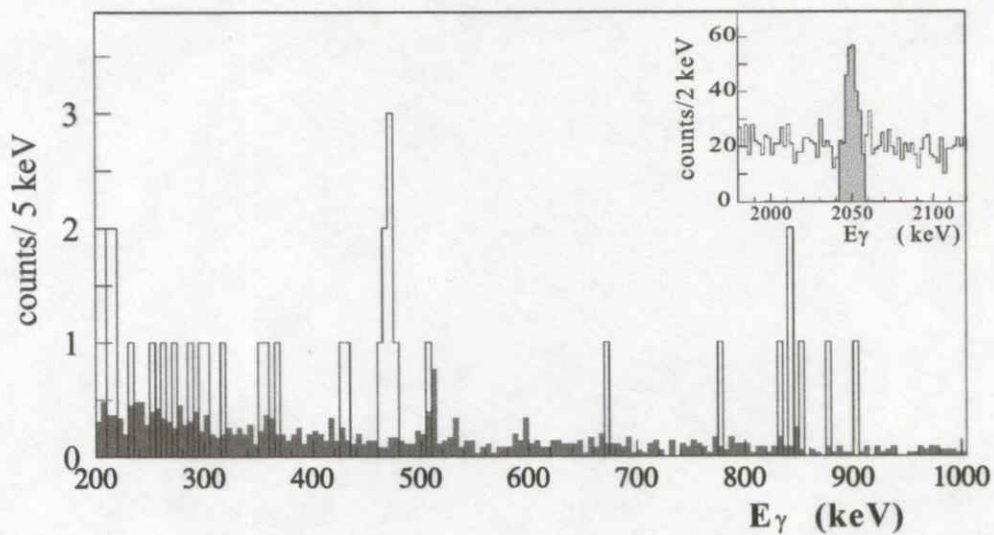


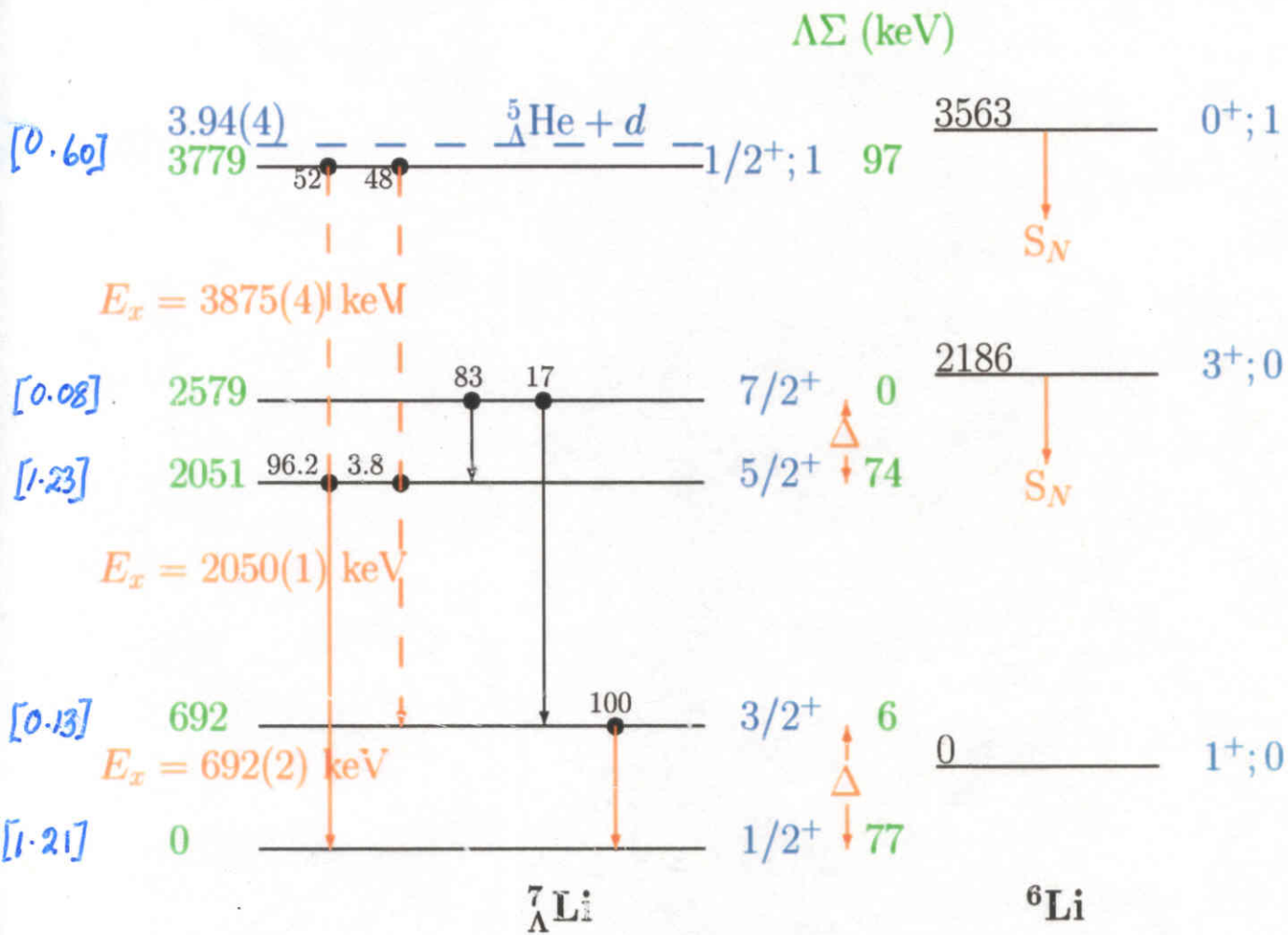
FIG. 2: $\gamma - \gamma$ coincidence spectrum from the $^{10}\text{B}(K^-, \pi^-)$ reaction.

$$E_{\gamma} = 470.8 \pm 1.9 \pm 0.6 \text{ keV}$$

${}^7_{\Lambda}\text{Li}$ γ rays – Hyperball, KEK E419

H. Tamura et al., PRL 84 (2000) 5963

K. Tanida et al., PRL 86 (2001) 1982



$\Delta = 0.432 \quad S_{\Lambda} = -0.010 \quad S_N = -0.380 \quad T = 0.021$

$T = 0.028$

$\Delta E(7/2^+ - 5/2^+) \approx \delta\delta$ Tamura

↑ reduced by larger S_{Λ}, T

df

Energy spacings in ${}^7_{\Lambda}\text{Li}$

Energy shifts in keV due to $\Lambda - \Sigma$ coupling for the lowest $T = 0$ (left) and $T = 1$ (right) states of ${}^7_{\Lambda}\text{Li}$.

0	95
74	101
6	97
77	
$T = 0$	$T = 1$

Contributions to the energy splitting are (in keV).

$$\Delta = 0.432 \quad S_{\Lambda} = -0.010 \quad S_N = -0.380 \quad T = 0.021$$

$3/2^+ - 1/2^+$ ground-state doublet separation

$\Lambda\Sigma$	Δ	S_{Λ}	S_N	T	ΔE
71	625	-1	-7	-4	692

$5/2^+ - 1/2^+$ separation $\Delta E = 2186 + \Delta E_{\Lambda N}$

$\Lambda\Sigma$	Δ	S_{Λ}	S_N	T	ΔE
3	76	11	-266	24	2051

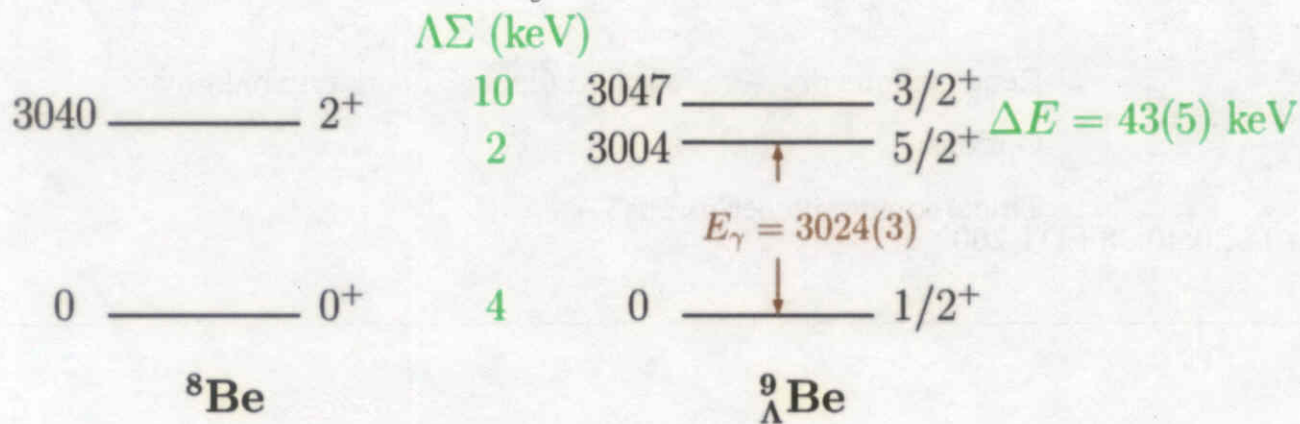
$1/2^+ - 1/2^+$ separation $\Delta E = 3565 + \Delta E_{\Lambda N}$

$\Lambda\Sigma$	Δ	S_{Λ}	S_N	T	ΔE
-20	415	0	-179	-2	3779

$7/2^+ - 5/2^+$ excited-state doublet separation

$\Lambda\Sigma$	Δ	S_{Λ}	S_N	T	ΔE
74	557	-22	-7	-50	528

hyp03-9



Old BNL E930 - H. Akikawa et al., PRL 88 (2002) 082501

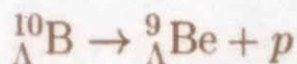
$E_\gamma = 3029(2), 3060(2)$ keV, $\Delta E = 31(3)$ keV

