

The Very Strange Spectroscopy Program at Jefferson Lab

Volker Credé

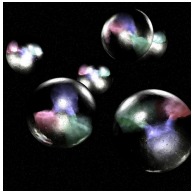
Florida State University, Tallahassee, FL

Excited Hyperons in QCD Thermodynamics at Freeze-Out

YSTAR 2016

Jefferson Lab

11/16/2016



Outline

- 1 Introduction
 - The Spectrum of Baryons
 - Lattice Calculations
- 2 Properties of Ξ Resonances
 - Experimental Situation
 - Recent Efforts in Photoproduction
- 3 Cascades at GlueX
 - Opportunities with Secondary K_L^0 Beams
- 4 Summary and Outlook



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Cascades at GlueX

- Opportunities with Secondary K_L^0 Beams

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Summary and Outlook

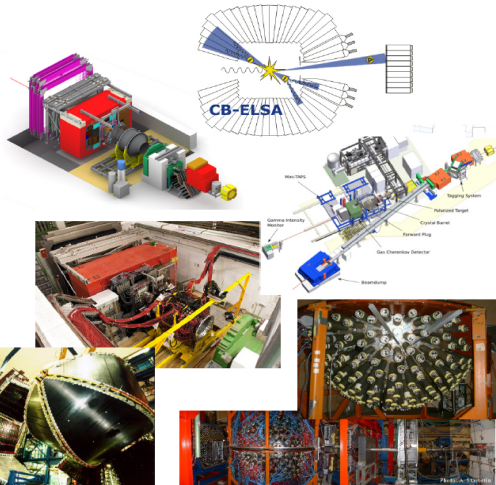


Baryon Spectroscopy in the 21st Century

Photoproduction

→ Toward Complete Experiments

- (Double-) Polarization
- Proton & Neutron Targets



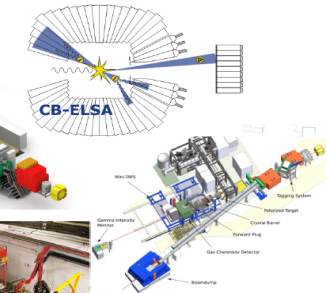
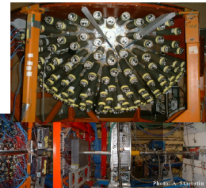
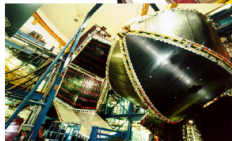
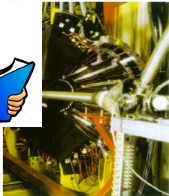
Baryon Spectroscopy in the 21st Century

Photoproduction

→ Toward Complete Experiments

- (Double-) Polarization
- Proton & Neutron Targets

Data are still difficult to interpret.



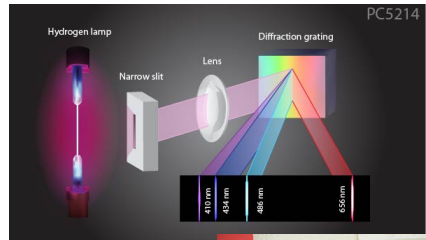
Why are Polarization Observables Important?



without polarizer ... but there is more.

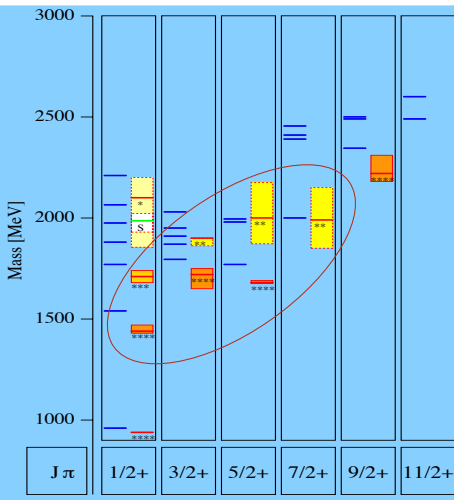


Atomic Spectrum of Hydrogen



Baryons are broad
and overlapping ...

Spectrum of N^* Resonances



V.C. & W. Roberts, Rep. Prog. Phys. **76** (2013)

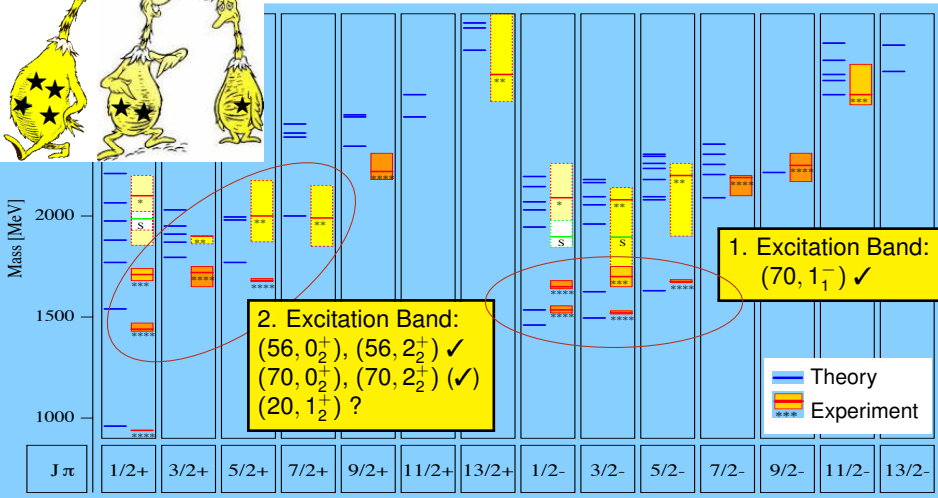
N^*	$J^P (L_{2l,2J})$	2010	2014
$N(1440)$	$1/2^+ (P_{11})$	***	***
$N(1520)$	$3/2^- (D_{13})$	***	***
$N(1535)$	$1/2^- (S_{11})$	***	***
$N(1650)$	$1/2^- (S_{11})$	***	***
$N(1675)$	$5/2^- (D_{15})$	***	***
$N(1680)$	$5/2^+ (F_{15})$	***	***
$N(1685)$			*
$N(1700)$	$3/2^- (D_{13})$	**	**
$N(1710)$	$1/2^+ (P_{11})$	**	**
$N(1720)$	$3/2^+ (P_{13})$	***	***
$N(1860)$	$5/2^+$		**
$N(1875)$	$3/2^-$		**
$N(1880)$	$1/2^+$		**
$N(1895)$	$1/2^-$		**
$N(1900)$	$3/2^+ (P_{13})$	**	**
$N(1990)$	$7/2^+ (F_{17})$	**	**
$N(2000)$	$5/2^+ (F_{15})$	**	**
$N(2040)$	$3/2^+$	*	*
$N(2060)$	$5/2^-$		**
$N(2100)$	$1/2^+ (P_{11})$	*	*
$N(2120)$	$3/2^-$		**
$N(2190)$	$7/2^- (G_{17})$	***	***
$N(2200)$	D_{15}	**	*
$N(2220)$	$9/2^+ (H_{19})$	***	***

