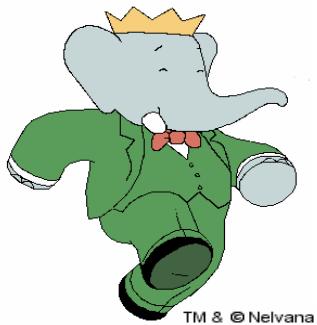


HYPERON & HYPERON RESONANCE PROPERTIES FROM CHARM BARYON DECAYS AT BABAR

Veronique Ziegler ~ The University of Iowa



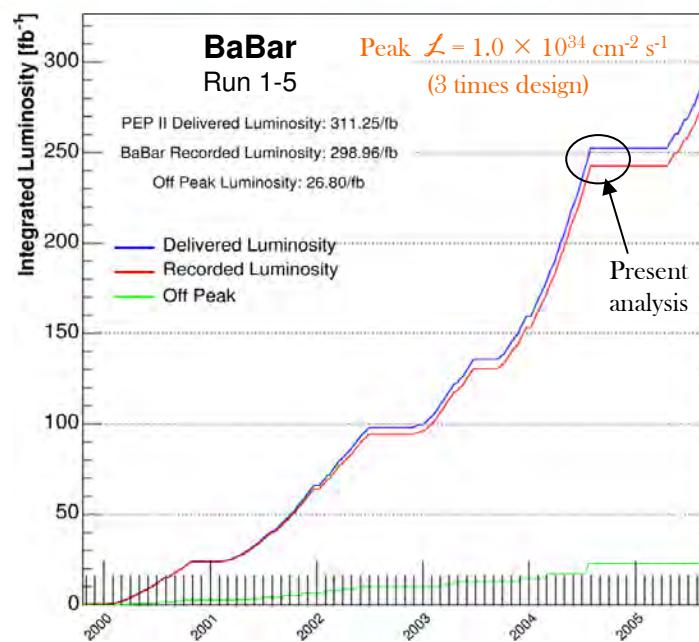
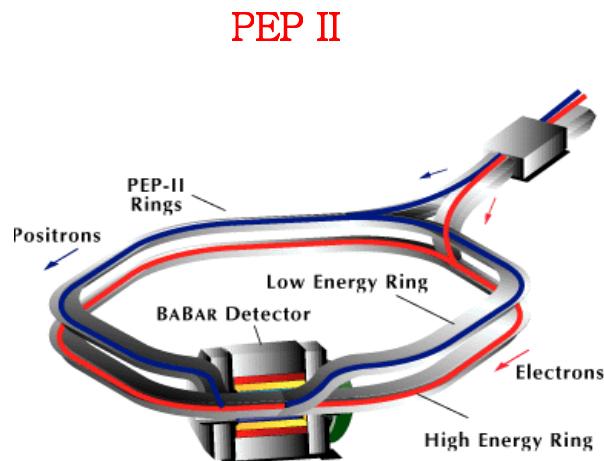
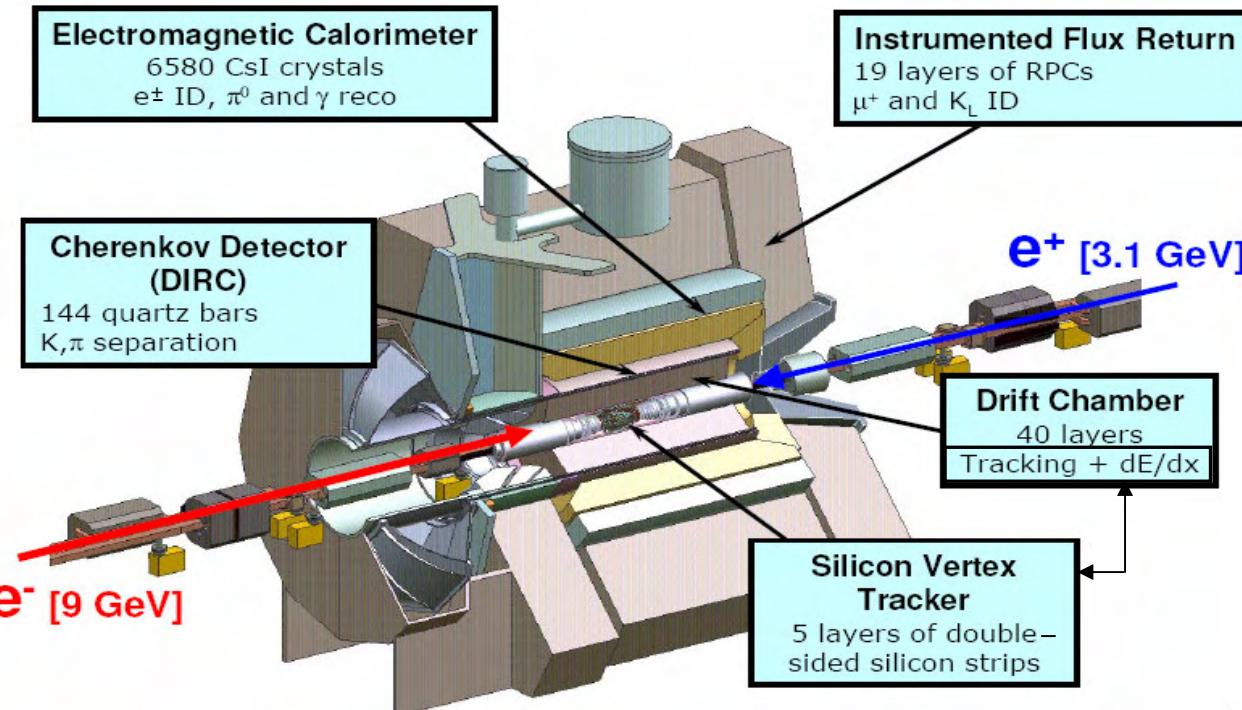
Cascade Workshop
Jefferson Lab, Dec 1 – 3, 2005

OVERVIEW

1. Introduction
 - PEP II and BaBar
2. Spin of the Ω^- from $\Xi_c^0 \rightarrow \Omega^- K^+$ and $\Omega_c^0 \rightarrow \Omega^- \pi^+$
3. Analysis of Λ_c^+ 3-Body Decays:
 - $\Lambda_c^+ \rightarrow (\Xi^- \pi^+) K^+$; the $\Xi^*(1530)$
 - $\Lambda_c^+ \rightarrow (\Lambda^0 \bar{K}^0) K^+$; the $\Xi^*(1690)$
4. Analysis of $\Xi_c^{+,0}$ 3-Body Decays:
 - $\Xi_c^+ \rightarrow (\Xi^- \pi^+) \pi^+$
 - $\Xi_c^+ \rightarrow (\Lambda^0 \bar{K}^0) \pi^+$ (if time permits)
 - $\Xi_c^0 \rightarrow (\Lambda^0 K^-) \pi^+$ (if time permits)
5. Summary

Note: (i) All results are (very) preliminary (analyses are ongoing & numbers are going to change)
(ii) Charge conjugation is implied throughout unless indicated otherwise [$e^+e^- \Rightarrow$ anti-baryon/baryon ratio ~ 1] 2

PEP II AND THE BABAR DETECTOR



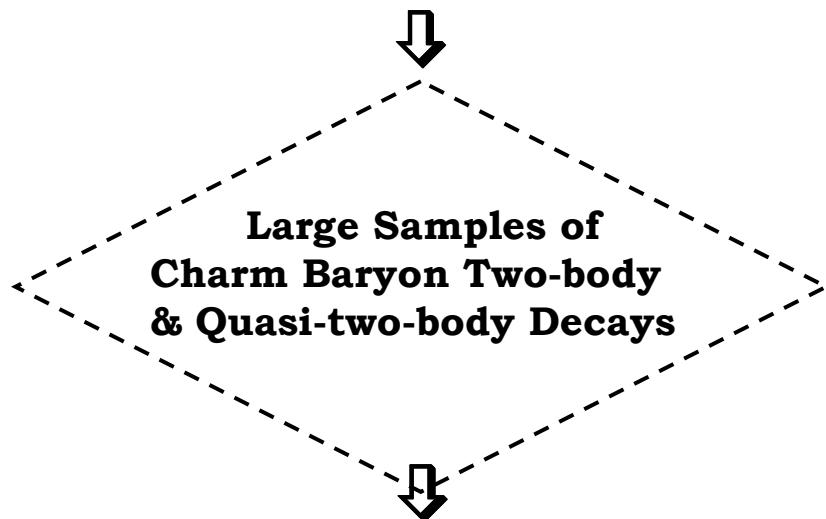
- ➡ 8 months shutdown
- ✳ Data-taking has resumed

BaBar as a Charm Baryon Factory

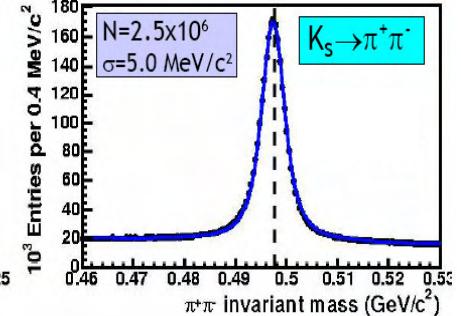
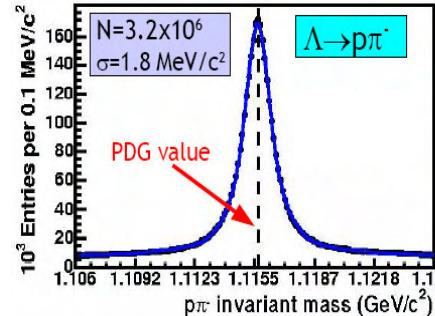
Present data sample contains:

- * > 300 M $Y(4S) \rightarrow B\bar{B}$ events
- * > 900 M $e^+e^- \rightarrow q\bar{q}$ events
- ↳ > 400 M $e^+e^- \rightarrow c\bar{c}$ events

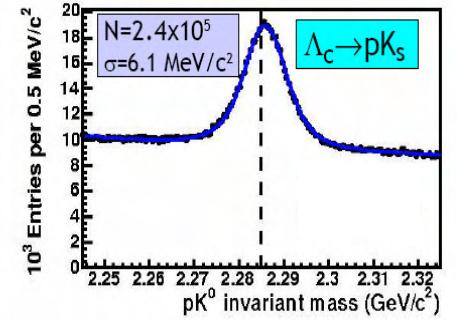
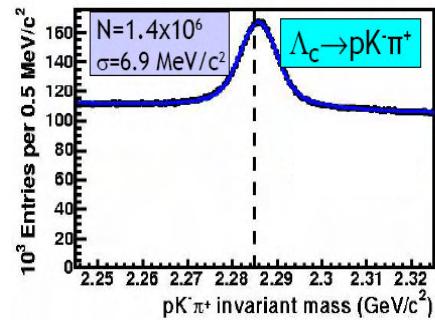
⇒ Charm Baryon (& Meson) Factory



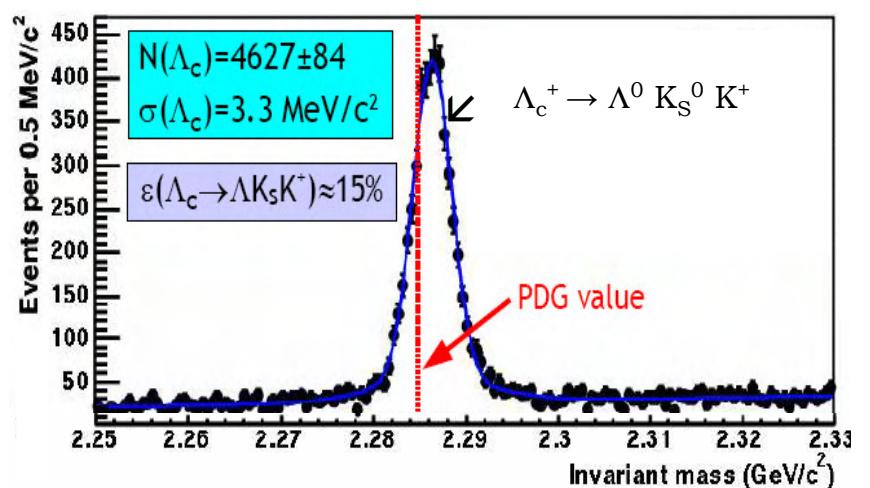
Excellent resolution



High statistics



Good statistics in rare decay modes



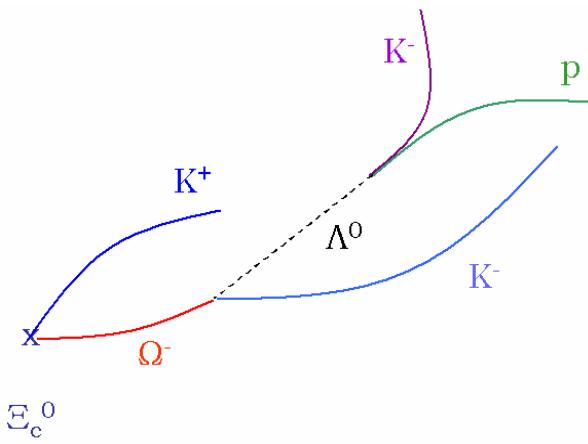
Ref. PRD 72, 052006 (2005) [Λ_c^+ Precision Mass Measurement] 4

The Ω^- Spin measured

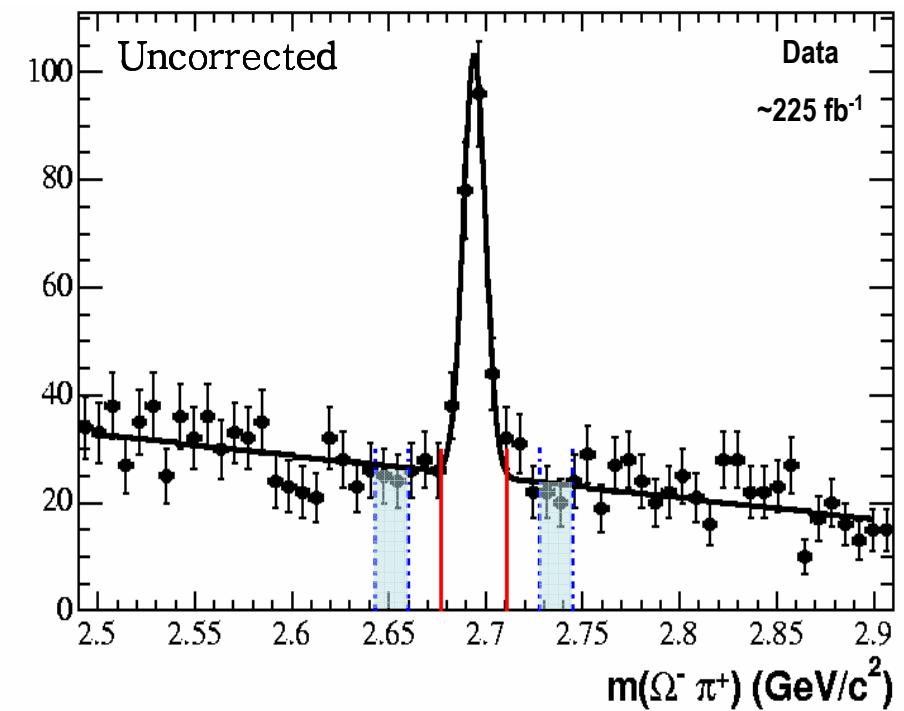
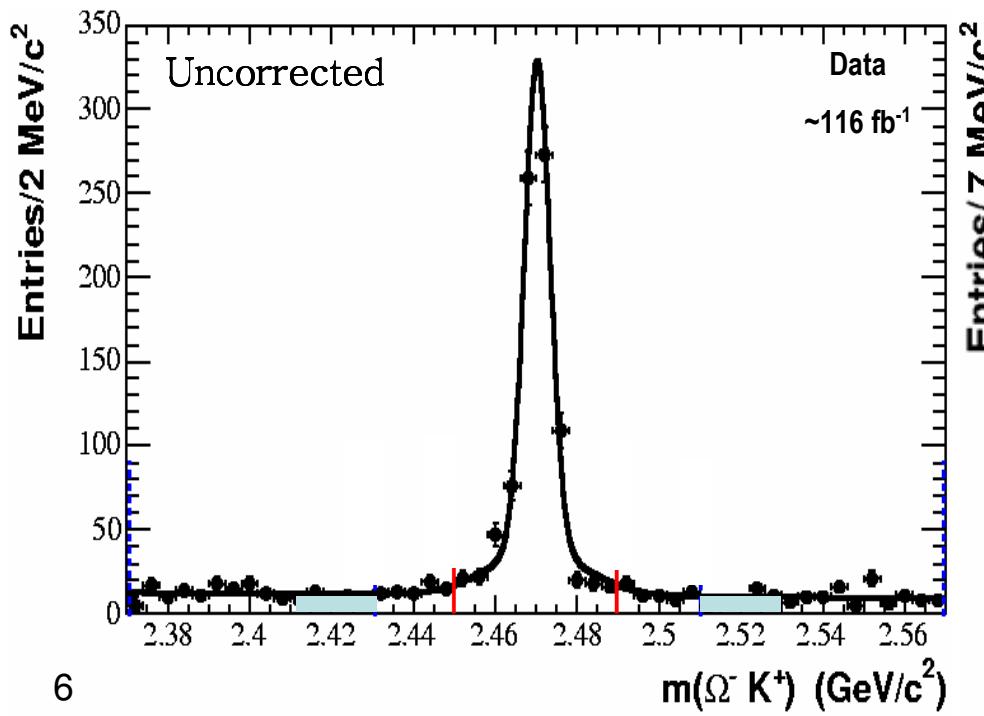
- from $\Xi_c^0 \rightarrow \Omega^- K^+$ decays
 - from $\Omega_c^0 \rightarrow \Omega^- \pi^+$ decays
-
- The present analyses *ASSUME* that the Λ_c^+ , $\Xi_c^{+,0}$ and the Ω_c^0 have spin 1/2.
 - We *MAY* be able to extend the present analyses to establish this.
 - Any ideas, suggestions, etc. concerning this would be most welcome!

Invariant Mass Distributions for

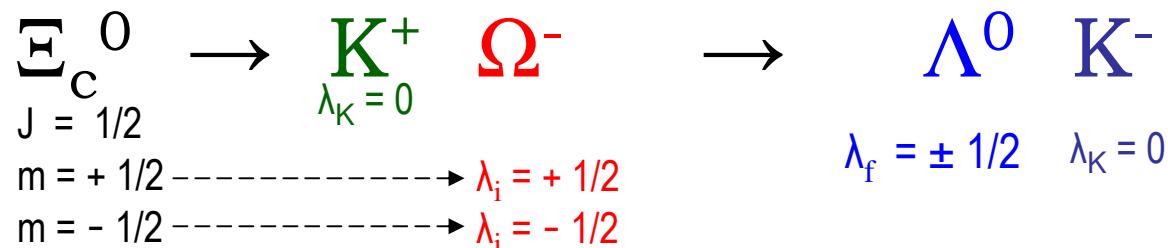
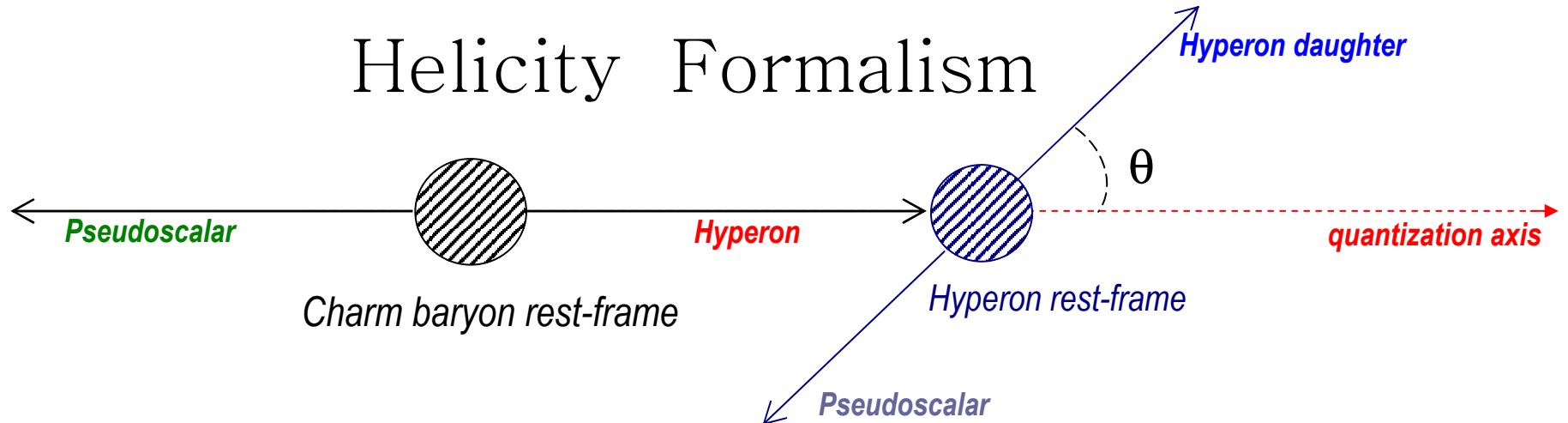
$\Xi_c^0 \rightarrow \Omega^- K^+$ and $\Omega_c^0 \rightarrow \Omega^- \pi^+$



- PID Information
 - Proton
 - Kaon
 - π^+, π^-
- { dE/dx & Cherenkov info (DIRC) }
- 3- σ mass cut on intermediate states
- intermd. state *mass-constrained* [Λ, Ω]
- $p^*(\Omega_c^0) > 2.25 \text{ GeV}/c$ [reduces background]
- $L_\Lambda > +1.5 \text{ mm}$ [sign \Leftrightarrow outgoing].
- $r_\Omega > +2.0 \text{ mm}$ [sign \Leftrightarrow outgoing].



