

# Experience on Coupling Correction in the ESRF electron storage ring

Laurent Farvacque & Andrea Franchi,  
on behalf of the  
Accelerator and Source Division

Future Light Source workshop 2012

Jefferson Lab, Newport News, VA, 5<sup>th</sup> to 9<sup>th</sup> March 2012

## Outlines

- Vertical emittance s in the presence of coupling
- Coupling correction via Resonance Driving Terms
- Experience in the ESRF storage ring (2010)
- Experience in the ESRF storage ring (2011)
- Benefits and drawbacks; operational considerations

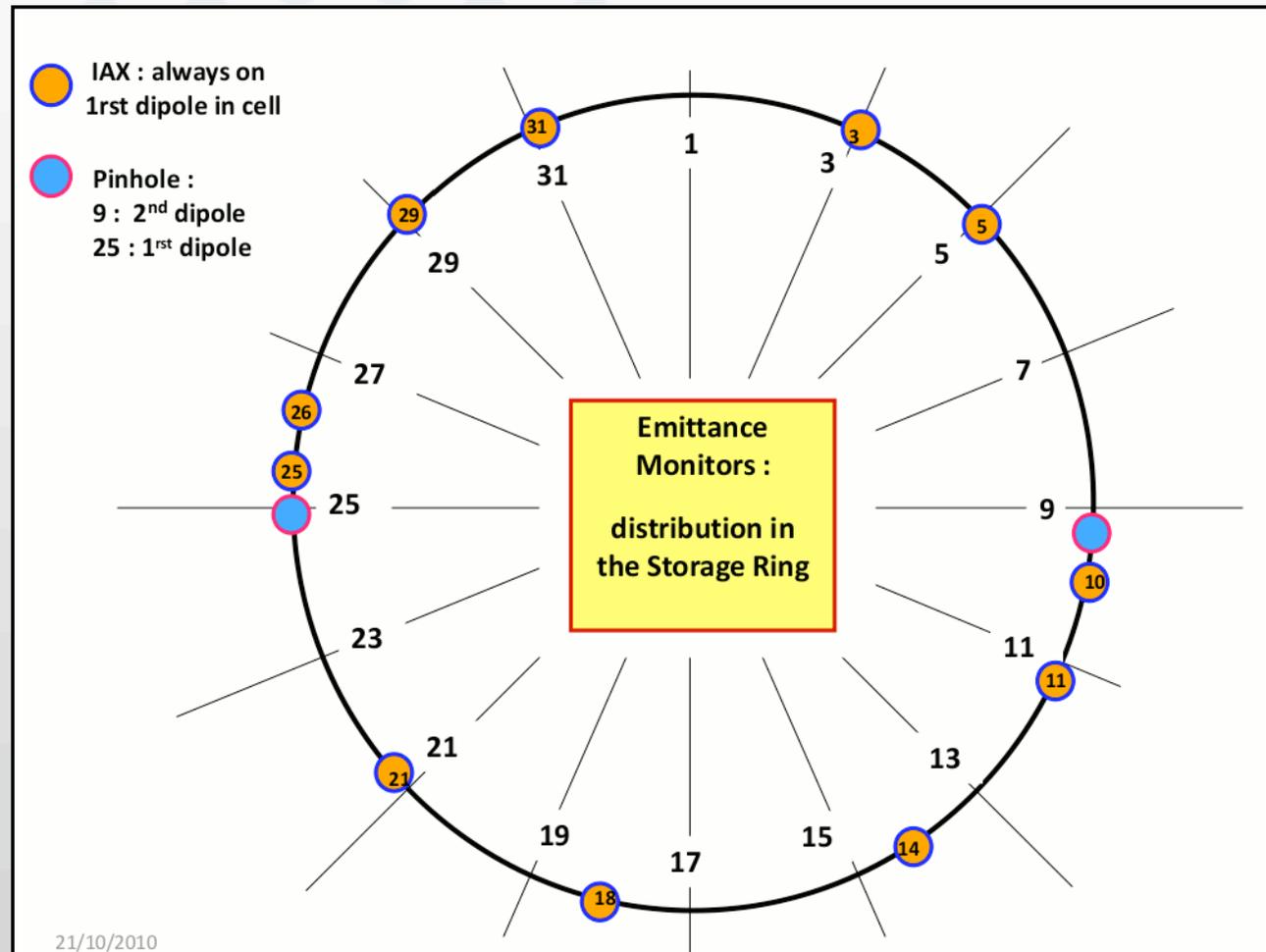
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# Meas. vertical emittance $E_y$ from RMS beam size

ESRF SR equipment:

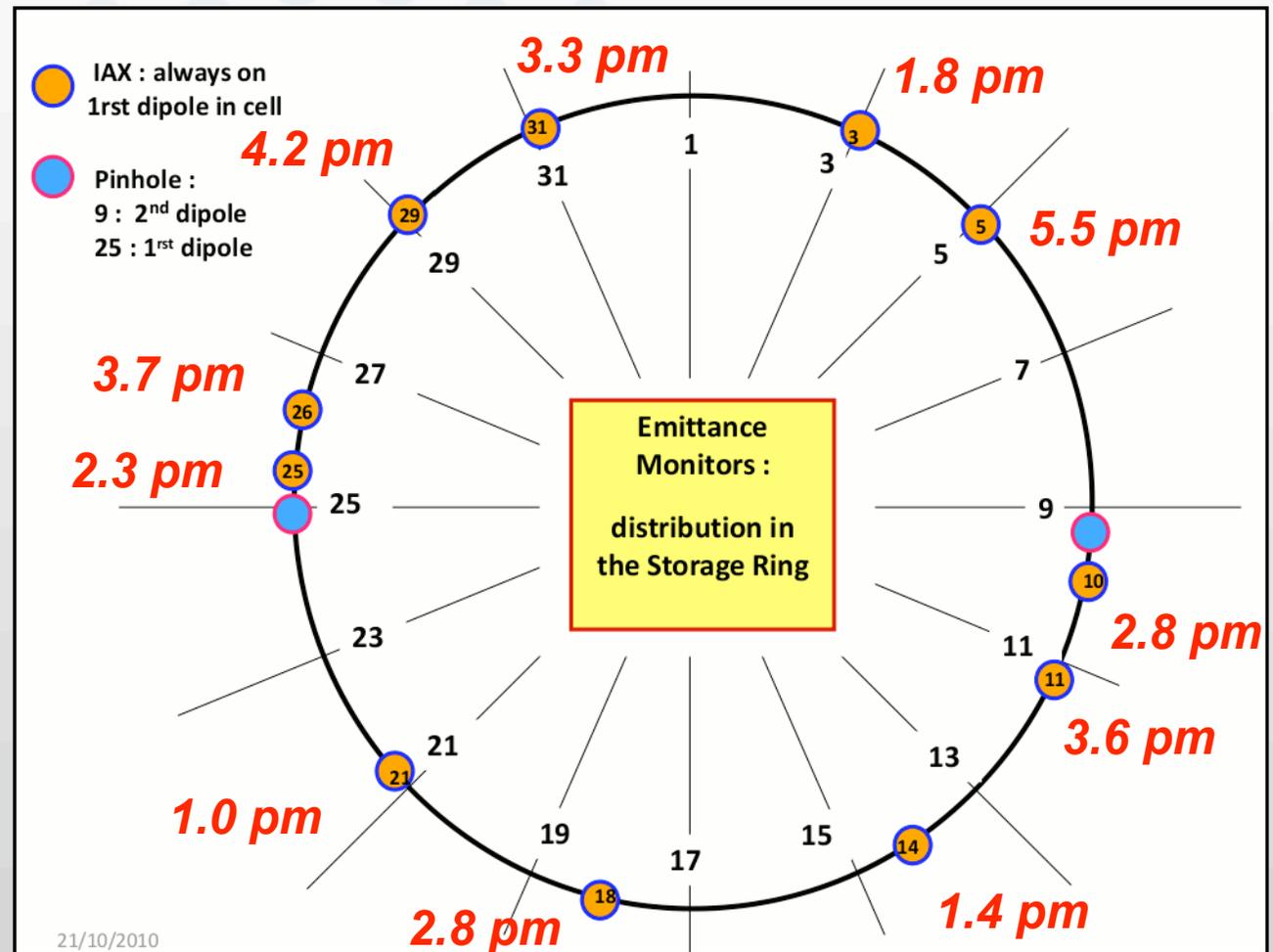
- 11 dipole radiation projection monitors (IAX)
- 2 pinhole cameras



# Meas. vertical emittance $E_y$ from RMS beam size

$E_x = 4.2$  nm

- Well corrected coupling
- Low beam current (20 mA)

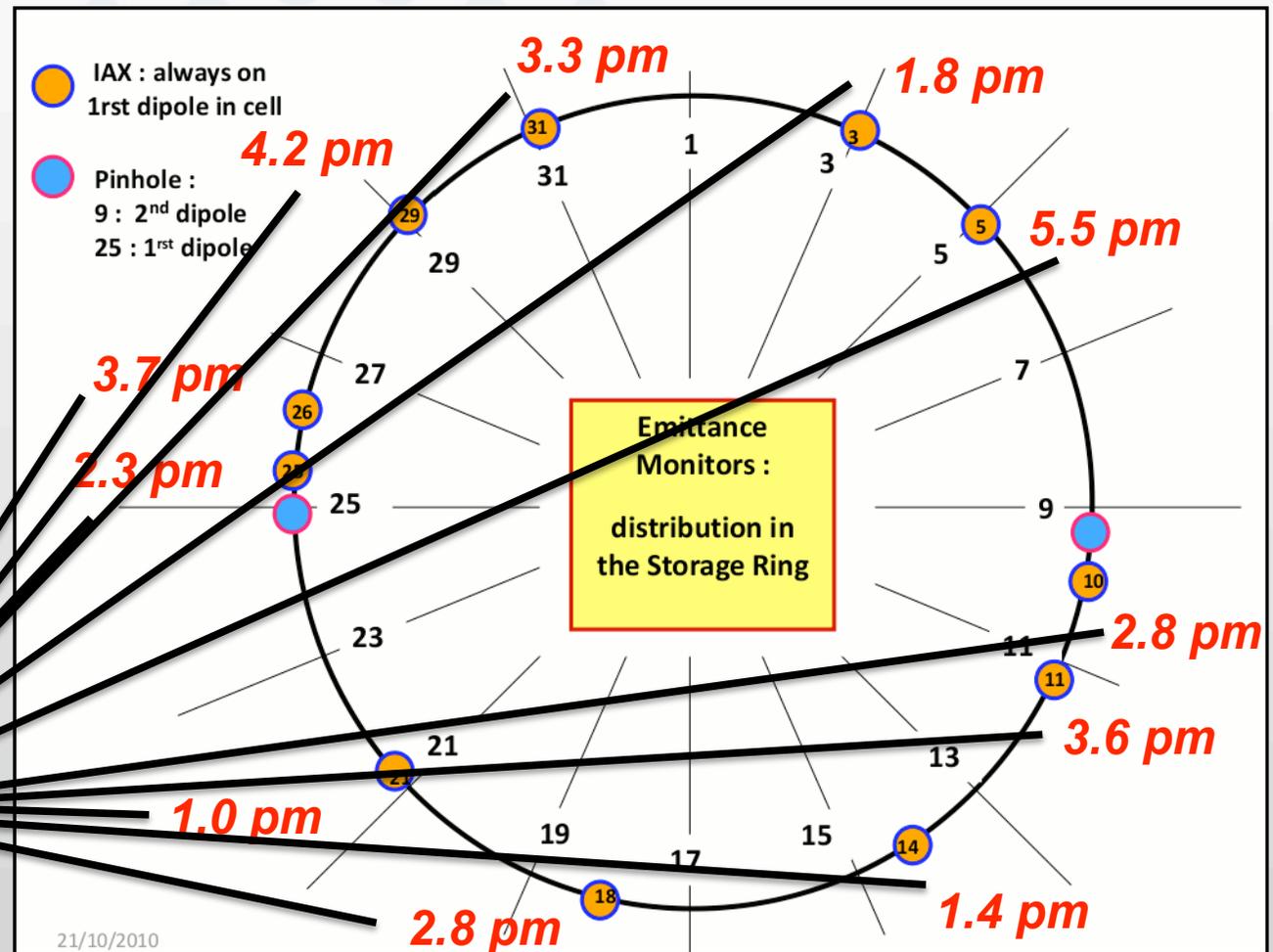


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$\bar{E}_y = 3.0 \text{ pm}$   
 $\pm 1.3 \text{ (STD)}$

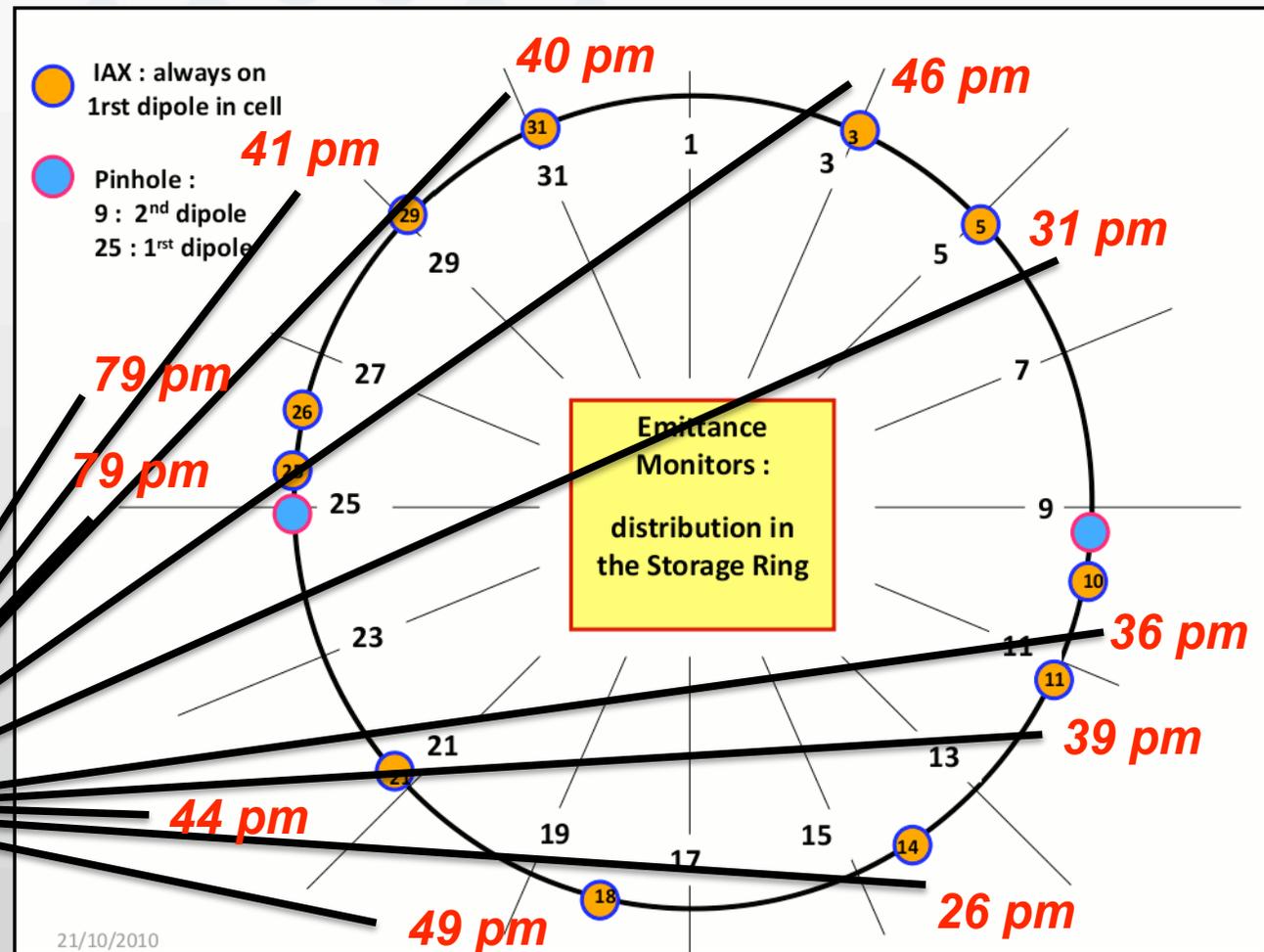


# Meas. vertical emittance $E_y$ from RMS beam size

$E_x = 4.2 \text{ nm}$

- Uncorrected coupling
- Low beam current (20 mA)

$\bar{E}_y = 46 \text{ pm}$   
 $\pm 18 \text{ (STD)}$



# Vertical emittances in the presence of coupling

Measurable apparent emittance:

$$\mathbb{E}_y(s) = \frac{\sigma_y^2(s)}{\beta_y(s)} = \frac{\langle y^2(s) \rangle - (\delta D_y(s))^2}{\beta_y(s)}$$

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$$\epsilon_y(s) = \sqrt{\sigma_y(s)\sigma_p(s) - \sigma_{yp}^2(s)}$$