13/2-



Spectrum of N^* Resonances (PDG < 2012)

— S. Capstick and N. Isgur, Phys. Rev. **D34** (1986) 2809



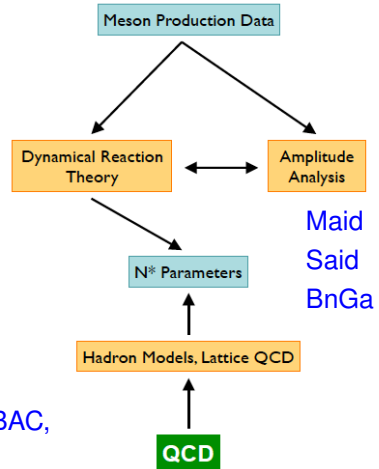
Extraction of Resonance Parameters in N^* Physics

- Double-polarization measurements
- Measurements off neutron and proton to resolve isospin contributions:
 - 1 $\mathcal{A}(\gamma N \rightarrow \pi, \eta, K)^{I=3/2} \iff \Delta^*$
 - 2 $\mathcal{A}(\gamma N \rightarrow \pi, \eta, K)^{I=1/2} \iff N^*$
- Re-scattering effects: Large number of measurements (and reaction channels) needed to extract full scattering amplitude.



Coupled Channels

Jülich, Gießen, EBAC,
 Kent State, etc.

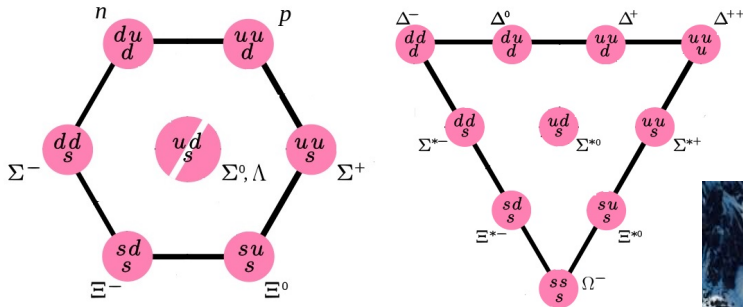


Open Issues in (Light) Baryon Spectroscopy

- ① What are the relevant degrees of freedom in (excited) baryons?
→ Can the high-mass states be described by the dynamics of three flavored quarks? To what extent are diquark correlations, gluonic modes or hadronic degrees of freedom important in this physics?
- ② Can we identify unconventional states in the strangeness sector, e.g. $\Lambda(1405)$ or the $N(1440)$?
- ③ What is the challenging situation with the $(20, 1_2^+)$ multiplet?
- ④ Can we identify the leading interactions between the constituents?
- ⑤ Do we understand the decay of high-mass baryon resonances?
Is a similar dynamical mechanism applicable (hadronic d.o.f.)?
- ⑥ What are the missing resonances and why are so many still missing?

Hyperon spectroscopy will help shed some light on the fascinating challenges in QCD Resonance Physics.

Cascade Spectrum and Multiplets



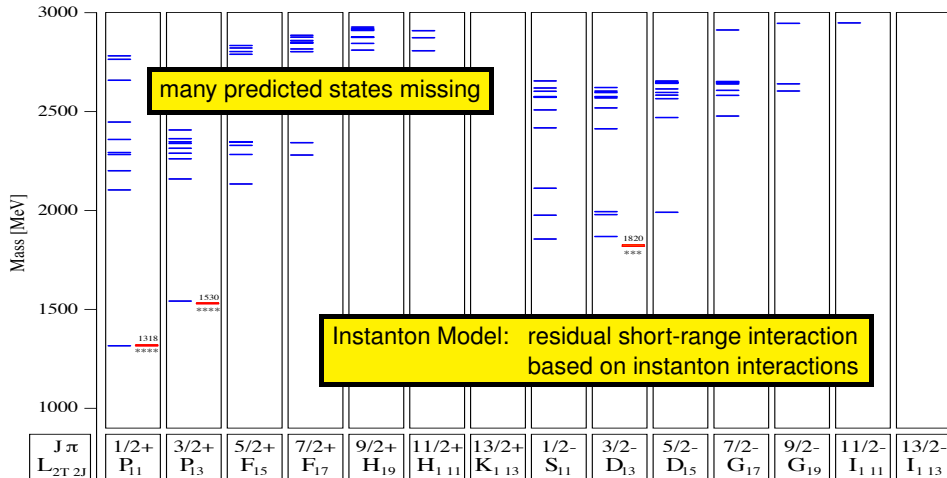
The decuplets consist of Δ^* , Σ^* , Ξ^* , and Ω^* resonances, but also the octets consist of an Ξ^* state.