Helicity Formalism



- ☞ $J(\Xi_c^0) = 1/2 \Rightarrow$ in Ξ_c^0 rest-frame [$m = \pm 1/2$] along z (quantization) axis
 - ☞ no angular momentum projection w.r.t. quantization axis $\Rightarrow \Omega^-$ helicity, $\lambda_i = \pm 1/2$
 - ☞ final state helicity $\lambda_f = \lambda_f(\Lambda^0) - \lambda_f(\text{pseudoscalar}) = \pm 1/2$
 - ☞ Decay amplitude for $\Omega^- \rightarrow \Lambda^0 K^-$: $A_{\lambda_i \lambda_f}^J = D_{\lambda_i \lambda_f}^{J*}(\phi, \theta, 0) A_{\lambda_f}$ ← Does not depend on λ_i
[Wigner-Eckart theorem]

→ Total Intensity: $I \propto \frac{1}{2} \sum_{\lambda_i, \lambda_f} \rho_i \left| A_{\lambda_i \lambda_f}^J \right|^2 = \frac{1}{2} \sum_{\lambda_i, \lambda_f} \rho_i \left| D_{\lambda_i \lambda_f}^{J^*}(\phi, \theta, 0) A_{\lambda_f} \right|^2$

↑ density matrix element for Ω^- spin projection i
= density matrix element for charm baryon parent

Helicity Formalism (2)

$$\begin{aligned}
 I &\propto \frac{1}{2} \sum_{\substack{\lambda_i = \pm 1/2, \\ \lambda_f = \pm 1/2}} \rho_i \left| D_{\lambda_i \lambda_f}^{J^*}(\phi, \theta, 0) A_{\lambda_f} \right|^2 \\
 &\propto \frac{1}{2} |A_{1/2}|^2 \left[\rho_{1/2} \left| D_{1/2 1/2}^{J^*}(\phi, \theta, 0) \right|^2 + \rho_{-1/2} \left| D_{-1/2 1/2}^{J^*}(\phi, \theta, 0) \right|^2 \right] \\
 &+ \frac{1}{2} |A_{-1/2}|^2 \left[\rho_{1/2} \left| D_{1/2 -1/2}^{J^*}(\phi, \theta, 0) \right|^2 + \rho_{-1/2} \left| D_{-1/2 -1/2}^{J^*}(\phi, \theta, 0) \right|^2 \right] \\
 &\propto \frac{1}{2} |A_{1/2}|^2 \left[\rho_{1/2} \left| d_{1/2 1/2}^J(\theta) \right|^2 + \rho_{-1/2} \left| d_{-1/2 1/2}^J(\theta) \right|^2 \right] \\
 &+ \frac{1}{2} |A_{-1/2}|^2 \left[\rho_{1/2} \left| d_{1/2 -1/2}^J(\theta) \right|^2 + \rho_{-1/2} \left| d_{-1/2 -1/2}^J(\theta) \right|^2 \right]
 \end{aligned}$$

$$D_{\lambda_i \lambda_f}^{J^*}(\phi, \theta, 0) = e^{i\phi} d_{\lambda_i \lambda_f}^J(\theta)$$

Define $\beta = (\rho_{1/2} - \rho_{-1/2}) \left[\frac{|A_{1/2}|^2 - |A_{-1/2}|^2}{|A_{1/2}|^2 + |A_{-1/2}|^2} \right]$

$\left(\frac{\rho_{1/2} - \rho_{-1/2}}{\rho_{1/2} + \rho_{-1/2}} \right) \neq 0$ (where $\rho_{1/2} + \rho_{-1/2} = 1$) \rightarrow possible since Ξ_c^0 decay violates parity conservation.

$\left[\frac{|A_{1/2}|^2 - |A_{-1/2}|^2}{|A_{1/2}|^2 + |A_{-1/2}|^2} \right] \neq 0$ \rightarrow possible since Ω^- decay violates parity conservation.

$\Rightarrow I \propto 1 + \beta \cos \theta$ J=1/2

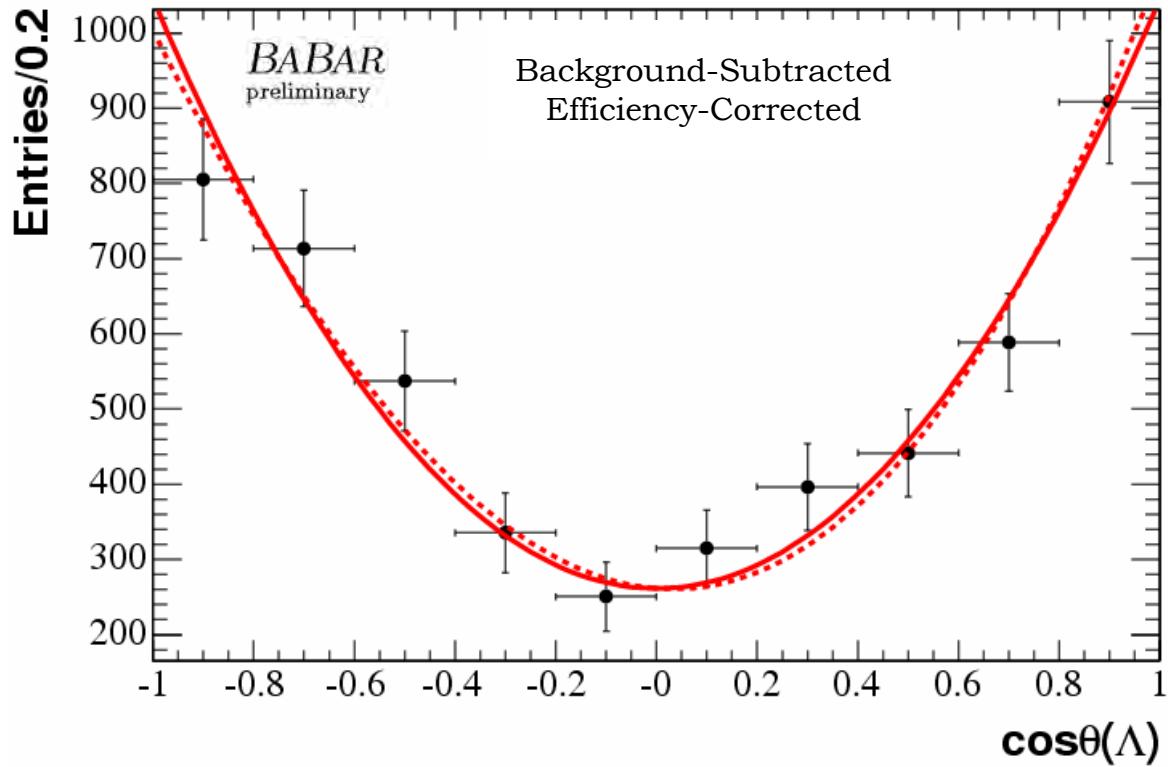
$\Rightarrow I \propto \frac{1}{4} (1 + 3 \cos^2 \theta + \beta \cos \theta (9 \cos^2 \theta - 5))$ J=3/2

c.f. E. Fermi et. al., PR 85, 936 (1952)
 π & p elastic scattering ($\beta = 0$)
 $J=1/2 \Rightarrow$ flat, $J=3/2 \Rightarrow 1 + 3 \cos^2 \theta$

$\Rightarrow I \propto \frac{1}{4} (1 - 2 \cos^2 \theta + 5 \cos^4 \theta + \beta \cos \theta (25 \cos^4 \theta - 26 \cos^2 \theta + 5))$ J=5/2

Spin measurement of Ω^- from $\Xi_c^0 \rightarrow \Omega^- K^+$, $\Omega^- \rightarrow \Lambda^0 K^-$ decays

Angular Distribution Parametrizations for $J_\Omega=3/2$ hypothesis



Negligible Decay Asymmetry Parameter
 $\beta = 0.04 \pm 0.06$

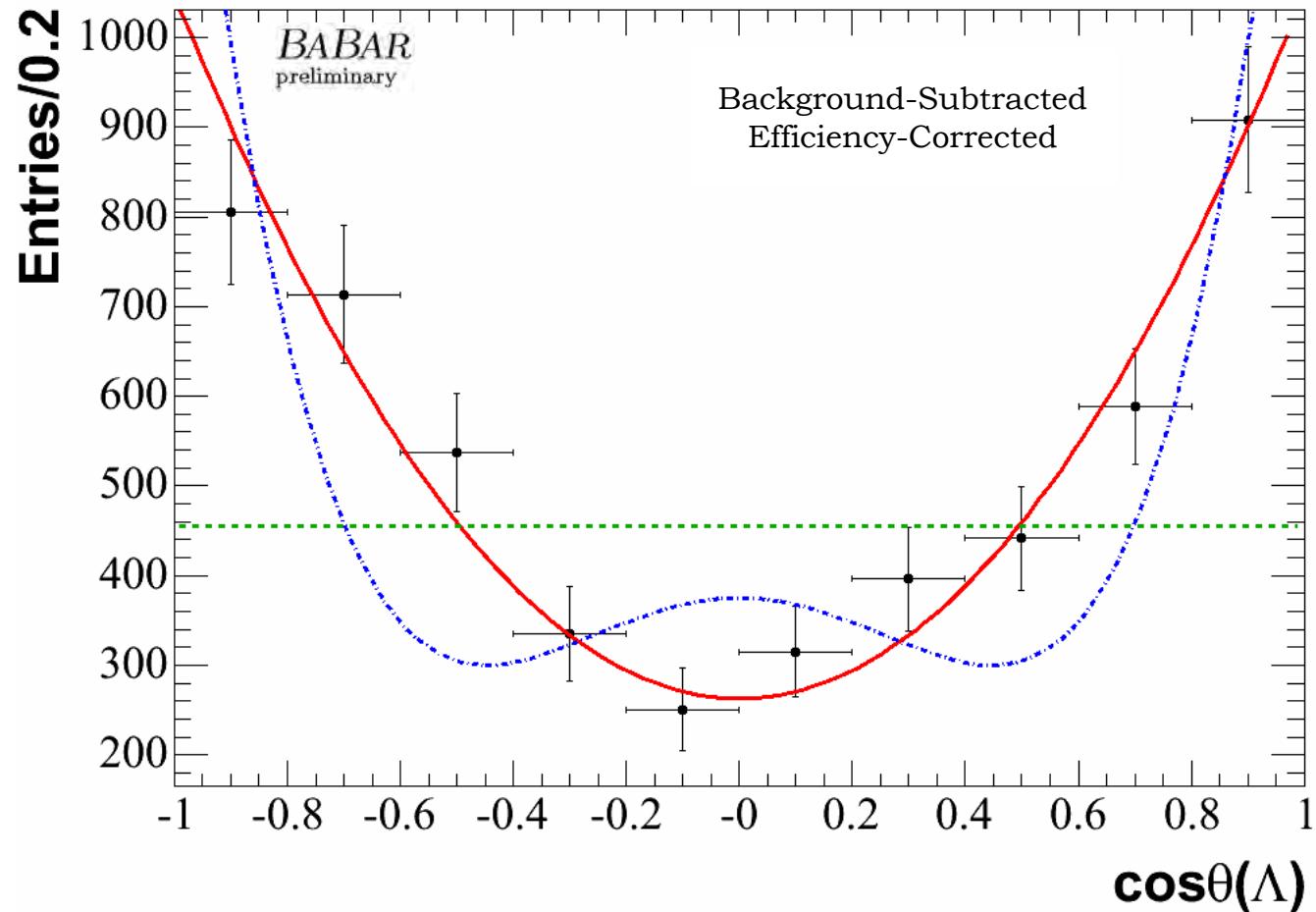
$$I \propto \frac{1}{4} (1 + 3 \cos^2 \theta)$$

No Asymmetry
 $\beta = 0$

$$I \propto \frac{1}{4} (1 + 3 \cos^2 \theta + \beta \cos \theta (9 \cos^2 \theta - 5))$$

Asymmetry
Fit for $\beta \rightarrow \beta = 0.04 \pm 0.06$

Spin measurement of Ω^- from $\Xi_c^0 \rightarrow \Omega^- K^+$, $\Omega^- \rightarrow \Lambda^0 K^-$ decays

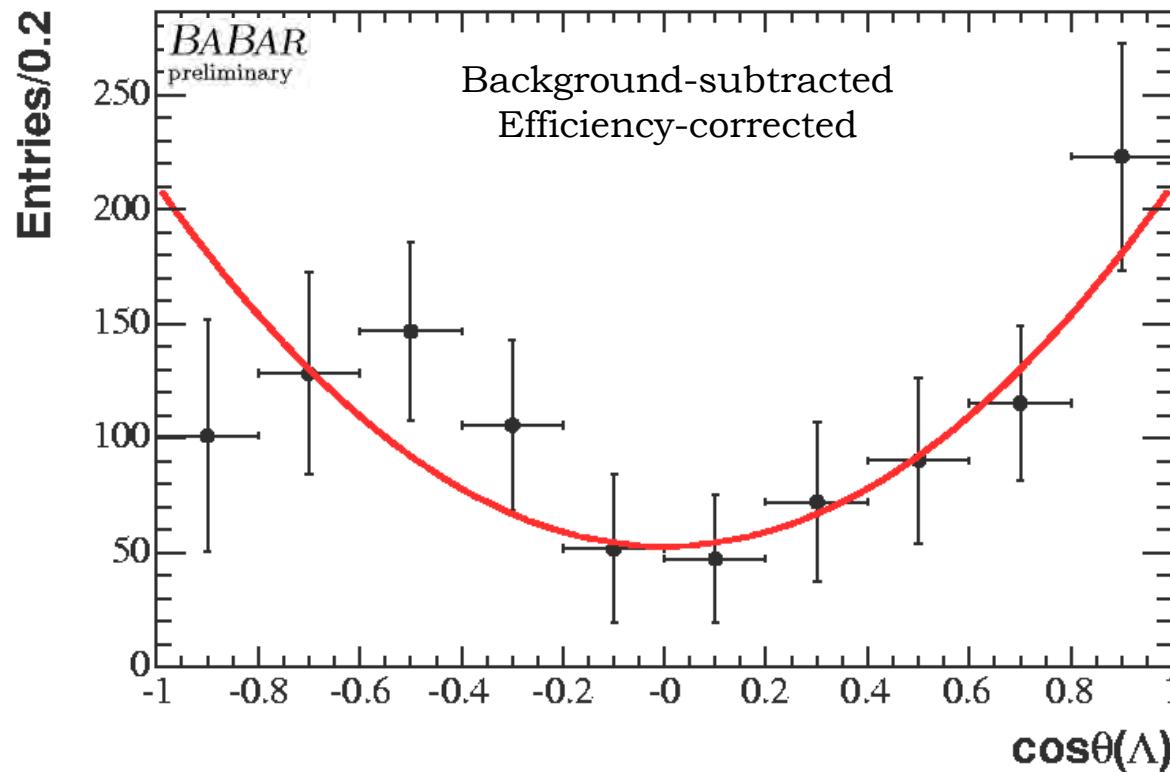


- | | | |
|------------------------|---|-------------------------------------|
| $J_\Omega = 1/2$ | $\Rightarrow I \propto 1$ | \rightarrow Fit Prob = 10^{-17} |
| — $J_\Omega = 3/2$ | $\Rightarrow I \propto (1+3\cos^2\theta)$ | \rightarrow Fit Prob = 0.64 |
| - - - $J_\Omega = 5/2$ | $\Rightarrow I \propto (1-2\cos^2\theta+5\cos^4\theta)$ | \rightarrow Fit Prob = 10^{-7} |

Spin measurement of Ω_c^0 from $\Omega_c^0 \rightarrow \Omega^- \pi^+$, $\Omega^- \rightarrow \Lambda^0 K^-$ decays

Fit parametrization $\alpha(1 + 3 \cos^2\theta)$ for $J_\Omega = 3/2$ hypothesis

→ Fit Prob = 0.69; $J(\Omega^-) = 1/2$ & $J(\Omega^-) = 5/2$ **consistent** with results from $\Xi_c^0 \rightarrow \Omega^- \pi^+$



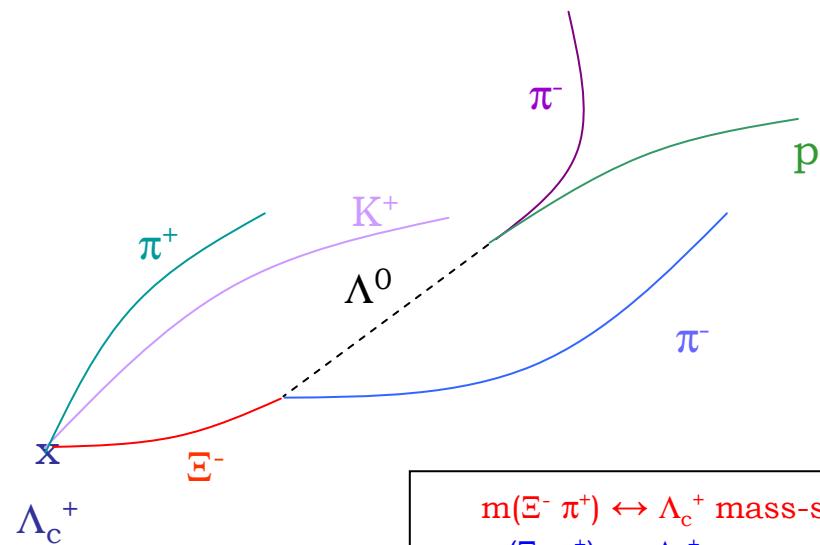
Conclusion: $J(\Omega^-) = 3/2$ [Assuming $J(\Xi_c^0) = J(\Omega_c^0) = 1/2$]

Extending the Spin Formalism to 3-body Decays

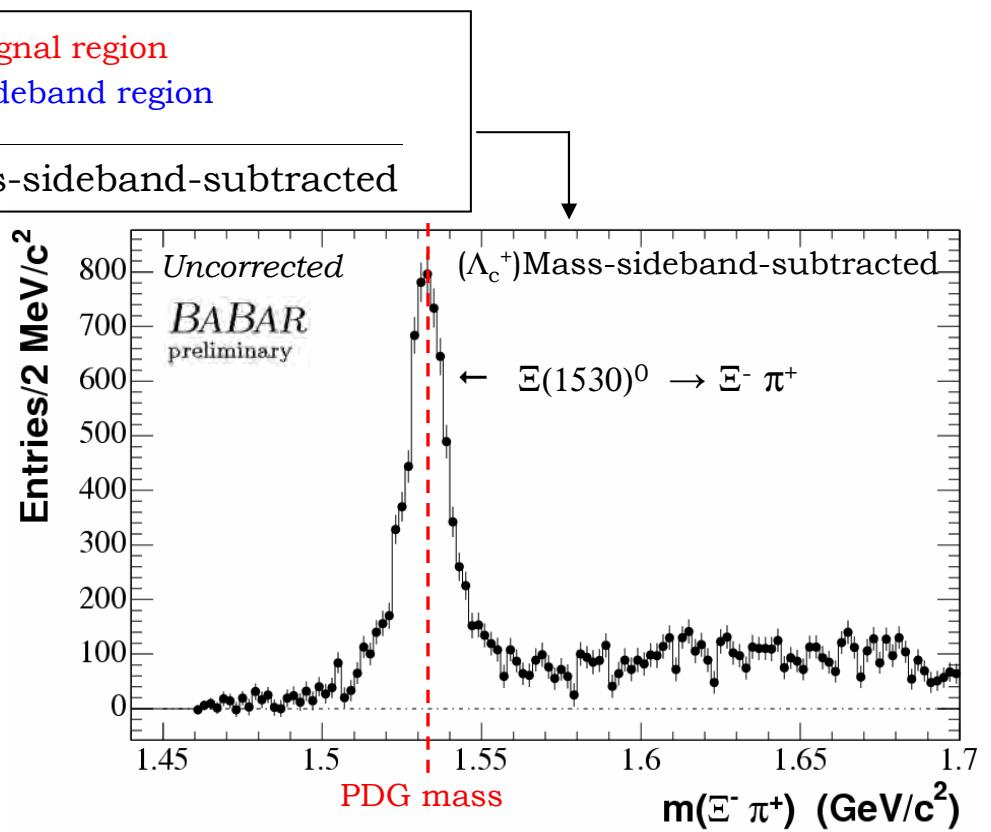
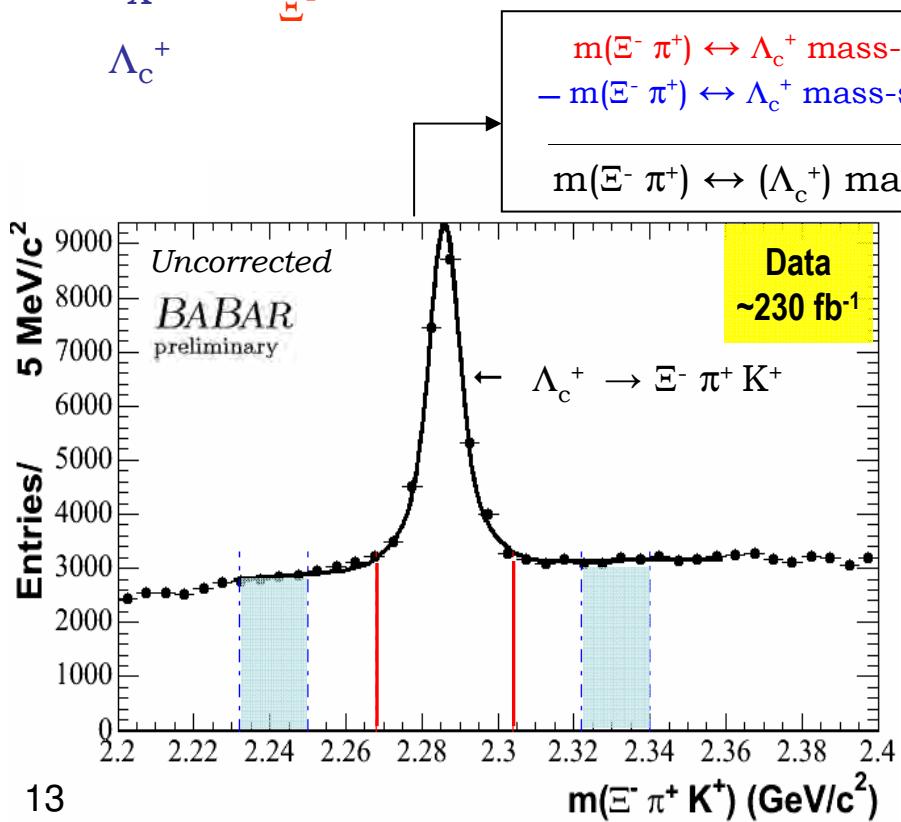
- The $\Xi(1530)^0$ Spin from $\Lambda_c^+ \rightarrow (\Xi^- \pi^+) K^+$
 - also mass, width info.
 - amplitude analysis (to be done)
- The $\Xi(1690)^0$ Spin from $\Lambda_c^+ \rightarrow (\Lambda^0 K_S^0) K^+$
 - also mass, width info.
 - amplitude analysis (to be done)
 - $(\Xi^- \pi^+)/(\Lambda \bar{K}^0)$ Branching Ratio Limit
(to be done)

“...nothing of significance on Ξ resonances has been added since our 1988 edition.” [PDG(2004), p 967]

Reconstructed $\Lambda_c^+ \rightarrow \Xi^- \pi^+ K^+$, $\Xi^- \rightarrow \Lambda^0 \pi^-$ Events



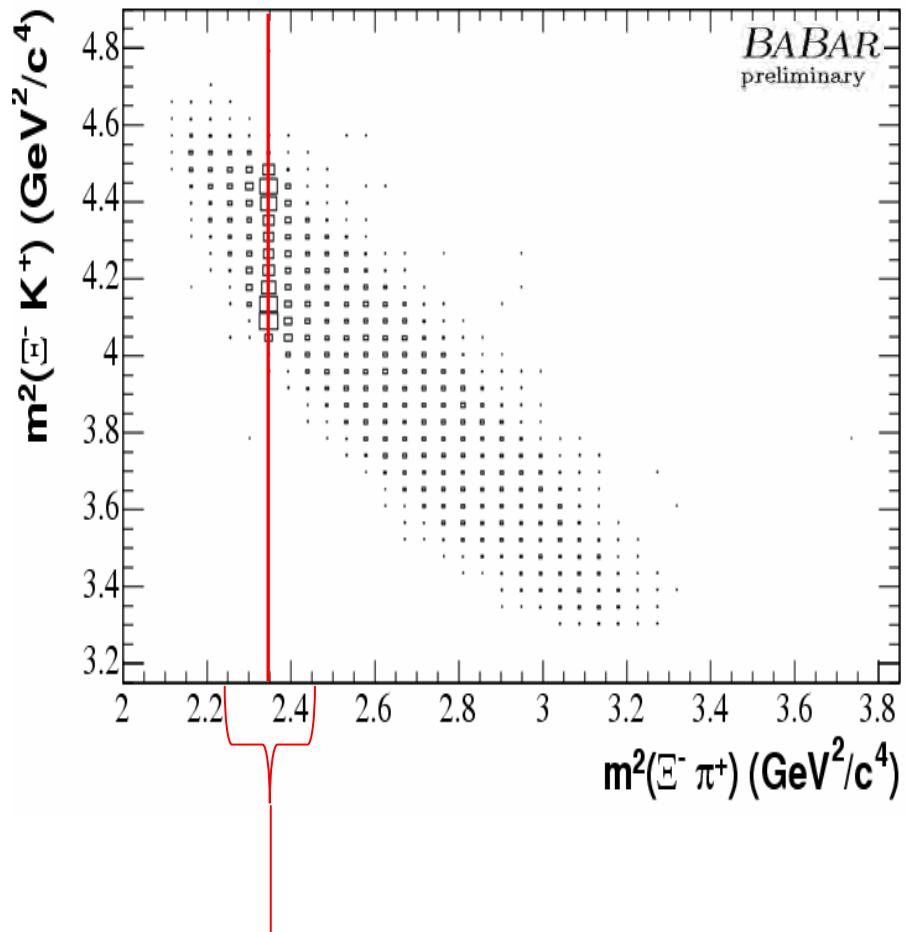
- PID Information
 - Proton
 - Kaon
 - π^+, π^-
- dE/dx & Cherenkov info (DIRC)
- 3- σ mass cut on intermediate states
- intermd. states *mass-constrained* [Λ , Ξ]
- $L_\Lambda > +1.5$ mm [*sign* $\not\Rightarrow$ outgoing].
- $r_\Xi > +1.5$ mm [*sign* $\not\Rightarrow$ outgoing].