$\Delta = 0.557$ $S_\Lambda = -0.013$ $S_N = -0.549$ $T = 0.038$

$\Lambda\Sigma$	Δ	S_Λ	S_N	T	ΔE
-8	-20	32	-1	38	43 keV
	-0.037	-2.464	0.003	0.994	

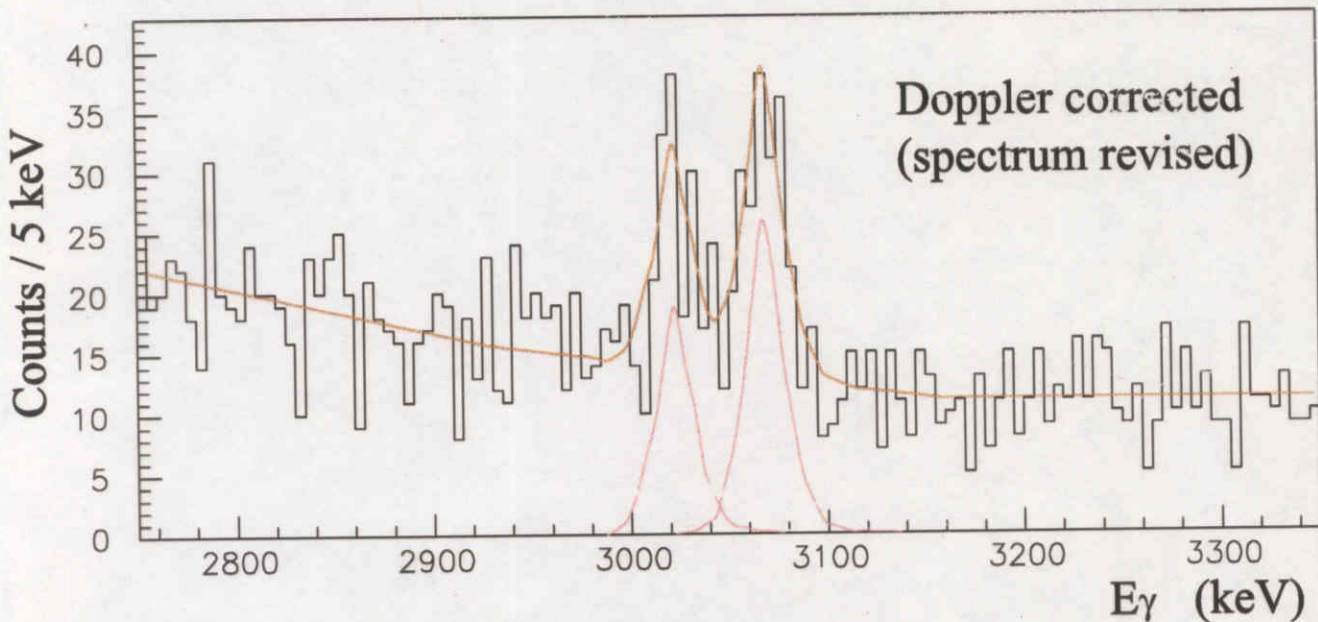
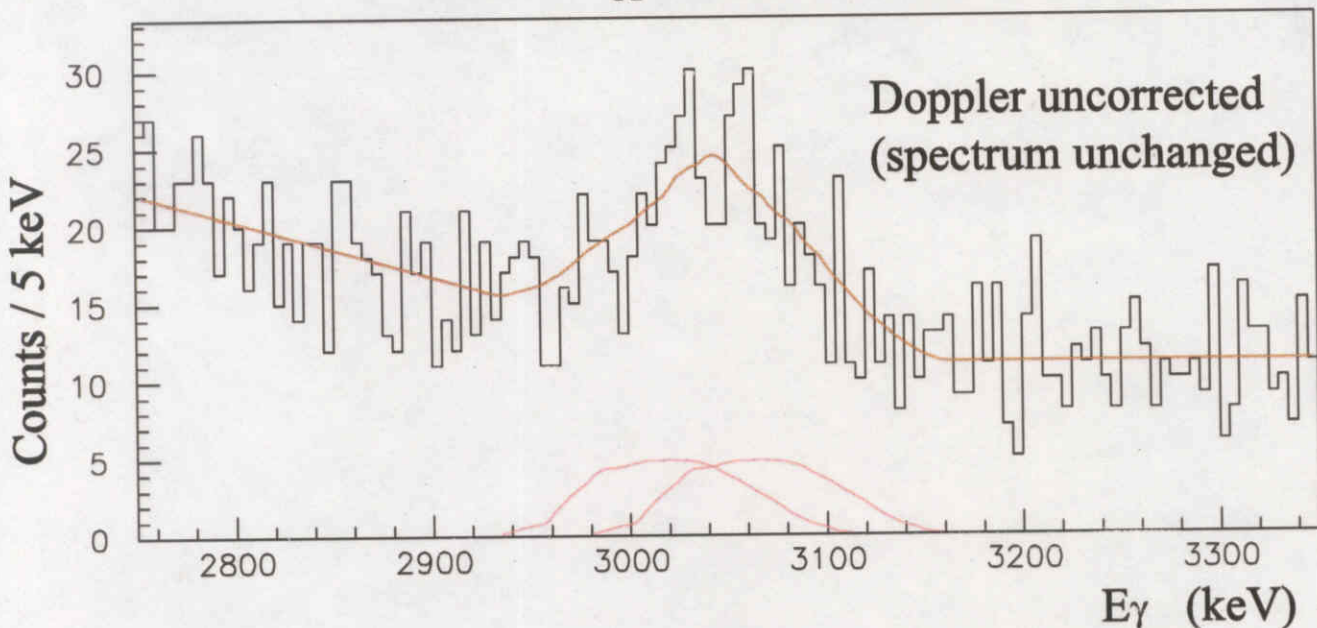
Order of 3/2⁺, 5/2⁺ not determined from this experiment.

In 2001 run on ¹⁰B target, the upper level is seen following



enabling us to deduce $J^\pi = 3/2^+$ for the upper member of the doublet.

E930 $^9\Lambda\text{Be}$ revised results



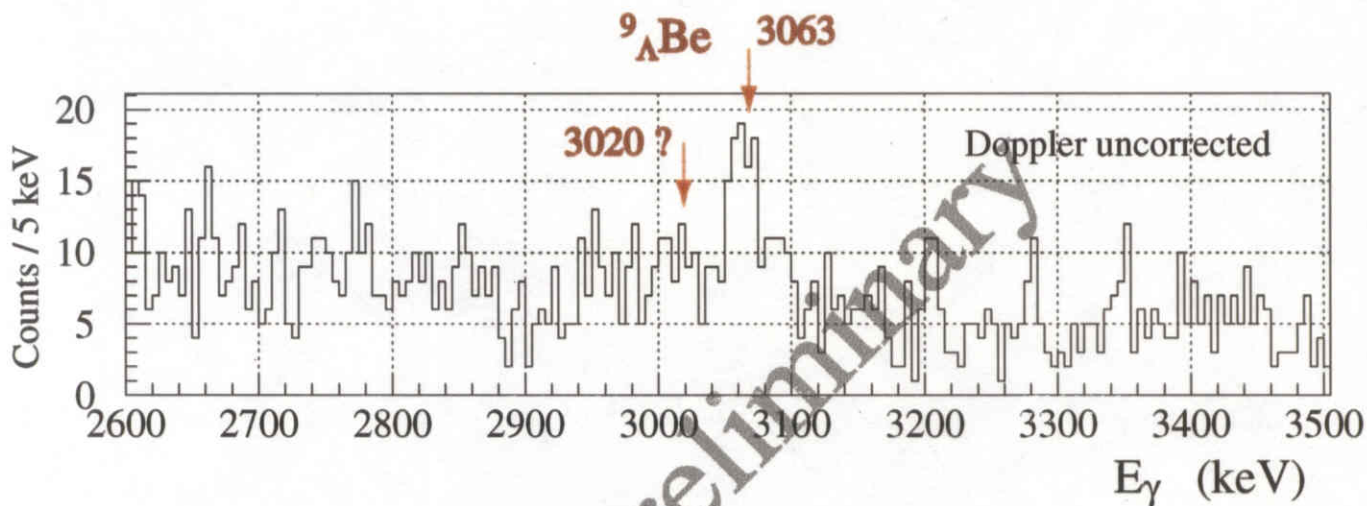
Both spectra are simultaneously fitted
with simulated peak shapes **Best fit for $\tau \sim 0.01$ ps**

Results $\tau < 0.10$ ps
 $\Delta E = 43 \pm 5$ keV
 $\chi^2/\text{dof} = 1.22$

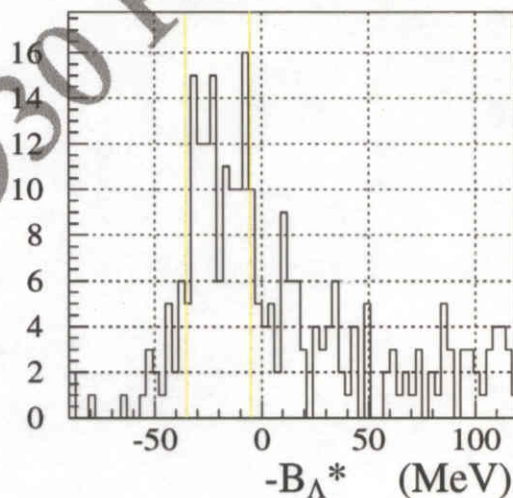
9L Be frag. e ps

Hyperfragments from $^{10}\text{B} (\text{K}^-, \pi^-)$ reaction : $^9_{\Lambda}\text{Be}$