→ We expect as many Ξ^* 's as N^* & Δ^* states together. Moreover, their properties should be related.



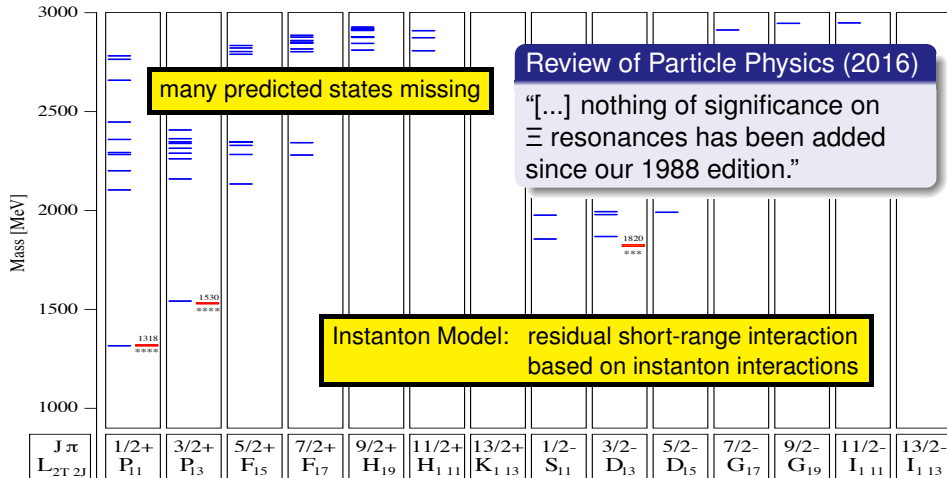
Cascade Resonances: Status as of 2016

— U. Loering, B. Ch. Metsch, H. R. Petry, Eur. Phys. J. **A10** (2001) 447-486



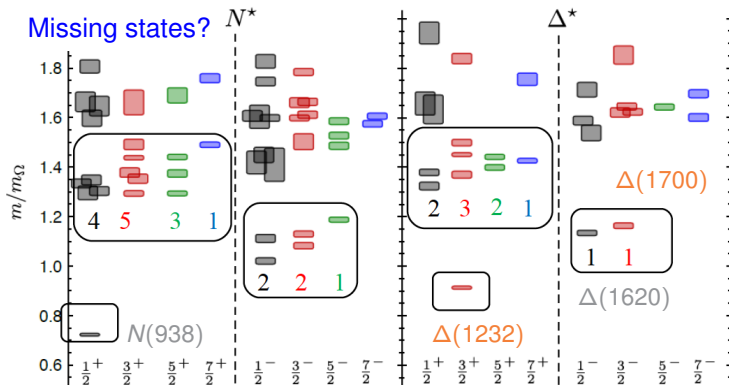
Cascade Resonances: Status as of 2016

— U. Loering, B. Ch. Metsch, H. R. Petry, Eur. Phys. J. **A10** (2001) 447-486



The N^* and Δ^* Spectrum from Lattice QCD

R. Edwards *et al.*, Phys. Rev. D **84**, 074508 (2011); Phys. Rev. D **87**, 054506 (2013)



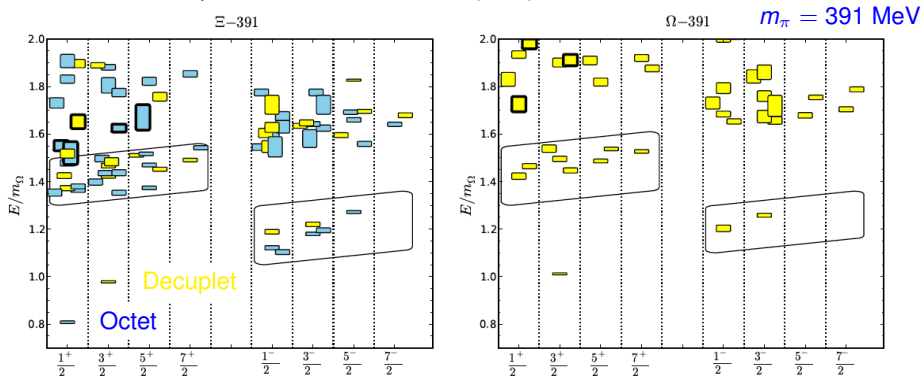
$m_\pi = 396$ MeV

Exhibits broad features expected of $SU(6) \otimes O(3)$ symmetry

→ Counting of levels consistent with non-rel. quark model, no parity doubling.

The Ξ^* and Ω^* Spectrum from Lattice QCD

R. Edwards *et al.*, Phys. Rev. D **87**, no. 5, 054506 (2013)



Exhibits broad features expected of $SU(6) \otimes O(3)$ symmetry

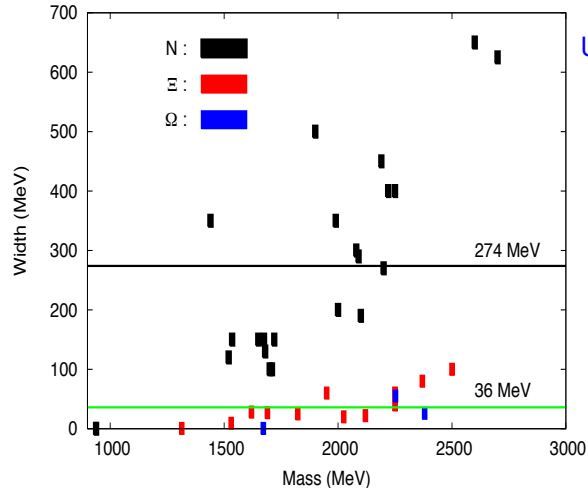
→ Counting of states of each flavor and spin consistent with QM for the lowest negative- and positive-parity bands.