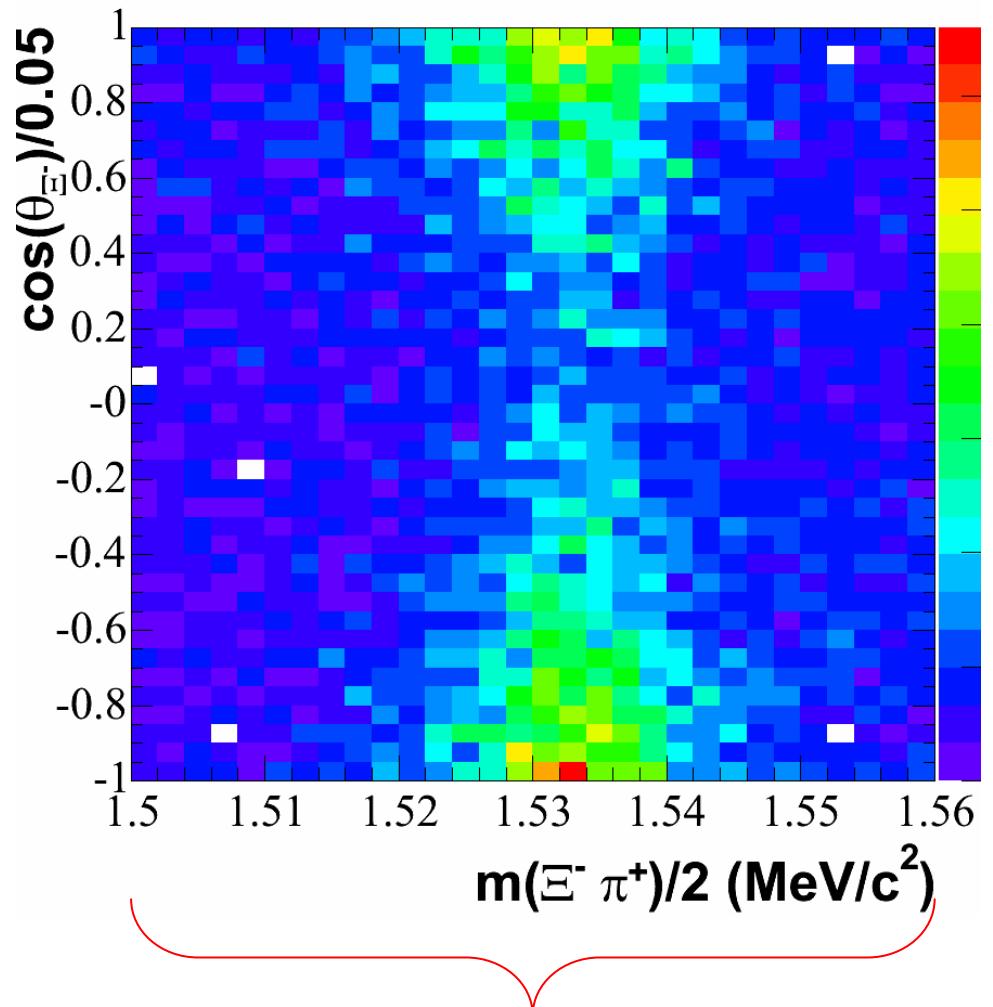
Resonant Structures in $\Lambda_c^+ \rightarrow \Xi^- \pi^+ K^+$, $\Xi^- \rightarrow \Lambda^0 \pi^-$ Events

Only ***obvious*** structure:

$$\Xi(1530)^0 \rightarrow \Xi^- \pi^+$$

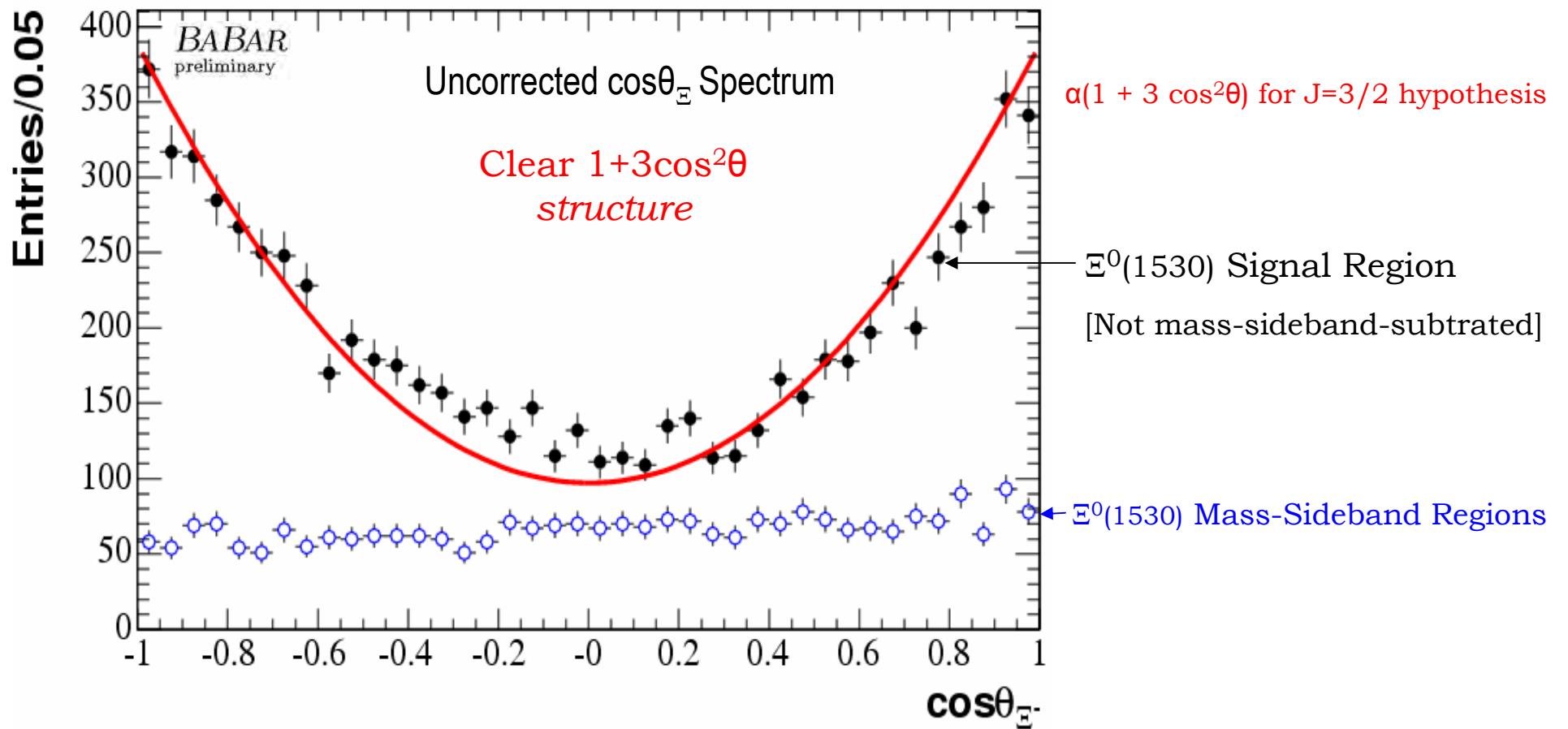


[$\Lambda_c^+ \rightarrow \Xi^- \pi^+ K^+$ signal region]



Spin measurement of $\Xi^0(1530)$ from $\Lambda_c^+ \rightarrow \Xi^0(1530) K^+$, $\Xi^0(1530) \rightarrow \Xi^- \pi^+$ decays

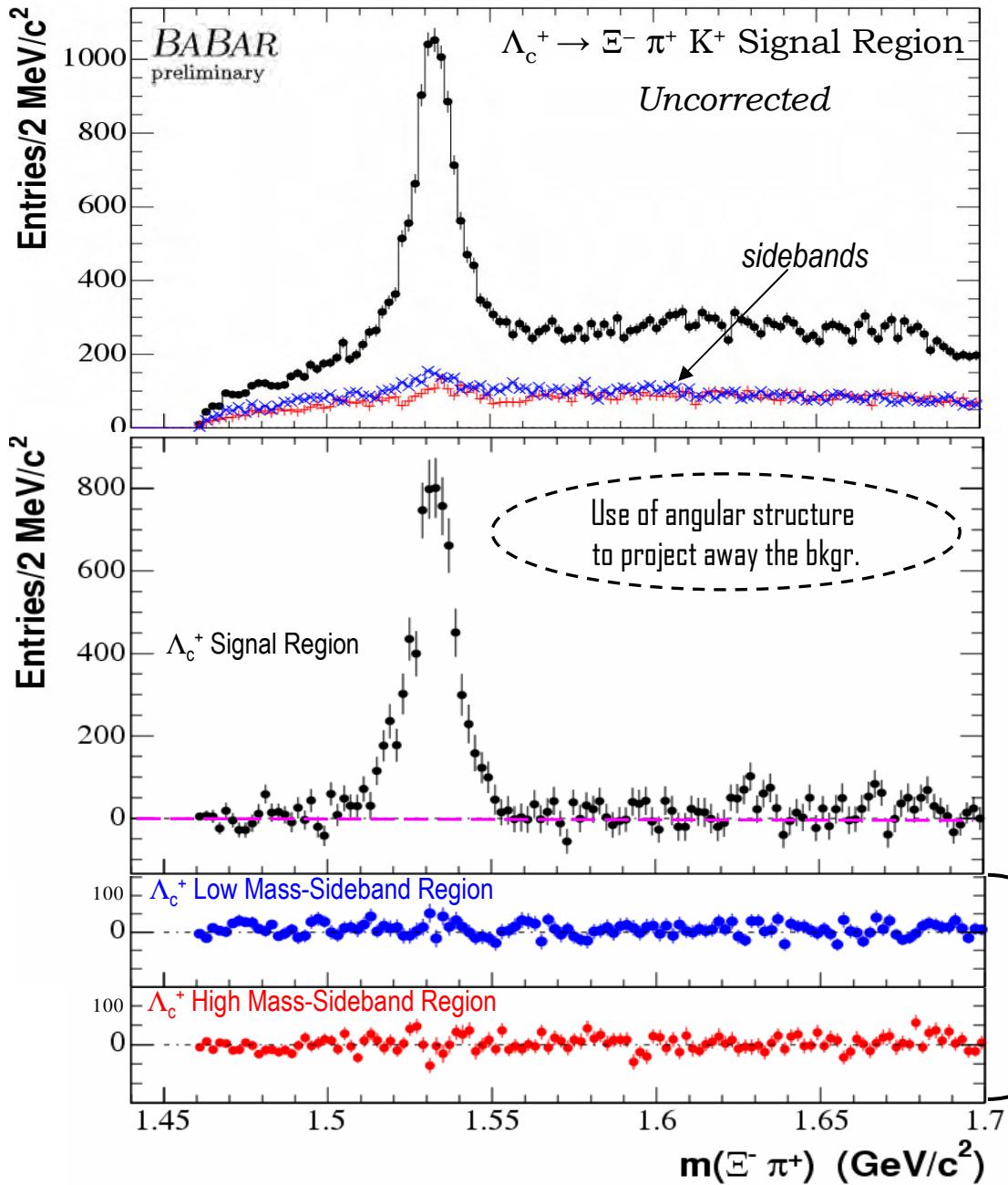
$\Lambda_c^+ \rightarrow \Xi^- \pi^+ K^+$



Skewed distribution due to:

- Efficiency loss at small angles → Not big effect
- $(\Xi^- \pi^+)$ system decay asymmetry → S-P wave interference (next slides)

Using the angular structure of $\Xi(1530)^0 \rightarrow \Xi^- \pi^+ \text{ candidates to project away background events}$



For pure spin 3/2:

$$dN/d\cos\theta = \alpha(1 + 3\cos^2\theta)$$

\Downarrow

Legendre polynomials orthogonality condition

\Downarrow

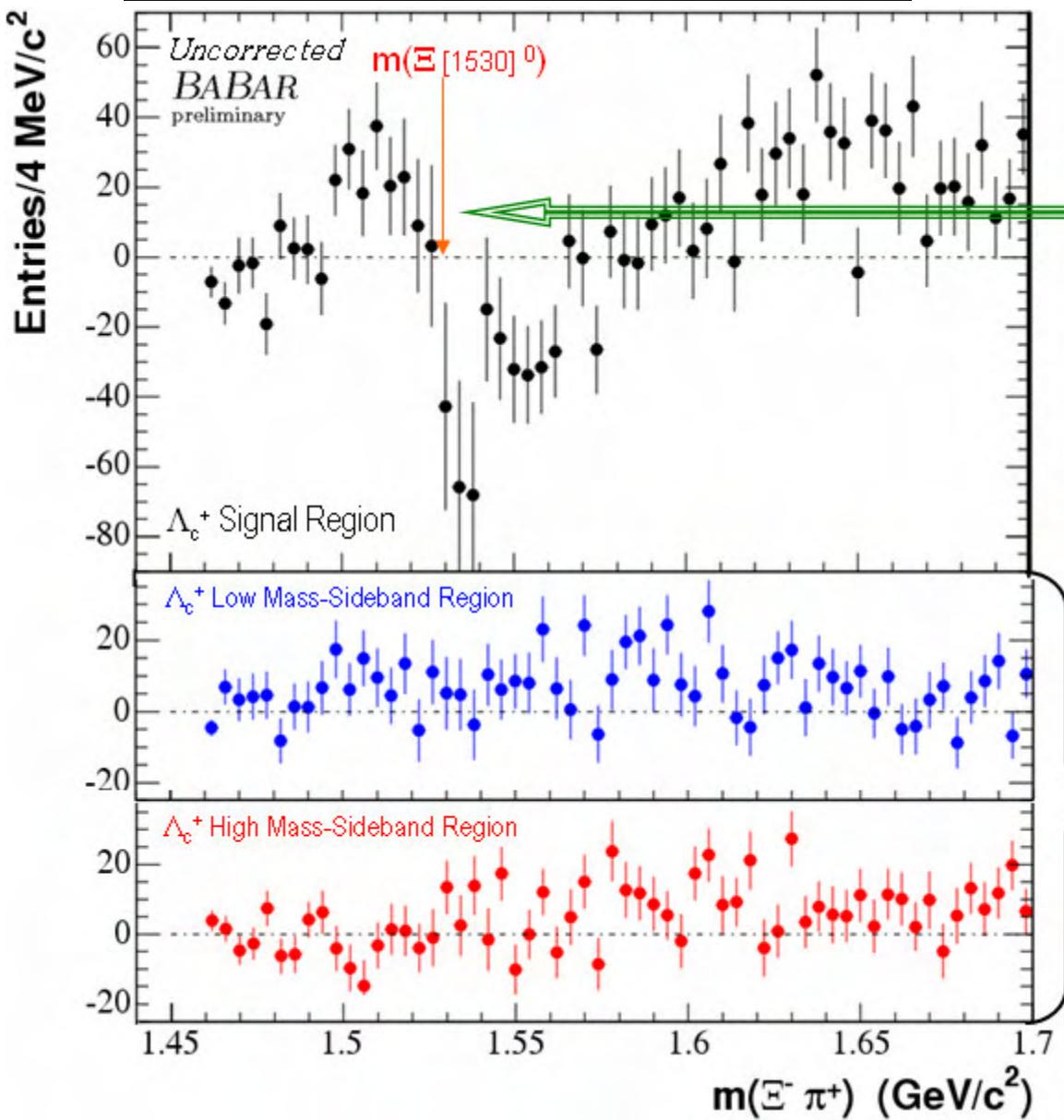
$$\text{Weight} = N \times P_2(\cos\theta)$$

Projects mass distribution having $\cos^2\theta$ component

\Rightarrow No $\cos^2\theta$ component in sideband distributions

Evidence of S-P wave interference in the ($\Xi^- \pi^+$) system produced in the decay $\Lambda_c^+ \rightarrow \Xi^- \pi^+ K^+$

$m(\Xi^- \pi^+)$ distribution weighted by $P_1(\cos\theta)$:



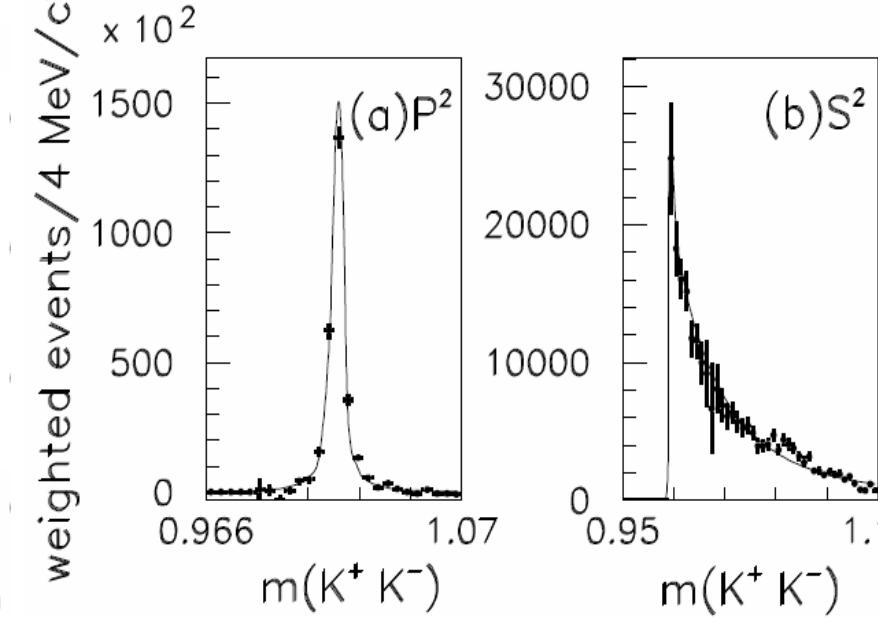
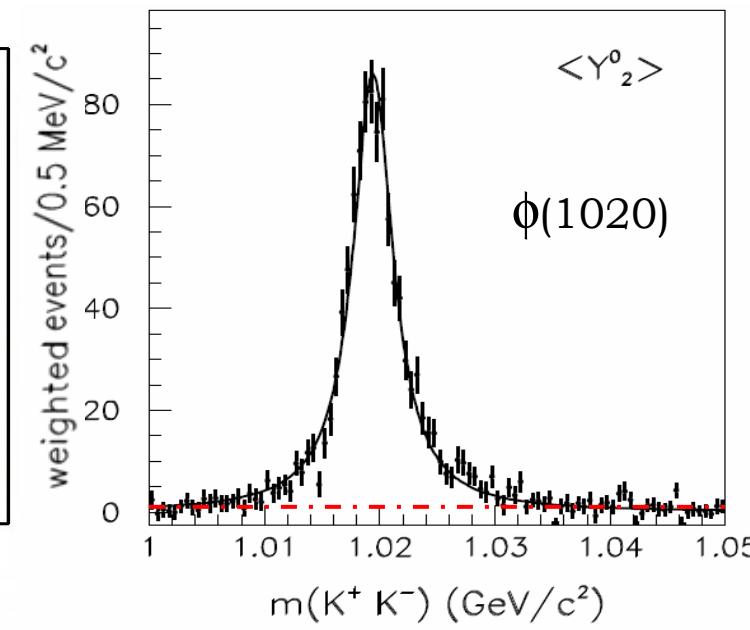
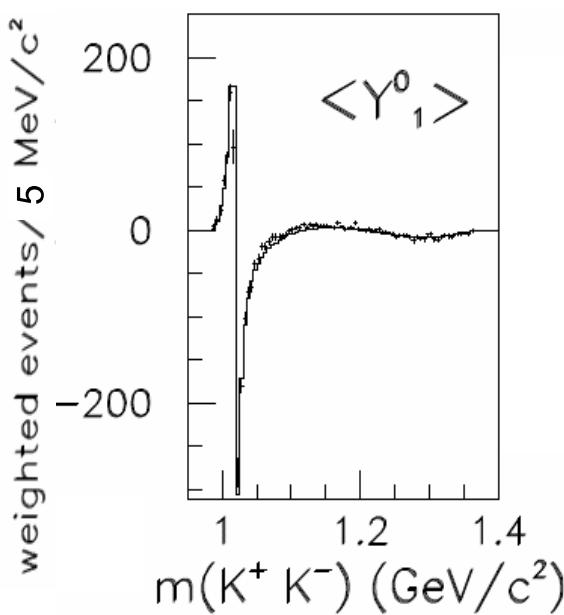
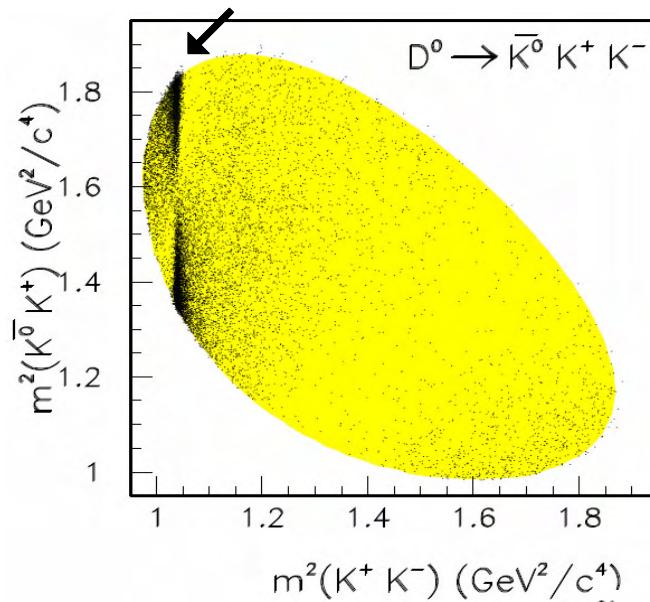
Classic S-P wave interference pattern as a function of $m(\Xi^- \pi^+)$

