



Simon Capstick, Florida State University

N* analysis white paper mtg. 11/4/06-1

Overview of N^* Physics

- Why study excited states of the nucleon?
- What do we know about N^* states?
- What are the goals of the N^* program?
- What developments are required to reach these goals?
 - Experimental and theoretical



Why study N^* states?

- What are their relevance to nuclear and strong-interaction physics?
 - The nucleus is a composite system
 - How much would we know about nuclei if we only studied their ground states?
 - The nucleon is a composite system
 - A full understanding of the nucleon requires knowledge of the spectrum and properties of its excited states



Why study N^* states?

- What are their relevance to nuclear and strong-interaction physics?
 - The nucleon is a confined system
 - Confinement is poorly understood
 - Highly-excited states are sensitive to details of how quarks are confined
 - Is the confining interaction screened by quark pair creation?
 - Do such states decay strongly by string breaking?
 - Can we see evidence of excitation of the glue?



Why study N^* states?

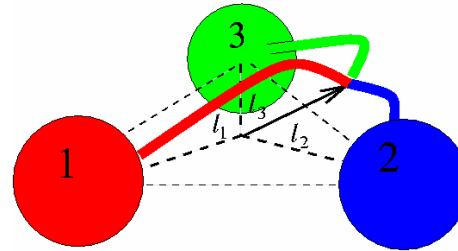
- What is the nature of the important effective degrees of freedom in low-energy QCD?
 - High-energy and Q^2 (hard) scattering probes QCD at short-distance
 - With care can apply perturbative QCD
 - QCD becomes complex and interesting in the soft (non-perturbative) regime
 - Can we identify effective degrees of freedom and their interactions?
 - Can we see the soft to hard transition?
- The spectrum and properties of N^* states are sensitive to their nature



Effective degrees of freedom

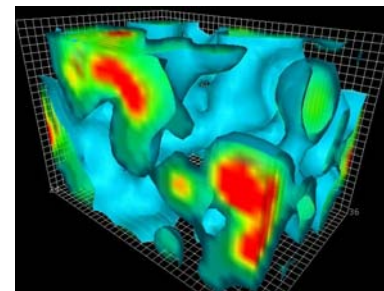
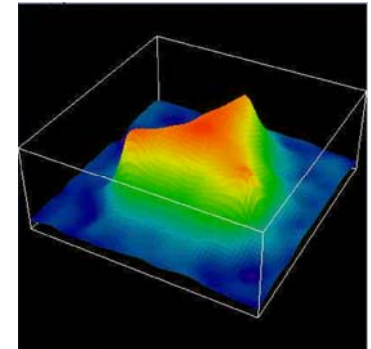
Low-energy QCD:

- Constituent quarks (CQs), confined by flux tubes?
- Confined CQs, elementary meson fields?
- Confined CQs, gas of instantons?
- Baryons and mesons interacting via chiral potentials?



P. Page, S.C. Flux-tube model of baryons & hybrids

Ichie, Bornyakov, Struer & Schierholz
QQQ action density



D. Leinweber et al.
QCD vacuum action density



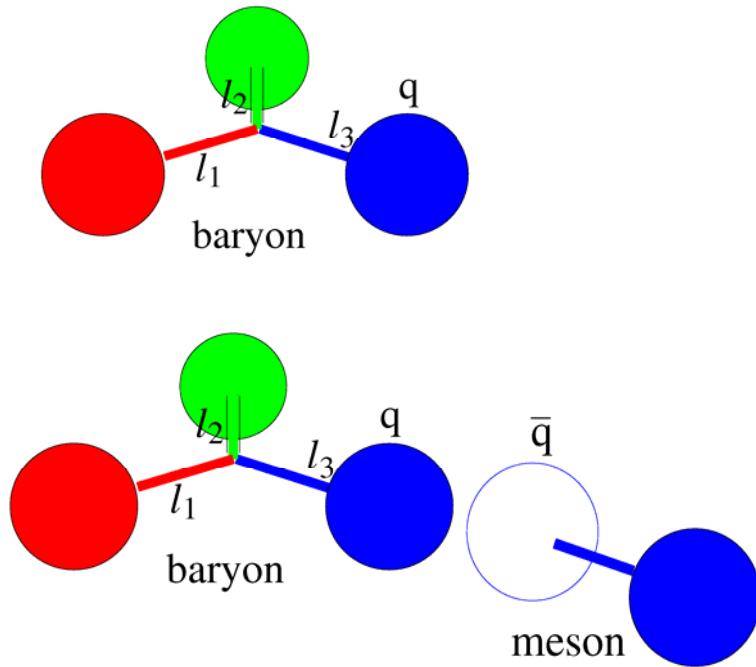
Why study N^* states?

- The N^* s (hadrons) are unique: bound states of strongly-interacting, relativistic confined constituents
- Nucleons interact strongly in nuclei, but:
 - Can isolate relevant low-energy d.f. (nucleons)
 - Can directly probe two-body potential in experiment
 - Few body bound states of most A exist to test model N - N , N - N - N ,... potentials
 - Can systematically expand around non-relativistic limit
 - Heavy effective degrees of freedom
 - Relatively large states



Uniqueness...

- Elementary d.f. are confined
 - Can only indirectly infer low-energy interaction
- Only qqq , $q\bar{q}$ exist as bound states
- Not non-relativistic systems (unless all quarks heavy)



N and Δ excited states

- PDG lists many excited N and Δ states discovered in π N elastic scattering

- Notation is $L_{2I,2J}$

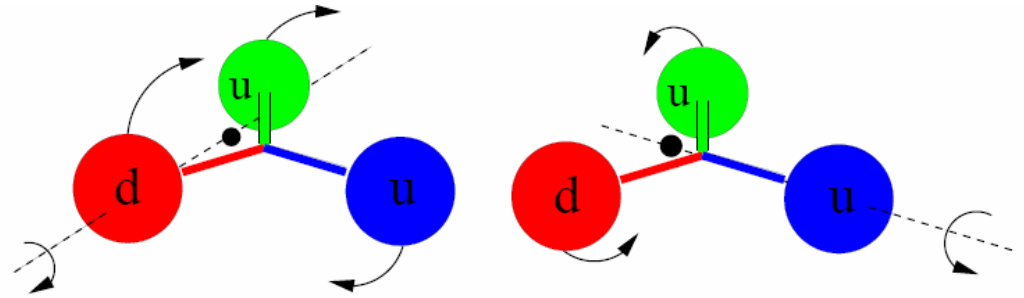
- L is (π, N) relative angular momentum
- I = total isospin (N=1/2, $\Delta=3/2$), J is total spin

<i>p</i>	P_{11}	****	$\Delta(1232)$	P_{33}	****
<i>n</i>	P_{11}	****	$\Delta(1600)$	P_{33}	***
<i>N</i> (1440)	P_{11}	****	$\Delta(1620)$	S_{31}	****
<i>N</i> (1520)	D_{13}	****	$\Delta(1700)$	D_{33}	****
<i>N</i> (1535)	S_{11}	****	$\Delta(1750)$	P_{31}	*
<i>N</i> (1650)	S_{11}	****	$\Delta(1900)$	S_{31}	**
<i>N</i> (1675)	D_{15}	****	$\Delta(1905)$	F_{35}	****
<i>N</i> (1680)	F_{15}	****	$\Delta(1910)$	P_{31}	****
<i>N</i> (1700)	D_{13}	***	$\Delta(1920)$	P_{33}	***
<i>N</i> (1710)	P_{11}	***	$\Delta(1930)$	D_{35}	***
<i>N</i> (1720)	P_{13}	****	$\Delta(1940)$	D_{33}	*
<i>N</i> (1900)	P_{13}	**	$\Delta(1950)$	F_{37}	****
<i>N</i> (1990)	F_{17}	**	$\Delta(2000)$	F_{35}	**
<i>N</i> (2000)	F_{15}	**	$\Delta(2150)$	S_{31}	*
<i>N</i> (2080)	D_{13}	**	$\Delta(2200)$	G_{37}	*
<i>N</i> (2090)	S_{11}	*	$\Delta(2300)$	H_{39}	**
<i>N</i> (2100)	P_{11}	*	$\Delta(2350)$	D_{35}	*
<i>N</i> (2190)	G_{17}	****	$\Delta(2390)$	F_{37}	*
<i>N</i> (2200)	D_{15}	**	$\Delta(2400)$	G_{39}	**
<i>N</i> (2220)	H_{19}	****	$\Delta(2420)$	$H_{3,11}$	****
<i>N</i> (2250)	G_{19}	****	$\Delta(2750)$	$I_{3,13}$	**
<i>N</i> (2600)	$I_{1,11}$	***	$\Delta(2950)$	$K_{3,15}$	**
<i>N</i> (2700)	$K_{1,13}$	**			