$-35 < -B_{\Lambda}^* < -5$ MeV *uncalibrated

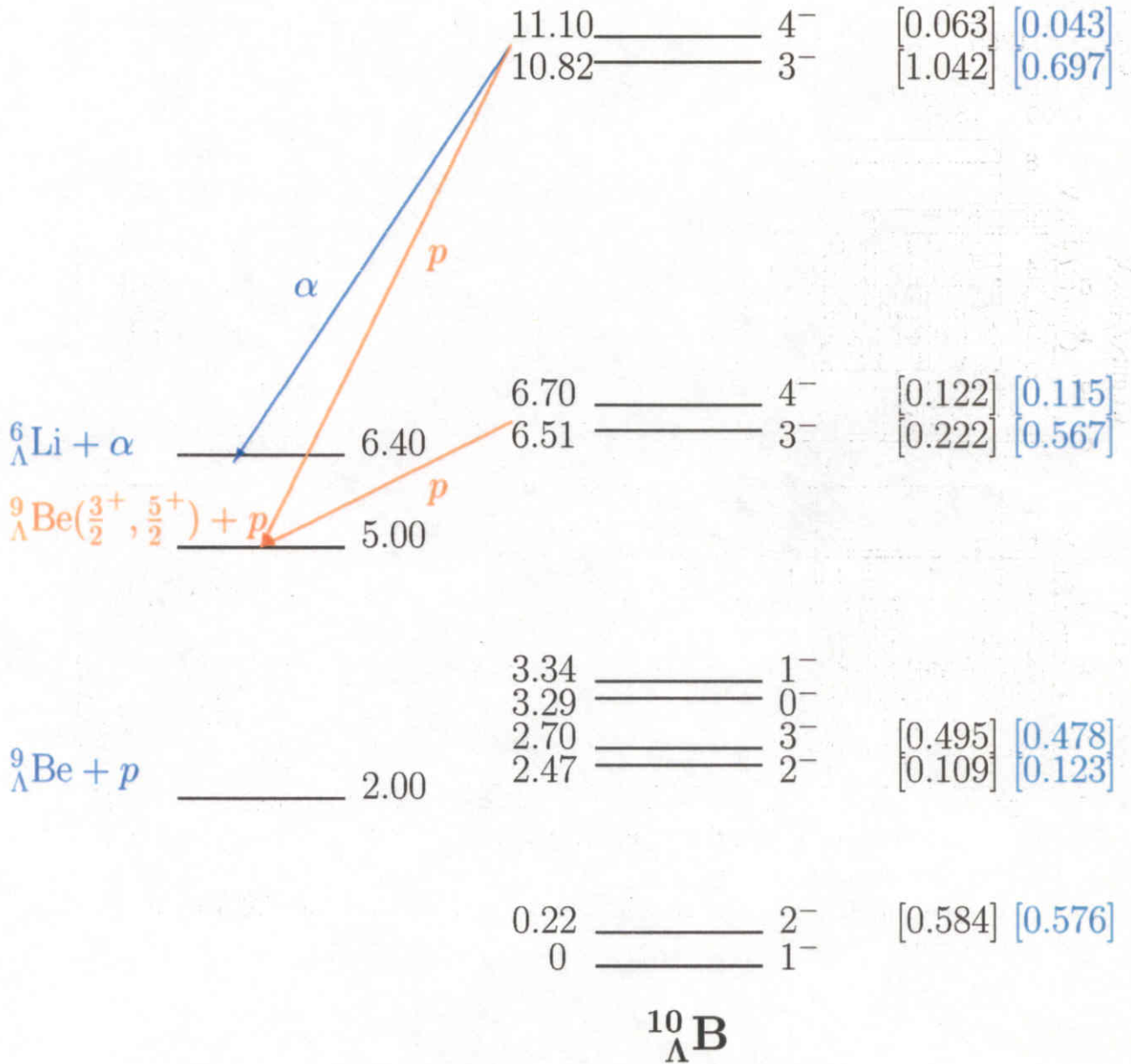


Excitation spectrum for 3063 keV peak



hyp03-4

Proton decay of $^{10}_{\Lambda}\text{B}$ to $^9_{\Lambda}\text{Be}$



hyp03-1

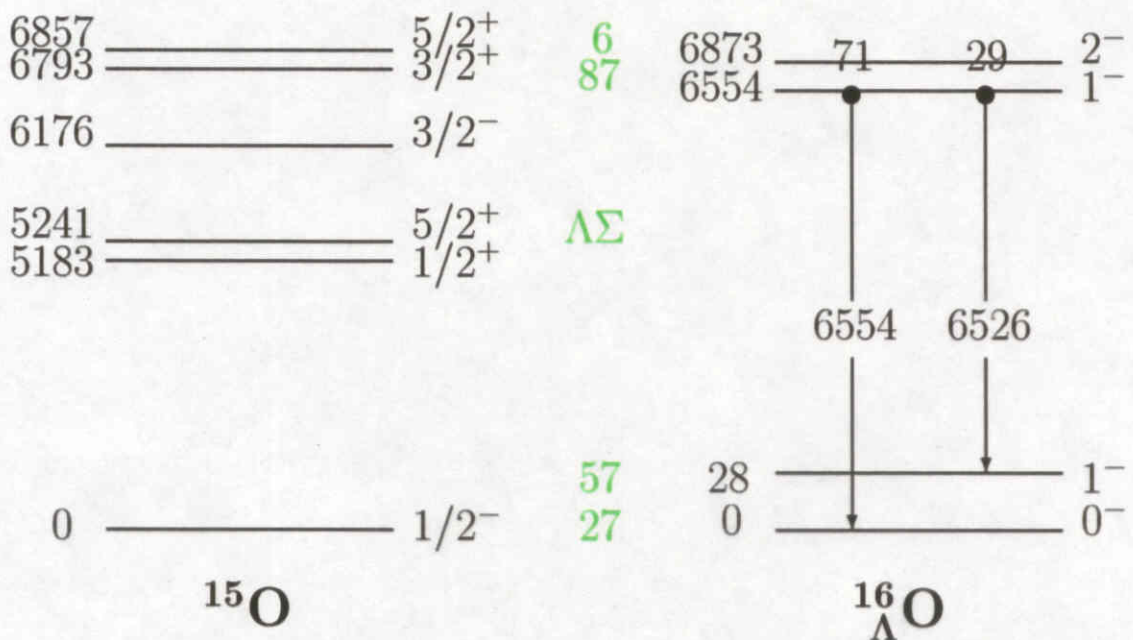
Formation and decay of ${}_{\Lambda}^{10}\text{B}$

- Four states of ${}^9\text{B}$ reached strongly by neutron removal from ${}^{10}\text{B}$
- The two $7/2^-$ states give rise to 3^- and 4^- states of ${}_{\Lambda}^{10}\text{B}$ above the ${}^9_{\Lambda}\text{Be}^* + p$ threshold
- 3^- is favored for the dominant $p_{3/2}$ removal by the coupling to get $\Delta L = 1$ and $\Delta S = 0$. Details depend on the amplitudes for $p_{1/2}$ and $p_{3/2}$
- Decay arises from ${}^9\text{B}(7/2^-) \rightarrow {}^8\text{Be}(2^+) + p$
- Recouple $(2^+ \times p_{3/2})7/2^- \times s_{\Lambda} \rightarrow (2^+ \times s_{\Lambda})J_f \times p_{3/2}$
- 4^- decays to ${}^9_{\Lambda}\text{Be}(5/2^+)$
- 3^- decays to $3/2^+$, $5/2^+$ in ratio of 32 to 3
- Overall: $3/2^+$ is strongly favored by proton emission
- Caveat: uppermost 3^- state doesn't α decay too much

Tensor Interaction updated

For pure $p_{1/2}^{-1} s_{\Lambda}$, the combination of parameters governing the doublet splitting is

$$E(1_1^-) - E(0^-) = -\frac{1}{3}\Delta + \frac{4}{3}S_{\Lambda} + 8T$$



$$\Delta = 0.468 \quad S_{\Lambda} = -0.011 \quad S_N = -0.354 \quad T = 0.030$$

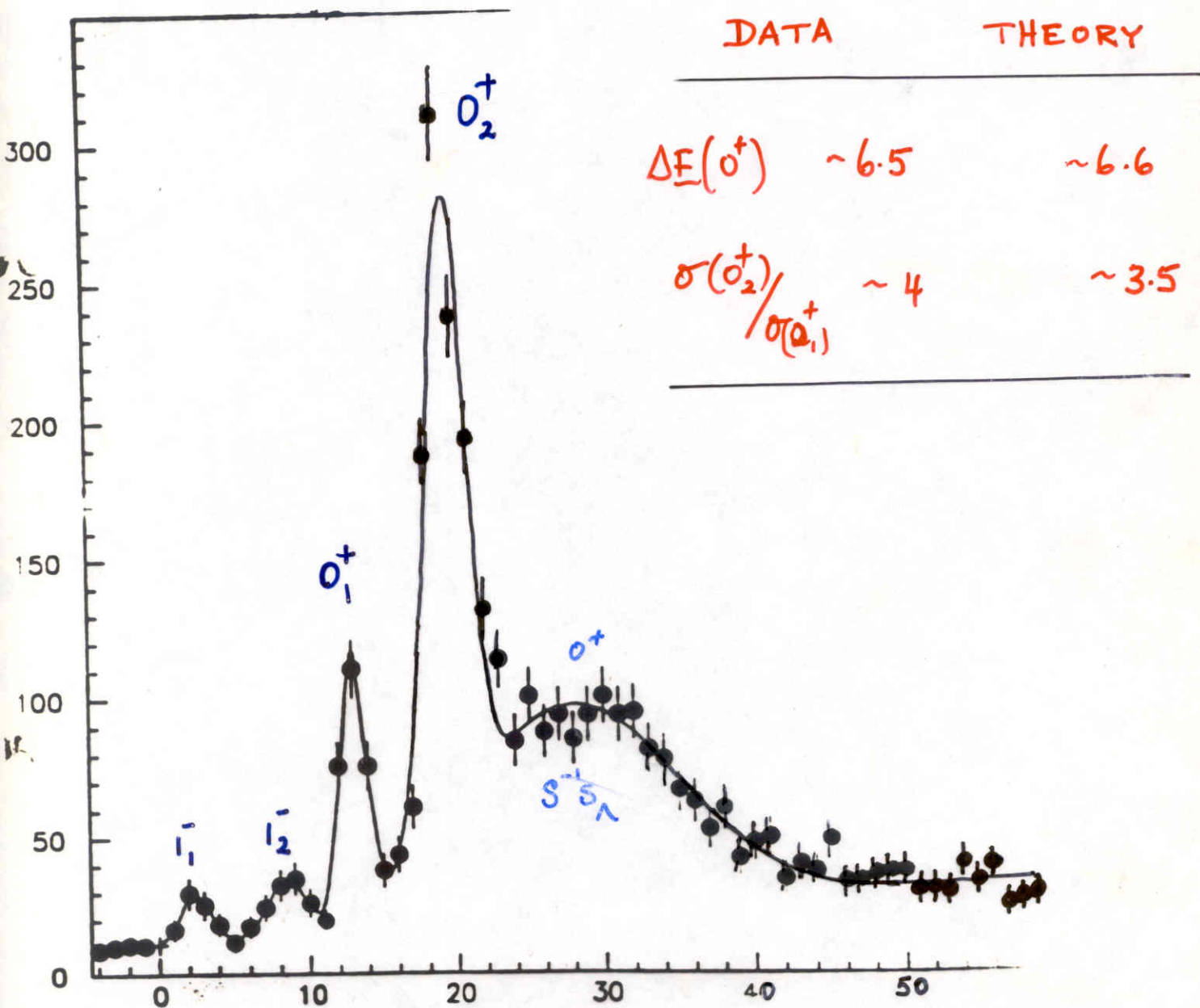
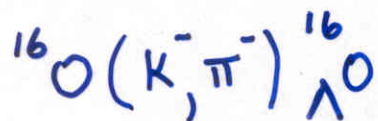
M. Ukai et al. - Phys. Rev. Lett. 93 (2004) 232501

$$E(1_2^- - 0_1^-) = 6561.7 \pm 1.1 \pm 1.7 \text{ keV} \quad (183 \pm 15 \pm 5 \text{ counts})$$

$$E(1_2^- - 1_1^-) = 6535.3 \pm 1.2 \pm 1.7 \text{ keV} \quad (127 \pm 15 \pm 5 \text{ counts})$$

$$\Delta E = 26.4 \pm 1.6 \pm 0.5 \text{ keV}$$

CERN



Strong 1^- and 0^+ states in $^{16}\text{O}(K^-, \pi^-)^{16}_{\Lambda}\text{O}$

25.4 _____ 0^+

$$s_{1/2}^{-1} s_{1/2\Lambda} = \sqrt{4/5} s^3 p^{12} s_{\Lambda} + \sqrt{1/5} s^4 p^{10} (02) (sd) s_{\Lambda}$$

17.1 _____ 0^+

$$p_{3/2}^{-1} p_{3/2\Lambda} + \epsilon s^4 p^{10} (sd) s_{\Lambda}$$

12.7 _____ $\frac{3}{2}^+$
12.1 _____ $\frac{1}{2}^+$

~ 12.5 _____

10.3 _____ $\frac{1}{2}^+; 1$

10.6 _____ 0^+ $^{15}\text{O} + \Lambda$
 $p_{1/2}^{-1} p_{1/2\Lambda} + \epsilon s^4 p^{10} (sd) s_{\Lambda}$