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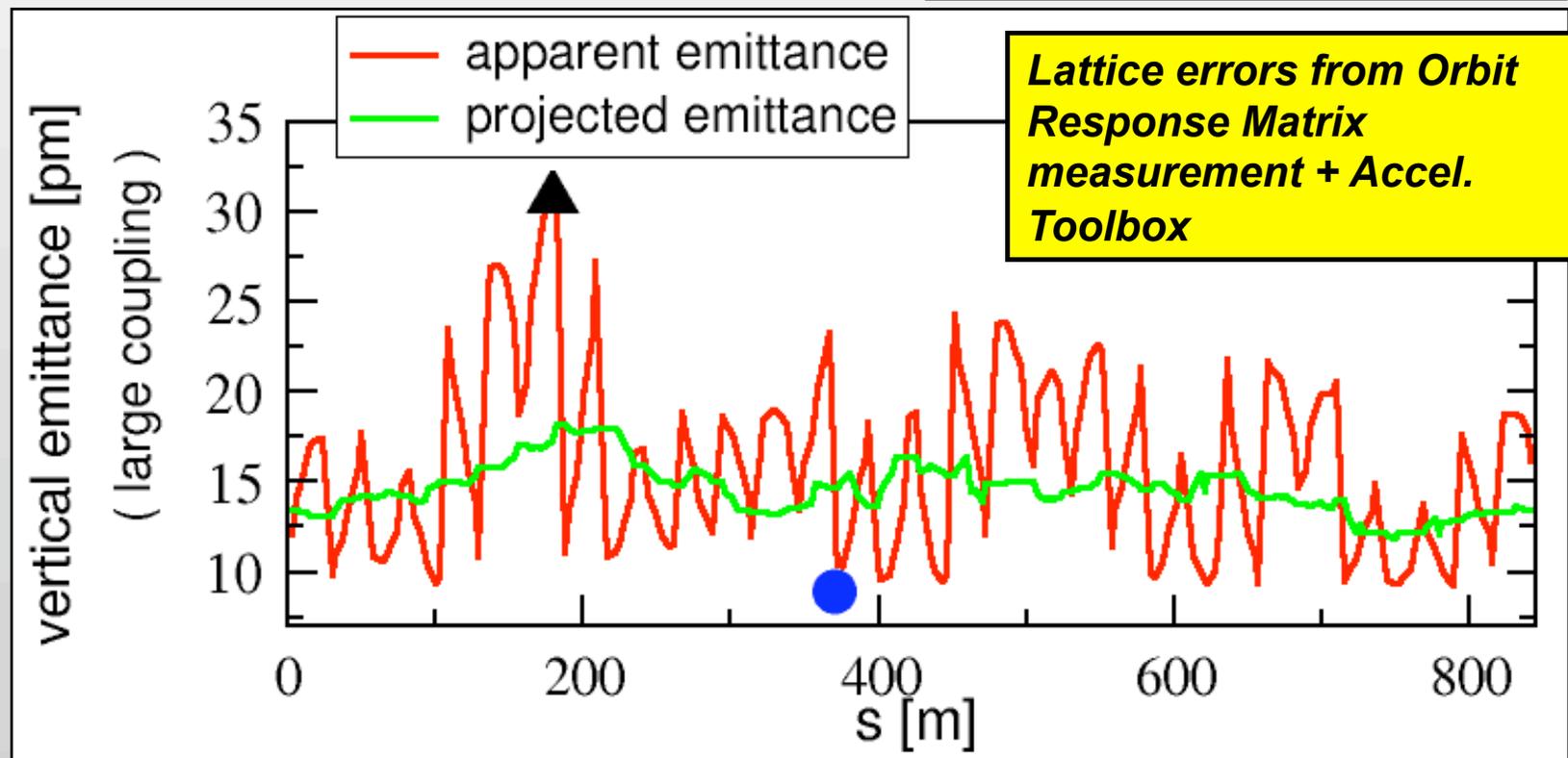
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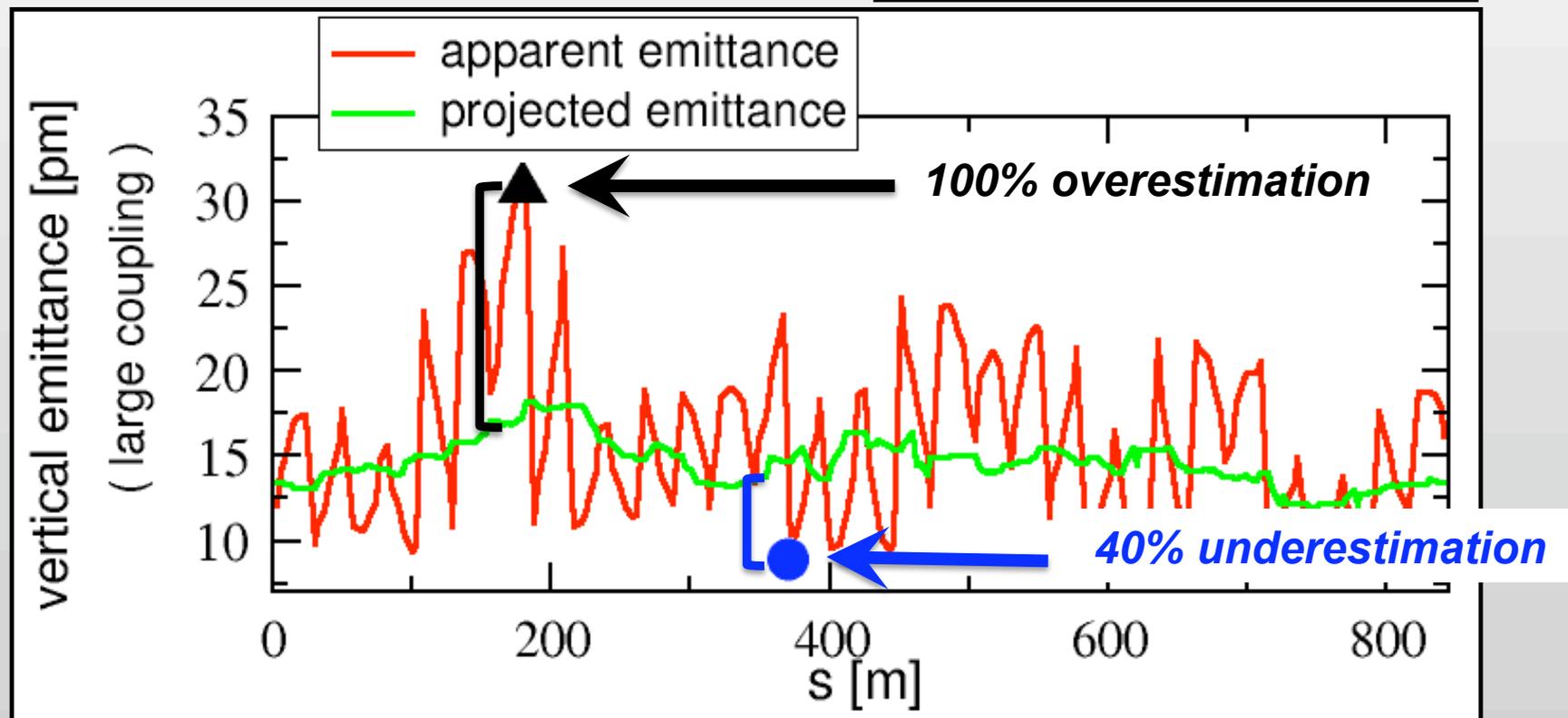
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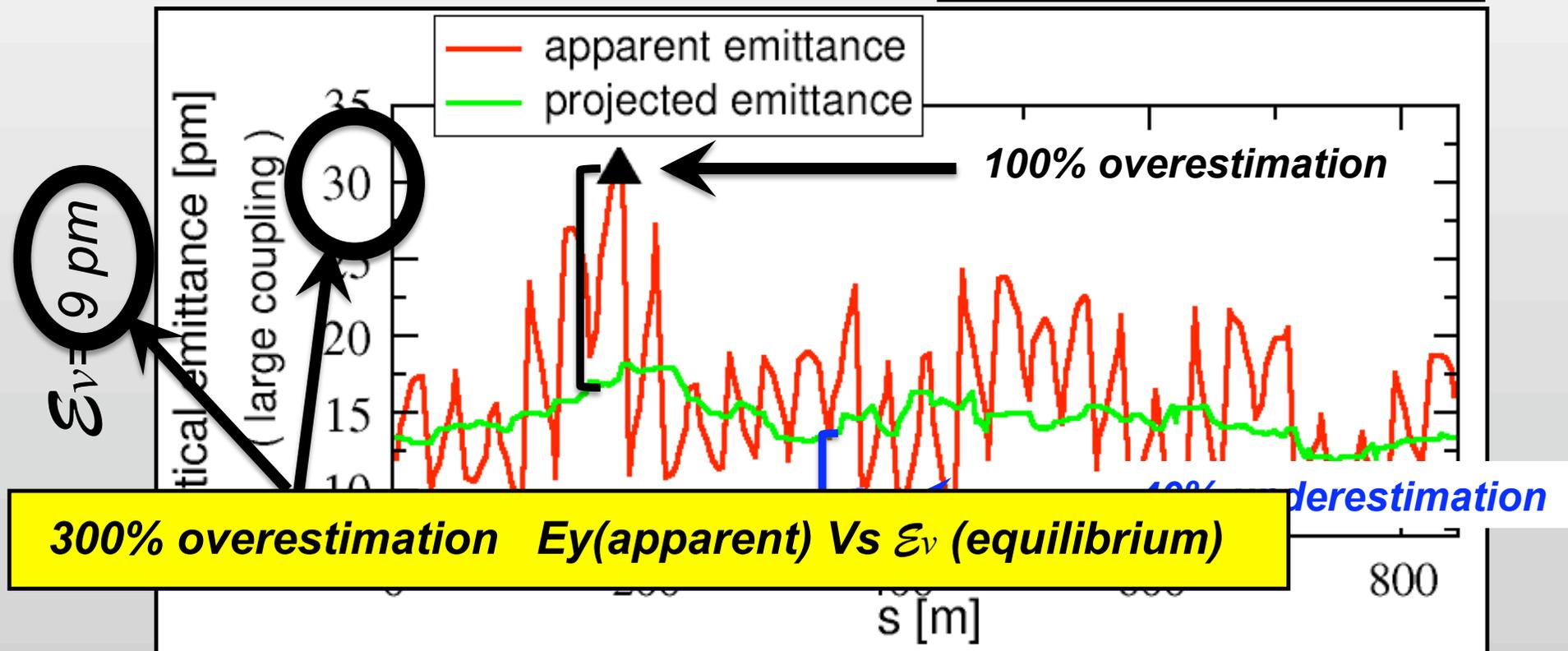
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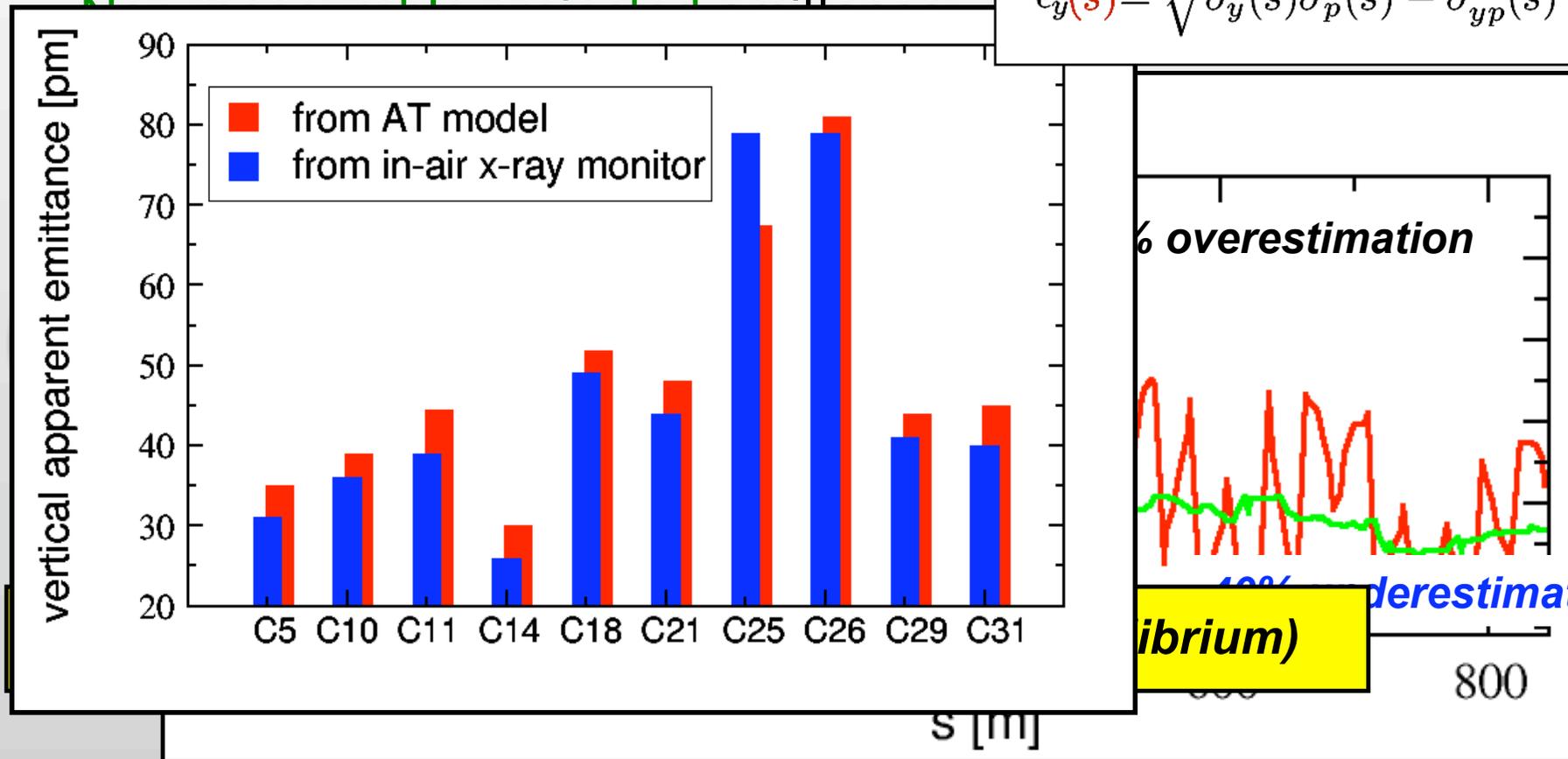


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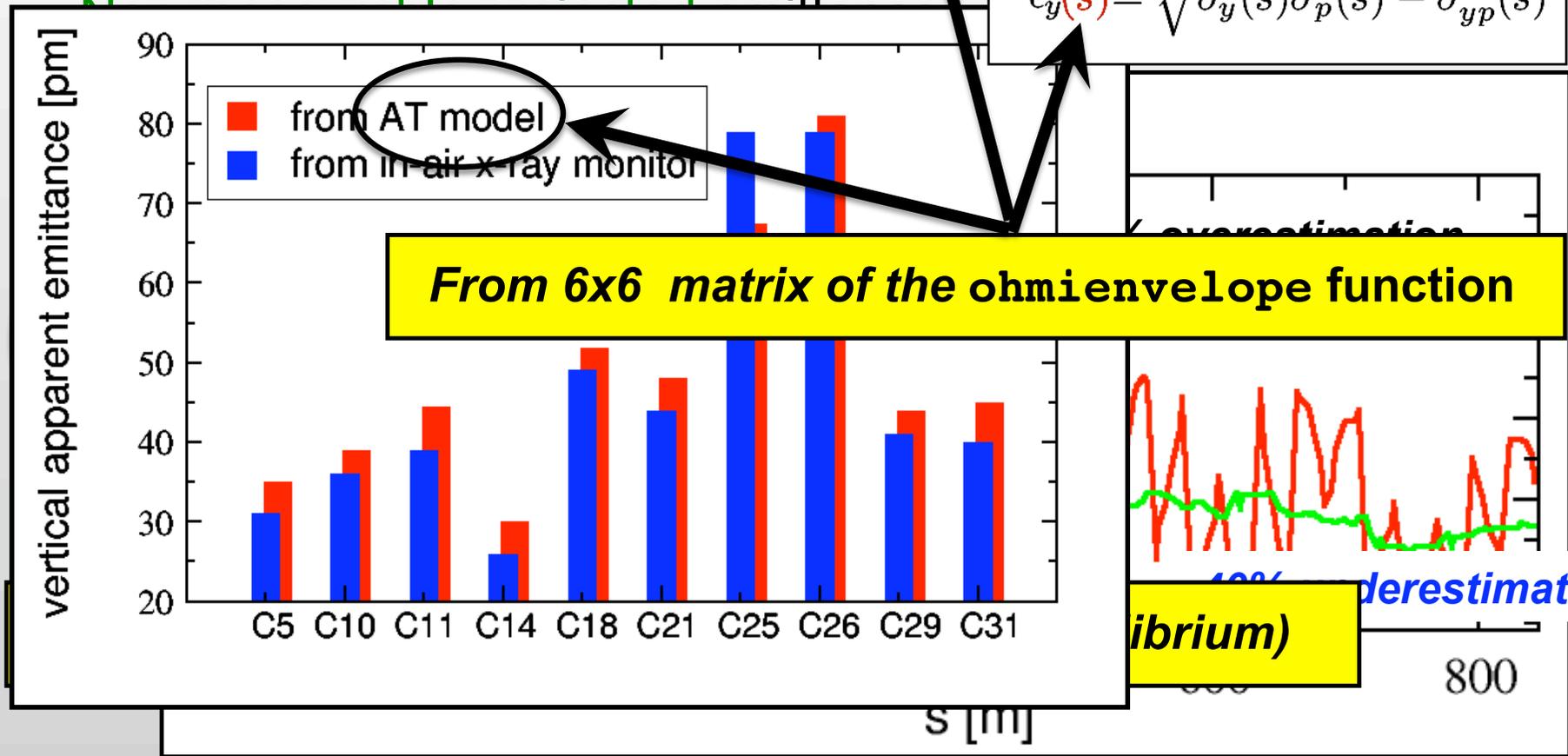