- Oscillation due to *rapid* Breit-Wigner P-wave phase motion and *slowly* varying S-wave phase. E.g. $D^0 \rightarrow \bar{K}^0 K^+ K^-$ [PRD72, 052008(2005)] (next slide)
- First clear *indication* of $\Xi(1530)^0$ Breit-Wigner phase motion
- ⇒ No structure; non-zero because of efficiency dependence on $\cos\theta$ (probably; to be confirmed)

$D^0 \rightarrow \bar{K}^0 (K^+ K^-)$ from BaBar

[PRD72, 052008(2005)]

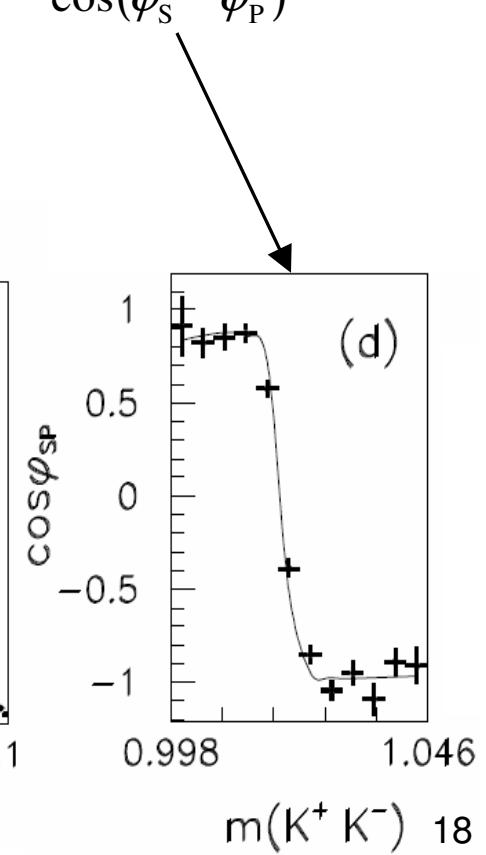
S-P interference
→ large asymmetry



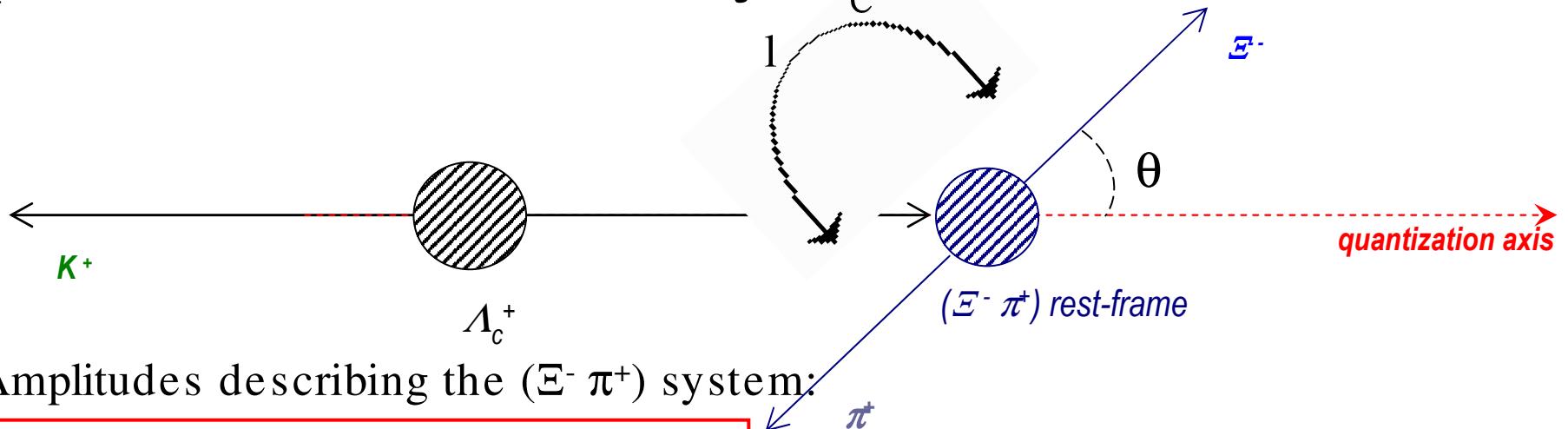
Amplitude Analysis of :

$\langle Y_0^0 \rangle$, $\langle Y_1^0 \rangle$, and $\langle Y_2^0 \rangle$

$\rightarrow |S|$, $|P|$
and
 $\cos(\varphi_S - \varphi_P)$



S-P wave description of the ($\Xi^- \pi^+$) system produced in the decay $\Lambda_c^+ \rightarrow \Xi^- \pi^+ K^+$



Amplitudes describing the ($\Xi^- \pi^+$) system:

$$S_{\lambda_f} \Leftrightarrow l=0, j=1/2 \quad \eta_{S_l} = (-1)^{l+1} = -1$$

$$P_{\lambda_f}^- \Leftrightarrow l=1, j=l-1/2=1/2 \quad \eta_{P_l^-} = (-1)^{l+1} = +1$$

$$P_{\lambda_f}^+ \Leftrightarrow l=1, j=l+1/2=3/2 \quad \eta_{P_l^+} = (-1)^{l+1} = +1$$

$$\Rightarrow \text{Total Intensity} \sim \sum_{\substack{\lambda_i=\pm 1/2, \\ \lambda_f=\pm 1/2}} \rho_i \left| D_{\lambda_i \lambda_f}^{1/2*}(\phi, \theta, 0) S_{\lambda_f} + D_{\lambda_i \lambda_f}^{1/2*}(\phi, \theta, 0) P_{\lambda_f}^- + D_{\lambda_i \lambda_f}^{3/2*}(\phi, \theta, 0) P_{\lambda_f}^+ \right|^2$$

ρ_i ($i = \pm 1/2$) \rightarrow density matrix elements describing the spin population of the Λ_c^+

where, λ_i = helicity of $(\Xi^- \pi^+)$ system = $\lambda_i(\Lambda_c^+)$

$$\lambda_f = \lambda_{\Xi^-} - \lambda_{\pi^+} = \lambda_{\Xi^-}$$

Helicity Formalism (3)

$$\begin{aligned}
I &\propto \sum_{\substack{\lambda_i = \pm 1/2, \\ \lambda_f = \pm 1/2}} \rho_i \left| D_{\lambda_i \lambda_f}^{1/2*}(\phi, \theta, 0) S_{\lambda_f} + D_{\lambda_i \lambda_f}^{1/2*}(\phi, \theta, 0) P_{\lambda_f}^- + D_{\lambda_i \lambda_f}^{3/2*}(\phi, \theta, 0) P_{\lambda_f}^+ \right|^2 \quad \text{where } \lambda_f = \lambda_{\Xi^-} \\
&= \rho_{1/2} \left(\left| d_{1/2 1/2}^{1/2}(\theta) S_{1/2} + d_{1/2 1/2}^{1/2}(\theta) P_{1/2}^- + d_{1/2 1/2}^{3/2}(\theta) P_{1/2}^+ \right|^2 + \left| d_{1/2 -1/2}^{1/2}(\theta) S_{-1/2} + d_{1/2 -1/2}^{1/2}(\theta) P_{-1/2}^- + d_{1/2 -1/2}^{3/2}(\theta) P_{-1/2}^+ \right|^2 \right) \\
&+ \rho_{-1/2} \left(\left| d_{-1/2 1/2}^{1/2}(\theta) S_{1/2} + d_{-1/2 1/2}^{1/2}(\theta) P_{1/2}^- + d_{-1/2 1/2}^{3/2}(\theta) P_{1/2}^+ \right|^2 + \left| d_{-1/2 -1/2}^{1/2}(\theta) S_{-1/2} + d_{-1/2 -1/2}^{1/2}(\theta) P_{-1/2}^- + d_{-1/2 -1/2}^{3/2}(\theta) P_{-1/2}^+ \right|^2 \right)
\end{aligned}$$

Parity conservation :

$$S_{-\lambda_f} = \eta_S \eta_\Xi \eta_\pi (-1)^{j-S_\Xi-S_\pi} S_{\lambda_f} = S_{\lambda_f} \quad (\eta_\Xi = +1, \eta_\pi = -1; j = 1/2, S_\Xi = 1/2, S_\pi = 0)$$

$$P_{-\lambda_f}^- = \eta_P \eta_\Xi \eta_\pi (-1)^{j-S_\Xi-S_\pi} P_{\lambda_f}^- = -P_{\lambda_f}^- \quad (j = 1/2); \quad P_{-\lambda_f}^+ = \eta_P \eta_\Xi \eta_\pi (-1)^{j-S_\Xi-S_\pi} P_{\lambda_f}^+ = P_{\lambda_f}^+ \quad (j = 3/2)$$

$$\begin{cases} S_{-1/2} = S_{1/2} \\ P_{-1/2}^- = -P_{-1/2}^+ \\ P_{-1/2}^+ = P_{1/2}^+ \end{cases}$$

$$\begin{aligned}
&= \frac{1}{2} \rho_{1/2} \left(\left| d_{1/2 1/2}^{1/2}(\theta) S_{1/2} + d_{1/2 1/2}^{1/2}(\theta) P_{1/2}^- + d_{1/2 1/2}^{3/2}(\theta) P_{1/2}^+ \right|^2 + \left| d_{1/2 -1/2}^{1/2}(\theta) S_{-1/2} - d_{1/2 -1/2}^{1/2}(\theta) P_{-1/2}^- + d_{1/2 -1/2}^{3/2}(\theta) P_{-1/2}^+ \right|^2 \right) \\
&+ \frac{1}{2} \rho_{-1/2} \left(\left| d_{-1/2 1/2}^{1/2}(\theta) S_{1/2} + d_{-1/2 1/2}^{1/2}(\theta) P_{1/2}^- + d_{-1/2 1/2}^{3/2}(\theta) P_{1/2}^+ \right|^2 + \left| d_{-1/2 -1/2}^{1/2}(\theta) S_{-1/2} - d_{-1/2 -1/2}^{1/2}(\theta) P_{-1/2}^- + d_{-1/2 -1/2}^{3/2}(\theta) P_{-1/2}^+ \right|^2 \right)
\end{aligned}$$

Assume ~ 0 to extract $\cos\theta$

$$\Rightarrow I \propto (\rho_{1/2} + \rho_{-1/2}) \left[|S_{1/2}|^2 + |P_{1/2}^-|^2 + |P_{1/2}^+|^2 \left(\frac{1 + 3\cos^2\theta}{4} \right) + 2 \operatorname{Re}(S_{1/2} P_{1/2}^{+*}) \cos\theta \right]$$

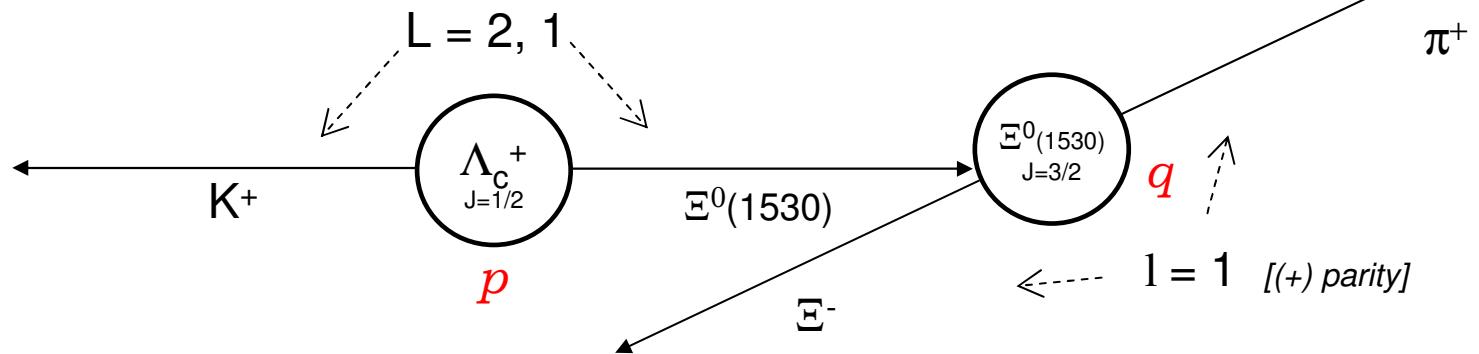
S-P interference

$$+ 2(\rho_{1/2} - \rho_{-1/2}) \left[\operatorname{Re}(S_{1/2} P_{1/2}^{-*}) \cos\theta + \operatorname{Re}(S_{1/2} P_{1/2}^{+*}) \left(\frac{3\cos^2\theta - 1}{2} \right) \right].$$

0

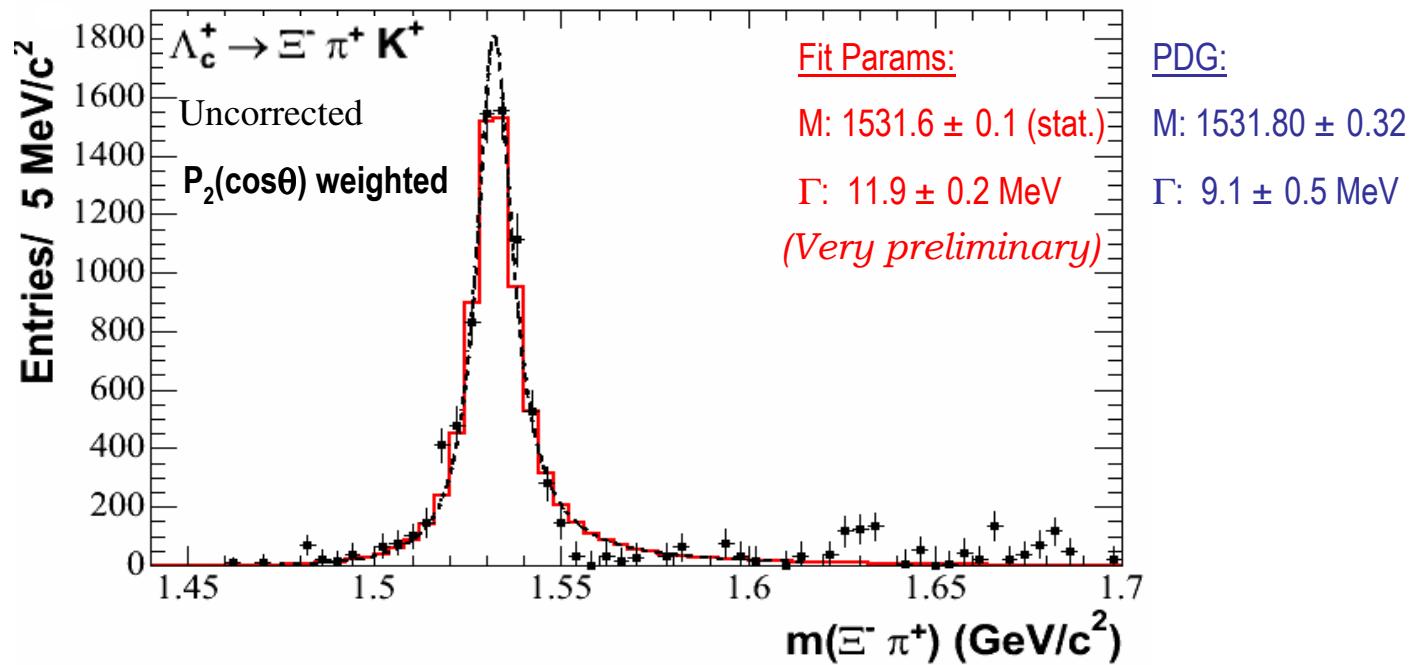
(Assume $\rho_{1/2} = \rho_{-1/2}$)

...towards a measurement of the mass & width of $\Xi^0(1530)$

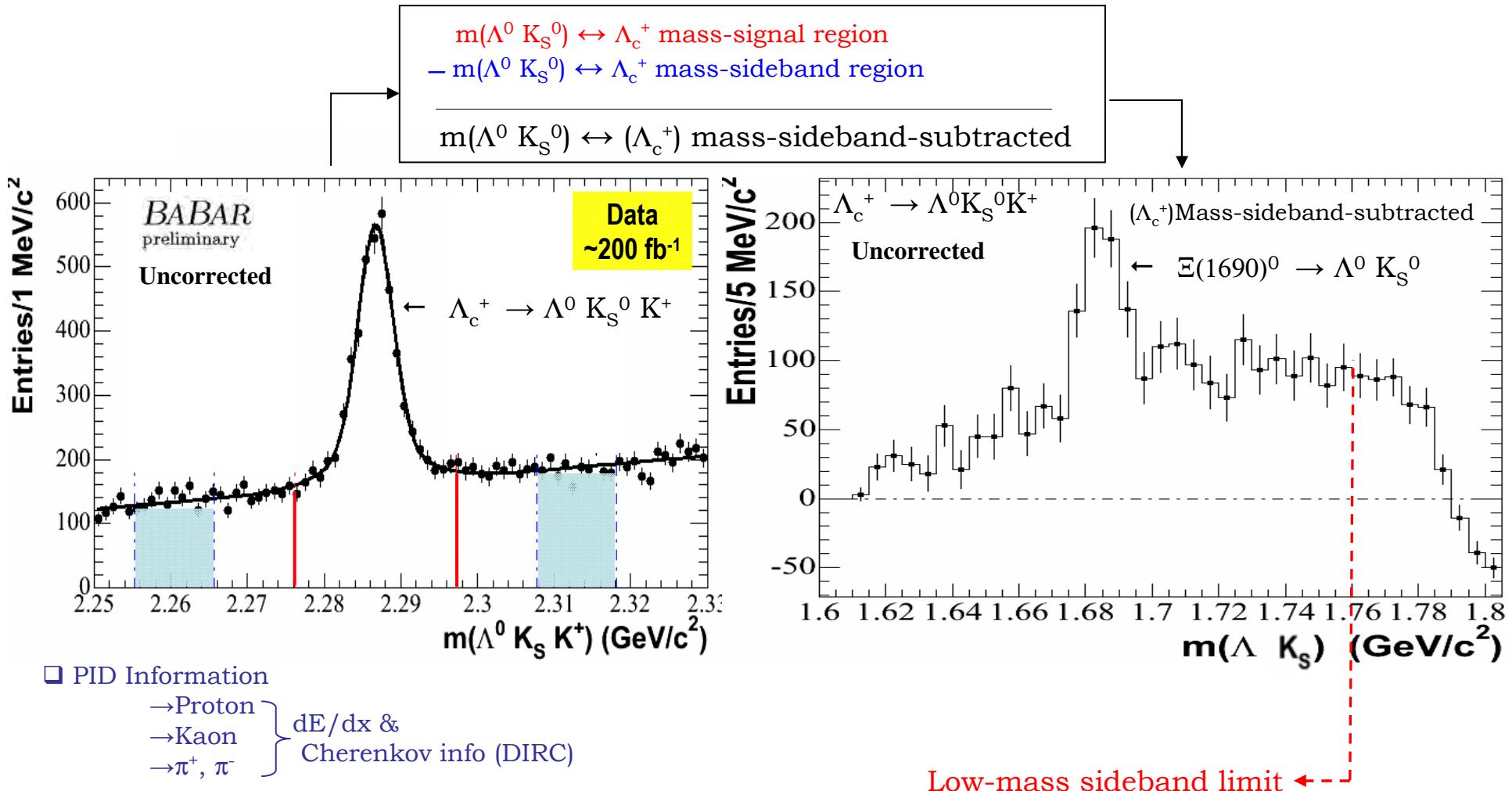


Fit with relativistic Breit-Wigner Function with $L=2$ & $l=1$
 [incorporating a Blatt-Weisskopf barrier factor ($R \sim 5 (\text{GeV})^{-1}$) and resolution “smearing”]

$$\frac{dN}{dm} = m \left(\frac{\mathbf{p}}{m_{\Lambda_c}} \frac{\mathbf{q}}{m} \right) (\mathbf{p})^{2L} \frac{1}{(m_0^2 - m^2)^2 + m_0^2 \Gamma_{tot}^2(m)} (\mathbf{q})^{2l}$$