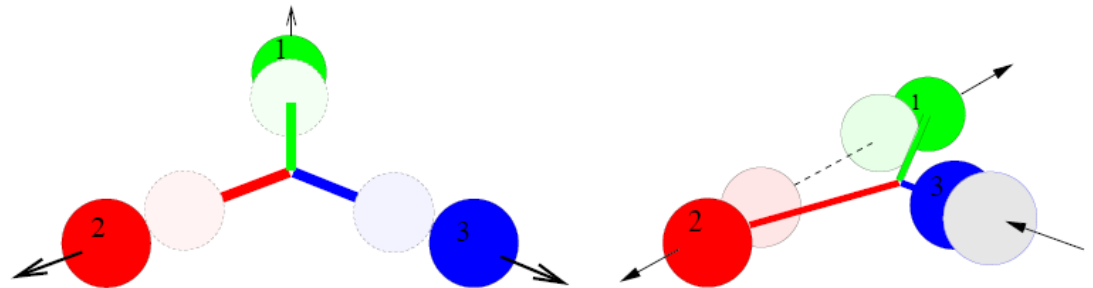


N and Δ excited states...

- Orbital excitations (two distinct kinds)



- Radial excitations (also two kinds)



“Missing” resonances

- If we were able to classify resonances into $SU(6)_{f_s} \otimes O(3)$ multiplets
 - Complicated by strong configuration mixing
- Good evidence for all negative parity N^* (Δ^*) resonances in lowest ($N=1$) band $[SU(6)_{f_s}, L^P] = [70, 1^-]$
 - Also $\Delta(1930)D_{35}$ & $\Delta(1950)F_{37}$ in $N=3$ band



“Missing” resonances

- Don't have enough states to fill out the positive-parity ($N=2$) multiplets
 - Not enough information to rule out a quark-diquark picture
 - Not enough information to establish or refute parity doubling higher in the spectrum

Isgur & Karl
Koniuk and Isgur

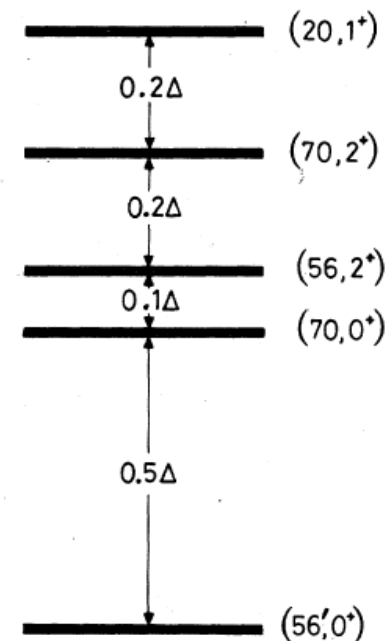


FIG. 1. The zeroth-order pattern of $N=2$ supermultiplets.



What do we really know?

Table 1. The status of the N and Δ resonances. Only those with an overall status of *** or **** are included in the main Baryon Summary Table.

Particle	$L_{2I,2J}$	Overall status	Status as seen in —						
			$N\pi$	$N\eta$	ΛK	ΣK	$\Delta\pi$	$N\rho$	$N\gamma$
$N(939)$	P_{11}	****							
$N(1440)$	P_{11}	****	****	*			***	*	***
$N(1520)$	D_{13}	****	****	*			****	****	****
$N(1535)$	S_{11}	****	****	****			*	**	***
$N(1650)$	S_{11}	****	****	*	***	**	***	**	***
$N(1675)$	D_{15}	****	****	*	*		****	*	****
$N(1680)$	F_{15}	****	****				****	****	****
$N(1700)$	D_{13}	***	***	*	**	*	**	*	**
$N(1710)$	P_{11}	***	***	**	**	*	**	*	***
$N(1720)$	P_{13}	****	****	*	**	*	*	**	**
$N(1900)$	P_{13}	**	**					*	
$N(1990)$	F_{17}	**	**	*	*	*			*
$N(2000)$	F_{15}	**	**	*	*	*	*	**	
$N(2080)$	D_{13}	**	**	*	*				*
$N(2090)$	S_{11}	*	*						
$N(2100)$	P_{11}	*	*	*					
$N(2190)$	G_{17}	****	****	*	*	*		*	*
$N(2200)$	D_{15}	**	**	*	*				
$N(2220)$	H_{19}	****	****	*					
$N(2250)$	G_{19}	****	****	*					
$N(2600)$	I_{111}	***	***						
$N(2700)$	K_{113}	**	**						

Particle	$L_{2I,2J}$	Overall status	Status as seen in —						
			$N\pi$	$N\eta$	ΛK	ΣK	$\Delta\pi$	$N\rho$	$N\gamma$
$\Delta(1232)$	P_{33}	****	****	F					****
$\Delta(1600)$	P_{33}	***	***	o			***	*	**
$\Delta(1620)$	S_{31}	****	****	r			****	****	***
$\Delta(1700)$	D_{33}	****	****	b	*		***	**	***
$\Delta(1750)$	P_{31}	*	*	i					
$\Delta(1900)$	S_{31}	**	**	d	*		*	**	*
$\Delta(1905)$	F_{35}	****	****	d*			**	**	***
$\Delta(1910)$	P_{31}	****	****	e			*	*	*
$\Delta(1920)$	P_{33}	***	***	n			**		*
$\Delta(1930)$	D_{35}	***	***		*				**
$\Delta(1940)$	D_{33}	*	*	F					
$\Delta(1950)$	F_{37}	****	****	o	*		****	*	****
$\Delta(2000)$	F_{35}	**	**	r				**	
$\Delta(2150)$	S_{31}	*	*	b					
$\Delta(2200)$	G_{37}	*	*	i					
$\Delta(2300)$	H_{39}	**	**	d					
$\Delta(2350)$	D_{35}	*	*	d					
$\Delta(2390)$	F_{37}	*	*	e					
$\Delta(2400)$	G_{39}	**	**	n					
$\Delta(2420)$	H_{311}	****	****						*
$\Delta(2750)$	I_{313}	**	**						
$\Delta(2950)$	K_{315}	**	**						

- **** Existence is certain, and properties are at least fairly well explored.
- *** Existence ranges from very likely to certain, but further confirmation is desirable and/or quantum numbers, branching fractions, *etc.* are not well determined.
- ** Evidence of existence is only fair.
- * Evidence of existence is poor.



A paragraph of caution

- From the PDG note on N and Δ resonances written by G. Hohler and R. Workman (GWU) in 2002:

“In the search for ‘missing’ quark-model states, indications of new structures occasionally are found. Often these are associated (if possible) with the one- and two-star states listed in Table 1. We caution against this: The status of the one- and two-star states found in the Karlsruhe-Helsinki (KH80) and Carnegie-Mellon/Berkeley (CMB80) fits is now doubtful.”



More caution

"I can make no objective statement that any of the states $S_{11}(2090)$ [3^{rd} N1/2-], $P_{11}(2100)$ [3^{rd} N*1/2+], and $D_{13}(2080)$ [3^{rd} N3/2-] exist."