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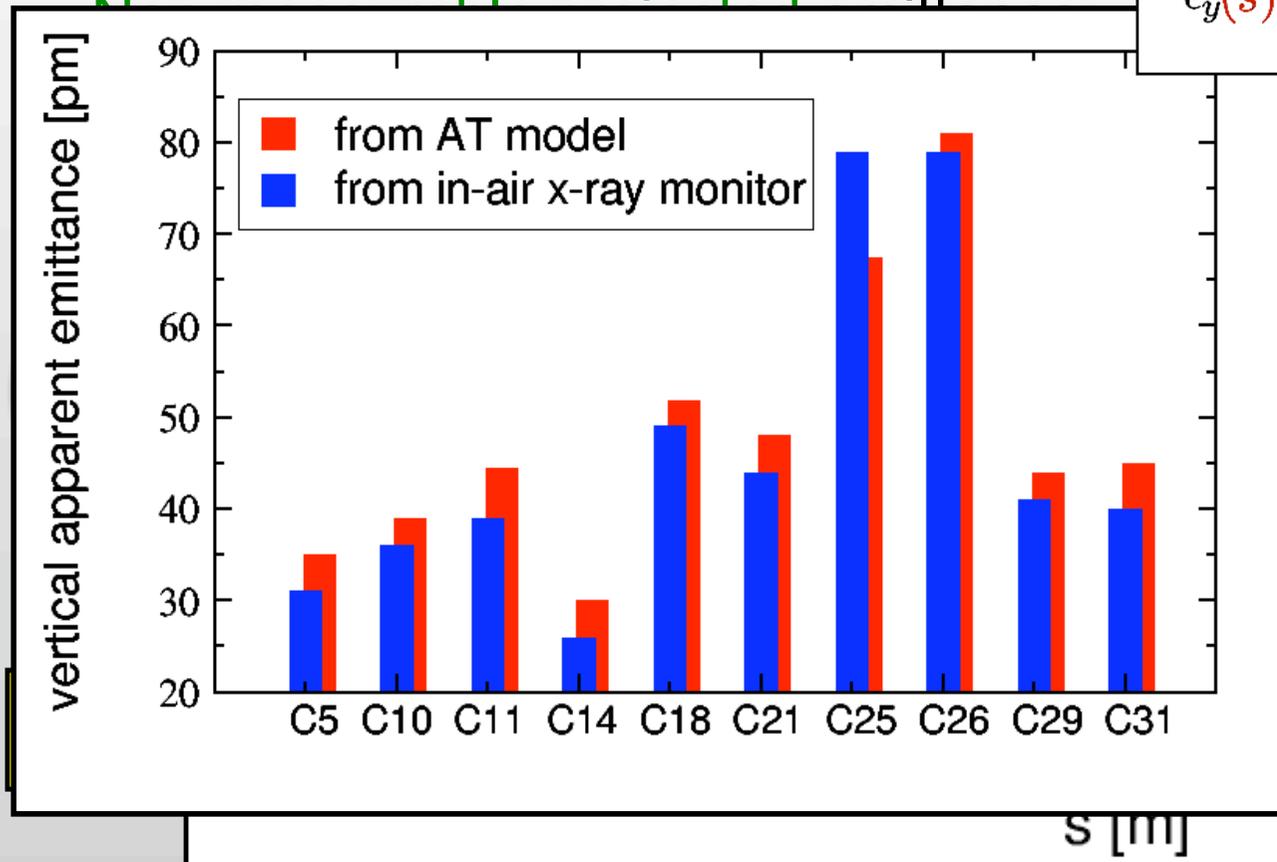
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$$\epsilon_y(s) =$$

**Which  
“vertical  
emittance”  
shall we  
choose,  
then?**



ibrium)

800

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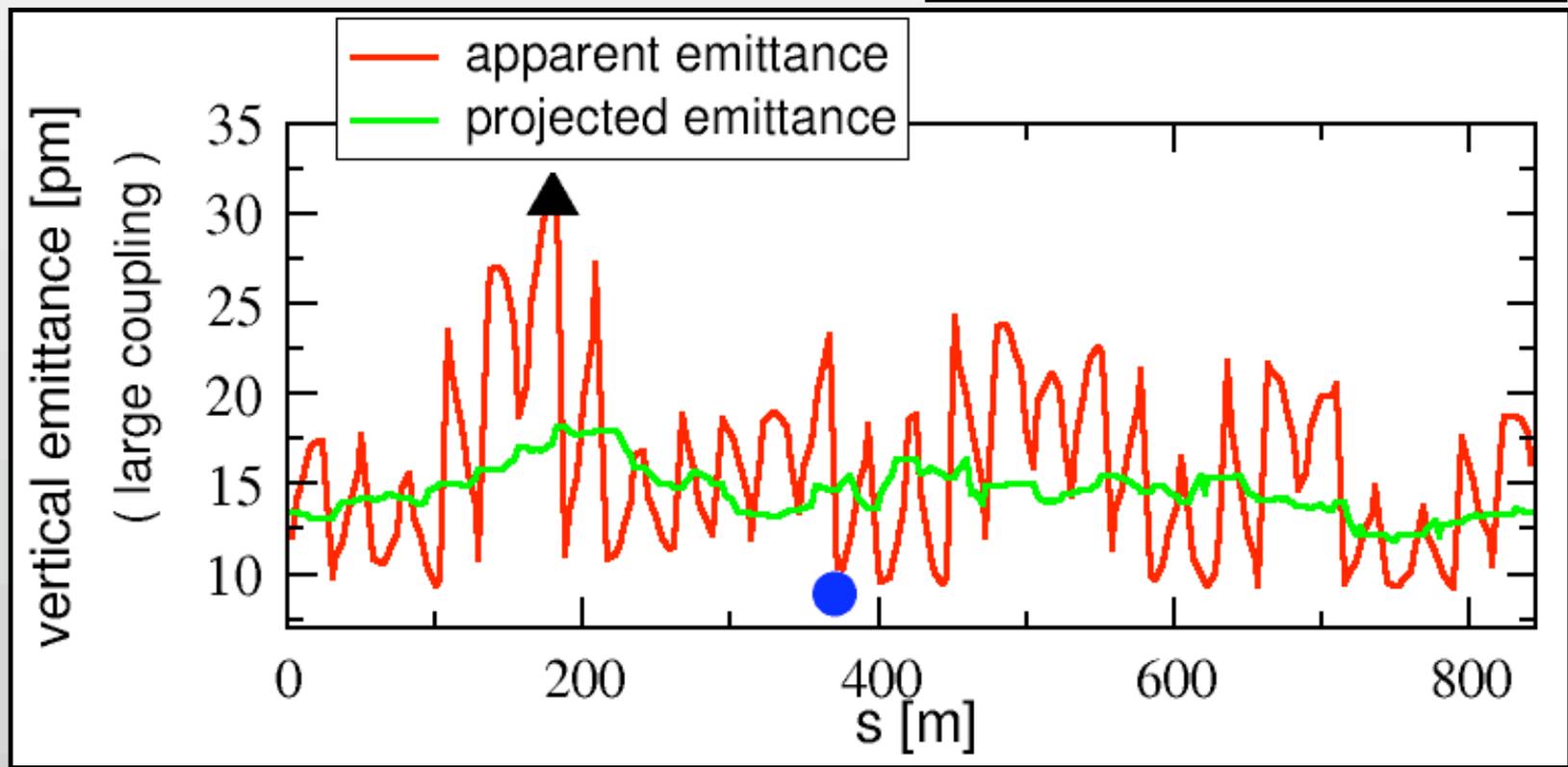
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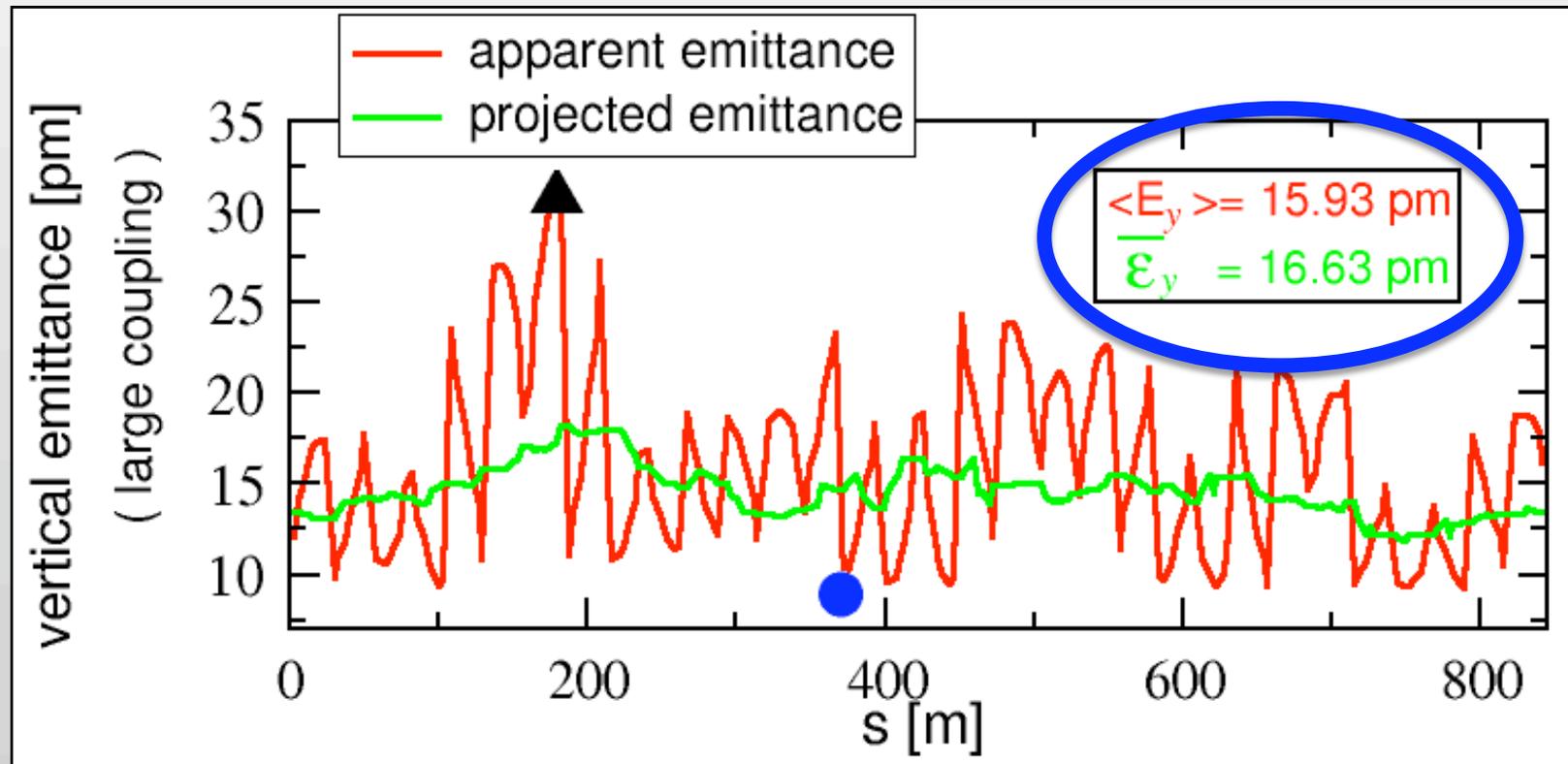
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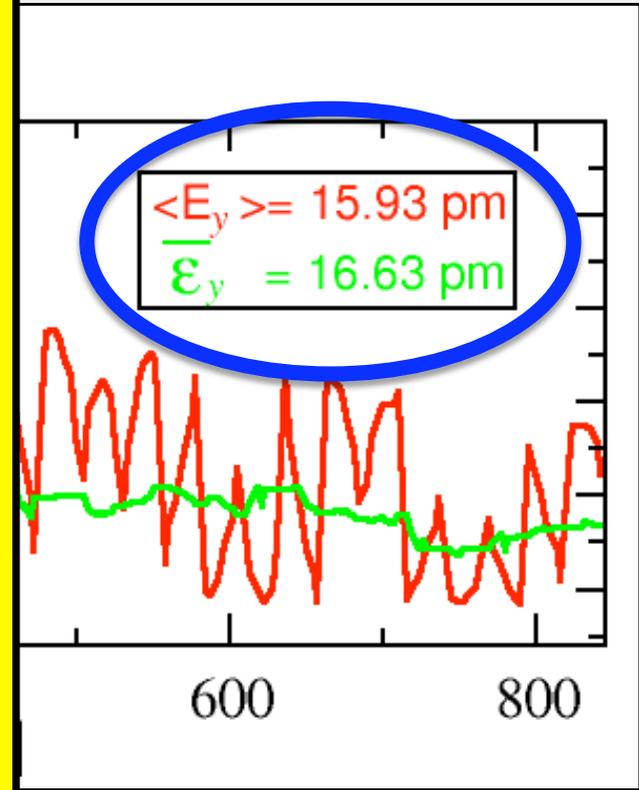
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## Definition of vertical emittance @ ESRF:

$$\bar{\epsilon}_y = \frac{1}{C} \oint \epsilon_y(s) ds \simeq \langle \mathbb{E}_y \rangle = \frac{1}{N} \sum_{n=1}^{n=N} \mathbb{E}_{y,n}$$

$$\delta\epsilon_y = \left( \sum_n (\mathbb{E}_{y,n} - \langle \mathbb{E}_y \rangle)^2 / N \right)^{1/2}$$

More details in PRSTAB-14-012804 (2011)



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## Vertical emittance reduction in the storage ring

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- time consuming

local minimum value

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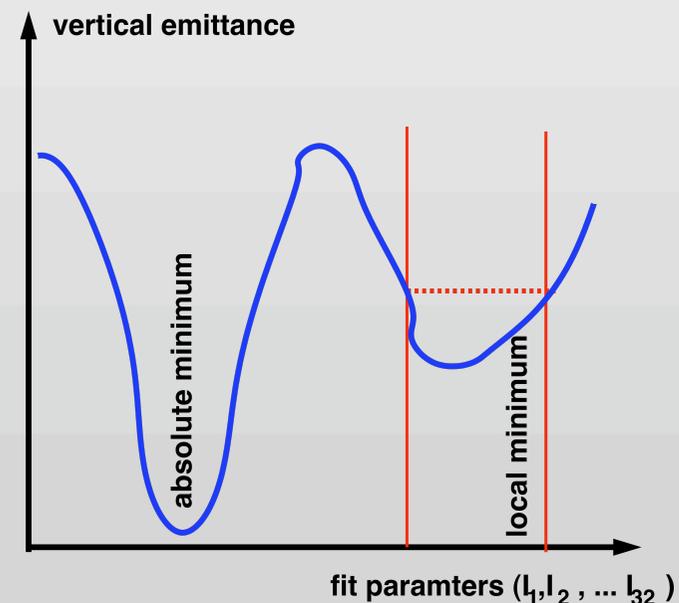
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  - time consuming
  - may get stuck into a local minimum value

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Details and formulas in PRSTAB-14-012804 (2011)

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  - faster
  - gets directly to absolute minimum value

Details and formulas in PRSTAB-14-012804 (2011)

## Coupling correction via Resonance Driving Terms

The lower the vertical dispersion and the coupling RDTs, the smaller the vertical emittances

Procedure [already independently developed by R. Tomas (for ALBA)]:

1. Build an error lattice model (quad tilts, etc. from Orbit Response Matrix or turn-by-turn BPM data) => RDTs and  $D_y$

$$\vec{F} = (a_1 * f_{1001}, a_1 * f_{1010}, a_2 * D_y) , \quad a_1 + a_2 = 1$$

1. Evaluate response matrix of the available skew correctors  $M$
2. Find via SVD a corrector setting  $\vec{J}$  that minimizes both RDTs and  $D_y$

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$$\text{ORM} = \begin{pmatrix} \mathbf{O}_{xx} & \mathbf{O}_{xy} \\ \mathbf{O}_{yx} & \mathbf{O}_{yy} \end{pmatrix}$$

Orbit Response Matrix  
at 224 BPMs after  
exciting 16x2 steerers  
(H,V)

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Fitting measured diagonal blocks from ideal ORM => focusing errors  $\Delta K_1$ .

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# Coupling correction via Resonance Driving Terms

Vertical dispersion  $D_y$  is measured at all 224 BPMs

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$$\begin{array}{l}
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From MADX or AT

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From MADX or AT

$$m_{w,c} = \frac{\sqrt{Q_w Q_v} e^{i(\Delta\phi_{w,x} \mp \Delta\phi_{w,y})}}{4 \Delta J_1^{(c)}},$$

1. Build an error lattice model (quad tilts, etc. from Orbit Response Matrix or turn-by-turn BPM data) → RDTs and  $D_y$

$$\vec{F} = (a_1 * f_{1001}, a_1 * f_{1010}, a_2 * D_y), \quad a_1 + a_2 = 1$$

1. Evaluate response matrix of the available skew correctors **M**
2. Find via SVD a corrector setting  $\vec{J}$  that minimizes both RDTs and  $D_y$

$$\vec{J} = -\mathbf{M} \vec{F} \quad \text{to be pseudo-inverted}$$

## Coupling correction via Resonance Driving Terms

$$\begin{pmatrix} a_1 \vec{f}_{1001} \\ a_1 \vec{f}_{1010} \\ a_2 \vec{D}_y \end{pmatrix}_{\text{meas}} = -\mathbf{M} \vec{J}_c,$$

$a_2=0.7$  (2010) ,  $0.4$  (2011)

$a_1+a_2=1$

Different weights on  $f_{1001}$  and  $f_{1010}$  tried, best if equal.

