

## Numerical estimates of chiral cloud contributions to tagged proton electroproduction

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# The TOPT Sullivan process (see Tim Londergan's talk!)

- $|N\rangle = \sqrt{Z_2} |N\rangle_0 + \sum_{M,B} \int dy f_{MB}(y) |M(y); B(1-y)\rangle$   
 $y = k^+/P^+$ :  $k$  meson,  $P$  nucleon

- time-ordered PT in the **inf. momentum frame (IMF)**

$$f_{\pi^- N}(y) = \frac{2g_{\pi NN}^2}{16\pi^2} \int_0^\infty \frac{dk_\perp^2}{(1-y)} \frac{F_{\pi N}^2(s_{\pi N})}{y(m_N^2 - s_{\pi N})^2} \left( \frac{k_\perp^2 + y^2 m_N^2}{1-y} \right)$$

$$F_{\pi N}(s_{\pi N}) = \exp[-(s_{\pi N} - m_N^2) / \Lambda^2] \text{ (for example!)}$$

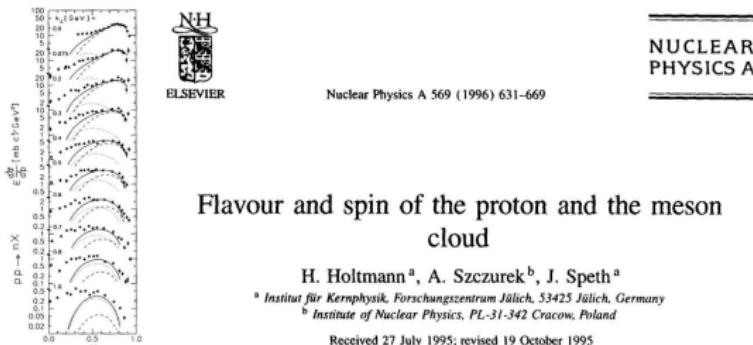
$$s_{\pi N} = \frac{m_\pi^2 + k_\perp^2}{y} + \frac{m_N + k_\perp^2}{1-y}$$

- a similar procedure gives  $f_{\rho N}(y)$

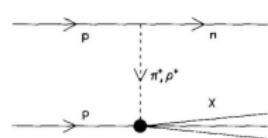
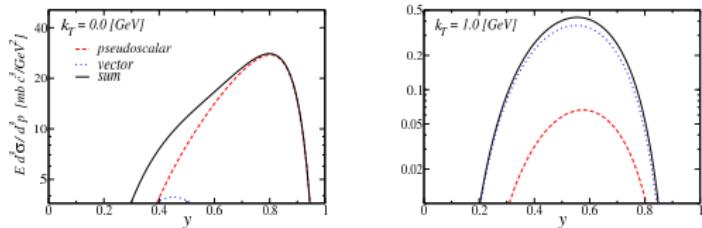
# constraints from hadroproduction

- $F_{\pi N}(s_{\pi N}) = \exp[-(m_N^2 - s)/\Lambda^2]$

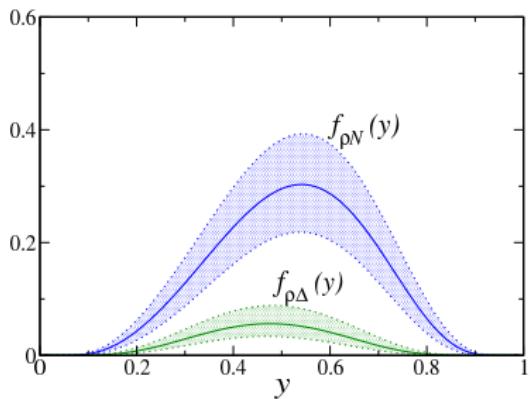
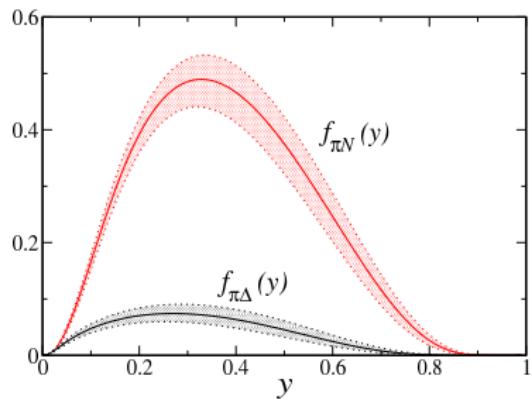
$\Lambda$  controls model output; must be **constrained**