~ 7.8 _____ $\frac{1}{2}^+, \frac{3}{2}^+$

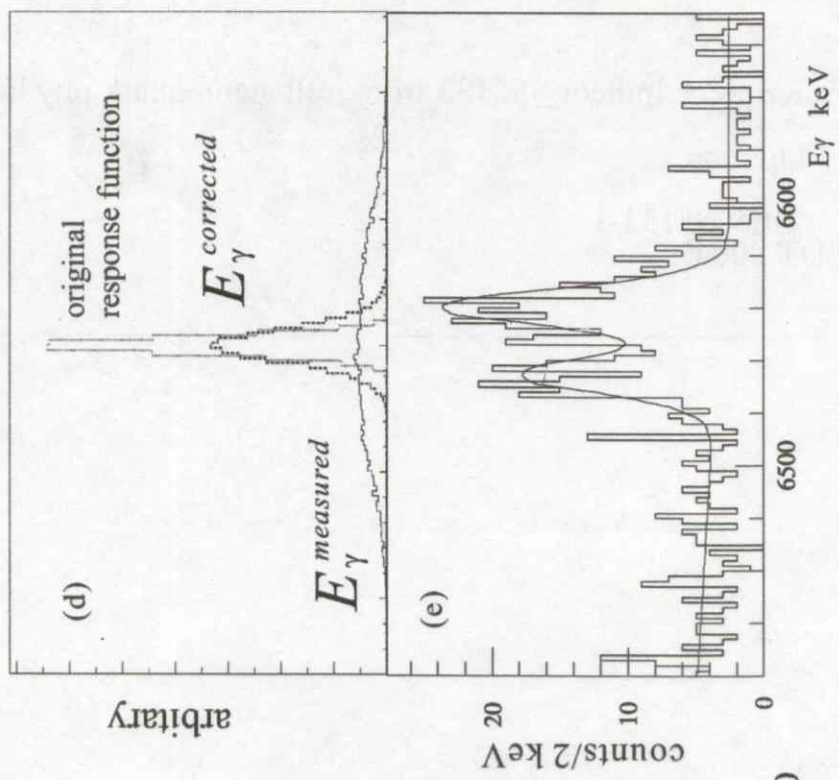
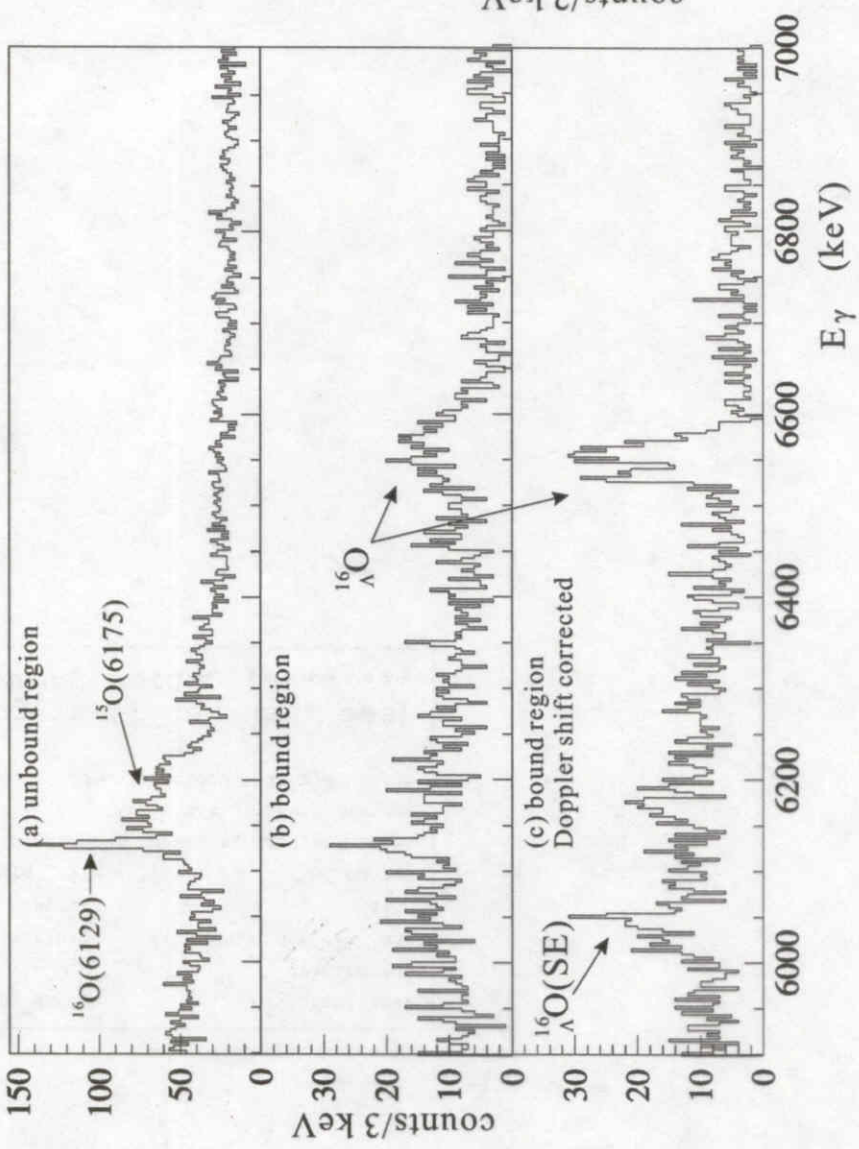
$^{15}_{\Lambda}\text{N} + p$

~ 6.5 _____ $1^-, 2^-$
 $p_{3/2}^{-1} s_{1/2\Lambda}$

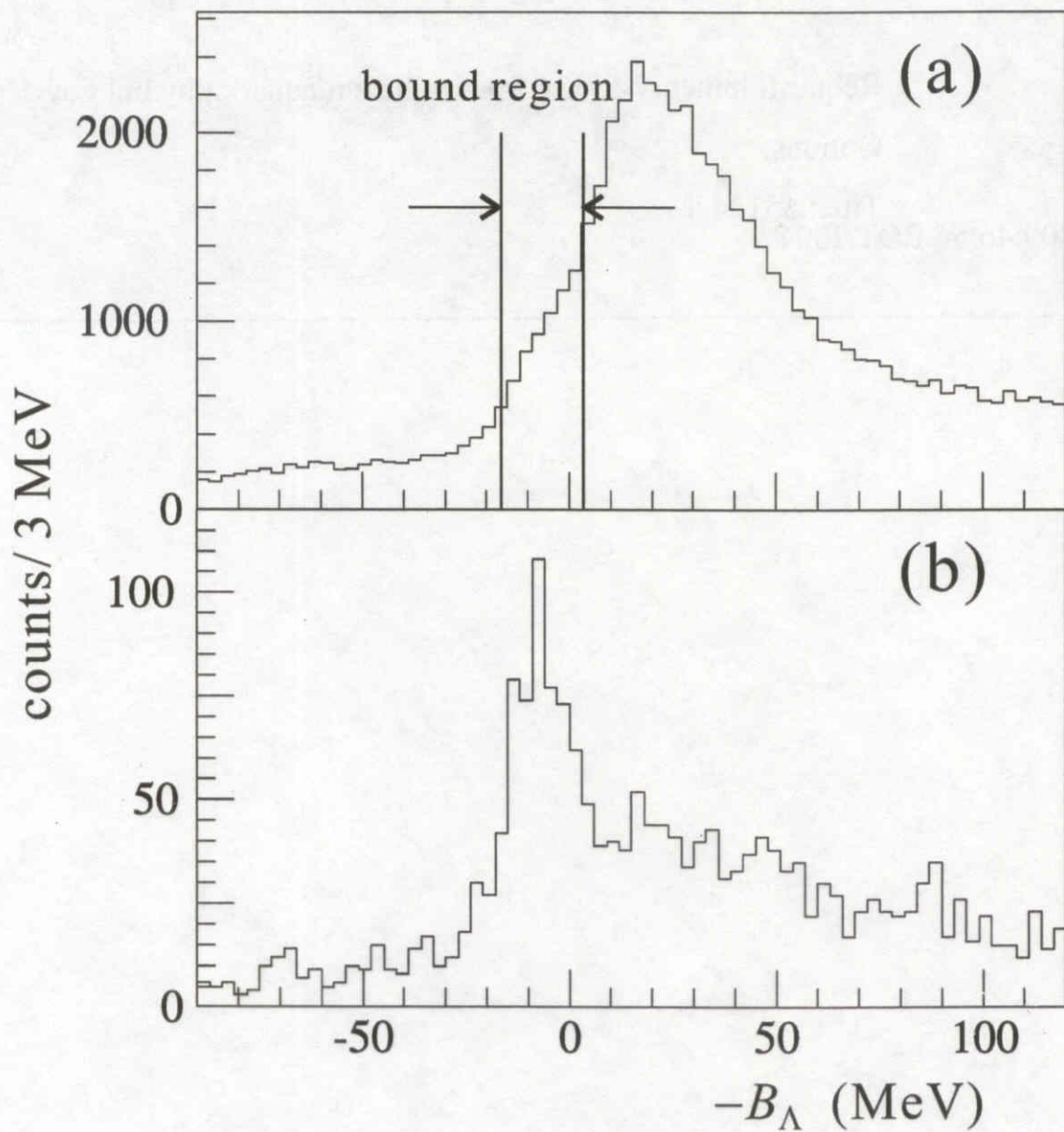
0 _____ $0^-, 1^-$
 $p_{1/2}^{-1} s_{1/2\Lambda}$

$^{16}_{\Lambda}\text{O}$

bnl05-1. Tex.



bn05_2



hyp03-8

${}^{16}_{\Lambda}\text{O}$ $\Delta E(1^- - 0^-)$ Experiment ~ 27 keV

$\Lambda\Sigma$	Δ	S_{Λ}	S_N	T	ΔE
	-0.382	1.378	-0.004	7.850	
-30	-179	-15	1	235	28 keV

${}^{15}_{\Lambda}\text{N}$ $\Delta E(1/2^+ - 3/2^+)$

$\Lambda\Sigma$	Δ	S_{Λ}	S_N	T	ΔE
	0.756	-2.250	0.035	-9.864	
44	354	25	-12	-296	110 keV

${}^{16}_{\Lambda}\text{O}$ $E(1_2^- - 1_1^-) = 6176 + \Delta E$ Experiment ~ 6532 keV