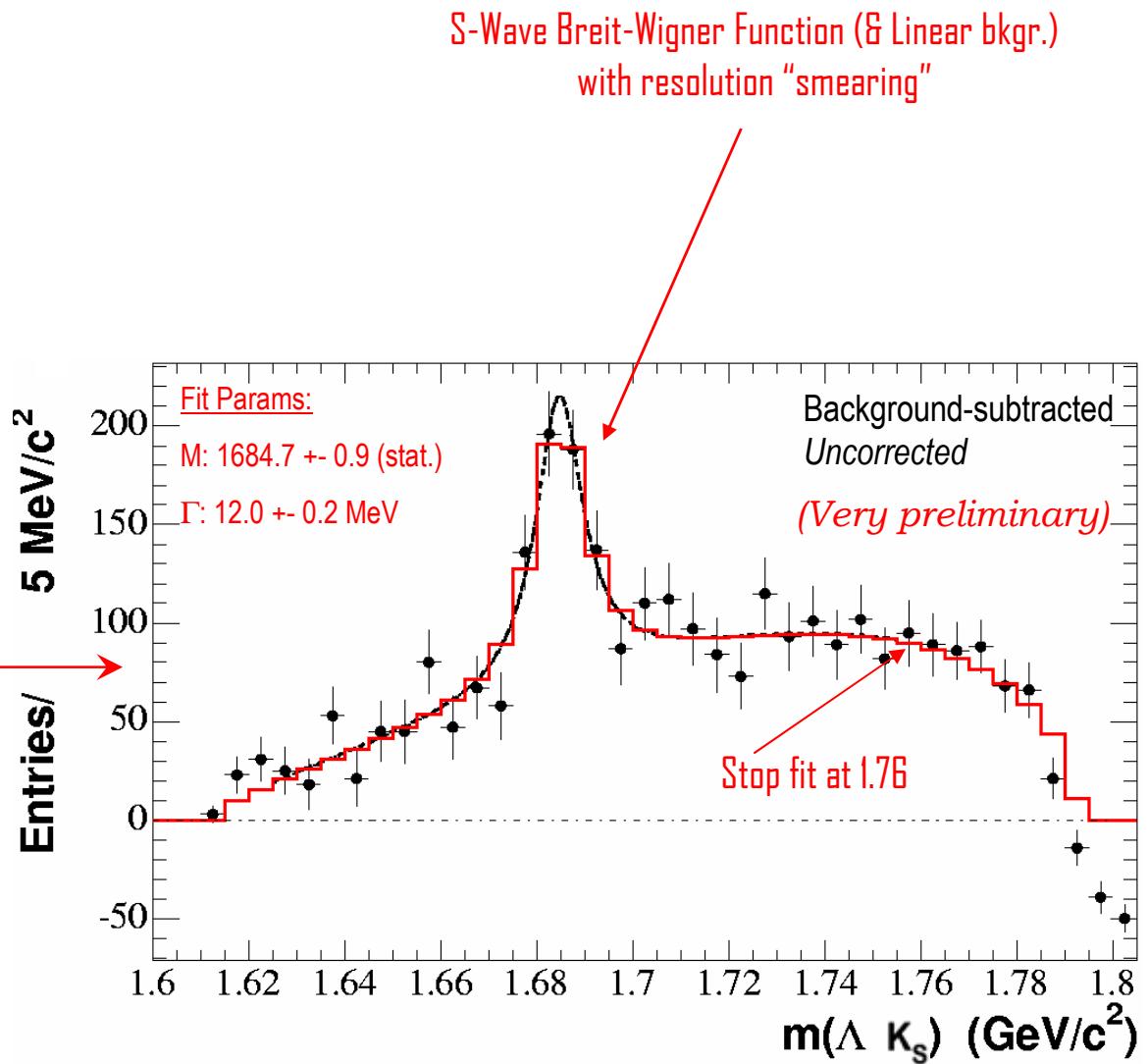
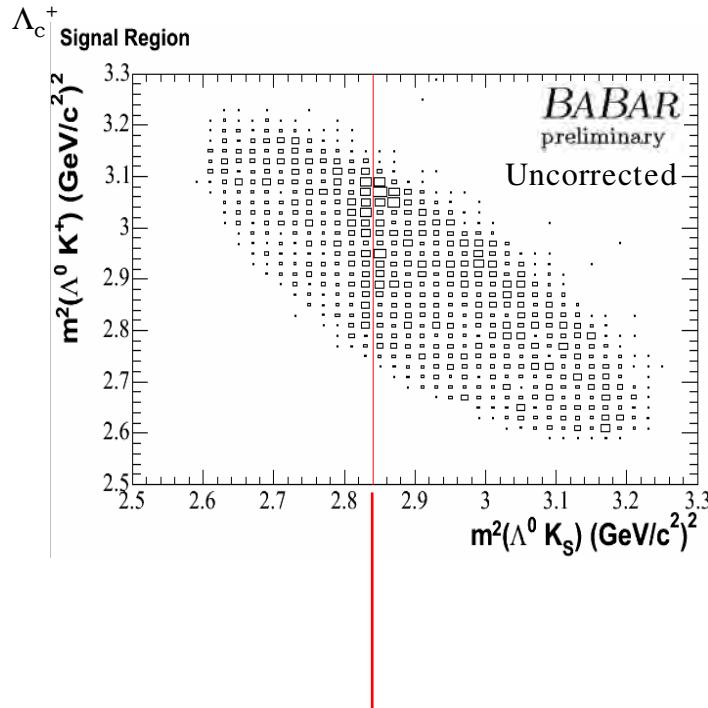


Reconstructed $\Lambda_c^+ \rightarrow \Lambda^0 K_S^0 K^+$ Events

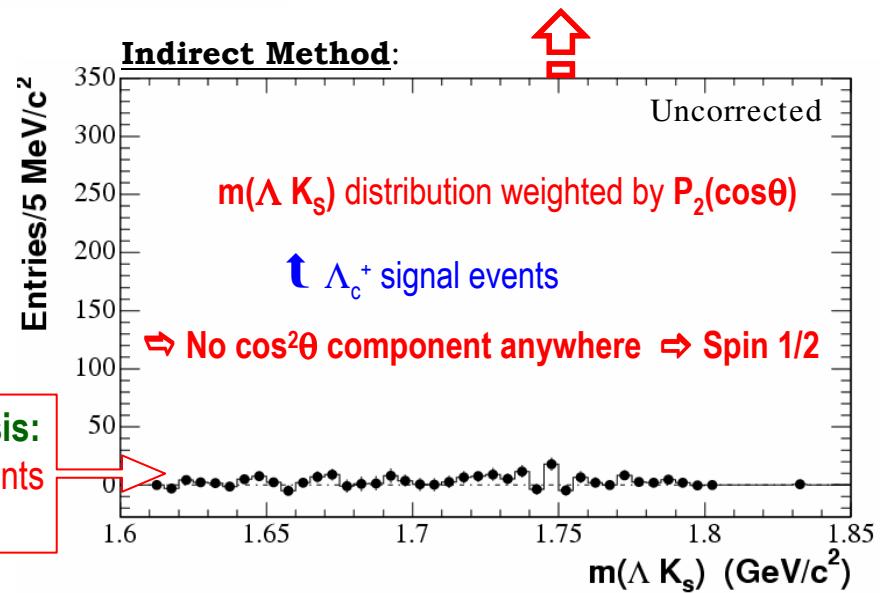
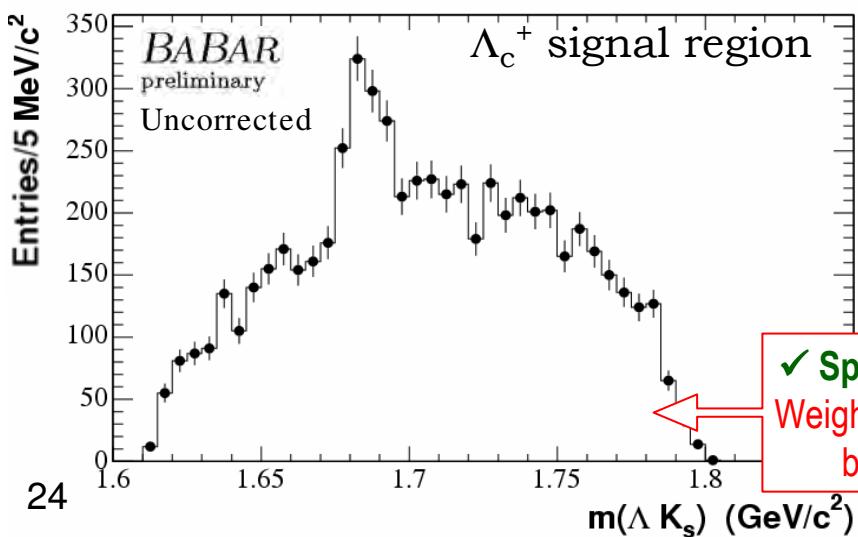
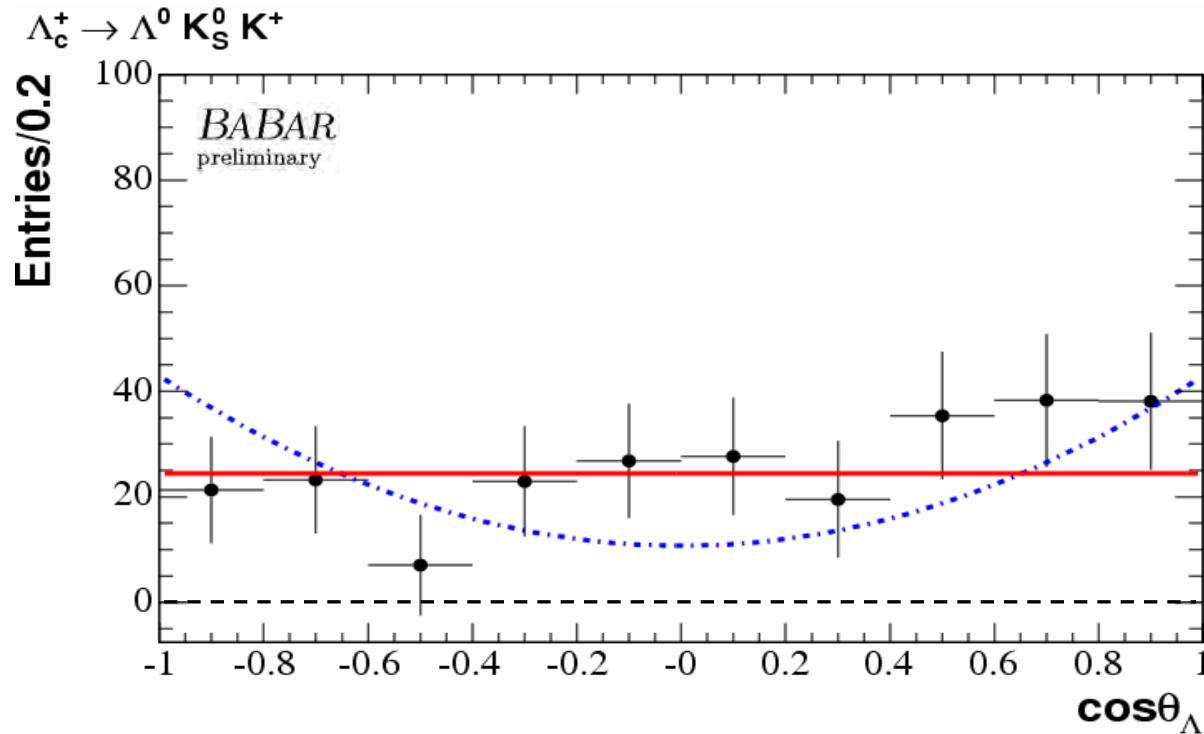


...towards a measurement of the mass & width of $\Xi(1690)^0 \rightarrow \Lambda^0 K_S^0$

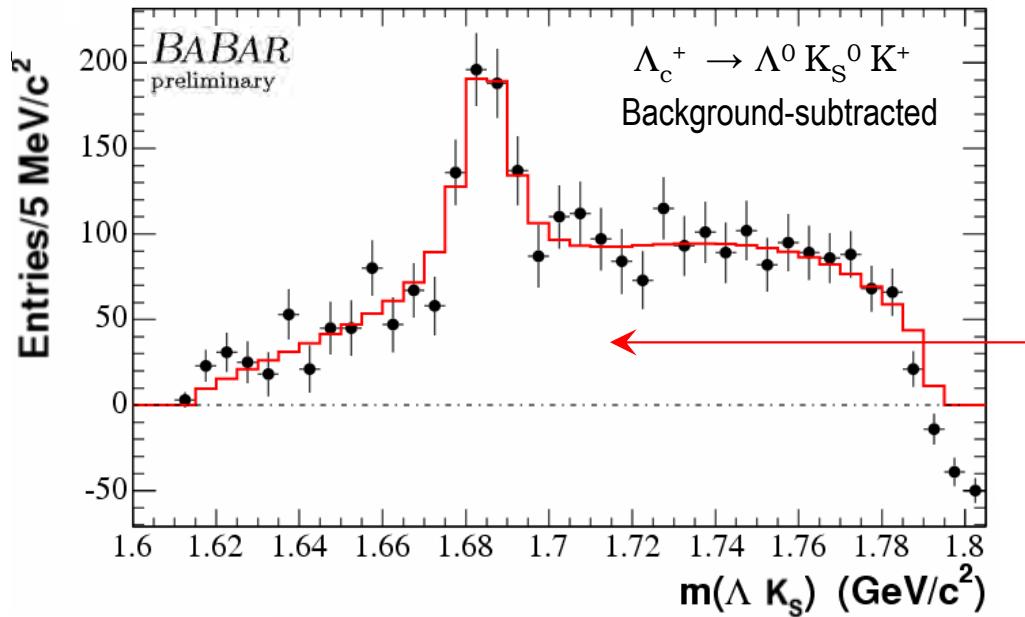
Only “obvious” structure:
 $\Xi(1690)^0 \rightarrow \Lambda^0 K_S^0$



Spin measurement of $\Xi(1690)^0$ from $\Lambda_c^+ \rightarrow \Xi(1690)^0 K^+$, $\Xi^0(1690) \rightarrow \Lambda^0 K_S^0$ decays

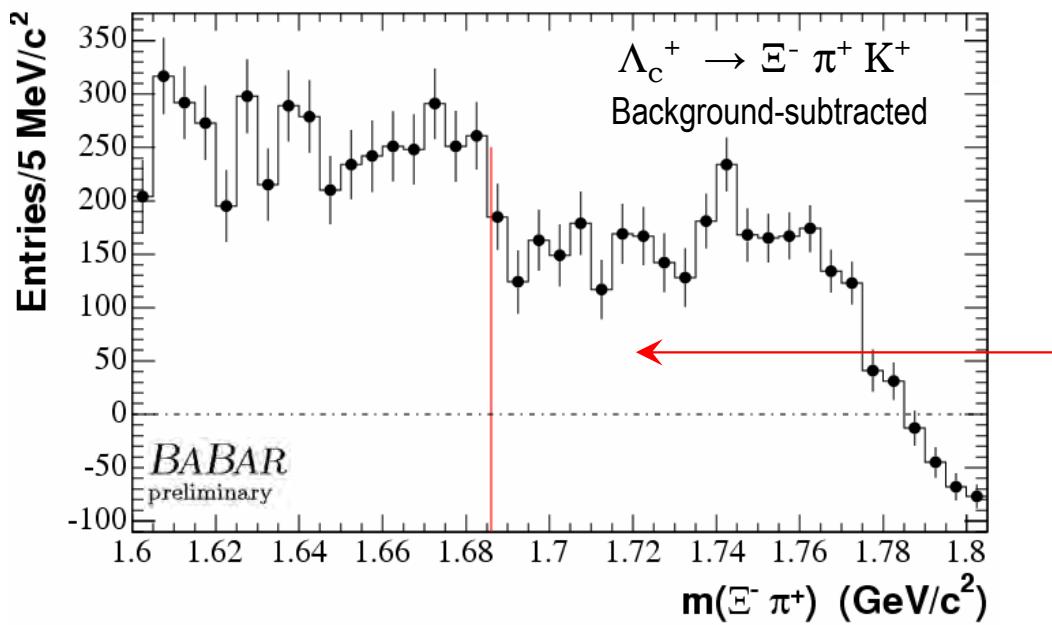


...towards an U.L. on $\text{BR}(\Xi(1690)^0 \rightarrow \Xi^- \pi^+) / \text{BR}(\Xi(1690)^0 \rightarrow \Lambda^0 K_S^0)$



Uncorrected ($\Lambda^0 K_S^0$) invariant mass
[$\Lambda_c^+ \rightarrow \Lambda^0 K_S^0 K^+$]

Clear signal for $\Xi(1690)^0 \rightarrow \Lambda^0 K_S^0$



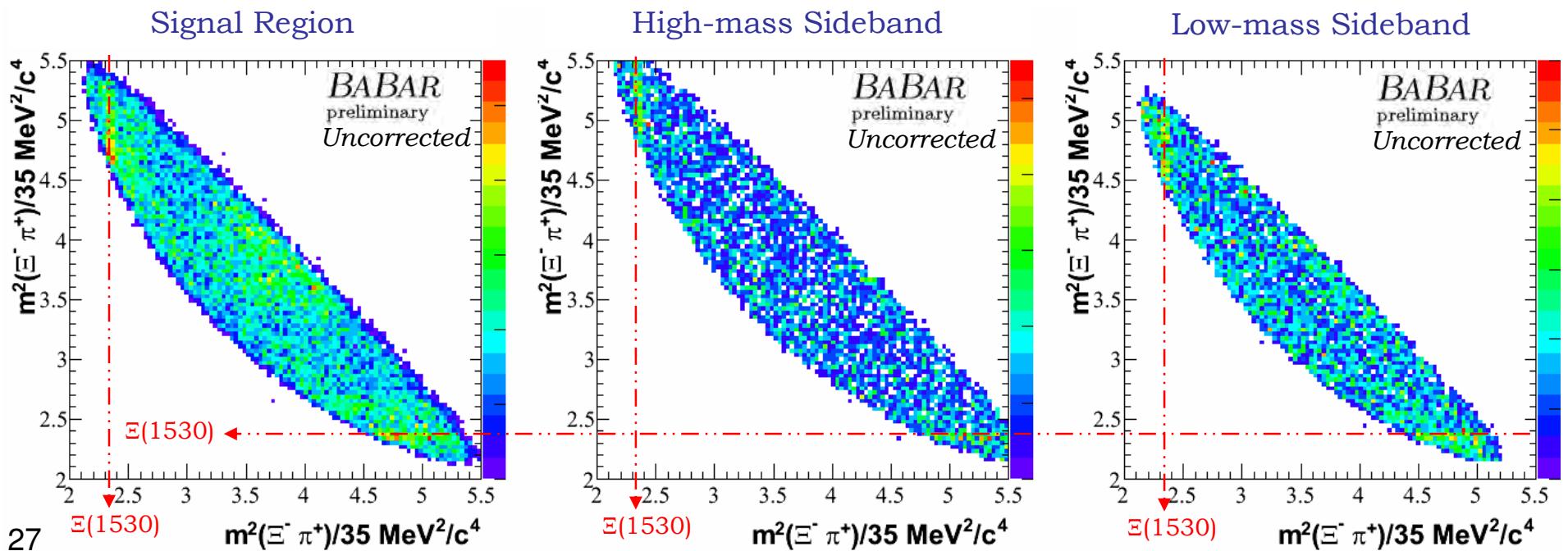
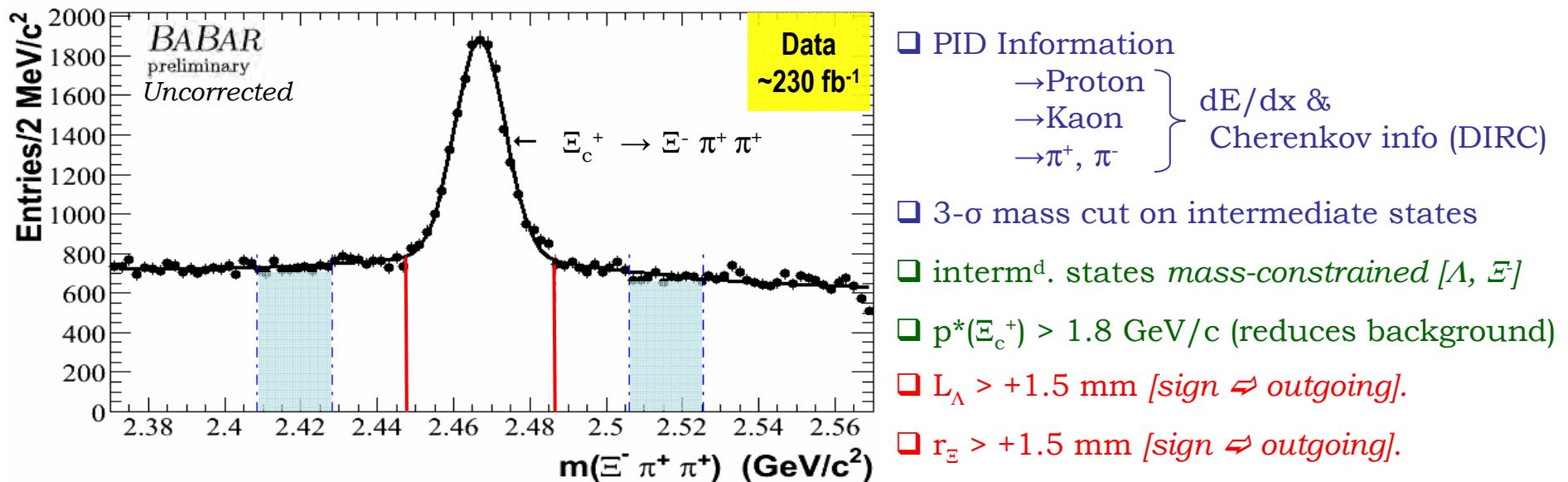
Uncorrected ($\Xi^- \pi^+$) invariant mass
[$\Lambda_c^+ \rightarrow \Xi^- \pi^+ K^+$]