"1* states are a dream, 2* states are a fantasy."

Steve Dytman, 2005



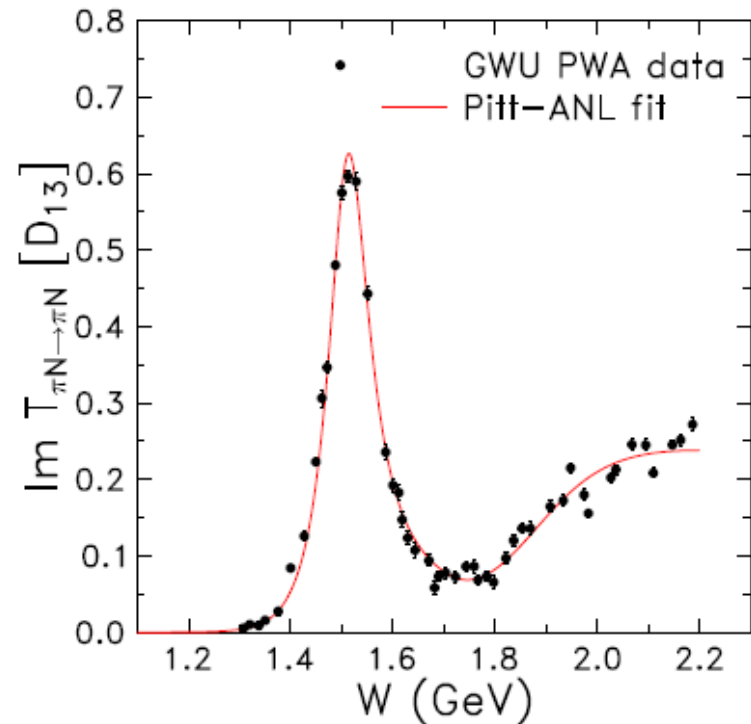
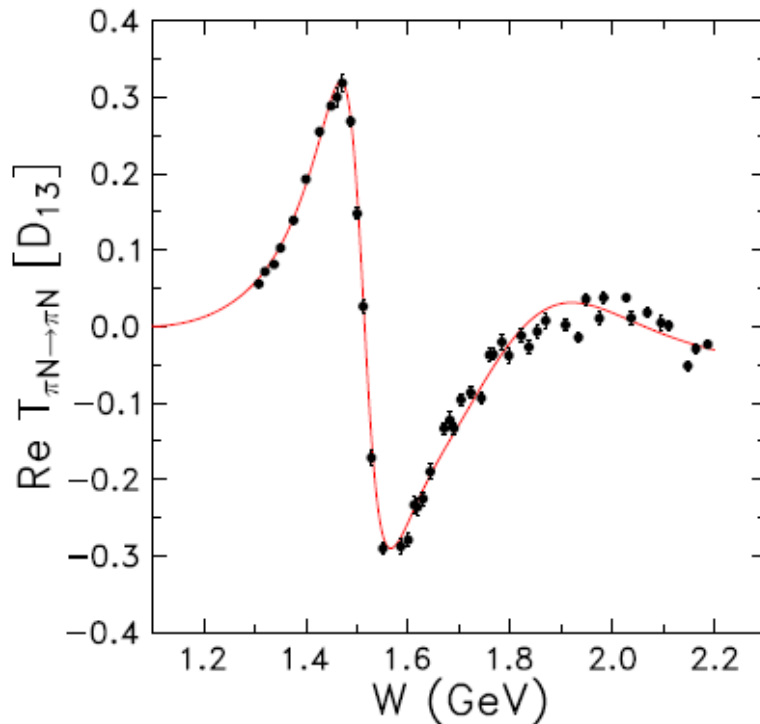
Scattering data analysis

- How do we extract baryon resonance parameters from data?
- Data is πN and $\gamma N \rightarrow \pi N, \pi\pi N (\rho N, \Delta\pi, \dots), \pi\pi\pi N (\omega N, \rho\Delta, \dots), \eta N, K\Lambda, K\pi\Lambda (K\Sigma), \dots$
 - For $\pi N \rightarrow \pi N$ have nearly complete data (missing some polarization observables); some inconsistencies
 - EM scattering labs (JLab, Mainz, Bonn, ...) are rapidly improving γN data in various final states, with beam and recently target polarization
- Find the mass, total width, final state channel couplings $\gamma_{B'M}$ of each resonance B with a given J^P
 - Recently done in two steps:
 - Partial-wave analysis (PWA) of scattering observables
 - Resonance parameters are extracted from fitting a model of scattering T matrix to PW amplitudes



GWU PWA / Pitt-ANL fit to $\pi N \rightarrow \pi N$

- Focus on $J^P = 3/2^-$ (D_{13} in πN), where PDG lists $N(1520)^{***}$, $N(1700)^{***}$, $N(2080)^{**}$

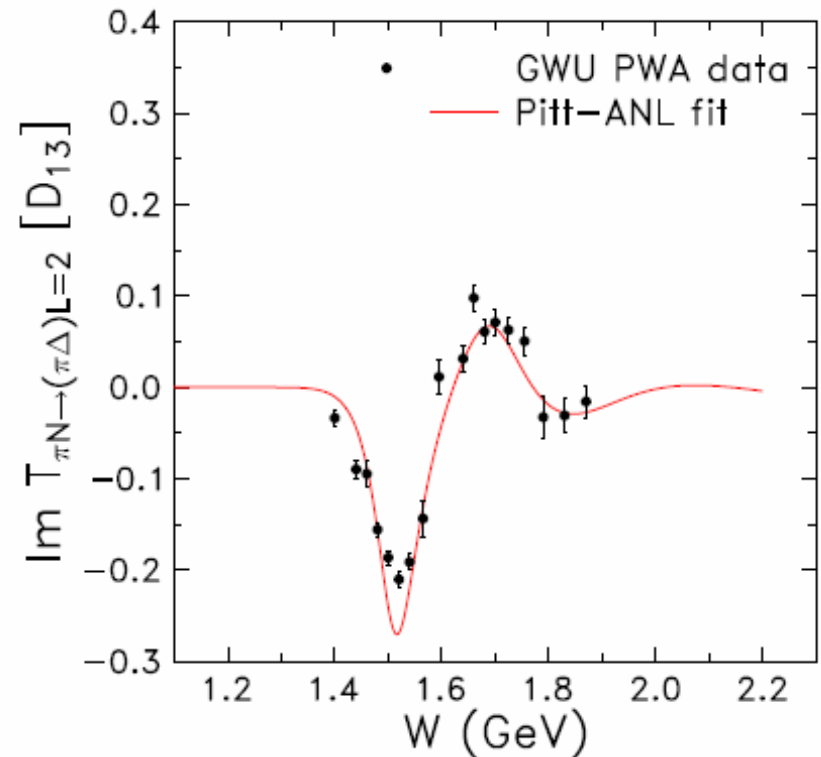
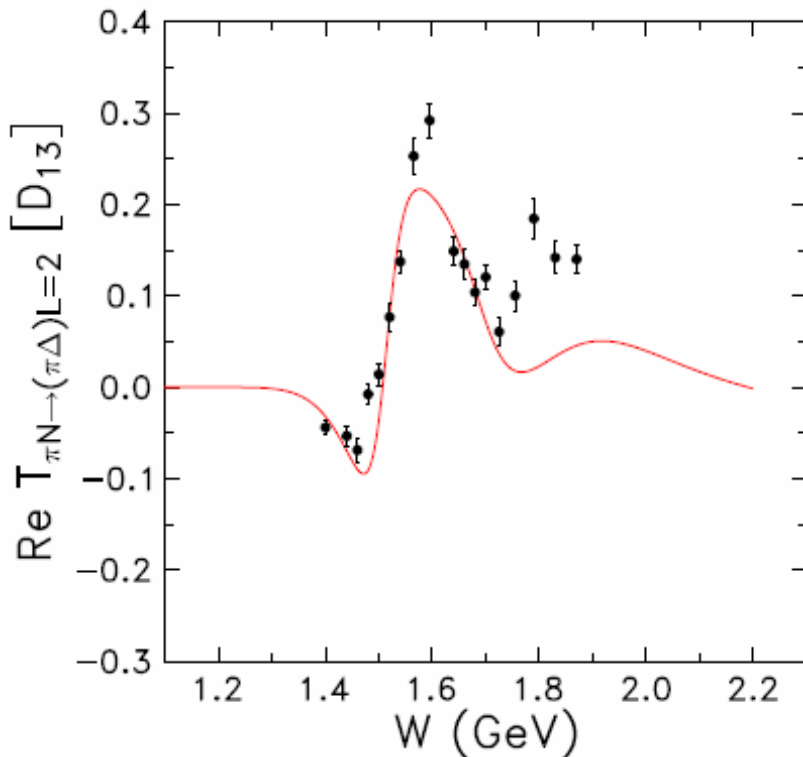