- **hadroproduction** fits: e.g.,  $p p \rightarrow n X$ ,  $p p \rightarrow \Delta^{++} X$



# hadronic splitting functions



- $\Lambda_N = (1.56 \pm 0.07) \text{ GeV}$

- $\Lambda_\Delta = (1.39 \pm 0.07) \text{ GeV}$

\*\*for  $y \in [0.05, 0.20]$ ,  $\pi - \Delta$  modes are  $\sim 30\%$  of  $\pi - N$ ;  
 $\rho$ -exchange minimal

# form factors and model dependence

**UV regularization** may be achieved in various ways

- **s-dependent** form factor, e.g.:

$$F_{\pi N}(s_{\pi N}) = \exp[-(s_{\pi N} - m_N^2) / \Lambda^2]$$

$$F_{\pi N}(s_{\pi N}) = \left( \frac{m_N^2 + \Lambda^2}{m_N^2 + s_{\pi N}} \right)^n, \quad n \in 1, 2$$

- **covariant, t-dependent** expressions –

$$F_{\pi N}(t) = \left( \frac{m_N^2 + \Lambda^2}{m_N^2 + t} \right)^n, \quad n \in 1, 2$$

$$t = k^2 = (P - p)^2$$

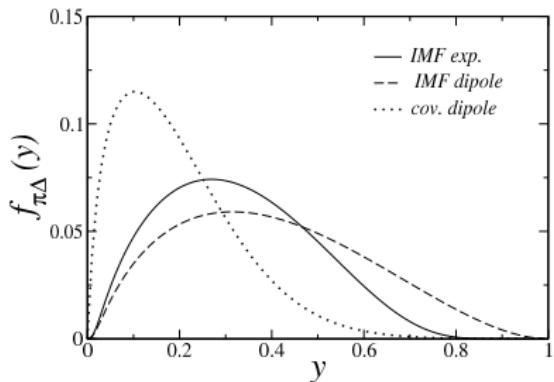
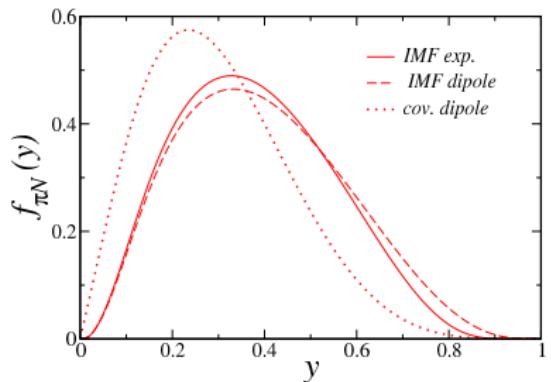
(though there are issues related to *reciprocity* and mom. conservation)

- **dimensional regularization**

→ a **systematic**, well-defined scheme (e.g.,  $\overline{MS}$ )

these effects **numerically**...

e.g., qualitative behaviors for  $f_{\pi N}(y)$ ,  $f_{\pi \Delta}(y)$  differ significantly according to the functional form of  $F(s_{\pi B})$ :