1. Build an error lattice model (quad tilts, etc. from Orbit Response Matrix or turn-by-turn BPM data) => RDTs and  $D_y$

$$\vec{F} = (a_1 * f_{1001}, a_1 * f_{1010}, a_2 * D_y) , \quad a_1 + a_2 = 1$$

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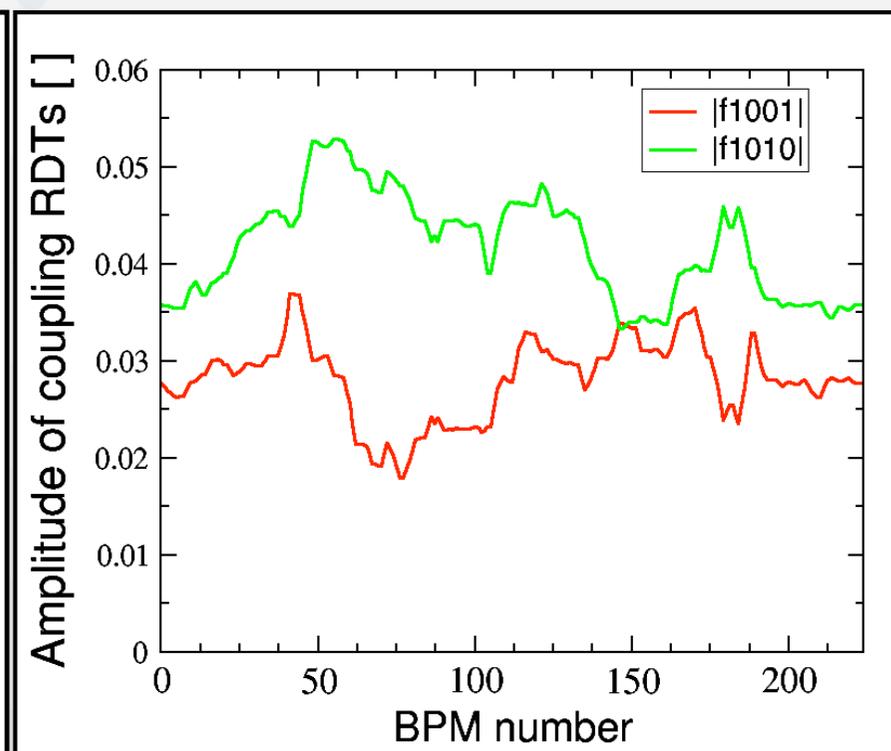
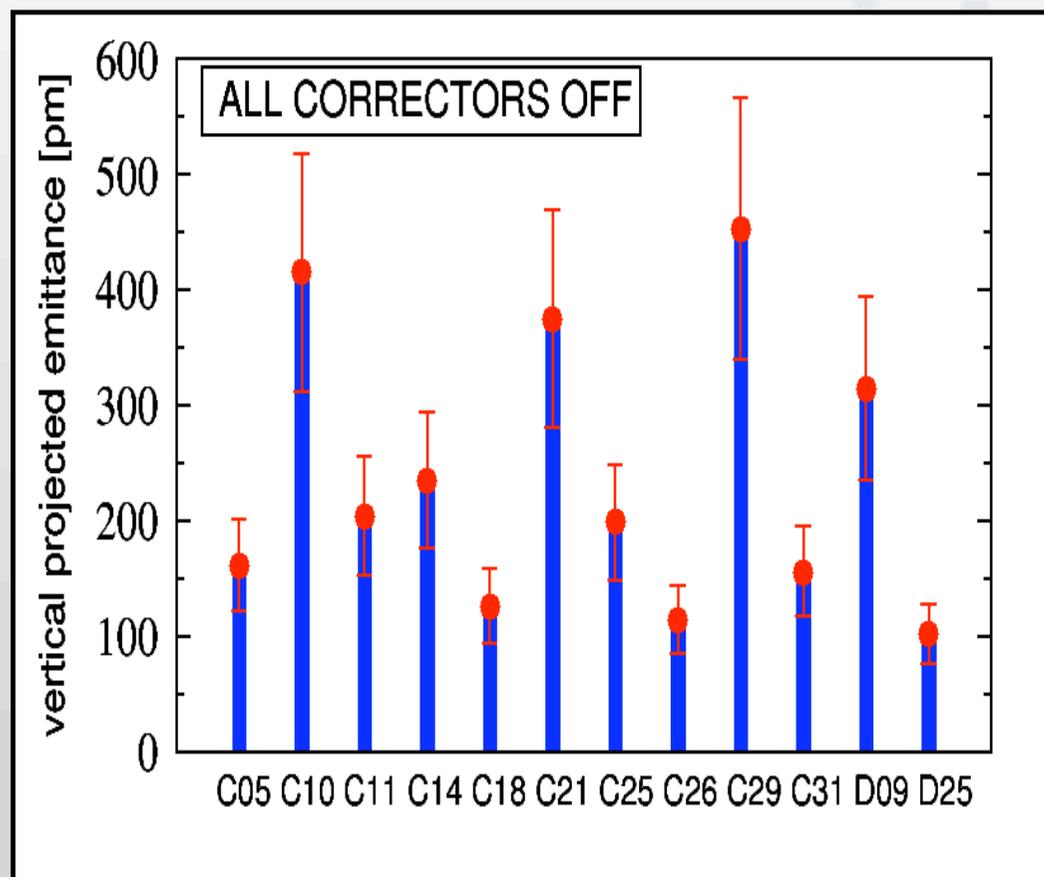
## Outlines

- Vertical emittances in the presence of coupling
- Coupling correction via Resonance Driving Terms
- **Experience in the ESRF storage ring (2010)**
- Experience in the ESRF storage ring (2011)
- Benefits and drawbacks; operational considerations

# 2010: Application in the ESRF storage ring

First RDT correction: January 16<sup>th</sup> 2010

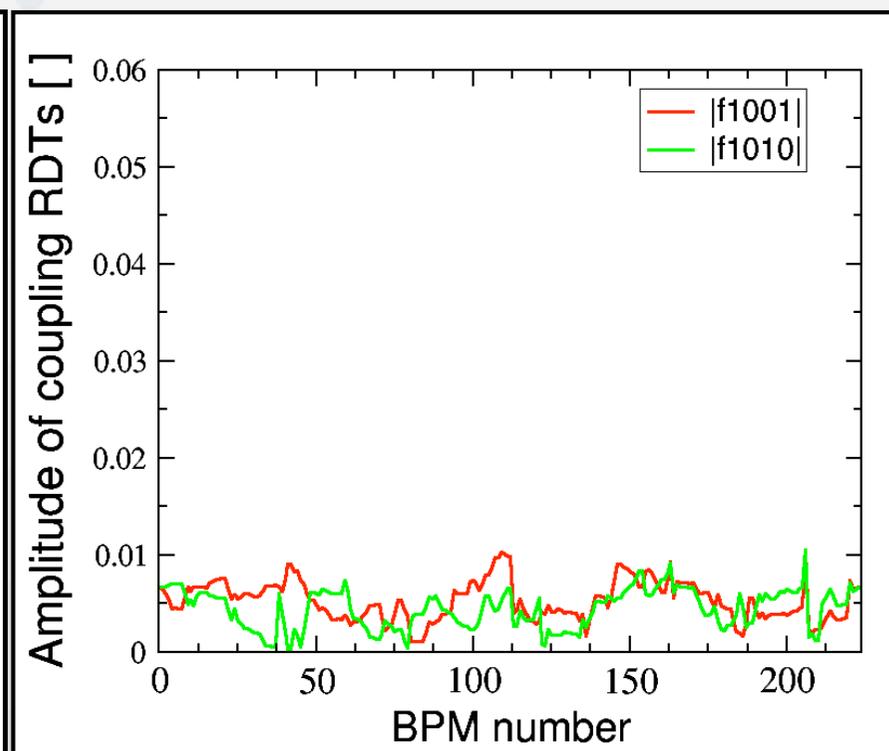
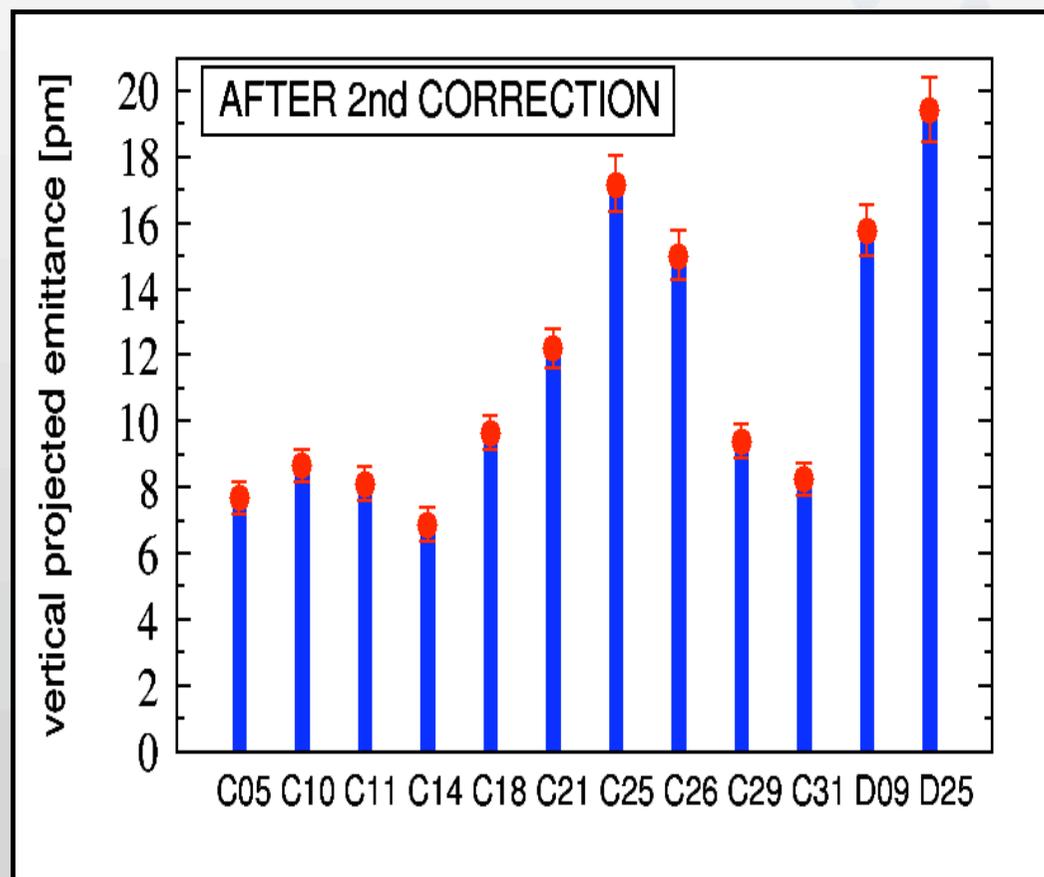
All skew correctors OFF:  $\bar{\epsilon}_y \pm \delta\epsilon_y = 237 \pm 122 \text{ pm}$



# 2010: Application in the ESRF storage ring

First RDT correction: January 16<sup>th</sup> 2010

After ORM measur. and RDT correction:  $\bar{\epsilon}_y \pm \delta\epsilon_y = 11.5 \pm 4.3 \text{ pm}$

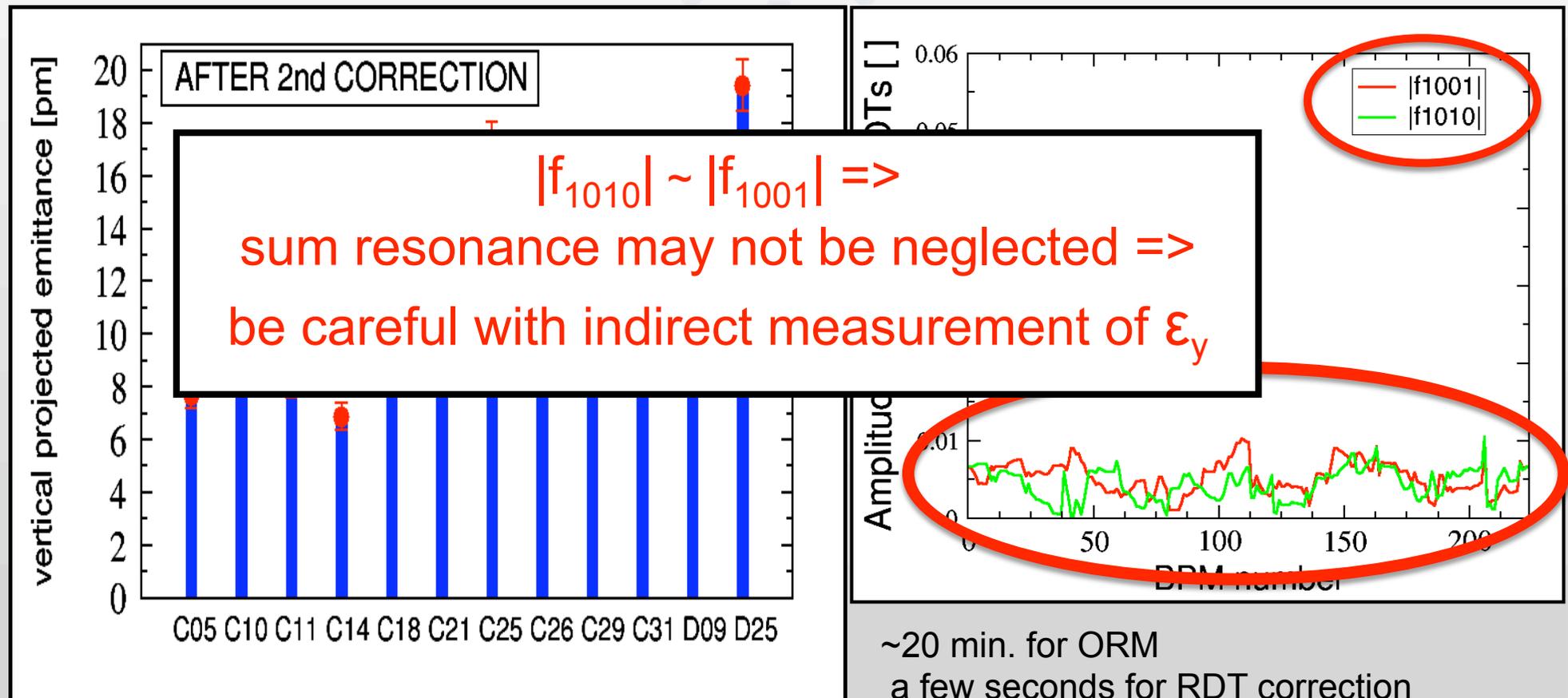


~20 min. for ORM  
a few seconds for RDT correction

# 2010: Application in the ESRF storage ring

First RDT correction: January 16<sup>th</sup> 2010

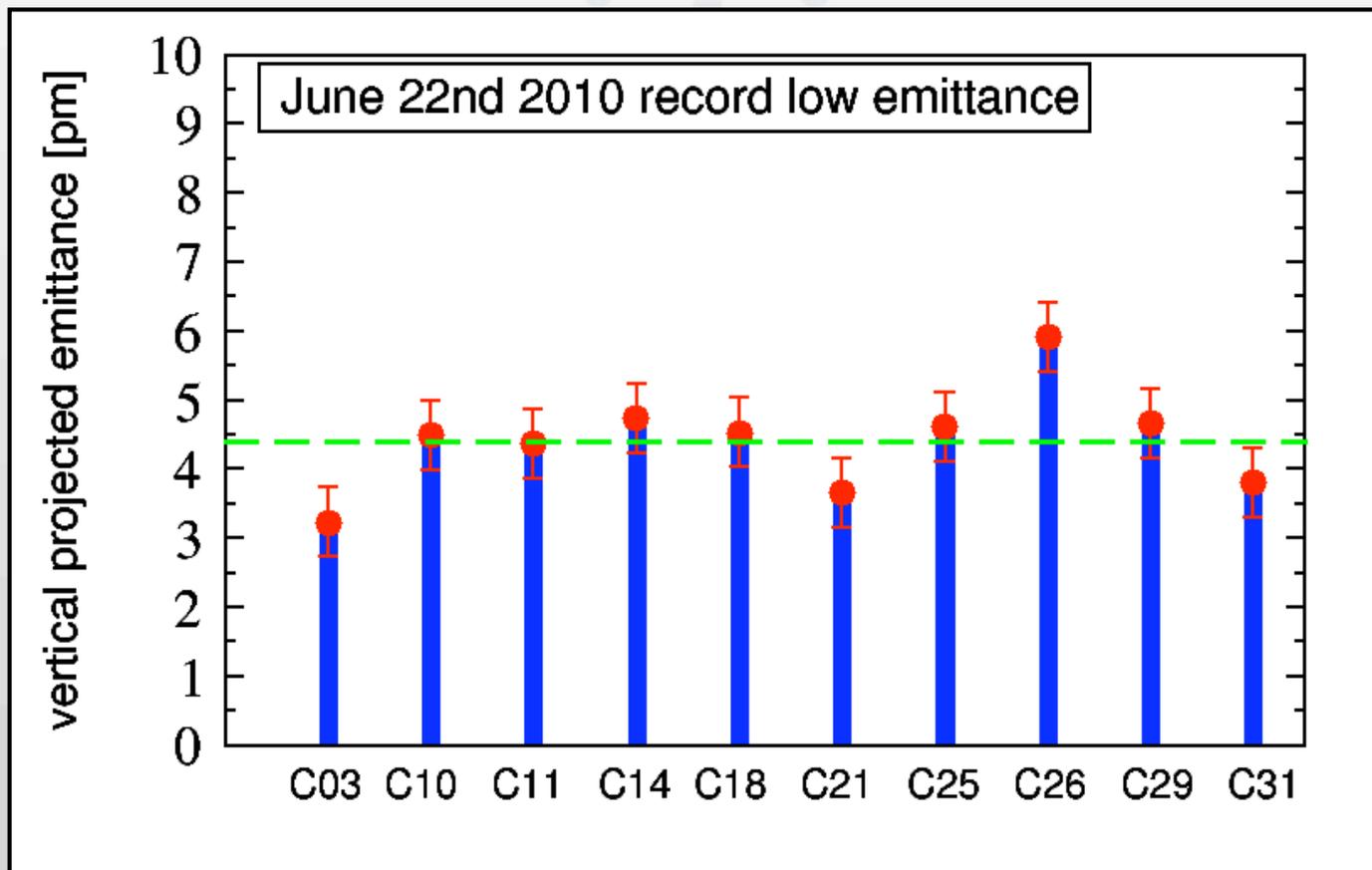
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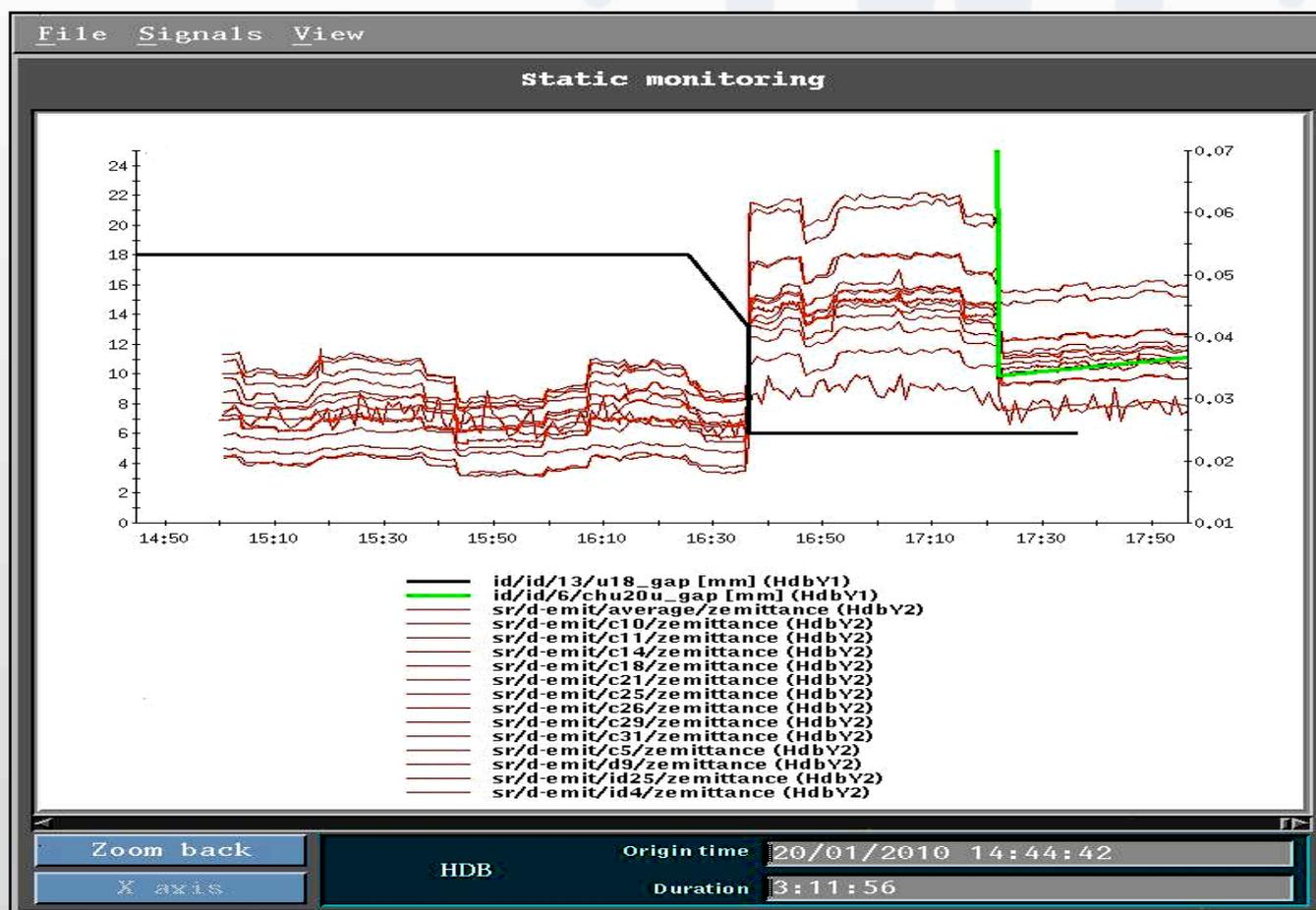
# 2010: Application in the ESRF storage ring