- No solid evidence for $N(1700)$ in $\pi N \rightarrow \pi N$



KSU isobar / Pitt-ANL fit, $\pi N \rightarrow (\pi\Delta)_D$

- Masses, widths and couplings of states consistent between πN elastic and $\pi N \rightarrow \pi\Delta$

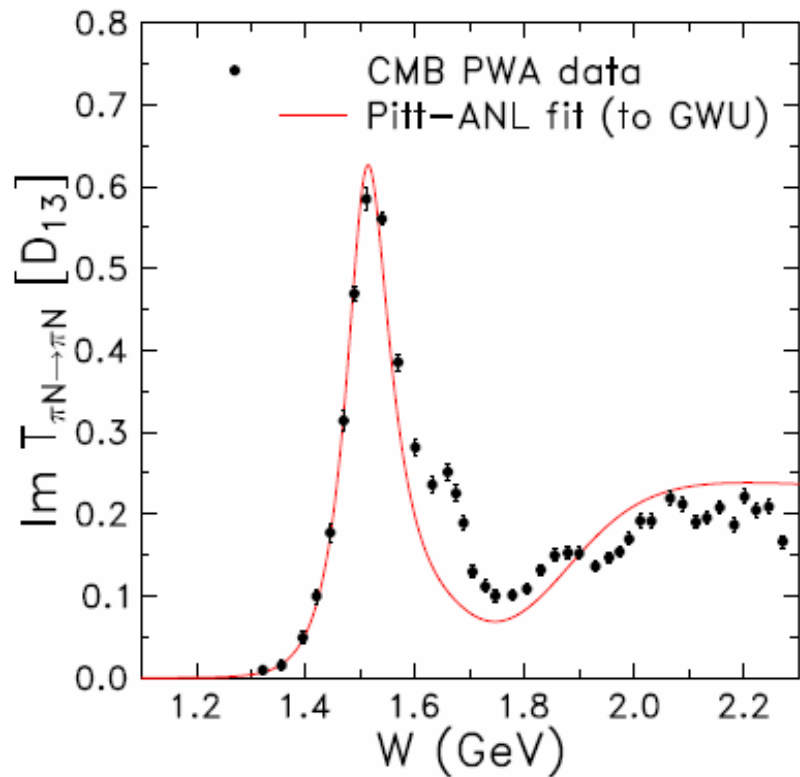
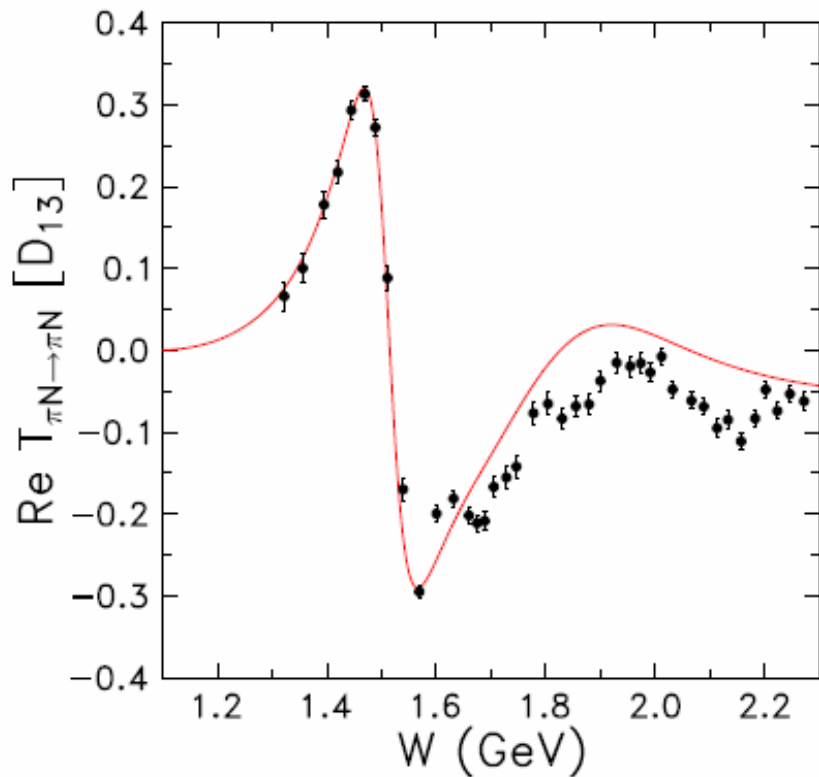


- $D_{13}(1700)$ weakly present in $\pi\Delta$ and also $K\Lambda$, with π and γ beams



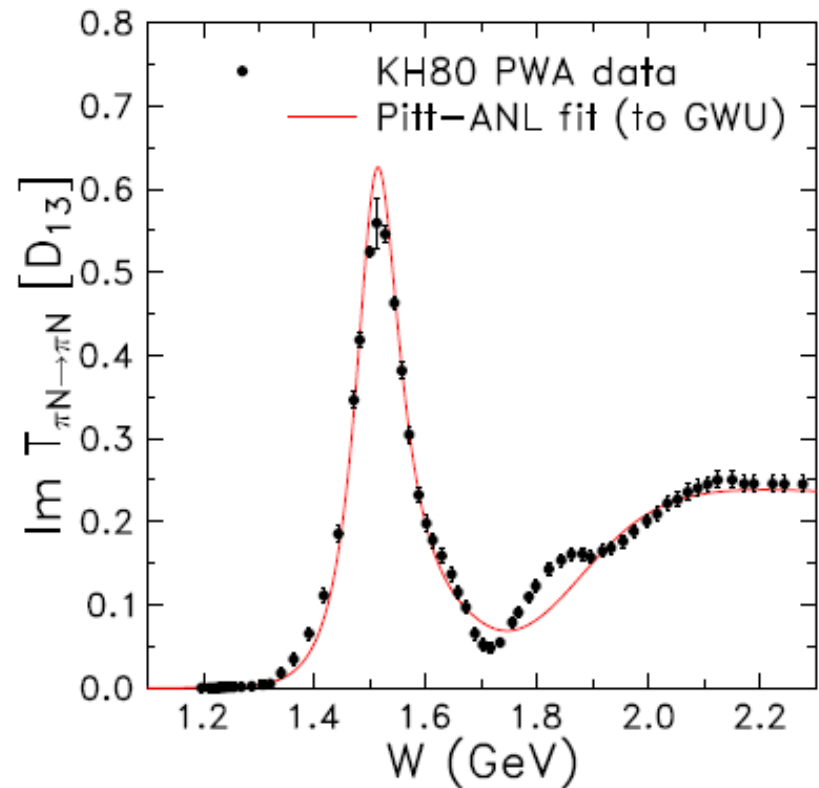
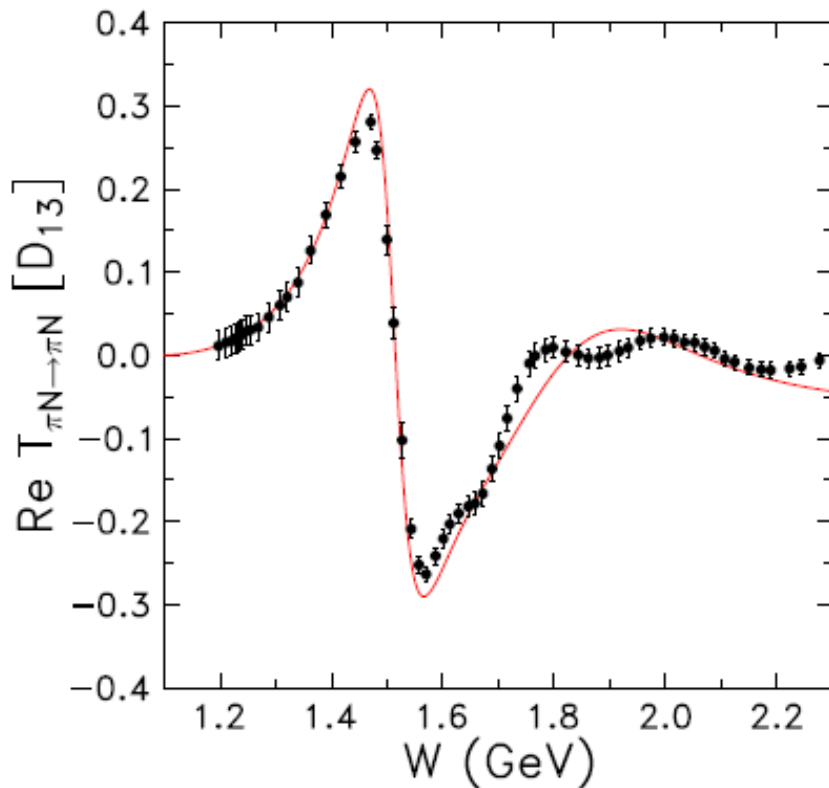
CMB energy-dependent PWA