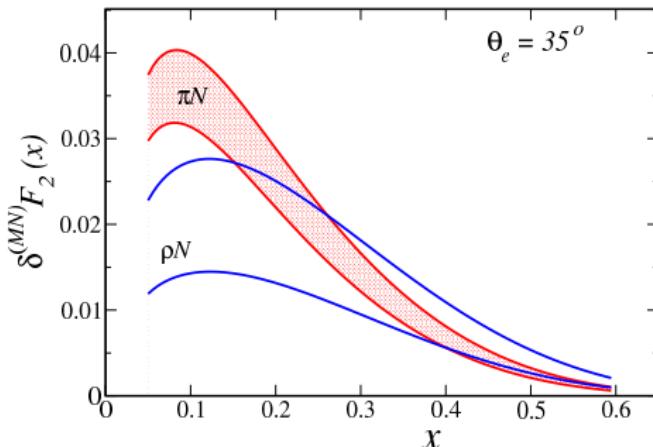


- N. B. *formal* limitations to **covariant** approach:  
 $\rightarrow f_{\pi N}(y) \neq f_{N\pi}(1 - y)$

# contributions to $e + n \rightarrow e' + X$

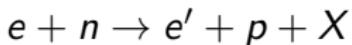
**inclusive:**  $\delta^{(\pi N)} F_2(x, Q^2) = \int_x^1 dy f_{\pi N}(y) F_2^\pi(\frac{x}{y}, Q^2)$

- $E = 11$  GeV scattering from  $\pi^-$ ,  $\rho^-$ ;  $0.05 \leq x \leq 0.6$   
 $25^\circ \leq \theta_e \leq 45^\circ$ , though  $Q^2$  dependence in  
 $F_2^\pi(x, Q^2) \sim \log(\log(Q^2/\Lambda_{QCD}^2))$  is weak



$**F_2^\pi(x, Q^2) \approx F_2^\rho(x, Q^2)$

# tagging in $k_{\perp}$



- **spectator tagging** in the target fragmentation region (TFR)  
→ finite  $k_{\perp}$  intervals

$$\begin{aligned}\delta^{(\pi N)} F_2(x, k_{\perp}^2, Q^2) &= \int_x^1 dy f_{\pi N}(y, k_{\perp}^2) F_2^{\pi}\left(\frac{x}{y}, Q^2\right) \\ f_{\pi N}(y, k_{\perp}^2) &= 2 \int_{k_{\perp}}^{k_{\perp}+\epsilon} dk'_{\perp} k'_{\perp} \cdot f_{\pi N}(y, k'^2_{\perp}) \\ f_{\pi N}(y) &= \int_0^{\infty} dk_{\perp}^2 f_{\pi N}(y, k_{\perp}^2)\end{aligned}$$

$$R(x, k_{\perp}^2, Q^2) = \delta^{(\pi N)} F_2(x, k_{\perp}^2, Q^2) / \delta^{(\pi N)} F_2(x, Q^2),$$

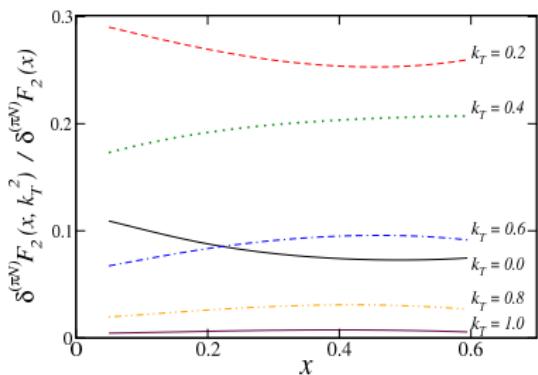
The parameter  $\epsilon = 0.1$  GeV is a  $k_{\perp}$  bin size