ESRF 2010 **temporary** record-low vertical emittance: June 22<sup>nd</sup>

At ID gaps open:  $\bar{\epsilon}_y \pm \delta\epsilon_y = 4.4 \pm 0.7$  pm



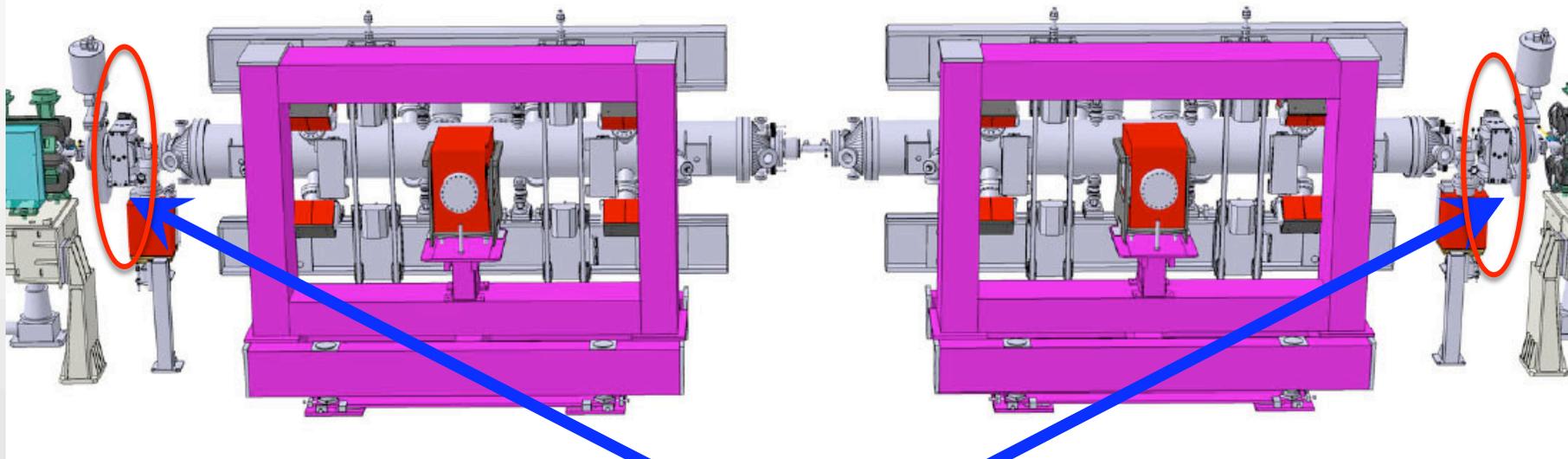
## 2010: Preserving vertical emittance during beam delivery



- Low coupling may not be preserved during beam delivery because of continuous changes of ID gaps that vary coupling along the ring

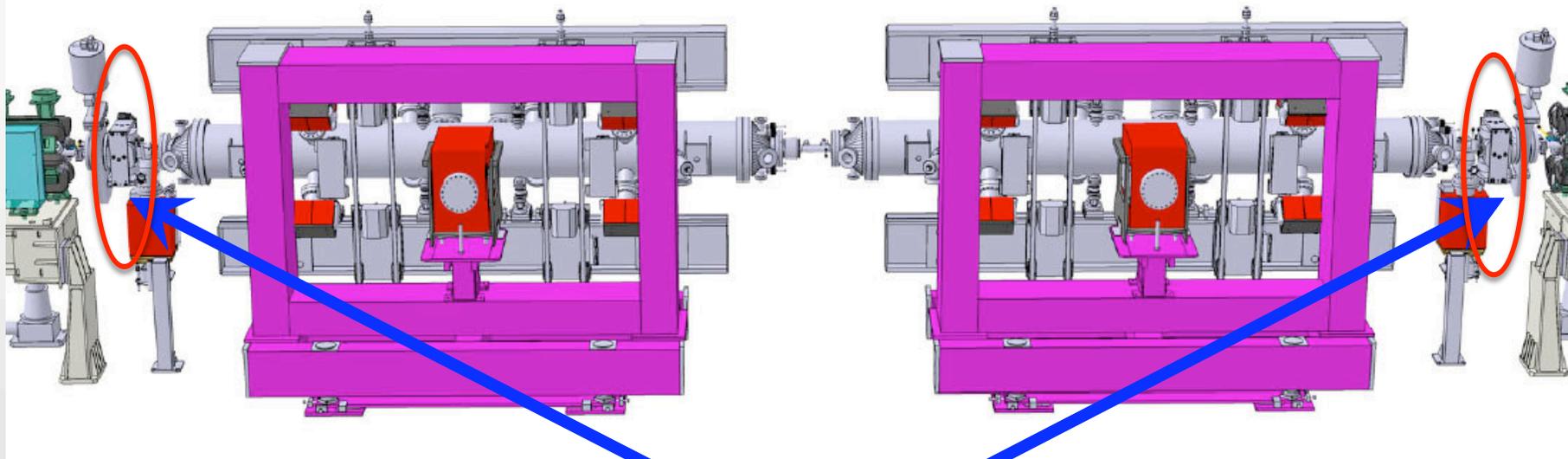
Apparent emittance measured at 13 monitors (red) on Jan. 20<sup>th</sup> 2010, during beam delivery and movements of two ID gaps (black & green)

## 2010: Preserving vertical emittance during beam delivery



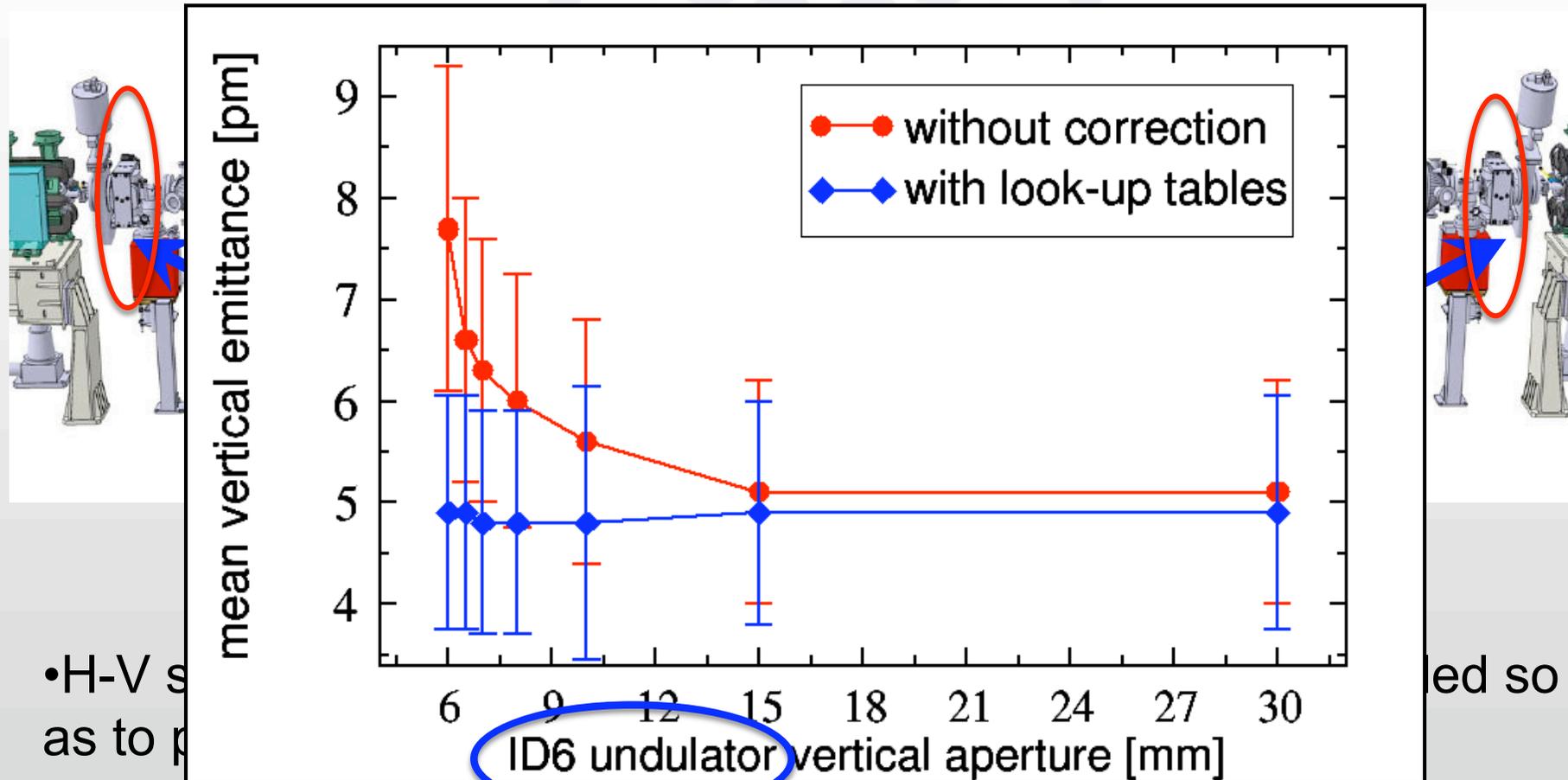
- H-V steerers at the ends of an ID straight section were cabled so as to provide skew quad fields.

## 2010: Preserving vertical emittance during beam delivery



- H-V steerers at the ends of an ID straight section were cabled so as to provide skew quad fields.
- Look-up tables (corrector currents Vs ID gap aperture) were defined so as to preserve the vertical emittance at any gap value.

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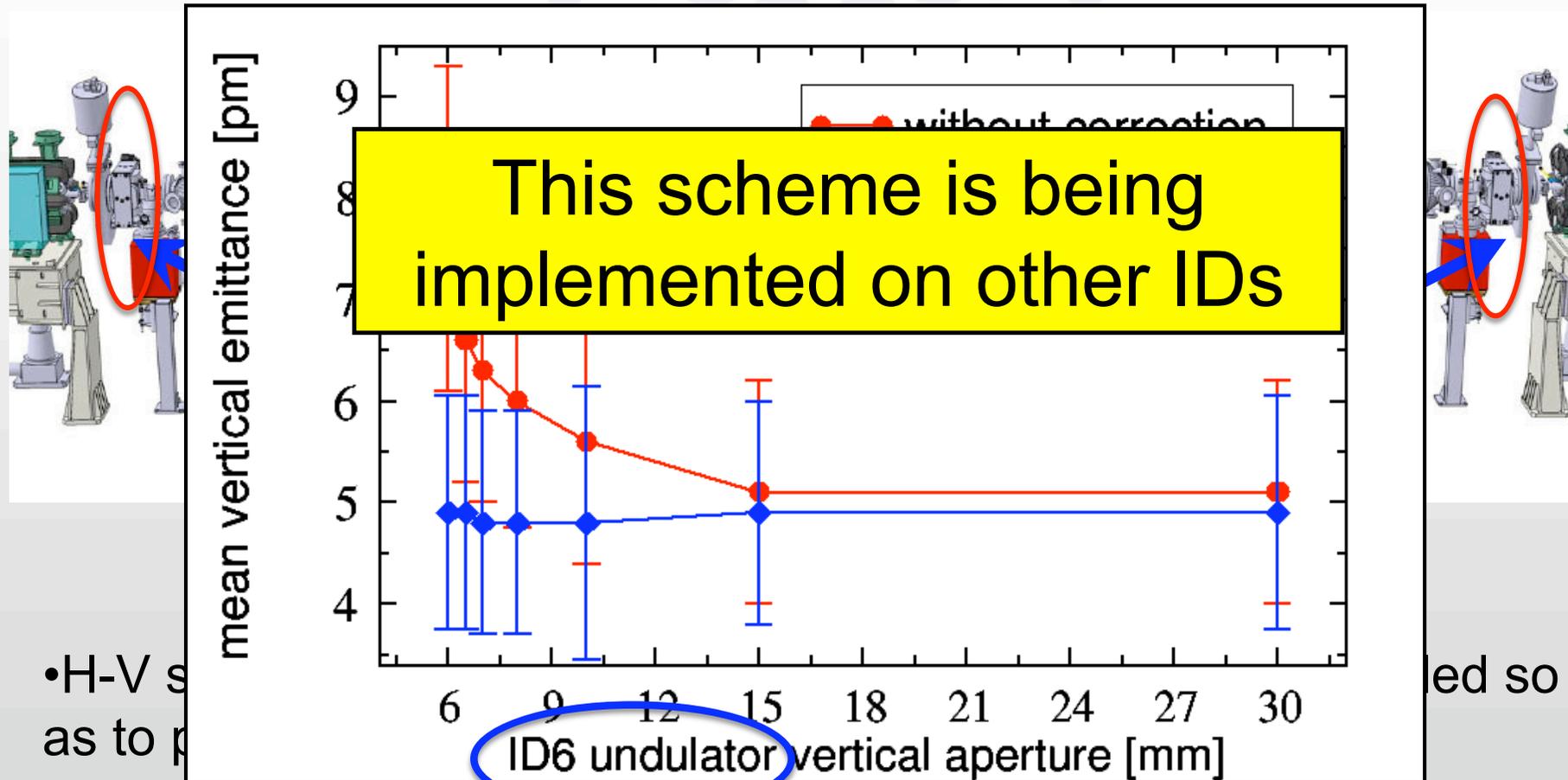


•H-V s  
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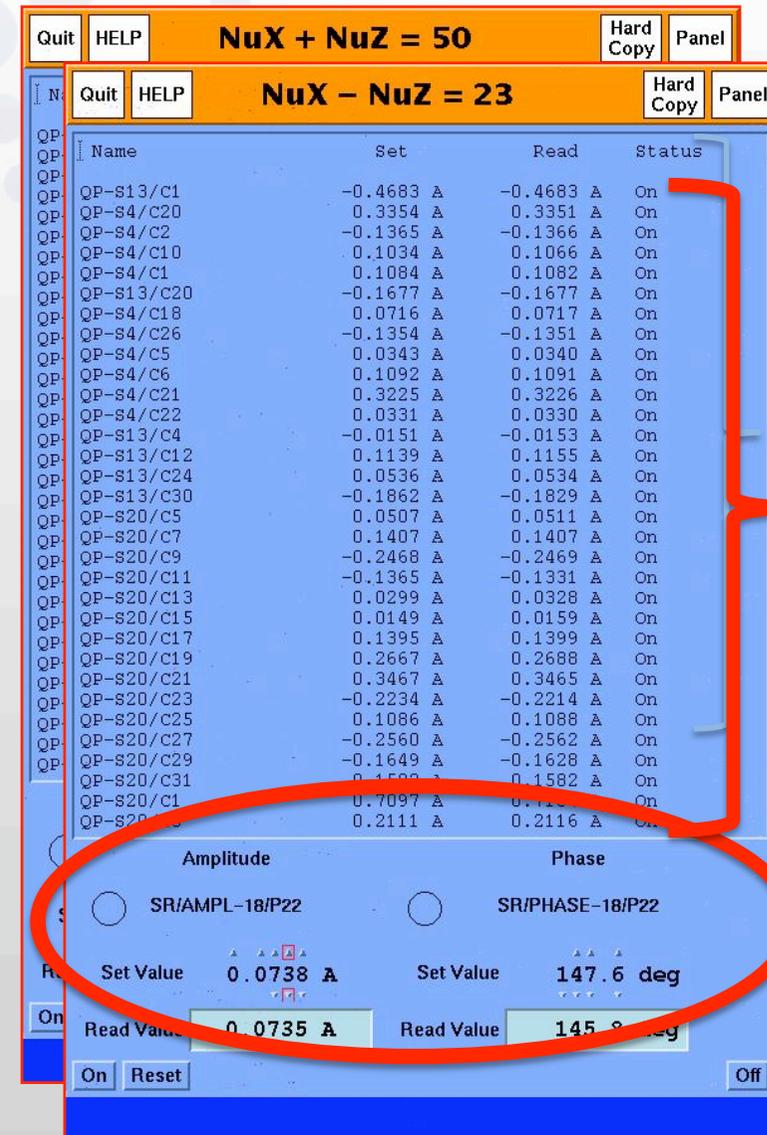
- Coupling may be represented by two complex vectors (for the sum and difference resonances respectively)  $C^\pm = |A^\pm| e^{i\varphi^\pm}$ .

$$C^- = -\frac{1}{2\pi} \oint ds j(s) \sqrt{\beta_x(s)\beta_y(s)} e^{-i(\phi_x(s) - \phi_y(s)) + is/R\Delta}$$

$$C^+ = -\frac{1}{2\pi} \oint ds j(s) \sqrt{\beta_x(s)\beta_y(s)} e^{-i(\phi_x(s) + \phi_y(s)) + is/R\Delta}$$

# 2010: Preserving vertical emittance during beam delivery

- Coupling may be represented by two complex vectors (for the sum and difference resonances respectively)  $C^\pm = |A^\pm| e^{i\varphi^\pm}$ .
- In the ESRF storage ring, on top of the RDT **static** correction,  $C^\pm$  may be **dynamically** varied in order to catch up coupling variations induced by ID gap movements.



