First results with two light flavours of maximally twisted mass quarks

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Outline

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Twisted Mass fermions

the twisted mass Dirac operator:

$$D_{\mathrm{tm}} = D_{\mathrm{W}} + m_0 + i\mu\gamma_5\tau_3$$
 .

[Frezzotti, Grassi, Sint, Weisz, 1999]

- Wilson Dirac operator D_W with bare mass m_0 .
- twisted mass parameter μ .
- τ_3 third Pauli matrix acting in flavour space
- D_{tm} is protected against unphysically small eigenvalues

Automatic $\mathcal{O}(a)$ improvement

If m_0 is tuned to its critical value $m_{\rm crit}$ (maximal twist) then ...

• observables are automatically $\mathcal{O}(a)$ improved.

[Frezzotti, Rossi, 2003]

Shown to work in practice for various observables in the quenched approximation [Jansen et al., 2004, 2005; Abdel-Rehim et al., 2004, 2005]

- Simplifies mixing during renormalisation
- Only one parameter (m_0) must be tuned

but...

parity and flavour symmetry explicitly broken

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Twisted Mass Fermions

Idea of the Proof

$$\langle O(x) \rangle^{\text{lat}} = \langle O(x) \rangle^{\text{c}} - a \int dy \langle O(x) \mathcal{L}_1(y) \rangle^{\text{c}} + a \sum_k \langle O_k(x) \rangle^{\text{c}} + \mathcal{O}(a^2)$$

- r.h.s.: all expt. values with cont. action: must obey symmetries of cont. action
- all operators in expansion must share lattice symmetries of O
- example: cont. symmetry modified Parity

$$ilde{\mathcal{P}}: \qquad egin{cases} \psi(ec{x},t) & o \ \gamma_0 \exp(i\omega\gamma_5 au_3)\psi(-ec{x},t) \ ar{\psi}(ec{x},t) & o \ ar{\psi}(-ec{x},t)\exp(i\omega\gamma_5 au_3)\gamma_0 \ eta \end{cases}$$

 O must be even under *P*, clover term is odd: term cancels in the expansion

Quenched Experiments Understanding the Phasestructur Algorithmic Improvements

A choice? Tuning to full twist

▷ O(a) ambiguity in m_{crit} does not harm automatic O(a) improvement

Several definitions available:

- 1. $m_{\rm crit}$ where $m_{\rm PS} = 0$ at $\mu = 0$ (Pion def.)
- 2. m_{crit} where $m_{\text{PCAC}} = 0$ at $\mu = 0$ (PCAC def.)
- 3. m_{crit} where $m_{\text{PCAC}} = 0$ for each value of $a\mu$ seperatly 4. ...
- Theoretical discussion in [Frezzotti, Martinelli, Papinutto, Rossi; Sharpe; Aoki, Bär]: do not use 1.

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Quenched Experiments Understanding the Phasestructur Algorithmic Improvements

Quenched Continuum Scaling of f_{PS}



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Generic Phasestructur of Wilson Fermions



This is generic for Wilson type fermions!

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Chosing the Gauge Action



tlSym is a theoretically sound compromise

Quenched Experiments Understanding the Phasestructur Algorithmic Improvements

Speeding up the HMC

Resurrection of Wilson fermions due to algorithmic improvements



Setup First Results Scaling

Setup

- We are using the tree-level Symanzik improved gauge action [Weisz, 1983]
- N_f = 2 mass-degenrate flavours of maximally twisted mass quarks
- Algorithm: HMC with multiple time scales and mass preconditioning [Urbach et al., 2005]
- Plan:
 - ► 3 lattice spacings: 0.075 0.125 fm
 - pseudo scalar masses in the range 250 550 MeV
 - volumes \geq 2 fm
- m_0 tuned to m_{crit} at the lowest mass at each lattice spacing

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Setup

eta	$L^3 imes T$	a [fm]	<i>m</i> _{PS} [MeV]	<i>N</i> _{therm}	N _{traj}
3.9	$24^3 imes 24$	pprox 0.095	pprox 280	1500	5000
			pprox 350	1500	5000
			pprox 430	1500	5000
			pprox 510	1500	5000
4.05	$32^3 imes 64$	pprox 0.075	pprox 280	1500	1200
			pprox 350	1500	500

$\beta = 4.05$ very preliminary!