# $k_\perp$ dependence

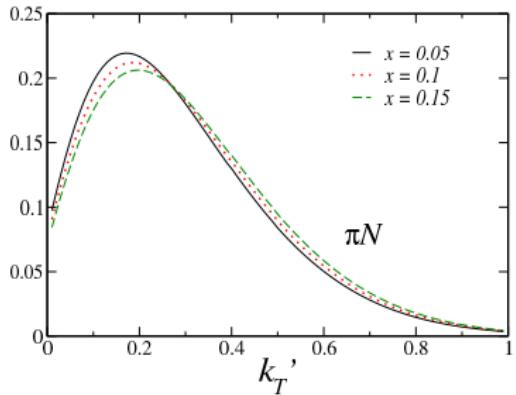
- tagged to inclusive structure functions:

$$\rightarrow \delta^{(\pi N)} F_2(x, k_\perp^2) / \delta^{(\pi N)} F_2(x)$$

... at fixed  $k_\perp$  ...



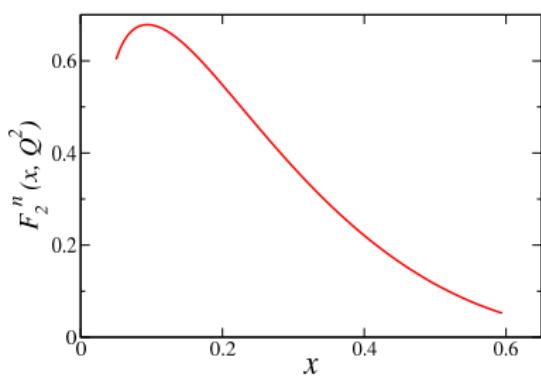
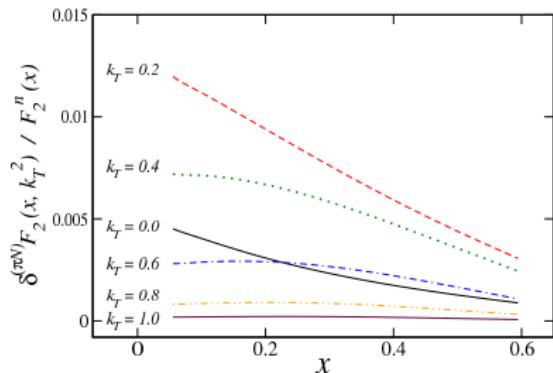
... and fixed  $x$ .



→  $k_\perp$  spectrum dominated by lower momenta,  $k_\perp \lesssim 400$  MeV;  
\*\* weak  $x$  **dependence** – cancellations in the  $F_2^\pi$  ratio

# contributions to $F_2^n(x)$

$F_2^n(x) = 2x \sum_q [q + \bar{q}](x)$ ,  $q \in \{u, d\}$  from LO CTEQ6.5,  
assuming *charge symmetry*



- N.B.:  $x$  distributions are for fixed  $\theta_e$ , **not** fixed  $Q^2$

\*\*  $Q^2 \rightarrow Q_0^2$  for  $x \rightarrow 0$ ;  $F_2^n(x, Q^2)$  non-monotonic!

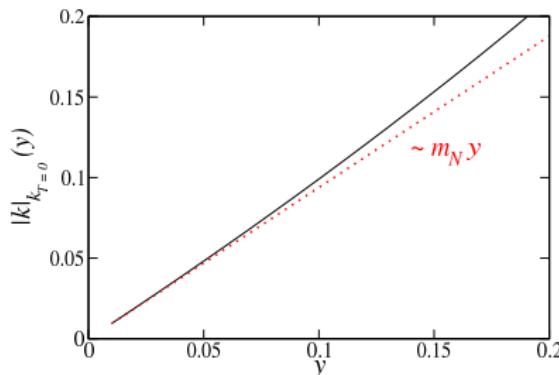
# kinematical limits from $|\vec{k}|$ tagging