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Baryon Widths: The Experimental Point of View



Unique features of Ξ^* and Ω^* :

- Strangeness $S > 1$
- Narrow widths:
 $\Gamma_{\Xi^*} \approx 10 - 20 \text{ MeV?}$

Why are Cascade Resonances Narrow?

Possible explanations:

1 Narrowness related to the number of light quarks

- Specifically, resonance width proportional to square of the number of light quarks: $\Gamma_{N^*, \Delta^*} : \Gamma_{\Lambda^*, \Sigma^*} : \Gamma_{\Xi^*} \approx 9 : 4 : 1$
(D. O. Riska, Eur. Phys. J. **A17**, 297 (2003))

2 Alternative explanation based on Cascade structure and decay modes

(S. Capstick *et al.*)

- Decays $\Xi^* \rightarrow \Xi\pi$ are suppressed relative to $N^*, \Delta^* \rightarrow N\pi$.
Non-rel. one-gluon exchange model: Chao, Isgur, Karl, PR **D23**, 155 (1981)
- Flavor symmetry requires s -quarks at ends of ρ oscillator; excitation energy is given by the square root of K/M where K will be equal for all quark pairs if the confinement potential is flavor independent.
 - Excitation of ρ costs less energy than the excitation of λ .
(Argument only valid for lowest states.)

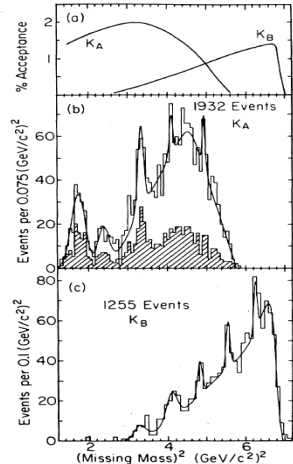
Measurements at BNL in $K^-p \rightarrow K_{\text{slow}}^+ + X^-$

“Existence of Ξ Resonances above 2 GeV”

(C.M. Jenkins *et al.*, Phys. Rev. Lett. **51**, 951 (1983))

Observed Ξ States:

$\Xi(1320)$	****	$I(J^P) = \frac{1}{2}(\frac{1}{2}^+)$
$\Xi(1530)$	****	$I(J^P) = \frac{1}{2}(\frac{3}{2}^+)$
$\Xi(1820)$	***	$I(J^P) = \frac{1}{2}(\frac{3}{2}^-)$
$\Xi(2030)$	***	$I(J^P) = \frac{1}{2}(\geq \frac{5}{2}^?)$
$\Xi(2370)$	***	$I(J^P) = \frac{1}{2}(??)$
$\Xi(2500)$	***	$I(J^P) = \frac{1}{2}(??)$



Excited Cascade Resonances at BaBar

BaBar collaboration has recently studied the $\Xi(1530)$ resonance in the decay $\Lambda_c^+ \rightarrow K^+ \Xi(1530)^0 \rightarrow K^+ (\Xi^- \pi^+)$ (V. Ziegler, MENU 2007)

- Complementary to the search in the reaction $\gamma p \rightarrow K^+ (\Xi^- \pi^+)$
- Dalitz plot shows only one dominant structure: $\Xi(1530)^0 \rightarrow \Xi^- \pi^+$
→ Spin-parity analysis favors a $J^P = 3/2^+$ assignment
- Evidence for S - P -wave interference in the $\Xi^- \pi^+$ system provides hints for possible $\Xi(1690)$ production
- Further indications for the $\Xi(1690)$ state have been found in the study of $\Lambda_c^+ \rightarrow \Lambda K_S K^+$
→ BaBar data favor a spin-1/2 assignment at the 56.4 % C.L.

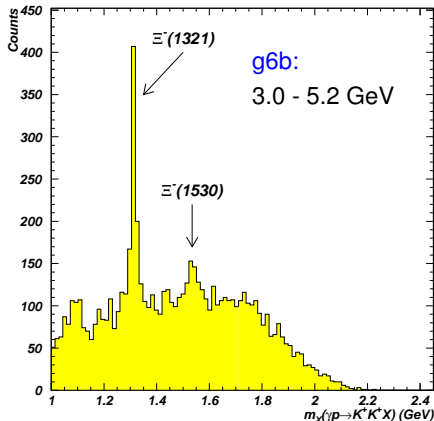
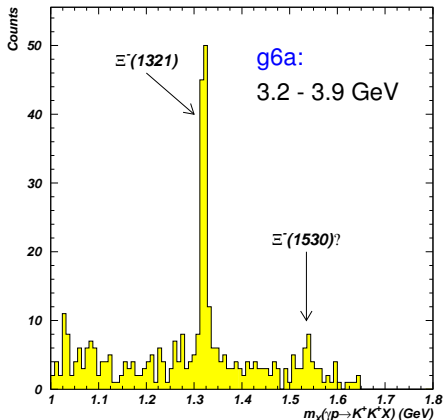
CLAS g6 Runs

First exclusive photoproduction of Ξ^-

J. Price *et al.*, PRC **71**, 058201 (2005)

Look for $\gamma p \rightarrow K^+ K^+ (X)$

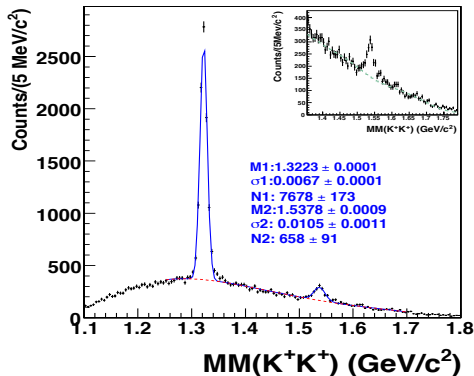
with $B = +1$, $Q = -1$, $S = -2$



CLAS g11a Run

More data mining based on much higher statistics

Guo *et al.*, PRC **76**, 025208 (2007)