No signal for $\Xi(1690)^0 \rightarrow \Xi^- \pi^+$

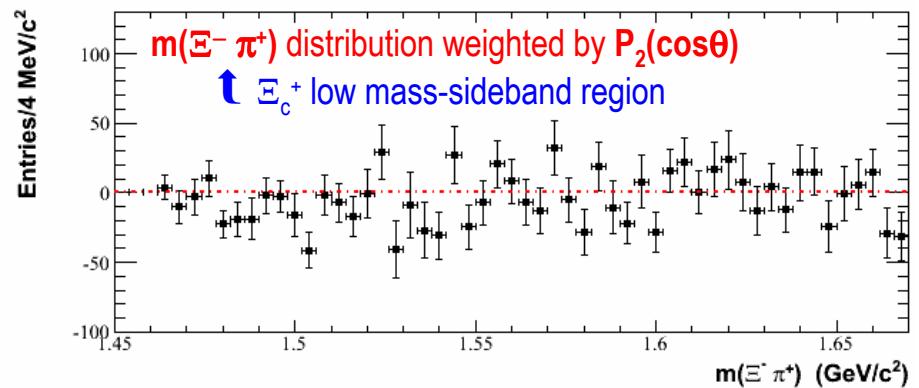
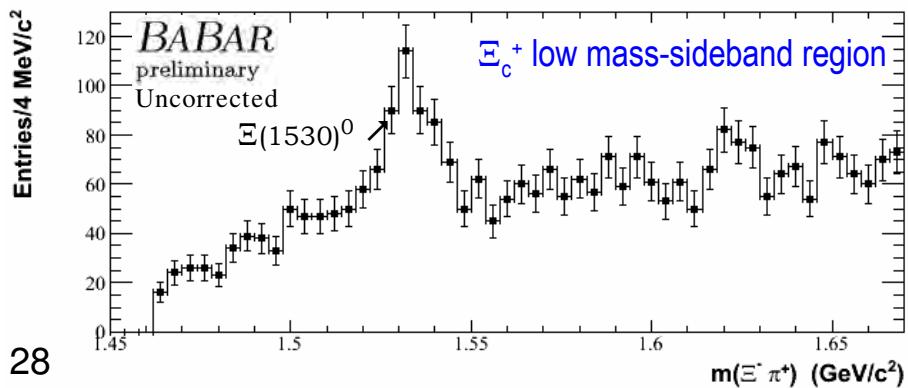
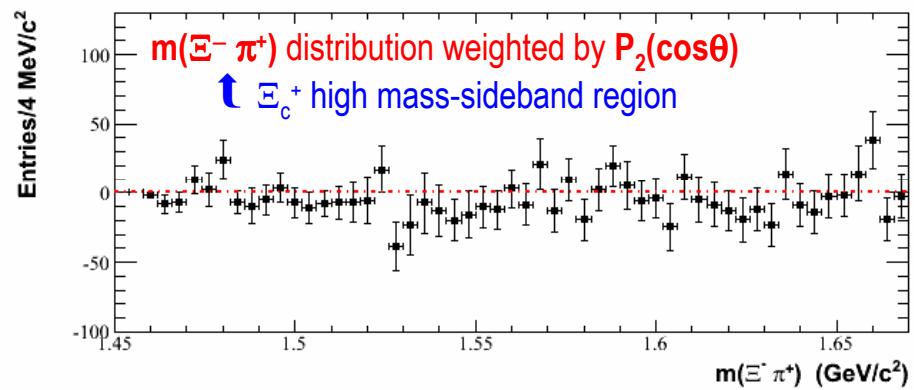
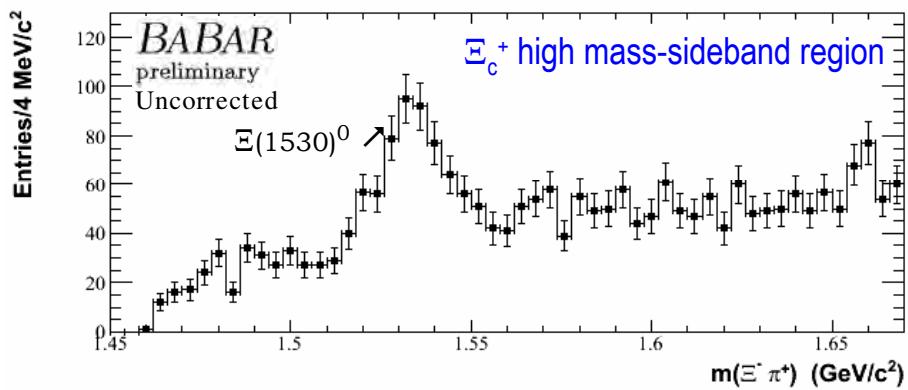
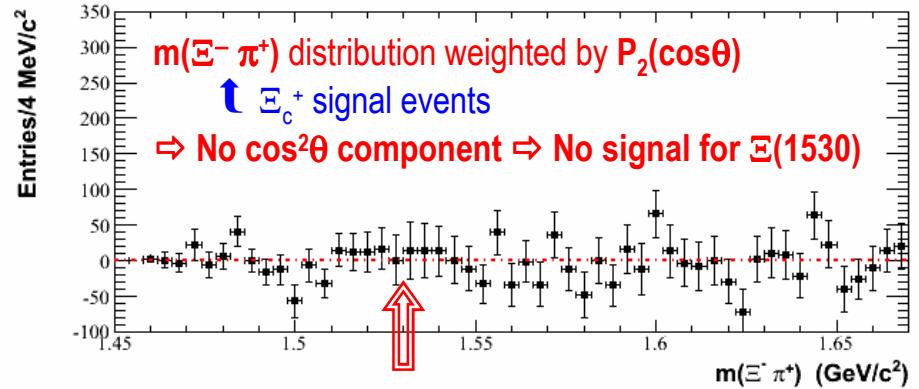
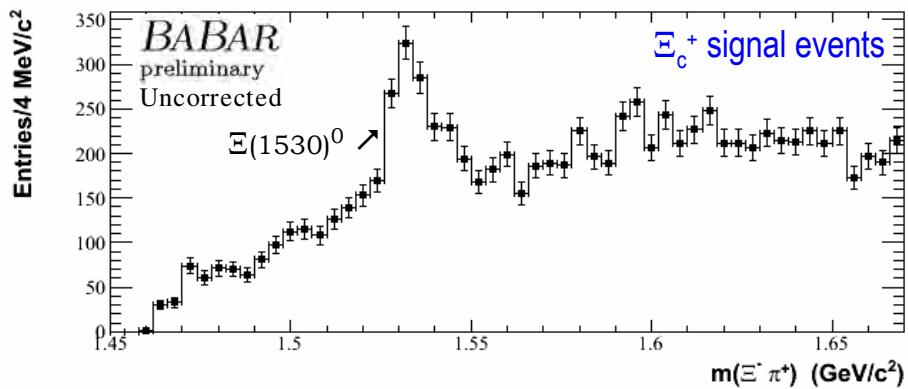
Investigation of $\Xi_c^{+,0}$ Decays to 3-body Final States

- $\Xi_c^+ \rightarrow \Xi^- \pi^+ \pi^+$
- $\Xi_c^+ \rightarrow \Lambda^0 K_S^0 \pi^+$ (if time permits)
- $\Xi_c^0 \rightarrow \Lambda^0 K^- \pi^+$ (if time permits)

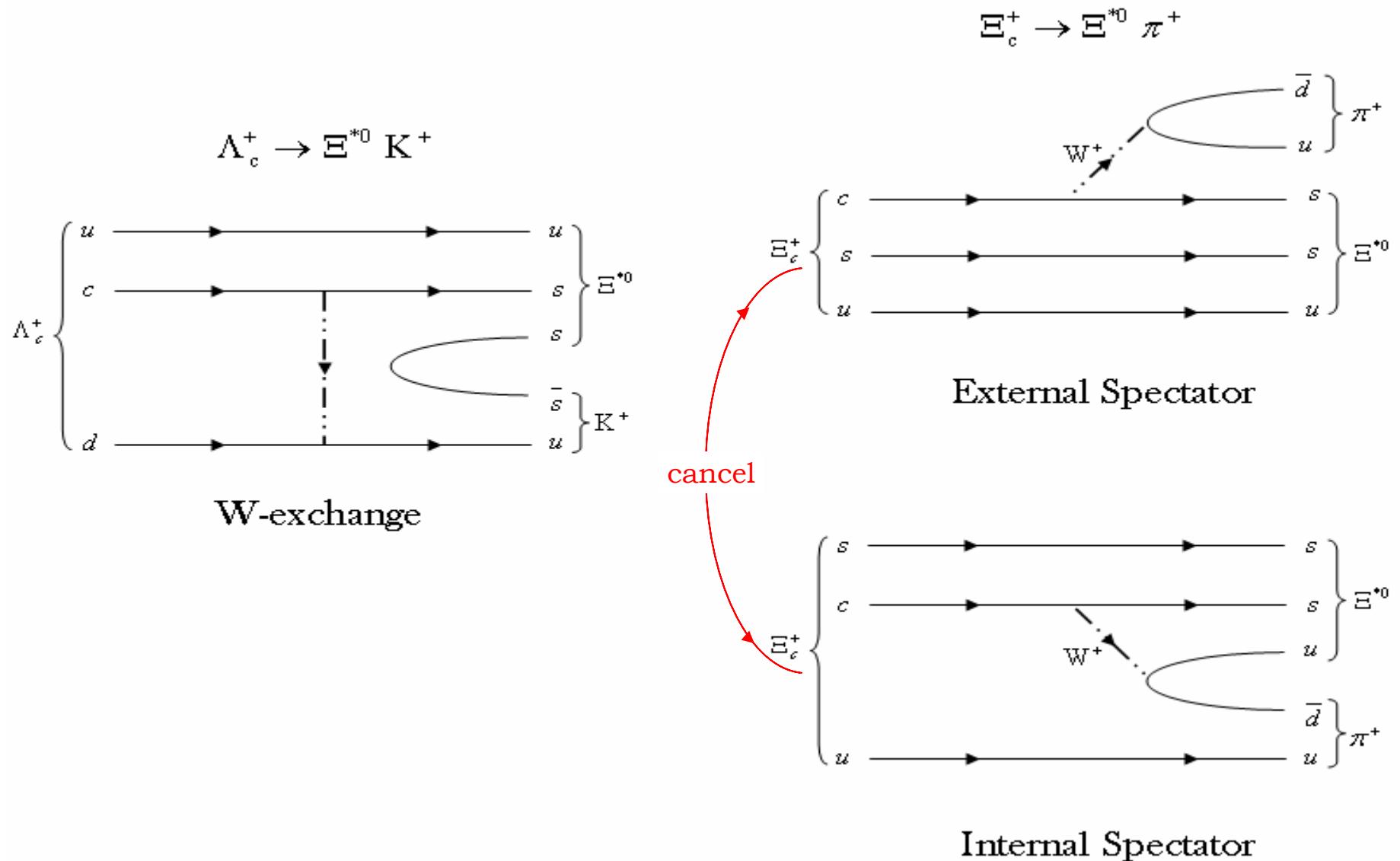
Reconstructed $\Xi_c^+ \rightarrow \Xi^- \pi^+ \pi^+$, $\Xi^- \rightarrow \Lambda^0 \pi^-$ Events



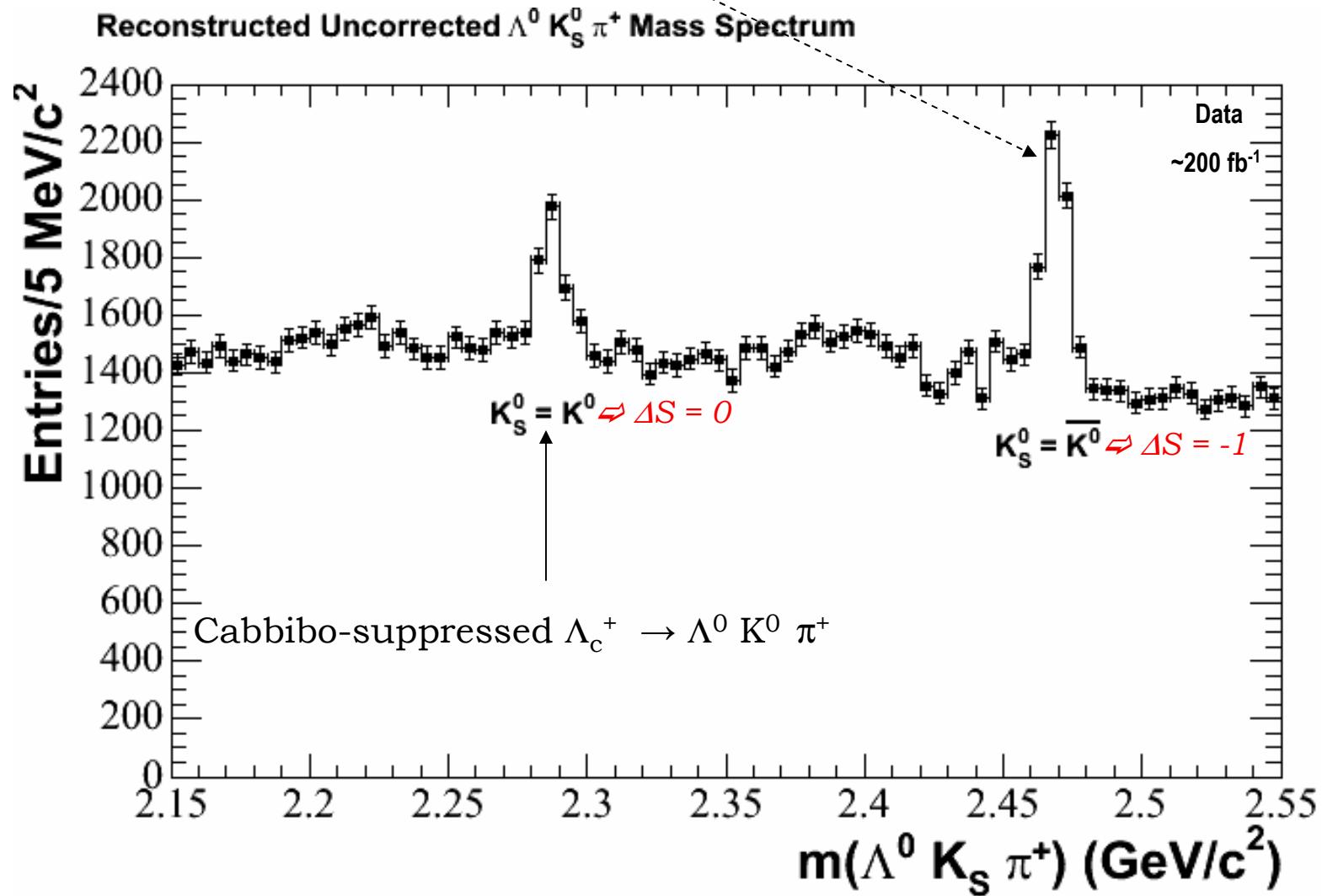
Using the angular structure of $\Xi(1530)^0 \rightarrow \Xi^- \pi^+$ candidates to show the presence of large $\Xi(1530)^0$ background



Ξ^{*0} Production in Λ_c^+ & $\Xi_c^{0,+}$ Decays

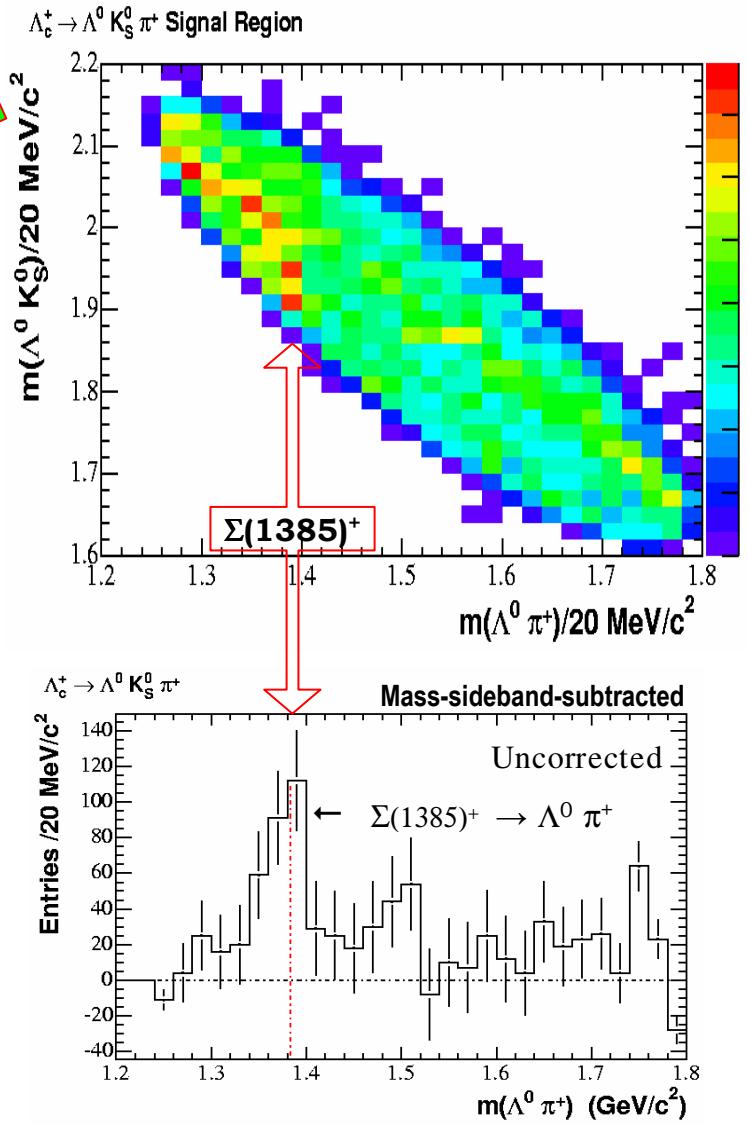
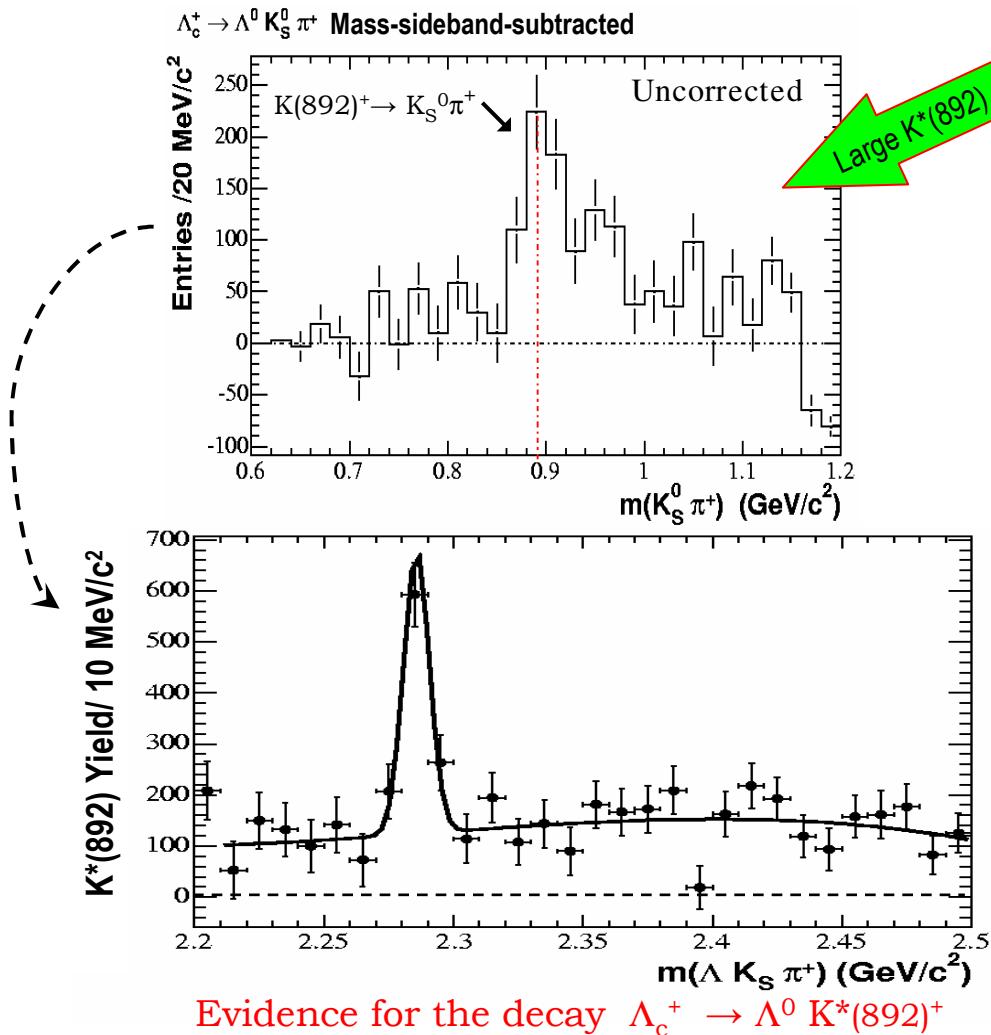


... Reconstructing $\Xi_c^+ \rightarrow \Lambda^0 K_S^0 \pi^+$ Events



$\Lambda_c^+ \rightarrow \Lambda^0 K^0 \pi^+$ Dalitz Plot Analysis

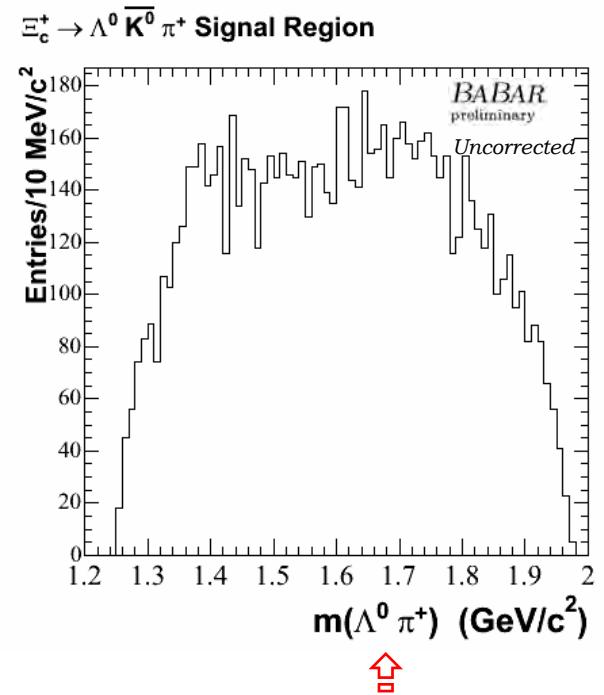
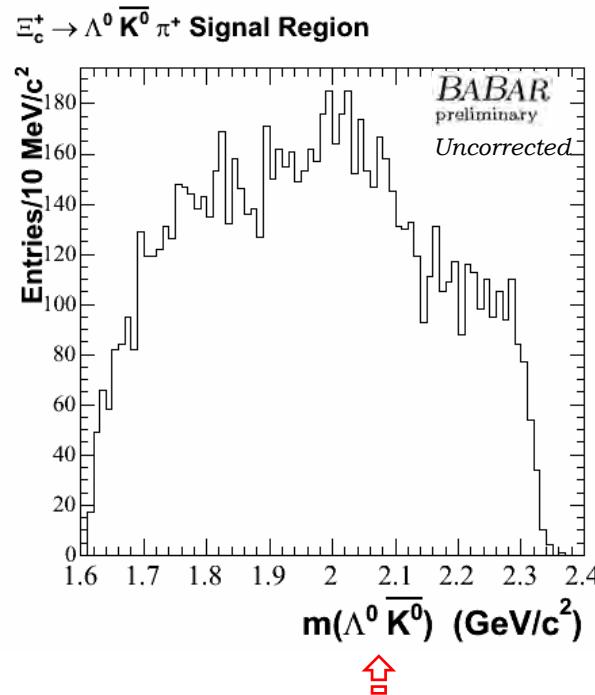
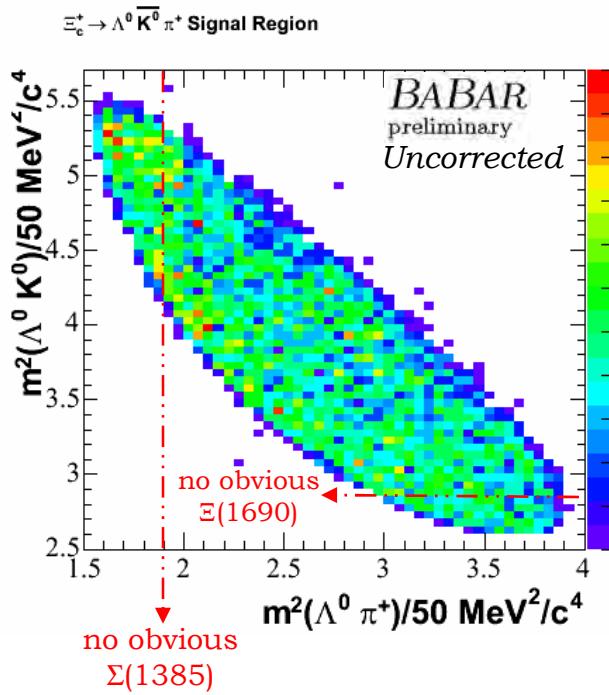
“Obvious” resonant structures