- Points are CMU-LBL PWA of same $\pi N \rightarrow \pi N$ elastic data, curves are Pitt-ANL fit to GWU PWA

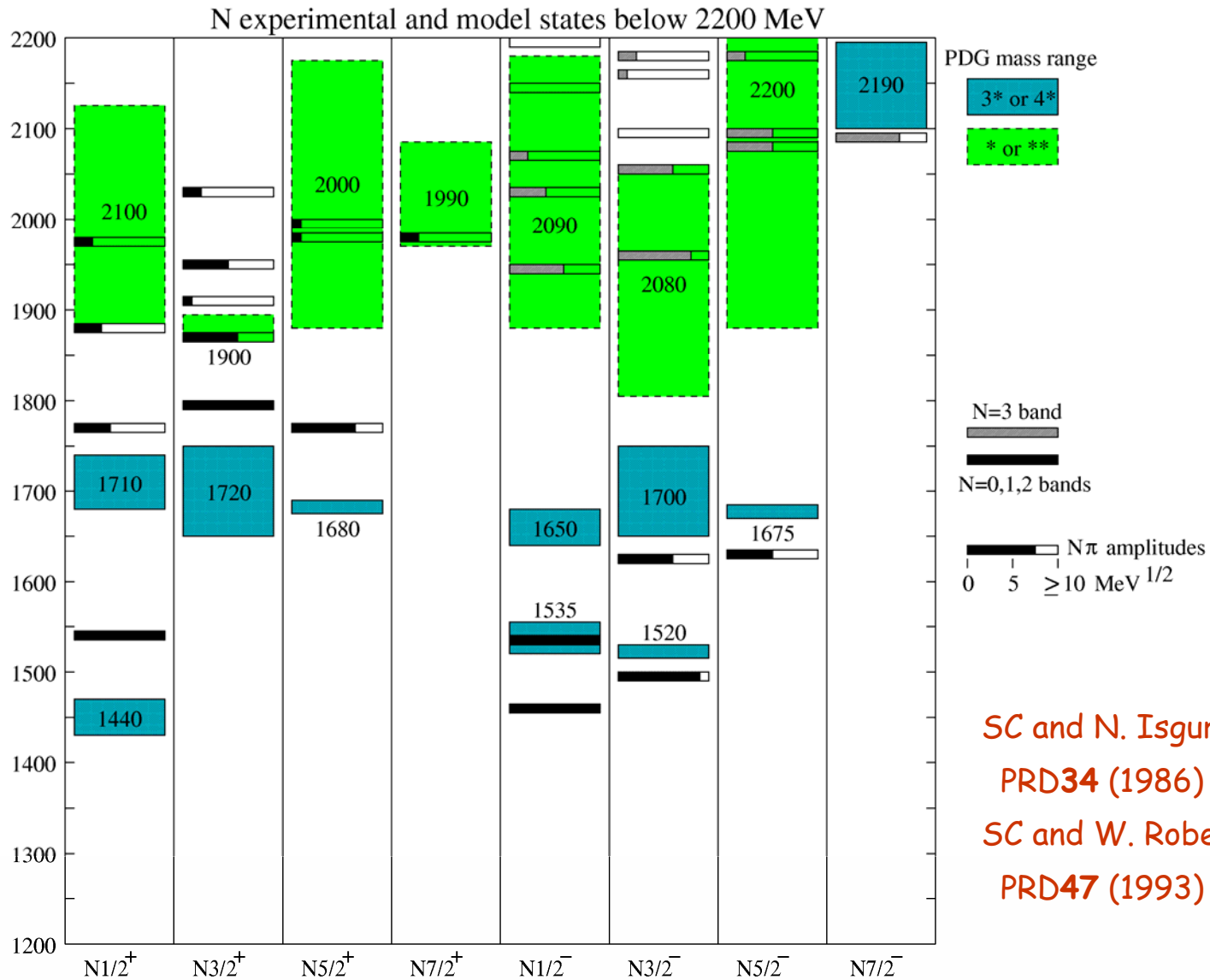


KH80 energy-dependent PWA

- Points are KH80 energy-dependent PWA of same $\pi N \rightarrow \pi N$ elastic data, curves are Pitt-ANL fit to GWU PWA