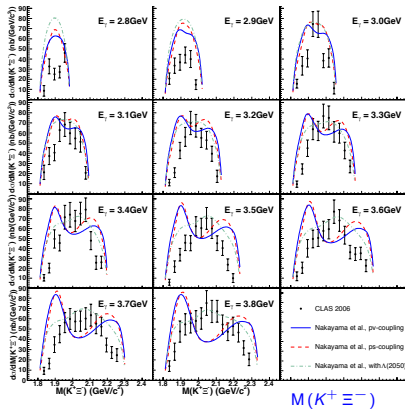


Reaction $\gamma p \rightarrow K^+ K^+ (X)$

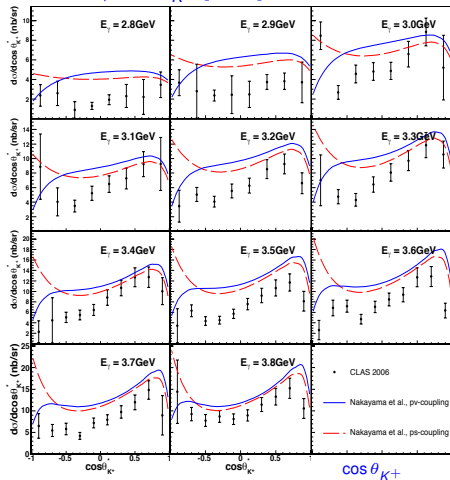
- Very strong $\Xi(1320)$ signal
 - Clear signal for $\Xi(1530)$
 - Ratio $N_{\Xi} / N_{\Xi(1530)} \approx 10 : 1$
- About the same as for the CLAS-g6 data.

CLAS g11a Run: Differential Cross Sections

E_γ range of 2.75 – 3.85 GeV

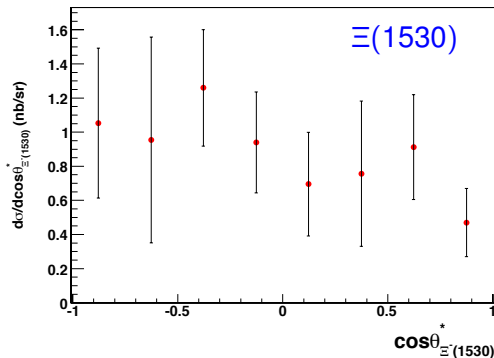
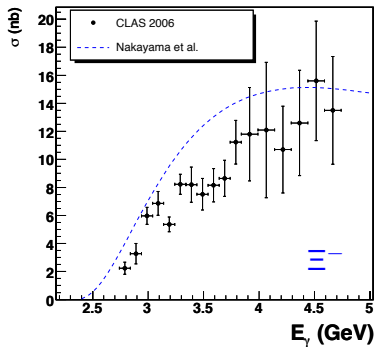


$\cos d\sigma/d\cos\theta_{K^+}$ [nb/sr]



CLAS g11a: Cross Sections of Ξ^- and $\Xi(1530)$

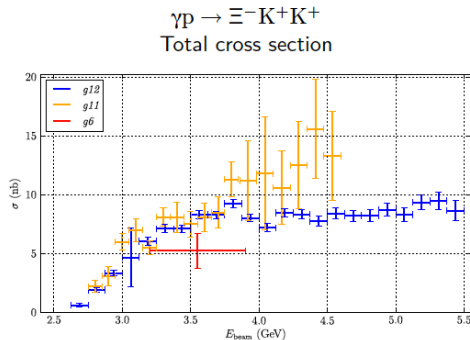
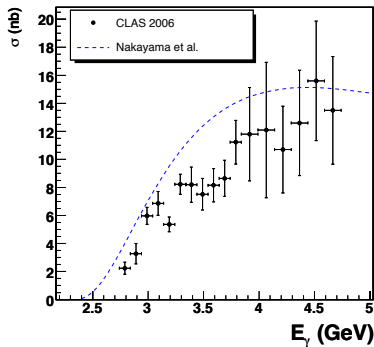
E_γ range of 2.75 – 4.75 GeV



K. Nakayama, Y. Oh, and H. Haberzettl, Phys. Rev. **C74**, 035205 (2006)

CLAS g12: Total Cross Section of Ξ^- (preliminary)

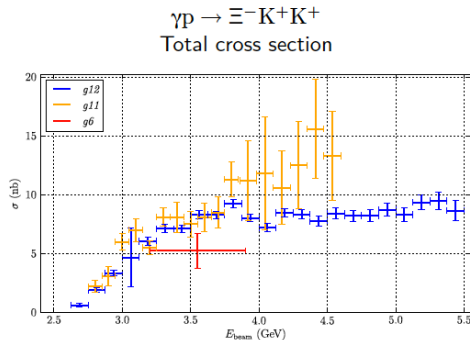
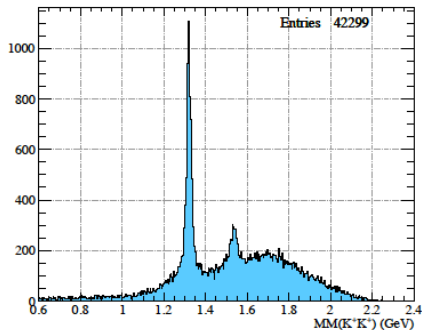
E_γ range of 2.75 – 4.75 GeV



K. Nakayama, Y. Oh, and H. Habermehl, Phys. Rev. **C74**, 035205 (2006)

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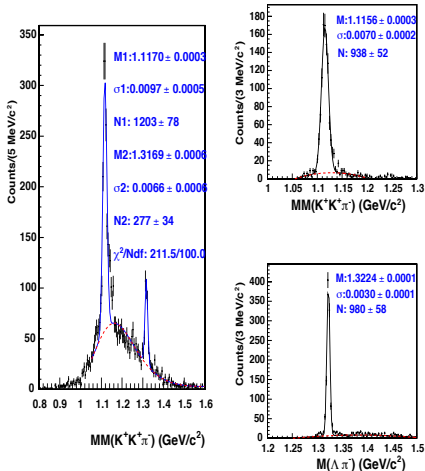
Johann Goetz (CLAS Collaboration), UCLA, Ph.D. Thesis