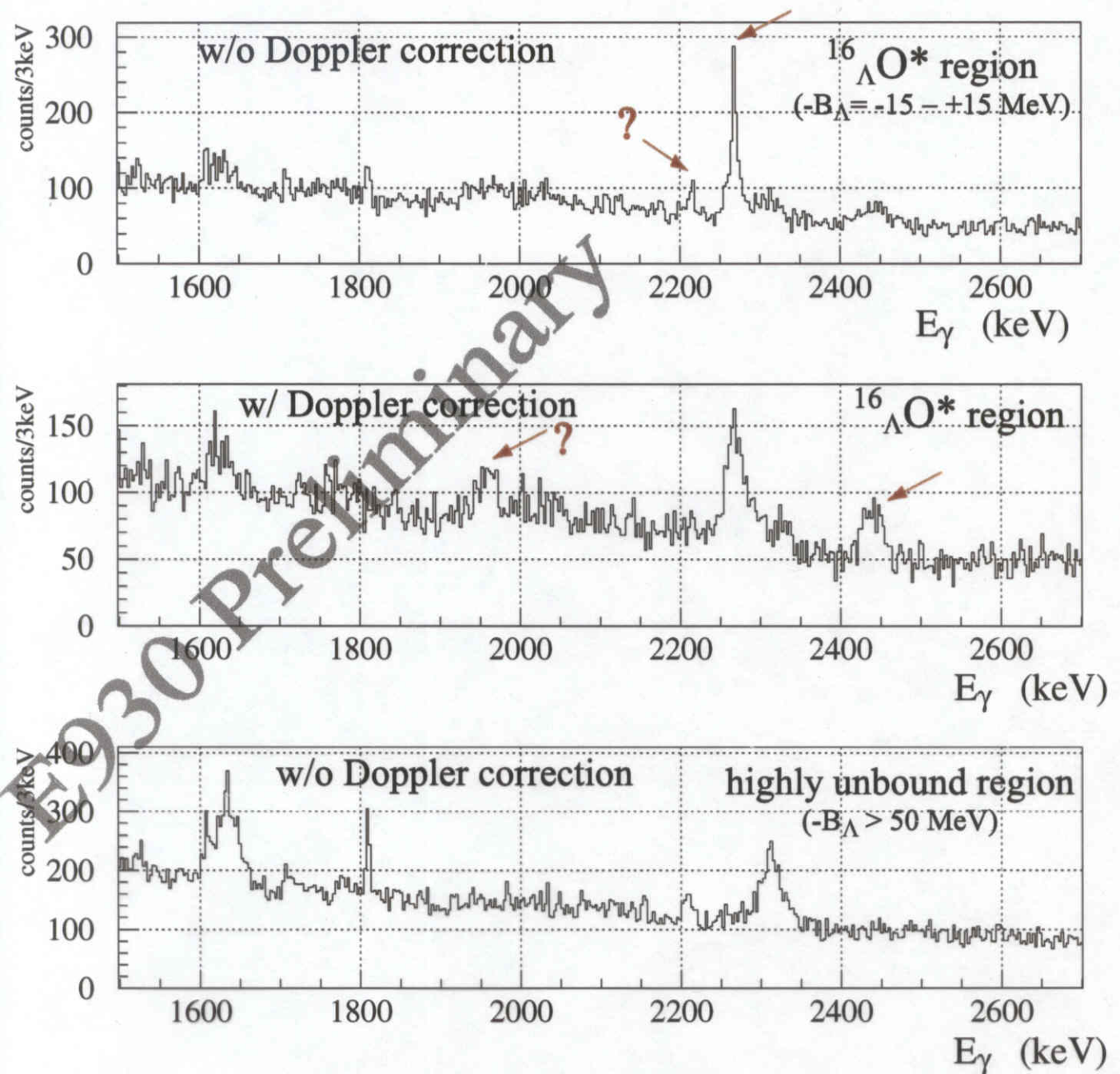
$\Lambda\Sigma$	Δ	S_{Λ}	S_N	T	ΔE
	-0.234	-1.257	-1.496	-0.708	
-30	-110	14	530	-21	350 keV

${}^{15}_{\Lambda}\text{N}$ $E(1/2^+; 1 - 3/2^+) = 2313 + \Delta E$ Experiment ~ 2263 keV

$\Lambda\Sigma$	Δ	S_{Λ}	S_N	T	ΔE
	0.284	-0.778	-0.249	-3.197	
-46	133	9	88	-96	85 keV

$$\Delta = 0.468 \quad S_{\Lambda} = -0.011 \quad S_N = -0.354 \quad T = 0.030$$

Candidates of $^{15}_{\Lambda}\text{N}$ γ rays
by $^{16}\text{O} (\text{K}^-, \pi^-)^{15}_{\Lambda}\text{N} + \text{p}$ reaction



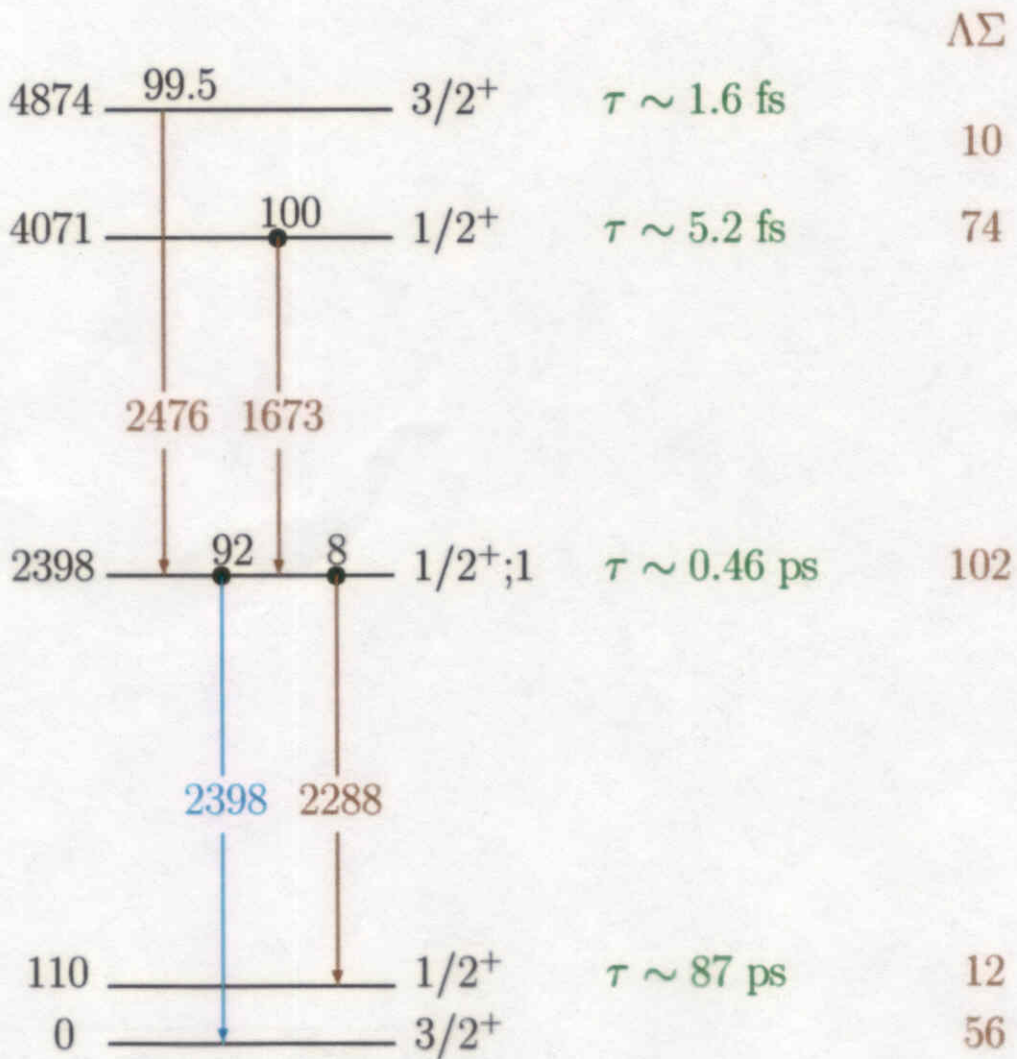
an 02-6

¹⁵N
Λ

The ¹⁵ΛN spectrum based on the three lowest levels of the core using the (8-16)2BME interaction of Cohen and Kurath for

$$\Delta = 0.468 \quad S_{\Lambda} = -0.011 \quad S_N = -0.354 \quad T = 0.030 .$$

which fit the results of E930 for ¹⁶ΛO.

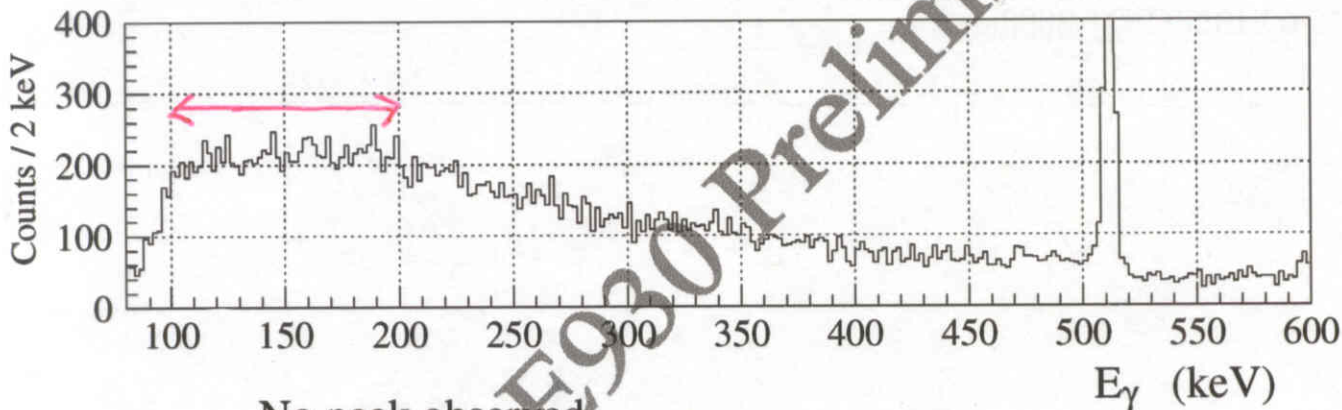


$$E(1/2^+) - E(3/2^+) = 0.756\Delta - 2.250S_{\Lambda} + 0.035S_N - 9.862T$$

$$\Lambda\Sigma \text{ contribution} = 44 \text{ keV}$$

hyp03-6
 $^{10}\text{B} (\text{K}^-, \pi^-) ^{10}_{\Lambda}\text{B}$ reaction

-40 < $-B_{\Lambda}^*$ < -10 MeV *uncalibrated
 (5 MeV lower than the $^9_{\Lambda}\text{Be}$ gate)



No peak observed
 (upper limit to be derived)

R.E. Chrien et al., PRC 41 (1990) 1062 no γ ray

$\Lambda\Sigma$ (keV)