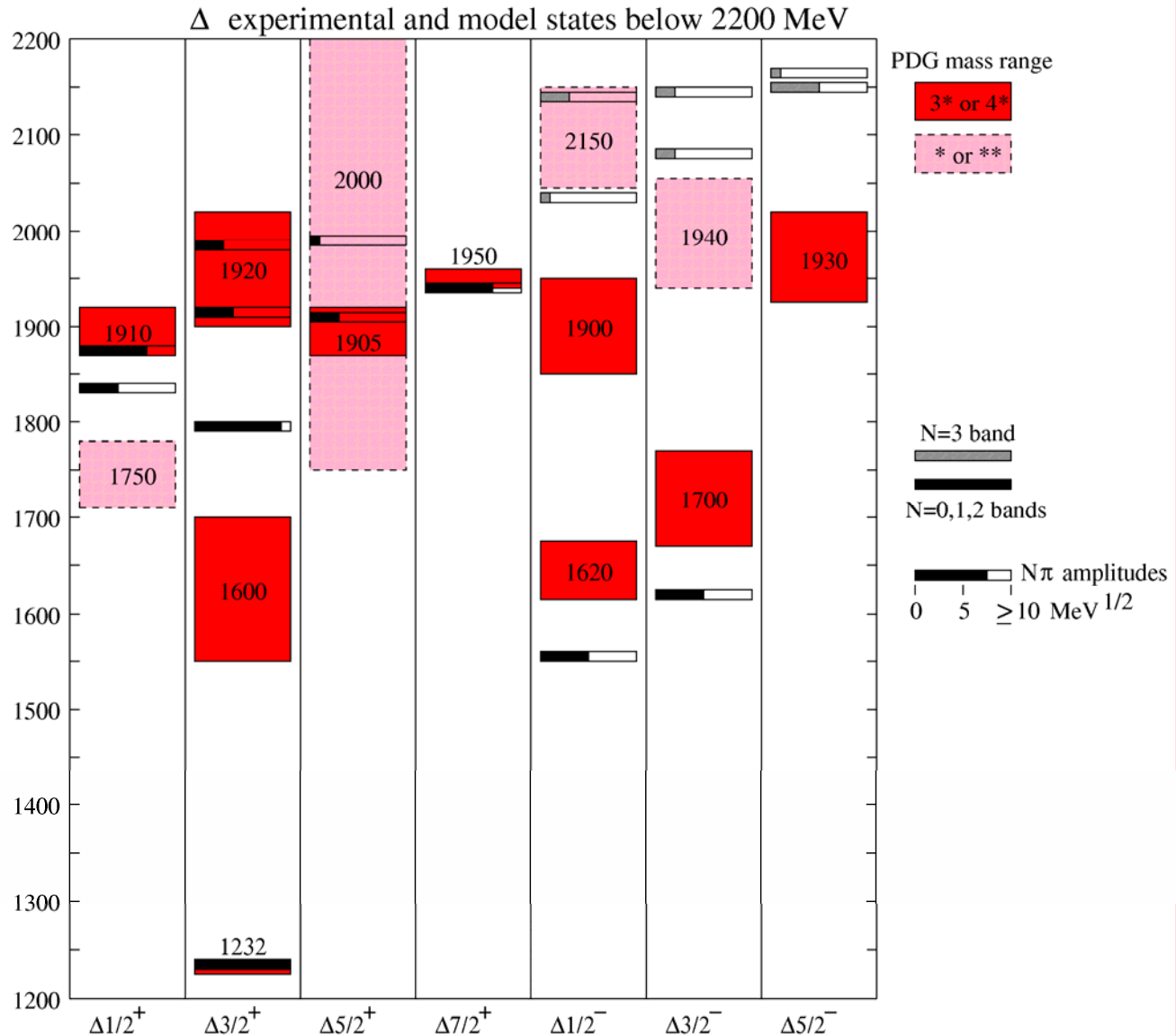
Nucleon model states and $N\pi$ couplings



SC and N. Isgur,
PRD34 (1986) 2809;
SC and W. Roberts,
PRD47 (1993) 2004



Δ model states and $N\pi$ couplings



What do we know about N^* states?

- EM transition amplitudes
 - Photo-couplings to proton and neutron
 - Allow calculation of partial widths $N^* \rightarrow \gamma N$
 - Resolved into helicity amplitudes $A^{p,n}_{1/2}$ and $A^{p,n}_{3/2}$ (photon spin \parallel or anti- \parallel nucleon spin)
 - Include the relative signs of $\gamma N \rightarrow N^* \rightarrow \pi N$
 - Largely from $\gamma N \rightarrow \pi N$
 - also $\gamma N \rightarrow \eta N$ [$S_{11}(1535)$]
 - This yields different photo-coupling $A^{p,n}_{1/2}$!



What do we know about N^* states?

- EM transition form factors
 - Single- π electro-production form factors
 - $e^- N \rightarrow e^- N^* \rightarrow e^- \pi N$
 - High-precision amplitudes published for $\Delta(1232)$ up to 6 GeV^2
 - Amplitudes published at low and intermediate Q^2 for $N(1440)P_{11}$, $N(1535)S_{11}$, $N(1520)D_{13}$
 - Analysis near completion for higher Q^2 values, and for $N(1680)F_{15}$
- Sensitive to structure of nucleon and N^*
 - Also to reaction mechanism !
 - Can probe evolution from soft to hard physics



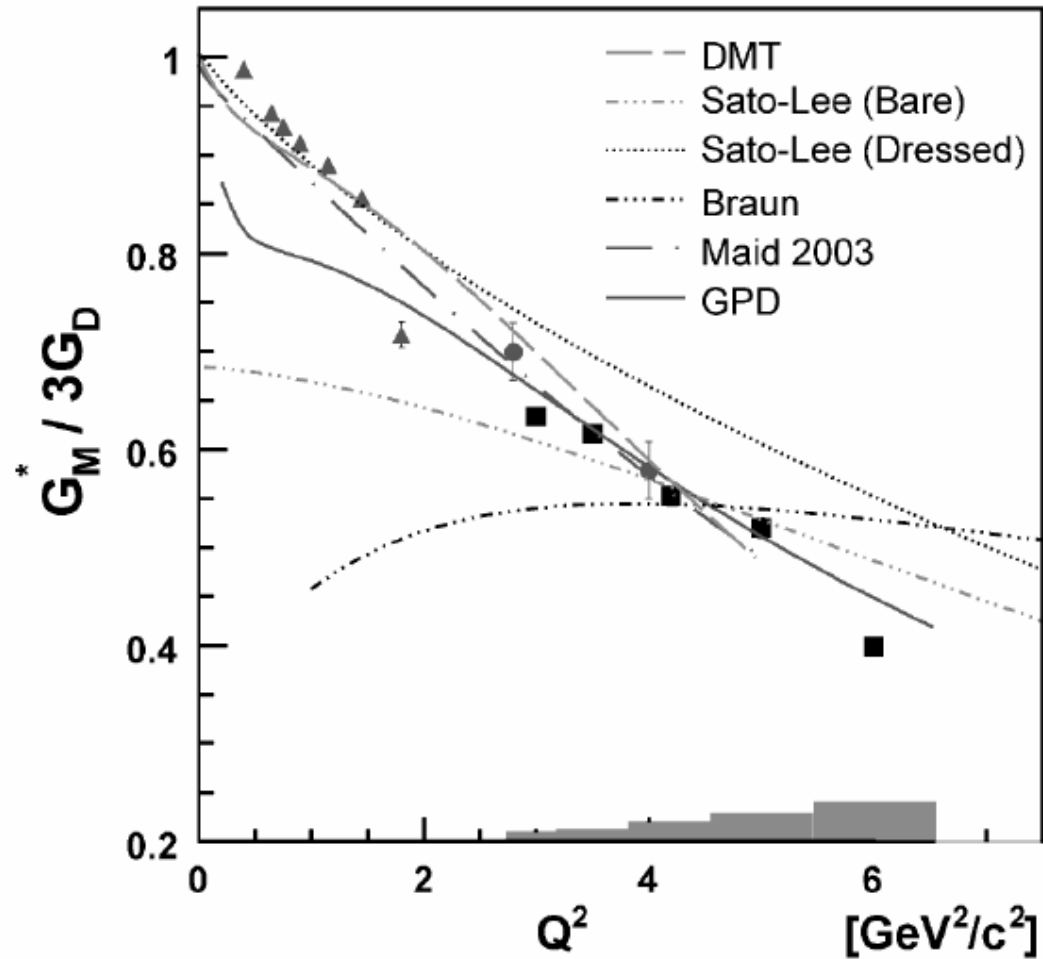
$\Delta(1232)$ EM transition form factors

CLAS (2002)

Hall C (1999)