- $|\vec{k}| \in [60, 170] \text{ MeV}$

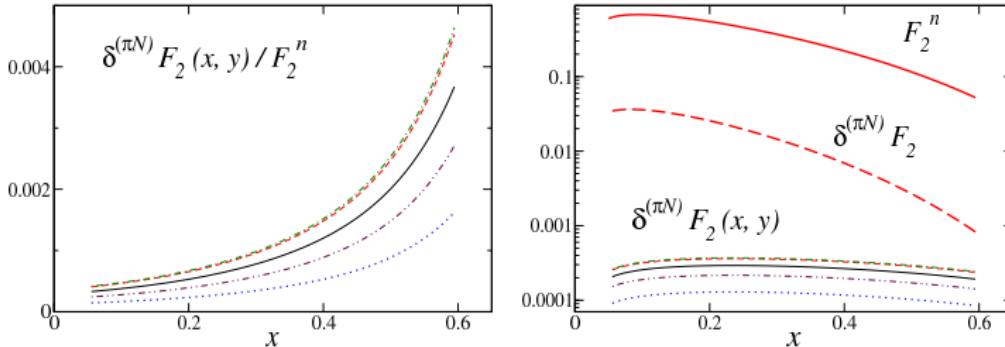
$$|\vec{k}| = \sqrt{k_{\perp}^2 + \frac{1}{4m_N^2(1-y)^2} \left( k_{\perp}^2 + (1 - [1-y]^2)m_N^2 \right)^2}$$

- in the limit  $k_{\perp}^2 = 0$ ,

$$|\vec{k}|_{k_{\perp}^2=0} = \frac{ym_N}{2} \left( \frac{2-y}{1-y} \right) \rightarrow y \lesssim |\vec{k}|/m_N$$



# $\delta^{(\pi N)} F_2(x, y)$ at fixed $|\vec{k}|$

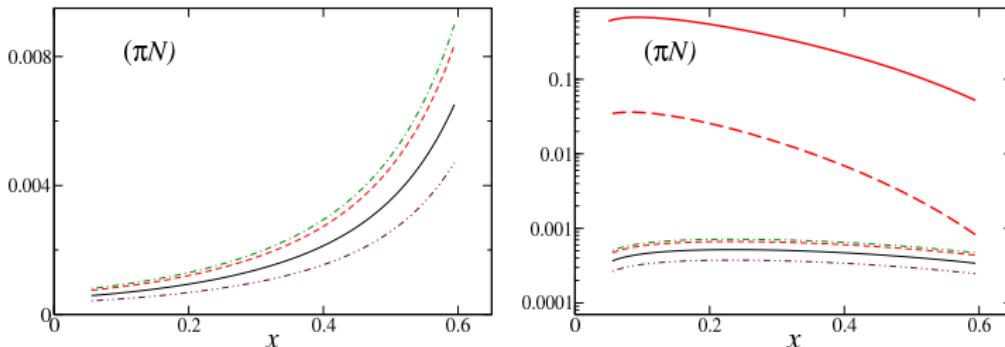


$$\delta^{(\pi N)} F_2(x, \mathbf{y} = \mathbf{0.05}) = f_{\pi N}(\mathbf{y} = \mathbf{0.05}) \cdot F_2^\pi(x)$$

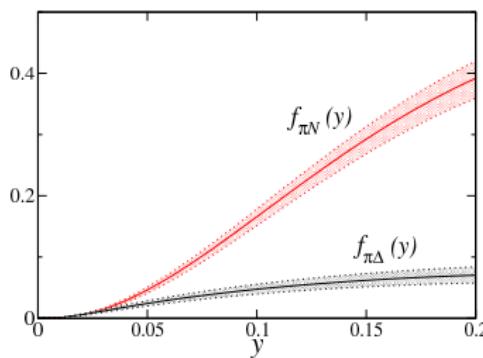
- $|\vec{k}| \in \{k_1, k_1 + 10\}$  MeV  
 $k_1 = 60, 80, 100, 130, 160$  MeV

picture depends importantly on the  $|\vec{k}|$  **binning scheme**  
\*\**(see talk by Thia)*