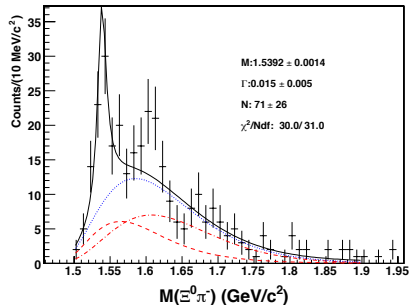
Upper Limits (integrated over 3.5-5.4 GeV):

- (1) $\Xi(1620)$: 0.78 nb (2) $\Xi(1690)$: 0.97 nb (3) $\Xi(1820)$: 1.09 nb

CLAS g11a: Excited States in $\gamma p \rightarrow K^+ K^+ \pi^- (X)$



- 1 Only $\Xi(1530)$ statistically significant
- 2 $\Xi(1620)$ signal “plausible”, but simulated K^{*0} events also peak in 1600 MeV/c^2 region ($\gamma p \rightarrow K^+ K^{*0} \Xi^0$, $K^{*0} \rightarrow K^+ \pi^-$)



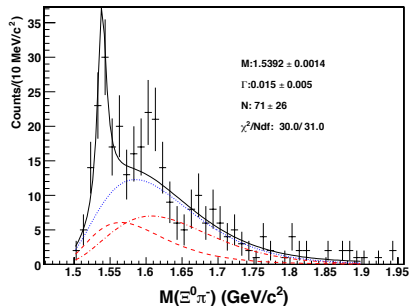
CLAS g11a: Excited States in $\gamma p \rightarrow K^+ K^+ \pi^- (X)$

From the paper: *Although a small enhancement is observed in the $\Xi^0 \pi^-$ invariant mass spectrum near the controversial 1-star Ξ^- (1620) resonance, it is not possible to determine its exact nature without a full partial wave analysis.*

Need high-statistics, high-energy data from an experiment designed to see Ξ states:

- 3- or 4-track trigger
- Reconstruction of full decay chain
- Higher photon energy
- Improved detectors

→ CLAS 12 and GlueX at Jefferson Lab
(L. Guo's talk on Opportunities at CLAS12)

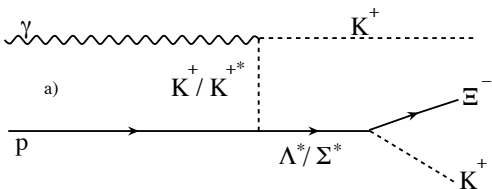


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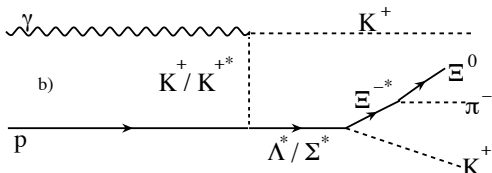


Possible Production Mechanisms



$K^+(\Xi^- K^+)$, $K^+(\Xi^0 K^0)$, $K^0(\Xi^0 K^+)$

→ Cross sections, beam asymmetries
(similar to $p\pi\pi$ & pKK^*)



Production of excited states via a

① forward-going K^0 meson

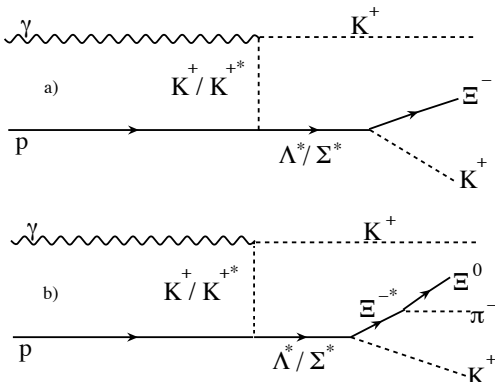
→ $K^0(\Xi^- \pi^+) K^+$, etc.

② forward-going K^+ meson

→ $K^+(\Xi^- \pi^+) K^0$,
 $K^+(\Xi^0 \pi^-) K^+$, etc.

* W. Roberts *et al.*, Phys. Rev. C **71**, 055201 (2005)

Possible Production Mechanisms



$K^+(\Xi^- K^+)$, $K^+(\Xi^0 K^0)$, $K^0(\Xi^0 K^+)$

→ Cross sections, beam asymmetries
(similar to $p\pi\pi$ & pKK^*)

At other facilities (for comparison):

$$K^- p \rightarrow K^+ \Xi^{*-}$$

J-PARC

$$K_L p \rightarrow K^+ \Xi^{*0}$$

Hall D ?

$$pp \rightarrow \Xi^* X$$

LHCb

$$\bar{p}p \rightarrow \Xi^* \Xi$$

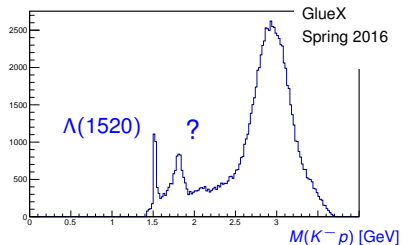
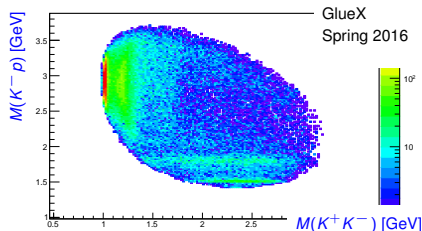
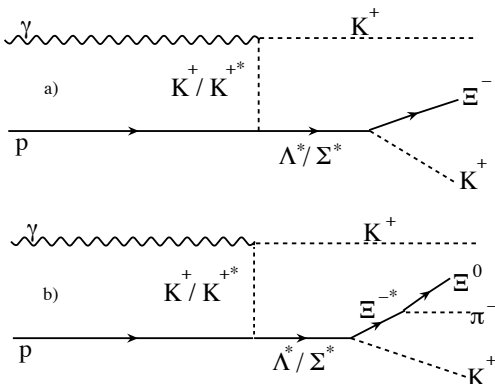
PANDA

$$e^+ e^- \rightarrow \Xi^* X$$

Belle II, BES III

* W. Roberts *et al.*, Phys. Rev. C **71**, 055201 (2005)