180 _____ 2^- 49

0 _____ 1^- 34

$^{10}_{\Lambda}\text{B}$

Only case in which Δ and $\Lambda\Sigma$ oppose one another

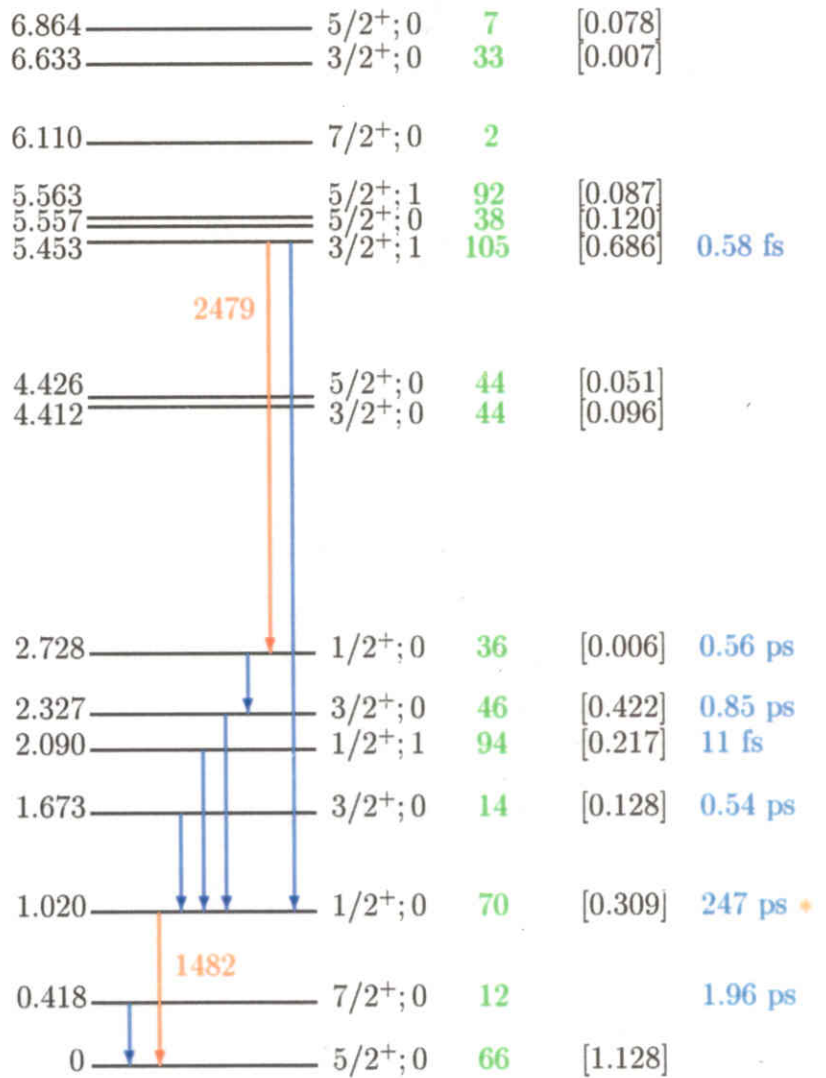
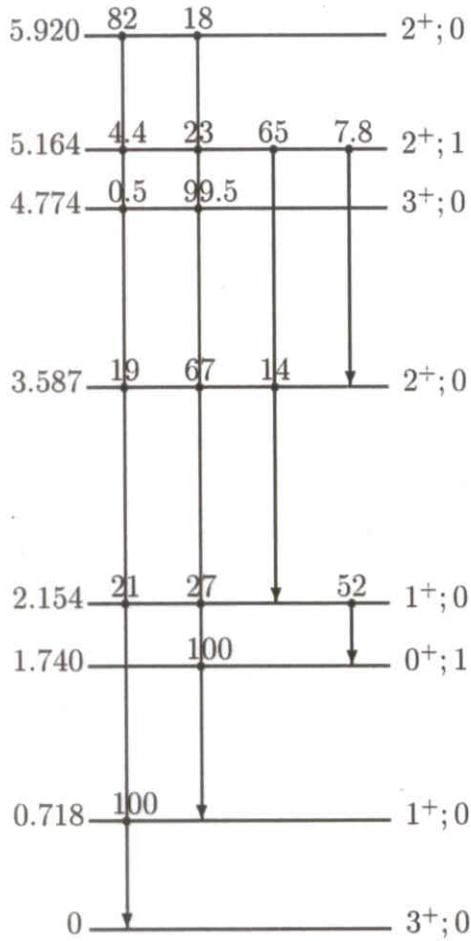
$\Lambda\Sigma$	Δ	S_{Λ}	S_N	T	ΔE
	0.579	1.413	0.013	-1.073	
-15	250	-14	-5	-32	180 keV

$^7_{\Lambda}\text{Li}$: $\Delta = 0.432$ $S_{\Lambda} = -0.010$ $S_N = -0.380$ $T = 0.030$

CK616 gives $\Delta E = 164$ keV - larger coefficient of T

anl02-11

7.72 — — — ${}_{\Lambda}^{10}\text{Be} + p$



${}^{10}\text{B}$

${}^{11}_{\Lambda}\text{B}$

$\Lambda\Sigma$

S

τ

* τ (weak) ~ 200 ps

For $E_{\gamma} = 1482$ keV, τ (EM) ~ 38 ps

This level serves as a collection point for γ rays

hyp03-2.ps

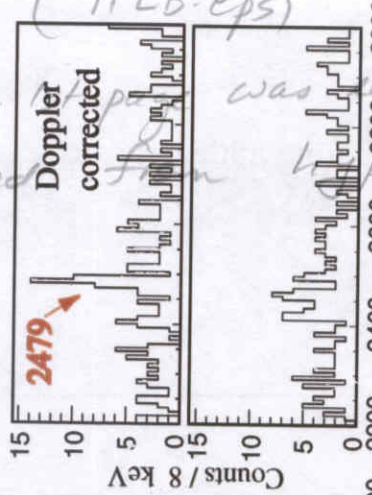
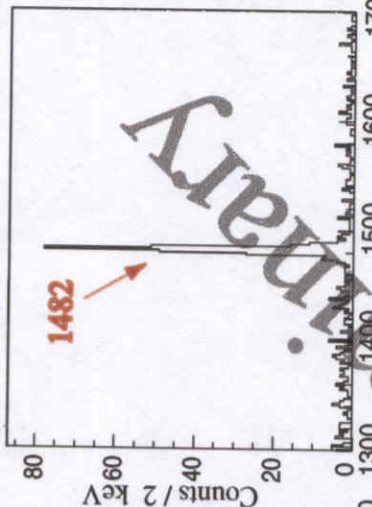
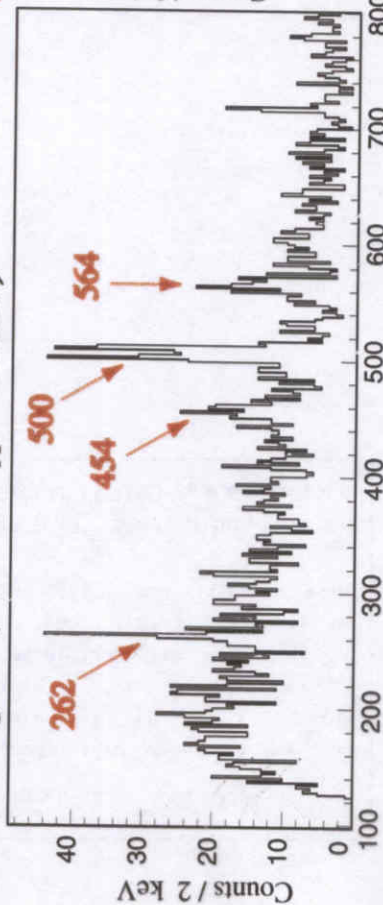
(11 LB-eps)

Note: A black ~~plot~~ was deleted out of the postscript file produced from hyp03-2

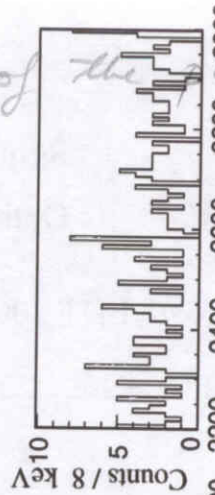
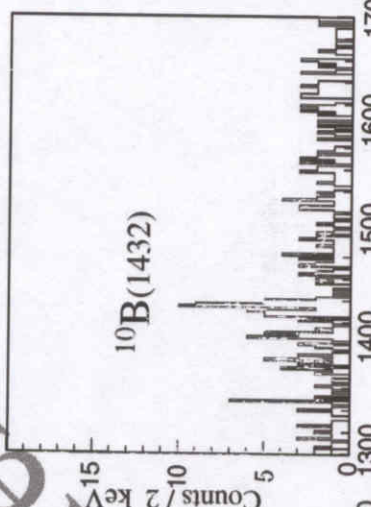
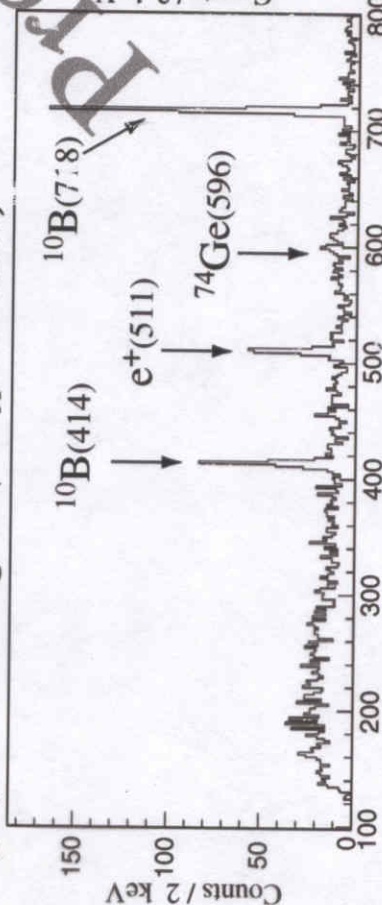
KEK E518 $^{11}\text{B}(\pi^+, \text{K}^+\gamma)^{11}\Lambda\text{B}$

Six γ rays from $^{11}\Lambda\text{B}$

Bound region ($-20 < -B_\Lambda < -2 \text{ MeV}$)