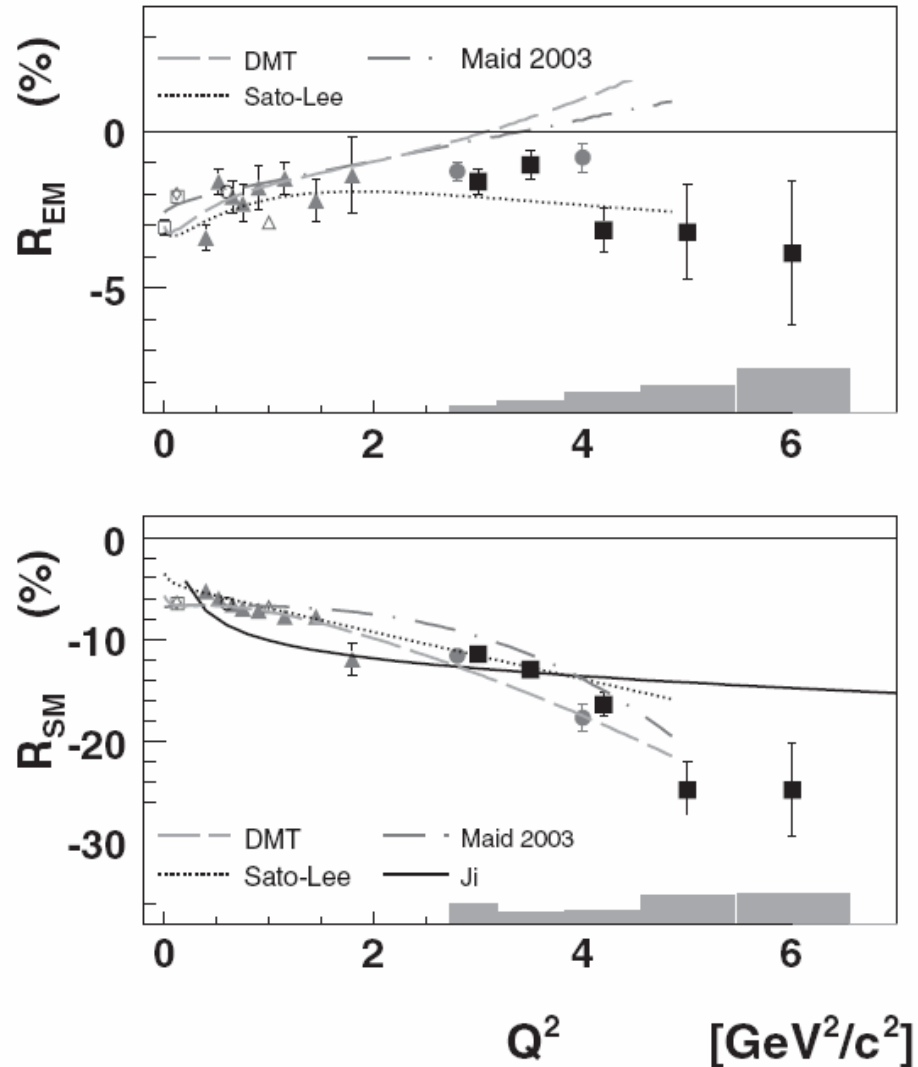
CLAS (2006)

Burkert & Lee
Int.J.Mod.Phys. E13,
1035(2004)



$\Delta(1232)$ EM transition form factors

Ratios of
small $E1+$, $S1+$
amplitudes to
dominant $M1+$
amplitude



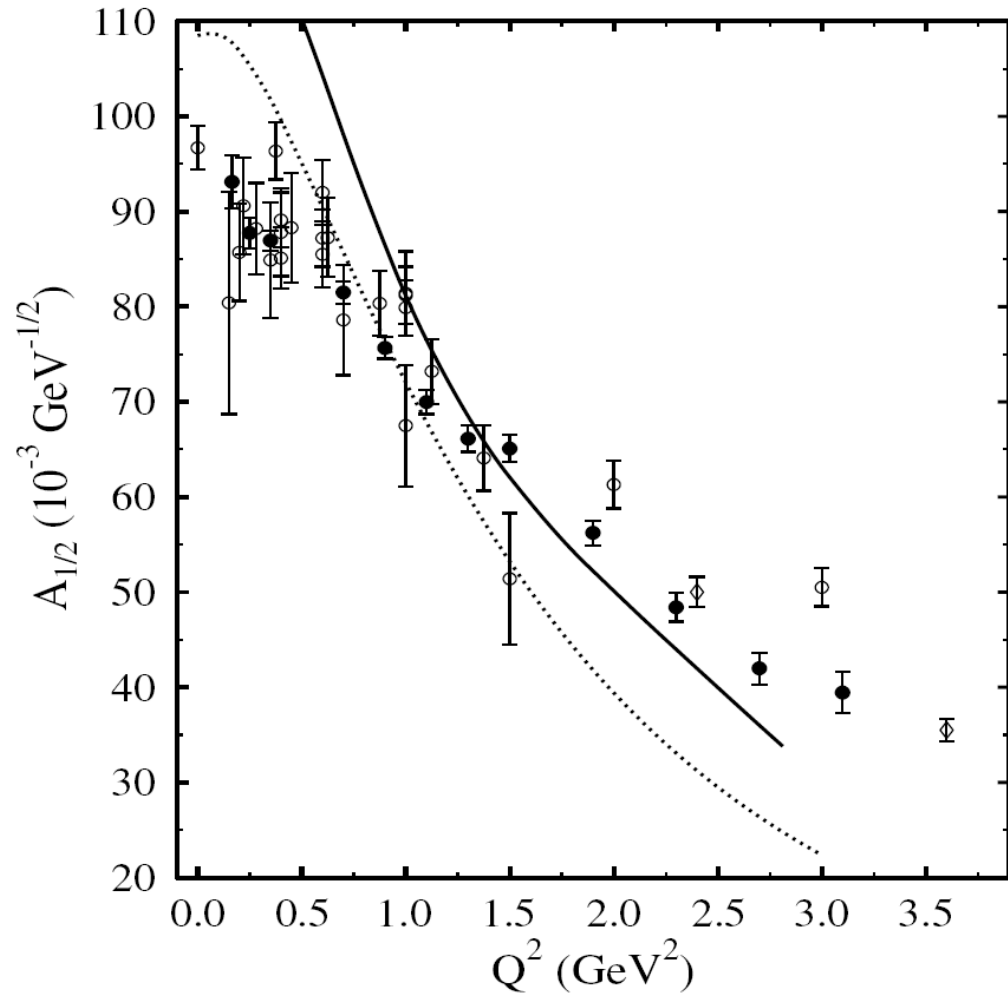
$S_{11}(1535)$ EM transition form factor

Previous expts.

Hall C

CLAS

- $N\eta$ bound state?



What are the goals of the N^* program?

- Firmly establish the existence of several positive-parity baryons (esp. N^* above 1800 MeV) that are currently missing or needing confirmation
 - Evidence for same state (mass, total width) in at least two channels
 - Extract photo-couplings and strong decay amplitudes into each channel



What are the goals of the N* program?

- Find convincing evidence for additional highly-excited (N=3 band) negative-parity baryons
- Extend measurements of EM transition form factors
 - Higher Q^2
 - Second resonance in a given partial wave
 - Significant differences in structure?



Developments required to meet our goals

- Experiment
 - Photo- and electro-production:
 - Polarization measurements (target, beam, recoil) currently underway and planned
 - Extraction of amplitudes for production off neutron
 - Talks in next session (1)
- Hadronic beams
 - E.g. a few hours of running with modern detection systems would replace world data set on $\pi N \rightarrow \pi\pi N$
 - See Winston Roberts' talk



Required developments...

- Theory

- Maintain and extend database and PWA for hadronic and EM production
- Develop unitary, couple-channel models of EM and strong transitions to multi-particle final states
 - Strong focus of this afternoon's second session and tomorrow morning's session



Required developments...