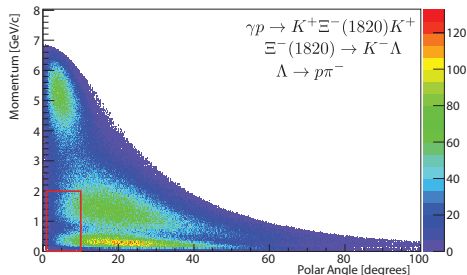
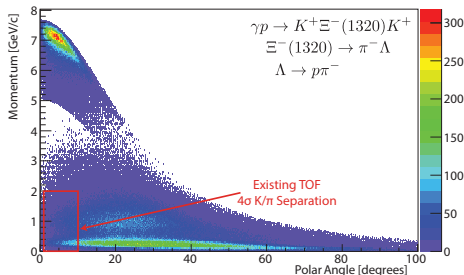
Possible Production Mechanisms



Courtesy of Sean Dobbs

Ξ Spectroscopy with the GlueX Detector

GlueX Proposal on “Decays to Strange Final States” (JLab PAC 39, 40 & 42)



Efficiency should be adequate for conducting a study of excited Ξ states with the baseline detector:

- Detailed studies of the production, especially of the ground state Ξ 's, and a parity measurement* will likely require enhanced kaon identification in the forward direction → Components of the BaBar DIRC for GlueX.

* e.g. Nakayama *et al.*, Phys. Rev. C **85**, 042201 (2012)

Ξ Spectroscopy with the GlueX Detector

The Ξ octet ground states (Ξ^0 , Ξ^-) will be challenging to study via exclusive t -channel (meson exchange) production. The typical final states have kinematics for which the baseline GlueX detector has very low acceptance due to:

- the high-momentum forward-going kaon and
- the relatively low-momentum pions produced in the Ξ decay.

The production of the Ξ decuplet ground state, $\Xi(1530)$, and other excited Ξ 's decaying to $\Xi\pi$ results in a lower momentum kaon at the upper vertex, and these heavier Ξ states produce higher momentum pions in their decays.

The lightest excited Ξ states are expected to decouple from $\Xi\pi$ and can be searched for and studied also in their decays to $\Lambda\bar{K}$ and $\Sigma\bar{K}$:

$$\begin{aligned}\gamma p \rightarrow K Y^* &\rightarrow K^+ (\bar{K}\Lambda)_{\Xi^-*} K^+, \quad K^+ (\bar{K}\Lambda)_{\Xi^{0*}} K^0, \quad K^0 (\bar{K}\Lambda)_{\Xi^{0*}} K^+, \\ \gamma p \rightarrow K Y^* &\rightarrow K^+ (\bar{K}\Sigma)_{\Xi^-*} K^+, \quad K^+ (\bar{K}\Sigma)_{\Xi^{0*}} K^0, \quad K^0 (\bar{K}\Sigma)_{\Xi^{0*}} K^+.\end{aligned}$$

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The production of the Ξ decuplet ground state, $\Xi(1530)$, and other excited Ξ 's decaying to $\Xi\pi$ results in a lower momentum kaon at the upper vertex, and these heavier Ξ states produce higher momentum pions in their decays.

The lightest excited Ξ states are expected to decouple from $\Xi\pi$ and can be searched for and studied also in their decays to $\Lambda\bar{K}$ and $\Sigma\bar{K}$:

$$\begin{aligned}\gamma p \rightarrow K Y^* &\rightarrow K^+ (\bar{K}\Lambda)_{\Xi^-*} K^+, \quad K^+ (\bar{K}\Lambda)_{\Xi^{0*}} K^0, \quad K^0 (\bar{K}\Lambda)_{\Xi^{0*}} K^+, \\ \gamma p \rightarrow K Y^* &\rightarrow K^+ (\bar{K}\Sigma)_{\Xi^-*} K^+, \quad K^+ (\bar{K}\Sigma)_{\Xi^{0*}} K^0, \quad K^0 (\bar{K}\Sigma)_{\Xi^{0*}} K^+.\end{aligned}$$

Ξ Spectroscopy with the GlueX Detector

Expected yields of Ξ states using (PAC 40 proposal):

$$N = \epsilon \sigma n_\gamma n_t T \quad \text{where}$$

$$\sigma_{\Xi(1320)} = 15 \text{ nb and } \sigma_{\Xi(1530)} = 2 \text{ nb at } E_\gamma = 5 \text{ GeV}$$

$$\epsilon_{\Xi(1820)} \approx 30 \% \text{ (BDT: signal purity 0.9)}$$

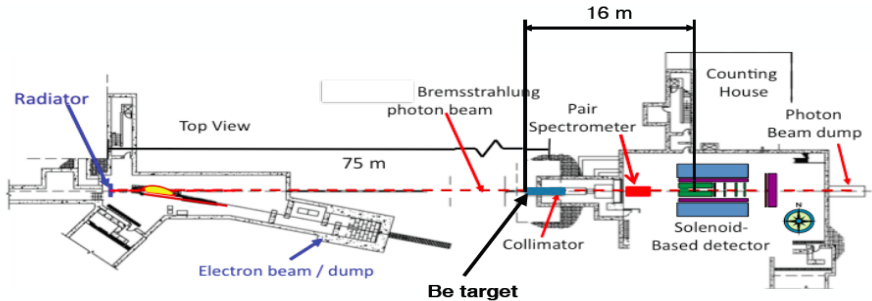
→ 800,000 $\Xi^-(1320)$ events

100,000 $\Xi^-(1530)$ events

90,000 $K^+ K^+ K^- \Lambda$ events (based on PYTHIA)

→ At least x10 more statistics than previous CLAS result.