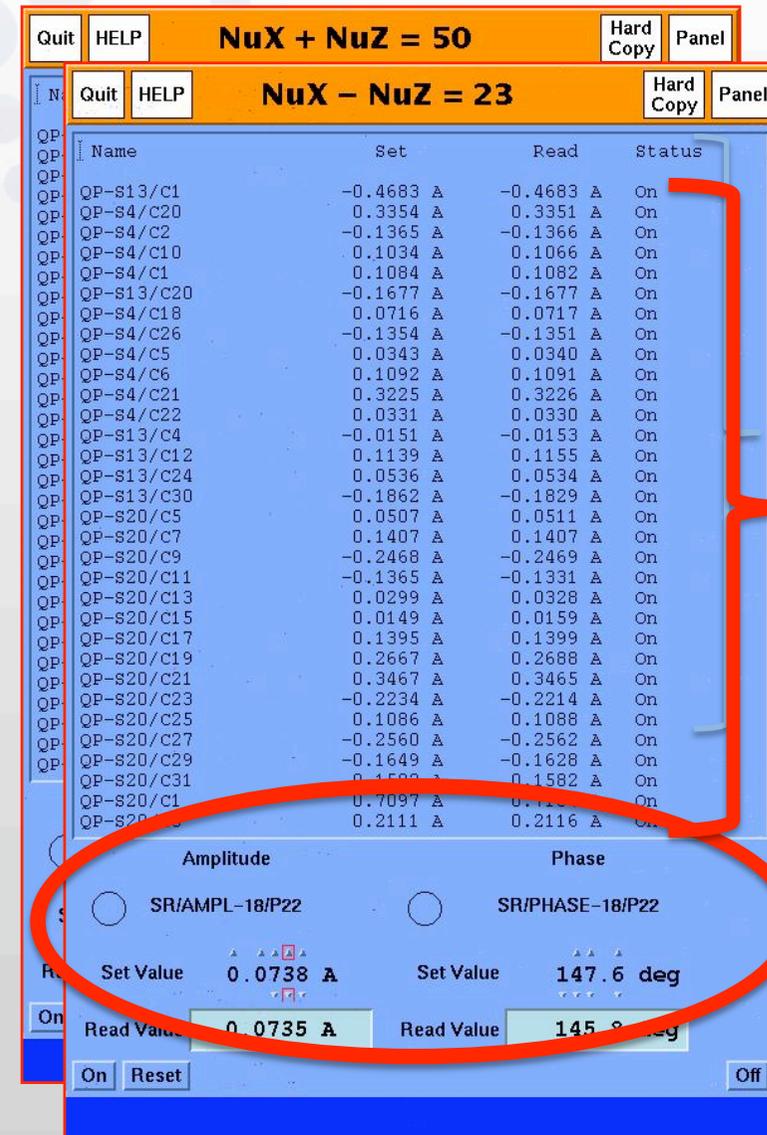
The screenshot shows a control interface for the NuX system. The top window is titled "NuX + NuZ = 50" and the bottom window is titled "NuX - NuZ = 23". Both windows have "Quit" and "HELP" buttons. The bottom window also has "Hard Copy" and "Panel" buttons. The main area is a table with columns "Name", "Set", "Read", and "Status". A red bracket on the right side of the table indicates "32 corrector skew quads". At the bottom, there are controls for "Amplitude" and "Phase" for "SR/AMPL-18/P22" and "SR/PHASE-18/P22". The "Amplitude" control shows a "Set Value" of 0.0738 A and a "Read Value" of 0.0735 A. The "Phase" control shows a "Set Value" of 147.6 deg and a "Read Value" of 145.8 deg. There are "On", "Reset", and "Off" buttons at the bottom.

Name	Set	Read	Status
QP-S13/C1	-0.4683 A	-0.4683 A	On
QP-S4/C20	0.3354 A	0.3351 A	On
QP-S4/C2	-0.1365 A	-0.1366 A	On
QP-S4/C10	0.1034 A	0.1066 A	On
QP-S4/C1	0.1084 A	0.1082 A	On
QP-S13/C20	-0.1677 A	-0.1677 A	On
QP-S4/C18	0.0716 A	0.0717 A	On
QP-S4/C26	-0.1354 A	-0.1351 A	On
QP-S4/C5	0.0343 A	0.0340 A	On
QP-S4/C6	0.1092 A	0.1091 A	On
QP-S4/C21	0.3225 A	0.3226 A	On
QP-S4/C22	0.0331 A	0.0330 A	On
QP-S13/C4	-0.0151 A	-0.0153 A	On
QP-S13/C12	0.1139 A	0.1155 A	On
QP-S13/C24	0.0536 A	0.0534 A	On
QP-S13/C30	-0.1862 A	-0.1829 A	On
QP-S20/C5	0.0507 A	0.0511 A	On
QP-S20/C7	0.1407 A	0.1407 A	On
QP-S20/C9	-0.2468 A	-0.2469 A	On
QP-S20/C11	-0.1365 A	-0.1331 A	On
QP-S20/C13	0.0299 A	0.0328 A	On
QP-S20/C15	0.0149 A	0.0159 A	On
QP-S20/C17	0.1395 A	0.1399 A	On
QP-S20/C19	0.2667 A	0.2688 A	On
QP-S20/C21	0.3467 A	0.3465 A	On
QP-S20/C23	-0.2234 A	-0.2214 A	On
QP-S20/C25	0.1086 A	0.1088 A	On
QP-S20/C27	-0.2560 A	-0.2562 A	On
QP-S20/C29	-0.1649 A	-0.1628 A	On
QP-S20/C31	0.1582 A	0.1582 A	On
QP-S20/C1	0.7097 A	0.7111 A	On
QP-S20/C3	0.2111 A	0.2116 A	On

32 corrector skew quads

# 2010: Preserving vertical emittance during beam delivery

- Coupling may be represented by two complex vectors (for the sum and difference resonances respectively)  $C^\pm = |A^\pm| e^{i\varphi^\pm}$ .
- In the ESRF storage ring, on top of the RDT **static** correction,  $C^\pm$  may be **dynamically** varied in order to catch up coupling variations induced by ID gap movements.
- A new software **automatically** minimizes  $C^\pm$  by looking at the average vertical emittance

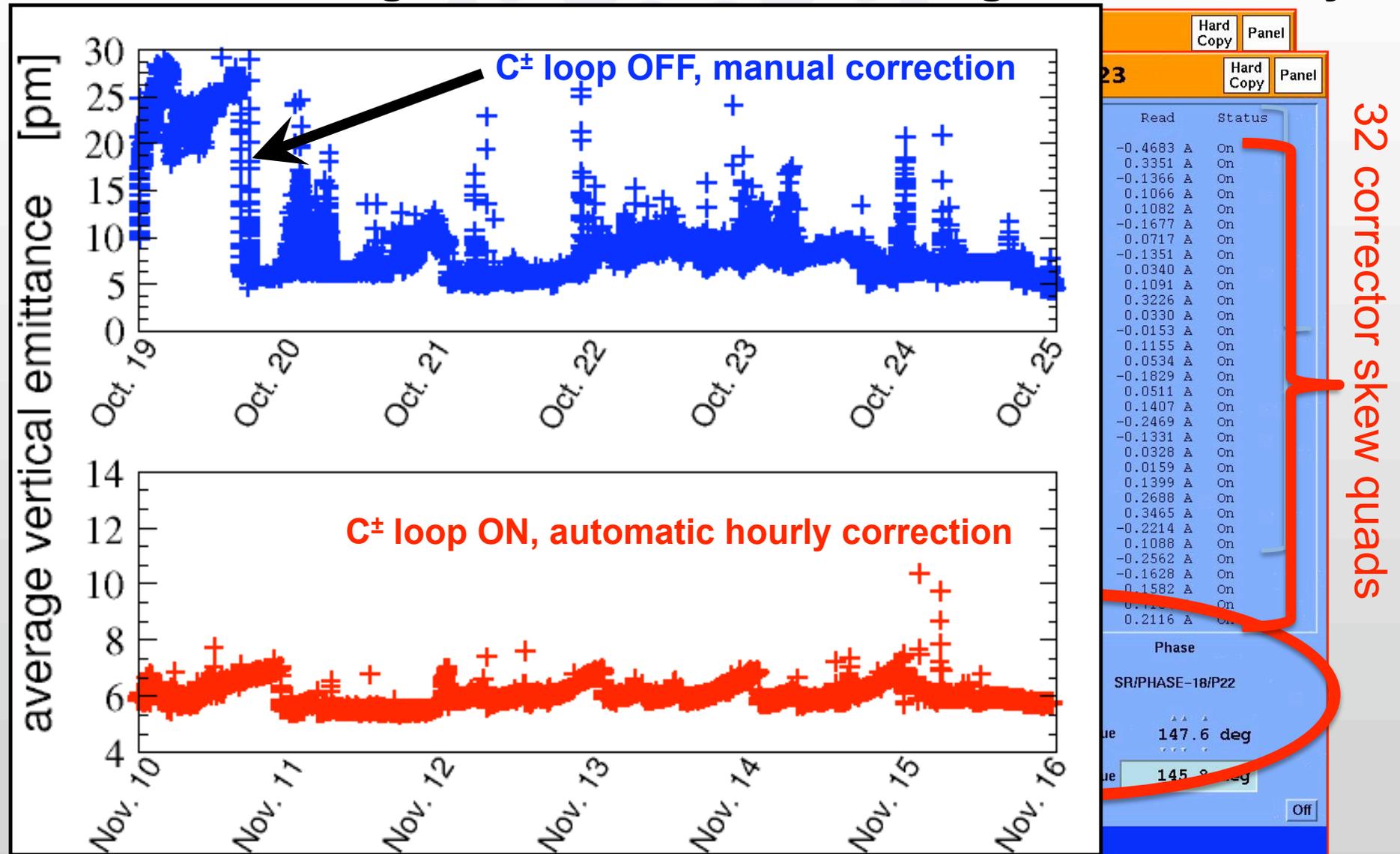


The screenshot shows a control interface for the NuX + NuZ = 50 system. It features a table of corrector skew quads with columns for Name, Set, Read, and Status. A red bracket on the right side of the table indicates that the 32 rows listed are '32 corrector skew quads'. Below the table, there are controls for Amplitude and Phase, with a red oval highlighting the Set Value fields (0.0738 A and 147.6 deg) and Read Value fields (0.0735 A and 145.8 deg).

Name	Set	Read	Status
QP-S13/C1	-0.4683 A	-0.4683 A	On
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QP-S13/C30	-0.1862 A	-0.1829 A	On
QP-S20/C5	0.0507 A	0.0511 A	On
QP-S20/C7	0.1407 A	0.1407 A	On
QP-S20/C9	-0.2468 A	-0.2469 A	On
QP-S20/C11	-0.1365 A	-0.1331 A	On
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QP-S20/C29	-0.1649 A	-0.1628 A	On
QP-S20/C31	0.1582 A	0.1582 A	On
QP-S20/C1	0.7097 A	0.7111 A	On
QP-S20/C3	0.2111 A	0.2116 A	On

32 corrector skew quads

# 2010: Preserving vertical emittance during beam delivery

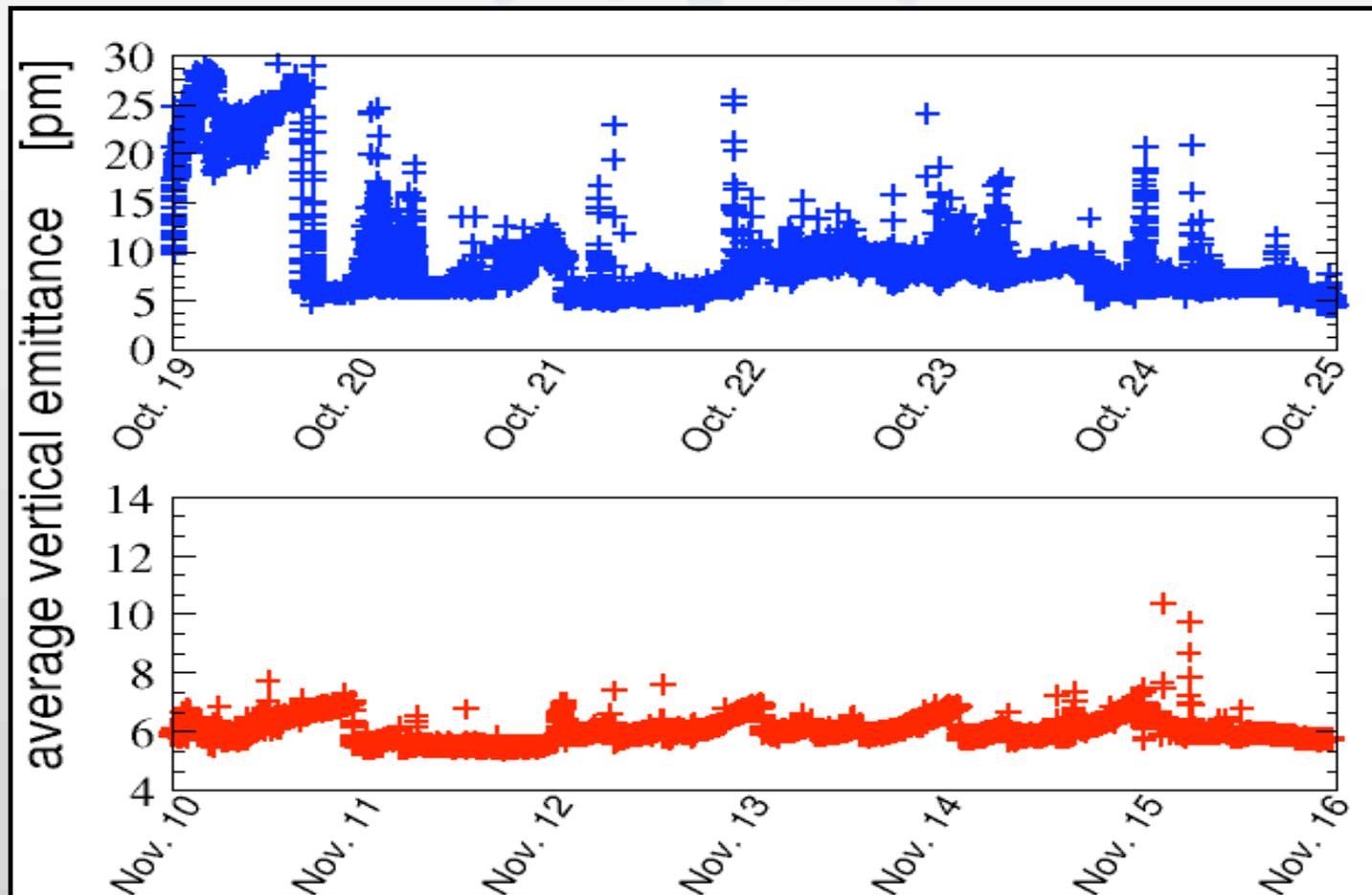


## Outlines

- Vertical emittances in the presence of coupling
- Coupling correction via Resonance Driving Terms
- Experience in the ESRF storage ring (2010)
- **Experience in the ESRF storage ring (2011)**
- Benefits and drawbacks; operational considerations

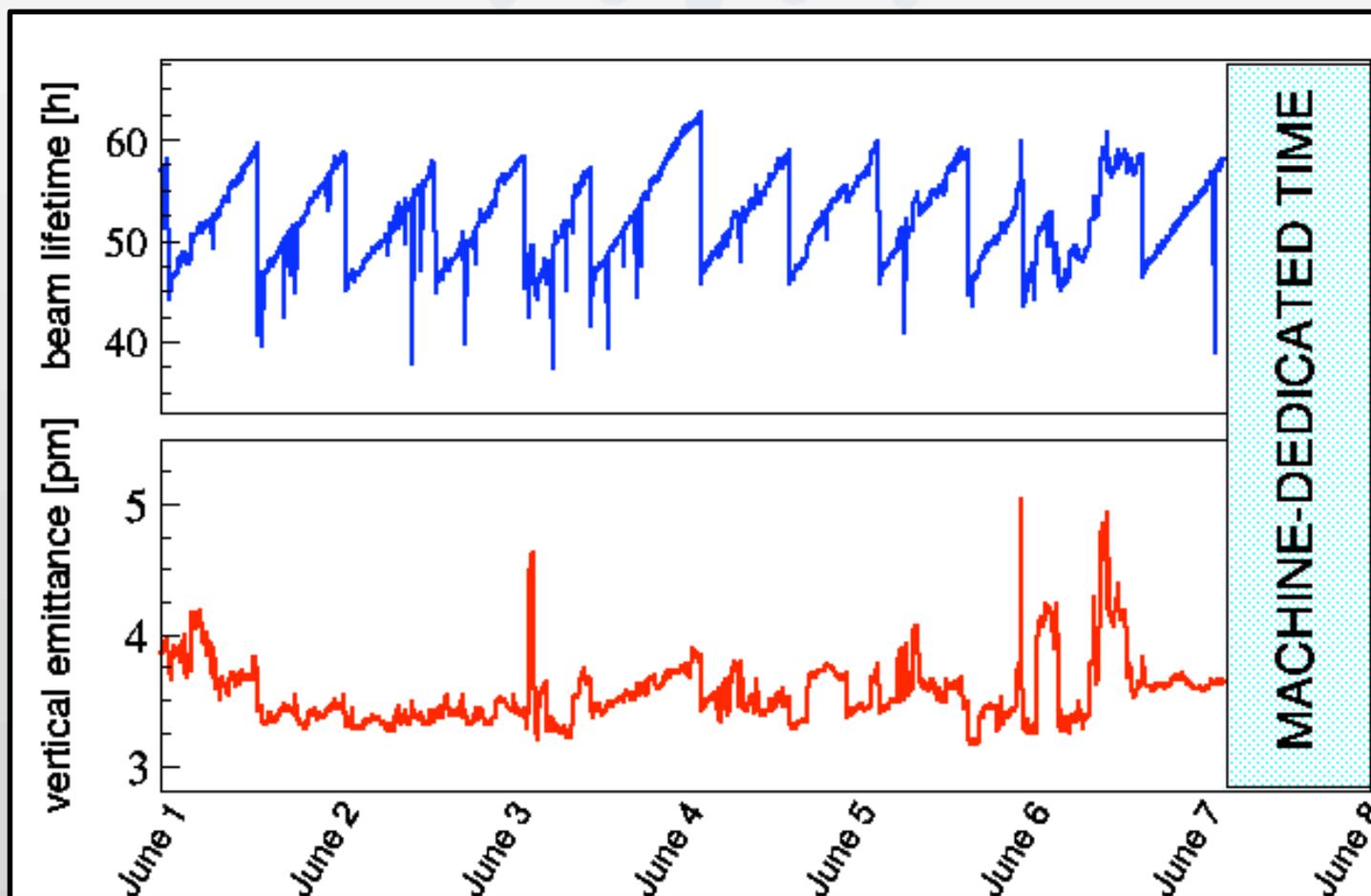
# 2011: Towards ultra-small vertical emittance