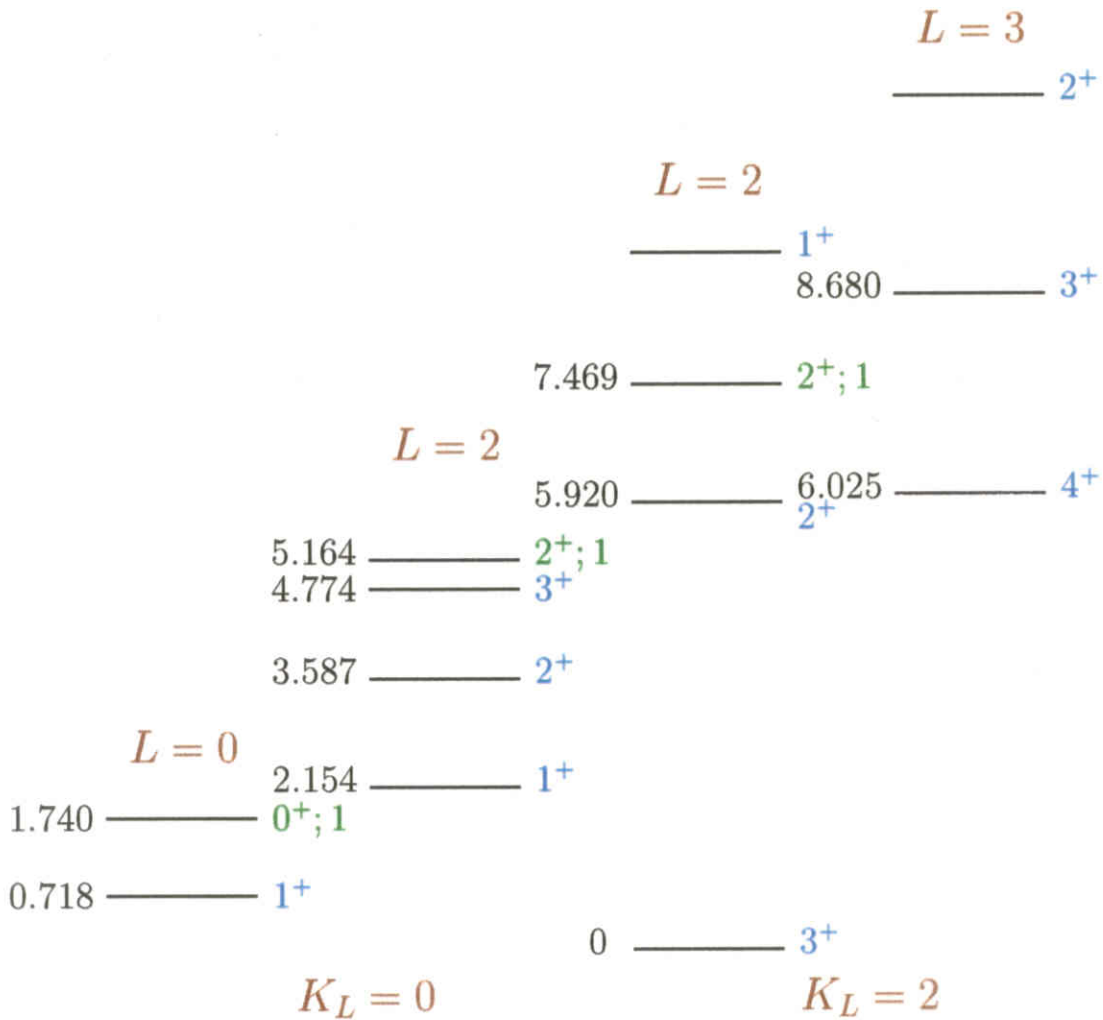
Highly Unbound region ($-B_\Lambda > 20 \text{ MeV}$)



E_γ (keV)

hyp03-3

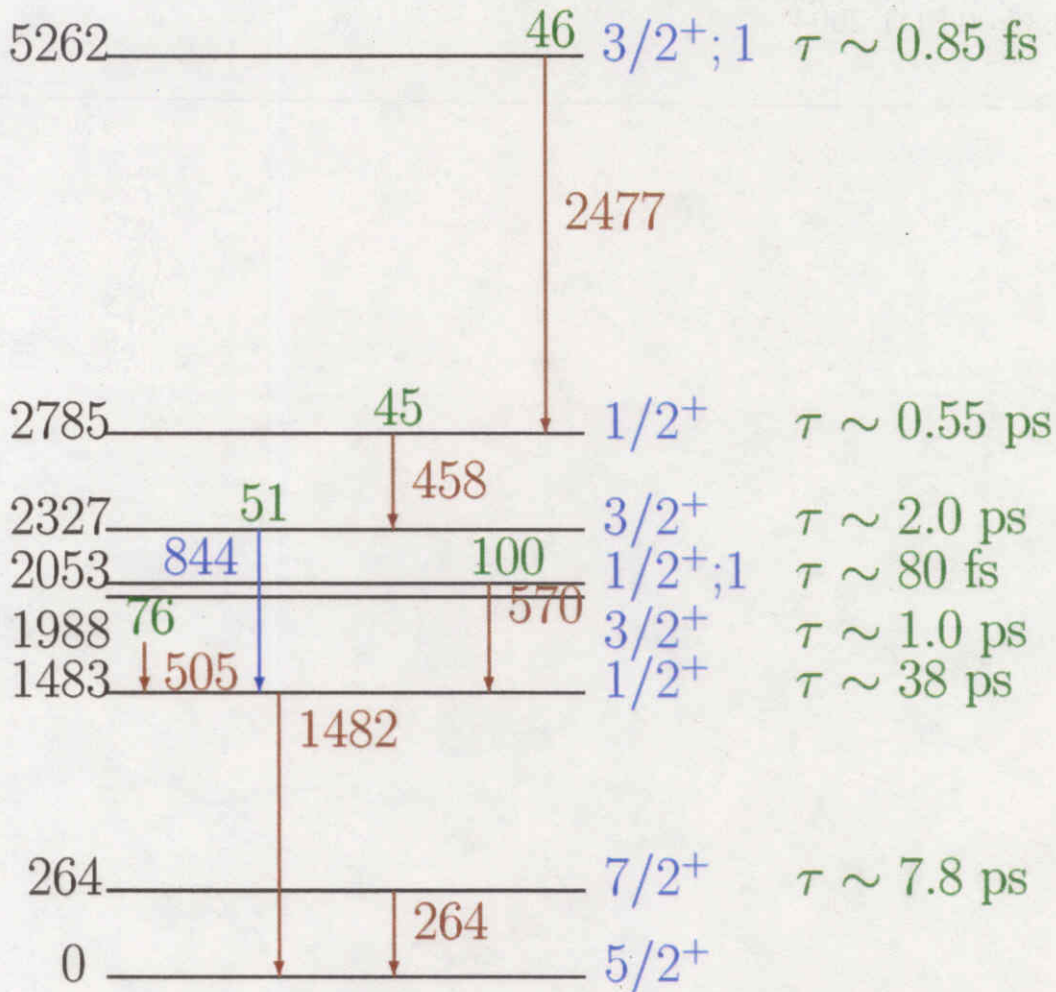
P-shell states of ^{10}B with $[42]$ symmetry.



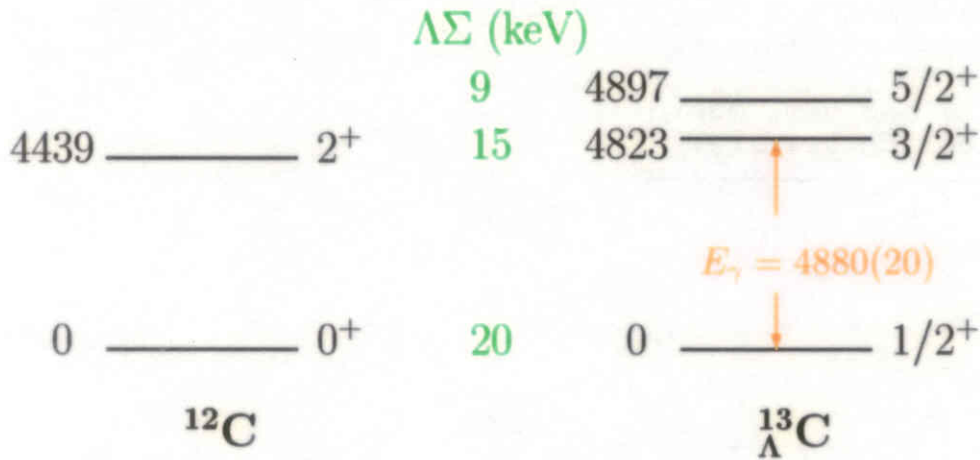
$T = 0$ states have $S = 1$ and $T = 1$ states have $S = 0$

hyp03-11

Speculations on the placement of $^{11}_{\Lambda}B$ γ rays.



- To reproduce the definitive 1482 keV line, the centroid of the lowest $1/2^+$, $3/2^+$ doublet needs to be high (small coefficient of S_N) and the separation needs to be small (Δ).
- Natural to identify the 2479 keV line with the strong M1 from the $3/2^+; 1$ level.
- For different core wave functions, ground-state doublet and $T=1$ levels are quite stable while $1/2^+$ and $3/2^+$ $T=0$ states are volatile.



BNL E929 - H. Kohri et al., PRC 65 (2002) 034607 S. Ajimura et al., Phys. Rev. Lett. 86 (2001) 4255

$\Lambda\Sigma$	Δ	S_Λ	S_N	T	ΔE
5	-27	19	472	-32	4831 keV
	-0.051	-1.449	-0.867	-1.100	

$$\Delta = 0.532 \quad S_\Lambda = -0.013 \quad S_N = -0.545 \quad T = 0.027$$

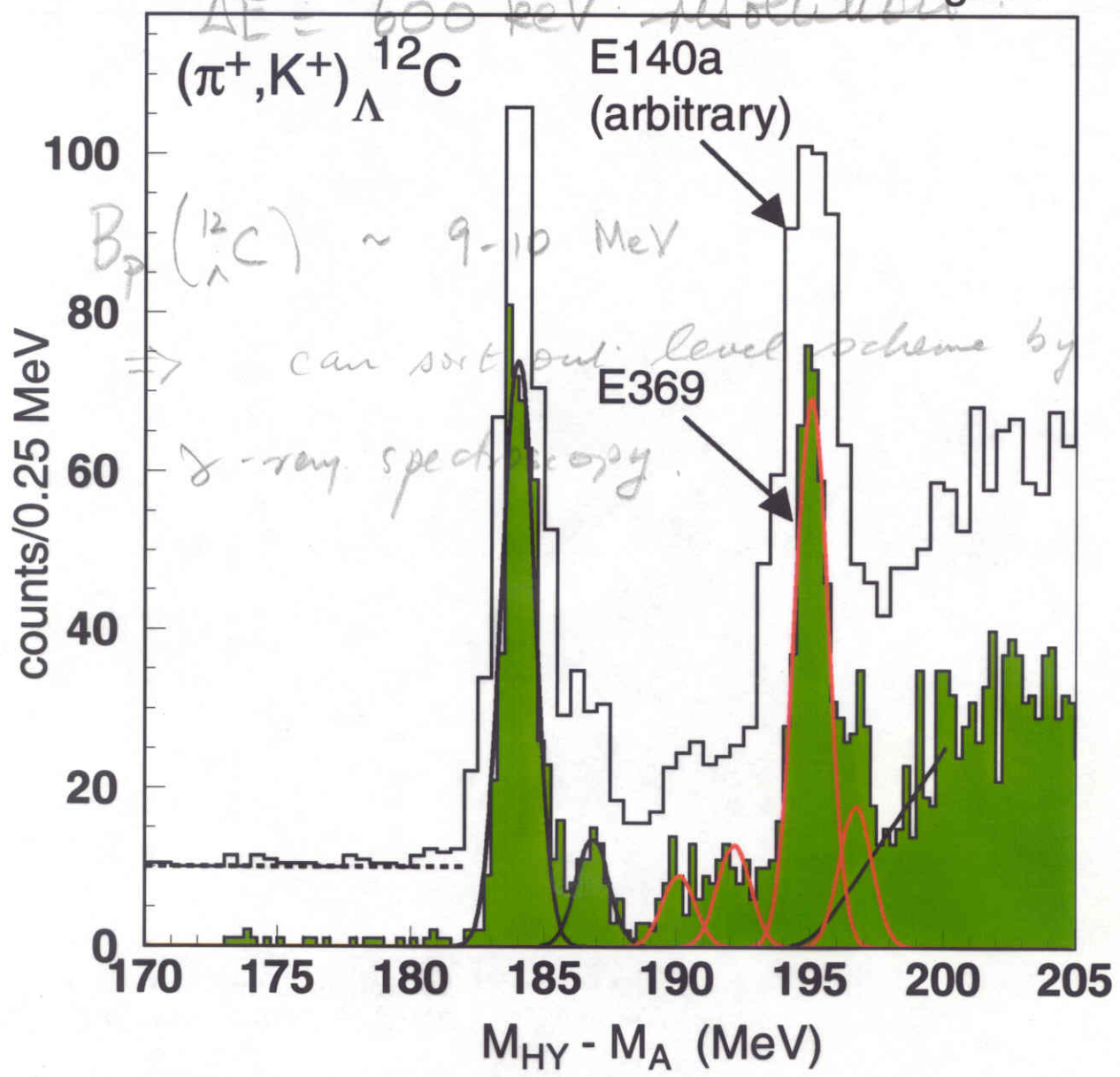
KEK E336 $E_x = 4.85(7)$ MeV from $^{13}\text{C}(\pi^+, K^+)^{13}_\Lambda\text{C}$