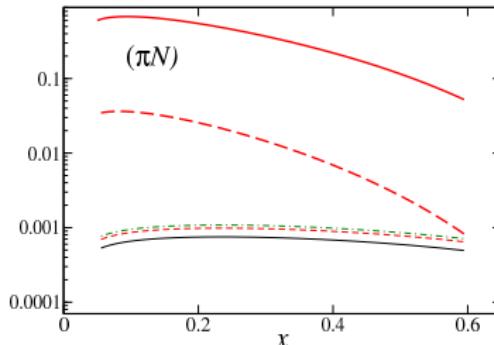
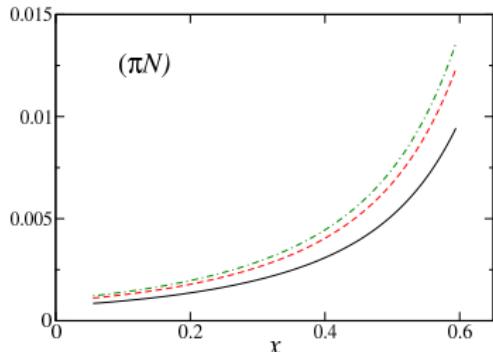
$$\delta^{(\pi N)} F_2(x, y), \quad y = 0.075$$



→ again, dependence on  $y$  controlled by  $f_{\pi N}(y)$ :



$$\delta^{(\pi N)} F_2(x, y), \textcolor{red}{y = 0.1}$$

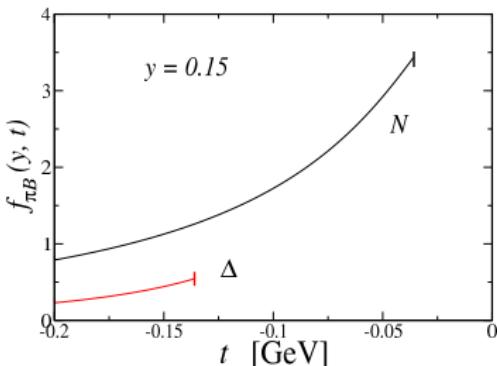
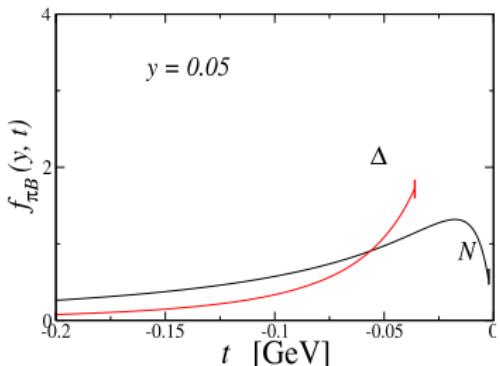


- at intermediate accessible  $y$ , measurements are sensitive only to  $|\vec{K}| \gtrsim 100$  MeV

still, these are  $\sim 1\%$  effects

# preliminary t distributions

- covariant  $f_{\pi N}(y, t)$  &  $f_{\pi \Delta}(y, t)$  before  $t$ -integration



$$\pi N: \quad t_{max} = -m_N^2 y^2 / (1 - y)$$

$$\pi \Delta \quad t_{max} = - (m_\Delta^2 - (1 - y)m_N^2) y / (1 - y)$$

- form factor dependence and **extrapolation** to  $t \sim m_\pi^2$  in progress (see talk by Christian Weiss!)

# conclusions

- have a *preliminary* assessment of pion mode contributions to  $F_2^n(x, Q^2)$

→ at accessible  $y$ ,  $|\delta^{\pi N} F_2(x, y)| / F_2^n \sim 1\%$

\*\* role of  $\rho$  **exchange minimal** at relevant kinematics  
 $(0 \leq y \leq 0.2)$

- $\Delta$  decays enter at  $\sim 30\%$  level and must be controlled systematically
- more thorough analysis of model dependence (**form factors,  $\Lambda$  determinations**) is required, and in progress  
→ as is the  $t \sim m_\pi^2$  **extrapolation**