- Theory...
 - Develop ab-initio and model approaches to the spectrum and properties of N^* s
 - Lattice QCD
 - Chiral models based on hadronic d.f., constituent quark models
 - Predict EM and strong transition form factors (models and lattice QCD)
 - Direct comparison to extracted values
 - Required input for calculation of re-scattering in dynamical models

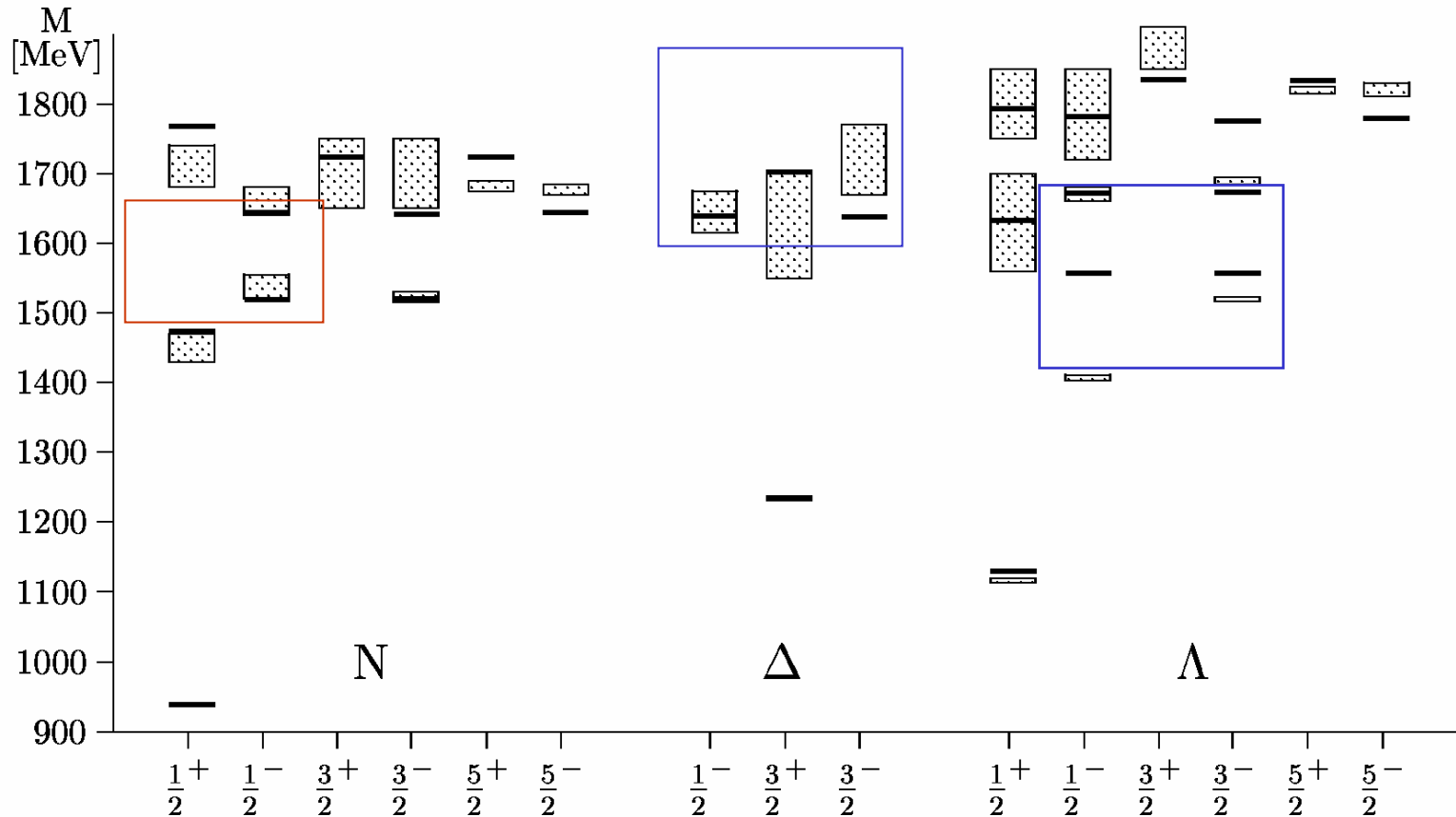


Backup slides...



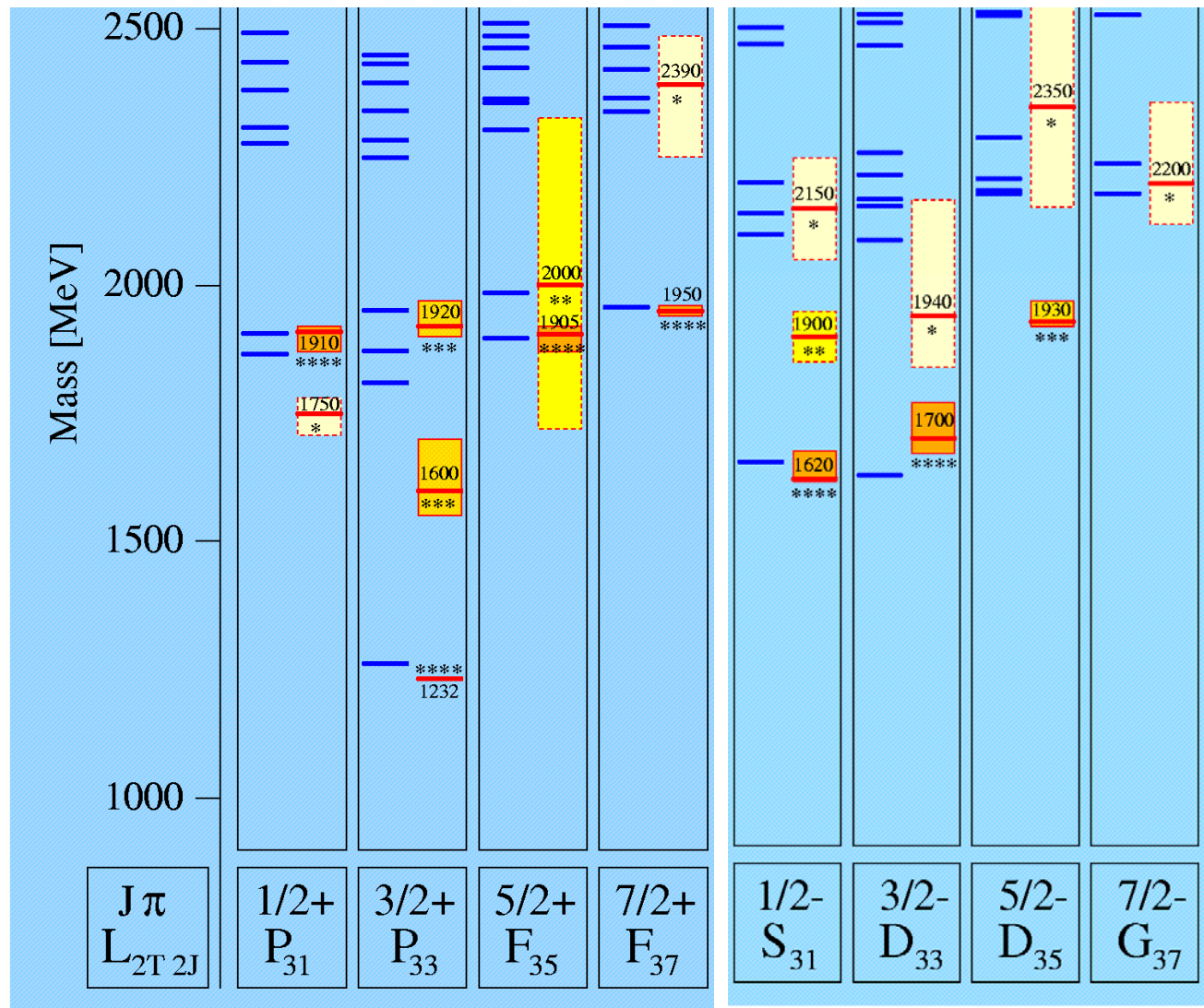
OBE spectrum...

- OBE Results for spectrum: *Glazman, Plessas, Theussl, Wagenbrunn, & Varga*



Instanton-induced interactions...

- spectrum of Δ^* only from confining potential
- Blask, Bohn, Huber, Metsch & Petry



N^* spectrum from 't Hooft's force