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12c.eps

$^{12}\text{C}(e,e'K^+)^{12}\text{B}$

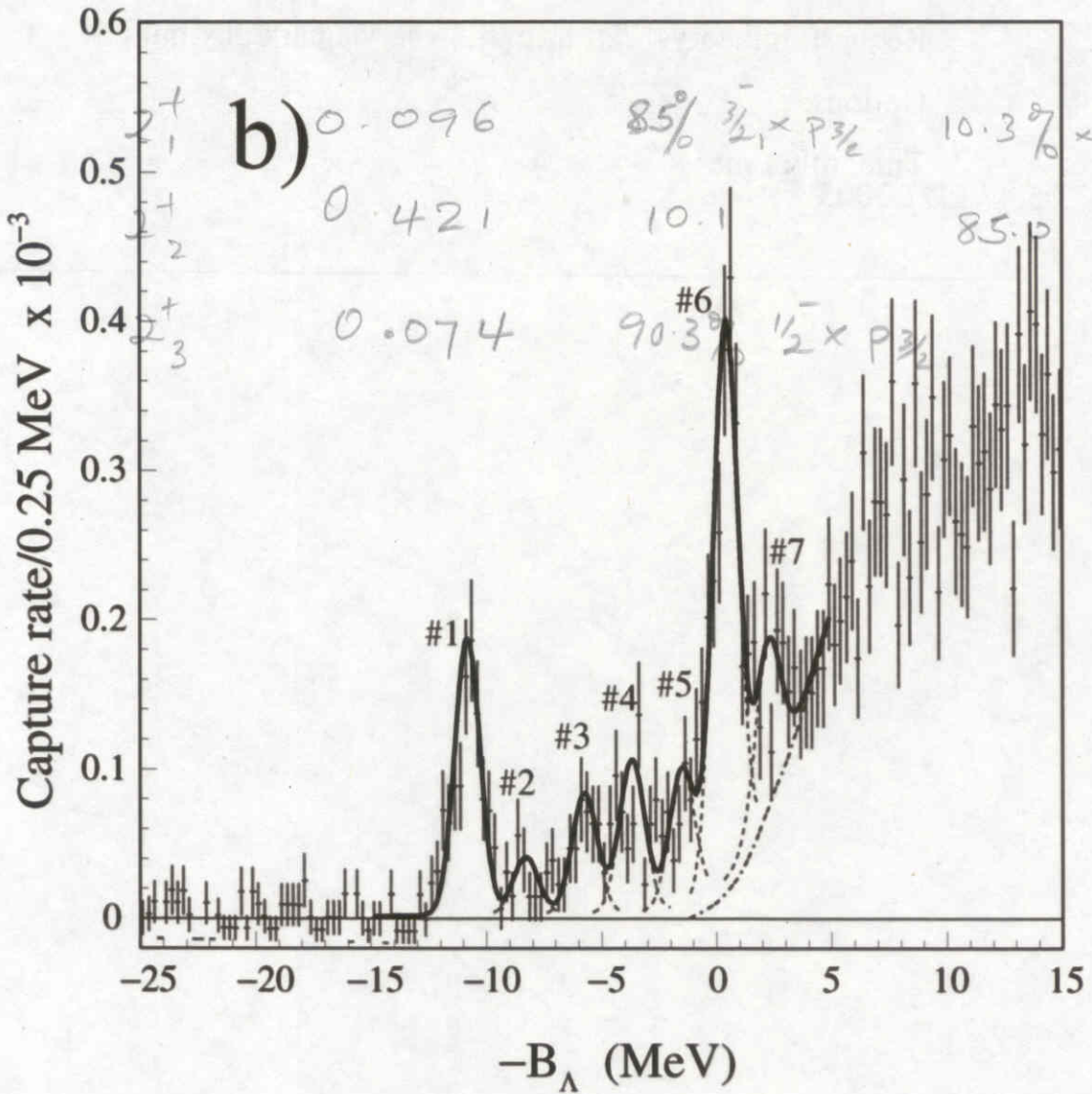
$\Delta E = 600 \text{ keV}$ resolution
 $^{12}\text{C} \ 0.9 \text{ g/cm}^2$



$\Delta E = 1.45 \text{ MeV}$

T. NAQAE

Jlab05_1.



Peak number	$-B_{\Lambda}$ (MeV)	E_x (MeV)	Capture rate/(stopped K^-) [$\times 10^{-3}$]
1	-10.94 ± 0.06	0	$1.01 \pm 0.11_{stat} \pm 0.10_{syst}$
2	-8.4 ± 0.2	2.54 ± 0.21	0.21 ± 0.05
3	-5.9 ± 0.1	5.04 ± 0.12	0.44 ± 0.07
4	-3.8 ± 0.1	7.14 ± 0.12	0.56 ± 0.08
5	-1.6 ± 0.2	9.34 ± 0.21	0.50 ± 0.08
6	0.27 ± 0.06	11.21 ± 0.09	2.01 ± 0.17
7	2.1 ± 0.2	13.04 ± 0.21	0.58 ± 0.18

Energy spacings in ${}_{\Lambda}^{12}\text{C}$

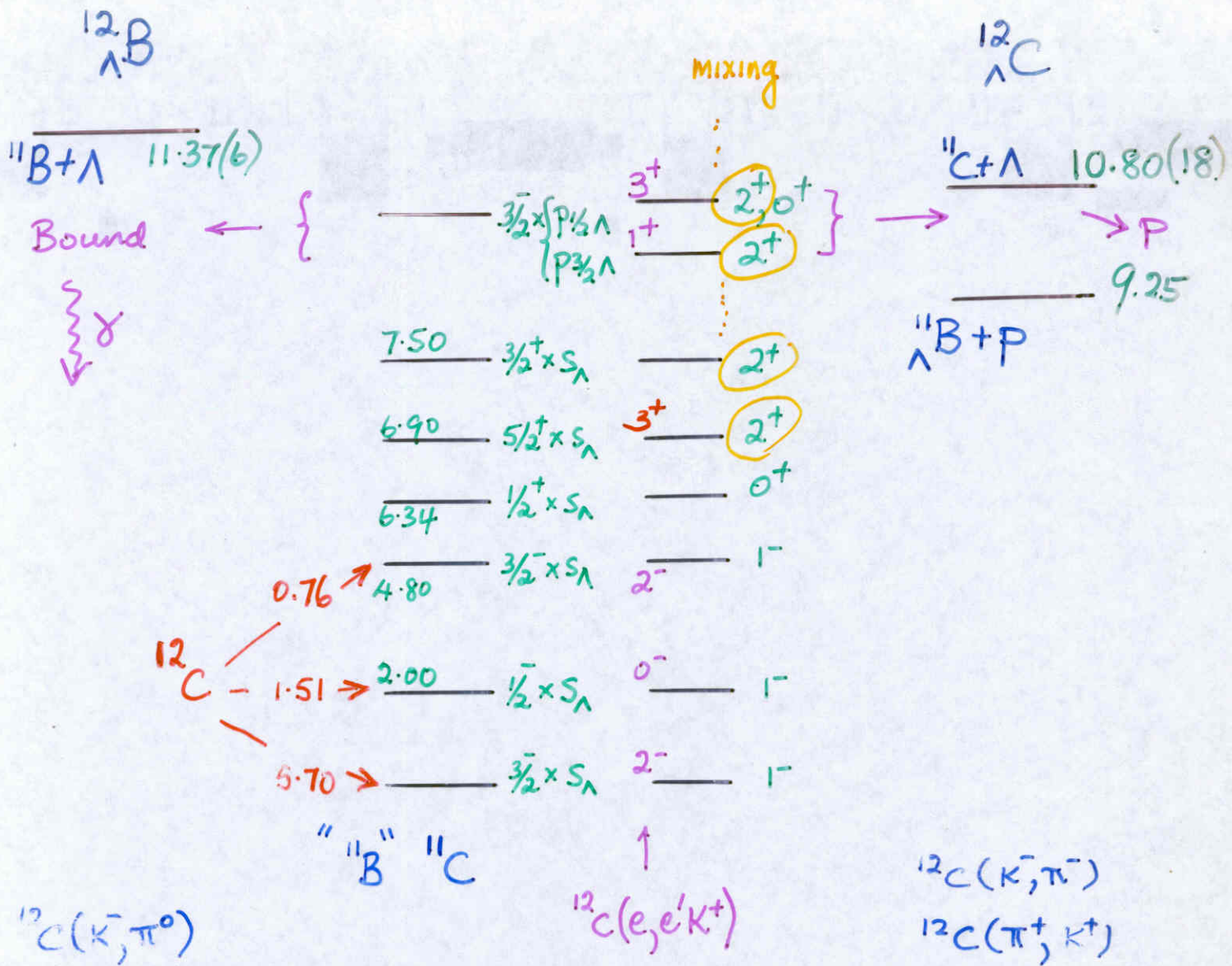
			$\Lambda\Sigma$ (keV)
5826	_____	1^-	28
5707	_____	2^-	35
5169	_____	3^-	15
4687	_____	2^-	106
2673	_____	0^-	23
2632	_____	1^-	49
233	_____	2^-	40
0	_____	1^-	97

J_n^π	$\Lambda\Sigma$	Δ	S_Λ	S_N	T	E_x
1_2^-	48	186	-13	464	23	2632 keV
1_3^-	70	226	6	751	34	5826 keV
2_1^-	57	264	-17	-24	-77	233 keV

KEK Experiment

$E_x(1_2^-)$ ($E_{core} = 2.00$) 2.51, 2.62 (E369), 2.70 (E336)

$E_x(1_3^-)$ ($E_{core} = 4.80$) 6.30, 5.92 (E369), 6.22 (E336)



Full shell-model basis

$$A = 11(0h\nu) \times p_\Lambda + A = 11(1h\nu) \times s_\Lambda$$

$$\langle p_n p_\Lambda | V_{\Lambda N} | (sd)_N s_\Lambda \rangle$$

Center of mass constraint