- Previously observed C.S. mode: $\Lambda_c^+ \rightarrow \Sigma^+ K^*(892)^0$

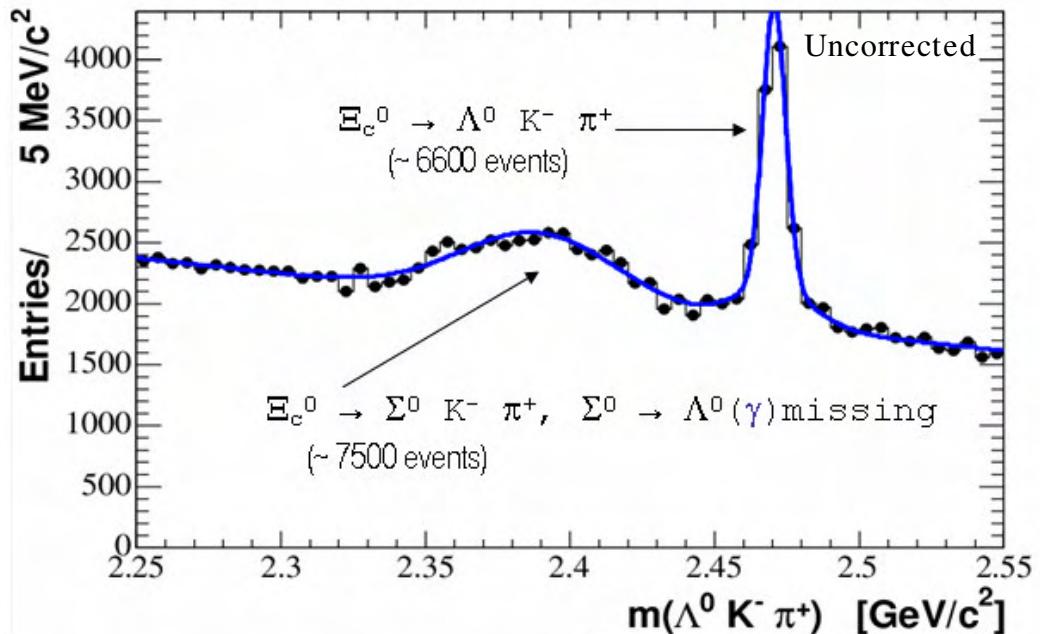
$\Xi_c^+ \rightarrow \Lambda^0 \bar{K}^0 \pi^+$ Dalitz Plot Analysis

No “obvious” resonant structures

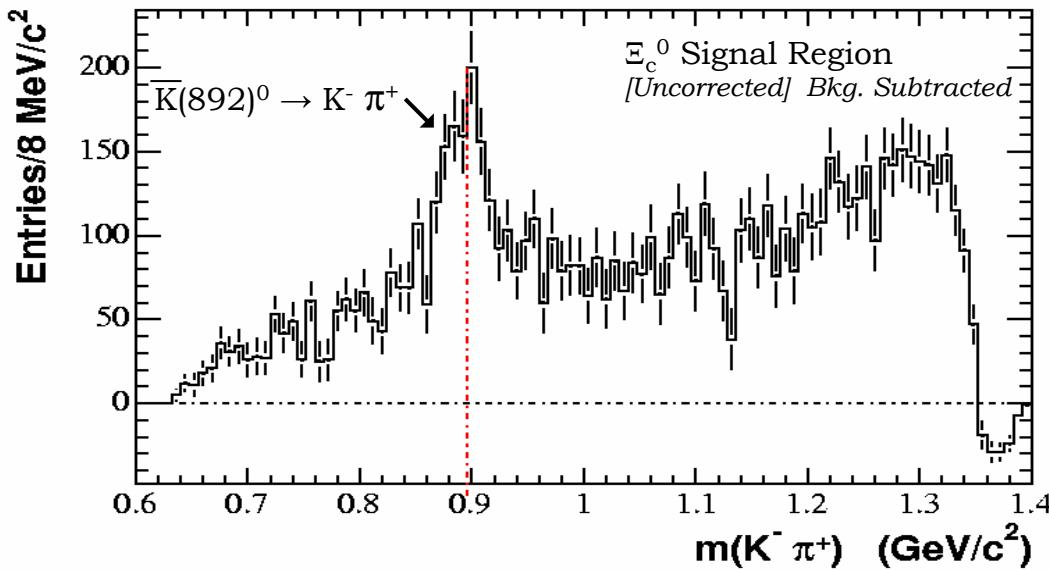


Reconstructed $\Xi_c^0 \rightarrow \Lambda^0 K^- \pi^+$ Events

- Particle Identification
 - Proton
 - Kaon
 - π^+, π^-
- { dE/dx & Cherenkov info (DIRC)
- 3- σ mass cut on intermediate state [Λ^0]
- $p^*(\Xi_c^0) > 2.25 \text{ GeV}/c$ [reduces background]
- $L_\Lambda > +0.9 \text{ mm}$ [sign \Leftrightarrow outgoing].



Strong $\bar{K}^*(892)$ Production



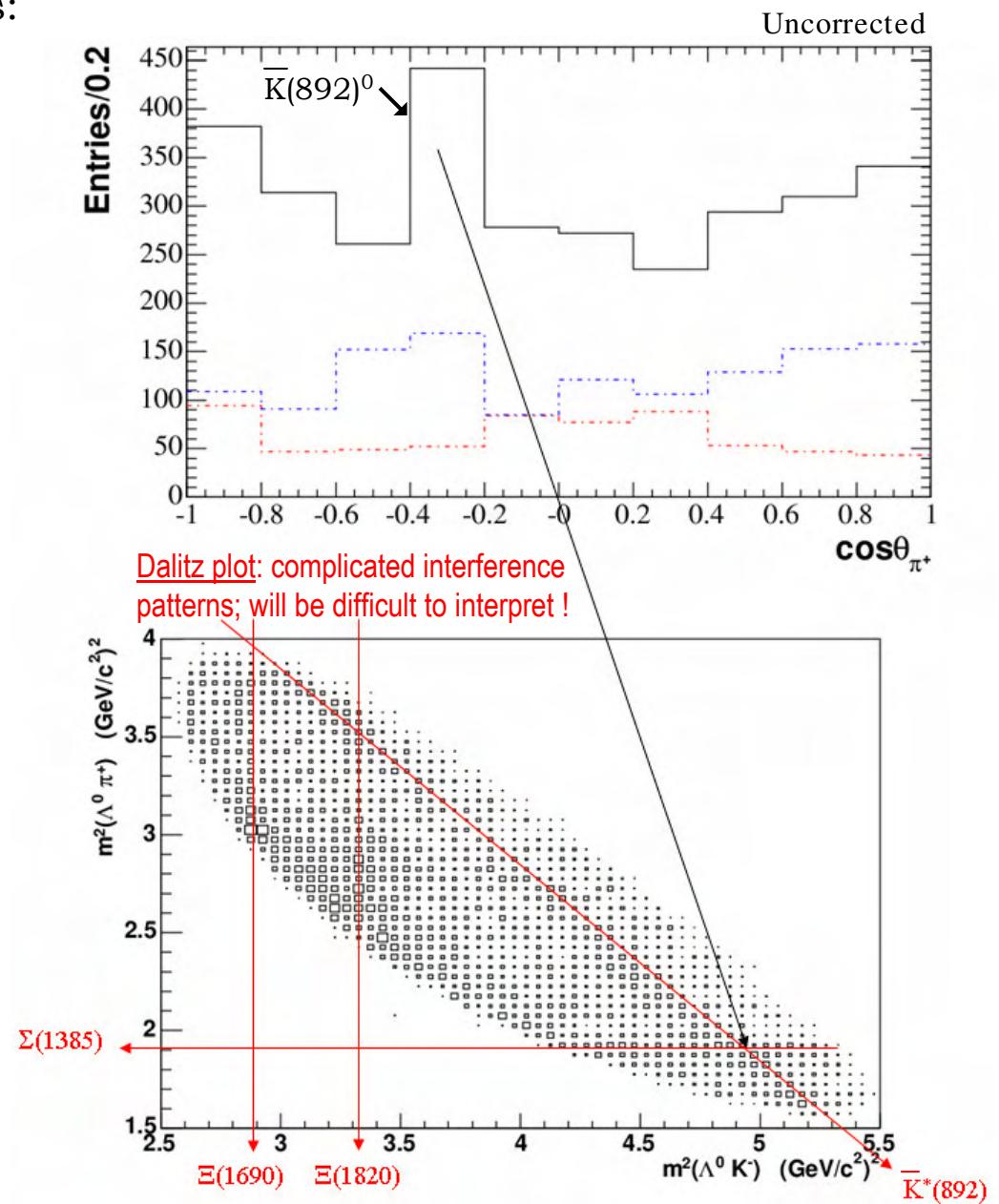
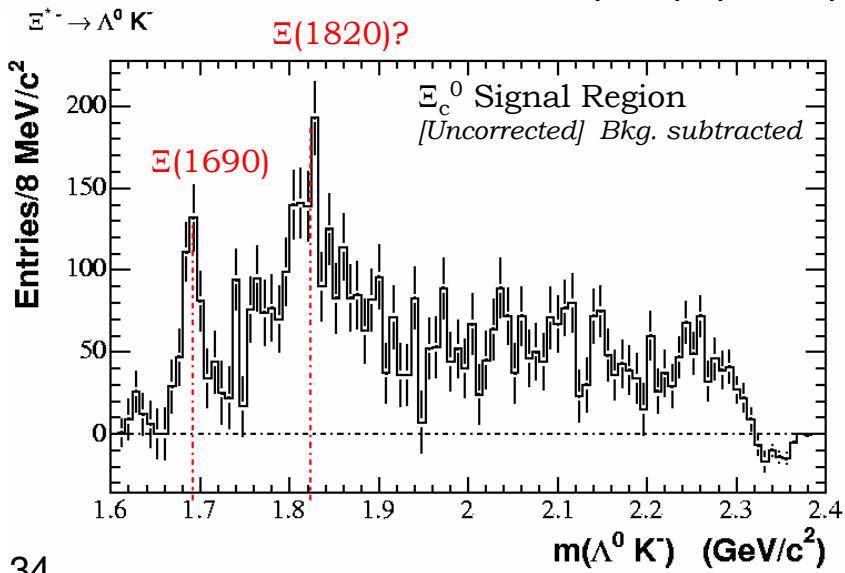
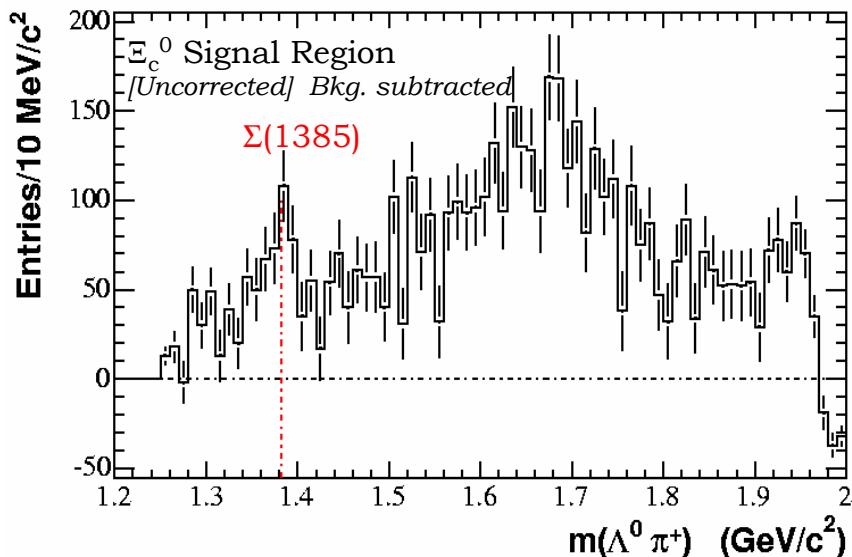
FIT:
 Σ^0 feed-down fixed mean: computed from kinematics assuming ($K \pi$) $\sim K^*(892)$
 Ξ_c^0 Signal width: Double Gaussian
 Σ^0 feed-down width: Single Gaussian

Σ^0 mode seems to be as large as Λ^0 mode

**Angular dist. of $\Sigma(1385)^+$ from $\Xi_c^0 \rightarrow \Sigma(1385)^+ K^-$,
 $\Sigma^+(1385) \rightarrow \Lambda^0 \pi^+$ decays**

- Possible Hyperon Resonant Structures:

- $\Sigma(1385, 1670(?))^+ \rightarrow \Lambda^0 \pi^+$
- $\Xi(1690, 1820)^- \rightarrow \Lambda^0 K^-$



SUMMARY(1)

Assuming Λ_c^+ , $\Xi_c^{+,0}$ and Ω_c^0 have spin 1/2:

- used the decay modes $\Xi_c^0 \rightarrow \Omega^- K^+$ and $\Omega_c^0 \rightarrow \Omega^- \pi^+$
to show that the Ω^- has spin 3/2; spin 1/2 and 5/2 are ruled out.
- used the decay mode $\Lambda_c^+ \rightarrow \Xi^- \pi^+ K^+$
 - to show that the spin of the $\Xi(1530)$ is 3/2
 - to extract the $\Xi(1530)$ lineshape almost free of background; should give high quality (M, Γ) measurements
 - to demonstrate $\Xi(1530)$ Breit-Wigner phase motion for the first time
 - to show the presence of an S-wave $\Xi^- \pi^+$ amplitude and the possibility of a $\Xi^- \pi^+$ amplitude analysis.
- used the decay mode $\Lambda_c^+ \rightarrow \Lambda^0 K_S^0 K^+$
 - to show the presence of a clear $\Xi(1690) \rightarrow \Lambda^0 K_S^0$ signal; should yield quality (M, Γ) measurements
 - to show that spin 1/2 is *slightly* favored for $\Xi(1690)$ ($\cos\theta$ distribution) and that spin $\geq 3/2$ is *strongly* disfavored for the $\Xi(1690)$ ($P_2(\cos\theta)$ -weighted mass distributions)
 - to show that the $\text{BR}(\Xi(1690) \rightarrow \Xi^- \pi^+)/\text{BR}(\Xi(1690) \rightarrow \Lambda^0 \bar{K}^0)$ is small; should be able to obtain U.L. estimate

SUMMARY(2)

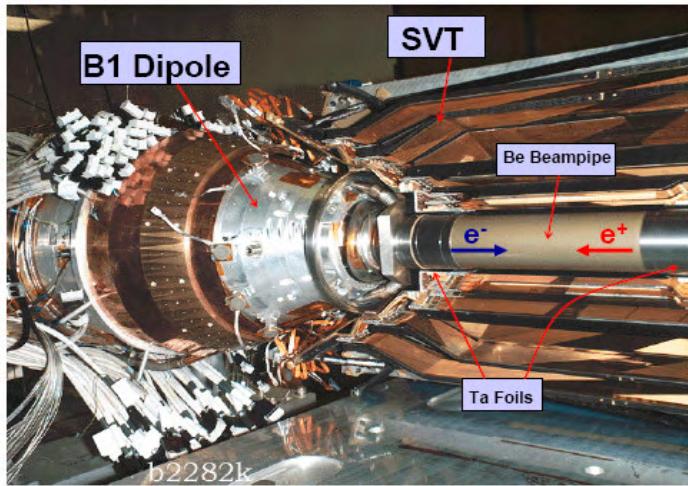
- used the decay mode $\Xi_c^+ \rightarrow \Xi^- \pi^+ \pi^+$
 - to show the absence of any significant $\Xi(1530)$ signal; but large $\Xi(1530)$ background in the Ξ_c^+ sidebands \Rightarrow careful analysis; ongoing.
- used the decay mode $\Lambda_c^+ \rightarrow \Lambda^0 \bar{K}^0 \pi^+$
 - to show first evidence for the C.S. decay $\Lambda_c^+ \rightarrow \Lambda^0 K(892)^0$
- used the decay mode $\Xi_c^+ \rightarrow \Lambda^0 \bar{K}^0 \pi^+$
 - to search for $\Xi(1690) \rightarrow \Lambda^0 K^0$; no signal apparent;
Dalitz plot very different from $\Lambda_c^+ \rightarrow \Lambda^0 \bar{K}^0 K^+$
- used the decay mode $\Xi_c^0 \rightarrow \Lambda^0 K^- \pi^+$
 - to show evidence for $\Xi(1690)^- \rightarrow \Lambda^0 K^-$ and indications for $\Xi(1820)$ and $\Sigma(1385)$ signals; however the Dalitz plot exhibits complicated interference patterns, and analysis will be difficult.

FUTURE PLANS & POSSIBILITIES

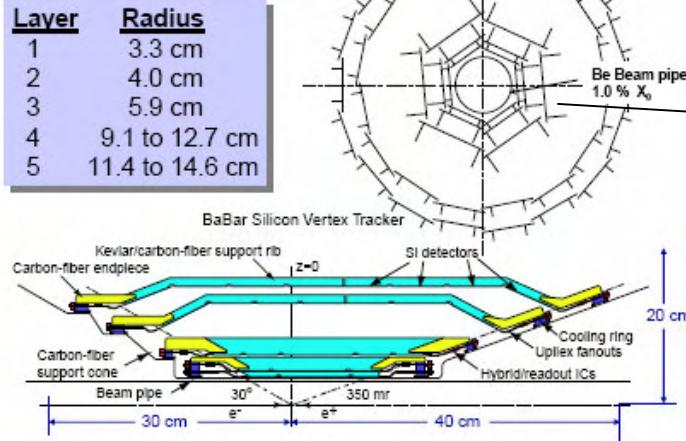
1. Obtain efficiency-corrected distributions and complete the analyses of the $\Xi(1530)$ and $\Xi(1690)$ signals; carry out the $(\Xi^- \pi^+)$ amplitude analysis to separate S and P wave amplitudes and demonstrate P-wave Breit-Wigner phase motion.
2. Use the decay chain $\Xi(1530) \rightarrow \Xi^- \pi^+$, $\Xi^- \rightarrow \Lambda^0 \pi^+$, $\Lambda^0 \rightarrow p \pi^-$ to measure the parity of the $\Xi(1530)$ by using the complete decay angular correlations (cf. Byers-Fenster spin-parity test)
3. Investigate the Λ^0 final states from Λ_c^+ decays when $\Lambda^0 \leftrightarrow \Sigma^0$ to look for $\Xi(1690) \rightarrow \Sigma^0 K^0$, $\Sigma^0 K^-$ [Thresholds 1690.2, 1686.3 MeV]; signal at threshold would favor S-wave \Rightarrow negative parity [e.g. $\Lambda_c^+ \rightarrow \Sigma^0 K_S^0 K^+$ from BaBar in PRD72, 052006(2005)]
4. “Reverse-engineer” $\Xi(1530)$ and Ω^- analyses to measure the charm baryon spin; the decay $\Lambda_c^+ \rightarrow \eta \Sigma(1385)^+$, $\Sigma(1385)^+ \rightarrow \Lambda^0 \pi^+$ might be helpful in this regard.
5. Incorporate available Run 5 data into the analyses
6. Perhaps extend approach to higher multiplicity decays
e.g. $\Lambda(1115)^0 \leftrightarrow \Lambda(1520)^0 \rightarrow K^- p$

BACKUP SLIDES

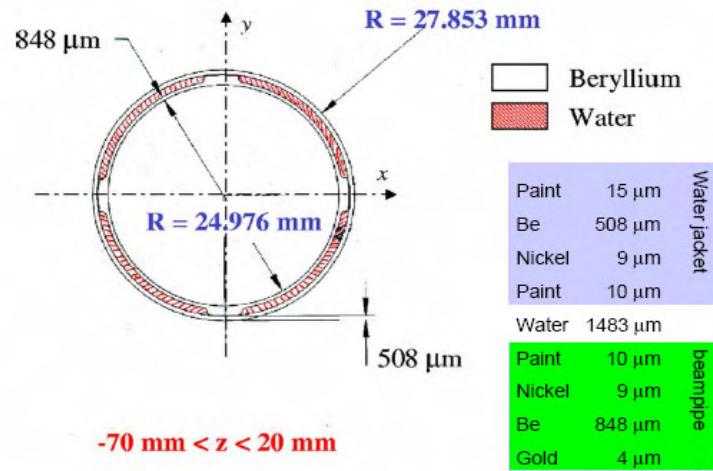
The Beampipe and Inner Detector Region



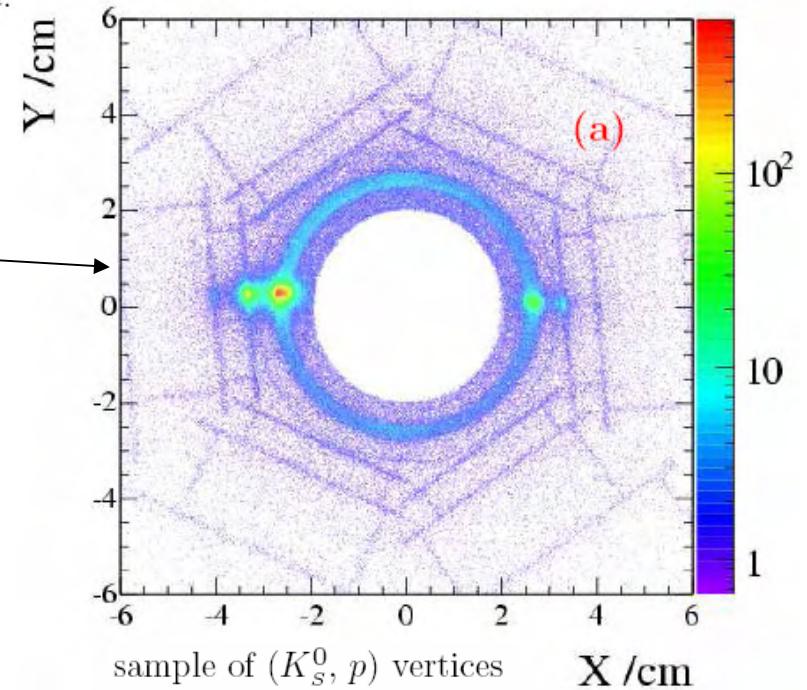
The beampipe, backward B1 magnet and positive x half of the SVT.