2010, with 32 skew quad correctors



# 2011: Towards ultra-small vertical emittance

2011, with 64 skew quad correctors

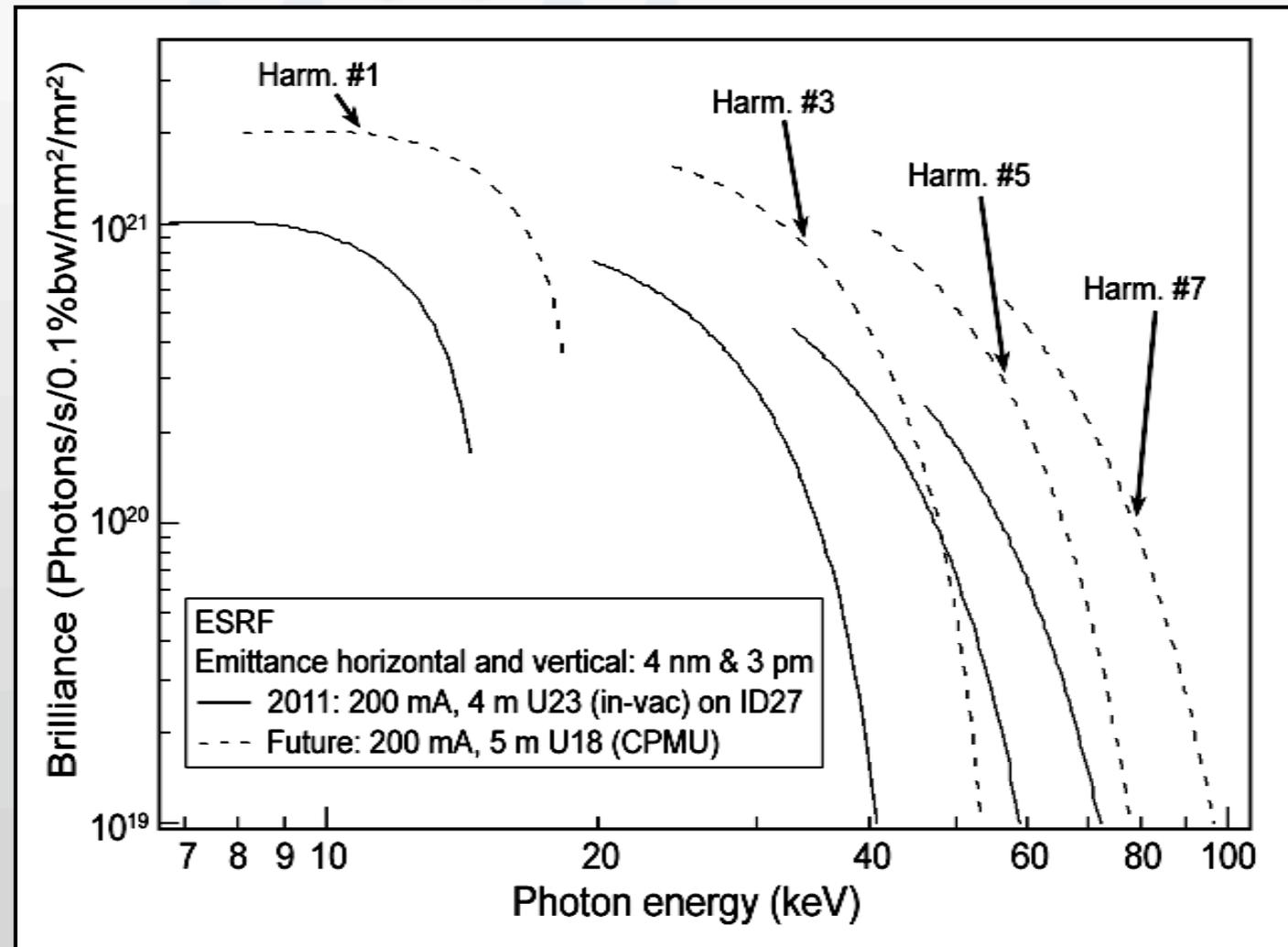


## Outlines

- Vertical emittances in the presence of coupling
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- Experience in the ESRF storage ring (2010)
- Experience in the ESRF storage ring (2011)
- **Benefits and drawbacks; operational considerations**

## Benefit: Brilliance @ $\epsilon_y = 3 \text{ pm}$ @200 mA

Solid curve:  
Brilliance of the X-ray beam emitted from the two in-vacuum undulators installed on ID27 (High Pressure beamline). Each undulator segment has a period of 23 mm, a length of 2 m and is operated with a minimum gap of 6 mm.



## Benefit: Injection Efficiency

- Injection tuning after shutdown (steering in the transfer line, septa optimization) observed to be more effective if performed after coupling correction in the storage ring

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Filling mode	inj. eff. until 2009 operation	inj. eff. as of 2010 operation	inj. eff. as of 2010 open IDs & scrapers
16 bunches (92mA)	30-50%	50-70% (*)	~100% (*)
7/8 +1 (200mA)	50-70%	70-90% (^)	~100% (^)

(\*) with new optics

(^) with lower chromaticity

## Drawback: reduced lifetime (7/8 +1 filling mode, @ 200 mA)

- LT in 2009 (@  $\varepsilon_y = 30$  pm) : 55-60 h

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- Discussion among users following the LT reduction (brilliance Vs intensity and stability). Two scenarios:
  - ✓ alternate weeks of beam delivery with low and large emittance
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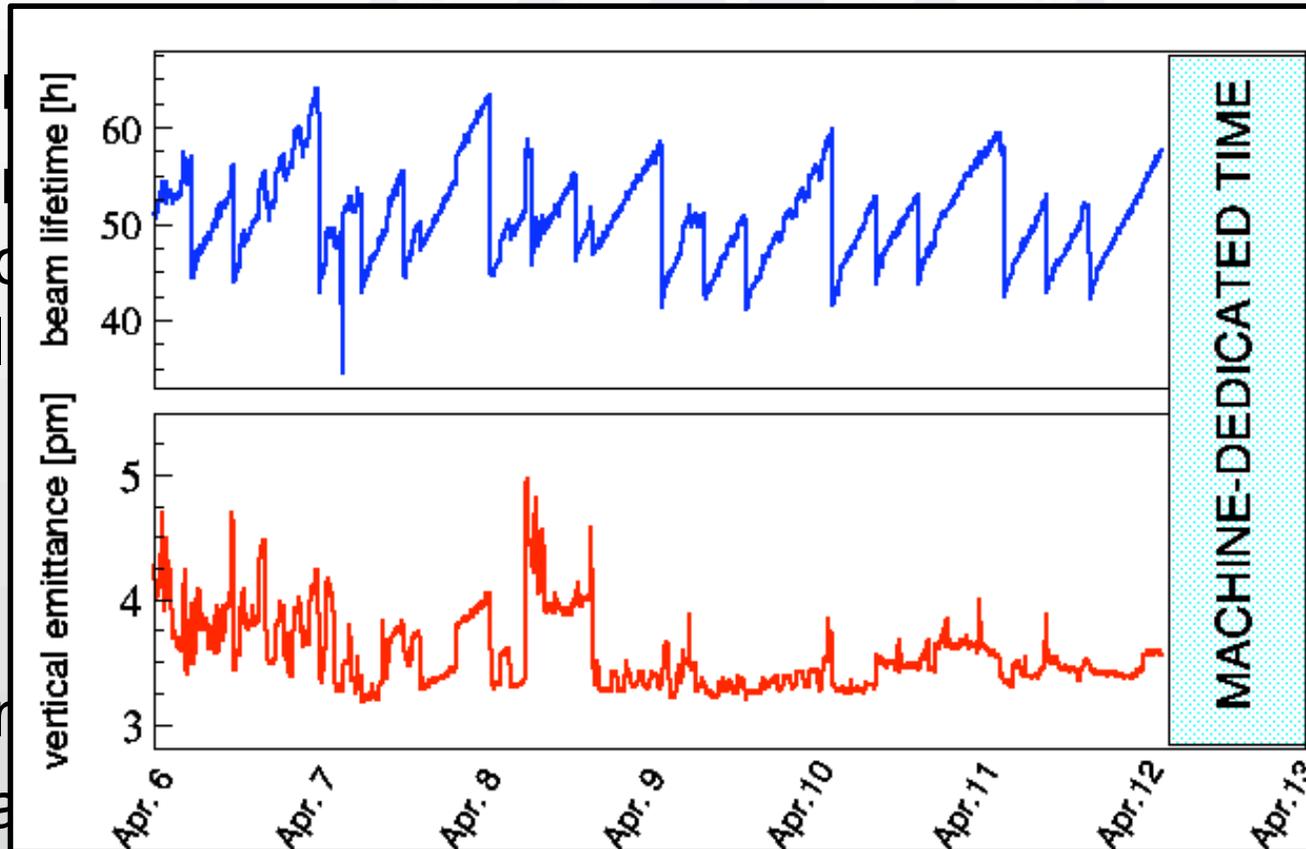
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- LT mid 2011(@  $\epsilon_y = 3-4$  pm): 45 h after new sextupolar resonance correction. Back to the two symmetric daily refills (9am, 9pm)

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- LT i
- LT i
- Disc
- (bril
- ✓
- ✓
- Mid
- two
- (9pm
- LT a



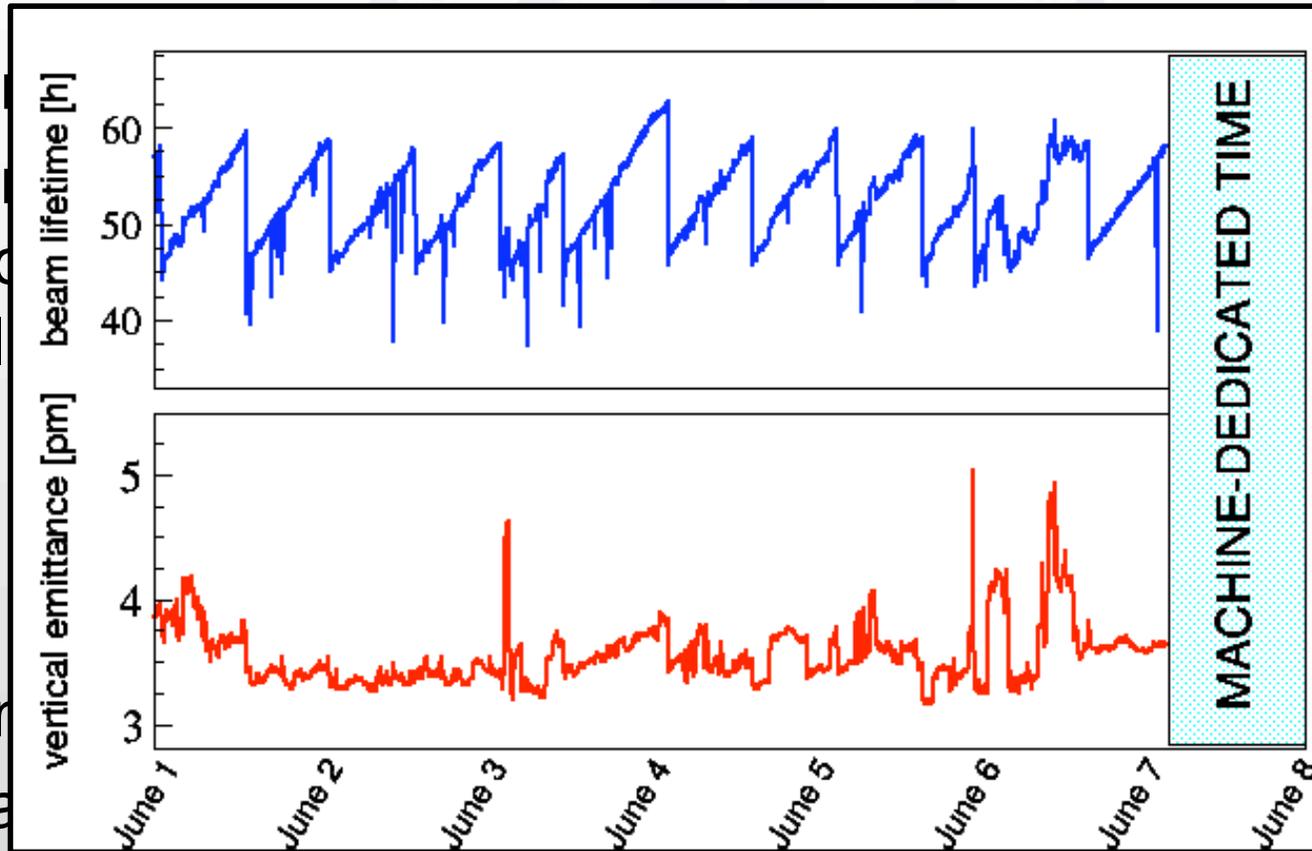
on  
DS:  
mittance  
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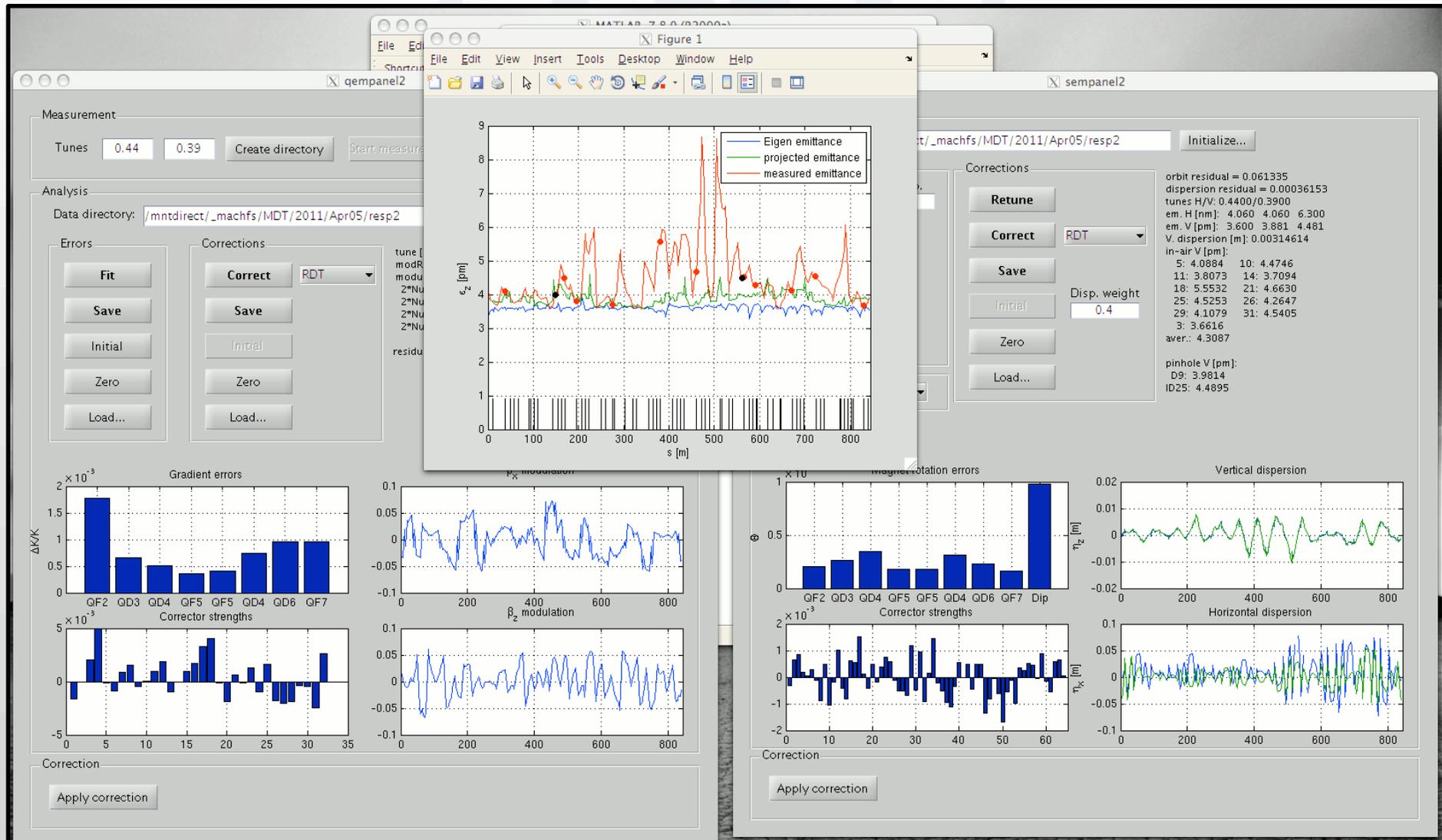