Opportunities with Secondary K_L^0 Beams in Hall D



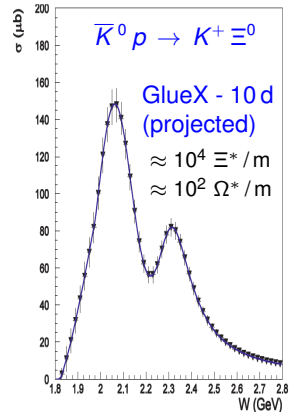
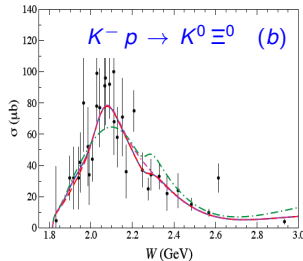
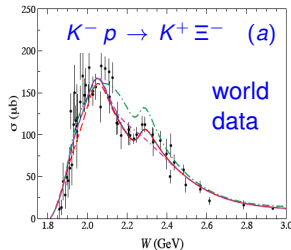
K_L^0 mesons from collimated photon beam on a Be target ($R = 2$ cm, $L = 40$ cm)

- $\Delta L \approx 16$ m (between Be & LH_2 targets); thick lead absorber to stop photons.
- ≈ 2000 K_L^0 / sec (x10 higher than in LASS experiment at SLAC).
- Resolution of $\Delta p/p \approx 0.3\%$ for K_L^0 momenta based on TOF.
- Reduced n rate compared to LASS.

Opportunities with Secondary K_L^0 Beams in Hall D

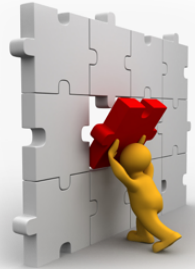
Possible reactions to be studied (elastic and charge-exchange reactions):

- 2- & 3-body reactions producing $S = -1$ hyperons
- 2-body reactions producing $S = -2$ hyperons
 $\rightarrow K_L^0 p \rightarrow K^+ \Xi^0; \pi^+ K^+ \Xi^-; K^+ \Xi^{0*}; \pi^+ K^+ \Xi^{*-}$
- 3-body reactions producing $S = -3$ hyperons
 $\rightarrow K_L^0 p \rightarrow K^+ K^+ \Omega^-; K^+ K^+ \Omega^{*-}$



Outline

- 1 Introduction
 - The Spectrum of Baryons
 - Lattice Calculations
- 2 Properties of Ξ Resonances
 - Experimental Situation
 - Recent Efforts in Photoproduction
- 3 Cascades at GlueX
 - Opportunities with Secondary K_L^0 Beams
- 4 Summary and Outlook



Summary and Outlook

Baryon Spectroscopy: Are we there, yet? Certainly not ...

New era in the spectroscopy of strange baryons (GlueX, LHCb, PANDA, ...)

- Mapping out the spectrum of Ξ baryons is the primary motivation (including parity measurements); some hope for peak hunting.
- Ground-state Ξ in $\gamma p \rightarrow KK \Xi$ will allow the spectroscopy of Σ^* / Λ^* states.

The multi-strange baryons provide a missing link between the light-flavor and the heavy-flavor baryons. Also:

- 1 Do the lightest excited Ξ states in certain partial waves decouple from the $\Xi\pi$ channel, confirming the flavor independence of confinement?
- 2 Ξ baryons as a probe of excited hadron structure?
 - Measurements of the isospin splittings in spatially excited Ξ states appear possible for the first time (similar to $n - p$ or $\Delta^0 - \Delta^{++}$).

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Backup Slides

SU(3) Flavor Symmetry

SU(3)_F symmetry is broken by the strange-light quark mass difference

→ Corrections in quark models are substantial

However:

- Some static properties, such as the masses of the baryons, are found to obey SU(3)_F symmetry:

$$\Delta m [N(1440) \frac{1}{2}^{+} - N(939) \frac{1}{2}^{+}] \approx \Delta m [\Lambda(1600) \frac{1}{2}^{+} - \Lambda(1115) \frac{1}{2}^{+}]$$

- Also some dynamic properties exhibit SU(3)_F symmetry:

- Similarity of near-threshold cross sections of the reactions $\pi^{-}p \rightarrow \eta n$ and $K^{-}p \rightarrow \eta \Lambda$ (S. Prakhov *et al.*, Phys. Rev. **C72**, 015203 (2005))
- Similarity in the Dalitz plots for the processes $\pi^{-}p \rightarrow \pi^0 \pi^0 n$ and $K^{-}p \rightarrow \pi^0 \pi^0 \Lambda$ (S. Prakhov *et al.*, Phys. Rev. **C69**, 042202 (2004))

SU(3) Flavor Symmetry: Implications

Conclusion:

Parallel members of different multiplets should exhibit a similar mass difference Δm .

→ Unfortunately, we cannot compare with any Ξ states because the $2^{\text{nd}} \Xi(?) P_{11}(J^P = \frac{1}{2}^+)$ has not been found, yet.

However, the $SU(3)_F$ symmetric basis may not be ideal:
 (Everything is strongly mixed.)

- Better choice (S. Capstick): “*uds*” basis where you (anti-)symmetrize only in *u, d* quark degrees of freedom.
 → Isospin much better symmetry than $SU(3)_F$.
- E.g.: $\phi_\Lambda = (ud - du)s/\sqrt{2}$ $\phi_\Sigma = uus, (ud + du)s/\sqrt{2}, dds$
 In Ξ states, symmetrize only in *ss* pair: $\phi_\Xi = ssu, ssd$