The geometry of the SVT layers



The radial geometry and material composition of the beampipe.

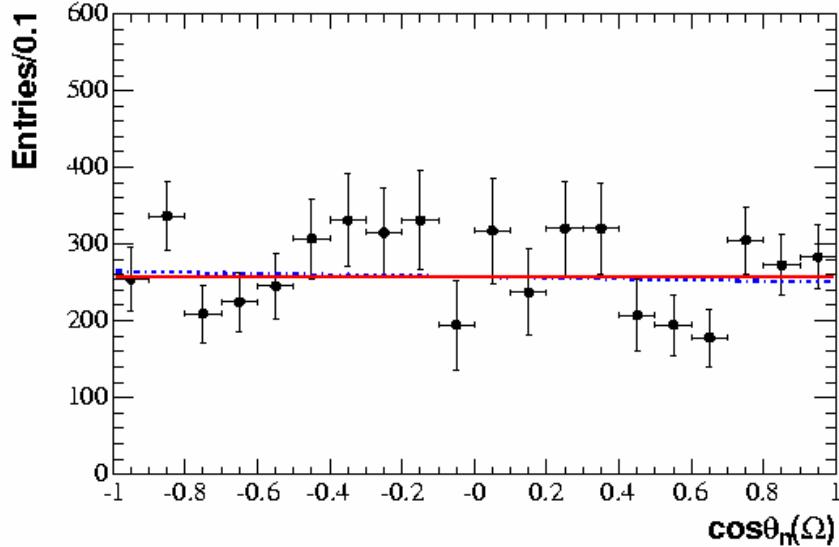
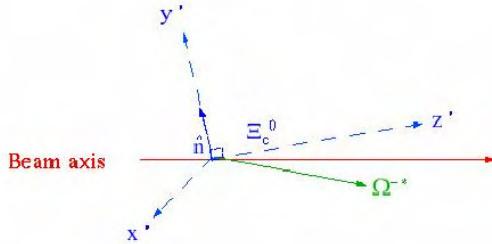


“Reverse” Engineering

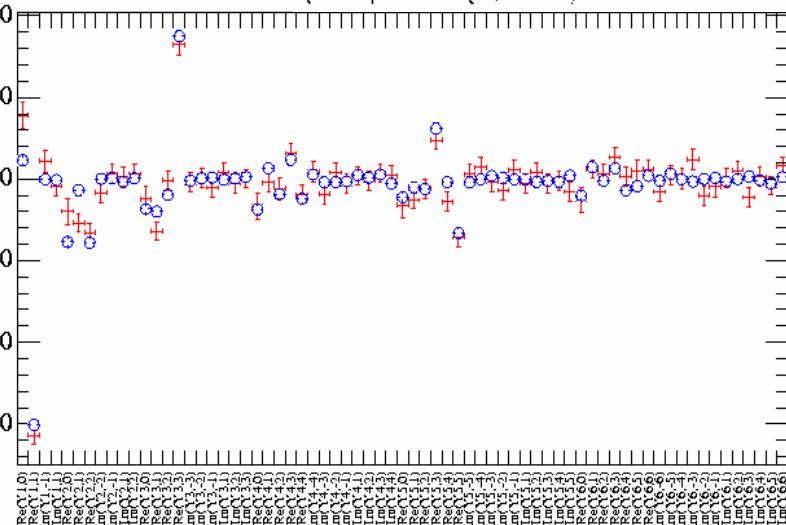
↳ allow for higher charm baryon spins

Ξ_c^0	Ω^-	1/2	3/2	5/2
1/2	x	✓	x	
3/2	?	x	x	
5/2	?	?		x

Polarization Study

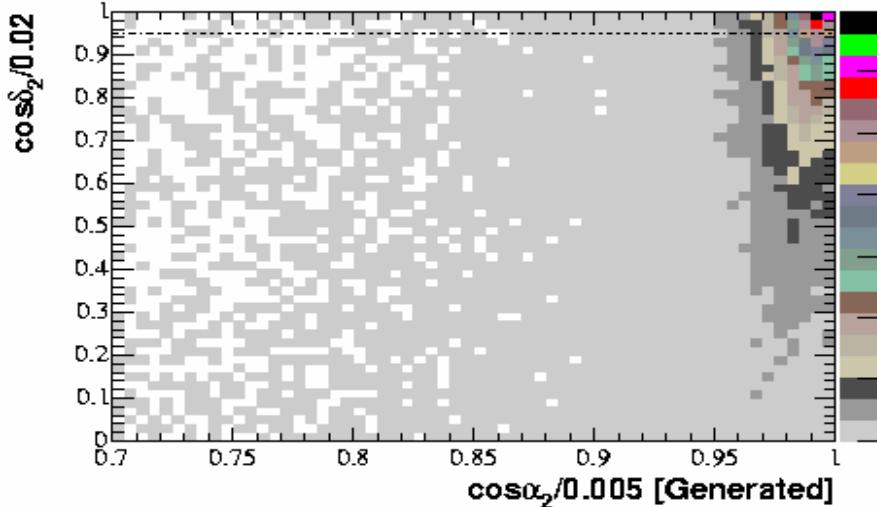


Isotropic decay $\Rightarrow \langle Y_L^M \rangle = \int \left(\frac{dN}{d\phi d\cos\theta} \right) Y_L^M(\theta, \phi) d\phi d\cos\theta \approx \sum \left(\frac{dN}{d\phi d\cos\theta} \right) Y_L^M(\theta, \phi) d\phi d\cos\theta = 0$. \Rightarrow parent baryon helicity states equally populated

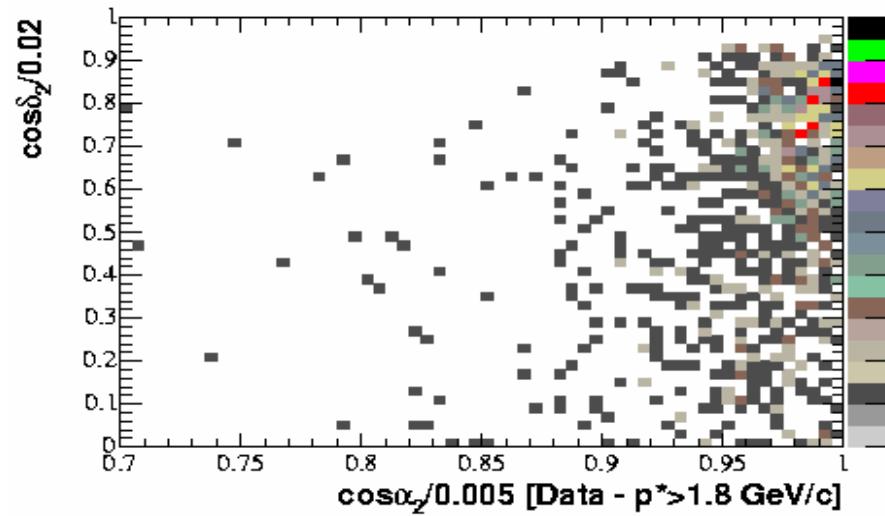


\Leftrightarrow The mass-sideband-subtracted unnormalized YLM moments of the Ξ_c^0 signal in data (red); superimposed are the corresponding moments for truth-matched Signal MC (blue circles).

Efficiency loss at small angles

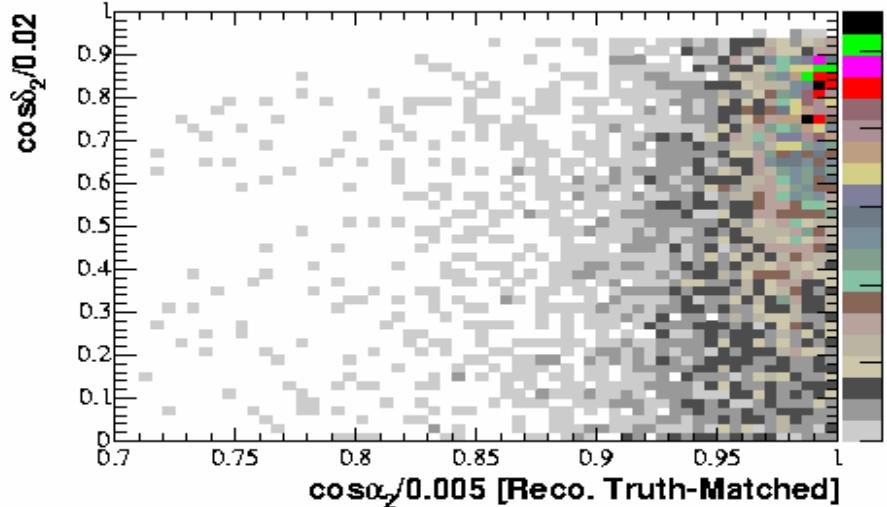


(a)



(c)

Figure 8: The scatter plots of the cosine of the angle between the K^- and the lab z-axis (δ_2) versus the opening cosine of the angle between the Ω^- and its decay kaon ($\cos\alpha_2$).



(b)

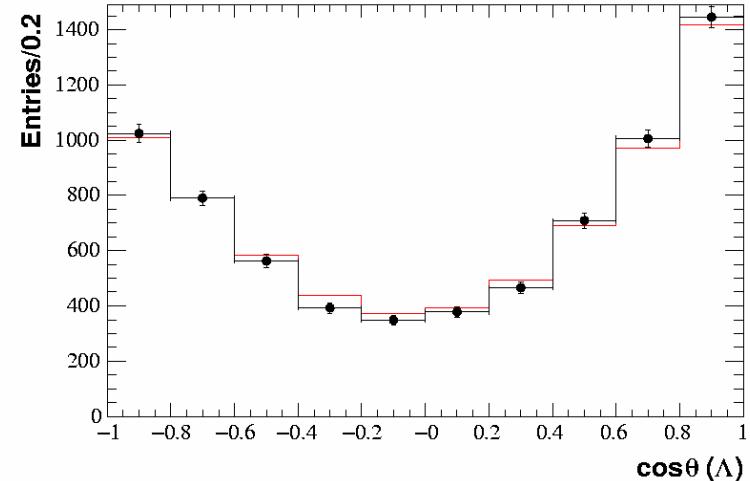
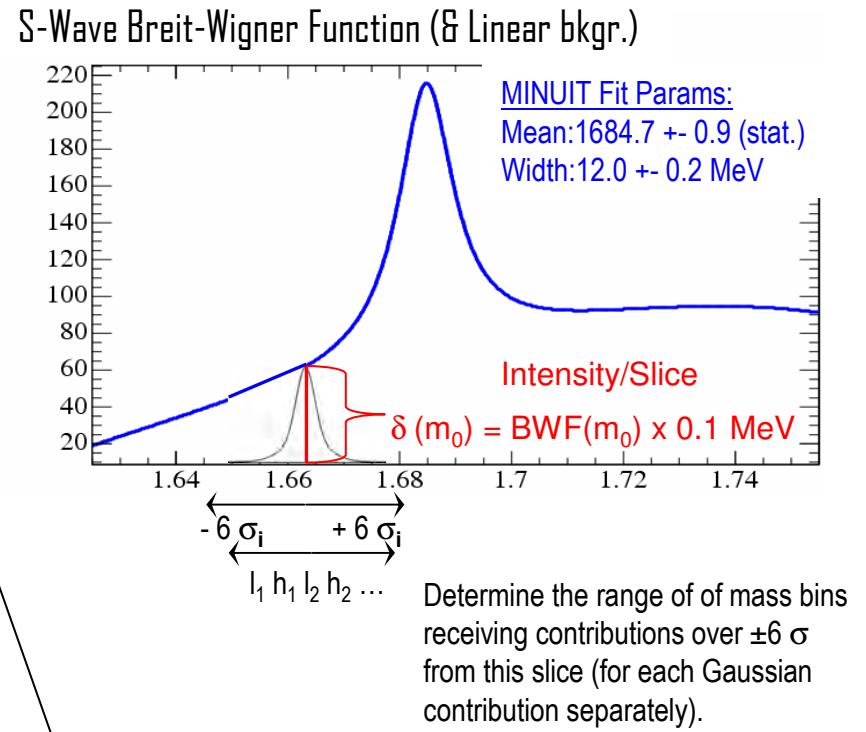
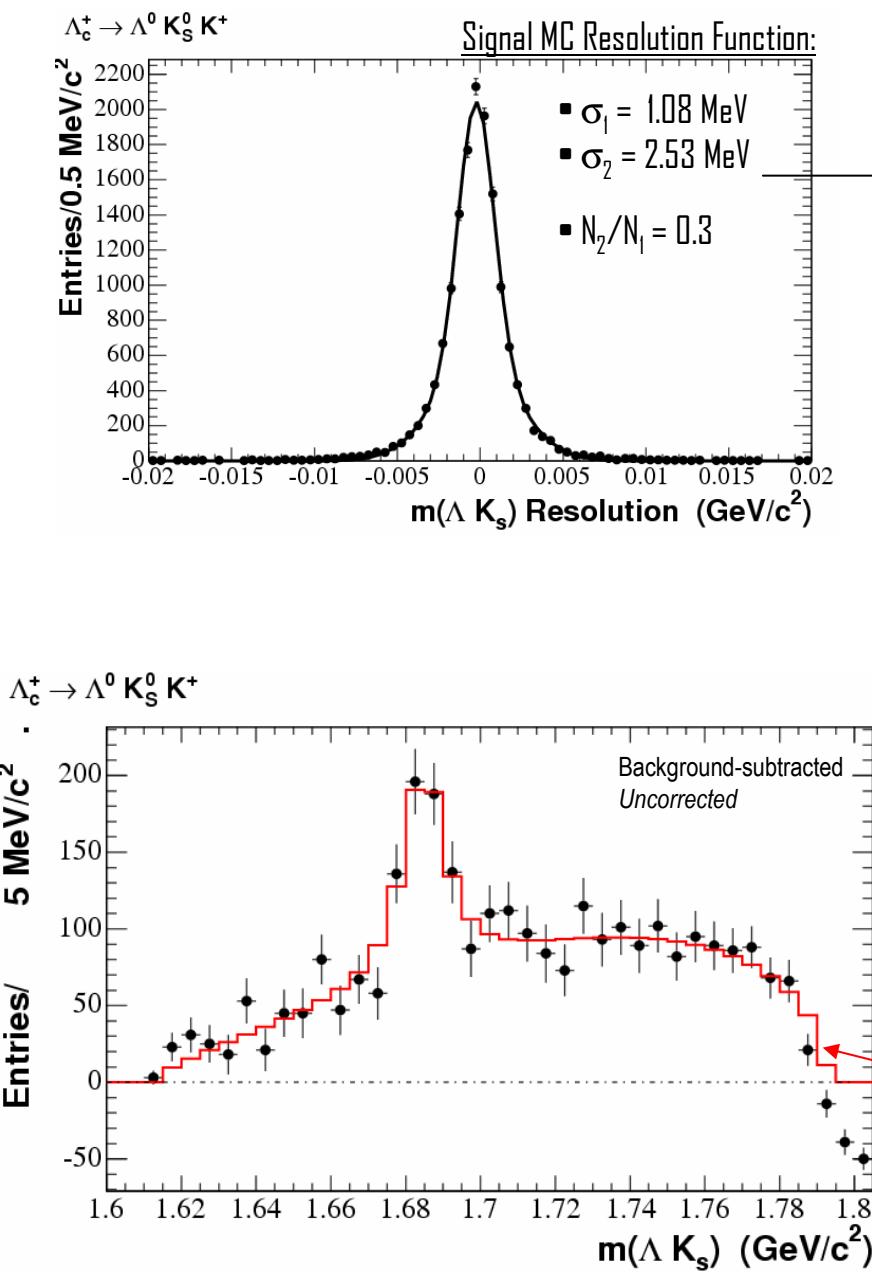


Figure 9: The reconstructed (red lines) and generated (black dots) MC distributions satisfying $\cos\delta_1 < 0.98$ and $\cos\alpha_2 < 0.99$.

...towards a measurement of the mass & width of $\Xi^0(1690) \rightarrow \Lambda^0 K_S^0$



→ **Smear** $\delta(m_0)$ over the relevant bins of the $\Xi(1690)$ mass distribution separately for the **core** & **wide** Gaussian of the **resolution** function:

- Signal contribution for **core** Gaussian [$\sigma_i = \sigma_1$]:
 $\sum_i \delta(m_0) \times (1 - N_2/N_1) \times (\text{erf}(h_i) - \text{erf}(l_i))/2$
- Signal contribution for **wide** Gaussian [$\sigma_i = \sigma_2$]:
 $\sum_i \delta(m_0) \times (N_2/N_1) \times (\text{erf}(h_i) - \text{erf}(l_i))/2$

→ **Accumulate** “smeared” contributions for each bin.

The $\Xi^*(1530)$ parity ambiguity

Amplitudes describing the $(\Xi^- \pi^+)$ system if the $\Xi^*(1530)$ has **negative** parity:

$$S_{\lambda_f} \Leftrightarrow l=0, j=1/2$$

$$\eta_S = (-1)^{l+1} = -1$$

$$P_{\lambda_f}^- \Leftrightarrow l=1, j=l-1/2=1/2$$

$$\eta_{P^-} = (-1)^{l+1} = +1$$

$$D_{\lambda_f}^- \Leftrightarrow l=2, j=l-1/2=3/2$$

$$\eta_{D^-} = (-1)^{l+1} = -1$$

$$\Rightarrow \text{Total Intensity} \sim \sum_{\substack{\lambda_i = \pm 1/2, \\ \lambda_f = \pm 1/2}} \rho_i \left| D_{\lambda_i \lambda_f}^{1/2*}(\phi, \theta, 0) S_{\lambda_f} + D_{\lambda_i \lambda_f}^{1/2*}(\phi, \theta, 0) P_{\lambda_f}^- + D_{\lambda_i \lambda_f}^{3/2*}(\phi, \theta, 0) D_{\lambda_f}^- \right|^2$$

$$\begin{aligned} \Rightarrow I &\propto (\rho_{1/2} + \rho_{-1/2}) \left[|S_{1/2}|^2 + |P_{1/2}^-|^2 + |D_{1/2}^-|^2 \left(\frac{1+3\cos^2\theta}{4} \right) + 2 \operatorname{Re}(P_{1/2}^- D_{1/2}^{-*}) \cos\theta \right] \xrightarrow{\text{P-D- interference}} \\ &+ 2(\rho_{1/2} - \rho_{-1/2}) \left[\operatorname{Re}(S_{1/2} P_{1/2}^{-*}) \cos\theta + \operatorname{Re}(S_{1/2} D_{1/2}^{-*}) \left(\frac{3\cos^2\theta - 1}{2} \right) \right]. \end{aligned}$$

- If $|P_{1/2}^-| \sim 0$ observed $\cos\theta$ dist. \Rightarrow positive parity, else no conclusion can be drawn re. parity.
- Angular dist. result^g from amplitude combinations $[S_{1/2}, P_{1/2}^+]$ & $[P_{1/2}^-, D_{1/2}^-]$ {both, $j=1/2, j=3/2\}$ are indistinguishable [eq. Minami Ambiguity in πp elastic scatt. {S. Minami, Prog. Theor. Phys. 11, 213(1954)}
 $\hookrightarrow d\sigma/d\Omega$ depends only on j , not on l]
- Detailed study of Ξ^- , Λ^0 decay correlation required (eg. Byers & Fenster)

The moments of the angular distribution for the $(\Xi^- \pi^+)$ system

Assuming that the $\Xi^*(1530)$ has **positive** parity:

$$\boxed{\begin{aligned} P_0(\cos \theta) &= \frac{1}{\sqrt{2}} \\ P_1(\cos \theta) &= \sqrt{\frac{3}{2}} \cos \theta \\ P_2(\cos \theta) &= \sqrt{\frac{5}{2}} \left(\frac{3 \cos^2 \theta - 1}{2} \right) \end{aligned}}$$

$$\frac{dN}{d \cos \theta} = \frac{1}{\sqrt{2}} \left(|S_{1/2}|^2 + |P_{1/2}^-|^2 + |P_{1/2}^+|^2 \right) P_0(\cos \theta) + \sqrt{\frac{2}{5}} |P_{1/2}^+|^2 P_2(\cos \theta) + 2 \sqrt{\frac{2}{3}} |S_{1/2}| |P_{1/2}^+| \cos(\varphi_s - \varphi_p) P_1(\cos \theta)$$

$$\frac{dN}{d \cos \theta} = \langle P_0 \rangle P_0(\cos \theta) + \langle P_1 \rangle P_1(\cos \theta) + \langle P_2 \rangle P_2(\cos \theta)$$

$$\Rightarrow \left\{ \begin{array}{l} \left(|S_{1/2}|^2 + |P_{1/2}^-|^2 + |P_{1/2}^+|^2 \right) = N \\ |P_{1/2}^+| = \sqrt{\sqrt{\frac{5}{2}} \langle P_2 \rangle} \\ \cos(\varphi_s - \varphi_p) = \frac{\sqrt{\frac{3}{8}} \langle P_1 \rangle}{\sqrt{\sqrt{\frac{5}{2}} \langle P_2 \rangle \left(N - \sqrt{\frac{5}{2}} \langle P_2 \rangle \right)}} \end{array} \right.$$