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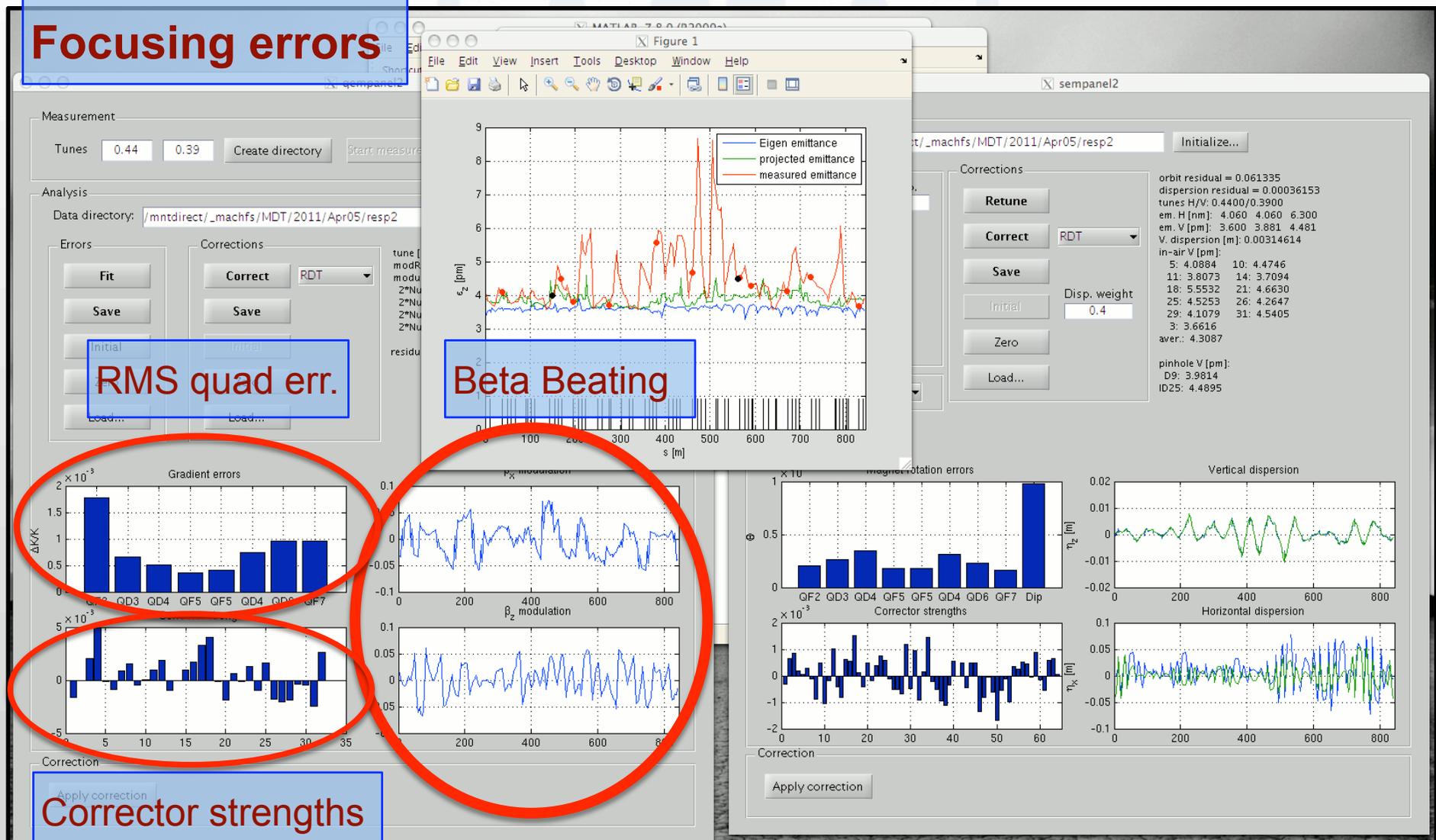
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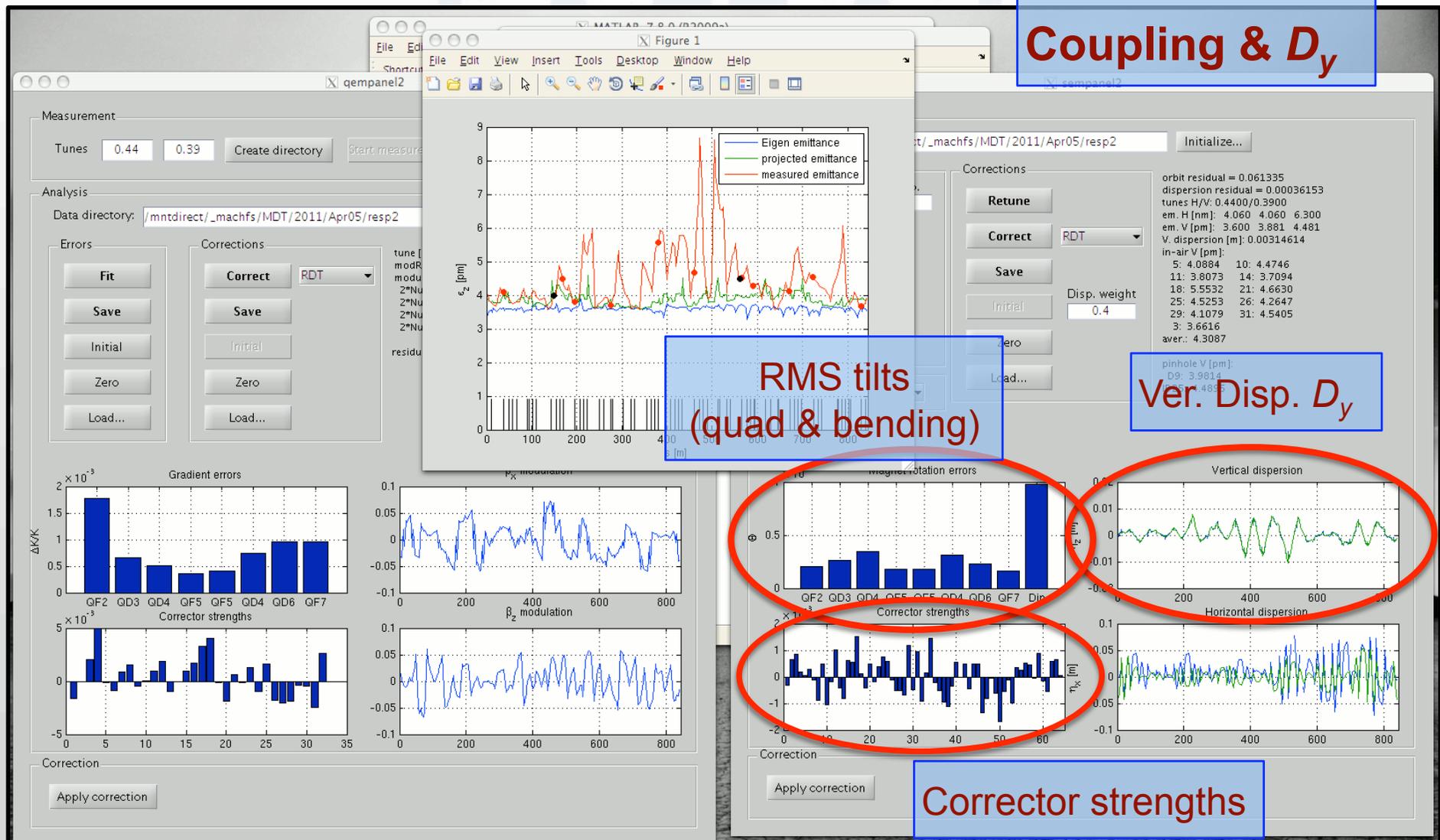
# Operational considerations: the ORM+correction software



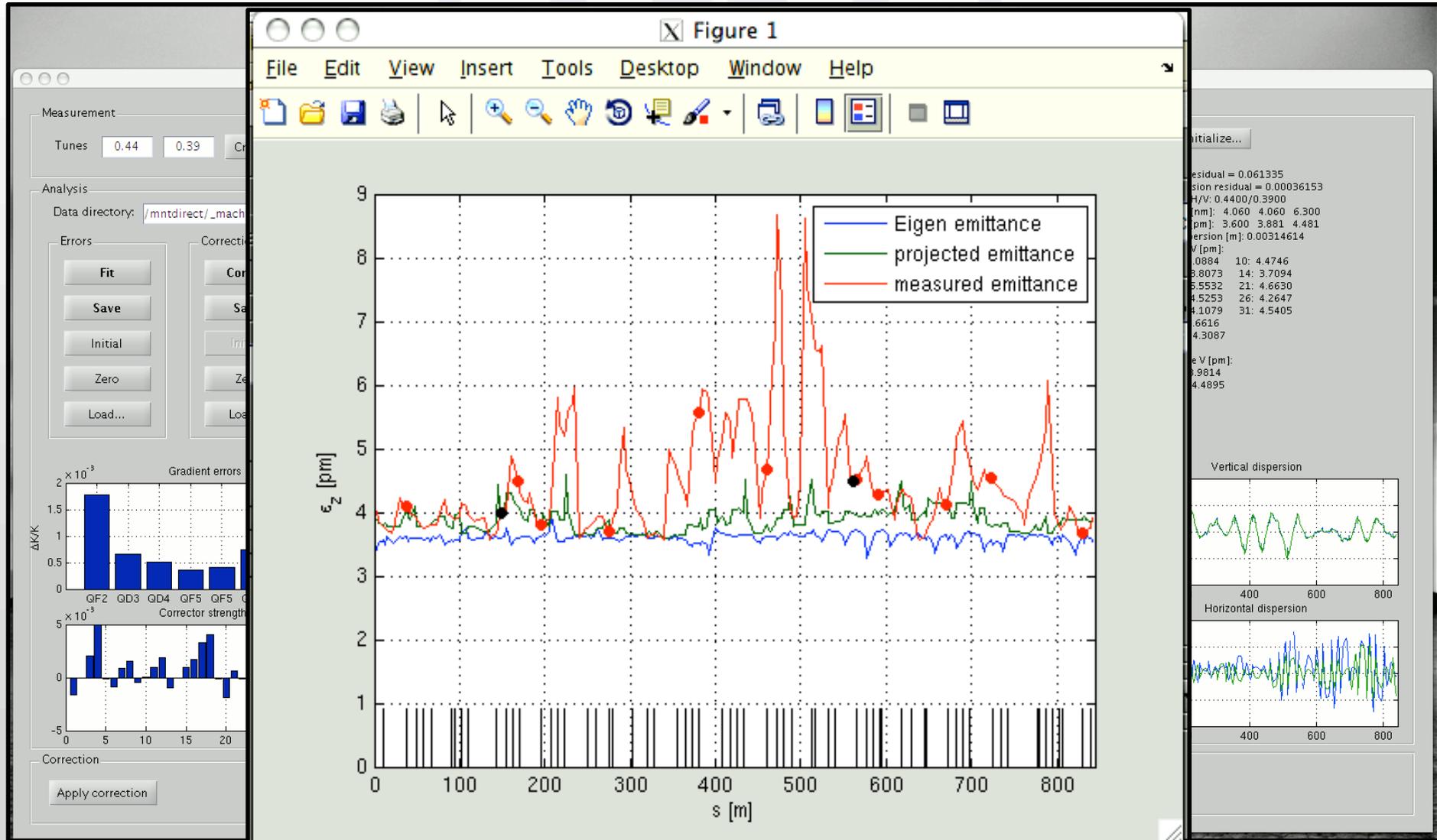
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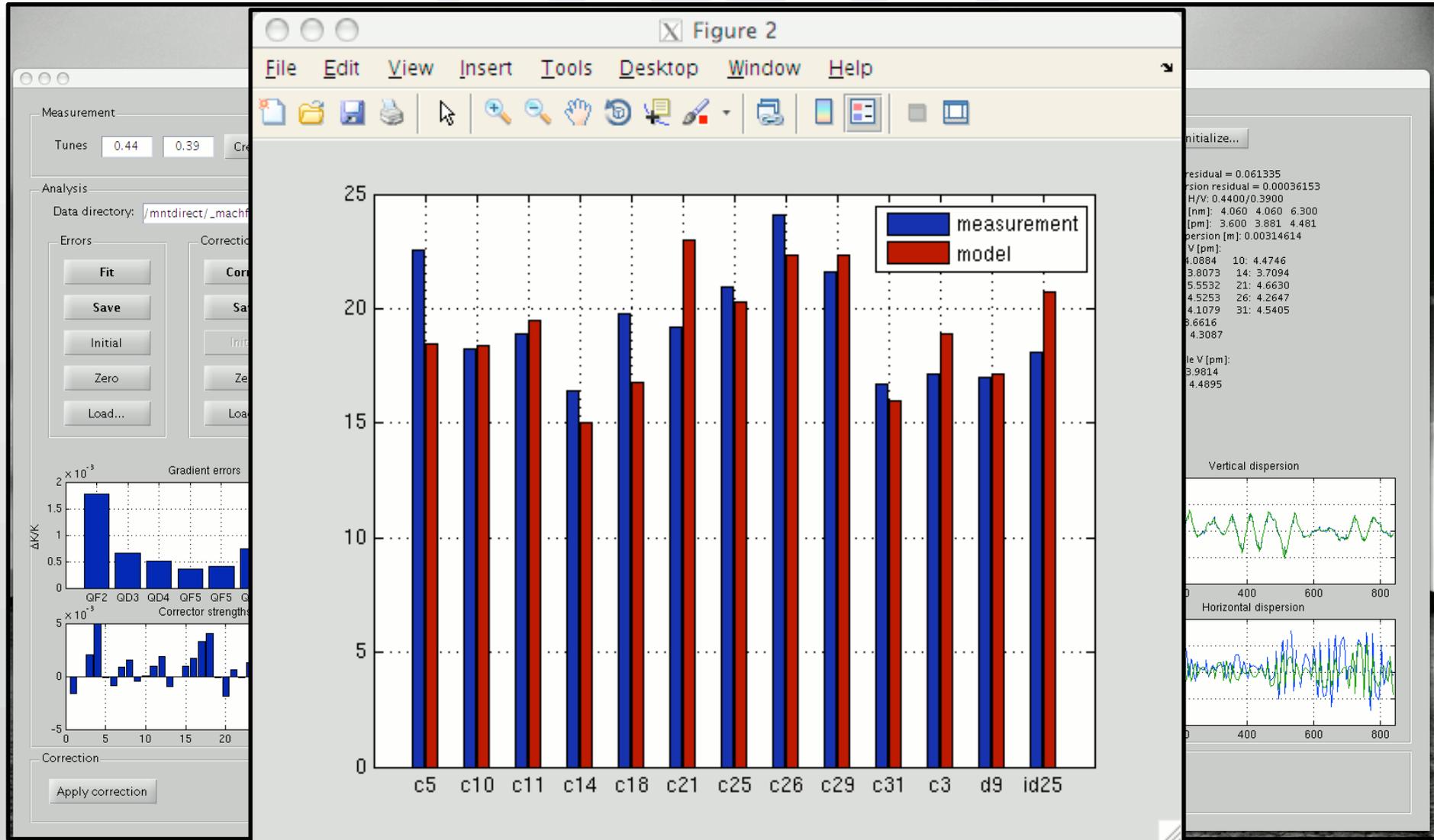
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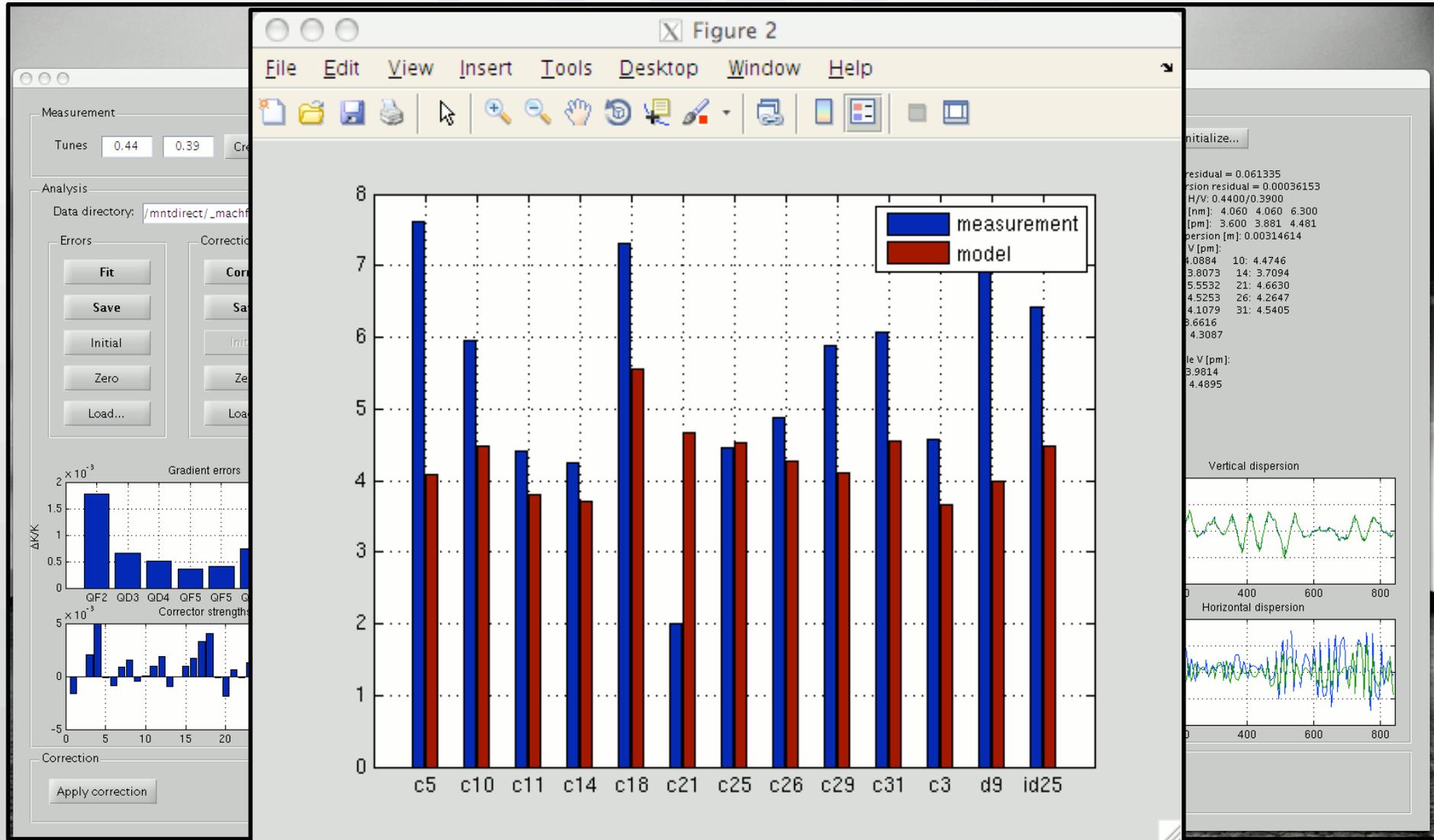
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- Coupling feed-forward runs continuously during beam delivery, under ID (and not OP) control system
- Coupling feedback acts hourly, but only if  $\bar{\varepsilon}_y > 5$  pm (adjustable)
- Looking into the future: under study the possibility of using the new AC orbit correction system to perform fast ORM measurements on all steerers in parallel (at different frequencies, ORM retrieved from harmonic analysis)

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## Conclusion

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- Two procedures to preserve small vertical emittance during beam delivery were successfully tested: as of spring 2011 stable  $\varepsilon_y = 3.2$ -4.5 pm delivered to users (lifetime of 45 hours after refilling @ 200 mA, 10 hours less than in the past only).