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Tuning to full twist

- ► m_{PCAC} = 0 at lowest aµ
- *m*_{PCAC} = 0 dependence visible
- no news: known from quenched



Setup First Results Scaling

Some simple observables

- First observables to look at: m_{PS} and f_{PS}
- f_{PS} at maximal twist can be obtained from

$$f_{
m PS}=rac{2\mu}{m_{
m PS}^2}|\langle 0|m{P}^1(0)|\pi
angle|$$

- Note that at maximal twist f_{PS} does not need to be renormalised
- We estimate finite size (FS) effects with NLO ChPT formula from Gasser and Leutwyler [Gasser, Leutwyler, 1987]
- Checked against resummed Lüscher formula

[Lüscher, 1986; Colangelo, Dürr, Haefeli, 2005]

► We use spin diluted random time slice sources, fuzzing [Michael] and variational methods [Michael, 1985 ;Lüscher, Wolff, 1990] Introduction Preparing the Ground Results Setup First Results Scaling

am_{PS} versus $a\mu$ at $\beta = 3.9$



$f_{\rm PS}$ at $\beta = 3.9$



$f_{\rm PS}$ at $\beta = 3.9$





 $f_{\rm PS}$ at $\beta = 3.9$

- Fits to the data with ChPT formulae in progress
- when the data is extrapolated linearly to the physical point we obtain:

 $f_{\pi} = 126.3 \pm 0.8 \pm 0.7 \text{ MeV}$

- ► First error comes from m_{PS}, f_{PS} and extrapolation, the second from r₀/a
- $r_0 = 0.5 \text{ fm}$ was used
- In our normalisation $f_{\rm PS} = 131 \, {\rm MeV}$

Setup First Results Scaling

Effects of Isospin breaking

Flavour symmetry explicitly broken by twisted mass term at finite *a*

- ► Expected to be largest in m[±]_{PS} - m⁰_{PS}
- ► $\beta = 3.9, a\mu = 0.004, am_{PS} = 0.1358(5):$ $m_{PS}^{\pm} - m_{PS}^{0} = 0.03(1)$
- A factor of 2 smaller than quenched
- Splitting in the vector mass compatible with 0



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Setting the scale

- ► Using the Sommer scale *r*₀
- ▶ Value of *r*⁰ not very well known
- ► Scale setting with f.i. f_K, m_{K*} etc. in progress
- Here I use $r_0 = 0.5$ fm
- μ dependence seems to be weak

$\beta = 3.9$



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Introduction eparing the Ground Results

Setup First Results Scaling

$\langle x \rangle$ for the Pion



Lowest moment of Non-Singlet Pion Parton Distribution Function $\langle x \rangle$

Results

First Results

Exploring p-decay [McNeile, Michael, 2003]

• ρ does not (yet) decay at $\beta = 3.9$: $a\Delta m \approx 0.15$ at $a\mu = 0.004$

uncharged vector meson at rest:

$$R(t) = \frac{\rho_0(0) \to \pi_+\pi_-(t)}{\sqrt{(\rho_0(0) \to \rho_0(0))(\pi_+\pi_-(0) \to \pi_+\pi_-(t))}}$$



• Assuming $m_{\rho} \approx m_{\pi\pi}$, $\mathbf{x} = \langle \rho | \pi \pi \rangle$:

$$R \propto \sum_{t=0}^{T} \mathbf{x} \mathbf{e}^{-m_{
ho}t} \mathbf{e}^{-m_{\pi\pi}(T-t)} = \mathbf{e}^{-mT} \cdot \mathbf{x} \cdot t$$

for $xt \ll 1$

Setup First Results Scaling

Exploring ρ -decay

• We extract $\bar{g} = 1.2(2)$, with

 $ar{g}=\Gamma m_
ho E_{\pi\pi}/k^3$

- experimental number: $\bar{g} = 1.39$
- Already well compatible
- Larger lattices needed for a decaying ρ.



Introduction eparing the Ground Results

Setup First Results Scaling

Preliminary continuum scaling

► r₀/a value at the lowest µ value

 masses not yet exactly matched



Conclusion

- mtmQCD stands on a sound basis
- First encouraging results with N_f = 2 flavours of maximally twisted mass quarks
- ▶ We can reach values for *m*_{PS} as low as 280 MeV
- Flavour symmetry breaking effects are visible, but significantly smaller than quenched
- Lattice artifacts in f_{PS} seem to be small
- First physics applications in progress
- $N_f = 2 + 1 + 1$ in progress: talk of Enno